

A generalized photon tracking approach to simulate spectral snow albedo and transmittance using X-ray microtomography and geometric optics

Theodore Letcher¹, Julie Parno¹, Zoe Courville¹, Lauren Farnsworth¹, and Jason Olivier¹

¹US Army Corps of Engineers Cold Regions Research and Engineering Laboratory, Hanover, NH, United States of America

Correspondence: Theodore Letcher (Theodore.W.Letcher@erdc.dren.mil)

Abstract.

A majority of snow radiative transfer models (RTMs) treat snow as a collection of idealized grains rather than an organized ice-air matrix. Here we present a generalized multi-layer photon tracking RTM that simulates light reflectance and transmittance of snow based on X-ray microtomography images, treating snow as a coherent 3D structure rather than a collection of grains. The model uses a blended approach to expand ray tracing techniques applied to sub-1 cm³ snow samples to snowpacks of arbitrary depths. While this framework has many potential applications, this study's effort is focused on simulating reflectance and transmittance in the visible and near-infrared (NIR) through thin snowpacks as this is relevant for surface energy balance and remote sensing applications. We demonstrate that this framework fits well within the context of previous work and capably reproduces many known optical properties of a snow surface, including the dependence of spectral reflectance on snow specific surface area and incident zenith angle as well as the surface Bidirectional Reflectance Distribution Function (BRDF). To evaluate the model, we compare it against reflectance data collected with a spectroradiometer at a field site in east-central Vermont. In this experiment, painted panels were inserted at various depths beneath the snow to emulate thin snow. The model compares remarkably well against the reflectance measured with a spectroradiometer, with an average RMSE of 0.03 in the 400 - 1600 nm range. Sensitivity simulations using this model indicate that snow transmittance is greatest in the visible wavelengths, limiting light penetration to the top 6 cm of the snowpack for fine grain snow but increasing to 12 cm for coarse grain snow. These results suggest that the 5% transmission depth in snow can vary by over 6 cm according to the snow type.

1 Introduction

Due to the highly reflective nature of snow, seasonal snowpacks make the surface significantly more reflective when present, impacting regional weather and climate. Correspondingly, the snow albedo feedback, caused by changes in seasonal snow cover extent and properties, represents one of the more dramatic markers of regional and global climate change (e.g., Hall, 2004; Déry and Brown, 2007; Flanner et al., 2011; Letcher and Minder, 2015; Thackeray and Fletcher, 2016). While snow is highly reflective, snow albedo is not equal for all snowpacks. For instance, snow albedo typically decreases with snow age due to metamorphic processes resulting in larger snow grains (e.g., Wiscombe and Warren, 1980; Aoki et al., 2000; Flanner and

25 Zender, 2006; Adolph et al., 2017). Snow albedo is also diminished by light absorbing impurities such as dust or black carbon that contaminate the snow (Doherty et al., 2010; Painter et al., 2012; Skiles et al., 2012; Dumont et al., 2014; Skiles et al., 2015; Skiles and Painter, 2019; Shi et al., 2021). Importantly, these two effects impact different parts of the electromagnetic spectrum, with grain size having a greater influence in the near-infrared (NIR), and the particle contamination influencing the visible region. Finally, even though thin snow covers are highly reflective, the surface albedo for a thin snow cover can be
30 influenced by the underlying ground surface depending on the snow microstructure (Perovich, 2007; Warren, 2013; Libois et al., 2013). Consequently, the detection of subnivean hazards is highly dependent on the microscopic properties of the overlying snowpack. Understanding these small-scale drivers of snow albedo is important for large-scale remote sensing applications and regional weather and climate modeling.

There are several documented approaches to model snow broadband and spectral albedo using radiative transfer models
35 (RTMs) in efforts to better understand and predict the effects of snow aging and impurities on snow optical properties. While a full review of snow radiative transfer is well beyond the scope of this paper, we refer the reader to He and Flanner (2020) for a rigorous overview of the different approaches. There are also numerous simplified parameterizations for snow albedo of varying complexity designed for implementation in weather and climate models (e.g., Verseghy, 1991; Dickinson, 1993; Gardner and Sharp, 2010; Vionnet et al., 2012; Saito et al., 2019; Bair et al., 2019).

40 At a fundamental level, the scattering of electromagnetic energy incident upon the boundary separating a snow grain and the surrounding air is determined by the different refractive indices for ice and air and the geometry of the interfaces. The absorption of light as it passes through solid ice is well understood and has a strong wavelength dependence (Grenfell and Perovich, 1981; Perovich and Govoni, 1991; Warren and Brandt, 2008). The scattering of visible and NIR light at an air/ice boundary is well described by the geometric optics approximation, where the wavelengths of visible and NIR light are small
45 relative to the size of the typical snow particle (e.g., Kokhanovsky and Zege, 2004). While the physics behind scattering and absorption are well understood within the geometric optics limit, the actual path of a light ray through a snowpack can be extraordinarily convoluted as the ray is constantly intersecting air/ice interfaces with very little absorption.

Seminal studies describing snow albedo modeling (e.g., Warren and Wiscombe, 1980; Wiscombe and Warren, 1980) and most subsequent approaches treat snow grains as independent scatterers, where the scattering properties of an individual grain
50 are not affected by adjacent grains and are independent of the spacing between grains and, thus, snow density. For simplification and computational efficiency, Mie theory is often used to determine the albedo of snow represented as a collection of spherical particles (e.g., Bohren and Beshta, 1979; Wiscombe, 1980). Yet although snow grain size is often most cited as the key driver of snow albedo, grain shape also has an impact, leading to inaccuracies with the spherical assumption (Aoki et al., 2000; Neshyba et al., 2003; Picard et al., 2009; Libois et al., 2013; Dang et al., 2016). Efforts to understand and simulate the impacts
55 of snow particle shape on snow spectral albedo have largely focused on leveraging the geometric optics approximation in various ways. For instance, Yang and Liou (1996) used ray tracing to compute the single scattering properties of idealized hexagonal columns, plates, and rosettes. Grundy et al. (2000) presented a Monte Carlo approach to estimate optical properties of computer-rendered 3D spheres that compared well with Mie theory. Their work was extended to estimate the scattering properties of irregularly shaped crystals.

60 Recently, there have been several efforts to characterize snow as a coherent medium rather than a collection of particles within the context of radiative transfer. For instance, Malinka (2014) combined stereological techniques and geometric optics to obtain the inherent optical properties of a snowpack. An additional study by Xiong et al. (2015) focused on determining the optical properties of an idealized mixed snow/air medium generated from a randomized bicontinuous 2D representation of the snow. X-ray microtomography (hereby: μ CT) is a powerful tool that has been used in many of these medium-based efforts. μ CT
65 has been used to support numerous snow radiative transfer methods including individual particle scattering, ray tracing, and analytical approaches (Haussener et al., 2012; Kaempfer et al., 2007; Malinka, 2014; Ishimoto et al., 2018; Xiong et al., 2015; Dumont et al., 2021). Collectively, RTM-focused studies of snow have greatly expanded the knowledge surrounding the optical properties of irregular snow grains and informed the role of snow microstructure on spectral reflectance and transmittance.

In this study, we build upon the approaches of Grundy et al. (2000), Kaempfer et al. (2007), Jacques (2010), and Randrianal-
70 isoa and Baillis (2010) to develop a Monte Carlo photon tracking snow RTM that focuses on representing snow as coherent 3D structure rather than a collection of particles. This framework employs ray tracing to simulate photon tracks through 3D renderings of snow samples measured using μ CT and is designed for broad applications, including studying the effects of snow type and snow depth on snow spectral albedo and transmittance in the visible and NIR. In section 2, we describe the model framework and μ CT data processing. In section 3, we demonstrate the model's capability to reproduce known optical
75 properties of snow, compare model output to spectral albedo measurements of objects buried beneath snow at various depths, and use the RTM to investigate snow transmittance. In sections 4 and 5, we present a broad discussion and conclusions.

2 Data and Methods

The RTM framework used here is divided into two distinct components. The first determines key snow optical properties by firing photons into 3D closed-surface renderings of snow samples derived from μ CT scans. The second is a 1D plane-parallel
80 photon tracking model that uses the optical properties derived from the first part. Both model components use the ice refractive indices reported by Warren and Brandt (2008) to compute scattering and absorption. Additionally, both models are Monte Carlo models that rely on a large number of sample rays to generate robust results. While computationally expensive, there are several advantages to the Monte Carlo approach. In particular, Monte Carlo models are useful for modeling single scattering properties of non-spherical particles and for 3D radiative transfer applications (e.g., Iwabuchi, 2006; Whitney, 2011). Additionally, this
85 approach lends itself well to parallelization.

One critical simplification we make in determining the optical properties of a given snow sample is that we ignore the wave properties of light, such as phase and diffraction, which limits its overall applicability and reduces accuracy. However, this simplification has been used successfully in numerous previous studies (e.g., Kaempfer et al., 2007; Haussener et al., 2012; Malinka, 2014; Xiong et al., 2015) and, because the diffraction pattern is strongly forward scattering (Xiong et al., 2015),
90 we anticipate that this simplification is appropriate here. Some work has been done incorporating diffraction into geometric optics scattering for non-spherical particles (Yang and Liou, 1996; Liou et al., 2011), but because this framework treats snow as a two-phase medium rather than a collection of particles, accounting for diffraction is less straightforward. Accordingly,

we acknowledge that diffraction may be more important for the longer NIR wavelengths, and should be a potential focus of future work. We also assume independent scattering which is a common assumption made in the geometric optics limit (e.g., Randrianalisoa and Baillis, 2010; Haussener et al., 2012; Xiong et al., 2015). This simplification neglects the effect of interference and is a reasonably good assumption for visible light. However, it likely reduces accuracy in the NIR, especially for densely packed particles.

2.1 Snow Optical Properties

The plane-parallel model requires four key optical properties: the extinction coefficient γ_{ext} [mm^{-1}], the ice path fraction F_{ice} , the absorption enhancement parameter B , and the scattering phase function $p(\cos \Theta)$. To obtain these parameters, we apply the photon tracking methods described in Kaempfer et al. (2007). In this framework, photons are initialized at a random position somewhere along the edge of a snow sample mesh and launched in a random direction into the sample. The photons then travel through the mesh, with their tracks determined according to fundamental geometric optics for unpolarized (natural) light, until they eventually exit the medium or are absorbed. Note that each intersection is assumed to occur on a flat infinite plane with a normal vector oriented towards the air phase. We assume a constant (i.e., wavelength independent) real index of refraction of 1.30.

As photons travel through the snow medium, they change direction according to Snell's law of refraction and a probabilistic representation of Fresnel's law of reflectance. Fresnel's law dictates that the fractional reflection and transmission of light at a boundary is related to the incident angle θ_i and the refractive indices n of the two media separated by the boundary:

$$R_{\text{h}} = \frac{n_1 \cos \theta_i - n_2 \sqrt{1 - \left(\frac{n_1}{n_2} \sin \theta_i\right)^2}}{n_1 \cos \theta_i + n_2 \sqrt{1 - \left(\frac{n_1}{n_2} \sin \theta_i\right)^2}}, \quad (1)$$

and

$$R_{\text{v}} = \frac{n_1 \sqrt{1 - \left(\frac{n_1}{n_2} \sin \theta_i\right)^2} - n_2 \cos \theta_i}{n_1 \sqrt{1 - \left(\frac{n_1}{n_2} \sin \theta_i\right)^2} + n_2 \cos \theta_i}, \quad (2)$$

where R_{h} and R_{v} are the horizontally and vertically polarized reflectances. Assuming that the radiation is unpolarized, the reflectance R is:

$$R = \frac{1}{2}(R_{\text{h}}^2 + R_{\text{v}}^2). \quad (3)$$

Through energy conservation, the transmittance T is:

$$T = 1 - R. \quad (4)$$

Then, if the vector normal to the boundary plane \hat{v}_n is oriented towards the medium with refractive index n_1 , the direction unit vectors for reflected and transmitted radiation are computed as \hat{v}_r and \hat{v}_t :

$$120 \quad \hat{v}_r = \hat{v}_i + 2 \cos \theta_i \hat{v}_n \quad (5)$$

and

$$\hat{v}_t = \frac{n_1}{n_2} \hat{v}_i + \left(\frac{n_1}{n_2} \cos \theta_i - \cos \theta_t \right) \hat{v}_n. \quad (6)$$

Once the photon has exited the mesh, characteristics of the photon track are used to extract the optical properties of the medium.

