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1 **Understanding influence of ocean waves on Arctic sea ice simulation: A modeling study**  
2 **with an atmosphere-ocean-wave-sea ice coupled model**

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14 **Abstract**

15       Rapid decline of Arctic sea ice has created more open water for ocean wave development  
16 and highlighted the importance of wave-ice interactions in the Arctic. Some studies have made  
17 contributions to our understanding of the potential role of the prognostic floe size distribution  
18 (FSD) on sea ice changes. However, these efforts do not represent the full interactions across  
19 atmosphere, ocean, wave, and sea-ice. In this study, we implement a modified joint floe size  
20 and thickness distribution (FSTD) in a newly-developed regional atmosphere-ocean-wave-sea  
21 ice coupled model and conduct a series of pan-Arctic simulation with different physical  
22 configurations related to FSD changes, including FSD-fixed, FSD-varied, lateral melting rate,  
23 wave-fracturing formulation, and wave attenuation rate. Firstly, our atmosphere-ocean-wave-  
24 sea ice coupled simulations show that the prognostic FSD leads to reduced ice area due to  
25 enhanced ice-ocean heat fluxes, but the feedbacks from the atmosphere and the ocean partially  
26 offset the reduced ice area induced by the prognostic FSD. Secondly, lateral melting rate  
27 formulations do not change the simulated FSD significantly, but they influence the flux  
28 exchanges across atmosphere, ocean, and sea-ice and thus sea ice responses. Thirdly, the  
29 changes of FSD are sensitive to the simulated wave height, wavelength, and wave period  
30 associated with different wave-fracturing formulations and wave attenuation rates, and the  
31 limited oceanic energy imposes a strong constraint on the response of sea ice to FSD changes.  
32 Finally, our results also demonstrate that wave-related physical processes can have impacts on  
33 sea ice changes with the constant FSD, suggesting the indirect influences of ocean waves on  
34 sea-ice through the atmosphere and the ocean.

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## 35 1. Introduction

36 Arctic sea ice, a major component in the climate system, has undergone dramatic changes  
37 over the past few decades associated with global climate change. September and March Arctic  
38 sea ice extent show decreasing trends of -13.1% and -2.6% per decade from 1979 to 2020,  
39 respectively (Perovich et al., 2020). The mean Arctic sea ice thickness has decreased by ~1.5-  
40 2 meters from the submarine period (1958-1976) to the satellite period (2011-2018), largely  
41 resulting from the loss of multiyear ice (Kwok, 2018; Tschudi et al., 2016). The drifting speed  
42 of Arctic sea ice exhibits an increasing trend based on satellite and buoy observations (e.g.,  
43 Rampal et al., 2009; Spreen et al., 2011; Zhang et al., 2022). As the Arctic Ocean has been  
44 dominated by thinner and younger ice, Arctic sea ice is more likely to be influenced by forcings  
45 from the atmosphere and the ocean.

46 Associated with the above Arctic sea ice changes, the Arctic fetch (open water area for  
47 ocean wave development) is less limited by the ice cover. The increased Arctic fetch and  
48 surface wind speed can lead to higher ocean waves in the Arctic Ocean based on observations,  
49 reanalysis, and future projections (Casas-Prat and Wang, 2020; Dobrynin et al., 2012; Liu et  
50 al., 2016; Stopa et al., 2016; Waseda et al., 2018). The higher ocean waves are more likely to  
51 propagate deeper into the ice pack and have sufficient energy to break sea ice into smaller floes  
52 (e.g., Kohout et al., 2014). Sea ice with mostly smaller floes has larger surface areas,  
53 particularly lateral surfaces. The increased lateral surface accelerates ice melting through  
54 enhanced ice-ocean heat fluxes (e.g., Steele, 1992). Some studies also showed that the ice-floe  
55 melting rate is associated with the horizontal mixing of oceanic heat across ice floe edge

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56 between open water and under-floe ocean by oceanic eddies, in particular sub-mesoscale eddies,  
57 and the strength of this effect depends on floe size (Gupta and Thompson, 2022; Horvat et al.,  
58 2016). The enhanced ice melting creates more open water (i.e., fetch), which is a favorable  
59 condition for further wave development as well as the ice-albedo feedback (Curry et al., 1995).  
60 These processes create a potential feedback loop between ocean waves and sea ice (e.g., Asplin  
61 et al., 2014; Thomson and Rogers, 2014).

62 Arctic cyclones and their high surface wind are the important drivers for large wave events  
63 in the Arctic Ocean. Previous studies showed that intense storms like the “Great Arctic Cyclone”  
64 of 2012 (Simmonds and Rudeva, 2012) and a strong summer cyclone in 2016 could be one of  
65 the contributors to the anomalously low sea ice extent in 2012 and 2016 (e.g., Lukovich et al.,  
66 2021; Parkinson and Comiso, 2013; Peng et al., 2021; Stern et al., 2020; Zhang et al., 2013).  
67 Statistical analyses based on cyclone-tracking algorithm across multiple reanalyses suggested  
68 that the number of Arctic cyclones shows a significantly positive trend in the cold season (e.g.,  
69 Sepp and Jaagus, 2011; Valkonen et al., 2021; Zahn et al., 2018). The increased cyclone  
70 activities and more open water areas cause more extreme wave events in the Arctic (e.g.,  
71 Waseda et al., 2021). Blanchard-Wrigglesworth et al. (2021) found that extreme changes in  
72 Arctic sea ice extent are correlated with distinct wave conditions during the cold season based  
73 on the observations.

74 The potential feedback loop associated with ocean waves and sea ice and more extreme  
75 wave events indicates the importance of representing these processes in climate models for  
76 improving sea ice simulation and prediction (e.g., Collins et al., 2015; Kohout et al., 2014).

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77 However, state-of-the-art climate models participating in the latest Coupled Model  
78 Intercomparison Project Phase 6 (CMIP6) have not incorporated the interactions between  
79 ocean waves and sea ice in their model physics (e.g., Horvat, 2021). The coupled effects of  
80 ocean waves and sea ice include; the amplitude of ocean waves decays as the waves travel  
81 under the ice cover due to the combination of scattering and dissipation (e.g., Squire, 2020).  
82 Crests and troughs of ocean waves exert strains on sea ice, and sea ice breaks if the maximum  
83 strain exceeds a certain threshold (e.g., Dumont et al., 2011). The wave-induced ice-breaking  
84 changes the size of floes, which in turn changes the floe size distribution (FSD; Rothrock and  
85 Thorndike, 1984). In addition to the interactions between ocean waves and sea ice, the floe size  
86 contributes to the changes in the atmospheric boundary layer (e.g., Schäfer et al., 2015; Wenta  
87 and Herman, 2019), mechanical responses of sea ice (e.g., Vella and Wettauer, 2008; Weiss  
88 and Dansereau, 2017; Wilchinsky et al., 2010), the flux exchanges across air-sea ice-ocean  
89 interfaces (Cole et al., 2017; Loose et al., 2014; Lu et al., 2011; Martin et al., 2016; Steele et  
90 al., 1989; Tsamados et al., 2014), and the scattering of ocean wave propagation (e.g., Montiel  
91 et al., 2016; Squire and Montiel, 2016). Thus, it is essential to have a prognostic FSD to  
92 properly reflect wave-ice interactions as well as other processes related to the floe size in  
93 climate models.

94       Recently, several studies have made contributions on understating responses of sea ice to  
95 the prognostic FSD (e.g., Bateson et al., 2020; Bennetts et al., 2017; Boutin et al., 2020; Horvat  
96 and Tziperman, 2015; Roach et al., 2018a, 2019; Zhang et al., 2015, 2016). However, these  
97 studies used simplified model complexity (i.e., standalone sea ice model, ice-wave coupling,

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98 ice-ocean coupling) and were unable to give a full representation of sea ice responses to the  
99 evolving states of atmosphere, ocean, and wave based on explicit model physics as well as  
100 feedbacks from sea ice to them. Motivated by this, here we introduce a newly-developed  
101 atmosphere-ocean-wave-sea ice coupled model, in which we implement physical processes  
102 that simulate the evolution of floe size distribution. We use this new coupled model to  
103 investigate the responses of sea ice to ocean waves, as well as interactions in the Arctic climate  
104 system. This paper is structured as follows. Section 2 provides an overview of the new coupled  
105 model, focusing on the wave component and the implementation of the prognostic FSD.  
106 Section 3 describes the design of numerical experiments and the related model configurations.  
107 Section 4 examines the responses of sea ice to wave-ice interactions with the prognostic FSD,  
108 as well as other ocean wave-related processes. Discussions and concluding remarks are  
109 provided in section 5.

110

## 111 **2. Model description**

112 The newly-developed atmosphere-ocean-wave-sea ice coupled model is based on  
113 Coupled Arctic Prediction System (CAPS, Yang et al., 2022), which consists of the Weather  
114 Research and Forecasting Model (WRF), the Regional Ocean Modeling System (ROMS), and  
115 the Community Ice Code (CICE). The detailed description of each model component in CAPS  
116 is referred to Yang et al. (2020; 2022). In this section, we focus on newly-added features in  
117 CAPS as described below.

### 118 **2.1. Wave model component**

119 To represent wave-ice interactions, an ocean wave model is coupled into CAPS, which is  
 120 the Simulating Waves Nearshore (SWAN). SWAN is a third-generation wave model and  
 121 includes processes of diffraction, refraction, wave-wave interactions, and wave dissipation due  
 122 to wave breaking, whitecapping, and bottom friction (Booij et al., 1999). Recently, the SWAN  
 123 model has implemented wave dissipation due to sea ice based on an empirical formula, which  
 124 is called IC4M2 (Collins and Rogers, 2017; Rogers, 2019). Specifically, the temporal  
 125 exponential decay rate of wave energy due to sea ice is defined as,

$$128 \quad S_{ice}/E = -2c_g k_i \quad (1)$$

126 where  $S_{ice}$  is the sink term induced by sea ice,  $E$  is the wave energy spectrum, and  $c_g$  is the  
 127 group velocity.  $k_i$  is the linear exponential rate that is a function of frequency as follow,

$$132 \quad k_i(f) = c_0 + c_1 f + c_2 f^2 + c_3 f^3 + c_4 f^4 + c_5 f^5 + c_6 f^6 \quad (2)$$

129 where  $c_0$  to  $c_6$  are the user-defined coefficients and their values as described in Section 3. In  
 130 the SWAN model, both the wind source term  $S_{in}$ , and the sea ice sink term are scaled by sea  
 131 ice concentration  $a_{ice}$ , which is provided by the CICE model through the coupler in CAPS,

$$133 \quad S_{ice} \rightarrow a_{ice} S_{ice} \quad (3)$$

$$134 \quad S_{in} \rightarrow (1 - a_{ice}) S_{in} \quad (4)$$

## 135 **2.2. Prognostic FSD**

136 For the prognostic FSD implemented in the CICE model, we follow the joint floe size and  
 137 thickness distribution (FSTD; Horvat and Tziperman, 2015). The FSTD is defined as a  
 138 probability distribution  $f(r, h) dr dh$ .  $f(r, h)$  represents the fraction of cell covered by ice with  
 139 floe size between  $r$  and  $r + \Delta r$ , thickness between  $h$  and  $h + \Delta h$ , and the FSTD satisfies,

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143 
$$\int_{\mathcal{R}} \int_{\mathcal{H}} f(r, h) dr dh = 1 \quad (5)$$

140 The ice thickness distribution  $g(h)$  (ITD; Thorndike et al., 1975), which is simulated by the  
 141 CICE model, and the FSD  $F(r)$ , can be obtained by integrating the FSTD over all floe sizes  
 142 and all ice thicknesses,

146 
$$\int_{\mathcal{R}} f(r, h) dr = g(h) \quad (6)$$

$$\int_{\mathcal{H}} f(r, h) dh = F(r)$$

144 Roach et al. (2018a) suggested the modified FSTD,  $L(r, h)$ , to preserve the governing  
 145 equations of ITD in the CICE model, which satisfies,

152 
$$\int_{\mathcal{R}} L(r, h) dr = 1 \quad (7)$$

147 and

153 
$$f(r, h) = g(h) L(r, h) \quad (8)$$

148 As described in Roach et al. (2018a), the implementation of the modified FSTD ignores the  
 149 two-way relationship between floe size, that is, physical processes associated with FSD  
 150 changes (i.e.,  $L(r, h)$  changes) are independent across each ice thickness category. The  
 151 governing equation of FSTD is defined as,

157 
$$\frac{\partial f(r, h)}{\partial t} = -\nabla \cdot (f(r, h) \vec{v}) + \mathcal{L}_T + \mathcal{L}_M + \mathcal{L}_W \quad (9)$$

154 The terms on the right-hand side represent advection, thermodynamics, mechanical, and wave-  
 155 induced floe-fracturing processes. For these terms, except the last term  $\mathcal{L}_W$ , we follow the  
 156 approach described in Roach et al. (2018a) and related values for coefficients as described in



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158 Section 3. The formulations of  $\mathcal{L}_W$  proposed by Horvat and Tziperman (2015) involve a  
 159 random function to generate sub-grid scale sea surface elevation to determine how floes are  
 160 fractured by ocean waves. As a consequence, simulations are not bitwise reproducible with the  
 161 formulation including a random function. To avoid this issue, we propose different approaches  
 162 for our implementation of FSTD as described below.

### 163 2.3. Floe fracturing by ocean waves

164 For the floe-fracturing term  $\mathcal{L}_W$ , we follow the formulation suggested by Zhang et al.  
 165 (2015), which has similar form as Horvat and Tziperman (2015) and can be described as,

$$171 \quad \mathcal{L}_W = -Q(r) f(r, h) + \int_{\mathcal{R}} \beta(r', r) Q(r') f(r', h) dr' \quad (10)$$

166 The first term on the right-hand side represents the areal fraction reduction due to floe-  
 167 fracturing and the second term is the areal fraction gain from other floe size categories that  
 168 have floe-fracturing. In equation (10),  $Q(r)$  is the probability that floe-fracturing occurs for  
 169 floe size between  $r$  and  $r + \Delta r$ , and  $\beta(r', r)$  is the redistributor that transfers fractured floe  
 170 from floe size  $r'$  to  $r$ .  $\mathcal{L}_W$  does not create or destroy ice so it must satisfy,

$$173 \quad \int_{\mathcal{R}} \mathcal{L}_W dr = 0 \quad (11)$$

172 In this study, we propose two different formulations for  $Q(r)$  and  $\beta(r', r)$ .

#### 174 (a) Equally-redistribution

175 We follow the same assumption in Zhang et al. (2015). That is, ice-fracturing by ocean  
 176 waves is likely to be a random process and the size of fractured floe does not have favored floe  
 177 size based on aerial photographs and satellite images (e.g., Steer et al., 2008; Toyota et al.,

178 2006, 2011). Thus, fractured floe is equally-redistributed into smaller floe sizes. The  
 179 redistributor is defined as,

$$182 \quad \beta(r_1, r_2) = \begin{cases} 1/(c_2 r_1 - c_1 r_1) & \text{if } c_1 r_1 \leq r_2 \leq c_2 r_1 \\ 0 & \text{if } r_2 < c_1 r_1 \text{ or } r_2 > c_2 r_1 \end{cases} \quad (12)$$

180 where  $c_1$  and  $c_2$  are constants that define upper- and lower-bound of floe size redistribution.  
 181 Details of  $\beta(r', r)$  in this formulation are referred to Zhang et al. (2015).

