



Persistent, Extensive Channelized Drainage Modeled Beneath Thwaites Glacier, West Antarctica

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Abstract. Subglacial hydrology is a leading control on basal friction and the dynamics of glaciers and ice sheets. At low discharge, subglacial water flows through high-pressure, sheet-like systems that lead to low effective pressures. However, at high discharge, subglacial water melts the overlying ice into localized channels that efficiently remove water from the bed, thereby increasing effective pressure and basal friction. Recent observations suggest channelized subglacial flow exists

- 5 beneath Thwaites Glacier, yet it remains unclear if stable channelization is feasible in West Antarctica, where surface melting is nonexistent and water at the bed is limited. Here, we use the MPAS-Albany Land Ice model to run a suite of over 130 subglacial hydrology simulations of Thwaites Glacier across a wide range of physical parameter choices to assess the likelihood of channelization. We then narrow our range of viable simulations by comparing modeled water thicknesses to previously observed radar specularity content, which indicates flat, spatially extensive water bodies at the bed. In all of our data-compatible
- simulations, stable channels reliably form within 100–200 km of the grounding line, and reach individual discharge rates of $35-110 \text{ m}^3 \text{ s}^{-1}$ at the ice-ocean boundary. While only one to two channels typically form across the 200 km width of the glacier in our simulations, their high efficiency drains water across the entire lateral extent of the glacier. We posit the large catchment size of Thwaites Glacier, its funnel-like geometry, and high basal melt rates together accumulate enough water to form stable channels. No simulations resembled observed specularity content when channelization is disabled. Our results
- 15 suggest channelized subglacial hydrology has two consequences for Thwaites Glacier dynamics: (i) amplifying submarine melting of the terminus and ice shelf, while (ii) simultaneously raising effective pressure within 100 km of the grounding line and increasing basal friction. The distribution of effective pressure implied from our modeling differs from parameterizations typically used in large-scale ice sheet models, suggesting the development of more process-based parameterizations may be necessary.

20 1 Introduction

Subglacial hydrology is a leading control on basal friction and frontal ablation rates of tidewater glacier termini, yet the morphology of subglacial drainage systems beneath the Antarctic Ice Sheet poorly characterized. Subglacial water can either flow through a highly pressurized, distributed network of bedrock cavities (Walder, 1986; Kamb, 1987), sediment canals





(Walder and Fowler, 1994), films (Weertman, 1972), and porous till (Clarke, 1987), or efficiently drain through arborescent
channels melted upward into basal ice (Röthlisberger, 1972). Water flow through a distributed system creates low effective pressures contributing to fast basal sliding (Walder, 1986; Kamb, 1987), whereas channelized drainage increases effective pressures (Röthlisberger, 1972; Schoof, 2010; Hewitt, 2011) and local submarine melt rates at the ice-ocean boundary (Slater et al., 2015). To date, most models of basin or ice sheet-scale Antarctic subglacial drainage have focused on hydropotential mapping (e.g., Stearns et al., 2008; Carter and Fricker, 2012; Le Brocq et al., 2013; Livingstone et al., 2013; Smith et al., 2017), and have only recently distinguished between conduit types under Antarctic glaciers (Dow et al., 2020; Wei et al., 2020). However, a growing body of work suggests a variety of drainage styles may be important in Antarctica, with obvious relevance to ice sheet dynamics.

In Antarctica, shallow hydropotential gradients and the lack of significant surface melt has led to the conventional paradigm that subglacial water fluxes are too small to permit stable channelized drainage beneath the ice sheets (e.g., Weertman, 1972;

- 35 Alley, 1989; Walder and Fowler, 1994; Carter et al., 2017). This assumption has led to the use of purely distributed subglacial hydrology models (e.g., Alley, 1996; Le Brocq et al., 2009), or simplifying approximations of effective pressure in large-scale Antarctic ice sheet models (e.g., Leguy et al., 2014; Asay-Davis et al., 2016; Yu et al., 2018; Nias et al., 2018; Cornford et al., 2020). However, channelized drainage under Antarctic ice sheets has recently been inferred through observations of ice shelf basal melt channels (Le Brocq et al., 2013; Marsh et al., 2016; Drews et al., 2017), radar specularity content (Schroeder et al.,
- 40 2013), and subglacial hydrology models (Dow et al., 2020; Wei et al., 2020). In the absence of surface meltwater, subglacial channels must be sustained through basal melting, and the presence of basal melt channels under ice shelves suggest that their grounded counterparts must persist stably for decades or centuries (Le Brocq et al., 2013; Marsh et al., 2016).

Thwaites Glacier contains enough ice to raise sea level 65 cm (Rignot et al., 2019), and may currently be undergoing an unstable retreat, likely triggered by increased melting of its ice shelf and terminus (Joughin et al., 2014; Rignot et al., 2014;

- 45 Seroussi et al., 2017; Milillo et al., 2019; Hoffman et al., 2019). Ice flux from Thwaites Glacier increased 76% between 1976–2013 (Mouginot et al., 2014), coinciding with thinning rates of up to 10 m yr⁻¹ and a surface acceleration of 100 m yr⁻¹ near the grounding line (Pritchard et al., 2009; Helm et al., 2014; Gardner et al., 2018). While bed topography primarily regulates Thwaites Glacier retreat, uncertainty in basal friction laws, ice flow models, and ice shelf melt parameterizations could affect mass loss projections for this century by up to 300% (Yu et al., 2018). As a prominent control on both basal friction and
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submarine melting, subglacial hydrology has the potential to be a critical component of Thwaites Glacier dynamics, yet the configuration of its drainage network is poorly understood.

Using a recent survey of radar specularity content, Schroeder et al. (2013) hypothesized that channelized subglacial drainage is pervasive within 75 - 100 km of the Thwaites Glacier grounding line. However, subsequent satellite detection of subglacial lakes led to the interpretation that such channels may only be ephemeral, forming only during lake drainage events (Smith

55 et al., 2017). Here, we pair remote sensing with the 2-dimensional subglacial hydrology model implemented within the MPAS-Albany Land Ice Model (MALI) (Hoffman et al., 2018), to provide a more complete picture of the likely configuration of the Thwaites Glacier subglacial drainage system. We run a suite of 138 modeling simulations, then compare our results with the observed radar specularity content of Schroeder et al. (2013) to define a subset of scenarios as possible representations of





reality. Results from this subset are then collated with ice shelf basal melt rates and common parameterizations of basal frictionto explore the significance of channelization on submarine melt rates and ice dynamics.

2 Methods

2.1 Model Framework

65 sheet that is designed to resemble the bulk flow of water through cavities on the lee-sides of bedrock bumps (Flowers and Clarke, 2002; Hewitt, 2011; Flowers, 2015), but may also reasonably describe flow through other porous media, such as till or till canals (Hewitt, 2011; Flowers, 2015; Hoffman et al., 2016). The distributed system discharge is given by:

$$\boldsymbol{q} = -k_{q}W^{\alpha_{1}}\left|\nabla\phi\right|^{\alpha_{2}}\nabla\phi\tag{1}$$

where k_q is the conductivity coefficient of the distributed system, W is the water thickness, and α_1 and α_2 are $\frac{5}{4}$ and $-\frac{1}{2}$, 70 respectively, to resemble a Darcy-Weisbach flow law. The hydropotential, ϕ , is defined as:

$$\phi = \rho_w g Z_b + P_w. \tag{2}$$

where ρ_w is the water density, g is the gravitational acceleration, Z_b is the bed topography, and P_w is the distributed water pressure. It is assumed all basal cavities remain filled, and thus water thickness is a function of cavity opening from basal sliding over bedrock bumps and creep closure:

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$$\frac{dW}{dt} = c_s \left| \boldsymbol{u}_b \right| \left(W_r - W \right) - c_{cd} A_b N^3 W$$
(3)

where c_s is a bed roughness parameter, u_b is the ice basal sliding velocity, W_r is the maximum bed bump height, c_{cd} is a creep scaling parameter for the distributed system, and A_b is the temperature-dependent ice flow rate parameter for basal ice. The effective pressure, N, is defined as the difference between the ice overburden and water pressures: $N = \rho_i g H - P_w$, for ice thickness H and ice density ρ_i .

