Permafrost saline water and Early to Mid-Holocene permafrost aggradation in Svalbard

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Abstract. Deglaciation in Svalbard was followed by seawater ingestion and deposition of marine (deltaic) sediments in fjord valleys, while elastic rebound resulted in fast land uplift and the exposure of these sediment to the atmosphere, in which the formation of epigenetic permafrost formed. This was then followed by the accumulation of aeolian sediments, with syngenetic permafrost formation. Permafrost was studied in the eastern Adventdalen Valley, Svalbard, 3-4 km from the maximum up-valley reach of post-deglaciation seawater ingestion, and its ground ice was analyzed for its chemistry. While ground ice in the syngenetic part is basically fresh, the epigenetic part has a frozen fresh-saline water interface (FSI), with chloride concentrations increasing from the top of the epigenetic part (at 5.5 m depth) to about 15\% that of seawater at 11 m depth. We applied a one-dimensional freezing model to examine the rate of top-down permafrost formation, which could accommodate with the observed frozen FSI. The model examined permafrost development under different scenarios of mean average air temperature, water-freezing temperature and the degree of pore-water freezing. We found that even at the relatively high air temperatures of the Early to mid-Holocene, permafrost could aggrade quite fast down to 15 to 33 m (the whole sediment fill of 20 m at this location) within 200 years. This, in turn, allowed freezing and preservation of the fresh-saline water interface despite of the relatively fast rebound rate, which apparently resulted in an increase in topographic gradients toward the sea. Permafrost aggradation rate could also be enhanced due to non-complete pore water freezing. We conclude that freezing must have started immediately after the exposure of the marine sediment to atmospheric conditions.
1. Introduction

Cycles of global warming and cooling are well documented in the geological history (e.g., Imbrie et al., 1993; Benn & Evans, 2014; Arnscheidt & Rothman, 2020). During the Pleistocene, these cycles followed Northern Hemisphere glaciation and deglaciation, which influenced both marine and land temperatures (Park et al., 2019). This also affected the extent of cryotic conditions in the periglacial environment (e.g. Murton, 2021), i.e., the distribution of permafrost, which currently covers 22% of the Northern Hemisphere land areas (Obu et al., 2019). While temperatures during the Holocene were significantly higher than during the Last Glacial period, the retreat of glaciers and the follow-up elastic rebound and exposure of new land in the Arctic and the sub-Arctic environment allowed freezing and the aggradation of permafrost (e.g. Landvik et al., 1988). Nevertheless, the relatively high temperatures during the Early and the mid-Holocene warm period raise questions about the timing of initiation and the extent of this process (e.g. Landvik et al., 1988; Humlum, 2005).

In Svalbard (Fig. 1), the fast retreat of glaciers during the end of Late-Pleistocene into the beginning of the Holocene resulted in the ingression of seawater in fjord valleys, which was followed by gradual uplifting and exposure due to elastic rebound. This resulted in epigenetic permafrost aggradation followed by the deposition of fluvial and aeolian sediments, and the formation of syngeneric permafrost during the last ca. 4 ka (Gilbert et al., 2018). In the present study, we use the presence of saline water in the epigenetic permafrost to constrain the timing of freezing.

Permafrost is a soil or rock, which has been below 0°C for at least two consecutive years (French, 2017). While winter freezing of the ground is common in a large extent of land areas, the existence of permafrost and its aggradation depends on the annual energy balance between atmosphere and the land (Black, 1954). Accordingly, permafrost develops when the land heat loss during winter exceeds the gain during the summer for long enough time. This is controlled by both seasonal solar radiation and the soil/rock thermal properties. Heat exchange between soil and the atmosphere is also strongly affected by land cover, whereby permafrost is usually not developed neither under the sea nor beneath warm-based glaciers (Waller et al., 2012). Nevertheless, permafrost can be present associated with taliks beneath lagoons as well as beneath bottom-fast ice in shallow water (Solomon et al., 2008). The extent and depth of permafrost can be significantly reduced by thick vegetation or snow cover (e.g. Grünberg et al., 2020).

During the last glacial cycle, the Barents Sea and the Svalbard area (Fig. 1) were covered by one to three ice caps (Mangerud et al., 2002; Patton et al., 2017). Glacier retreat has been followed since by
elastic rebound, which is well documented in Svalbard (Bondevik et al., 1995; Lønne & Nemec, 2004; Sessford et al., 2015), with a land rise of up to 130 m in eastern Svalbard and 65 m in the western part of the archipelago (Forman, 2004). In western Svalbard, the focus of this study, research indicates a fast land rise of 19-15 mm y\(^{-1}\) during Early to the mid-Holocene (11.7 – 8.2 ka BP), which decreased to 5 - 4 mm y\(^{-1}\) toward the end of mid-Holocene (Salvigsen, 1984; Sessford et al., 2015) and ca. 1 mm y\(^{-1}\) during the late Holocene (last 4 ka, e.g. Forman et al., 2004).

Land uplift and exposure is accompanied by the establishment of a surficial drainage system, as well as the development of a groundwater flow network, which strongly depends on the rate of permafrost deepening (Edmunds et al., 2001). The permeability of frozen soils is greatly reduced (Burt and Williams, 1976; Cochand et al., 2019), such that extensive permafrost prevents penetrating of surface water and recharging of groundwater (McEwen & de Marsily, 1991). While in sporadic and discontinuous permafrost, groundwater flow is possible through non-frozen sections or taliks, flow is practically impossible through continuous permafrost land areas (Lemieux et al., 2008; Walvoord and Kurylyk, 2016), while it may be active in sub-permafrost zones. Flow may also be enhancing cryopegs which holds overcooled liquid brines (Ahonen 2001), or move among existing cryopegs (Iwahana et al., 2021).

Although cryopegs was identified in Adventdalen (Tavacoli et al., 2021), water paths were not yet described. Water flow along faults in continuous permafrost has been described in Adventdalen Svalbard in relation to pingos (Hornum et al., 2021).

According to the Ghyben-Hertzberg approximation (Bear & Dagan 1964; Verruijt 1968), depth from seawater level to the fresh-saline water interface should be about 1:40 of the groundwater head above sea level. This ratio increases with decreasing salinity of saline water. With typical Early to mid-Holocene rebound rates of 15 to 4.5 mm y\(^{-1}\) (Sessford et al., 2015), and assuming that the groundwater table (saturated conditions) followed the topography, the fresh-saline interface is expected to be pushed downwards to as deep as 120 to 36 m respectively, within 200 years after exposure. A groundwater table of 1 m below the surface would result in a delay of 100 to 200 years, but also in this case a sediment section of tens of meters will be completely flushed within several hundred years. This is unless sediment freezing practically halts flow in the subsurface.

The objective of this paper is to test the presented hypothesis by studying the ground ice geochemistry of a permafrost core from Adventdalen, Svalbard, and by using a 1-D numerical heat transfer model to simulate permafrost aggradation under various surface temperature conditions and degrees of freezing.
2. Study site

Adventdalen is a U-shaped glacially eroded valley located in western Spitsbergen, Svalbard, centred on 78.110N, 16.180E (Fig. 1a). During the last glacial cycle, the valley was eroded to the basement, which was then covered by glacial deposits (Elverhøi et al., 1995; Gilbert et al., 2018). This was followed by deglaciation, which was completed ca. 10.5 ka BP (Mangerud et al., 1992; Svendsen & Mangerud, 1997; Lønne & Lyså, 2005; Farnsworth et al, 2020). Deglaciation was followed by up-valley seawater ingressation, up to 13.5 km from the current end of the fjord (Cable et al., 2018; Lønne & Nemec, 2004) and subsequent valley infilling with sediment and a delta front prograding downvalley. Elastic rebound resulted in the exposure of the eastern part of the valley before 9.5 ka BP, which progressed down-valley, arriving at the current coastline location at about 4 ka (Gilbert et al., 2018). The exposed surface was first covered by fluvial sediments, followed by aeolian deposits during 4-2 ka (Gilbert et al., 2018). Permafrost in Svalbard, both epigenetic and syngenetic, is continuous and is estimated to be >100 m thick in the valleys (Humlum, 2005). The active-layer thickness is commonly 60–100 cm in the valley bottom sediments (Christiansen and Humlum, 2003; Gilbert et al., 2018; Weinstein et al., 2019; Strand et al., 2020).

