1 2	Evaluation of six geothermal heat flux maps for the Antarctic Lambert-Amery glacial system
3	Haoran Kang ¹ , Liyun Zhao ^{1*} , Michael Wolovick ⁴ , John C. Moore ^{1,2,3*}
4 5	¹ College of Global Change and Earth System Science, Beijing Normal University, Beijing 100875, China
6 7	² CAS Center for Excellence in Tibetan Plateau Earth Sciences, Beijing 100101, China
8	³ Arctic Centre, University of Lapland, Rovaniemi, Finland
9	⁴ Alfred Wegener Institute, Bremerhaven, Germany
10	* Corresponding author
11 12	Corresponding author: Liyun Zhao (zhaoliyun@bnu.edu.cn); John C. Moore (john.moore.bnu@gmail.com)
13 14	Abstract
14 15	Basal thermal conditions play an important role in ice sheet dynamics, and they are
16	sensitive to geothermal heat flux (GHF). Here we estimate the basal thermal conditions,
17	including basal temperature, basal melt rate, and friction heat underneath the Lambert-
18 19	Amery glacier system in east Antarctica, using a combination of a forward model and an inversion from a 3D ice flow model. We assess the sensitivity and uncertainty of
20	basal thermal conditions using six different GHFs. We evaluate the modelled results
21	using all observed subglacial lakes. The different GHFs lead to large differences in
22	simulated spatial patterns of temperate basal conditions. The two recent GHF fields
23	inverted from aerial geomagnetic observations have the highest GHF, produce the
24	largest warm-based area, and match the observed distribution of subglacial lakes better
25	than the other GHFs. The modelled basal melt rate reaches ten to hundreds of mm per
26	year locally in Lambert, Lepekhin and Kronshtadtskiy glaciers feeding the Amery ice
27	shelf, and ranges from 0-5 mm yr ⁻¹ on the temperate base of the vast inland region.
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The Lambert-Amery system in East Antarctica is believed to be relatively stable against 30 climate change and has changed little over several decades of observations (King et al., 31 32 2007). However, there is also evidence of extensive subglacial rifts and lakes (Fretwell 33 et al., 2013; Jamieson et al., 2016; Cui et al., 2020a). Jamieson et al. (2016) report a 34 large subglacial drainage network in Princess Elizabeth Land (PEL), which would 35 transport water from central PEL toward the Lambert-Amery region. The complexity 36 of the subglacial environment may influence the stability and basal mass balance of this 37 area. 38

39 Ice temperature is an important factor in the rheology of ice (Budd et al., 2013) and ice

40 flow. Whether the basal ice is at the melting point influences the movement of the ice

41 to a great extent. Ice at the melting point can lead to water flowing along hydraulic 42 greatients and accumulating in least depressions (Frieker et al. 2016). The meltivater 43 lubricates the ice/bed interface or saturates any sediment till layer, allowing higher ice 44 velocities via basal sliding. For instance, the rapid retreat of Thwaites and Pope glaciers 45 in the Amundsen Sea sector of West Antarctica is being facilitated by high heat flow in 46 the underlying lithosphere (Dziadek et al., 2021). This bed-ice linkage forms the basis 47 for making inferences on basal conditions via surface observations (Pattyn, 2010), or 48 relict landforms (e.g. Näslund et al., 2005).

49

50 The ice temperature is controlled by deformational heat generated from strain within 51 the ice, advection of heat due to lateral ice motion and the descent rate of ice from the 52 surface, conduction of heat through the ice and frictional heating from basal sliding. Ice 53 temperature is hard to evaluate because of the scarcity of in-situ measurements, 54 typically obtained from boreholes that are very rarely drilled through the Antarctic ice 55 sheet. GHF is an important boundary condition for ice temperature simulation, and is generally the largest source of uncertainty. Hence geophysical survey methods are used 56 to indirectly map GHF. To date GHF datasets have been estimated from seismic models 57 58 (Shapiro and Ritzwoller, 2004; An et al., 2015; Shen et al., 2020), derived from airborne magnetic surveys (Li et al., 2021; Martos et al., 2017) and satellite geomagnetic data 59 60 (Maule et al., 2005; Purucker, 2013).

61

62 Extensive ice penetrating radar data has been collected recently over Princess Elizabeth 63 Land (PEL; Fig. 1d), including the eastern part of the Lambert-Amery system (Cui et 64 al., 2020a). This fills in large data gaps from older surveys, and provides the basis for our study. The radar surveys reveal ~1100 km long canyons (Fig. 1c) that are incised 65 66 hundreds of meters deep into the subglacial bed that extend from the Gamburtsev 67 Subglacial Mountains (GSM) to the coast of the Western Ice Shelf (WIS). Li et al. (2021) collected airborne magnetic data that can be combined with radar ice thicknesses and 68 69 estimated depths at which the bedrock reaches its Curie temperature, to invert for the geothermal flux. The resulting higher resolution data set (Li et al., 2021) implies a larger 70 71 heat flux than previous estimates in this region. Furthermore, recently discovered 72 subglacial lakes, including potentially the second largest subglacial lake in Antarctica, add evidence for more widespread basal melting in the region than was thought based 73 on the much sparser earlier survey data (Cui et al., 2020b). The complex subglacial 74 topography, relatively high geothermal heat flux and subglacial lakes imply a complex 75 76 distribution of basal thermal conditions and subglacial water networks. These 77 heterogenous basal conditions will have shaped much of the ice flow and mass balance 78 of the Lambert-Amery system. This motivates us to investigate how the basal thermal 79 conditions inferred from the new high-resolution topography dataset can be reconciled 80 with surface ice velocities and existing geothermal heat flow maps.

