

31 1. INTRODUCTION

32 Massive ice sheets or mountain glaciers respond to various climatic forcings that operate on wide geographic
33 scales from local to global. Winter precipitation and summer air temperature are generally considered the most critical
34 factors in controlling glacial mass balance and extent. Understanding the impact of climate on past glacial cycles
35 necessitates a thorough understanding of the timing and amplitude of glacial dynamics. The most recent planet-wide
36 glacial expansion occurred during the global Last Glacial maximum (gLGM) as a result of changes in major climate
37 forcings, e.g., reduced summer insolation, lower tropical sea surface temperatures, and low atmospheric CO₂ content.
38 The remnants of paleoglacial deposits of gLGM are the best preserved among all the ice ages. The gLGM has been
39 extensively studied to ascertain the late Pleistocene changes in ice volume, sea-level fluctuations, feedback on climate,
40 etc. The timing of gLGM has been established using both the marine (e.g., Shackleton, 1967; Shackleton, 2000;
41 Thompson et al., 2003; Skinner and Shackleton, 2005) and terrestrial (e.g., An et al., 1991; Wang et al., 2001; Jouzel
42 et al., 2007; Clark et al., 2009; Fletcher et al., 2010;) paleoclimatic proxies. Based on proxy records, the timing of
43 gLGM is constrained between 26.5 and 19 ka, during which the ice sheets and mountain glaciers reached their
44 maximum and the global sea level was at its minimum (Clark et al., 2009).

45 The timing and extent of the maximum glaciation in many regions worldwide are poorly understood because
46 distinct ice masses respond differently to local and regional climatic conditions. New geochronological techniques
47 such as in situ cosmogenic surface exposure dating (e.g., Hughes et al., 2013; Heyman, 2014) permit reliable temporal
48 comparisons between the maximum advances of different mountain glaciers.

49 Evidence from mid-latitude glaciers reveals more complex behavior than that of synchronized ‘global’
50 glaciations. In some parts of Asia, for example, the largest glacial extent occurred before Marine Isotope Stage (MIS)
51 2, >100 ka in the northeastern Tibetan plateau (Heyman et al., 2011a) and late MIS 5/MIS 4 in the Kanas lake, Chinese
52 Altai (Gribenski et al. 2018). In the Tian Shan (Koppes et al., 2008; Li et al., 2014; Blomdin et al., 2016), Altai
53 (Blomdin et al., 2018), Khangai (Rother et al., 2014; Smith et al., 2016; Batbaatar et al., 2018; Pötsch, 2017), and
54 Eastern Sayan, Khovsgol (Gillespie et al., 2008; Batbaatar and Gillespie, 2016) mountains, the largest glaciers dated
55 back to MIS 3, while the MIS 2 glaciers appeared to be smaller (Fig. 1). It is noteworthy that most of the MIS 3
56 advances are based on a few and/or widely scattered ages of moraine boulders (Blomdin et al., 2016; Gribenski et al.,
57 2018). On the other hand, in the Gichgeniyn range with arid climate conditions, the significant cirque glacier advanced
58 during MIS 1 (Batbaatar et al., 2018). These studies suggest that glaciers in continental interior Asia respond to
59 regional-scale climate fluctuation in different ways; hence, the last glacial maxima differed from place to place.
60 Equilibrium Line Altitude (ELA) depression of MIS 2 maximum varied ~100 to 1100 m from the arid to humid
61 continental environments. ELA depression estimated 800-1100 m in sub-humid regions (Russian Altai, Khangai,
62 Eastern Sayan, SE Tibetan plateau), 500-600 m in semi-arid Gobi Altai mountains, and 100-600 m in the arid northern
63 Tibetan plateau and Tian Shan (Batbaatar, 2018; see the locations in Fig. 1).

64 In addition to regional climate conditions, non-climatic factors may also control the local extent and dynamics
65 of glaciation. Topographic factors such as catchment morphology, valley width and length, slope, and aspect, can
66 influence glacier dynamics and affect the style of glaciation (Kirkbride and Winkler, 2012; Barr and Lovell, 2014).
67 Glacier mass balance varies with slope aspect, snow avalanche, and wind drifting snow. The north-south aspect

68 contrast in mid-latitude regions with steeper slopes, and higher relief can generate substantial differences in insolation
69 and melt. This difference may be more significant for cirque, small mountain glaciers, or niche glaciers than large
70 valley glaciers or ice caps (Evans and Cox, 2005).

71 Although spatio-temporal variations in the glacial extent in response to regional climate change have been
72 mentioned in numerous studies, the influence of topoclimatic factors has not been adequately explored. The present
73 study aims to evaluate how topographic shading affects fluctuations in the glacier surface mass balance and consequent
74 changes in glacier thickness and length (advance and retreat) using 2D ice surface model. The spatial and temporal
75 responses of contrastively oriented paleo glaciers to the aspect-driven microclimate are of particular interest to us. We
76 evaluated the response of two mountain glaciers, the south-facing Ikh Artsan glacier and the north facing Jargalant
77 glacier in southwest Mongolia (Jargalant; Fig. 1), to topo-climatic factors. Reliable temporal comparisons between
78 the maximum advances of the two mountain glaciers were made using in situ cosmogenic surface exposure dating
79 (e.g., Heyman, 2014; Hughes et al., 2013). This research will improve our understanding of how mid-latitude glaciers
80 respond to topographic changes.

81

82 2. STUDY AREA

83 2.1 General settings of the study area.

84 The Gobi-Altai range, a ~800 km long NW-SE trending isolated arc of mountains, is bordered in the northwest by the
85 Mongolian Altai range and separated from the Khangai range by Valley of Lakes (Gobi Lakes Valley). Ikh Bogd
86 massif (Ikh Bogd means ‘great saint’ or ‘great sacred mountain’ in Mongolian) is located in the central Gobi-Altai
87 range. Ikh Bogd, Gobi-Altai range is one of the key sites for paleoglaciological, paleoenvironmental research in
88 landlocked arid, semi-arid central Asia.

89 This massif is over 50 km long, 25 km wide, and rises ~2 km above the surrounding arid piedmont. Terguun
90 Bogd (3957 m asl), the massif's highest peak, is also the highest point in the Gobi-Altai range (Fig. 1b). Ikh Bogd's
91 current stress regime is dominated by a network of thrust faults and sinistral strike-slip faults, that combine to form
92 transpressional pop-up structures (Cunningham et al., 1996; Bayasgalan et al., 1999; Vassallo et al., 2007; Vassallo
93 et al., 2011). The highest part (>3000 m) of the flat summit plateau consists mainly of granite, while lower parts are
94 mostly occupied by gneiss (EIC, 1981; Jolivet et al., 2007; Vassallo et al., 2011).

95 The flat summit plateau is thought to be a remnant of a formerly extensive Mesozoic erosion surface (Berkey
96 and Morris, 1924; Devyatkin, 1974; Jolivet et al., 2007), surviving most of the Cenozoic due to its rapid and recent
97 uplift after long-term quiescence (Jolivet et al., 2007). Accordingly, erosion in Ikh Bogd is limited to several deep
98 gorges. The summit plateau is well-preserved in unincised areas because of the young age of the massif and arid
99 regional climate (Vassallo et al., 2011).

100 Headwater systems of intermittent streams merge and turn into main streams, which later flow out of the
101 mountain front and transport abundant sediments into large alluvial fans. Alluvial fans from adjacent valleys coalesce
102 (forming bajadas) and stretch to huge endorheic intermontane basins like the Gobi Lakes Valley (Fig. 2). Numerous
103 prior investigations suggest that the summit plateau of the Ikh Bogd massif lacks Quaternary glacial landforms (e.g.,
104 Jolivet et al., 2007; Vassallo et al., 2011). However, some well-preserved moraine ridges have been identified and
105 mapped in some cirques of the neighboring massifs including Ikh Artsan, Jargalant (Batbaatar et al., 2018).

106
107

108 2.2 Climate

109 Ikh Bogd massif is in the cold Gobi Desert, with high amplitude in diurnal and annual temperatures. The
110 climate of the study area is characterized by a dry, cold winter with limited snowfall and hot summer with more than
111 65% yearly precipitation coming in summer (Batbaatar et al., 2018). Bayankhongor (Fig. 2), the nearest aimag center
112 to the study area (the largest unit of Mongolian province), is 140 km away and receives 190 mm of precipitation per
113 year (2005-2019 average, NAMHEM, 2020), while it drops to 100 mm (Yu et al., 2017, Fig. 2b, 2c, and 2d) near Orog
114 lake (1168 m a.s.l, Zhang et al., 2022). The closest weather stations to Ikh Bogd are Bayangobi (1540 m a.s.l) in the
115 south and Bogd (1240 m a.s.l) in the north. The long-term mean annual temperature measured as 3.2 °C in Bayangobi
116 and 4.4 °C in Bogd (Fig. 2c and 2d). The average January temperature was approximately -18 °C in both stations
117 (NAMHEM, 2020).

118 Ikh Bogd experiences long winter, a lower mean annual temperature ($-10\text{ }^{\circ}\text{C}$), and higher precipitation (200
119 mm) than its surrounding regions (Fig. 2a, 2b). Even in summer, the temperature is mostly below $0\text{ }^{\circ}\text{C}$ at altitudes
120 above 3800 m a.s.l in Ikh Bogd (Long-term monthly temperatures are calculated using a dry lapse rate of $9.8\text{ }^{\circ}\text{C}/\text{km}$
121 from nearby Bayangobi weather station; Supplementary 1). It begins to snow in the nearby Gobi Lakes Valley around
122 the end of September, although it melts quickly. Nonetheless, due to the relatively cold temperature, a thin snow cover
123 persists on the summit plateau of Ikh Bogd between the end of September and the middle of April. Occasionally,
124 precipitation in the form of snow occurs during the summer (Landsat imagery, Farr et al., 2007). Compared to the cool
125 summer of Ikh Bogd, surrounding areas have warm summers. The July temperature rises to about $21.8\text{ }^{\circ}\text{C}$ in
126 Bayangobi and $23.0\text{ }^{\circ}\text{C}$ in Bogd. (Fig. 2d; NAMHEM, 2020).

127 Strong Siberian high pressure prohibits the entrance of westerlies during winter, while westerlies and
128 southwesterlies are still effective during summer in the study area. The orientation and shape of mobile dunes
129 northwest of Orog lake record the direction of prevailing winds from the northwest (Yu et al., 2019; Mischke et al.,
130 2020; NAMHEM, 2020). Much colder than present-day winters and summers in Mongolia are consistent with the
131 strengthening of the winter high pressure over northern Eurasia. LGM summers were 1 to $7\text{ }^{\circ}\text{C}$ colder than today in
132 Mongolia. The southward shift of westerly storm tracks should, therefore, contribute to the lower than present
133 precipitation values (Tarasov et al., 1999). Multi-proxy records indicate that the local LGM climate if the study area
134 was very dry and harsh (Yu et al., 2019).

135 3. METHODOLOGY

136 3.1. Field investigation and geomorphologic mapping

137 We conducted the fieldwork around the Mongolian Altai in July 2018. Prior to fieldwork, we identified glacial
 138 erosional and depositional landforms from the ALOS PALSAR DEM with 12.5 m resolution (JAXA/METI, 2007)
 139 and oblique imageries of © ArcGIS Earth and © Google Earth. Only two categories of glacial landforms could be
 140 identified and mapped from the satellite imageries and DEM analysis, the glacial cirques and hummocky moraines.
 141 Glacial cirques, with amphitheater-like glacial erosional landforms, were easily recognized around the highest
 142 mountain areas. Identification of hummocky moraine has been made from the previous studies (Batbaatar et al., 2018)
 143 and oblique imageries of © ArcGIS Earth and © Google Earth imagery, since the DEM is of insufficient resolution to
 144 show the hummocky topography clearly. The mapping was performed in a GIS environment and mapped on 30 m
 145 Shuttle Radar Topographic Mission (SRTM), satellite imagery of © Bing Maps and © ArcGIS Earth. Pre-identified
 146 moraines were confirmed during fieldwork. They were then categorized based on their stratigraphic position and
 147 separation between moraine ridges. The naming of landforms (e.g., valleys) in the research area was based on locality
 148 names from a 1:100000-scale topographic map of Mongolia (ALAMGCM, 1970) and a conversation with local
 149 herders.

150

151 3.2. Equilibrium Line Altitude

152 Ikh Bogd massif is unglaciated today. Furthermore, the nearest modern glaciers to the study area are in Otgontenger
 153 (Khangai) and Sutai (Mongolian Altai), which are approximately 350 to 550 km north and west of the Ikh Bogd massif,
 154 respectively. Thus, we could not calculate present ELAs or ELA depression; hence only ELAs for former glaciers (Ikh
 155 Artsan and Jargalant paleoglaciers) were estimated.

156 The THAR method may include a large error when glacier geometry is complex (Benn and Lehmkuhl 2000).
 157 Yet, it is more suitable for our study area because it has simple glacier morphology. A relatively lower value of THAR
 158 (Meierding 1982) is commonly used in previous studies of mid-latitude glaciers; however, a higher value is applicable
 159 according to glacier type or location. We also used a higher THAR ratio of 0.58 because the Ikh Bogd massif must
 160 have a higher ratio due to its arid environment during the last glaciation (Gillespie et al. 2008; Felauer et al., 2012;
 161 Lehmkuhl et al., 2018).

$$162 \text{ELA} = A_t + 0.58(A_h - A_t) \quad (1)$$

163 where A_h and A_t are the headwall and toe altitudes, respectively.

164 A major problem exists in defining the headwall limit of a former glacier, which is very subjective and
 165 arbitrary (Porter 2001). The glacial headwall altitude was considered to be 1/3 of the altitude difference between the
 166 cirque floor and the top of the rock cliff, which was a similar ratio for schrund-lines estimation in White Mountains,
 167 New Hampshire, USA (Goldthwait, 1970). Headwall altitude is extracted from ALOS PALSAR DEM with 12.5 m
 168 resolution (JAXA/METI, 2007). The altimetric error (vertical uncertainty) of the DEM is ~5-7 m (Chai et al., 2022,
 169 Ferreira and Cabral, 2022). Glacial toe altitude was measured in the field using GPS and confirmed with the altitude
 170 from the DEM.

171

172 3.3. Cosmogenic ^{10}Be surface exposure dating

173 We used cosmogenic ^{10}Be surface exposure dating based on the specific sampling procedure described below to
174 determine the timing of the last glacial advances in Ikh Bogd massif (Gosse and Phillips, 2001; Khandsuren et al.,
175 2019). We sampled quartz-rich granitic boulders on the moraine crests, which were not reworked and represented
176 single, distinguishable ice-marginal positions. We sampled boulders that are rooted in the upper flat surface of the
177 moraine crest and away from steep slopes to avoid post-depositional movement such as rolling and sliding downslope.
178 We excluded boulders smaller than 50 cm above ground level that are likely to have been buried, exhumed, or heavily
179 eroded. Samples were obtained by chisel and hammer from the top surfaces of boulders (less than 5 cm thick) to avoid
180 the edging effect. We sampled at least five boulders from each single moraine crest to statistically screen any outliers
181 such as inheritance or post-glaciation reworking.

182 We followed the laboratory works of Korea University Geochronology Laboratory (Seong et al., 2016), with
183 the revised procedure of Kohl and Nishiizumi (1992). Rock samples were crushed and sieved to obtain a
184 monomineralic quartz and avoid grain size dependency. Meteoric ^{10}Be and other contaminations were removed by
185 successive HF/HNO₃ leaching. Purified quartz grains (250~500 μm) were first spiked with ~1047.8 ppm concentrated
186 ^9Be carrier and then dissolved with HF/HNO₃. Fluorides were removed by perchloric (HClO₄) acid, while Be was
187 separated from other ions (cations/anions) using ion-exchange chromatography columns. Beryllium hydroxide was
188 recovered using ammonium hydroxides. Consequently, Be(OH)₂ gels were dried on high-temperature hotplates. They
189 were calcinated to be oxide forms in a furnace at higher temperatures (800 °C). BeO samples were mixed with
190 Niobium powder to get conductivity and targeted in aluminum target to be loaded into 6 MV tandem Accelerator Mass
191 Spectrometry (AMS) for $^{10}\text{Be}/^9\text{Be}$ ratio measurement in the Korea Institute of Science and Technology. $^{10}\text{Be}/^9\text{Be}$ ratios
192 for each sample were measured relative to the 07KNSTD standard sample 5-1 (Nishiizumi et al., 2007), having a
193 $^{10}\text{Be}/^9\text{Be}$ ratio of $2.71 \times 10^{-11} \pm 4.71 \times 10^{-13}$ (calibrated error). The measured average ^{10}Be to ^9Be ratio of the processing
194 blank was $4.53 \times 10^{-15} \pm 1.6 \times 10^{-15}$ (n=2). The exposure ages were calculated using Cronus-Earth online calculator v3
195 (Balco et al., 2008). ^{10}Be production rate scaling was based on the time-dependent and nuclide-specific LSDn scaling
196 (Lifton et al., 2014). Several studies on the last glacial history in continental central Asia (e.g. Rother et al., 2014,
197 Batbaatar et al., 2018) present ^{10}Be exposure ages referenced to other scaling methods. For a simple comparison, we
198 recalculated their exposure ages with LSDn scaling model. Errors of exposure ages were represented by external
199 uncertainty (1 σ confidence level).

200 We tested the boulder populations to find outliers using the Chauvenet and Pierce criterion and normalized
201 deviation methods (Ross, 2003; Chauvenet, 1960, Batbaatar et al., 2018) before we assigned deglaciation ages of
202 moraine sequences. The idea behind using Chauvenet's criterion is to find a probability band centered on the mean of
203 a normal distribution containing all samples. Any data points that lie outside this probability band can be considered
204 to be outliers. In contrast, Peirce's criterion is based on Gaussian distribution, and the data point is rejected if its
205 deviation from the mean exceeds the maximum allowed deviation (calculated from the standard deviation of the group
206 and Peirce's criterion table). For the normalized deviation, a sample in groups was rejected if its normalized deviation
207 from the group mean (excluding the tested sample) was greater than two (Batbaatar et al., 2018). The sample was
208 excluded from the group if its exposure age was recognized as an outlier in any of these three methods. We also

209 calculated the reduced chi-square value and the relative uncertainty of the group (Balco, 2011) after rejecting outliers.
210 The arithmetic mean and group standard deviation were considered as a representation of the group age. However, we
211 also calculated the total uncertainty, including group standard deviation and external uncertainty (systematic
212 uncertainty) of each sample within the group (Batbaatar et al., 2018). We presented minimum exposure ages assuming
213 zero erosion because it has been negligible (at least for the sampled surface) since the boulders were deposited based
214 on field observations and considering almost negligible erosion in arid regions. We also performed boulder erosion
215 sensitivity tests on our exposure ages, using erosion rates of 1-4 mm kyr⁻¹ (Blomdin et al., 2018). We omitted
216 corrections for snow cover and vegetation change due to the ephemeral winter snow cover at the elevations of the
217 sampled boulders (e.g., Gosse and Phillips, 2001) because modern winter snow cover (Oct-Apr) is very thin and no
218 tree cover exists due to aridity.

219 After rejecting the outliers, Welch's t-test statistics were also used to compare the exposure ages of distal
220 moraines of two groups (M_{IA1} and M_{JI}). Welch's t-test assumes that the sample means being compared for two groups
221 are normally distributed and that the groups have unequal variances. The null hypothesis (H_0) states the means of the
222 two groups are same, while the alternative hypothesis (H_a) states that the means of two groups are unequal. We also
223 performed the t-test with the total uncertainty of the groups instead of group variances at a 0.05 significance level.

