Review Article: Global Monitoring of Snow Water Equivalent using High Frequency Radar Remote Sensing

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Abstract. Seasonal snow cover is the largest single component of the cryosphere in areal extent, covering an average of 46 million square km of Earth's surface (31% of the land area) each year, and is thus an important expression of, and driver, of the Earth's climate. In recent years, Northern Hemisphere spring snow cover has been declining at about the same rate (~ -13%/decade) as Arctic summer sea ice. More than one-sixth of the world's population relies on seasonal snowpack and glaciers for a water supply that is likely to decrease this century. Snow is also a critical component of Earth's cold regions' ecosystems, in which wildlife, vegetation, and snow are strongly interconnected. Snow water equivalent (SWE) describes the quantity of water stored as snow on the land surface, and is of fundamental importance to water, energy, and geochemical cycles. Quality global SWE estimates are lacking. Given the vast seasonal extent combined with the spatially variable nature of snow distribution at regional and local scales, surface observations are not able to provide sufficient SWE information. Satellite

observations presently cannot provide SWE information at the spatial and temporal resolutions required to address science and high socio-economic value applications such as water resource management and streamflow forecasting. In this paper, we review the potential contribution of X- and Ku-Band Synthetic Aperture Radar (SAR) for global monitoring of SWE. SAR can image the surface during both day and night regardless of cloud cover, allowing high-frequency revisit at high spatial resolution as demonstrated by missions such as Sentinel-1. The physical basis for estimating SWE from X- and Ku-band radar measurements at local scales is volume scattering by millimetre-scale snow grains. Inference of global snow properties from SAR requires an interdisciplinary approach based on field observations of snow microstructure, physical snow modelling, electromagnetic theory, and retrieval strategies over a range of scales. New field measurement capabilities have enabled significant advances in understanding snow microstructure such as grain size, density, and layering. We describe radar interactions with snow-covered landscapes, the small but rapidly growing number of field datasets used to evaluate retrieval algorithms, the characterization of snowpack properties using radar measurements, and the refinement of retrieval algorithms via synergy with other microwave remote sensing approaches. This review serves to inform the broader snow research, monitoring, and applications communities on progress made in recent decades, and sets the stage for a new era in SWE remote-sensing from SAR measurements.

1 Introduction

Seasonal snow on land is responsible for a number of important processes and feedbacks that affect the global climate system, freshwater availability to billions of people, biogeochemical activity including exchanges of carbon dioxide and trace gases, and ecosystem services. Despite this importance, snow mass (commonly expressed as the 'snow water equivalent' or SWE) is a poorly observed component of the global water cycle. Given the vast area of northern hemisphere snow extent (exceeding 45×10^6 km^2 each winter), surface observing networks are insufficient as a sole source of information for snow monitoring. Satellite remote sensing is the only means to monitor SWE consistently and continuously at continental scales. Optical satellite imagery acquired under cloud-free conditions can provide information on where and when snow is on the ground, but does not support the retrieval of SWE. Long time series of snow mass information are available from satellite passive microwave measurements (Luojus et al., 2021), but at coarse spatial resolution (gridded at 25 km spatial resolution), mountain areas across which high values of SWE occur are excluded, and bias correction is required under deep snow conditions (>150 mm SWE; Pulliainen et al., 2020). Land surface models driven by meteorology from atmospheric reanalysis can produce hemispheric-scale SWE information at coarse spatial resolutions (e.g. Kim et al., 2021), but there is a large spread between products due to differences in the meteorological forcing data (especially precipitation) and a pronounced negative bias in mountain areas (Wrzesien et al., 2019a; Cao and Barros, 2020; Lundquist et al., 2019). Differential airborne and ground-based lidar altimetry (Deems et al., 2013; Meyer et al., 2021) and spaceborne stereo photogrammetry (Deschamps-Berger et al., 2020) can provide snow depth information at high resolution by differencing repeat digital elevation models but are limited to small spatial domains and sparse temporal sampling. C-band radar has recently been applied to retrieve snow depth in mountainous regions

70 (Lievens et al., 2019) using empirical relationships derived from ground-based measurements; however, this approach is not demonstrated for the comparatively shallow snowpack found across large regions of the northern hemisphere. Airborne and tower-based measurements have also identified the possibility of retrieving snow parameters from L-band interferometric SAR (Deeb et al., 2011), P-band signals of opportunity (Shah et al., 2017; Yueh et al., 2021), wideband auto-correlation radiometry (Mousavi et al., 2019), and FM-CW radar (Yan et al., 2017).

75 Ku- and X-band radar measurements, in contrast, provide a viable pathway to produce SWE information at the temporal and spatial scales necessary to advance operational environmental prediction, climate monitoring, and water resource management across the northern hemisphere (see Section 2 for an overview of the scientific requirements for snow mass information). Significant progress was made over the past decade in understanding the Ku-band and X-band radar response to variations in SWE, snow microstructure, and snow wet/dry state. The ESA Cold Regions Hydrology High-Resolution Observatory

80 (CoReH2O) mission (dual-frequency X- and Ku-band; completed Phase A at ESA in 2013; ESA, 2012; Rott et al., 2010) was a major impetus.The potential for Ku-band radar was previously explored at NASA as part of the Snow and Cold Land Processes Mission and supporting Cold Land Processes Experiment (Yueh et al., 2009). Experimental tower and airborne measurements have been used to advance understanding of the physics of backscatter response to snow microstructure and SWE (Lemmetyinen et al., 2018; King et al., 2018), including the complicating effects of forest cover (Montmoli et al., 2016;

85 Cohen et al., 2015). Innovative new field measurement of snow microstructure parameters (Löwe et al., 2013; Kinar and Pomeroy 2015) now provide the quantitative observational basis for radar modelling of layered snowpacks (Tsang et al., 2018) and radar retrieval algorithms (Zhu et al., 2018). Radar forward models and potential algorithm approaches have matured over the past decade, which has allowed new retrieval pathways to emerge which build on approaches first proposed for CoReH2O. The purpose of this review is to summarize the status of all the components necessary to fully develop the scientific readiness

90 for a potential future radar mission focused on seasonal snow mass. This includes the theoretical sensitivity to SWE via volume scattering processes includingthe influence of surface and ground contributions (Section 3), and approaches to SWE retrieval as supported by physical snow and radiative transfer modelling (Section 4). Results from previous ground, tower, and airborne measurement campaigns are also reviewed. The sensitivity of Ku-band SAR measurements to SWE are limited to a threshold of approximately 150 mm (about 1 meter of snow depth depending on density) because of saturation of radar volume scattering.

95 Thus, synergy with C-band Sentinel 1 data for snow depths beyond 1 meter (Lievens et al., 2019) is also explored. Other synergies with interferometric SAR, radar tomography, passive microwave, and L- and C- band SAR measurements are also described to provide ancillary information and to improve retrieval performance (Section 5).

2 Scientific Objectives of Global Remote Sensing of SWE and Spatial and Temporal Requirements

High priority science objectives require snow mass information at moderate spatial resolution (250-500m) and frequent revisit

100 (~3-5 days; ESA, 2012; Derksen et al., 2021), a measurement paradigm that is currently not available. As outlined below, these science requirements support applications related to climate services and operational environmental prediction including

quantifying snow mass contributions to water, energy, and geochemical cycles, better prediction of spring flooding, and adaptation of cold-regions water resources to climate change.

    1.   Inventory how much water is stored as seasonal snow, and how it varies in space and time.

105   The amount, distribution, and variability of terrestrial SWE across the northern hemisphere is poorly quantified because surface networks are inadequate, and existing gridded SWE datasets have divergent climatologies (Wrzesien et al., 2019a) and anomalies (Mudryk et al., 2015). Alpine regions are particularly problematic because the course spatial resolution of existing products (typically 25 km grid spacing or more, with some new analyses available at 9 km) is incompatible with the scale of SWE variability (<100 metres, e.g. Grünewald et al., 2010). SWE estimates derived from models at continental scale are

110   subject to uncertainties in both meteorologic forcing data and model parameterizations (e.g. Kim et al., 2021). SWE is highly sensitive to changing temperature and precipitation in a warming climate; confident projections of resultant changes are uncertain because we lack baseline SWE estimates. SWE can change rapidly from day to day and across local areas due to the influence of individual weather events, but we currently do not have any means to track these changes with sufficient spatial or temporal resolution. The lack of a baseline snow inventory negatively impacts many aspects of hydrological resource

115   management. With projections of continued climate warming and shifts to snow cover resources (including precipitation phase changes and timing of spring melt), addressing this capability is more pressing than ever.

    2.   Properly initialize snow in environmental prediction systems including numerical weather prediction (NWP) and streamflow forecasting.