Since snow is weakly absorbing, here we assume that $\gamma_{\text{ext}} \approx \gamma_{\text{sca}}$ where γ_{sca} is the scattering coefficient and is inversely
 125 proportional to the distance traveled between scattering events that occur at air/ice boundaries in the snowpack. Accordingly, we calculate it by computing the mean distance traveled between scattering events along a given photon path averaged over all photons (e.g., Randrianalisoa and Baillis, 2010):

$$\gamma_{\text{sca}} = \frac{1}{\frac{1}{N} \sum_{i=1}^N \bar{d}_i}, \quad (7)$$

where N is the total number of photons used in the model and \bar{d}_i is the average distance between scattering events along
 130 photon track i . It is important to note that scattering events are defined at the outward facing side of the mesh surface such that scattering events only occur when either a photon incident on a particle is reflected at the particle surface, or when a photon traveling within the ice phase is transmitted through the ice/air boundary into the air phase. That is, internal reflections are not considered discrete scattering events (Randrianalisoa and Baillis, 2010).

The mean ice path fraction F_{ice} for a given photon track is the ratio of the distance traveled within ice and the total distance
 135 traveled throughout the medium. Here, F_{ice} for a given snow sample is taken as the average F_{ice} over all photon tracks.

The absorption enhancement parameter B quantifies the absorption path length extension due to internal reflections within a snow particle and can be quantified by the ratio of the actual internal photon path-length through a sample medium and the internal path-length following a straight line (Libois et al., 2019). In this framework, B is computed by taking the ratio of F_{ice} following photon tracks and F_{ice} following a straight path through the sample:

$$140 \quad B = \frac{\overline{F_{\text{ice}}}}{F_{\text{ice, straight}}}. \quad (8)$$

In essence, this ratio compares the internal path length of a photon track that allows for internal reflections to a path that does not.

The scattering phase function is obtained by aggregating scattering angles associated with all scattering events. Scattering events are defined to be consistent with the computation of γ_{sca} in that internal reflections are not considered discrete scattering events.

To determine the phase function for the medium, scattering angles are first divided into a prescribed number of finite bins, each with width $d\Theta$. Then, for a given photon track, scattering angles are computed as follows:

1. When the photon track within the air phase of the medium is incident on the mesh surface, the incident angle ($\hat{\Omega}'$) is saved and an initial energy value ($W=1$) is assigned to the ray entering the ice phase of the mesh.
2. At the incident intersection (i_0), the scattering angle of the incident ray and the reflected ray is computed as the dot product of the incident angle and the angle of the reflected ray determined by Eq. (5):

$$\cos \Theta = \hat{\Omega}' \cdot \hat{\Omega}. \quad (9)$$

3. The ray then continues along its track through the medium, and at each boundary intersection, the reflection and transmission are calculated following Eqs. (1-4).
4. At each subsequent intersection within the ice phase ($i_{1...n_i}$), the scattering angle between the incident ray and the transmitted ray is computed from Eq. (9).
5. Then the computed scattering angle is added to the appropriate bin (j) and is weighted by the total remaining energy (W) multiplied by either R at i_0 or T otherwise.
6. The energy of the internal ray decreases at each intersection as it is scattered away from the particle such that the weight applied to the scattering angles (W) is expressed as:

$$W_i = \begin{cases} R_0 & i = 0 \\ T_0 T_i & i = 1 \\ T_0 \left(\prod_{n=1}^{i-1} R_n \right) T_i & i > 1 \end{cases}. \quad (10)$$

Note, that Eq. (10) does not account for the absorption of energy within the particle.

Most rays exit the ice phase of the mesh after 1 to 3 internal reflections, however we continue to track the internal ray until W is less than 0.01 to generate a more complete phase function. Once W has been depleted, the model continues tracking the original photon through the mesh. This process is illustrated schematically in Fig. 1.

At the end of the ray tracing model, the resulting distribution of energy, integrated over all photon tracks, is converted to a phase function defined relative to the total energy initially incident on the air/ice boundaries (Grundy et al., 2000):

$$p(\cos \Theta_j) = \frac{4\pi N_j}{N \sin \Theta_j d\Theta}, \quad (11)$$

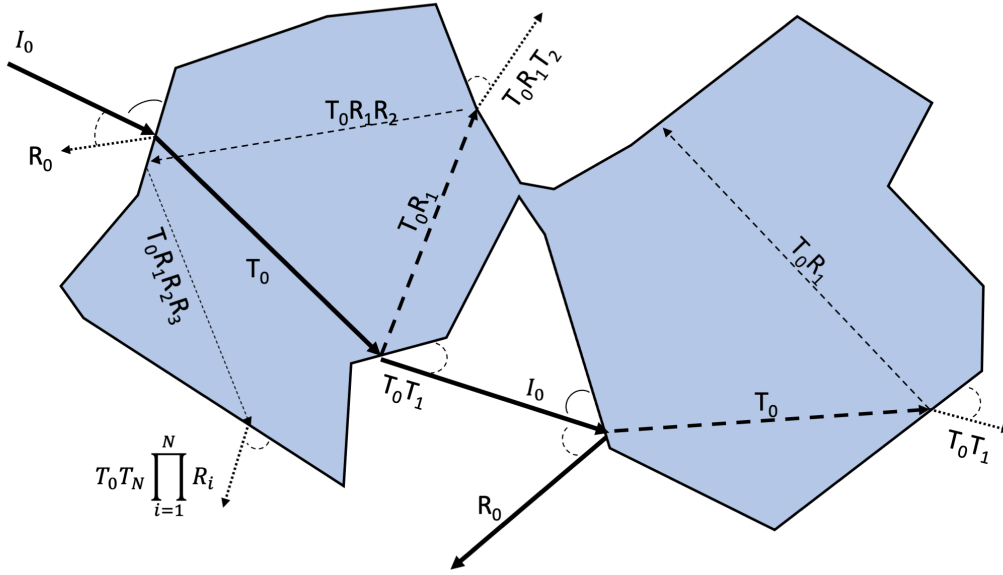


Figure 1. Schematic illustrating the scattering phase function. The thick solid lines represent the actual photon track through the medium. Dashed lines within the ice phase represent the extended internal rays that are followed until 99% of the energy incident upon the mesh surface is scattered. Scattered rays following the extended ray path are indicated by the dotted lines within the air phase and are annotated with their respective weights (W).

where N is the total photon energy and N_j is the total photon energy directed into bin j . In this study, the number of
 170 bins used to represent the phase function is 180. Accordingly, $d\Theta = 1^\circ$. To illustrate this component of the model, the optical properties for an example snow mesh are shown in Fig. 2.

2.2 1D plane-parallel photon tracking model

Once the optical properties of the snow sample are determined by launching photons through μ CT sample volumes, the plane-parallel model is used to simulate snow spectral albedo, transmittance, and Bidirectional Reflectance Distribution Function
 175 (BRDF). The plane-parallel model is used in place of a brute-force application of the explicit photon tracking model described by Kaempfer et al. (2007) in order to allow for the computationally feasible simulation of spectral albedo and transmittance for snow covers with depths exceeding 1 cm with sufficient grain resolution. Additionally, it is used to avoid complications associated with lateral boundary treatment and stitching multiple μ CT scans together into a single coherent snow lattice.

The model used here is largely based on the framework presented in Jacques (2010) and is similar to the model described
 180 in Picard et al. (2016), which track individual photon packets as they follow unique paths through the specified media. Here, discrete snow layers with optical properties constant throughout each layer are first prescribed. Then initial photon vector positions (\mathbf{X}_0) with cartesian components of (x_0, y_0, z_0) are specified with random x and y coordinates, and z coordinates

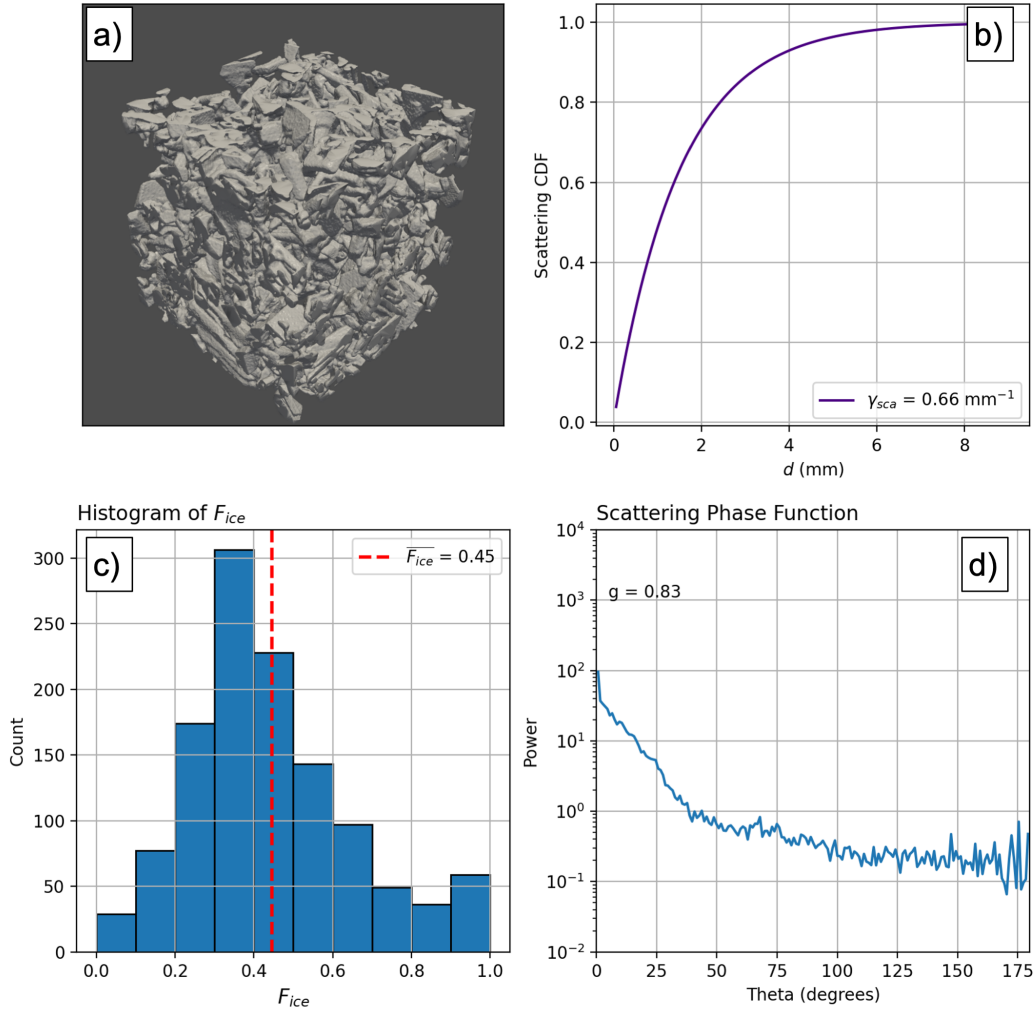


Figure 2. (a) 3D rendering of the snow sample used to generate the optical properties. (b) Cumulative distribution function of scattering as a function of distance (mm) and γ_{sca} . (c) Histogram of F_{ice} . The red dashed line indicates the mean value. (d) Scattering phase function. 1200 individual photon tracks were used to generate the optical properties shown in this figure. The asymmetry parameter (g) is the average of the geometric asymmetry parameter computed from the phase function as $g_G = \frac{1}{2} \int p(\cos\Theta) \cos\Theta \sin\Theta d\Theta$ and the diffraction asymmetry parameter $g_D \simeq 1$ according to Kokhanovsky and Zege (2004) and Libois et al. (2013).

equal to the snow surface height. Each photon packet is given an initial energy of unity ($E = 1$) and an initial direction vector (\mathbf{V}_0):

$$185 \quad \mathbf{V}_0 = [\sin\theta \cos\phi, \sin\theta \sin\phi, -\cos\theta], \quad (12)$$

where θ is the solar zenith angle, and ϕ is the azimuth angle clockwise from x . The initial direction can be prescribed as downward pointing with uniformly random zenith and azimuth angles representing isotropic diffuse radiation, or at any specified zenith/azimuth angle (i.e., direct radiation), or as a mixture of both diffuse and direct radiation.

For a given photon, once the position is set, the photon is launched into the medium, and travels a distance s before experiencing a scattering event. s is computed statistically using the Beer-Lambert law and the medium scattering coefficient (Jacques, 2010):

$$s = -\frac{\ln \zeta}{\gamma_{\text{sca}}}, \quad (13)$$

where ζ is a random uniform number between 0 and 1. The new position in the medium is:

$$\mathbf{X} = \mathbf{X}_0 + s\mathbf{V}_0 \quad (14)$$

At the scattering event, the photon packet is given a new direction unit vector according to the scattering phase function. Because this framework treats the scattering phase function as a probability distribution function (PDF), the scattering angle Θ is determined by choosing a random sample from $p(\cos \Theta)$ PDF:

$$P(\cos \Theta) = \frac{p(\cos \Theta)d\Omega}{4\pi}, \quad (15)$$

where P is the probability of light being scattered into a cone with solid angle $d\Omega$ in the direction Θ from the incident radiation given the phase function.