224 Since our study area is considered to be a well-preserved paleo peneplanation surface, the ¹⁰Be concentration
225 of the flat summit plateau must be very high. If our sampled boulders have an "inherited" component from the summit
226 plateau, the apparent exposure age should significantly exceed the moraine deposition age. We assumed that the ¹⁰Be
227 concentration from extremely old boulders could represent the concentration of the summit plateau itself. Hence, we
228 tried to calculate exposure age and the lowest erosion rate of the summit plateau using the highest measured ¹⁰Be
229 concentration from the oldest moraine boulder. Therefore, we selected the highest point (3625 m, 44.6°N, 100.2°E)
230 between the Jargalant and Ikh Artsan cirques that is representative of the summit plateau. The minimum erosion rate
231 was calculated with the "Erosion rate calculator" of Cronus Earth V3.0.2 using elevation and geographical coordinate
232 of the selected point, sampling thickness, and ¹⁰Be concentration of the oldest boulder, considering the shielding factor
233 as 1 (unshielded).

234
235

236 **3.4. The 2D ice surface modelling**

237

238 A 2D ice surface model covering 22-16 ka was used to examine the influence of aspect on glacier mass
239 balance and dynamics and to explain the empirical dating results. The model calculates glacier mass balance variation
240 and corresponding vertical changes in the glacial ice surface (3.4.1). Furthermore, it defines the glacier toe location
241 (3.4.2) relative to the changing ELA via ice thickening or thinning. Our simulation cannot model actual glaciers; rather,
242 it examines the possibility that variable melt rates could cause a significant difference in mass balance (Fig. 3).

243

244 **3.4.1 Glacial surface mass balance model: glacial thinning and thickening.**

245 Glacier mass balance (m) is determined by the summation of net ablation (a , see 3.4.1.1) and accumulation (c , see
246 3.4.1.2) over a stated period (t):

$$247 \quad m = a + c = \int_{t_1}^{t_2} (a + c) dt \quad (2)$$

248 To infer the net gain and loss of glacier mass along the longitudinal profile for both catchments, we calculated and
249 plotted the variations in June, July, August (JJA; see 3.4.1.1) melt and winter precipitation (i.e., snow through the
250 whole year; see 3.4.1.2) during 22-16 ka ago. The elevation of the profile was taken from DEM with 12.5 m spatial
251 resolution in 5 m spatial intervals. Site parameters and input parameters of this model are described in Tables 1 and 2.
252

253 **3.4.1.1 Glacier ablation: Temperature-index glacier melt model**

254 We assumed that the topography (aspect and slope) is the main factor producing a difference in daily incoming solar
255 radiation on the south- and north-facing slopes. The earth's surface receives more energy as the solar altitude angle (α)
256 is high (zenith angle and angle of incidence are low). The diurnal changes in solar altitude angle are caused by the
257 earth's rotation around its axis, which varies from morning to evening. At sunrise and sunset, the solar altitude angle
258 is 0 degrees, and it reaches its maximum value at noon. Accordingly, in the mountainous area of the northern
259 hemisphere, the south-facing slope receives the highest energy at noon. The north-facing slope, on the other hand,
260 receives little or no energy due to the topographic shading effect (Fig. 2e). Such a diurnal cycle of insolation would
261 result in a major variation in the yearly or long-term mass balance of mountain glaciers (by surface melt) flowing on
262 south- and north-facing slopes on a long-term scale.

263 **Calculating orbital parameters**

264 Combined influence caused by the slow changes in axial tilt (obliquity), shape of the Earth's orbit
265 (eccentricity), and axial precession results in long-term cyclical changes in daily incoming solar radiation. First, we
266 computed long-term variations in orbital parameters such as obliquity, eccentricity, and longitude of the perihelion
267 (Berger and Loutre, 1991). These main orbital elements cause the long-term variation of solar declination (δ) that
268 produce seasonal variation in solar altitude at the given latitude. Then, the long-term variation of solar declination was
269 used to calculate the hour angle (ω), zenith angle (Z), and angle of incidence (θ) (Eq. 3-11). We calculated all values
270 above related to the orbital parameters in time-dependent manner (Fig. 3).

271 **Calculating hour angle**

272 To define aspect-driven contrast in potential direct solar radiation between south-facing and north-facing
273 valleys, we calculated hourly insolation (Eq. 12) with the same input parameters, except for the topography (aspect
274 and slope; Fig. 3). We calculated cell-by-cell sunrise and sunset hour angles of given topography for each valley (Eqs.
275 3-9) and gave 15° of increment for every one hour to calculate the hourly insolation, starting from the sunrise hour
276 angle until it exceeds the sunset hour angle.
277

278 Sunrise and sunset hour angles on the inclined surface were calculated as a function of latitude, solar declination,
279 slope, and azimuth (Iqbal, 1963). Sunrise hour angle for horizontal surface:

$$280 \quad \omega_s = \cos^{-1} (-\tan\phi \tan\delta) \quad (3)$$

282

283 The following equations give the sunrise and sunset hour angles on the surface oriented toward the east.

284
$$\omega_{sr} = \min \left[\omega_s, \cos^{-1} \left(\frac{-xy - \sqrt{x^2 - y^2 + 1}}{x^2 + 1} \right) \right] \quad (4)$$

285

286
$$\omega_{ss} = -\min \left[\omega_s, \cos^{-1} \left(\frac{-xy + \sqrt{x^2 - y^2 + 1}}{x^2 + 1} \right) \right] \quad (5)$$

287

288 The following equations give the sunrise and sunset hour angles on the surface oriented toward the west.

289
$$\omega_{sr} = \min \left[\omega_s, \cos^{-1} \left(\frac{-xy + \sqrt{x^2 - y^2 + 1}}{x^2 + 1} \right) \right] \quad (6)$$

290
$$\omega_{ss} = -\min \left[\omega_s, \cos^{-1} \left(\frac{-xy - \sqrt{x^2 - y^2 + 1}}{x^2 + 1} \right) \right] \quad (7)$$

291

292 where x and y are kinds of coefficient to make the equations above simpler (Eq. 1.6.7 of Iqbal, 1983).

293
$$x = \frac{\cos \phi}{\sin \gamma \tan \beta} + \frac{\sin \beta}{\tan \gamma} \quad (4)$$

294

295
$$y = \tan \delta \left(\frac{\sin \phi}{\sin \gamma \tan \beta} - \frac{\cos \phi}{\tan \gamma} \right) \quad (5)$$

296

297 Equations 3-9 are for calculating hour angles in arbitrary surfaces, where ω_s is the sunrise hour angle for horizontal
 298 surfaces, ω_{sr} , ω_{ss} is the sunrise and the sunset hour angles on the inclined surface, ϕ is the latitude, δ is the solar
 299 declination angle, β is the slope inclination angle, and γ is the surface azimuth angle.

300

301 **Calculating zenith angle and angle of incidence**

302 Then, the local zenith angle (Z) and the angle of incidence (θ) were calculated using hour angles at one-hour
 303 intervals (ω). The zenith angle is angle between sun rays and normal plane to the surface ($90^\circ - \alpha$) and approximated
 304 as a function of latitude, solar declination angle, and hour angle (Iqbal, 1983):

305

306
$$Z = \sin \delta \sin \phi + \cos \delta \cos \phi \cos \omega \quad (10)$$

307

308 and the angle of incidence on the arbitrary oriented surfaces is expressed as:

309

310
$$\cos \theta = (\sin \phi \cos \beta - \cos \phi \sin \beta \cos \gamma) \sin \delta + (\cos \phi \cos \beta + \sin \phi \sin \beta \cos \gamma) \cos \delta \cos \omega + \cos \delta \sin \beta \sin \gamma \sin \omega \quad (11)$$

311

312 where β is the slope inclination angle and γ is the surface azimuth angle.

313

314 **Calculating daily insolation and daily melt**

315 Hourly potential clear-sky direct solar radiation (I) was calculated as (Hock, 1999):

$$316 \quad I = I_0 \left(\frac{R_m}{R} \right)^2 \Psi_a \left(\frac{P}{P_0 \cos Z} \right) \cos \theta \quad (12)$$

317 where I_0 is solar constant (1368 W m^{-2}), $(R_m/R)^2$ is the eccentricity correction factor of the Earth's orbit for the time
 318 considered with R the instantaneous Sun-Earth distance, and R_m is the mean Sun-Earth distance, Ψ_a is the mean
 319 atmospheric clear-sky transmissivity ($\Psi_a=0.75$: (Hock, 1998)), P_h is the atmospheric pressure (NOAA, 1976), P_0 is
 320 the mean atmospheric pressure at sea level, Z is the local zenith angle, and θ is the angle of incidence between the
 321 normal to the grid slope and the solar beam. Therefore, hourly insolation was summed into daily insolation for
 322 corresponding day length (not for 24 hours; Fig. 3).

323

324 We calculated daily melt with following equation using daily insolation value (Eq. 12).

325

$$326 \quad a = \begin{cases} \left(\frac{1}{n} MF + a_{ice} I \right) T & : T > 0 \\ 0 & : T \leq 0 \end{cases} \quad (13)$$

327 MF is a melt factor ($\text{mm d}^{-1} \text{ } ^\circ\text{C}^{-1}$), a_{ice} is a radiation coefficient for ice surfaces, I is potential clear-sky direct solar
 328 radiation at the ice surface (W m^{-2}), and T is the time-dependent monthly mean temperature ($^\circ\text{C}$). Furthermore, we
 329 integrated (summed) the daily melt into monthly and summer melt, which is the same with the total ablation in this
 330 model (Fig. 3).

331

332 **Calculating time-dependent temperature.**

333

We calculated the time-dependent temperature of the study area in the following order:

334

335

336

337

1) Present-day monthly air temperatures (T) for both cirque headwall altitudes (3533.3 m in Jargalant, 3508.3 m in
 Ikh Artsan) were calculated from the two nearest national weather stations using a summer adiabatic lapse rate of $8 \text{ } ^\circ\text{C}$
 km^{-1} (Batbaatar et al., 2018). Bayangobi weather station (1540 m a.s.l.) is 27 km SE of the study region, and Bogd
 (Horiult) weather station (1240 m a.s.l.) is 45 km NW (Fig. 2c).

338

339

340

341

342

343

2) We use only summer temperature because even today, monthly mean temperatures between August to May are less
 than $0 \text{ } ^\circ\text{C}$, in which no melt occurs (NAMHEM, 2020). The long-term average of the extreme minimum temperature
 at the mean glacial toe altitude (Ikh Artsan and Jargalant) is $-5.2 \text{ } ^\circ\text{C}$ (calculated from Bayankhongor 1874 m) a.s.l
 using a lapse rate of $8 \text{ } ^\circ\text{C}/\text{km}$. The JJA mean temperature at the cirque headwall altitude was measured as $5.4 \text{ } ^\circ\text{C}$ in
 the Ikh Artsan valley and $3.5 \text{ } ^\circ\text{C}$ in the Jargalant valley. We chose the value of $5.4 \text{ } ^\circ\text{C}$ for the summer temperature of
 the study area and used further calculations (see supplementary 1 file).

344

345

346

347

348

3) We obtained a time-dependent summer temperature since 22 ka. LGM summer temperature was easily calculated
 by subtracting known LGM summer temperature anomaly ($1\text{--}7 \text{ } ^\circ\text{C}$ by Tarasov et al., 1999) from the present-day
 temperature of the study area. The modern and LGM summer temperature of the study area ($5.4 \text{ } ^\circ\text{C}$) was calibrated to
 Greenland temperature data from the NGRIP ice core (Buizert et al., 2018) since 22 ka to obtain time-dependent
 temperature variation (see supplementary 2 file).

349

350

4) LGM summer temperature anomalies ranging from $-5.0 \text{ } ^\circ\text{C}$ to $-6 \text{ } ^\circ\text{C}$ were applied to calculate glacial melt since 22
 ka (see supplementary 2 file).

351
352 **3.4.1.2 Glacier accumulation and snow data**
353 Climatologies at high resolution for the Earth's land surface areas (CHELSA) provides a high resolution, downscaled
354 centennial climate model data since 20 ka. We used CHELSA-TraCE21k 1 km monthly precipitation time series
355 (Karger et al., 2017). Precipitation data between 22–20 ka was considered the same as 20 ka data. Only snowfall at
356 the mean altitude of each valley was considered glacial accumulation, which occurs when the monthly average
357 temperature is below 0 °C.

358
359 **3.4.2 Glacial advance and retreat model based on glacier thickness change**
360 Finally, a simple 2D ice surface model reconstructed paleoglacier behavior for 22–16 ka in the study area. First, we
361 created small initial glacial surface profiles on both valleys using the 2D ice surface model developed by Benn and
362 Hulton (2010). We computed the ice surface elevation (ice thickness) along the profiles in both valleys with this model.
363 The model requires (1) assumed yield stress describing a glacier's basal shear stress and (2) a shape factor accounting
364 for the valley-drag effects. We plot the ice profile with 5 m spacing along the mid-line of each valley (Fig. 8d, e),
365 assuming constant basal shear stress of 50, 100, 150, 200, and 300 kPa. Shape factors were calculated perpendicular
366 to the profile with the same spacing with the profile. Subsequently, we calculated the glacier mass balance for 22–16
367 ka using our temperature-index melt model results and paleo snow accumulation data. Therefore, we applied
368 corresponding paleo mass balance values on the initial ice thickness profiles. Ikh Artsan and Jargalant glaciers are
369 mostly developed within a cirque. The maximum erosion related to the rotational movement beneath a cirque is closely
370 linked to the ELA for cirque glaciers (Dahl et al., 2003). Hence, in our model, the thickest ice surface related to the
371 maximum erosion was considered as ELA. Accordingly, variations in paleo ELAs were calculated regarding the ice
372 thickness change. Eventually, we used the simple quadratic function formula ($f(x)=ax^2 + bx + c$) to determine the
373 location of the glacial toe based on ELA and headwall altitude values (Benn and Hulton, 2010). With the glacial toe
374 location, we could evaluate the paleoglacier advance and retreat at any time of interest.

375

376 4. RESULTS

377

378 4.1 Field observation and moraine stratigraphy

379 In Ikh Bogd, late Quaternary glaciation is almost confined within the cirque, extensive valley glacier
380 networks were absent. Glaciers in Ikh Artsan and Jargalant valleys were also restricted in the cirques and flowed
381 shortly down to elevations of ~3000 m a.s.l. Jargalant valley merges to the largest valley on the northern flank called
382 Bituut river valley (Fig. 1b). This large drainage only experienced glaciations in the form of short cirque-valley
383 glaciers, like in Jargalant valley. The massif was limited to small single (no networking) cirque-valley glaciers is best
384 explained by the arid climate of the interior of the Gobi Desert.

385 Ikh Artsan cirque is smaller and its glacial valley is shorter (~1 km) than Jargalant. The best-preserved
386 moraines, with at least seven to eight morainal crests, occur in the Ikh Artsan cirque (Fig. 4; Fig. 6a; Batbaatar et al.,
387 2018). The farthest moraine sequence (M_{IA1}) was distinguished by down-valley stratigraphic position and long flat
388 ridge along the valley side (Fig. 4a). M_{IA1} moraine is composed of thick, unsorted glacial debris of different particle
389 sizes (from silt to boulder) with huge granitic boulders at the top. Towards the left, the moraine is cut by an intermittent
390 stream, forming a deep valley (Fig. 4).

391 The Jargalant paleoglacier has a larger accumulation area and length than Ikh Artsan glacier, advancing 1.5
392 km downvalley. The moraine stratigraphy of Jargalant hummocky moraine was quite complicated. The original
393 moraine surface of the inner moraines has been dissected by longitudinal stream forming the parallel moraine mounds
394 or elongated moraine ridges along the valley. In the field, we matched such uneroded surfaces (or ridges) with the
395 similar elevation and assumed them as an individual sequence. Stratigraphically, we identified four different moraine
396 sequences in the Jargalant complex (M_{J4} , M_{J3} , M_{J2} , and M_{J1} , from youngest to oldest; Figs. 5 and 6). M_{J4} , M_{J3} , and M_{J2}
397 moraines are distinctively separated on the left side of the valley. Elongated moraine feature (M_{J3} , M_{J2}) at the right
398 side of the valley looks like a single flow feature. However, we assumed that the original form of the moraine
399 (separation) had been removed or reworked by the stream erosion (Fig. 6c). According to these matters, some moraine
400 boundaries are still uncertain, hence we marked the boundary with dashed line (Fig. 5 and Fig. 6b, c). M_{J4} moraine
401 lies between 3365–3410 m a.s.l, containing angular to sub-angular clast-supported pebble to boulders. Downvalley
402 from the M_{J4} moraine, M_{J3} and M_{J2} moraines have been longitudinally dissected by stream channels and uneroded
403 moraine surface forms elongated parallel moraine ridges with smooth matrix-supported flat tops and steep clast-
404 supported sides. These streams are filled with the till and angular water-lain sediments. The oldest moraine (M_{J1}) was
405 deposited further downvalley, consisting of a single moraine ridge with large granitic boulders lying on the finer
406 matrix-supported deposit. We mapped the extent of the most distal moraine ridge from the lower end of M_{J2} moraine
407 to the point where the slope changes abruptly. We speculate that this oldest moraine may have extended far enough to
408 reach the Bituut valley; however, beyond this point, the moraine would have been reworked by post glacial processes
409 and lateral erosion of Bituut river (Fig. 5 and Fig. 6b, c).

410

411 4.2. Late Pleistocene ELA reconstruction

412 LGM ELA was calculated for M_{IA1} and M_{J1} moraines (Table 3). We estimated the former ELA using a headwall
 413 altitude of 3508–3532 m. The terminal moraine was also identified at an elevation of 3222 m a.s.l in the Ikh Artsan
 414 valley. Accordingly, the ELA for the M_{IA1} moraine was 3388 m a.s.l. In contrast, a large terminal moraine was
 415 deposited at 2998 m a.s.l in Jargalant valley. The ELA associated with M_{J1} moraine was 3308 m a.s.l., about 80 m
 416 lower than M_{IA1} moraine.

417

418 **4.3. ^{10}Be surface exposure age dating**

419 We present 28 new ^{10}Be exposure ages obtained from the boulders associated with five different moraine sequences,
 420 M_{IA1} in Ikh Artsan valley and M_{J1} , M_{J2} , M_{J3} , and M_{J4} in Jargalant (Table 4; Fig. 6).

421 **Ikh Artsan valley:** seven granitic boulders (IAM001 to 007) sampled from the most distal moraine ridge ranged in
 422 age between 21.2 ± 1.5 to 19.1 ± 1.3 ka. ^{10}Be exposure ages from this moraine sequence were well-clustered, and none
 423 of the three methods (Chauvenet, Pierce, and standardized deviation) detected outliers. The moraine formation age
 424 was found to be 20.1 ± 0.7 ka (20.1 ± 1.6 ka with total uncertainty), $R\chi^2$ was 0.29, and group relative uncertainty was
 425 calculated as 4% (Fig. 7).

426 **Jargalant valley:** twenty-one granitic moraine boulders on the four moraine sequences were targeted. Five to seven
 427 boulders from each moraine crest were sampled. Outliers were detected and rejected by Pierce and normalized
 428 deviation criteria. Because, the results from Pierce and normalized deviation methods were consistent, however,
 429 Chauvenet method could not recognize some outliers which were recognized by Pierce and normalized deviation
 430 criteria. Exposure ages from the innermost M_{J4} moraine ranged from 636.2 ± 45.1 to 177.3 ± 11.3 ka. The oldest
 431 age (JAM003, 636.2 ± 45.1 ka) was excluded, and the four remaining ^{10}Be exposure ages provided a mean age of
 432 212.9 ± 45.9 ka (212.9 ± 47.9 ka with total uncertainty). Five boulders from the M_{J3} moraine ranged in age between
 433 209.0 ± 26.1 to 35.9 ± 8.0 ka. The group mean age was calculated as 69.9 ± 39.4 ka (69.9 ± 41.5 ka with total
 434 uncertainty) after rejecting an outlier of 209.0 ± 26.1 ka (JAM008). Boulders from the M_{J2} moraine yielded ages from
 435 284.9 ± 18.4 to 162.1 ± 10.2 ka with a mean exposure age of 193.7 ± 36.7 ka (193.7 ± 41.1 ka with total uncertainty)
 436 after rejecting the oldest age of 284.9 ± 18.4 ka (JAM012). Samples from the distal moraine of Jargalant valley (M_{J1})
 437 ranged in age from 18.9 ± 1.7 to 10.6 ± 0.8 ka. The arithmetic mean age for this moraine sequence was 17.2 ± 1.5 ka
 438 (17.2 ± 2.1 ka with total uncertainty) without the youngest age of 10.8 ± 0.5 ka (JAM016). The group was relatively
 439 well clustered, and its relative uncertainty was 9% and $R\chi^2 = 1.18$ (Fig. 7). For erosion rates of 1-4 mm kyr⁻¹, an
 440 exposure age of 10 ka calculated assuming zero erosion would underestimate the true age by 1-4% and an age of 20
 441 ka by 2-7%. Samples with longer exposures (boulders with inheritance) older than 100 ka, were increasingly sensitive
 442 to erosion; i.e., JAM10 (123.8 ka) had an impact, increasing ages with 12-125% for 1-4 mm kyr⁻¹ and JAM03 (636.2
 443 ka) was saturated even for 1 mm kyr⁻¹ boulder erosion rate.