Meteorological data is measured continuously for more than 100 years at the Svalbard Airport (e.g. Nordli et al., 2020), located on the Adventfjorden coast, ca. 12 km northwest of our study site. Mean annual air temperature (hereafter MAAT) was −5.9 °C from 1971 to 2000, although in 2018 it was merely -1.8 °C. Mean annual precipitation during 1971-2000 was 196 mm, while in 2018 it was 177 mm (Strand et al., 2021). MAAT and sea surface temperature during Early to the mid-Holocene was 2-4 °C higher than today, as suggested by marine mollusc’s shells (Mangerudn & Svendsen, 2018), lacustrine alkenons (van der Bilt et al., 2018), flora DNA (Alsos et al., 2016) and models incorporating physical and biological considerations (e.g. Park et al., 2019). Since the mid-Holocene, a continuous decline in MAAT is recorded, which changed into a fast temperature rise during the last several decades (e.g. Christiansen et al., 2013).

The study site, Adventdalen East (ADE), is located on a river terrace (78.1722° N 16.0613° E), 9.8 km upvalley from the Adventfjorden at 23 m a.s.l (Fig. 1a and b). We drilled at the same S1 location as Gilbert et al., (2018). The permafrost section (valley-fill sediments) at the ADE site (ca. 20m) consists of a syngenetic part from 1.0- 5.5 m depth, which includes a shallow 1.5 m of fine-grained aeolian deposits and thick ice bodies of segregation ice intruded above fluvial gravel channel fill (Gilbert et al., 2018).
Below 5.5 m the epigenic permafrost consists of 3-4 m of fluvial sediments (mud and pebbles, ice-rich). This is underlain by back-delta, deltaic and fore-delta sediments (5.5-17.5 m), which cover glacial sand deposits (17.5-20 m) (Gilbert et al., 2018). The study site was deglaciated by 11.3 ka and emerged above seawater at 9.2 ka (Gilbert et al., 2018), exposing it to atmospheric conditions then, which allowed the development of a groundwater system on one hand and possibly the aggradation of permafrost on the other hand.
Figure 1. (a) Study site ADE is located at the Adventdalen, Svalbard, on a river terrace. Map provided with courtesy of Norwegian Polar Institute. (b) Drilling at ADE, spring 2017 top. Cores samples before processing at UNIS cold room lab, bottom.

3. Methods

Two cores, placed 0.5 m apart, one 13 m and the other 9 m long, were retrieved at ADE in March 2017, using the UNIS permafrost drill-rig (Gilbert et al., 2015), which has core barrels of 43 mm diameter (ID). Core length, borehole depth, core condition, and gravel content were recorded in the field. Retrieved core sections were placed in plastic bags and marked with a serial number and an arrow pointing towards the core top. Cores were stored at -18°C in a freezer at UNIS until processing. Cores were sectioned in
a cold room (-5°C) to 0.5 m depth intervals (Fig 1b). Intervals of the same depth in the two cores were combined to gain enough ground-ice per section for Ra isotope measurements. Samples were first scraped and then crashed to small chips, which were placed in 250 ml centrifuge tubes. Ra-free water (up to 40 ml) was added to some of the tubes, to facilitate the extraction of pore fluid. Samples were then thawed in a microwave set to 600 W for 2 min, followed by centrifuging for 8 min (11,000 RPM, high G) to separate thawed water from the soil. Extracted water was run through 3 μm, followed by 0.45 μm filters. Most of the water was used for Ra isotopes analysis (see Weinstein et al., 2019), while 30-60 ml was used for chemistry analyses. Water of the added Ra-free water was analysed to correct for element concentrations. Major elements were analysed in the Geological Survey of Israel (GSI) by ICP-AES (Optima 3000), where Sc was added as an internal standard, whereas Cl⁻ and SO₄²⁻ was determined by potentiometer titration, using Metrohm 702 SM Titrino Titrator connected to a chlorine electrode. The error for all majors is considered less than 5%.

4. Ground ice chemistry

Major elements of thawed ground ice are presented in Table 1 and concentration profiles of Cl⁻, Na²⁺ and SO₄²⁻ are shown in Fig. 2 a-c. While the salinity of ground ice in the syngenetic permafrost is that of fresh water (e.g. Cl⁻: 10-74 mg L⁻¹, Na²⁺: 10-33 mg L⁻¹ and SO₄²⁻: 9-31 mg L⁻¹), epigenetic permafrost ground ice demonstrates a trend of increasing concentrations down to 9-12 m depth: 440-3600, 80-2700 and 150-740 mg L⁻¹ of Cl⁻, Na²⁺ and SO₄²⁻, respectively. Between 9-12 m, concentrations are quite scattered, and the increasing pattern is less clear. While the Cl⁻ content (Fig. 2a) of the ground ice is no more than 15% seawater salinity, and the salinity of a deeper-seated saline water end member could be significantly higher, the observed increased salinity clearly presents a fresh-saline water interface.

The ionic ratio of Na²⁺ to Cl⁻ in both epigenetic and the syngenetic permafrost mostly exceeds 1 (Fig. 2d), significantly higher than in seawater (0.86), which is probably the result of sediment dissolution (e.g. of micas), since ion exchange should result in either a conservative behaviour (during freshening, as is the case in the ADE marine section) or in Na⁺ depletion (in the case of salinization, e.g. Russak and Sivan, 2010). On the other hand, SO₄/Cl in the epigenetic permafrost is close to that of seawater (Fig. 2f), implying a relative conservative behaviour. Nevertheless, SO₄/Cl in the syngenetic part is very variable (Fig. 2f), reaching ratios as high as 2, which could be due to shale dissolution (Hindshaw et al., 2016; Cabel et al., 2018). High concentration of SO₄ was also recorded in sub-permafrost (Pingo) water,
which was attributed to gypsum dissolution (Hodson et al., 2020). Ca/Cl decreases with depth in the syngenetic permafrost and is very low (<0.01) in the epigenetic permafrost (Fig. 2e), which is in agreement with freshening experiments in fresh-saline water zones (Russak and Sivan 2010). The high ratio of Ca/Cl and SO$_4$/Cl at -5.45 m depth is enigmatic and may present paleo active layer - permafrost table zone were major and minor elements concentrate (e.g. Cary and Mayland, 1972; Kokelj et al., 2002) but it should be further studied.

Table 1. Major elements (mg/L) of grownd-ice samples of the ADE core.

