A generalized photon-tracking approach to simulate spectral snow albedo and transmittance using X-ray microtomography and geometric optics

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Abstract.

A majority of snow radiative transfer models (RTM) treat snow as a collection of idealized grains rather than an organized ice-air matrix. Here we present a generalized multi-layer photon-tracking RTM that simulates light reflectance and transmittance of snow based on X-ray microtomography images, treating snow as a coherent structure rather than a collection of grains. The model uses a blended approach to expand ray-tracing techniques applied to sub-1 cm³ snow samples to snowpacks of arbitrary depths. While this framework has many potential applications, this study's effort is focused on simulating reflectance and transmittance in the visible and near-infrared (NIR) through thin snowpacks as this is relevant for surface energy balance and remote sensing applications. We demonstrate that this framework fits well within the context of previous work and capably reproduces many known optical properties of a snow surface, including the dependence of spectral reflectance on snow specific surface area and incident zenith angle as well as the surface Bidirectional Reflectance Distribution Function (BRDF). To evaluate the model, we compare it against reflectance data collected with a spectroradiometer at a field site in east-central Vermont. In this experiment, painted panels were inserted at various depths beneath the snow to emulate thin snow. The model compares remarkably well against the reflectance estimated from the spectroradiometer measurements, with an RMSE of 0.03. Sensitivity simulations using this model indicate that snow transmittance is greatest in the visible wavelengths, limiting light penetration to the top 6 cm of the snowpack for fine grain snow but increasing to 12 cm for coarse grain snow. These results suggest that the 5% transmission depth in snow can vary by over 6 cm according to the snow type.

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1 Introduction

Due to the highly reflective nature of snow, seasonal snowpacks make the surface significantly more reflective when present, impacting regional weather and climate. Correspondingly, the snow albedo feedback, caused by changes in seasonal snow cover extent and properties, represents one of the more dramatic markers of regional and global climate change (e.g., Hall, 2004; Déry and Brown, 2007; Flanner et al., 2011; Letcher and Minder, 2015; Thackeray and Fletcher, 2016). While snow is

highly reflective, snow albedo is not equal for all snowpacks. For instance, snow albedo typically decreases with snow age due to metamorphic processes resulting in larger snow grains (e.g., Wiscombe and Warren, 1980; Aoki et al., 2000; Flanner and Zender, 2006; Adolph et al., 2017). Snow albedo is also diminished by light absorbing impurities such as dust or black carbon that contaminate the snow (Doherty et al., 2010; Painter et al., 2012; Skiles et al., 2012; Dumont et al., 2014; Skiles et al., 2015; Skiles and Painter, 2019; Shi et al., 2021). Importantly, these two effects impact different parts of the electromagnetic spectrum, with grain size having a greater influence in the near-infrared (NIR), and the particle contamination influencing the visible region. Finally, even though thin snow covers are highly reflective, the surface albedo for a thin snow cover can be influenced by the underlying ground surface depending on the snow microstructure (Perovich, 2007; Warren, 2013; Libois et al., 2013). Consequently, the detection of subnivean hazards is highly dependent on the microscopic properties of the overlaying snowpack. Understanding these small-scale drivers of snow albedo is important for large-scale remote sensing applications and regional weather and climate modeling.

There are several documented approaches to model snow broadband and spectral albedo using radiative transfer models (RTMs) in efforts to better understand and predict the effects of snow aging and impurities on snow optical properties. While a full review of snow radiative transfer is well beyond the scope of this paper, we refer the reader to He and Flanner (2020) for a rigorous overview of the different approaches. There are also numerous simplified parameterizations for snow albedo of varying complexity designed for implementation in weather and climate models (e.g., Verseghy, 1991; Dickinson, 1993; Gardner and Sharp, 2010; Vionnet et al., 2012; Saito et al., 2019; Bair et al., 2019).

At a fundamental level, the scattering of electromagnetic energy incident upon the boundary separating a snow grain and the surrounding air is determined by the different refractive indices for ice and air and the geometry of the interfaces. The absorption of light as it passes through solid ice is well understood and has a strong wavelength dependence (Grenfell and Perovich, 1981; Perovich and Govoni, 1991; Warren and Brandt, 2008). The scattering of visible and NIR light at an air/ice boundary is well described by the geometric optics approximation, where the wavelengths of visible and NIR light are small relative to the size of the typical snow particle (e.g., Kokhanovsky and Zege, 2004). While the physics behind scattering and absorption are well understood within the geometric optics limit, the actual path of a light ray through a snowpack can be extraordinarily convoluted as the ray is constantly intersecting air/ice interfaces with very little absorption.

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Seminal studies describing snow albedo modeling (e.g., Warren and Wiscombe, 1980; Wiscombe and Warren, 1980) and most subsequent approaches treat snow grains as independent scatterers, where the scattering properties of an individual grain are not affected by adjacent grains and are independent of the spacing between grains and, thus, snow density. For simplification and computational efficiency, Mie theory is often used to determine the albedo of snow represented as a collection of spherical particles (e.g., Bohren and Beschta, 1979; Wiscombe, 1980). Yet although snow grain size is often most cited as the key driver of snow albedo, grain shape also has an impact, leading to inaccuracies with the spherical assumption (Aoki et al., 2000; Neshyba et al., 2003; Picard et al., 2009; Libois et al., 2013; Dang et al., 2016). Efforts to understand and simulate the impacts of snow particle shape on snow spectral albedo have largely focused on leveraging the geometric optics approximation in various ways. For instance, Yang and Liou (1996) used ray-tracing to compute the single scattering properties of idealized hexagonal columns, plates, and rosettes. Grundy et al. (2000) presented a Monte Carlo approach to estimate optical properties

of computer-rendered 3D spheres that compared well with Mie theory. Their work was extended to estimate the scattering properties of irregularly shaped crystals.

Recently, there have been numerous efforts to characterize snow as a coherent medium rather than a collection of particles within the context of radiative transfer. For instance, Malinka (2014) combined stereological techniques and geometric optics to obtain the inherent optical properties of a snowpack. An additional study by Xiong et al. (2015) focused on determining the optical properties of an idealized mixed snow/air medium generated from a randomized bicontinuous 2D representation of the snow. X-ray microtomography (hereby: μ CT) is a powerful tool that has been used in many of these medium-based efforts. μ CT has been used to support numerous snow radiative transfer methods including individual particle scattering, ray-tracing, and analytical approaches (Haussener et al., 2012; Kaempfer et al., 2007; Malinka, 2014; Ishimoto et al., 2018; Dumont et al., 2021). Collectively, RTM-focused studies of snow have greatly expanded the knowledge surrounding the optical properties of irregular snow grains and informed the role of snow microstructure on spectral reflectance and transmittance.