Then the new direction vector is determined from Θ (Jacques, 2010):

$$\begin{aligned} \mu_x &= \frac{\sin \Theta (\mu_{x_0} \mu_{z_0} \cos \phi - \mu_{y_0} \sin \phi)}{\sqrt{1 - \mu_{z_0}^2}} + \mu_{x_0} \cos \Theta \\ \mu_y &= \frac{\sin \Theta (\mu_{y_0} \mu_{z_0} \cos \phi - \mu_{x_0} \sin \phi)}{\sqrt{1 - \mu_{z_0}^2}} + \mu_{y_0} \cos \Theta, \\ \mu_z &= -\sqrt{1 - \mu_{z_0}^2} \sin \Theta \cos \phi + \mu_{z_0} \cos \Theta \end{aligned} \quad (16)$$

where ϕ is given as a uniform random number between 0 and 2π , the 0 subscript represents the incident direction, and μ_x , μ_y , and μ_z make up the components of the unit direction vector.

Photon energy is depleted over distance s according to the ice absorption coefficient and F_{ice} as determined from the μCT data instead of using a medium absorption coefficient:

$$E = E_0 \left(e^{-\kappa_\lambda s F_{\text{ice}} \eta} \right), \quad (17)$$

where E is the new photon energy, and E_0 is the incident photon energy, and κ_λ is the wavelength dependent absorption coefficient of ice based on the imaginary part of the refractive index k :

$$\kappa_\lambda = \frac{4\pi k}{\lambda}. \quad (18)$$

The parameter η is a non-dimensional scaling parameter that relates F_{ice} , B , and ρ_s to absorption following expressions given in Libois et al. (2013, 2019):

$$\eta = \left(1 - \frac{(B-1)\rho_s}{\rho_{\text{ice}}}\right). \quad (19)$$

where ρ_s is density of the snow sample. η is typically within 10% of unity for a majority of snow samples, but can enhance absorption by as more than 25% in snow with $\rho_s > 350 \text{ kg m}^{-3}$ and $B > 1.7$.

To achieve statistical energy conservation, a "Russian Roulette" function is used to determine whether or not to fully absorb (i.e., kill) the photon packet once its energy falls below a prescribed threshold (Iwabuchi, 2006; Jacques, 2010). This is given as:

$$E = \begin{cases} mE & \zeta \leq 1/m \\ 0 & \zeta > 1/m \end{cases}, \quad (20)$$

where ζ is a random number between 0 and 1, and m is a prescribed constant on the order of 1-10. In essence, the Russian Roulette technique achieves energy conservation by proportionally compensating for the energy removed from the model when photons are killed. By treating absorption continuously rather than probabilistically, the number of photons required to attain a robust solution is significantly reduced, and further ensures reliable model integration.

If the z position of a photon packet with an upward trajectory is above the top of the snow surface (i.e., it has exited the top of the snowpack), the remaining energy within the packet is added to the total reflected energy and the photon is eliminated. In an open lower-boundary configuration, if a photon packet z position is less than 0 (i.e., it has exited the bottom of the snowpack) the remaining energy is added to the total transmitted energy, and the photon is eliminated. Alternatively, a lower boundary can be simulated with a specified spectral reflectance such that a portion of the photon energy will be absorbed at the lower boundary, and the remaining energy will be reflected upward. Once all photons have been eliminated from the model, the simulation is complete.

This model is extended to a multilayer configuration by simply defining unique optical properties corresponding to specified depths throughout the snowpack. When a photon packet travels from one layer to another, its trajectory and energy depletion are determined by the optical properties of the new layer. To illustrate this, two photon tracks are plotted on a 2D plane as they travel throughout an idealized two-layer 20 cm deep snowpack (Fig. 3).

2.3 Directional Conic Reflectance Function

The reflectance of a surface is often described using the concept of a BRDF (e.g., Stamnes and Stamnes, 2016). The BRDF represents the directional PDF of reflectance for a ray of light impacting the surface from a specified incident direction. To estimate the BRDF from this model, we follow the method described in Kaempfer et al. (2007), which approximates the BRDF using the Directional Conic Reflectance Function (DCRF). The DCRF is a discretized BRDF that computes the energy reflected into a cone in the direction: θ_r, ϕ_r subtended by solid angle $d\Omega$:

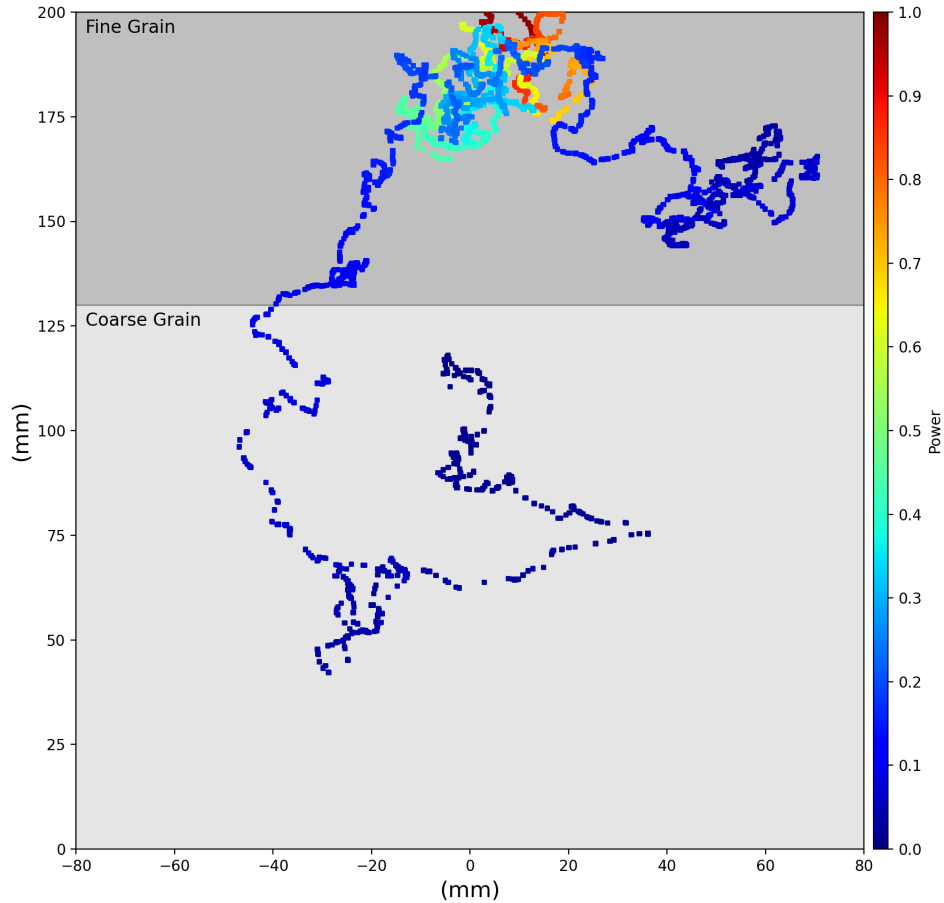


Figure 3. x/z cross section of two photons within a multi-layered snowpack 20 cm deep. The color scale indicates the fractional energy of the photon packet. The background shading indicates the layers of the snowpack.

$$DCRF(\theta_i, \phi_i, \theta_r, \phi_r) = \frac{I_r(\theta_r, \phi_r)}{I_i(\theta_i, \phi_i) \cos \theta_i d\Omega}, \quad (21)$$

where I is the radiative flux, and the subscripts i , and r correspond to the incident and reflected radiation, respectively.

2.4 Snow sampling and spectroradiometer measurements in the field

To evaluate the model, we collected snow samples and spectral reflectance measurements of the snow surface at Union Village Dam (UVD) in Thetford, Vermont several times throughout the 2020-21 winter. The UVD site is a broad flat clearing surrounded by deciduous forests spanning approximately 40000 m², and bounded on the southern end by the Ompompanoosuc River. During each data collection, a snow pit was excavated and standard snow characteristics, such as snow depth, density,

and grain size were measured manually. Several snow samples were carefully extracted at several depths spanning the height of the snow cover in columns adjacent to the snow pit sidewalls in cylindrical containers 7 cm high x 1.9 cm in diameter, with a 1-2 cm overlap in the depth of each sample. Three replicate samples, spaced laterally < 10 cm from one another, at each depth were collected. The specific samples used in this analysis were taken from the surface, 0-7 cm, in the case of the fine grain sample, and from 14-19 cm depth in the case of the coarse grain sample. These samples were transported in a hard, plastic cooler for 10 miles from the UVD site to the Cold Regions Research and Engineering Laboratory (CRREL). The fine grain sample was imaged 18 days after snow sampling, while the coarse grain sample was imaged 53 days after snow sampling. All samples were stored at -30 °C to limit metamorphic change in the intervening timeframe. These samples were not casted (i.e. not preserved using a pore-filler).

Spectral reflectance data were collected using a Malvern Panalytical ASD FieldSpec 4 Hi-Res: High Resolution Spectroradiometer. The FieldSpec 4 has a spectral range of 350-2500 nm and a spectral resolution of 3 nm in the visible and 10 nm in the SWIR. The data collection was performed within 1.5 hours of solar noon in order to limit high zenith angle impacts. The FieldSpec 4 requires optimization, which adjusts and improves the detector sensitivities for the probe and light source currently in use. An optimization was conducted prior to the start of data collection and any time lighting conditions changed in order to ensure accurate reflectance readings. Data collections were taken 2.5 to 3 feet above the snow surface at nadir using a 5 degree field of view optic lens, resulting in a measurement footprint diameter of approximately 6 cm. The collection strategy employed included taking a white reference reading from a pure reflective panel and five readings at different locations on the target surface; the mean of the five readings was used as the reflectance value for that specific location.

In this paper, we focus specifically on data collected on 12 February 2021 as this day had the most stable ambient lighting conditions and resulted in the majority of our snow and reflectance measurements. At the time of the measurements, the sky was covered with a high, optically thick overcast, and as a result the ambient lighting conditions were generally diffuse. The snow was dry and approximately 34 cm deep, and was roughly characterized as a layer of relatively fresh snow approximately 10 cm deep overlying a layer comprised of larger mixed refrozen snow grain clusters and facets, separated by a 1 cm thick ice crust. We performed an initial evaluation of the model against measurements to focus on the effect of shallow snow on the spectral albedo.

To measure the effects of a shallow snowpack, a 16"x16" aluminum panel painted black was inserted horizontally into the snowpack through the snow pit sidewall at three depths (10 cm, 4.5 cm, and 2.5 cm) with care as not to damage the smooth snow surface (Fig. 4). This panel was strongly absorptive in the visible and NIR spectrum with a constant reflectance of approximately 4 % throughout the entire 350 - 2500 nm range. Since there was no appreciable difference between the measured spectral albedo of the virgin snow (i.e., no inserted panel) and the panel inserted at 10 cm, we limit our analysis to the 4.5 and 2.5 cm panel depths.

2.5 μ CT sampling and Mesh Generation

The snow samples were characterized at the microscale with a cold-hardened Bruker Skyscan 1173 μ CT scanner housed in a -10 °C cold room equipped with a Hamamatsu 130/300 tungsten X-ray source, which produces a fixed conical, polychromatic



Figure 4. Photograph of the black aluminum panel inserted into the snow pit sidewall approximately 2.5 cm from the surface.

beam with a spot size of $<5 \mu\text{m}$ and a flat panel sensor camera detector. Each sample was scanned with 38 kV X-rays at 196 mA and a nominal resolution of approximately $20 \mu\text{m}$ as the sample was rotated 180° in 0.6° steps with an exposure time of 300-350 ms. Based on estimates of the minimum grain size from manual field measurements, the resolution of the μCT , at $20 \mu\text{m}$, is roughly on the order of one tenth the linear size of the minimum grain size we were imaging. We used the commonly employed Nyquist sampling criterion, which requires a minimum of 2.3 pixels per linear feature, to determine that the resolution was sufficient for the grain sizes we sampled. X-rays were detected using a 5 Mp (2240 x 2240) flat panel sensor utilizing 2 x 2 binning, and projection radiographs were averaged over four frames. The resulting 1120 x 1120 pixel radiographs were then reconstructed into 2D gray-scale horizontal slices using NRecon software (Bruker), which utilizes a modified Feldkamp cone-beam algorithm to produce a vertical stack of gray-scale cross-section images. Image reconstruction processing included sample-specific post alignment, Gaussian smoothing using a kernel size of 2 to reduce noise, sample-specific ring artifact correction of dead pixels, beam hardening correction, and X-ray source thermal drift correction. A cylindrical volume of

interest with a diameter of 1.6 cm was selected from the scanned samples in order to eliminate edge effects caused by the sampling process.

295 Resulting grayscale images are segmented into two phases: air (lowest X-ray absorption), and snow (highest X-ray absorption). Segmenting thresholds for each phase are determined by finding the local minimum between peaks on the histogram showing all grayscale values, and using that value as a global threshold for each scanned sample. The resulting binarized data are despeckled so that any objects less than 2 pixels in diameter were removed.