444 Our age dating results from most distal moraines of Ikh Artsan (20.1 ± 1.6 ka) and Jargalant (17.2 ± 2.1)
 445 coincide within the narrow range (19.2-18.5 ka) as we apply total uncertainties to the group mean. However, T-test
 446 reveals ($T=3.928$, $P=0.001$) that the exposure ages from the distal moraine of Ikh Artsan presented a statistically
 447 significant difference from that of the Jargalant based on standard deviations (variance) of the two groups. Likewise,

448 the exposure ages of the two groups were different in 0.05 significance level ($T=2.665$, $P=0.044$) using total
449 uncertainties instead of the variance.

450 Boulders from inner moraines (M_{J4} , M_{J3} , and M_{J2}) presented older (~636.2–35.9 ka) exposure than the timing
451 of the maximum extent unlike morphostratigraphy-the inner moraines should be younger than the distal moraine (M_{J1}).
452 The unexpected, significant inheritance has been widely recognized around the globe in the previous studies (Ciner et
453 al., 2017; more references therein), possibly overestimating the real deposition age of moraine. We interpret that the
454 unexpected older exposure ages (~636.2–35.9 ka) from M_{J4} , M_{J3} , and M_{J2} moraines of Jargalant valley strongly imply
455 the inheritance from the summit plateau. These unusually old boulders are pieces of the summit plateau that were
456 transported onto the glacier surface by rockfall, which seems to happen in recent times as well. For temperate glacier,
457 rock fracturing occurs not only on the headwall above the glacier, but also within the bergschrund (bottom of the
458 headwall) by ice segregation. This kind of undermining (sapping) process or/and glacial debutressing would drive
459 consequent upper headwall collapse and give a large amount of rock supply to the glacier (Sanders et al., 2012; Table
460 4; Fig. 6b). ^{10}Be concentration of the oldest sample (JAM003 with ^{10}Be concentration of $\sim 262.9 \times 10^5$) likely represents
461 nuclide concentration at the surface of the summit plateau. The production rate for the summit plateau (60.49 atoms
462 $\text{g}^{-1} \text{yr}^{-1}$) must be higher than the moraine samples (38.45 atoms $\text{g}^{-1} \text{yr}^{-1}$) due to its higher elevation (3625 m) than
463 sampling sites and 100% exposure (topographic shielding is 1) to cosmic-ray bombardment. With a high ^{10}Be
464 concentration of JAM003 and production rate of summit plateau (3625 m a.s.l), the assuming exposure age of the flat
465 summit plateau was calculated as 442.3 ± 29.8 ka, and the corresponding erosion rate was calculated as 1.23 ± 0.10
466 mm kyr^{-1} .

467 **4.4. Results from 2D ice surface modelling**

468 We ran the potential direct solar radiation model applying to a 12.5 m resolution DEM for a more realistic
469 comparison. The model suggests that the aspect largely affects the incoming potential clear-sky solar radiation. The
470 result approved that the south-facing slopes in mountainous regions receive more solar radiation than the north-facing
471 slope in our study area. At solar noon, the sun is always directly south in the northern hemisphere; hence southern
472 slopes of the mountainous area receive their maximum insolation. However, the orientations of the two valleys are
473 not true north or south. The azimuth of the Ikh Artsan is 247° (SSW), and for the Jargalant it is 40° (NNE). According
474 to the exact orientation, the peak of the daily insolation contrast between two valleys is calculated between 3 to 4 pm,
475 not at noon. The current June solstice incoming daily solar radiation in Ikh Artsan valley was 8527.34 WH m⁻² and
476 7714.35 WH m⁻² in Jargalant valley, whereas solar radiation was lower during 22 ka, 8460.07 WH m⁻² in Ikh Artsan
477 and 7604.54 WH m⁻² in Jargalant. Although both valleys received maximum insolation in the first to the middle half
478 of June, the maximum difference in incoming daily solar radiation occurred at the end of August. The main difference
479 in the daily incoming solar radiation ranges from 10–24% on summer days over the period of 22–16 ka. The spatial
480 distribution of potential direct solar radiation of the study area is given in Fig. 8. Typically, the total daily insolation
481 anomaly of summer solstice in 20 ka from present-day and integrated total daily insolation for 22–16 ka were described
482 on the 12.5 m grid cells (Fig. 8d, e). In the same way, 14% excess of total summer insolation was observed on the
483 southern slope during the modelling time interval of 22–16 ka (Fig. 8f; see supplementary 2 file).

484 For simplicity, the melt was calculated (Eq. 12) along specific profiles of Ikh Artsan and Jargalant valleys
485 (Fig. 8e, f). In accordance with the incoming solar radiation contrast, melt rates on south-facing slopes exceed those
486 on north-facing slopes, as would be expected. If modern glaciers existed in Ikh Bogd, the present-day summer melt
487 would be calculated as 4.0 m in Ikh Artsan valley and 3.7 m in Jargalant, respectively. This was a substantially high
488 melt rate in the arid, cool climate of the study area. The temperature-index melt model discovered that 5% of melt
489 excess in June solstice of any year between 22–16 ka was observed on the south-facing slope. Approximately 8% of
490 the difference in summer melt in any year was observed for 22–16 ka (Fig. 8f, see supplementary 2 file)

491 We run our 2D ice surface model for many times using different values of basal shear stress, LGM summer
492 temperature anomalies, and site temperature (Supplementary material 2). The cirque and valley dimensions reflect the
493 glacier size (including thickness), and the intensity of former glacial erosion (Barr and Spagnolo, 2015). The normal
494 stress acting on the glacier bed is mainly a result of the weight (thickness) of a glacier. Jargalant glacier is 2.7 times
495 larger in area than Ikh Artsan and twice as long in glacier length, forming a large, deep, and well-developed cirque.
496 According to the glacial valley size, we chose the higher basal shear stress for Jargalant valley (200 kPa) and the
497 smaller value for Ikh Artsan valley (100 kPa). LGM summer temperature anomalies ranging from -6 °C to -5 °C with
498 0.1 °C intervals were applied the same for both glaciers. Some previous studies suggest that temperature is lower on
499 the north-facing slopes at the same altitude. On the north-facing slope of Taibai, Qinling mountains, JJA monthly
500 mean temperature is measured 0.5–1 °C lower than on the south-facing slope in the altitude range of 1250–3750 m
501 (Tang and Fang, 2006). Therefore, we applied two different temperature values for north-facing Jargalant glacier; 1)
502 using the same present-day temperature with Ikh Artsan valley; and 2) using the lower present-day temperature for
503 Jargalant valley than Ikh Artsan.

504 **Case 1.** Applying the same present-day temperature: When we use the same present-day temperature and the
505 same LGM anomaly of $-5.5\text{ }^{\circ}\text{C}$, the modelled chronology of the maximum extents (20.2 ka) of two glaciers were
506 similar and consistent with the Ikh Artsan terminal moraine age dating result (20.1 ka). According to this model (case),
507 Jargalant moraine advanced maximally 20.1 ka and probably reached to Bituut valley.

508 **Case 2.** Applying the different present-day temperatures: For the Jargalant glacier, we applied lower present-
509 day temperature by $-1\text{ }^{\circ}\text{C}$ to $-0\text{ }^{\circ}\text{C}$ (at $0.1\text{ }^{\circ}\text{C}$ interval) than Ikh Artsan. The run yielded different chronologies of
510 maximum ice expansions. Only a small temperature change between the south- and north-facing slope forced two
511 glaciers to behave asynchronously, the north-facing glacier got have 2.70–3.46 kyr of lag in the timing of the maximum
512 extent. When we applied $-5.5\text{ }^{\circ}\text{C}$ of LGM summer temperature anomaly and present-day summer temperature in
513 Jargalant $0.5\text{ }^{\circ}\text{C}$ lower than in Ikh Artsan, Ikh Artsan glacier reached its maximum extent near 20.2 ka. In contrast,
514 the Jargalant glacier maximally advanced approximately at 17.1 ka. This result perfectly fits our ^{10}Be moraine age
515 dating results (20.1 ka and 17.2 ka).

516 5. DISCUSSION

517

518 5.1. Asynchronous glaciation in mid-latitude ranges

519 Recent glacial chronologies from mid-latitude mountain ranges in North Atlantic region document that Laurentide,
520 Scandinavian ice sheets and number of valley glaciers behaved synchronously, advancing to their maximum extent at
521 roughly the same time as the gLGM (26.5–19 ka). However, some experienced pre-LGM glacial maxima, while others
522 stagnated, re-advanced, continuously advanced even farther during the subsequent Heinrich Stadial 1 (HS-1, 17.5-
523 14.5 ka), displaying both inter-range and intra-range asynchrony (Laabs et al., 2009; Young et al., 2011; Licciardi and
524 Pierce 2018; Palacio et al., 2020).

525 In Europe, large-scale inter-range asynchrony (several tens of kyr) of last glacial termination was common.
526 Cosmogenic surface dating from the Alps and Turkey provides nearly synchronous last glacial maxima with the gLGM
527 (26.5–19 ka, MIS 2). Whereas other numerical dating techniques, including radiocarbon, U-series, and OSL, indicate
528 earlier local glacial maxima (80–30 ka, MIS 4 to MIS 3) in the Cantabrian Mountains, Pyrenees, Italian Apennines
529 and Pindus Mountains (e.g., Jimenez-Sanchez et al., 2013; Oliva et al., 2019). Another inter-range asynchrony was
530 observed in mountain glaciers of North America. They reached their maximum extent from as old as 25–24 ka for
531 some moraines and outwash in the Sierra Nevada to as young as 17–15 ka for some terminal moraines in the Rocky
532 Mountains but a clear central tendency exists with a mean of ~19.5 ka (Young et al., 2011; Laabs et al., 2020; Palacios
533 et al., 2020). Relatively younger ages (HS-1) across the mountains located in the higher latitude were interpreted as a
534 sign of glacial post-LGM culmination in response to increased delivery of westerly derived moisture which reached
535 the northern continental interior of the western U.S after the large ice sheets started to retreat (Licciardi et al., 2001;
536 Licciardi et al., 2004; Thackray, 2008). For instance, younger exposure ages of the last glacial maxima in the western
537 Uinta mountains, compared to mountain ranges farther east and north, reflected the influence of pluvial Lake
538 Bonneville after the recession of the Laurentide ice sheet to the north (Laabs et al., 2009).

539 Medium scale inter-range asynchrony (several thousand years) was observed in the Yellowstone plateau.
540 Terminal moraines dated to ~17 ka are common in valleys along the northeastern mountains (e.g., Eightmile, Chico,
541 Pine Creek, S.Fork Deep Creek, Cascade Canyon, and Gallatin) of the Great Yellowstone plateau. Glaciers in the
542 Teton Range (southwestern part of the plateau) have terminal moraine with the age of ~15 ka. Local LGM maxima
543 dated to ~19.8 to 18.2 ka in the western part of the plateau (Beartooth Uplift). Licciardi and Pierce (2018) suggested
544 that shifting orographic precipitation patterns due to the formation of ice dome and change in ice flow direction caused
545 asynchrony in the Great Yellowstone region.

546 Very few glacial chronologies, if any at all, record intra-range asynchrony during the most recent glacial
547 termination. Age dating results from some relatively well-studied mountain ranges (Wasatch, Uinta, Bighorn ranges
548 in North America) present intra-range asynchrony in glacial maxima in their various aspect (Laabs et al., 2020). Some
549 of them had LGM ages ranging from hundreds to thousands of years from valley to valley. In the Wasatch range,
550 terminal moraines dated to ~21.9 ka (Laabs and Munroe, 2016), ~20.8 ka, 17.3 ka (Laabs et al., 2011) in three western
551 valleys, 19.6 ka in the southwestern valley and 17.6 ka and 17.3 ka in the southeastern valleys (Quirk et al., 2020).
552 Similarly, the last glacial terminal moraine age difference of ~1 kyr was observed between the north-facing and south-

553 facing slope, Eastern Pyrenees (Delmas et al., 2011; Delmas et al., 2008). Even glaciers on the same oriented slope
554 contain some chronology difference. LGM moraine chronology from the three valleys on the east side of the central
555 Sawatch range varies from 22.3 ka to 19.9 ka (Young et al., 2011).

556 Nevertheless, we suggest that some internal, external, analytical uncertainties associated with sampling,
557 measurements, or/and statistical approach can cause the low magnitude of asynchrony in such small intra-range or
558 massif. Some studies have attributed intra-range asynchrony in terminal moraine ages to contrasting valley glacier
559 response times related to topography, ice dynamics and/or differences in glacier shape and hypsometry (Young et al.,
560 2011, Licciardi and Pierce, 2018). As mentioned above, large and medium-scale asynchrony in the mountain glaciers
561 across the North Atlantic region is mostly explained by precipitation distribution due to the relative location of the
562 moisture source area and atmospheric circulation contributed by topography. However, the intra-range or intra-massif
563 scale of asynchrony in the last glacial period needs further research to understand fully.

564

565

566 **5.2. Inter-range asynchrony in ice expansion of last glacial cycle across the western Mongolia**

567 Some ^{10}Be exposure ages of the glacial erratic from the mountain ranges nearby Ikh Bogd show the
568 significant glacial advances between LGM to the Holocene (Fig. 9). The largest ice extent was dated as ~22.0 ka on
569 the western flank of the Sutai (Batbaatar et al., 2018). On the other hand, the farthest ice expansion corresponds to
570 MIS 3 in the Khangai mountain range (Rother et al., 2014; Smith et al., 2016; Pötsch, 2017; Batbaatar et al., 2018).
571 In the Gichgeniyn mountains, Holocene (8–7 ka) glaciers advanced with a similar magnitude to their local LGM
572 position. Generally, two main glacial stages, LGM and post LGM (~17–16 ka), were observed within MIS 2 in
573 Mongolia (Rother et al., 2014; Batbaatar and Gillespie, 2016; Smith et al., 2016; Pötsch, 2017; Batbaatar et al., 2018).

574 Previous studies using granulometric, palynological, ostracod, and geochemical proxies from the Gobi Lakes
575 Valley reveal occurrence of cold and dry climates during the local LGM (19–18 ka) and Younger Dryas (Felauer et
576 al., 2012; Lee et al., 2013; Yu et al., 2017; Lehmkuhl et al., 2018; Yu et al., 2019; Mischke et al., 2020; Fig. 9). These
577 results are consistent with our exposure ages from two valleys. The warming trend was also present in the Gobi Lakes
578 Valley, where lakes once were desiccated during local LGM, and experienced water level increase after local LGM
579 (e.g., Yu et al., 2017; Mischke et al., 2020).

580

581

582 **5.3. Aspect effect on the asynchronous glacial dynamic in Ikh Bogd**

583 Our age dating result reveals that abrupt deglaciation occurred since ~20 ka in the Ikh Artsan glacier.
584 Exposure ages from the M_{J1} moraine (17 ka) should represent one of the following: glacier culmination, survival, or
585 temporary glacial stagnation of the LGM glacier, or glacier re-advance (Fig. 10). In either case, the culmination of the
586 Jargalant glacier near 17 ka implies a major difference in glacier mass balance between south- and north-facing
587 glaciers. Changes in glacier mass balance in small massif or mountain (intra-range) could show large spatial variation
588 due to local topography-induced factors, such as i) snow avalanching, ii) preferential deposition of wind-drifted snow
589 (Florentine et al., 2020), iii) solar radiation and iv) temperature.

- 590 i. Periodically occurring snow avalanches support glacial accumulation. Most avalanches have steep
591 slopes between 25° and 50° to slide down (Luckman, 1977). Ikh Artsan and Jargalant valleys are
592 connected to the flat summit plateau and are less steep than the threshold slope of 25°. The average slope
593 was measured as 23° for Jargalant and 18.2° for Ikh Artsan. Very wet snow lubricated with water can
594 cause an avalanche on a slope of only 10 to 25° (Luckman, 1977). However, it is not significantly
595 relevant to our study area because Ikh Bogd and its neighboring area experienced very cold and
596 conditions during MIS 2 (e.g., Yu et al., 2019).
- 597 ii. Wind-drifted snow accumulation occurs either with or without snowfall. Wind deflates the snow from
598 the windward slope and redistributes it into the leeward slope. However, the prevailing wind direction
599 of the study area is northwest to southeast, which is almost perpendicular to the orientations of the two
600 valleys. We assume the wind direction during MIS 2 was similar to the present with much strength.
601 Therefore, wind-drifted snow may not significantly affect glacier accumulation. For that reason, we used
602 the same precipitation value in both valleys.
- 603 iii. North-facing slopes in the northern hemisphere receive less solar radiation because of the aspect effect.
604 Ikh Bogd locates in a mid-latitude great sunlight climate; furthermore, it has steeper relief which can
605 enhance the aspect effect. (Evans and Cox, 2005). Topographic shading can also influence glacier
606 response and mass balance in mountainous areas (Olson and Rupper, 2019). As expected, our modelling
607 results demonstrate that the north-facing slope receives less summer insolation than the south-facing
608 slope, resulting in reduced glacial melt (5-10%) under the same temperature conditions.
- 609 iv. The vegetation, discontinuous permafrost, and modern and paleoglacier distribution and their magnitude
610 in semi-arid mid-latitude regions have contrasting temperatures and soil moisture on sunny and shady
611 slopes (Evans 2006; Barr and Spagnolo, 2015; Klinge et al., 2021). As a result of topographically induced
612 differences of solar radiation and evapotranspiration, forests (consisting of Siberian larch) and
613 discontinuous permafrost are limited to north-facing slopes, whereas mountain steppe covers south-
614 facing slopes in Mongolian forest-step zone (Klinge et al., 2021; Fig. 8b, c). Klinge et al. (2021)
615 determined that the annual incoming solar radiation, permafrost table depth, and soil moisture
616 (topographic wetness index) are significantly correlated. Aspect-driven solar radiation and temperature
617 contrast also give more glacier, lower (altitude) glacier, and larger glacier on the poleward slope (e.g.,
618 Evans 2006; Barr and Spagnolo, 2015). For instance, Sutai mountain (closest modern glacier to Ikh Bogd)
619 has large, well-developed valley glaciers that flow northward into low altitude from the ice dome. Still,
620 the glaciers at the south-facing slope end near the summit margin without developing into valley glaciers
621 (Fig. 8c). According to these facts, a small temperature difference is likely to be real and needs to be
622 considered. Our temperature index melt model revealed that applying lower temperature to the north-
623 facing glacier than to the south-facing glacier results in a large melt difference between the two valleys
624

625 Among the four topography-aspect induced factors, two are applicable on our study area; incoming solar radiation
626 and temperature difference in south- and north-facing slopes. Our temperature index melt model suggests that an

627 aspect-driven insolation change affects the amount of melt, however in a very small amount. This small reduction in
 628 the melt due to the shading effect could not cause a significant difference in glacial mass balance or long-term glacier
 629 stagnation or advance. Under the same temperature and different insolation, glaciers on the south- and north-facing
 630 slopes across small regions behave almost synchronously. Both Ikh Artsan and Jargalant glaciers culminated near 20.2
 631 ka and abruptly retreated to the cirque headwall. Also, their changes in glacial dynamic were almost the same (See
 632 supplementary 2 file). However, no glacier stagnation was observed in the Jargalant valley around 17 ka (i.e., this
 633 result does not match our exposure age dating). We sampled from possible most distal moraine from Jargalant valley
 634 to avoid sampling from reworked boulders in the steep slope. Likewise, we could not find any other evidence that the
 635 Jargalant glacier reached the trunk valley of the Bituut river. If we consider both glaciers moved synchronously, the
 636 most distal moraine must locate more downvalley from the ~17 ka culmination. In this case, the geological evidence
 637 (terminal moraine) near 20 ka must have been degraded by Bituut mainstream or/and reworked with the mass
 638 movement.