Land surface data assimilation is an important component of state-of-the-art environmental prediction systems.The

120   initialization of land surface conditions (such as snow, soil moisture and temperature) is a requirement for numerical weather prediction and other forecasting systems such as streamflow prediction. Satellite data from the SMOS and SMAP missions are presently assimilated to improve soil moisture initial conditions (e.g. Carrera et al., 2019). Parallel activities have not been sustained for seasonal snow because assimilation of existing satellite measurements does not sufficiently improve land surface model performance (de Lannoy et al., 2010). Addressing this gap is important because evidence shows that a more realistic

125   initialization of SWE can improve streamflow forecasts, especially during extreme events (Vionnet et al., 2020) and at lead times greater than 2 weeks (Abaza et al., 2020; Wood et al., 2016). The current inability to plan and respond to snow-related runoff events is costly: if effectively managed, runoff from snow melt has a global economic value in the trillions of dollars (Sturm et al., 2017), but also poses a risk through loss and damage associated with flood events. For example, the devastating floods in the Canadian Rockies, foothills and downstream areas of southern Alberta and south eastern British Columbia during

130   June 2013 provides a compelling case for of the need for improved snow information to support hydrological modelling during extreme events (Pomeroy et al, 2016). Additionally, high-resolution satellite-derived SWE can support development of improved downscaling techniques for existing coarsely gridded products (Manickam and Barros, 2020).

    3.   Validate and support improvement of the representations of snow processes and feedbacks in regional and global

135   climate models.

Gridded SWE datasets are required for the verification of models used for seasonal prediction (e.g. Sospedra-Alfonso and Merryfield, 2017), and the validation of historical climate model simulations which underpin climate projections (e.g. Mudryk et al., 2020). Earth observation-derived products make a small contribution to the current suite of available gridded SWE products for climate model analysis: reanalysis and snow models form the primary basis for the evaluation of seasonal prediction and coupled climate model simulations. The first assessment of CMIP6 model simulations by Mudryk et al. (2020) identified two key findings: (1) excessive snow mass at the hemispheric scale is a feature of CMIP6 models, and (2) nearly all models increase snow extent too slowly during the accumulation season and decrease snow extent too slowly during the snowmelt period. These findings would be strengthened through the support of appropriate moderate resolution satellite SWE datasets. Furthermore, more detailed analysis at the grid point scale is needed to effectively link the model parameterizations of the (usually diagnosed) snow cover fraction to the prognostic snow mass.

4. Address the role of snow properties across high latitudes in influencing terrestrial carbon cycling, trace-gas exchanges, and permafrost.

Snow is an important insulator of the underlying soil, influencing the thermal regime and corresponding carbon fluxes in winter (Natali et al., 2019). Permafrost is warming across the northern hemisphere (Biskaborn et al., 2019) with implications on vegetation, surface hydrology, landscapes, and the carbon cycle. Addressing the drivers of these changes requires a sound understanding of the role of seasonal snow, but current snow mass datasets do not meet the requirements of state-of-the-art permafrost models (Obu et al., 2019) which provide continental scale estimates of permafrost extent, thermal state, and active layer thickness.

3 Radar interaction with snow covered landscapes

3.1 Theoretical descriptions of radar-landscape interactions

In this section, we describe volume scattering from a snowpack, rough surface scattering from the snow-soil interface, and the attenuation of radar waves by forest canopies.

3.1.1 Interaction of radar waves with snowpack by the Radiative Transfer Model (RTM)

Microwave signals emitted from a SAR system are scattered by the mm-scale ice grains that make up the snow and at boundaries between snowpack layers with different dielectric properties. The SAR system measures the portion of the signal returned to the sensor (i.e. the backscatter). Because volume scattering increases with snow mass, measurement of backscatter allows estimation of snow mass. Structural changes in snow that impact snow backscatter are densification and metamorphism that introduce vertical heterogeneity in snow grain sizes and snow density, and thus impact snow depth and SWE.

Historically, the first model developed for microwave scattering of snow was by Chang et al. (1976), which assumed Mie scattering from a collection of ice spheres in a single layer to solve a radiative transfer equation for passive remote sensing

applications. The first active remote sensing model (Zuniga et al, 1979) used the Born approximation with snow represented by a random medium characterized by a correlation function and associated correlation length. Since these early models, a variety of radiative-transfer microwave scattering models have been developed with representations of (i) snow microstructure, (ii) absorption coefficient, (iii) effective permittivity, (iv) scattering phase matrices, and (v) layering effects. Analytical and numerical solution methods are used to solve these equations (Tsang et al. (1985), Ulaby et al. (1986), and Fung et al. (2010)). A historical review of different models is given in Shi et al., (2016). Rapid progress has been made recently due to the advancement of high-performance parallel computations and efficient computation methods for characterizing the complex microstructure of snow and full wave solutions of Maxwell's equations (Ding et al., 2010; Xu et al., 2012; Tan et al., 2017; Tsang et al., 2018).

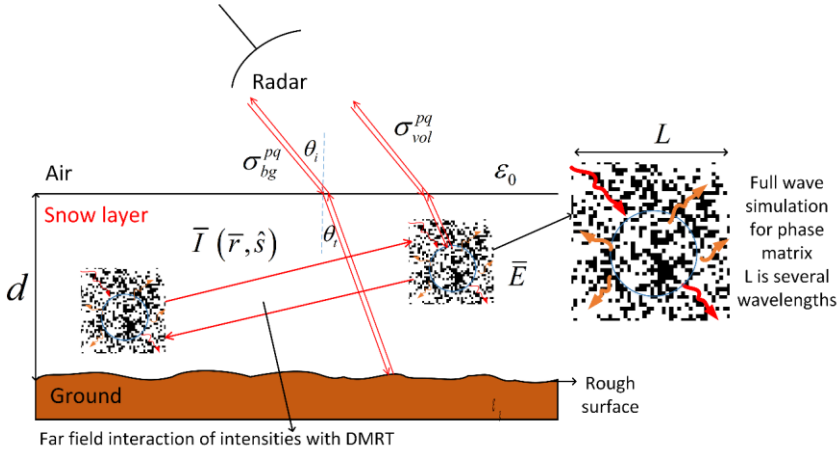



Figure 1: **Main contributions to radar scattering from snow covered ground. Scattering at air/snow interface is neglected, and the snow layer is assumed homogeneous. The snow depth is d. ε_0 is the air permittivity and ε_g is the soil permittivity. θ_i is the incident angle of radar. $\overline{E}(\overline{r})$ is the internal electrical field and $\overline{I}(\overline{r}, \hat{s})$ is the specific intensity within the snowpack.**

Consider an incident wave from the radar at an incident angle θ_i. In the theoretical modelling of volume scattering and surface scattering, the computed solutions of our work are based on all orders of multiple volume scattering, surface scattering, and volume surface interaction. The volume-surface interactions are between the snow volume scattering and the snow/ground interface and the air/snow interface (Chang etal 2014, Tan etal 2015, Tan etal 2017). The full DMRT with boundary conditions are solved to generate the Look-up tables (LUT) for physical based retrieval and for establishing regression formulas of backscattering versus important geophysical variables such as snow water equivalent and scattering albedo. To simplify the explanation of scattering physics, we give a simple physical formula below that expresses the total backscatter σ_{tot}^{pq} from the snowpack over the ground arising from two contributions as shown in Figure 1. The two contributions are i) the volume

scattering component σ_{vol}^{pq} from the snowpack and ii) the rough surface scattering σ_{bg}^{pq} from the underlying soil. The expression is:

190 $\quad \sigma_{tot}^{pq} = \sigma_{vol}^{pq} + \sigma_{bg}^{pq} exp(-2\tau sec\theta_t) + \sigma_{air/snow}^{pq}$ (1)

where p and q refer to the polarization state e.g. σ_{tot}^{HV} represents backscatter emitted at vertical polarization and received at horizontal polarization. Scattering from the underlying rough soil surface is attenuated by the snow layer, represented by the two-way attenuation factor of $exp(-2\tau sec\theta_t)$. The quantity τ is the optical thickness of the snowpack and θ_t is the refraction angle in snow which is related to $\boldsymbol{\theta_i}$, the incident angle in air, by Snell's law Because of the low permittivity contrast between air and snow, the scattering ($\sigma_{air/snow}^{pq}$) from the air/snow interface (Rott et al., 2010) can be neglected except for wet snow .

195 Below we consider the σ_{vol}^{pq} volume scattering term. The rough surface scattering of snow/soil interface, σ_{bg}^{pq} , will be considered in Section 3.1.2.

