



A topographically-controlled tipping point for complete Greenland ice-sheet melt

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Abstract.

A major impact of anthropogenic climate change is the triggering of tipping points, such as the complete mass loss of the Greenland ice sheet (GrIS). At present, the GrIS is losing mass at an accelerated rate, largely due to a steep decrease in its surface mass balance (SMB, the balance between snow accumulation and surface ablation from melt and associated runoff). Previous work on the magnitude and nature of a threshold for GrIS complete melt remains controversial. Here, we explore a potential SMB threshold for GrIS complete melt, and the processes controlling the nature of this threshold. To this end, we use the Community Ice Sheet Model v.2 (CISM2) forced with different levels of SMB previously calculated with the full-complexity Community Earth System Model v.2 (CESM2). The SMB calculation in CESM2 has been evaluated with contemporary observations and high-resolution modelling, and includes an advanced representation of surface melt and snow/ firn processes.

We find a positive SMB threshold for complete GrIS melt of 230 ± 84 Gt/yr, corresponding to a 60% decrease from the GrIS pre-industrial SMB. The ice-sheet response to sustained melt is highly non-linear, and determined by the effect of the SMB-height feedback in response to surface melt and Glacial Isostatic Adjustment (GIA). While the former process increases melt and promote runaway retreat, GIA-induced bedrock uplift stabilises the ice margin and delays deglaciation. The GrIS is tipping from $\sim 50\%$ mass towards complete melt when the melt-induced surface lowering outweighs the GIA-induced bedrock uplift and the initially positive SMB becomes and remains negative for at least a few thousand years. We also find that the GrIS is tipping towards complete melt when the ice margin in the central west unpins from a coastal region with high bedrock elevation and SMB. Based on the minimum ice-sheet configuration in modelling studies of the GrIS during the last interglacial, we suggest that a stabilising effect of this midwestern topographic pinning point might have occurred in the past.



20 1 Introduction

The Greenland Ice-Sheet (GrIS) is the largest freshwater reservoir in the northern Hemisphere, storing currently 7.42 m of Sea Level Equivalent (SLE, Morlighem et al., 2017). At present, the GrIS is losing mass at an accelerated pace, with ice loss rates over the last decade up to six times higher than in the 1980s (Mouginot et al., 2019). This is due to both atmospheric and ocean warming, causing enhanced surface melt and runoff, and increased ice discharge to the ocean (Mouginot et al., 2019). While until the late 1990s ice discharge has been the main source of ice loss, over the last two decades the contribution of surface processes has continuously increased, and as of today 50% of the overall GrIS mass loss increase is due to a decrease in Surface Mass Balance (SMB, *i.e.*, the balance between snow accumulation and surface ablation from melt and associated runoff) of around 160 Gt/yr (Mouginot et al., 2019; The IMBIE Team, 2020). In the future, the GrIS is expected to continue losing mass, with its contribution to Global Mean Sea-Level (GMSL) largely depending on the amount of greenhouse gas forcing to the climate system (0.01-0.10 m under SSP1-2.6, 0.09-0.18 m under SSP5-8.5 relative to 1995–2014, see Fox-Kemper, 2021, and references therein). Regardless of the emissions pathways, there is broad agreement that the GrIS mass loss over the 21st century and beyond will be dominated by SMB, while the influence of ice discharge to the ocean will diminish as the marine margins retreat to higher grounds (Robinson et al., 2012; Fürst et al., 2015; Goelzer et al., 2020; Gregory et al., 2020; Payne et al., 2021). Most of the projected decrease in SMB at the end of the century is attributed to an increase in surface melt and to the loss in refreezing capacity of the firn layer (Fettweis et al., 2013; Vizcaino et al., 2015; Sellevold and Vizcaíno, 2020; Noël et al., 2022). Over longer, multi-centennial and millennial timescales, another important source for future GrIS mass loss is the SMB-height feedback: *i.e.*, as the surface topography lowers due to ice thinning, the near surface air temperature warms and leads to further ice melt. A number of paleo and future ice-sheet modelling studies agree in showing that this self-amplifying mechanism can cause GrIS partial or near-complete melt over multi-millennia (Robinson et al., 2012; Levermann et al., 2013; Plach et al., 2019; Gregory et al., 2020), with ice loss possibly accelerated by the lower surface albedo in response to surface melt which tends to further decrease the SMB (SMB-albedo feedback: Box et al., 2012; Goelzer et al., 2016; Zeitz et al., 2021). Robinson et al. (2012) showed that while a negative integrated SMB is a sufficient condition for GrIS complete melt, not accounting for the evolving ice-sheet topography and SMB-height feedback (as done for example in Gregory and Huybrechts, 2006; Noël et al., 2021) is likely to result in an overestimation of the temperature threshold for ice-sheet loss. Modelling studies including this mechanism (either explicitly, or parametrized) estimated a Global Mean Temperature (GMT) threshold for GrIS complete melt over the next millennia between 1.6 K and 3 K above pre-industrial levels, with the rate of GrIS decline depending on the amount of warming above the threshold (Robinson et al., 2012; Levermann et al., 2013; Clark et al., 2016; Van Breedam et al., 2020; Gregory et al., 2020; Zeitz et al., 2022; Höning et al., 2023). Paleo data and modelling indicate that during the last interglacial period (LIG, ~130-115 kyr BP) it is unlikely that the GMT exceeded 2 K above pre-industrial levels (Capron et al., 2014), and the GrIS contributed no more than 4 m to GMSL (Helsen et al., 2013; Goelzer et al., 2016; Plach et al., 2019; Sommers et al., 2021). This suggest that during the LIG the threshold for complete GrIS melt had not been passed, or the warming had been too little or too short to induce a full GrIS collapse. Another possible paleo-analogue for 21st century warming is the mid-Pliocene Warm Period (mPWP, ~3.264-3.025 Myrs BP, Haywood et al., 2011), which is



55 estimated to have been 2-3 K warmer than pre-industrial. GrIS simulations for this period yield extremely variable ice-sheet configurations, ranging from an ice-free state to a near modern GrIS depending on the climate forcing selected (Dolan et al., 2015). Altogether, paleo and future modelling studies both suggest the existence of a threshold for GrIS complete melt in a warmer climate; however, there is still uncertainty on the nature of this threshold, and whether or not the GrIS would exhibit a tipping point behaviour once this threshold is passed. A recent study using an ice-sheet model coupled to a low-resolution atmosphere Global Circulation Model (GCM) found a gradual, almost linear decline of GrIS equilibrium mass in response to sustained global mean warming (Gregory et al., 2020), rather than the sharp threshold behaviour found in earlier work (Robinson et al., 2012; Levermann et al., 2013). A better understanding of the mechanisms regulating the GrIS response to sustained warming is needed to determine the existence of tipping points for GrIS complete ice-sheet melt, and as such reduce uncertainties on the GrIS long-term Sea Level Rise (SLR).

65 Here, we determine a SMB threshold for GrIS complete melt, and we explore the processes controlling the nature of this threshold, as well as timing and pattern for GrIS decay. To this end, we use the higher-order Community Ice Sheet Model v.2 (CISM2, Lipscomb et al., 2019) forced with progressively decreasing SMB levels calculated with the full-complexity Community Earth System Model v.2 (CESM2, Danabasoglu et al., 2020) in a fully-coupled simulation of the global climate and GrIS (Muntjewerf et al., 2020b). The SMB calculation in CESM2 is based on a surface energy balance calculation, and includes an advanced representation of snow/firn processes, such as snow compaction, refreezing, and surface albedo (Muntjewerf et al., 2021; Sellevold and Vizcaíno, 2020). In our simulations, the SMB forcing is updated as the GrIS surface elevation evolves through an Elevation Classes (ECs) calculation in the land component of CESM2 (Muntjewerf et al., 2021), while bedrock changes due to Glacial Isostatic Adjustment (GIA) effect are accounted for in CISM2 through the Elastic Lithosphere-Relaxing Asthenosphere (ELRA) method (Lipscomb et al., 2019).

75 The paper is structured as follows: in Section 2, we briefly describe CISM2 (2.1), the SMB forcing (2.2) and the experimental setup (2.3). In Section 3 we analyse the main results, which are organised in three subsections on (3.1) thresholds, (3.2) pattern and timescales, and (3.3) processes for GrIS complete melt. In Section 4 we first discuss the thresholds found here in the context of the existing literature and end-of-century projections (4.1), and the existence of a tipping point for GrIS decay (4.2). We then draw our main conclusions and suggest possible future research directions (4.3).