81

82 Ice sheet models can be used to simulate the dynamics and thermodynamics of the ice 83 sheet. Glaciologists have combined ice sheet models with measurements of vertical 84 temperature profiles or thawed basal states to constrain GHF of the ice sheets (e.g. 85 Pattyn, 2010; Rezvanbehbahani et al., 2019). In the Lambert-Amery glacial system, 86 Pittard et al. (2016) suggest that ice flow is most sensitive to the spatial variation in the 87 underlying GHF near the ice divides and along the edges of the ice streams.

88

89 In this study, we simulate ice basal temperatures and basal melt rates in the Lambert-90 Amery system using the new high-resolution digital elevation model, along with six 91 different published GHF maps as forcing for an off-line coupling between a basal 92 energy and water flow model and a 3D full-Stokes ice flow model. We evaluate the 93 quality of the resulting basal temperature field incorporating the Stokes model estimates 94 of ice advection, strain and frictional heating under the different GHF maps using all 95 available observed subglacial lakes and surface velocities. Hence, we make inferences 96 on which GHF maps yield the best match with observations in the region.

97

98 2 Regional Domain and Datasets

99 Our modeled domain is part of the Lambert-Amery system. It consists of two drainage 100 basins: the Lambert Glacier Basin, the American Highland Basin, along with about half 101 of the Amery Ice Shelf (Fig. 1). The 2D domain boundary outlines are defined by the 102 inland ice catchment basin boundary, the central streamline, and the ice front of Amery 103 Ice Shelf. The central streamline was chosen by selecting a point at the confluence of 104 Lambert Glacier and Lepekhin Glaicer and then advecting that point downstream to the 105 ice front using the observed velocity field. The inland sub-basin and the central 106 streamline of the Amery Ice Shelf were chosen as boundaries because the mass flux 107 across them is assumed to be zero by definition. 108





Fig. 1. The domain topography and location with domain boundary overlain. (a) surface elevation;
(b) ice thickness; (c) bed elevation; (d) the location of our domain in Antarctica. The solid black
curve is the outline of the study domain, including the central streamline of Amery ice shelf and the
boundary of inland sub-basins based on drainage-basin boundaries defined from satellite ice sheet

surface elevation and velocities (Mouginot et al., 2017; Rignot et al., 2019). The solid red curve is

115 the grounding line of Amery ice shelf (Morlighem et al., 2020). The dotted black curve is the 116 dividing line between Lambert Glacier Basin and the American Highland Basin. The dotted red 117 curves in (b) and (d) are the boundary of ice thickness data from Cui et al. (2020a), inside which we 118 incorporates data from Cui et al. (2020a). The white stars in (c) denote the locations of observed 119 subglacial lakes (Wright and Siegert, 2012; Cui et al., 2021), and the region within the white line at 120 (1800E, 300N) is potentially the second largest subglacial lake in Antarctic. The red arrows in (c) 121 indicate the routing through the deep subglacial canyon system from GSM to WIS. The sub-basins 122 names of Lambert-Amery system are labeled in (d), ML for MacRobertson Land basin, FG for 123 Fisher glacier basin, MG for Mellor glacier basin, LG for Lambert glacier basin, AH for American 124 Highland basin, and AIS for Amery Ice Shelf.

125

The surface elevation, bedrock elevation, and ice thickness from Cui et al. (2020a) are
used in most of the domain (Fig. 1b; Table 1) with additional data are from MEaSUREs
BedMachine Antarctica, version 2 at a resolution of 500 m (Morlighem et al., 2020).
The bed elevation is calculated by subtraction of the ice thickness from the surface
elevation.

131

132 The surface ice velocity data are obtained from MEaSUREs InSAR-based Antarctic ice

133 velocity Map, version 2 with resolution of 450 m (Rignot et al., 2017). Data were largely

acquired during the International Polar Years 2007 to 2009, and between 2013 and 2016.

- 135 Additional data acquired between 1996 and 2016 were used as needed to maximize 136 coverage.
- 137

138 Ice sheet surface temperature data are prescribed by ALBMAP v1 with a resolution of 139 5 km (Le Brocq et al., 2010) and come from monthly estimates inferred from AVHRR 140 data averaged over 1982-2004. Subglacial lake locations are from the fourth inventory 141 of Antarctic subglacial lakes (Wright and Siegert, 2012), with the addition of the newly 142 discovered lakes (Cui et al., 2020b).

143

144 Six GHF datasets (Fig. 2; Table 2) are used in this study. All the datasets are interpolated

- 145 into the same 2.5 km resolution.
- 146
- 147 Table 1 Datasets used in this study.

Variable name	Dataset	Resolution	Reference
surface elevation, bedrock	MEaSUREs BedMachine	500 m	Morlighem et al., 2020;
elevation, and ice thickness Antarctica version 2		300 m	Cui et al., 2020
	MEaSUREs InSAR-based		
surface ice velocity	Antarctic ice velocity Map,	450 m	Rignot et al., 2017
	version 2		
surface temperature	ce temperature ALBMAP v1		Le Brocq et al., 2010;
subglassial lakas logation	The fourth inventory of		Wright and Siegert, 2012;
subgracial lakes location	Antarctic subglacial lakes		Cui et al., 2021

148

149 Table 2 The six GHF datasets used in this study.

GHF map	Reference	Method	Mean (mW m ⁻²)	Range (mW m ⁻²)
Martos	Martos et al., 2017	airborne	72	47-90
Shen An	Shen et al., 2020 An et al., 2015	geomagnetic data seismic model seismic model	50 55	43-59 40-66

	Shapiro	Shapiro and Ritzwoller, 2004	seismic model	54	45-58
	Purucker	Purucker, 2013	Satellite geomagnetic data	47	26-47
_	Li	Li et al., 2021	airborne geomagnetic data	72	52-90





152 Fig. 2. The spatial distribution of GHF over our domain as described in Fig. 1. See Table 2 for the

153 GHF map details.

154

155 **3 Model**

Our goal is to infer the basal thermal conditions, including basal temperature and basal melt rate in the domain. Geothermal heat flux, englacial heat conduction and basal friction heat are the main heat sources that determine the basal thermal conditions. Therefore, we need to model both ice flow velocity and stress for basal friction heat and ice temperature for englacial heat conduction.