Multiple volume scattering effects within snow are calculated by the dense medium radiative transfer equation (DMRT). The DMRT is a partially coherent model having coherent interactions and incoherent interactions. The incoherent interactions are

200 based on the classical radiative transfer equation (RTE):

$\frac{d\bar{I}(\bar{r},\hat{s})}{ds} = -\kappa_e \bar{I}(\bar{r},\hat{s}) + \int_{4\pi} d\Omega' \bar{\bar{P}}(\bar{r},\hat{s},\hat{s}')\bar{I}(\bar{r},\hat{s}')$ (2)

where $\bar{I}(\bar{r},\hat{s})$ is the specific intensity at the position $\bar{r}$ in direction $\hat{s}$, $\bar{\bar{P}}(\bar{r},\hat{s},\hat{s}')$ is the phase matrix, and the extinction coefficient κ_e is the sum of the scattering and absorption coefficients, $\kappa_e = \kappa_s + \kappa_a$. The distinctive difference of DMRT from classical RTM is the coherent interaction part in which the extinction coefficients κ_e and the phase matrix $\bar{\bar{P}}(\bar{r},\hat{s},\hat{s}')$ are

205 obtained by solutions of Maxwell equations including coherent wave interactions among the ice grains that are in the near field and intermediate fields distance ranges from each other (Liang et al., 2008; Ding et al., 2010). In solving Maxwell's equations, the dense medium effects and snow microstructure are accounted for.

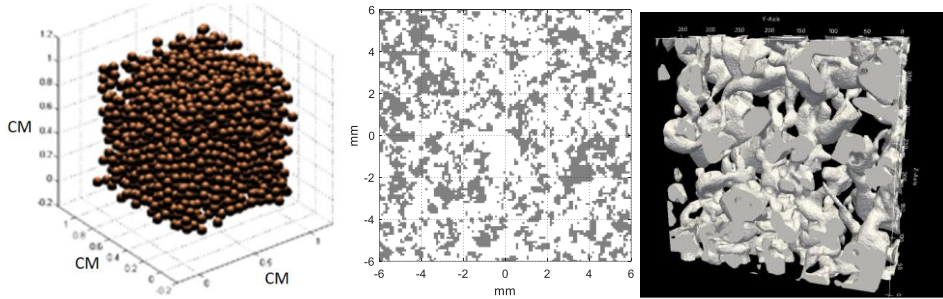



Figure 2: **Microstructural descriptions of the snowpack: (a) sticky hard sphere theoretical model, (b) a bi-continuous medium with**
210 **ice crystals in dark and air in white based on parameters $\langle\zeta\rangle$= 1 mm, and b=1.0 and (c) 3-D image from x-ray microtomography**
with ice crystals shown in white and air voids in black.

The volume scattering σ_{vol}^{pq} depends on snow microstructure; the response of microwave radiation to snow microstructure has been studied extensively. We describe the five different electromagnetic models. 1) In Chang et al., (1976), collections of spheres are used for the microstructure. The scattering by individual spheres are added incoherently. However, it is not valid for snow as particles are densely packed, meaning electromagnetic (EM) waves scattered from individual grains interact coherently within distance scales of several wavelengths. 2) DMRT has been applied to the cases of hard spheres (Tsang et al., 1985), sticky hard spheres (Tsang et al., 2007) and distributions of sphere sizes (Tsang et al., 1992). The coherent interactions are described analytically by the quasi-crystalline approximation (QCA) of Mie scattering for closely packed spheres. Figure 2 (a) gives a visual representation of the sticky hard sphere microstructure. 3) The approach of Hallikainen et al. (1987) empirically relates grain size directly to scattering coefficient. In this case, the model was derived from experimental observations of extinction behaviour and the relations to traditional grain size measurements. The direct connection between scattering and grain size means the model is simpler to apply, albeit with potentially large errors due to limited observations and variations with snow types. 4) A different representation of snow is a random medium of ice and air (Figure 2 (b)). Mätzler (1998) treats scattering by characterizing the microstructure autocorrelation length, using the improved Born approximation (IBA) and the random medium assumption. 5) The generalized bicontinuous medium approach uses two parameters to characterize snow microstructure: a mean grain size $\langle \zeta \rangle$ and an aggregation parameter b. There are two features: (1) the microstructures are computer generated and (ii) the auto-correlation functions are derived analytically (Chang etal 2014) The aggregation parameter b represents the adherence of ice grains together to form clusters. A smaller b parameter values produce greater aggregation. The b parameters chosen for X- to Ku-bands fall in the range of 1.0 to 2.0 (Chang et al., 2014; Tan et al., 2015; Xiong & Shi, 2019). With development of computational electromagnetics , numerical solutions of Maxwell's Equations in 3D are also used (Ding et al., 2010; Xu et al., 2012; Tan et al., 2017).

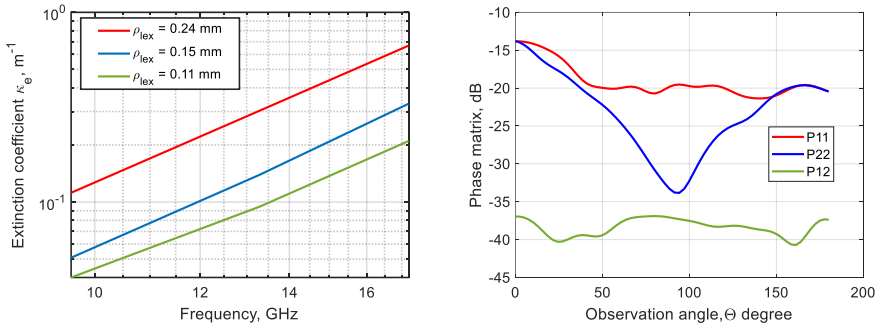



Figure 3: **(a) Frequency dependence of the extinction coefficient from X- to Ku-band and (b) phase matrices at 13.3 GHz for different values of microstructure correlation length ρ_{lex}. Snow parameters are volume fraction $f_v = 0.20$, aggregation parameter $b = 1.2$, and correlation length 0.15 mm. P11 and P22 are co-polarized phase matrix elements and P12 is a cross-polarized phase matrix element.**

EM models thus have evolved in part due to knowledge advances from our improved ability to measure snow microstructure. Stereological approaches led to advances in treating snow as a random medium using correlation functions (Wiesmann et al., 1998). X-ray micro-computed tomography (μ-CT) has emerged to image the 3-dimensional structure of snow (Kerbrat et al. 2008), as illustrated in Figure 2 (c), which has fed advances such as the dual active/passive Snow Microwave Radiative Transfer (SMRT) model (Picard et al., 2018). SMRT was developed to understand how to represent microstructure faithfully at scales relevant for microwave scattering and has the potential to allow direct use of correlation functions from μ-CT. Application of μ-CT-derived microstructure parameters in SMRT removes the need for empirical grain scale factors with frequency-dependent model performance governed by the quality of microstructure model fit (Sandells et al, 2021). EM models have been adapted to work with field-derived measurements as well. Field methods to measure microstructure are more fully discussed in section 3.3.1. It is to be noted that the random medium model and the bicontinuous model both use the autocorrelation function. These advances reduce the uncertainties in interpreting remote sensing observations and support the design of remote sensing missions to observe seasonal changes in snow storage.

Figure 3 illustrates the volume scattering of snow with bicontinuous DMRT. Figure 3 (a) shows the frequency dependence of the extinction coefficients κ_e for different values of microstructure correlation length and with aggregation parameter $b = 1.2$. The results show the increase of extinction with increasing correlation length. The exponential of the frequency dependence is 3.3 from X- to Ku-band, which is less than the fourth-power law of Rayleigh scattering. This difference is due to the dense media effect, and the power law exponent is found to depend on the aggregation parameter b. The phase matrices at 13.3 GHz for snow are shown in Figure 3 (b). The phase matrix gives bistatic scattering as a function of the angle θ between the incident direction $\hat{s}$ and scattered direction $\hat{s}'$. In Figure 3 (b), P11 and P22 are co-polarization phase matrix elements and P12 is the cross-pol phase matrix. The phase matrix exhibits a dipole scattering pattern. The cross-polarization P12 is much larger than would be calculated by the sphere models because of the irregular shapes of the aggregates in the bicontinuous medium. The computed phase matrix and the extinction coefficients are substituted into the RTE which is then solved to calculate backscattering. The results in figure 4-6 are an illustration of the bicontinuous model (Tan et al. 2015.) The results as a function of SWE for a homogenous snow layer are shown in Figure 4 for 6 channels with VV polarization at 10.2 GHz, 13.3 GHz, and 16.7 GHz in Figure 4 (a) and VH polarization for the same frequencies in Figure 4 (b). In Chang etal 2014), the results were compared with the Finnish NoSREx backscattering dataset within which tower measurements were taken over snowpacks with SWE up to 120 mm. The bicontinuous-DMRT model results are in good agreement with backscatter observations over the 6 channels of multiple frequencies and polarizations, albeit with a frequency-dependent bias for the cross-pol results. Both the model predictions and measurements show high correlations with SWE with stronger correlations at 13.3 and 16.7 GHz than at 10.2 GHz. Several years of NoSRex data were analysed and the results of retrieval performance on the data were illustrated in the paper by Zhu et al. 2018