2 Method

80 2.1 Ice-Sheet Model description

CISM2 is a parallel, three-dimensional thermomechanical ice-sheet Model (ISM) which solves equations for the conservation of mass, momentum, and internal energy (Lipscomb et al., 2019). In this study, CISM2 solves a depth-integrated viscosity approximation of the Stokes equations for incompressible viscous flow (DIVA, Goldberg, 2011). At the horizontal resolution used in this study for the Greenland domain (4 km), the DIVA outperformed other hybrid or zero-order solvers in terms of both model performance and representation of the ice-flow physics (Robinson et al., 2022). Basal sliding is calculated using a pseudo-plastic sliding law which incorporates linear, plastic and power-law behaviour (Aschwanden et al., 2016). Ocean



forcing at the marine-terminating outlet glaciers is not accounted here, and floating ice is immediately removed based on a simple flotation criterion. GIA is parameterized using the Elastic-Lithosphere/Relaxing-Asthenosphere (ELRA) model (see for example Rutt et al., 2009), which allows to take account for a regional bedrock response to changes in ice load. The main
90 CISM2 parameter values used in this study are provided in Table A1. Finally, while a more detailed description of all the CISM2 features and options can be found in Lipscomb et al. (2019), we highlight that the same model setup used here has been previously applied in fully coupled simulations of the global climate and the GrIS over the next centuries (Muntjewerf et al., 2020b, a) as well as in the past (Sommers et al., 2021).

2.2 SMB forcing

95 Here, we first provide a brief description of the general SMB calculation in CESM2 and how it is downscaled onto the CISM2 grid. Then, we describe the novel forcing method used in this study.

The SMB calculation is done in the land component of CESM2 (Community Land Model v.5, CLM5 Lawrence et al., 2019) and is defined as:

$$SMB = Precipitation - Runoff - Sublimation;$$

100 $Precipitation = Rain + Snowfall;$

$$Runoff = Rain + Melt - Refreezing.$$

Snowfall is calculated from the total precipitation depending on the surface temperature (100% snowfall if the temperature is below -2 K, 100% rain if the temperature is above 0 K, and linear interpolation in between). Rainfall can contribute positively to the SMB if it refreezes within the snowpack. Snow and ice melt are calculated based on the melt energy available within the
105 ice column, which depends on the sum of net surface radiation, latent and sensible turbulent surface fluxes, and ground heat fluxes at the atmosphere-snow interface (Lawrence et al., 2019). In order to overcome the challenge of resolving steep SMB gradients around the ice-sheet margins at relatively coarse typical CLM5 resolutions (1° in Muntjewerf et al., 2020b), the SMB is calculated at 10 Elevation Classes (ECs), with boundaries at 0, 200, 400, 700, 1000, 1300, 1600, 2000, 2500, 3000, and 10000 m. This is done first by downscaling the CLM5 grid cell temperature to the EC elevation using a uniform lapse rate of
110 -6 K/km. A vertically uniform relative humidity is then assumed to determine the potential temperature, specific humidity, air density, and surface pressure over each EC. The interpolated fields are then used to calculate the SMB components in each EC. After annual SMB is calculated at each EC in CLM5, it is then downscaled to the higher-resolution CISM2 domain through horizontal bilinear interpolation and linear vertical interpolation between adjacent ECs to the ice-sheet model surface elevation. More details on the SMB calculation and on the CESM2/CISM2 coupling are provided in Muntjewerf et al. (2021).

115 For this study, we use a functionality of CESM2 that allows to run CISM2 within the Earth System Model architecture, forced with multiple-ECs SMB previously calculated in CLM5. Under this setup, the SMB forcing fields are provided on the CLM5 grid. During runtime, every year the CESM2 coupler performs the trilinear (bilinear horizontal + linear vertical) interpolation to the surface elevation on the CISM2 4 km Greenland domain. In this way, the SMB is automatically updated



during runtime for changes in ice-sheet geometry. This allows us to account for the SMB-height feedback based on snow/ice
120 processes and energy fluxes at the ice-sheet surface.

2.3 Experimental setup

In this study, we force CISM2 with multiple-ECs SMB from a published, fully coupled CESM2/CISM2 simulation of the
global climate and GrIS under an idealized, high Greenhouse Gas (GHGs) scenario (hereinafter referred to as BG-1pct run,
Muntjewerf et al., 2020b). In this simulation, atmospheric CO₂ concentration is increased by 1% every year until it reaches
125 four times pre-industrial values at year 140, after which it is kept fixed. From the BG-1pct run, we select several 23 years-long
intervals corresponding to different SMB, and transient global mean and GrIS warming levels (values are shown in Table 1, see
also Fig.1a). The choice of the intervals length results as a compromise between keeping the SMB standard deviation within
the range of pre-industrial values and a sampling rate large enough to prevent data aliasing. In each simulation, we cycle the 23
years-long, multiple-ECs SMB forcing until a stable ice-sheet configuration is reached. Each run is restarted from the BG-1pct
130 run at the last year of the corresponding forcing interval (initial and final year of each forcing interval are shown in Table
A2). Additional sensitivity tests are performed by repeating some runs in which we (1) switch off the GIA parametrization in
CISM2 and (2) increase sliding velocities, by prescribing lower values (2.3° and 0.5°) of the minimum friction angle in the
pseudo-plastic sliding law (see Table A1).

3 Results

135 Here we first describe the relationship between SMB forcing and final GrIS volume, to provide an SMB threshold for GrIS
complete melt. We then illustrate the pattern and timescales for ice retreat, in particular for simulations close to the SMB
threshold. We conclude by assessing the processes that determine the GrIS response to sustained warming.

3.1 Thresholds for GrIS complete melt

In our simulations, the GrIS exhibit a sharp threshold behaviour, with a highly non-linear relationship between initial SMB
140 forcing and final GrIS mass (Fig. 1b). In Table 1 the SMB forcing, the corresponding transient global mean and GrIS warming
above pre-industrial, and the resulting final GrIS volume are provided for each run. Final GrIS states are clustered in three main
groups: (a) “low melt”, with less than 25% GrIS mass loss (b) “medium melt”, with around 50% GrIS mass loss, (c) “complete
melt”, with more than 80% GrIS mass loss. GrIS limited loss (<25%) is obtained for an initial SMB forcing above 317±97
Gt/yr, and transient global mean and GrIS warming above pre-industrial below 2.8 K and 2.2 K, respectively. Compared to
145 the fully coupled CESM2/CISM2 pre-industrial control simulation (hereafter BG-PIcontrol run, Lofverstrom et al., 2020, see
Table 2), this means that low GrIS melt is achieved for a decrease in SMB not exceeding 50% of the equilibrium pre-industrial
SMB. An ice loss of around 50% of the initial GrIS mass is obtained for intermediate SMB forcing (between 40 and 50% of
the pre-industrial equilibrium SMB) and global mean warming values (between 2.8 and 3.4 K above pre-industrial). We find
that the GrIS is bound to completely melt if the initial SMB forcing is lower than 230±84 Gt/yr (Fig. 1b and Table 1). This is a



150 decrease of around 60% of the GrIS equilibrium SMB at the end of the BG-PIcontrol run. The SMB threshold corresponds, in
the BG-1pct run, to a transient global mean and GrIS warming above pre-industrial of 3.4 K and 3.2 K, respectively (Fig. 1a
and Table 1).

3.2 Pattern and timescales of GrIS retreat

In the “low melt” simulations, ice loss mostly takes place at the southwestern margin, with limited retreat in the north occurring
155 in the +2.8 K run (see inset in Fig. 1b). The southwestern GrIS margin retreats all the way to the east in the “medium melt”
simulations, until a large ice cap in the southern tip of Greenland is disconnected from the GrIS main body. In these simulations,
showing an intermediate GrIS loss, significant retreat also occurs in the north, whereas the midwestern ice-sheet margin remains
close to the coast (see inset in Fig. 1b). When the SMB threshold for complete GrIS melt is passed, the GrIS retreats all the
way towards the east, with isolated ice caps of variable size remaining in regions of high bedrock elevation (see inset in Fig.
160 1b). Timescales for ice loss increase sharply as the initial SMB forcing gets close to the threshold for GrIS complete mass
loss. In the “low melt” simulations, minimum GrIS volume is reached within the first 15 kyrs (Fig. 2 and Table 1). Timescales
are doubled for the “medium melt” simulations, in which the GrIS attains minimum volume after around 30-35 kyrs. The
simulation immediately above the SMB threshold (+3.4 K run) shows the highest response time, as the GrIS keeps decreasing
until 40 kyrs, after a retreat slowdown between 15 and 20 kyrs (Fig. 2 and Table 1). For the other simulations in the “complete
165 melt” group, timescales decrease quickly as the initial SMB forcing gets lower and moves away from the threshold. For a
positive initial SMB forcing, the shortest GrIS deglaciation time is around 12 kyrs, whereas if the initial SMB forcing is
negative Greenland becomes mostly ice-free in 8 kyrs or less (Fig. 2). Detailed GrIS retreat pattern and timescales for each
simulation are displayed in Supplementary Videos V1-10.