183 For the probability  $Q(r)$ , Zhang et al. (2015) used a user-defined coefficient to reflect  
 184 wave conditions and determine  $Q(r)$ . Zhang et al. (2016) suggested that the coefficient is a  
 185 function of wind speed, fetch, ITD, and FSD. Since CAPS has a wave component to simulate  
 186 wave conditions, we reformulate  $Q(r)$  to include simulated wave information from the coupler,  
 187 and  $Q(r)$  is defined as,

$$194 \quad Q(r) = c_w H(\varepsilon) \exp \left[ -\alpha \left( \frac{1-r}{r_{max}} \right) \right] \quad (13)$$

188 where  $H(\varepsilon)$  is the Heaviside step function, the exponential function determines the fraction of  
 189 each floe size participating in fracturing, and user-defined coefficients,  $c_w$  and  $\alpha$ , control the  
 190 upper-bound of  $Q(r)$  and the shape of the exponential function. To include wave conditions  
 191 from the SWAN model, we apply the floe-fracturing parameterization suggested by Dumont et  
 192 al. (2011) to calculate the strain induced by ocean waves on ice floes, and use this  
 193 parameterization to define  $H(\varepsilon)$  as,

$$197 \quad H(\varepsilon) = \begin{cases} 1, & \text{if } \varepsilon \geq \varepsilon_c \\ 0, & \text{if } \varepsilon < \varepsilon_c \end{cases} \quad (14)$$

$$198 \quad \varepsilon = \frac{2\pi^2 h_{ice} A_{wave}}{L_{wave}^2} \quad (15)$$

195 where the strain  $\varepsilon$  is proportional to the ice thickness  $h_{ice}$  and the mean amplitude of wave  
 196  $A_{wave}$ , and inversely proportional to the square of the mean surface wavelength  $L_{wave}$ . If the

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199 strain exceeds the strain yield limit  $\varepsilon_c$  (see Section 3), floe-fracturing occurs (i.e.,  $H(\varepsilon) = 1$ ).  
200 The distribution of wave heights is, in general, a Rayleigh distribution, which allows us to use  
201 the simulated significant wave height from the SWAN model to determine the mean wave  
202 amplitude with the following relationship (e.g., Bai and Bai, 2014),

$$A_{wave} = \frac{H_{wave}}{2} \cong \frac{5}{16} H_s \quad (16)$$

203 where  $H_{wave}$  is the mean wave height, and  $H_s$  is the significant wave height.

204  
205 The exponential function is built on that the wave strain on ice floes is separated by the  
206 wavelength (e.g., Dumont et al., 2011, their Fig. 4). Floe size smaller than the wavelength is  
207 more likely to move along with ocean waves with little bending (e.g., Meylan and Squire, 1994).  
208 That is, the exponential function preferentially has a higher fraction for larger floes.

209 (b) Redistribution based on a semi-empirical wave spectrum

210 As discussed in Dumont et al. (2011, their Fig. 4), fractured floes have a maximum size  
211 with half of the surface wavelength. Thus, the wave distribution of different wavelengths in  
212 each grid cell allows us to predict floe sizes after fracturing. The sea surface elevation is a result  
213 of the superimposition of waves with different periods, amplitudes, and directions in space and  
214 time. Empirical wave spectra have been proposed to describe wave conditions with a finite set  
215 of parameters. Based on wave observations from a wide variety of locations, Bretschneider  
216 (1959) suggested the formulation of wave spectrum, which is used to formulate the  
217 redistribution of fractured floe as described below.

218 The Bretschneider wave spectrum is defined as,

---

221 
$$S_B(T) = \frac{1.25H_s^2 T^5}{8\pi T_p^4} \exp\left[-1.25\left(\frac{T}{T_p}\right)^4\right] \quad (17)$$

219 where  $T_p$  is the peak wave period, and the spectral wave amplitude is defined as (Dumont et  
220 al., 2011),

224 
$$A(T) = \sqrt{\frac{4\pi S_B(T)}{T}} \quad (18)$$

222 Similar to the distribution of wave height, Bretschneider (1959) found that the distribution of  
223 wave period is, in general, a Rayleigh distribution and defined as,

228 
$$P(T) = 2.7\left(\frac{T}{T_{ave}}\right)^3 \exp\left[-0.675\left(\frac{T}{T_{ave}}\right)^4\right] \quad (19)$$

225 where  $T_{ave}$  is the mean surface period. With the deep-water surface wave dispersion relation  
226  $L(T) = gT^2/2\pi$ , the corresponding wave length for each wave period bin can be obtained,  
227 and the wave-strain distribution can be calculated with the modified equation (15),

231 
$$\varepsilon(T) = \frac{2\pi^2 h_{ice} A(T)}{L(T)^2} \quad (20)$$

229 Combined with the Heaviside step function defined in the equation (14), the probability of floe-  
230 fracturing for each wave period is obtained,

237 
$$P_f(T) = H(\varepsilon(T))\bar{P}(T) \quad (21)$$

232 where  $\bar{P}(T)$  is the normalized  $P(T)$ . Based on  $P_f(T)$  and the assumption that fractured floes  
233 have a maximum size with half of the surface wavelength, the redistributor  $\beta(r_1, r_2)$  can be  
234 obtained based on following criteria: 1) floe size between  $r$  and  $r + \Delta r$  (in radius) must be  
235 greater than half of wavelength  $L(T)$ , 2) floes fractured by the wavelength  $L(T)$  have the size  
236 of  $L(T)/2$ , and 3)  $P_f(T)$  represents the fraction of floe with  $r$  and  $r + \Delta r$  transferred to new

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238 size with  $r'$  and  $r' + \Delta r$  determined by the criterion (2). The probability  $Q(r)$  is the summation  
239 of  $P_f(T)$  and represents the total fraction of floe participating in wave-fracturing.

### 240 **3. Model configurations and experiment designs**

241 The WRF, ROMS, SWAN, and CICE models use the same model grid with 320 (440) x-  
242 (y-) grid points and  $\sim 24$ km horizontal resolution (Fig. 1). Initial and boundary conditions for  
243 the WRF, ROMS, CICE models are generated from the Climate Forecast System version 2  
244 (CFSv2, Saha et al., 2014) operational analysis, archived by National Centers for  
245 Environmental Information (NCEI), National Oceanic and Atmospheric Administration  
246 (NOAA). In our configurations, the SWAN model starts with the calm wave states (i.e., zero  
247 wave energy in all frequencies). The modified FSTD,  $L(r, h)$ , is initialized based on the power-  
248 law distribution of floe number,  $N(r) \propto r^{-a}$  (e.g., Toyota et al., 2006), with the exponent  $a$  as  
249 2.1 for all grid cells. Physical parameterizations of each model component are mostly identical  
250 to those used in Yang et al. (2022) and summarized in Table 1.

251 Cassano et al. (2011) suggested that the use of a higher model top (10 mb) or applying  
252 spectral nudging in the upper model levels leads to significantly reduced biases in pan-Arctic  
253 atmospheric circulation in the standalone WRF model. Thus, compared with Yang et al. (2022),  
254 we change the model top of the WRF model in CAPS from 50 mb to 10 mb. With coupling to  
255 the SWAN model in CAPS, the corresponding configurations are modified to reflect wave  
256 effects on the atmosphere and the ocean. In the Mellor-Yamada-Nakanishi-Niino planetary  
257 boundary layer scheme (MYNN; Nakanishi and Nino, 2009), the surface roughness,  $z_0$ , is  
258 modified to include the effect of waves based on the following formulation,

---

279 
$$z_0 = 1200H_s \left( \frac{H_s}{L_{wave}} \right)^{4.5} + \frac{0.11\nu}{u_*} \quad (22)$$

259 where  $\nu$  is the viscosity, and  $u_*$  is the friction velocity (Taylor and Yelland, 2001; Warner et al.,  
260 2010). For the interaction of ocean waves and currents, the vortex-force (VF) formulation is  
261 applied that represents conservative (e.g., vortex and Stokes-Coriolis forces) and non-  
262 conservative wave effects. The non-conservative wave effects in the VF formulation include  
263 wave accelerations for currents and wave-enhanced vertical mixing (Kumar et al., 2012;  
264 Uchiyama et al., 2010). The dissipated wave energy due to surface wave breaking and  
265 whitecapping is transferred to the ocean surface layer as additional turbulent kinetic energy,  
266 which in turn enhances the vertical mixing. For the effect of currents on the dispersion relation  
267 in wave propagation, we employ a depth-weighted current to account for the vertically-sheared  
268 flow following Kirby and Chen (1989). As discussed in previous studies (e.g., Naughten et al.,  
269 2017; Yang et al., 2022), the upwind third-order advection (U3H, Table 1) scheme, which is an  
270 oscillatory scheme, can lead to increased non-physical frazil ice formation. To address this  
271 issue, we implement the upwind flux limiter suggested by Leonard and Mokhtari (1990) to  
272 reduce false extrema caused by the oscillatory behavior of the U3H scheme. The value of  
273 yielding strain  $\varepsilon_c$ , described in Section 2.3 is chosen as  $\cong 3 \times 10^{-5}$  (Dumont et al., 2011;  
274 Horvat and Tzipermann, 2015; Langhorne et al., 1998). The floe welding parameter in the  
275 thermodynamic term  $\mathcal{L}_T$ , is chosen as  $1 \times 10^{-7} \text{ km}^{-2} \text{ s}^{-1}$ . Roach et al. (2018b) found a lower  
276 bound of floe welding parameter as  $1 \times 10^{-9} \text{ km}^{-2} \text{ s}^{-1}$  in the autumn Arctic based on the  
277 observations. Also, the floe welding process only occurs in the freezing condition (Roach et al.,  
278 2018a), and the freezing condition is determined by net ice mass increase by thermal mass

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280 change (see Figure 3). The floe welding parameter will behave like a step function during the  
 281 freeze-thaw transition. For the user-defined coefficients in equation (4), all experiments use the  
 282 equally-redistributed formulation described in Section 2.3 with  $c_w$  as 0.8 and  $\alpha$  as 1.0. Based  
 283 on the formation of  $\mathcal{L}_T$  in the equation (9) (see Roach et al., 2018a), the floe size change  
 284 through the lateral surface is determined by both the floe size and the lateral melting rate. In  
 285 the existing sea ice models, the lateral melting rate  $w_{lat}$  is all based on the empirical  
 286 formulation suggested by Perovich (1983, hereafter P83),

293 
$$w_{lat} = m_1 \Delta T^{m_2} \quad (23)$$

287 where  $\Delta T$  is the temperature difference between sea surface temperature (SST) and the freezing  
 288 point, and  $m_1, m_2$  are empirical coefficients based on the observations from a single sea ice  
 289 lead in the Canadian Arctic. This empirical formulation is also the default lateral melting rate  
 290 in the CICE model. Maykut and Perovich (1987, hereafter MP87) showed a different approach  
 291 to parameterize the lateral melting rate that includes the friction velocity  $u_*$  based on the  
 292 observations from the Marginal Ice Zone Experiment, which is defined as,

300 
$$w_{lat} = u_* m_3 \Delta T^{m_4} \quad (24)$$

294 Both formulations (Equ. 23, 24) are examined in this study (see Table 2). In the equation (2),  
 295 the user-defined coefficients for the wave attenuation are set as  $c_2 = 1.06 \times 10^{-3}$  and  $c_4 =$   
 296  $2.3 \times 10^{-2}$  (case 1), which follow the polynomial of Meylan et al. (2014, hereafter M14) from  
 297 the observations with 10-25m floe in diameter in the Antarctic, and  $c_2 = 2.84 \times 10^{-4}$  and  
 298  $c_4 = 1.53 \times 10^{-2}$  (case 2), which follow the polynomial of Rogers et al. (2018, hereafter R18)  
 299 based on the observations for pancake and frazil ice in the Arctic.

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301 In this study, a series of numerical experiments for the pan-Arctic sea ice simulation have  
302 been conducted, starting from January 1<sup>st</sup>, 2016 to December 31<sup>st</sup>, 2020. Table 2 provides the  
303 details of the configurations for these experiments, which allow us to examine the influence of  
304 ocean waves and related physical processes on Arctic sea ice simulation in the atmosphere-  
305 ocean-wave-sea ice coupled framework. Specifically, these experiments focus on 1) the  
306 comparison between constant FSD and prognostic FSD (Exp-CFSD and Exp-PFSD), 2) sea ice  
307 responses to different lateral melting rate parameterizations (Exp-CFSD, Exp-PFSD, Exp-  
308 LatMelt-C and Exp-LatMelt-P), 3) the difference between the equally-redistributed  
309 formulation and the Bretschneider formulation for floe fracturing (Exp-PFSD and Exp-  
310 WaveFrac-P), and 4) the contribution of different wave attenuation rates to sea ice changes  
311 (Exp-CFSD, Exp-PFSD, Exp-WaveAtt-C and Exp-WaveAtt-P).

## 312 **4. Results**

### 313 **4.1 Constant vs. Prognostic floe size**

314 Figure 2 shows the evolution of sea ice area (SIA) for all experiments conducted in this  
315 study (as well as the values of seasonal maximum and minimum SIA for all experiments are  
316 summarized in Table S1). SIA is calculated as the sum of the ice-covered area of all grid cells  
317 (cell-area times sea ice concentration). In addition to the evolution of SIA, the 2016-2020  
318 averaged March and September sea ice concentration (SIC) for all experiments are shown in  
319 Figure S1. Compared with Exp-CFSD, which uses a constant floe diameter (300m) in the  
320 lateral melting scheme (Steele, 1992), Exp-PFSD uses the equations described in Section 2.2  
321 to determine the prognostic FSD and related physical processes (see Table 2). With the



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322 prognostic FSD, the evolution of SIA in Exp-PFSD (Fig. 2a, red line) shows smaller SIA in the  
323 melting months (June to September) and similar magnitude of SIA in other months compared  
324 to that of Exp-CFSD (Fig. 2a, blue line) during 2016-2018. After that, Exp-PFSD simulates  
325 smaller SIA than that of Exp-CFSD for most months during 2019-2020, especially for the  
326 seasonal maximum of 2019 and SIA after May 2020.

327 Figure 3 shows the evolution of sea ice mass budget terms with cell-area weighted  
328 averaging over the entire model domain with a 15-day running-average for smoothing out high-  
329 frequency fluctuations for all experiments. The most notable difference between Exp-CFSD  
330 and Exp-PFSD is the magnitude of basal melt (red lines) and lateral melt (grey lines). In Exp-  
331 CFSD, basal melt plays the dominant role in reducing sea ice mass compared to lateral melt  
332 which has negligible contribution to the total mass change. As discussed in Maykut and  
333 Perovich (1987), the inclusion of friction velocity in calculating the lateral melting rate results  
334 in  $w_{lat} \rightarrow 0$  as  $u_* \rightarrow 0$ , which contributes to negligible lateral melt in Exp-CFSD. By contrast,  
335 Exp-PFSD with prognostic floe size shows that lateral melt has the major contribution in  
336 reducing ice mass (Fig. 3b), a result of smaller floe size near the ice edge simulated by Exp-  
337 PFSD (Fig. 10a). It is also notable that the increased lateral melt in Exp-PFSD tends to be  
338 compensated by the decreased basal melt (Fig. 3b). The overall ice melt due to oceanic  
339 processes in Exp-PFSD (i.e., the sum of lateral melt and basal melt) does not change  
340 significantly compared to that of Exp-CFSD (Fig. S2e). The melting potential in the CICE  
341 model of CAPS, the available energy from the ocean to melt sea ice, is defined as the vertical  
342 integral of the difference between ocean temperature and freezing point within the surface layer

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343 (to 5-meter depth in CAPS) from the ROMS model. When the available oceanic energy is less  
344 than the sum of heat fluxes used for lateral and basal melt, the CICE model performs a linear  
345 scaling to maintain the relative magnitude of heat fluxes for lateral and basal melt. Thus, the  
346 increased energy consumption by lateral melt due to smaller floe size reduces the available  
347 energy for basal melt. Such change between lateral and basal melt has been shown in some  
348 studies (e.g., Bateson et al., 2020, 2022; Roach et al., 2018a, 2019; Smith et al., 2022; Tsamados  
349 et al., 2015). Although the rough compensation, Exp-PFSD simulates more ice melted by the  
350 oceanic energy compared to Exp-CFSD from January to July (Fig. S2e).