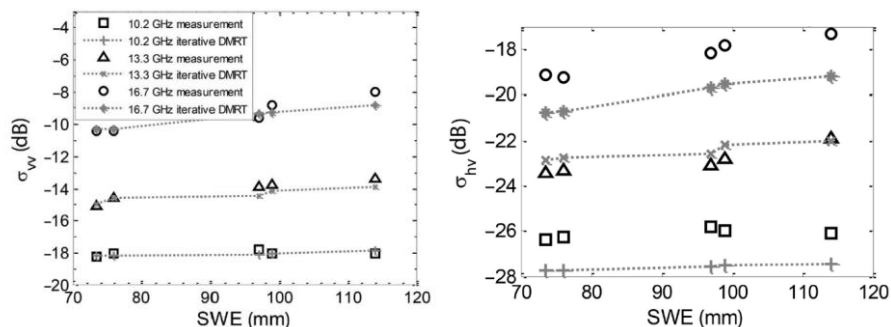



Figure 4: Comparison of the DMRT/ bicontinuous media model using NoSREx 2010-2011 data backscatter against SWE for vertical co-pol (left) and cross-pol (right) at 10.2GHz, 13.3GHz, and 16.7GHz. Figures are adapted from Tan et al., 2015.

1. Because of snow accumulation events and weather patterns, snow cover can have layering structures that correspond to variations of snow densities and grain sizes. Extensive work has been done in studying multi-layered models of snow using the HUT model (Lemmetyinen et al., 2010), the DMRT-ML model (Picard et al., 2013), and the MEMLS model (Proksch et al., 2015). Recent experimental work indicates that multi-layered radiative transfer modeling may shed light on snow radar interaction (Thompson and Kelly 2021a; 2021b). For the case of DMRT , a multi-layer DMRT model with different dense media phase matrices and extinction coefficients for each layer are used (Liang etal 2008, Chang etal 2014 Tan etal 2015) . Both the quasi-crystalline approximation (QCA) model and the bicontinuous model have been used for a multilayer snow medium (Chang etal 2014)

2. Structural anisotropy is a characteristic feature of natural snow packs (e.g. Leinss et al., 2020). This causes changes of the phase matrix with the incidence angles and scattered angles. There are two models in the bicontinuous model: isotropic correlation functions and anisotropic correlations functions (Tan etal 2016) . Both have been developed and simulations performed. In the retrieval, only the isotropic correlation functions versions have been used in the DMRT LUT.

3.1.2 Interaction of radar waves with the ground surface beneath snowpack

Because the dielectric contrast between dry snow and soil exceeds that between dry snow and air, the contribution of rough surface scattering arises primarily from the snow-soil rough interface and not from the air/snow interface (although it is noted that the air/snow interface may have a stronger scattering contribution when the snow is wet, but this is outside the domain of SWE retrieval using X/Ku band volume scattering). Rough surface scattering from the snow/soil interface contributes to radar observations as indicated by the term $\sigma_{bg}^{pq} exp(-2\tau sec\theta_t)$ in Equation (1). This term is affected by the rough soil surface scattering σ_{bg}^{pq} and by attenuation through the snow $exp(-2\tau sec\theta_t)$. The rough soil surface scattering contribution is not related to SWE and therefore should be removed when retrieving SWE. A "subtraction" of surface scattering has been used to improve the accuracy of SWE retrieval (Zhu et al., 2018). The approach for removing $\sigma_{bg}^{pq} exp(-2\tau sec\theta_t)$ involves a

295   combination of data and electromagnetic models, and is a significant part of the retrieval algorithm that will be discussed later in this section. Here we discuss methods for calculating scattering from the snow/soil interface at L, C , X- and Ku-bands.

Classical physical models for rough surface scattering include the small perturbation method (SPM) and the Kirchhoff approach (Ishimaru, 1978; Tsang and Kong 2001). Advanced analytical methods include the advanced integral equation model (AIEM, Chen et al., 2003) and small slope approximation and its extensions (Voronovich, 1994; Elfouhaily and Johnson 2007).

300   Fully numerical solutions based on the use of Monte Carlo simulations are also available to avoid approximation in the electromagnetic physics. In all these models, surface roughness can be described in part using the parameter kh, which is the product of the EM wavenumber k of the medium above the rough surface and the surface rms height h. Previous studies using analytical models and numerical simulations for snow or land sensing applications have emphasized cases having $kh < 3$ due to a past focus on L-band sensors. For example, using a times series of SMAP VV and HH polarized backscatter

305   measurements, both the surface soil moisture and surface rms height were retrieved at 3km resolution for the April 13- July 7, 2015 period of SMAP radar operation (Kim et al 2017). Results from this product show a global median surface rms height of 2cm, with rms heights up to 5 cm in mountain regions. A surface rms height of 5 cm at 17 GHz would represent a kh value is 18 for the air/soil interface and 21.6 for the snow/soil interface (the larger value for the snow/soil interface is due to the larger electromagnetic wavenumber in snow). Past studies emphasizing $kh < 3$ therefore limit applications

310   to L or C bands. Recently, we have performed numerical surface scattering simulations having kh up to 15 ($h = 4.16\ cm$ for 17.2 GHz) to widen the applicability of full wave simulations up to Ku band (Zhu 2021, Zhu et al 2021)

Surface scattering models typically describe the soil surface as a stationary Gaussian random process, so that knowledge of its covariance function is sufficient to describe its properties. The covariance function is further parametrized in terms of its rms height and correlation length. Ground measurements have been made of these properties (Oh et al., 1992; Oh, and Kay, 1998;

315   Ulaby and Long, 2015), and measured correlation lengths are typically found to be limited to a maximum of 10 cm. We label these roughness measurements as "limited correlation length up to 10 cm". However, in the global retrieval of soil moisture using six months of the NASA Soil Moisture Active Passive (SMAP) radar data at L-band, the roughness was modelled as having a constant correlation length to rms height ratio (Kim et al., 2012; Kim et al., 2014, Kim et al 2017) that ranged from 5 to 20. These two methods for describing the correlation length differ significantly for rms heights beyond 2cm; our studies

320   have found that the constant ratio approach gives more acceptable results. Surface scattering also depends on the soil permittivity which in turn depends on soil moisture (which describes the volume of water present per unit volume of soil) and texture (which describes soil composition). Given these parameters, empirical models (Mironov et al., 2004; Peplinski et al., 1995) are available to calculate the soil permittivity. In addition to soil properties, land-cover including litter and vegetation, as well as rock outcrops, impact the spatial variability of surface permittivity and backscattering.

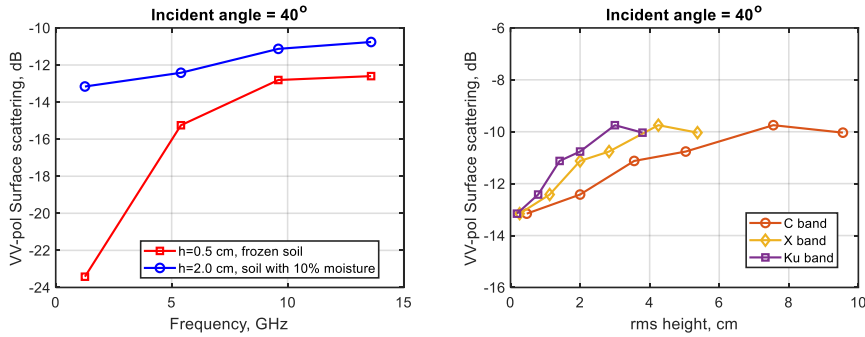



Figure 5: (a) Backscattering at VV-polarization as a function of frequency: red curve is results with frozen soil (permittivity 4+1i) and rms height 0.5 cm and blue curve is results with soil of 10% moisture and rms height 2 cm. (b) Backscattering at VV-polarization as a function of rms height with soil of 10% moisture at C-, X-, and Ku-band.

Full wave simulations based on numerical solutions of Maxwell's equations (NMM3D) were applied to L-band radar backscatter analysis for the SMAP mission (Huang et al., 2010; Huang and Tsang, 2012). The full wave simulations were used to generate a look up table (LUT, Liao et al., 2016). The LUT was initially used for the air/soil interface. Also, the LUT was based on the incident angle of the upper medium and the relative dielectric constant between the two media on the two sides of the rough surfaces. By adjusting the relative dielectric constants and the incidence angle using Snell's law, the NMM3D LUT can also be applicable for   all combinations of relative dielectric constants including snow/soil , air/snow, or snow/permafrost interfaces, among others.