3.3 Processes controlling ice retreat

170 In our simulations, the response of the GrIS to sustained warming is primarily determined by the interplay of surface melt and
GIA, which are interconnected through the SMB-height feedback. For every initial SMB forcing level, the ice-sheet loses mass
during the first 10-15 kyrs, and the SMB further decreases due to ice thinning and surface elevation lowering (Fig. 2). However,
the impact of ice thinning is mitigated, and in some cases counterbalanced, by GIA: while the ice sheet thins and retreat, the
bedrock uplifts, thus increasing the surface elevation and, consequently the SMB (see bottom panel in Fig. 2 and Supplementary
175 Video xxx). This interplay is key in determining whether the ice-sheet will disappear or not: GrIS complete loss is achieved
only in simulations where the surface lowering outweighs the bedrock uplift, and the SMB becomes and remains negative
for at least a few thousand years (Fig.2). When this does not happen, the GrIS eventually reaches a more stable configuration
as in the “low melt” or “medium melt” groups. In the simulations that are closest to the threshold for complete GrIS melt,
the interplay of SMB-height feedback and GIA is also causing self-sustained, quasi-periodic ice-sheet oscillations ranging
180 between 3% and 12% of the initial GrIS mass. In fact, in some cases the increase in SMB due to GIA-induced bedrock uplift
can promote ice thickening and margin readvance. This mechanism is then reverted when the isostatic subsidence resulting
from ice thickening causes the SMB to decrease again, enough to promote ice thinning and margin retreat (see Supplementary



Videos). The amplitude and periodicity of these oscillation increase as the initial SMB forcing gets closer to the threshold for complete GrIS melt. The highest oscillation amplitude and periodicity is obtained in the simulation immediately after the SMB
185 threshold is crossed (+3.2 K run, with a volume oscillations of 12% of the initial ice mass and over cycles of 30 kyrs, see Fig. A1). If GIA is switched off, the response of the GrIS changes drastically. When we turn off GIA for a simulation in the “medium melt” group (+3.2 K run), SMB-height feedback due to surface lowering alone causes a rapid deglaciation in 10 kyrs (Fig.3). This is equivalent, both in terms of final GrIS mass and timing response, to a simulation in the “complete melt” group, with an initial SMB forcing well above the threshold (+4.0 K run). For other simulations in the “complete melt” group, removing
190 the GIA effect greatly reduces the timescales for GrIS destabilization and substantial mass loss, except when the original timescales are already shorter than 5 kyrs with isostasy included (Fig.3). Our sensitivity tests (described in Subsection 2.3) also show that ice discharge does not play a role in determining the long-term GrIS equilibrium response to sustained warming. In fact, while the increase in ice discharge affects the overall GrIS mass budget over centuries, the long-term ice-sheet response remains unchanged, and is determined solely by the SMB evolution (see Fig. A2).

195 A comparison of the simulations immediately below and above the SMB threshold for GrIS complete melt (+3.2 K and +3.4 K runs, Fig. 4) indicates that the ice margin position in the central west is crucial to determine the final ice-sheet state. In particular, a group of isolated ice caps with high bedrock elevation and SMB (Fig. 4 and A3) act as a topographic pinning point for the GrIS. In fact when the ice margin remains sufficiently close to these topographic highs to reestablish connection during margin readvances within self-sustained oscillations, the ice loss in the southwest and north remains limited (see left panel in
200 Fig. 4 and Supplementary Video V5). When instead the midwestern margin loses permanently contact with the topographic pinning point, the SMB-height feedback causes a runaway ice retreat towards the east, and more than 80% of the GrIS mass is lost. This tipping behaviour is clear in the first simulation above the SMB threshold (+3.4 K run, see central panel in Fig. 4), with the runaway retreat occurring only after 20 kyrs, when the connection between the ice sheet and the topographic pinning point is permanently lost. In the remaining simulations after the SMB threshold is crossed, the connection between
205 the midwestern margin and the topographic pinning point is lost earlier (around 15 kyrs or less) and the retreat pattern is more uniform in time (see right panel in Fig. 4, A4 and Supplementary Videos V5-7).

4 Discussion

In this section, we compare the thresholds found here with the existing literature. Even though our simulations are not meant to represent realistic scenarios, we will also try to put the thresholds found here in the context of end-of-century future projections.
210 Then, we will discuss the GrIS tipping point behaviour and the stabilizing effect of the topographic pinning point found in the central west. We will then summarise our conclusions and suggest possible future research directions.

4.1 Thresholds for complete GrIS melt

Here we have found a positive SMB threshold of 230 ± 84 Gt/yr for complete GrIS melt. This corresponds to a 60% decrease from the GrIS equilibrium SMB calculated in the BG-PIcontrol run (591 ± 83 Gt/yr, see Table 2 and Lofverstrom et al., 2020). In



215 this pre-industrial run, no corrections are applied to the SMB, and the GrIS is left free to evolve. Although CESM2 compares
reasonably well with ERA-Interim and RACMO2 for several key controls on GrIS SMB (surface melt, runoff, longwave
radiation van Kampenhout et al., 2020; Noël et al., 2020), this approach led to an overestimation of the GrIS initial extent
(15%), volume (13%) and as a consequence, of a pre-industrial SMB, which is higher than in uncoupled CESM2 experiments
and present-day observations (see Table 2 and Lofverstrom et al., 2020). In view of this, the positive SMB threshold found here
220 is coupled-model dependent, and it remains complicated to analyse in the context of end-of-century projections, or to make a
direct comparison with other modelling studies and recent observations. Constraining ISM simulations to GrIS changes during
the LIG, Robinson et al. (2012) found a positive SMB threshold for complete ice-sheet melt ranging between 150-340 Gt/yr.
This agrees reasonably well with our study, although in Robinson et al. (2012) the pre-industrial SMB is lower (around 400
Gt/yr). In the fully coupled CESM2/CISM2 projection for the SSP5-8.5 scenario, the SMB crosses our threshold for GrIS
225 instability between years 2060-2080, and by the end of the century it has become negative (Muntjewerf et al., 2020a). In our
simulations, a negative SMB forcing leads to a relatively rapid GrIS deglaciation in less than 10 kyrs (Table 1 and Fig. 2).
While fully coupled CESM2/CISM2 simulations for lower emission scenarios (SSP1-2.6, SSP2-4.5, SSP3-7.0) are currently
not available, in the corresponding CESM2-only future projections the SMB over the GrIS at the end of the century is well
below the threshold found here, regardless of the emission scenario considered (see Table 2). This comparison, however, must
230 be considered carefully as (a) the GrIS pre-industrial SMB is lower in CESM2-only runs, (b) in CESM2-only runs, the SMB
is calculated over a fixed present-day GrIS topography, and as such the SMB-height feedback is not accounted for.

The SMB threshold found here corresponds to a transient global mean and GrIS warming of 3.4 K and 3.2 K above pre-
industrial, respectively. Our global mean warming threshold is at the high end of previous ice-sheet modelling studies with
climate forcing (a) calculated offline with GCMs (3.1 K, Gregory and Huybrechts, 2006) (b) interactively calculated with
235 regional models or intermediate complexity Earth System Models (1.6-3 K, Robinson et al., 2012; Levermann et al., 2013;
Gregory and Huybrechts, 2006; Höning et al., 2023). We highlight however that in our forcing method the SMB has not fully
equilibrated with the climate, and a more sustained warming of 3.4 K above pre-industrial would likely result in a lower SMB
as the snow pack deteriorates (ablation area expansion, less refreezing capacity). To properly determine a global mean warming
threshold for complete GrIS melt would require running further CESM2/CISM2 fully or asynchronously coupled experiments,
240 which is computationally too expensive and out of the scope of this study.

