Exploring the Use of Multi-source High-Resolution Satellite Data for Snow Water Equivalent Reconstruction over Mountainous Catchments

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Abstract. The hydrological cycle is strongly influenced by the accumulation and melting of seasonal snow. For this reason, mountains are often claimed to be the "water towers" of the world. In this context, a key variable is the snow water equivalent (SWE). However, the complex processes of snow accumulation, redistribution, and ablation make its quantification and prediction very challenging. In this work, we explore the use of multi-source data to reconstruct SWE at a high spatial resolution (HR) of 25 m. To this purpose, we propose a novel approach based on i) in-situ snow ~~precipitation data and Synthetic Aperture Radar (SAR) images to determine the pixel state, i.e. whether it is undergoing an SWE increase (accumulation) or decrease (ablation), ii) a daily HR time-series of snow cover area (SCA) maps derived by high- and low-resolution multispectral optical satellite images to define the days of snow presence, and iii) a degree-day model driven by in-situ temperature to determine the potential melting. Given the typical high spatial heterogeneity of snow in mountainous areas, the use of HR images represents an important novelty that allows us to sample its distribution more adequately, thus resulting in highly detailed spatialized information. The proposed SWE reconstruction approach also foresees a novel SCA time-series regularization technique that models impossible The hydrological cycle is strongly influenced by the accumulation and melting of seasonal snow. For this reason, mountains are often claimed to be the "water towers" of the world. In this context, a key variable is the snow water equivalent (SWE). However, the complex processes of snow accumulation, redistribution, and ablation make its quantification and prediction very challenging. In this work, we explore the use of multi-source data to reconstruct SWE at a high spatial resolution (HR) of 25 m. To this purpose, we propose a novel approach based on i) in-situ snow precipitation data~~ depth/SWE and temperature data, and Synthetic Aperture Radar (SAR) images to determine the pixel state, i.e. whether it is undergoing an SWE increase (accumulation) or decrease (ablation), ii) a daily HR time-series of snow cover area (SCA) maps derived by high- and low-resolution multispectral optical satellite images to define the days of snow presence, and iii) a degree-day model driven by in-situ temperature to determine the potential melting. Given the typical high spatial heterogeneity of snow in mountainous areas, the use of HR images represents an important novelty that allows us to sample its distribution more adequately, thus resulting in highly detailed spatialized information. The proposed SWE reconstruction approach also foresees a novel SCA time-series regularization technique that models impossible transitions based on the pixel state, i.e. the erroneous

change of the pixel class from snow to snow-free when it is expected to be in accumulation or equilibrium and, vice versa, from snow-free to snow when it is expected to be in ablation or equilibrium. Furthermore, it reconstructs the SWE for the entire hydrological season, including late snowfalls. The approach does not require spatialized precipitation information as input, which is usually affected by uncertainty. The method provided good results in two different test catchments: the South Fork of the San Joaquin River, California, and the Schnals catchment, Italy. It obtained good agreement both when evaluated against HR spatialized reference maps (showing an average bias of -22 mm~~) and against manual measurements (showing an average bias of -5 mm) . The main sources of error are discussed to provide insights into the main advantages and disadvantages of the method that may be of interest for several hydrological and ecological applications.transitions based on the pixel state, i.e. the erroneous change of the pixel class from snow to snow-free when it is expected to be in accumulation or equilibrium and , vice versa, from snow-free to snow when it is expected to be in ablation or equilibrium. Furthermore, it reconstructs the SWE for the entire hydrological season, including late snowfalls. The approach does not require spatialized precipitation information as input, which is usually affected by uncertainty. The method provided good results in two different test catchments: the South Fork of the San Joaquin River, California, and the Schnals catchment, Italy. It obtained good agreement both when evaluated against HR spatialized reference maps~~ , a root mean square error (RMSE) of 212 mm, and a correlation of 0.74), against a daily dataset at coarser resolution (showing an average bias of ~~-22 mm~~-44 mm, an RMSE of 127 mm, and a correlation of 0.66) and against manual measurements (showing an average bias of -5 mm, an RMSE of 191 mm, and a correlation of 0.35). The main sources of error are discussed to provide insights into the main advantages and disadvantages of the method that may be of interest for several hydrological and ecological applications.

1 Introduction

Seasonal snow accumulation and melt are crucial for the hydrological cycle and the total water supply. Mountains are claimed to be "the water towers of the world" given the large impact of snow on local and global water resources (Immerzeel et al., 2020). The contribution of snow-dominated catchments to streamflow ranges from 40% of total flow to sometimes more than 95%, depending on the region (Viviroli et al., 2003). Therefore, it is essential to estimate the amount of water stored during winter to forecast river discharge and to correctly plan human activities such as agriculture irrigation, drinking water supply, and hydropower production (DeWalle and Rango, 2008; Beniston et al., 2018). In mountain regions, the snow distribution is highly variable in space and time due to redistribution processes (Balk and Elder, 2000), thus limiting the effectiveness of available in-situ measurements. Especially in remote areas, continuous and spatialized observations are rare (Rees, 2005). Hence, remote sensing (RS) represents a valuable tool for snow hydrology.

A correct spatial characterization of snow properties requires both knowledge about the extent of the snow cover, i.e., the snow cover area (SCA), and appropriate snowpack information. A key variable is the snow water equivalent (SWE), i.e., the total amount of water stored in the snowpack released upon complete melting. Although a long list of SCA detection methods that exploit multispectral optical satellites is available in the literature (e.g., Dietz et al., 2012; Dong, 2018), we do not have

operational methods to directly map SWE with high spatial resolution (HR). Direct SWE observations are limited to point measurements by manual sampling, snow scales or snow pillows (Archer and Stewart, 1995; Meløysund et al., 2007), or with a limited spatial footprint (~ 500 m) such as cosmic ray neutron probes (Schattan et al., 2019). Spatialized snow depth (SD)

60   information can be provided by differential lidar altimetry (Painter et al., 2016) or stereo photogrammetry (Deschamps-Berger et al., 2020). However, these methods can be applied only to limited areas and with a low temporal sampling. Moreover, the derivation of SWE from SD requires additional a priori information to infer the snow density (Helfricht et al., 2018). Physically-based snow models represent a valid alternative (e.g., Lehning et al., 2006; Vionnet et al., 2012; Endrizzi et al., 2014) that can provide HR SWE information on large areas. Nonetheless, their accuracy is strongly limited by the uncertainty in the input

65   data (Engel et al., 2017; Günther et al., 2019) and by the gravitational and wind-induced snow redistribution processes (Jost et al., 2007; Mott et al., 2018). One of the main challenges is to obtain an accurate precipitation field given the strong spatial variability of the variable related to orography, a generally scarce sampling density of the phenomenon that strongly influences the interpolation results, and possible inaccuracies in the measurements caused, for example, by undercatching (e.g., Prein and Gobiet, 2017).

70   Passive and active microwave sensors can potentially provide information about the snowpack. In particular, the first ones are used to retrieve long time-series of SWE by exploiting the correlation between brightness temperature and SWE (Pulliainen et al., 2020). However, the observations are limited by a spatial resolution of 25 km and are not suitable for mountain regions. Active microwave sensors, such as Synthetic Aperture Radars (SARs), were investigated for HR retrieval of SWE (Ulaby et al., 1981; Shi et al., 1994; Baghdadi et al., 1997; Rott et al., 2010) and differential SWE (Guneriussen et al., 2001; Leinss et al.,

75   2015). Despite the better spatial resolution, active microwave sensors suffer from the complexity of non-linear effects introduced on the total backscattering, such as snow layering, surface roughness, snow density, grain type and size, which in turn are all affected by the complex snow metamorphism and change in time. Furthermore, all of these techniques work only in dry snow conditions, whereas the scarce penetration of the electromagnetic signal in wet conditions invalidates their applicability to monitor the evolution of the SWE during the melting season. For more details on SWE retrieval using SAR acquisitions,

80   several review articles are available (e.g., Tsang et al., 2021).

Despite recent developments, SAR is still far from providing unambiguous information on SWE in all conditions. However, it represents a promising tool to monitor the melting phases of the snowpack, i.e., the moistening, ripening, and runoff phases, or in other words, the presence and evolution of liquid water inside the snowpack (Marin et al., 2020). ~~When combined with~~

85   ~~optical data~~If the snow regime presents distinct ablation and accumulation periods, the onset of runoff (i.e., when the SWE reaches its maximum) derived by SAR adds value to the snow depletion curve (SDC) when combined with optical data. The SDC is a function that describes the relationship between SCA and SD or SWE (Cline et al., 1998). Thus, time-series of SCA can be used to provide an indirect measurement of SWE (Yang et al., 2022). SWE is a function of the duration of the snow cover, which intrinsically considers the energy exchanges responsible for the melting process (Durand et al., 2008). For

90   example, shallow snowpacks and high melt rates are associated with an SDC having a high derivative, while deep snowpacks and low melt rates are characterized by a longer curve (e.g., Pimentel et al., 2015, 2017). Consequently, spatial accumulation

and ablation variabilities, which are related to the topography of the study area (Anderton et al., 2002), result in different persistence of the snowpack (Luce et al., 1998). Therefore, knowing the SDC and the SWE maximum at the end of the accumulation for a catchment allows deriving the evolution of SWE during melting. This intuitive idea opens the possibility of assimilating SCA and SDC information into physically-based snow models to correct SWE evolution and improve simulations (Arsenault and Houser, 2018).

Similarly, SDC can be exploited in combination with distributed snowmelt models to reconstruct SWE time-series in reanalysis (Martinec and Rango, 1981; Molotch and Margulis, 2008; Rittger et al., 2016). Unlike the methods that require known precipitations and meteorological forces to redistribute the snowpack during the accumulation, SWE reconstruction builds the SWE time-series backward from the last day of snow presence up to the peak of accumulation. To this purpose, these approaches exploit the estimation of the potential melt energy and the knowledge about the presence of snow cover, thus simplifying the solution of the problem. The SWE reconstruction approaches show good performance showed good performances over large basins and even mountain ranges , outperforming the accuracy provided by snow models or spatial interpolation approaches of in-situ SWE measurements (Bair et al., 2016). Nevertheless, the accuracy of the results depends on a robust estimation of both the potential melting and SCA. For the first one, several methods were proposed that range from a simple yet robust degree-day (DD) model (Martinec and Rango, 1981) to a complete radiation energy computation that also takes into account the snow albedo (Bair et al., 2016). To estimate SCA, many works presented in the literature exploit low-resolution (LR) multispectral satellite images, since their large swath allows a high repetition time, i.e., with a daily or sub-daily acquisition. This mitigates cloud obstruction issues and involves a proper SCA sampling. However, LR images do not provide sufficient spatial detail on the variability of the snow cover evolution in the mountains, which is on the order of a few dozen meters. Moreover, the use of LR images results in a non-linear combination of the different contributions of the elements within the pixel, and this may induce large errors in the snow classification approaches, especially in complex terrains. On the other hand, the use of HR snow maps introduces important benefits in both determining SWE and forecasting streamflow (Molotch and Margulis, 2008; Li et al., 2019). Landsat products were used to retrieve SCA in many papers in the literature (e.g., Molotch et al., 2004; Molotch and Bales, 2005, 2006). However, a Landsat satellite acquires an image every 16 days (at the equator). With the introduction of the Copernicus Sentinel-2 (S2) mission, HR images are made available with an improved temporal resolution of 5 days (at the equator). This opens up new opportunities to monitor heterogeneous snow conditions in the mountains. Unfortunately, due to cloud coverage, useful acquisitions are reduced by 50% in the Alps (Parajka and Blöschl, 2006). Therefore, even if the Landsat images are exploited together with the S2 images, only a few acquisitions are available per month. Recently, we proposed an approach to the reconstruction of daily HR snow cover maps. The approach performs a gap-filling and a downscaling of the snow cover fraction (SCF) maps derived at LR based on the idea that the melting and accumulation patterns repeat interannually (Premier et al., 2021; Revuelto et al., 2021). Therefore, by observing partial HR or LR acquisitions it is possible to reconstruct a daily HR snow cover.

This work explores the use of multi-source satellite data to reconstruct HR daily SWE time-series at a spatial resolution of 25 m. To achieve such detail, we propose as main novelties the use of a daily HR SCA time-series together with accurate

information on the melting phase from SAR data. To this purpose, we also introduce the concept of the snow state of a pixel, which represents the direction of the change in SWE for that pixel, that is, *accumulation* (SWE increase), *ablation* (SWE decrease) or *equilibrium* (constant SWE). This allows reconstructing SWE without the need for spatialized precipitation data.

130 Indeed, the method redistributes the amount of melting by exploiting the information about the state rather than quantifying the precipitation input. Moreover, the state allows us to set up a novel regularization of the SCA time-series. In the paper, we also present a critical analysis of the main sources of error to provide insights into the main advantages and disadvantages of the method that may be of great interest for several hydrological and ecological applications. We explore the applicability of the method to two mountainous catchments: i) the South Fork of the San Joaquin River (SFSJR), located in the Sierra Nevada

135 - California (USA), and ii) the Schnals catchment, located in the Alps - South Tyrol (Italy).

The paper is structured into five sections. Sec. 2 presents the different steps of the proposed approach to reconstruct the daily HR SWE. The two test sites considered for experimental validation and the related dataset are presented in Sec. 3. The results obtained are illustrated in Sec. 4. In Sec. 5, we discuss the main sources of errors of the method and the novel SCA

140 regularization. Finally, Sec. 6 draws the conclusions of the work and gives indications for further exploitation of the proposed approach.

2 Proposed approach to HR SWE reconstruction

The presented approach is made up of three main parts: i) identification of the state, ii) characterization of the snow season from the regularized SCA time-series, and iii) calculation of the SWE. The details will be illustrated in the following three sub-

145 sections. As depicted in Fig. 1, the method starts with the identification of the state, i.e., accumulation, ablation or equilibrium (see Sec. 2.1). The state information is used first in this step both to regularize the SCA time-series taking into account impossible transitions and to correctly determine the beginning and end of the season (see Sec. 2.2). With impossible transitions, we indicate an erroneous change of the pixel class from *snow* to *snow-free* when the state is *accumulation* or *equilibrium*, or vice versa, the change from *snow-free* to *snow* when the state is ablation or equilibrium. The regularized time-series of SCA is then

150 used with the potential melting to reconstruct the daily HR SWE maps (see Sec. 2.3). The state information is used again in this step i) to redistribute the total amount of SWE calculated for the melting in the accumulation period, and ii) to include late snowfalls that occur after the peak of accumulation to the reconstruction. Both cases are generally omitted in state-of-the-art SWE reconstruction methods (e.g., Martinec and Rango, 1981; Molotch and Margulis, 2008).

2.1 Identification of the state

155 ~~Let us introduce the three states that~~ Three states are introduced to describe possible SWE changes within a pixel, i.e., ΔSWE between two times $t-1$ and t. As illustrated in Table 1, the states are: i) *accumulation* which represents an increase in SWE (ΔSWE > 0), ii) *ablation* which represents a reduction in SWE (ΔSWE < 0), and iii) *equilibrium* which represents a stable SWE (ΔSWE $= 0$).

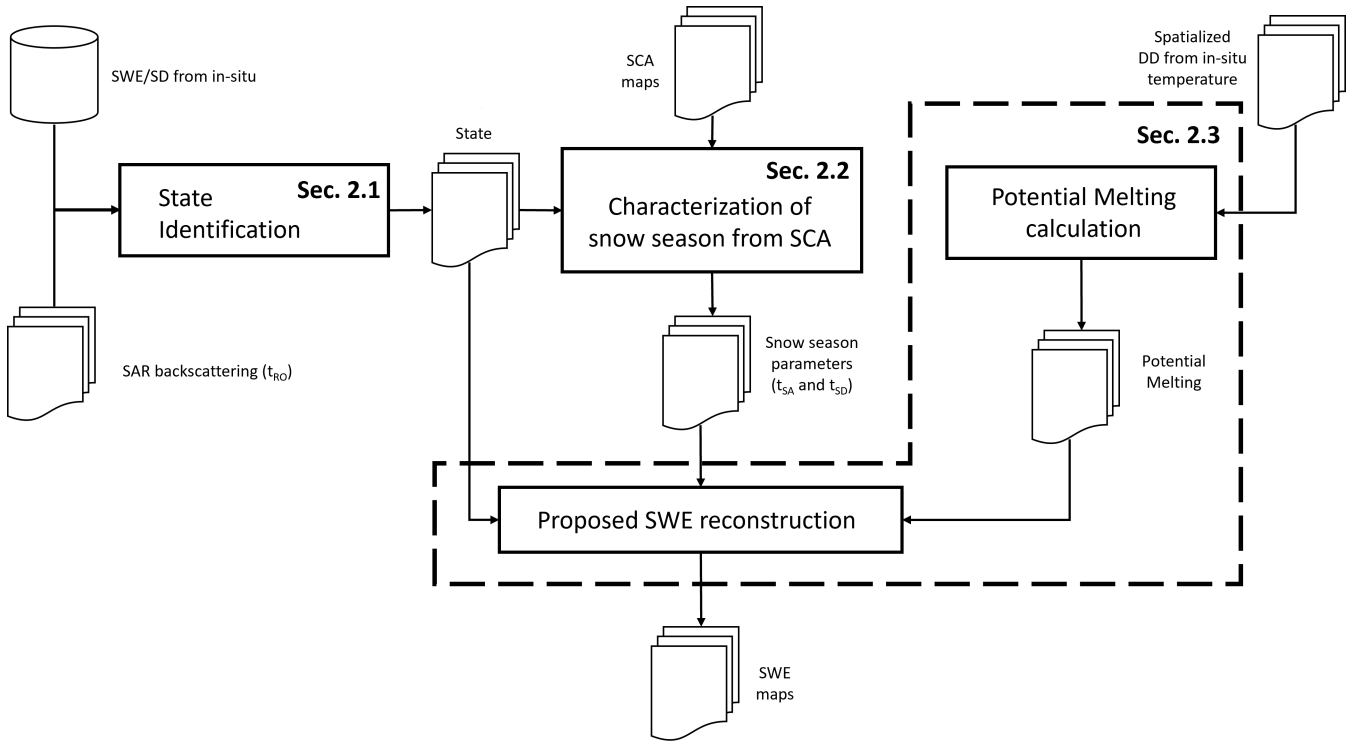



Figure 1. Workflow of the proposed approach showing the three main steps: i) state identification, ii) characterization of snow season from SCA, and iii) SWE reconstruction. The inputs are: i) SWE or SD from automatic weather stations (AWSs), ii) SAR backscattering time-series, iii) a daily HR SCA time-series, and iv) daily spatialized potential melting maps derived from AWSs. As output, we obtain the daily HR SWE maps.

Table 1. Definition of the three possible states: *accumulation*, *ablation* and *equilibrium*. The possible class transitions at pixel level associated with the state are described.

State	ΔSWE	Class transition t-1	t	Description
Accumulation	>0	■	□	Snow on bare ground
		□	□	Snow on snow
Ablation	<0	□	■	Snowpack disappearance
		□	□	Snowpack reduction
Equilibrium	=0	□	□	Stable snowpack
		■	■	Bare ground

Legend: □ = snow ■ = snow-free

The phenomena that cause an SWE variation are several, such as snowfall, melting, sublimation, human activities, or redistribution due to wind or gravitational transport, e.g., avalanches. However, we refer mainly to snowfalls if *accumulation* and to melting if *ablation*. Indeed, we propose to estimate the SWE to be added to the reconstruction by considering a quantity proportional to the snow depth/SWE ~~variations~~daily increment. Thus, in an ideal case, we include only fresh snow as the main driver. Similarly, the amount of SWE to be subtracted is calculated using a DD model and, therefore, it only represents ~~melted snow~~melting. Trivially, SWE remains constant when *equilibrium*. Note that the state is defined on a daily scale, which corresponds to the temporal resolution of the exploited HR SCA time-series. In this work, the diurnal fluctuations in meteorological forces are not considered.

The state varies pixel-wise due to the topography and meteorology of the study area. However, it is difficult to extrapolate this information with the necessary spatial detail. In the following paragraphs, we propose simplified strategies for the *accumulation* and *ablation* determination. If none of them is identified, the state is *equilibrium*.