In this study, we build upon the approaches of Grundy et al. (2000), Kaempfer et al. (2007), Jacques (2010), and Xiong et al. (2015) to develop a Monte Carlo photon-tracking snow RTM that focuses on representing snow as coherent 3D structure rather than a collection of particles. This framework employs ray-tracing to simulate photon tracks through 3D renderings of snow samples measured using μ CT and is designed for broad applications, including studying the effects of snow type and snow depth on snow spectral albedo and transmittance in the visible and NIR. In section 2, we describe the model framework and μ CT data processing. In section 3, we demonstrate the model's capability to reproduce known optical properties of snow, compare model output to spectral albedo measurements of objects buried beneath snow at various depths, and use the RTM to investigate snow transmittance. In sections 4 and 5, we present a broad discussion and conclusions.

2 Data and Methods

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The RTM framework used here is divided into two distinct components. The first determines key snow optical properties by firing photons into 3D closed-surface renderings of snow samples derived from μ CT scans with a voxel resolution of ≈ 20 μ m. The second is a semi-quantized 1D plane-parallel Monte Carlo model that uses the optical properties derived from the first part.

In the plane-parallel model, individual photon packets are initialized at the snow surface with a prescribed incident direction into the snowpack. Then, each packet has a unique path whereby all of the energy contained within a given packet travels in the same direction and the amount of energy within a given packet is depleted continuously according to absorption within the medium. The plane-parellel model is used to simulate spectral albedo and transmittance in the visible and NIR (i.e., $380 \le \lambda \le 1600$ nm) for snowcovers with arbitrary depths and known lower boundaries. In both model components, the ice refractive indices reported by Warren and Brandt (2008) are used to compute scattering and absorption.

While computationally expensive, there are several advantages to the Monte Carlo approach. In particular, Monte Carlo models are useful for modeling single scattering properties of non-spherical particles and for 3D radiative transfer applications

(e.g., Iwabuchi, 2006; Whitney, 2011). Additionally, the Monte Carlo approach lends itself well to parallelization, and the semi-quantized approach described here reduces the number of photons required to achieve a statistically robust result.

One critical simplification we make in this model is that we ignore the wave properties of light, such as phase and diffraction, which limits its overall applicability and reduces accuracy. However, this simplification has been used successfully in numerous previous studies (e.g., Kaempfer et al., 2007; Malinka, 2014; Xiong et al., 2015) and, because the diffraction pattern is strongly forward scattering (Xiong et al., 2015), we anticipate that this simplification is appropriate here. While some work has been done incorporating diffraction into geometric optics scattering for non-spherical particles (Yang and Liou, 1996; Liou et al., 2011), because this framework treats snow as a two-phase medium rather than a collection of particles, accounting for diffraction is less straightforward. Accordingly, we acknowledge that diffraction may be more important for the longer NIR wavelengths, and should be a potential focus of future work.

100 2.1 Snow Optical Properties

The plane-parallel model requires three key optical properties: the extinction coefficient (γ_{ext} [mm⁻¹]), the mean path fraction traveled within ice (F_{ice}), and the scattering phase function ($p(\cos\Theta)$). In considering a photon of light traveling through the snow medium along a path, the photon is considered extinct when it intersects and is scattered along an air/ice boundary or is absorbed within the ice. The extinction coefficient is then inversely proportional to the mean distance traveled between these scattering and absorption events. The phase function determines the change in direction of the ray during a scattering event, and the ice-path fraction, when combined with the spectrally variable ice absorption coefficient ($\kappa(\lambda)$), determines the mean energy depleted from the ray for a given distance traveled between scattering events. In this model, γ_{ext} is determined for a given snow sample following the method described in Xiong et al. (2015). In this framework, photons are initialized at a random position within the snow sample, and launched in a random direction for a specified distance (L). If the photon is initialized within the air, the probability of extinction (P_{ext}) is 1 if a boundary is intersected over L, otherwise it is 0. In the case where the photon is initialized within the ice medium, P_{ext} =1 if a boundary is intersected over L, otherwise it is given as:

$$P_{ext} = 1 - e^{-\kappa_{\lambda}L},\tag{1}$$

where κ_{λ} is the wavelength-dependent absorption coefficient of ice, which is related to the imaginary part of the ice refractive index (k):

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$$\kappa_{\lambda} = \frac{4\pi k}{\lambda}$$
. (2)

This slight modification is made to account for the added probability of extinction due to absorption of the photon within the ice particle. Using this method, a probability of extinction can be determined for distance L. This method is repeated for several distances ranging from the voxel resolution (20 μ m) to the width of the snow sample volume (e.g., 10 mm). The extinction coefficient is then determined using a curve fit to the Beer-Lambert law:

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$$P_{ext} = 1 - e^{-\gamma_{ext}L}$$
, (3)

The mean fractional ice path (F_{ice}) is determined by tracking individual photons as they travel throughout the snow sample. This framework closely mimics that of Kaempfer et al. (2007) in that photons travel through the snow medium and change direction according to Snell's law of refraction and a probabilistic representation of Fresnel's law of reflectance. Here, a photon is initialized at a random starting point somewhere along an edge of the snow sample and launched in a random direction into the snow sample. The photon is tracked until it exits the medium, and the F_{ice} is the ratio of the distance traveled within ice and the total distance traveled. This is repeated for a large number of photons to determine an average F_{ice} .

Fresnel's law dictates that the fractional reflection and transmission of light at a boundary is related to the incident angle (θ_i) and the refractive indices (n) of the two media separated by the boundary:

$$R_{h} = \frac{n_{1}\cos\theta_{i} - n_{2}\sqrt{1 - \left(\frac{n_{1}}{n_{2}}\sin\theta_{i}\right)^{2}}}{n_{1}\cos\theta_{i} + n_{2}\sqrt{1 - \left(\frac{n_{1}}{n_{2}}\sin\theta_{i}\right)^{2}}},\tag{4}$$

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$$R_{v} = \frac{n_{1}\sqrt{1 - \left(\frac{n_{1}}{n_{2}}\sin\theta_{i}\right)^{2} - n_{2}\cos\theta_{i}}}{n_{1}\sqrt{1 - \left(\frac{n_{1}}{n_{2}}\sin\theta_{i}\right)^{2} + n_{2}\cos\theta_{i}}},$$
(5)

where R_h and R_v are the horizontally and vertically polarized reflectances. Assuming that the radiation is unpolarized (e.g., natural light), the reflectance (R) is:

$$R = \frac{1}{2} \left(R_h^2 + R_v^2 \right). \tag{6}$$

Through energy conservation, the transmittance (T) is:

$$T = 1 - R. (7)$$

Then, if the vector normal to the boundary plane $(\hat{v_n})$ is oriented towards the medium with refractive index n_1 , the direction unit vectors for reflected and transmitted radiation are computed as $(\hat{v_r})$ and $(\hat{v_t})$:

$$\hat{v_r} = \hat{v_i} + 2\cos\theta_i \hat{v_n} \tag{8}$$

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$$\hat{v_t} = \frac{n_1}{n_2} \hat{v_t} + \left(\frac{n_1}{n_2} \cos \theta_t - \cos \theta_t\right) \hat{v_n},\tag{9}$$

We note that F_{ice} is determined by both the density of snow and the prevalence of internal reflections and, accordingly, is related to the absorption enhancement parameter B described in Kokhanovsky and Zege (2004). B quantifies the absorption path length extension due to internal reflections within a snow particle, and can be quantified by the ratio of the actual internal photon path-length through a sample medium and the internal path-length following a straight line (Libois et al., 2019). In this study we compute B for each snow sample following this method for comparison against previous work (Kokhanovsky and Zege, 2004; Libois et al., 2014).