4.2 GrIS tipping point behaviour

Our simulations indicate that the GrIS response to sustained warming is highly non-linear, and that the ice-sheet is tipping
from 50% mass towards complete melt once that the positive SMB threshold is passed. This agrees well with early modelling
studies (Gregory and Huybrechts, 2006; Robinson et al., 2012; Levermann et al., 2013). However, this is in contradiction with
245 the results presented in Gregory et al. (2020), which suggests a gradual, almost linear GrIS decline in response to sustained
global mean warming. In their study, Gregory et al. (2020) used an ISM coupled to a low-resolution atmosphere GCM, and
adopted a similar EC approach as done in CESM2 for the SMB calculation. Here, CISM2 is not bi-directionally coupled to
CESM2, and as such we do not account for increased cloudiness and snowfall as the ice-sheet margin moves towards the



interior. In Gregory et al. (2020), these processes result in an increase in precipitation which in some cases counterbalances the
250 SMB-height feedback and lead to the multiple stable GrIS states. However, in our simulations the GrIS tipping behaviour is
determined by the interplay of SMB-height feedback and GIA, with the latter not being accounted for in Gregory et al. (2020).
While we cannot exclude that accounting for ice-sheet/atmospheric circulation feedbacks would stabilise the GrIS and change
the SMB threshold, it is also difficult to determine if they would drastically change the non-linear nature of the GrIS response
to sustained warming found here. Another recent study by Zeitz et al. (2022) found a similar, non-linear impact of the interplay
255 between GIA and SMB-height on the GrIS response to sustained warming, with final GrIS states clustered in three main groups
for a global warming exceeding 2 K above pre-industrial (“partial recovery”, “oscillations”, “loss”). Zeitz et al. (2022) used
a different ISM and GIA parametrisation than in our study, thus suggesting that the GrIS tipping behaviour simulated here is
unlikely to depend on our model setup. Our study also agrees well with (Zeitz et al., 2022; Plach et al., 2019) in showing that
increased ice discharge rates have no effect on the long-term GrIS equilibrium response to sustained warming.

260 We find that the GrIS is tipping towards complete melt if the ice margin in the central west retreats enough to disconnect
from a group of isolated ice caps with high bedrock elevation and SMB. If the ice margin remains pinned to this topographic
pinning point, GrIS loss is limited also in southwestern and northern Greenland, and does not exceed 50% of the initial GrIS
mass. The presence of this topographic feature of the GrIS, in combination with a stable midwestern margin position and
limited ice loss in the southwest and north has been consistently simulated in ice-sheet modelling studies of the LIG (Helsen
265 et al., 2013; Plach et al., 2019; Goelzer et al., 2016; Sommers et al., 2021). In these simulations, the midwestern margin
remains pinned to the topographic pinning point, and the GrIS does not lose more than 4 m SLE. In particular, in the fully
coupled CESM2/CISM2 simulation of the LIG, the GrIS extent at 123 kyrs ago is extremely similar to those in our simulations
belonging to the ‘medium melt’ group (see Fig. 3 in Sommers et al., 2021). After this time, however, the SMB becomes positive
and the GrIS starts to readvance towards the west. This suggests that around 123 kyrs the GrIS might have been close to tipping
270 towards a much reduced state. Compared with other modelling studies indicating a GrIS tipping point behaviour in response
to sustained warming, our study agrees in showing that the ice-sheet retreats towards the east, and that the midwestern margin
remains close to the coast before tipping (Robinson et al., 2012; Höning et al., 2023; Zeitz et al., 2022).

4.3 Conclusions and future research

Here, we have used a state-of-the-art, higher-order Ice-Sheet Model (CISM2) to (1) determine a SMB threshold for GrIS
275 complete melt, (2) investigate the nature of this threshold, (3) understand the processes controlling the ice-sheet response. We
forced CISM2 with different levels of SMB, previously calculated at multiple Elevation Classes with a full-complexity Earth-
System Model (CEMS2) which includes an advanced representation of snow/firn processes, surface albedo and melt. In our
simulations, the SMB is updated as the ice-sheet surface elevation changes through the Elevation Classes (ECs) method, and
bedrock changes due to GIA effects are accounted for in CISM2 through the ELRA parametrization.

280 We have found a positive SMB threshold for complete GrIS melt of 230 ± 84 Gt/yr, corresponding to a 60% decrease from
the GrIS pre-industrial equilibrium SMB. This SMB threshold corresponds to a transient global mean and GrIS warming of 3.4
K and 3.2 K above pre-industrial, respectively. The thresholds found here are in overall agreement with previous studies. In our



simulations, the response of GrIS to sustained warming is highly non-linear, and final ice-sheet state are clustered in three main groups: (a) “low melt” (<25% mass loss), (b) “medium melt” (~50% mass loss), (c) “complete melt” (>80% mass loss). This tipping behaviour is determined by the effect of SMB-height feedback in response to surface melt and GIA. While topographic lowering due to surface melt promote further melt and ice loss, GIA causes a bedrock uplift which yields in turn reduced melt, ice thickening and margin stabilisation or readvance. The GrIS is tipping from ~50% mass towards complete loss when the melt-induced surface lowering outweighs the GIA-induced bedrock uplift, and the initially positive SMB becomes and remains negative for at least a few thousand years. A similar tipping behaviour of the GrIS, resulting from the interplay of SMB-height feedback and GIA, has been also simulated in other studies. However, literature also suggests that ice-sheet/atmosphere stabilising feedbacks might dampen the non-linear response of the GrIS to sustained warming. We also found that whether the GrIS will tip towards complete melt or not depends on the ice-sheet margin position in the central west. When the ice margin remains pinned to a coastal region with high bedrock elevation and SMB, GrIS loss is limited also in the southwest and north and remains close to ~50% of its initial mass. Previous modelling studies of the GrIS during the LIG show that the ice-sheet had, at its minimum extent, a similar configuration as in our simulations in the “medium melt” group. In view of this, we suggest that a stabilising effect of the midwestern topographic pinning point might also have occurred during the LIG.

The modelling approach presented here includes an advanced representation of the SMB-height and albedo feedback through the CESM2 melt energy calculation, snow/firn model and Elevation Classes approach. Nevertheless, the main caveat of this study is that CISM2 is not bi-directionally coupled to CESM2, and as such we do not account for a number of ice-sheet/atmosphere feedbacks (*e.g.*, increase in cloud cover and precipitation as the GrIS retreats towards the interior). To better understand the nature of the response of the GrIS to sustained warming, further coupled modelling (and as such, computational) efforts should be dedicated to fully resolve how these negative feedbacks interact with SMB-height feedback and GIA. In addition, future modelling studies of the GrIS during the LIG could shed light on how close the GrIS might have been to tipping at its minimum extent, and which processes might have prevented that.

Code and data availability. CESM2 is an open source model, available at <https://www.cesm.ucar.edu>. Computing and data storage resources, including the Cheyenne supercomputer (doi:10.5065/D6RX99HX), were provided by the Computational and Information Systems Laboratory (CISL) at NCAR. Forcing files from the fully coupled simulations and setup scripts to reproduce our simulations are stored in the Cheyenne supercomputer and available upon request.

Video supplement. Supplementary Videos can be found on Zenodo (<https://doi.org/10.5281/zenodo.8384527>).

Author contributions. MV planned the research; MS performed an initial set of simulations; MP performed the remaining simulations, analysed the output and wrote the manuscript. All authors discussed the results and reviewed and edited the manuscript.



Competing interests. The contact author has declared that none of the authors has any competing interests.

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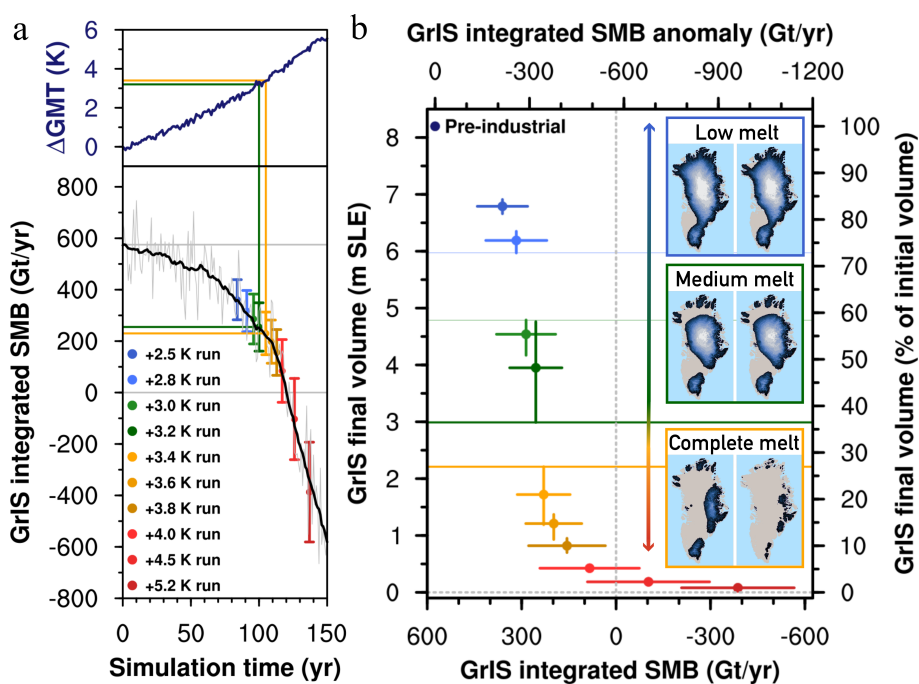


Figure 1. (a) Timeseries of (upper panel) Global Mean Temperature (GMT) anomaly relative to pre-industrial and (bottom panel) GrIS integrated Surface Mass Balance in the fully coupled BG-1pct simulation (Muntjewerf et al., 2020b). In the bottom panel, the SMB forcing used in our simulations ($\text{avg} \pm \text{stddev}$) is indicated in different colors for each run (see the inset legend). Green and yellow lines highlight the transition between “medium” to “complete” GrIS melt. (b) Scatter plot of GrIS integrated SMB forcing ($\text{avg} \pm \text{stddev}$, x-axis) vs GrIS final volume ($\text{avg} \pm \text{min/max}$, y-axis) in each simulation. Colors for each simulation as in the inset legend in (a). In the inset maps, GrIS final extent is showed for two simulations belonging in each group (for the “complete melt” group, +3.2 K and +4.0 K runs are shown).