80 The channelized system formulation resembles that of Werder et al. (2013), where channel discharge is given by:

$$\boldsymbol{Q} = -k_Q S^{\alpha_1} \left| \nabla \phi \right|^{\alpha_2} \nabla \phi \tag{4}$$

where k_Q is the channel conductivity coefficient. Channel cross-sectional area, S, is a function of creep closure, and melting/freezing due to the dissipation of potential energy, Ξ , and pressure-dependent changes to the sensible heat of water, Π :

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$$\frac{dS}{dt} = \frac{1}{\rho_i L} (\Xi - \Pi) - C_{cc} A_b N^3 S.$$
 (5)





Here, L is the latent heat of melting and C_{cc} is a creep scaling parameter for channels. Ξ includes dissipation terms for both the distributed and channelized systems, so that:

$$\Xi = \left| \frac{d\phi}{ds} \right| + \left| \frac{d\phi}{ds} l_c \boldsymbol{q}_c \right| \frac{P_w}{ds} \tag{6}$$

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where s is the along-channel spatial coordinate, and q_c is the discharge in the distributed system within a distance, l_c , from the channel. Using this formulation, channels may only develop if there exists sufficient discharge in the distributed system for melting to overcome creep closure. In our experiments, we disabled the pressure-dependent melting/freezing term, Π , to avoid nonphysical instabilities arising from intricate bed topography.

Closing the system of equations requires the conservation of water mass within the combined distributed and channelized subglacial drainage systems, and a conservation of energy equation for the production of basal meltwater. Conservation of mass is written as:

$$\frac{dW}{dt} = -\nabla \cdot \boldsymbol{q} - \left[\frac{\partial S}{\partial t} + \frac{\partial Q}{\partial s}\right] \delta(x_c) + \frac{m_b}{\rho_w},\tag{7}$$

where $\delta(x_c)$ is the Dirac delta function applied along the locations of the linear channels and m_b is the production of basal meltwater. Conservation of energy is written as

$$m_b L = G + \boldsymbol{u}_b \cdot \boldsymbol{\tau_b} \tag{8}$$

100 for basal shear τ_b and geothermal flux G.

The model runs on an explicit forward Eulerian time step that fulfills advective and diffusive Courant-Friedrichs-Lewy (CFL) conditions for the distributed system, and advective CFL conditions for the channelized system. Model outputs are written at 1 month intervals and all reported results are averaged over five years of model time to smooth any minor remaining transients in the system.

105 2.2 Thwaites Model Domain

We ran the majority of our simulations on a variable resolution domain of Thwaites Glacier that has a 4 km cell spacing over the fast flowing regions and coarsens to 14 km at the interior ice divide, for a total of 4267 grid cells. An additional simulation was performed with a higher resolution mesh that uses 1 km cell spacing in fast flowing regions, coarsening to 8 km at the interior ice divide, for a total of 75500 cells. The bedrock and ice geometry were interpolated onto the model mesh using

- 110 conservative remapping from the BedMachine Antarctica v1 ice thickness and bed elevation dataset (Morlighem et al., 2020). However, a maximum bed elevation of 1200 m and a ice thickness of 550 m was imposed over Mt. Takahe (>250 km from the terminus) to avoid instabilities arising from steep bed topography. The resulting thickness gradients were then smoothed by running only the ice dynamics and geometry evolution portions of MALI for 15 years. The geothermal flux was interpolated from the 15 km resolution dataset of Martos et al. (2017). The ice sliding velocity (u_b) and basal shear stress (τ_b) fields
- 115 required by the subglacial hydrology model follow the methods used by Hoffman et al. (2018) to generate a present-day initial





condition, where a basal friction parameter is optimized in order to minimize the misfit between modeled and observed ice surfface velocity (Perego et al., 2014).

Within the subglacial hydrology model, no flow lateral boundary conditions were applied at the ice-covered lateral boundaries of the model domain. At the glacier grounding line, a Dirichlet boundary condition on the hydropotential (ϕ) was applied equal to the hydropotential of seawater at each grid cell seaward of the grounding line,

$$\phi_o = \rho_w g Z_b - \rho_o g Z_b,\tag{9}$$

where $\rho_o = 1028 \text{ kg m}^{-3}$ is the density of ocean water. Note this boundary condition results in hydropotential values close to zero but spatially varying as ocean pressure varies along the grounding line with the thickness of the ocean water column. Additionally, inflow from the ocean to the subglacial drainage system is disallowed if the hydropotential underneath the grounded

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ice falls below the ocean hydropotential. This condition can occur due to a spatially variable, ocean-lateral boundary condition and the assumption of constant density within the subglacial drainage system, which in combination with subglacial channelization, can locally result in modeled inflow of ocean water. The model was spun-up with channelization disabled and a k_q value of 1.5×10^{-3} m^{7/4} kg^{-1/2} to allow water pressures to equilibrate at > 90 % overburden pressure. All other simulations were then initialized from the steady-state solution of this run.

130 2.3 Parameter Sweep and Sensitivity Analysis

Four primary yet poorly constrained parameters exist in equations 1, 3, and 4: k_q , k_Q , W_r , and c_s . While some theoretical and observational basis exists for the values of these parameters, the appropriate values are uncertain and likely vary by glacier basin. To address this uncertainty, we ran 113 different channel-enabled simulations within a plausible parameter space based on observations and theory, and compared results to multiple limiting criteria described below to identify the most realistic parameter combinations. The remaining 25 simulations in our parameter sweep were conducted disallowing channelization.

Observations of jökulhlaups suggest the typical Manning roughness, n, of subglacial channels ranges from 0.023 – 0.12 m^{-1/3} s (Nye, 1976; Clarke, 1982; Bjornsson, 1992; Clarke, 2003). We can translate these Manning roughness values to the equivalent channel conductivity range of 0.03 – 0.17 m^{7/4} kg^{-1/2} using (Werder et al., 2013):

$$k_Q^2 = \frac{1}{\rho_w g n^2 (\frac{2}{\pi})^{2/3} (\pi + 2)^{4/3}}.$$
(10)

- However, jökulhlaups do not provide an exhaustive range of roughness characteristics for channel flow, and dye-trace breakthrough curves have indicated that *n* values for low-discharge, high-friction subglacial channels could be as low as n = 0.68 m^{-1/3} s (Gulley et al., 2012), or $k_Q = 0.006$ m^{7/4} kg^{-1/2}. On the other extreme, the Manning roughness of a smooth brass pipe is 0.009 m^{-1/3} s (Chow, 1959), or $k_Q = 0.44$ m^{7/4} kg^{-1/2}, which we consider a generous upper end-member for k_Q . We therefore ran our model with k_Q ranging from 0.005 - 0.5 m^{7/4} kg^{-1/2} to encompass the full set of plausible values.
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Because k_q may be chosen to portray porous flow through cavities in till or bedrock, we selected k_q values to be within the appropriate range of till or greater. Estimates for the hydraulic conductivity, κ , of subglacial till ranges widely from $10^{-12} - 5 \times 10^{-4} \text{ m s}^{-1}$ (Fountain and Walder, 1998), which can be converted to an equivalent distributed conductivity coefficient in





our model via (Bueler and van Pelt, 2015):

$$k_q = \frac{\kappa}{\rho_w g W^{1/4} |\nabla \phi|^{-1/2}}.$$
(11)