351 Figure 4 shows the evolution of ice-ocean heat flux, the friction velocity at the ice-ocean  
352 interface, and the temperature difference between SST and freezing point for Exp-CFSD and  
353 Exp-PFSD. These variables are the average of ice-covered cells with at least 1% ice  
354 concentration, and the ice-ocean heat flux is weighted by the ice concentration so that the  
355 weighted heat flux represents the mean value of the cell, rather than the mean value of the ice-  
356 ocean interface. It should be noted that cells with negative values of the temperature difference  
357 (i.e., supercooled water) are forced to be zero. This is consistent with the treatment in the CICE  
358 model for the calculation of ice-ocean heat flux. As shown in Fig. 4a and Fig. S2e, the evolution  
359 of ocean-induced ice melt is consistent with that of the ice-ocean heat flux for both Exp-CFSD  
360 and Exp-PFSD. Both Exp-CFSD and Exp-PFSD show relatively similar evolution of the  
361 friction velocity (Fig. 4b). The temperature difference of Exp-PFSD is much smaller than that  
362 of Exp-CFSD (Fig. 4c). The ice-ocean heat flux is the total heat flux from ocean to ice through  
363 ice bottom surface and lateral surface. Although Exp-PFSD has smaller temperature difference

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364 as well as the melting potential under ice-covered cells, the larger total ice surface area due to  
365 smaller floe size increases the efficiency of Exp-PFSD extracting energy from the ocean. The  
366 smaller temperature difference of Exp-PFSD and the compensation between lateral and basal  
367 melt suggest that the ocean surface layer of Exp-PFSD is closer to the freezing point compared  
368 to that of Exp-CFSD. Energy loss from the ocean through air-sea heat flux that further cools  
369 the upper ocean, freshwater input (e.g., ice melting, precipitation) that raises the freezing point,  
370 as well as non-physical numerical oscillations (Naughten et al., 2017; Yang et al., 2022), can  
371 lead to increased frazil ice formation of Exp-PFSD as shown in Fig. 3a-b and Fig. S2g.

372         Figure 5 shows the heat flux budget at the ice surface averaged for all ice-covered cells.  
373 The positive ice-atmosphere heat fluxes of Exp-CFSD and Exp-PFSD in July (Fig. S3a)  
374 correspond to top melt in Fig. 3a-b and Fig. S2b (as well as Table S2). The ice-atmosphere heat  
375 flux not only determines the magnitude of ice surface melt in summer but also the energy loss  
376 from the ice interior in winter, which is crucial for ice growth. As shown in Fig. S3a, Exp-  
377 PFSD loses more energy to the atmosphere than that of Exp-CFSD in most winters. The  
378 conductive heat flux also shows similar evolution, suggesting that more energy is conducted to  
379 the ice top from ice layers below in Exp-PFSD (Fig. S3b). The loss of ice energy then  
380 contributes to increased ice growth at the ice bottom as shown in Fig. 3a-b and Fig. S2f (as  
381 well as Table S2). Generally, the net shortwave flux of Exp-PFSD is larger (ice gains more  
382 energy) than that of Exp-CFSD, especially during the melting season (Fig. S3c). In contrast to  
383 the net shortwave flux, for most of the time, the net longwave flux of Exp-PFSD is smaller (i.e.,  
384 ice loses more energy) than that of Exp-CFSD (Fig. S3d). Exp-PFSD loses more energy

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385 through sensible heat flux compared to Exp-CFSD (Fig. S3e). For latent heat flux, there are no  
386 common features between Exp-PFSD and Exp-CFSD, suggesting the difference in the  
387 simulation of atmospheric transient systems (Fig. S3f).

388 The ice mass budget in Fig. 3 is not directly related to the evolution of SIA in Fig. 2 since  
389 each process acts differently in changing SIA. For vertical processes (i.e., top melt, basal melt),  
390 ice must be vertically-melted completely to reduce SIA. Lateral melt, on the contrary, can  
391 directly reduce SIA (Smith et al., 2022). Figure 6 shows the evolution of SIA changes due to  
392 thermal processes (top melt, basal melt, lateral melt, frazil ice formation) and dynamical  
393 processes (transport, ridging). For thermal area changes, Exp-PFSD (red line), in general,  
394 shows comparable ice area changes compared to Exp-CFSD (blue line) for most of the period  
395 (Fig. 6a). Compared with Fig. S2g, the timings that Exp-PFSD shows more thermally-increased  
396 ice area correspond to increased frazil ice formation, which primarily occurs in open water. In  
397 contrast to thermal area changes, dynamical area changes of Exp-PFSD tend to reduce ice area  
398 relative to that of Exp-CFSD (Fig. 6e). Dynamically-induced area changes are partly due to the  
399 ridging scheme (Lipscomb et al., 2007) that favors the conversion of thin ice to thicker ice and  
400 reduces total ice area but preserves the total volume. In general, Exp-PFSD has a higher fraction  
401 of ice in the thinner ITD range than Exp-CFSD.

402 Based on geographic features, we define the following subregions for further analysis: 1)  
403 Barents and Greenland Seas (ATL, 45W-60E, 65N-85N), 2) Laptev and Kara Seas (LK, 60E-  
404 150E, 65N-85N), and 3) Beaufort, Chukchi, and East Siberian Seas (BCE, 150E-120W, 65N-  
405 85N, see black boxes in Fig. 1 for the geographic coverage of subregions). The fetches of ATL,

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406 LK, and BCE regions are limited by the surrounding continents and the seasonal evolution of  
407 ice-covered areas. The ATL region is only partially-limited by ice-covered areas while the LK  
408 and BCE regions can be fully-covered by sea ice in winter. Figure 7 shows the evolution of sea  
409 ice extent, sea ice area, domain-averaged significant wave height, melting potential, and heat  
410 flux at the ocean surface ( $FLUX_{OCN}$ , including ice-ocean and atmosphere-ocean interfaces) of  
411 Exp-CFSD and Exp-PFSD. As shown in Fig. 7a-i, it is clear that the higher (lower) significant  
412 wave height corresponds to less (more) regional ice coverage for all subregions. For the melting  
413 potential (Fig. 7j-l), the difference between Exp-CFSD (blue line) and Exp-PFSD (red line) in  
414 August, in general, is correlated with  $FLUX_{OCN}$  in July (Fig. 7m-o). The more (less) incoming  
415 heat flux to the ocean due to less (more) ice-covered area increases (decreases) energy stored  
416 in the ocean surface layer. However,  $FLUX_{OCN}$  alone cannot explain the difference in the  
417 melting potential for the entire period. For example, Exp-PFSD shows more melting potential  
418 after December 2019 in the ATL region (Fig. 7j), and more melting potential in December 2017  
419 in the LK region (Fig. 7k) compared to Exp-CFSD. These timings do not show corresponding  
420  $FLUX_{OCN}$  in the preceding month, suggesting the contribution of different processes. Figure 8  
421 shows the evolution of wave energy dissipation due to whitecapping and the difference of  
422 temperature profile in the upper 150m for Exp-CFSD and Exp-PFSD. As described in section  
423 3, wave energy dissipation increases the turbulent kinetic energy in the surface layer and thus  
424 vertical mixing. Dissipation due to surface wave breaking is zero for most of the period.  
425 Occasionally, there are non-zero dissipations due to surface wave breaking for Exp-CFSD and  
426 Exp-PFSD. The evolution of wave dissipation due to whitecapping (Fig. 8a-c) is in good

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427 agreement with that of significant wave height in Fig. 7g-i. This suggests that stronger wave  
428 conditions associated with less ice-covered areas increase the effect of vertical mixing.  
429 Combined with the warmer upper ocean in Exp-PFSD after January 2020 in the ATL region  
430 and in December 2017 in the LK region in Fig. 8d-e, the strengthened vertical mixing brings  
431 warmer water of the subsurface upward and maintains/increases the melting potential in the  
432 subregions. Figure 8d-f also shows that the warmer signal in the upper ocean (at least to 60m  
433 depth) of Exp-PFSD persists after July 2018 in the ATL region while the LK and BCE regions  
434 show seasonal oscillation of ocean temperature in the upper ocean for the entire simulation.  
435 Combined with the regional SIA shown in Figure 7d-f, seasonal fully ice-covered states in the  
436 LK and BCE regions force the upper ocean to restore to certain states (i.e., near freezing point  
437 under sea ice, near zero melting potential shown in Fig. 7k-l) for both Exp-CFSD and Exp-  
438 PFSD, which might mitigate the effects of ocean wave activities and other processes on the  
439 upper ocean. With less restoring effect by sea ice on the upper ocean in the ATL region, the  
440 difference of thermally-induced mass change between Exp-PFSD and Exp-CFSD shows a  
441 larger variation once the upper ocean difference starts to persist after July 2018 (Fig. 8d, S4d)  
442 while the variations in the LK and BCE regions remain relatively unchanged for the entire  
443 simulation (Fig. S4e-f).

444         Additionally, atmospheric circulation responds to the changes in the spatial distribution of  
445 sea ice (Fig. S1). As shown in Figure S5, Exp-PFSD tends to have anomalous anti-cyclonic  
446 circulations in September compared to Exp-CFSD, but there is no consistent center of action  
447 during the entire period. In March, Exp-PFSD tends to simulate anomalous cyclonic

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448 circulations in the Barents-Kara Sea for most of the years compared to Exp-CFSD, except in  
449 2019. The responses in the atmospheric state in both experiments also influence sea ice  
450 movement, which further contributes to the regional ice differences in Fig. 7a-f, as well as the  
451 heat flux budgets in Fig. S3.

## 452 **4.2 Sensitivity to lateral melting rate parameterization**

453 In addition to the floe size as discussed in the above section, the lateral melting rate ( $w_{lat}$ )  
454 is an important factor contributing to the relative strength of lateral and basal melt. As described  
455 in section 3, we conduct the experiments with the lateral melting rate suggested by Perovich  
456 (1983, P83), and Maykut and Perovich (1987, MP87) (see Table 2), to examine the sensitivity  
457 of Arctic sea ice simulation to different lateral melting rate parameterizations. As shown in Fig.  
458 2b, the simulated summer sea ice area of Exp-LatMelt-C (green line) and Exp-LatMelt-P (grey  
459 line), in general, is larger than those of Exp-CFSD (blue line) and Exp-PFSD (red line).

460 As shown in the sea ice mass budget (Fig. 3a, 3c), Exp-LatMelt-C, which does not include  
461 the friction velocity in the formulation (Equ. 23), but keeps other model configurations same  
462 as Exp-CFSD only shows a slightly larger contribution to lateral melt during summer months  
463 (Fig. S6d). Also, the contribution to basal melt by Exp-LatMelt-C is generally smaller than that  
464 in Exp-CFSD (Fig. S6c). Similar to the experiments with the MP87 scheme, Exp-LatMelt-P  
465 with the prognostic FSD also shows the compensation between lateral melt and basal melt  
466 compared to Exp-LatMelt-C (Fig. 3c, 3d). Exp-LatMelt-P shows stronger lateral melt  
467 compared to Exp-PFSD, which is contributed by the P83 formulation (Fig. S6d). Despite the  
468 stronger lateral melt in Exp-LatMelt-P, its basal melt is smaller compared to Exp-PFSD (Fig.

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469 S6c). Thus, the ocean-induced melt of Exp-LatMelt-P is broadly similar to that of Exp-PFSD.  
470 The result of Exp-LatMelt-P and Exp-PFSD suggests that the changes in lateral and basal melt  
471 due to different lateral melting rate parameterizations are mostly controlled by the available  
472 energy from the ocean (i.e., melting potential).

473 Exp-LatMelt-P simulates more basal growth in winter (Fig. S6f), which is contributed by  
474 more energy loss to the atmosphere (Fig. 5a), in comparison to Exp-PFSD. Also, more frazil  
475 ice formation is simulated in Exp-LatMelt-P than Exp-PFSD during most of the simulation  
476 period (Fig. S6g). The combined effects of the above processes lead to Exp-LatMelt-P showing  
477 less total ice melt in summer and similar ice growth in winter compared to Exp-PFSD (Fig.  
478 S6a). Due to more frazil ice formation, Exp-LatMelt-P shows more thermally-increased ice  
479 area compared to Exp-PFSD (Fig. 6, Fig. S6g). Frazil ice formation reduces open-water areas  
480 and blocks the energy exchange between the atmosphere and the ocean. That is, the upper ocean  
481 under sea ice in Exp-LatMelt-P receives less incoming flux from the atmosphere (i.e., solar  
482 radiation) during April to September (not shown) to balance the energy consumption by ice  
483 melt, which leads to smaller ocean temperature difference compared to Exp-PFSD (Fig. 4c,  
484 green and red lines).

485 Figure 9 shows the spatial distribution of sea ice concentration, sea surface temperature,  
486 and friction velocity in September 2020 for the experiments using MP87 and P83 schemes.  
487 Exp-CFSD, Exp-PFSD, and Exp-LatMelt-C simulate large areas with ice concentration less  
488 than 5% (they are mostly much less than 1%, Fig. 9a-c). In opposite to these three experiments,  
489 Exp-LatMelt-P does not show wide areas with non-zero and infinitesimal ice concentration



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490 (Fig. 9d). Although these areas only account for a tiny fraction of total sea ice, they may still  
491 be a source of uncertainty for sea ice simulations. Ice-existed cells can be influenced by all  
492 processes involved in sea ice mass budget (Fig. 3) while ice-free cells can only be affected by  
493 frazil ice formation and dynamical advection. Under these small-ice areas, SST is well above  
494 the freezing point (Fig. 9e-h) and the friction velocity is mostly less than  $5 \times 10^{-4} \text{ m/s}$  (Fig.  
495 9i-l). In our configuration of the CICE model, the minimum value of friction velocity is set to  
496  $5 \times 10^{-4} \text{ m/s}$ . This suggests that the friction velocity is the limit factor for heat flux  
497 transferred into sea ice in the small-ice areas. For basal heat flux, the formulation in the CICE  
498 model is based on Maykut and McPhee (1995), which is controlled by the friction velocity and  
499 the temperature difference. Thus, basal heat fluxes with small friction velocities may not be  
500 large enough to satisfy the energy convergence (in conjunction with conductive heat flux at the  
501 ice bottom) at the ice-ocean interface to melt ice if the temperature difference does not show a  
502 larger magnitude. Since the MP87 scheme includes the friction velocity, lateral heat flux is also  
503 limited in small-ice areas. Exp-PFSD has a much smaller floe size (compared to 300m) in these  
504 small-ice areas, but the increased strength of lateral melt does not overcome the limitation of  
505 friction velocity to melt ice completely (Fig. 9b). The P83 scheme, which does not include the  
506 friction velocity, is controlled by the temperature difference, but the effect of lateral melting in  
507 Exp-LatMelt-C is largely constrained by constant 300m floe diameter. Liang et al. (2019)  
508 suggested these small-ice areas can be eliminated by assimilating SST observations. The results  
509 of Exp-LatMelt-P suggest a model physic approach that considers the prognostic FSD and the  
510 lateral melting rate to reduce the coverage of small-ice near the ice-edge.