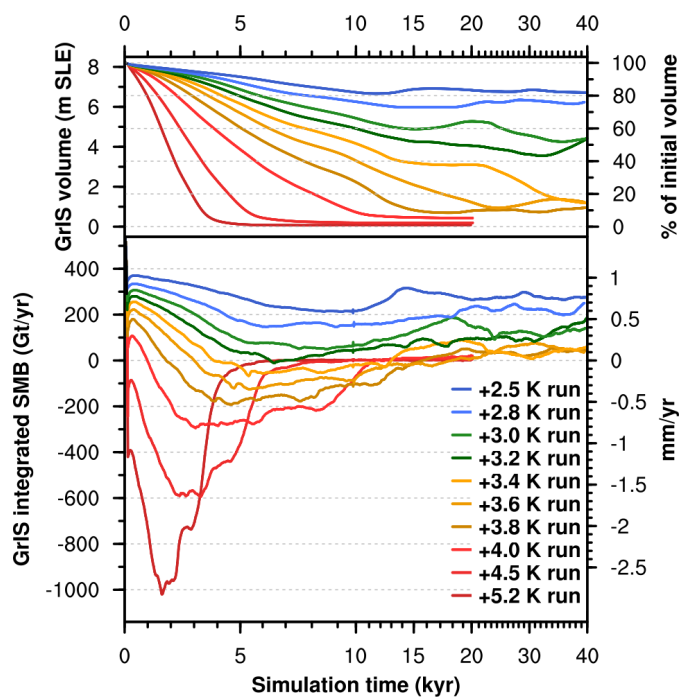


Figure 2. Timeseries of (upper panel) GrIS volume and (bottom panel) integrated Surface Mass Balance for the main runs presented in this study. Note that simulation time in the x-axis is irregular (minor tickmarks every 1000 years).

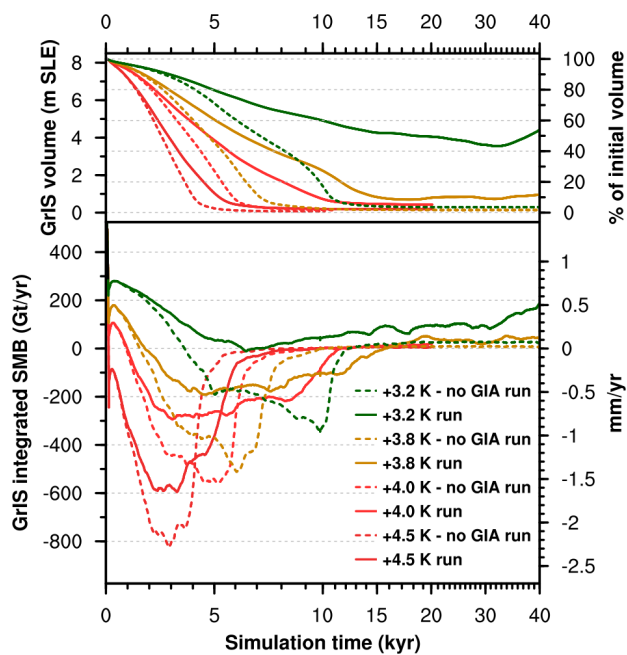


Figure 3. Timeseries of (upper panel) GrIS volume and (bottom panel) integrated Surface Mass Balance for selected sensitivity simulations with GIA turned on (solid lines) and GIA turned off (dashed lines). Note that simulation time in the x-axis is irregular (minor tickmarks every 1000 years).

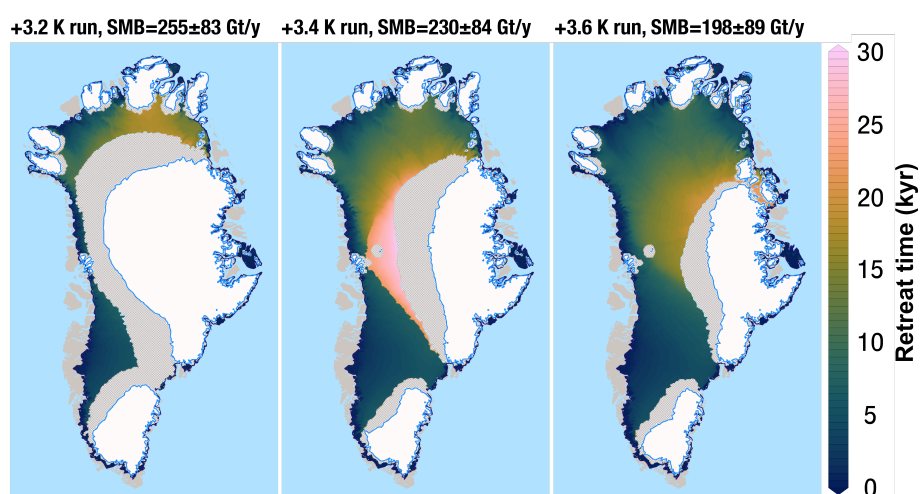


Figure 4. Map of GrIS retreat time for the (left) +3.2 K run, (center) +3.4 K run, (right) +3.6 K run. Ice-sheet areas showing GIA-induced margin oscillations are shown in grey, whereas areas continuously ice-covered throughout each run are filled in white.



Δ GMT	Δ GrISMT	SMB (avg \pm stddv)	Δ SMB	Final vol. (min/ avg /max)	Min. vol. time
Low melt					
+2.5 K	+2.0 K	361 \pm 80 Gt/yr	-230 Gt/yr	6.66 / 6.79 / 6.91 m SLE	11 kyrs
+2.8 K	+2.2 K	317 \pm 97 Gt/yr	-274 Gt/yr	5.97 / 6.19 / 6.35 m SLE	14 kyrs
Medium melt					
+3.0 K	+2.7 K	286 \pm 94 Gt/yr	-305 Gt/yr	4.17 / 4.54 / 4.79 m SLE	35 kyrs
+3.2 K	+2.9 K	255 \pm 83 Gt/yr	-336 Gt/yr	2.99 / 3.95 / 4.76 m SLE	31 kyrs
Complete melt					
+3.4 K	+3.2 K	230 \pm 84 Gt/yr	-361 Gt/yr	1.19 / 1.72 / 2.21 m SLE	40 kyrs
+3.6 K	+3.7 K	198 \pm 89 Gt/yr	-392 Gt/yr	0.93 / 1.21 / 1.37 m SLE	25 kyrs
+3.8 K	+4.0 K	156 \pm 122 Gt/yr	-435 Gt/yr	0.70 / 0.82 / 0.95 m SLE	17 kyrs
+4.0 K	+4.2 K	84 \pm 158 Gt/yr	-507 Gt/yr	0.43 / 0.42 / 0.42 m SLE	12 kyrs
+4.5 K	+5.0 K	-103 \pm 194 Gt/yr	-695 Gt/yr	0.18 / 0.19 / 0.19 m SLE	8 kyrs
+5.2 K	+5.9 K	-387 \pm 179 Gt/yr	-978 Gt/yr	0.07 / 0.08 / 0.09 m SLE	5 kyrs

Table 1. First four columns: values from each of the 23 years-long intervals in the fully coupled BG-1pct run used to force our simulations (transient global mean and GrIS anomaly to pre-industrial, GrIS integrated SMB, GrIS integrated SMB anomaly to pre-industrial). In the last two columns, final GrIS volume (minimum/average/maximum) and time needed to reach minimum GrIS volume in our simulations.



