

# Summer sea ice floe size distribution in the Arctic: High-resolution optical satellite imagery and model evaluation

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## Supplementary Materials

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### S1 Perimeter density

In this study, we use the perimeter density per unit ice area  $P_i$  (units:  $\text{m}^{-1}$ ) to evaluate the model performance, as it reduces  
15 the impacts of partially captured floes at the edge of the image for the FSD retrieval (Perovich, 2002; Perovich and Jones, 2014). There are a number of ways to calculate  $P_i$ . In the following, we describe how the FSD models calculate  $P_i$ , as well as how  $P_i$  can be calculated from the observational FSD data.

#### Calculation of $P_i$ in the FSD models

In FSD models,  $P_i$  is calculated from number FSD  $n_i$  distributed into floe size categories  $i$  as follows:

$$20 P_i = \frac{\sum_{i=1}^{12} (2\gamma r_i n_i (r_{i_{max}} - r_{i_{min}}))}{c_{ice}}, \quad (1)$$

where  $r_i$ ,  $r_{i_{max}}$  and  $r_{i_{min}}$  are the midpoint, upper and lower limit for each floe size category  $i$ .  $n_i$  ( $\text{m}^{-3}$ ) is the average number  
FSD for floe size category  $i$ . Here  $\gamma$  is a floe shape parameter, for example  $\gamma = 1$  is the assumption of square floes,  $\gamma = \pi$  is  
for circular floes. From the analysis of MEDEA-derived FSD results, the mean floe shape parameter  $\gamma$  is 2.27 in the Chukchi  
Sea region and 2.23 in the Fram Strait region, respectively.  $c_i$  represents the area-weighted sea ice concentration in the  
25 selected region.

The areal FSD  $f(r)$  and number FSD  $n(r)$  are related by

$$f(r) = \gamma r^2 n(r). \quad (2)$$

We can also relate the areal FSD  $f(r)$  and CFND  $N(r)$  by

$$\int_{r_0}^{\infty} f(r)dr = \int_{r_0}^{\infty} \gamma r^2 dN(r), \quad (3)$$

30 where  $r_0$  is the lowest cut-off of floe size  $r$ . In the prognostic models (FSDv2-WAVE and CPOM-FSD),  $P_i$  is calculated from the areal FSD for floe size category  $f_i$  ( $m^{-1}$ ). By combining Eqs. (1) and (2),  $P_i$  for prognostic model  $P_{i\_prog}$  can be calculated by

$$P_{i\_prog} = 2 \sum_{i=1}^{12} \frac{f_i(r_{imax} - r_{imin})}{r_{ice} c_{ice}}. \quad (4)$$

For WIPoFSD model, a truncated power law FSD is applied,

$$35 \quad n(r|r_{min} \leq r \leq r_{var}) = cr^{-\alpha}, \quad (5)$$

where,  $r_{min}$  is the minimum floe radius within floe size categories. The power-law exponent  $\alpha$  value used in this study is set to 2.56. The floe size parameter  $r_{var}$  varies between  $r_{min}$  and the maximum floe radius  $r_{max}$  in response to four FSD evolution processes described by Bateson et al. (2020, 2022). The normalization constant  $c$  can be defined from that the integral of areal FSD over all floe sizes equal to the fraction of sea ice,

$$40 \quad \gamma \int_{r_{min}}^{r_{var}} n(r)r^2 dr = c_i \quad (6)$$

$$\text{Hence } c = \frac{(3-\alpha)c_i}{(r_{var}^{3-\alpha} - r_{min}^{3-\alpha})\gamma} \quad (7)$$

$P_i$  for WIPoFSD can be calculated from

$$P_{i\_wipofsd} = \frac{\int_{r_{min}}^{r_{var}} 2\gamma r n(r) dr}{c_{ice}} = \frac{2(3-\alpha)(r_{var}^{2-\alpha} - r_{min}^{2-\alpha})}{(2-\alpha)(r_{var}^{3-\alpha} - r_{min}^{3-\alpha})}. \quad (8)$$

In this study, we used daily outputs from the FSD models to calculate  $P_i$ . To obtain  $P_i$  from the daily model outputs, we  
45 calculated an area-weighted mean, on the same date as the observations, over the grid cells within the study areas of the Chukchi Sea and the Fram Strait.

#### Calculation of $P_i$ from the observations

To ensure matching with the model outputs, the FSD observation data were binned into the same 12 floe size categories used by the FSD models (Gaussian spacing). By deriving the number of all floes with effective floe radius  $r = \sqrt{\frac{a}{\pi}}$  (Horvat and

50 Tziperman, 2015), the radius of a circle that has the same area as a floe, within every floe size category, the average number FSD for each floe size category  $n_i$  can be calculated by

$$n_i = \frac{N_i}{A_{ocean}(r_{imax} - r_{imin})}, \quad (9)$$

where  $N_i$  is the number of floes with radius between  $r_{imin}$  and  $r_{imax}$  in the image covering an ocean area of  $A_{ocean}$  (units:  $m^2$ ) with floe radius between  $r_{imin}$  and  $r_{imax}$ .

55 Similarly, the average areal FSD for floe size category  $f_i$  can be calculated by

$$f_i = \frac{A_{floe_i}}{A_{ocean}(r_{imax} - r_{imin})}. \quad (10)$$

$A_{floe_i}$  is the area of floes with radius between  $r_{i_{min}}$  and  $r_{i_{max}}$  in the image.