The final binarized images are then used to construct 3D representations of dry snow samples for input into the RTM. This
300 is accomplished through the use of open-source image processing and 3D visualization software packages accessed through Python (Schroeder et al., 2004; Van der Walt et al., 2014; Sullivan and Kaszynski, 2019).

To build a full sample mesh, a contour-based surface reconstruction process was developed to generate snow surfaces from the voxels that make up the snow sample. This method uses a subset of the binary sample array, including both snow and adjacent air voxels. The subset array is then refined to increase the resolution. A Gaussian filter is applied to smooth the refined
305 array, diminishing the pixelated appearance of the voxelized snow-air interface, producing a smooth level set from which to extract the snow surface. The smoothed level set is then used to define an isosurface at the snow-air boundary, providing control over where the boundary is drawn with respect to the voxels.

Finally, to extract the isosurface from the 3D voxel array, we apply the Marching Cubes method. This algorithm iterates through defined cubes (i.e. voxels) and determines, through knowledge of the pixel values at the cube vertices, if the isosurface
310 intersects that cube. If so, it creates triangular patches via a lookup table that are eventually connected to form the isosurface boundary. The original algorithm presented by Lorensen and Cline (1987) can lead to cracks and over the years has been improved by many (Nielson and Hamann, 1991; Scopigno, 1994; Natarajan, 1994; Chernyaev, 1995; Lewiner et al., 2003). For this work, we used the adaptation implemented by Lewiner et al. (2003), which improved the algorithm to resolve face and internal ambiguities, extended the lookup table, and guaranteed correct topology. As a final step, each grain is “repaired”
315 to remove any defects and degenerate elements and ensure a manifold surface according to Attene (2010), and then decimated to reduce the overall number of triangles that comprise the surface thereby lowering the computational requirements. Overall, this method appears to accurately characterize the snow within the μ CT sample with computed mesh snow sample densities within 1.5% of snow densities computed from the raw voxels. Figure 5 shows a 2D cross section comparing air/ice boundaries to the raw pixels of the image and selected example 3D rendered μ CT samples are shown in Figure 6.

320 3 Results

3.1 General Evaluation

An initial evaluation of the model is performed by simulating the spectral albedo for two idealized 60 cm deep snowpacks with uniform optical properties throughout. For these snowpacks, the optical properties are determined from 3D meshes generated by two characteristically distinct μ CT samples. One mesh is representative of fresh, fine-grained snow near the surface, and
325 the other of large facets near the bottom of the snowpack (Fig. 7). For each mesh, the total mesh volume is approximately

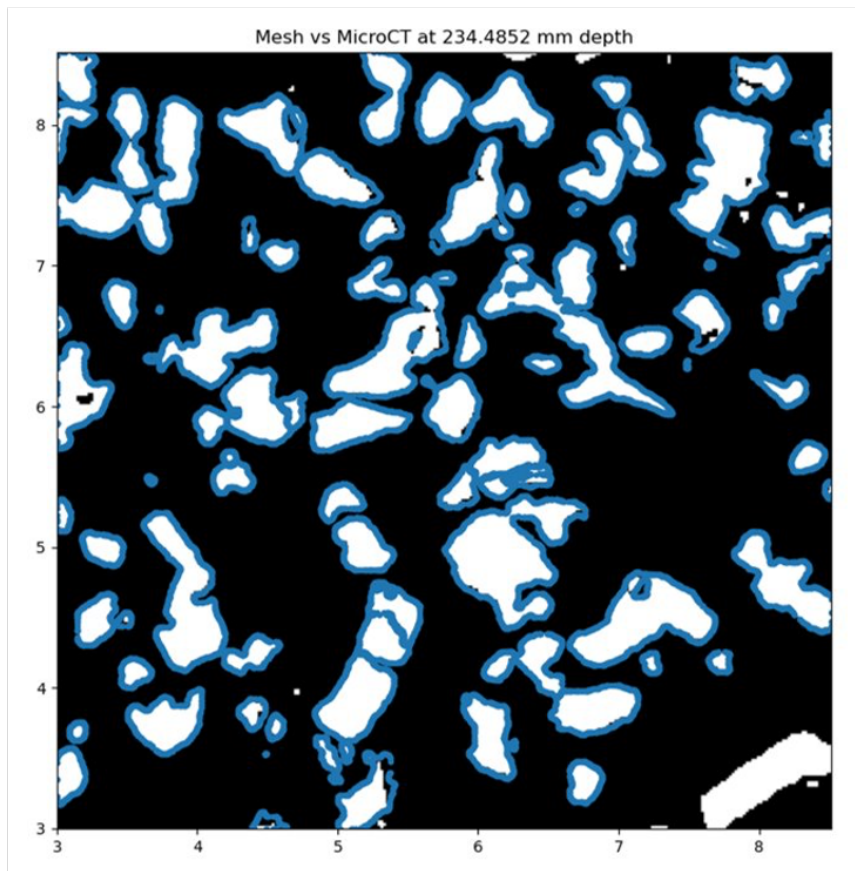


Figure 5. 2D Cross-sectional slice of a binarized μ CT scan with corresponding mesh boundaries superimposed shown as the blue lines.

800 mm³. Additional physical and optical properties of each mesh are presented in Table 1. For each sample, the spectral albedo is computed for wavelengths between 400-1600 nm at 20 nm intervals with diffuse incident radiation. This comparison demonstrates that the model capably reproduces a known behavior of spectral albedo, namely the strong sensitivity of NIR albedo to snow microstructure (Fig. 8). The spectral albedo is relatively uniform between the two snowpacks for the spectral range between 400 and 800 nm, and then the albedos diverge, with a more rapid decrease in albedo for the coarse grain snow.

We then assess the dependence of simulated spectral albedo on incident zenith angle for the fine grain snow sample at four different wavelengths to evaluate the model's ability to simulate anisotropy in the surface reflectance (Fig. 9). This analysis shows an increase in albedo at high zenith angles that is most pronounced in the NIR that represents the functional dependence between albedo and $\cos(\theta)$. This result is broadly consistent with results from previous studies that compare snow albedo and zenith angle (e.g., Li and Zhou, 2003; Kokhanovsky and Zege, 2004; Xiong et al., 2015). As a related evaluation, the model-simulated DCRF is computed as a function of zenith angle (Fig. 10). This analysis reveals that the reflectance is mostly isotropic for zenith angles less than approximately 55° at which point the surface becomes increasingly forward scattering,

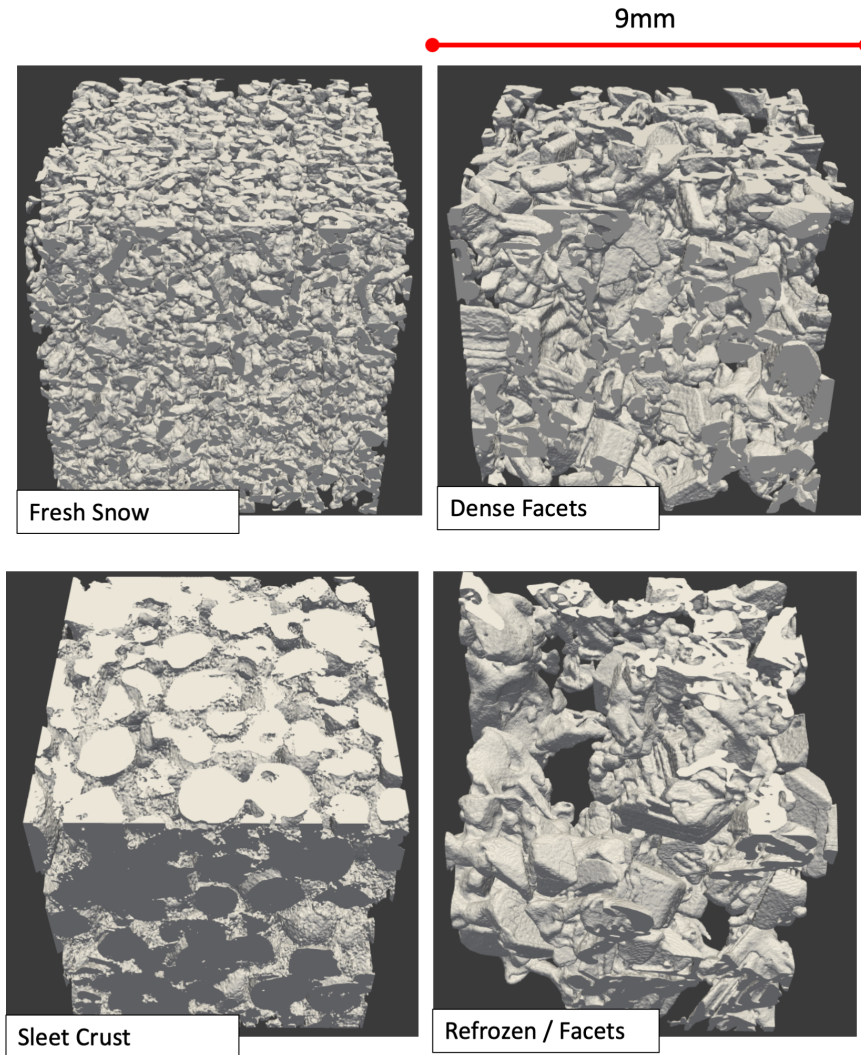


Figure 6. Example 3D renderings of selected μ CT samples representing different types of snow grains.

consistent with previous observational and modeling studies (Aoki et al., 2000; Hudson et al., 2006; Kaempfer et al., 2007; Dumont et al., 2010; Xiong et al., 2015; Jiao et al., 2019).

340 Finally, we use the model to provide an initial assessment of the impacts of snow microstructure on simulated spectral transmittance at specified depths within a homogenous snowpack. To accomplish this, the optical properties of the μ CT samples in Fig. 7 are used to simulate and compare the spectral transmittance at varying depths (Fig. 11). The transmittance is highest at the short, non-absorptive, wavelengths and gradually decreases throughout the NIR, broadly matching quantitative snow transmittance results reported in Perovich (2007) and Libois et al. (2013). The depth of the 5% transmittance contour for the

345 fine grain snow sample is approximately 6 cm for the visible, and decreases to approximately 2 cm for the NIR (Fig. 11a),

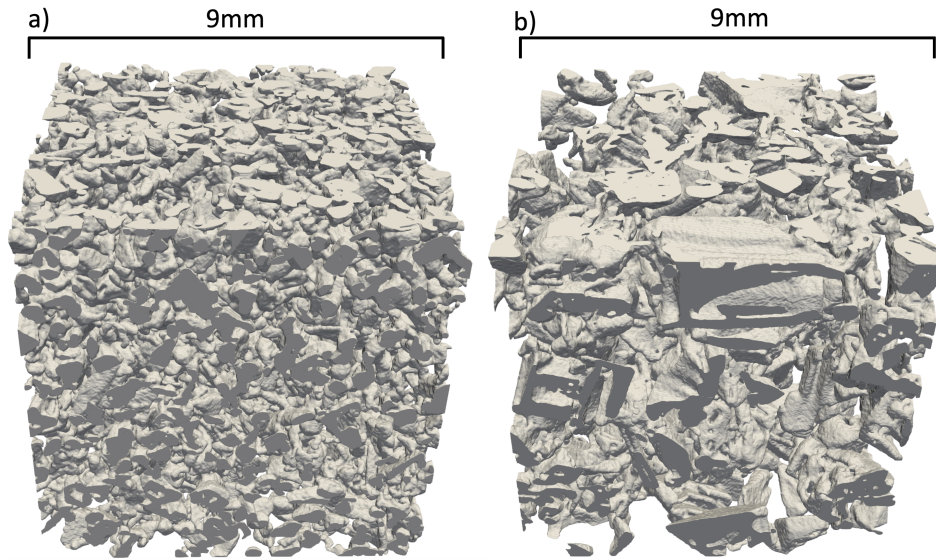


Figure 7. 3D renderings of mesh samples used to generate the optical properties for the general evaluation and snow transmittance comparisons. a) Fine grain sample, and b) Coarse grain sample.

Table 1. Physical and optical properties of the fine grain and coarse grain mesh samples. Note that SSA and ρ_s are computed directly from the μ CT sample. The geometric (g_G) and total asymmetry parameters (g) are computed as described in Fig. 2.

Property	Fine Grain	Coarse Grain
SSA ($\text{m}^2 \text{kg}^{-1}$)	18.4	12.9
ρ_s (kg m^{-3})	287.0	232.4
γ_{sca} (mm^{-1})	1.10	0.65
F_{ice}	0.48	0.44
B	1.52	1.60
g_G	0.64	0.66
g	0.82	0.83

indicating that the fine grain snow penetration length is on the order of only a few centimeters. In contrast, the transmittance for the coarse grain snow is greater near the surface, and the depth of the 5 % contour correspondingly increases to 12.5 cm for the visible and 5 cm for the NIR (Fig. 9b).