Runs	Pre-ind.	Contemporary (1995-2014)	Mid-century (2031-2050)	End-of-century (2080-2099)
CESM2/CISM2				
Pre-ind.	591±83 Gt/yr			
Hist.		571±80 Gt/yr		
SSP5-8.5			359±84 Gt/yr	-511±283 Gt/yr
CESM2-only				
Hist.		390±28 Gt/yr		
SSP1-2.6			252±65 Gt/yr	88±97 Gt/yr
SSP2-4.5			267±58 Gt/yr	21±80 Gt/yr
SSP3-7.0			227±76 Gt/yr	-269±106 Gt/yr
SSP5-8.5			192±90 Gt/yr	-906±307 Gt/yr

Table 2. Comparison of GrIS integrated Surface Mass Balance ($\text{avg} \pm \text{stddev}$) for fully coupled CESM2/CISM2 simulations and CESM2-only simulations for pre-industrial, historical and available SSP scenarios contributing to CMIP6. Note that in the CESM2-only runs the Surface Mass Balance is calculated and integrated over the prescribed, present-day observed GrIS elevation.

Appendix A: Supplementary Figures and Tables

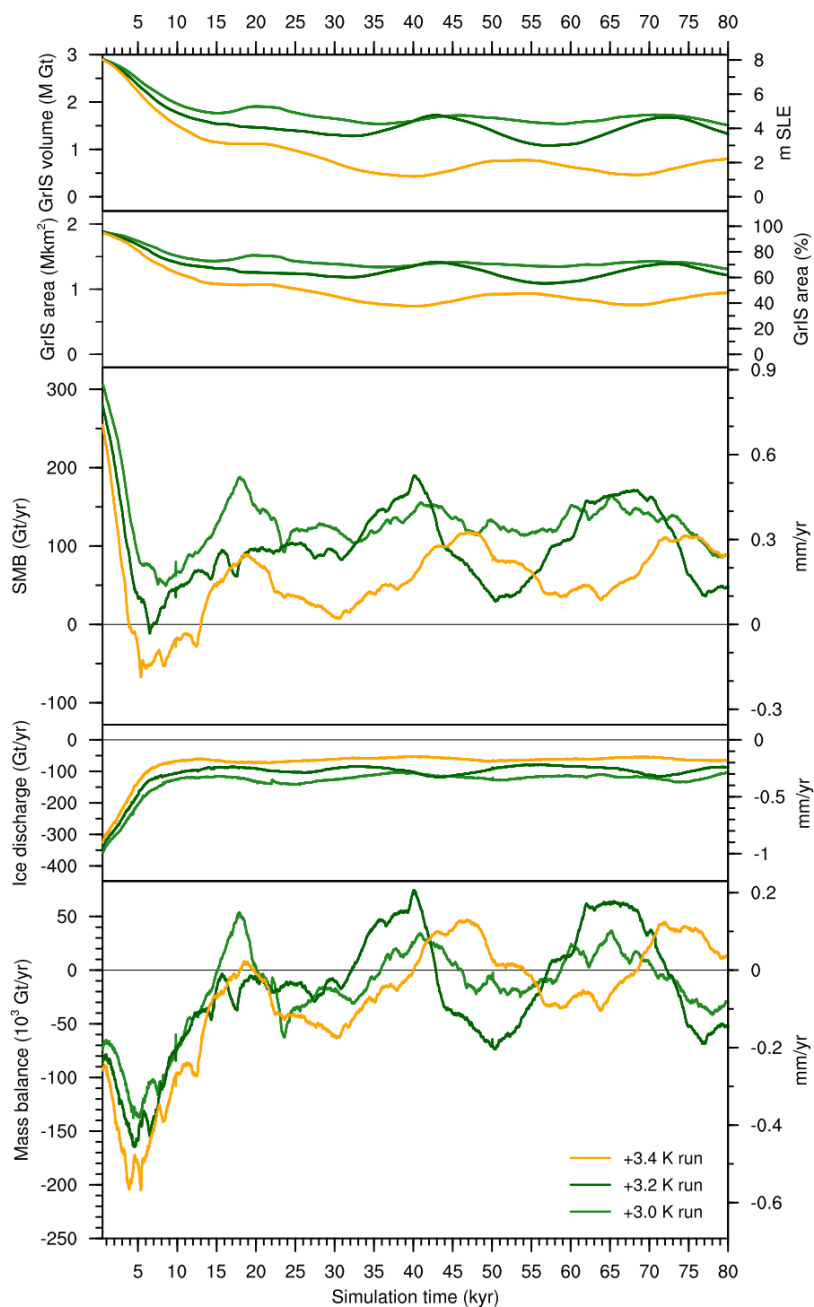


Figure A1. Timeseries of GrIS volume, area, Surface Mass Balance, ice discharge and mass balance for selected simulations extended until 80 kyr, to show the quasi-periodicity of GIA-induced oscillations.

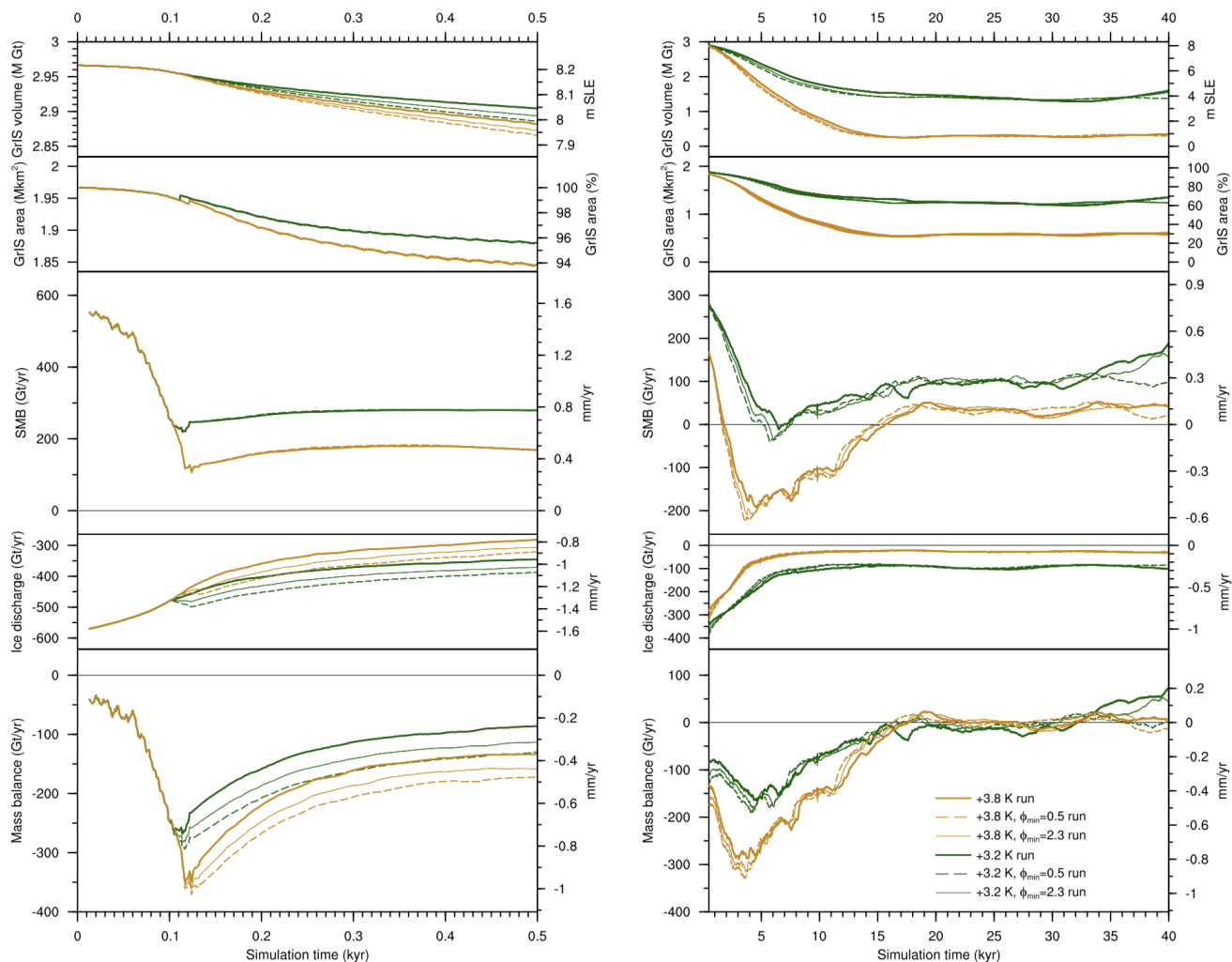


Figure A2. Timeseries of GrIS volume, area, Surface Mass Balance, ice discharge and mass balance for selected sensitivity simulations with increased ice discharge through reduced minimum friction angle in pseudo-plastic sliding law (solid thick line: $\phi_{\min}=5$, solid thin line: $\phi_{\min}=2.3$, dashed line: $\phi_{\min}=0.5$). On the left, values between in the first 500 years are shown. On the right, we show values between 500 and 40,000 years.

