

1 A computationally efficient statistically downscaled 100 m resolution 2 Greenland product from the regional climate model MAR

3 Marco Tedesco^{1,2}, Paolo Colosio³, Xavier Fettweis⁴ and Guido Cervone⁵

4 ¹Lamont-Doherty Earth Observatory, Columbia University, New York, 10964, USA

5 ²NASA GISS, New York, 10025, USA

6 ³Department of Civil, Environmental, Architectural Engineering and Mathematics, University of Brescia, Brescia, 25123, Italy

7 ⁴Department of Geography, SPHERES research unit, University of Liège, Liège, 4000, Belgium

8 ⁵Institute for Computational and Data Sciences and Earth and Environmental Systems Institute, The Pennsylvania State
9 University, University Park, PA, 16801, USA

10 *Correspondence to:* Marco Tedesco (mtedesco@ldeo.columbia.edu)

11 **Abstract.** The Greenland Ice Sheet (GrIS) has been contributing directly to sea level rise and this contribution is projected to
12 accelerate over the next decades. A crucial tool for studying the evolution of surface mass loss (e.g., surface mass balance,
13 SMB) consists of regional climate models (RCMs) which can provide current estimates and future projections of sea level rise
14 associated with such losses. However, one of the main limitations of RCMs is the relatively coarse horizontal spatial resolution
15 at which outputs are currently generated. Here, we report results concerning the statistical downscaling of the SMB modeled
16 by the Modèle Atmosphérique Régional (MAR) RCM from the original spatial resolution of 6 km to 100 m building on the
17 relationship between elevation and mass losses in Greenland. To this goal, we developed a geospatial framework that allows
18 the parallelization of the downscaling process, a crucial aspect to increase the computational efficiency of the algorithm. The
19 results obtained in the case of the SMB, surface and air temperature are assessed through the comparison of the modeled
20 outputs with in-situ and satellite measurements, show a considerable improvement in the case of the downscaled product
21 with respect to the original, coarse output with the coefficient of determination (R^2) increasing from 0.868 for the
22 original MAR output to 0.935 for the SMB downscaled product. Moreover, the value of the slope and intercept of the linear
23 regression fitting modeled and measured SMB values shifts from 0.865 for the original MAR to 1.015 for the downscaled
24 product in the case of the slope and from the value -235mm w.e. yr⁻¹ (original) to -57 mm w.e. yr⁻¹ (downscaled) in
25 the case of the intercept, considerably improving upon results previously published in the literature.

27 The Greenland Ice Sheet (GrIS) has been contributing directly to sea level rise since the beginning of the century
28 through meltwater runoff and ice mass loss. Hörhold et al. (2022) found that modern temperatures over North and Central
29 Greenland are 1.5 °C warmer than the twentieth century and that meltwater run-off, a major contributor to sea level rise, has
30 been consequently enhanced. The duration of surface melting as well as melt extent have also been increasing since 1979,
31 as measured by passive microwave satellite observations (e.g., Tedesco et al. 2013, Colosio et al., 2021). Moreover, Hanna et
32 al. (2021) found that over the 1972-2018 period each 1°C of summer warming corresponds to 116 Gt of surface mass loss and
33 26 Gt of solid ice discharge increase. A key tool for studying the evolution of surface mass loss (e.g., surface mass balance,
34 SMB) over the GrIS is represented by (polar) regional climate models (RCMs), which, differently from remote sensing
35 observations (that can provide information about surface height changes but are unable to attribute height change to a mass
36 change without more information about snow/firn compaction, e.g., Smith et al., 2023) can provide information on the mass
37 loss and represent an irreplaceable tool to provide future projections of such losses. A widely used model in this regard is the
38 *Modèle Atmosphérique Régional* (MAR, Fettweis et al., 2013, 2017, 2020; Tedesco et al., 2013), a coupled surface-
39 atmospheric model forced at its boundaries with reanalysis data. However, one of the limitations of MAR (and of RCMs in
40 general) lies in the horizontal spatial resolution at which outputs can be generated. This is due to computational considerations
41 as well as to the physics behind the models. Currently, MAR simulations over Greenland are generated at a horizontal spatial
42 resolution of 6 km (e.g., Colosio et al., 2021). Such spatial resolution does not allow capturing fine-scale processes
43 occurring in areas characterized by complex topography (e.g., glaciers terminating in fjords) or small glaciated surface (e.g.,
44 ice caps). Moreover, the knowledge of mass loss at a horizontal spatial resolution higher than the one currently available (e.g.,
45 100s of meters) might allow a better characterization of the spatial inputs of runoff and freshwater to the surrounding
46 oceans.

47 To address the limitations associated with the current horizontal spatial resolution of the MAR model, statistical
48 downscaling can be used to enhance the spatial resolution of the modeled outputs. For example, Hanna et al. (2005, 2008,
49 2011) statistically downscaled reanalysis data over the GrIS. A statistical downscaling technique based on elevation correction
50 was also applied by Franco et al. (2012) to the 25 km MAR outputs to reconstruct GrIS SMB at 15 km spatial resolution.
51 Following that, Noël et al. (2016) applied an elevation dependent statistical downscaling technique to SMB components
52 simulated by the *Regional Atmospheric Climate Model* (RACMO2) at 11 km resolution to reconstruct a daily dataset of SMB
53 over the GrIS over a 1 km resolution grid. Here, we build upon the approach proposed by Noël et al. (2016) to generate a 100
54 m, statistically downscaled output of MAR SMB over the whole GrIS. Beside applying the approach to a different set of
55 modeled outputs (MAR instead of RACMO) and the enhanced spatial resolution with respect to Noël et al. (2016), we developed
56 a geospatial framework that allows the parallelization of the downscaling process which increases the computational efficiency
57 of the algorithm. In the following, we first describe the datasets used for our approach (Section 2), then we introduce the
58 methodology (Section 3), followed by the results (Section 4) and our conclusions and future work (Section 5).

59 **2 Datasets**

60 **2.1 MAR Model**

61 Modeled quantities to be downscaled are obtained from the regional climate model MAR (Colosio et al., 2021;
62 Alexander et al., 2014; Fettweis et al., 2013; Fettweis et al., 2017; Tedesco et al., 2013). MAR is a modular atmospheric model
63 that uses the sigma-vertical coordinate to simulate airflow over complex terrain and the Soil Ice Snow Vegetation Atmosphere
64 Transfer scheme (SISVAT) (e.g., De Ridder and Gallée, 1998) as the surface model. The snow model in MAR, which is based
65 on the CROCUS model of Brun et al. (1992), calculates albedo for snow and ice as a function of snow grain properties, which
66 in turn depend on energy and mass fluxes within the snowpack. Lateral and lower boundary conditions are prescribed from
67 reanalysis datasets. Sea-surface temperature and sea-ice cover are prescribed over the ocean using the same reanalysis data.
68 The atmospheric model within MAR interacts dynamically with SISVAT. MAR outputs have been assessed over the GrIS
69 by many authors (e.g., Fettweis et al., 2017, 2020; Alexander et al., 2014).

70 In this study, we use the output from MAR version v3.11.5 characterized by an enhanced computational efficiency
71 and improved snow model parameters (Fettweis et al., 2020; Delhasse et al., 2020). The model is 6-hourly forced at the
72 boundaries from 1950 using ERA5 reanalysis (Hersbach et al., 2020), the newest generation of global atmospheric reanalysis
73 data that superseded ERA- Interim (Dee et al., 2011), and output is produced at a horizontal spatial resolution of 6 km.
74 Specifically, we focus our attention on daily air temperature (TT variable, being the temperature above 2 m from the surface),
75 surface temperature (ST variable) and surface mass balance (SMB) outputs.

76 **2.2 Digital Elevation Model**

77 For the Digital Elevation Model (DEM), we adopt the ArcticDEM data product (Porter et al., 2018, Figure 1).
78 ArcticDEM is a National Geospatial-Intelligence Agency (NGA) and National Science Foundation (NSF) public-private
79 initiative to produce high-quality DEM of the Arctic applying stereo auto-correlation techniques to high-resolution optical
80 satellite images and adopting the SETSM open-source photogrammetric software (Noh and Howat, 2015). Further information
81 about the dataset can be found at <https://www.pgc.umn.edu/guides/arcticdem/introduction-to-arcticdem/>. Specifically, we
82 use a DEM provided at the spatial resolution of 100 m. The data are projected to the National Snow and Ice Data Center
83 (NSIDC) Sea Ice Polar Stereographic North and referenced to WGS84 datum. The overall dataset is composed of 403,920,000
84 cells and is distributed as a GeoTIFF with a total size of approximately 1.6 Gb.

85 **2.3 PROMICE Surface Mass Balance measurements**

86 The main objective of this work is to obtain a high-resolution SMB dataset from the downscaling of the MAR model
87 suitable for local (i.e., glacier scale) studies. Consequently, we carried out a validation of our results by comparing the original
88 SMB outputs from MAR at a spatial resolution of 6 km and the downscale outputs at 100 m with in-situ SMB measurements.

89 For this purpose, we used the dataset collected by Machguth et al. (2016), containing 2955 SMB measurements from 46 sites,
90 reported in Figure 1 as blue dots and available on GEUS Dataverse portal (Machguth, 2022; last access 16/02/2023). Such
91 a comprehensive dataset spans from 1892 to 2015. From the 123 years, we focused our attention to the period 1980 - 2015
92 when the largest portion of the dataset is temporally located and the MAR outputs are available. From the 2955 measurements
93 we obtained 1982 suitable SMB measurements to be used for validation. The SMB measurements are carried out by computing
94 the difference of stake readings between two dates. The observations are identified by the measuring site (i.e., the area or
95 location, containing at least one measuring point), measuring point (i.e., specific stakes, associated with multiple readings)
96 and the actual readings (i.e., the SMB measurement). In Table 1 we report the number of readings for each measuring site
97 considered, together with its coordinates (WGS 84) and time period when the measurements were collected. Measurement
98 periods are various, covering specific seasons (summer or winter SMB) or an entire year (annual SMB). In some cases, also
99 short-term (at least one month) and multi-year measurements are present. We reconstructed the SMB in correspondence of the
00 measurement location as an algebraic sum of the daily simulated SMB between the start and end dates of the measurement.
01 In order, as a metric to assess the performance of the downscaled product, we compute the root mean squared error (RMSE)
02 and the least-square linear regression parameters (slope and intercept) between model outputs (SMB original and
03 downscaled) and measurements.

04 **2.4 GC-Net air temperature**

05 To test the results of the applied downscaling procedure at local scale we also compare the values of near surface air
06 temperature obtained from MAR with in-situ measurements. We use data from the Greenland Climate Network (GC-Net;
07 Steffen et al., 1996), a set of Automatic Weather Stations (AWS) located all around the GrIS and continuously measuring
08 air temperature, wind speed, wind direction, humidity, pressure, and other parameters. Since direct measurements of surface
09 temperature are not available as continuous records at multiple sites around Greenland, we use the air temperature records
10 measured at 3 m above ground level. Specifically, we consider 17 selected stations reported in Figure 1 as red triangles.
11 Specific location and elevation for each station are also reported in Table 2 in the Results section. The AWS thermometers
12 collect air temperature measurements at sub-daily temporal scale while MAR outputs are provided at daily temporal resolution.
13 Consequently, we compute daily average air temperatures for the comparison with the modeled and downscaled near-
14 surface temperatures (TT variable).