| Sample name | Depth (m) | Permafrost Type | Cl$^-$ | Br$^-$ | SO$_4^{2-}$ | SiO$_2$ | Na$^+$ | K$^+$ | Sr | Ca$^{2+}$ | Mg$^{2+}$ | Freezing state of sample
<table>
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<tbody>
<tr>
<td>Sea water conc.$^2$</td>
<td></td>
<td></td>
<td>19,354</td>
<td>67.3</td>
<td>2,712</td>
<td>10,760</td>
<td>399</td>
<td>7.9</td>
<td>412</td>
<td>1,290</td>
<td>15.1</td>
<td>Frozen</td>
</tr>
<tr>
<td>DR-AD-55</td>
<td>-1.3</td>
<td>Syngenetic</td>
<td>27.1</td>
<td>0.5</td>
<td>19.0</td>
<td>13.0</td>
<td>10.7</td>
<td>17.0</td>
<td>0.2</td>
<td>5.4</td>
<td>15.1</td>
<td>Frozen</td>
</tr>
<tr>
<td>DR-AD-58</td>
<td>-2.1</td>
<td>Syngenetic</td>
<td>12.8</td>
<td>0.6</td>
<td>30.7</td>
<td>14.0</td>
<td>19.8</td>
<td>4.1</td>
<td>0.4</td>
<td>8.8</td>
<td>27.8</td>
<td>Frozen</td>
</tr>
<tr>
<td>DR-AD-52</td>
<td>-2.9</td>
<td>Syngenetic</td>
<td>74.1</td>
<td>0.7</td>
<td>8.9</td>
<td>9.0</td>
<td>13.6</td>
<td>44.7</td>
<td>0.6</td>
<td>12.7</td>
<td>35.2</td>
<td>Frozen-icy</td>
</tr>
<tr>
<td>DR-AD-57</td>
<td>-3.3</td>
<td>Syngenetic</td>
<td>13.9</td>
<td>0.5</td>
<td>27.9</td>
<td>5.9</td>
<td>32.6</td>
<td>4.4</td>
<td>0.1</td>
<td>3.6</td>
<td>7.6</td>
<td>Frozen-icy</td>
</tr>
<tr>
<td>DR-AD-56</td>
<td>-3.5</td>
<td>Syngenetic</td>
<td>10.0</td>
<td>0.3</td>
<td>12.3</td>
<td>5.3</td>
<td>13.3</td>
<td>4.5</td>
<td>0.1</td>
<td>1.5</td>
<td>2.6</td>
<td>Frozen-icy</td>
</tr>
<tr>
<td>DR-AD-61</td>
<td>-4.0</td>
<td>Syngenetic</td>
<td>14.5</td>
<td>0.7</td>
<td>13.0</td>
<td>11.6</td>
<td>9.5</td>
<td>5.2</td>
<td>0.2</td>
<td>3.6</td>
<td>8.8</td>
<td>Frozen</td>
</tr>
<tr>
<td>DR-AD-63</td>
<td>-4.7</td>
<td>Syngenetic</td>
<td>26.8</td>
<td>11.6</td>
<td>30.0</td>
<td>12.8</td>
<td>13.6</td>
<td>0.1</td>
<td>1.7</td>
<td>2.6</td>
<td>Frozen</td>
<td></td>
</tr>
<tr>
<td>DR-AD-59</td>
<td>-5.5</td>
<td>Epigenetic</td>
<td>67.4</td>
<td>0.6</td>
<td>146.6</td>
<td>20.9</td>
<td>83.3</td>
<td>16.0</td>
<td>0.5</td>
<td>13.6</td>
<td>27.0</td>
<td>Partly frozen</td>
</tr>
<tr>
<td>DR-AD-53</td>
<td>-6.3</td>
<td>Epigenetic</td>
<td>438.1</td>
<td>1.9</td>
<td>116.1</td>
<td>19.4</td>
<td>422.0</td>
<td>6.7</td>
<td>0.5</td>
<td>14.2</td>
<td>6.1</td>
<td>Frozen</td>
</tr>
<tr>
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<td>-7.1</td>
<td>Epigenetic</td>
<td>847.0</td>
<td>369.5</td>
<td>38.1</td>
<td>828.7</td>
<td>22.7</td>
<td>0.1</td>
<td>11.6</td>
<td>Frozen</td>
<td></td>
<td></td>
</tr>
<tr>
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<td>-8.3</td>
<td>Epigenetic</td>
<td>1678.4</td>
<td>465.1</td>
<td>21.2</td>
<td>1296.3</td>
<td>29.1</td>
<td>0.1</td>
<td>0.5</td>
<td>Frozen</td>
<td></td>
<td></td>
</tr>
<tr>
<td>DR-AD-67</td>
<td>-8.8</td>
<td>Epigenetic</td>
<td>3677.6</td>
<td>570.4</td>
<td>25.0</td>
<td>1680.1</td>
<td>55.6</td>
<td>0.1</td>
<td>2.2</td>
<td>Partly frozen</td>
<td></td>
<td></td>
</tr>
<tr>
<td>DR-AD-54</td>
<td>-9.4</td>
<td>Epigenetic</td>
<td>2145.1</td>
<td>7.9</td>
<td>508.2</td>
<td>9.1</td>
<td>2497.5</td>
<td>194.6</td>
<td>0.3</td>
<td>17.0</td>
<td>Partly frozen</td>
<td></td>
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<tr>
<td>DR-AD-66</td>
<td>-10.4</td>
<td>Epigenetic</td>
<td>3500.4</td>
<td>738.9</td>
<td>24.8</td>
<td>2705.8</td>
<td>42.4</td>
<td>0.4</td>
<td>9.5</td>
<td>Partly frozen</td>
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<tr>
<td>DR-AD-60</td>
<td>-11.8</td>
<td>Epigenetic</td>
<td>2412.6</td>
<td>7.0</td>
<td>408.1</td>
<td>20.5</td>
<td>2319.8</td>
<td>98.0</td>
<td>0.6</td>
<td>18.3</td>
<td>Partly frozen</td>
<td></td>
</tr>
</tbody>
</table>

$^1$ after Gilbert et al., 2018

$^2$ after de Baar et al., 2017, Salinity of 35%
Figure 2. Major element concentrations in ground ice from Adventdalen-East (ADE) deep drillhole: (a) Cl, (b) Na\(^+\) & (c) SO\(_4\)\(^2-\) in mg/L. Figures (d) - (f) present selected equivalent ratios along the profile. Dashed line separates the syngentic and the epigenetic permafrost (Gilbert et al., 2018).
5. Model of permafrost formation

5.1 Conceptual model

To study the rate of permafrost formation, we developed a numerical model that solves the temperature distribution in space and time and freezing front progression, i.e. Stefan solution (e.g., Šarler, 1995). Considering low horizontal temperature variations, the problem was reduced to one dimensional depth-dependent heat transfer with moving internal phase transition boundary. Various analytical and numerical methods have been developed to obtain stable solution of the Stefan problem (e.g., Crank, 1984). However, unlike the simple and clean single component systems, many natural systems, including water saturated porous rocks, change their phases under a specified temperature range rather than isothermally (Lunardini, 1987; Rühaak et al., 2015). In this case, evolving “mushy zone” emerges, which separates between the solid and liquid regions, where the thawing or freezing begins and proceeds, accompanied by latent heat absorbance or release (e.g., Crank, 1984; Yang et al., 2020).

Following this approach, instead of the mathematical boundary, we use a narrow transition mushy zone (shaded area in Fig. 3), with pore space consisting of a mixture of ice and water (Rubinstein, 1982). The local enthalpy in the mushy zone takes values in the range between those of the pure solid and liquid, and the temperature is approximated by a constant value, \( T = T_{wlt} \), equal to the phase change temperature (Crank, 1984).

Heat exchange in the sub-surface is controlled by the ground temperature gradient, as well as by the soil thermal properties (i.e. thermal conductivity, Burn, 2011). Above ground, the main factor is the air temperature, which is measured and reported as MAAT (Luo et al., 2018; Szafraniec & Dobiński, 2020) and was taken as representing the MAGST (Mean Annual Ground Surface Temperature). Initial surface temperature was defined according to the temperature of the shallow seawater during mid-Holocene (2°C, Rasmussen et al., 2012), while the initial temperature profile (black solid line in Fig. 3) was defined using the regional average geothermal gradient of 0.033°C m\(^{-1}\), as discussed by Olaussen et al., (2019) and Betlem et al., (2018). The lower boundary of the model was set at 300 m depth, with temperature of 12°C according to the initial temperature distribution. Throughout the simulation, we searched for the depth and time-dependent temperature distribution \( T(z,t) \), schematically shown as a dashed line in Fig. 3.

Several MAAT values were used for the modelling: (1) the current -5.8°C (measured at the Adventdalen 'Polygons' site, (Christiansen, 2005), 7 km from the fjord; (2) -4°C, which was taken from climate
simulation models for the mid-Holocene (Park et al., 2019; see also Mangerud and Svendsen 2018; Van der Bilt et al., 2019); (3) -3°C and 0°C assumed by Humlum (2005) for the mid-Holocene. While snow may cause differences between MAAT and MAGST due to thermal insulation (Zhang, 2005), it was found that in western Svalbard, specifically in the flat landforms at Adventdalen, the differences between MAAT and MAGST are less than 0.5°C (Christiansen, 2005; Lüthi 2010; Etzelmüller et al., 2011; Farnsworth 2013). Therefore, MAAT was taken as representing MAGST. Amplitude of seasonal temperature oscillation at the surface was set to 12°C, similar to the current fluctuation (Nordli et al., 2014; Christiansen, 2005; Osuch & Wawrzyniak, 2017).

To distinguish between a frozen and water saturated cell, we defined a time and depth-dependent freezing ratio, \( B(z,t) \), shown by points line in Fig. 3. \( B=1 \) means that the soil is water-saturated, while in the case of \( B=0 \) pore space is fully ice-saturated. In the mushy zone (shaded area in Fig. 3), the \( B \)-value changes between 0 and 1, and the rate of its change defines the amount of energy or latent heat associated with water-ice phase transition. Since it is now well-established that permafrost is not necessarily fully frozen (e.g. Keating et al., 2017; Oldenborger & LeBlanc, 2018; see Table 1), we also investigated permafrost aggradation under “partial freezing” conditions of 25% and 50%. Note that our model assumes fully-saturated pore-water conditions, since freezing starts at sea level, soon after exposure, therefore groundwater level is expected to be at the surface.
Figure 3. Schematic freezing profile during the top-down (epigenetic) freezing process. Initial and the developing geothermal gradients are also shown; the mushy region with constant temperature is the depth zone where phase transition occurs. Dotted line schematically represents the freezing condition, where $B=0$ stands for fully frozen and $B=1$ for liquid only. Active layer seasonality is neglected.