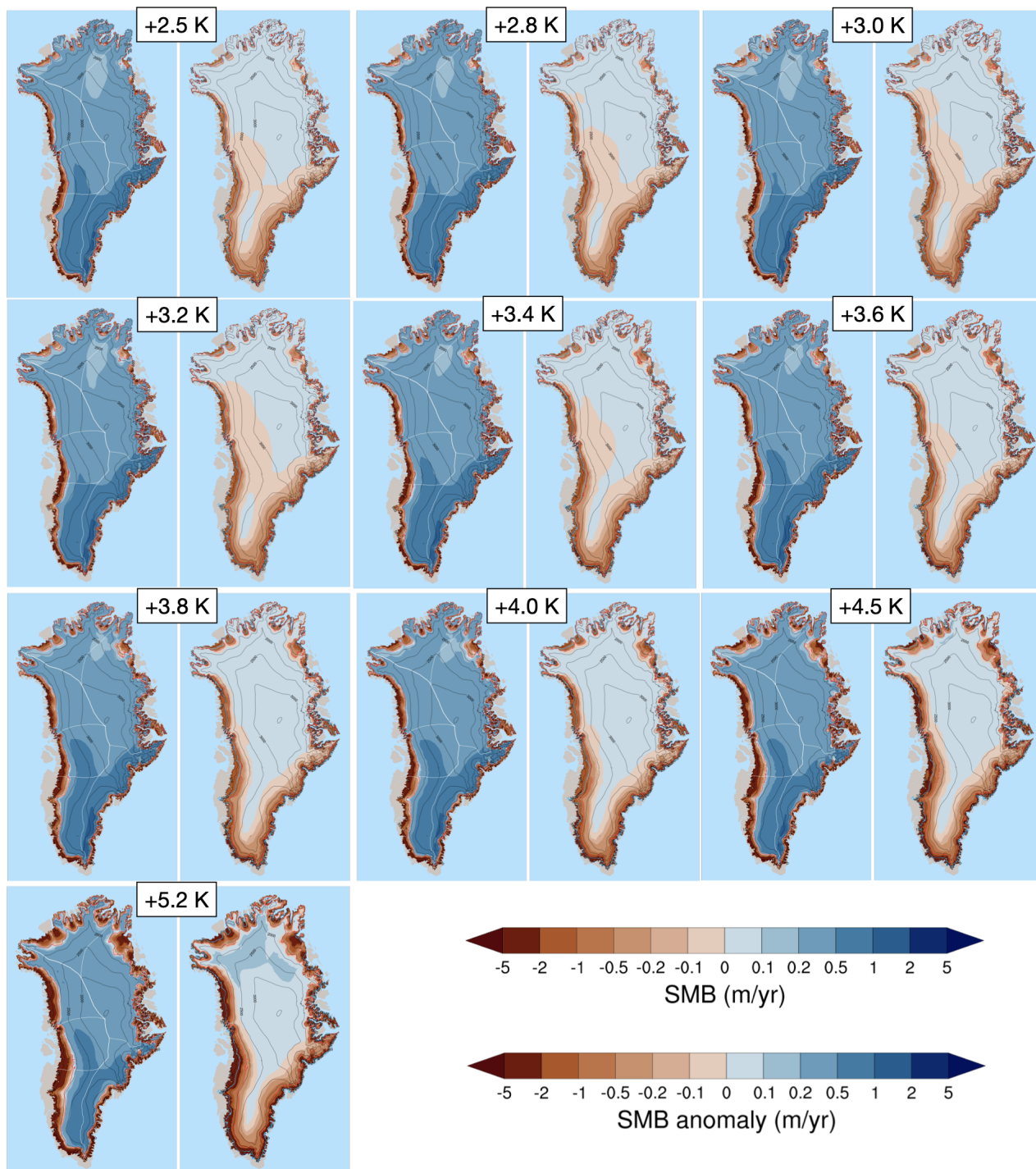


Figure A3. Average SMB forcing for each simulation (left: absolute values, right: anomaly to pre-industrial SMB simulated with CESM2/CISM2, Lofverstrom et al. (2020)).

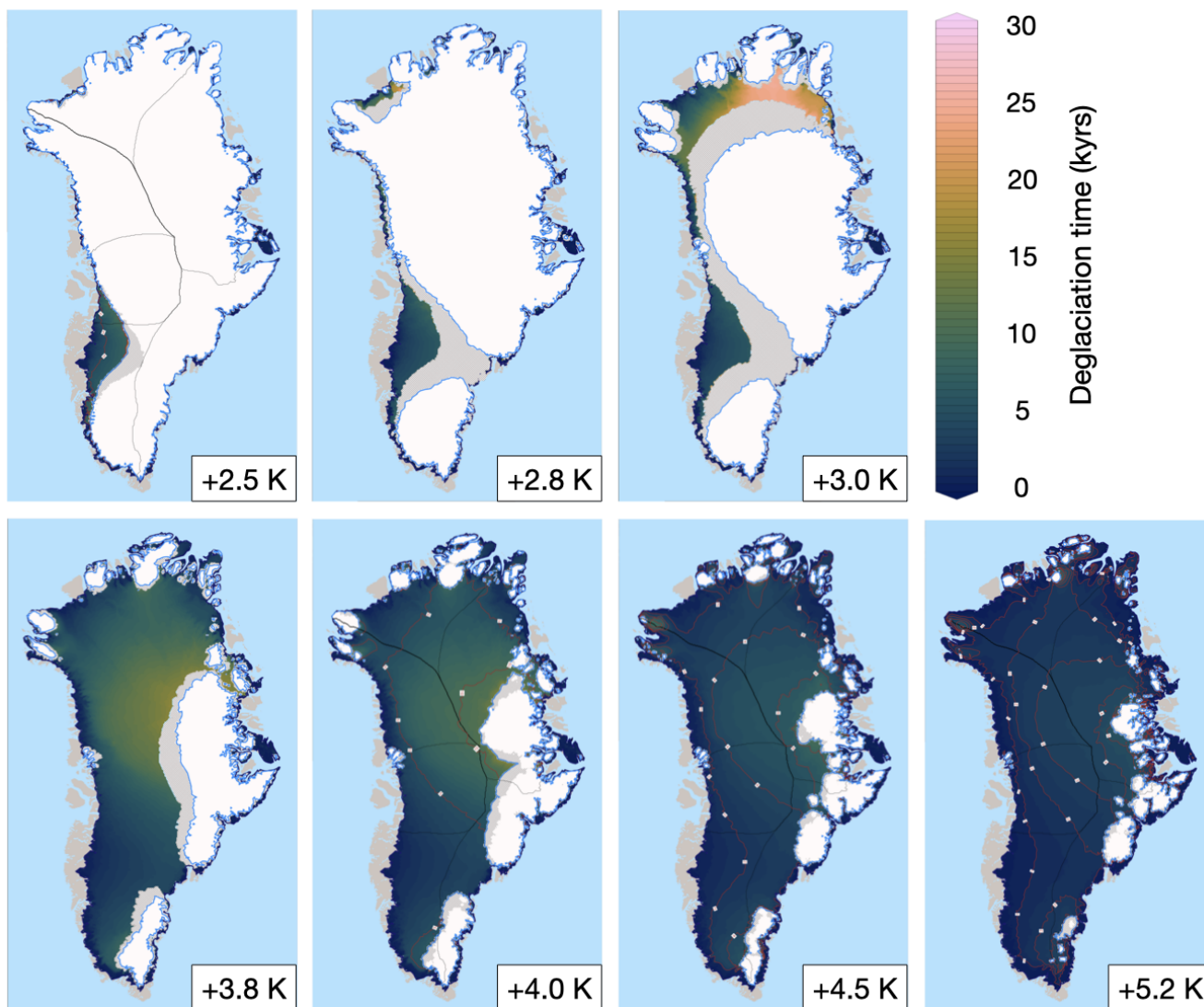


Figure A4. Map of GrIS retreat time for the simulations not shown in Fig. 4. Ice-sheet areas showing GIA-induced margin oscillations are shown in grey, whereas areas continuously ice-covered throughout each run are filled in white.