Using a characteristic W of 0.1 (see below) and |∇φ| of 100 Pa m⁻¹ (approximated from our model domain), we estimate the conductivity coefficient of subglacial till in our model would be 10⁻¹⁵ – 10⁻⁶ m^{7/4} kg^{-1/2}, which should span our lower limit for k_q. In practice, however, simulations with k_q < 1.5 × 10⁻⁵ m^{7/4} kg^{-1/2} were over-pressurized and did not reach steady-state. Although no proper upper bound exists for k_q, we assume subglacial water pressures beneath Thwaites Glacier are similar to the neighboring Pine Island Glacier, and are thus near ice overburden pressure (Gillet-Chaulet et al., 2016). We
therefore attempted to limit our k_q parameter sweep to values that kept the average water pressure > 90% flotation, which typically occurred for k_q ≤ 5 × 10⁻³ m^{7/4} kg^{-1/2} across different bed roughness combinations.

In theory, W_r represents the characteristic bed bump height (decimeter-scale), while c_s represents the characteristic meterscale bed bump spacing (Figure 1). Typical values used for W_r and c_s are ~ 0.1 m (e.g., Schoof, 2010; Hewitt, 2011; Schoof et al., 2012; Werder et al., 2013; de Fleurian et al., 2018; Dow et al., 2020) and ~ 0.5 m⁻¹ (e.g., Schoof et al., 2012; Werder

- et al., 2013; Hoffman and Price, 2014; de Fleurian et al., 2018; Dow et al., 2020), respectively. To account for some amount of variability from these values, we ran our model with 6 different combinations of W_r = 0.05 m, 0.1 m, 0.2 m, and 1.0 m and c_s = 0.25 m⁻¹, 0.5 m⁻¹, and 1.0 m⁻¹, holding one at the default value of W_r = 0.1 m or c_s = 0.5 m⁻¹, and varying the other parameter. For each set of bed parameter combinations, we ran between 7 29 channel-enabled simulations with k_q and k_Q values within their plausible ranges. We spaced k_q and k_Q samples at consistent intervals, and stopped sampling conductivity
 parameter space when runs failed to reach steady-state or were under-pressurized (< 90% flotation).
 - Additionally, for each pair of bed roughness parameters, we ran 4-5 simulations with channelization disabled across a similar range of k_q values (25 runs total). These were used as counter-examples to explore the impact of subglacial channel drainage under Thwaites Glacier.
- By design, the parameter sweep forces our model to operate at the limit of its ability to remain stable, and we thus found it useful to define two separate steady-state criteria. We categorized runs as either reaching a pressure steady-state or a flux steadystate. Pressure steady-state was defined as $\langle \frac{\partial N_{ij}}{\partial t} N_{ij}^{-1} \rangle \leq 0.5\%$, where $\langle \rangle$ denotes an average over all grounded grid cells *j* and time steps *i* over 5 years of model time. Flux steady-state was attained when the area-integrated version of equation 7 upstream of a specified cross-glacier transect was met within 0.5% when averaged over 5 years. Transects were defined every 50 km within 200 km of the grounding line (Figure 4). We report results regarding water thickness and water pressure from pressure
- 175 steady-state runs, but only report discharge results from runs that also meet the flux steady-state at each transect. We use this approach because water pressure and thickness fields from pressure steady-state runs strongly resemble their flux steady-state neighbors in parameter space, yet the channel model fails to reach equilibrium in some runs due to local channel instabilities that do not affect area-averaged water pressure or water thickness. Therefore, we have confidence that pressure steady-state runs still yield useful information about water pressure and thickness. Simulations that did not reach either steady-state criteria,
- 180 or had water pressures < 90% flotation, were discarded.



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2.4 Model Comparison with Observed Specularity Content

All simulations that reached a pressure steady-state were compared with observed radar specularity content from Thwaites Glacier (Schroeder et al., 2013) to further narrow the range of viable parameter combinations. Specularity content determined from airborne ice-penetrating radar is commonly used for detecting subglacial water bodies beneath ice sheets (e.g., Schroeder et al., 2013, 2015; Young et al., 2016, 2017; Dow et al., 2020), and has recently been used to validate a subglacial hydrology model of Totten Glacier, East Antarctica (Dow et al., 2020). Although our methods differ, we rely on the same concepts that make specularity content a useful tool for subglacial hydrology model validation.

Ponding within the subglacial drainage system creates flat, reflective surfaces that cause bright specular returns, as opposed to bedrock, which has a lower dielectric contrast to ice, and whose rough texture scatters energy (Schroeder et al., 2015).

- 190 Similarly, the curved surface of less uniform conduits such as channels or rough linked cavities scatters energy uniformly in all directions, creating areas of low specularity content, despite the presence of water (Schroeder et al., 2013). High specularity content, therefore, unequivocally depicts flat-surfaced water bodies in an inefficient distributed system, while low specularity content can either represent a distributed system below its capacity, or the existence of water in rougher, more variably shaped conduits, such as channels.
- 195 To compare specularity content with our model output, we first averaged the specularity content from the North-South and East-West radar transects from Schroeder et al. (2013) onto a 5 km grid. We then defined a water thickness to bump height ratio, R_{wt} , which indicates the degree to which modeled conditions would produce flat and extensive interfaces between water and ice at the glacier bed, and therefore highly specular surfaces:

$$R_{wt} = \frac{W}{W_r}.$$
(12)

- 200 For $R_{wt} \gtrsim 1$, distributed water thickness nears or exceeds bed bump height, thus creating a flat, highly-specular surface of water. However, for $R_{wt} \ll 1$ bedrock geometry determines the roughness of the lower interface, and the location is considered rough-surfaced and non-specular (Figure 1). With a proper value of k_q , R_{wt} can also parameterize till saturation, with low and high R_{wt} indicating under-saturated (non-specular) till and saturated (specular) till, respectively. For easy comparison, R_{wt} was calculated for each model grid cell, then interpolated onto the same 5 km grid as the specularity content data.
- To avoid over-interpretation, we limited our comparison to catchment-scale features by creating binary masks of specularity content and R_{wt} (Figure 2). Grid cells were labeled high/low specularity content or R_{wt} if their value was above/below a threshold value. In reality, there is a gradual transition in which a non-specular surface becomes specular with the addition of water, and our binary masks are therefore sensitive to the artificial choice of critical threshold. To better capture the transitional behavior, we created 11 specularity content masks with specularity thresholds, S^{crt} , ranging 0.15 – 0.25 at evenly-spaced intervals of 0.01, and 6 R_{wt} masks per simulation with thresholds, R_{wt}^{crt} , ranging 0.95 – 1.0 at intervals of 0.01. The 66
- combinations of specularity content and R_{wt} masks were then compared using two criteria:
 - 1. The masks were divided into four zones based on Schroeder et al. (2013): a near-terminus non-specular zone thought to have channelized flow, a lower specular zone approximately at the transition zone of Schroeder et al. (2013), an upper





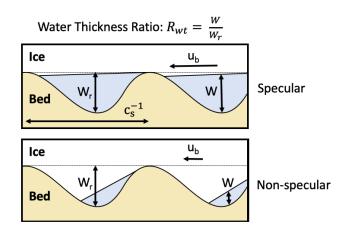


Figure 1. Schematic of a specular and non-specular distributed system, as defined by the water thickness ratio, R_{wt} . Physical representations of bed roughness parameters are included.

specular zone where ponding is thought to occur, and an upper non-specular zone likely containing little basal water. The specularity content and R_{wt} masks had to agree for a majority of the cells within each zone.