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### 511 4.3 Sensitivity to floe-fracturing parameterization

512 The equally-redistributed formulation (hereafter PF1) for floe-fracturing described in  
513 section 2.3.a does not have preferential floe size after fracturing (i.e., a stochastic process).  
514 However, the size of fractured floes can be predicted based on the properties of surface ocean  
515 waves, particularly wavelength (Dumont et al. 2011; Horvat and Tziperman, 2015). In this  
516 section, we conduct an experiment (Exp-WaveFrac-P, see Table 2), which utilizes a semi-  
517 empirical wave spectrum to redistribute fractured floes (see section 2.3.b for details and  
518 hereafter PF2) to explore the effects of different wave-fracturing formulations on Arctic sea ice  
519 simulation. As shown in Fig. 2c, Exp-WaveFrac-P (orange line) simulates larger SIA in summer  
520 and comparable SIA in winter compared to that of Exp-PFSD (red line).

521 By applying different formulations for floe-fracturing (as well as different lateral melting  
522 rate formulations), the FSD responds accordingly. To quantify the responses of FSD associated  
523 with different physical configurations (Table 2), the representative floe radius  $r_a$ , as well as its  
524 tendency due to different processes in the equation (9) are utilized and calculated as (Roach et  
525 al., 2018a),

$$526 \quad r_a = \frac{\int_{\mathcal{R}} \int_{\mathcal{H}} r f(r, h) dr dh}{\int_{\mathcal{R}} \int_{\mathcal{H}} f(r, h) dr dh} \quad (25)$$

$$527 \quad \frac{dr_a}{dt} = \frac{\int_{\mathcal{R}} \int_{\mathcal{H}} r \frac{df(r, h)}{dt} dr dh}{\int_{\mathcal{R}} \int_{\mathcal{H}} f(r, h) dr dh} \quad (26)$$

528 Figure 10 shows the spatial distribution of the representative floe radius in winter and  
529 summer for all experiments with the prognostic FSD. As described in section 3,  $L(r, h)$  is  
530 initialized by the power law distribution with the exponent as 2.1 for all experiments. Exp-

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531 WaveFrac-P shows a smaller floe radius in the Chukchi and East Siberian Seas and north of  
532 Greenland at the early stage of simulation compared to experiments using PF1 formulation (Fig.  
533 10a-o, upper panel). Small-floe areas in Exp-WaveFrac-P are mostly contributed by the effect  
534 of wave-fracturing where decreasing tendency of floe radius can extend further into the central  
535 Arctic from the Atlantic and the Bering Strait compared to PF1 experiments (Fig. S7). After  
536 September 2016, the representative floe radii of PF experiments emerge, that is, Exp-  
537 WaveFrac-P has a smaller floe size compared to PF1 experiments for both winter and summer  
538 (Fig. 10a-o). In summer, Exp-WaveFrac-P shows mostly fully-fractured floe (<10m, Fig. 10k-  
539 o, bottom panel). The stronger wave-fracturing shown in Exp-WaveFrac-P is partly contributed  
540 by the semi-empirical wave spectrum used in PF2. The simulated wave parameters under ice-  
541 covered area are mostly with  $H_s < 0.01 \text{ m/s}$  and  $T_p > 15 \text{ s}$ . The constructed wave spectrum  
542 and amplitude based on simulated wave parameters under sea ice and equations (17) and (18)  
543 still include the contribution from high-frequency waves ( $T = 2s \text{ bin}$ ), especially in the ice  
544 pack far from the ice edge. The high-frequency waves only account for a small fraction in the  
545 wave period distribution  $\bar{P}(T)$ , and have small wave amplitude  $A(T)$  ( $\sim 7 \times 10^{-4}m$ ). The  
546 strain of the high-frequency bin based on equation (20) still exceeds the yielding strain and  
547 then fractures ice floe into the smallest floe size category. Observational and numerical studies  
548 showed that high-frequency waves rapidly decay and reach the “zero” transmission state for  
549 high-frequency waves when traveling under sea ice (e.g., Collins et al., 2015; Liu et al., 2020).  
550 Despite the over-fracturing behavior shown in Exp-WaveFrac-P, the prevalence of small-floe  
551 does not translate into the stronger ocean-induced ice melt but weaker melt in summer

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552 compared to Exp-PFSD (Fig. 3d-e, Fig. S8e), indicating the limiting role of melting potential.  
553 The weaker ocean-induced ice melt in the summer of Exp-WaveFrac-P corresponds to smaller  
554 ice-ocean heat fluxes (Fig. S9a), which is contributed by both smaller friction velocity and  
555 temperature difference (Fig. S9b-c).

#### 556 **4.4 Sensitivity to wave-attenuation parameterization**

557 We have shown that ocean waves can alter the upper ocean through wave-enhanced  
558 mixing, which may affect sea ice locally (Fig. 8, see section 4.1). The results from PF1 and  
559 PF2 experiments imply that the simulated wave parameters can determine how ice floes are  
560 fractured. As described in section 2.1, we can choose different coefficients in equation (2) to  
561 control the wave attenuation rate of each frequency. In this section, we conduct experiments  
562 using R18 coefficients (see section 3 and Table 2) to study the impacts of wave-attenuation rate  
563 on Arctic sea ice simulation. The simulated sea ice area in Exp-WaveAtt-C (Fig. 2d, light-blue  
564 line) resembles that in Exp-CFSD (Fig. 2d, blue line) before 2019. After 2019, Exp-WaveAtt-  
565 C simulates smaller SIA compared to Exp-CFSD. Since both Exp-CFSD and Exp-WaveAtt-C  
566 use constant floe size, which allows us to neglect the effect of the spatial distribution of floe  
567 size and the MP87 scheme, which makes lateral melt have a negligible contribution (Fig. S10d),  
568 basal melt is the primary factor for the ocean-induced ice melt during the entire period (Fig. 3a,  
569 3f, and Fig. S10e). The strength of basal melt in Exp-WaveAtt-C is weaker than that in Exp-  
570 CFSD from April 2018 to January 2020 (Fig. S10c). Basal growth of Exp-WaveAtt-C is also  
571 smaller than that of Exp-CFSD in the winter of 2018 and 2019 (Fig. S10f). Compared to Exp-  
572 CFSD, Exp-WaveAtt-C shows stronger top melt in the summer of 2018 (Fig. S10b). The

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573 combined effects of the above processes lead to a thinner ice state in Exp-WaveAtt-C before  
574 2019 (Fig. S10a). The thinner state of Exp-WaveAtt-C in the winter of 2019 causes more open  
575 water be created by basal melt (regardless of its smaller magnitude) and thus smaller SIA (Fig.  
576 2d), which is also shown in the thermally-induced ice area changes that Exp-WaveAtt-C has  
577 smaller magnitude in the corresponded period (Fig. 6d). As discussed in section 4.1, top melt  
578 and basal growth is in good agreement with the ice-atmosphere heat flux (Fig. S10, S11a). That  
579 is, ice mass and area changes described above are mainly driven by the ice-atmosphere heat  
580 flux associated with the atmospheric responses to the changes in ocean wave conditions.

581 Different from the M14 experiments, the simulated SIA of Exp-WaveAtt-C (light-blue  
582 line) and Exp-WaveAtt-P (yellow line) show relatively similar evolution during 2016-2020  
583 (Fig. 2d). The R18 coefficients represent weaker wave attenuation relative to the M14  
584 coefficients. Thus, ocean waves in the R18 experiments are expected to transmit further into  
585 the ice pack while maintaining relatively higher wave energy. To quantify to what extent the  
586 ice can be affected by ocean waves, we calculate the wave-affected extent (WAE), which is  
587 defined as the sum of the area of cells with ice concentration greater than 15% and significant  
588 wave height greater than 30cm (Cooper et al., 2022). Figure 11 shows the evolution of WAE  
589 for the M14 and R18 experiments with a 15-day running average to smooth the high-frequency  
590 changes of wave conditions. The weaker attenuation in Exp-WaveAtt-C and Exp-WaveAtt-P  
591 results in generally larger WAE compared to Exp-CFSD and Exp-PFSD (as well as all previous  
592 experiments with M14 coefficients, not shown). The direct impact of larger WAE in Exp-  
593 WaveAtt-P is that the representative floe radius is mostly smaller than 10m (fully-fractured by

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594 ocean waves) (Fig. 10p-t). The decreasing tendency of floe radius due to wave-fracturing is the  
595 dominant factor contributing to the fully-fractured condition (Fig. S7). Similar to Exp-  
596 WaveFrac-P, the fully-fractured condition does not lead to stronger ocean-induced melt due to  
597 limited oceanic energy (Fig. 3b, 3e, 3g, S10e).

## 598 **5. Conclusions and Discussions**

599 This study investigates the impacts of ocean waves on Arctic sea ice simulation based on  
600 a newly-developed atmosphere-ocean-wave-sea ice coupled model, which is built on the  
601 Coupled Arctic Prediction System (CAPS) by coupling the Simulating Waves Nearshore  
602 (SWAN) and the implementation of the modified joint floe size and thickness distribution  
603 (FSTD). A set of pan-Arctic experiments with different configurations of FSD-related  
604 processes are performed for the period 2016-2020. Specifically, we examine the contrasting  
605 behaviors of sea ice between constant and prognostic floe size, the responses of sea ice to  
606 different lateral melting rate formulations, and the sensitivity of sea ice to the simulated wave  
607 parameters under the atmosphere-ocean-wave-sea ice coupled framework.

608 The results of FSD-fixed and FSD-varied experiments show that the simulated sea ice  
609 area is generally lower with smaller floe size associated with physical processes that change  
610 FSD. According to sea ice mass budget analysis, smaller floe size contributes to increased  
611 lateral melt, but its effect is reduced by decreased basal melt. The combined effects of lateral  
612 and basal melt associated with smaller floe size result in relatively more ice melt by the ocean  
613 energy, which is similar to previous studies (e.g., Bateson et al., 2022; Roach et al., 2019; Smith  
614 et al., 2022). The simulations in Smith et al. (2022) with varying lateral melting strength based

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615 on the Community Earth System Model version 2 (CESM2) with a slab-ocean model showed  
616 minimal change in frazil ice formation. In our simulation with a full ocean model, the enhanced  
617 ice melt by the ocean, though it is partially balanced by increased frazil ice formation due to  
618 the depletion of melting potential in the surface layer. This suggests negative feedback from  
619 the full ocean physics. Our simulations also show that the prevalence of small floes does not  
620 necessarily lead to stronger ice melting due to limited oceanic energy. To further illustrate the  
621 constraint role of limited oceanic energy, the mixed layer depths (MLDs) based on 0.1 degree  
622 Celsius difference relative to the surface temperature (e.g., Courtois et al., 2017, their Table 2)  
623 for Exp-CFSD and Exp-PFSD are shown in Figure 12. In general, Exp-CFSD and Exp-PFSD  
624 (as well as other experiments, not shown) exhibit similar evolution of MLD, that is MLD is  
625 deeper (up to 150m) in March and shallower (up to 80m) in September. MLD in the open  
626 waters is broadly similar across all experiments and MLD near the ice edge (15% ice  
627 concentration, black contour in Fig. 12) is shallower (10-30m) relative to other areas. In March,  
628 MLDs under ice-covered areas become deeper as lead time increases. To calculate the heat  
629 content within MLD, the same approach for calculating melting potential in the ROMS model  
630 is used, which is defined as the vertical integral from the surface to MLD of the difference  
631 between ocean temperature and freezing point. The calculated values of heat content and  
632 melting potential have the same unit ( $W/m^2$ ) and directionality (positive downward) as ice-  
633 ocean heat flux, and they represent the “maximum” heat flux that the ice can extract. Figures  
634 13 and 14 show the heat content of MLD and melting potential for Exp-CFSD and Exp-PFSD  
635 in March and September. As shown in Fig. 13-14, Exp-PFSD shows less melting potential (0-

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636 5m) and the heat content within MLD under ice-covered areas compared to Exp-CFSD. This  
637 feature is more pronounced in September than in March. Also, heat content in MLD near the  
638 ice edge of Exp-PFSD reduces more than other ice-covered areas compared to that of Exp-  
639 CFSD, suggesting the role of ice-ocean heat flux. Figures 13 and 14 further support the  
640 constraint role of limited oceanic energy to ice melting with respect to varied floe size not only  
641 in the surface layer (i.e., melting potential) but also in the mixed layer.

642 Our fully-coupled simulations also show that atmospheric states respond to changing ice  
643 distributions and then modify the energy budget at the ice surface that determines top melt in  
644 summer and basal growth in winter. The FSD-varied experiments, in general, show more  
645 energy loss from ice to the atmosphere in winter, and all experiments show year-to-year  
646 variations of energy gain for sea ice in summer.

647 The depletion of ocean energy in the surface layer as well as enhanced frazil ice formation  
648 are the direct responses to the changes of ice-ocean coupling with the prognostic FSD. The  
649 fractured sea ice enlarges the ice-ocean heat flux while the freezing temperature is still  
650 determined by the sea surface salinity in the ocean model. However, the local salinity at the  
651 ice-ocean interface can be significantly lower than sea surface salinity, and thus higher freezing  
652 temperature locally due to the meltwater from sea ice (e.g., the false-bottom, Notz et al., 2003).  
653 Schmidt et al. (2004) proposed the ice-ocean heat flux formulation that considers the local  
654 salinity equilibrium but its formulation is only for the ice-bottom interface. The generalization  
655 of ice-ocean heat flux with the consideration of local salinity equilibrium for both bottom and  
656 lateral interface might yield a more realistic ice-ocean coupled simulation. Although the lateral



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657 melting rate formulation does not have a major effect on the simulated floe size distribution,  
658 the simulated sea ice area and ice mass budget are sensitive to the choice of the formulation.  
659 The lateral melting rate formulations applied in this study as well as previous laboratory results  
660 are not related to the ice properties (i.e., ice thickness and floe size, Josberger and Martin, 1981;  
661 Maykut and Perovich, 1987; Perovich, 1983). A recent laboratory study suggested that the  
662 lateral melting rate is a function of temperature difference and the ratio of floe size to ice  
663 thickness (Li et al., 2021). Smith et al. (2022) also suggested that Arctic sea ice simulation can  
664 be sensitive to the lateral melting rate of Perovich (1983) with different weights on each ice  
665 thickness category. Further studies are required to investigate improved lateral melting rate  
666 parameterization with observational constraints (e.g., data from the MOSAiC campaign in  
667 2020, Nicolaus et al., 2021) within the prognostic FSD framework.