639 When we set the site temperature of Jargalant slightly colder (-0.1 to -1 °C) than in the Ikh Artsan, glaciers started
 640 to behave differently, i.e., they retreat from their distal location asynchronously. When we apply 0.5 °C colder
 641 temperature to Jargalant than Ikh Artsan, 2D ice surface modelling results are consistent with age dating results. The
 642 Ikh Artsan glacier abruptly retreated from its maximum extent near 20.2 ka (age dating result was 20.1 ka). In contrast,
 643 the Jargalant glacier advanced almost continuously until 17.8 ka and then began to retreat from its maximum extent
 644 by 17.1 ka (age dating result was 17.2 ka) with a brief stagnation around its maximum extent. This result suggests that
 645 the exposure age of ~17 ka corresponds to the most extensive glaciation in Jargalant valley. We also assume that the
 646 exposure age (17.2 ± 1.5 ka) of the distal moraine (M_{J1}) is the age for maximum extent for the Jargalant valley (Figs.
 647 6b and 6c) because this moraine was not like the small ridge left as a glacier stagnates during its retreat. The M_{J1}
 648 moraine was larger than the other moraine sequences, large enough to mark the maximum advance of the glacier.

649 Based on the age dating and 2D ice surface modelling, we propose that the glaciers on the north- and south-
 650 facing slopes of Ikh Bogd may have behaved asynchronously. Glacier volume and area changes are likely to be
 651 sensitive to temperature changes in semi-arid and arid regions, such as Ikh Bogd. The glaciers of Ikh Artsan and
 652 Jargalant behaved asynchronously due to aspect-induced temperature differences rather than differences in solar
 653 insolation.

654
 655

656 **5.4. Morphostratigraphic mismatch in exposure age dating from erratic boulders, Jargalant valley**

657 **5.4.1. Inheritance from the summit plateau**

658 The massif has a steep slope; in particular, the slope reaches 32–70° along cirque walls and incised valleys.
 659 Colluvial materials covering hillslopes and long boulder corridors were mainly the results of the active mass wasting
 660 process. Particularly, rockfall deposits forming scree and talus apron must be the product of steep slope failure of the
 661 summit plateau (Fig. 11). We expected that inner moraine crests would present Holocene or HS-1 exposure in light of
 662 morphostratigraphy. M_{J2} , M_{J3} , and M_{J4} moraine crests have exposure ages ranging from 636.2 to 35.9 ka (Table 4, Fig.
 663 6). According to moraine stratigraphy, exposure ages of inner moraines cannot be older than the age of the distal

664 moraine. The apparent ages show antiquity and scatter in its distribution, which cannot be a single geologic event;
665 associating the mean age with the specific timing of glacial termination is not appropriate (Heyman et al., 2011b). It
666 was more likely that the exposure ages from M_{J2} , M_{J3} , and M_{J4} moraines were due to the inherited ^{10}Be concentration
667 produced during prior exposure in the boulders recycled from the cirque wall or paleo summit plateau by rockfall or
668 toppling during glaciation and/or paraglacial period. During termination of the farthest moraine, glacier was long
669 enough to pluck the fresh rocks out along its bed. Also, thick glacier would not allow inherited rocks fall onto the
670 glacier ice (Fig. 12d). After glacier retreat to the cirque, glacier thinning allowed rockfalls with inheritance to the ice
671 surface. Increase of inherited boulders would be contributed by enhanced rock-slope failure (de-buttressing) right after
672 rapid deglaciation (Cossart et al., 2008 ; Ballantyne and Stone, 2012; Hashemi et al., 2022) and ice segregation along
673 the bergschrund. Boulders with inheritance transported to the glacier toe as supraglacial debris. Plucking out by the
674 shortened glacier was not efficient to supply fresh rocks relative to the rock supply with summit plateau inheritance
675 (Fig. 12e).

676

677

678 **5.4.2. Cenozoic evolution of the low-lying, high-elevated summit plateau**

679 The flat summit plateau of the Ikh Bogd massif is considered an uplifted paleo-peneplanation surface. The
680 basement structure of Ikh Bogd was formed by the collision of the WNW-ESE to ENE-WSW oriented amalgamated
681 terranes throughout the Precambrian and Paleozoic (Şengör et al., 1993). $^{40}\text{Ar}/^{39}\text{Ar}$ ages from extrusive volcanic on
682 the Ikh Bogd summit and apatite fission-track data show two significant uplifts that occurred in the Gobi-Altai range
683 and Ikh Bogd history (Jolivet et al., 2007; Vassallo et al., 2007). The first uplift related to early to mid-Jurassic, the
684 region experienced crustal shortening events greater than 2 km. Gobi-Altai has been observed elsewhere in central
685 Asia through this event that is possibly due to a collision between Mongol-Okhotsk and Siberia or the Lhasa and
686 Qiangtang block to the far south in Tibet (Traynor and Sladen, 1995; Dewey et al., 1988; Cunningham, 2010). The
687 present erosional surface of the summit plateau formed just after this Jurassic exhumation and was preserved under a
688 negligible erosion rate. Preservation of this flat summit plateau and its fission-track age indicate quiescence without
689 significant vertical crustal motions continued until the last uplift began (Jolivet et al., 2007; Vassallo et al., 2007;
690 Cunningham, 2010).

691 The Gobi-Altai range is one of the northernmost far-fields affected by the Cenozoic tectonic collision of India
692 into Asia, which initiated the late Cenozoic reactivation and present-day stress regime (Cunningham et al., 1996;
693 Vassallo et al., 2007). According to the apatite fission track data of Vassallo et al. (2007), the onset of the last and
694 ongoing uplift corresponds to the late Cenozoic, 5 ± 3 Ma. This tectonic reactivation is responsible for creating the
695 high topography (~ 4000 m a.s.l) seen today, in the response to which faster exhumation is initiated as well (Vassallo
696 et al., 2007).

697 The paleo-erosion surfaces at high altitudes experienced rapid uplift after a long time of quiescence with low
698 erosion. Cosmogenic nuclides-based denudation rates from global paleo-erosion surfaces in diverse climatic, tectonic,
699 and lithologic environments do not exceed ~ 20 m Myr^{-1} (Byun et al., 2015). We obtained erosion rate for flat summit
700 plateau using production rate at summit plateau and ^{10}Be concentrations of reworked boulders from M_{J4} , M_{J3} , and M_{J2}

701 moraines. Calculated bedrock erosion rate for last ~600 ka for summit plateau ranged from 1.23 ± 0.10 mm kyr⁻¹ to
702 25.8 ± 5.75 m Myr⁻¹. The erosion rate of 25.8 ± 5.75 m Myr⁻¹ was thought to be a maximum value because erosion
703 probably increases with the increasing elevation of the uplifting massif. This result was harmonious with the long-
704 term (since the last uplift) exhumation rate of 23.6 ± 3 m Ma⁻¹ (Vassallo et al., 2011) and Holocene erosion rate of 28
705 m Myr⁻¹ (Jolivet et al., 2007) for the massif. Whereas flatness and the lowest erosion rate of 1.23 ± 0.10 mm Myr⁻¹
706 reveal negligible erosion and notable preservation of paleo-surface for several hundred thousand years. If this erosion
707 rate reflects an average rate that can be applied to the entire flat surface and has been maintained for the total uplift
708 period of the massif (Vassallo et al., 2007), it would account for only the 2 to 7.6 m of erosion.

709 6. CONCLUSIONS

710 Central Asian valley glaciers, including Ikh Bogd massif, expanded and shrank, presenting more complex behavior
711 relative to large ice sheets in the northern hemisphere. Regional climate and local non-climatic factors have been
712 playing an essential role in this complexity. Our ^{10}Be dating documents that glacier culmination in Ikh Artsan valley
713 on the southern slope occurred at 20.1 ka (M_{IA1}), generally falling within the gLGM, whereas large terminal moraine
714 formed around 17.2 ka (M_{J1}) in the Jargalant valley on the northern slope.

715 Asynchrony in glacier expansion has been reported from some of areas in the globe but has not been clearly
716 studied with a combination of geochronologic and numerical modeling approaches. Due to aspect-driven solar
717 insolation change, paleoglacier in the north-facing Jargalant valley melted slower (5-10%) than the glacier in Ikh
718 Artsan valley. However, this amount of melt difference could not produce glacier advance or stagnation for a long
719 period. Asynchronous glaciation was observed across the study area if the LGM summer temperature in Jargalant
720 valley was considered colder than Ikh Artsan and age dating result and modelling result were consistent when we
721 apply 0.5 °C lower temperature to Jargalant to than in Ikh Artsan. According to the lower temperature case, Jargalant
722 glacier retreated from the most extensive position 3000 years later than Ikh Artsan glacier. In the other words, our
723 modelling reveals that the temperature difference driven by aspect on both slopes significantly affects the glaciers to
724 survive longer than when the aspect-driven insolation only affects the glacier melt.

725 The glacial retreat began soon after the peak of local glacial maximum on both valleys and left several
726 sequences of inner moraines in their heads (cirques). Inner moraine at the south-facing cirque dated to ~ 13.5 ka
727 (Batbaatar et al., 2018), however on the north-facing cirque, transported boulders show a significantly old exposure
728 age (636.2 to 35.9 ka) for inner moraines (M_{J2} - M_{J4}). The summit plateau of the Ikh Bogd massif is one of the oldest
729 known tectonically uplifted surfaces on Earth. It is more likely that extremely old exposure ages are the result of
730 inheritance recycled from rock falls from the paleo-erosional surface of the summit plateau.

731 *Data availability.* The data that supports the findings of this study are available within the article [and its
732 supplementary material]

733

734 *Author contributions.* YBS planned the study and proceeded a field investigation with JSO, PK, KS, and CHL. YBS
735 designed a funding acquisition. JSO designed ^{10}Be lab experiments with RHH and BYY. CHL and MKS developed
736 a matlab code of the 2D ice surface modelling and performed the simulation. PK and YBS prepared the manuscript
737 with contributions from all co-authors.

738

739 *Competing interests.* The contact author has declared that neither they nor their co-authors have any competing
740 interests.

741

742 *Disclaimer.* Publisher's note: Copernicus Publications remains neutral with regard to jurisdictional claims in
743 published maps and institutional affiliations.

744

745 *Acknowledgments.* This work was supported by the Ministry of Education of the Republic of Korea and the National
746 Research Foundation of Korea (NRF-2018S1A5A2A01031348 for Y.B.S). We thank Dr. Dash for his sincere and
747 productive comments on the earlier version of the manuscript.

748

749 **REFERENCES**

- 750 ©JAXA/METI., 2007. ALOS PALSAR L1.0 High-resolution terrain corrected dataset. Accessed through ASF DAAC,
751 <https://asf.alaska.edu>, 25 June 2009. <https://doi.org/10.5067/J4JVCFDDPEW1>
- 752 ALAMGCM.: Topographic map of Mongolia, Geodesy and Cartography division of Agency for Land Administration
753 and Management, Geodesy and Cartography of Mongolia, Ulaanbaatar, Mongolia, 1970.
- 754 An, Z., Kukla, G., Porter, S.C., Xiao, J.: Late Quaternary dust flow on the Chinese loess plateau, *Catena*, 18(2), 125-
755 132, [https://doi.org/10.1016/0341-8162\(91\)90012-M](https://doi.org/10.1016/0341-8162(91)90012-M), 1991.
- 756 Balco, G: Contributions and unrealized potential contributions of cosmogenic nuclide exposure dating to glacier
757 chronology, 1990–2010. *Quat. Sci. Rev.* 30, 3–27. <https://doi.org/10.1016/j.quascirev.2010.11.003>, 2011
- 758 Balco, G., Stone, J.O., Lifton, N.A., Dunai, T.J.: A complete and easily accessible means of calculating surface
759 exposure ages or erosion rates from ^{10}Be and ^{26}Al measurements, *Quat. Geochronol.*, 3(3), 174-195,
760 <https://doi.org/10.1016/j.quageo.2007.12.001>, 2008.
- 761 Ballantyne, C.K., Stone, J.O.: Timing and periodicity of paraglacial rock-slope failures in the Scottish Highlands,
762 *Geomorphology*, 186, 150-161, <https://doi.org/10.1016/j.geomorph.2012.12.030>, 2013.
- 763 Barr, I.D., Lovell, H.: A review of topographic controls on moraine distribution, *Geomorphology*, 226, 44-64,
764 <https://doi.org/10.1016/j.geomorph.2014.07.030>, 2014.
- 765 Barr, I. D., & Spagnolo, M.: Glacial cirques as palaeoenvironmental indicators: Their potential and limitations. *Earth-
766 Sci. Rev.* 151, 48-78, <https://doi.org/10.1016/j.earscirev.2015.10.004>, 2015
- 767
- 768 Batbaatar, J.: Quaternary Glaciation in Central Asia (Doctoral dissertation), 2018.
- 769 Batbaatar, J., Gillespie, A.R.: Outburst floods of the Maly Yenisei. Part II—new age constraints from Darhad basin,
770 *Int. Geol. Rev.*, 58(14), 1753-1779, <https://doi.org/10.1080/00206814.2016.1193452>, 2016.
- 771 Batbaatar, J., Gillespie, A.R., Fink, D., Matmon, A., Fujioka, T.: Asynchronous glaciations in arid continental climate,
772 *Quat. Sci. Rev.*, 182, 1-19, <https://doi.org/10.1016/j.quascirev.2017.12.001>, 2018.
- 773 Bayasgalan, A., Jackson, J., Ritz, J.F., Carretier, S.J.T.: Field examples of strike-slip fault terminations in Mongolia
774 and their tectonic significance. *Tectonics*, 18(3), 394-411, <https://doi.org/10.1029/1999TC900007>, 1999.
- 775 Benn, D. I., Hulton, N. R.: An Excel™ spreadsheet program for reconstructing the surface profile of former mountain
776 glaciers and ice caps, *Comput. Geosci*, v. 36, no. 5, p. 605-610, <https://doi.org/10.1016/j.cageo.2009.09.016>,
777 2010,
- 778 Benn, D.I., Lehmkuhl, F.: Mass balance and equilibrium-line altitudes of glaciers in high-mountain environments,
779 *Quat. Int.*, 65(Supplement C), 15-29, [https://doi.org/10.1016/S1040-6182\(99\)00034-8](https://doi.org/10.1016/S1040-6182(99)00034-8), 2000.
- 780 Berger, A., Loutre, M.-F.: Insolation values for the climate of the last 10 million years, *Quat. Sci. Rev.*, v. 10, no. 4,
781 p. 297-317, [https://doi.org/10.1016/0277-3791\(91\)90033-Q](https://doi.org/10.1016/0277-3791(91)90033-Q), 1991,
- 782 Berkey, C.P., Morris, F.K.: The peneplanes of Mongolia, *Am. Mus. Novit.*, 136, 1-11, 1924.
- 783 Blomdin, R., Stroeven, A.P., Harbor, J.M., Gribenski, N., Caffee, M.W., Heyman, J., Rogozhina, I., Ivanov, M.N.,
784 Petrakov, D.A., Walther, M.: Timing and dynamics of glaciation in the Ikh Türgen Mountains, Altai region,
785 High Asia, *Quat. Geochronol.*, 47, 54-71, <https://doi.org/10.1016/j.quageo.2018.05.008>, 2018.

- 786 Blomdin, R., Stroeven, A.P., Harbor, J.M., Lifton, N.A., Heyman, J., Gribenski, N., Petrakov, D.A., Caffee, M.W.,
787 Ivanov, M.N., Hättestrand, C., Rogozhina, I., Usubaliev, R.: Evaluating the timing of former glacier
788 expansions in the Tian Shan: A key step towards robust spatial correlations, *Quat. Sci. Rev.*, 153, 78-96,
789 <https://doi.org/10.1016/j.quascirev.2016.07.029>, 2016.
- 790 Buizert, C., Keisling, B., Box, J., He, F., Carlson, A., Sinclair, G., and DeConto, R.: Greenland-wide seasonal
791 temperatures during the last deglaciation, *Geophys. Res. Lett.*, v. 45, no. 4, p. 1905-1914,
792 <https://doi.org/10.1002/2017GL075601>, 2018.
- 793 Byun, J., Heimsath, A.M., Seong, Y.B., Lee, S.Y.: Erosion of a high-altitude, low-relief area on the Korean Peninsula:
794 implications for its development processes and evolution, *Earth Surf. Process. Landf.*, 40(13), 1730-1745,
795 <https://doi.org/10.1002/esp.3749>, 2015.
- 796 Chai, L. T., Wong, C. J., James, D., Loh, H. Y., Liew, J. J. F., Wong, W. V. C., & Phua, M. H.: Vertical accuracy
797 comparison of multi-source Digital Elevation Model (DEM) with Airborne Light Detection and Ranging
798 (LiDAR). In *IOP Conference Series: Earth. Environ. Sci.*, 1053, No. 1, p. 012025, IOP Publishing,
799 10.1088/1755-1315/1053/1/012025, 2022.
- 800 Chauvenet, W.: A Manual of spherical and practical astronomy-Vol. 1: Spherical astronomy; Vol. 2: Theory and use
801 of astronomical instruments. Method of least squares, 5th ed., revised and corr, Dover Publication, New York,
802 1960
- 803 Chen, Y., Li, Y., Wang, Y., Zhang, M., Cui, Z., Yi, C., Liu, G.: Late Quaternary glacial history of the Karlik Range,
804 easternmost Tian Shan, derived from ¹⁰Be surface exposure and optically stimulated luminescence datings,
805 *Quat. Sci. Rev.*, 115, 17-27, <https://doi.org/10.1016/j.quascirev.2015.02.010>, 2015.
- 806 Ciner, A., Sarikaya, M. A., Yildirim, C.: Misleading old age on a young landform? The dilemma of cosmogenic
807 inheritance in surface exposure dating: Moraines vs. rock glaciers, *Quat. Geochronol.*, 42, 76-88,
808 <https://doi.org/10.1016/j.quageo.2017.07.003>, 2017.
- 809 Clark, P.U., Dyke, A.S., Shakun, J.D., Carlson, A.E., Clark, J., Wohlfarth, B., Mitrovica, J.X., Hostetler, S.W.,
810 McCabe, A.M.: The last glacial maximum, *Science*, 325(5941), 710-714,
811 <https://doi.org/10.1126/science.1172873>, 2009.
- 812 Cossart, E., Braucher, R., Fort, M., Bourlès, D., Carcaillet, J.: Slope instability in relation to glacial debuttressing in
813 alpine areas (Upper Durance catchment, southeastern France): evidence from field data and ¹⁰Be cosmic ray
814 exposure ages, *Geomorphology*, 95(1-2), 3-26, <https://doi.org/10.1016/j.geomorph.2006.12.022>, 2008.
- 815 Cunningham, D.: Tectonic setting and structural evolution of the Late Cenozoic Gobi-Altai orogen, *J. Geol. Soc.*
816 *London.*, 338(1), 361-387, <https://doi.org/10.1144/SP338.17>, 2010.
- 817 Cunningham, W.D., Windley, B.F., Dorjnamjaa, D., Badamgarov, J., Saandar, M.: Late Cenozoic transpression in
818 southwestern Mongolia and the Gobi-Altai-Tien Shan connection, *Earth Planet. Sci. Lett.*, 140(1-4), 67-81,
819 [https://doi.org/10.1016/0012-821X\(96\)00048-9](https://doi.org/10.1016/0012-821X(96)00048-9), 1996.
- 820 Dahl, S. O., Bakke, J., Lie, Ø., & Nesje, A.: Reconstruction of former glacier equilibrium-line altitudes based on
821 proglacial sites: an evaluation of approaches and selection of sites. *Quat. Sci. Rev.*, 22(2-4), 275-287,
822 [https://doi.org/10.1016/S0277-3791\(02\)00135-X](https://doi.org/10.1016/S0277-3791(02)00135-X), 2003