2.1.1 Accumulation identification

The *accumulation* identification can be retrieved from a network of automatic weather stations (AWSs) that provide continuous information about the occurrence and elevation of snowfall events, for example, direct SWE measurements or indirect precipitation/SD measurements. ~~Although continuous~~ Continuous SWE measurements are ~~scarcely available, using~~ unfortunately scarcely available. By mean pluviometers and temperature observations, it is possible to split precipitation between liquid and solid (Mair et al., 2013) and identify the state accordingly. However, these stations are rarely installed at high elevations. SD sensors are more suitable for our purpose, but their observations are often affected by wind and gravitational transport, leading to deposition/removal that can be falsely interpreted as *accumulation*/*ablation*. Hence, even if the AWSs are generally situated in locations undisturbed from the wind action, it is more convenient to dispose of a large number of AWSs that need to be filtered to exclude possible sensor errors or wind/gravitational redistribution. ~~For these reasons, the increase in SWE/SD should be greater than a certain threshold SD_{min}/SWE_{min} that is fixed at 2 cm for SD according to the values found in the literature (Engel et al., 2017), resulting in a value of 2 mm for SWE when considering the typical density of fresh snow (100 kg/m³).~~

~~It is important to note that a station is~~ In fact, a station is usually representative of a limited area whose extension is highly variable depending on the complexity of the terrain. In the case of a well-monitored area with stations distributed with elevation, it is possible to divide the catchment into different elevation belts where the snowfall events can be considered nearly homogeneous. However, in many basins, this might be far from reality. As a common configuration for snow monitoring, we have a single station located at a high point of the catchment, which is informative enough to identify the accumulation events but not their extent. Furthermore, it has been shown in the literature that estimating the snowfall limit can be very challenging (e.g., Fehlmann et al., 2018). ~~In a poorly monitored catchment,~~

Therefore, the method can be adapted based on the availability of the in-situ observations. In this study, we made use of SWE and snow depth measurements, since they were available in our analyzed basins. To consider that a snowfall is occurring, the

increase in SWE/SD should be greater than a certain threshold SD_{min}/SWE_{min} that is fixed at 2 cm for SD according to the values found in the literature (Engel et al., 2017), resulting in a value of 2 mm for SWE when considering the typical density of fresh snow (100 kg/m^3). Unfortunately, the basins are poorly monitored in terms of these variables and consequently, the snowfall limit cannot be estimated in an appropriate manner. Hence, we consider that snowfalls occur throughout the snow-covered area of the catchment. We acknowledge that this assumption may result in less accurate SWE estimation, especially in the case of mixed states. For example, snowfall can be observed at high elevations, together with rain-on-snow at low elevations, causing snowmelt. However, we assume that the effect of these events on the total SWE balance is small enough to be considered negligible as we will discuss in Sec. 5.2.

In summary, when the AWSs show an increment greater than a defined threshold, we identify the state as *accumulation*.

2.1.2 Ablation identification

The ablation can be identified by using a snowmelt model. We consider here the simple temperature index model, which is an empirical model that ~~takes advantage of the intuitive concept that air temperature is~~ makes use of air temperature as a proxy of ~~melting~~the melting (Ohmura, 2001). When the temperature exceeds a fixed threshold, we expect that the pixel melts. However, this is a simplified approach that does not consider all the components that contribute to snowmelt. More complex formulations include estimates of radiation, sensible heat, latent heat, and ground heat fluxes (e.g., Ismail et al., 2023). Moreover, temperature observations may be sparse, thus affecting the accuracy of the spatialization.

Multi-temporal SAR observations derived from Sentinel-1 (S1) can detect the presence of a melting snowpack, as explained by Marin et al. (2020). The authors investigated the relationship between the SAR backscattering and the three melting phases, i.e., the moistening, ripening, and runoff phase. In detail, they showed that if the SAR backscattering presents a decrease of at least 2 dB, the snowpack gets moistened (Nagler and Rott, 2000). Initially, at the beginning of the moistening phase this decrease affects only the afternoon measurements. When it also affects the morning measures, the ripening phase starts. Finally, the backscattering increases as soon as the SWE starts to decrease, which corresponds to the beginning of the runoff phase. This moment represents the first contribution of the snowpack to the release of water. Empirical experiments on five selected test sites showed that the melting phases were identified with an RMSE of 6 days for the moistening phase, 4 days for the ripening phase, and 7 days for the runoff phase.

The multi-temporal analysis of the SAR backscattering represents a novel way to identify the ongoing melting in a spatialized manner. The runoff onset (t_{RO}) represents the time when the snowpack is isothermal. In this way, information about the cold content of the snowpack is incorporated into the DD model excluding incorrect early melting. However, the methodology presented by Marin et al. (2020) may fail in areas such as forests. ~~For this reason,~~ As shown by (Darychuk et al., 2023), the characteristic "U-shape" signature of the backscattering signal is less evident in mature forest, also depending on canopy structure, composition and density. The signal can be noisier due to the scattered contribution by canopy. Hence, we propose applying the method only ~~if a pixel presents the characteristic~~ for pixels that present a clear "U-shape" ~~signature of the backscatteringsignal~~backscattering, which can be also present for forested areas. To this purpose, we apply a multi-temporal

analysis to the different available S-1 tracks. First, we identify if a drop of at least -2B is present in the time-series. Second, the minimum is selected after this drop. When more tracks are available, we set the first minimum as the beginning of the runoff. Therefore, we propose to consider in *ablation* a pixel for the entire period ranging from the backscattering minimum to the disappearance of the snow cover identified by optical-derived time series. For the pixels that do not present the characteristic "U-shape", we rely on the DD model for the identification of the melting state.

In summary, we propose identifying the state of *ablation* for a specific date and a single pixel if the following conditions are met: i) there is no *accumulation* on the date in question, ii) the SAR backscattering shows an increase after a relevant drop of at least -2dB, indicating that the minimum value corresponding to t_{RO} has been reached, and iii) the degree day (as shown in Eq. 2) is greater than 0.

2.2 Characterization of the snow season from regularized SCA time-series

A necessary input for the proposed SWE retrieval is a daily HR SCA time-series, or in other words, the date of snow appearance t_{SA} and disappearance t_{SD}. As mentioned in the Introduction, such a product is not available directly from remotely sensed images due to limitations in the revisit time and cloud obstruction. Therefore, it is necessary to reconstruct it. Among the various methods present in the literature, we use the approach proposed by Premier et al. (2021), which merges information coming from a sparse long HR time-series and a continuous daily LR time-series acquired in the period of interest. Gap-filling and downscaling steps are performed by applying a set of hierarchical rules based on historical analyzes and topographical features. The main idea behind the approach is that snow patterns persist over time and follow a regular distribution that is strongly dependent on the topography and meteorology of the area of interest (Mendoza et al., 2020). We refer the reader to Premier et al. (2021) for details.

Despite the generally accurate results of the above-mentioned approach (the overall accuracy is empirically estimated to be around 92%), the HR SCA output is still affected by possible inconsistencies. Errors may arise either from the classification algorithm applied to the multispectral input images or from the reconstruction approach. In detail, we can highlight the presence of two main sources of errors: i) an underestimation of snow presence in forested areas when the snow falls below the canopy and thus is not visible from the satellite point of view (i.e., snow on the ground), and ii) the missed identification of snow-patches at the end of the season. The first error source is due to the fact that the classification methods used for snow retrieval for both HR and LR images rely only on the spectral information measured inside the resolution cell of the sensor without a dedicated module for inferring the presence of snow when hidden by the canopy. This affects the detection of snow on the ground, particularly for HR images, since the small resolution cell is likely to contain a majority fraction of the canopy, especially over very dense forests. This problem is instead mitigated for LR pixels that are likely to contain not only forested areas but also open fields where the snow is visible, increasing in this way the possibility of detecting the snow presence. Therefore, it is possible to observe local decreases in SCA mainly in correspondence with an HR acquisition. The second error involves mostly LR images whose spatial detail is not enough to detect mixed pixels with low SCF. This is an error that

persists over time since LR acquisitions are more frequent than HR acquisitions, while a local increase of SCA is shown in correspondence with an HR acquisition.

The state concept introduced in Sec. 2.1 can be used to regularize the SCA. According to Table 1, only transitions of the pixel class that are coherent with the state are allowed. When *accumulation* the pixel can only turn from *snow-free* to *snow* if snow falls on bare ground, or it can continue to be *snow* if snow falls on already deposited snow. Similarly, when *ablation* the pixel can only turn from *snow* to *snow-free* if the snow cover disappears, or it can remain *snow* if the snow cover partially melts. Finally, when *equilibrium* the pixel continues to be *snow* or *snow-free* depending on the situation. Therefore, we can define the impossible transitions: i) a pixel cannot turn from *snow* to *snow-free* from $t-1$ to t if *accumulation* or *equilibrium*, and ii) a pixel cannot turn from *snow-free* to *snow* from $t-1$ to t if *ablation* or *equilibrium*.

When facing a wrong transition, we do not know a priori whether the correct label is the one at $t-1$ or the one at t. To derive the correct interpretation, we consider an appropriate time window and compute the most frequent label according to the majority rule. The time window is chosen differently in the case where we are facing a recent or an old date of snow appearance t_{SA}. In detail, for a given pixel, we consider:

- a *recent date of snow appearance* when $t-t_{SA} < 10$ days. In this period, we often observe missed detection of snow under the canopy, especially by HR sensors. Under this condition, we do not expect fast changes, since the temperatures are likely to be low, and thus the potential melting is low (see Eq. 1). Consequently, we propose to consider a daily time window of ± 5 days from t to check what is the most persistent label of the considered pixel (Parajka and Blöschl, 2006);

- an *old date of snow appearance* when $t-t_{SA} > 10$ days. If the final melting has already started, changes may be quick, and the most common situation is the missed detection of mixed pixels as snow patches. We observe that in this period HR sensors detect snow patches that are completely omitted by LR sensors. In this case: i) the dates after t are not informative since the snow patches disappear quickly, and ii) daily SCA may not be informative when derived from LR. For this reason, we consider only the last up to five dates when an HR was originally acquired in a time window between t_{SA} and t.

Once we determine the state and whether we are handling a recent or old t_{SA}, we can compute the most frequent label in the considered time window and apply the following correction (see Algorithm 1). The correction is performed by advancing forward in time, i.e., we assume that the previous labels are always coherent with the previous states. If we are in *accumulation* or *equilibrium*, a transition from *snow* to *snow-free* is not allowed. If the pixel is labeled *snow* in $t-1$, then it means that, for the sake of coherence, it turned into *snow* in t_{SA}. We also know the date of the most recent ablation t_{lastAB}, i.e., the last chance that the pixel had to become *snow-free*. Therefore, we compute the most frequent label accordingly with the majority rule described in the previous paragraph, which varies depending on whether the snowfall is old or recent. If i) the most frequent label is *snow*, t is replaced with *snow*; ii) the most frequent label is *snow-free*, all times starting from t_{lastAB} (or t_{SA}, $t_{lastAB} < t_{SA}$) up to $t-1$ are replaced with *snow-free*.

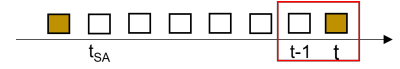
Analogously, the transition from *snow-free* to *snow* is not allowed in *ablation* or *equilibrium*. If the pixel is labeled as *snow-free* at $t-1$, it means that, for the sake of coherence, it turned to *snow-free* at t_{SD}. We also know the date of the most recent

accumulation t_{lastAC}, i.e., the last chance that the pixel had to become *snow*. Hence, we compute the most frequent label

295   accordingly with the majority rule, and if it results that i) the most frequent label is *snow-free*, t is replaced with *snow-free*; ii) the most frequent label is *snow*, all times starting from t_{lastAC} (or t_{SD}, $t_{lastAC} < t_{SD}$) up to $t-1$ are replaced with *snow*.

Algorithm 1 Regularization of the snow cover maps with the state.

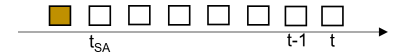
if *Accumulation or Equilibrium* **then**

    # Transition *snow* to *snow-free* is not allowed!

    # The pixel is *snow* from $t_{SA} \leq t-1$. Between t_{SA} and $t-1$ all states are possible.

    # $t_{lastAB} :=$ most recent ablation date, i.e. last chance to get *snow-free*. If $t_{lastAB} < t_{SA}$ then $t_{lastAB} = t_{SA}$

    if $t - t_{SA} < 10$ *days* **then**
        | **Recent** t_{SA}**:** check $t \pm 5$ days and compute the most frequent label
    else
        | **Old** t_{SA}**:** check last up to 5 HR from t_{SA} to t and compute the most frequent label
    end

    if *most frequent label is snow* **then**

        set t as *snow*

    else

        set $[t_{lastAB}; t-1]$ as *snow-free*

    end

if *Ablation or Equilibrium* **then**

    # Transition *snow-free* to *snow* is not allowed!

    # The pixel is *snow-free* from $t_{SD} \leq t-1$. Between t_{SD} and $t-1$ all states are possible.

    # $t_{lastAC} :=$ most recent accumulation date, i.e. last chance to get *snow*. If $t_{lastAC} < t_{SD}$ then $t_{lastAC} = t_{SD}$.

    if $t - t_{SA} < 10$ *days* **then**
        | **Recent** t_{SA}**:** check $t \pm 5$ days and compute the most frequent label
    else
        | **Old** t_{SA}**:** check last up to 5 HR from t_{SA} to t and compute the most frequent label
    end

    if *most frequent label is snow* **then**

        set $[t_{lastAC}; t-1]$ as *snow*

    else

        set $t-1$ as *snow-free*

    end

2.3 HR SWE reconstruction

Once the state is defined as described in Sec. 2.1, and the daily HR SCA time-series is regularized coherently with the state as described in Sec. 2.2, we can apply the proposed approach to HR SWE reconstruction. As illustrated in Fig. 2, this operation

300 requires calculating the total amount of melting and redistributing it during the snow season according to the preservation of mass and the state. To this purpose, we estimate the daily potential melting with the DD model. For a generic time interval $[t-1; t]$, the potential melting $M_{t-1,t}$ is estimated through the following equation:

$$M_{t-1,t} \, [mm] = a \, [mm^o C^{-1} d^{-1}] \cdot DD_{t-1,t} \, [^o Cd] \; if \; t > t_{RO} \tag{1}$$

where a is the so-called DD factor and varies depending on the area and the snow period. Note that potential melting is

305 considered only after the runoff onset as detected by S1 data. We used a value of $a = 4.5$ mm^o C^{-1}d^{-1} for the SFSJR and $a = 5.2$ mm^{o}C^{-1}d^{-1} for the Schnals catchment. The coefficient is calibrated by considering the measured SWE and temperature at the AWSs (if available) and also taking into account the range of values derived in previous literature works (Hock, 2003). $DD_{t-1,t}$ is the DD given by the cumulative sum of the hourly temperatures exceeding a certain threshold:

$$DD_{t-1,t} = \sum_{t-1}^{t} T_h \; if \; T_h > \hat{T} \tag{2}$$

310 The threshold temperature $\hat{T}$ is set to 0^oC.

The DD is first calculated for each station and then spatially interpolated using a three-dimensional universal kriging routine with linear variogram and elevation as external drift (Murphy et al., 2020). The choice arises from the results of a leave one out (LOO) cross-validation (see Appendix B). The variogram parameters are automatically calculated at each time step using a "soft" L1 norm minimization scheme. The number of averaging bins is set to 6 (default value). The kriging is performed on

315 the daily DD values instead of on the raw hourly temperature values to reduce computational times.

We can determine the total amount of melting M_{tot} by summing all daily $M_{t-1,t}$ for all those days in *ablation* within the time range $[t_{SA}; t_{SD}]$. It is worth noting that a single pixel may have more than one snow period, and hence we can have more than a couple of t_{SA}-t_{SD}. M_{tot}, which has to be equal to the total accumulation A_{tot}, is then calculated as follows:

$$A_{tot} = M_{tot} = \sum_{t=t_{SA}}^{t_{SD}} M_{t-1,t} \quad if \quad ablation \quad for \quad t \tag{3}$$

320 Consequently, it is possible to reallocate the total accumulation on days that are in *accumulation*:

$$A_{t-1,t} = k_{t-1,t} A_{tot} \quad if \quad accumulation \quad for \quad t \tag{4}$$

where $k_{t-1,t}$ is a coefficient that represents the amount of snowfall. If we have a network made by S AWSs with measured SWE (or similarly, SD), k is set proportional to the observed snowfalls:

$$k_{t-1,t} = \frac{\sum_{s=1}^{S}(SWE_t^s - SWE_{t-1}^s)}{\sum_t \sum_{s=1}^{S} S(SWE_t^s - SWE_{t-1}^s)} \quad if \quad accumulation \quad for \quad t \tag{5}$$

Note that the number of days in *accumulation* varies for each pixel, and consequently, the coefficient is a function of time and space. Thus, it is possible to determine the final output, i.e., a daily HR SWE time-series, by applying pixel-wise the following rules:

$$SWE(t) = \begin{cases} 0 & \text{if} \quad \textit{snow-free} \\ SWE(t-1) & \text{if} \quad \textit{equilibrium} \\ SWE(t-1) - M_{t-1,t} & \text{if} \quad \textit{ablation} \\ SWE(t-1) + A_{t-1,t} & \text{if} \quad \textit{accumulation} \end{cases} \quad (6)$$

It may happen that during *ablation* temperatures are low and the term $M_{t-1,t}$ is equal to 0, thus coinciding with the *equilibrium* state.

It is worth stressing the fact that although sublimation, redistribution, and gravitational transport are not explicitly taken into account in Eq. 6, their consequences are implicitly observed as a longer persistence of snow on the ground that is detectable through the use of an accurate SCA time-series. Moreover, by providing an approximation of the accumulation events, we also consider late snowfalls that can occur during the main melting season and that are a major source of error in state-of-the-art methods (Slater et al., 2013a).