In Figure 5(a), we plot VV backscattering as a function of frequency for $h = 0.5$ and 2 cm. In Figure 5(b), we further plot the VV backscattering as a function of rms height at C-, X-, and Ku-bands. Both figures show saturation effects, meaning that the rough surface scattering saturates at large rms heights (~ 3-6 cm) and at higher frequencies. The new results of kh up to 15 are useful for studying rough surface radar backscattering at X- and Ku- bands for snow/soil interfaces.

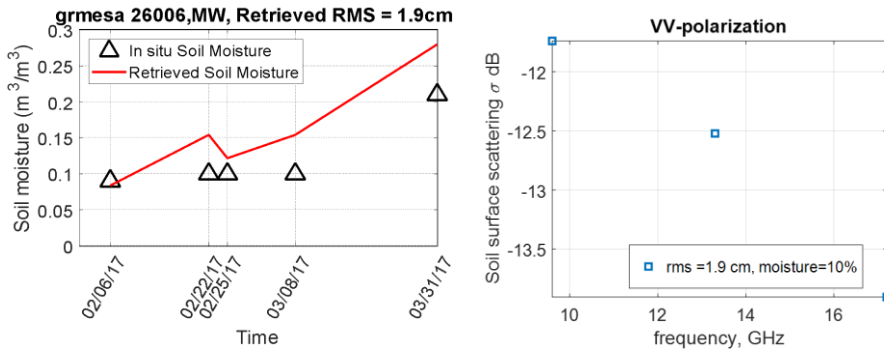
To estimate rough surface scattering at X band and Ku band, there are two approaches labeled (a) and (b) in what follows. Approach (a) uses snow-free radar observations at X- and Ku-bands at a specific location to estimate the surface backscattering (Rott et al., 2010). Such an approach neglects any changes in soil properties and background land-cover during the snow-on season. In approach (b), surface backscattering is estimated using a combination of measurement data and electromagnetic models.   The measurement data includes backscattering data at L, C, X, and /or Ku band under snow free or snow-on conditions, and the NMM3D LUT is used to model surface backscattering. As a first step, co-polarized radar time series observations at L- and C-band, which have greatly reduced sensitivity to snow volume scattering, are used to estimate the soil permittivity and surface roughness. The use of a C-band measured time series together with the past L-band time series data enhances the existing L band algorithm in retrieving rms height and soil moisture, and the retrieval is performed either in the presence or absence of snow. When snow is present, Snell's law is used to adjust the incident angle at the snow-soil interface

350 to account for the snow refraction effects. The surface rms heights and soil permittivities obtained are then used in the NMM3D LUT to predict the surface backscattering contribution (σ_{bg}^{pq}) at X and Ku bands; note this captures any dynamically varying roughness or permittivity conditions in performing the surface scattering correction. We assume the availability of matchup L- and/or C-band SAR observations with revisit periods of approximately 10 days, as are or will be available from the the Sentinel-1 and NISAR systems, as well as future proposed continuation missions, so that such datasets are likely to be available

355 during the time frame of a future snow observing mission.

Consider for example L-band UAVSAR radar full polarization observations under snow-on conditions (Liao et al., 2016). The UAVSAR dataset examined was collected from February to March 2017 in the SnowEx 2017 campaign using 5 flights over the Grand Mesa region in Colorado, United States. In-situ soil moisture measurements were also collected throughout 2017 from an installed meteorological observation station. We apply the time series retrieval algorithm developed for the SMAP

360 mission (Kim et al., 2012, Kim et al 2017) based on the NMM3D LUT at the station location (i.e. at a point location). From the retrieved soil permittivity, the soil moisture is derived using Mironov's empirical model (Mironov et al., 2004). The comparison of retrieved and measured soil moistures is shown in Figure 6 (a). The retrieval soil moisture is in good agreement with the measured in-situ soil moisture for a period of 8 weeks from February 6 to March 31, 2017. ~~The agreement achieved shows a root mean square error (RMSE) of 0.047m^3/m^3, a correlation of 0.95 and a bias of 0.039m^3/m^3, and that the soil~~

365 ~~moisture at this site remained relatively constant during the dry snow season (February 6 to March 8, 2017).~~ In addition to retrieving the soil moisture time series, the rms height at this location was also retrieved and estimated as 1.9 cm. Note the Kim et al. 2017 algorithm retrieves a single rms height estimate for the time series because surface roughness is assumed to remain constant over the time series duration (so that wet and frozen soils are assumed to have the same rms height.)

370 **Figure 6 (a) Retrieval of soil moisture compared with in situ-measurements. The retrieved rms height is 1.9 cm. The retrieval is based on based on L-band UAVSAR data from SnowEx 2017 campaign. The measured soil moisture is from SnowEx 2017 campaign meteorological observations with a measured soil temperature of 0.6° C. The location of the station is 39.03388° N, 108.21399° W with an elevation of 3033m. (b) Simulated surface scattering with snow attenuation from X- to Ku-band at VV polarization. Snow parameters are with depth of 54 cm, density of 183 kg m^{-3}, $\langle\zeta\rangle$ = 1.2 mm, and b=1.2. Blue marks are based on the SnowEx 2017**

375 **campaign data shown in (a).**

We next apply the retrieved rms height (1.9 cm) and the soil properties from Figure 6 (a) to calculate the surface scattering contributions with snow attenuation, $\sigma_{bg}^{pq} exp(-2\tau sec\theta_t)$, at 9.6, 13.4, and 17.2 GHz as shown in Figure 6(b). The results show that the rough soil surface scattering contribution , including snow attenuation , is around -12dB at X band and decreases to -14 dB at 17.2 GHz; higher frequencies such as Ku band typically experience higher volume scattering and greater attenuation of the surface scattering contributions. Continued studies are required to improve and validate this approach, including extending NMM3D surface modelling studies and the associated LUT into cases with rms heights of 4 wavelengths or more so that the LUTs can be applied at 17.2 GHz for rms heights up to 7 cm. Also, unlike snow volume scattering, rough surface scattering has a stronger dependence on incidence angle and polarization. Thus, the effects of topographical slopes that cause changes in incidence angles, particularly in mountainous regions, should be included in the retrieval. Although it is noted that the sample size in Figures 6a and 6b is small, the increasing availability of L and C band time series measurements and the extension of full wave simulations from L band to Ku band up to $kh = 20$, is expected to make the retrieval of surface rms heights and permittivities feasible so that robust surface scattering corrections can be achieved at X and Ku bands. Further extensions to consider the snow/permafrost interface are also under development.

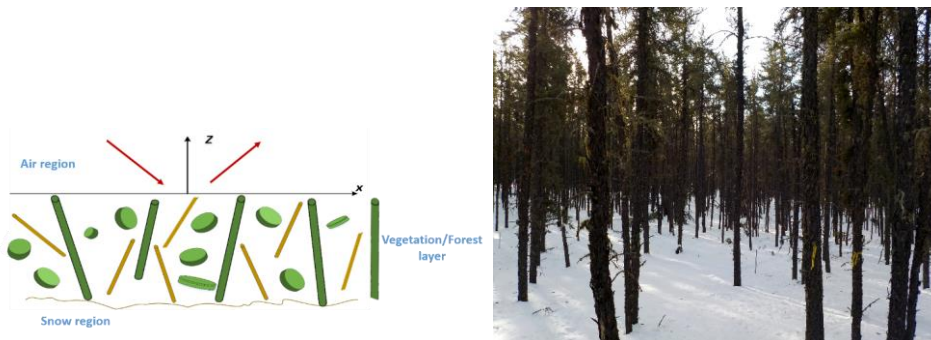



Figure 7. (a) RTE assumption: uniformly randomly-positioned scatterers which are statistical homogeneous. (b) Illustration of trees for a forest with snow cover beneath. The picture was taken on March 14th 2017 in a Jack Pine stand situated in the Boreal Ecosystem Research and Monitoring Sites (BERMS), Saskatchewan, Canada.