Another factor affecting the rate of permafrost formation is the water-freezing temperature (hereafter: WFT), which varies with salinity (Morgenstern & Anderson, 1973), as well as due to other environmental factors (Farouki, 1981; Morgenstern & Anderson 1973). Since salinities in the ADE site, down to 12 m, do not exceed 15% that of seawater, fresh water freezing temperature is the most appropriate for our simulations. Nevertheless, we also conducted simulations with WFT of $-2^\circ$C, which is close to that of seawater ($T_m=-1.9^\circ$C, Marion et al., 1999; Bodnar, 1993), as well as with $-6^\circ$C, following the reports of Gilbert et al., (2019) and Tavakoli et al., (2021) about high salinities (up to 73 ppt) in cryopegs in Adventdalen.

For simplicity, thermal conductivity was calculated considering three major components water, ice and dry sediment. While the thermal conductivity of water and ice are well defined (e.g. 0.569 and 2.24 W m$^{-1}$ K$^{-1}$, respectively, e.g. Williams and Smith, 1989), the range of conductivity values for dry sediment in
the literature is large, from 0.25 to 8.8 W m$^{-1}$ K$^{-1}$ (Farouki, 1981; Williams and Smith, 1989). In Adventdalen, a recently published freezing model, used thermal conductivity of 0.5 W m$^{-1}$ K$^{-1}$ for quaternary sediments (Hornum et al., 2020). We decided to mainly use the value of 0.35 W m$^{-1}$ K$^{-1}$ for the dry sediment to test the lower edge of thermal conductivity (i.e. anticipated slower freezing), while we also present results using a high value of 3 W m$^{-1}$ K$^{-1}$ (Overduin et al., 2019).

Porosity is an important factor in the aggradation or thawing of permafrost (Hornum et al., 2020). It determines both the amount of heat released or required during freezing/thawing, and the thermal characteristics of the soil (ice has significantly higher thermal conductivity than water; Farouki, 1981).

Porosity of sediments at ADE was mainly set to its average value, 0.3 (Gilbert et al., 2018), although we also tested the effect of other porosity values (Appendix 1). Bedrock ($\geq$25 m depth) porosity was taken as 0.1, the value suggested by Hornum et al. (2020), assuming that the bedrock is mainly composed of fractured shales (Grundvåg et al., 2019; Benn and Evans, 2014).

Freezing temperature and degree of freezing were kept uniform in each of the simulations, although as pore water freezes, the remaining fluid becomes saltier, further lowering the freezing temperature of the remaining solute (Herut et al., 1990), such that fully frozen pore space (i.e. 100% freezing) can only be reached at extremely low temperatures, which are not relevant to our study sites, as well as to most other permafrost areas (Homshaw, 1980; Dobinski, 2011).

The 1-D freezing model provides a good approximation of freezing rate and permafrost aggradation as shown by many studies (e.g., Harada & Yoshikawa, 1996; Kukkonen & Šafanda, 2001; Farbrot et al., 2007; Etzelmüller et al., 2011; Hornum et al., 2020). Such models actually provide the maximum rates of freezing propagation, as lateral heat transport by groundwater flow is neglected. Neglecting lateral heat transfer is quite justified, considering that (1) upstream shallow groundwater arrive from areas that were exposed earlier, therefore should not be warmer than the ADE groundwater, (2) experimental data suggest that a temperature drop by a tenth of a centigrade below 0°C reduces the hydraulic conductivity by several orders of magnitude (Burt & Williams, 1976; Rühaak et al., 2015). Nevertheless, as stressed above, soon after freezing initiates, the hydraulic conductivity dramatically decreases and the impact of lateral flow can be neglected.
5.2 Mathematical formulation

The heat conduction equation for time and depth-dependent temperature profile, $T(z,t)$, is (Crank, 1984):

$$\rho C_p \frac{\partial T}{\partial t} = \frac{\partial}{\partial z} \left( \kappa \frac{\partial T}{\partial z} \right) + Q \quad (1)$$

where $Q$ is the energy sink or source, representing the latent heat associated with water-ice phase transition, $\rho$ is the soil density, $C_p$ is the specific heat capacity and $K$ is heat conductivity. The depth and time-dependent material properties were calculated assuming linear superposition of the soil, water, and ice properties (e.g., Lunardini, 1988). Thus, the depth-dependent density, heat capacity, and thermal conductivity were calculated using the porosity, $\theta$, and freezing ratio, $B(z,t)$:

$$\rho = (1 - \theta) \rho_{soil} + \theta \left( (1 - B) \rho_{ice} + B \rho_{water} \right)$$

$$\kappa = (1 - \theta) \kappa_{soil} + \theta \left( (1 - B) \kappa_{ice} + B \kappa_{water} \right) \quad (2)$$

$$C_p = (1 - \theta) C_{psoil} + \theta \left( (1 - B) C_{pice} + B C_{pwater} \right)$$

The thermal properties and density used for all system components (soil, ice and water) are listed in Table 2.

Out of the mushy zone, for either $B=0$ or $B=1$ (unfrozen sediments), the heat exchange leads to its cooling below or heating above the freezing temperature. When no latent heat is involved, assuming homogeneous heat conductivity, the heat conduction equation (1) is reduced to:

$$\frac{\partial T}{\partial t} = D \frac{\partial^2 T}{\partial z^2} \quad (3)$$

where $D$ (diffusivity) [$m^2 s^{-1}$] defined as:

$$D = \frac{\kappa}{\rho C_p}$$

In the mushy zone, where the water-ice phase transition occurs, both the $B$ value and the thermal properties ($C_p$ and $K$) are depth-dependent. Accordingly, the complete heat conduction equation (1) is solved, including the latent heat term. The heat source/sink is equal to the mass of the freezing/thawing water per unit time multiplied by the latent heat, $L$. The water mass is equal to the rate of the $B$-value change times porosity and density. Finally, the source term is:

$$Q = -L \theta \rho \frac{\partial B}{\partial t} \quad (4)$$
We neglected the kinetics of the phase transition and assumed that thermodynamic equilibrium is established instantaneously in the mushy zone. This means that the rate of freezing/thawing is defined by the heat flux to and from the mushy zone with $0 < B < 1$. Substituting (4) into (1) and using $\frac{\partial T}{\partial t} = 0$ leads to:

$$\theta L \rho \frac{\partial B}{\partial t} = \frac{\partial}{\partial z} \left( \kappa \frac{\partial T}{\partial z} \right)$$

(5)

The above equations are solved numerically for two functions $T(z,t)$ and $B(z,t)$, using the explicit-in-time finite difference scheme. These functions were approximated using the constant grid steps in depth $\Delta z$ and in time $\Delta t$:

$$T_{n,m} = T(n\Delta z, m\Delta t)$$

$$B_{n,m} = B(n\Delta z, m\Delta t)$$

where $n$ is the grid point number ($z = n\Delta z$) and $m$ is the time step number ($t = m\Delta t$). With this notation, the finite difference form of the heat conduction equation (1) is:

$$\rho_n C_p n \frac{T_{n,m+1} - T_{n,m}}{\Delta t} = \frac{1}{\Delta z^2} \left[ \frac{\kappa_{m+1} + \kappa_m}{2} (T_{n+1,m} - T_{n,m}) - \frac{\kappa_m + \kappa_{m-1}}{2} (T_{n,m} - T_{n,m-1}) \right] + L\rho \frac{B_{n,m+1} - B_{n,m}}{\Delta t}$$

(6)

where density and the thermal properties are calculated using equation (2).