In this framework, the phase function represents localized scattering at an air/ice interface as is done in Haussener et al. (2012) and Xiong et al. (2015). Here, the phase function is determined by tracking scattering angles during the algorithm used to determine F_{ice} . During this procedure, the phase function is first divided into a prescribed number of finite bins (j)with width, $d\Theta$. Each time a photon intersects an air/ice boundary the scattering angle is computed for both the reflected and transmitted directions where the cosine of the scattering angle (Θ) is the dot product between the directional unit vector of radiation incident on the boundary $(\hat{\Omega}')$ and the directional unit vector of the scattered radiation $(\hat{\Omega})$ in the Cartesian coordinate space:

$$155 \quad \cos\Theta = \hat{\Omega}' \cdot \hat{\Omega}. \tag{10}$$

Then, reflected and transmitted scattering angles are added to their respective bins weighted by the R and T computed from egs 6 and 7, respectively.

At the end of the ray-tracing model, the resulting distribution of energy is converted to a phase function defined relative to the total energy initially incident upon the rendered snow sample following Grundy et al. (2000):

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$$p(\cos\Theta_j) = \frac{4\pi N_j}{N\sin\Theta_j d\Theta},$$
 (11)

where N is the total photon energy and N_j is the total photon energy directed into bin j. In this study, the number of bins used to represent the phase function is 180. Accordingly, $d\Theta = 1^{\circ}$. To illustrate the procedure for generating the optical properties, we show the curve fit for γ_{ext} , F_{ice} , and $p(\cos\Theta)$ for a rendered μ CT sample of snow collected in the field (Fig. 1).

2.2 1D plane-parallel photon-tracking model

165 Once the optical properties of the snow sample are determined by launching photons through μ CT sample volumes, the planeparallel model is used to simulate snow spectral albedo, transmittance, and Bidirectional Reflectance Distribution Function (BRDF). The 1D model is used in place of the explicit photon-tracking model described by Kaempfer et al. (2007) in order to

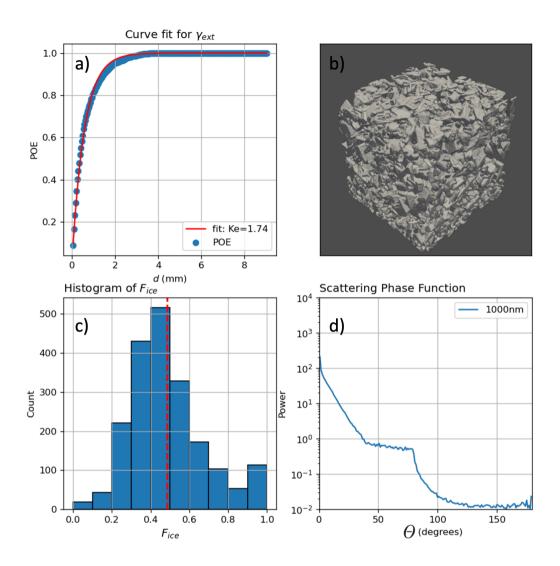


Figure 1. Top left: Probability of extinction and curve fit following eq. 3. Top right: 3D rendering a snow sample. Bottom Left: Histogram of F_{ice} . Bottom Right: Scattering phase function.

allow for the computationally feasible simulation of spectral albedo and transmittance for snow covers with depths exceeding 1 cm with sufficient grain resolution. Additionally, it is used to avoid complications associated with lateral boundary treatment and stitching multiple μ CT scans together into a single coherent snow lattice. The 1D model used here is largely based on the framework presented in Jacques (2010) and is similar to the model described in Picard et al. (2016). In this model, discrete, plane-parallel, snow layers with optical properties constant throughout each layer are first prescribed. Then a photon packet is initialized at some starting position (X_0) with cartesian components of (x_0, y_0, z_0) and an initial energy of unity (E = 1). An initial unit direction vector (V_0) for the photon is given in cartesian coordinates as:

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$$V_0 = \left[\sin\theta\cos\phi, \sin\theta\sin\phi, -\cos\theta\right],$$
 (12)

where θ is the solar zenith angle, and ϕ is the azimuth angle clockwise from x. This initial direction can be prescribed randomly (i.e., diffuse radiation), or at any specified zenith/azimuth angle (i.e., direct radiation), or as a mixture of both diffuse and direct radiation.

Once the initial position is set, the photon is launched into the medium, and travels a distance s before experiencing a scattering event. s is computed statistically using the Beer-Lambert law and the medium extinction coefficient (Jacques, 2010):

$$s = -\frac{ln\zeta}{\gamma_{ext}},\tag{13}$$

where ζ is a random uniform number between 0 and 1. The new position in the medium is:

$$X = X_0 + sV_0 \tag{14}$$

At the scattering event, the photon packet is given a new direction unit vector according to the scattering phase function. 85 Because this framework treats the scattering phase function as a probability distribution function (PDF), the scattering angle Θ is determined by choosing a random sample from $p(\cos \Theta)$ PDF:

$$P(\cos\Theta) = \frac{p(\cos\Theta)d\Omega}{4\pi},\tag{15}$$

where P is the probability of light being scattered into a cone with solid angle $d\Omega$ in the direction Θ from the incident radiation given the phase function.

Then the new direction vector is determined from Θ (Jacques, 2010):

$$\mu_{x} = \frac{\sin\Theta\left(\mu_{x_{0}}\mu_{z_{0}}\cos\phi - \mu_{y_{0}}\sin\phi\right)}{\sqrt{1 - \mu_{z_{0}}^{2}}} + \mu_{x_{0}}\cos\Theta$$

$$\mu_{y} = \frac{\sin\Theta\left(\mu_{y_{0}}\mu_{z_{0}}\cos\phi - \mu_{x_{0}}\sin\phi\right)}{\sqrt{1 - \mu_{z_{0}}^{2}}} + \mu_{y_{0}}\cos\Theta,$$

$$\mu_{z} = -\sqrt{1 - \mu_{z_{0}}^{2}}\sin\Theta\cos\phi + \mu_{z_{0}}\cos\Theta$$
(16)

where ϕ is given as a uniform random number between 0 and 2π , the 0 subscript represents the incident direction, and μ_x , μ_y , and μ_z make up the components of the unit direction vector.