668 As discussed in Horvat and Tziperman (2015), the FTSD is sensitive to the wave  
669 attenuation coefficients. Our simulations also show substantially contrasting behaviors in the  
670 simulated floe size distribution associated with simulated wave parameters, suggesting that  
671 several aspects need further investigation. First, the empirical wave attenuation (i.e., IC4M2)  
672 may have reasonable performance in simulating the changes of wave energy spectrum locally  
673 with specific ice conditions (e.g., Liu et al., 2020). However, the dissipation of wave energy  
674 varies spatially for the pan-Arctic (as well as pan-Antarctic) scale simulation with the different  
675 sea ice properties (i.e., ice concentration, ice thickness, floe size). Thus, a viscous boundary  
676 layer model (Liu et al., 1991) or a viscoelastic model (Wang and Shen, 2010) for wave  
677 attenuation, which provides spatially-varied wave attenuation with respect to sea ice properties,

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678 might be able to give more realistic simulations in the wave-fracturing process and thus the  
679 floe size distribution. Also, the current implementation of sea ice effects in the SWAN model  
680 does not include the reflection and scattering due to sea ice, which redistributes the wave energy  
681 spatially and potentially changes the wave-fracturing behavior. Second, the probability of floe-  
682 fracturing  $Q(r)$  in both formulations applied in this study are uncertain. Both formulations  
683 result in floe-fracturing into smaller floe size categories within a short time interval as long as  
684 the simulated wave parameters satisfy the yielding strain. This strong contribution in the wave-  
685 fracturing term is not easily balanced by the floe-welding term. The floe-welding term (Roach  
686 et al., 2018a, b) acts to reduce the floe number density so that it is less effective in increasing  
687 the representative floe radius if the floe is mostly fractured with the smallest floe size. Third,  
688 the attenuated wave energy by sea ice does not influence sea ice conditions in this study. As  
689 suggested by Longuet-Higgins and Steward (1962), the attenuated wave energy is transferred  
690 into the ocean (as we described in section 3 for wave-enhanced mixing) or sea ice. For sea ice,  
691 the transferred energy acts as a stress, called wave radiation stress (WRS), pushing sea ice to  
692 the direction of wave propagation. By including the WRS in the momentum equation of ice,  
693 the WRS then can affect sea ice drift (e.g., Boutin et al., 2020).

694 For quantitative applications (e.g., forecasting sea ice), more observations (especially  
695 ocean waves under sea ice and FSD) are needed to reduce uncertainties in the atmosphere-  
696 ocean-wave-sea ice coupled model, particularly wave-related processes in ice-covered regions.  
697 Horvat et al. (2019) developed a new technique to retrieve pan-Arctic scale FSD climatology  
698 and seasonal cycle from CryoSat-2 radar altimeter and this method can resolve floe size from

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699 300 m to 100 km and potentially up to 20 m scale if applied to ICESat-2 data. ICESat-2  
700 altimetry also provides a new opportunity to observe ocean waves in sea ice at hemispheric-  
701 scale coverage by directly observing the vertical displacements of the ice surface (e.g., Horvat  
702 et al., 2020). In situ observations, despite their limited spatial coverage, are valuable wave  
703 spectra measurements for wave-physics validation and improvement (e.g., Cooper et al., 2022;  
704 Liu et al., 2020).  
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706 Code and data availability: The outputs of pan-Arctic simulations analyzed in this study  
707 are archived at <https://doi.org/10.5281/zenodo.7922725>.

708

709 Author contributions: CYY and JL designed the model experiments, developed the  
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711 the results. DC provided constructive feedback on the manuscript.

712

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714

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1097 **7. Tables**

1098 Table 1 The summary of physic parameterizations used in all pan-Arctic simulations.

|                         |   |
|-------------------------|---|
| WRF physics             |   |
| Cumulus                 | Grell-Freitas (Freitas et al. 2018)   |
| Microphysics            | Morrison 2-moment (Morrison et al. 2009)  |
| Longwave radiation      | CAM spectral band scheme (Collins et al. 2004)  |
| Shortwave radiation     | CAM spectral band scheme (Collins et al. 2004)  |
| Boundary layer          | MYNN (Nakanishi and Niino, 2009)  |
| Land surface            | Unified Noah LSM (Chen and Dudhia, 2001)  |
| ROMS physics            |   |
| Tracer advection        | Upwind third-order horizontal advection (U3H; Shchepetkin, and McWilliams, 2005)<br>Centered fourth-order vertical advection (C4V; Shchepetkin, and McWilliams, 2005) |
| Tracer vertical mixing  | Generic Length-Scale scheme (Umlauf and Burchard, 2003)   |
| CICE physics            |   |
| Ice dynamics            | EVP (Hunke and Dukowicz, 1997)  |
| Ice thermodynamics      | Bitz and Lipscomb (1999)  |
| Shortwave albedo        | Delta-Eddington (Briegleb and Light, 2007)  |
| SWAN physics            |   |
| Exponential wind growth | Komen et al. (1984)   |
| Whitecapping            | Komen et al. (1984)   |
| Quadruplets             | Hasselmann et al. (1985)  |
| Depth-induced breaking  | Battjes and Janssen (1978)  |
| Bottom friction         | Madsen et al. (1988)  |
| Sea ice dissipation     | Collins and Rogers (2017); Rogers (2019)  |

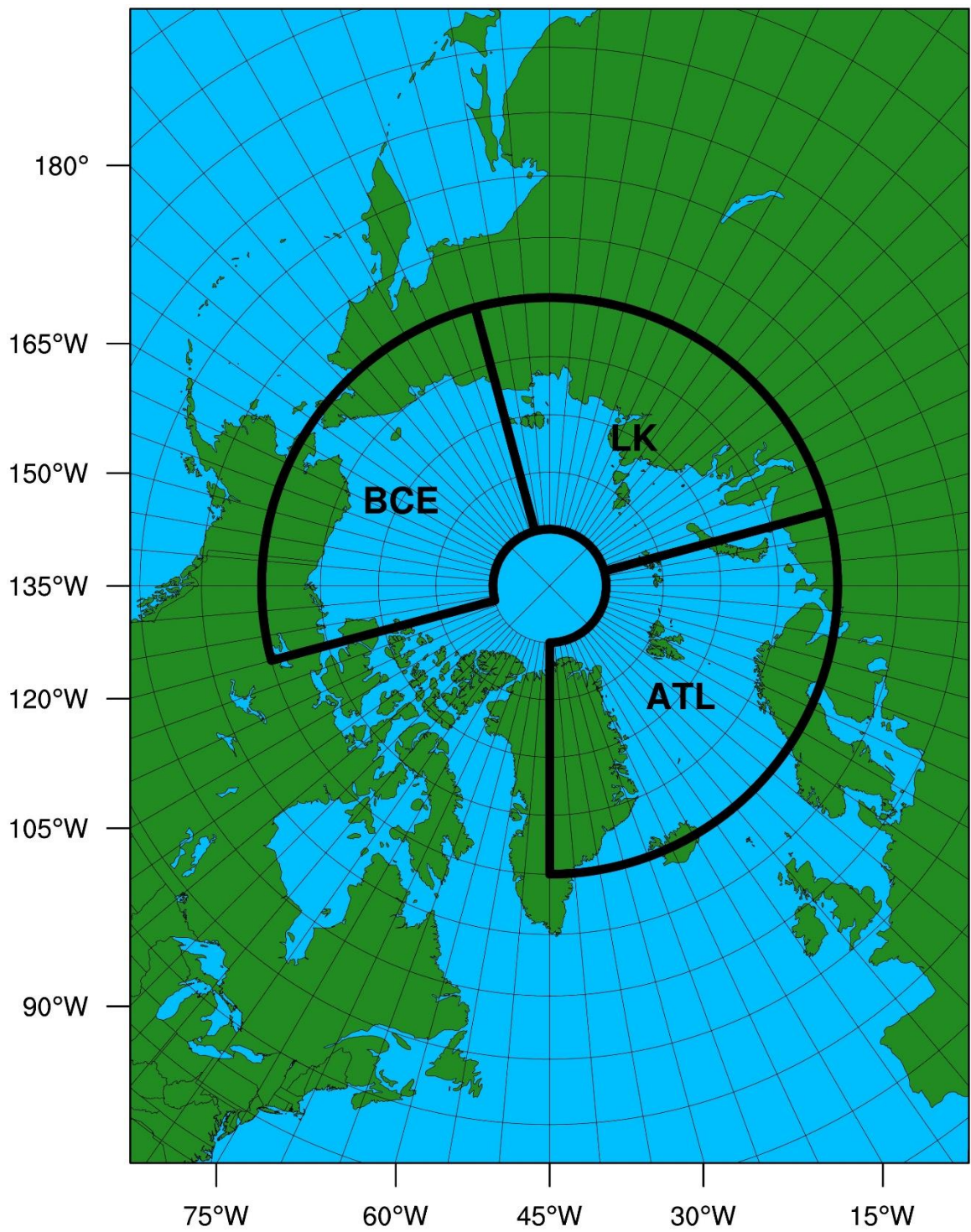
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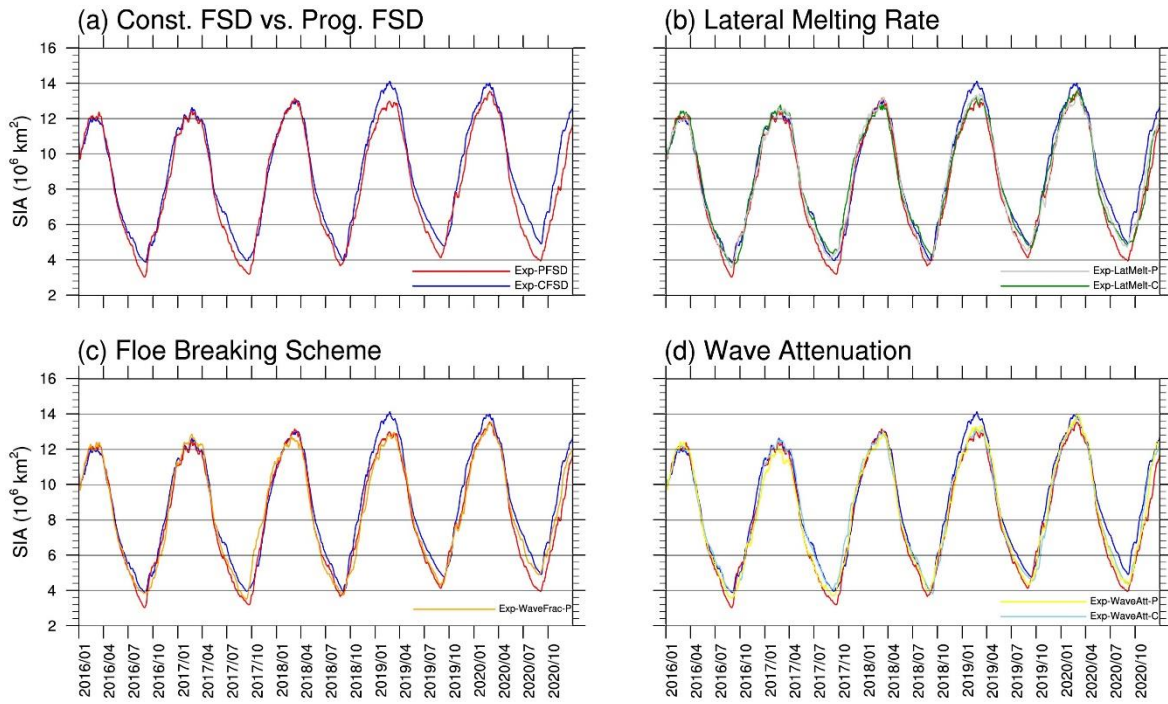
1101 Table 2 The summary of the experiments conducted in this study and their main changes in the  
 1102 experiment design. MP87: Maykut and Perovich (1987). P83: Perovich (1983). M14: Meylan  
 1103 et al. (2014). R18: Rogers et al. (2018).

| Experiment     | Floe size   | Lateral melting rate | Wave fracturing formulation | Wave attenuation coefficients |
|----------------|-------------|----------------------|-----------------------------|-------------------------------|
| Exp-CFSD       | Const. 300m | MP87                 | None                        | M14                           |
| Exp-PFSD       | FSTD        | MP87                 | Equally (PF1)               | M14                           |
| Exp-LatMelt-C  | Const. 300m | P83                  | None                        | M14                           |
| Exp-LatMelt-P  | FSTD        | P83                  | Equally (PF1)               | M14                           |
| Exp-WaveFrac-P | FSTD        | MP87                 | Bretschneider (PF2)         | M14                           |
| Exp-WaveAtt-C  | Const. 300m | MP87                 | None                        | R18                           |
| Exp-WaveAtt-P  | FSTD        | MP87                 | Equally (PF1)               | R18                           |