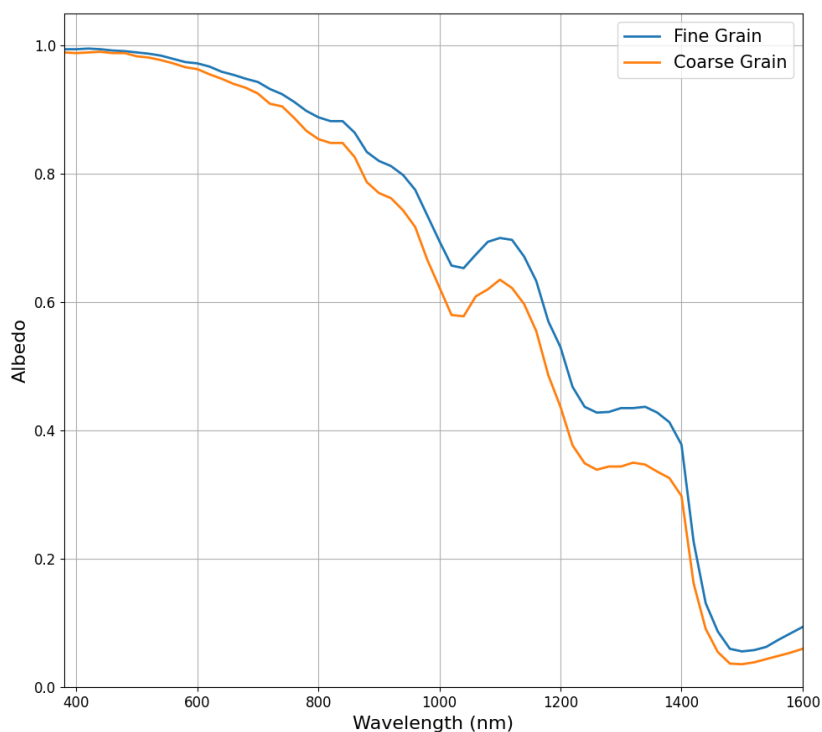


Figure 8. Simulated spectral albedo for fine grain and coarse grain snow samples for 100% diffuse radiation. Note these simulations were run with 25000 photons for a snow depth of 60 cm.

3.2 Evaluation against UVD Data

350 To evaluate the model’s ability to simulate the effect of the underlying surface on snow spectral albedo for shallow snow, optical properties used in the plane-parallel model were determined from four approximately 800 mm³ μ CT samples, with each sample representing a 2 cm thick layer within the top 8 cm of the snowpack. The RTM is then configured with 4 layers according to these optical properties (given in Table 2). The top three layers are each 2 cm thick, and the bottom layer is 28 cm thick, such that the entire snow depth amounted to 34 cm. We chose this configuration in accordance with the hypothesis
 355 that the snow microstructure below 8 cm had little impact on the measured surface spectral albedo. To simulate the panels, the snowpack depth is modified to be 4.5 and 2.5 cm deep with a lower boundary consistent with the spectral reflectivity of the black panel (Table 2).

There is generally good agreement between the observations and the model (Fig. 12) and in particular, the model accurately simulates the impact of the inserted panel on the surface albedo for wavelengths shorter than 1000 nm for both the 4.5 and
 360 2.5 cm depths. The model spectral albedo decreases more rapidly than the observations with wavelength in the 800 - 1000 nm region, particularly for the virgin snow sample. This leads to a slight underestimate in albedo in the NIR range for wave-

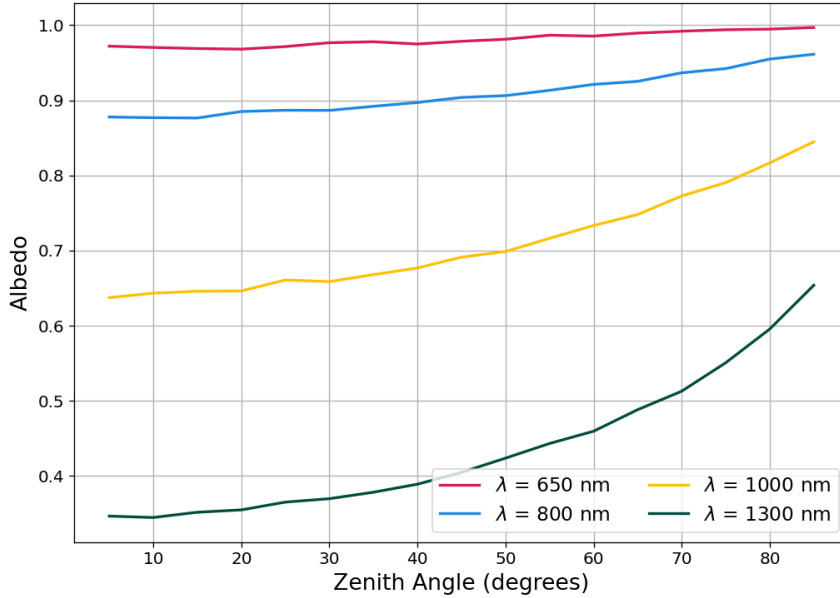


Figure 9. Simulated spectral albedo as a function of incident zenith angle for selected wavelengths. Note these simulations were run with 25000 photons for a snow depth of 60 cm.

Table 2. Physical and simulated optical properties of the top 8 cm of snow measured at the UVD site on 12 February 2021. SSA and ρ_s are computed directly from the μ CT sample. Note that the depths correspond to the RTM model depths for the virgin snow calculation. The geometric (g_G) and total asymmetry parameters (g) are computed as described in Fig. 2

depth [cm]	SSA ($\text{m}^2 \text{kg}^{-1}$)	ρ_s (kg m^{-3})	γ_{sca} (mm^{-1})	F_{ice}	B	g_G	g
1 (32-34)	26.1	147	0.90	0.32	1.89	0.64	0.82
2 (30-32)	27.2	178	1.07	0.34	1.69	0.68	0.84
3 (28-30)	21.1	250	1.13	0.44	1.57	0.62	0.81
4 (0-28)	18.4	287	1.08	0.49	1.59	0.64	0.82

lengths shorter than 1400 nm. We suspect that beyond 1400 nm, differences between the model and observations is due to the limitations of the assumptions made as part of the geometric optics approximation as the approximate particle size parameter is < 1000 for $\lambda > 1400$ nm. The simulated spectral albedos converge to the same value at approximately 950 nm, which matches the observed behavior of measurements collected over 4.5 and 2.5 cm panel depths. This behavior does not match the observed behavior of the virgin snow, which has an albedo higher than the panel observations until approximately 1400 nm. It is unknown if the cause of this difference is due to the model or is related to observational uncertainty caused by imperfect

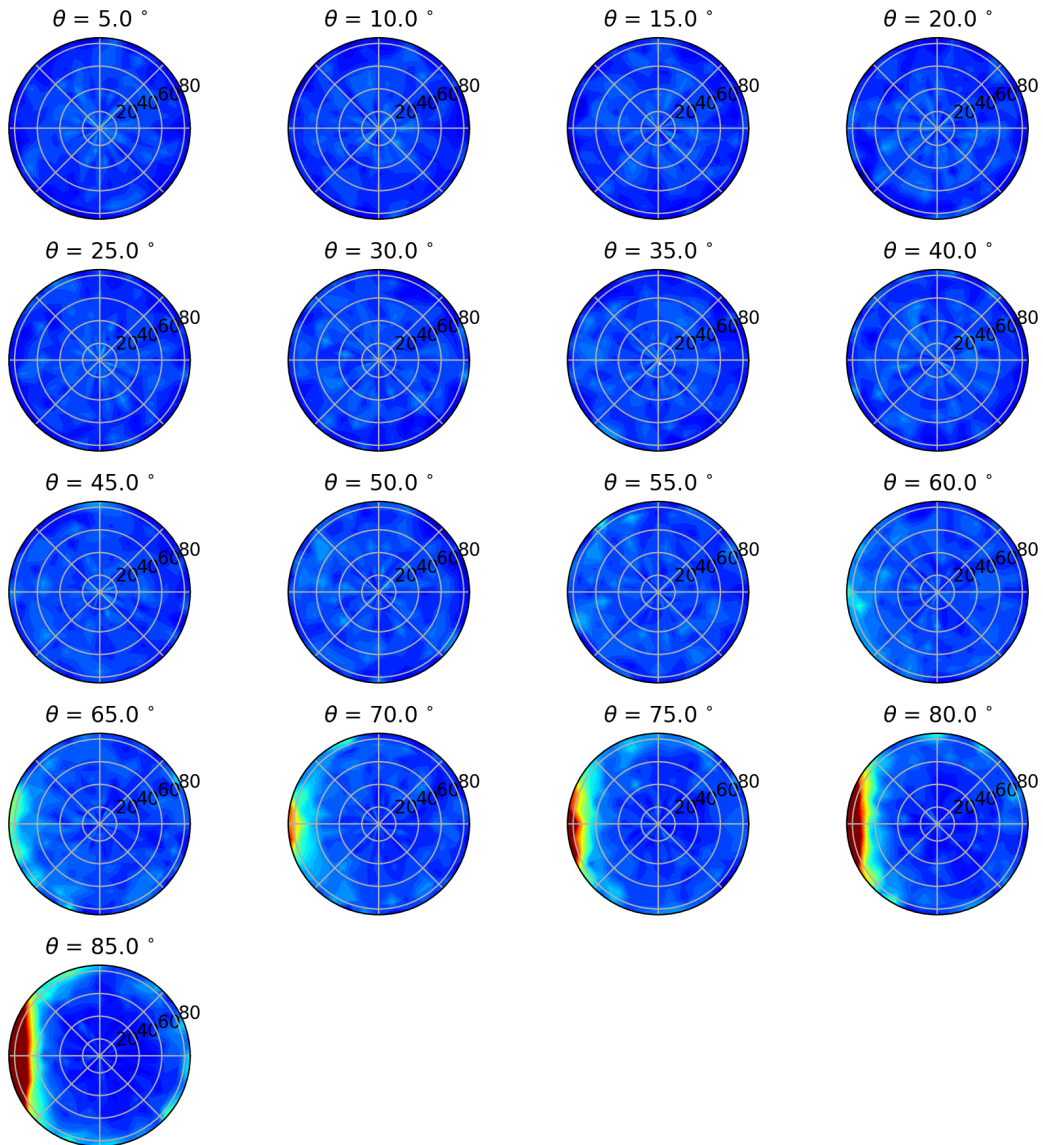


Figure 10. Polar plots of DCRF at 1000 nm for incident zenith angles ranging from 5 - 89°. Reflected azimuthal direction is on the theta axis, and reflected zenith angle is on the r axis. Color scale ranges from 0-1.5.

lighting conditions. Therefore, we are careful to note that this comparison is presented as an initial evaluation of our modeling framework and not a robust evaluation of its accuracy.

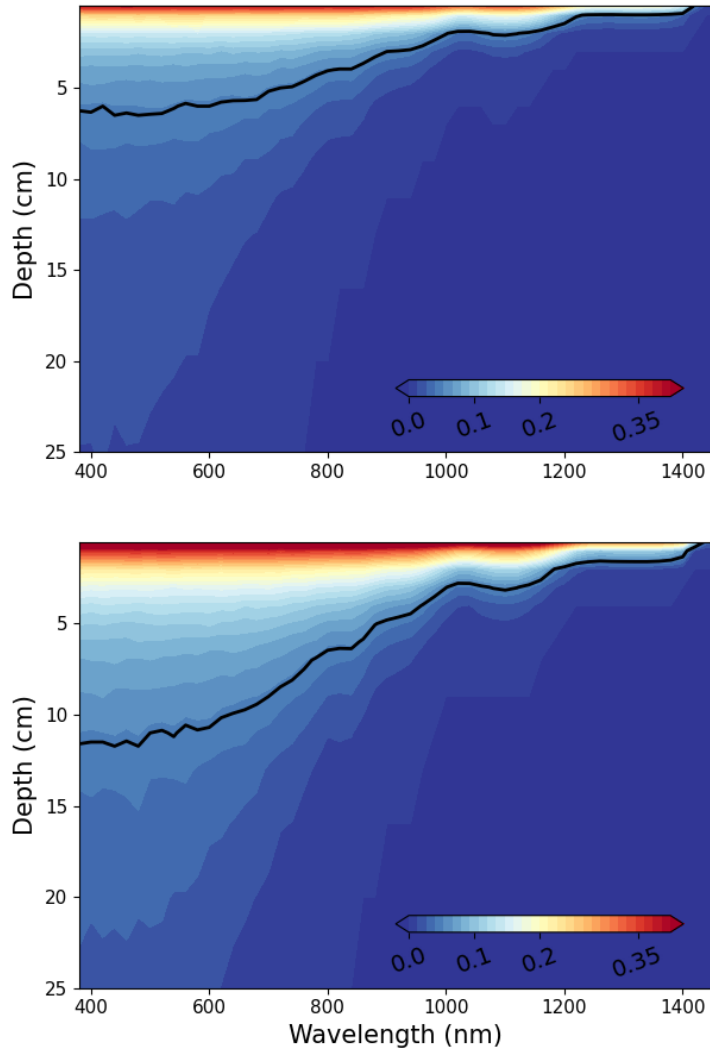


Figure 11. Simulated transmittance of a) the fine grain snow, and b) the coarse grain samples contoured as a function of depth and wavelength. Solid black lines mark the depth of the 5 % transmittance contour.