Equation (6) is solved using time step $\Delta t = 10,800$ s (i.e. 3 hours) and a depth spacing $\Delta z = 0.25$ m. The solution was obtained for the model size down to 300 m depth, summing up to 1,200 grid points. These numerical parameters satisfy the von Neumann stability condition for explicit-in-time numerical scheme (e.g., Ames, 1977) for the material properties of Table 2. The numerical code was written with Python (Wang & Oliphant, 2012). It allows simulating the permafrost dynamics and sub-surface sediments freezing under various scenarios of MAAT, water freezing temperatures (WFT) and freezing extent of pore space water.
Table 2: 1-D heat transfer model physical parameters of water, ice and dry soil

<table>
<thead>
<tr>
<th></th>
<th>Thermal conductivity $\kappa$ [W m$^{-1}$ K$^{-1}$]</th>
<th>Heat capacity $C_p$ [J K$^{-1}$ Kgb$^{-1}$]</th>
<th>Density $\rho$ [Kg m$^{-3}$]</th>
<th>Diffusivity $D$ [m$^2$s$^{-1}$]$^*$</th>
<th>Latent heat $L$ [J Kgb$^{-1}$]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ice</td>
<td>2.24</td>
<td>2100</td>
<td>916.2</td>
<td>1.17X10$^{-6}$</td>
<td>334000</td>
</tr>
<tr>
<td>Water</td>
<td>0.569</td>
<td>4192</td>
<td>999.85</td>
<td>1.36X10$^{-7}$</td>
<td></td>
</tr>
<tr>
<td>Soil (Silt)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>dry unfrozen</td>
<td>0.35 and 3</td>
<td>837</td>
<td>2400</td>
<td>1.74x10$^{-7}$</td>
<td>unfrozen</td>
</tr>
<tr>
<td>dry frozen</td>
<td></td>
<td>712</td>
<td></td>
<td>2.04x10$^{-7}$</td>
<td>frozen</td>
</tr>
</tbody>
</table>

* $D=\kappa/\rho*C_p$

5.3 Model results

We present the results of model runs with variable combinations of surface temperature, water freezing temperature and sediments porosities and thermal conductivities. Complementary modelling results are presented in the Appendix. In all cases, simulations started in the spring (May) and followed an amplitude of 12°C around the chosen (fixed) MAAT.

We first present simulations with MAAT of -4 ± 12°C, WFT 0°C, and complete (100%) freezing. Results in parentheses are for sediment thermal conductivity of 3 W m$^{-1}$ K$^{-1}$. Figure 4a presents results of a one-year simulation, with temperature profiles shown every second month. The model suggests that freezing under these conditions can reach down to two (3) meters within the first year. The freezing depth increases to 4 (6) m within 6 years with a slight, but significant deepening of the inflection point (Fig. 4b).

After 50 years, freezing arrives at 10-11(16-17) m, and within 1000 years the freezing front is already at 50 (73) m (Fig. 4c) in the sedimentary basement rocks (considering that sediment cover at ADE is ca. 25 m). The depth affected by cooling also progresses with time (<50 m in 50 years, >150 m in 1000 years) and T profile approaches linearity.
Figure 4. 1-D freezing model results for: (a) 1 year; the model starts (and finishes) at spring, defined as mid-time between minimum and maximum surface T (e.g. May), followed by summer increase in temperature (solid and dashed lines), cooling and start of freezing during fall (dotted line, e.g. November), followed by colder winter months (two-points dashed line and wide dashed line) and concluding in the spring (one point dashed line); (b) 6 years (starting in spring). MAAT $-4 \pm 12^\circ$C, WFT set at $0^\circ$C, 100% freezing. (C) Model simulation for 50 to 1000 years. Black circles dots denote $-4^\circ$C. Note the different scale between (a) (b) and (c).

Lowering the WFT results in decrease of the freezing rate. For example, with WFT of $0^\circ$C the freezing front will reach 15 (23) and 21 (37) m after 100 and 200 years while with WFT of $-2^\circ$C and $-5^\circ$C it will reach 11 (15) and 16 (20) m and 4.75 (2.5) and 6.75 (2.5) m during the same periods, respectively (Fig. 5). Surprisingly, permafrost aggrades even under WFT of $-5^\circ$C, which is lower than the MAAT of $-4^\circ$C. This is because the thermal conductivity of ice is higher than that of water (Farouki, 1981), which results in a deeper advance of the winter freezing front (through ice) than the advance of summer thawing (through water). Permafrost aggradation was not observed under WFT of $-5^\circ$C when using a dry sediment conductivity of 3 W m$^{-1}$ K$^{-1}$. 
Figure 5. Results of 1-D freezing simulations with mid-Holocene MAAT of -4±12°C (Park et al., 2019) and pore-water freezing temperature (WFT) taken as 0°C, -2°C and -5°C. Simulations were run for 100 and 200 years.

In Figure 6, we examine the effect of partial freezing. Partial freezing (25% and 50% in our scenarios) result in deepening of the freezing depth, but differences are relatively small. With MAAT of -4°C and WFT of 0°C, after 200 years freezing depth will reach 21, 22 and 25 m with 100% 50% and 25% freezing, respectively. Lowering WFT to -2°C, freezing depth become even more similar (16 to 15.25 m, Fig 6). This is because of the trade-off between reducing latent heat and the lower thermal conductivity of the partially frozen pore space. With a WFT of -5°C, the trend changes, and permafrost aggradation will occur only under the 100% freezing scenario, while with partial freezing of 25-50%, it will not aggrade deeper than 2 m (Fig. 6), i.e. no permafrost will develop (assuming active layer depth of 1-2 m), which further suggests that when WFT is lower than the average MAAT (-4°C), aggradation is controlled by the ice thermal conductivity rather than by latent heat. Last, with WFT of -6°C (i.e. significantly lower than the MAAT), there is no apparent permafrost aggradation also with 100% freezing (assuming active layer depth of 2 m, Fig. 6), although permafrost does develop to ca. 3.5 m after 1000 year (not shown).
thermal conductivity of 3 W m⁻¹ K⁻¹, 25% partial freezing will result in significantly deeper (10 m) permafrost aggradation. However, with WFT of -2 °C, aggradation rates with 100% and 25% freezing turn similar, and with WFT of -5 or lower, permafrost will not aggrade.

Figure 6. Mid-Holocene permafrost aggradation with variable freezing degrees. MAAT was set to -4 °C (Park et al., 2019), and freezing proportions were taken as 100%, 50% and 25%. The shaded/grayish zone represents a hypothetical, conservative, active layer, which is taken as 2 m thick. We note that active layer in Adventdalen is usually ≤1 m, and 2 m was chosen due to the higher temperature during the mid-Holocene.

In general, higher MAAT results in a lower aggradation rate e.g. with MAAT of 0°C and WFT of 0°C 100% freezing and Thermal conductivity of 0.35 W m⁻¹ K⁻¹ freezing depth will reach 12 m within 200 years.
Changing the thermal conductivity to $3 \ \text{W m}^{-1}\text{K}^{-1}$ will result in 9.5 m freezing depth. For the same setting, but with MAAT of $-4^\circ\text{C}$ the freezing front will result in significant deepening. While with thermal conductivity of $3 \ \text{W m}^{-1}\text{K}^{-1}$, it will reach 37 m and for thermal conductivity of $0.35 \ \text{W m}^{-1}\text{K}^{-1}$, it will reach 21 m (Figure 7a). Setting the system to 25% freezing, freezing depth will reach 47 and 25 m respectively (Fig. 7b). However, we show that even with MAAT > WFT (e.g., $0^\circ\text{C}$ and $-2^\circ\text{C}$, respectively) freezing will arrive at 3.5 m after 200 years and 8 m after 1000 years (not shown). As mentioned above, this is due to the asymmetry in the seasonal freezing/thawing process. Higher conductivity during winter (frozen pore space) enhances the loss of heat, while the lower conductivity during summer (warming front goes through thawed pore space) slows the thawing process (Kukkonen & Šafanda, 2001). We note that lower proportions of freezing (e.g., 25%) will have the effect of reducing this asymmetry due to the higher proportions of liquid water in the cryotic pore-space, therefore lower thermal conductivity during freezing. Accordingly, permafrost deepening is hardly observed in the scenario of MAAT=0 $^\circ\text{C}$ (in particular with WFT= $-2^\circ\text{C}$).
Figure 7. Early and mid-Holocene freezing depth in the first 50 and 200 years with MAAT -4°C and WFT of 0 and -2°C and with thermal conductivity (TC) of 0.35 and 3 W m⁻¹ K⁻¹. (a) 100% freezing, (b) 25% freezing. Also shown are curves of two scenarios of corresponding depths of the fresh-saline water interface, using a 1:40 Ghyben-Hertzberg (G-H) approximation for isostasy of 4.5 and 15 mm y⁻¹. See text for more details. (c) and (d) are zoomed in of (a) and (b) for the first 50 years. The fast deepening in figures a, and b is due to change in porosity as the freezing front reaches the bedrock (25 m). The legend is the same for all figures.
6. Discussion