Photon energy is depleted over distance s according to the ice absorption coefficient and F_{ice} as determined from the μ CT data instead of using a medium absorption coefficient:

$$E = E_0 \left(e^{-\kappa_{\lambda} s F_{ice}} \right), \tag{17}$$

where E is the new photon energy, and E_0 is the incident photon energy.

To achieve statistical energy conservation, a "Russian Roulette" function is used to determine whether or not to fully absorb (i.e., kill) the photon packet once its energy falls below a prescribed threshold (Iwabuchi, 2006; Jacques, 2010). This is given as:

$$E = \begin{cases} mE & \zeta \le 1/m \\ 0 & \zeta > 1/m \end{cases},\tag{18}$$

where ζ is a random number between 0 and 1, and m is a prescribed constant on the order of 1-10. In essence, the Russian Roulette technique achieves energy conservation by proportionally compensating for the energy removed from the model when photons are killed. By treating absorption continuously rather than probabilistically, the number of photons required to attain a robust solution is significantly reduced, and further ensures stable model integration.

If the z position of a photon-packet is above the top of the snow surface (i.e., it has exited the top of the snowpack), the remaining energy within the packet is added to the total reflected energy and the photon is eliminated. In an open lower-boundary configuration, if a photon-packet z position is less than 0 (i.e., it has exited the bottom of the snowpack) the remaining energy is added to the total transmitted energy, and the photon is eliminated. Alternatively, a lower boundary can be simulated with a specified spectral reflectance such that a portion of the photon energy will be absorbed at the lower boundary, and the remaining energy will be reflected upward. Once all photons have been eliminated from the model, the simulation is complete.

This model is extended to a multilayer configuration by simply defining unique optical properties corresponding to specified depths throughout the snowpack. When a photon packet travels from one layer to another, its trajectory and energy depletion are determined by the optical properties of the new layer. The basic premise of this model is illustrated in figure 2, which traces the position and energy of two photons on a 2D plane as they travel throughout an idealized two-layer 20 cm deep snowpack.

2.3 Directional Conic Reflectance Function

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The reflectance of a surface is often described using the concept of a BRDF (e.g., Stamnes and Stamnes, 2016). The BRDF represents the directional PDF of reflectance for a ray of light impacting the surface from a specified incident direction. To estimate the BRDF from this model, we follow the methods described in Kaempfer et al. (2007), which approximates the BRDF using the Directional Conic Reflectance Function. The DCRF is a discritized BRDF that computes the energy reflected into a cone in the direction: θ_r , ϕ_r subtended by solid angle $d\Omega$:

$$DCRF(\theta_i, \phi_i, \theta_r, \phi_r) = \frac{I_r(\theta_r, \phi_r)}{I_i(\theta_i, \phi_i)\cos\theta_i d\Omega},\tag{19}$$

where I is the radiative flux, and the subscripts i, and r correspond to the incident and reflected radiation, respectively.

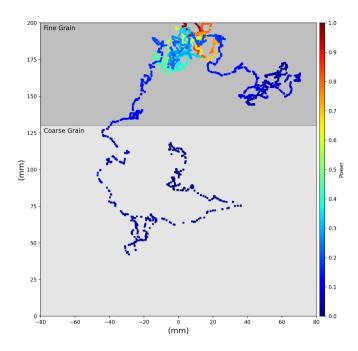


Figure 2. x/z cross section of two photons within a multi-layered snowpack 20 cm deep. The color scale indicates the fractional energy of the photon packet. The background shading indicates the layers of the snowpack.

2.4 Snow sampling and spectroradiometer measurements in the field

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To evaluate the model, we collected snow samples and spectral reflectance measurements of the snow surface at Union Village Dam (UVD) in Thetford, Vermont several times throughout the 2020-21 winter. The UVD site is a broad flat clearing surrounded by deciduous forests spanning approximately 40000 m², and bounded on the southern end by the Ompompanoosuc River. During each data collection, a snow pit was excavated and standard snow characteristics, such as snow depth, density, and grain size were measured manually. Several snow samples were carefully extracted at several depths spanning the height of the snow cover in columns adjacent to the snow pit sidewalls in cylindrical containers 7 cm high x 1.9 cm in diameter, with a 1-2 cm overlap in the depth of each sample. Three replicate samples, spaced laterally < 10 cm from one another, at each depth were collected. The specific samples used in this analysis were taken from the surface, 0-7 cm, in the case of the fine grain sample, and from 14-19 cm depth in the case of the coarse grain sample. These samples were transported in a hard, plastic cooler for 10 miles from the UVD site to the Cold Regions Research and Engineering Laboratory (CRREL). The fine grain sample was imaged 18 days after snow sampling, while the coarse grain sample was imaged 53 days after snow sampling. All samples were stored at -30 °C to limit metamorphic change in the intervening timeframe. These samples were not casted (i.e. not preserved using a pore-filler).

Spectral reflectance data were collected using a Malvern Panalytical ASD FieldSpec 4 Hi-Res: High Resolution Spectroradiometer. The FieldSpec 4 has a spectral range of 350-2500 nm and a spectral resolution of 3 nm in the visible and 10 nm in the SWIR. The data collection was performed within 1.5 hours of solar noon in order to limit high zenith angle impacts. The FieldSpec 4 requires optimization, which adjusts and improves the detector sensitivities for the probe and light source currently in use. An optimization was conducted prior to the start of data collection and any time lighting conditions changed in order to ensure accurate reflectance readings. Data collections were taken 2.5 to 3 feet above the snow surface at nadir using a 5 degree field of view optic lens, resulting in a measurement footprint diameter of approximately 6 cm. The collection strategy employed included taking a white reference reading from a pure reflective panel and five readings at different locations on the target surface; the mean of the five readings was used as the reflectance value for that specific location.

In this paper, we focus specifically on data collected on 12 February, 2021 as this day had the most stable ambient lighting conditions and resulted in the majority of our snow and reflectance measurements. At the time of the measurements the sky was covered with a high optically thick overcast, and as a result the ambient lighting conditions were generally diffuse. The snow was dry and approximately 34 cm deep, and was roughly characterized as a layer of relatively fresh snow approximately 10 cm deep overlying a layer comprised of larger mixed refrozen snow grain clusters and facets, separated by a 1 cm thick ice crust. We performed an initial evaluation of the model against measurements to focus on the effect of shallow snow on the spectral albedo.

To measure the effects of a shallow snowpack, a 16"x16" aluminum panel painted black was inserted horizontally into the snowpack through the snow pit sidewall at three depths (10 cm, 4.5 cm, and 2.5 cm) with care as not to damage the smooth snow surface (e.g., Fig. 3). This panel was strongly absorptive in the visible and NIR spectrum with a constant reflectance of approximately 4 % throughout the entire 350 - 2500 nm range. Since there was no appreciable difference between the measured spectral albedo of the virgin snow (i.e., no inserted panel) and the panel inserted at 10 cm, we limit our analysis to the 4.5 and 2.5 cm panel depths.