2. The two masks needed to have an overall correlation coefficient of ≥ 0.35 , which was empirically tuned to select for similar patterns between masks when paired with the first criterion.

Simulations that did not meet these criteria were deemed unrealistic and were excluded from further analysis.

3 Results

220 3.1 Channel-Enabled Parameter Sweep

3.1.1 Model Tuning and Correspondence with Specularity Content

Of our channel-enabled runs, 39 met our pressure steady-state criterion, while 23 of those also met our flux steady-state criterion across all transects. 20 pressure steady-state runs, including 14 flux steady-state runs, had at least one R_{wt} and specularity mask combination that met our comparison criteria, and were therefore considered possible representations of reality. Each of these runs showed a strong resemblance between R_{wt} and specularity content masks (Figure 2). Hereafter, all steady-state runs that

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runs showed a strong resemblance between R_{wt} and specularity content masks (Figure 2). Hereafter, all steady-state runs that had at least one R_{wt} and specularity content mask combination that met our two comparison criteria, and had average water pressures of > 90% flotation, will be referred to as data-compatible. Runs additionally meeting flux steady-state (FSS) criteria will be referred to as data-compatible FSS runs.

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Average water pressures in data-compatible runs were between 91-96% flotation, and in general, runs that did not correspond with specularity content had water pressures outside of this range. Data-compatible runs either had k_q values of 1.5×10^{-4} or 5×10^{-4} m^{7/4} kg^{-1/2} (Figure 3), with the only exceptions occurring when $W_r = 0.05$ m or $W_r = 1.0$ m, in which data-





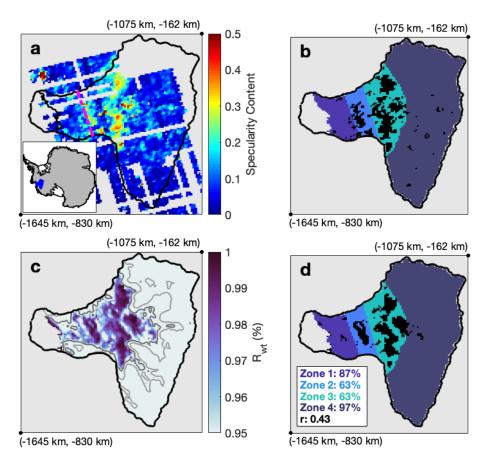


Figure 2. An example comparison of catchment-scale features identified with binary masks of observed specularity content and modeled R_{wt} . **a**) radar specularity content (Schroeder et al., 2013) and **c**) R_{wt} for a data-compatible FSS model run, together with their coinciding binary masks, **b**) ($S^{crt} = 0.19$) and **d**) ($R_{wt}^{crt} = 0.98$), respectively. The pink dashed line in **a** marks the transition between highly-specular, distributed drainage and channel-dominated drainage, as hypothesized in Schroeder et al. (2013). The four zones used for comparison between specularity content and R_{wt} are color-coded in **b** and **d**. Light and dark gray lines in **c** are the 50% and 90% R_{wt} contours, respectively. The percent match between masks within each zone and the overall correlation are given in **d**. The locations of map corners are given in Standard Antarctic Polar Stereographic coordinates. The inset in **a** shows the location of Thwaites Glacier (blue).

compatible k_q values reached 1.5×10^{-3} and 5×10^{-5} m^{7/4} kg^{-1/2}, respectively. This range of k_q is above that of pure glacial till, and is consistent with a bed composed of both till and bedrock, as is thought to be the case for Thwaites Glacier (Joughin et al., 2009; Muto et al., 2019b, a).

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For the channelized conductivity values, all data-compatible runs had k_Q values of $0.005 - 0.1 \text{ m}^{7/4} \text{ kg}^{-1/2}$, coinciding with the expected range given by dye-trace breakthrough curves and Jökulhlaup observations (Nye, 1976; Clarke, 1982; Bjornsson, 1992; Clarke, 2003; Gulley et al., 2012). No runs with $k_Q = 0.5 \text{ m}^{7/4} \text{ kg}^{-1/2}$, outside of our brass pipe upper limit, reached either steady-state criterion. Typical channel velocities in our data-compatible runs do not exceed the typical observed Jökulh-





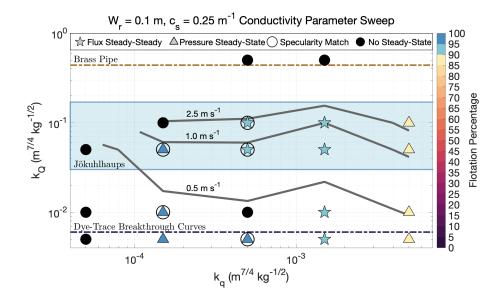


Figure 3. The conductivity parameter sweep for bed roughness parameters $W_r = 0.1 \text{ m}$ and $c_s = 0.25 \text{ m}^{-1}$. Stars represent runs that reached flux (and pressure) steady-state, triangles symbolize pressure steady-state simulations, and filled black circles depict runs that did not reach either steady-state criterion. Symbols for steady-state runs are color-coded by the average flotation percentage of grounded ice. Circles around stars or triangles indicate runs that matched observed specularity content, and are considered data-compatible. Gray lines are 95th percentile channel velocity contours for channels with $Q > 5 \text{ m}^3 \text{ s}^{-1}$. k_Q limits determined from a brass pipe and dye-trace breakthrough curves are plotted as brown and dark-blue dashed lines, respectively, and the blue shaded area represents the typical observed Jökulhlaup k_Q range.

laup range of 0.6 – 2.7 m s⁻¹ (Magnusson et al., 2007; Werder and Funk, 2009, Figure 3), which provides an additional loose
constraint on the validity of our channel model, although currently no observations of subglacial flow velocities exist from Antarctica.

3.1.2 Extent of Channelization in Data-Compatible Simulations

Subglacial channels were ubiquitous in all data-compatible FSS runs. In most of these runs, channels with discharges over 5 m³ s⁻¹ extended at least 150 km from the glacier terminus, with some channels reaching farther than 200 km (Figure 4). The initiation of these channels generally coincided with the upper specular zone observed in Schroeder et al. (2013). However, channel discharge between 150 - 200 km was divided between 2 to 4 small channels, each with an individual discharge of less than 20 m³ s⁻¹. At 150 km from the terminus, distributed discharge was still the dominant mode of drainage, with average channelized and distributed discharges of 27 ± 18 and 42 ± 19 m³ s⁻¹ (± indicates standard deviations), respectively, across data-compatible runs.