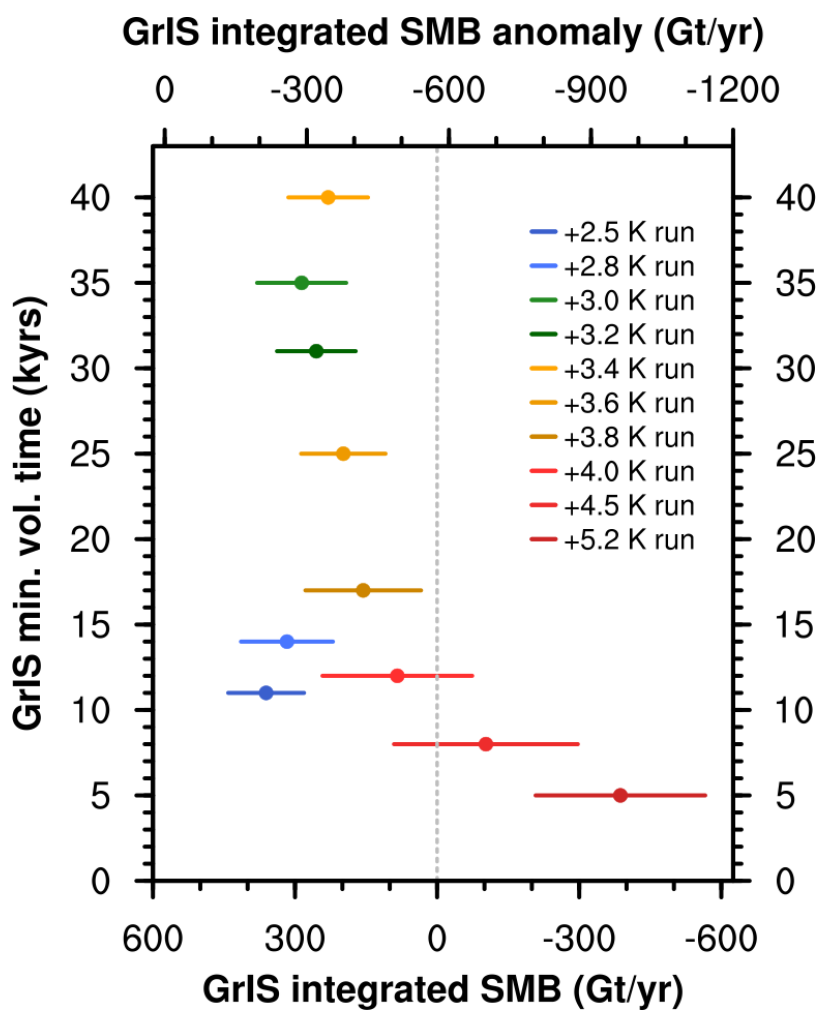


Figure A5. Scatter plot of GrIS integrated SMB forcing (avg±stddev, x-axis) vs time needed to reach minimum GrIS volume in our simulations (y-axis) in each simulation.

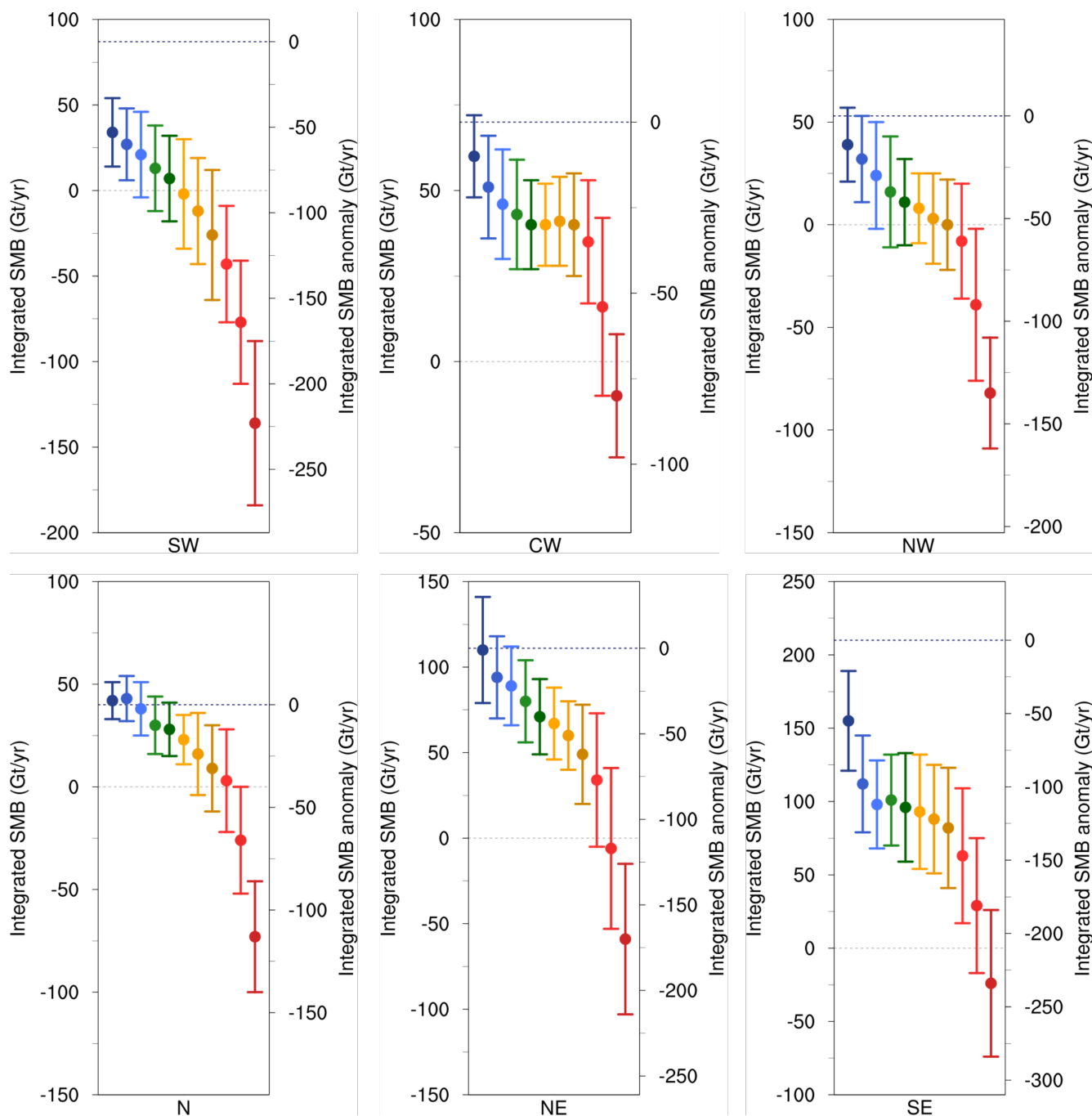


Figure A6. Forcing Surface Mass Balance (avg±stddev) in each run integrated over each IMBIE basin, following the basin definition as in “Rignot, E., & Mouginot, J. (2012). Ice flow in Greenland for the international polar year 2008–2009. *Geophysical Research Letters*, 39(11).”



Parameter	Short description	Value
F_g	Constant geothermal heat flux	0.05 W/m ²
ϕ_{\max}	Maximum friction angle in pseudo-plastic sliding law, for $B \geq B_{\max}$	40°
ϕ_{\min}	Minimum friction angle in pseudo-plastic sliding law, for $B \leq B_{\max}$	5°
B_{\max}	Bed elevation above which $\phi = \phi_{\max}$	700 m
B_{\min}	Bed elevation below which $\phi = \phi_{\min}$	-300 m
q	Exponent for pseudo-plastic sliding law	0.5
u_0	Threshold velocity for pseudo-plastic sliding law	100 m/yr
l_p	Lithosphere update period	100 yr
τ_r	Characteristic mantle relaxation time	3000 yr

Table A1. Model parameters used in the main CISM2 simulations presented in this study (note that in sensitivity tests with increased sliding we used a lower value for the minimum friction angle in pseudo-plastic sliding law.)



Simulations	Forcing years	SMB (avg \pm stddv)	Δ SMB
+2.5 K	74-96	361 \pm 80 Gt/yr	-274 Gt/yr
+2.8 K	81-103	317 \pm 97 Gt/yr	-305 Gt/yr
+3.0 K	86-108	286 \pm 94 Gt/yr	-336 Gt/yr
+3.2 K	90-112	255 \pm 83 Gt/yr	-361 Gt/yr
+3.4 K	95-117	230 \pm 84 Gt/yr	-392 Gt/yr
+3.6 K	99-101	198 \pm 89 Gt/yr	-435 Gt/yr
+3.8 K	103-125	156 \pm 122 Gt/yr	-435 Gt/yr
+4.0 K	107-129	84 \pm 158 Gt/yr	-507 Gt/yr
+4.5 K	116-138	-103 \pm 194 Gt/yr	-695 Gt/yr
+5.2 K	131-150	-387 \pm 179 Gt/yr	-978 Gt/yr

Table A2. Values from each of the 23 years-long intervals in the fully coupled BG-1pct run used to force our simulations (transient global mean anomaly to pre-industrial, initial and final forcing years, GrIS integrated SMB, GrIS integrated SMB anomaly to pre-industrial).