3   Study Areas and Dataset Description

To assess the performance of the proposed method, we consider two different test areas. The first one is the South Fork of the San Joaquin River (SFSJR) located in California, USA, in the Sierra Nevada. For this test site, we considered three hydrological seasons that spanned from 1 October 2018 to 30 September 2021. The considered basin has an area of around 970 km^2 and a mean elevation of 3070 m, ranging from a minimum elevation of 1930 m to a maximum elevation of 4150 m. The percentage of forest area in this catchment is around 32% (Shimada et al., 2014). SWE maps with a resolution of 50 m are made available by the Airborne Snow Observatory (ASO). ASO couples an imaging spectrometer, a laser scanner, and a physical model that provides an estimate of the snow density to derive accurate SWE maps (Painter et al., 2016). The product presents an uncertainty that derives from both the snow depth retrieval (< 0.02 m at a resolution of 50 m) and the snow density modeling (13–30 kg m^{-3}). This dataset represents our main reference for this study, given its high spatial detail comparable with the proposed output. However, we consider also an additional dataset at $\sim$500 m resolution, i.e., the Western United States daily snow reanalysis (WUS–SR) product (Fang et al., 2022). A snow pillow for continuous SWE measurements and an AWS providing air temperature are available at the Volcanic Knob (VLC) station, located at an elevation of around 3050 m. Unfortunately, this is the only station within the catchment. For this reason, as explained in Sec. 2.1 we assumed that the accumulation occurs across all the snow-covered area. However, we also considered other 6 snow pillows and 10 stations with continuous temperature measurements within a radius of approximately 15 km from the catchment (see 3a). These data were downloaded from the United States Department of Agriculture (USDA) Natural Resources Conservation Service (NRCS)

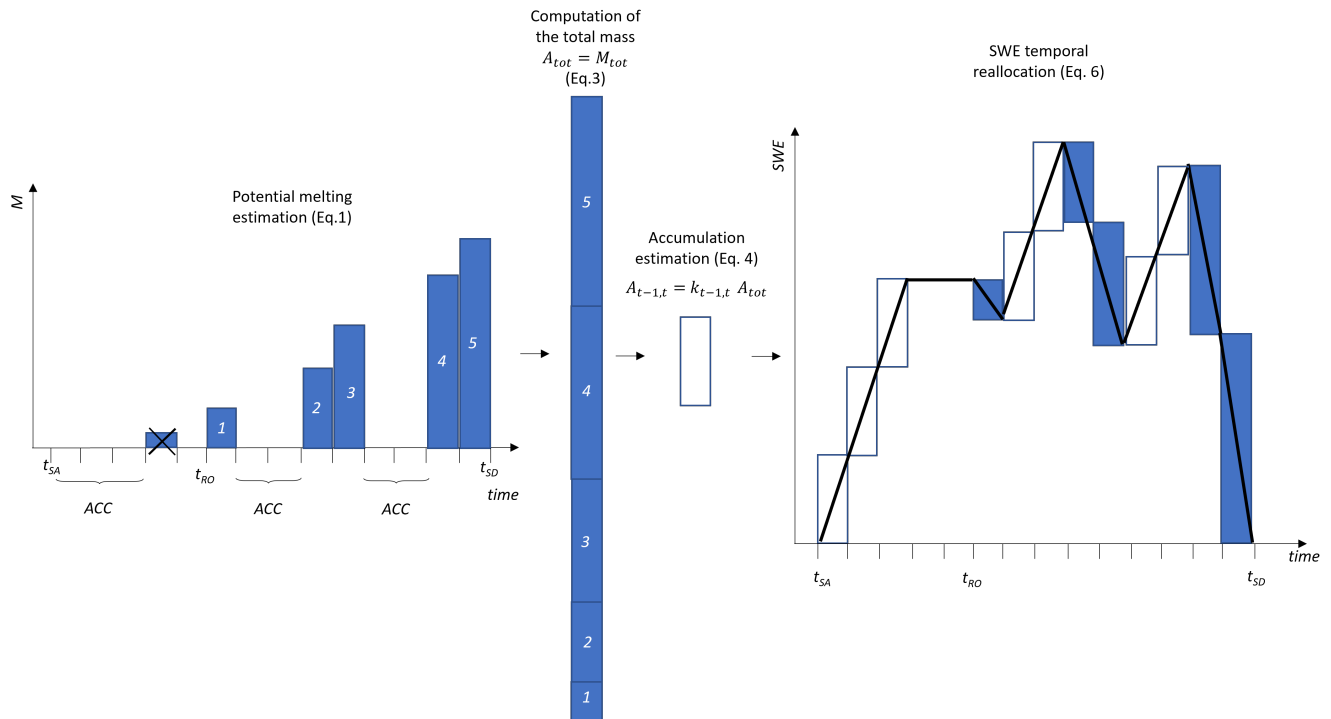



Figure 2. Illustration of the reconstruction and temporal reallocation of the SWE for a given pixel. Starting from the left side of the figure, the state is identified for each day of the snow season (delimited by t_{SA} and t_{SD}) and the potential melting is estimated according to Eq.1. Incorrect melting events prior to the runoff onset are excluded. The sum of all the potential melting at the different days represent the total amount of SWE for that pixel. This is redistributed during the *accumulation* day using Eq.4. For this illustrative example, a constant k is considered. As one can notice the reconstructed SWE can represent *accumulation* (even as late spring snowfall), *ablation* and *equilibrium* conditions.

Snowpack Telemetry (SNOTEL) network (see https://www.wcc.nrcs.usda.gov/snow/) and from the California Data Exchange Center (CDEC) (see https://cdec.water.ca.gov/).

355   The second catchment is the Schnals (Senales in Italian - for brevity we will report the German name only) located in the Vinschgau (Venosta) Valley in South Tyrol (Italy) in the Alps. For this catchment, we analyzed two hydrological seasons spanning from 1 October 2019 to 30 September 2021. The considered area has an extent of approximately 220 km² and a mean elevation of 2370 m, ranging from a minimum of 590 m up to a maximum of 3550 m. The percentage of forest area is around 25% for this catchment (Shimada et al., 2014). Manual SWE measurements are available for the hydrological season

360   2020/21 (collected by the Avalanche Center of the Bolzano Province - Lawinenwarndienst - see https://lawinen.report/weather/snow-profiles - and by Eurac Research, Institute for Earth Observation). Furthermore, we considered the operating temperature and SD sensors of the Province of Bozen (see https://data.civis.bz.it/it/dataset/misure-meteo-e-idrografiche). An overview of the Schnals catchment and the location of available measurements is provided in Fig. 3b.

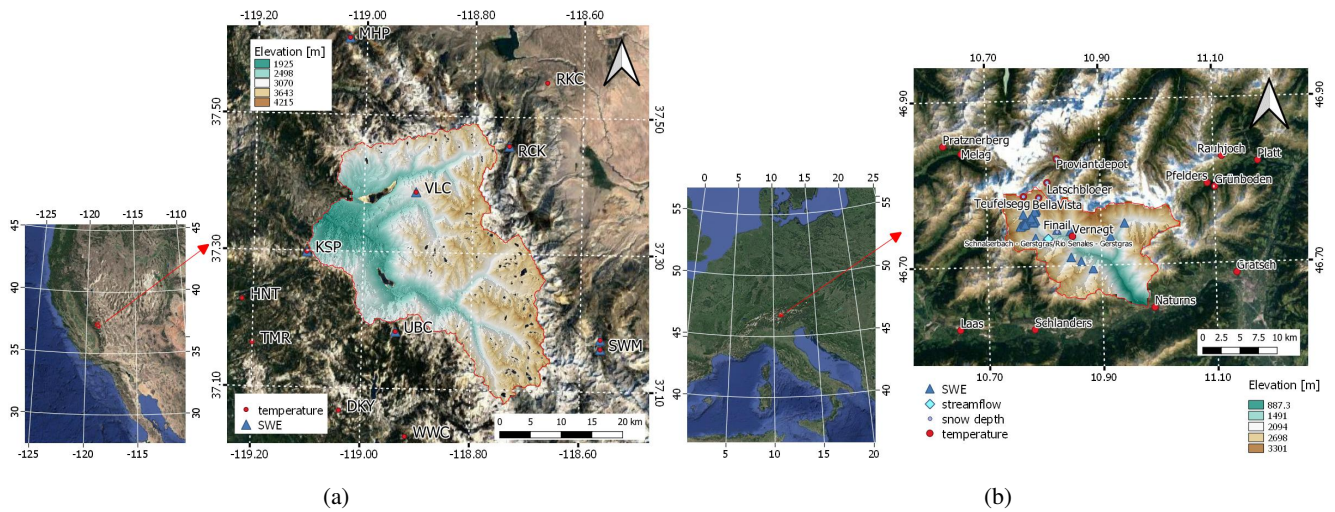



Figure 3. Overview of the two test sites: a) South Fork of the San Joaquin River, California, USA, and b) Schnals catchment, South Tyrol, Italy. Background image ©Google Maps 2022.

The HR daily SCA time-series is derived using the method proposed by Premier et al. (2021). The input data used for the reconstruction are the S2, Landsat-8 and MODIS data. The method requires as input a long time-series of HR images. Therefore, we downloaded a total of about 400 scenes for SFSJR and 700 scenes for Schnals from https://earthexplorer.usgs. gov. The following steps are applied to opportunely preprocessed the data: i) conversion from digital number to Top of the Atmosphere (ToA) reflectance values, ii) cloud masking through the algorithm s2cloudless available at https://github.com/ sentinel-hub/sentinel2-cloud-detector (Zupanc, 2017), iii) SCF detection through an unsupervised statistical learning approach (Barella et al., 2022) (RMSE of 22.82 and an MBE of 6.95), and iv) binarization of the classification results (SCF>10%). Daily MODIS data are needed for the analzyed hydrological seasons. The ready-to-use MOD10 version 6.1 are distributed by the National Snow and Ice Data Center (see https://nsidc.org/data/MOD10A1) (Hall and Riggs, 2021). The NDSI values are converted to SCF by using the algorithm proposed by Salomonson and Appel (2004). The output is a daily SCA time-series with a spatial resolution of 25 m.

The S1 data are downloaded from https://search.asf.alaska.edu/ and pre-processed (i.e., precise orbit application, thermal noise removal, border noise removal, beta naught calibration, tile assembly, co-registration, multi-temporal filtering, terrain correction, geo-coding, and sigma naught calibration). These steps are performed using SNAP (Sentinel Application Platform) and some custom tools. The images are also resampled at 25 m using the same spatial grid as for the SCA maps. Three tracks are available for each test site, i.e. track 64, 137, and 144 for the SFSJR and track 15, 117, and 168 for Schnals, with a total number of around 480 and 350 downloaded images, respectively. For this work, we considered the VV polarization only, which is more suitable for runoff onset identification (Marin et al., 2020). The temporal resolution of each separated track is 6 days. For this reason, the backscattering is daily interpolated, and a multi-temporal analysis is carried out for the three tracks

separately. If at least one track shows a drop of at least 2 dB in the signal (Nagler and Rott, 2000) w.r.t. a moving average of the 12 previous days, we look for the minimum after the drop and for this moment onward the pixel is considered to be in *ablation*.

385 ## 4 Experimental Results

In this section, we present the results obtained for SFSJR and for Schnals.

4.1 South Fork of the San Joaquin River

The proposed SWE maps are aggregated at a resolution of 50 m and compared to the corresponding ASO maps, for a total of 12 dates. Furthermore, we also compare the results with the daily Western United States snow reanalysis (WUS–SR) dataset at 390 500 m provided by Fang et al. (2022). The results of the intercomparison with ASO are reported in Table 2. The analysis shows a good correlation between the two products, with an average correlation coefficient of 0.740. The average bias is -22 mm, the average percent bias (PBIAS) is -19%, and the average RMSE is 212 mm. Our SWE maps underestimate the SWE compared to ASO for the first two seasons, 2018/19 and 2019/20, while overestimating it for 2020/21, which was the driest season with SWE below average (see Appendix A Fig. A1). A possible explanation is that a drier season leads to earlier melting. As the 395 DD method does not consider seasonality in the DD factor a, it is possible that we overestimate the potential melting during the first phase of the season when melting rates are lower due to less energy radiation input (Musselman et al., 2017; Ismail et al., 2023). Additionally, the five SWE maps from the first season, 2018/19, show decreasing RMSE values from mid-winter to late-summer acquisitions. Larger errors during the mid-winter season (around the maximum SWE) are probably due to error propagation (Slater et al., 2013b; Rittger et al., 2016).

Table 2. Results of the intercomparison between the proposed SWE and ASO maps for the SFSJR. Bias, RMSE, and correlation are calculated pixel-wise, while SWE is calculated for the whole basin.

Date	BIAS [mm]	PBIAS [%]	RMSE [mm]	Correlation [-]	SWE ASO [mm]	SWE proposed [mm]
2019/03/17	-82	-11	315	0.73	778	699
2019/05/02	-33	-5	299	0.84	679	647
2019/06/09	-7	-1	268	0.88	511	504
2019/07/04	-37	-24	185	0.86	177	143
2019/07/14	-41	-58	164	0.80	106	67
2020/04/15	-71	-21	242	0.63	389	321
2020/05/05	-53	-26	224	0.67	250	199
2020/05/23	-91	-112	235	0.65	166	78
2020/06/08	-18	-58	161	0.66	48	30
2021/02/26	12	6	125	0.67	186	198
2021/03/31	81	29	168	0.73	191	271
2021/05/03	74	50	160	0.80	72	145

Similarly, Table 3 presents the results of the comparison between the proposed SWE dataset and the WUS-SR dataset, where metrics are computed pixel-wise by aggregating the proposed SWE at a 500 m resolution. An average value is then computed for the entire season. The comparison reveals a systematic negative bias, which may be attributed to the different modeling of snow under canopy. The correlation between the proposed and WUS-SR datasets is lower than that between the proposed and ASO datasets. For further comparison, Appendix C includes additional analyses of the proposed approach, WUS-SR, and ASO at a 500 m resolution. The analysis shows that the WUS–SR dataset also correlates worse with ASO. However, the three time-series show a consistent behaviour.

Table 3. Results of the intercomparison between the proposed SWE and WUS–SR for the SFSJR. Bias, RMSE, and correlation are calculated pixel-wise. The proposed SWE was aggregated to 500 m resolution.

Season	BIAS [mm]	PBIAS [%]	RMSE [mm]	Correlation [-]
2018/19	-51	-22	174	0.73
2019/20	-51	-40	108	0.63
2020/21	-31	-25	100	0.63

Good agreement is also confirmed when comparing the total amount of SWE estimated through the three approaches in the catchment. Fig. 4 shows the time-series of the total SWE for the three hydrological seasons. In the plot, it is possible to appreciate the large SWE variability that can occur for different seasons and that is well represented by all three time-series. The first hydrological season 2018/19 shows the highest amount of SWE, while the others are drier. For reference, the SWE regime for the catchment is reported in Fig. A1 in Appendix A.

The Volcanic Knob (VLC) VLC monitoring site, which is located within the analyzed area, is also used to evaluate the obtained results, and it shows good agreement between the proposed time-series and the in-situ measurements (refer to Fig. 5). Note that the WUS-SR presents a delay in detecting the t_{SD} probably due to the coarser resolution, i.e., 500 m, despite a similar trend. It is worth noting that the first year, 2018/19, is also used to set up the constant DD factor a used for the DD model, that is then kept constant for the other seasons. The found value is in accordance with values found numbers present in the literature (Hock, 2003; Ismail et al., 2023). The validity of the chosen value is also confirmed by the good agreement of the results for the next two seasons. However, a delay in detecting t_{RO} is observed in season 2018/19 that results in a smaller SWE peak.

We also propose here a more detailed analysis on a specific date. To keep this analysis concise, we propose to consider a date during the full melting season, a period of particular interest from a hydrological perspective. The considered date is the 9 June 2019. For the analysis on the other dates and the intercomparison with the WUS-SR dataset, please refer to the Appendix C. Fig. 6 reports the proposed SWE map, the ASO SWE map and the bias map calculated as the pixel-wise difference between the proposed and the reference ASO map at 50 m. In general, it is possible to notice a good agreement between the two maps. The proposed method is capable of reproducing spatial patterns similar to those detected by ASO. This finding demonstrates that the use of HR input data achieves a unique spatial detail, which represents one of the main advantages of the proposed method. Upon closer inspection of a specific area, this similarity can be better appreciated. Nevertheless, it is possible to notice

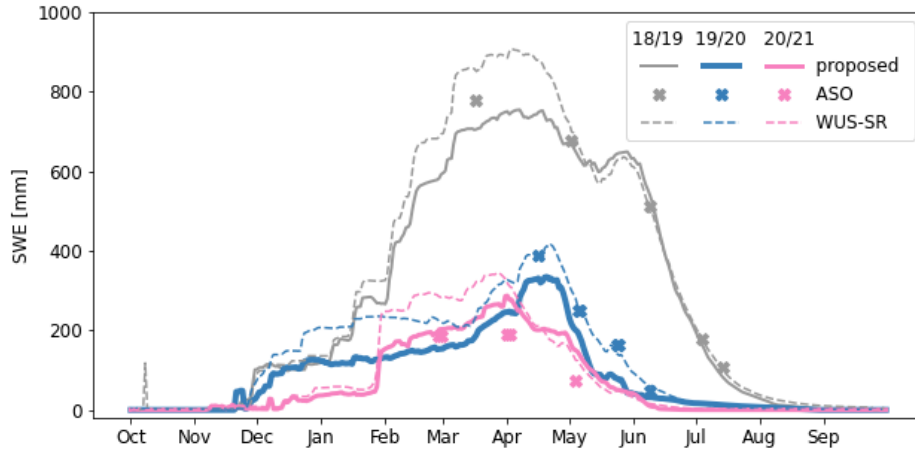



Figure 4. Time-series of the total SWE for the SFSJR over the three analyzed seasons. Continuous lines represent the proposed time-series, dashed lines the WUS–SR dataset, and crosses represent the ASO reference.

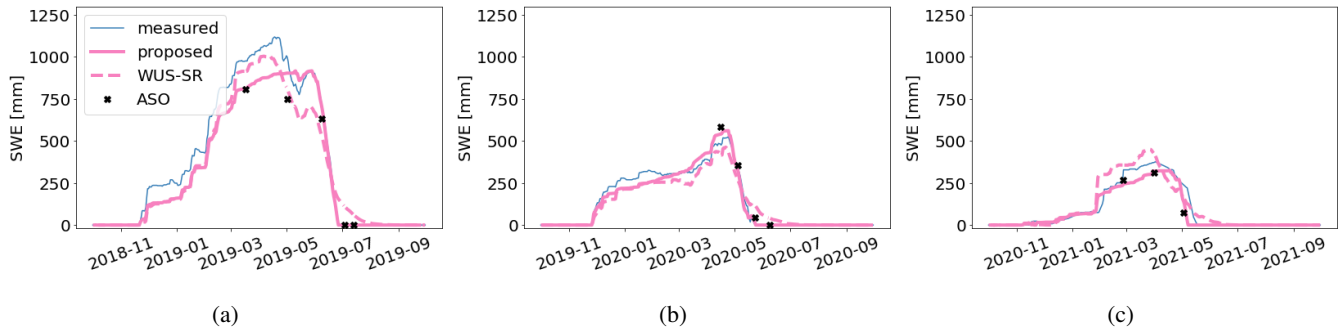



Figure 5. SWE obtained by the proposed approach (pink continuous line) is compared against the measured SWE (in blue), the WUS-SR SWE (pink dashed line), and ASO SWE (black crosses) at the Volcanic Knob test site for the hydrological seasons a) 2018/19, b) 2019/20, and c) 2020/21. To extract SWE at the considered location, the original spatial resolution of each dataset is maintained.

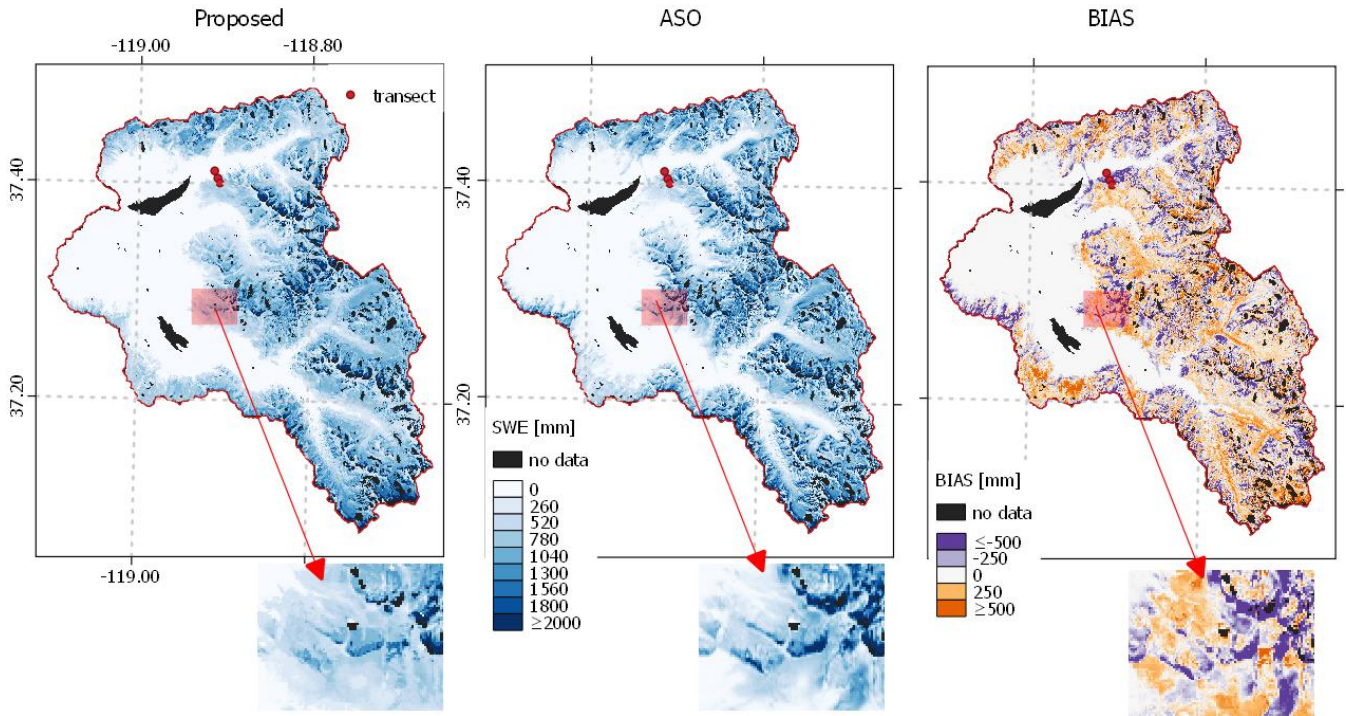



Figure 6. Proposed SWE map (on the left), ASO SWE map (in the centre) and bias map calculated as difference between the proposed and ASO SWE (on the right) for the 9 June 2019 for the SFSJR. A zoom is shown under the correspondent maps. A transect is shown with three green dots in the North area of the catchment.

a tendency of the proposed SWE maps to underestimate SWE especially in some areas exposed to the north. This could be attributed to either i) an error introduced by the DD model, which only considers temperature and may not account for radiation differences associated with different aspects (Ismail et al., 2023), or ii) an error in the snow depth retrieval or snow density modeling introduced in the ASO maps.