6.1 Ground ice salinity and the frozen interface

When the freezing front propagates downwards in a recently emerged land and epigenetic permafrost is formed, it might freeze old subsurface brines (Cascoyne, 2000). As the freezing process proceeds, solute concentrations in the non-frozen residual water commonly increase (e.g., Cocks and Brower, 1974; Herut et al., 1990; El Kadi and Janajreh, 2017). This results in a pore space with high salt concentrations. These brines may then migrate away from the freezing surface, driven by density and capillary forces, and coalesce to form separate saline water lenses (‘cryopegs’; Cascoyne, 2000). The level of salinity and water composition will depend on the initial water composition and the extent of freezing. Complete permafrost freezing can hardly be obtained, since the eutectic point of seawater freezing is at -36°C to -54°C (Gitterman 1937; Ringer 1905; Nelson & Thompson 1954; Marion et al., 1999), while in Adventdalen permafrost temperatures does not usually get below -6°C, below depth of zero annual amplitude (ZAA) (Christiansen et al., 2010), and are never lower than -12°C even in the shallow permafrost (Christiansen et al., 2020; Isaksen et al., 2007). Although the eutectic point is well below the expected temperature values, the freezing-salt expulsion process still prevails. Under these conditions, the permafrost pore space should hold a small fraction of residual brine solution, which contains most of the solutes originally dissolved in the bulk pore-space water. Partly frozen permafrost has been often observed in the study area during drilling, in particular deeper than a few meters. This was also found in both geophysical and geochemical observations (e.g., Keating et al., 2018; Weinstein et al., 2019). Nevertheless, when ground ice is thawed, the extracted fluid from the relatively large segments used in this study should roughly indicate the salinity of the original in situ pore fluid, assuming no major brine migration had occurred. Pore-water composition may be significantly altered from the original fluid that circulated in the sediments (e.g. seawater) due to ion exchange or dissolution prior to or even after cryotic conditions occurred, which is reflected in the Na/Cl and SO$_4$/Cl ratios in the thawed ground ice (Fig. 2). Nevertheless, Cl$^-$ concentration is probably close to and represents the salinity of the original pore fluid. We note that while in certain cases permafrost contains lenses or pockets of unfrozen brine-containing cryotic soils (‘cryopegs’, e.g. Van Everdingen, 1998), which are commonly attributed to the segregation and migration of fluids (i.e. non in situ). The relatively low salinity (Fig. 2) and the evident mixing profile (Fig. 2a, b and C), suggest that this is not the case in the ADE site, and that the observed fresh-seawater
interface is an in situ observation. We relate to the chemistry of the extracted fluid as 'ground ice chemistry', although it could as well be that some of it was not actually frozen.

Cable et al., (2018) presented ground ice chemistry of cores from the Adventdalen, albeit closer to the current fjord (<4 km), west of the ADE site. In these cores, chloride, sodium and sulphate concentrations at depths of 3-11 m were up to 50% that of seawater. At ADE, farther away from the sea, ground ice in the epigenetic permafrost, 5.5 m from the surface and deeper, shows a gradual increase in salinity (i.e., fresh-saline interface), with Cl\textsuperscript{-} concentrations reaching 15% that of seawater at 9 m below the surface. Although salinities do not change much between 9-12 m, it is likely that more saline water, close to seawater salinity, either exists today or existed in the past (prior to freezing) at deeper permafrost levels. The existence of a fresh-saline interface in the very shallow permafrost, in the top of the epigenetic permafrost, suggests that freezing at ADE occurred straightaway after emergence above seawater. This is further discussed below.

6.2 Rebound, exposure and fresh-saline interface deepening

Assuming that Early Holocene (11-8 ka BP) precipitation was slightly higher than present (200 mm per year, Kjellman et al., 2020; McFarlin et al., 2018), and using a conservative infiltration factor of 0.2 (whether thawing snow or direct rain) and the porosity used in our simulations (0.3), this amounts to an effective annual infiltration of ca. 130 mm per year. This could easily keep-up with the Early Holocene rebound rates of 15 mm \text{y}^{-1} (established for the nearby Sassendalen Valley, Salvigsen, 1984; Sessford et al., 2015), therefore preserving the groundwater table close to the surface of the emerging land. Using a Ghyben-Herzberg approximation (Bear & Dagan 1964), this would result in an Early Holocene fresh-saline interface deepening of ca. 60 m in 100 years (Fig. 7), assuming the saline water body had a common seawater density of 1,025 kg m\textsuperscript{-3}. FSI deepening could even be faster, if the deep-water body is less saline than seawater. Even if sub-aerial exposure occurred later, during the mid-Holocene, when the rebound rate decreased to 4.5 mm \text{y}^{-1} (Forman et al., 2004), the fresh-saline interface would still deepen at a rate of 180 mm \text{y}^{-1}, i.e. 18 m in 100 years (Fig. 7).

The existence of a mixing zone at the top of the epigenetic permafrost (from 5.5 m below the current terrain surface), with Cl\textsuperscript{-} content 15% that of seawater at 3.5 m below the Early Holocene surface, suggests that the marine sediment section at ADE was hardly flushed with meteoric water. This further suggests that permafrost aggradation commenced shortly after emergence above the sea (e.g., Kasprzak et al., 2020). Indeed, some of the simulated freezing scenarios can clearly cope with the above
fresh-saline interface deepening rates (e.g., MAAT of -4°C and WFT of 0°C, Fig. 7). Moreover, assuming that partial freezing (e.g., 50-25%) can also block flushing, this results in even faster permafrost aggradation (Fig. 7b). However, as permafrost deepens, freezing rate slows down (e.g., Fig. 7), and none of the scenarios can cope with the assumed deepening of the fresh-saline interface, which should result in flushing of deeper zones.

It seems likely that the key factor in fresh-saline interface fossilization in a continuous permafrost landscape is the permanent freezing of the very shallow permafrost, which hydraulically disconnects the sub-permafrost zone from the surface and prevents recharge of this zone with meteoric water. As shown (Fig. 6 and 7), freezing of the top 3-5 m can occur within several years even with the relatively high temperatures of the Early to mid-Holocene (e.g., MAAT of -4°C or even warmer, Fig. 7), therefore, the fresh-saline interface could effectively be preserved.

We did not include salt diffusion in our model (e.g. Angelopoulos et al., 2019), a process that will reduce WFT as freezing progresses. It can explain the reason for partially frozen samples extracted from the epigenetic section (table 1). Including salt diffusion, we assume the freezing front may have advanced somewhat slowly than suggested by our model.

### 6.3 Permafrost aggradation during the Holocene

Gilbert et al., (2018), suggested that our drilling site at ADE emerged from the sea at 10 to 9 Ka BP and that the delta front advanced westwards at a rate of 4.4 m y⁻¹ prior to 9.2 Ka, which decreased to 0.9 m y⁻¹ during the rest of the Holocene. Considering the relatively high rebound rates during 9 to 8 ka (e.g., 15-19 mm y⁻¹), this suggests that the land surface at ADE reached 3-4 meters above sea level and a topographic gradient of 1-2% towards the sea within 200 years. Assuming the groundwater table was close to the surface, this should further result in a good flushing of the subsurface, unless freezing took control (Fig. 8). The observed mixing zone, which reaches the very top of the pre-Late Holocene surface, suggests that freezing started within just a few years after exposure.