- 823 Delmas, M., Calvet, M., Gunnell, Y., Braucher, R., & Bourlès, D.: Palaeogeography and ^{10}Be exposure-age
824 chronology of Middle and Late Pleistocene glacier systems in the northern Pyrenees: implications for
825 reconstructing regional palaeoclimates, *Palaeogeog. Palaeoclimatol. Palaeoecol.*, 305(1-4), 109-122,
826 <https://doi.org/10.1016/j.palaeo.2011.02.025>, 2011.
- 827 Delmas, M., Gunnell, Y., Braucher, R., Calvet, M., & Bourlès, D.: Exposure age chronology of the last glaciation in
828 the eastern Pyrenees, *Quat. Res.*, 69(2), 231-241, <https://doi.org/10.1016/j.yqres.2007.11.004>, 2008.
- 829 Devyatkin, E.: Structures and formational complexes of the Cenozoic activated stage. *Tectonics of the Mongolian*
830 *People's Republic*, Nauka, 41, 182-195, 1974.
- 831 Dewey, J.F., Shackleton, R.M., Chengfa, C., Yiyin, S.: The tectonic evolution of the Tibetan Plateau, *Philos. Trans.*
832 *Royal Soc. A.*, 327(1594), 379-413, <https://doi.org/10.1098/rsta.1988.0135>, 1988.
- 833 EIC.: Geologic map of Mongolia 1:1000000. Environment Information Center of National Agency for Meteorology,
834 Hydrology and Environmental Monitoring, Ulaanbaatar, Mongolia, 1981.
- 835 Evans, I. S.: Local aspect asymmetry of mountain glaciation: a global survey of consistency of favoured directions for
836 glacier numbers and altitudes. *Geomorphology*, 73(1-2), <https://doi.org/10.1016/j.geomorph.2005.07.009>
837 166-184, 2006
- 838 Evans, I.S., Cox, N.J.: Global variations of local asymmetry in glacier altitude: separation of north-south and east-
839 west components, *J. Glaciol.*, 51(174), 469-482, <https://doi.org/10.3189/172756505781829205>, 2005.
- 840 Felauer, T., Schlütz, F., Murad, W., Mischke, S., Lehmkuhl, F.: Late Quaternary climate and landscape evolution in
841 arid Central Asia: A multiproxy study of lake archive Bayan Tohomin Nuurç, Gobi desert, southern Mongolia,
842 *J. Asian. Earth. Sci.*, 48, 125-135, <https://doi.org/10.1016/j.jseaes.2011.12.002>, 2012.
- 843 Ferreira, Z. A., & Cabral, P.: A Comparative study about vertical accuracy of four freely available digital elevation
844 models: a case study in the Balsas river watershed, Brazil. *ISPRS Int. J. Geo-Inf.*, 11(2), 106,
845 <https://doi.org/10.3390/ijgi11020106>, 2022
- 846 Fletcher, W.J., Goni, M.F.S., Allen, J.R., Cheddadi, R., Combourieu-Nebout, N., Huntley, B., Lawson, I., Londeix,
847 L., Magri, D., Margari, V.: Millennial-scale variability during the last glacial in vegetation records from
848 Europe, *Quat. Sci. Rev.*, 29(21-22), 2839-2864, <https://doi.org/10.1016/j.quascirev.2009.11.015>, 2010.
- 849 Florentine, C., Harper, J., Fagre, D.: Parsing complex terrain controls on mountain glacier response to climate forcing,
850 *Glob. Planet. Change.*, 191, 103209, <https://doi.org/10.1016/j.gloplacha.2020.103209>, 2020.
- 851 Gillespie, A.R., Burke, R.M., Komatsu, G., Bayasgalan, A.: Late Pleistocene glaciers in Darhad basin, northern
852 Mongolia, *Quat. Res.*, 69(2), 169-187, <https://doi.org/10.1016/j.yqres.2008.01.001>, 2008.
- 853 Goldthwait, R.P.: Mountain glaciers of the Presidential Range in New Hampshire, *Arc. Alp. Res.*, 2(2), 85-102,
854 <https://doi.org/10.1080/00040851.1970.12003566>, 1970.
- 855 Gosse, J.C., Phillips, F.M.: Terrestrial in situ cosmogenic nuclides: theory and application, *Quat. Sci. Rev.*, 20(14),
856 1475-1560, [https://doi.org/10.1016/S0277-3791\(00\)00171-2](https://doi.org/10.1016/S0277-3791(00)00171-2), 2001.
- 857 Gribenski, N., Jansson, K. N., Preusser, F., Harbor, J. M., Stroeven, A. P., Trauerstein, M., ... & Zhang, W.: Re-
858 evaluation of MIS 3 glaciation using cosmogenic radionuclide and single grain luminescence ages, Kanas
859 Valley, Chinese Altai. *J. Quat. Sci.*, 33(1), 55-67, <https://doi.org/10.1002/jqs.2998>, 2018

- 860 Hashemi, K., Sarıkaya, M.A., Görüm, T., Wilcken, K.M., Çiner, A., Žebre, M., Stepišnik, U., Yıldırım, C.: The
861 Namaras rock avalanche: Evidence of mid-to-late Holocene paraglacial activity in the Central Taurus
862 Mountains, SW Turkey, *Geomorphology*, 408, 108261, <https://doi.org/10.1016/j.geomorph.2022.108261>,
863 2022.
- 864 Heyman, J.: Paleoglaciation of the Tibetan Plateau and surrounding mountains based on exposure ages and ELA
865 depression estimates, *Quat. Sci. Rev.*, 91, 30-41, <https://doi.org/10.1016/j.quascirev.2014.03.018>, 2014.
- 866 Heyman, J., Stroeven, A.P., Caffee, M.W., Hättestrand, C., Harbor, J.M., Li, Y., Alexanderson, H., Zhou, L., Hubbard,
867 A.: Palaeoglaciology of Bayan Har Shan, NE Tibetan Plateau: exposure ages reveal a missing LGM
868 expansion, *Quat. Sci. Rev.*, 30(15-16), 1988-2001, <https://doi.org/10.1016/j.quascirev.2011.05.002>, 2011a.
- 869 Heyman, J., Stroeven, A.P., Harbor, J.M., Caffee, M.W.: Too young or too old: evaluating cosmogenic exposure
870 dating based on an analysis of compiled boulder exposure ages, *Earth Planet. Sci. Lett.*, 302(1-2), 71-80,
871 <https://doi.org/10.1016/j.epsl.2010.11.040>, 2011b.
- 872 Hock, R.: Modelling of glacier melt and discharge: ETH Zurich-, 1999, A distributed temperature-index ice-and
873 snowmelt model including potential direct solar radiation, *J. Glaciol.*, v. 45, no. 149, p. 101-111,
874 <https://doi.org/10.3189/S0022143000003087>, 1998,
- 875 Hock, R.: A distributed temperature-index ice-and snowmelt model including potential direct solar radiation, *J.*
876 *Glaciol.*, 45(149), 101-111, <https://doi.org/10.3189/S0022143000003087>, 1999.
- 877 Hughes, P.D., Gibbard, P.L., Ehlers, J.: Timing of glaciation during the last glacial cycle: evaluating the concept of a
878 global 'Last Glacial Maximum'(LGM). *Earth-Sci. Rev.*, 125, 171-198,
879 <https://doi.org/10.1016/j.earscirev.2013.07.003>, 2013.
- 880 Iqbal, M.: *An Introduction to Solar Radiation*, New York, Academic Press, 1983
- 881 Jiménez-Sánchez, M., Rodríguez-Rodríguez, L., García-Ruiz, J.M., Domínguez-Cuesta, M.J., Farias, P., Valero-
882 Garcés, B.L., Moreno, A., Valcárcel, M.: A review of glacial geomorphology and chronology in northern
883 Spain: timing and regional variability during the last glacial cycle. *Geomorphology* 196, 50–64,
884 <https://doi.org/10.1016/j.geomorph.2012.06.009>, 2013
- 885 Jolivet, M., Ritz, J.-F., Vassallo, R., Larroque, C., Braucher, R., Todbileg, M., Chauvet, A., Sue, C., Arnaud, N., De
886 Vicente, R.: Mongolian summits: an uplifted, flat, old but still preserved erosion surface, *Geology*, 35(10),
887 871-874, <https://doi.org/10.1130/G23758A.1>, 2007.
- 888 Jones, R., Small, D., Cahill, N., Bentley, M., Whitehouse, P.: iceTEA: tools for plotting and analysing cosmogenic-
889 nuclide surface-exposure data from former ice margins, *Quat. Geochronol.*, 51, 72-86,
890 <https://doi.org/10.1016/j.quageo.2019.01.001>, 2019.
- 891 Jouzel, J., Stievenard, M., Johnsen, S.J., Landais, A., Masson-Delmotte, V., Sveinbjörnsdóttir, A., Vimeux, F., Von
892 Grafenstein, U., White, J.W.: The GRIP deuterium-excess record, *Quat. Sci. Rev.*, 26(1-2), 1-17,
893 <https://doi.org/10.1016/j.quascirev.2006.07.015>, 2007.
- 894 Karger, D.N., Conrad, O., Böhner, J., Kawohl, T., Kreft, H., Soria-Auza, R.W., Zimmermann, N.E., Linder, H.P.,
895 Kessler, M.: Climatologies at high resolution for the earth's land surface areas. *Sci. Data.*, 4, 170122,
896 <https://doi.org/10.1038/sdata.2017.122>, 2017.

- 897 Khandsuren, P., Seong, Y.B., Oh, J.S., Rhee, H.H., Sandag, K., Yu, B.Y.: Late Quaternary glacial history of Khentey
898 Mountains, Central Mongolia, *Boreas*, 48(3), 779-799, doi.org/10.1111/bor.12386, 2019.
- 899 Kirkbride, M., Winkler, S.: Correlation of Late Quaternary moraines: impact of climate variability, glacier response,
900 and chronological resolution, *Quat. Sci. Rev.*, 46, 1-29, https://doi.org/10.1016/j.quascirev.2012.04.002,
901 2012.
- 902 Klinge, M., Schneider, F., Dulamsuren, C., Arndt, K., Bayarsaikhan, U., & Sauer, D.: Interrelations between relief,
903 vegetation, disturbances, and permafrost in the forest-steppe of central Mongolia. *Earth Surf. Process.*
904 *Landf.*, 46(9), 1766-1782, https://doi.org/10.1002/esp.5116, 2021
- 905 Kohl, C.P., Nishiizumi, K.: Chemical isolation of quartz for measurement of in situ -produced cosmogenic nuclides,
906 *Geochim. Cosmochim. Acta*, 56(9), 3583-3587, https://doi.org/10.1016/0016-7037(92)90401-4, 1992.
- 907 Koppes, M., Gillespie, A.R., Burke, R.M., Thompson, S.C., Stone, J.: Late quaternary glaciation in the Kyrgyz Tien
908 Shan. *Quat. Sci. Rev.*, 27(7-8), 846-866, https://doi.org/10.1016/j.quascirev.2008.01.009, 2008.
- 909 Laabs, B. J., Licciardi, J. M., Leonard, E. M., Munroe, J. S., & Marchetti, D. W.: Updated cosmogenic chronologies
910 of Pleistocene mountain glaciation in the western United States and associated paleoclimate inferences, *Quat.*
911 *Sci. Rev.*, 242, 106427, https://doi.org/10.1016/j.quascirev.2020.106427, 2020.
- 912 Laabs, B. J. C., & Munroe, J. S.: Late Pleistocene mountain glaciation in the Lake Bonneville basin, In *Developments*
913 *in Earth. Surf. Process.*, Vol. 20, pp. 462-503, https://doi.org/10.1016/B978-0-444-63590-7.00017-2, 2016
- 914 Laabs, B. J., Marchetti, D. W., Munroe, J. S., Refsnider, K. A., Gosse, J. C., Lips, E. W., ... & Singer, B. S.; Chronology
915 of latest Pleistocene mountain glaciation in the western Wasatch Mountains, Utah, USA. *Quaternary*
916 *Research*, 76(2), 272-284, https://doi.org/10.1016/j.yqres.2011.06.016, 2011
- 917 Laabs, B. J., Refsnider, K. A., Munroe, J. S., Mickelson, D. M., Applegate, P. J., Singer, B. S., & Caffee, M. W.:
918 Latest Pleistocene glacial chronology of the Uinta Mountains: support for moisture-driven asynchrony of the
919 last deglaciation, *Quat. Sci. Rev.*, 28(13-14), 1171-1187, https://doi:10.1016/j.quascirev.2008.12.012, 2009.
- 920 Lee, M.K., Lee, Y.I., Lim, H.S., Lee, J.I., Yoon, H.I.: Late Pleistocene–Holocene records from Lake Ulaan, southern
921 Mongolia: implications for east Asian palaeomonsoonal climate changes, *J. Quat. Sci.*, 28(4), 370-378,
922 https://doi.org/10.1002/jqs.2626, 2013.
- 923 Lehmkuhl, F., Grunert, J., Hülle, D., Batkhishig, O., Stauch, G.: Paleolakes in the Gobi region of southern Mongolia,
924 *Quat. Sci. Rev.*, 179, 1-23, https://doi.org/10.1016/j.quascirev.2017.10.035, 2018.
- 925 Li, Y., Liu, G., Chen, Y., Li, Y., Harbor, J., Stroeven, A.P., Caffee, M., Zhang, M., Li, C., Cui, Z.: Timing and extent
926 of Quaternary glaciations in the Tianger Range, eastern Tian Shan, China, investigated using ¹⁰Be surface
927 exposure dating, *Quat. Sci. Rev.*, 98, 7-23, https://doi.org/10.1016/j.quascirev.2014.05.009, 2014.
- 928 Licciardi, J. M., Clark, P. U., Brook, E. J., Elmore, D., & Sharma, P.: Variable responses of western US glaciers during
929 the last deglaciation, *Geology*, 32(1), 81-84, https://doi.org/10.1130/G19868.1, 2004
- 930 Licciardi, J. M., Clark, P. U., Brook, E. J., Pierce, K. L., Kurz, M. D., Elmore, D., & Sharma, P.: Cosmogenic ³He
931 and ¹⁰Be chronologies of the late Pinedale northern Yellowstone ice cap, Montana, USA, *Geology*, 29(12),
932 1095-1098, https://doi.org/10.1130/0091-7613(2001)029<1095:CHABCO>2.0.CO;2, 2001.

- 933 Licciardi, J. M., & Pierce, K. L.: History and dynamics of the Greater Yellowstone Glacial System during the last two
934 glaciations, *Quat. Sci. Rev.*, 200, 1-33, <https://doi.org/10.1016/j.quascirev.2018.08.027>, 2018
- 935 Lifton, N., Sato, T., Dunai, T.J.: Scaling in situ cosmogenic nuclide production rates using analytical approximations
936 to atmospheric cosmic-ray fluxes, *Earth Planet. Sci. Lett.*, 386, 149-160,
937 <https://doi.org/10.1016/j.epsl.2013.10.052>, 2014.
- 938 Luckman, B. H.: The Geomorphic Activity of Snow Avalanches. *Geografiska Annaler: Series A, Phys. Geogr.*,
939 59(1-2), 31-48, <https://doi.org/10.1080/04353676.1977.11879945>, 1977.
- 940 Meierding, T. C.: Late Pleistocene glacial equilibrium-line altitudes in the Colorado Front Range: a comparison of
941 methods. *Quat. Res.*, 18(3), 289-310. *Research 18*, 289-310, [https://doi.org/10.1016/0033-5894\(82\)90076-X](https://doi.org/10.1016/0033-5894(82)90076-X),
942 1982
- 943 Mischke, S., Lee, M.K., Lee, Y.I.: Climate history of southern Mongolia since 17 ka: The ostracod, gastropod and
944 charophyte record from Lake Ulaan, *Front. Earth Sci.*, 8, 221, <https://doi.org/10.3389/feart.2020.00221>,
945 2020.
- 946 NAMHEM.: Climate data. Institute for Hydrology and Aviation Meteorological Center of National Agency for
947 Meteorology, Hydrology and Environmental Monitoring, Ulaanbaatar, Mongolia, 2020.
- 948 Nishiizumi, K., Imamura, M., Caffee, M., Southon, J., Finkel, R., McAninch, J.: Absolute calibration of ^{10}Be AMS
949 Standards, *Nucl. Instrum. Methods Phys. Res. B.*, 258(2), 403-413,
950 <https://doi.org/10.1016/j.nimb.2007.01.297>, 2007.
- 951 National Oceanic and Atmospheric Administration.: US standard atmosphere (Vol. 76)., 1976
- 952 Oliva, M., Palacios, D., Fernández-Fernández, J. M., Rodríguez-Rodríguez, L., García-Ruiz, J. M., Andrés, N., ... &
953 Hughes, P. D.: Late Quaternary glacial phases in the Iberian Peninsula, *Earth-Sci. Rev.*, 192, 564-600,
954 <https://doi.org/10.1016/j.earscirev.2019.03.015>, 2019.
- 955 Olson, M., & Rupper, S.: Impacts of topographic shading on direct solar radiation for valley glaciers in complex
956 topography, *The Cryosphere*, 13(1), 29-40, 2019.
- 957 Palacios, D., Stokes, C. R., Phillips, F. M., Clague, J. J., Alcalá-Reygosa, J., Andrés, N., ... & Ward, D. J.: The
958 deglaciation of the Americas during the Last Glacial Termination, *Earth-Sci. Rev.*, 203, 103113,
959 <https://doi.org/10.1016/j.earscirev.2020.103113>, 2020.
- 960 Porter, S.C.: Snowline depression in the tropics during the Last Glaciation. *Quat. Sci. Rev.*, 20(10), pp.1067-
961 1091, [https://doi.org/10.1016/S0277-3791\(00\)00178-5](https://doi.org/10.1016/S0277-3791(00)00178-5), 2001
- 962 Pötsch, S.: Dynamics and paleo-climatic forcing of late Pleistocene glaciers in the Turgen and Khangai mountains
963 (Mongolia) reconstructed from geomorphology, ^{10}Be surface exposure dating, and ice flow modelling. Ph.D.
964 thesis, Greifswald, Finsterwalde, 2017.
- 965 Quirk, B. J., Moore, J. R., Laabs, B. J., Plummer, M. A., & Caffee, M. W.: Latest Pleistocene glacial and climate
966 history of the Wasatch Range, Utah, *Quat. Sci. Rev.*, 238, 106313,
967 <https://doi.org/10.1016/j.quascirev.2020.106313>, 2020.
- 968 Ross, S.M.: Peirce's criterion for the elimination of suspect experimental data, *J. Eng. Technol.*, 20(2), 38-41, 2003.