Fig. 7a displays the mean SWE values for different elevation, slope, and aspect ranges. The most significant changes are observed when analyzing the different elevation ranges. The trend is quite consistent, with an increase in SWE as elevation increases up to approximately 3500 m a.s.l., while the trend is reversed for higher elevations. These areas generally have very steep slopes, resulting in a marked tendency for snow to be subject to gravitational transport. The two SWE maps only differ for elevations higher than about 4100 m a.s.l., where the proposed SWE starts to increase again, while the ASO continues to decrease. The slope analysis shows larger differences, especially when considering steep slopes. The proposed method underestimates SWE compared to ASO. We generally expect lower SWE for these steeper slopes that promote gravitational transport. The aspect analysis correctly indicates a larger amount of SWE for north-facing areas. As mentioned earlier, we can observe an underestimation of the SWE for north-facing slopes when comparing our maps with the ASO. Conversely, we would expect an overestimation of the SWE for the north-facing areas, as the DD method does not consider radiation effects. However, we

(a) (b)

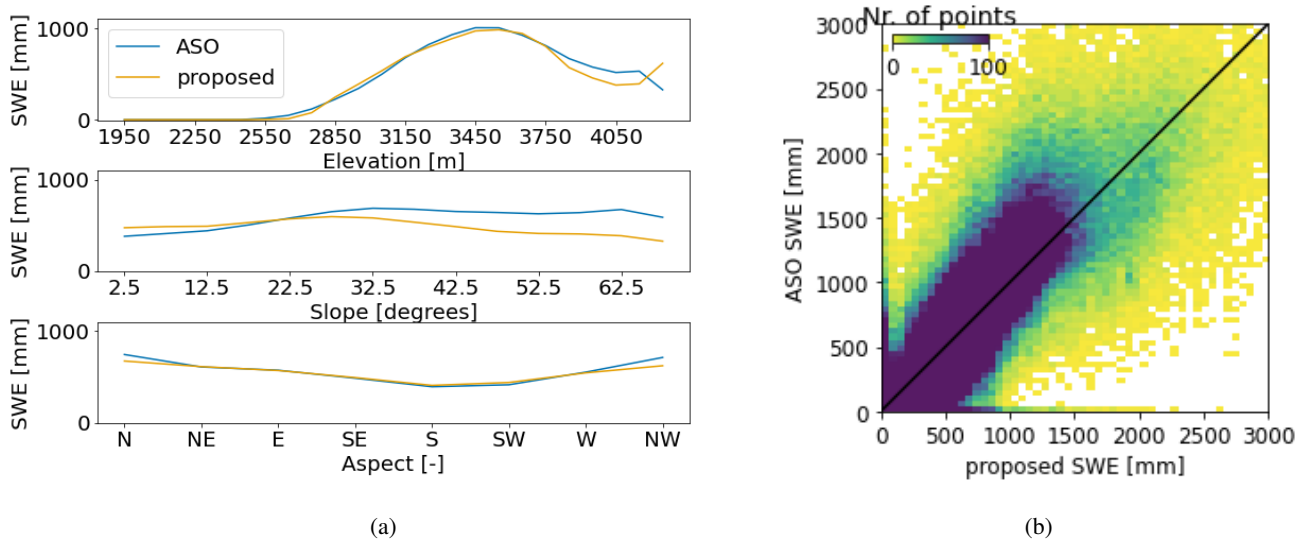



Figure 7. Mean SWE value for different elevation, slope and aspect belts (on the left). The proposed SWE (in orange) is evaluated against ASO (in blue) for the 9 June 2019 for the SFSJR. On the right, dispersion graph for the same date.

never observe this overestimation when considering this and other available reference dates presented in Appendix C.

Fig. 7b shows the dispersion graph for the proposed method and ASO. In general, a strong correlation can be observed,
445 albeit with significant dispersion, which is also confirmed by the computed correlation and RMSE value reported in Table 2. However, the majority of the points are clustered around the diagonal line.

Fig. ~~8~~ 8b shows the time series for the 2018/19 season for three points along a selected transect. A zoom of the transect is reported in Fig. 8a (see Fig. 6 for their location in the basin). It is ~~possible to observe that the~~ interesting to notice that the three points differ in terms of forest coverage. While the low and high elevation points are not directly located in the canopy, this
450 is not the case of the mid elevation point. The proposed SWE presents ~~the~~ an expected behavior, i.e., longer snow persistence and increasing SWE for higher elevation. ~~Despite~~ However, the mid-elevation point shows a later runoff onset w.r.t. the other points, that is probably due to the fact that the timing detected by S1 is less reliable in that area. This might introduce an underestimation of SWE for that pixel. However, despite some differences that can be due to the different spatial resolution between the two products, ~~this trend~~ an increasing SWE for increasing elevation is respected also for the WUS-SR dataset.
455 On the other hand, the ASO shows a higher SWE for the mid elevation point. Note that even though we use ASO as a main reference, there may be inconsistencies present, such as possible inaccurate estimation of the snow density by the model. Interestingly, the figure also correctly shows a variability in the three poposed SWE time-series. Notwithstanding the stations are used to identify the *accumulation* state, the SWE time-series does not necessarily present the same shape everywhere as for

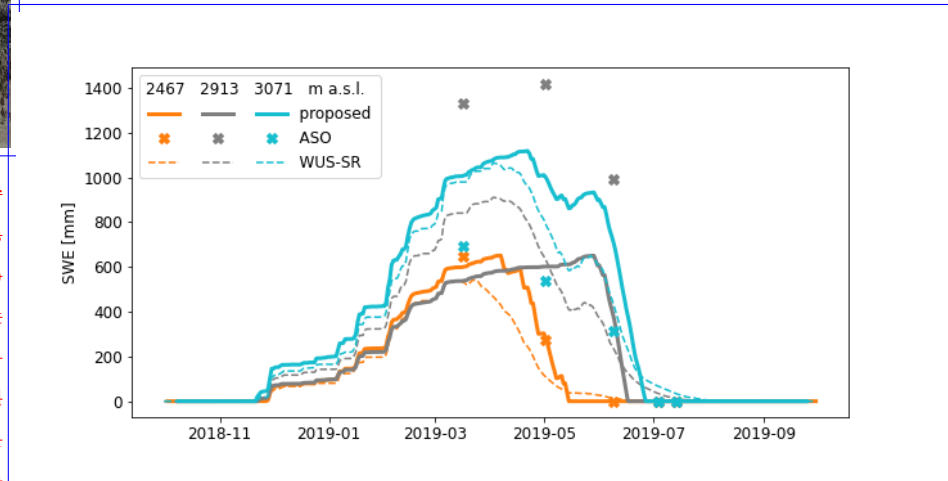
(a) ~~SWE time-series in 2018/19 for the proposed approach (continuous lines), WUS-SR (dashed lines) and ASO (crosses) for a transect in the SFSJR reported in Fig. 6. To extract SWE at the considered locations, the original spatial resolution of each dataset is maintained.~~

(b)

Figure 8. On the left, a zoom of the transect in the SFSJR reported in Fig. 6. Background image ©Google Maps 2022. On the right, the SWE time-series in 2018/19 for the proposed approach (continuous lines), WUS-SR (dashed lines) and ASO (crosses) for the same transect. To extract SWE at the considered locations, the original spatial resolution of each dataset is maintained.

the station (see Figs. 8 and 5). The final result is influenced not only by the persistence of the snow, but also by the potential melting, which varies depending on the elevation. This is calculated using kriging with external drift.

4.2 Schnals catchment

For the Schnals valley, spatialized SWE data to be used as reference are unfortunately not available. However, manual SWE measurements for the hydrological season 2020/21 were collected along spatial transects. The location of the measurements is shown in Fig. 3b. The results show a bias of -5 mm, an RMSE of 191 mm, and a correlation of 0.35. Fig. 9 shows the proposed reconstructed SWE plotted against the manual measurements. Despite a generally good agreement, we observe some significant differences and a worse performance compared to the analysis performed for the Californian catchment. However, the reference dataset is insufficiently informative and represents only a few points that may not be entirely representative of the intra-pixel variability, especially in complex terrains. As shown by the SWE measurements acquired in Schnalstal by Warscher

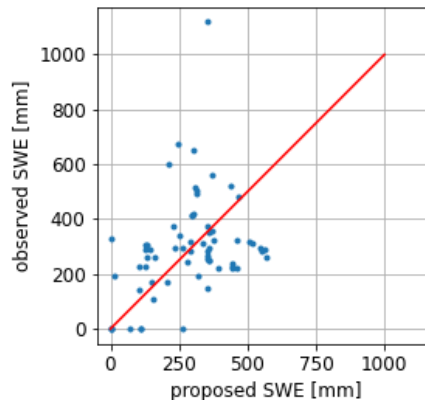



Figure 9. Proposed SWE (x-axis) against observed SWE (y-axis) for the season 2020/21 in the Schnals catchment (see Fig. 3b).

(a)   (b)

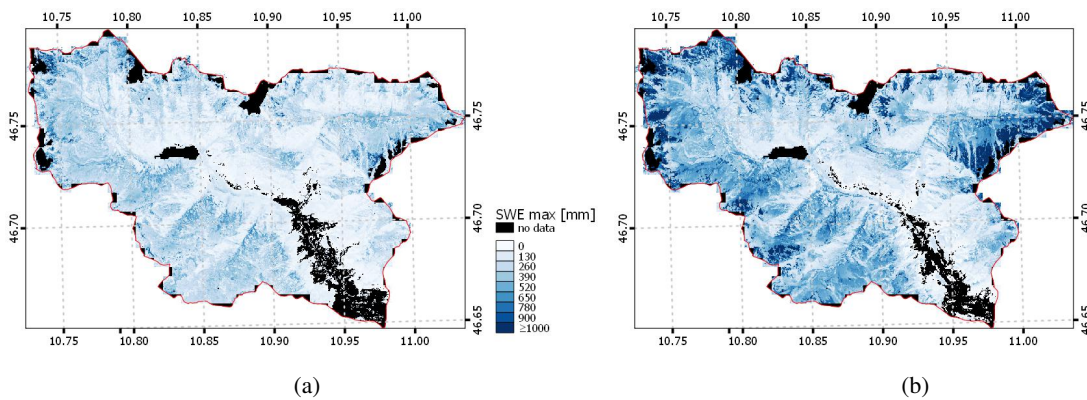



Figure 10. Maximum of SWE for the Schnals catchment for the hydrological seasons a) 2019/20 and b) 2020/21.

et al. (2021), a high spatial heterogeneity of the SWE can be encountered when considering a pixel with a size of 25 m. This
470   results in inherent difficulties in appropriately evaluating the output.

Fig. 10 shows the map of the maximum SWE for the two analyzed hydrological seasons. From these highly detailed maps,
it is possible to see that the season 2020/21 is characterized by a higher amount of SWE. However, the two years show similar
patterns that are consistent with the morphology of the study area. In detail, we can notice that there is a higher amount of SWE
especially in the East part of the catchment that corresponds to the glacierized area of the Roteck/Monte Rosso mountain. We
475   found a longer persistence of snow for these North exposed slopes and consequently a larger amount of reconstructed SWE.

Due to the absence of an appropriate dataset for the SWE intercomparison in the Schnals valley, we carry out a qualitative
analysis of the correlation between SWE and riverine discharge. To achieve this, we analyze i) the discharge measured at
Schnalserbach - Gerstgras; ii) the SWE variations that are associated with runoff (i.e., only when they are associated with a

decrease in SWE) for the corresponding subcatchment, and iii) the precipitation measured at Vernagt. Refer to Fig. 3b for the location of the outlet point and pluviometer. Fig. 11 shows good agreement in terms of both timing and quantity between snow-generated runoff and discharge, confirming that the catchment is snowmelt dominated. The discharge starts increasing in correspondence with the snowmelt, and it starts decreasing when the snowmelt is reduced for both periods. The first year shows a delay, while the response is more direct for the second season. More than differences in terms of precipitation, we ascribe this situation to a different snowmelt rate. Indeed, the season 2019/20 shows an earlier, weaker, and longer distributed snowmelt period, interrupted by periods with low SWE output (such as the end of March-beginning of April, beginning of May, or middle of June). This situation may favor ground infiltration with a predominance of subsurface runoff w.r.t. surface runoff, contributing slowly to the discharge. On the other hand, the 2020/21 season shows a long and high intensity SWE release (end of May-end of June) that may cause a sudden saturation of the soil, with predominant surface runoff contributing more directly to the discharge. This hypothesis may also be confirmed by recent literature, showing that when snowmelt is earlier, it is also less intense, and the runoff response could be reduced, with strong implications for future climate change impacts (Musselman et al., 2017). However, other contributions should also be considered, such as the storage of water in the two reservoirs present in the territory. While a proper analysis requires a complete hydrological study and a hydraulic characterization of the watershed properties, we believe that this simplified analysis demonstrates the potential of the presented results in a real application.

5   Discussion

The results indicate that the proposed method is capable of reproducing the SWE with high geometrical detail and in an accurate way. Particularly good agreement w.r.t. other datasets is achieved when considering the results on a catchment scale. The method demonstrates good performance in reproducing the expected SWE behavior when analyzing the topography of the study area. However, when considering a reference with comparable spatial resolution, significant differences are observed. In this section, we discuss the main sources of errors and weaknesses that may affect the results and provide a simplified sensitivity analysis of the parameters that play a role in the proposed approach. Furthermore, we also provide a detailed discussion of the effectiveness of the novel SCA regularization introduced through the state definition.

5.1   Sensitivity analysis

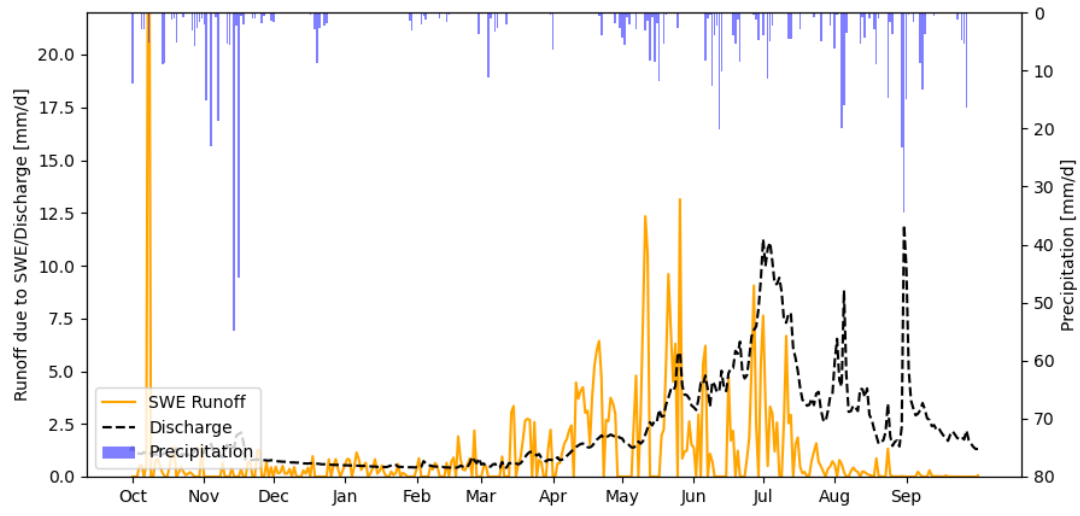
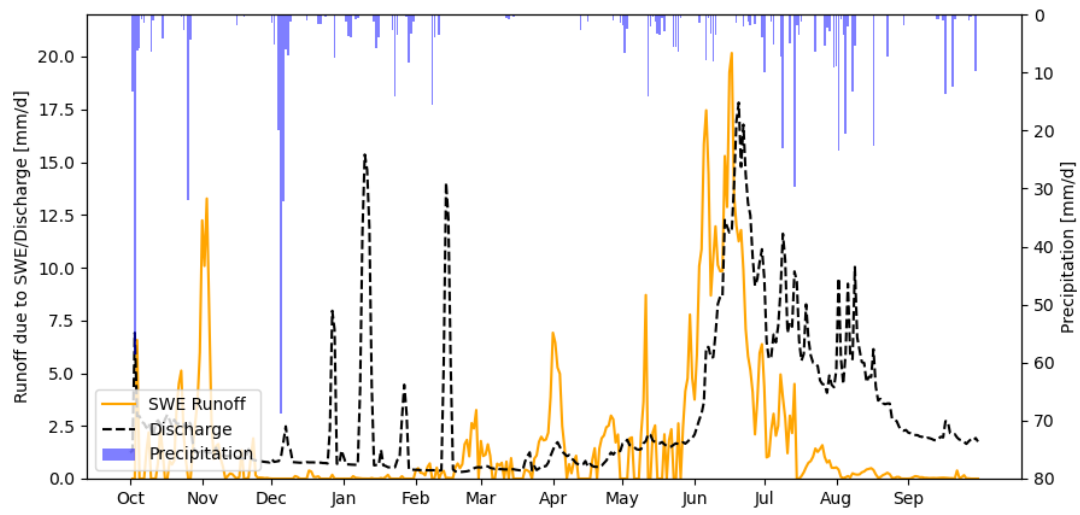
The potential sources of errors in the method are represented by i) a wrong state identification, ii) the incorrect identification of t_{SA} and t_{SD}, which in turn depends on the accuracy of both the SCA time-series and the state, and ii) the use of a DD model for the potential melting estimation, which in turn depends on the ~~goodness of the temperature data~~quality of air temperature recordings, the interpolation routines, and the simplified assumption of the method itself, which does not take into account different energy inputs due to either topographical features or different periods of the year. Since the input data are subject to several degrees of preprocessing, it is difficult to perform a complete sensitivity analysis of the method. This has been partially covered by other works (e.g., Slater et al., 2013b; Ismail et al., 2023). Here, we present a simplified sensitivity analysis on

(a)

(b)

Figure 11. Snow generated runoff (in orange), discharge (dashed black line) and precipitations (in blue) for a subcatchment in the Schnals valley closed at Schnalserbach - Gerstgras (see Fig. 3b) for the seasons: a) 2019/20 and b) 2020/21.

the parameters that play a role in the proposed approach. For the sake of clarity, we investigate how the most important parameters affect the final SWE reconstruction by considering the pixel where the station Volcanic Knob provides continuous SWE measurements in the Sierra Nevada catchment. These parameters are i) the DD factor a, ii) the SWE threshold SWE_{min} used to identify the states, iii) the time of snow disappearance (t_{SD}), iv) the time of snow appearance (t_{SA}), and v) the time of the runoff onset detected by S1 (t_{RO}). We vary each of these parameters separately, keeping the others constant and equal to the optimal case (see Table 4). The test is carried out for the 2018/19 season. Although this analysis is not exhaustive, it gives an overview of the most important sources of error.

Table 4. Optimal parameters values for the pixel with the Volcanic Knob station.

Parameter	Unit	Value
a	$\text{mm}^o\text{C}^{-1}\text{d}^{-1}$	4.8
SWE_{min}	mm	2
t_{SD}	d	2019/06/27
t_{SA}	d	2018/11/22
t_{RO}	d	2019/04/22

In Fig. 12a a varies from 3 to 6 by steps of 0.2 $\text{mm}^o\text{C}^{-1}\text{d}^{-1}$. It is possible to notice that the error increases linearly when a moves away from the optimal value, that is 4.5 $\text{mm}^o\text{C}^{-1}\text{d}^{-1}$, as set for the SWE reconstruction.