Our simulations suggest that both cryotic conditions (i.e., <0°C) and actual ground ice formation were started very soon after exposure to the atmosphere (Fig. 5, 6 and 7), and that significant freezing depths of 15-33 m (or even 20-37 m considering higher thermal conductivity, Fig 7) could be achieved with 200 years (Fig. 6 and 7). This is true for both the Early to mid-Holocene warmer period (Kutzbach & Guetter, 1986; McFarlin et al., 2018; Mangerud and Svendsen, 2018; Park et al., 2019; Kjellman et al., 2020) and
for any sub-zero MAAT, regardless the size of the annual fluctuations. We even tested MAAT of +1 °C and found that some freezing could occur (not shown), which is a seasonal effect, derived from the different thermal conductivities of ice and water. Our simulations are in good agreement with Harada & Yoshikawa (1996), who used 1-D model with a MAGST of -5.7 °C but not completely saturated sediments and found that 533 years are needed to freeze 31.7 m of sediments in Moskuslagoon, slightly to the west of our site, on the Adventfjorden shore.

The ADE site was free of sea water in the Early Holocene, prior to 9.2 ka BP (Gilbert et al. 2019). At that time, an abrupt cooling has been described in Svalbard (Mangerud and Svendsen, 2017; van der Bilt et al., 2018, 2019). The presented model results show that the initiation of permafrost and its gradual aggradation is possible under relatively high temperatures (yet MAAT ≤ 0 °C) of the mid-Holocene. Christiansen et al. (2013), pointed out that local topographic conditions and winds in Adventdalen can induce lower temperatures at low altitude depressions, which could enhance the permafrost aggradation during the mid-Holocene.

Our simulations also show that lower percentage of freezing (e.g., 25%) may enhance the permafrost aggradation rate (e.g., Fig. 7b); however, this is not true for lower WFT (e.g., -2 °C) or for relatively high MAAT (e.g. 0 °C), which as mentioned above is due to the trade-off between latent heat and thermal conductivity differences between ice and liquid water. Nevertheless, MAAT of 0 °C seems unlikely (e.g., Van der Bilt et al., 2019).

In summary, the simulations suggest that permafrost aggradation could and did occur immediately following exposure also during the relatively warm period of early to mid-Holocene (8-10 ka BP). This is in disagreement with Hornum et al., 2020, who suggested that while freezing did occur during the Early Holocene the ground thawed during the mid-Holocene and refroze at about 6.5 Ka BP.

Pleistocene permafrost dynamics were studied in other permafrost regions. While in some areas there are records of permafrost degradation and peatland expansion already in the Early Holocene (post deglaciation, e.g., Lenz et al., 2015; Kaufman et al., 2015; Grinter et al., 2018; Li et al., 2021), cumulated evidence indicates that air temperature during this period was highly variable, sometimes higher and sometimes lower than presently (Kaufman et al., 2015). Nevertheless, it is a common observation that during the Holocene Thermal Maximum (mid-Holocene, 8.2-4.2 ka BP) permafrost has been degrading and thermokarst peaked (e.g., Lenz et al., 2015; Ulrich et al., 2017; Anderson et al., 2019). Permafrost aggradation resumed post-6 ka, and mainly during the past 4-3 ka (e.g., Grinter et al., 2018; Treat and
Jones, 2018). As shown above, we believe that this was not the case in Svalbard, and exposed lands continued freezing throughout the Pleistocene.

**Stage 1**: 22K Ka BP: Last glacial cycle, the glacier advances, and the valley bottom is eroded down to the bedrock (Elverhøi et al., 1995). The FSI is probably located at the meeting point of the sea and land.

**Stage 2**: 10-10.5 Ka BP: Maximal sea ingression (Lønne & Nemec, 2004) and deltaic sediments deposition (Gilbert et al., 2018). The FSI migrates eastward to the new location where sea and land meet.

**Stage 3**: 9.5 Ka BP: The FSI migrates westward and freezes when temperatures drop sharply. Freezing front (from top down) exceeds fresh water lateral flow. Epigenetic permafrost aggrads.

**Stage 4**: ADE site at present. Fluvial and aeolian deposition freeze syngenetically (Gilbert et al., 2018).
Figure 8. Conceptual presentation of the type of ground water freezing processes in Adventdalen since the last glacial cycle with a focus on the fresh-saline water interface (FSI) at the ADE site.

7. Summary and conclusions

Arctic landscapes, including western Svalbard, was rising relatively fast in the Early to mid-Holocene due to glacial isostatic rebound. Accordingly, the preservation of a frozen saline water (mixing zone) at a very shallow depth 15 to 33 m (the whole sediment fill of 20 m at this location) is taken as evidence for fast permafrost aggradation, which could halt the infiltration of fresh meteoric water and the flushing of saline water to the sea. This is despite of the prevailing relatively high temperatures during this period.

Our modelling confirms that freezing could progress relatively fast down the exposed Adventdalen sediments, i.e. to 15-33 m within 200 years, even under the reconstructed relatively high mid-Holocene air temperature of -4°C used in the 1-D model.

The modelling further suggests that permafrost may aggrade even when water freezing temperature (WFT) is slightly lower than MAAT, which is due to the differences in thermal properties between ice and liquid water.

Non-complete freezing of the cryogenic pore space could result in faster deepening of the freezing front when MAAT is smaller than WFT or even when it is higher, but in the latter case the difference is not large (e.g., MAAT < 0°C and 0 < WFT > -2 °C). However, when MAAT >> WFT (e.g., MAAT = 0 °C and WFT ≤ -2 °C), the presence of liquid water in the pore space and its lower thermal conductivity would result in a halt of permafrost aggradation.

This concept of fast freezing under relatively high air temperatures may suggest that recently exposed areas may still go through permafrost aggradation even under the current global warming. Also, it could imply that a short (years to decades) cooling period could significantly slow down permafrost thawing.

8. Appendix

Appendix 1: Porosity analyses

Selected simulation results demonstrating the effects of the porosity values on the rate of permafrost formation with thermal conductivities of 0.35 and 3 W m⁻¹ K⁻¹, are presented in figures 9 - 12. In general, higher porosity (i.e., more pore water to freeze) will result in slower permafrost aggradation (Fig. 9 and
due to the higher latent heat involved. Nevertheless, with low soil thermal conductivity and with lower WFT (i.e., closer to MAAT, Fig. 10a) the differences in aggradation rates with different porosity values are small and even negligible (Fig. 9a and 11a). when thermal conductivity is an order of magnitude higher porosity values are much notable.

Figure 9. Simulations of freezing front progress with different porosities and two thermal conductivities (TC), for MAAT of -4 °C, WFT of 0 °C and 100% freezing. Inset present results for 1000 years. The fast deepening at depth > 25 m is due to change in porosity as the freezing front reaches the bedrock.
Figure 10. Simulations as in Fig. 9, but with WFT of -2 °C.

Figure 11. Simulations as in Fig. 9 (MAAT = -4 °C, WFT = 0 °C), but with 25% freezing.
Figure 12. Simulations as in Fig. 9 (MAAT = -4 °C and WFT = -2 °C) but with 25% freezing.

9. Code availability

# 1-D freeze/thaw model code – copy and paste code rows into Python (Spider-Anaconda).
# This Python-script describes the 1-D Heat transfer model code developed for the research first Rotem et al., (202….). The 1-D model is a transient one-dimensional heat transfer model suitable for simulating permafrost dynamics. The core of the model is an explicit forward-difference time approximation of the one-dimensional heat transfer equation. This script is tailored to simulate the Holocene ground temperature development in Adventdalen, Svalbard, but may be modified to fit other purposes.
#Usage must be cited by reference to Rotem et al. (202….).