A transition occurs between 50–100 km from the terminus from a distributed-dominated to a channel-dominated system, coinciding with the region where Schroeder et al. (2013) hypothesized channelization begins under Thwaites Glacier. In our model, all data-compatible runs had formed at least one channel transporting $> 10 \text{ m}^3 \text{ s}^{-1}$ by 100 km from the terminus, and





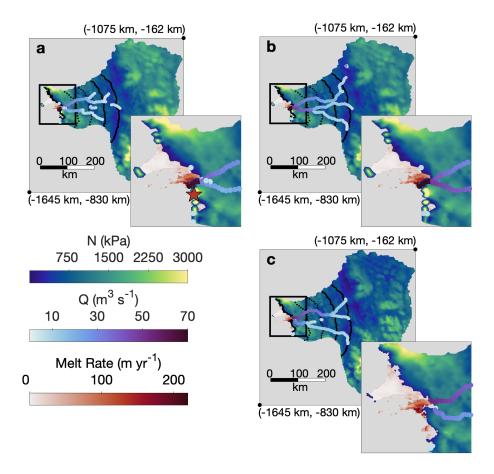


Figure 4. a) Average effective pressure and channel discharge across all data-compatible FSS runs. **b–c**) Effective pressure and channel discharge for **c**) the high-resolution model, and **b**) its low-resolution counterpart. The insets are enlarged views of the black boxes, and the star in **a** indicates the location of the secondary channel seen in one data-compatible FSS run. Sub-ice-shelf melt rates from Adusumilli et al. (2020) are plotted in all frames. For clarity, only channels with $Q > 5 \text{ m}^3 \text{ s}^{-1}$ are pictured in each frame. Transects spaced every 50 km from the terminus are shown as black lines (used in Figure 5), with the dotted lines spanning the transition zone of Schroeder et al. (2013). The locations of map corners are given in Standard Antarctic Polar Stereographic coordinates.

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by 50 km, these channels had grown and converged into 1-2 primary channels, each draining up to 50 m³ s⁻¹ of water. Our 50 km transect is the first at which channelized drainage slightly outweighs distributed drainage, with discharges of 55 ± 21 and 47 ± 20 m³ s⁻¹, respectively (Figure 5). Consistent with Joughin et al. (2009), basal friction melting is the primary contributor of melt in our model, and the 50–100 km transition to channelized flow coincides with a substantial increase in basal friction melt rate.

Channelized discharge grows rapidly within 50 km of the terminus. By the point at which water reaches the grounding line, channelized drainage accounts for $127 \pm 24 \text{ m}^3 \text{ s}^{-1}$ of runoff into the ocean, whereas only $25 \pm 21 \text{ m}^3 \text{ s}^{-1}$ is expelled through the distributed system (Figure 5). In all data-compatible FSS runs, the majority of channel discharge at the grounding line

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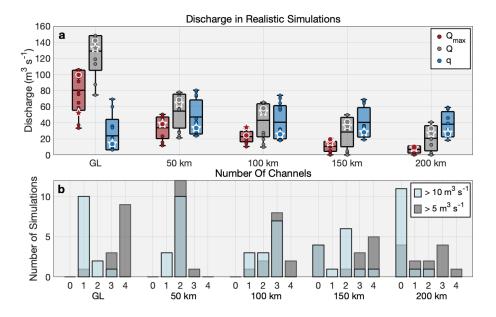


Figure 5. a) Total distributed (blue) and channel discharge (gray), as well as the discharge of the largest channel (red) across each transect (see Figure 4) for all data-compatible FSS runs (circles). Boxplots indicate the maximum, minimum, mean, and standard deviations. The stars indicate the high-resolution model, and the white-edged circles designate its low-resolution counterpart. b) The number of channels with $Q > 5 \text{ m}^3 \text{ s}^{-1}$ (gray) and $Q > 10 \text{ m}^3 \text{ s}^{-1}$ (blue) at each transect for all data-compatible FSS runs.

occurred through one primary channel with a discharge of $80 \pm 24 \text{ m}^3 \text{ s}^{-1}$ near the center of the grounding line $(-1.5369 \times 10^6 \text{ m}, -4.7298 \times 10^5 \text{ m}; \text{Standard Antarctic Polar Stereographic})$. This location corresponds to the region of high basal melting observed at the Thwaites Ice Shelf in Adusumilli et al. (2020) (Figure 4). In one simulation, a secondary channel intersects the grounding line with a discharge of $38 \text{ m}^3 \text{ s}^{-1}$ at $(-1.5310 \times 10^6 \text{ m}, -4.8585 \times 10^5 \text{ m})$ where we lack basal melt data (Figure 4a). Other channelized discharge across the grounding line occurs through very small channels ($\leq 10 \text{ m}^3 \text{ s}^{-1}$ scattered along the marine boundary.

3.2 Grid Resolution Sensitivity Analysis

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One data-compatible FSS simulation ($k_Q = 0.05 \text{ m}^{7/4} \text{ kg}^{-1/2}$, $k_q = 4 \times 10^{-4} \text{ m}^{7/4} \text{ kg}^{-1/2}$, $c_s 0.5 \text{ m}^{-1}$, $W_r = 0.1 \text{ m}$) was rerun to flux steady-state with the high-resolution domain. The high-resolution run matched observed specularity content, and produced effective pressures and water fluxes that closely resembled its low-resolution counterpart. High-resolution channels

- followed very similar pathways as those in the low resolution model (Figure 4b–c), and distributed and channelized discharges at each transect were approximately equal to those at low-resolution (Figure 5a). The main exception occurred at the grounding line, where the two main channels reached the ocean independently in the high-resolution model, but merge just above the
- grounding line with lower resolution (Figure 4b–c). This explains the almost twofold discrepancy of maximum channel disobserve at the grounding line between the two resolutions (Figure 5c). Additionally, the high resolution run had lower effective





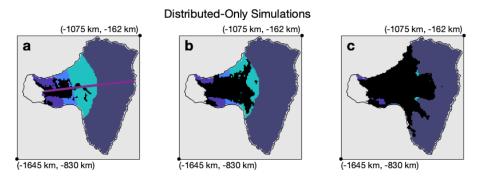


Figure 6. Three typical R_{wt} binary mask configurations for distributed-only runs. Masks depict regions where R_{wt} is above its threshold value, and thus the distributed system is at or above its capacity. Masks generally resembled one of these three patterns, or had no substantial regions of $R_{wt} \ge R_{wt}^{crt}$. Color-coding corresponds to the same zones as used in Figure 2. Purple line in **a** is the center-line transect used in Figure 7.

pressures near the upper domain boundary, although effective pressures within 300 km of the terminus are in strong agreement with the low-resolution model.

3.3 Distributed-only Model Configuration

Average water pressures in our 25 distributed-only simulations ranged from 74-98% flotation, and all met our flux steady-state
criteria. However, no distributed-only run had a R_{wt} field that matched observed specularity content. In particular, the greatest mismatch occurred between 0 – 50 km and 100 – 150 km of the grounding line, where R_{wt} was consistently over R^{crt}_{wt}, but where observed specularity content was low (Figure 6). In other cases where the average flotation percentage was below 90%, water thicknesses were too low to produce any regions of R_{wt} ≥ R^{crt}_{wt}. Furthermore, distributed-only simulations had unrealistically low effective pressures within 150 km of the terminus. Of the runs with an average water pressure over 90% flotation, many were at or near flotation within 200 km of the terminus (Figure 7a). Within 50 km of the terminus, the average effective pressure across these distributed-only runs was one-third that of data-compatible channel-enabled scenarios.