15 **2.5 Landsat-8 surface temperature**

16 As in situ measurements are only available at point scale, it is not possible to assess the potential improvement of the
17 downscaling approach on spatially distributed fields. In the absence of spatially distributed, high spatial resolution SMB
18 outputs, we use surface temperature fields from seven different Landsat-8 scenes covering the Jakobshavn and the Helheim
19 Glaciers, acquired on 5 June 2015, 30 June 2015 (two images), 9 July 2015 (two images), 16 July 2015, and 18 July 2015. The

20 Landsat-8 surface temperature product has been available at 30 m spatial resolution since April 2013 and is generated from
21 Landsat Collection 2 Level-1 thermal infrared bands and other parameters obtained from satellite observations and reanalysis
22 data. The images were downloaded from the USGS Earth Explorer data portal (<https://earthexplorer.usgs.gov/>, last access
23 17/01/2023). We compared the Landsat-8 observations with the original and downscaled MAR outputs of surface temperature
24 (ST variable).

25 **3. Methods**

26 **3.1 Downscaling methodology**

27 We adopted the approach used by Noël et al. (2016), in which a statistical downscaling method was applied to
28 RACMO to achieve a 1-km horizontal resolution. Here, we use a similar methodology applied to MAR, but instead downscale
29 the product to 100 m horizontal resolution. The method exploits the potential dependency of the modeled variables (e.g.,
30 surface temperature, runoff) with elevation. In order, to overcome the large number of cells and reduce the computational time,
31 we parallelized the procedure through a combination of geospatial tools (in the software R) so that our approach can also be
32 used for near-real time generation of downscaled maps over a specific region of the GrIS.

33 The first step involves the calculation of the local dependency of the MAR outputs with respect to the elevation. For
34 this step we refer to the methodology proposed by Noël et al. (2016). Accordingly, we compute the local linear regression
35 (least squares) between the specific variable and the elevation (obtained from the MAR DEM) obtaining the values of slope
36 (m_{6km}) and intercept (q_{6km}). The linear regression is carried out for each pixel of the MAR 6 km resolution DEM using the
37 values of the adjacent pixels with a minimum of 6 points used for the regression. In the case of pixels with less than 5 adjacent
38 pixels (e.g., margins of the ice sheet), we compute m and q for that pixel by interpolation. Such regression is carried out for
39 every day and pixel of the region of interest. Figure 2 provides an example of such a procedure. Parallelizing such
40 procedure for each MAR pixel, we obtain the daily maps of m_{6km} and q_{6km} for the considered MAR output variable. Differently
41 from Noël et al. (2016), we downscale the SMB output of MAR directly, rather than downscaling the components of the SMB
42 (runoff and sublimation) and then approximating SMB as the sum of its components. We opted for this choice because we
43 found that downscaling directly SMB provides better performance of the downscaling when compared with in-situ
44 measurements. Then, the m_{6km} and q_{6km} maps are reprojected to the Polar Stereographic coordinate system which is used
45 by the DEM. The original MAR data are distributed by providing only the coordinates for the center of each grid cell. To
46 create a continuous grid, and avoid introducing errors, the coordinates for the four corners of each MAR grid are computed,
47 and then they are transformed into the Polar Stereographic coordinate system. The result is a shapefile that contains a polygon
48 for each MAR grid. Additionally, the new shapefile contains metadata to ease computations, such as a unique MAR grid ID,
49 the Polar Stereographic coordinates for the center of the grid, the corresponding coordinates in longitude and latitudes for
50 the center of the grid. The next step consists in fragmenting the high-resolution DEM into a series of smaller files,
51 specifically one for each polygon of the reprojected MAR cells generated in the previous steps. There are a total of 55,144

52 files generated through each step, which are less than the total number of cells in the original MAR output. This discrepancy
53 is due to the fact that the DEM is limited to only areas covered by the ice sheet, and it thus does not cover all the locations of
54 where MAR output is generated. While it might seem counterintuitive that maintaining over 55,000 small files is more efficient
55 than maintaining a single file, the answer lies in the fact that this preprocessing step translates our problem into a
56 parallelization one that can be efficiently solved using multi-core and multi-node infrastructure. Because the DEM is required
57 for downscaling each grid cell, which are computed simultaneously in parallel, each task needs to read only a small file of a
58 few kb, rather than one larger file, and it also avoids file system bottlenecks when multiple processes try accessing the same
59 file. Most file systems do not allow for concurrent access to the same file, and therefore if hundreds of tasks try to read the
60 same file, each task would have to idle in a queue for the file access to become available. This problem is prevented by
61 generating a DEM file for each MAR grid, so that both input/output transfer rate and file access are optimized. Furthermore,
62 because the DEM are segmented using the original Polar Stereographic projection, which matches the reprojected MAR grid,
63 no further transformation is required, further speeding up the downscaling process. The final step consists in obtaining the
64 high-resolution maps of slope and intercept (m_{100m} and q_{100m}) by bilinear interpolation of m_{6km} and q_{6km} over the high-
65 resolution DEM grid. While this process was not parallelized in the current version, it is possible to speed it up using a parallel
66 solution. Finally, the downscaled variable is obtained by applying the high-resolution linear regression coefficients to the
67 high-resolution DEM as

$$68$$

$$69 \quad VAR_{100m} = m_{100m}H_{100m} + q_{100m}, \quad (1)$$

70

71 where VAR is the generic downscaled variable computed as a linear function of high-resolution elevation of the DEM (H_{100m})
72 through the coefficients previously obtained (m_{100m} and q_{100m}). Since the origin of the MAR DEM and the high-resolution
73 DEM is different, errors in terms of mass conservation can arise. For example, within a MAR pixel the average elevation of
74 the high-resolution DEM might be higher than the original MAR elevation, possibly leading to the previously mentioned mass
75 conservation error (e.g., the original MAR pixel suggests for a day a lower mass loss than the ensemble of the high-resolution
76 pixels). For this reason, differently from Noël et al. (2016), we decided to provide physical constraints (SMB mass
77 conservation within each pixel at the original MAR spatial resolution) to be satisfied as the very final step of the downscaling
78 procedure.

79 In this research, we apply the downscaling methodology to daily near-surface temperature, surface temperature and
80 SMB MAR outputs .

81 3.2 Spatial autocorrelation analysis and variograms

82 Beside RMSE, slope and intercept, we also focus on evaluating the potential improvements of the downscaled
83 product with respect to the original coarser resolution MAR outputs in terms of capability to describe the spatial distribution
84 of the considered variable. To this aim, we perform a spatial autocorrelation analysis using variograms. Variogram analysis is
85 generally adopted in geostatistical analyses to evaluate autocorrelation of spatial data (Edward et al., 1989, Webster and Oliver,
86 2001). Autocorrelation and variogram analysis are geostatistical tools that can be used to quantify spatial variability using
87 metrics such as the spatial correlation length (simply correlation length hereafter). Though these techniques were mainly
88 designed to support the prediction of values at locations where measurements are not available, they can be used for
89 characterizing processes across the scale spectrum (Herzfeld, 1993). Once process scales are known, the scale ranges over
90 which process relationships (and thus spatial pattern) are consistent must be determined. This can support the
91 identification of spatial scales at which the process interactions change (e.g., scale breaks), being such scales critical
92 for measurement or model interests (Mark and Aronson, 1984; Vedyushkin, 1994). Geostatistical methods such as spatial
93 covariance, variogram analysis, and spectral analysis (Webster and Oliver, 2001) quantify the spatial pattern of variability of
94 an observed property over a scale range from the minimum sample separation to the distance at which the variable becomes
95 spatially independent. This quantified variability can, then, be used for spatial estimation based on a finite number of data
96 points. In our case, we fit the experimental variogram with a circular model, as this is the model that provided
97 us with the highest R^2 when fitting the experimental data. The formal expression of the experimental variogram can be
98 written as:

$$00 \quad \gamma(\delta) = \frac{1}{2N(\delta)} \sum_{i,j \in N(\delta)} (x_i - x_j)^2, \quad (2)$$

01
02 where γ is the semi-variance, $N(\delta)$ is the number of data pairs (i -th and j -th) distanced by d while x_i and x_j are the corresponding
03 variable values. The fitting spherical function is, then, used to compute the three main parameters characterizing the variogram:
04 the sill, the range and the nugget effect. The sill is defined as the maximum value at which the fitted curve becomes flat; such
05 variance value is reached at a certain distance called *range*, beyond which the data are no longer autocorrelated. The range can
06 be seen as a scale break (where data are no longer correlated). Of course, there can also be several scale breaks before the sill
07 is reached, depending on the drivers controlling the modeled process. The nugget corresponds to $\gamma(0)$ and it should be ideally
08 0. The departure from 0 can be interpreted as the result of measurement errors or highly localized variability (Webster and
09 Oliver, 2001). Following Colosio et al. (2021), we focus our attention on the range, the descriptor of the correlation length,
10 comparing the range values computed for the original MAR temperature outputs, the downscaled temperature and the surface
11 temperature observed by Landsat-8.

12 To further investigate and quantify possible improvements in terms of spatial description of the variable of interest by the
13 downscaled product, we also compute the so-called Structural Similarity Index Measure (SSIM). Such an index has been
14 introduced by Wang et al. (2004) to provide a similarity measure between two images. This index can objectively quantify a
15 qualitative aspect such as the similarity between two images. Considering a pair of images (X,Y) to be compared, the values
16 assumed by the SSIM are bounded by a unique maximum ($SSIM(X,Y)=1$) in case $X=Y$, otherwise $SSIM(X,Y)<1$. We compute
17 such a similarity index for both original and downscaled MAR ST outputs, considering as reference the Landsat-8 surface
18 temperature image.

19 **4 Results and discussion**

20 **4.1 Surface and near-surface temperature**

21 We first tested the downscaling algorithm with the MAR near-surface temperature outputs. We compared the results
22 obtained with air temperature measurements from 17 AWS of the GC-Net. We performed the comparison by computing RMSE
23 and R^2 between the modeled (original and downscaled) and the observed variable. The results obtained for the original
24 MAR and the downscaled temperatures are reported in Table 2. Both R^2 and RMSE obtained for the downscaled temperatures
25 do not exhibit significant improvements or worsening with respect to the original coarser resolution output. The difference
26 between the 6 km and 100 m resolution is in the order 10^{-3} for R^2 and 10^{-2} °C for RMSE, with improvements in some stations
27 (Swiss Camp, Crawford Pt. 1, NASA-U, Summit, Crawford Pt. 2, KAR, JAR2 and KULU) and worsening in others (Tunu-N,
28 JAR1, South Dome and NASA-E). However, such small differences appear to be randomly distributed in space, without any
29 clear correlation with elevation or latitude/longitude. Such results demonstrate that the applied downscaling methodology does
30 not introduce errors in case of the TT variable at point scale.