In Fig. 12b the SWE threshold varies from 0 to 20 by steps of 1 mm. As expected, the higher the threshold, the greater the error. Indeed, for thresholds that are too large, the method does not detect *accumulation* states. A snow threshold of 2 mm, as used in this work, is acceptable.

In Fig. 12c t_{SD} varies in a range of ±15 days w.r.t. the optimal day. Both underestimating and overestimating t_{SD} introduces important errors in the reconstruction. Indeed, at the end of the melting season the temperature is high and consequently the potential melting. A difference of ±5 days (which corresponds to the repetition time of S2) already introduces an RMSE of approximately 50 mm.

In Fig. 12d t_{SA} varies in a range of ±15 days w.r.t. the optimal day. The shift of t_{SA} does not strongly affect the RMSE as t_{SD} does. For negative shifts, the RMSE is constant since no SWE is added to the reconstruction. Indeed, for these days, we find that the coefficient k (see Eq. 4) is 0 since it is calculated from the AWSs. In other words, it means that the accumulation is not really happening before at least one station detects an increase in SWE. This might introduce an error if some pixels are in *accumulation* before the station reports it, but it does not affect the maximum amount of SWE for those pixels, which is determined only by the days in *ablation*.

In Fig. 12e t_{RO} varies in a range of ±15 days w.r.t. the optimal day. Furthermore, the shift of t_{RO} does not strongly affect the RMSE as does t_{SD}. The RMSE for negative shifts remains constant after a certain point, since for those days Eq. 1 returns 0 potential melting due to negative temperatures. This means that anticipating the melting phase is less critical than postponing it, since the temperatures and consequently the potential melting are lower.

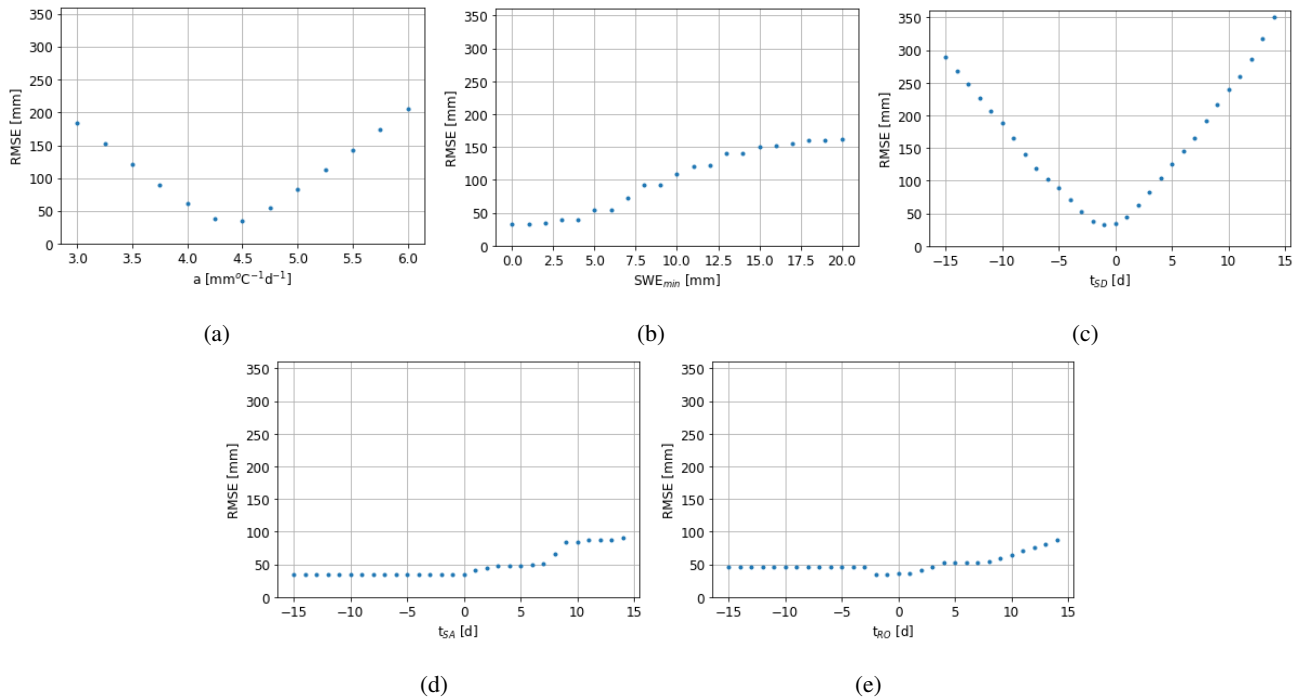



Figure 12. Sensitivity analysis on: a) the DD factor (a), b) the SWE threshold (SWE_{min}), c) the time of snow disappearance (t_{SD}), d) the time of snow appearance (t_{SA}), and e) the time of the runoff onset detected by S1 (t_{RO}). One parameter is varied while the others are kept constant and equal to the optimal value as reported in Table 4.

In general, we can summarize that changes in a and t_{SD} are expected to strongly affect the results. The DD factor a cannot be considered a constant parameter and has to vary in space and time to minimize the SWE reconstruction error, as pointed out by many researchers (e.g., Ismail et al., 2023). On the other hand, given the high temperature and potential melting values at 540 the end of the ablation, an incorrect estimate of t_{SD} can significantly impact the reconstruction of the SWE peak, resulting in either an overestimation or underestimation. Therefore, the introduction of an accurate daily HR time series can greatly benefit the SWE reconstruction.

5.2 SCA regularization

Figs. 13 and 14 show the SCA before and after regularization for the SFSJR and Schnals catchments, respectively. As explained 545 in Sec. 2.2, the raw reconstructed SCA presents two issues: i) strong decreasing peaks in correspondence to HR acquisitions at the beginning of the season, indicating an underestimation of SCA in forested areas, and ii) small increasing peaks in correspondence to HR acquisitions in the late melting phase, indicating the presence of snow patches that are not visible in LR images. In contrast, the regularized SCA is more stable, and the spurious oscillations, especially during the coldest winter period, are corrected. The effectiveness of the correction is also visible when looking at the regularized image. Fig. 15 represents

a common situation where atmospherically corrupted and mixed pixels are classified erroneously. The proposed correction improves snow detection, especially in these complicated cases.

An underestimation of SCA is observed in May 2019 for the SFSJR catchment (see Fig. 13a). A careful examination of the conditions that led to the flattening of the SCA during the late snowfall reveals that the stations indicate a long period as *accumulation* (from 16 to 29 May), whereas the peak starts decreasing in the original SCA time-series from 21 May. By applying the rule for a recent snowfall (see Sec. 2.2 and Algorithm 1), the majority of the pixels are labeled as *snow-free*. In other words, the peak lasts only a few days, so the label *snow* does not persist for a long time. This implies a replacement with *snow-free* backward until the day of the last ablation. It is possible that the AWSs present some sensor errors, but this could also be the case of a mixed state inside the catchment. In other words, the AWSs detect snowfall, but this is most likely occurring at high elevations, while the SCA decreases due to ongoing melting or rain-on-snow, especially in the lower elevation belts of the catchment. Indeed, the SCA decrease from $\sim 100\%$ to $\sim 80\%$ means that low elevations become *snow-free*. However, we expect that such ephemeral snowfall does not significantly affect the total amount of SWE, as shown in Sec. 4.1.

On the other hand, an evident case where an overestimation of the SCA is introduced is in the season 2020/21 in May/June for the SFSJR (see Fig. 13c). This overestimation is caused by the fact that the AWSs do not indicate an *accumulation* in correspondence with the peaks that occur in the late melting phase. Therefore, the label is corrected according to the majority rule in *ablation* in the case of old snowfall. Most of the pixels were *snow* in previous HR acquisitions, leading to the propagation of the class backward and the consequent overestimation of the SCA. This could be a reason for an overestimation of the SWE as shown in the results (see Sec. 4.1).

It is evident that the effectiveness of the SCA regularization is strongly influenced by the reliability of the state identification. At the current state, the main limitation of the proposed method is represented by the *accumulation* identification which is not provided at a pixel level. Future research should focus on this point and exploit remote sensing observations rather than sparse AWSs information. For example, a possible indicator of an ongoing accumulation is represented by a SCA increase. However, small variations may be due to errors. Furthermore, snowfalls on already snow-covered areas cannot be identified. A possible alternative is represented by the use of SAR data. Recent works have shown that the backscattering seems to be sensitive to the presence of fresh snow, showing an increase in the backscattering in correspondence with a snowfall (e.g., Tsang et al., 2021; Lievens et al., 2022). However, the poor temporal resolution may strongly affect the *accumulation* rather then the *ablation*, since the snowfall is expected to be a more rapid phenomenon.

6 Conclusions

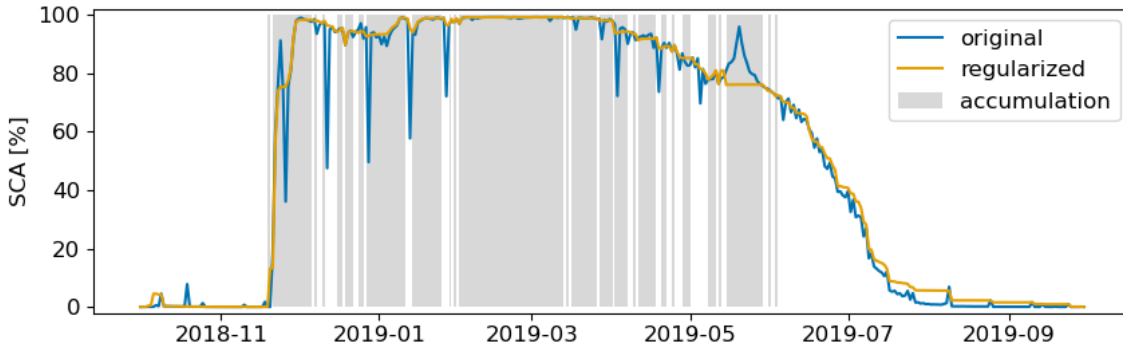
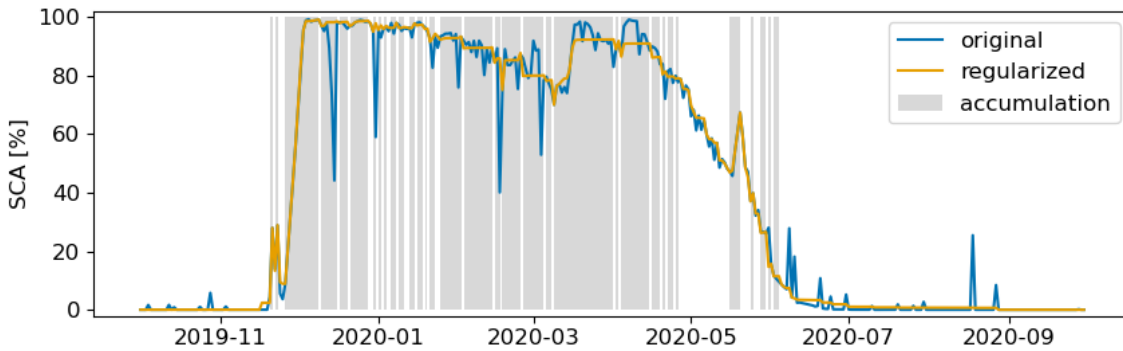
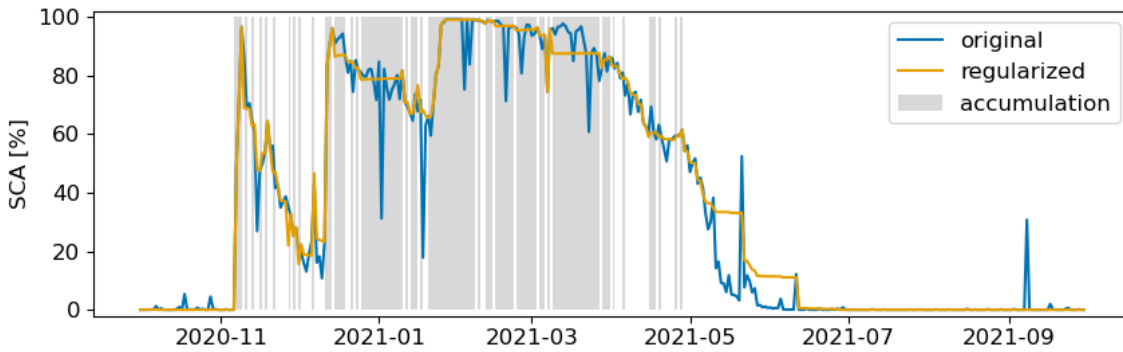
In this work, we explored the use of multi-source satellite data to reconstruct HR daily SWE time-series at a spatial resolution of 25 m. The proposed approach involves the following step: i) determining the state (i.e., *accumulation*, *ablation*, or *equilibrium*) using in-situ SD/SWE ~~observations~~ and temperature observations, and S1 multitemporal backscattering data, ii) identifying the dates of snow appearance and disappearance from a daily HR snow cover time-series derived by fusing high- and low-

(a)

(b)

(c)

Figure 13. SCA time-series in the SFSJR for the hydrological seasons a) 2018/19, b) 2019/20 and c) 2020/21. Original input version (in blue) and regularized version (in orange). The gray background color corresponds to an *accumulation* state.

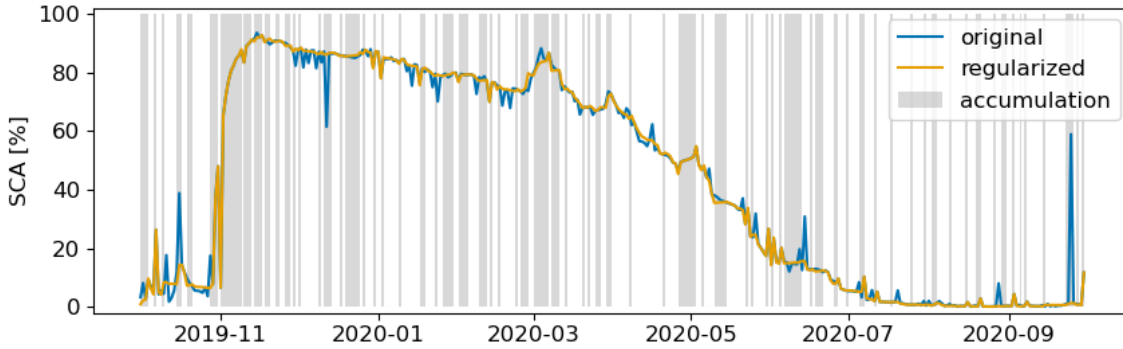
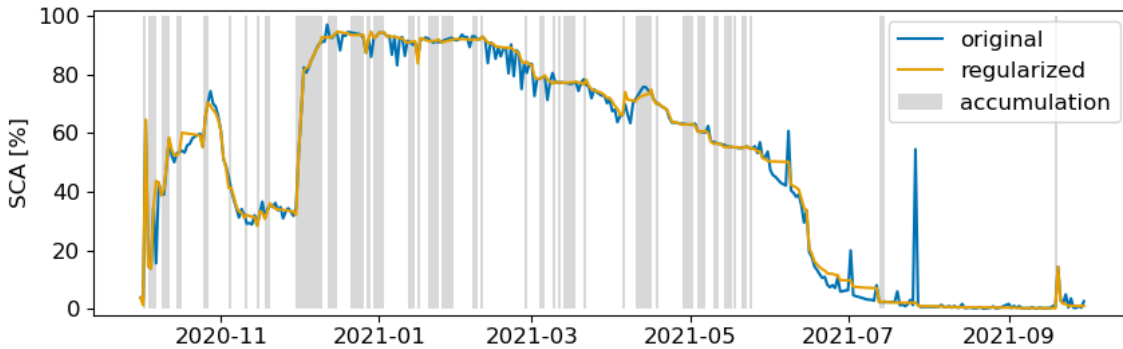



Figure 14. SCA time-series in the Schnals catchment for the hydrological seasons a) 2019/20 and b) 2020/21. Original input version (in blue) and regularized version (in orange). The gray background color corresponds to an *accumulation* state.

resolution optical sensors, and iii) estimating the potential melting from in-situ temperature observations using a DD model. We proposed a novel regularization of the SCA time-series that considers the state information. The regularization corrects

585   impossible transitions, i.e., erroneous changes of the pixel class from *snow* to *snow-free* when *accumulation* or *equilibrium* and, vice versa, from *snow-free* to *snow* when *ablation* and *equilibrium*. Finally, the SWE is added or removed from the reconstruction according to the state, with the amount determined by the potential melting calculated using the DD model.

The proposed novel state concept is utilized throughout the different steps of the method, resulting in a SWE reconstruction that incorporates the accumulation phase and potential late snowfalls. Furthermore, spatialized precipitation data, which can be

590   unreliable on complex terrains, is not required as the method redistributes the amount of melting by leveraging state information rather than quantifying precipitation input. The state also enables the implementation of a new regularization of the SCA time-

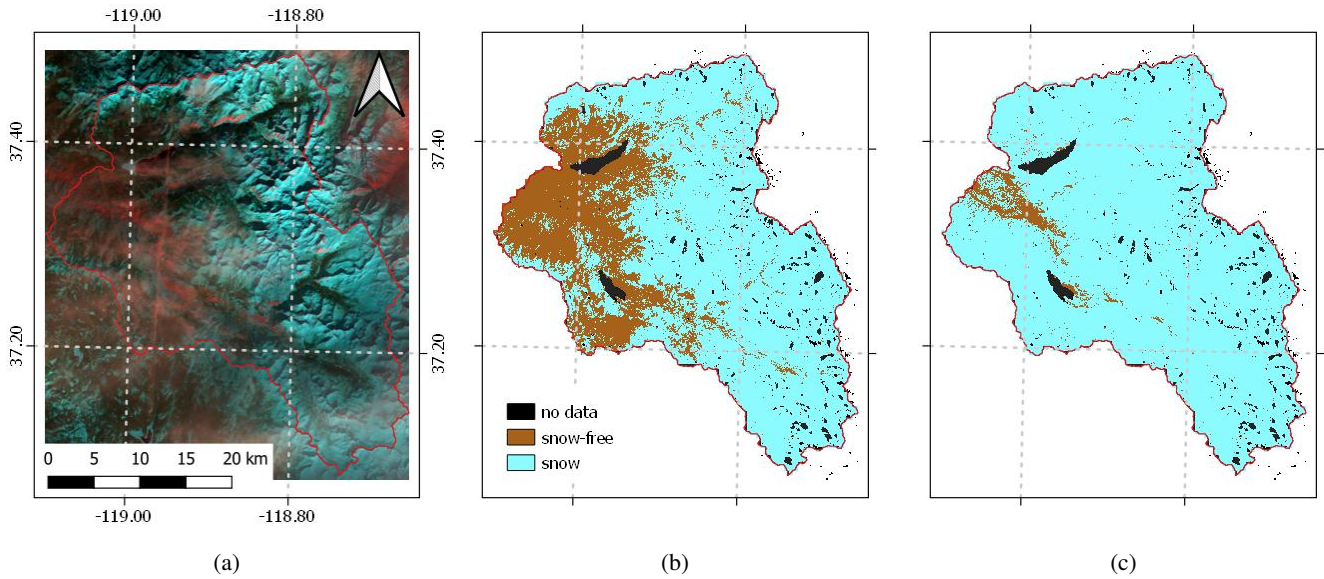



Figure 15. Example of a regularized snow map on 12 January 2020 for the SFSJR: a) false-color composition (R:SWIR,G:NIR,B:RED), b) original snow cover map, and c) regularized snow cover map.

series. Additionally, the use of a daily HR SCA time-series in combination with melting phase information from SAR data is introduced as a further innovation.

The method was tested in two mountainous catchments: i) the SFSJR, located in the Sierra Nevada - California (USA), and ii) the Schnals catchment, located in the Alps - South Tyrol (Italy). The results obtained demonstrated the effectiveness of the proposed approach in estimating HR SWE. For the first catchment, the results were evaluated against ASO SWE at 50 m, showing an average bias of -22 mm, an RMSE of 212 mm, and a correlation of 0.74. When evaluated against the daily WUS-SR dataset at 500 m resolution, they showed a bias of -44 mm, an RMSE of 127 mm, and a correlation of 0.66. For the second site, the results were evaluated against manual measurements, showing a bias of -5 mm, an RMSE of 191 mm, and a correlation of 0.35. The obtained results were extensively discussed, considering possible hydrological applications of such a dataset. In this sense, we showed that the results are very promising since they i) are able to capture the typical spatial variability of an HR map, ii) show spatial patterns that are consistent with a reference with comparable spatial resolution, as well as with the topography of the study area, iii) provide ~~a reliable global balance at a catchment~~ consistent trends when considering the basin scale, iv) reproduce the variability of different hydrological seasons, and v) require limited meteorological and ground snow observations.