4 Discussion

4.1 A Reconciled Framework for Channelization Beneath Thwaites Glacier

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The key result of our study is the likely existence of stable subglacial channels beneath Thwaites Glacier. In our model, channels typically extended over 100–200 km inland, and had grounding line discharges of $80 \pm 24 \text{ m}^3 \text{ s}^{-1}$, much larger than the maximum discharges of $1-5 \text{ m}^3 \text{ s}^{-1}$ and $< 25 \text{ m}^3 \text{ s}^{-1}$ modeled at Getz (Wei et al., 2020) and Totten (Dow et al., 2020) glaciers, respectively. No distributed-only experiments matched observed specularity content, and all had unrealistically high





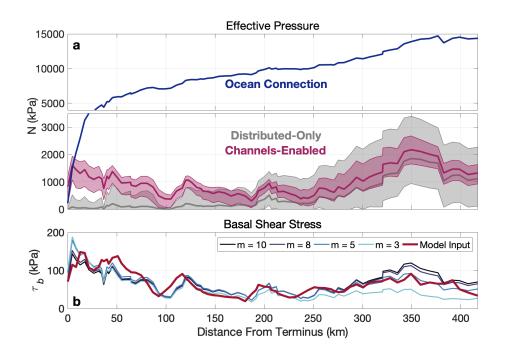


Figure 7. a) The range and mean (solid line) of effective pressures along the center-line transect in Figure 6a for all data-compatible FSS, channel-enabled runs (magenta) and all distributed-only runs above 90% flotation (gray). Shown in blue is the calculated effective pressure if assuming a perfect hydrostatic connection with the ocean. Note the different y-axis scale in the upper panel. b) Basal shear stress used as input in our model (red) plotted with reconstructed basal shear stress using a Budd-style friction law (blue). Blue hues represent different exponents used in the friction law. All lines follow the same center-line transect as in **a**.

water pressures within 100 km of the terminus. This strongly argues that channelized drainage is necessary to explain observed radar specularity content.

295 Certain geometric and hydrologic conditions at Thwaites Glacier are unfavorable to the development of subglacial channels, and thus the extent of channelization in our model is somewhat surprising. In theory, subglacial channels should develop when the distributed system reaches a critical discharge that is inversely proportional to the hydropotential gradient (Schoof, 2010; Hewitt, 2011). In Greenland, it is believed that glaciers are unable to reach this critical threshold farther inland where gentle surface slopes weaken the hydropotential gradient and thick ice may expedite creep closure (Chandler et al., 2013; Meierbachtol

- 300 et al., 2013; Dow et al., 2014). Similar logic could also apply to the thicker and broader Antarctic ice sheets, especially given their insignificant surface melt input. Yet, our model consistently depicts subglacial channels extending 100–200 km inland in all parameter choices. These channels could be explained by the large catchment size (189000 km²) of Thwaites Glacier (Joughin et al., 2009), its funnel-like geometry, and high basal melt rates of $3.5 \text{ km}^3 \text{ yr}^{-1}$ (Joughin et al., 2009), which together accumulate enough water to exceed the critical discharge threshold within 100–200 km from the grounding line. At first, the
- 305 critical discharge may only be met locally (e.g., Hewitt, 2011) through the accrual of water in topographic depressions, which the subglacial channels tend to follow. High basal friction melt rates of $100 1000 \text{ mm yr}^{-1}$ in the terminal 100 km, as





calculated for our model input and by Joughin et al. (2009), are then likely responsible for the increased channelization near the grounding line.

- Previous work has offered contrasting hypotheses on the persistence of subglacial channels beneath Thwaites Glacier. Orig-310 inally, Schroeder et al. (2013) argued radar scattering from widespread concave channels produced the near-terminus, nonspecular region they observed. However, an extensive channelized system may not allow for the isolation of subglacial lakes, and the discovery of subglacial lakes beneath Thwaites Glacier suggested channels may be ephemeral, forming only during subglacial lake drainage events (Smith et al., 2017). Based on our model, we here present a refinement of the hypothesis of Schroeder et al. (2013) that leaves room for the development of the subglacial lakes observed by Smith et al. (2017).
- 315 Our model indicates the near-terminus, non-specular zone of Schroeder et al. (2013) depicts a below-capacity distributed system, whose water has been partially evacuated by a small number of large, stable channels. In such a system, it is expected that isolated areas of the bed exist in which subglacial lakes may form. Disconnected portions of the drainage network are common beneath alpine and Greenland glaciers, particularly in the summer when channels draw water from the surrounding distributed system, leading to the isolation of poorly connected basal cavities (Murray and Clarke, 1995; Gordon et al., 1998;
- 320 Andrews et al., 2014; Hoffman et al., 2016; Chu et al., 2016; Rada and Schoof, 2018). Disconnected areas may exist year-round, or may reconnect following a reconfiguration of the channelized system or the collapse of channels in the winter (Hoffman et al., 2016; Rada and Schoof, 2018). However, substantial subannual reshaping of the drainage system should not occur in the absence of a seasonal melt cycle, like at Thwaites Glacier, and thus parts of the bed may remain disconnected for extended periods of time. This would allow disconnected water to gradually pool into lakes that drain when they periodically exceed their
- 325 hydropotential seal (Fowler, 1999). Such drainage events could act as similar catalysts for drainage network reconfigurations as the seasonal melt cycles of alpine and Greenland glaciers.

Even at flux steady-state, periodic subglacial lake filling and draining occurs near channels in our high-resolution model, principally between 80–200 km, within the region they are observed in Smith et al. (2017). These lake drainage events are much smaller (dW = 0.1 - 1 cm) and recur more frequently ($\sim 1-3$ years) than those observed, but may represent similar

- 330 processes taking place. Consistent with theory (Carter et al., 2017), modeled subglacial lakes tend to form in low-lying bed topography where the till is thought to accumulate (Joughin et al., 2009; Muto et al., 2019b, a), and it is likely our spatially constant k_q is too high in these areas to represent flow through saturated till. Assigning a smaller k_q in till-laden regions may facilitate growth of larger subglacial lakes, due to the decreased conductivity of the substrate. With a small enough k_q , the modeled periodic subglacial lake drainage events may resemble those observed. It is also possible our model inaccurately
- 335 portrays these subglacial lakes because it does not account for drainage through canal incision into underlying till (Carter et al., 2017). While subglacial lakes are compatible with our framework for channelization, and some evidence for them exists in our model, further work is needed to understand their behavior beneath Thwaites Glacier.





Implications of Channelization on Thwaites Glacier Dynamics 4.2

Channelization and Submarine Melting at the Grounding Line 4.2.1

The rapid and potentially unstable retreat of Thwaites Glacier is likely driven by enhanced sub-ice-shelf melting (Rignot et al., 340 2014; Joughin et al., 2014; Seroussi et al., 2017; Yu et al., 2018; Milillo et al., 2019; Hoffman et al., 2019), resulting in part from intruding warm Circumpolar Deep Water (CDW) flowing along bathymetric troughs to the grounding line (Nakayama et al., 2019; Milillo et al., 2019; Hogan et al., 2020). The most rapid retreat (12–18 km between 1992–2011) was recorded at the glacier's central, fast-flowing core (Rignot et al., 2014), where the retreat has continued at a rate of 0.6 km yr⁻¹ until at least 2017 (Milillo et al., 2019). Ice shelf submarine melt rates exceed 200 m yr⁻¹ at the fast-flowing core, coincident with the 345 recent formation of a prominent sub-shelf cavity (Adusumilli et al., 2020; Bevan et al., 2021).