- 969 Rother, H., Lehmkuhl, F., Fink, D., Nottebaum, V.: Surface exposure dating reveals MIS-3 glacial maximum in the
970 Khangai Mountains of Mongolia, *Quat. Res.*, 82(2), 297-308, <https://doi.org/10.1016/j.yqres.2014.04.006>,
971 2014.
- 972 Sanders, J. W., Cuffey, K. M., Moore, J. R., MacGregor, K. R., & Kavanaugh, J. L.: Periglacial weathering and
973 headwall erosion in cirque glacier bergschrunds. *Geology*, 40(9), 779-782, <https://doi.org/10.1130/G33330.1>,
974 2012
- 975 Şengör, A., Natal'In, B., Burtman, V.: Evolution of the Altaid tectonic collage and Palaeozoic crustal growth in Eurasia,
976 *Nature*, 364(6435), 299-307, <https://doi.org/10.1038/364299a0>, 1993.
- 977 Seong, Y.B., Dorn, R.I., Yu, B.Y.: Evaluating the life expectancy of a desert pavement, *Earth-Sci.Rev.*, 162, 129-154,
978 <https://doi.org/10.1016/j.earscirev.2016.08.005>, 2016.
- 979 Shackleton, N.: Oxygen isotope analyses and Pleistocene temperatures re-assessed, *Nature*, 215(5096), 15-17,
980 <https://doi.org/10.1038/215015a0>, 1967.
- 981 Shackleton, N.J.: The 100,000-year ice-age cycle identified and found to lag temperature, carbon dioxide, and orbital
982 eccentricity, *Science*, 289(5486), 1897-1902, <https://doi.org/10.1126/science.289.5486.1897>, 2000.
- 983 Skinner, L., Shackleton, N.: An Atlantic lead over Pacific deep-water change across Termination I: implications for
984 the application of the marine isotope stage stratigraphy, *Quat. Sci. Rev.*, 24(5-6), 571-580,
985 <https://doi.org/10.1016/j.quascirev.2004.11.008>, 2005.
- 986 Smith, S.G., Wegmann, K.W., Ancuta, L.D., Gosse, J.C., Hopkins, C.E.: Paleotopography and erosion rates in the
987 central Hangay Dome, Mongolia: Landscape evolution since the mid-Miocene, *J. Asian. Earth. Sci.*, 125, 37-
988 57 DOI: <https://doi.org/10.1016/j.jseaes.2016.05.013>, 2016.
- 989 Tang, Z., & Fang, J.: Temperature variation along the northern and southern slopes of Mt. Taibai, China, *Agric. For.*
990 *Meteorol.*, 139(3-4), 200-207, <https://doi.org/10.1016/j.agrformet.2006.07.001>, 2006.
- 991 Tarasov, P., Peyron, O., Guiot, J., Brewer, S., Volkova, V., Bezusko, L., Dorofeyuk, N., Kvavadze, E., Osipova, I.,
992 and Panova, N.: Last Glacial Maximum climate of the former Soviet Union and Mongolia reconstructed from
993 pollen and plant macrofossil data, *Clim. Dyn.*, v. 15, no. 3, p. 227-240,
994 <https://doi.org/10.1007/s003820050278>, 1999,
- 995 Thackray, G. D.: Varied climatic and topographic influences on Late Pleistocene mountain glaciation in the western
996 United States, *J. Quat. Sci.*, Published for the Quaternary Research Association, 23(6-7), 671-681,
997 <https://doi.org/10.1002/jqs.1210>, 2008.
- 998 Thompson, W.G., Spiegelman, M.W., Goldstein, S.L., Speed, R.C.: An open-system model for U-series age
999 determinations of fossil corals, *Earth Planet. Sci. Lett.*, 210(1-2), 365-381, [https://doi.org/10.1016/S0012-821X\(03\)00121-3](https://doi.org/10.1016/S0012-821X(03)00121-3), 2003.
- 1000
- 1001 Traynor, J., Sladen, C.: Tectonic and stratigraphic evolution of the Mongolian People's Republic and its influence on
1002 hydrocarbon geology and potential, *Mar. Pet. Geol.*, 12(1), 35-52, [https://doi.org/10.1016/0264-8172\(95\)90386-X](https://doi.org/10.1016/0264-8172(95)90386-X), 1995.
- 1003

- 1004 Vassallo, R., Jolivet, M., Ritz, J.-F., Braucher, R., Larroque, C., Sue, C., Todbileg, M., Javkhlanbold, D.: Uplift age
1005 and rates of the Gurvan Bogd system (Gobi-Altay) by apatite fission track analysis, *Earth Planet. Sci. Lett.*,
1006 259(3-4), 333-346, <https://doi.org/10.1016/j.epsl.2007.04.047>, 2007.
- 1007 Vassallo, R., Ritz, J.-F., Carretier, S.: Control of geomorphic processes on ^{10}Be concentrations in individual clasts:
1008 Complexity of the exposure history in Gobi-Altay range (Mongolia), *Geomorphology*, 135(1-2), 35-47,
1009 <https://doi.org/10.1016/j.geomorph.2011.07.023>, 2011.
- 1010 Wang, Y.-J., Cheng, H., Edwards, R.L., An, Z., Wu, J., Shen, C.-C., Dorale, J.A.: A high-resolution absolute-dated
1011 late Pleistocene monsoon record from Hulu Cave, China, *Science*, 294(5550), 2345-2348,
1012 <https://doi.org/10.1126/science.1064618>, 2001.
- 1013 Young, N. E., Briner, J. P., Leonard, E. M., Licciardi, J. M., & Lee, K.: Assessing climatic and nonclimatic forcing
1014 of Pinedale glaciation and deglaciation in the western United States, *Geology*, 39(2), 171-174,
1015 <https://doi.org/10.1130/G31527.1>, 2011.
- 1016 Yu, K., Lehmkuhl, F., Diekmann, B., Zeeden, C., Nottebaum, V., Stauch, G.: Geochemical imprints of coupled
1017 paleoenvironmental and provenance change in the lacustrine sequence of Orog Nuur, Gobi Desert of
1018 Mongolia, *J. Paleolimnol.*, 58(4), 511-532, <https://doi.org/10.1007/s10933-017-0007-7>, 2017.
- 1019 Yu, K., Lehmkuhl, F., Schlütz, F., Diekmann, B., Mischke, S., Grunert, J., Murad, W., Nottebaum, V., Stauch, G.,
1020 Zeeden, C.: Late Quaternary environments in the Gobi Desert of Mongolia: Vegetation, hydrological, and
1021 palaeoclimate evolution, *Palaeogeogr. Palaeoclimatol. Palaeoecol.*, 514, 77-91,
1022 <https://doi.org/10.1016/j.palaeo.2018.10.004>, 2019.
- 1023 Zhang, S., Zhao, H., Sheng, Y., Chen, S., Li, G., & Chen, F.: Late Quaternary lake level record of Orog Nuur, southern
1024 Mongolia, revealed by optical dating of paleo-shorelines, *Quat. Geochronol.*, 72, 101370,
1025 <https://doi.org/10.1016/j.quageo.2022.101370>, 2022.
- 1026

1027 **LIST OF TABLES**

1028 Table 1. Site parameters and glacier parameters used for the 2D ice surface model

1029 Table 2. Key parameters of glacial mass balance model

1030 Table 3. LGM ELA reconstruction

1031 Table 4. Result of ^{10}Be exposure age dating

1032

1033

1034 **LIST OF FIGURES**

1035 Figure 1. Study area

1036 Figure 2. The present-day climate of Mongolia

1037 Figure 3. Source code structure diagram of 2D ice surface modelling

1038 Figure 4. Photo composites of the Ikh Artsan valley and paleoglacial evidence

1039 Figure 5. Geomorphologic setting and moraine stratigraphy in Jargalant valley

1040 Figure 6. ^{10}Be Exposure ages (ka) for moraine sequences1041 Figure 7. Kernel Density Plot (KDP) of estimated ^{10}Be exposure ages from distal moraine crests in Jargalant and Ikh
1042 Artsan valleys1043 Figure 8. Asymmetric distribution of potential clear-sky direct solar radiation, glacial melt, and vegetation on the
1044 south- and north-facing slopes.1045 Figure 9. Temporal and spatial distributions of glacial and paleo-lacustrine records in the neighboring regions of Ikh
1046 Bogd massif

1047 Figure 10. Asynchronous advance and retreat pattern of Ikh Bogd paleoglacier during 22-16 ka

1048 Figure 11. Rockfall deposits in Jargalant valley

1049 Figure 12. Inheritance from the uplifted paleo-surface of Ikh Bogd

1050 **Table 1.** Site parameters and glacier parameters used for the 2D ice surface model

Variable	Value	Unit
Time interval	22-16	ka
Day type	1 (calendar day)	
Day interval	152-243 (summer)	
Average elevation of site	3265.3	m
Modern summer temperature of Ikh Artsan	5.4	°C
Modern summer temperature of Jargalant	4.9	°C
LGM anomaly	-5.5	°C
Snow ratio (when temperature is below 0°C)	0.35	
Elevation of initial glacier's toe (Ikh Artsan)	3385.1	m
Elevation of initial glacier's toe (Jargalant)	3360.9	m
Elevation of the distal moraine (Ikh Artsan)	3222.2	m
Elevation of the distal moraine (Jargalant)	2997.2	m
Headwall altitude (Ikh Artsan)	3508.3	m
Headwall altitude (Jargalant)	3533.3	m
Glacial bed shear stress (Ikh Artsan)	100	kPa
Glacial bed shear stress (Jargalant)	200	kPa

1051

1052

1053 **Table 2.** Key parameters of glacial mass balance model

Variable	Optimized values/Unit	Variable	Optimized values/Unit
Mass balance calculation (m, mm)		Air pressure calculation (P_h, Pa)	
c	Accumulation mm, m	P ₀	Pressure at reference point (sea level) 1013.25 Pa
a	Ablation/melt mm, m	T _h	Air temperature at the height h Pa
Melt calculation (a, m)		T ₀	Air temperature at the reference point 288.15 K
n	Number of time steps per day	M	Mass per air molecule 0.0290 kg mol ⁻¹
MF	Melt factor 1.8 mm d ⁻¹ °C ⁻¹	g	Acceleration due to gravity 9.8067 m s ⁻²
a _{ice}	Radiation coefficient for ice surfaces 0.0008	R	Universal gas constant 8.3143 mol K
I	Potential clear-sky direct solar radiation at the glacier W m ⁻²	L	Atmospheric lapse rate -0.008 K m ⁻¹
T	Monthly air temperature °C	Zenith angle calculation (Z, °) and angle of incidence (θ, °)	
Insolation calculation (I, w m⁻²)		δ	Solar declination angle °/Radian
I ₀	Solar constant 1367 W m ⁻²	φ	Latitude °/Radian
R _m /R	Eccentricity correction factor of the earth's orbit	ω	Hour angle °/Radian
Ψ _a	Atmospheric transmissivity 0.75	β	Slope inclination angle °/Radian
P _h	Air pressure at the height Pa	γ	Surface azimuth angle °/Radian
P ₀	Air pressure at reference point (sea level) 1013.25 Pa		
Z	Zenith angle °		
θ	Angle of incidence °		

1054

1055 **Table 3.** LGM ELA reconstruction

Sites	Top of the rock cliff (m a.s.l.)	Altitude of cirque floor (m a.s.l.)	Headwall altitude ^a (m a.s.l.)	Toe altitude, LGM (m a.s.l.)	THAR ELA ^b (m a.s.l.)
Jargalant valley	3620	3360	3533	2997	3308
Ikh Artsan valley	3560	3385	3508	3222	3388
Average					3348

1056 ^a Headwall altitude for LGM glaciers was selected at one-third of the altitude difference between the top of the rock
1057 cliff and the cirque floor (Goldthwait, 1970).

1058 ^b THAR of 0.58 was used for calculating LGM ELA (Batbaatar et al., 2018). ALOS PALSAR DEM with spatial
1059 resolution of 12.5 m is used to extract corresponding elevations. Altimetric error (vertical uncertainty) is ~5-7 m (Chai
1060 et al., 2022, Ferreira and Cabral, 2022).

1061

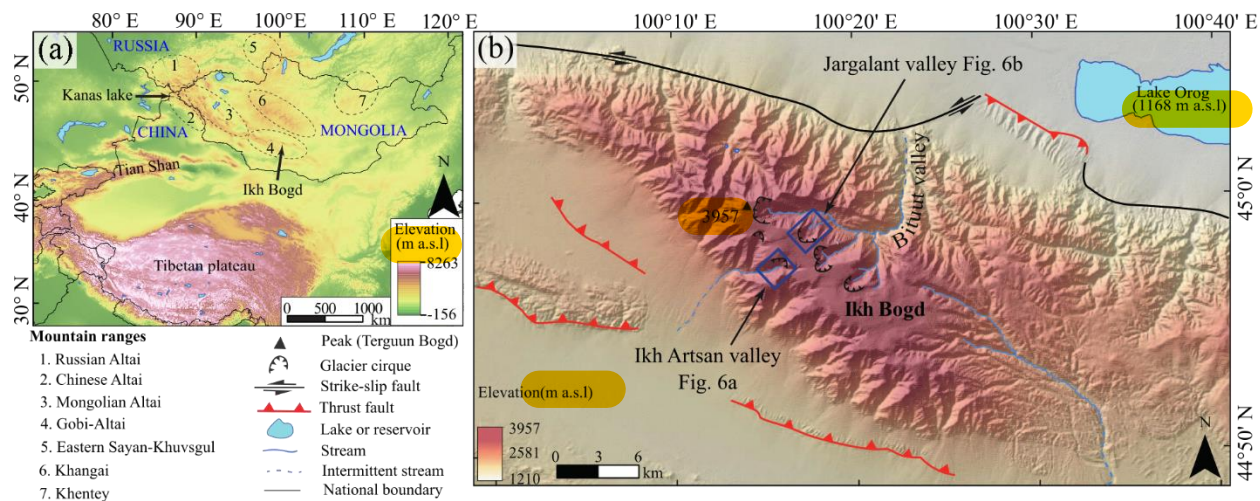
Table 4. Result of ^{10}Be exposure age dating

Moraine group	Name	Latitude (°N, DD)	Longitude (°E, DD)	Elevation (m a.s.l)	Thickness (cm)	Shielding factor ^b	Quartz ^c (g)	Be carrier ^d (g)	$^{10}\text{Be}/^9\text{Be}^{e,f}$ (10^{-15})	^{10}Be conc. ^{d,f} (10^5 atoms g^{-1})	Exposure age ^{f,g,i} (ka)	
											LSDn	
	IAM001	44.95421	100.2602	3289	2	0.7746	20.3	0.3729	6.0 ± 0.2	7.7 ± 0.3	19.9 ± 1.4	19.9 ± 1.4
	IAM002	44.95429	100.26022	3290	2.5	0.7746	17.52	0.3796	5.3 ± 0.2	8.0 ± 0.3	20.7 ± 1.4	20.7 ± 1.4
	IAM003	44.95427	100.2603	3289	3.5	0.7746	20	0.3849	6.1 ± 0.2	8.1 ± 0.3	21.2 ± 1.5	21.2 ± 1.5
M _{IAl}	IAM004	44.95438	100.26035	3289	3.5	0.7746	14.69	0.3958	4.1 ± 0.1	7.6 ± 0.3	19.9 ± 1.4	19.9 ± 1.4
	IAM005	44.95435	100.26015	3290	3	0.7746	19.75	0.3704	5.7 ± 0.2	7.4 ± 0.2	19.3 ± 1.3	19.3 ± 1.3
	IAM006	44.95437	100.26006	3288	3.5	0.7746	19.54	0.3812	5.7 ± 0.2	7.7 ± 0.2	20.3 ± 1.4	20.3 ± 1.4
	IAM007	44.95438	100.26004	3288	4	0.7746	18.96	0.3738	5.3 ± 0.2	7.2 ± 0.2	19.1 ± 1.3	19.1 ± 1.3
	JAM001	44.97614	100.29007	3412	3	0.8218	16.91	0.3842	78.6 ± 0.6	124.9 ± 1.6	278.9 ± 18.1	278.9 ± 18.1
	JAM002	44.97627	100.29012	3411	4	0.8218	20	0.3993	57.0 ± 0.6	79.7 ± 1.1	177.3 ± 11.3	177.3 ± 11.3
M ₁₄	JAM003	44.97651	100.29021	3411	2.5	0.8218	20.03	0.3871	194.3 ± 1.2	262.9 ± 3.1	636.2 ± 45.1	636.2 ± 45.1
	JAM004	44.97654	100.28988	3409	3	0.8218	20	0.382	70.9 ± 0.6	94.8 ± 1.3	208.9 ± 13.3	208.9 ± 13.3
	JAM005	44.97665	100.29008	3409	2.5	0.8218	20.03	0.375	64.8 ± 0.5	84.9 ± 1.1	186.6 ± 11.8	186.6 ± 11.8
	JAM006	44.97891	100.29092	3350	3	0.8363	20.02	0.3708	12.3 ± 2.6	15.9 ± 3.4	35.9 ± 8.0	35.9 ± 8.0
	JAM007	44.97886	100.29079	3351	3	0.8363	20.03	0.3707	25.3 ± 5.0	32.8 ± 6.5	74.1 ± 15.7	74.1 ± 15.7
M ₁₃	JAM008	44.97894	100.29084	3350	3	0.8363	20.42	0.3932	68.9 ± 7.0	92.9 ± 9.5	209.0 ± 26.1	209.0 ± 26.1
	JAM009	44.97891	100.29095	3348	3.5	0.8363	19.97	0.3832	15.3 ± 2.7	20.5 ± 3.7	45.8 ± 8.7	45.8 ± 8.7
	JAM010	44.97897	100.29089	3348	3.5	0.8363	19.97	0.3856	40.9 ± 5.7	55.2 ± 7.7	123.8 ± 19.4	123.8 ± 19.4
	JAM011	44.98058	100.29328	3293	2.5	0.8598	19.91	0.3903	52.3 ± 0.5	71.7 ± 1.0	162.1 ± 10.2	162.1 ± 10.2
	JAM012	44.98083	100.29321	3289	2	0.8598	19.97	0.3785	93.6 ± 0.6	124.2 ± 1.5	284.9 ± 18.4	284.9 ± 18.4
M ₁₂	JAM013	44.98095	100.29263	3289	4	0.8598	20.22	0.3794	81.0 ± 4.1	106.4 ± 5.5	246.6 ± 20.6	246.6 ± 20.6
	JAM014	44.98096	100.29259	3292	3	0.8598	20.38	0.3812	61.0 ± 6.4	79.9 ± 8.4	181.9 ± 23.0	181.9 ± 23.0
	JAM015	44.98096	100.2926	3292	3	0.8598	20.04	0.3894	59.4 ± 5.2	80.8 ± 7.1	184.0 ± 20.3	184.0 ± 20.3
	JAM016	44.98224	100.29684	3193	3.5	0.8852	19.91	0.3872	3.0 ± 0.1	4.0 ± 0.2	10.6 ± 0.8	10.6 ± 0.8
	JAM017	44.98232	100.29693	3191	3	0.8852	20.05	0.3935	4.8 ± 0.3	6.6 ± 0.4	16.3 ± 1.4	16.3 ± 1.4
M ₁₁	JAM018	44.98232	100.29693	3191	2.5	0.8852	20.06	0.3864	5.8 ± 0.4	7.8 ± 0.5	18.9 ± 1.7	18.9 ± 1.7
	JAM019	44.98326	100.29745	3170	3	0.8935	20.17	0.3962	4.4 ± 0.2	6.0 ± 0.3	15.1 ± 1.3	15.1 ± 1.3
	JAM020	44.98379	100.29716	3172	3.5	0.9311	20.14	0.3865	5.8 ± 0.2	7.7 ± 0.2	18.2 ± 1.2	18.2 ± 1.2
	JAM021	44.98385	100.29712	3171	3	0.9311	20.04	0.3879	5.4 ± 0.2	7.3 ± 0.2	17.4 ± 1.2	17.4 ± 1.2

1062

1063 ^a Sampling thickness of the boulders' outermost exposed surfaces.1064 ^b Topographic shielding factors for each sampling site were measured at intervals of 30°.1065 ^c Weight of the pure quartz. The density of granite (2.7 g cm^{-3}) was used to calculate exposure age.1066 ^d A mean value of process blank samples ($4.53 \times 10^{-15} \pm 1.62 \times 10^{-15}$) was used for correction.