The main sources of error are discussed to provide insights into the main advantages and disadvantages of the method that may be of great interest for several hydrological and ecological applications. It was found that the main sources of errors arise from the potential melting calculation and from the time of snow disappearance. To address potential melting errors, we presented a method that incorporates spatialized information from S1 to determine when the snowpack is subject to runoff

610 and prevent false early melting. Secondly, we introduced the use of HR SCA for SWE reconstruction, which is more adequate to sample the SCA variations due to the complex topography of mountainous catchments. Technological limitations are still present, such as the necessity of merging LR and HR sensors given the absence of daily optical HR acquisitions, the absence of an appropriate observation to determine the accumulation state pixel-wise, and the scarce temporal resolution of SAR acquisitions. Although the proposed approach attempts to overcome all these limitations, we expect that further improvements

615 will also be introduced by future satellite missions, such as Copernicus LSTM and ROSE-L, which will acquire new important information for SWE retrieval. This will not only improve the proposed method but also enable the development of near-real-time predictors of SWE for large hydrological and ecological applications.

Code and data availability. The implemented code can be made available upon request to the authors. All the raw input data are freely available as indicated in Sec. 3. The dataset output related to this article will be made available in an open repository after publication or

620 requested directly to the authors.

Appendix A: In-situ snow measurements

State characterization is performed by observing available SWE or SD in-situ measurements. For the SFSJR, SWE continuous measurements are available for 7 different sites. As shown in Fig. 3a, only one station is within the considered area, i.e., the Volcanic Knob station (VLC). For this station, SWE records are available starting from 2000. This allowed us to perform

625 an analysis of the SWE regime. In ~~the following plots~~Fig.A1, we show the average SWE for all recorded years, the range of variation, and the current SWE. It is possible to see that the first season presents high SWE, while the other two seasons are under the average regime, especially the last one. For the SWE reconstruction, we also considered the stations in the surrounding area to smooth out possible sensor errors or redistribution effects.

In the Schnals catchment, SWE continuous records are available only for the location Bella Vista. For this reason, the

630 decision on the state is based on the SD records available for 5 stations (see Fig. 3b). Three stations are within the study area and the remaining two are very close to the study area (maximum 5 km).

Appendix B: Degree-day estimation

The DD is estimated from available in-situ temperature observations for both catchments. Regarding SFSJ, the temperature is available at 11 different stations located within a radius of approximately 15 km from the study area (see Fig. 3a). Due to

635 the presence of some gaps in the data, we excluded from the computation of the DD the station "RKC" for season 2018/19, "WWC" for 2019/20 and "DKY","VLC", and "UBC" for 2020/21. For the Schnals catchment, the temperature is available in 15 different locations within a maximum distance of around 10 km (see Fig. 3b). Once the DD is computed for each station through Eq. 2, the DD is spatially interpolated with the kriging routine as explained in Sec. 2.3. The goodness of the spatial

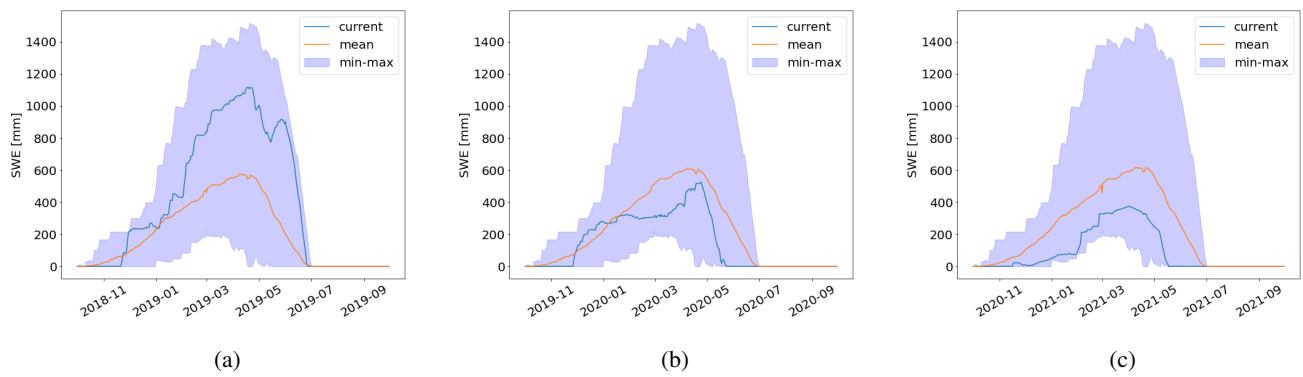



Figure A1. Average SWE (in orange) against the current SWE (in blue) and the range min-max SWE (in violet) at the Volcanic Knob test site for the hydrological seasons a) 2018/19, b) 2019/20 and c) 2020/21. SWE records are available starting from 2000.

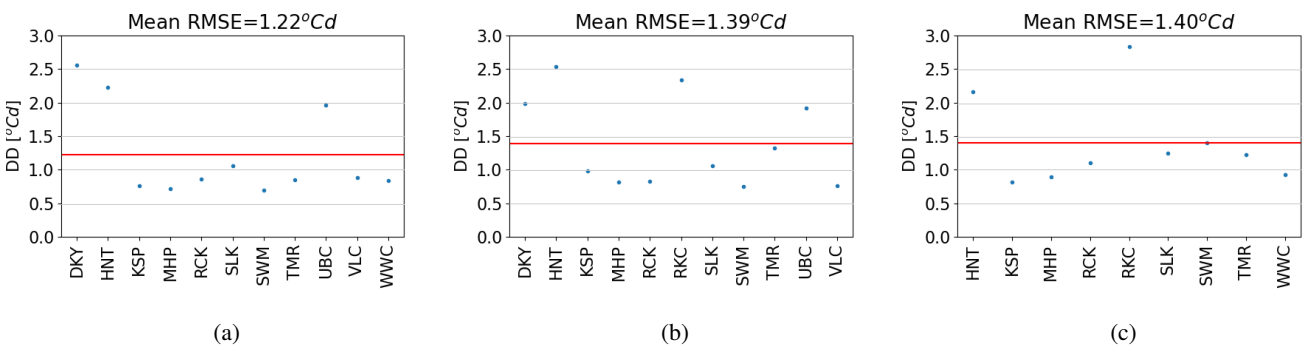



Figure B1. Leave-one-out cross validation results for the SFSJR for the hydrological seasons a) 2018/19, b) 2019/20 and c) 2020/21.

interpolation is tested through a leave one out (LOO) cross-validation. The results in terms of root mean square error (RMSE) are reported in Fig. B1 for SFSJR and in Fig. B2 for Schnals, showing a mean RMSE that never exceeds 1.5^{o}Cd.

Appendix C: SWE results for the South Fork of the San Joaquin River

Fig. C1 shows the SWE maps derived with the proposed method, the ASO reference maps, the bias calculated as the difference between the proposed and the reference maps and the dispersion graphs for the 12 analyzed dates over three hydrological seasons (2018-2021) for the SFSJR. The maps have a spatial resolution of 50 m. The scatterplots suggest a dispersion, even though most of the points are generally concentrated on the diagonal.

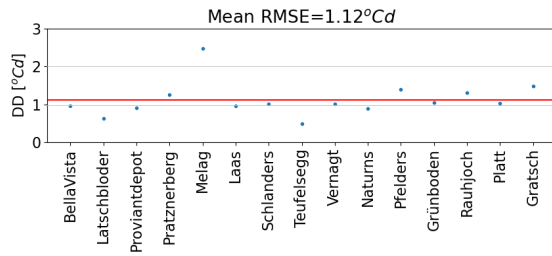
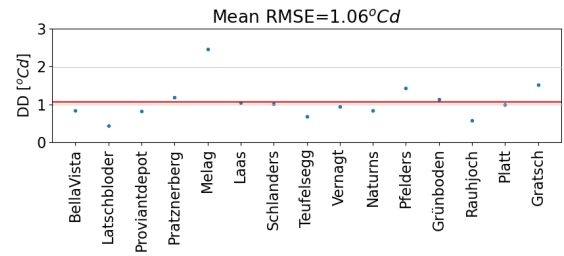
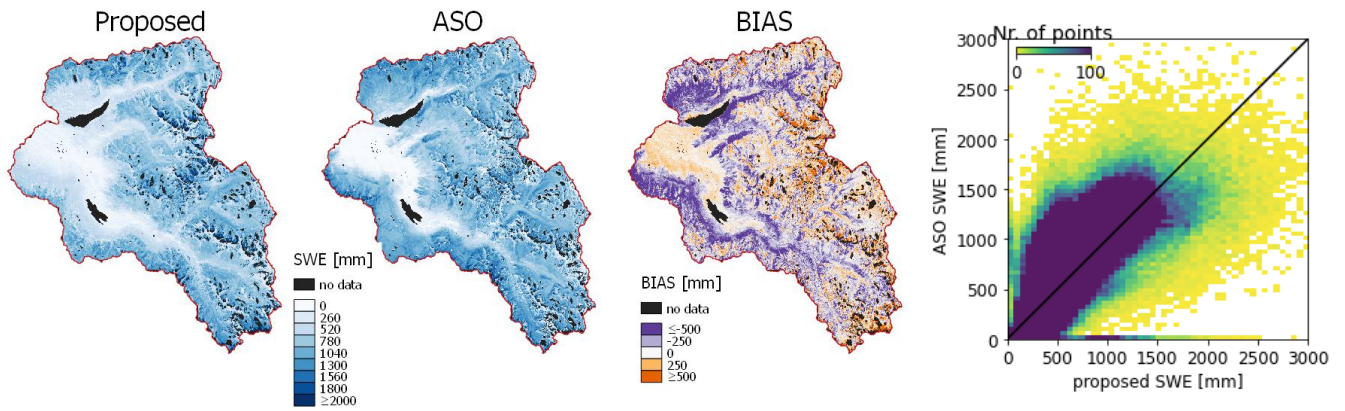
Similarly, Fig. C2 shows the SWE maps derived with the proposed method, the ASO SWE maps, the WUS-SR SWE maps, and the dispersion graphs between the proposed and the WUS-SR SWE for the same 12 analyzed dates over three hydrological seasons (2018-2021) for the SFSJR. The maps have a spatial resolution of 500 m.

(a)   (b)

Figure B2. Leave-one-out cross validation results for the Schnals catchment for the hydrological seasons a) 2019/20 and b) 2020/21).

Fig. C3 shows the mean SWE calculated for different elevation, slope and aspect bands for the 12 dates when also the ASO reference is available. The analysis is carried out for the proposed method and ASO only, as the high spatial resolution allows for a better appreciation of the complex topographical variability. We can notice a general good agreement showing that the proposed method is able to represent the typical topographical variability of the snow processes. The two datasets show similar trends when compared for different elevation belts. In general, a tendency of the proposed maps to underestimate SWE for lower elevations can be observed, while overestimating SWE for higher elevations. The slope analysis shows larger differences, especially for some dates (i.e., 9 June 2019 and the three images acquired for year 2020) and when considering steep slopes. The proposed method underestimates SWE w.r.t. ASO. However, we generally expect lower SWE for these steeper slopes that promote gravitational transport. The aspect analysis suggests an underestimation for the north facing slope when comparing our dataset with ASO (except for year 2021).

In conclusion, we also present in Table C1 the results of the intercomparison between the proposed SWE and the WUS-SR dataset versus ASO for the SFSJR. Bias, RMSE, and correlation are calculated pixel-wise. To this purpose, the proposed and ASO maps were aggregated at a resolution of 500 m. It is possible to notice that the proposed SWE presents a higher bias (an average of -34 mm versus 16 mm), while the RMSE is lower (151 mm versus 193 mm) and the correlation is higher (0.83 versus 0.65).

Author contributions. VP and CM designed the research; VP carried out the experiments and processing; RB provided the HR snow maps from S2; all the authors contributed to the analysis and interpretation of the results; VP wrote the paper based on inputs and feedbacks from all coauthors.

Competing interests. The authors declare that they have no conflict of interest.

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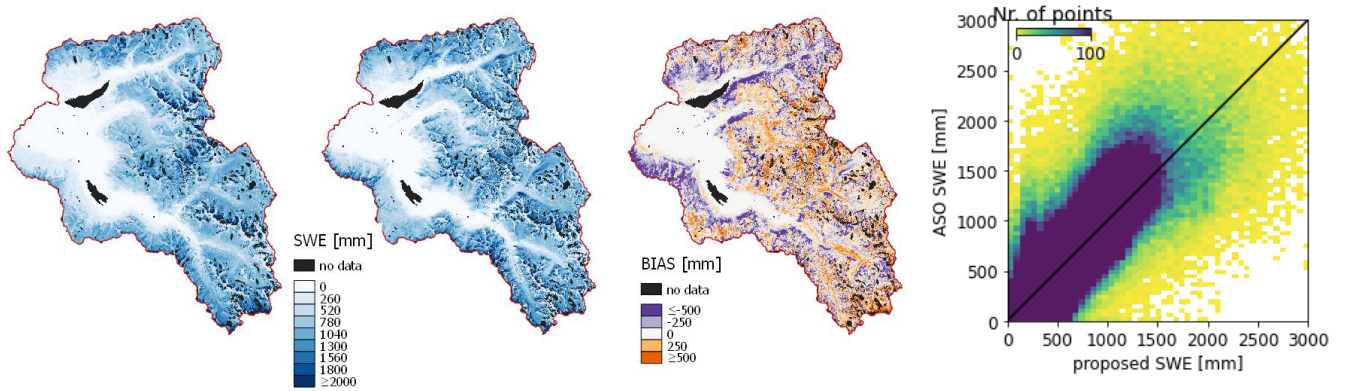
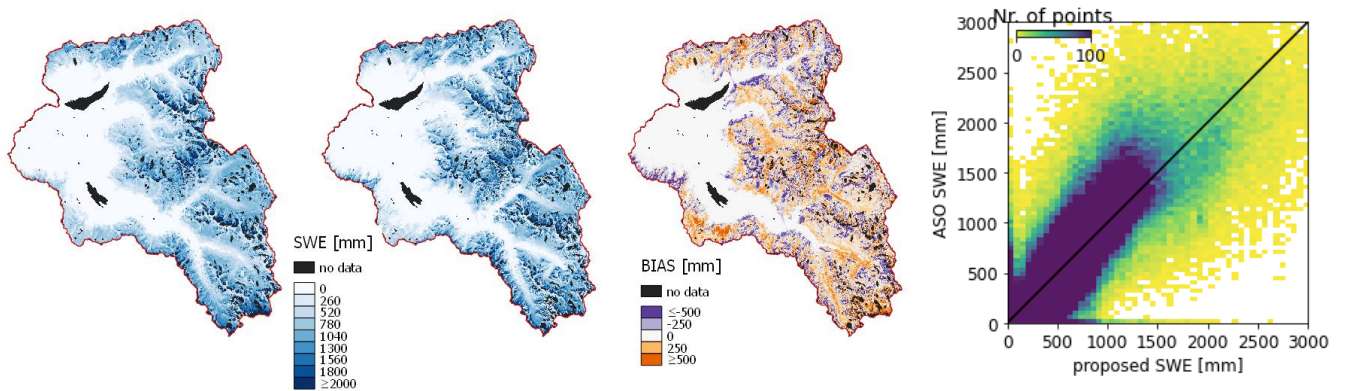
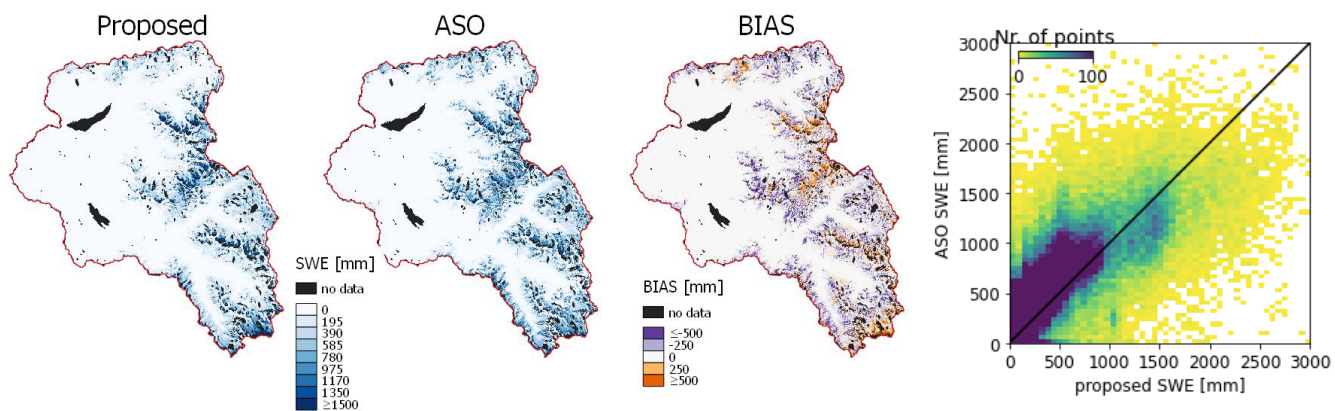
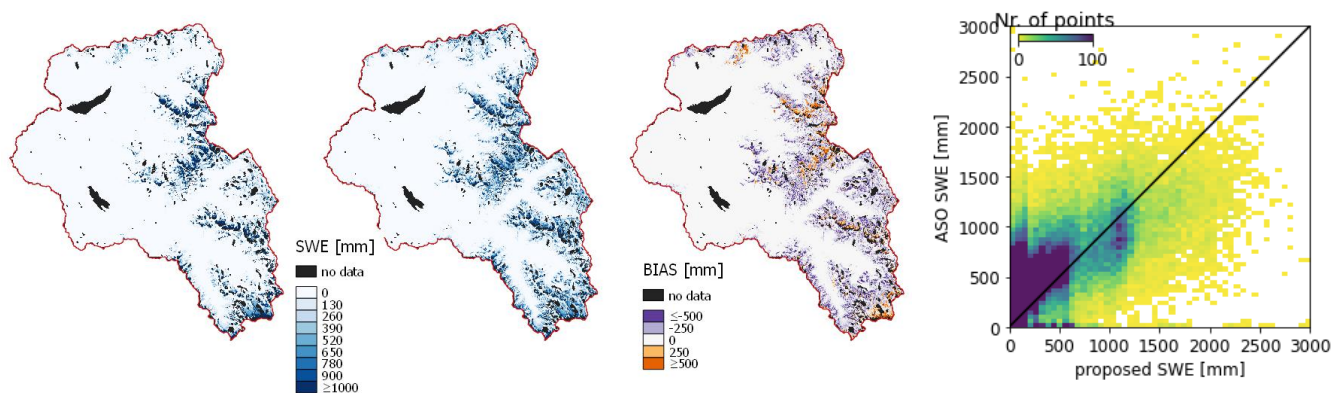

(b) 2 May 2019.

(c) 9 June 2019.

Figure C1. Proposed SWE (left), ASO SWE (centre-left), bias (centre-right) and dispersion graph (right) for the 12 analyzed dates over the three hydrological seasons (2018-2021) for the SFSJR.

(d) 4 July 2019.