31 To evaluate the results over a wider area, we considered two Landsat-8 surface temperature images collected over
32 two different areas of the ice sheet. The two selected areas are located on the eastern and western coasts of Greenland and
33 show a variable topography. In Figure 3 we report the surface temperature image from Landsat-8 (Figure 3a), the original ST
34 output at 6 km spatial resolution (Figure 3b) and the downscaled ST at 100 m resolution (Figure 3c) for one of the selected
35 Landsat-8 scenes.

36 In Figure 4 where we report the histograms of the difference between Landsat-8 surface
37 temperature and the original ST (Figure 4a) and the downscaled one (Figure 4b) for the same image. The results show no
38 differences in terms of mean difference (μ), with an average difference of 2.7°C in both cases, similarly to the AWS
39 comparison. Also, the standard deviation (σ) remains unvaried at 2.6 °C. Similar results have been obtained for all the
40 compared Landsat-8 images, with mean differences ranging between -0.59°C and 3.44°C for the downscaled product (2.09°C
41 on average) and between -0.62°C and 3.43°C for the original MAR data (2.07°C on average). The similarity in mean
42 differences is not surprising considering the physical constraints imposed for the ST to maintain the average ST constant
for each MAR pixel as the final step of the downscaling procedure. These results indicate that in case of ST the downscaling

43 algorithm does not introduce significant improvements or errors in terms of overall difference with observed temperature
44 (expressed as RMSE for the AWS case and spatial average difference for the Landsat-8 image).

45 Considering such results in terms of difference at point scale and spatially averaged difference, we evaluated possible
46 improvements in terms of spatial information content and spatial description obtained in the downscaled product. We report
47 in Figure 5 the results of the variogram analysis performed for two sub-regions of interest within the same Landsat-8 image
48 shown in Figure 3. The two areas have been selected because of the strong differences in topography and elevation gradients.
49 Concerning the results obtained over the topographically more complex area, we observe that the scale break of the downscaled
50 temperature (blue line) is 13.5 km, better capturing the one from Landsat-8 data (11.5 km, red line) with respect to the original
51 MAR outputs (24.1 km, black line, Figure 5). On the other hand, the same analysis performed over an area in a more interior
52 region of the ice sheet, where downscaling might lead to less improvement in view of the reduced topography, does not present
53 improvements in terms of spatial autocorrelation (Figure 5b) and that all three datasets do not reach the variogram plateau
54 within the considered distance. In order to extend the comparison to another area of the ice sheet, we performed the same
55 variogram based analysis for another Landsat-8 scene in the surroundings of Jakobshavn glacier collected on 11 June (Figure
56 6a). The map also shows the two regions of interests (ROI) selected for the analysis. We selected ROI₁ as this area is
57 characterized by a large topographic gradient within a relatively small distance and to understand the potential improvement
58 of the downscaling procedure over regions that are outside the main ice sheet (e.g., smaller glaciers). On the other hand, ROI₂
59 contains both strong and mild elevation gradients (e.g., nunataks and ice sheet elevation gently increasing as moving towards
60 the interior). In case of ROI₁ (Figure 6b), the variogram analysis indicates that the scale break distance for Landsat-8
61 when considering only the pixels where the DEM is available is 7.5 km. This value becomes 14.6 km for the high-resolution
62 map of ST and 24.7 km in the case of the original MAR outputs, suggesting that the downscaled product is able to perform
63 better than the original one in terms of spatial scale similarity with respect to the Landsat-8 data. The mean difference between
64 Landsat-8 and the downscaled (original MAR) surface temperature, considering only the pixels where the DEM is available,
65 are 1.69 °C (1.7 °C) with a standard deviation of 2.02 °C (2.14 °C), with differences of the same order of magnitude obtained
66 in the previous analysis for the other Landsat-8 image. When considering all pixels within the ROI (e.g., also where no DEM
67 is available), the mean differences between Landsat-8 and downscaled (original) MAR surface temperature become 1.89 °C
68 (2.12 °C) with a standard deviation of 2.15 °C (2.23 °C). In this case, the scale breaks for the original and the downscaled MAR
69 versions are similar, ~ 25 km (~ 16km in the case of Landsat-8). We point out that the scale breaks are sensitive to the different
70 physical processes driving the spatial properties. The ROI₂ contains both strong and mild elevation gradients given the presence
71 of nunataks and the slow ice sheet increasing elevation after the ice cliff begins. The area is covered by most of its portion
72 containing the ice sheet (right of the image) by the DEM, which, however, is absent in the case of the left portion of the ROI,
73 containing fjords and the ocean. The scale breaks for the Landsat-8, downscaled and original MAR cases for the portion of the
74 ROI₂ where the DEM is available are close to each other, on the order of ~ 25 km. We observe an improvement in the SSIM
75 in the case of the downscaled data by 30 % (from 0.33 in the case of the original MAR resolution to 0.43 in the case of
76 downscaled MAR). Unexpectedly, despite the mean and standard deviation of the distribution of the differences between

77 the Landsat-8 data and the simulated quantities remains similar, we notice a reduction in both the mean (from 0.86°C for
78 original MAR to 0.83°C for the downscaled product) and of the standard deviation (from 0.71°C for original MAR to 0.63°C
79 for the downscaled product) when downscaling the MAR output. We further note that when considering all pixels (including
80 those where no DEM), the SSIM of the two products improves from 0.11 (original) and 0.14 (downscaled) and that the scale
81 break of the original MAR products is larger (~ 63 km) than the one of the Landsat-8 data (~ 21 km). In synthesis, the
82 downscaling does not introduce any considerable bias on the original value, preserves the total integrated quantity of energy
83 within each area and improves the spatial performance of the MAR outputs by generating a product that has a spatial
84 structure that is closer to the one of the observed remote sensing dataset.

85 **4.2 Surface Mass Balance**

86 After applying the downscaling algorithm to surface temperature, we applied it to MAR SMB outputs of SMB and
87 assessed the results obtained with in situ measurements from the dataset collected by Machguth et al. (2016). As mentioned,
88 we compared 1982 SMB measurements carried out between 1980 and 2015 and localized in the ablation area of the GrIS
89 (Table 1). Figure 7 shows the scatterplots of the comparison of modeled SMB from the original MAR (Figure 7a) and the
90 downscaled product (Figure 7b) with in situ measured SMB. Our results show that the downscaled product better estimates
91 the measured SMB, exhibiting an increased R^2 from an already relatively high value of 0.868 for the original MAR to 0.935
92 for the downscaled product. As a comparison, Noël et al. (2016) obtained an increase of R^2 from the downscaling of SMB
93 outputs of the RACMO regional climate model from 0.47 in the case of the original 11 km spatial resolution outputs to 0.78
94 in case of the downscaled SMB (1 km resolution). As explained in Fettweis et al. (2020), the SMB was extrapolated
95 (interpolated + corrected) to the common 1km grid by applying an elevation gradient as done in this study. One of the key
96 issues raised by the first SMB model intercomparison performed by Vernon et al. (2013) was the high dependency of modeled
97 integrated SMB values to the ice sheet mask used. To mitigate this problem, we interpolate all model outputs to the same 1 km
98 grid used in the Ice Sheet Model Intercomparison Project for CMIP6 (ISMIP6). This resolution is chosen because the highest
99 resolution model outputs (e.g. RACMO2.3p2) are available at 1 km and choosing a coarser resolution could compromise their
00 quality. A common grid also allows a comparison on two common ice sheet masks: the contiguous Greenland Ice Sheet, which
01 is common to all the models and the Greenland Ice Sheet plus peripheral ice caps and mountain glaciers, common to all the
02 models except the two PDD models. Unless otherwise indicated, the SMB components have been interpolated to 1 km using
03 a simple linear interpolation metric of the four nearest inverse-distance-weighted model grid cells. Moreover, as done in Le
04 clec'h et al. (2019), the interpolated 1 km SMB and runoff fields have been corrected for elevation differences between the
05 model native topography and the GIMP 250 m topography (upscaled to 1 km here), using time- and space-varying SMB–
06 elevation gradients, similar to Franco et al. (2012) and Noël et al. (2016). No correction was applied to precipitation after
07 interpolation to 1 km. We point out that, in our case, the starting value of R^2 for the original MAR product already exceeds the
08 value obtained in the case of the downscaled RACMO outputs.

09 The values of slope and intercept of the best-fitting line improve as well when considering the downscaled product.
10 The value of the slope shifts from 0.865 for the original MAR to 1.015 for the downscaled product; similarly, the intercept
11 increases from the value -235 mm w.e. yr⁻¹ of the coarse resolution outputs to -57 mm w.e. yr⁻¹ of the downscaled
12 SMB, closer to its optimal value (i.e., null intercept). As a comparison, the downscaling algorithm of Noël et al. (2016) applied
13 to RACMO improved the estimate of SMB in terms of slope from 0.72 to 1.03, with a slight increase of the intercept (from
14 70 mm w.e. yr⁻¹ to 100 mm w.e. yr⁻¹). The RMSE between modeled and measured SMB also decreases in the case
15 of the downscaled product from 669 mm w.e. yr⁻¹ for the 6 km outputs to 511 mm w.e. yr⁻¹ for the 100 m case,
16 significantly improving the estimate of SMB at local scale. Noël et al. (2016) obtained a reduction of the RMSE passing from
17 a value of 1200 mm w.e. yr⁻¹ for the 11 km RACMO outputs to a value of 740 mm w.e. yr⁻¹ for the 1 km case. Fettweis
18 et al. (2020) compared MAR and RACMO, among 13 models of four types (positive degree day models, energy balance
19 models, regional climate models and general circulation models), SMB estimates with the same PROMICE in situ
20 measurements within the GrIS SMB model intercomparison project (GrSMBMIP). They considered only the measurements
21 collected between 1980 and 2012 and with measurement periods longer than 3 months. They also excluded the records
22 located outside the 1 km ice mask they used for the intercomparison of the models, for a total of 1438 SMB measurements.
23 The model versions in this case are MARv3.9.6, an older version than the one we adopted and at the spatial resolution of 15
24 km, and RACMO2.3p2 (Noël et al., 2019), a new version of the one adopted in Noël et al. (2016) and with a spatial resolution
25 of 5.5 km. From the comparison, they obtained a RMSE of 480 mm w.e. yr⁻¹ for MAR and 630 mm w.e. yr⁻¹ for
26 RACMO. In both cases, the RMSE is lower than the one obtained in this work for MAR (both original and downscaled) and
27 by Noël et al. (2016) for RACMO. The difference can be related to the differences in spatial resolution and model versions
28 and, most probably, to the sub-sampling of the SMB measurements discarding short-term records (i.e., measurement period
29 lower than 3 months), suggesting that the bias might be dissipated for longer observation periods.