370 3.3 Snow optical and physical properties

The first component of the model is used independently of the plane-parallel model to assess the relationship between common snow physical properties and the simulated optical properties from this framework. To demonstrate this, we compare snow specific surface area (SSA) and snow sample density (ρ_s) to γ_{sca} and F_{ice}^i . This analysis is performed by generating optical properties from several μCT sample volumes collected on different dates and locations during the 2020-2021 winter season,

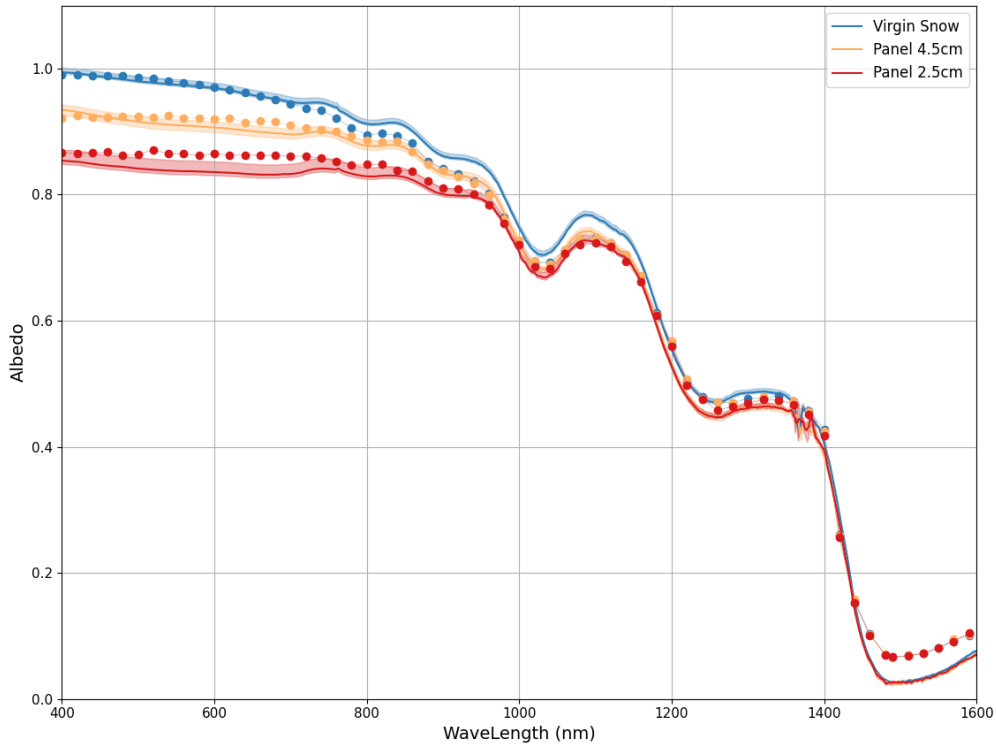


Figure 12. Simulated and observed spectral albedo for three different snow depths. The solid lines indicate observations and dotted lines indicate simulations. The shading around the observations indicates the inter-quartile range of the measurements computed from the five snow and two reference scans collected during each measurement, providing an assessment of measurement uncertainty. The mean RMSE of the simulated albedo compared to measurement-derived albedo over 400-1600 nm is equal to 0.03.

375 spanning a wide range of snow types. Note that each μCT sample is approximately 800 mm^3 and the sample SSA and ρ_s are determined from the μCT 3D rendering.

This analysis reveals that F_{ice} has a very robust relationship with snow density (Fig. 13a) described by the linear fit:

$$F_{\text{ice}} = 0.0008\rho_s + 0.22, \quad (22)$$

380 with $r^2 = 0.92$. In Figure 13b, γ_{sca} is compared to the product of ρ_s and SSA, to match the analytical formula described in Kokhanovsky and Zege (2004). The results show a clear linear relationship fit to:

$$\gamma_{\text{ext}} = 0.21\rho_s\text{SSA} - 0.01, \quad (23)$$

with $r^2 = 0.78$.

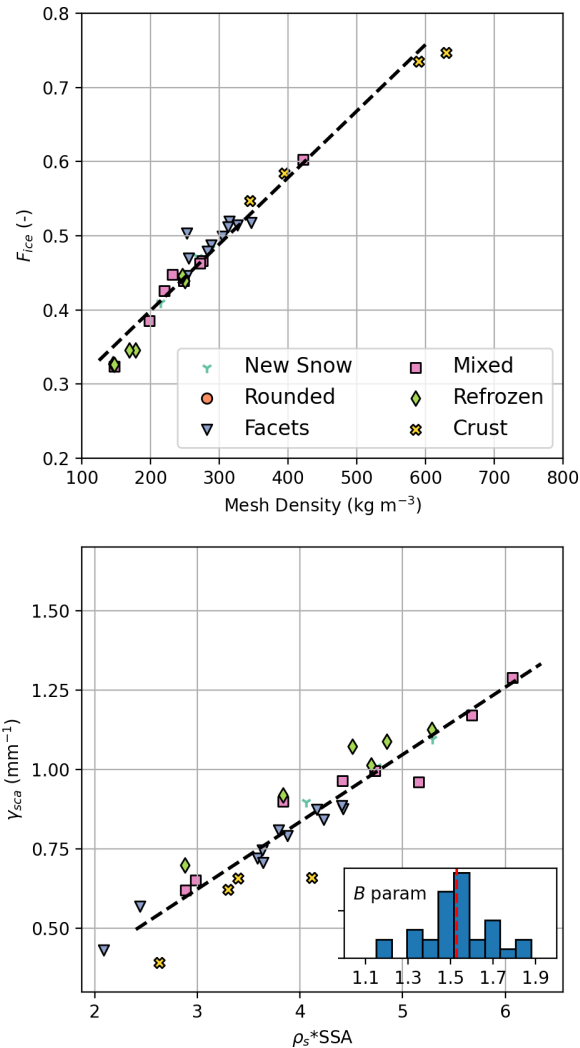


Figure 13. Optical properties for $\lambda=1000$ nm computed from μ CT photon tracking compared against sample physical properties. a) F_{ice} vs. ρ_s and b) γ_{sca} vs. $SSA \cdot \rho_s$. Linear regression lines are shown in black dashed lines. Marker shapes and colors are indicative of the observed grain forms determined through visual assessment during snow pit analysis. Note that in panel (b) a histogram of the estimated B parameters for all of the μ CT samples is shown, inset. $B_{mean} = 1.53$ is shown as the vertical red line.

The estimated B parameter is distributed normally around a mean of 1.49, consistent with the results reported in Libois et al. (2014). We note that there is no significant relationship between B and snow grain form or size, however there is a general tendency for B to be highest for samples with higher SSA and smaller grains, which is qualitatively consistent with Kokhanovsky and Zege (2004) and Libois et al. (2014).

385

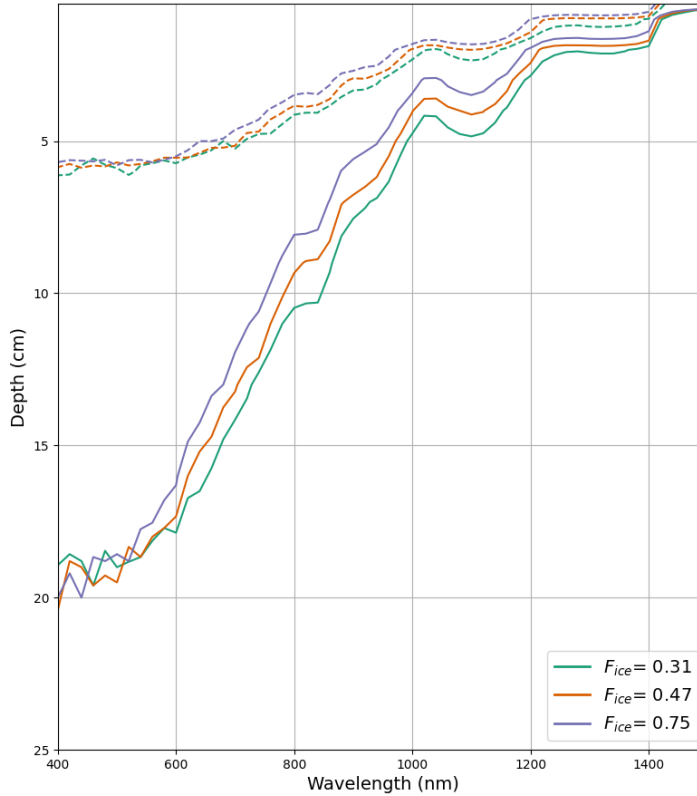


Figure 14. Depth of simulated 5% transmittance contour as a function of wavelength for varying F_{ice} at two scattering coefficients: $\gamma_{sca} = 0.39$ (solid lines) and $\gamma_{sca} = 1.29$ (dashed lines).

To further assess how these two specific snow optical properties, γ_{sca} and F_{ice} , affect the greater simulated spectral transmittance, we perform a sensitivity analysis by comparing the 5% transmittance contour depth for three fractional ice paths: 0.31, 0.47, 0.75 at two fixed γ_{sca} values: 1.29, 0.39 mm^{-1} (Fig. 14). The two γ_{sca} values correspond to the max and min values found in the previous analysis and presented in Fig. 13b. The three F_{ice} values correspond to the max, min, and mean values (Fig. 13a). We compare the influence of F_{ice} at both the max and min γ_{sca} values, since we anticipate the strength of its influence will vary according to γ_{sca} . We note that high values of γ_{sca} are more likely to coincide with high values of F_{ice} due to the shared dependence of these variables on snow density in most snowpacks.

The results of this analysis indicate that both γ_{sca} and F_{ice} impact snow transmittance in accordance with relationships discussed in Libois et al. (2013). Specifically, the approximate factor of 3 decrease in the scattering coefficient corresponds to an approximate factor of 3 increase in depth of the 5% transmittance contour, consistent with a linear relationship between γ_{sca} and penetration depth (L). Additionally, the simulated factor-increase in penetration depth is approximately the square root of the factor increase in F_{ice} , for $\lambda > 600$ nm, consistent with the $L \approx \sqrt{B * \kappa_{abs}}$ presented in Libois et al. (2013).

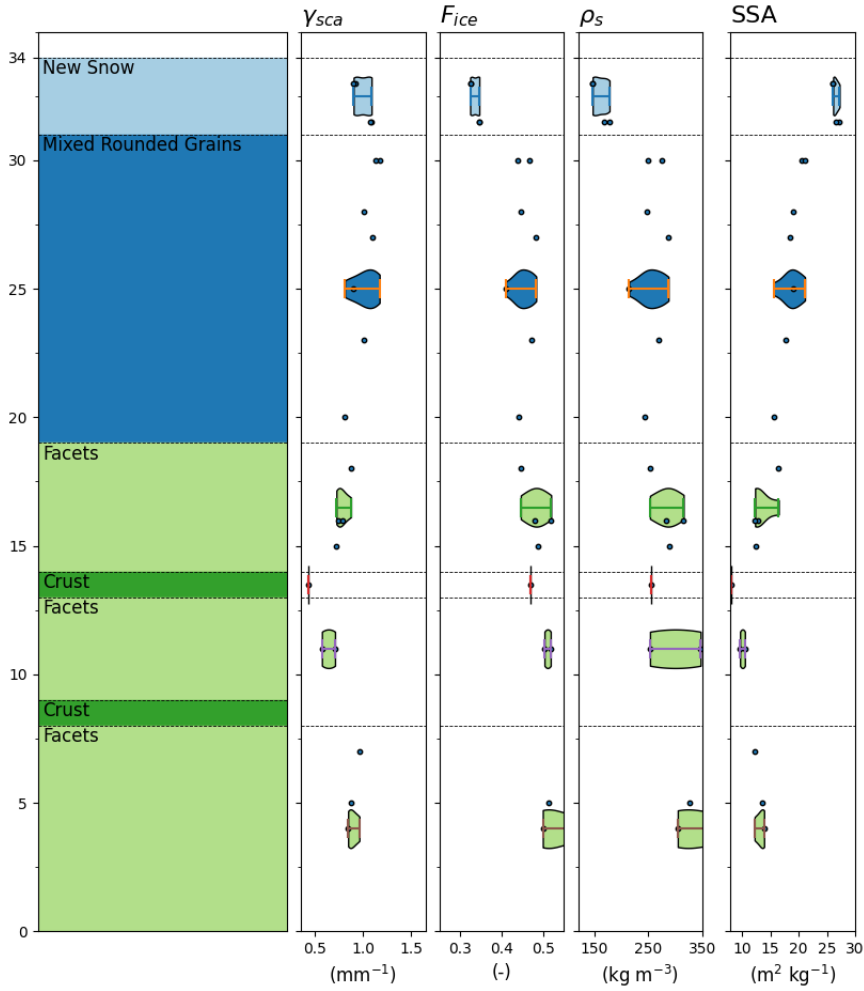


Figure 15. Snow pit stratigraphy (left) compared against γ_{sca} , F_{ice} , ρ_s , and SSA. Each dot represents a μ CT sample at a specified depth. Violin plots show estimated probability distributions for each observer-identified snow layer according to the samples collected with the layer.