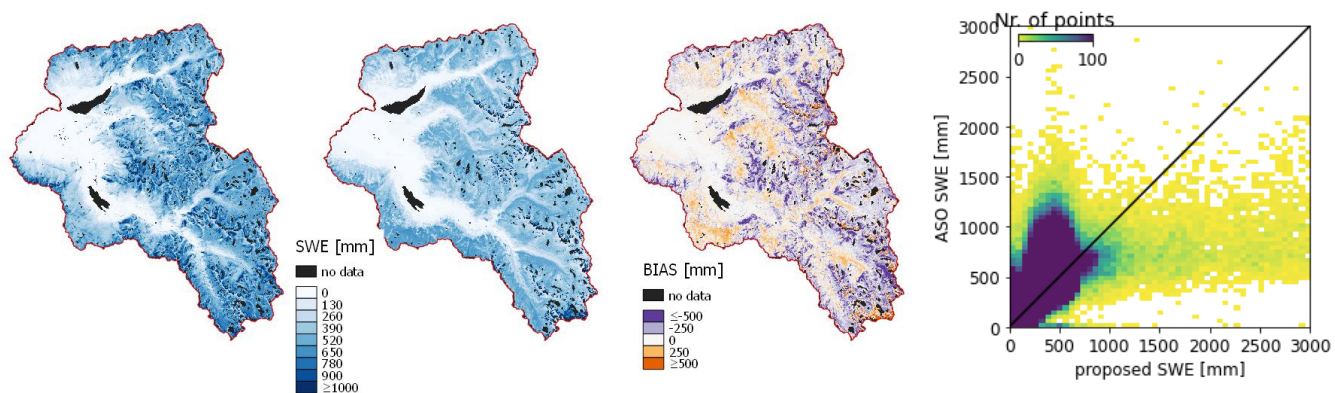
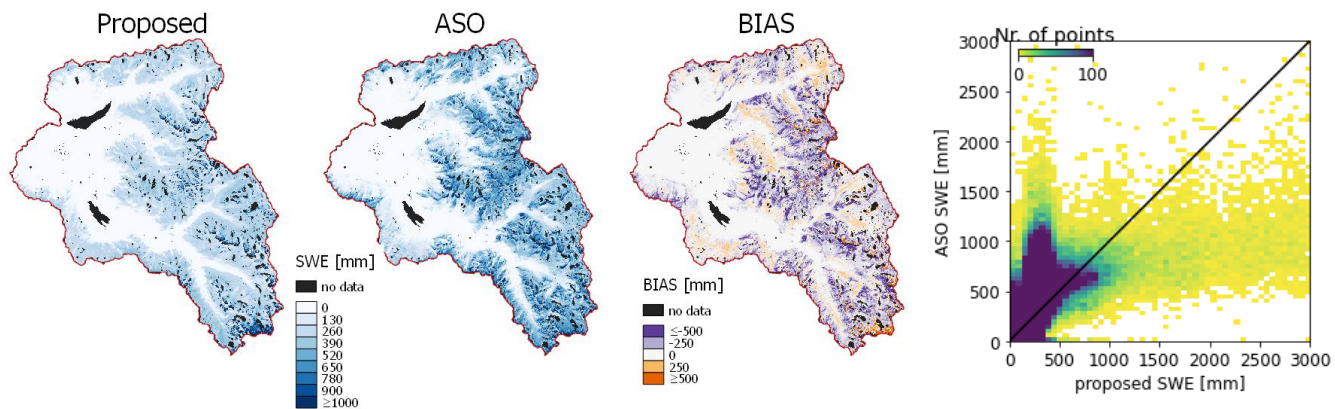
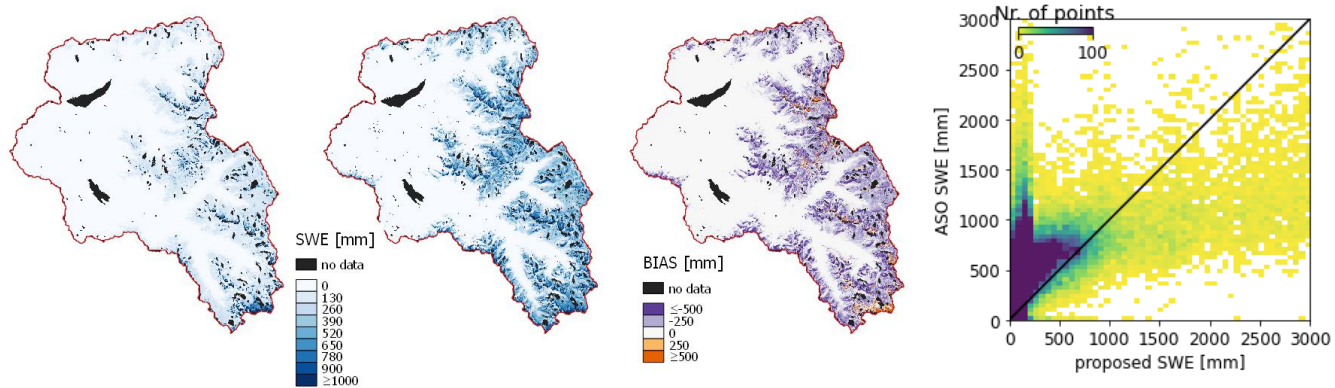
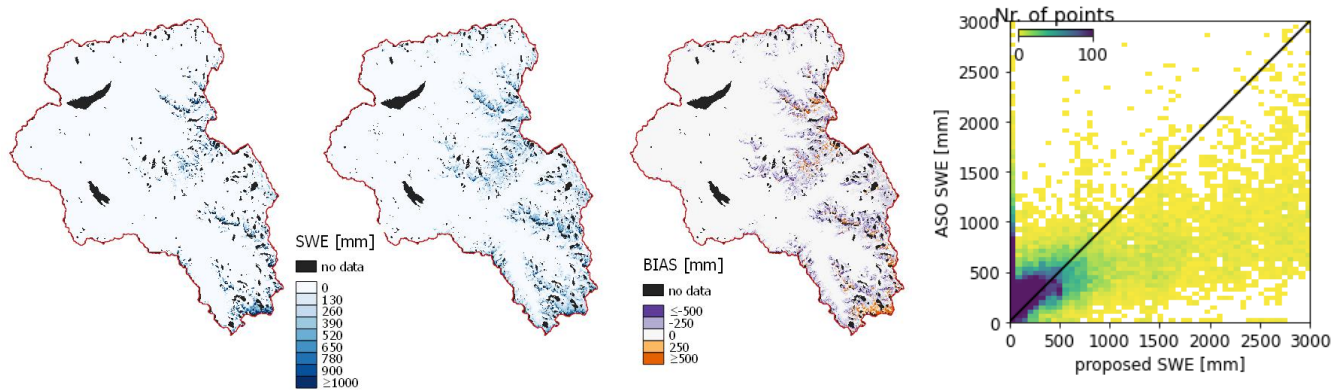
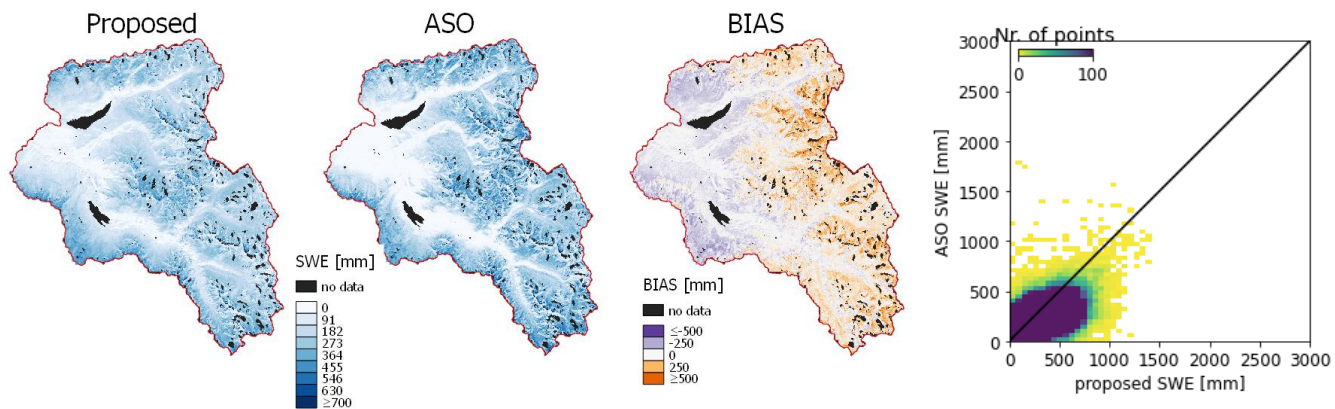
(e) 14 July 2019.

(f) 15 April 2020.

Figure C1. Proposed SWE (left), ASO SWE (centre-left), bias (centre-right) and dispersion graph (right) for the 12 analyzed dates over the three hydrological seasons (2018-2021) for the SFSJR. (cont.)

(g) 5 May 2020.

(h) 23 May 2020.

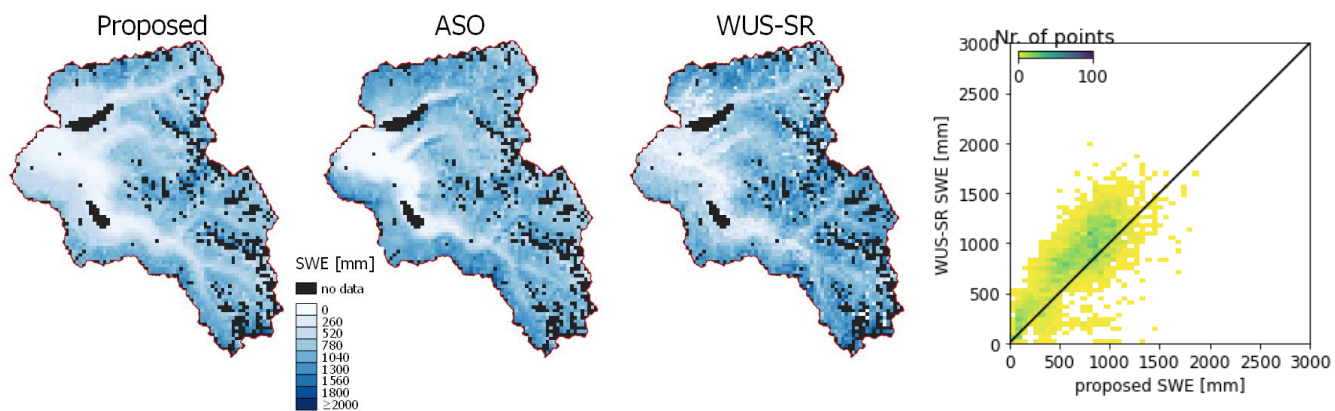
(i) 8 June 2020.

Figure C1. Proposed SWE (left), ASO SWE (centre-left), bias (centre-right) and dispersion graph (right) for the 12 analyzed dates over the three hydrological seasons (2018-2021) for the SFSJR. (cont.)

Proposed — ASO — BIAS

(j) 26 February 2021.

(k) 31 March 2021.

(l) 3 May 2021.

Figure C1. Proposed SWE (left), ASO SWE (centre-left), bias (centre-right) and dispersion graph (right) for the 12 analyzed dates over the three hydrological seasons (2018-2021) for the SFSJR. (cont.)

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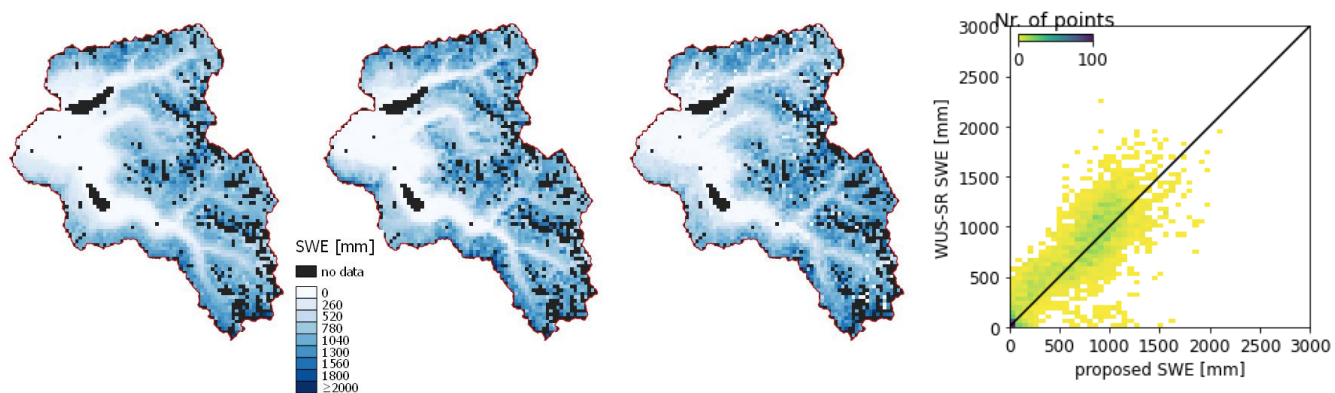
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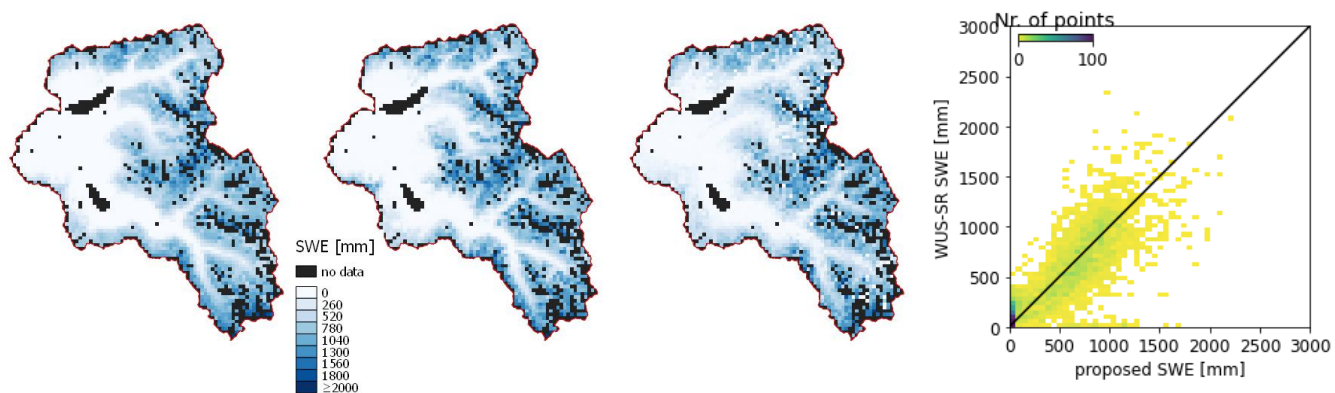
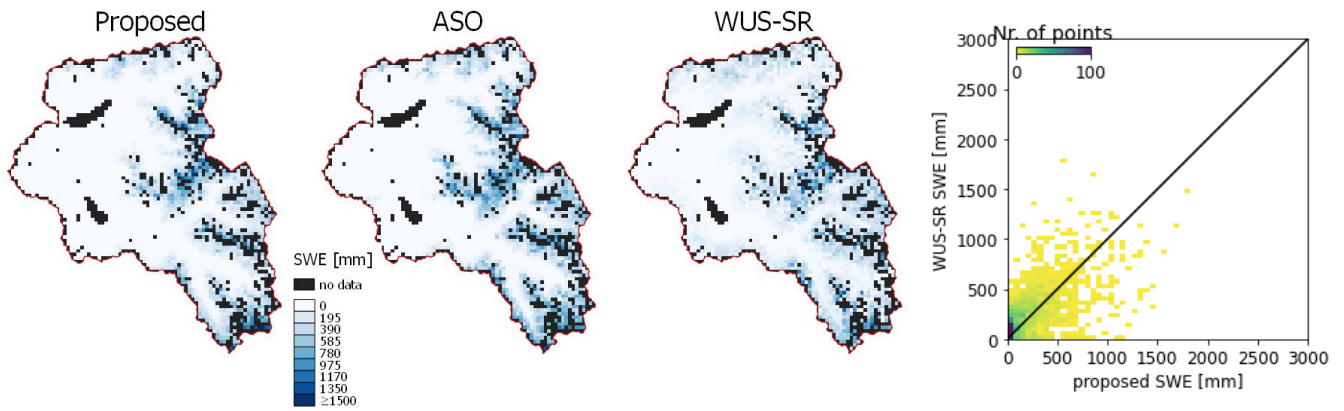
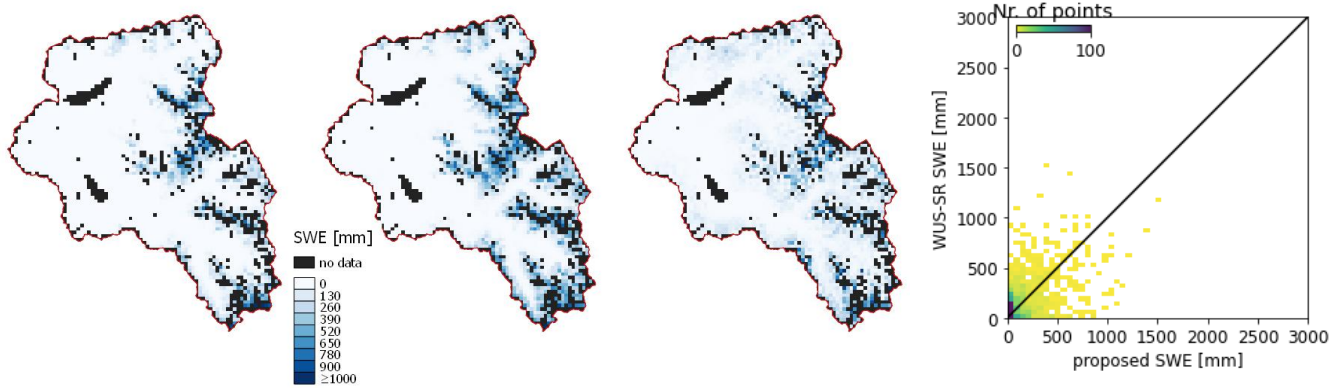

(c) 9 June 2019.

Figure C2. Proposed SWE (left), ASO SWE (centre-left), WUS-SR SWE (centre-right) and dispersion graph (right) for the 12 analyzed dates over the three hydrological seasons (2018-2021) for the SFSJR.

(d) 4 July 2019.