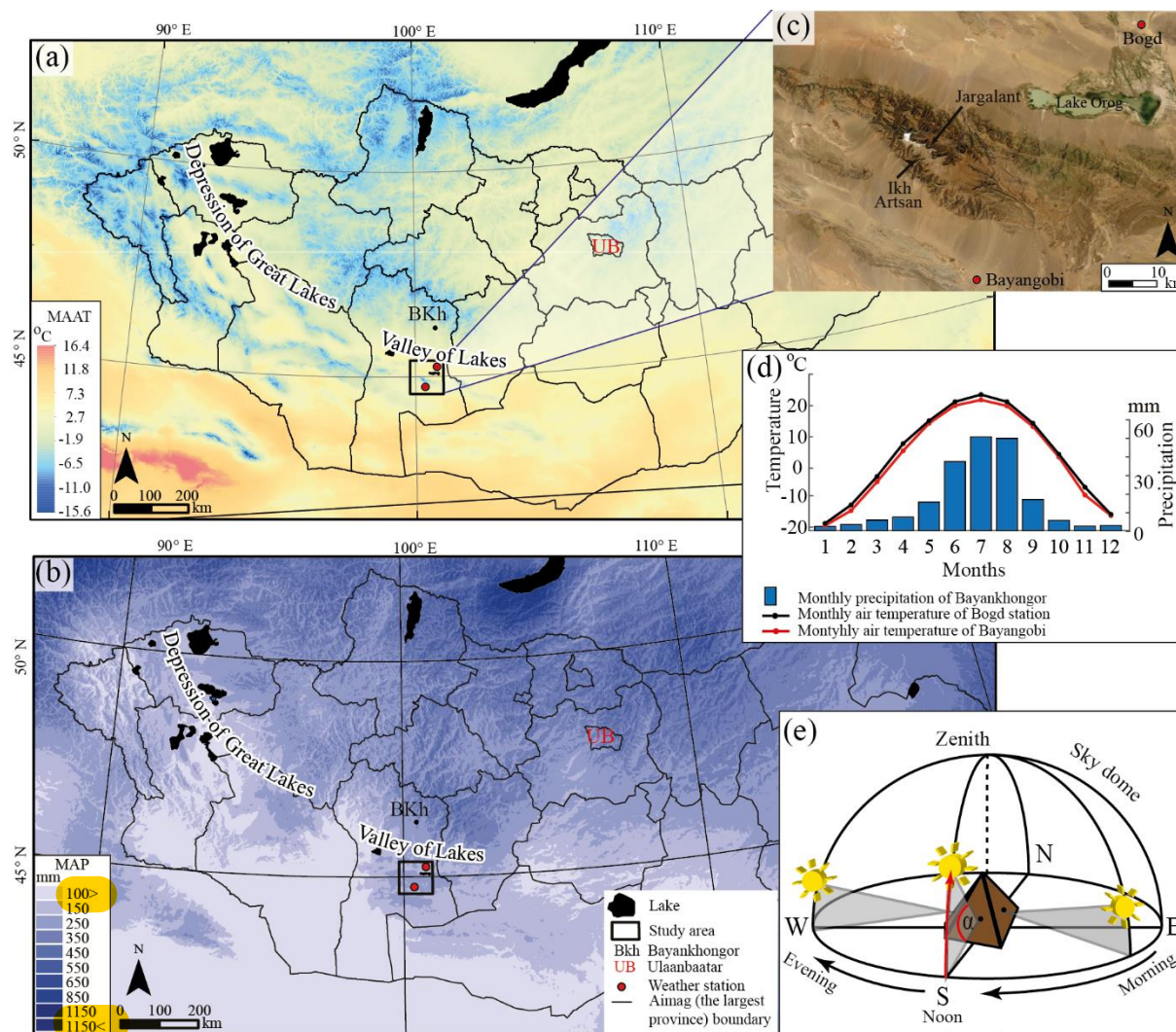
- 1067 ^e Ratios of $^{10}\text{Be}/^9\text{Be}$ were normalized with 07KNSTD reference sample 5-1 prepared by Nishiizumi et al. (2007) with
1068 a $^{10}\text{Be}/^9\text{Be}$ ratio of $2.71 \times 10^{-11} \pm 4.71 \times 10^{-13}$ (calibrated error) and using a ^{10}Be half-life of 1.36×10^6 years (Chmeleff
1069 et al., 2010; Korschinek et al., 2010)
- 1070 ^f Uncertainties were calculated at the 1σ confidence level.
- 1071 ^g Exposure ages, assuming zero erosion were calculated using CRONUS-Earth online calculator version 3.0.2 (Balco
1072 et al., 2008).
- 1073 ^h Constant production rate of the ^{10}Be model of Stone (2000) was used for calculating exposure age.
- 1074 ⁱ Constant production rate of the ^{10}Be model of Lifton et al. (2014) was used.



1075

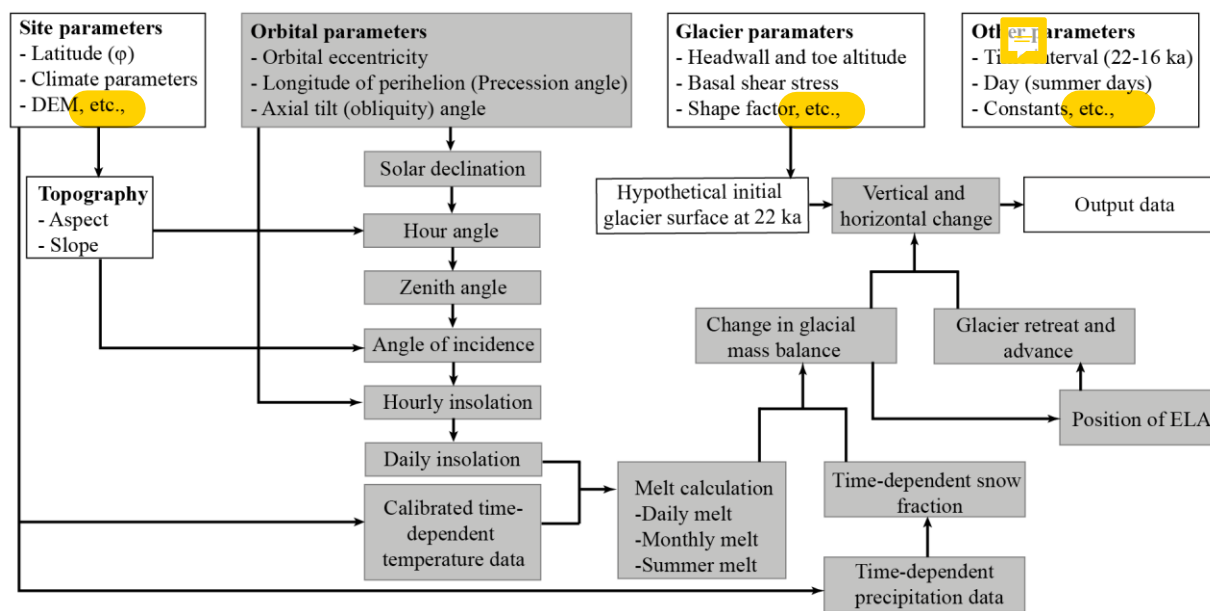
1076 **Fig. 1.** Study area. (a) Central Asian glaciated mountain ranges during late Quaternary. (b) Study area. Boxed areas
 1077 indicate Ikh Artsan and Jargalant valleys. See the detailed maps of both valleys visualized in Figs. 4-6. The background
 1078 image is shaded SRTM DEM with 30 m resolution.

1079



1080

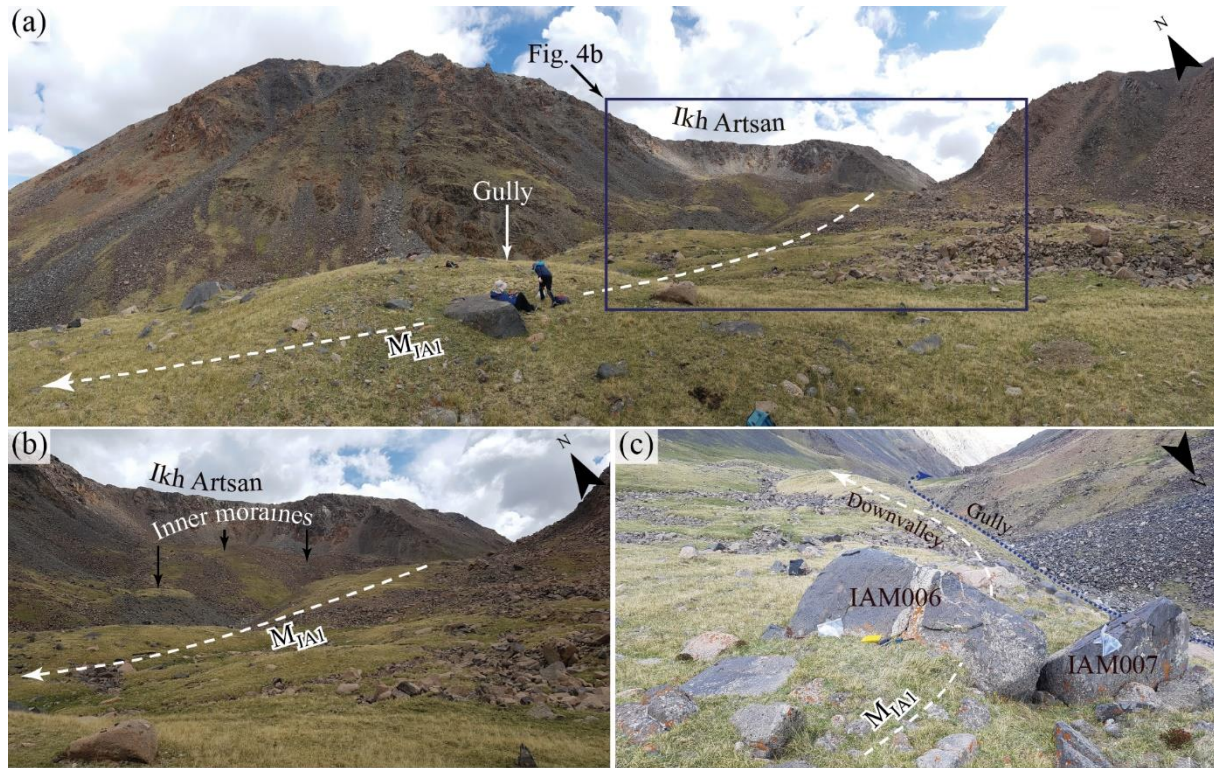
1081 **Fig. 2.** The present-day climate of Mongolia. (a) Mean annual air temperature across Mongolia. (b) Mongolian mean
 1082 annual precipitation. BKh (black dot) represents Bayankhongor aimag (the largest unit of province) center, and UB is
 1083 Ulaanbaatar, the capital of Mongolia. Red dots mark the nearest weather stations to the study area. Temperature data
 1084 (CHELSA_Bio10_01, at 30 arc-second) and precipitation data (CHELSA_Bio10_12, at 30 arc-second) are long-term
 1085 (1973-2013) annual means. Source: Bioclim Bio1 data, CHELSA V 1.2 (Karger et al., 2017). (c) The exact locations
 1086 of the nearest weather stations to the massif, Bayangobi (1540 m a.s.l) and Bogd (1240 m a.s.l). (d) Long-term (1989-
 1087 2019) monthly mean temperature from Bogd station (black graph) and Bayangobi station (red graph). Monthly mean
 1088 precipitation (2005-2019) of Bayankhongor is described as blue bar chart (NAMHEM, 2020). (e) Solar altitude angles
 1089 on the mountain slopes with different aspect. Solar altitude angles (α) at different hour angles (morning to evening).
 1090 Solar altitude angle is 0 degree at sunrise and reaches its maximum value at noon. In the mountainous area of northern
 1091 hemisphere, south-facing slope receives highest energy at noon, however, north-facing slope receives less or no energy
 1092 due to topographic shading effect.



1093

1094

Fig. 3. Source code structure diagram of 2D ice surface modelling



1095

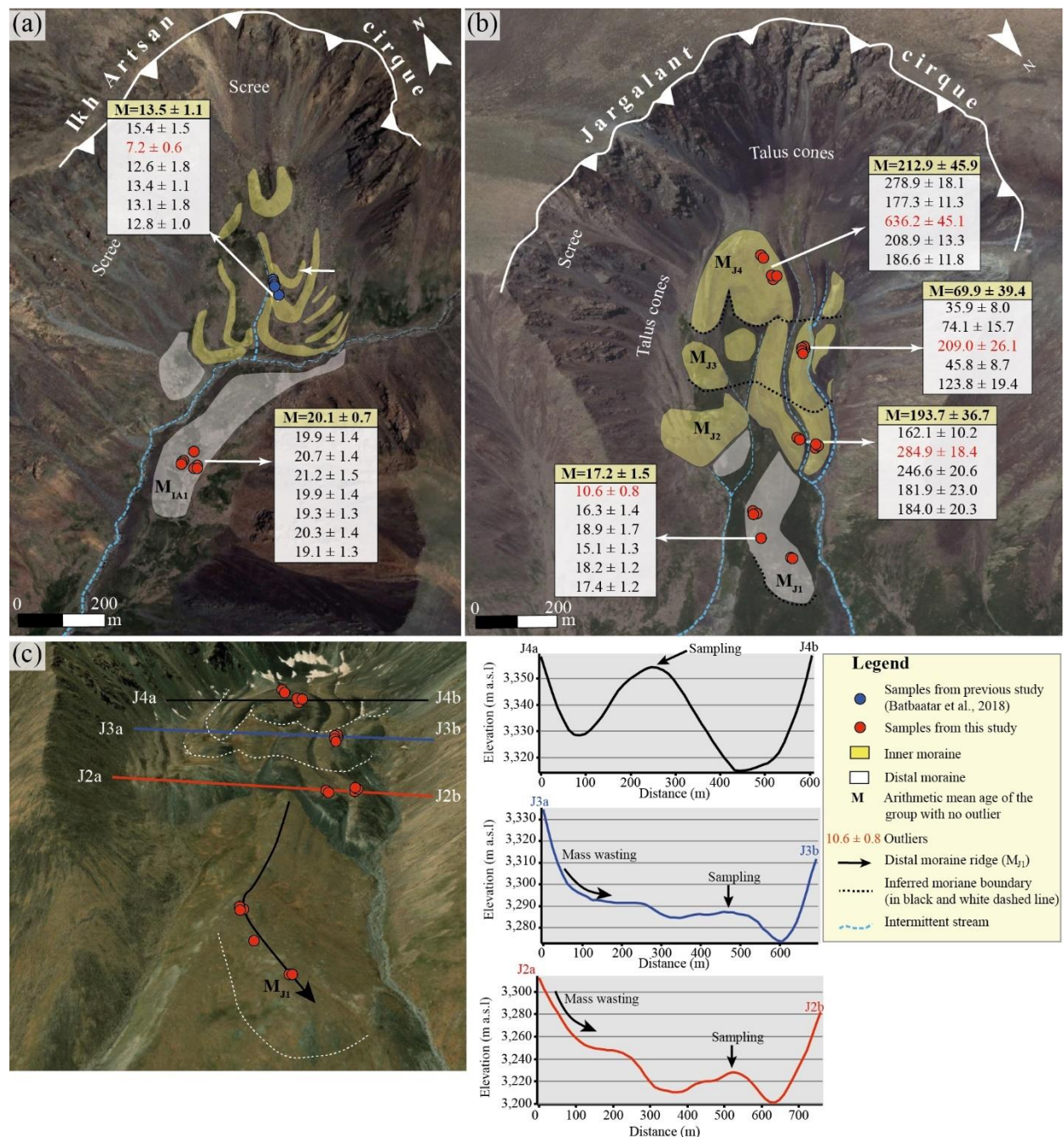
1096 **Fig. 4.** Photo composites of the Ikh Artsan valley and paleoglacial evidence. (a) Ikh Artsan glacial cirque and **distal**
 1097 **moraine ridge**. The white dashed arrow represents M_{IA1} moraine ridge, which marks the farthest extent of late
 1098 Quaternary glaciation. (b) Distal and inner moraine sequences (Batbaatar et al., 2018). (c) IAM006 and IAM007
 1099 sampling boulders are on the M_{IA1} moraine ridge.



1100

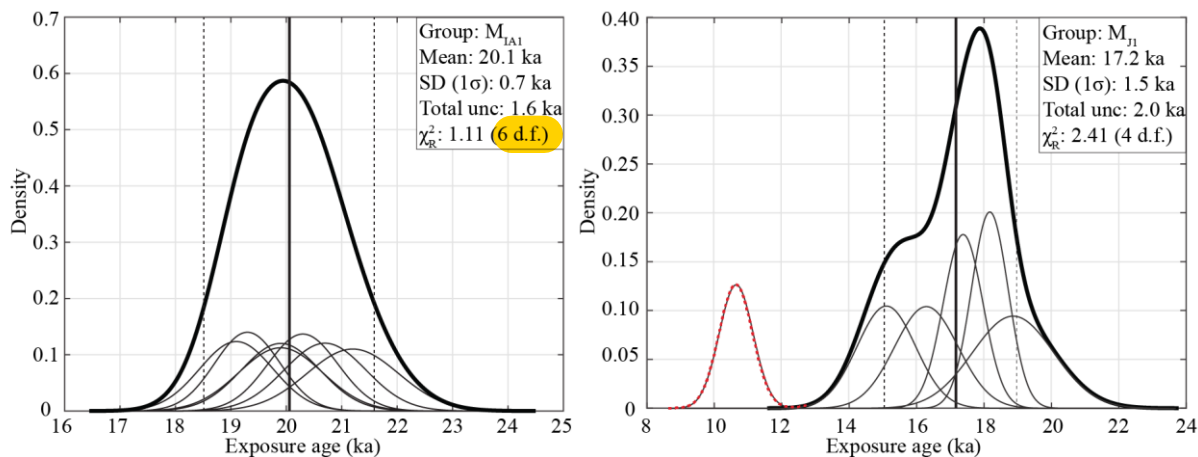
1101 **Fig. 5.** Geomorphologic setting and moraine stratigraphy in Jargalant valley. (a) Jargalant valley and Bituut trunk
 1102 valley that extends from the cirque near the highest peak (3957 m a.s.l.). Jargalant valley is one of the large tributaries
 1103 of Bituut valley, while covered by a large amount of late Quaternary moraine complex. (b) The stratigraphic boundary
 1104 between M_{J4} and M_{J3} moraines in the Jargalant cirque. Moraines are dissected by longitudinal gullies. (c) Pair of M_{J2}
 1105 moraine and oldest M_{J1} moraine ridge. Horses (red circle) are for scale. (d) Boulder sizes on M_{J2} moraine range from
 1106 sub-meter to several meters. (e) Downvalley view of the moraine sequences from the uppermost moraine sequence.

1107



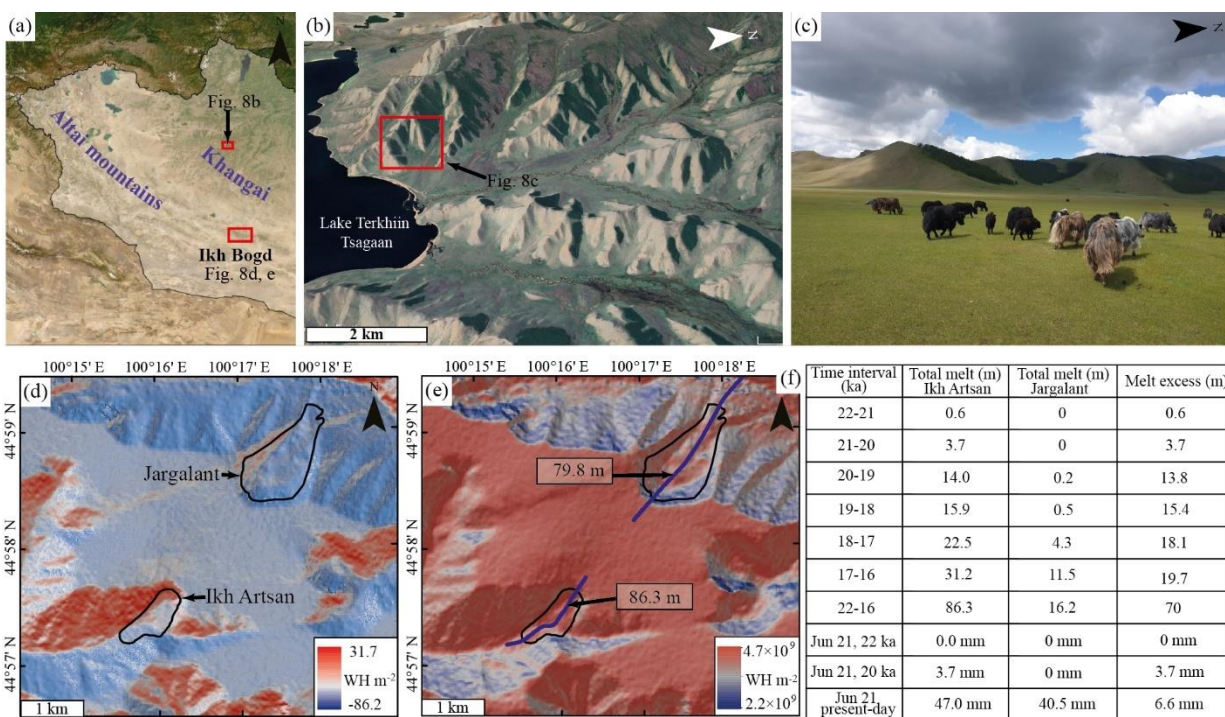
1108

1109 **Fig. 6.** ¹⁰Be Exposure ages (ka) for outer (white) and inner (yellow) moraine sequences. (a) Exposure ages from Ikh
 1110 Artsan moraine sequences. (b) Age dating result of Jargalant hummocky moraine complex. Background images of (a)
 1111 and (b) are © Bing Maps (2023) aerial imageries. (c) Cross-section view of inner moraine sequences (M_{J4} ~ M_{J2}) of
 1112 Jargalant valley. Background image is oblique imagery of © ArcGIS Earth (2023) V1.16.0.3547. Mass wasting
 1113 deposits on the moraine surface and intermittent stream incision have altered the original moraine morphologies.
 1114 Samples were taken from the highest intact point of the longitudinally elongated moraine ridge, which thought to be
 1115 unaffected by reworking processes. Since the exposure age dating result from inferred inner moraine sequences (M_{J4}
 1116 ~ M_{J2}) shows high inheritance, which cannot contribute the inferred moraine sequences.