30 To further investigate our results, we compute the variation in RMSE between the 6 km spatial resolution MAR
31 outputs and the downscaled product for different elevation classes, longitude and latitude ranges and for each specific
32 glacier/location (i.e., for each station ID, Table 1) of the PROMICE in situ SMB dataset. The RMSE difference is computed
33 as $\Delta\text{RMSE} = \text{RMSE}_{100\text{ km}} - \text{RMSE}_{6\text{ km}}$ (i.e., improvements are characterized by negative values of ΔRMSE) and the results
34 obtained are reported in Figure 8 grouped by location (Figure 8a), elevation (Figure 8b), latitude (Figure 8c) and longitude
35 (Figure 8d). The results exhibit improvements in the estimate of SMB at all the altitudes besides the 100-200 m asl, 200-300
36 m asl and 1300-1400 m asl elevation classes, with the best performance obtained at 700-800 m asl and 800-900 m asl elevation
37 classes. The results grouped by latitudinal bands show the highest improvements in south Greenland; a decrease in performance
38 has been recorded in the latitudinal band 67.5-70 °N where the only Paakitsoq JAR ($\Delta\text{RMSE} = 181$ mm w.e. yr⁻¹, worst
39 result obtained) and Swiss Camp/ST2 ($\Delta\text{RMSE} = -127$ mm w.e. yr⁻¹) measurement sites are located, and the improvement
40 obtained in case of Swiss Camp is strongly counterbalanced by the reduced performances in Paakitsoq JAR. However, the
41 longitudinal classes do not present any decrease of the performances, indicating that the worsening in the spotted critical
42 stations is counterbalanced by the improvements measured in the others. We obtained a decrease in performances in 6 out of

22 considered cases with the worst result obtained for the already presented Paakitsoq JAR case. In the 5 other cases (i.e., Hans Tausen Ice Cap, Nioghalvfjerdingsfjorden, Isortoq, Nordbo Glacier and K-Transect) we recorded an average Δ RMSE of 26 mm w.e. yr⁻¹ (ranging from 6 mm w.e. yr⁻¹ to 80 mm w.e. yr⁻¹). On the other hand, we obtained an improvement in 16 out of 22 measurement sites with the best performances in the case of A.P. Olsen Ice Cap (Δ RMSE= -611 mm w.e. yr⁻¹). In the other 15 cases (i.e., Qaanaaq Ice Cap, Petermann, Hare Glacier, Kronprins Christian Land, Storstrømmen, Freya Glacier, Violin Glacier, Helheim, Isortuarssup Sermia, Qamanarssup Sermia, Kangilinnguata Sermia, Qapiarfup, Amitsuloq Ice Cap, Tasersiaq and Swiss Camp/ST2) we found an average decrease in RMSE of 183 mm w.e. yr⁻¹ (ranging between 59 mm w.e. yr⁻¹ and 371 mm w.e. yr⁻¹). Even if such reduction of performances in terms of SMB estimate accounts for 27% of the considered stations, it does not compromise the overall improvement, being smaller in terms of average, minimum and maximum absolute values of Δ RMSE than the results obtained for the stations where improvement occurred.

5 Conclusions and future work

We applied a statistical downscaling technique to increase the horizontal spatial resolution of the outputs of the MAR regional climate model from 6 km to 100 m for the surface temperature and SMB quantities. The approach builds on the dependency of such quantities on elevation, as originally proposed in Noël et al. (2016). Here, however, the technique was applied to the output of a different climate model (RACMO) and the spatial resolution of the downscaled product was 1 km, rather than 100 m. Moreover, differently from Noël et al. (2016), we imposed a mass conservation so that the overall mass obtained for each pixel at high resolution nested within a coarse resolution one is preserved. To address the computational issues associated with the relatively high spatial resolution, we developed a geospatial, parallelized framework that allows us to perform the downscaling over the whole ice sheet in an efficient way.

We, first, tested our approach by applying it to surface temperature data and assessing the outputs using both in-situ and satellite data. Our results showed no significant improvement or deterioration of the downscaled product with respect to the original MAR outputs. This confirms that our approach was not introducing any bias and was properly implemented. However, we found improvement of the downscaled surface temperature when analyzing the skills of the downscaled product to capture the spatial scales (e.g., scale breaks) of the observed surface temperature fields. The results obtained in the case of the SMB show a considerable improvement in the case of the downscaled product with respect to the original, coarse output. In the case of the downscaled MAR product, the R^2 value increases from 0.868 for the original MAR to 0.935 for the SMB product with the value of the slope and intercept shifting from 0.865 for the original MAR to 1.015 for the downscaled product in the case of the intercept and from the value -235mm w.e. yr⁻¹ of the coarse resolution outputs to -57 mm w.e. yr⁻¹ in the case of the slope. As a reference, Noël et al. (2016) obtained an increase of R^2 from the downscaling of SMB outputs of the RACMO regional climate model from 0.47 in the case of the original 11 km spatial resolution outputs to 0.78 in case of the downscaled SMB (1 km resolution) and a shift in the slope and intercept

75 from 0.72 to 1.03 (slope) and from 70 mm w.e. yr⁻¹ to 100 mm w.e. yr⁻¹ (intercept). An analysis of the performance of
76 the downscaled product for different elevation classes, longitude and latitude ranges and for each specific glacier/location
77 where SMB in-situ data is available shows that the downscaled product does not perform as expected for 27% of the stations.
78 . However, we point out that the deterioration of the performance over those stations (expressed in terms of changes
79 on the average error Δ RMSE) is much smaller than the improvement obtained in the remaining cases.

80 The next step is to implement a similar approach for downscaling MAR outputs over both the Greenland and
81 Antarctica ice sheet using machine learning (ML) based approaches. Indeed, the approach proposed here cannot be easily
82 extended to Antarctica, where surface melting does not exhibit a strong dependency from elevation, as most of it occurs over
83 ice shelves, at the sea level and where little elevation gradients exist. Moreover, improvements to the downscaling of the SMB
84 can be obtained by either considering complementary inputs that can improve estimates of losses (e.g., remotely sensed albedo)
85 or of mass gains (e.g., accumulation). ML tools can help in this regard. ML tools have, indeed, been used for improving
86 predictions beyond that of state-of-the-art physical models or for improving parameterization in models. In particular,
87 conditional generative adversarial networks (C-GANs or simply GANs in the following) can be successfully applied to the
88 problems discussed above (Goodfellow et al., 2014). GANs is a class of ML tools in which two neural networks compete with
89 each other in a min-max optimization problem. The first network, called generator, aims to generate new data samples that are
90 indistinguishable from the training data (e.g., high-resolution melting maps obtained from the remote sensing observations)
91 by the other network, called discriminator. In our case the GAN aims to generate high-resolution melting maps that are
92 indistinguishable by the second network from high-resolution remote sensing observations or numerical model outputs. We
93 have already started to build the architecture for this framework and are in the phase of collecting the necessary datasets and
94 are building the proper data framework to perform such work.

95 **Code and data availability**

96 The MAR v3.11.5 code and outputs are available at <https://www.mar.cnrs.fr/> and <ftp://climato.be/fettweis/MARv3.11>.
97 Automatic weather station data are available on EnviDat portal (<https://www.envidat.ch/#/metadata/gcnet>, Steffen et al.,
98 2020, last access 16/02/2023). Surface mass balance measurements are available on GEUS Dataverse portal
99 (<https://doi.org/10.22008/FK2/5VNBQA>, Machguth, 2015, last access 16/02/2023). Landsat-8 images are available on the
00 USGS Earth Explorer portal (<https://earthexplorer.usgs.gov/>, last access 16/02/2023). Downscaled data is available at
01 <https://doi.org/10.5281/zenodo.7803611>. Downscaling code is available upon request to mtesesco@ldeo.columbia.edu.

02 **Authors contributions**

03 MT, PC and GC designed the study and the methodology. GC optimized the algorithm parallelization. PC and MT performed
04 the comparison with measured and remotely sensed observations and wrote the first draft of the paper. XF ran the
05 MARv3.11.5 model and provided the outputs. All the authors discussed the results and contributed to the paper.

06 **Competing interests**

07 Xavier Fettweis is a member of the editorial board of *The Cryosphere*,

08 **Acknowledgment**

09 This work was supported by the NASA grant 80NSSC17K0351, NSF grants OPP-1713072 and OPP-2136938 and the Heising-
10 Simons Foundation grant HSFOUND 2019-1160. PC would like to thank Lamont-Doherty Earth Observatory and University
11 of Brescia for the support provided.

12 **References**

- 13 Alexander, P. M., M. Tedesco, X. Fettweis, R. Van De Wal, C.J.P.P. Smeets, and M.R. Van Den Broeke: Assessing spatio-
14 temporal variability and trends in modelled and measured Greenland Ice Sheet albedo (2000–2013). *The Cryosphere*, 8, 2293–
15 2312, doi: 10.5194/tc-8-293-2014, 2014.
- 16 Brun, E., David, P., Sudul, M., and Brunot, G.: A numerical model to simulate snow-cover stratigraphy for operational
17 avalanche forecasting, *J. Glaciol.*, 38, 13–22, 1992.
- 18 Collection 2 Landsat 8-9 OLI (Operational Land Imager) and TIRS (Thermal Infrared Sensor) Level-2 Science Product Digital
19 Object Identifier (DOI) number: /10.5066/P9OGBGM6. [Last access, 16/02/2023].
- 20 Colosio, P., Tedesco, M., Ranzi, R., and Fettweis, X.: Surface melting over the Greenland ice sheet derived from enhanced
21 resolution passive microwave brightness temperatures (1979–2019), *The Cryosphere*, 15, 2623–2646,
22 <https://doi.org/10.5194/tc-15-2623-2021>, 2021.
- 23 De Ridder, K. and Gallée, H.: Land Surface-Induced Regional Climate Change in Southern Israel, *J. Appl. Meteorol.*, 37,
24 1470–1485, 1998.
- 25 Dee, D. P., Uppala, S. M., Simmons, A. J., Berrisford, P., Poli, P., Kobayashi, S., Andrae, U., Balmaseda, M. A., Balsamo,
26 G., Bauer, P., Bechtold, P., Beljaars, A. C. M., van de Berg, L., Bidlot, J., Bormann, N., Delsol, C., Dragani, R., Fuentes, M.,
27 Geer, A. J., Haimberger, L., Healy, S. B., Hersbach, H., Hólm, E. V., Isaksen, L., Kållberg, P., Köhler, M., Matricardi, M.,
28 McNally, A. P., Monge-Sanz, B. M., Morcrette, J.-J., Park, B.-K., Peubey, C., de Rosnay, P., Tavolato, C., Thépaut, J.-N. and

29 Vitart, F.: The ERA-Interim reanalysis: configuration and performance of the data assimilation system, *Q.J.R. Meteorol. Soc.*,
30 137(656), 553–597, doi:10.1002/qj.828, 2011.