161

162 We solve an inverse problem by a full-Stokes model, implemented in Elmer/Ice, to infer 163 the basal friction coefficient such that the modelled velocity best fits observations (Gagliardini et al., 2013). Using the best-fit basal friction coefficient, we obtain the ice 164 165 flow velocity, stress and basal friction heat. A proper initial ice temperature is needed 166 in solving the inverse problem. To get it, we use a forward model that consists of an 167 improved Shallow Ice Approximation (SIA) thermomechanical model with a 168 subglacial hydrology model (Wolovick et al., 2021a). The forward model uses the modelled velocity direction and basal slip ratio from the full-Stokes inverse model to 169 170 constrain its solution. We do steady state simulations by coupling the two models. We 171 will describe the forward model in Section 3.1 and the inverse model in Section 3.2, 172 then the coupling in Section 3.3.

173 **3.1 Forward Model**

The forward model consists of a thermomechanical steady state model using an 174 175 improved Shallow Ice Approximation (SIA) in equilibrium with the subglacial hydrological system (Wolovick et al., 2021a). It has internal consistency between three 176 177 components: ice flow, ice temperature, and basal water flux. The numerical model 178 requires three coupled components to be consistent with one another: (1) integration for 179 balance flux and englacial temperature downhill in the ice surface, (2) integration for 180 basal water flux and freezing rate downhill in the hydraulic potential, and (3) rheology 181 and shape function computations to determine the distribution of ice flux and shear 182 heating. The model performs a fixed-point iteration for consistency between these three 183 components. In addition. we improve on the model used in Wolovick et al. (2021a) by 184 combining the observed velocity field, the velocity field from the full-Stokes model, 185 and the surface gradient direction to compute a merged flow direction field for step (1). 186 The observations are used where flow is fast, Elmer/Ice modelled velocity is used where 187 flow is slow, and the surface gradient is only used near the margins of the domain where 188 the Elmer velocity field is not reliable (Fig. 3). The simulation is done on a finite 189 difference mesh with resolution of 2.5 km.

190

191 The surface accumulation rate we used in the forward thermal model is the mean of 192 Arthern et al. (2006) and Van de Berg et al. (2005). Both were accessed through the

- Arthern et al. (2006) and Van de Berg et al. (2005).ALBMAP v1 dataset (Le Brocq et al., 2010).
- 194

195 One key complexity is how to deal with basal thermal boundary condition. At the 196 bottom of ice shelves, we set basal temperature equal to the pressure melting point. At 197 the bed of grounded ice, the boundary condition can be either Dirichlet or Neumann 198 condition depending on the basal melting and subglacial water conditions. The basal 199 boundary conditions are given by,

200
$$-k(T)\frac{dT}{dz} = G, \text{ for } T < T_m \text{ and } m = 0;$$
(1)

$$T = T_m, \text{ for } m \neq 0, \tag{2}$$

where T_m is the pressure-dependent melting temperature, *G* is GHF, taking six GHF datasets listed in Table 2. The thermal condition will switch from Neumann (Eq 1) to Dirichlet (Eq 2) if the basal temperature exceeds the pressure-dependent melting point. The opposite switch from Dirichlet to Neumann is determined by the hydrology model, if there is insufficient water input to supply a large freezing rate.

207





Fig. 3. Velocity direction fields, in degrees clockwise from grid north. The first row shows the direction from surface gradient (a), Elmer/Ice modelled velocity (b), and the observed velocity direction (c). The middle row (d-f) shows the 3 corresponding weighting fields (the sum of these weights is 1). The bottom row shows the difference between the direction of surface gradient and Elmer/Ice modelled velocity (g), the difference between the observed velocity direction and Elmer/Ice modelled velocity h), and the merged velocity field used in the forward model (i).

215 One improvement on the method from Wolovick et al. (2021a) is that a temperate basal 216 ice layer with non-zero thickness is permitted in our model in the case that the modelled 217 basal ice temperature reaches the pressure melting point. We do this using a weak-form 218 solution in which the volumetric englacial melt rate rises steeply as temperature exceeds 219 the melting point. The englacial melting absorbs latent heat and serves to limit 220 temperature rise. We parameterize the increase in volumetric melt rate as an 221 exponential function of temperature with a 1 K e-folding temperature, and a prefactor 222 given by the englacial strain heating and the latent heat of fusion. All englacial 223 meltwater generated this way is assumed to immediately drain to the bed.

Another key component of the forward model is the shape function determining the distribution of horizontal velocity with depth. We also improve the shape function in Wolovick et al. (2021a) by adding basal slip ratio, $\hat{u}_b = u_b/\bar{u}$, where u_b is the basal velocity magnitude and \bar{u} is the vertically averaged horizontal velocity magnitude. The slip ratio is taken from the full-Stokes inverse model. Other than the addition of a spatially variable slip ratio, the shape function calculation is unchanged from Wolovick et al. (2021a).