4 Discussion

400 Overall, this framework shows promise as a research tool for better understanding visible and NIR snow radiative transfer through snowpacks with irregularly shaped and arranged grains. However, there are numerous uncertainties in this framework that should be addressed in future work to better understand its capabilities and limitations.

For instance, there are broader questions surrounding the definition of the scattering coefficient γ_{sca} and the phase function $p(\cos \Theta_j)$ for weakly absorbing porous media in the geometric optics limit. While, fundamentally, γ_{sca} is the inverse of the mean
 405 free path traveled by a photon between scattering events within the medium, there is some ambiguity as to how a scattering

event is defined. Traditionally, and in most applications, a scattering event is defined as occurring at a particle. That is, light intersects a particle, and is scattered away from the particle, and internal reflections within the particle are considered as part of a single, larger, scattering event (e.g., Van De Hulst, 1957; Kokhanovsky and Zege, 2004; Randrianalisoa and Baillis, 2010; Malinka, 2014). However, more recent studies have considered scattering along dielectric boundaries separating the air/ice
410 phase such that internal reflections within a given particle are counted as distinct scattering events (e.g., Xiong et al., 2015). While ray tracing techniques such as the one presented here are well-suited to the latter definition, this model conforms to the former, "particle", approach such that the optical properties generated are consistent with a majority of accepted methods. However, we note that reconciling these definitions is a worthy topic of future research, and that the model framework presented here is a potentially useful tool for these efforts.

415 An additional source of uncertainty in computing the optical properties is the method used to estimate the absorption enhancement parameter B directly from ray tracing. Formulas presented in Libois et al. (2019) show that B can be related to F_{ice} and snow density following:

$$B = \frac{\left(F_{ice} - \frac{\rho_{ice}}{\rho_s F_{ice}} \right)}{\left(F_{ice} - 1 \right)}. \quad (24)$$

However, estimating B from the sample density and F_{ice} generally leads to values much larger than those computed from Eq.
420 (8). We speculate that this discrepancy is due to the fact that some photon tracks through the rendered mesh do not adequately represent the snow sample. Specifically, some photons traveling through the mesh take short paths through a single particle before exiting the sample, resulting in an F_{ice} close to 1. This is supported by the presence of a peak at 0.95 in the histogram of F_{ice} shown in Fig. 2b. Since Eq. (24) indicates a non-linear increase in B with F_{ice} , these non-representative paths have a disproportionately large influence on B in Eq. (24).

425 Another possible source of uncertainty in this framework is the assumption that the optical properties computed from volume μ CT samples on the order of 1 cm^3 are homogeneous laterally, and can be extrapolated to characterize representative layer depths. To elucidate upon this uncertainty, we compare the optical and physical properties of the 20 rendered μ CT samples collected at UVD on 12 February 2021 to the observed snow pit stratigraphy (Fig. 15). Here we show that the top layer of the snowpack has more homogeneous physical and optical properties than the buried layers. In particular there is substantial
430 variability in γ_{sca} and F_{ice} within the rounded grains and the upper-most facet layers. Further investigation into this variability in the facet layer spanning the 14-18 cm layer reveals that this variability is caused largely by the fact that some μ CT samples within this layer contained unusually large pore spaces, which caused lower SSA and γ_{sca} values. We suspect that this variability has limited impacts on the simulated spectral albedo for the shallow snow simulations, since the top snow layer is relatively homogeneous. However, this variability is likely to have more significant impacts for simulations focused on older snowpacks
435 with larger and less uniformly distributed snow grains.

Finally, there are several assumptions we used to simplify our model that are worth additional discussion. First, we've taken the real part of the ice refractive index to be constant at 1.30, which is the refractive index of ice at $\lambda = 1000 \text{ nm}$. While this is generally a good assumption, there is a minor wavelength dependence throughout the visible and NIR range that could affect

the optical properties of the medium and potentially influence the plane-parallel model. Further, it has been shown that spectral
440 albedo in the NIR ($\lambda > 1400$ nm) is sensitive to which refractive index database is used to represent absorption (Carmagnola
et al., 2013; Dumont et al., 2021). While we do not explore this sensitivity here, we note it as a potential source of error.
Finally, the derivation of optical properties is based on the underlying assumption that snow is weakly absorbing such that
 γ_{ext} can be approximated with γ_{sca} . While snow is weakly absorbing in the visible range, it is more absorptive in the NIR,
and accordingly we expect that this assumption can lead to increased uncertainty beyond 1400 nm. Despite these sources of
445 potential uncertainty, as demonstrated in Fig. 12, simulated and observed albedos are in good agreement for $\lambda < 1400$ nm.

5 Conclusions

In this work we have presented a blended photon tracking radiative transfer model in an effort to better understand the com-
plicated influence of snowpack microstructure on snow spectral transmittance in the geometric optics limit. A primary goal
of this modeling approach is to expand upon previous approaches aimed at incorporating 3D renderings of real snow mi-
450 crostructure into radiative transfer models for snowpacks of arbitrary depth, while maintaining the ray tracing methods utilized
in the original Kaempfer et al. (2007) model. To accomplish this, existing methods for simulated photon interactions with
rendered elements are employed to determine key optical properties of the snow (Grundy et al., 2000; Kaempfer et al., 2007;
Randrianalisoa and Baillis, 2010).

An evaluation of this framework for consistency with known behavior of spectral snow albedo revealed that this framework
455 can successfully reproduce the dependency of spectral albedo and grain size, as well as the surface anisotropy at high incident
zenith angles, found in previous studies. Furthermore, an initial comparison of the simulated snow albedo against albedo
measured in the field over snow with varying depths indicates that the model can simulate the effects of an underlying surface
on spectral albedo with sufficient accuracy.

In comparing two different snow samples, it was revealed that snow microstructure has a large impact on snow transmittance
460 in the visible spectrum and near the snow surface, increasing the 5 % transmittance depth at 400 - 650 nm from approximately
6 cm for a fine grain snow sample to 12.5 cm depth for a coarse grain sample. These values and the ability to further constrain
the transmittance depths of shallow snowpacks will allow for improved capabilities for determining the optical properties
of shallow snowpacks. A brief sensitivity analysis of the optical properties revealed that lowering the medium scattering
coefficient acted to increase the transmittance depth in the visible bands, while the ice-path fraction (F_{ice}) impacted the rate at
465 which albedo and transmittance decreased as a function of wavelength in the NIR.

Overall, while current efforts are focused on using this model to better understand snow transmittance, it shows promise as
a broadly applicable snow RTM that has a strong direct connection to μCT snow samples. While currently it is limited to the
geometric optics approximation for clean snow and unpolarized radiation, ongoing and anticipated future efforts are aimed at
incorporating polarization, parameterizing diffraction, and including light absorbing particulates (LAPs). In particular, recent
470 multiphase image segmentation techniques (West et al., 2018; Hagenmuller et al., 2019) could be used to better separate snow,
air, and LAPs in a μCT sample allowing for the impact of LAPs to be determined through ray tracing. Furthermore, because

the model operates entirely as a photon tracking model, it is a natural fit with macroscale ray tracing and therefore could be used to investigate the reflectance of rough snow surfaces such as sun cups or sastrugi.

Code and data availability. The mesh generation and radiative transfer model code are publicly available at Letcher and Parno (2022a).

475 Supporting ASD data and analysis code is publicly available at Letcher and Parno (2022b)

Author contributions. Theodore Letcher performed a majority of the model physics implementation, structural development, and coding, in addition to coordinating the model analysis and manuscript preparation. Julie Parno led research and coding efforts related to the 3D mesh generation and rendering and performed major research and coding efforts related to the first component of model, she also coordinated a majority of the fieldwork activity. Zoe Courville provided research support, participated in snow sampling and coordinated μ CT analysis.

480 Lauren Farnsworth performed a large portion of μ CT scans and a majority of the μ CT image post processing and analysis. Jason Olivier participated in fieldwork and provided background on the ASD instrumentation and sampling for the manuscript. Theodore, Julie, and Jason performed the RTM simulations and assisted in code debugging. All authors provided writing support for the manuscript.

Competing interests. The authors declare that no competing interests are present

Acknowledgements. We wish to acknowledge Dr. Arnold Song from Dartmouth College in Hanover, New Hampshire for providing relevant code examples to facilitate 3D shape rendering. We also wish to thank Taylor Hodgdon from CRREL for providing occasional support and advice on using Python to perform mesh generation and rendering. We thank Dr. Bert Davis, and Dr. Ned Bair for providing valuable initial feedback on the manuscript. Funding support for this research was provided by the U.S. Army Engineer Research and Development Center (ERDC) Cold Weather Military Research project. Finally, we would like to sincerely thank the assigned journal editor, and the reviewers for providing thorough and engaging rounds of review which substantially improved the quality of this manuscript.

485

490 **References**

- Adolph, A. C., Albert, M. R., Lazarcik, J., Dibb, J. E., Amante, J. M., and Price, A.: Dominance of grain size impacts on seasonal snow albedo at open sites in New Hampshire, *Journal of Geophysical Research: Atmospheres*, 122, 121–139, 2017.
- Aoki, T., Aoki, T., Fukabori, M., Hachikubo, A., Tachibana, Y., and Nishio, F.: Effects of snow physical parameters on spectral albedo and bidirectional reflectance of snow surface, *Journal of Geophysical Research: Atmospheres*, 105, 10 219–10 236, 2000.
- 495 Attene, M.: A lightweight approach to repairing digitized polygon meshes, *The visual computer*, 26, 1393–1406, 2010.
- Bair, E. H., Rittger, K., Skiles, S. M., and Dozier, J.: An examination of snow albedo estimates from MODIS and their impact on snow water equivalent reconstruction, *Water Resources Research*, 55, 7826–7842, 2019.
- Bohren, C. F. and Beschta, R. L.: Snowpack albedo and snow density, *Cold Regions Science and Technology*, 1, 47–50, 1979.
- Carmagnola, C., Domine, F., Dumont, M., Wright, P., Strellis, B., Bergin, M., Dibb, J., Picard, G., Libois, Q., Arnaud, L., et al.: Snow spectral
500 albedo at Summit, Greenland: measurements and numerical simulations based on physical and chemical properties of the snowpack, *The Cryosphere*, 7, 1139–1160, 2013.
- Chernyaev, E.: Marching cubes 33: Construction of topologically correct isosurfaces, Tech. rep., 1995.
- Dang, C., Fu, Q., and Warren, S. G.: Effect of snow grain shape on snow albedo, *Journal of the Atmospheric Sciences*, 73, 3573–3583, 2016.
- Déry, S. J. and Brown, R. D.: Recent Northern Hemisphere snow cover extent trends and implications for the snow-albedo feedback, *Geo-
505 physical Research Letters*, 34, 2007.
- Dickinson, R. E.: Biosphere atmosphere transfer scheme (BATS) version 1e as coupled to the NCAR community climate model, NCAR Tech. Note TH-387+ STR, 1993.
- Doherty, S., Warren, S., Grenfell, T., Clarke, A., and Brandt, R.: Light-absorbing impurities in Arctic snow, *Atmospheric Chemistry and Physics*, 10, 11 647–11 680, 2010.
- 510 Dumont, M., Brissaud, O., Picard, G., Schmitt, B., Gallet, J.-C., and Arnaud, Y.: High-accuracy measurements of snow Bidirectional Reflectance Distribution Function at visible and NIR wavelengths—comparison with modelling results, *Atmospheric Chemistry and Physics*, 10, 2507–2520, 2010.
- Dumont, M., Brun, E., Picard, G., Michou, M., Libois, Q., Petit, J., Geyer, M., Morin, S., and Josse, B.: Contribution of light-absorbing impurities in snow to Greenland’s darkening since 2009, *Nature Geoscience*, 7, 509–512, 2014.
- 515 Dumont, M., Flin, F., Malinka, A., Brissaud, O., Hagenmuller, P., Lapalus, P., Lesaffre, B., Dufour, A., Calonne, N., Rolland du Roscoat, S., et al.: Experimental and model-based investigation of the links between snow bidirectional reflectance and snow microstructure, *The Cryosphere*, 15, 3921–3948, 2021.
- Flanner, M. G. and Zender, C. S.: Linking snowpack microphysics and albedo evolution, *Journal of Geophysical Research: Atmospheres*, 111, 2006.
- 520 Flanner, M. G., Shell, K. M., Barlage, M., Perovich, D. K., and Tschudi, M.: Radiative forcing and albedo feedback from the Northern Hemisphere cryosphere between 1979 and 2008, *Nature Geoscience*, 4, 151–155, 2011.
- Gardner, A. S. and Sharp, M. J.: A review of snow and ice albedo and the development of a new physically based broadband albedo parameterization, *Journal of Geophysical Research: Earth Surface*, 115, 2010.
- Grenfell, T. C. and Perovich, D. K.: Radiation absorption coefficients of polycrystalline ice from 400–1400 nm, *Journal of Geophysical
525 Research: Oceans*, 86, 7447–7450, 1981.