3.1.3   Interaction of radar waves with forests and vegetation above snowpack

The interaction of radar waves with vegetation initially began with the water-cloud model (Attema and Ulaby, 1978) (Figure 7 (a)). It was then extended by using RTE to include scattering effects in addition to absorption. Computation codes of RTE exists such as the MIMICS model (Ulaby et al., 1990) and in the Torgata model (Ferrazzoli and Guerriero, 1995 Ferrazzoli

400 etal 1999)). In addition, the discrete scatterers model using distorted Born approximations (DBA) have been used (Lang and Sighu 1983, Karam etal 1992). The RTE and DBA models use the same assumptions and give the same results aside from a factor of 2 in the double bounce of volume surface interaction term.   Bindlish and Barros (2001) applied the water cloud model formulation to the parameterization of vegetation backscatter from C- and L-band radar measurements using three vegetation parameters (a measure of vegetation density, a measure of vegetation architecture, and a dimensionless vegetation
405 correlation length) to characterize different types of vegetation in rangeland, winter wheat crops and pasture. They found that the estimation of land-cover and land-use class specific parameters resulted in significant improvements in retrieval of soil moisture, which suggests that a similar approach could be used for snow retrieval using multifrequency data along with detailed ancillary vegetation data sets to estimate the place-based parameters for the water-cloud model. Zoughi et al. (1986) conducted X-band radar measurements to identify the contributions from leaves, petioles, twigs, and branches of pine, oak, sycamore and
410 sugar maple trees to backscatter and attenuation. In addition to quantitative differences related to tree architecture and vegetation moisture content, they reported that the backscatter is mainly produced by the top layers of the canopy, petioles (tree microstructure) can significantly affect backscatter depending on their size relative to wavelength, leaves play an equally important role in attenuation and backscatter, whereas twigs and branches dominated in terms of backscatter with weak attenuation when leaves were not present.   They did not consider the effect of tree trunks.
415 In CoReH2O Phase A the impact of forests on radar signals of snow-covered ground was studied (ESA, 2012). Model and data analyses were carried out by Kugler etal 2014 and Montomoli et al. (2016). The forest model selected in CoREH2O are based on the radiative transfer equations (RTE). It accounts for scattering of trunks, branches of different size and needles, as well as for differences in the structure of vertical layers. Effects of differences in cover fraction, tree height and biomass were analysed. The model gives a multifaceted description of forest properties and for estimating the impact of the forest parameters
420 on the backscatter of snow-covered forests. The CoREH2O RTE based studies,   indicate that, during the winter period, the presence of dormant herbaceous or short vegetation have small contributions to backscattering and do not affect the sensitivity to SWE. For the effects of coniferous forests (CF), the simulation results show that in the case of low fractional cover of CF (<25%), contributions of snow volume scattering are the dominant contributions to the radar signal, with the radar signals correlating with SWE. When the forest density or the fractional cover increases, the sensitivity to SWE decreases. The
425 sensitivities are much affected by CF larger than 75%.   . In addition to forest density and structure, snow interception in the canopy can vary widely in time and depending on snow type and canopy architecture and modify the transmissivity and scattering characteristics.

Recently, since 2017, instead of using the RTE/DBA models, we have used full wave simulations based on a hybrid method
430 of combining wave multiple scattering theory (W-MST) and commercial software in computational electromagnetics such as HFSS and FEKO . The "waves" MST are based on Maxwell equations and different from that of multiple scattering in RTE which only considers incoherent multiple scattering of leaves branches etc. . Full wave simulation results have been computed for L, S, and C Bands. The results of full wave simulations show two distinct differences from that of the results of the

RTE/DBA model : (i) the full wave simulations show more penetration than predicted by the RTE model with differences that can be several times and (ii) the full wave simulations show weaker frequency dependence than the RTE model. We cannot at this moment extrapolate the conclusions to X Band and Ku Band for trees. However, preliminary results running full wave simulations of needle leaves at X band and Ku band show significant differences from the RTE model. Thus, in the near future , there will be extensive full wave simulations and new measurements to study the effects of trees and forests at X band and Ku band.

The reasons for the differences are that the basic DBA/ RTE have two basic assumptions

The first assumption is that scatterers such as trunk, leaves, primary , secondary and tertiary branches etc are individual , isolated scatterers that are uniformly positioned in the layer, such as that shown in figure 7a. . The reason for this assumption is that the RTE model was first used for microwave remote sensing of cloud and rainfall . The assumption of uniform random positions is the same as homogenization, meaning that there is an effective attenuation rate κ_e. For a forest height of d, the Beer-Lambert Law or the Foldy approximation states that the transmission through forest/vegetation is given by the expression $e^{-\tau sec\theta_i}$ where the optical thickness τ is equal to $\kappa_e d$

r However, in forests, such as coniferous forests (Figure 7 (b)), aspen forests and deciduous forests, the scatterers are aggregated in trees. Unlike clouds, which do not have gaps, there are gaps between the trees. Thus, waves, such as those in the Ku-band at 17.2 GHz with wavelengths of 1.74cm, can pass through gaps when gap sizes are larger than these wavelengths. The consequence of the assumption is that RTE underestimates the transmission. The second assumption is that the leaves and branches are assumed to be single scatterers, and they scatter independently. The extinction coefficients and phase matrices of equation (2) are calculated by adding the scattering cross section of the branches and leaves. This assumption is valid for cloud and rainfall as the water droplets can be assumed to be single scatterers However, the geometry (Figure 7(b)) is that the branches and leaves are attached to the tree. For a coniferous forest, there are primary branches and secondary branches attached to a tree. The needle leaves are aggregated and are attached to branches. Thus, the entire tree itself should be treated as a single scatterer rather than an individual branch or an individual leaf. Therefore, the phase matrix of a tree should be used rather than incoherently adding the scattering cross sections of branches, leaves, and the trunk for a tree. Using a tree as a single scatterer give results that have weaker frequency dependence than that predicted by RTE/DBA.

Full wave simulations to solve Maxwell equations among trees or plants were deemed to be computationally formidable. Recently, a computationally efficient hybrid method (HB) has been developed to perform full wave simulations (Huang et al., 2017; Huang et al., 2019; Gu et al., 2021, 2022). The hybrid method is a combination of commercial-off-the-shelf software of computational electromagnetics , the Foldy-Lax wave multiple scattering equations , and iterations based on the averaged multiple orders of scattering . The hybrid method consists of three steps. In the first step, a plant or a tree is treated as a single scatterer. Commercial-off-the-shelf software is used to calculate the scattering T matrix in vector cylindrical waves of a single plant or a single tree. We have used the commercial software of HFSS and FEKO (**Altair FEKO: https://www.altair.com/feko/**).

In the second step, coherent wave multiple scattering theory (W-MST) among the plants and trees are formulated by using the Foldy-Lax multiple scattering equations. The formulation uses T matrices and vector addition theorem of vector cylindrical

470 waves (Tsang etal , 2001). In the third step, the Foldy Lax equations are iterated to obtain solutions in multiple orders of scattering, and averages are taken over realizations after several orders at a time to obtain the averaged solution. The third step makes use of the property that the averaged solution of orders of multiple scattering have faster convergence than the obtaining exact solution of a single realization through matrix iteration methods such as conjugate gradient or bi-conjugate gradient. NMM3D full wave methods and simulation results can be found in Huang et al., 2017; Huang et al., 2019; Gu et al., 2021,

475 2022) Below we illustrate two examples.

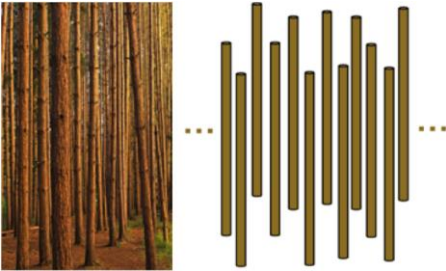
Simulations were performed for the transmission through a simulated forest (Huang et al., 2019) consisting of 196 cylinders representing tree trunks. Each cylinder is of of 20 m height and 12 cm diameter , and the cylinders area arranged as shown in Figure 8. The results are tabulated in Table 1. The results show that the transmission is almost twice that of RTE.

480 **Figure 8: Tree trunks (left) are modelled as dielectric cylinders (right). The figure is adapted from Huang et al., 2019.**

Table 1: transmission coefficient from RTE based on distorted Born approximation (RTE/DBA) and the hybrid method from Figure 8. The table is adapted from Huang et al., 2019.

	RTE/DBA	Hybrid method
Transmission	0.35	0.66

To consider frequency dependence, we next show an example of the transmission through a field consisting of 196 wheat

485 plants (Figure 9 (a)) at L-, S- and C-bands (Gu et al., 2021, 2022) as a function of VWC. Results of Figure 9 (b) are compared with RTE. Firstly, the results show the transmission of full wave simulations are much larger than RTE. Secondly, the transmission at C-band is only slightly less than that at S-band showing the frequency dependence is weak between S band and C band. . On the other hand, RTE shows big drop in transmission from S- to C-band indicating that RTE predicts a strong increase of attenuation with frequency from S band to C band. On the other hand, the full wave simulation results have

490 little difference between S band and C band, showing "saturation " with frequency.