232 **3.2 Inverse Model with full-Stokes Model**

The spatial distribution of basal friction in the domain is modelled by solving an inverse problem using the three-dimensional the full-Stokes model, Elmer/Ice, an open source finite element method package(Gagliardini et al., 2013). The inverse model is based on adjusting the spatial distribution of the basal friction coefficient to minimize the misfit between simulated and observed surface velocities. The modelled velocity is obtained by solving the full-Stokes equation, which includes conservation equations for both the momentum and mass of the ice,

240
$$div \,\boldsymbol{\tau} - gradp = \rho_i \, \vec{g} \,, \tag{3}$$

$$div \, \vec{v} = 0, \tag{4}$$

242 where $\boldsymbol{\tau}$ is the deviatoric stress tensor, p is the isotropic pressure, ρ_i is ice density, \vec{g} is

the acceleration due to gravity $(0, 0, -9.81) \text{ m} \cdot \text{s}^{-2}$, \vec{v} is ice velocity. According to Glen's flow relation, deviatoric stress is related to the deviatoric part of the strain rate tensor, $\vec{\varepsilon}_E$, which can be described by $\tau = 2\eta \vec{\varepsilon}_E$, where the effective viscosity of the ice, η , is sensitive to the temperature-dependent flow rate factor A(T) calculated using an Arrhenius equation (Cuffey and Paterson, 2010). The ice temperature distribution comes from the forward model in section 3.1.

249

250 **3.2.1 Mesh Generation and Refinement**

Firstly, we use GMSH (Geuzaine and Remacle, 2009) to generate an initial 2-D horizontal footprint mesh with the boundary described in section 2. Then we refine the mesh by an anisotropic mesh adaptation code called the Mmg library (http://www.mmgtools.org/). The resulting mesh is shown in Fig. 4 and has minimum and maximum element sizes of approximately 1000 m and 8000 m. The 2-D mesh is then vertically extruded using 10 equally spaced, terrain following layers.





Fig. 4. The refined 2-D horizontal domain footprint mesh (a). Boxes outlined in (a) are shown in detail overlain with surface ice velocity in (b) and (c), and with ice thickness in (d).

261 **3.2.2 Boundary Condition**

The ice surface is assumed to be stress-free. At the ice front, the normal stress under the sea surface is equal to the hydrostatic water pressure. On the lateral boundary, the normal stress is equal to the ice pressure applied by neighboring glaciers and the normal velocity is assumed to be 0. The bed for grounded ice is assumed to be rigid, impenetrable, and fixed over time. Since we perform a stress-balance snapshot in the full-Stokes model, we do not need to prescribe surface mass balance or basal mass balance in the boundary conditions.

269

The normal basal velocity is set to 0 at the ice-bed interface. The linear sliding law is used to describes the relationship between the basal sliding velocity, \vec{u}_b , and the basal

272 shear force, \vec{t}_b , on the bottom of grounded ice,

$$\vec{\tau}_b = C \ \vec{u}_b.$$

To avoid non-physical negative values, $C = 10^{\beta}$ is used in the simulation. We call β the basal friction coefficient rather than *C*. *C* is initialized to a constant value of 10^{-4} MPa m⁻¹ yr (Gillet-Chaulet et al., 2012), and then replaced with the inverted *C* in subsequent inversion steps.

(5)

278

279 3.2.3 Surface Relaxation

We relax the free surface of the domain by a short transient run to reduce the nonphysical spikes in initial surface geometry (Zhao et al., 2018). The transient simulation period here is 0.5 yr with a timestep of 0.01 yr.

283

284 **3.2.4 Inversion and Improvement for Basal Friction Coefficient**

285 Taking the results from the surface relaxation as our ice geometry we use an inverse

model to retrieve the basal friction coefficient, the deviatoric stress field and ice velocity field. The inverse model adjusts the basal friction coefficient C to minimize the value of the cost function (Morlighem et al., 2010), which is defined as the difference between

289 the simulated surface velocity and the observed,

290
$$J_0 = \int_{\Gamma_s} \frac{1}{2} \left(|\vec{u}| - |\vec{u}_{obs}| \right)^2 d\Gamma$$
(6)

291 where Γ_s is the ice surface, \vec{u} and \vec{u}_{obs} are the simulated and observed surface velocities.

292

To avoid over-fitting of the inversion solution to non-physical noise in the observations,a regularization term,

295
$$J_{reg} = \frac{1}{2} \int_{\Gamma_s} \left(\left(\frac{\partial C}{\partial x} \right)^2 + \left(\frac{\partial C}{\partial y} \right)^2 \right) d\Gamma, \tag{7}$$

is added to the cost function, then the total cost function is defined as,

 $297 J_{tot} = J_0 + \lambda J_{reg}, (8)$

where λ is a positive regularization weighting parameter. An L-curve analysis (Hansen and Johnston, 2000) has been done for inversions to find the optimal λ by plotting the term J_{reg} as the function of J_0 . The optimal value of 10^{10} is chosen for λ to minimize J_0 .

301

Basal friction in reality depends on basal temperature, i.e., it is relatively large on cold beds since the ice is frozen, and small on warm bed where basal temperature reaches pressure-melting point allowing the ice to slide (Greve and Blatter, 2009). However, in the inverse model, basal friction coefficient (Eq 5) is adjusted to match velocity observations without regard to basal temperature, which leads to unrealistic noise manifested as local spikes in modelled basal friction heat (Fig. 5a).