#For references cited below see:…

#Importing relevant packages for Python

import numpy as np
import matplotlib.pyplot as plt
import sys
import pandas as pd

n = 1201 # number of point grid
m1 = 20 # number of snapshots – i.e. No. of curves as display in fig. 4 and 5, or No. of sub sets of data to be exported.
m2 = 365*50 # number of steps for every snapshot
m = m1*m2 # number of time step

dt = 3600.0*24.0/8 #1/8 of a day 10800 sec
t_final = dt*m #defines the final time step
t_days= t_final/3600./24. #converts time steps to days
t_snap= dt*m2/3600./24.
print ('t_snap')
z = 300.0 # meters depth
dz = (z/(n-1)) # meter - defines the cell width if cell width (dz).
Tfr=0 # Freezing temperature define as WFT in article

# define depth-porosity profile
Depth = np.zeros(n)
por = np.zeros(n)
for i in range (0,n):
    Depth [i] = -i*dz
    por[i] = 0.3 # sediment’s porosity
    if Depth[i] < -25.0: # change from sediment’s porosity to rock porosity
        por[i] = 0.1

L = 334000.0 # J/kg water and ice Latent heat

# Density of materials
p_ice = 916.2       # Kg/m^3
p_water = 999.85    # Kg/m^3
p_soil = 2400.0     # Kg/m^3

#Defines Heat conductivity (K) & Heat Capacity (Cp) as function of porosity.
K_dufsoil  = 0.35   #or 3W/(m*K)  K_dufsoil = k of dry soil at temperatures ca. 5 °C centigrade.
K_dfsoil  = 0.35    #or 3 W/(m*K) K_dfsoil = k of dry soil at temperatures lower than 0 °C
Cp_dufsoil = 837    #heat capacity of dry soil (silt) in ca. 10 °C Cp_dufsoil = Heat capacity of dry soil
                    #above 0 °C.
Cp_dfsoil = 712     #heat capacity of dry soil (silt) in ca. -10 °C Cp_dfsoil = Heat capacity of dry soil
                    #below 0 °C.
K_ice     = np.zeros(n)
K_water   = np.zeros(n)
Cp_ice    = np.zeros(n)
Cp_water  = np.zeros(n)

for i in range (0,n):
    K_ice[i] = 2.24 *por[i] + K_dfsoil *(1-por[i])                # W/(m*K) regression with 0<B<1 -1.651x
                + 2.22
    K_water[i] = 0.569*por[i] + K_dufsoil*(1-por[i])             # W/(m*K)
    Cp_ice[i] = 2100.0*por[i] + Cp_dfsoil *(1-por[i])            # j/(K*Kg)
    Cp_water[i] = 4192.0*por[i] + Cp_dufsoil*(1-por[i])         # j/(K*Kg) regression with 0<B<1 2.192x
                    + 2. considering 90% soil and 10% water.

#control on model stability condition for explicit-in-time numerical scheme
dd2=K_ice[i]/(p_soil*Cp_ice[i])*dt/dz/dz
dd3=K_water[i]/(p_soil*Cp_water[i])*dt/dz/dz
if dd2>0.25 or dd3>0.25:
    print(' Values must be < 0.25 ')
    print(dd2,dd3)
    print(i,Depth[i],por[i])
x=np.linspace(0,z,n)

creating time field for data export

for i in range (0,n):
    time[i]=0+dt*i

#initial conditions
B=np.ones(n)            # B is a variable between 0 and 1 considering the ratio of ice or water in a cell.
B=1=water, B=0=ice creates an array of 1

T=np.ones(n)        # Initial Temperature 2 Centigrade creates array of 2 centigrade across the soil profile
for i in range(0,n-1):
    T[i]= 2.0 + 0.033*i*dz   #Thermal gradient 0.033 centigrade per m

#Define working arrays
Tn=np.zeros(n)              # creates an array for each one of the variables

Bnew=np.zeros(n)
K=np.zeros(n)
Cp=np.zeros(n)
p=np.zeros(n)
dE2=np.zeros(n)

for j1 in range(0,m1):      #a loop on the snapshots
    for j2 in range(0,m2):

        Boundary conditions
        Time=(j1*m2+j2)*dt/3600./24./365    #years
        T[0]=12*np.sin(2.*np.pi*Time)-4   #surface temperature for seasonal variation
        B[0]=0.       #B=1=water, B=0=ice
if $T[0]>0$

$B[0]=1$

$T[n-1] = 2 + 0.033*z$  #bottom of profile temperature. when sediments exposed to air it still has the sea water temperature.

$B[n-1]=1.$  #B=1=water, B=0=ice

for $i$ in range(0,n):

# calculate mixture properties each variable is calculated with linear ratio to B (ice to water ratio in a cell).

$K[i]=K_{ice}[i]*(1.0-B[i])+K_{water}[i]*B[i]$

$Cp[i]=Cp_{ice}[i]*(1.0-B[i])+Cp_{water}[i]*B[i]$

$p[i]=p_{ice}*(1.0-B[i])+p_{water}*B[i]$

for $i$ in range(1,n-1):

# loop over internal points. the dE2 (energy equation) equation is split for more convenient calculations

$dE2[i]=K[i]/2.0 * (T[i]-T[i])/dz$

$dE2[i]=dE2[i]-(K[i]+K[i+1])/2.0 * (T[i]-T[i+1])/dz$

$dE2[i]=dE2[i]*dt$  # Total energy flux into cell "i"

$T[i]=T[i]+dE2[i]/(p_{soil}*Cp[i]*dz)$  # conduction calculating the new temperature in the next cell.

$Bnew[i]=B[i]$  # calculating the new ice/water ratio in the next cell

if dE2[i]<0.0 and $T[i]<Tfr$:  #condition that verify the amount of energy and the new temperature. if the energy gets less than 0 value it means that energy is escaping the cell and it will cool down or freezes.

if $B[i]>0.0001$:  # Freezing

$Bnew[i]=B[i]+(dE2[i]-(T[i]-Tfr)*(p[i]*Cp[i]*dz))/(p[i]*L*dz*por[i])$  # the Bnew depends on the amount of energy that has been used to freeze the previous cell - the rest of the energy

if $Bnew[i]>0.0$:  # if the condition is true the new temperature equals freezing temperature.

$T[i]=Tfr$

else:

$T[i]=Tfr+Bnew[i]*(L*por[i])/Cp[i]$  # if the condition is false (Bnew <0.0) the new temp. equals the freezing temp.+Bnew.
Bnew[i]=0.

if dE2[i]>0.0 and Tn[i]>Tfr:

    if B[i]<0.9999:  # Thawing
        Bnew[i]=B[i]+(dE2[i]-T[i]-Tfr)*(p[i]*Cp[i]*dz)/(p[i]*L*dz*por[i])
        if Bnew[i]<1.0:
            Tn[i]=Tfr
        else:
            Tn[i]=Tfr+(Bnew[i]-1.0)*(L*por[i])/Cp[i]
            Bnew[i]=1.

for i in range(1,n-1):
    T[i]=Tn[i]
    B[i]=Bnew[i]

plt.plot(T,-x, 'r',label="Temperature",linewidth=0.5)

#exporting data to csv file. Graphs was created with Microsoft Excel.
name_dict =
    ' Temperature': T,[:0]
    ' time':time,[:0]
    ' depth': Depth,[:0]
    ' B': B,[:0]
    ' K': K,[:0]
    ' Cp': Cp,[:0]
    ' p': p,[:0]
    ' dE2': dE2[:0]
{
    df = pd.DataFrame(name_dict)
df.to_csv(r'C:\Users\ADMIN\Desktop\Python\Dotan\1Dmodel_1.csv', mode='a', header=True, float_format='%.3f')  # defines the location of the data exported

pd.read_csv('trial2.csv').count()

# Commands for graph in python script. Graphs for article was created with Microsoft Excel.
axes1 = plt.gca()
plt.ylabel('Depth')
plt.legend(loc = "lower left")
plt.grid()
axes2 = axes1.twiny()
axes1.set_xlabel("Temperature")
plt.plot(B, -x, 'g', linestyle='--', linewidth=0.7, label="B")
axes2.set_xticks([0., .2, .4, .6, .8, 1.0])
axes2.set_xlabel("B")
plt.legend(loc = "lower left")
plt.show()

10. Data availability

All raw data can be provided by the corresponding authors upon request.
11. Executable research compendium (ERC)

12. Sample availability

13. Supplement link: the link to the supplement will be included by Copernicus, if applicable.

14. Author contribution:

DR, YW, and HHC planned the drilling campaign; DR and YW, processed the cores and lab work in UNIS Svalbard; DR and YH preformed the water chemistry analysis at GSI; VL and DR developed the 1-D model; DR, YW and VL wrote the manuscript. All authors commented on the manuscript.

15. Competing interests:

The authors declare that they have no conflict of interest.

16. Disclaimer

17. Acknowledgments

We would like acknowledge Ullrich (Ulli) Neuman for leading the 2017 drilling campaign in Adventdalen. Andreas Alexander and Graham L. Gilbert for field assistance. Danni Rohdent for lab assistance. Gerd-Irena and UNIS logistics for their assistance with field and laboratory gear. GSI geochemical lab members Olga Berlin, Galit Sharabi and Dina Siber for their assistance with chemistry analysis. Yosi Yechiel for consulting about various issues of the article. The drilling campaign was supported by an Arctic Field Grant from the Norwegian Research Council, Project Number: 269988 RiS ID: 10664.

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