31 Delhasse, A., Kittel, C., Amory, C., Hofer, S., van As, D., S. Fausto, R., and Fettweis, X.: Brief communication: Evaluation
32 of the near-surface climate in ERA5 over the Greenland Ice Sheet, *The Cryosphere*, 14, 957–965, [https://doi.org/10.5194/tc-](https://doi.org/10.5194/tc-14-957-2020)
33 14-957-2020, 2020.

34 Fettweis, X., Gallée, H., Lefebvre, F. and van Ypersele, J.-P.: Greenland surface mass balance simulated by a regional climate
35 model and comparison with satellite-derived data in 1990–1991, *Climate Dynamics*, 24(6), 623–640, doi:10.1007/s00382-
36 005-0010-y, 2007.

37 Fettweis, X., Franco, B., Tedesco, M., van Angelen, J. H., Lenaerts, J. T. M., van den Broeke, M. R., and Gallée, H.: Estimating
38 the Greenland ice sheet surface mass balance contribution to future sea level rise using the regional atmospheric climate model
39 MAR, *The Cryosphere*, 7, 469–489, <https://doi.org/10.5194/tc-7-469-2013>, 2013.

40 Fettweis, X., Box, J. E., Agosta, C., Amory, C., Kittel, C., Lang, C., van As, D., Machguth, H. and Gallée, H.: Reconstructions
41 of the 1900–2015 Greenland ice sheet surface mass balance using the regional climate MAR model, *The Cryosphere*, 11(2),
42 1015–1033, doi:10.5194/tc-11-1015-2017, 2017.

43 Fettweis, X., Hofer, S., Krebs-Kanzow, U., Amory, C., Aoki, T., Berends, C. J., Born, A., Box, J. E., Delhasse, A., Fujita, K.,
44 Gierz, P., Goelzer, H., Hanna, E., Hashimoto, A., Huybrechts, P., Kapsch, M.-L., King, M. D., Kittel, C., Lang, C., Langen,
45 P. L., Lenaerts, J. T. M., Liston, G. E., Lohmann, G., Mernild, S. H., Mikolajewicz, U., Modali, K., Mottram, R. H., Niwano,
46 M., Noël, B., Ryan, J. C., Smith, A., Streffing, J., Tedesco, M., van de Berg, W. J., van den Broeke, M., van de Wal, R. S. W.,
47 van Kampenhout, L., Wilton, D., Wouters, B., Ziemen, F., and Zolles, T.: GrSMBMIP: intercomparison of the modelled 1980–
48 2012 surface mass balance over the Greenland Ice Sheet, *The Cryosphere*, 14, 3935–3958, [https://doi.org/10.5194/tc-14-3935-](https://doi.org/10.5194/tc-14-3935-2020)
49 2020, 2020.

50 Franco, B., Fettweis, X., Lang, C., and Erpicum, M.: Impact of spatial resolution on the modelling of the Greenland ice sheet
51 surface mass balance between 1990–2010, using the regional climate model MAR, *The Cryosphere*, 6(3), 695-711, 2012.

52 Goodfellow, Ian J., Pouget-Abadie J., Mirza M., Xu B., Warde-Farley D., Ozair S., Courville A., and Bengio Y.: Generative
53 adversarial networks, *Commun. Acm*, 63(11), 139-144, 2004.

54 Hanna, E., Huybrechts, P., Janssens, I., Cappelen, J., Steffen, K., and Stephens, A.: Runoff and mass balance of the Greenland
55 ice sheet: 1958–2003, *Journal of Geophysical Research: Atmospheres*, 110(D13), 2005.

56 Hanna, E., Huybrechts, P., Steffen, K., Cappelen, J., Huff, R., Shuman, C., Irvine-Fynn, T., Wise, S., and Griffiths, M.:
57 Increased runoff from melt from the Greenland Ice Sheet: a response to global warming, *Journal of Climate*, 21(2), 331-341,
58 2008.

59 Hanna, E., Huybrechts, P., Cappelen, J., Steffen, K., Bales, R. C., Burgess, E., McConnell, J. R., Steffensen, J. P., Van den
60 Broeke, M., Wake, L., Bigg, B., Griffiths, M., and Savas, D.: Greenland Ice Sheet surface mass balance 1870 to 2010 based
61 on Twentieth Century Reanalysis, and links with global climate forcing, *Journal of Geophysical Research: Atmospheres*,
62 116(D24), 2011.

63 Hanna, E., Cappelen, J., Fettweis, X., Mernild, S. H., Mote, T. L., Mottram, R., Steffen, K., Ballinger, T.J., and Hall, R. J.:
64 Greenland surface air temperature changes from 1981 to 2019 and implications for ice-sheet melt and mass-balance change,
65 *International Journal of Climatology*, 41, E1336-E1352, 2021.

66 Hersbach, H., Bell, B., Berrisford, P., Hirahara, S., Horányi, A., Muñoz-Sabater, J., Nicolas, J., Peubey, C., Radu, R., Schepers,
67 D., Simmons, A., Soci, C., Abdalla, S., Abellan, X., Balsamo, G., Bechtold, P., Biavati, G., Bidlot, J., Bonavita, M., Chiara,
68 G., Dahlgren, P., Dee, D., Diamantakis, M., Dragani, R., Flemming, J., Forbes, R., Fuentes, M., Geer, A., Haimberger, L.,
69 Healy, S., Hogan, R. J., Hólm, E., Janisková, M., Keeley, S., Laloyaux, P., Lopez, P., Lupu, C., Radnoti, G., Rosnay, P.,
70 Rozum, I., Vamborg, F., Villaume, S. and Thépaut, J. N.: The ERA5 global reanalysis, *Quarterly Journal of the Royal*
71 *Meteorological Society*, doi:10.1002/qj.3803, 2020.

72 Hörhold, M., Münch, T., Weißbach, S., Kipfstuhl, S., Freitag, J., Sasgen, I., Lohmann, G., Vinther, B., and Laepple, T.: Modern
73 temperatures in central–north Greenland warmest in past millennium, *Nature* 613, 503–507, 2023.

74 Le Clec’H, S., Quiquet, A., Charbit, S., Dumas, C., Kageyama, M. et al.. A rapidly converging initialisation method to simulate
75 the present-day Greenland ice sheet using the GRISLI ice sheet model (version 1.3). *Geoscientific Model Development*, 2019,
76 12 (6), pp.2481-2499.10.5194/gmd-12-2481-2019 . hal-02328234

77 Machguth, H., H.H. Thomsen, W. Weidick, A.P. Ahlstrøm, J. Abermann, M. Andersen, S.B. Andersen, A.A. Bjørk, J.E. Box,
78 R. Braithwaite, C.E. Bøggild, M. Citterio, P. Clement, W. Colgan, R.S. Fausto, K. Gleie, S. Gubler, B. Hasholt, B. Hynek,
79 N.T. Knudsen, S.H. Larsen, S.H. Mernild, J. Oerlemans, H. Oerter, O.B. Olsen, C.J.P. Smeets, K. Steffen, M. Stober, S.
80 Sugiyama, S. van As, M.R. van den Broeke and R.S.W. van de Wal.: Greenland surface mass-balance observations from the
81 ice-sheet ablation area and local glaciers, *Journal of Glaciology*. 62: 861-887, doi: 10.1017/jog.2016.7, 2016.

82 Machguth, H.: Historical surface mass balance measurements from the ice-sheet ablation area and local glaciers,
83 <https://doi.org/10.22008/FK2/5VNBQA>, GEUS Dataverse, V1, 2022. [Last access 16/07/2022].

84 Mark, D. M., and Aronson, P. B.: Scale-dependent fractal dimensions of topographic surfaces: an empirical investigation, with
85 applications in geomorphology and computer mapping, *Journal of the International Association for Mathematical Geology*,
86 16, 671-683, 1984.

87 Noël, B., van de Berg, W. J., Machguth, H., Lhermitte, S., Howat, I., Fettweis, X., and Van Den Broeke, M. R.: A daily, 1 km
88 resolution data set of downscaled Greenland ice sheet surface mass balance (1958–2015), *The Cryosphere*, 10(5), 2361-2377,
89 2016.

90 Noël B, van de Berg, W. J., Lhermitte, S., and van den Broeke, M. R.: Rapid ablation zone expansion amplifies north Greenland
91 mass loss, *Sci Adv.*, 5, eaaw0123, <https://doi.org/10.1126/sciadv.aaw0123>, 2019.

92 Noh, M. J., and Howat, I. M.: Automated stereo-photogrammetric DEM generation at high latitudes: Surface Extraction with
93 TIN-based Search-space Minimization (SETSM) validation and demonstration over glaciated regions, *GIScience & Remote*
94 *Sensing*, 52.2 (2015): 198-217, 2015.

95 Porter, C., Morin, P., Howat, I., Noh, M. J., Bates, B., Peterman, K., Keesey, S., Schlenk, M., Gardiner, J., Tomko, K., Willis,
96 M., Kelleher, C., Cloutier, M., Husby, E., Foga, S., Nakamura, H., Platson, M., Wethington, M. Jr., Williamson, C., Bauer,

97 G., Enos, J., Arnold, G., Kramer, W., Becker, P., Doshi, A., D'Souza, C., Cummins, P., Laurier, F., Bojesen, M.: ArcticDEM,
98 Harvard Dataverse, <https://doi.org/10.7910/DVN/OHHUKH>, 2018. [Last access 16/02/2023].

99 Smith, B. E., Medley, B., Fettweis, X., Sutterley, T., Alexander, P., Porter, D., & Tedesco, M. (2023). Evaluating Greenland
00 surface-mass-balance and firn-densification data using ICESat-2 altimetry. *The Cryosphere*, 17(2), 789-808.
01 <https://doi.org/10.5194/tc-17-789-2023>

02 Steffen, K., Houtz, D., Vandecrux, B., Abdalati, W., Bayou, N., Box, J., Colgan, W., Espona Pernas, L.; Griessinger, N., Haas-
03 Artho, D., Heilig, A., Hubert, A., Iosifescu Enescu, I., Johnson-Amin, N., Karlsson, N. B., Kurup, R., McGrath, D., Naderpour,
04 R., Pederson, A. Ø., Perren, B., Phillips, T., Plattner, G., Proksch, M., Revheim, M. K., Saettele, M., Schneebeli, M., Sampson,
05 K., Starkweather, S., Steffen, S., Stroeve, J., Walter, B., Winton, Ø. A. and Zwally, J., Greenland Climate Network (GC-Net)
06 Data., EnviDat 2020, <https://www.doi.org/10.16904/envidat.1>, 2020.

07 Tedesco, M., Fettweis, X., Mote, T., Wahr, J., Alexander, P., Box, J. E., and Wouters, B.: Evidence and analysis of 2012
08 Greenland records from spaceborne observations, a regional climate model and reanalysis data, *The Cryosphere*, 7, 615–630,
09 <https://doi.org/10.5194/tc-7-615-2013>, 2013.