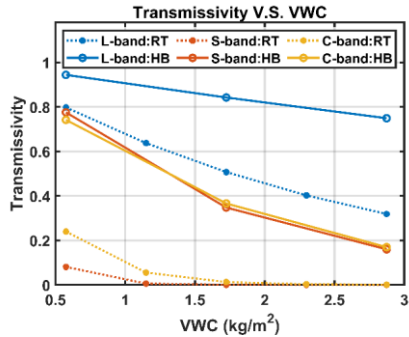
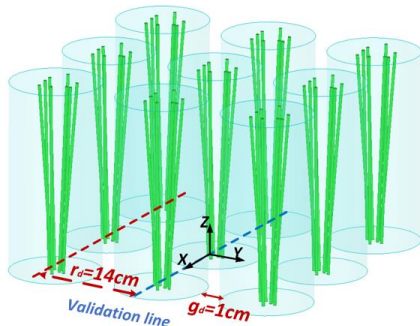



Figure 9: (a) Scattering from wheat plants are the radius of the circumscribing cylinder 6.5 cm, distance between the centres of 2 circumscribing cylinders is r_d =14 cm, the closest distance between 2 circumscribing cylinders is g_d = 1 cm. Figure is adapted from Gu et al., 2021. (b) Transmission of microwave through wheat of different calculated using the hybrid method and the RTE vary with volume water content (VWC).

At Ku-band (17.2 GHz), the wavelength is 1.74 cm, which is much smaller than the gaps in trees. The wave can travel in straight lines as rays through the gaps. In such scenario, the Ku-band waves will travel like the case of lidar which has been shown to be able to penetrate forest canopies. In wireless communication, ray tracing has been performed as a path-loss model in forests (Ling et al., 1989; Kurt et al., 2017). However, ray tracing, in the opposite extreme of RTE, has no frequency dependence although frequency dependence can be introduced in an ad hoc manner such as by only keeping the dominant scatterers at the operating frequency. .

3.2 Experimental measurements of radar-landscape interactions

Collection of experimental data is a prerequisite for the development of Earth Observation satellites. Ground-based and airborne sensors provide means to collect observations of the geophysical parameter of interest in a relatively controlled environment. These measurements provide the basis for the validation of forward modelling approaches and development of retrieval algorithms prior to launch of the space-borne mission. The measurements also help to understand the spatial resolution and temporal requirements for a spaceborne mission.

Ground-based sensors deployed on tower structures allow near-continuous observations over extended periods, which are critical for understanding both slow and seasonal processes as well as rapid phenomena induced by diurnal changes at the sensor foot-print. Such temporal features are of particular importance for seasonal snow cover. Airborne observations, or the deployment of ground-based sensors on other mobile platforms, provide the ability to expand localized observations to a larger

scale, allowing to observe the effect of heterogeneous land cover and vegetation on Earth Observation signatures. Seasonal
515 snow presents a particularly challenging target for observations, due to the high variability of snow over both temporal and
spatial scales. Hence, several both localized, ground-based campaigns as well as airborne sensor deployments have been
conducted in recent years, in an attempt to understand radar signatures from seasonal snow cover. These campaigns have
covered diverse snow and climatological conditions.

Table 2: Summary of ground-based active microwave sensors for snow studies.

Ground-Based Campaign	Dates	Sensor	Freq.	Pol.	Location/snow regime	Data availability
Can-CSI, CASIX	2009-2011	UW-Scat	9.6, 17.2 GHz	VV, VH, HV,HH	Churchill, Manitoba, Canada Tundra, Taiga, Lakes, Sea Ice	Available from Dr Richard Kelly rejkelly@uwaterloo.ca
NoSREx	2009 - 2013	ESA SnowScat	10-17 GHz (stepped frequency)	VV, VH, HV, HH	Sodankylä, Finland / boreal forest	ESA EO campaign portal
SnowEx '17	2017	UW-Scat	9.6, 17.2 GHz	VV, VH, HV, HH	Grand Mesa, Colorado, USA	NSIDC
APRESS	2019 - 2021*	ESA WBScat	1-40 GHz	VV, VH, HV, HH	Davos-Laret, Switzerland / Alpine Sodankylä, Finland / boreal forest	Not yet available

520 **3.2.1 In situ radar experiments and signatures**

The ground-based campaigns are summarized in Table 2. Ground-based campaigns of Can-CSI and CASIX were conducted
between 2009 and 2010, and multiple field campaigns were completed near Churchill, Manitoba, Canada, as part of the Phase
A science activities of CoReH2O. These campaigns aimed to evaluate the potential for dual-frequency X- and Ku-band snow
properties retrievals in subarctic environments. Central to Churchill campaigns was deployment of the University of Waterloo
525 Scatterometer (UW-Scat), a novel ground-based radar system analogous to the proposed configuration of CoReH2O (King et
al., 2012). In Europe, ESA initiated the deployment of SnowScat (Werner et al., 2010), a stepped frequency, fully-polarimetric
ground-based radar in a series of campaigns in the boreal forest zone in Northern Finland (Lemmetyinen et al., 2016). The

campaign was called NoSREx and operated SnowScat over four winter seasons, complemented by passive microwave radiometry and regular snow microstructural observations. These campaigns have been instrumental in enhancing our understanding of snow-microwave interactions and providing data to develop and evaluate forward models simulating backscattering from snow cover (King et al., 2015; Tan et al., 2015; Proksch et al., 2015a), as well as developing retrieval approaches (Cui et al., 2016; Lemmetyinen et al., 2018).

Previously, in section 3.1.1, we have made use of the NoSREx campaign 6 channels of backscattering data of VV at 10.2 GHz, 13.3 GHz and 18.7 GHz, and HV at 10.2 GHz, 13.3 GHz and 18.7 GHz in comparisons with the simulation results of bicontinuous-DMRT models. The comparisons have validated both the ground campaign measurements and the physical models (Tan et al., 2015).

Recent ground campaigns include APRESS in which the ESA WBScat instrument, a full-polarization radar operating at 1-40 GHz, was deployed for a full winter season in 2019-2020 measuring an Alpine snowpack in Davos, Switzerland. For the winter of 2020-2021, the instrument was set up in Sodankylä, Finland, to collect data over a sparsely forested site. These sensors and deployment have generated and will continue to generate critical datasets for characterizing the radar backscattering of snow, the effects of rough surface scattering, and forests. They will help to advance retrieval development when coupled with advancements in field methodology and forward modelling capabilities.

3.2.2 Airborne experiments and signatures

Airborne campaigns (listed in Table 3) provided the first experimental demonstration of the sensitivity of Ku-band polarimetry scatterometer (POLSCAT) backscattering to SWE (Yueh et al., 2009). CoReH2O provided further impetus for the development of new airborne sensors. The ESA SnowSAR (a dual-polarization, airborne, side-looking SAR operating at X- and Ku-bands (Coccia et al., 2011; Meta et al., 2012) was deployed at several sites in Northern Finland, the Austrian Alps, Northern Canada and Alaska between 2011 and 2013. The purpose of the flight campaigns was to collect data over a range of climatological snow classes and land cover regimes. All flight campaigns were supported by extensive measurement of snow properties, including vertical profiles of snow stratigraphy and microstructure. The campaigns have enabled the further assessment of e.g., vegetation effects on backscatter (Cohen et al., 2015; Montomoli et al., 2016), the effect of spatially variable microstructure (King et al., 2018) and further elaboration of modelling and retrieval capabilities (Zhu et al., 2018). Figure 10 demonstrates the effect of changing snow conditions on the observed Ku-band co-polarized backscatter during two of the SnowSAR flights in Finland. The differences between open area and forested area has been addressed and illustrated in Montomoli et al., 2016 using the models of classical radiative transfer. Results of full wave simulations are currently being studied.

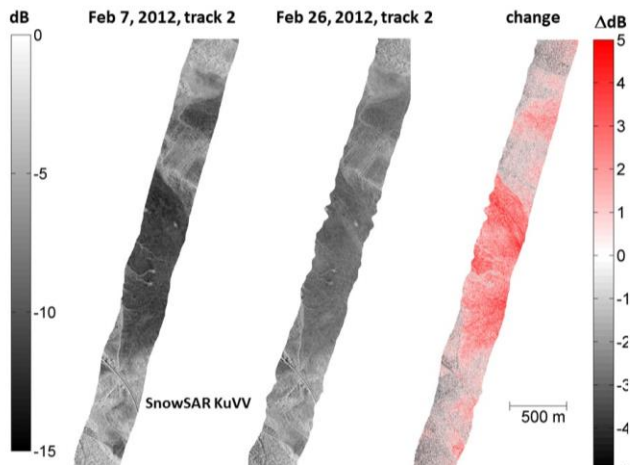



Figure 10: Demonstration of observed Ku-band VV-pol backscattering from two consecutive SnowSAR flight campaigns in Sodankylä, Finland. The difference in backscatter is depicted on the right, with red implying an increase. Increases of measured backscattering are correlated with the increase of SWE. The measured SWE between the flights increased on average by 41 mm in non-vegetated areas, which show the highest increase (Figure adapted from Lemmetyinen et al., 2014).