In all but one of our low-resolution data-compatible FSS runs, both main channels converge near the grounding line directly above the subshelf cavity described in Bevan et al. (2021) (Figure 4a-b). In our high-resolution model, one channel intersects the grounding line at this location, while the second reaches the ocean 16 km to the east, also in the region of high subshelf

- melting (Figure 4c). Subglacial discharge plumes, formed from channelized subglacial water entering the ocean, amplify local 350 submarine melting through turbulent heating and the entrainment of deep and often warm water, such as CDW, along the terminus and ice shelf (Jenkins, 2011; Slater et al., 2015; Asay-Davis et al., 2017). While it would be an over-interpretation of our model to regard the exact locations of subglacial channels as reality, the ubiquitous conjunction of large channels (33-106 $m^3 s^{-1}$) with high subshelf melt rates at the grounding line in all data-compatible scenarios strongly suggests channelized
- subglacial discharge augments submarine melting in this region. Recent ocean modeling of the Pine Island Ice Shelf cavity 355 supports this assertion, and indicates subglacial discharge localized at the grounding line, and of similar magnitude to what occurs in our model, can explain the local ice shelf melt rates of $\sim 200 \text{ m yr}^{-1}$ observed at Pine Island Glacier (Nakayama et al., 2021).
- Additionally, CDW reaches the Thwaites Glacier grounding line through a series of bathymetric troughs and sills that 360 moderate its flow (Nakayama et al., 2019; Hogan et al., 2020), and it is possible the entrainment of ambient water into subglacial discharge plumes may further enhance CDW flushing of the Thwaites subshelf cavity, similar to the subglacial plume-driven renewal of Greenland fjords (Gladish et al., 2015; Carroll et al., 2017; Zhao et al., 2021). However, plume-driven buoyancy forcing may only have a minimal effect on cavity circulation beneath the Pine Island Ice Shelf (Nakayama et al., 2021), and thus it could be assumed that the comparable grounding line fluxes given by our model are still too weak to significantly enhance CDW advection to Thwaites Glacier. 365

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4.2.2 Implications of Channelization for Effective Pressure and Basal Sliding

Despite contributing to high ice-shelf basal melt rates and potential loss of ice-shelf buttressing, our model suggests subglacial channels may have a stabilizing effect on basal drag near the grounding line. Effective pressures are $3 \times$ higher within 50 km of the grounding line in channel-enabled runs than in distributed-only runs (Figure 7d). This region of high effective pressure coincides with a distributed system that is operating below its capacity (Figure 2), something not reproducible in distributed-



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only simulations (Figure 7a-c). Only 1-3 principal channels exist within the terminal 100 km; nevertheless, comparison with distributed-only experiments indicates that a small number of channels are still able to efficiently evacuate water from the entire region, due to their lower hydropotential compared to the surrounding area. Higher effective pressure in the terminal 100 km implies higher basal friction, which has been shown to be a leading control on the retreat and mass loss of Thwaites Glacier (Yu et al., 2018) and surface velocities at the neighboring Pine Island Glacier (Gillet-Chaulet et al., 2016; Joughin et al., 2019).

- High basal shear stress associated with competent bedrock is already thought to exist within 80 km of the grounding line (Joughin et al., 2009), and may work in tandem with channelized subglacial drainage to help buttress against further retreat. Smith et al. (2017) noted that the small (< 10%) increase in ice velocity observed after subglacial lake drainage events may
- indicate an insensitivity of Thwaites Glacier dynamics to its subglacial hydrology. However, the linked subglacial lake drainage event measured by Smith et al. (2017) beneath Thwaites Glacier in 2013–2014 had an average discharge of $160 - 240 \text{ m}^3 \text{ s}^{-1}$ 380 over 6 months; only 3-5 times greater than modeled channel discharge 50 km from the terminus, and 1-2 times greater than the largest modeled channels at the grounding line. Any pre-existing channels of similar size to those in our model could, therefore, help accommodate the additional flux from lake drainage events, which may explain the relatively minor increase in ice velocity they observed. Thus, this lake drainage event could also be interpreted as evidence of channelized drainage 385 stabilizing glacier dynamics, as is indicated by our model. As Thwaites Glacier continues to thin and retreat, we expect the subsequent changes in glacier geometry and meltwater input to continually reshape its subglacial drainage network. Our results suggest this will alter ice dynamics, and should be taken into account when considering the uncertainty in model projections.

Ice dynamics models have recently started implementing effective pressure-dependent sliding laws supported by current theory. However, a challenging problem is how to best parameterize effective pressure in order to solve for basal shear stress.

- 390 A common approach is to approximate effective pressure by assuming a perfect hydrostatic connection with the ocean (e.g., Leguy et al., 2014; Asay-Davis et al., 2016; Yu et al., 2018; Nias et al., 2018; Cornford et al., 2020, and others), shown for our model domain in Figure 7a. Effective pressure using an ocean connection assumption is in fair agreement with our channel-enabled runs within 5 km of the grounding line, but is up to an order of magnitude too high further inland, indicating a parameterization based on an open ocean connection may only be realistic near the terminus. This suggests a regularized-
- Coulomb friction law (e.g., Joughin et al., 2019) may be appropriate for Thwaites Glacier, as it only accounts for effective 395 pressure where effective pressure is low and basal sliding speeds are high, such as near the grounding line (Schoof, 2005). However, our channel-enabled model indicates effective pressure actually decreases between 5–100 km from the grounding line, and maintains its proportionality to basal shear stress throughout the entire domain (Figure 7b). This implies basal shear stress stays in the Coulomb regime even within the glacier interior, and thus a yield stress or semi-plastic Budd-type law may
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To test this hypothesis we attempt to reconstruct our input basal shear stress using a Budd-style friction law of the form: $\tau_b = CNu_b^{1/m}$, where u_b is a model input, N is solved for by the hydrology model, and C is a tunable basal slipperiness coefficient. Here, m is the bed-dependent stress exponent that is likely between 5–10 for Pine Island Glacier (Gillet-Chaulet et al., 2016; Nias et al., 2018; Joughin et al., 2019), which is assumed to have similar basal properties to Thwaites Glacier.

work equally well for Thwaites Glacier, as has previously been successful at Pine Island Glacier in reproducing observed

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surface velocities (Gillet-Chaulet et al., 2016).





Figure 7b illustrates the results using four plausible values of m and accompanying C values that minimize the root mean square error with the model input. All four versions effectively recover the input basal shear stress, with the best agreement using m = 5 or m = 8, which is consistent with previous work (Gillet-Chaulet et al., 2016; Nias et al., 2018; Joughin et al., 2019). Therefore, we assert that a Budd-style friction law is appropriate for Thwaites Glacier, assuming accurate knowledge of the effective pressure field. Based on these results we caution against the continued usage of the hydrostatic ocean connection

parameterization for effective pressures beyond the marginal 5 km for Thwaites Glacier, which may produce unrealistically

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4.3 Model Considerations

slow sliding velocities.

Our results highlight the need for validation of subglacial hydrology models across the entirety of a glacier. We found a wide range of parameter values resulted in steady-state configurations, and most had some degree of channelization coincident with the location of observed anomalously high sub-ice-shelf melting. However, many simulations had water pressures and discharges that were either too low or too high to be realistic, and without comparison with radar specularity content, it would have been easy to arbitrarily choose the wrong parameters and base our conclusions on an unrealistic model. Borehole validation has been previously attempted for a small alpine glacier (Rada and Schoof, 2018), but the scale of Antarctic and

- 420 Greenland glaciers makes this unattainable for ice sheets. We therefore suggest that ice-penetrating radar, such as used in this paper and in Dow et al. (2020), or other broad-scale proxies for basal water, is the best approach for validation of ice sheet subglacial hydrology models. While our comparison between R_{wt} and specularity content is somewhat *ad hoc*, it selected for a coherent grouping of parameters, water pressures, and channel velocities within the expected realistic range, which gives us confidence in its effectiveness. Comparison criteria may need customization to be applicable at other glaciers, but the overall
- 425 methodology presented in this paper should be beneficial in many settings. Bed conditions differ within and between glacier basins, and we stress our parameter choices should not be extrapolated to other glaciers without validation.