308

311

309 We improve the parameterization of β via *C* in Eq 5 (Section 3.2.2) by considering 310 basal temperature T_{bed} ,

$$\beta_{new} = \beta_{old} + \alpha (T_M - T_{bed}), \tag{9}$$

312 where β_{old} is that from by the inverse model, α is a positive factor to be tuned, T_M is 313 pressure-dependent melting temperature. β_{new} equals β_{old} at a bed with temperate ice, 314 and is larger than β_{old} at a bed with ice temperature lower than T_M . We tune α in the 315 range of [0.1, 2] with an interval of 0.1, and find the local spikes in modelled friction 316 heat become fewer (Fig. 5) as α increases from 0.1 to 1, but stay almost constant with 317 α from 1 to 2. Therefore, we take α to be 1, and use the parameterization of β_{new} in Eq 318 5 in all the simulations. Using Eq 9, the difference of simulated and observed surface 319 velocity is unchanged over the region except for some parts of the inland boundary.



321 Fig. 5. Comparison of modelled basal friction heat with basal friction coefficient β_{old} (a) and β_{new} 322 with $\alpha = 1$ (b). The white square is enlarged.

323

324 3.2.5 Basal Melt Rate

Based on the inverted basal velocity and basal shear stress, we can calculate the basal friction heat. We then produce the basal melt rate using the thermal equilibrium as

327 follows (Greve and Blatter, 2009):

328
$$M = \frac{G + \vec{u}_b \vec{\tau}_b + k(T) \frac{dT}{dz}}{\rho_i L},$$
 (10)

329 where *M* is the basal melt rate, *G* is GHF, $\vec{u}_b \vec{\tau}_b$ is the basal friction heat, $-k(T) \frac{dT}{dz}$ is

the upward heat conduction, ρ_i is the ice density, and L is latent heat of ice melt. The

ice-bed interface gets heat through GHF and friction heat but loses heat from upwardheat conduction.

333 **3.3 Experimental Design of coupled simulations**

We design the coupled simulations in an 8-step scheme for coupling the forward modeland inverse model similar as Zhao et al. (2018):

- We run the forward model with the velocity direction taken from a mixture of the surface gradient and surface velocity observations, and get an initial modelled englacial temperature.
- 339 2. We do surface relaxation in Elmer/Ice with the englacial temperature from step340 1.
- 341 3. Taking the results from step 2 as the initial state, we do an inversion in Elmer/Ice
 342 using the modeled englacial temperature from step 1, to get a modelled surface
 343 velocity best fit to the observed surface velocity. The modelled surface velocity
 344 will remove some artifacts in the observed field.
- 345
 346
 We run the forward model using the velocity directions derived by merging the
 Bilmer/Ice modelled velocity, the surface gradient and the surface velocity

- observations. We use the modelled velocity by the full-Stokes inverse model to
 constrain the basal slip ratio, then constrain rheology and shape function in the
 forward model. Then we get an updated modelled englacial temperature.
- 350 5. We run the inverse model in Elmer/Ice with the improved englacial temperature351 from step 4, and get an updated modelled velocity.
- 352 6. We run the forward model again using the ratio of basal sliding to column353 average velocity in Elmer/Ice from step 5 to constrain the slip ratio, and get a
 354 further updated basal temperature.
- 355 7. We run the inverse model again in Elmer/Ice with the improved englacial
 temperature from step 6, and get an updated modelled velocity and stress.
- 357 8. We analyze the modelled results in step 7, calculate basal friction heat and basal358 melt rate.
- 359
- 360 We perform the above procedure for all six sets of GHF to produce six different results
- 361 for the basal thermal conditions.

362 4 Simulation Results

363 **4.1 Ice Velocity**

364 In the inverse model, the misfit between the modeled and the observed surface velocity is minimized. Therefore, we get very similar distributions of modeled surface velocity 365 field using different GHFs. Fig. 6 shows the modelled velocity in the experiment using 366 Martos et al. (2017) GHF as an example. The modeled surface velocity shows spatial 367 368 similarities to the observed surface velocity (Fig. 6a, b). Three fast-flowing outlet glaciers (Lambert Glacier, Lepekhin Glacier and Kronshtadtskiy Glacier) deliver ice to 369 370 the ice shelf. The velocity of the Lambert glacier exceeds 800 m yr⁻¹ at the grounding line. The Lepekhin Glacier and the Kronshtadtskiy Glacier have maximum flow 371 velocities of about 200 and 400 m yr⁻¹ at their grounding lines, respectively. Regions 372 373 with large differences between modeled and observed surface velocity occupy a small fraction of the whole area (Fig. 6c) and are associated with high velocity gradients. Ice 374 velocity decreases with depth. Fig. 6c shows modeled basal ice velocity. The maximum 375 basal velocity on Lambert Glacier exceeds 500 m yr⁻¹ near the grounding line, and 376 maximum basal velocities on Lepekhin Glacier and the Kronshtadtskiy Glacier reach 377 about 150 and 200 m yr⁻¹ at the grounding line. 378



Fig. 6. (a) Observed surface velocity, (b) modeled surface velocity in the experiment using Martos et al. (2017) GHF, (c) modeled basal velocity. The white solid lines in (a), (b), and (c) represent speed contours of 30, 50, 100 and 200 m yr⁻¹, respectively. The three fast-flowing outlet glaciers in plot (a) from left to right are Lambert, Lepekhin and Kronshtadtskiy glaciers.