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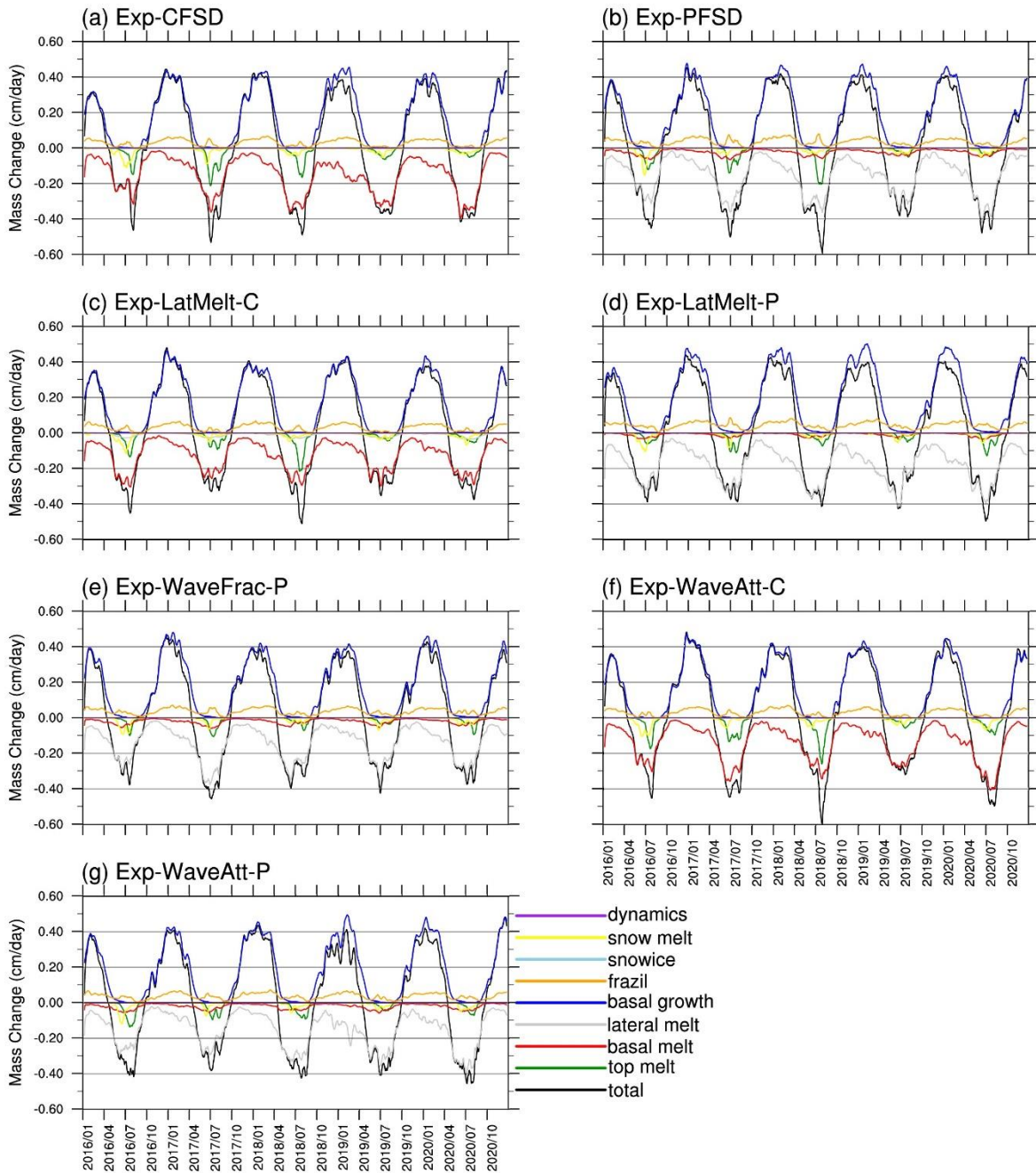
1107  
1108 Figure 1 The model domain used in CAPS for pan-Arctic sea ice simulations. Black boxes  
1109 indicate the subregions for analysis performed in this study.  
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1112 Figure 2 Time-series of Arctic sea ice area for Exp-CFSD (blue line), Exp-PFSD (red line),  
 1113 Exp-LatMelt-C (green line), Exp-LatMelt-P (grey line), Exp-WaveFrac-P (orange line), Exp-  
 1114 WaveAtt-C (light-blue line) and Exp-WaveAtt-P (yellow line).  
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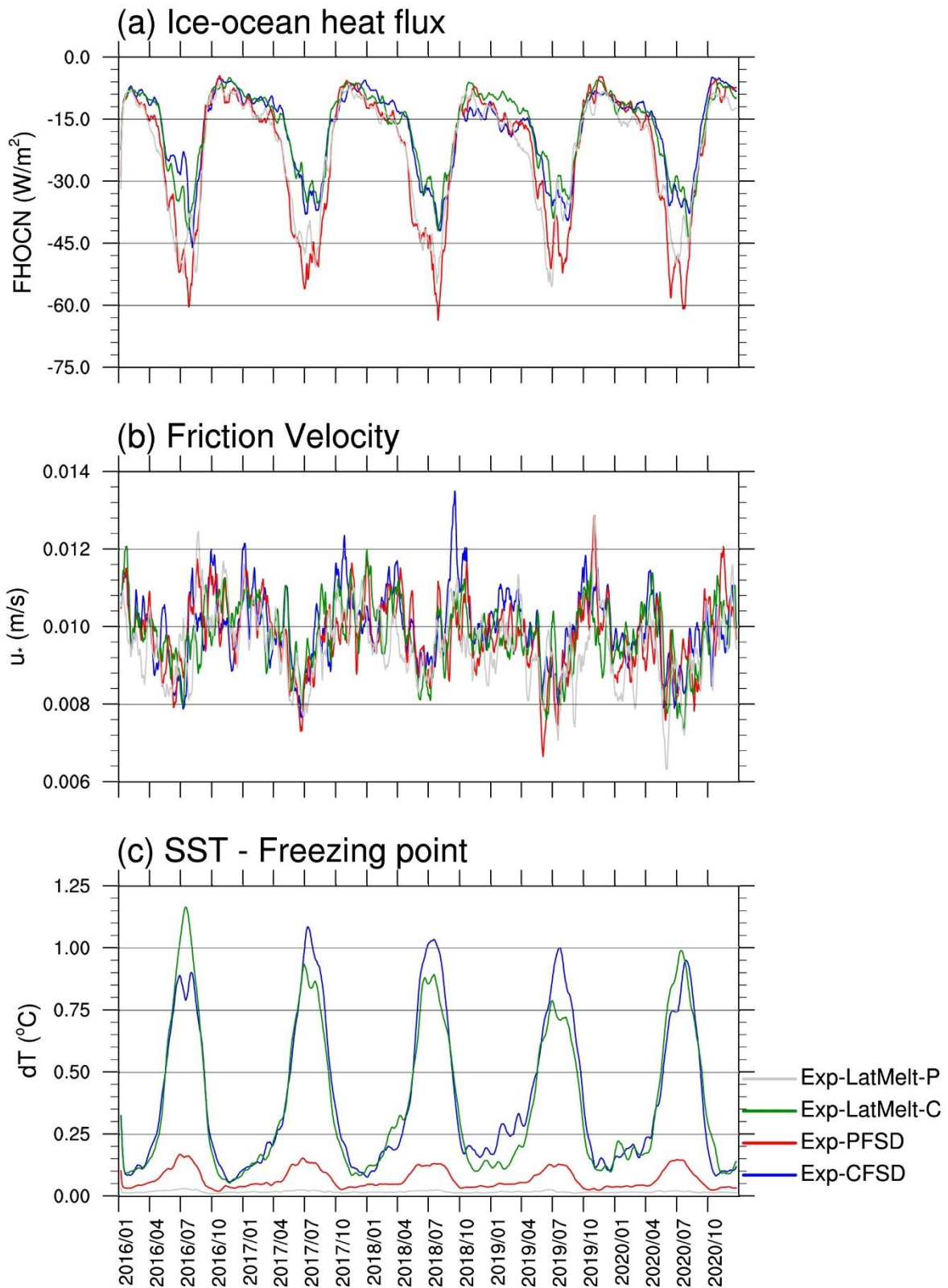




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1117 Figure 3 Time-series (15-day running-averaged) of sea ice mass budget terms for (a) Exp-  
 1118 CFSD, (b) Exp-PFSD, (c) Exp-LatMelt-C, (d) Exp-LatMelt-P, (e) Exp-WaveFrac-P, (f) Exp-  
 1119 WaveAtt-C, and (g) Exp-WaveAtt-P. Ice mass budget terms include: total mass change (black  
 1120 line), sea ice melt at the air-ice interface (top melt, green line), sea ice melt at the bottom of the  
 1121 ice (basal melt, red line), sea ice melt at the sides of the ice (lateral melt, grey line), sea ice  
 1122 growth at the bottom of the ice (basal growth, blue line), sea ice growth by supercooled open  
 1123 water (frazil, orange line), sea ice growth due to transformation of snow to sea ice (snowice,  
 1124 light-blue line), and sea ice mass change due to dynamics-related processes (dynamics, purple  
 1125 line) (Notz et al., 2016; Yang et al., 2022). For reference, snow melt term (yellow line) is  
 1126 included.





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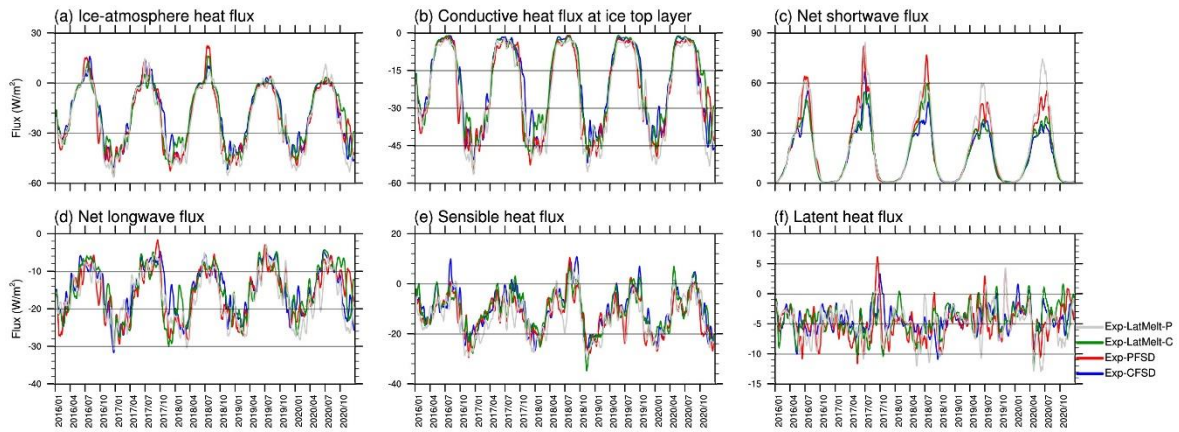
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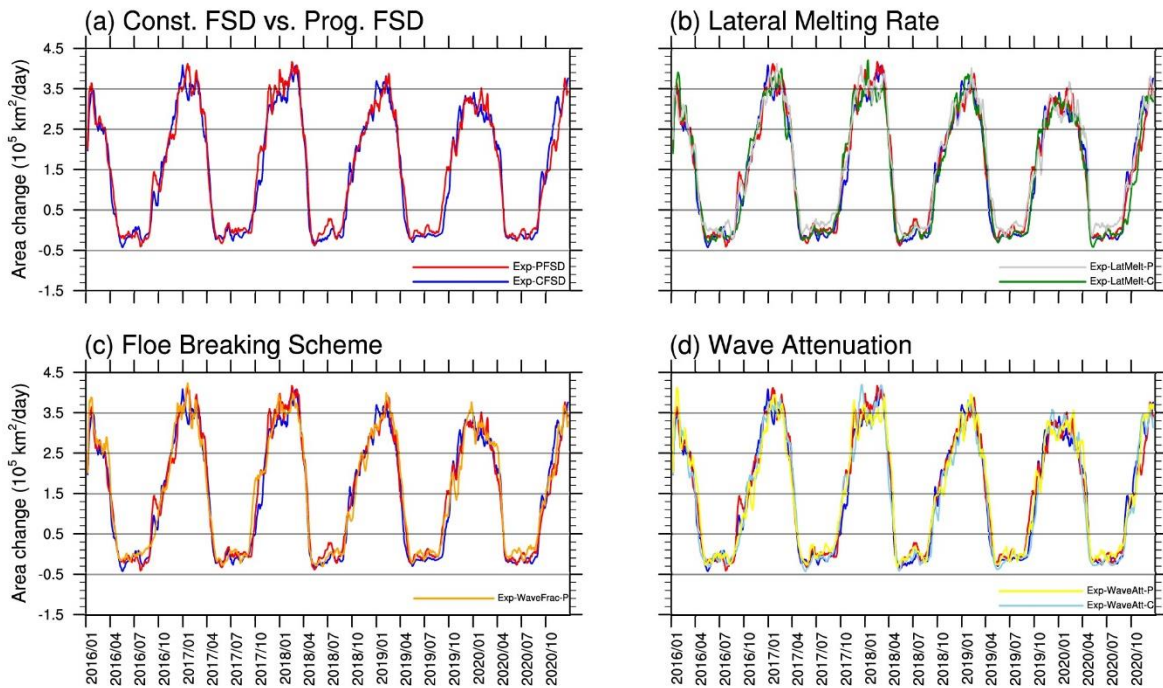
Figure 4 Time-series (15-day running-averaged) of (a) ice-ocean heat flux, (b) friction velocity at ice-ocean interface, and (c) the temperature difference between SST and freezing point for Exp-CFSD (blue line), Exp-PFSD (red line), Exp-LatMelt-C (green line), and Exp-LatMelt-P (grey line). Note: (a) is positive downward and weighted by ice concentration.



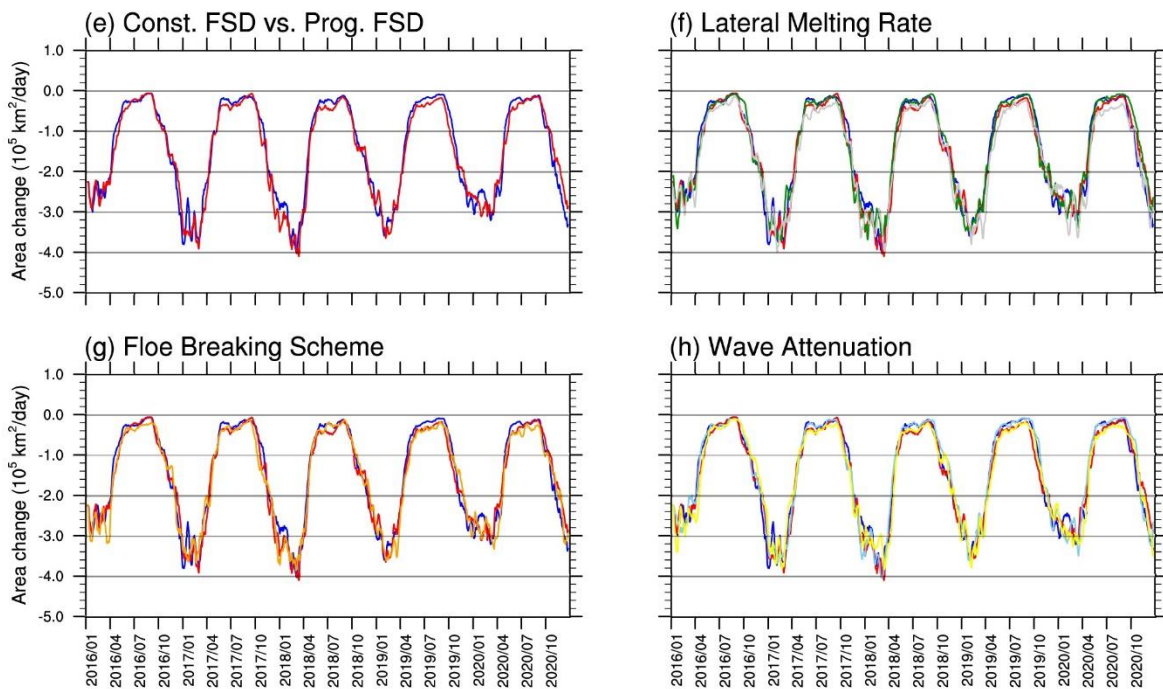
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Figure 5 Time-series (15-day running-averaged) of (a) ice-atmosphere heat flux, (b) conductive heat flux at the ice top layer, (c) net shortwave flux, (d) net longwave flux, (e) sensible heat flux, and (f) latent heat flux for Exp-CFSD (blue line), Exp-PFSD (red line), Exp-LatMelt-C (green line), and Exp-LatMelt-P (grey line). Note: (a)-(e) are positive downwards and weighted by ice concentration.