Now based on the equations described above, we can calculate  $P_i$  from the observations using three different methods. From Eqs. (3) and (9), we can produce perimeter density per unit sea ice area from observations using the number FSD,

$$60 \quad P_{i\_obs1} = \frac{\sum_{i=1}^{12} (2\gamma r_i N_i)}{A_{ice}}, \quad (11)$$

where  $A_{ice}$  is the total area of sea ice within the image.

Based on Eqs. (4) and (10), the perimeter density can be calculated by,

$$P_{i\_obs2} = \sum_{i=1}^{12} \frac{2A_{floe_i}}{r_i A_{ice}}. \quad (12)$$

Additionally, we can calculate the floe perimeter density directly from our images,

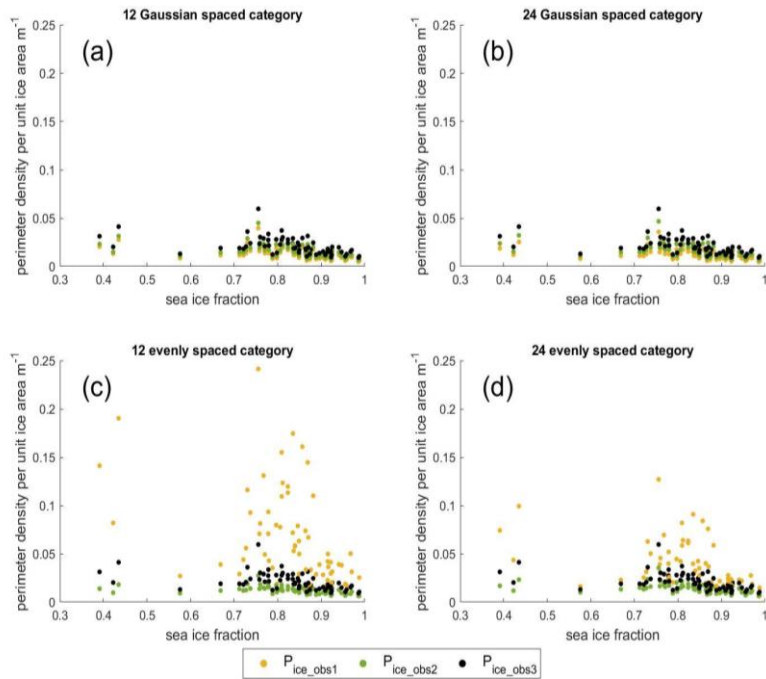
$$65 \quad P_{i\_obs3} = \frac{p_{floe}(r_{1_{min}} < r < r_{12_{max}})}{A_{ice}}, \quad (13)$$

where  $p_{floe}$  is the total perimeter of floes with radius between  $r_{1_{min}}$  and  $r_{12_{max}}$  in the image. In Sect. S2, we will test the sensitivity of calculating the perimeter density using Eqs. (11), (12) and (13).

## S2 Sensitivity to the floe size category binning and $P_i$ calculation methods.

In this section, we check the sensitivity of calculating  $P_i$  for different binning methods and different  $P_i$  calculation methods (Eqs. (11), (12) and (13) in Sect. S1). To test the sensitivity of the binning methods, we organised the observational FSD data into four different binning methods: 12 Gaussian-spaced bins, 24 Gaussian-spaced bins, 12 evenly spaced bins, and 24 evenly spaced bins. For the binning, we discarded any ice floes with the effective radius smaller than 0.1 m or larger than 951 m.

Figure S1 shows the results in the relationship between  $P_i$  and SIC. As can be seen in Figure S1, the  $P_i$  values from evenly spaced binning methods are very sensitive to the different  $P_i$  calculation methods (Figure S1c and d). On the other hand, the  $P_i$  values from Gaussian spaced binning methods are much less sensitive to the different  $P_i$  calculation methods and there are very small differences in the sensitivities between 12 Gaussian spaced binned data and 24 Gaussian spaced binned data (Figure S1a and S1b). Among the three different  $P_i$  calculation methods,  $P_{i\_obs2}$  (Eq. (12), estimated using the floe area) shows the smallest variation throughout the four different binning methods. Based on this, we selected  $P_{i\_obs2}$  to calculate  $P_i$  and use it as the metric for the model-observation comparison and the 12 Gaussian-spaced binning method to match with the model configuration in Roach et al. (2018a) and Bateson et al. (2022).



**Figure S1.** Relationship between perimeter density per unit ice area and SIC for (a) 12 Gaussian-spaced binning, (b) 24 Gaussian-spaced binning, (c) 12 evenly spaced binning, and (d) 24 evenly spaced binning. The perimeter density has been calculated by Eq. (11) ( $P_{i\_obs1}$ , yellow scatter), Eq. (12) ( $P_{i\_obs2}$ , green scatter) and Eq. (13) ( $P_{i\_obs3}$ , black scatter).

85 **Table S1.** Difference in  $P_i$  ( $\text{km}^{-1}$ ) of small floes within floe size category 1 and 2 ( $r < 14.29$ ) between models and observations in the Chukchi Sea region and the Fram Strait region.

	FSDV2-WAVE		CPOM-FSD		WIPOFSD	
	CS <sup>a</sup>	FS <sup>b</sup>	CS	FS	CS	FS
<b>May</b>	132.28	186.44	45.79	71.05	94.91	106.25
<b>June</b>	113.14	179.92	46.47	41.93	93.70	107.29
<b>July</b>	50.27	92.74	33.99	17.60	92.86	110.47
<b>August</b>	/	28.93	/	17.42	/	124.40
<b>Mean</b>	98.56	122.01	42.08	37.00	93.83	112.10

<sup>a</sup> Chukchi Sea.

<sup>b</sup> Fram Strait.

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