2.5 μ CT sampling and Mesh Generation

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These snow samples were characterized at the microscale with a cold-hardened Bruker Skyscan 1173 μ CT scanner housed in a -10 °C cold room equipped with a Hamamatsu 130/300 tungsten X-ray source, which produces a fixed conical, polychromatic beam with a spot size of <5 μ m and a flat panel sensor camera detector. Each sample was scanned with 38 kV X-rays at 196 mA and a nominal resolution of approximately 20 μ m as the sample was rotated 180° in 0.6° steps with an exposure time of 300-350 ms. Based on estimates of the minimum grain size from manual field measurements, the resolution of the μ CT, at 20 μ m, is roughly on the order of 10 times the linear size of the minimum grain size we were imaging. We used the commonly employed Nyquist sampling criterion, which requires a minimum of 2.3 pixels per linear feature, to determine that the resolution was sufficient for the grain sizes we sampled. X-rays were detected using a 5 Mp (2240 x 2240) flat panel sensor utilizing 2 x 2 binning, and projection radiographs were averaged over four frames. The resulting 1120 x 1120 pixel radiographs were then reconstructed into 2D gray-scale horizontal slices using NRecon software (Bruker), which utilizes a modified Feldkamp cone-beam algorithm to produce a vertical stack of gray-scale cross-section images. Image reconstruction processing included



Figure 3. Photograph of the black aluminum panel inserted into the snow pit sidewall approximately 2.5 cm from the surface.

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sample-specific post alignment, Gaussian smoothing using a kernel size of 2 to reduce noise, sample-specific ring artifact correction of dead pixels, beam hardening correction, and X-ray source thermal drift correction. A cylindrical volume of interest with a diameter of 1.6 cm was selected from the scanned samples in order to eliminate edge effects caused by the sampling process.

Resulting grayscale images are segmented into two phases: air (lowest X-ray absorption), and snow (highest X-ray absorption). Segmenting thresholds for each phase are determined by finding the local minimum between peaks on the histogram showing all grayscale values, and using that value as a global threshold for each scanned sample. The resulting binarized data are despeckled so that any objects less than 2 pixels in diameter were removed.

The final binarized images are then used to construct 3D representations of dry snow samples for input into the RTM. This is accomplished through the use of open-source image processing and 3D visualization software packages accessed through Python (Schroeder et al., 2004; Van der Walt et al., 2014; Sullivan and Kaszynski, 2019).

To build a full sample mesh, a contour-based surface reconstruction process was developed to generate snow surfaces from the voxels that make up the snow sample. This method uses a subset of the binary sample array, including both snow and adjacent air voxels. The subset array is then refined to increase the resolution. A Gaussian filter is applied to smooth the refined array, diminishing pixelated appearance of the voxelized snow-air interface, producing a smooth level set from which to extract the snow surface. The smoothed level set is then used to define an isosurface at the snow-air boundary, providing control over where the boundary is drawn with respect to the voxels.

Finally, to extract the isosurface from the 3D voxel array, we apply the Marching Cubes method. This algorithm iterates through defined cubes (i.e. voxels) and determines, through knowledge of the pixel values at the cube vertices, if the isosurface intersects that cube. If so, it creates triangular patches via a lookup table that are eventually connected to form the isosurface boundary. The original algorithm presented by Lorensen and Cline (1987) can lead to cracks and over the years has been improved by many (Nielson and Hamann, 1991; Scopigno, 1994; Natarajan, 1994; Chernyaev, 1995; Lewiner et al., 2003). For this work, we used the adaptation implemented by Lewiner et al. (2003), which improved the algorithm to resolve face and internal ambiguities, extended the lookup table, and guaranteed correct topology. As a final step, each grain is "repaired" to remove any defects and degenerate elements and ensure a manifold surface according to Attene (2010), and then decimated to reduce the overall number of triangles that comprise the surface thereby lowering the computational requirements. Overall, this method appears to accurately characterize the snow within the μ CT sample with computed mesh snow sample densities within 1.5% of snow densities computed from the raw voxels. Figure 4 shows a 2D cross section comparing air/ice boundaries to the raw pixels of the image and selected example 3D rendered samples are shown in Figure 5.

3 Results

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3.1 General Evaluation

An initial evaluation of the model is performed by simulating the spectral albedo for two idealized 60 cm deep snowpacks with uniform optical properties throughout. For these snowpacks, the optical properties are determined from 3D meshes generated by two characteristically distinct μ CT samples. One mesh is representative of fresh, fine-grained snow near the surface, and the other of large facets near the bottom of the snowpack (Fig. 6). For each mesh, the total mesh volume is approximately 800 mm³. Additional physical and optical properties of each mesh are presented in Table 1. For each sample, the spectral albedo is computed for wavelengths between 400-1600 nm at 20 nm intervals with diffuse incident radiation. This comparison demonstrates that the model capably reproduces a known behavior of spectral albedo, namely the strong sensitivity of NIR albedo to snow microstructure (Fig. 7a). The spectral albedo is relatively uniform between the two snowpacks for the spectral range between 400 and 800 nm, and then the albedos diverge, with a more rapid decrease in albedo for the coarser-grained snow.

We then assess the dependence of simulated spectral albedo on incident zenith angle for the fine grain snow sample at four different wavelengths to evaluate the model's ability to simulate anisotropy in the surface reflectance (Fig. 7b). This analysis shows an exponential increase in albedo at high zenith angles that is most pronounced in the NIR, consistent with the results

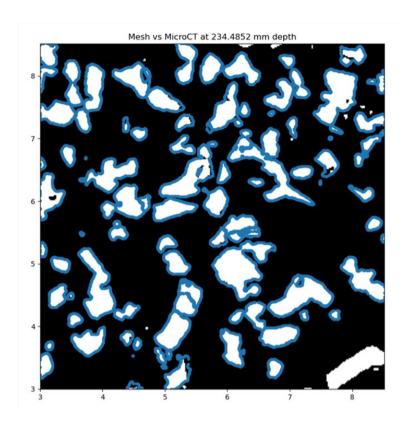


Figure 4. 2D Cross-sectional slice of a binarized μ CT scan with corresponding mesh boundaries superimposed shown as the blue lines.

Table 1. Physical and optical properties of the fine grain and coarse grain mesh samples. Note that SSA and ρ_s are computed directly from the μ CT sample.

Property	Fine Grain	Coarse Grain	
$SSA (m^2 kg^{-1})$	18.4	12.9	
$\rho_s (\mathrm{kg} \; \mathrm{m}^{-3})$	286.99	282.4	
$\gamma_{ext}~(\mathrm{mm}^{-1})$	2.22	1.65	
F_{ice}	0.48	0.49	
B	1.55	1.48	

from previous studies that compare snow albedo and zenith angle (e.g., Li and Zhou, 2003; Kokhanovsky and Zege, 2004; Xiong et al., 2015). As a related evaluation, the model-simulated DCRF is computed as a function of zenith angle (Fig. 8). This analysis reveals that the reflectance is mostly isotropic for zenith angles less than approximately 55° at which point the surface becomes increasingly forward scattering, consistent with previous observational and modeling studies (Aoki et al., 2000; Hudson et al., 2006; Kaempfer et al., 2007; Dumont et al., 2010; Xiong et al., 2015; Jiao et al., 2019).