384

385 **4.2 Basal Ice Temperature and Heat Conduction**

386 In Fig. 7 we show the modelled basal temperature from the six experiments. The 387 modelled ice basal temperatures in the fast-flowing regions are all at the pressure 388 melting point ("warm"). However, there are significant differences in the modelled 389 distribution of warm-based conditions in the slow-flowing region using different GHFs. 390 The basal temperature is highly dependent on the GHF. In the experiment using Li et 391 al. (2021) GHF (Fig. 7f), which has the highest GHF within the domain, the basal 392 temperature is at the melting point over most of the domain, with extensive cold based 393 regions confined to the southern part. The experiment using Martos et al. (2017) GHF 394 (Fig. 7a), which has the second highest GHF, yields the second largest area of warm 395 base, and the experiment using Purucker (2013) GHF (Fig. 7e), with the lowest GHF 396 gives the smallest warm-based area which is concentrated around the fast-flowing ice. 397 All experiments display cold basal temperatures to the southwest of the Lambert Glacier 398 Basin, associated with thin ice over subglacial mountains (Fig. 1c).



Basal Temperature(relative to PMP) (°C)

400 Fig. 7. Modelled basal temperature relative to pressure melting point, (a) to (f) corresponding to the

GHF (a) to (f) in Fig. 2. The ice bottom at the pressure-melting point is delineated by a white contour.



403

Fig. 8. Modelled heat change of basal ice by upward englacial heat conduction (unit: mW m⁻²). The
negative sign means that the upward englacial heat conduction causes heat loss from the basal ice
as defined by the color bar with cooler colors representing more intense heat loss by conduction. (a)
to (f) corresponding to the GHF (a) to (f) in Fig. 2. The white solid curves represent modelled speed
contours of 30, 50, 100 and 200 m yr⁻¹, the same as in Fig. 6b.

Fig. 8 show the modelled heat change of basal ice by upward englacial heat conduction in the six experiments. In most regions of the fast-flowing tributaries with velocity higher than 30 m yr⁻¹, the heat loss caused by upward basal heat conduction is lower than 30 mW m⁻² in all experiments, reflecting the development of a temperate basal 414 layer that limits the basal thermal gradient. For the vast inland areas, experiments yield

415 heat loss by upward heat conduction in the range of 45-60 mW m⁻² except for the

416 experiment driven by the Purucker (2013) GHF which has lower values around 30-45

- 417 mW m⁻². This is because the upward heat conduction equals GHF where basal 418 temperature is below the pressure melting point, and the Purucker (2013) GHF is lower
- 418 the pressure melting point, and the Purucker (2013) GHF is lower 419 than the others.
- 419 t 420

421 **4.3 Basal Friction Heat**

There is no significant difference in modelled basal friction heat across these 6 experiments, reflecting the fact that all of them have been tuned to match the surface velocity observations. So, we show only the modelled basal friction driven by Martos et al. (2017) GHF (Fig. 5b). As expected, basal friction heat is high in fast-flowing regions. The three fast-flowing tributaries have friction heat amounting to more than 50 mW m⁻², with the Lambert and Kronshtadtskiy glaciers having 2000 mW m⁻² at the grounding line.

429

430 **4.4 Basal Melt Rate**

431 We get the basal melt rate using the thermal balance equation (Eq 10). Fig. 9 shows the 432 modelled basal melt rate in the six experiments using different GHF. Regions with basal 433 melt rate coincide with a warm base where basal temperatures reach the pressure-434 melting point. There are significant differences in the area of basal melting among the 435 six experiments due to large variability in GHF. The experiments using Li et al. (2021) 436 and Martos et al. (2017) GHF yield the largest area with basal melting. In contrast, the 437 experiment using Purucker (2013) GHF gives the least area with basal melting (Fig. 438 10).

439

The modelled basal melt rate is below 5 mm yr⁻¹ in the parts of the vast inland region 440 441 that are warm based. Higher basal melt rates occur in fast-flowing regions (Fig. 9) where frictional heat is high (Fig. 5b), despite the differences in GHF (Fig. 2). Basal 442 melt rate is above 10 mm yr⁻¹ near the grounding line, reaching 500 mm yr⁻¹ at the 443 444 grounding line of the central flowline running onto Amery ice shelf. Thus, in fast-445 flowing regions, frictional heat is the dominant factor rather than GHF, consistent with 446 Larour et al. (2012) who noted that slower flowing ice in the interior of the ice sheet 447 will be more sensitive to the GHF, but frictional heat dominates GHF in regions of fast 448 ice flow.

449

450 We use the positions of observed subglacial lakes to validate simulated regions with 451 basal melting (Fig. 9). The modelled warm base in the experiment using Li et al. (2021) 452 GHF covers all the observed subglacial lakes in the domain (Fig. 9f), including the 453 recently discovered second-largest subglacial lake in Antarctica (Cui et al., 2020b). The 454 warm base in the experiment using Martos et al. (2017) GHF covers the second most 455 observed subglacial lakes (Fig. 9a), and the experiment using An et al. (2015) GHF the 456 third (Fig. 9c). The experiment using Shen et al. (2020) GHF captures two subglacial 457 lakes in the southwest of the domain (Fig. 9b), while the experiment using Shapiro and Ritzwoller (2004) GHF missed many known subglacial lakes in the southwest of the
domain, but successfully captures the recently discovered second-largest subglacial
lake (Fig. 9b, d). The experiment using Purucker et al. (2013) GHF performs worst in
recovering subglacial lake locations (Fig. 9e).

462

463 There are localized negative values of basal melt rate, indicating basal refreezing at

three locations (Fig. 9). The modelled refreezing locations are generally characterized

by large gradients in ice thickness, typically thinning by 700 m across a distance of 2

466 km. Radar surveys have not yet been done to confirm these freeze-on locations.