## Thermal Area Changes

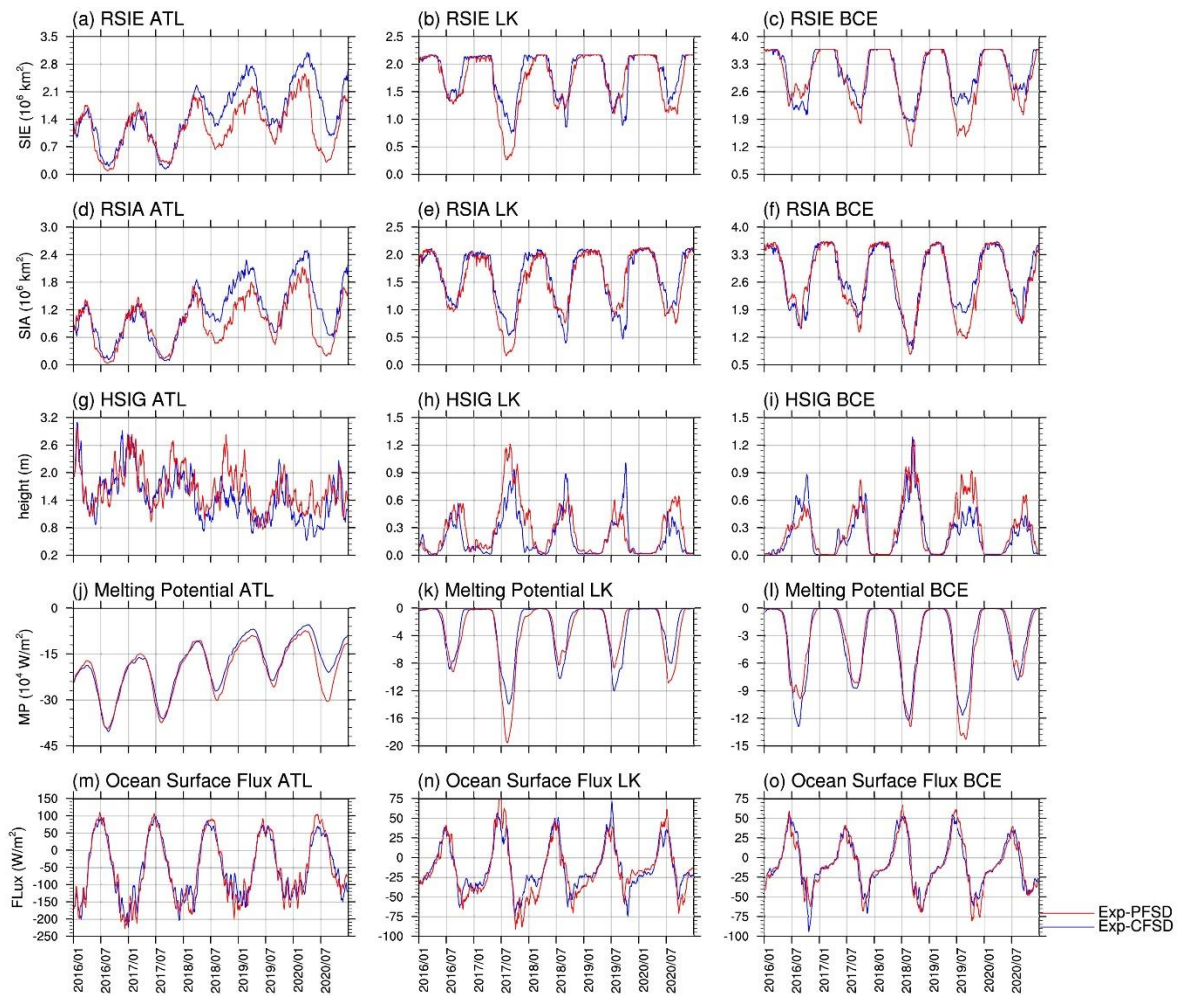


## Dynamical Area Changes



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1140 Figure 6 Time-series (15-day running-averaged) of sea ice area changes due to thermal  
 1141 processes (a-d, upper panel) and dynamical processes (e-h, bottom panel) for Exp-CFSD (blue  
 1142 line), Exp-PFSD (red line), Exp-LatMelt-C (green line), Exp-LatMelt-P (grey line), Exp-  
 1143 WaveFrac-P (orange line), Exp-WaveAtt-C (light-blue line) and Exp-WaveAtt-P (yellow line).

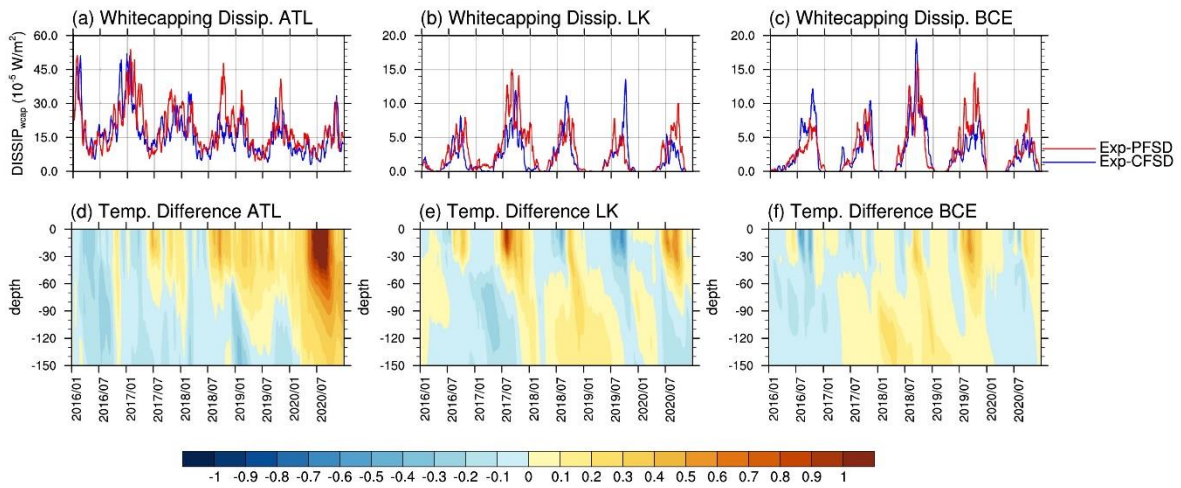


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Figure 7 Time-series of (a-c) ice extent, (d-f) ice area, (g-i) significant wave height, (j-l) melting potential, and (m-o) heat flux at the ocean surface in ATL, LK, and BCE regions for Exp-CFSD (blue line) and Exp-PFSD (red line). Note: significant wave height, melting potential, and heat flux at the ocean surface are region-averaged and 15-day running-averaged values.



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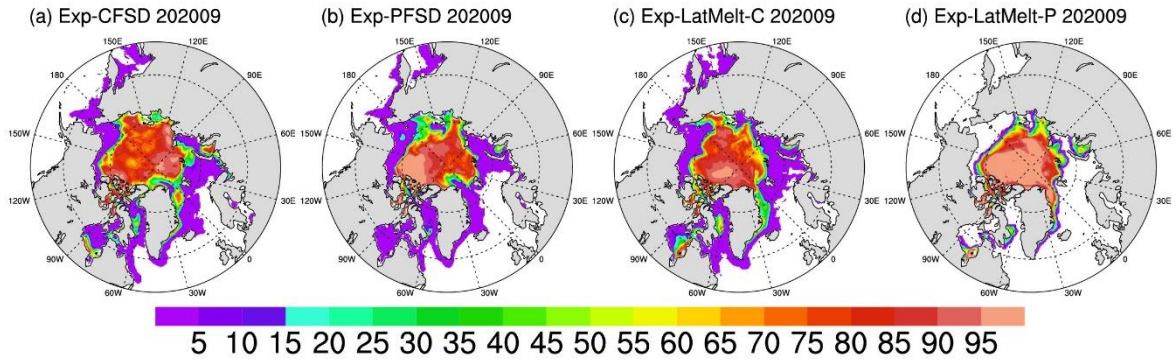
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1152 Figure 8 Time-series (15-day running-averaged) of white capping dissipation averaged over (a)  
1153 ATL, (b) LK, and (c) BCE regions for Exp-CFSD (blue line) and Exp-PFSD (red line), and the  
1154 temperature profile difference between Exp-CFSD and Exp-PFSD in the upper 150 m averaged  
1155 over (d) ATL, (e) LK, and (f) BCE regions.

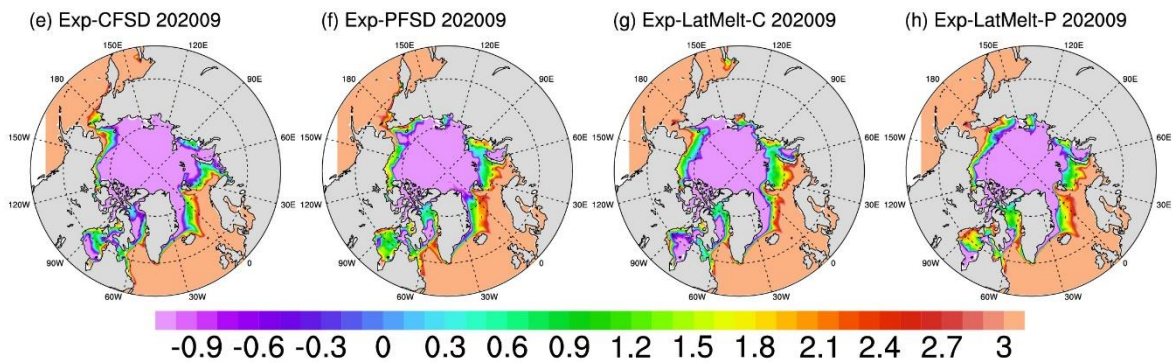
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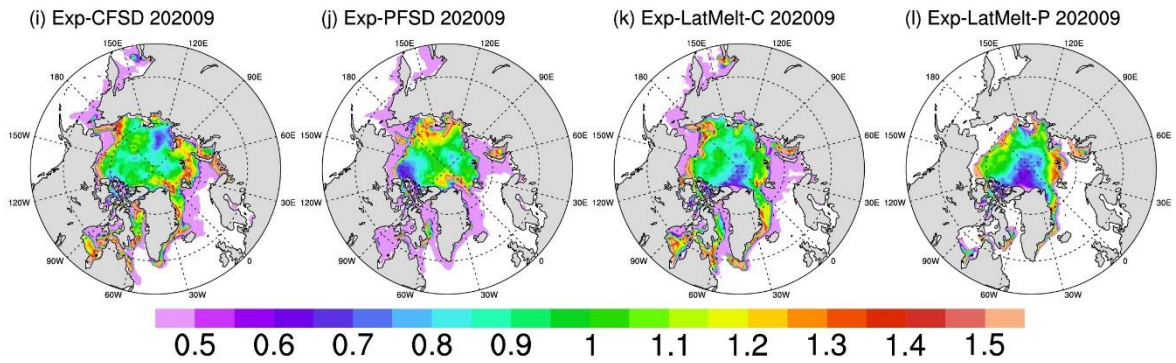
## Sea Ice Concentration (1)



## Sea Surface Temperature (°C)



## Friction Velocity ( $10^{-3}$ m/s)



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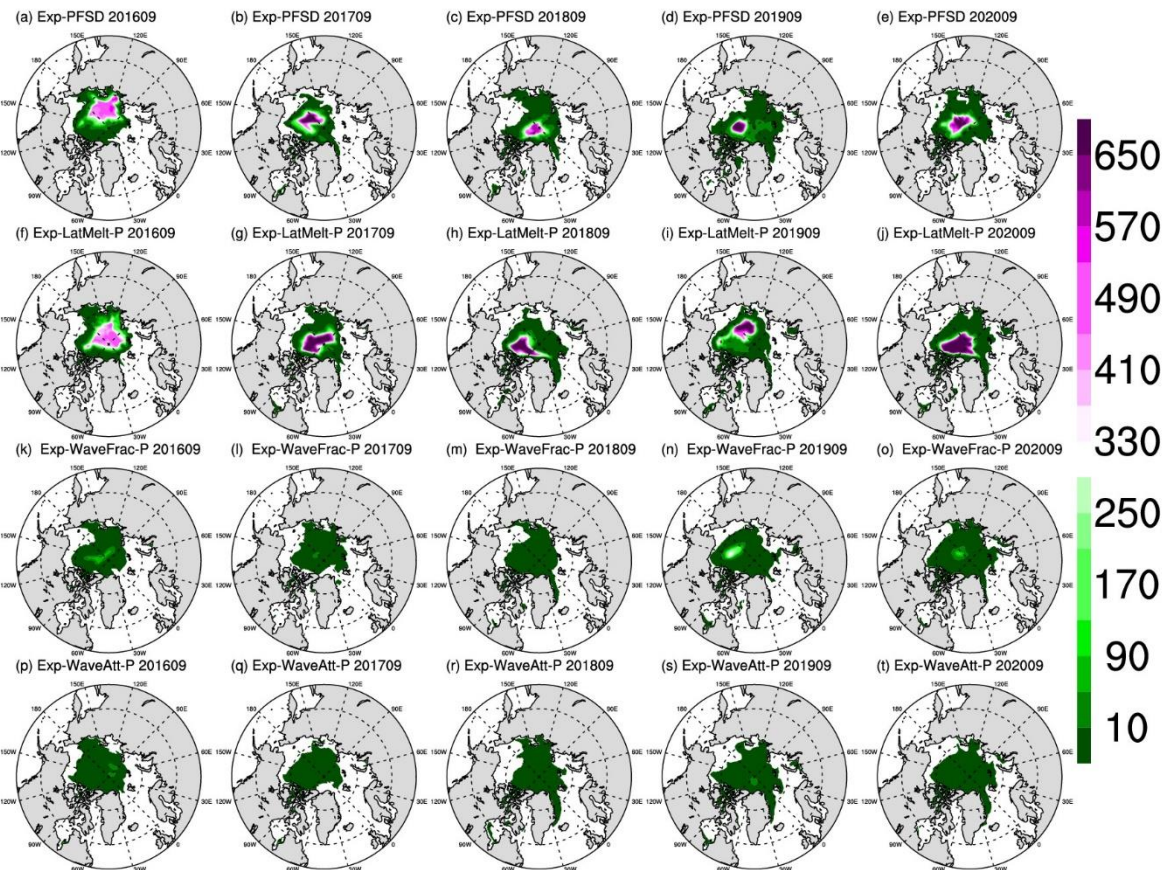
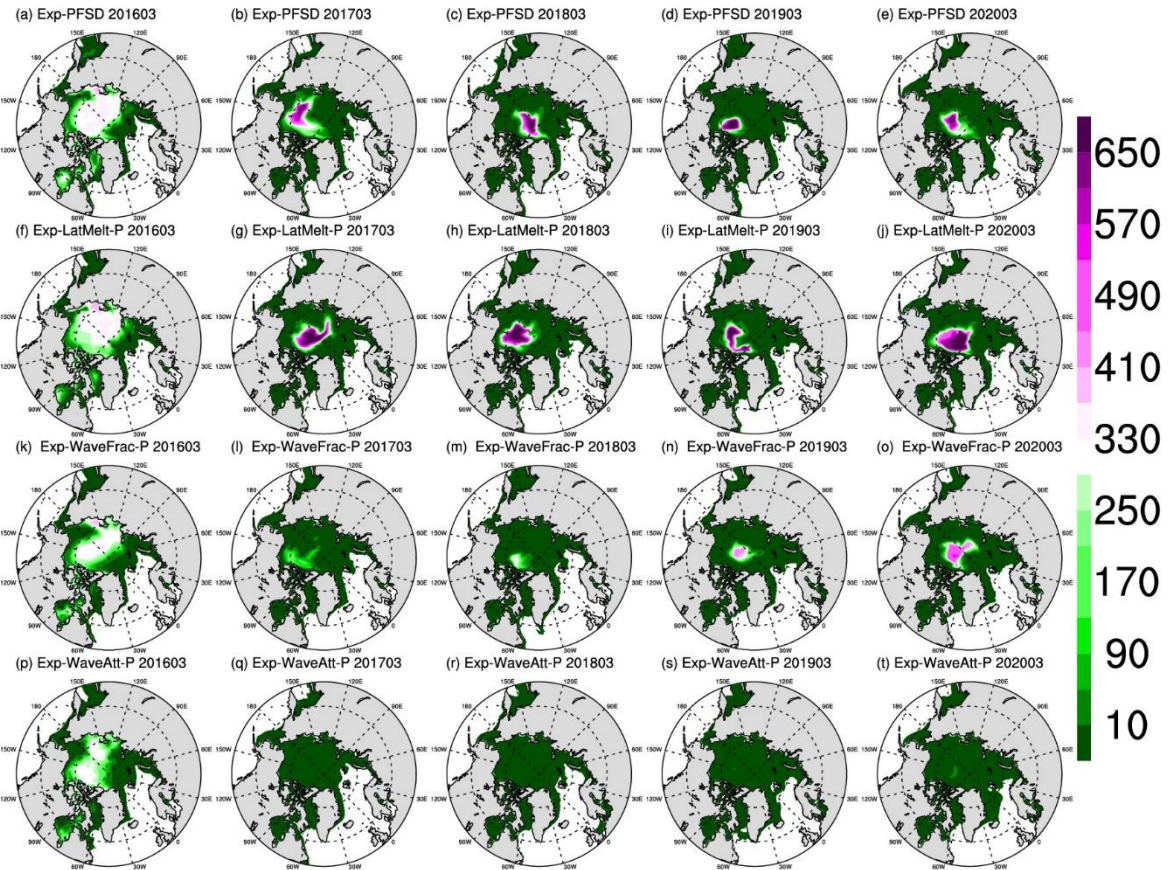
1159 Figure 9 The monthly-mean of (a-d) sea ice concentration, (e-h) sea surface temperature, and

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1161 LatMelt-P.