Many assumptions built into subglacial hydrology models remain unsupported, and it is uncertain how such assumptions may influence our results. We therefore deem it necessary to consider the primary underlying simplifications that may impact this paper. Our choice to ignore pressure-dependent melting/freezing in Equation 5 neglects the effects of supercooling, which

- 430 would lead to the abatement of R-channels and the expansion of the distributed system as water flows out of a prominent overdeepening. Supercooling has been shown to decrease channelization in other subglacial hydrology models (de Fleurian et al., 2018). However, the overdeepening within 100 km from the grounding line, in which channelization becomes pronounced, is far from meeting the supercooling threshold of Werder (2016). Furthermore, the upward bed slope in the terminal 100 km is only 60% of the downward surface slope, and should therefore allow for sufficient dissipative heating to continu-
- 435 ally grow channels (Alley et al., 1998). We therefore do not expect the neglect of Π in Equation 5 to significantly affect our conclusions.

Uniform parameterizations of the distributed system do not account for realistic heterogeneity in bed geometry or lithology, both of which can locally influence distributed connectivity (Murray and Clarke, 1995; Gordon et al., 1998; Andrews et al., 2014; Hoffman et al., 2016; Rada and Schoof, 2018; Downs et al., 2018). The bed of Thwaites Glacier is thought to consist





- of alternating regions of bedrock and glacial till (Joughin et al., 2009; Muto et al., 2019a, b; Holschuh et al., 2020) that could 440 potentially affect the connectivity of the distributed system, and thus conductivity and discharge. Currently, all subglacial hydrology models assume a consistent k_q across their domains, although allowing k_q to vary with bed lithology may account for spatial differences in connectivity and produce more realistic results (Hoffman et al., 2016).
- Modeling (Joughin et al., 2009) and seismic data (Muto et al., 2019b, a) suggest bed elevation could serve as a reasonable proxy for bed lithology under Thwaites Glacier, where subglacial till (low conductivity) accumulates in depressions and ex-445 posed bedrock (high conductivity) primarily exists at topographic highs. Regions of high specularity content coincide with low-lying troughs, and it is therefore conceivable that imposing a high k_q above these troughs, and low k_q within them, could reproduce the observed specularity content without the need for channelization. However, our results suggest the minimum k_q necessary to prevent channelization would still be high enough over a majority of the domain to drop water pressures below
- 450 realistic levels. Lowering k_q within troughs, but maintaining the same k_q at higher elevations as used in our data-compatible FSS runs could help pool water into subglacial lakes in till-laden depressions (see Section 4.1), but it seems unlikely this would divert enough water to preclude the overall growth of channels in the terminal 100 km. Furthermore, the location of modeled channelized flow at the grounding line presents a convincing explanation for the anomalously high sub-ice-shelf melt rates observed at the same position, something that would be lacking in a purely distributed system. We acknowledge the neglect of a spatially variable k_q could create some uncertainty in our discharge results, but is likely minimal, and our k_q parameter
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sweep may already account for this variability.

As described in Downs et al. (2018), the value of k_q used in subglacial hydrology models is a proxy for the connectivity of orifices linking cavities in the bed. Models assume the orifices scale with cavity size; however, in their original conception, orifices behave like small R-channels that may enlarge with turbulent melting (Kamb, 1987; Fowler, 1987). Downs et al. (2018) used this argument to scale k_q with meltwater input, which better captured seasonal water pressures. Although Thwaites Glacier lacks a seasonal meltwater cycle, we could use the same argument to justify use of a different distributed system flow law.

Darcy or Darcy-Weisbach flow laws are used almost ubiquitously in subglacial hydrology models (e.g., Schoof, 2010; Hewitt, 2011; Werder et al., 2013; Hewitt, 2013; Hoffman and Price, 2014; Downs et al., 2018; Hoffman et al., 2018; de Fleurian et al., 2018; Dow et al., 2020, and others), yet these laws are largely unvalidated in the subglacial environment. Distributed

- discharge with a Darcy-Weisbach turbulent flow law, as used in this paper, has a $\frac{5}{4}$ power dependency with water thickness. 465 However, in other flow laws, such as Darcy porous media flow or Poiseuille laminar flow, the exponent may vary between 1 and 3 (e.g., Hewitt, 2011, 2013; Kyrke-Smith and Fowler, 2014; Kyrke-Smith et al., 2014). In practice, the use of a higher exponent could produce similar behavior to a melt-dependent k_q , and could account for a larger connectivity with increased meltwater, driven by the dissipative melting and opening of orifices. Although such a flow law would increase efficiency of the
- distributed system and potentially minimize channelization, we do not believe its use would dramatically change our results. 470 Water thicknesses using a Darcy-Weisbach law are fairly uniform within 200 km of the grounding line (Figure 2c), which suggests an increased dependency of discharge on water thickness may make little difference in our model.





5 Conclusions

This paper leverages observations from a variety of sources to select for the subglacial hydrology model scenarios that are the most likely representations of reality. Our range of possible steady-state scenarios highlights the need for thorough parameter sweeps in subglacial hydrology models, which are then winnowed to the most realistic grouping of simulations based on extensive observations. We emphasize validation of subglacial hydrology models within the glacier interior, and not just at its terminus, is necessary to properly constrain realistic drainage behavior. Furthermore, our work demonstrates subglacial hydrology models still produce a range of results that are compatible with data, and thus model results should be reported as a suite of possible scenarios, instead of one feasible configuration.

Our work presents an updated conceptual model for the subglacial drainage system beneath Thwaites Glacier. Our model indicates a few stable channels exist within 200 km of the grounding line, and coalesce into 1-2 large stable channels within the terminal 50–100 km. These channels intersect the ice-ocean boundary directly at the location of highest sub-ice-shelf melt rates, suggesting they play an important role in frontal ablation and grounding line retreat. However, in the interior of the

- 485 glacier, subglacial channels efficiently evacuate water from a broad portion of the bed, thereby increasing basal friction within 100 km of the grounding line and potentially buttressing against further retreat. At this point, it remains unclear how common such drainage systems are in Antarctica, or what impact subglacial channels have on sub-ice-shelf cavity circulation and ice dynamics. We expect the subglacial drainage network to continually reconfigure with future changes in meltwater production and glacier geometry, which will subsequently lead to spatially and temporally evolving basal shear stress and frontal ablation
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influence of subglacial channels on future retreat and mass loss.

Code and data availability. Model output, radar data, processing files, and the MALI model code used to perform the simulations described can be obtained online at https://doi.org/10.5281/zenodo.5593376.

rates. Further work with a fully coupled ice dynamics-subglacial hydrology model will be necessary to determine the exact

Author contributions. AH and MH conceived of the study and designed the simulation plan. AH conducted the model simulations, developed and carried out the analysis, wrote the majority of the manuscript, and created the figures. MH also assisted with analysis and writing of the paper, designed and implemented the MALI subglacial hydrology model, and created the Thwaites model domain. SP established funding for the research, provided experience in ice sheet modeling, and gave extensive guidance throughout the research process. DS contributed his expertise in radar specularity analysis and interpretation, which was critical for comparison with model results. All authors contributed to editing the manuscript and discussing methodology.

500 Competing interests. The authors declare they have no competing interests in the publication of this article.





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