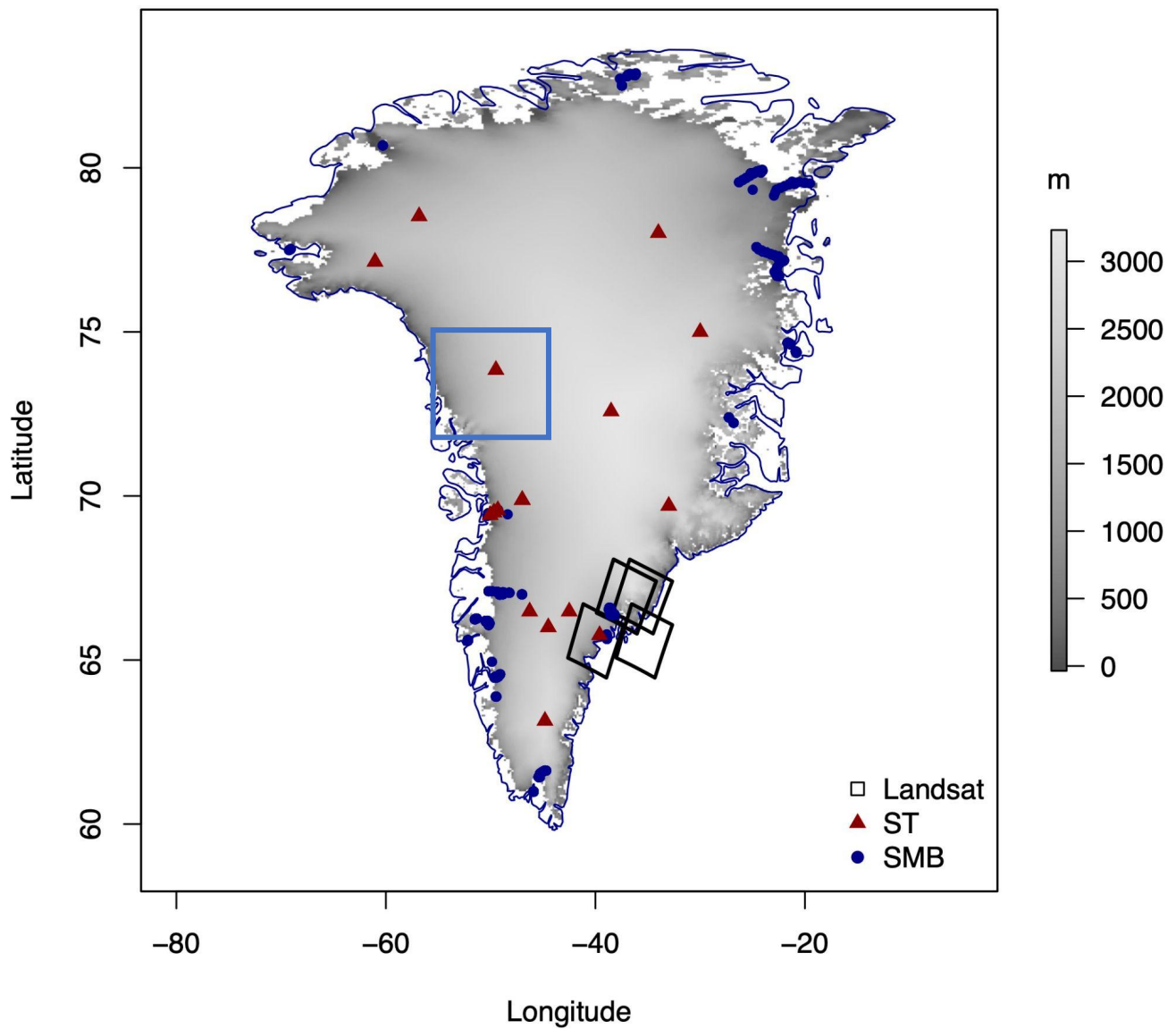
10 Tedesco, M., Cervone, G., Colosio, P. and Fettweis, X.: A computationally efficient statistically downscaled 100 m resolution
11 Greenland product from the regional climate model MAR: accompanying dataset. <https://doi.org/10.5281/zenodo.7803611>

12 Vedyushkin, M. A.: Fractal properties of forest spatial structure, *Vegetatio*, 113, 65-70, 1994.

13 Wang, Z., Bovik, A. C., Sheikh, H. R. and Simoncelli, E. P., Image quality assessment: from error visibility to structural
14 similarity, *IEEE transactions on image processing*, 13(4), 600-612, 2004.

15 Webster, R., and Oliver, M. A.: *Geostatistics for environmental scientists*, John Wiley & Sons, 2007.

16



18

19 **Figure 1: Map of Greenland ice sheet. The digital elevation model (DEM) at 100 m resolution is represented in greyscale, the GC-**
 20 **Net air temperature locations are plotted as red triangles and the PROMICE surface mass balance measurements locations are**
 21 **reported as blue dots. The two rectangles indicate the Jakobshavn (blue) and Helheim (black) regions.**

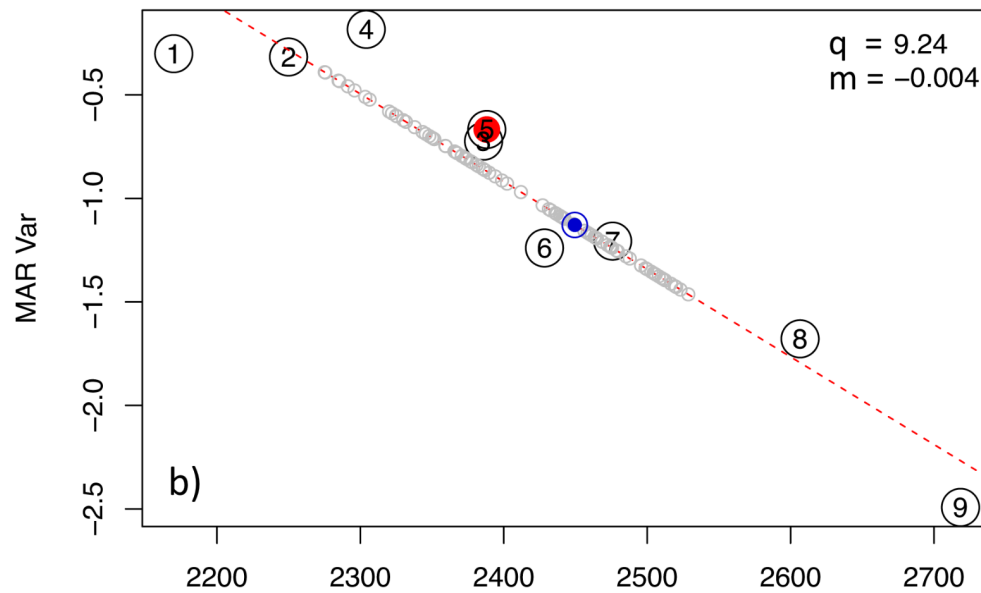
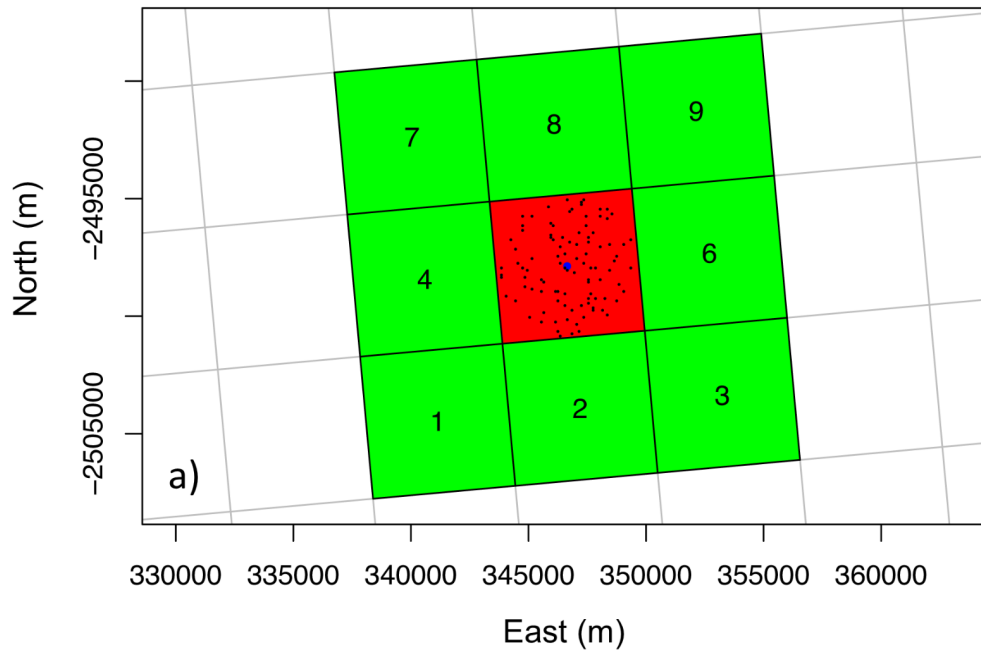
22

ID	Glacier/Site name	Latitude [°]	Longitude [°]	Measurement years	Points	Readings
126	Qaanaaq Ice cap	77° 30' 36'' N	69° 9' 0'' W	2012-2015	6	12
128	Petermann	80° 41' 2'' N	60° 17' 35'' W	2002-2013	2	4
130	Hans Tausen Ice Cap	82° 29' 24''	37° 30' 0'' W	1995 and earlier	5	13
140	Hare Glacier	82° 50' 24'' N	36° 40' 12'' W	1994-95	29	62
170	Kronprins Christian Land	79° 46' 48'' N	25° 11' 24'' W	1993-1994, 2008-2013	20	62
180	Nioghalfvjerdsfjorden	79° 30' 0'' N	21° 36' 0'' W	1996-1997	13	13
215	Storstrømmen	77° 30' 0'' N	23° 0' 0'' W	1989-1994	22	113
220	A.P. Olsen Ice Cap	74° 38' 24'' N	21° 26' 60'' W	2008-2013	17	56
230	Freya Glacier	74° 22' 48'' N	20° 49' 12'' W	2008-2013	29	93
232	Violin Glacier	72° 20' 60'' N	26° 58' 48'' W	2008-2013	2	12
254	Helheim	66° 24' 36'' N	38° 20' 24'' W	2008-2010	21	118
270	Isertoq	65° 42' 0'' N	38° 53' 24'' W	2007-2013	2	15
315	Nordbo Glacier	61° 30' 0'' N	45° 22' 12'' W	1977-83	41	200
412	Isortuarssup Sermia	63° 47' 60'' N	49° 47' 60'' W	1983-1988	3	9
414	Qamanarssup Sermia	64° 30' 0'' N	49° 23' 60'' W	1979-1988, 2007-2013	20	164
416	Kangilinnuata Sermia	64° 52' 48'' N	49° 17' 60'' W	2010-2013	1	3
420	Qapiarfiup	65° 34' 48'' N	52° 12' 36'' W	1980-1989	5	75
440	Amitsuloq Ice Cap	66° 8' 24'' N	50° 19' 12'' W	1981-1990	26	422
450	Tasersiaq	66° 15' 36'' N	51° 23' 60'' W	1982-1989	6	111
454	K-Transect	67° 5' 60'' N	48° 51' 36'' W	1990-2013	11	193
456	Paakitsoq, JAR	69° 29' 24'' N	49° 51' 36'' W	1982-1992, 1996-2013	22	220

458	Swiss Camp/ST2	69° 33' 53'' N	49° 19' 51'' W	1990-2014	2	12
-----	----------------	----------------	----------------	-----------	---	----

23
24
25

Table 1: PROMICE surface mass balance measurements information for the selected Glaciers and measurements sites.