1117

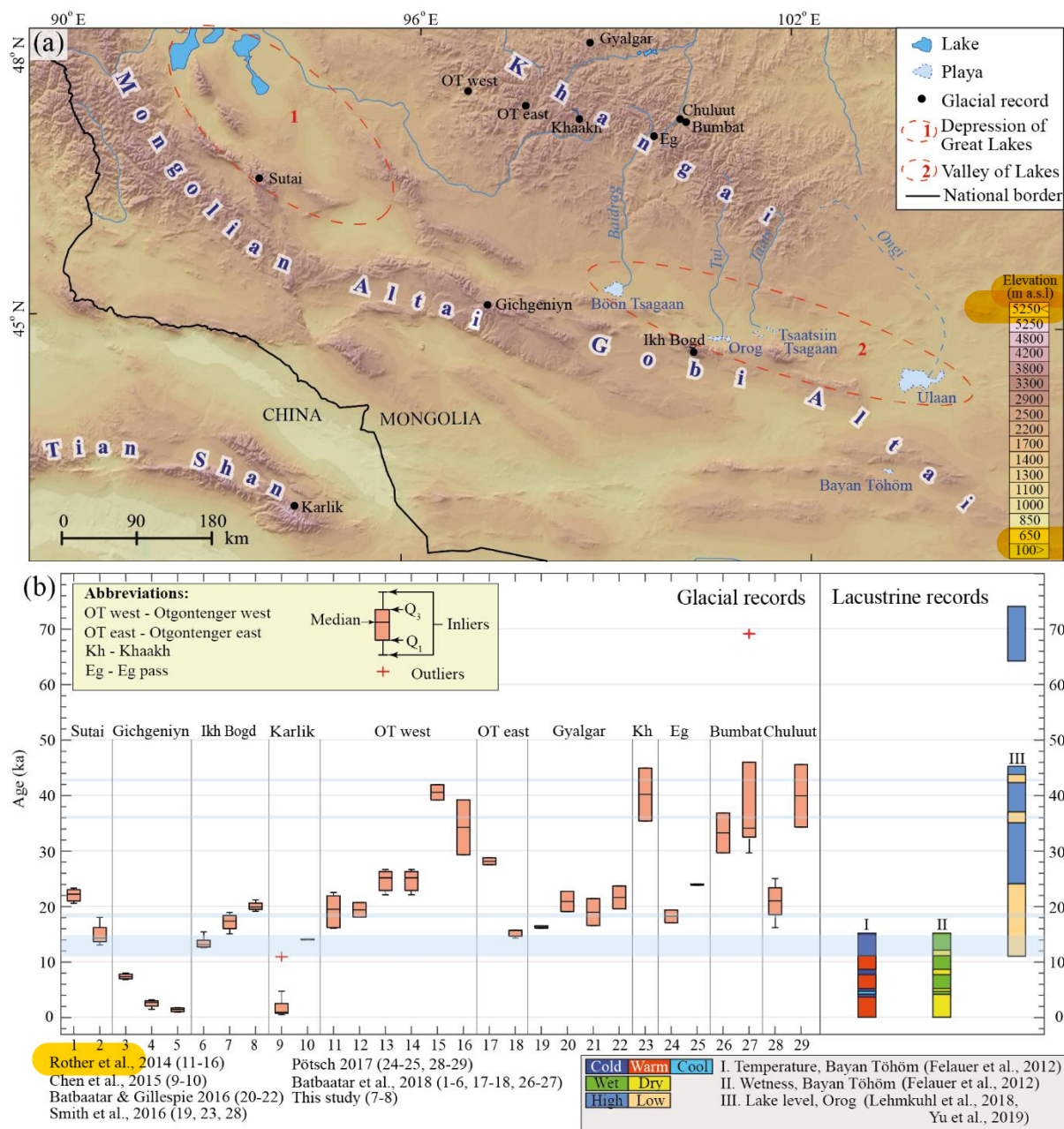
1118 **Fig. 7.** Kernel density plot (KDP) of estimated ^{10}Be exposure ages from distal moraine crests in Jargalant and Ikh
 1119 Artsan valleys. Plots were created using IceTEA Matlab code by Jones et al. (2019). (a) KDP of exposure ages of the
 1120 most extensive moraine sequence (M_{IA1}) in Ikh Artsan valley. No outlier was detected. The arithmetic mean was
 1121 calculated and marked as a bold solid vertical line. (b) KDP of exposure ages from the oldest (M_{J1}) moraine sequence
 1122 in Jargalant valley. The outlier was excluded by Chauvenet, Pierce, and the standardized deviation method in the 1
 1123 sigma range. The thick solid lines represent the cumulative density curve, the dashed red line shows excluded outlier,
 1124 and solid, narrow black lines show individual density curves for each sample. The range of total uncertainty of the
 1125 group is marked as two vertical dashed lines. The sample statistics were calculated after rejecting outliers, while
 1126 internal errors were used to create KDP and calculate sample statistics.



1127

1128 **Fig. 8.** Asymmetric distribution of potential clear-sky direct solar radiation, glacial melt, and vegetation on the south-
 1129 and north-facing slopes. (a) Location map of Ikh Bogd and lake Terkhiin Tsagaan. (b, c) Tree distribution on north-
 1130 facing slope, north of lake Terkhiin Tsagaan (© Google Earth 2022; photo taken by authors). (d) Anomaly of total
 1131 clear-sky direct solar radiation of June solstice in 20 ka from modern value. (e) Integrated total summer insolation for
 1132 22-16 ka. The purple line represents profile along midline in Ikh Artsan and Jargalant valley. Integrated total melt was
 1133 calculated in Ikh Artsan as 86.3 m and 79.8 m in Ikh Artsan valley for 22-26 ka at the same temperature. (f) Integrated
 1134 total melt calculation for Ikh Artsan and Jargalant valley considering average summer temperature in Jargalant is 0.5
 1135 lower than that in Ikh Artsan.

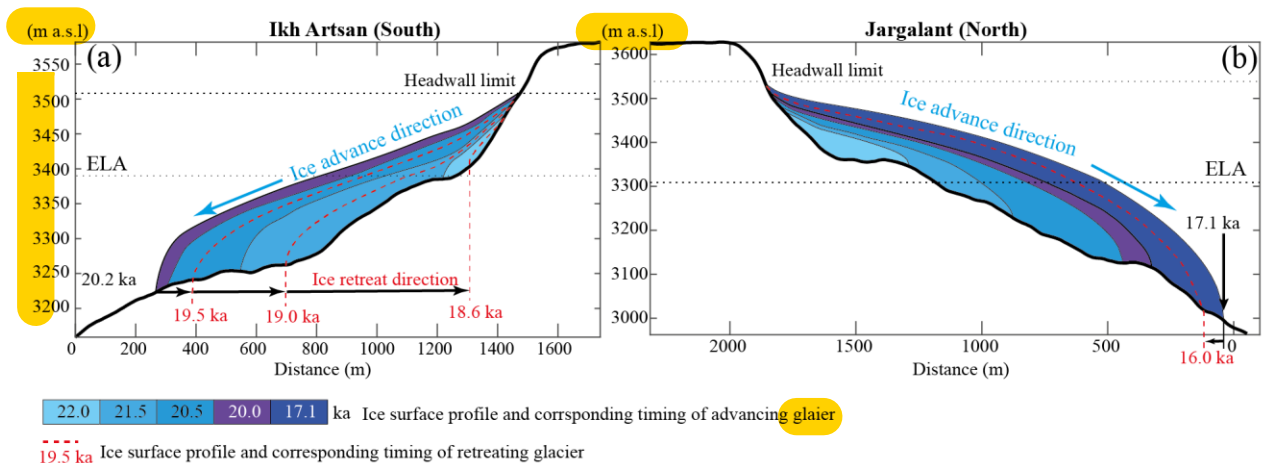
1136



1137

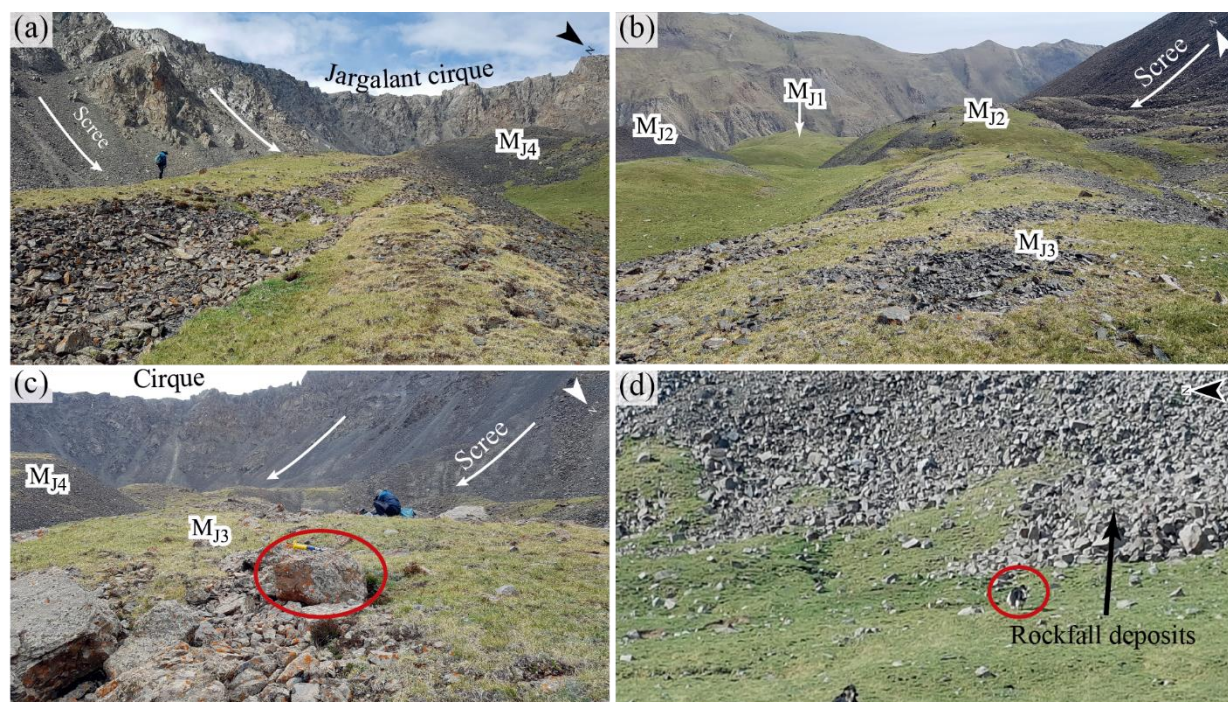
1138 **Fig. 9.** Temporal and spatial distributions of glacial and paleo-lacustrine records in the neighboring regions of Ikh
 1139 Bogd massif. (a) Locations of the ^{10}Be age dating sites for paleoglaciers and paleo lacustrine proxies. (b) Age dating
 1140 results from glaciers and lacustrine proxies. Glacial records on the left are the ^{10}Be exposure age dating results
 1141 representing 29 individual moraine groups. Exposure ages were recalculated with Cronus Earth V3, using the LSDn
 1142 scaling factor (Lifton et al., 2014). Only effective ages were plotted after outlier rejection using the Chauvenet, Peirce,
 1143 and normalized deviation method. On each box, central mark indicates the median, and the bottom and top edges of
 1144 the box indicate the 25th (Q_1) and 75th (Q_3) percentiles, respectively. The whiskers extend only to the data points
 1145 considered inliers, and the additional outliers were detected from the effective ages and plotted individually using the
 1146 '+' marker symbol. The shaded light blue sections on the age interval present the major harsh periods (playa phase of
 1147 Orog, Yu et al., 2019). Lacustrine records on the right present temperature (I) and wetness data (II) in lake Bayan
 1148 Töhöm and lake level record of lake Orog (III).

1149



1150

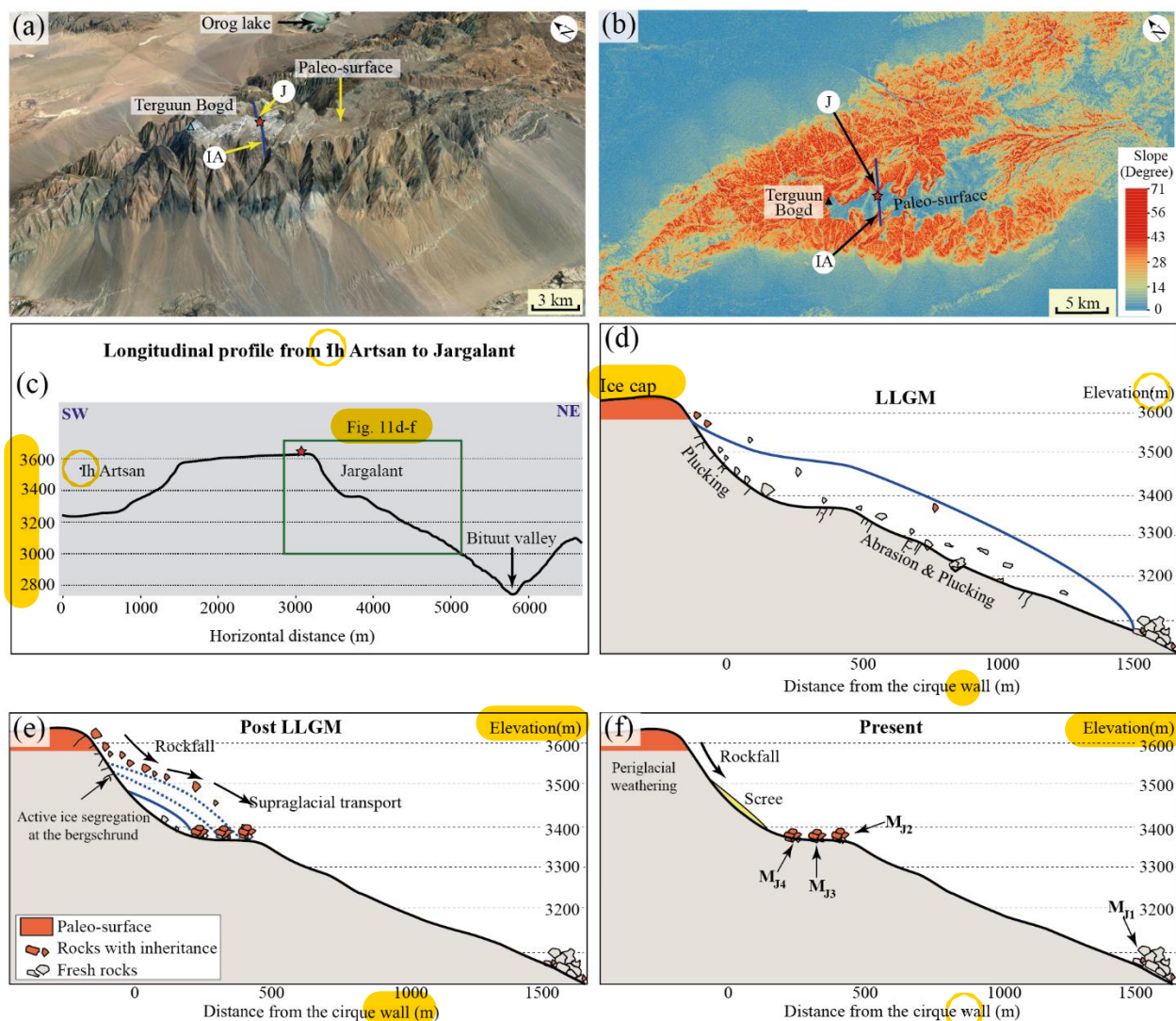
1151 **Fig. 10.** Asynchronous advance and retreat pattern of Ikh Bogd paleoglacier during 22-16 ka. (a) Paleoglacier in Ikh
 1152 Artsan valley advanced between 22.0 and 20.2 ka and retreated from 20.2 to 18.6 ka. (b) Paleoglacier in Jargalant
 1153 valley most expanded downvalley between 22.0 and 17.1 ka. Small retreat is observed during 17.1-16.0 ka. The
 1154 present-day summer temperature in the north-facing valley was considered 0.5 °C lower than in the south-facing valley.
 1155 The present-day temperature is calibrated to Greenland (NGRIP) paleotemperature data (Buizert et al., 2018) using
 1156 an LGM summer temperature anomaly of -5.5 °C. Headwall altitudes of the LGM paleoglaciers were used to mark
 1157 the maximum thickness of the glacier.



1158

1159 **Fig. 11.** Rockfall deposits in Jargalant valley. The scree or talus cone was on the cirque wall. M_{J4} , M_{J3} , and M_{J2}
 1160 moraine formed within a Jargalant cirque, consequently outer edges of moraine ridges near the cirque wall were
 1161 covered with talus deposit. (a) Rockfall deposit on the southeastern cirque wall, near M_{J4} moraine. (b) Scree covering
 1162 on M_{J2} moraine that is dissected by an intermittent stream. (c) Sampling site of M_{J3} moraine and scree on the southern
 1163 and southwestern wall of the cirque, near M_{J4} , M_{J3} moraine. JAM010 was taken from the circled boulder. Chisel, for
 1164 scale, is on the boulder. (d) Rockfall deposit on the eastern slope of the cirque. Yak (circled) is for scale.

1165



1166

1167 **Fig. 12.** Inheritance from the uplifted paleo-surface of Ikh Bogd massif. (a) 3D view of the paleo-planation surface
 1168 (© Google Earth, 2022). (b) Slope map of Ikh Bogd, location of the Ikh Artsan (IA) and Jargalant (J) valley. The
 1169 green triangle represents the highest peak of the massif, Terguun Bogd. Exposure age and erosion rate (Table 2) were
 1170 calculated using the highest concentration of the boulder from M_{J4}-M_{J2} (Fig. 11a) for the point location marked as red star
 1171 (Fig. 11b; 3625 m). (c) Longitudinal profile along a dark blue line (See Fig. 11b) connecting Ikh Artsan and
 1172 Jargalant valley from SW to NE. (d) LGM (Local LGM ~17 ka) glacial extent. Plucking of fresh rocks was intensive
 1173 due to glacial length and thickness. (e) Enhanced supply of highly inherited rocks into M_{J4}, M_{J3}, and M_{J2}
 1174 moraine series which are formed by successive glacial advances or/and stagnation. According to a shortage of glacier
 1175 length, low number of fresh rocks are plucked out. Thinned glacier allows intensive ice segregation along the
 1176 bergschrund and more inherited rockfalls into the ice surface. Hence, boulder supply with inheritance of paleo
 1177 surface would increase. (f) Present-day rockfall deposit without supraglacial transport.