467

468





471 locations of observed subglacial lakes, and the area surrounded by the black line is the likely second

472 largest subglacial lake in Antarctica. There is modelled basal refreezing at three local places painted

- 473 in black.
- 474

475 **5 Discussion**

476 Uncertainties and bias in our simulations can come from several sources. We expect 477 that the present-day accumulation rate field will be higher than the long-term average, 478 because of lower accumulation rate during glacial periods. This will tend to increase 479 the downward advection of cold ice in our model, lowering the basal temperature in 480 comparison to reality. On the other hand, we also expect that the modern-day surface 481 temperature will be higher than the long-term average temperature, again because of 482 lower temperatures during glacial periods. This will tend to increase our modeled basal 483 temperature in comparison with reality. It is unclear which of these competing biases 484 is stronger.

485

486 Subglacial topography has an influence on geothermal heat at kilometer scales. 487 Typically, it has been assumed that subglacial ridges receive less heat flow and 488 subglacial valleys receive more heat flow, in comparison to the regional average (e.g., 489 van der Veen et al., 2007; Colgan et al., 2021). However, the effect depends on 490 subglacial rock type. Heat tends to follow the path of least resistance to the surface. The 491 thermal conductivity of rock varies with lithology, and can be either greater or smaller 492 than the thermal conductivity of ice (Willcocks & Hasterok, 2019), thus the sign of the 493 topographic effect on GHF can be either negative or positive. Without knowing a priori 494 whether the topographic effect will be positive or negative, it is hard to apply a 495 topographic correction field to the GHF input field.

496

497 GHF distribution largely governs basal thermal conditions. Many previous studies 498 (Larour et al., 2012; Pattyn, 2010; Pittard et al., 2016; Van Liefferinge and Pattyn, 2013; 499 Van Liefferinge et al. 2018) on basal temperature and basal melt have used the Shapiro 500 and Ritzwoller (2004), Fox Maule et al. (2005), Purucker (2013), and An et al. (2015) 501 GHF datasets, with few making use of the more recent Martos et al. (2017) and Li et al. 502 (2021) GHF datasets. In this study, we find that the Li et al. (2021) and Martos et al. 503 (2017) GHF datasets have higher GHF than the earlier datasets in the Lambert-Amery 504 domain and consequently have the largest area with warm base. The warmer basal 505 conditions best match the observed distribution of subglacial lakes. However, it should 506 be noted that observations of subglacial lakes are a one-sided constraint. A model result 507 that misses the observed lakes is clearly too cold at that location. But if the model result 508 shows basal melt at a place with no observed lakes, it is not clear whether this is because 509 the model is too warm, or if the subglacial water exists in a form other than ponded 510 lakes.

511

512 A lake complex beneath Devon Island ice cap in Canada exists at temperatures well 513 below pressure melting point due to large concentrations of dissolved salts (Rutishauser 514 et al., 2018), and while no similar ones are known to exist beneath the Antarctic ice 515 sheet, direct measurements of ice temperatures above water bodies are rare. 516 Furthermore, relatively high electrical conductivity beds such as water saturated clays 517 can give rise to false positives in radar detections of subglacial water bodies (Talalay et 518 al., 2020).

519

520 Our simulations make improvements on previous approaches. We use the full-Stokes 521 flow model in the inversion of basal friction field rather than a simplified physics model 522 as in Wolovick et al. (2021a). We also improve on the treatment of the basal friction 523 field by imposing a larger basal friction where the ice bottom is colder than the pressure 524 melting point, and which increases with temperature difference from freezing point. 525 These modifications produce more physically meaningful results since we expect 526 frozen beds to have high basal friction. Hence, the basal friction field is constrained by 527 simulated temperatures in addition to producing the best fitting match of simulated and 528 observed surface velocities.

529

530 Van Liefferinge and Pattyn (2013) estimated basal temperature for the Antarctica ice 531 sheet using three GHF datasets (Fox Maule et al., 2005; Shapiro and Ritzwoller, 2004; 532 Purucker, 2013), and each of the datasets were improved by the method in Pattyn (2010). 533 Their modeled temperatures show spatial similarities to the our experiment field using 534 Purucker et al. (2013) GHF. Pittard et al. (2016) did sensitivity experiments of the 535 Lambert-Amery glacial system based on 3 GHF fields (Fox Maule et al., 2005; An et 536 al., 2015; Shapiro and Ritzwoller, 2004) using the ice dynamics model PISM, and found 537 that modelled basal temperature reached the pressure melting point only under the fastflowing ice, with maximum melting rates of 500 mm yr⁻¹ at places very close to the 538 grounding line of the central flowline onto the Amery ice shelf. We also model 539 540 maximum basal melt at similar locations in the six GHF experiments. However, the 541 Pittard et al. (2016) region of basal melt is mainly confined to the Lambert glacier 542 tributary and matches only that of our experiment using Purucker (2013) GHF.

543

We analyze the contribution of GHF and frictional heat to basal melt. The basal friction is a significant heat sources only under fast-flowing ice. Most GHF distributions (except Martos et al., 2017 and Li et al., 2021) in the grounded ice sheet near the ice shelf are homogeneous, but frictional heating in the fast-flowing ice is more than 10 times higher than that in the slow-flowing ice. Thus slower flowing ice in the interior of the ice sheet is more sensitive to the GHF than fast-flowing ice (Larour et al., 2012).