26

27 **Figure 2: Elevation downscaling procedure example for a generic variable. In panel (a) the considered MAR pixel (red) and the**
 28 **surrounding pixels (green) adopted for the local linear regression are represented. The blue dot represents 100 m pixel location**
 29 **centered within the considered MAR pixel. In panel (b) the variable value of each considered pixel is reported as numbered circle.**
 30 **The dashed red line represents the linear regression computed for such pixels, the blue circle represents the downscaled variable for**
 31 **the blue pixel in panel (a) and the grey circles represent the downscaled variable for a group of 100 m pixels randomly picked within**
 32 **the considered MAR pixel which locations are represented as black dots in panel (a).**

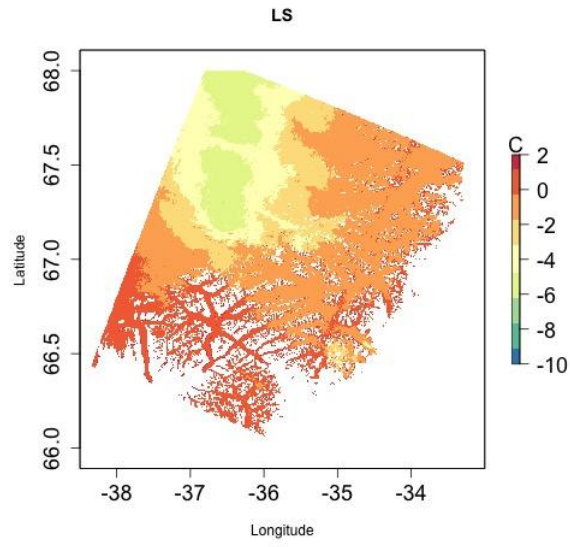
33

Station	Latitude [°]	Longitude [°]	Elevation [m]	R ₂ MAR _{6km}	R ₂ MAR _{100m}	RMSE MAR _{6km}	RMSE MAR _{100m}
Swiss Camp	69° 34' 06" N	49° 18' 57" W	1149	0.945	0.945	2.37	2.36
Crawford Pt.1	69° 52' 47" N	46° 59' 12" W	2022	0.872	0.873	3.95	3.95
NASA-U	73° 50' 31" N	49° 29' 54" W	2369	0.788	0.789	5.35	5.34
GITS	77° 08' 16" N,	61° 02' 28" W	1887	0.915	0.915	3.4	3.4
Humboldt	78° 31' 36" N	56° 49' 50" W	1995	0.801	0.801	5.64	5.64
Summit	72° 34' 47" N	38° 30' 16" W	3254	0.837	0.84	4.62	4.58
Tunu-N	78° 01' 0" N	33° 59' 38" W	2113	0.937	0.936	3.17	3.2
DYE2	66° 28' 48" N	46° 16' 44" W	2165	0.94	0.94	2.72	2.72
JAR1	69° 29' 54" N	49° 40' 54" W	962	0.787	0.786	4.37	4.38
Saddle	66° 00' 02" N	44° 30' 05" W	2559	0.935	0.935	2.77	2.77
South Dome	63° 08' 56" N	44° 49' 00" W	2922	0.915	0.915	2.76	2.77
NASA-E	75° 00' 00" N	29° 59' 59" W	2631	0.882	0.881	3.94	3.97
Crawford Pt.2	69° 54' 48" N	46° 51' 17" W	1990	0.893	0.894	3.62	3.61
NASA-SE	66° 28' 47" N	42°30' 00" W	2425	0.86	0.86	3.83	3.83
KAR	69° 41' 58" N	33° 00' 21" W	2579	0.935	0.936	2.6	2.57
JAR2	69° 25' 12" N	50° 03' 27" W	568	0.706	0.709	4.79	4.76
KULU	65° 45' 30" N	39° 36' 06" W	878	0.59	0.595	5.22	5.19

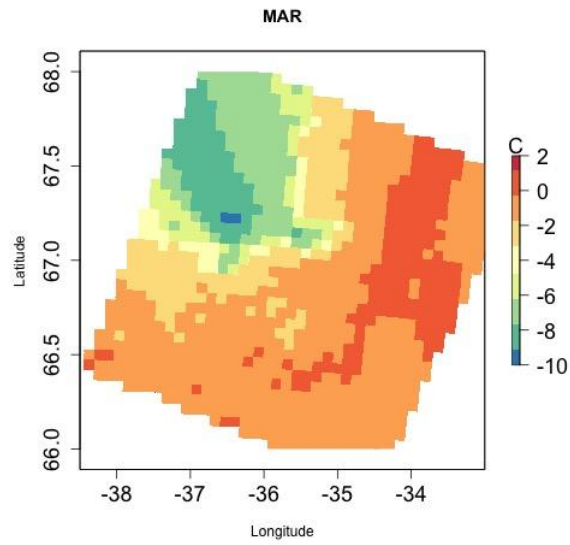
Table 2: Root-mean-square error and R² computed comparing MAR_{6km} and MAR_{100m} with air temperature measurements from the GC-Net considered stations. Longitude, latitude and elevation of the station are also reported.

34
35
36
37

38
39

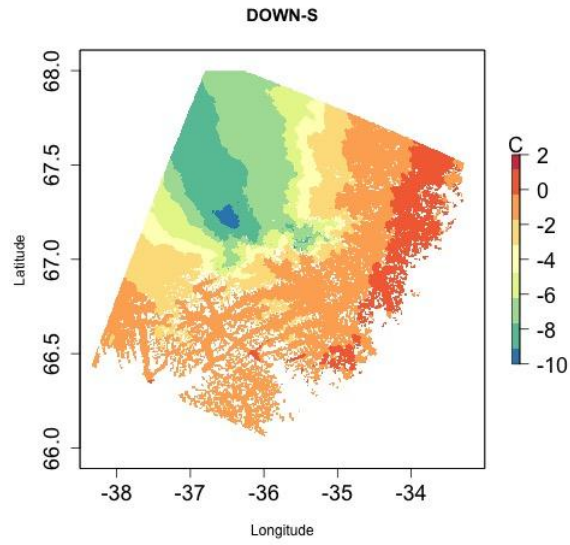


(a)



(b)

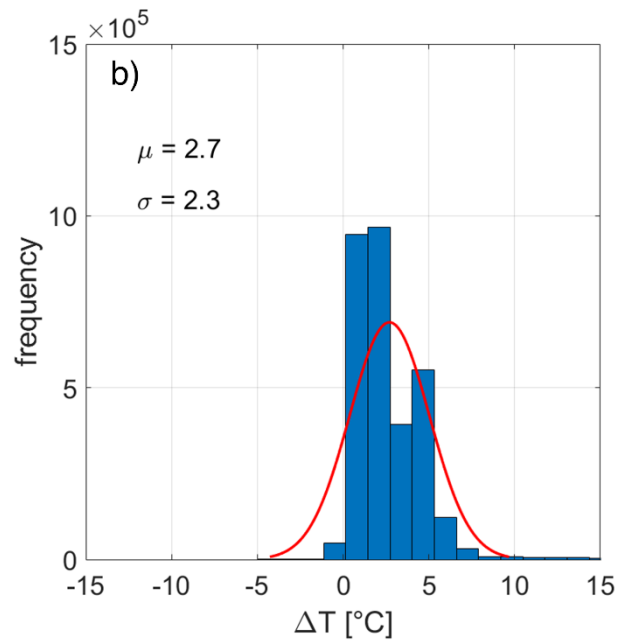
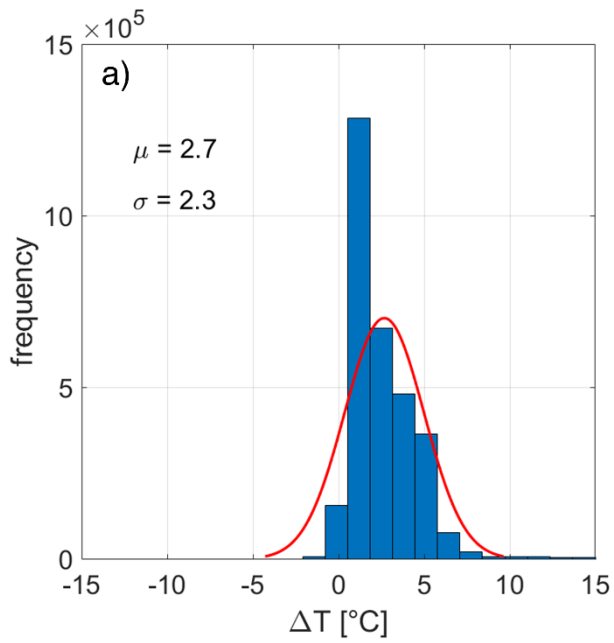
40
41



(c)

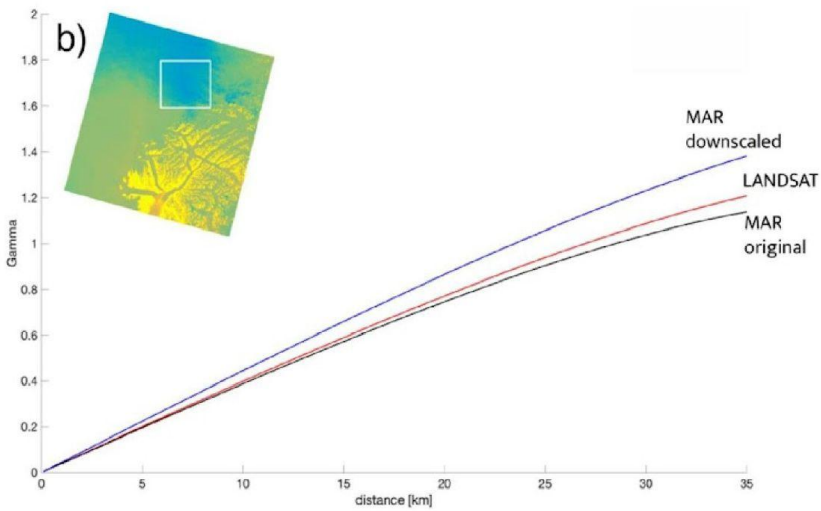
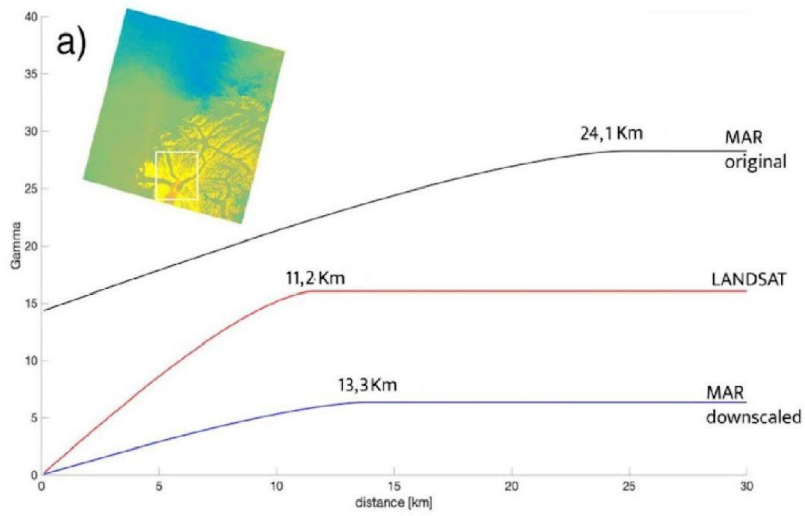
42
43
44
45
46
47
48

Figure 3: Maps of temperature from (a) Landsat-8, (b) MAR_{6km}v2 and (c) MAR_{100m} over the area covered by the Landsat 8 selected image on 30 June 2015. The blue dot reported to every map represents the 6 km pixel of the original MAR grid reported in red in Figure 2a.