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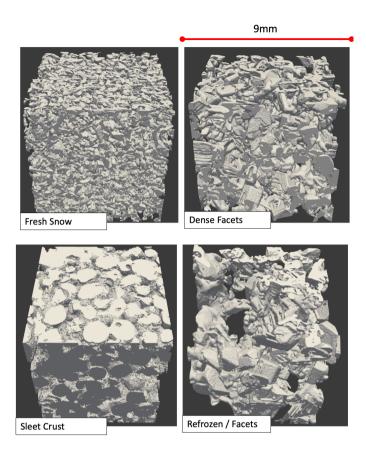


Figure 5. Example 3D renderings of selected μ CT sample representing different types.

Finally, we use the model to provide an initial assessment of the impacts of snow microstructure on simulated spectral transmittance at specified depths within a homogenous snowpack. To accomplish this, the optical properties of the μ CT samples in Fig. 6 are used to simulate and compare the spectral transmittance at varying depths (Fig. 9). The transmittance is highest at the short, non-absorptive, wavelengths and gradually decreases throughout the NIR, broadly matching quantitative snow transmittance results reported in Perovich (2007) and Libois et al. (2013). The depth of the 5% transmittance contour for the fine grain snow sample is approximately 6 cm for the visible, and decreases to approximately 2 cm for the NIR (Fig. 9a), indicating that the fine grain snow penetration length is on the order of only a few centimeters. In contrast, the transmittance for the coarse grain snow is greater near the surface, and the depth of the 5% contour correspondingly increases to 12.5 cm for the visible and 5 cm for the NIR (Fig. 9b).

3.2 Evaluation against UVD Data

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To evaluate the model's ability to simulate the effect of the underlying surface on snow spectral albedo for shallow snow, optical properties used in the plane-parallel model were determined from four approximately 800 mm³ μ CT samples, with

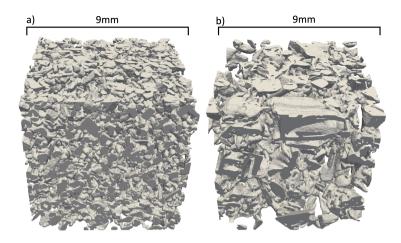


Figure 6. 3D renderings of mesh samples used to generate the optical properties for the general evaluation and snow transmittance comparisons. a) Fine grain sample, and b) Coarse grain sample.

Table 2. Physical and simulated optical properties of the top 8 cm of snow measured at the UVD site on 12 February, 2021. SSA and ρ_s are computed directly from the μ CT sample. Note that the depths correspond to the RTM model depths for the virgin snow calculation.

depth [cm]	$SSA (m^2 kg^{-1})$	$\rho_s (\mathrm{kg \ m}^{-3})$	$\gamma_{ext}~(\mathrm{mm}^{-1})$	F_{ice}	B
1 (32-34)	26.1	147	1.41	0.32	1.89
2 (30-32)	27.2	178	1.85	0.34	1.64
3 (28-30)	21.1	250	2.30	0.44	1.52
4 (0-28)	18.4	287	2.22	0.48	1.55

each sample representing a 2 cm thick layer within the top 8 cm of the snowpack. The RTM is then configured with 4 layers according to these optical properties (given in Table 2). The top three layers are each 2 cm thick, and the bottom layer is 28 cm thick, such that the entire snow depth amounted to 34 cm. We chose this configuration in accordance with the hypothesis that the snow microstructure below 8 cm had little impact on the measured surface spectral albedo. To simulate the panels, the snowpack depth is modified to be 4.75 and 2.5 cm deep with a lower boundary consistent with the spectral reflectively of the black panel (Table 2).

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There is generally good agreement between the observations and the model (Fig. 10) and in particular, the model accurately simulates the impact of the inserted panel on the surface albedo for wavelengths shorter than 1000 nm for both the 4.5 and 2.5 cm depths. The model spectral albedo decreases more rapidly with wavelength in the 800 - 1000 nm region, particularly for the virgin snow sample. This leads to a slight underestimate in albedo in the NIR range for wavelengths shorter than 1400 nm, beyond which there is a slight overestimate. However, for wavelengths longer than 1400 nm, differences between the model

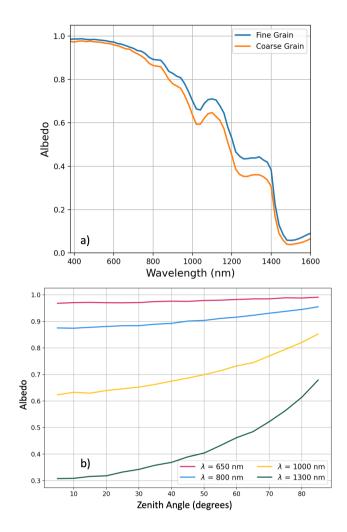


Figure 7. a) Simulated spectral albedo for fine grain and coarse grain snow samples for 100% diffuse radiation. b) Simulated spectral albedo as a function of incident zenith angle for selected wavelengths. Note that both simulations were run with 25000 photons for a snow depth of 60 cm.

and observations may be due to the limitation of the geometric optics approximation as the approximate particle size parameter is < 1000 for $\lambda > 1400$ nm.

3.3 Snow optical and physical properties

The model can also be leveraged to assess the relationship between common snow physical properties and the simulated optical properties from this framework. To demonstrate this, we compare snow specific surface area (SSA) and snow sample density (ρ_s) to γ_{ext} and F_{ice} . This analysis is performed by generating optical properties from several μ CT sample volumes collected

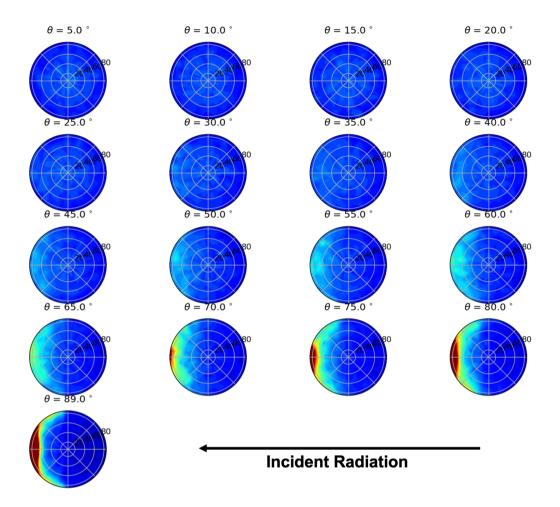


Figure 8. Polar plots of DCRF at 1000 nm for incident zenith angles ranging from $5 - 89^{\circ}$. Reflected azimuthal direction is on the theta axis, and reflected zenith angle is on the r axis. Color scale ranges from 0-1.5.

on different dates and locations during the 2020-2021 winter season, spanning a wide range of snow types. Note that each μ CT sample is approximately 800 mm³ and the sample SSA and ρ_s are determined from the μ CT 3D rendering.