550

551 GHF has its largest impact on the basal melt of the inland ice sheet. There are two 552 principle ways to constrain GHF: (1) direct measurement (2) inversion by multiple 553 geophysical methods. The GHFs used in this study are based on inversion of satellite 554 or aero magnetic data and seismic tomography. Direct observations of heat flux are 555 difficult to obtain in Antarctica, and satellite data are low resolution. The most efficient 556 methods is to invert the heat flux through aerial geomagnetic observation such as for 557 the Martos and Li GHF fields. However, there are still large data gaps in remote regions, 558 especially in PEL, leaving just inversion using satellite magnetic data with a lower 559 resolution. The Li et al. (2021) field uses the latest aeromagnetic data to estimate the

- 560 GHF in the PEL region and this gives higher values than derived previously.
- 561

To validate the modelled basal melt, we use the locations of detected subglacial lakes. There may be many other undiscovered subglacial lakes beneath the study area, and further discoveries would help us validate the model results, and possibly refine GHF maps. In addition, further observational constraints with a two-sided sensitivity to ice temperature, such as observations of subglacial freeze-on or measurements of englacial attenuation, would help us to identify areas in which the GHF maps are too warm, in addition to those areas in which they are too cold.

569

570 6 Conclusions

571 In this paper, we estimate the basal thermal conditions of the Lambert-Amery system 572 by coupling a forward model and an inverse model, based on six different GHF datasets. 573 We analyze the contribution of GHF, heat conduction, and basal friction to the modelled 574 basal melt rate. We verify the result using the locations of all known subglacial lakes,

574 basar men rate. we verify the result using the locations of all known subgracial is 575 and evaluate the reliability of six GHF datasets in our study domain.

576

577 Our approach is distinct from that used to find GHF fields employed by Wolovick et al.

578 (2021a), in particular the use of a full Stokes model allows the method to be extended 579 to fast flowing ice streams and ice shelf domains where neither the shallow ice nor 580 shallow shelf-approximations are valid. We also improve the basal friction calculation 581 to include information on the basal ice temperature relative to its pressure melting point. 582 This procedure results in removal of unrealistic noise manifested as local spikes in 583 modelled basal friction heat.

584

585 We find significant differences in the spatial extent of temperate ice in the slow flowing 586 areas among the six experiments due to large variability in GHF. The experiments using 587 Li et al. (2021) and the Martos et al. (2017) GHF yield the largest area with basal 588 melting, and match the subglacial lake locations best. In contrast, the experiments using 589 Purucker (2013) GHF gives the least area with basal melting and the worst match with 590 subglacial lakes locations. We suggest GHF datasets from Li et al. (2021) and Martos 591 et al. (2017) as the most suitable choice for this study region. We cannot make our own 592 GHF map from our analysis since while we can pick the GHF in places where the Li 593 and Martos geothermal heat flow maps are consistent and both agree with the 594 observations, we do not know which (if either) are correct where the Li and Martos 595 GHF datasets disagree and there are no observations. In order to make this 596 determination we would need additional observational constraints on the basal thermal 597 state, such as measured basal temperatures from deep ice cores, or observed refreeze-598 on, but neither are available in the region.

599

600 The fast flowing region has smaller modelled basal friction coefficients, and faster basal 601 velocities, but there are large differences in basal melting rates between the 6 GHF

602 datasets. The fast-flowing tributaries have frictional heating in the range of 50-2000

603 mW m⁻². In the vast inland areas, our experiments generally yield high upward heat

604 conduction in the range of 45-60 mW m⁻² which means that GHF dominates the heat

605 content of the basal ice in the slow flow regions. The modelled basal melt rate reaches

- $50-500 \text{ mm yr}^{-1}$ locally in three very fast flow tributaries (Lambert, Lepekhin and $50-500 \text{ mm yr}^{-1}$ locally in three very fast flow tributaries (Lambert, Lepekhin and $50-500 \text{ mm yr}^{-1}$ locally in three very fast flow tributaries (Lambert, Lepekhin and $50-500 \text{ mm yr}^{-1}$ locally in three very fast flow tributaries (Lambert, Lepekhin and $50-500 \text{ mm yr}^{-1}$ locally in three very fast flow tributaries (Lambert, Lepekhin and $50-500 \text{ mm yr}^{-1}$ locally in three very fast flow tributaries (Lambert, Lepekhin and $50-500 \text{ mm yr}^{-1}$ locally in three very fast flow tributaries (Lambert, Lepekhin and $50-500 \text{ mm yr}^{-1}$ locally in three very fast flow tributaries (Lambert, Lepekhin and $50-500 \text{ mm yr}^{-1}$ locally in three very fast flow tributaries (Lambert, Lepekhin and $50-500 \text{ mm yr}^{-1}$ locally in three very fast flow tributaries (Lambert, Lepekhin and $50-500 \text{ mm yr}^{-1}$ locally in three very fast flow tributaries (Lambert, Lepekhin and $50-500 \text{ mm yr}^{-1}$ locally in three very fast flow tributaries (Lambert, Lepekhin and $50-500 \text{ mm yr}^{-1}$ locally in three very fast flow tributaries (Lambert, Lepekhin and $50-500 \text{ mm yr}^{-1}$ locally in three very fast flow tributaries (Lambert, Lepekhin and $50-500 \text{ mm yr}^{-1}$ locally in three very fast flow tributaries (Lambert, Lepekhin and $50-500 \text{ mm yr}^{-1}$ locally in three very fast flow tributaries (Lambert, Lepekhin and $50-500 \text{ mm yr}^{-1}$ locally in three very fast flow tributaries (Lambert, Lepekhin and $50-500 \text{ mm yr}^{-1}$ locally in three very fast flow tributaries (Lambert, Lepekhin and $50-500 \text{ mm yr}^{-1}$ locally (Lambert, Lambert, Lepekhin and $50-500 \text{ mm yr}^{-1}$ locally (Lambert, Lambert, Lambert, Lambert,
- 607 Kronshtadtskiy glaciers) feeding the Amery ice shelf, and is in the range of 0-5 mm yr⁻ 608 1 in the inland region.
- 609

610 Data availability

- 611 All data sets used are publicly available.
- 612

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