49
50
51
52

Figure 4: Histograms of the difference (a) between the 6 km MAR temperature and Landsat-8 temperature and (b) between 100 m MAR temperature and Landsat-8 temperature.



54

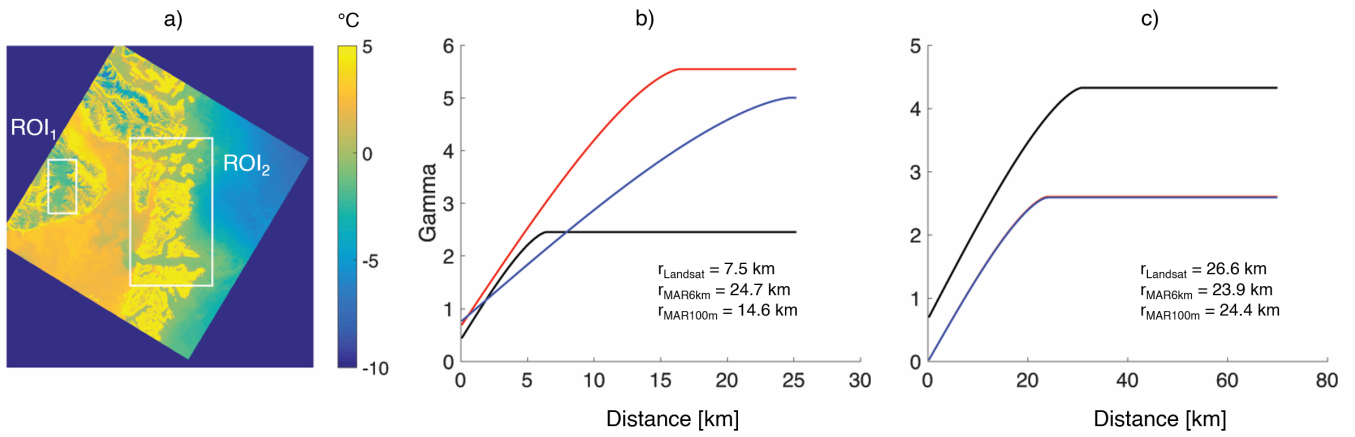
55

56

57

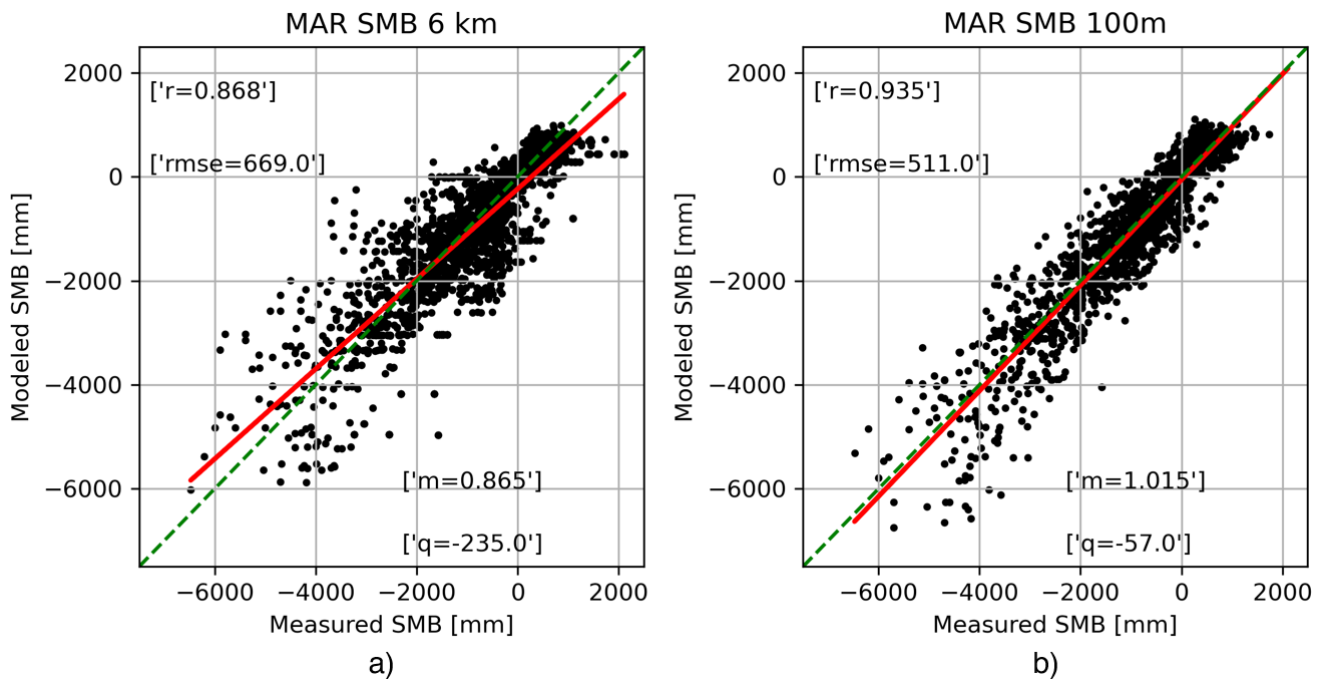
Figure 5: Modeled semi variograms for the Landsat-8, MAR_{6km} and MAR_{100m} computed over two regions of interest reported in the inset.

58



59
 60 **Figure 6: (a) Landsat-8 temperature captured on 11 June 2015 over areas around the Jakobshavn Glacier and (b, c) modeled semi**
 61 **variograms for the Landsat-8, MAR_{6km} and MAR_{100m} computed over (b) the first region of interest (ROI₁) and (b) the second**
 62 **of interest (ROI₂).**

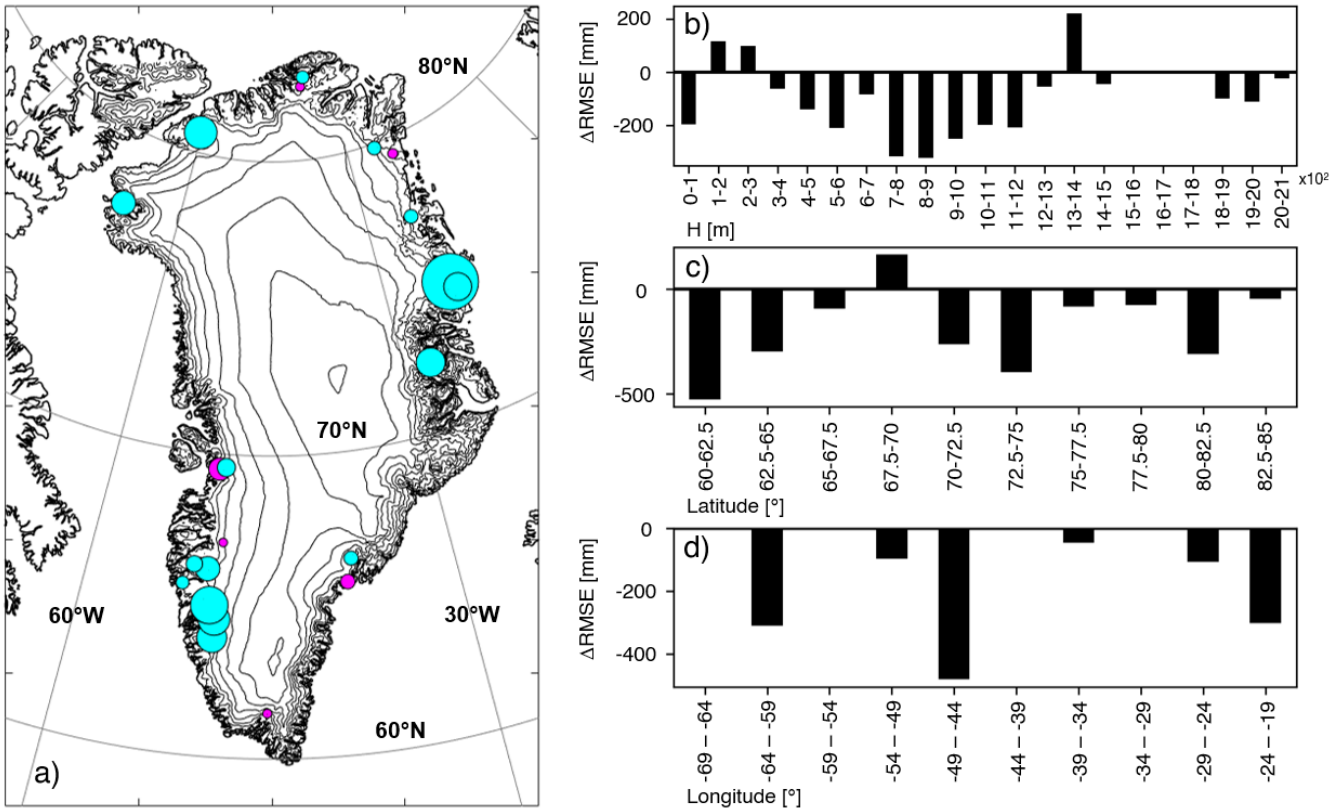
63



64

65 **Figure 7: Comparison between measured and modeled surface mass balance from (a) original 6 km MAR and (b) downscaled**
 66 **100 m MAR.**

67



68
69
70
71
72
73

Figure 8: Difference between original and downscaled MAR modeled surface mass balance RMSE with respect to the measured surface mass balance data ($RMSE_{100m} - RMSE_{6km}$) by (a) glacier, (b) elevation, (c) latitude and (d) longitude. In the bubble chart map the contour lines are plotted every 500 m (original MAR_{6 km} DEM), positive values (worsening) of $\Delta RMSE$ are reported in magenta while negative values (improvement) in cyan.