- Grundy, W., Douté, S., and Schmitt, B.: A Monte Carlo ray-tracing model for scattering and polarization by large particles with complex shapes, *Journal of Geophysical Research: Planets*, 105, 29 291–29 314, 2000.
- Hagenmuller, P., Flin, F., Dumont, M., Tuzet, F., Peinke, I., Lapalus, P., Dufour, A., Roulle, J., Pézard, L., Voisin, D., et al.: Motion of dust particles in dry snow under temperature gradient metamorphism, *The Cryosphere*, 13, 2345–2359, 2019.
- 530 Hall, A.: The role of surface albedo feedback in climate, *Journal of Climate*, 17, 1550–1568, 2004.
- Haussener, S., Gergely, M., Schneebeli, M., and Steinfeld, A.: Determination of the macroscopic optical properties of snow based on exact morphology and direct pore-level heat transfer modeling, *Journal of Geophysical Research: Earth Surface*, 117, 2012.
- He, C. and Flanner, M.: *Snow Albedo and Radiative Transfer: Theory, Modeling, and Parameterization*, in: *Springer Series in Light Scattering*, pp. 67–133, Springer, 2020.
- 535 Hudson, S. R., Warren, S. G., Brandt, R. E., Grenfell, T. C., and Six, D.: Spectral bidirectional reflectance of Antarctic snow: Measurements and parameterization, *Journal of Geophysical Research: Atmospheres*, 111, 2006.
- Ishimoto, H., Adachi, S., Yamaguchi, S., Tanikawa, T., Aoki, T., and Masuda, K.: Snow particles extracted from X-ray computed microtomography imagery and their single-scattering properties, *Journal of Quantitative Spectroscopy and Radiative Transfer*, 209, 113–128, 2018.
- 540 Iwabuchi, H.: Efficient Monte Carlo methods for radiative transfer modeling, *Journal of the atmospheric sciences*, 63, 2324–2339, 2006.
- Jacques, S. L.: Monte Carlo modeling of light transport in tissue (steady state and time of flight), in: *Optical-thermal response of laser-irradiated tissue*, pp. 109–144, Springer, 2010.
- Jiao, Z., Ding, A., Kokhanovsky, A., Schaaf, C., Bréon, F.-M., Dong, Y., Wang, Z., Liu, Y., Zhang, X., Yin, S., et al.: Development of a snow kernel to better model the anisotropic reflectance of pure snow in a kernel-driven BRDF model framework, *Remote Sensing of Environment*, 221, 198–209, 2019.
- 545 Kaempfer, T. U., Hopkins, M., and Perovich, D.: A three-dimensional microstructure-based photon-tracking model of radiative transfer in snow, *Journal of Geophysical Research: Atmospheres*, 112, 2007.
- Kokhanovsky, A. A. and Zege, E. P.: Scattering optics of snow, *Applied Optics*, 43, 1589–1602, 2004.
- Letcher, T. and Parno, J.: CRREL-GOSRT/CRREL-GOSRT: CRREL-GOSRT First Public Release, <https://doi.org/10.5281/zenodo.7086881>, 2022a.
- 550 Letcher, T. and Parno, J.: CRREL-GOSRT/TC_Paper_Supporting_Data: Supporting Data, <https://doi.org/10.5281/zenodo.7083432>, 2022b.
- Letcher, T. W. and Minder, J. R.: Characterization of the simulated regional snow albedo feedback using a regional climate model over complex terrain, *Journal of Climate*, 28, 7576–7595, 2015.
- Lewiner, T., Lopes, H., Vieira, A. W., and Tavares, G.: Efficient implementation of marching cubes' cases with topological guarantees, 555 *Journal of graphics tools*, 8, 1–15, 2003.
- Li, S. and Zhou, X.: Accuracy assessment of snow surface direct beam spectral albedo derived from reciprocity approach through radiative transfer simulation, in: *IGARSS 2003. 2003 IEEE International Geoscience and Remote Sensing Symposium. Proceedings (IEEE Cat. No. 03CH37477)*, vol. 2, pp. 839–841, IEEE, 2003.
- Libois, Q., Picard, G., France, J., Arnaud, L., Dumont, M., Carmagnola, C., and King, M.: Influence of grain shape on light penetration in 560 snow, *The Cryosphere*, 7, 1803–1818, 2013.
- Libois, Q., Picard, G., Dumont, M., Arnaud, L., Sergent, C., Pougatch, E., Sudul, M., and Vial, D.: Experimental determination of the absorption enhancement parameter of snow, *Journal of Glaciology*, 60, 714–724, 2014.

- Libois, Q., Lévesque-Desrosiers, F., Lambert-Girard, S., Thibault, S., and Domine, F.: Optical porosimetry of weakly absorbing porous materials, *Optics Express*, 27, 22 983–22 993, 2019.
- 565 Liou, K., Takano, Y., and Yang, P.: Light absorption and scattering by aggregates: Application to black carbon and snow grains, *Journal of Quantitative Spectroscopy and Radiative Transfer*, 112, 1581–1594, 2011.
- Lorensen, W. E. and Cline, H. E.: Marching cubes: A high resolution 3D surface construction algorithm, *ACM siggraph computer graphics*, 21, 163–169, 1987.
- Malinka, A. V.: Light scattering in porous materials: Geometrical optics and stereological approach, *Journal of Quantitative Spectroscopy*
570 *and Radiative Transfer*, 141, 14–23, 2014.
- Natarajan, B. K.: On generating topologically consistent isosurfaces from uniform samples, *The Visual Computer*, 11, 52–62, 1994.
- Neshyba, S. P., Grenfell, T. C., and Warren, S. G.: Representation of a nonspherical ice particle by a collection of independent spheres for scattering and absorption of radiation: 2. Hexagonal columns and plates, *Journal of Geophysical Research: Atmospheres*, 108, 2003.
- Nielson, G. M. and Hamann, B.: The asymptotic decider: resolving the ambiguity in Marching Cubes., in: *IEEE visualization*, vol. 91, pp. 575 83–91, 1991.
- Painter, T. H., Bryant, A. C., and Skiles, S. M.: Radiative forcing by light absorbing impurities in snow from MODIS surface reflectance data, *Geophysical Research Letters*, 39, 2012.
- Perovich, D. K.: Light reflection and transmission by a temperate snow cover, *Journal of Glaciology*, 53, 201–210, 2007.
- Perovich, D. K. and Govoni, J. W.: Absorption coefficients of ice from 250 to 400 nm, *Geophysical Research Letters*, 18, 1233–1235, 1991.
- 580 Picard, G., Arnaud, L., Domine, F., and Fily, M.: Determining snow specific surface area from near-infrared reflectance measurements: Numerical study of the influence of grain shape, *Cold Regions Science and Technology*, 56, 10–17, 2009.
- Picard, G., Libois, Q., and Arnaud, L.: Refinement of the ice absorption spectrum in the visible using radiance profile measurements in Antarctic snow, *The Cryosphere*, 10, 2655–2672, 2016.
- Randrianalisoa, J. and Baillis, D.: Radiative properties of densely packed spheres in semitransparent media: A new geometric optics approach,
585 *Journal of Quantitative Spectroscopy and Radiative Transfer*, 111, 1372–1388, 2010.
- Saito, M., Yang, P., Loeb, N. G., and Kato, S.: A novel parameterization of snow albedo based on a two-layer snow model with a mixture of grain habits, *Journal of the Atmospheric Sciences*, 76, 1419–1436, 2019.
- Schroeder, W. J., Lorensen, B., and Martin, K.: *The visualization toolkit: an object-oriented approach to 3D graphics*, Kitware, 2004.
- Scopigno, R.: A modified look-up table for implicit disambiguation of Marching Cubes, *The visual computer*, 10, 353–355, 1994.
- 590 Shi, T., Cui, J., Chen, Y., Zhou, Y., Pu, W., Xu, X., Chen, Q., Zhang, X., and Wang, X.: Enhanced light absorption and reduced snow albedo due to internally mixed mineral dust in grains of snow, *Atmospheric Chemistry and Physics*, 21, 6035–6051, 2021.
- Skiles, S. M. and Painter, T. H.: Toward understanding direct absorption and grain size feedbacks by dust radiative forcing in snow with coupled snow physical and radiative transfer modeling, *Water Resources Research*, 55, 7362–7378, 2019.
- Skiles, S. M., Painter, T. H., Deems, J. S., Bryant, A. C., and Landry, C. C.: Dust radiative forcing in snow of the Upper Colorado River
595 Basin: 2. Interannual variability in radiative forcing and snowmelt rates, *Water Resources Research*, 48, 2012.
- Skiles, S. M., Painter, T. H., Belnap, J., Holland, L., Reynolds, R. L., Goldstein, H. L., and Lin, J.: Regional variability in dust-on-snow processes and impacts in the Upper Colorado River Basin, *Hydrological Processes*, 29, 5397–5413, 2015.
- Stamnes, K. and Stamnes, J. J.: *Radiative transfer in coupled environmental systems: an introduction to forward and inverse modeling*, John Wiley & Sons, 2016.

- 600 Sullivan, C. B. and Kaszynski, A.: PyVista: 3D plotting and mesh analysis through a streamlined interface for the Visualization Toolkit (VTK), *Journal of Open Source Software*, 4, 1450, <https://doi.org/10.21105/joss.01450>, 2019.
- Thackeray, C. W. and Fletcher, C. G.: Snow albedo feedback: Current knowledge, importance, outstanding issues and future directions, *Progress in Physical Geography*, 40, 392–408, 2016.
- Van De Hulst, H. C.: *Light scattering by small particles*, John Wiley and Sons, 1957.
- 605 Van der Walt, S., Schönberger, J. L., Nunez-Iglesias, J., Boulogne, F., Warner, J. D., Yager, N., Gouillart, E., and Yu, T.: scikit-image: image processing in Python, *PeerJ*, 2, e453, 2014.
- Verseghy, D. L.: CLASS—A Canadian land surface scheme for GCMs. I. Soil model, *International Journal of Climatology*, 11, 111–133, 1991.
- Vionnet, V., Brun, E., Morin, S., Boone, A., Faroux, S., Moigne, P. L., Martin, E., and Willemet, J.-M.: The detailed snowpack scheme Crocus and its implementation in SURFEX v7. 2, *Geoscientific Model Development*, 5, 773–791, 2012.
- 610 Warren, S. G.: Can black carbon in snow be detected by remote sensing?, *Journal of Geophysical Research: Atmospheres*, 118, 779–786, 2013.
- Warren, S. G. and Brandt, R. E.: Optical constants of ice from the ultraviolet to the microwave: A revised compilation, *Journal of Geophysical Research: Atmospheres*, 113, 2008.
- 615 Warren, S. G. and Wiscombe, W. J.: A model for the spectral albedo of snow. II: Snow containing atmospheric aerosols, *Journal of Atmospheric Sciences*, 37, 2734–2745, 1980.
- West, B. A., Hodgdon, T. S., Parno, M. D., and Song, A. J.: Improved workflow for unguided multiphase image segmentation, *Computers & geosciences*, 118, 91–99, 2018.
- Whitney, B. A.: Monte Carlo radiative transfer, in: *Fluid Flows To Black Holes: A Tribute to S Chandrasekhar on His Birth Centenary*, pp. 151–176, World Scientific, 2011.
- 620 Wiscombe, W. J.: Improved Mie scattering algorithms, *Applied optics*, 19, 1505–1509, 1980.
- Wiscombe, W. J. and Warren, S. G.: A model for the spectral albedo of snow. I: Pure snow, *Journal of Atmospheric Sciences*, 37, 2712–2733, 1980.
- Xiong, C., Shi, J., Ji, D., Wang, T., Xu, Y., and Zhao, T.: A new hybrid snow light scattering model based on geometric optics theory and vector radiative transfer theory, *IEEE Transactions on Geoscience and Remote Sensing*, 53, 4862–4875, 2015.
- 625 Yang, P. and Liou, K.: Geometric-optics–integral-equation method for light scattering by nonspherical ice crystals, *Applied Optics*, 35, 6568–6584, 1996.