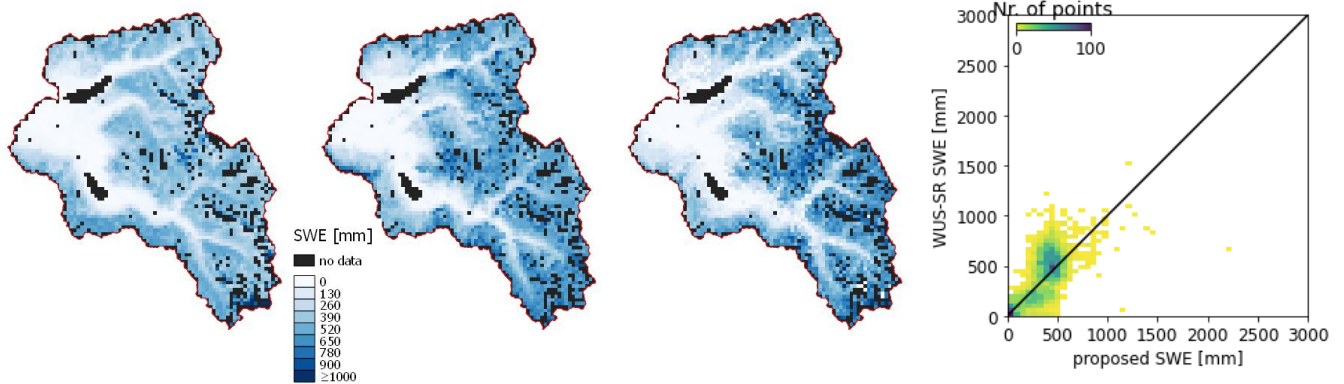
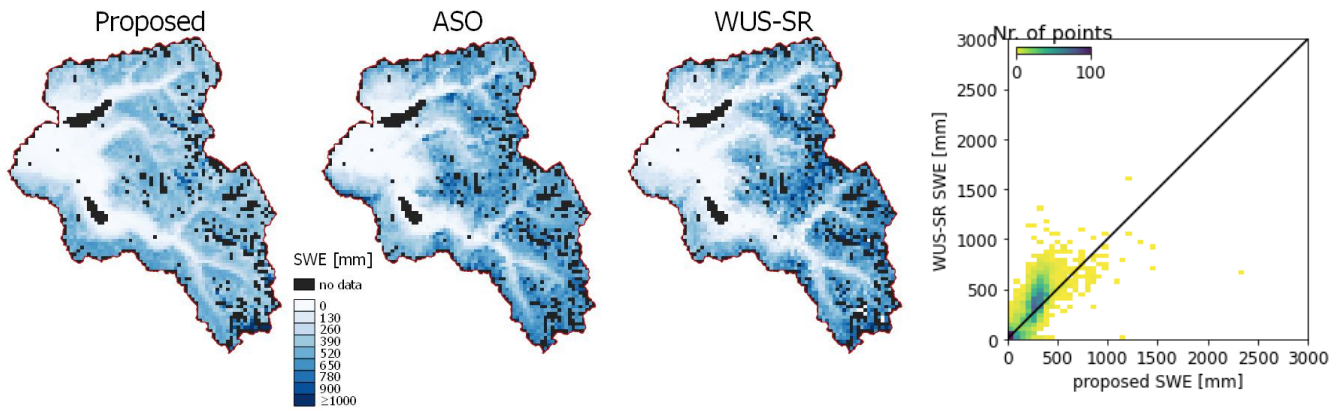
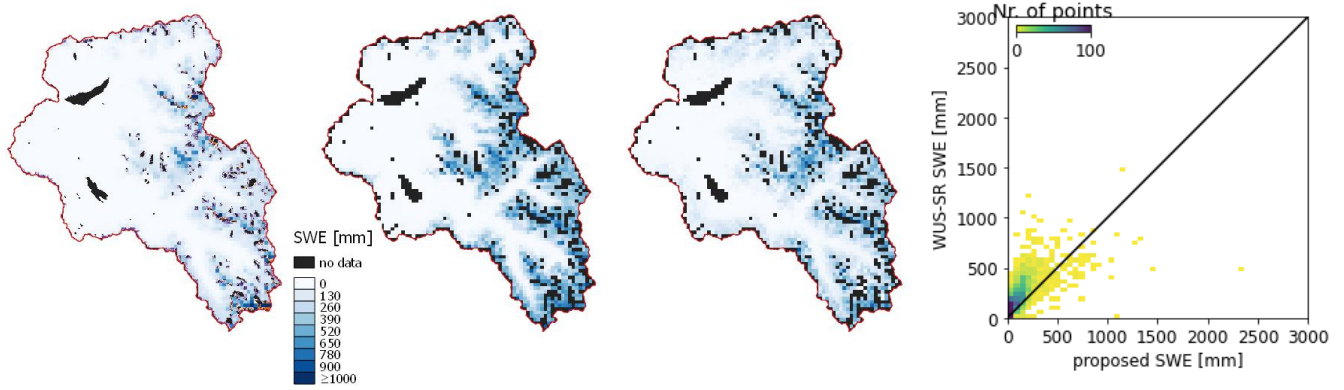
(e) 14 July 2019.

(f) 15 April 2020.

Figure C2. Proposed SWE (left), ASO SWE (centre-left), bias (centre-right) and dispersion graph (right) for the 12 analyzed dates over the three hydrological seasons (2018-2021) for the SFSJR. (cont.)

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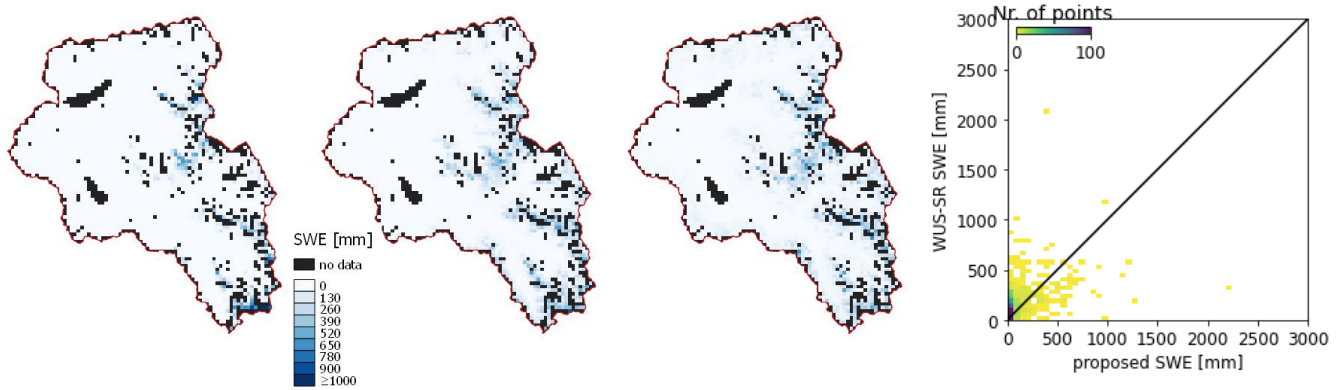
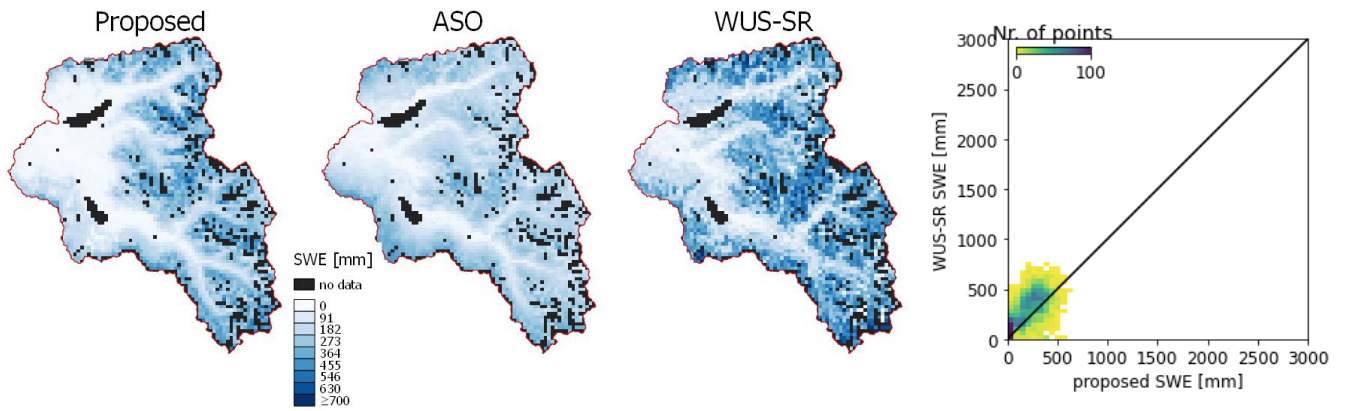

(h) 23 May 2020.

(i) 8 June 2020.

Figure C2. Proposed SWE (left), ASO SWE (centre-left), bias (centre-right) and dispersion graph (right) for the 12 analyzed dates over the three hydrological seasons (2018-2021) for the SFSJR. (cont.)

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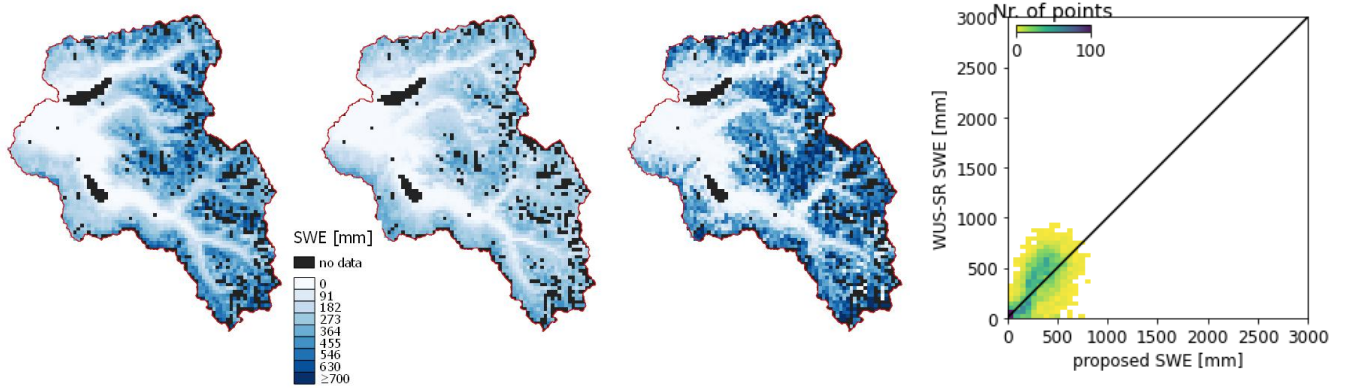
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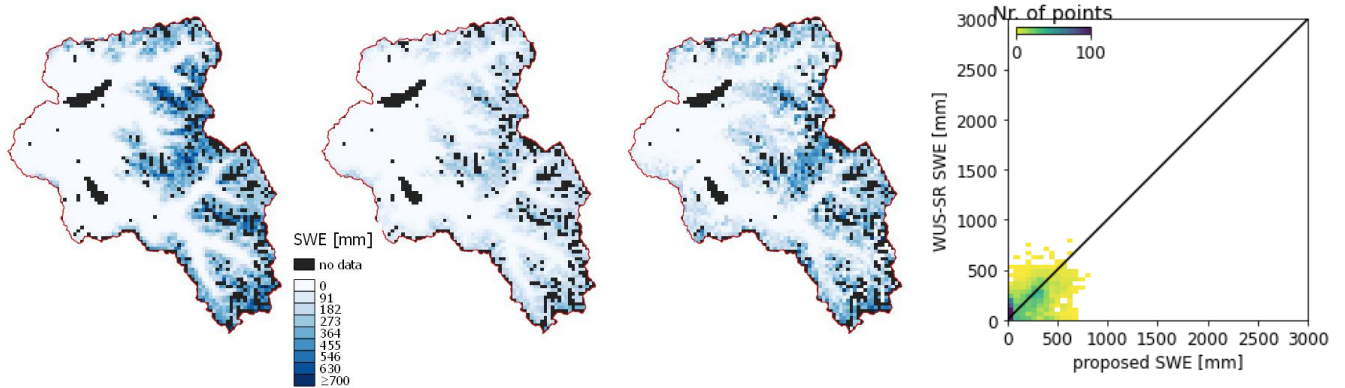
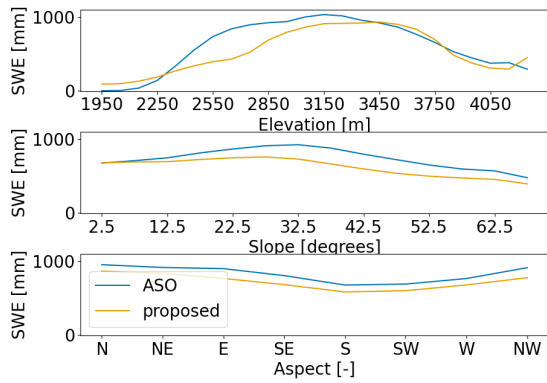

(l) 3 May 2021.

Figure C2. Proposed SWE (left), ASO SWE (centre-left), bias (centre-right) and dispersion graph (right) for the 12 analyzed dates over the three hydrological seasons (2018-2021) for the SFSJR. (cont.)

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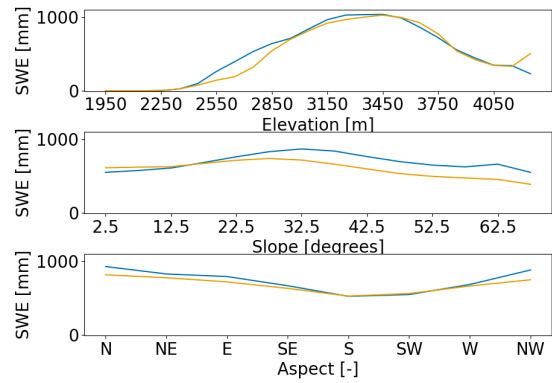
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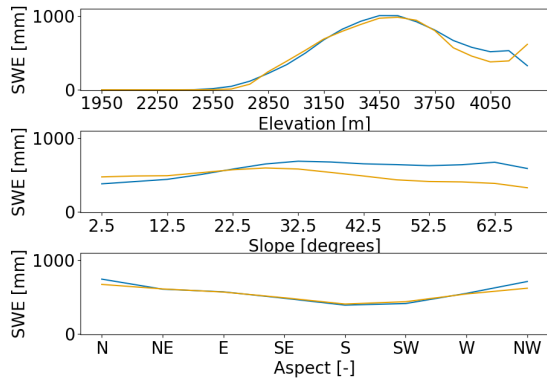
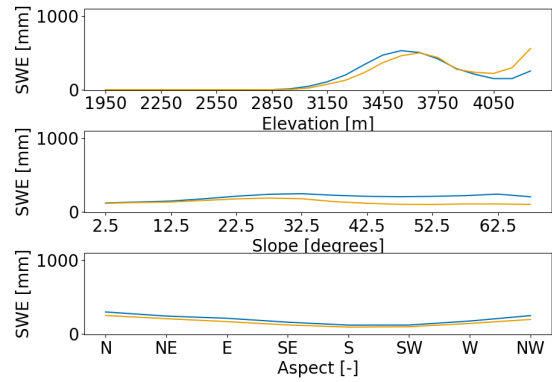

(c) 9 June 2019.

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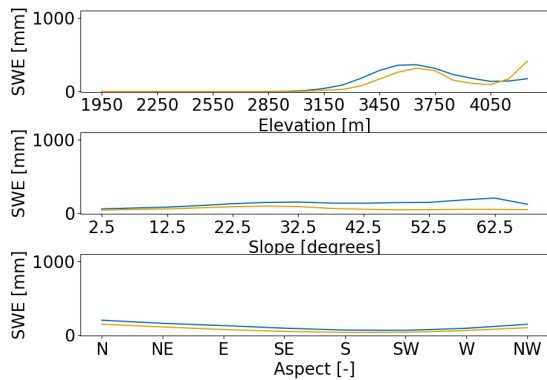
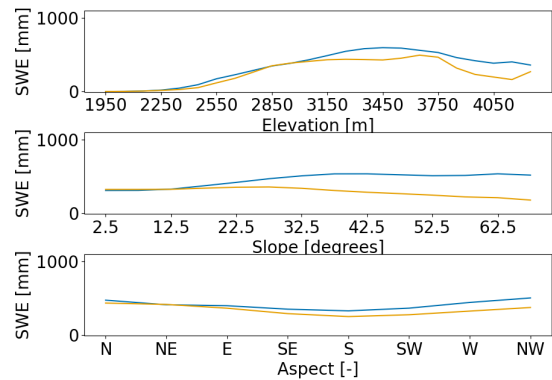
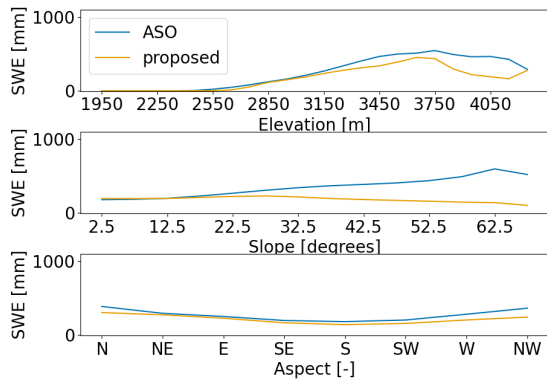

(e) 14 July 2019.

(f) 15 April 2020.

Figure C3. Mean SWE value for different elevation, slope and aspect belts. The proposed SWE dataset (in orange) is evaluated against ASO (in blue) for the 12 analyzed dates over the three hydrological seasons (2018-2021) for the SFSJR.

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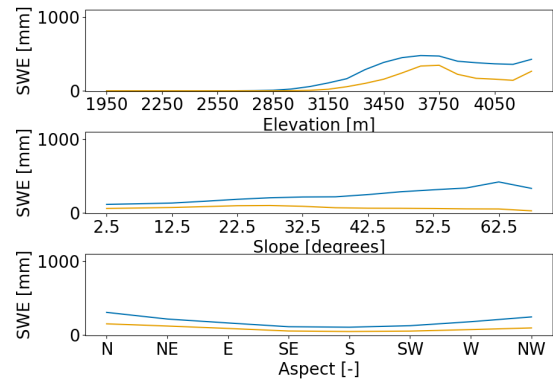
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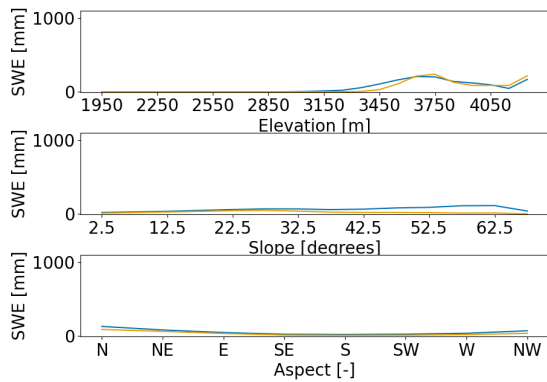
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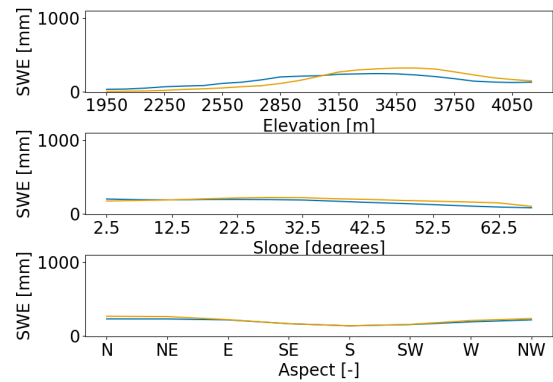
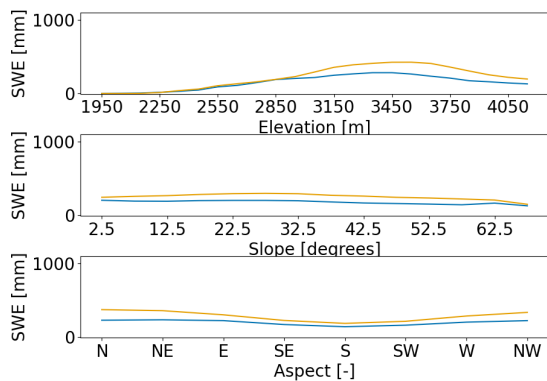
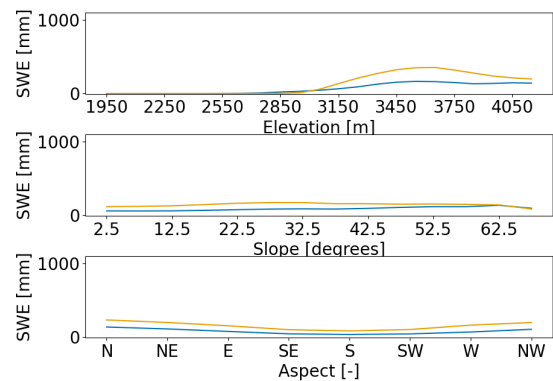

(j) 26 February 2021.

(k) 31 March 2021.

(l) 3 May 2021.

Figure C3. Mean SWE value for different elevation, slope and aspect belts. The proposed SWE dataset (in orange) is evaluated against ASO (in blue) for the 12 analyzed dates over the three hydrological seasons (2018-2021) for the SFSJR (cont.).

Table C1. Results of the intercomparison between the proposed SWE and the WUS-SR dataset versus ASO for the SFSJR. Bias, RMSE, and correlation are calculated pixel-wise. To this purpose, the proposed and ASO SWE maps were aggregated at a resolution of 500 m.

Date	BIAS [mm]		RMSE [mm]		Correlation [-]	
	proposed	WUS-SR	proposed	WUS-SR	proposed	WUS-SR
2019/03/17	-121	36	242	292	0.80	0.66
2019/05/02	-61	-4	208	307	0.90	0.77
2019/06/09	-25	-32	182	302	0.93	0.79
2019/07/04	-49	-14	129	201	0.90	0.71
2019/07/14	-51	-20	125	163	0.84	0.65
2020/04/15	-73	-26	159	169	0.80	0.78
2020/05/05	-59	5	151	154	0.82	0.80
2020/05/23	-95	-27	179	150	0.79	0.78
2020/06/08	-25	3	96	100	0.72	0.70
2021/02/26	5	96	92	157	0.75	0.65
2021/03/31	74	119	124	202	0.85	0.72
2021/05/03	65	54	121	121	0.89	0.66

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