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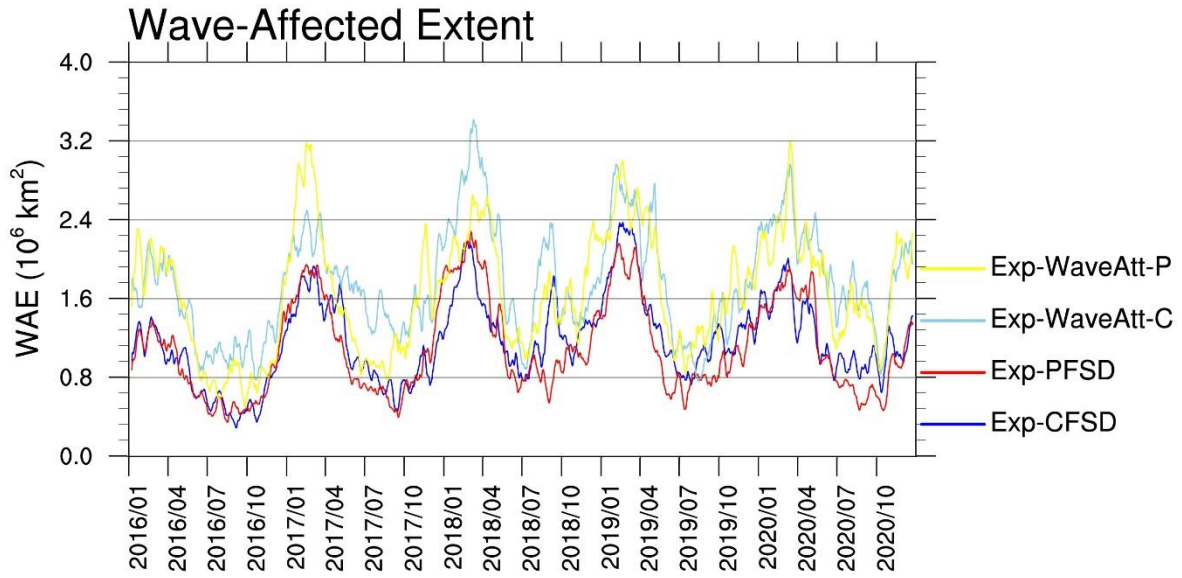






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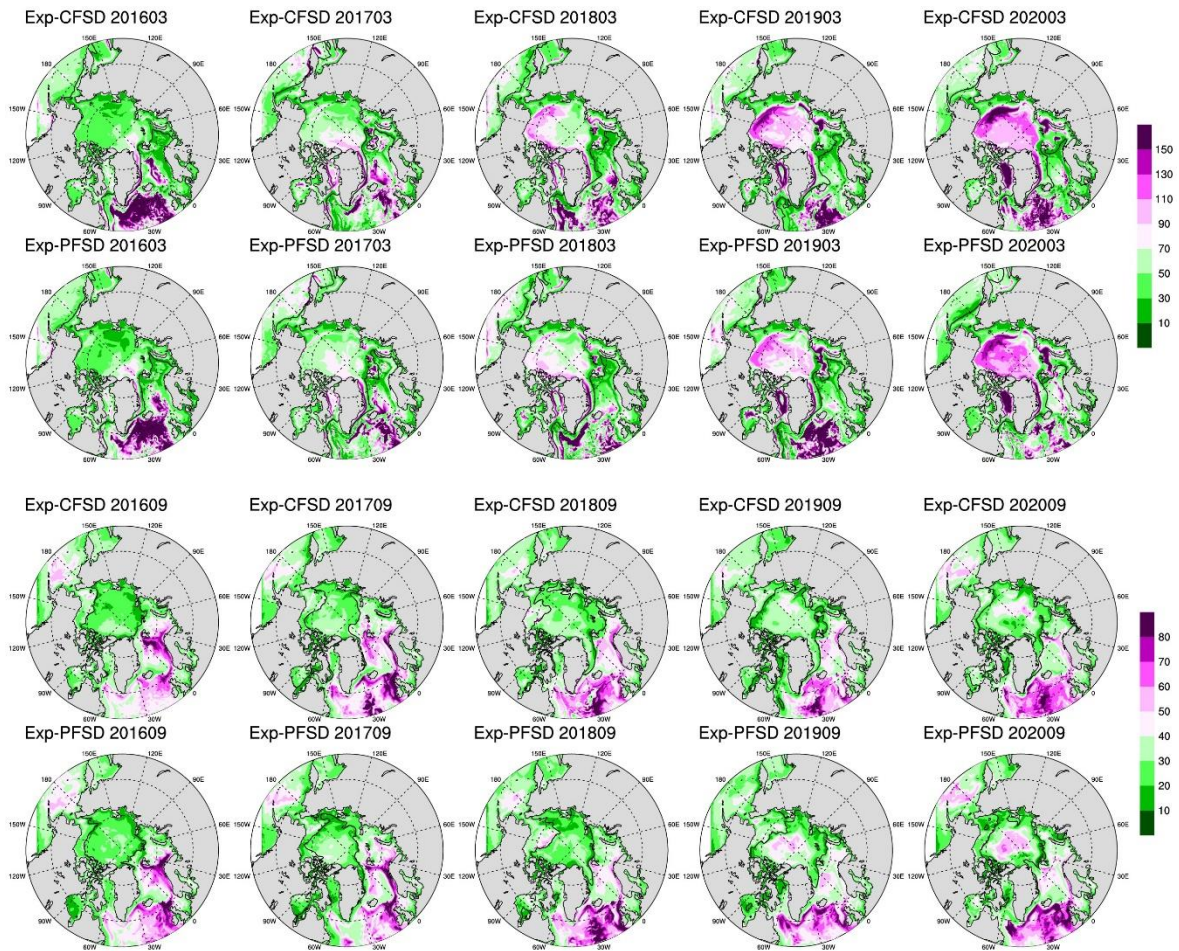
1164 Figure 10 The spatial distribution of the representative floe radius in March (upper panel) and  
1165 September (bottom panel) of (a-e) Exp-PFSD, (f-j) Exp-LatMelt-P, (k-o) Exp-WaveFrac-P, and  
1166 (p-t) Exp-WaveAtt-P for 2016-2020. Note: cells with less than 15% ice concentration are  
1167 treated as missing values.  
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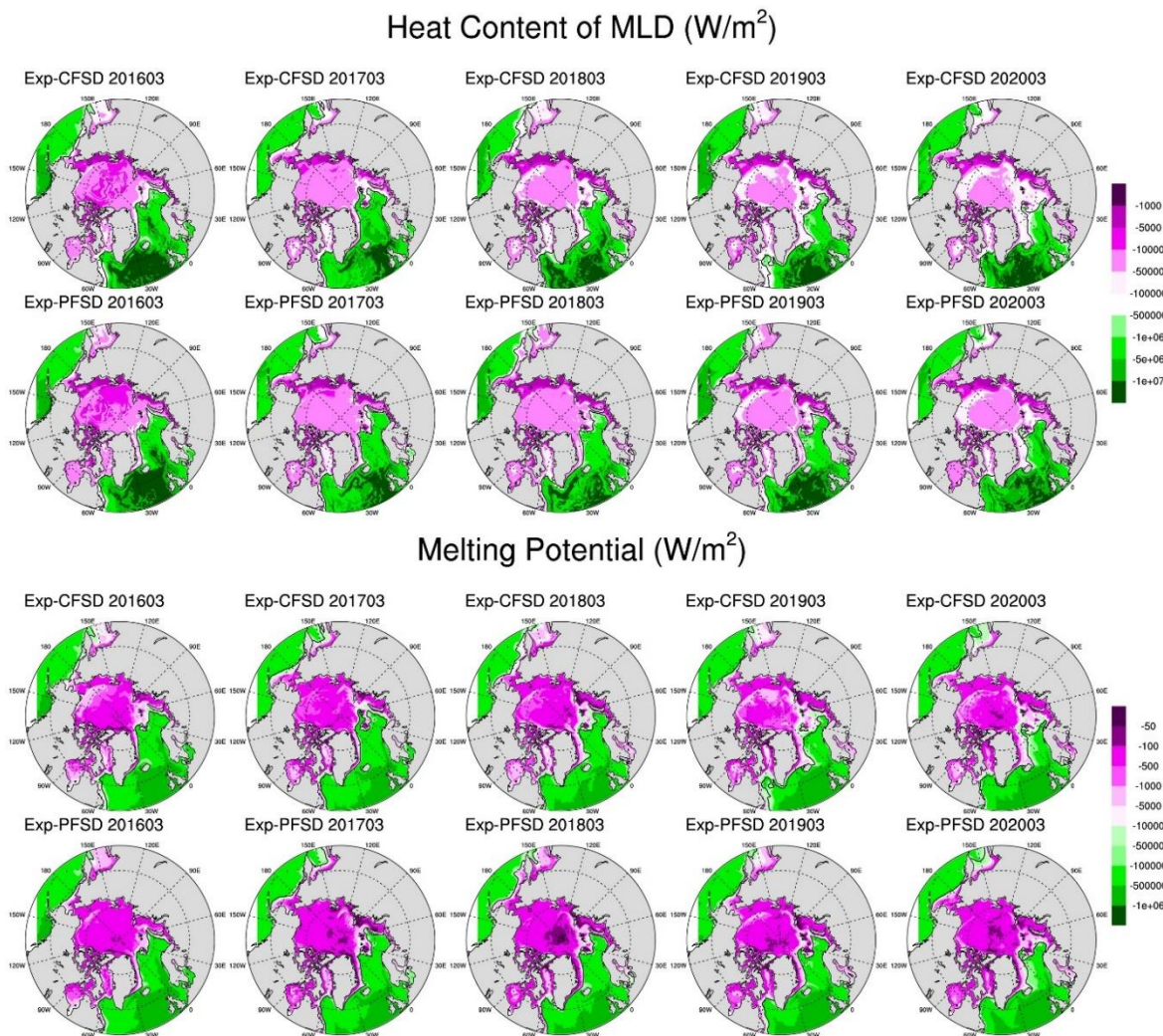
1170 Figure 11 Time-series (15-day running-averaged) of Arctic wave-affected extent for Exp-CFSD  
 1171 (blue line), Exp-PFSD (red line), Exp-WaveAtt-C (light-blue line) and Exp-WaveAtt-P (yellow  
 1172 line).

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Figure 12 Monthly mean of MLD in March (top panel) and September (bottom panel) of Exp-CFSD and Exp-PFSD for 2016-2020. Note: the black contour represents the average location of 15% ice concentration.

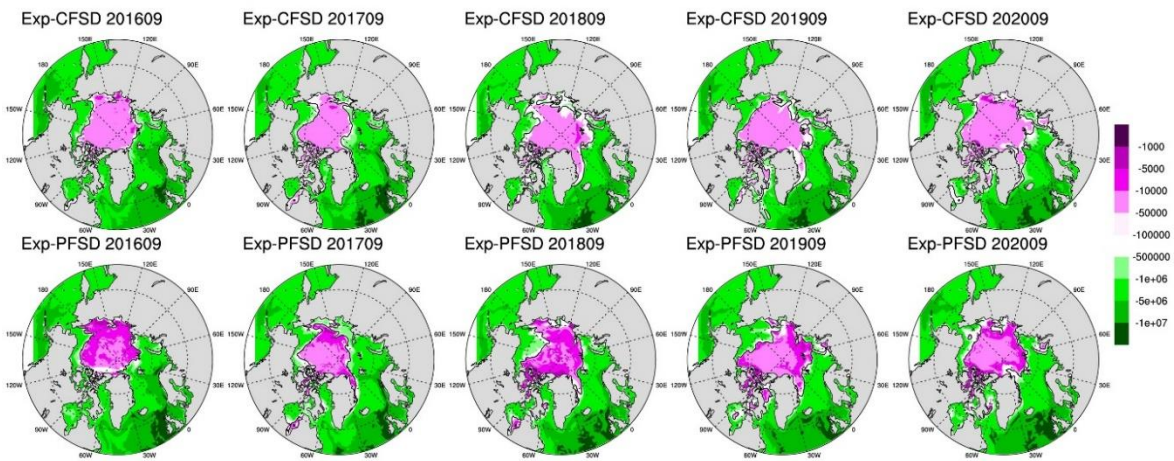


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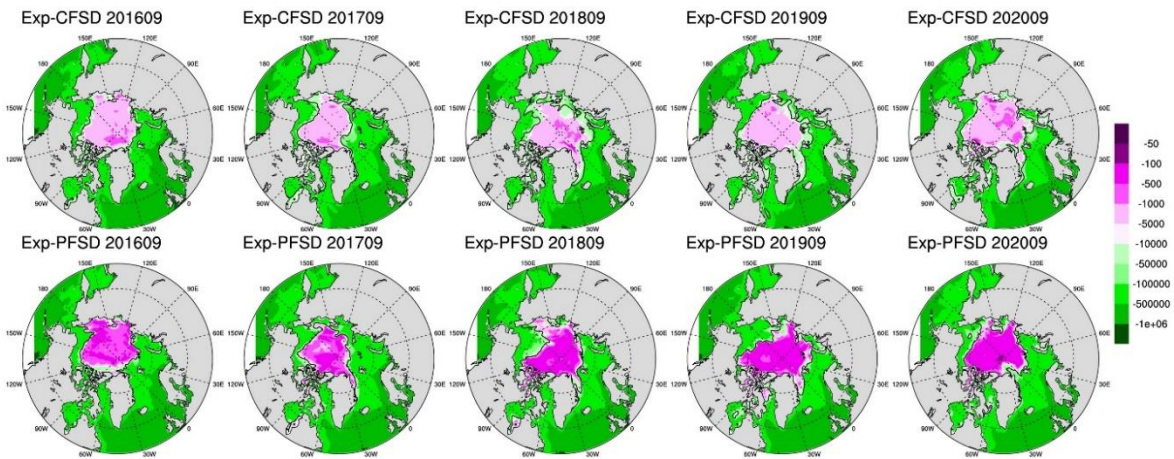
Figure 13 March-averaged heat content of MLD (top panel) and melting potential (bottom panel) of Exp-CFSD and Exp-PFSD for 2016-2020. Note: the black contour represents the average location of 15% ice concentration.



### Heat Content of MLD ( $W/m^2$ )



### Melting Potential ( $W/m^2$ )



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Figure 14 Same as Figure 13, but for September-averaged values.