This analysis reveals that F_{ice} has a very robust relationship with snow density (Fig. 11a) described by the linear fit:

$$F_{ice} = 0.0008\rho_s + 0.22, (20)$$

with $r^2 = 0.92$. In Figure 11b, γ_{ext} is compared to the product of ρ_s and SSA, to match the analytical formula described in Kokhanovsky and Zege (2004). The results show a clear linear relationship fit to:

$$\gamma_{ext} = 0.092 + 0.4\rho_s SSA, \tag{21}$$

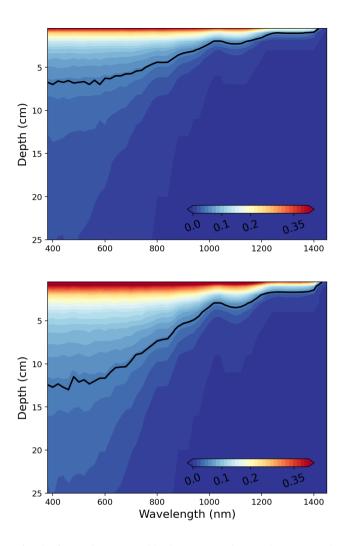


Figure 9. Simulated transmittance of a) the fine grain snow, and b) the coarse grain samples contoured as a function of depth and wavelength. Solid black lines mark the depth of the 5 % transmittance contour.

with $r^2 = 0.73$.

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The estimated B parameter is distributed normally around a mean of 1.49, consistent with the results reported in Libois et al. (2014). We note that there is no significant relationship between B and snow grain form or size, however there is a general tendency for B to be highest for samples with higher SSA and smaller rounded grains consistent with Kokhanovsky and Zege (2004) and Libois et al. (2014).

To further assess how these two specific snow optical properties, γ_{ext} and F_{ice} , affect the greater simulated spectral transmittance, we perform a sensitivity analysis by comparing the 5% transmittance contour depth for three fractional ice paths:

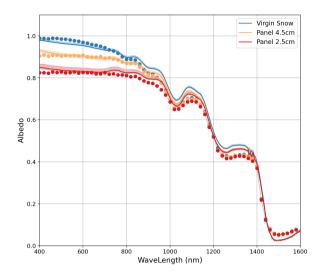


Figure 10. Simulated and observed spectral albedo for three different snow depths. The solid lines indicate observations and dotted lines indicate simulations. The shading around the observations indicates the inter-quartile range of the measurements computed from the five snow and two reference scans collected during each measurement, providing an assessment of measurement uncertainty. The mean RMSE of the simulated albedo compared to measurement-derived albedo over 400-1600 nm is equal to 0.04

0.31, 0.47, 0.75 at two fixed γ_{ext} values: 2.65, 0.91 mm⁻¹. The two γ_{ext} values correspond to the max, min values found in the previous analysis and presented in Fig. 12b. The three F_{ice} values correspond to the max, min, and mean values (Fig. 12a). We compare the influence of F_{ice} at both the max and min γ_{ext} values, since we anticipate the strength of its influence will vary according to γ_{ext} . We note that high values of γ_{ext} are more likely to coincide with high values of F_{ice} due to the shared dependence of these variables on snow density in most snowpacks.

The results of this analysis indicate that both γ_{ext} and F_{ice} impact snow transmittance in accordance with relationships discussed in Libois et al. (2013). Specifically, the factor of 3 decrease in the extinction coefficient corresponds to a factor of 3 increase in depth of the 5 % transmittance contour, consistent with a linear relationship between γ_{ext} and penetration depth (L). Additionally, the simulated factor-increase in penetration depth is approximately the square root of the factor increase in F_{ice} , for $\lambda > 600$ nm, consistent with the $L \approx \sqrt{B * \kappa_{abs}}$ presented in Libois et al. (2013).

4 Discussion

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Overall, this framework shows promise as a research tool for better understanding visible and NIR snow radiative transfer through snowpacks with irregularly shaped and arranged grains. However, there are numerous uncertainties in this framework that should be addressed in future work to better understand its capabilities and limitations.

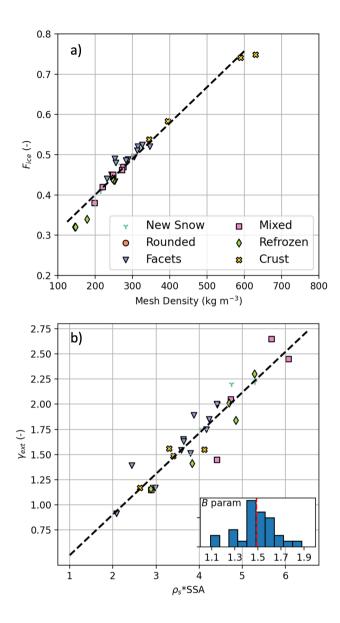


Figure 11. Optical properties for λ =1000 nm computed from μ CT photon-tracking compared against sample physical properties. a) F_{ice} vs. ρ_s and b) γ_{ext} vs. SSA* ρ_s . Linear regression lines are shown in black dashed lines. Marker shapes and colors are indicative of the observed grain forms determined through visual assessment during snow pit analysis. Note that in panel (b) a histogram of the estimated B parameters for all of the μ CT samples is shown, inset. $B_{mean}=1.49$ is shown as the vertical red line.

For example, foundational work on light scattering in a collection of weakly absorbing particles indicates that, ignoring diffraction, γ_{ext} is given as $\gamma_{ext} = \rho_s SSA/4$ (e.g., Van De Hulst, 1957; Kokhanovsky and Zege, 2004). In this work, we find γ_{ext} to be related to $\rho_s SSA$ by a factor of approximately 2/5, rather than 1/4 (eq. 21). We speculate that this is because the

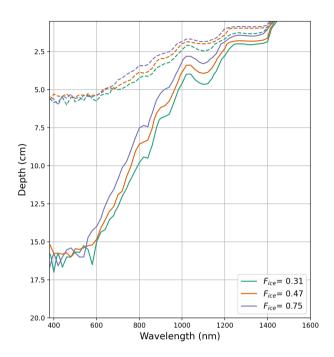


Figure 12. Depth of simulated 5% transmittance contour as as a function of wavelength for varying F_{ice} at two extinction coefficient: $\gamma_{ext} = 0.91$ (Solid lines) and $\gamma_{ext} = 2.65$ (Dashed lines).

method for determining γ_{ext} described in Xiong et al. (2015) and extended into three-dimensions here, initializes photons randomly throughout the sample, which relaxes the assumptions regarding particle projected area implicit within the γ_{ext} = $\rho_s SSA/4$ relationship. To explore this, we performed a test in which we computed γ_{ext} for artificial snow samples comprised of rendered spheres generated with specified ρ_s and SSA (not shown). The results of this test were in broad agreement with the 2/5 factor, and more similar to results presented in Xiong et al. (2015), supporting this hypothesis. However, more work should be performed in the future to better understand this discrepancy.

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One possible significant source of uncertainty in this framework is the assumption that the optical properties computed from volume μ CT samples on the order of 1 cm³ are homogeneous laterally, and can be extrapolated to characterize representative layer depths. To elucidate upon this uncertainty, we compare the optical and physical properties of the 20 rendered μ CT samples collected at UVD on 12 February 2021 to the observed snow pit stratigraphy (Fig. 13).

Here we show that the top layer of the snowpack has more homogeneous physical and optical properties than the buried layers. In particular there is substantial variability in γ_{ext} and F_{ice} within the rounded grains and the upper-most facet layers. Further investigation into this variability in the facet layer spanning the 14-18 cm layer reveals that this variability is caused largely by the fact that some μ CT samples within this layer contained unusually large pore spaces, which caused lower SSA and

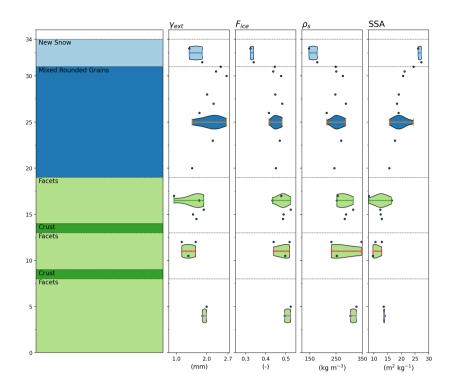


Figure 13. Snow pit stratigraphy (right) compared against γ_{ext} , F_{ice} , ρ_s , and SSA. Violin plots show estimated probability distributions for each observer-identified snow layer according to the samples collected with the layer.

 γ_{ext} values. We suspect that this variability has limited impacts on the simulated spectral albedo for the simulations focused on shallow snow, since the top most snow layer is relatively homogeneous. However, this variability is likely to have more significant impacts for simulations focused on older snowpacks with larger and less uniformly distributed snow grains.

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Similar to several previous studies (Carmagnola et al., 2013; Dumont et al., 2021), we found model discrepancies to be greater in the NIR, underestimating albedo between 800 and 1400 nm, and overestimating above 1400 nm. This could, in part, be due to the observations as the lighting conditions were not ideal. An additional potential source of uncertainty in the model are the ice refractive indices, which we have taken to be constant. For example, Carmagnola et al. (2013) attributed their discrepancies to their choice of ice refractive index, with varying values reported in the literature.

Ideally, the optical properties used in the model should vary slightly with wavelength as there are minor spectral variations in γ_{ext} and $p(\cos\Theta)$. We chose to leave the optical properties independent of wavelength to reduce the computational burden of running the photon-tracking model for several wavelengths. Cursory sensitivity tests performed to assess the impact of this choice on the optical properties supported the use of wavelength-independent optical properties, as both $p(\cos\Theta)$ and γ_{ext} exhibited generally a negligible dependence on wavelength for $\lambda > 1400$ nm (not shown), and we anticipate that source of uncertainty is small relative to the sources discussed above.

5 Conclusions

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In this work we have presented a blended photon-tracking radiative transfer model in an effort to better understand the complicated influence of snowpack microstructure on snow spectral transmittance in the geometric optics limit. A primary goal of this modeling approach is to expand upon previous approaches aimed at incorporating 3D renderings of real snow microstructure into radiative transfer models for snowpacks of arbitrary depth, while maintaining the Monte Carlo aspects of the model. To accomplish this, existing methods for simulated photon interactions with rendered elements are employed to determine key optical properties of the snow (Grundy et al., 2000; Kaempfer et al., 2007; Xiong et al., 2015).

An evaluation of this framework for consistency with known behavior of spectral snow albedo revealed that this framework can successfully reproduce the dependency of spectral albedo and grain size, as well as the surface anisotropy at high incident zenith angles, found in previous studies. Furthermore, an initial comparison of the simulated snow albedo against albedo measured in the field over snow with varying depths indicates that the model can simulate the effects of an underlying surface on spectral albedo with sufficient accuracy.

In comparing two different snow samples, it was revealed that snow microstructure has a large impact on snow transmittance in the visible spectrum and near the snow surface, increasing the 5 % transmittance depth at 400 - 650 nm from approximately 6 cm for a fine grain snow sample to 12.5 cm depth for a coarse grain sample. These values and the ability to further constrain the transmittance depths of shallow snowpacks will allow for improved capabilities for determining the visibility of subnivean hazards. A brief sensitivity analysis of the optical properties revealed that lowering the medium extinction coefficient acted to increase the transmittance depth in the visible bands, while the fractional ice path (F_{ice}) impacted the rate at which albedo and transmittance decreased as a function of wavelength in the NIR.

Overall, while current efforts are focused on using this model to better understand snow transmittance, it shows promise as a broadly applicable snow RTM that has a strong direct connection to μ CT snow samples. While currently it is limited to the geometric optics approximation for clean snow and unpolarized radiation, ongoing and anticipated future efforts are aimed at improving the grain segmentation and rendering process, incorporating polarization, parameterizing diffraction, and including light absorbing particulates (LAPs). In particular, recent multiphase image segmentation techniques (West et al., 2018; Hagenmuller et al., 2019) could be used to better separate snow, air, and LAPs in a μ CT sample allowing for the impact of LAPs to be determined through ray-tracing. Furthermore, because the model operates entirely as a photon-tracking model, it is a natural fit with macroscale ray-tracing and therefore could be used to investigate the reflectance of rough snow surfaces such as sun cups or sastrugi.

Code and data availability. The mesh generation and RTM code with associated documentation is available in preliminary 'as is' format on Github at (lhttps://github.com/wxted/CRREL-GOSRT.git). Sample data files used to generate figure 9a is available on Github as sample data. Additional limited sample data, including rendered microCT meshes, and spectroradiometer data used for this paper are available upon request.

Author contributions. Theodore Letcher performed a majority of the model physics, structural development, and coding, in addition to coordinating the model analysis and manuscript preparation. Julie Parno led research and coding efforts related to the 3D mesh generation and rendering and assisted in general coding, she also coordinated a majority of the fieldwork activity. Zoe Courville provided research support, participated in snow sampling and coordinated μ CT analysis. Lauren Farnsworth performed a large portion of μ CT scans and a majority of the μ CT image post processing and analysis. Jason Olivier participated in fieldwork and provided background on the ASD instrumentation and sampling for the manuscript. Theodore, Julie, and Jason performed the RTM simulations and assisted in code debugging. All authors provided writing support for the manuscript.

Competing interests. The authors declare that no competing interests are present

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