Recent airborne campaigns including SnowEx 2017, SnowEx 2020, and TVCExp 2019 have deployed a new generation of airborne systems to address known uncertainties including penetration in dense vegetation, background interactions, and InSAR applications (Table 3). As part of ongoing research at Trail Valley Creek, a new Ku-band InSAR (13.285 GHz) developed by the University of Massachusetts was deployed during the winter of 2018-2019. This system was developed to allow rapid deployment aboard common commercial platforms, leading to three successful acquisition periods throughout the winter. Coupled with objective measurements of snow microstructure and a distributed network of soil permittivity sensors, these data are now being used to develop InSAR and backscatter retrieval methods for future missions. The Snow Water Equivalent SAR and Radiometer (SWESARR) is a tri-band synthetic aperture radar (SAR) and a tri-band radiometer. Both the active and passive bands utilize a highly novel current sheet array (CSA) antenna feed. SWESARR has three active (9.65, 13.6, 17.25 GHz) and three passive (10.65, 18.7, 36.5 GHz) bands. Radar data are collected in dual polarization (VV, VH) while the radiometer makes single polarization (H) observations. During SnowEx 2020, NASA Goddard's SWESARR demonstrated for the first time that X-band, low Ku-band and high Ku-band SAR acquisition can be made through a single antenna feed. Data collected during this campaign coincided with detailed measurements of vegetation structural properties and under canopy snow properties that will be critical to address the effects of vegetation and forests in SWE retrieval.

Airborne campaigns are planned for 2022-2023 for both Canada and US SnowEx. These future campaigns will address the following questions: (a)What is the maximum forest density for retrievable SWE at Ku-band? Recent full wave simulations using Maxwell equations suggest that penetration through forests is higher than predicted by past models of radiative transfer.

(b) What is the saturation maximum depth retrievable SWE at X and Ku-bands? Using cross polarizations, can we have higher
580 depth of penetration such as 1 meter to 3 meters? (c) What is the impact of stratigraphy and how snow physics models can
help to retrieve SWE in the presence of stratigraphy? (d) How permafrost and the changing freeze depth in some areas would
affect the surface scattering contributions and the ability to subtract surface scattering estimated under snow-free conditions.
With 6 measurements in SWESARR which are co-polarization, and cross polarization at three frequencies, what are the
optimum combinations of polarization and frequencies for SWE retrieval?

585 **Table 3: summary of airborne deployments of active microwave sensors for snow studies.**

Airborne Campaign	Dates	Sensor	Freq.	Pol.	Location/snow regime	Data availability
CLPX-I, -II	2002, 2003	JPL POLSCAT	13.95 GHz	VV, VH, HV, HH	Colorado, USA / Alpine & prairie	NSIDC
SnowSAR	2010 -2011	ESA SnowSAR	9.6, 17.2 GHz	VV, VH	Sodankylä and Saariselkä, Finland / Taiga & tundra	ESA EO campaign portal
AlpSAR	2011 -2012	ESA SnowSAR	9.6, 17.2 GHz	VV, VH	Leutasch, Mittelbergferner, Rotmoos, Austria / Alpine	ESA EO campaign portal
TVCExp	2012 -2013	ESA SnowSAR	9.6, 17.2 GHz	VV, VH	Trail Valley Creek, NWT, Canada / Tundra	Not yet available
SnowEx '17	2017	ESA SnowSAR	9.6, 17.2 GHz	VV, VH	Grand Mesa, Colorado, USA / Alpine	NSIDC
TVCExp	2018-19	UMass Ku-InSAR	13.285 GHz	VV	Trail Valley Creek, NWT, Canada / Tundra	Not yet available
SnowEx '20	2020	NASA SWESARR	9.65, 13.6, 17.25 GHz	VV, VH	Grand Mesa, Colorado, USA / Alpine	NSIDC

*ongoing

3.3 Linking field measurements of snow with theoretical models of snow-radar interactions

Quantification of physical snow processes through objective measurements has revolutionized our understanding of microwave interactions with complex snowpacks at multiple scales (millimetre to kilometre). Objective methods of determining snow grain size in the field have only been available over the last decade. Prior to this, grain size was typically quantified visually with a hand lens or microscope (Fierz et al., 2009) and could be subject to errors of up to 1 mm in grain size estimation (Leppänen et al., 2015). Laboratory processing methods include gas absorption (Legagneaux et al., 2002) and thin section imaging techniques (H. Bader et al., 1939). As described in section 3.1.1, μ-CT measurements of snow samples obtained in the field have revolutionized our ability to model EM interaction from snow. Today, field-based instruments can quantify the snow specific surface area (SSA) rapidly in the field either through near-infrared reflectance (e.g. Gallet et al., 2009) or penetrometry (Proksch et al., 2015b). SSA is often related to an effective sphere diameter, that is the diameter of a sphere with the measured SSA (Mätzler, 2002). In practice, these metrics must often be scaled to match output from radiative transfer models (Montpetit et al., 2012). In addition to advances in sensors, experiement design has advanced significantly in support of radar remote sensing measurements: Appendix A provides an example experiment design that has been used in recent field campaigns. In practice, the time requirements of faster traditional measurements with longer history must be weighed against the newer measurements which are sometimes more time consuming with fewer trained operators. Here, we describe how this new knowledge of microscale variability over seasonal timescales can be leveraged to inform algorithms applied at landscape-scales.

3.3.1 Spatial variability of field measurements

At the landscape scale, understanding snow spatial variability is of critical importance with respect to the development of methodologies that can observe and model discrete and bulk properties of snowpack with low uncertainty. Mountains, hills, and valleys exert aerodynamic roughness controls on snowfall trajectory, enhancing snow accumulation and redistribution processes often dominated by blowing snow and sublimation. Exposed topography (e.g. alpine areas or open upland plateaus) are typically scoured of snow while enhanced accumulation is found in gullies or on the lee-side of plateaus (Pomeroy et al., 1993; Liston and Sturm, 1998). Once accumulated, the persistence of snow on the landscape is influenced by terrain slope and aspect which control a snowpack's energy budget; the incoming heat energy to north-facing slopes is radically different to that for south-facing slopes that can lead to pronounced variations of SWE at the landscape scale (Lopez-Moreno et al., 2014). Local slope angles also cause changes in the incidence angle of radar backscattering, which may impact assumptions underpinning microwave retrieval algorithms because rough surface scattering has a strong angular dependence.

The distribution of tree canopy, woody biomass, and the fragmentation characteristics of the vegetation stands play a significant role in how snow accumulates in a forested landscape. Metrics describing plant functional types (e.g. deciduous/coniferous or broadleaf/needleleaf, canopy densities and heights, etc.), are used to quantify spatial difference in simulations of sub-canopy snow and microwave radiative transfer. Correcting for forest microwave attenuation has shown that forest transmissivity plays

an important role in the observability of the sub-canopy snow. However, transmissivity changes through the season as the woody biomass undergoes progressive cooling at temperatures below 0° C (Li et al., 2020). Moreover, observed transmissivity of a tree stand is also impacted by the forest gap fraction or forest fragmentation. Landscape metrics can be used to characterize these ecological factors using high-spatial-resolution active and passive optical observations (Vander Jagt et al., 2013). The impact of low stand shrub vegetation is also important for snow accumulation in subalpine, tundra and sub-tundra regions, and in the understorey of forested environments. Shrub-dominated landscapes retain snow more effectively than graminoid plant cover but less than forest-covered regions (Marsh et al., 2010).

The soil type and state affect microwave observations of snow at the landscape scale because, at microwave wavelengths, the soil relative permittivity can play an important role in how reflected or backscattered energy is attenuated at the snow-ground interface. Generally, relative permittivity of soil is controlled by the texture, moisture content, and thermal heat content of the soil. Seasonal change in soil water state (liquid or frozen), is also important since relative permittivity changes significantly as the surface soil moisture changes state. This is all complicated by the variability in soil type at the landscape scale, and especially the mix of organic and inorganic content; peat soil landscapes are very complex in their microwave response whilst inorganic soils are somewhat simpler to characterize. In agricultural landscapes, especially post-harvest, the surface soil layer tends to be more spatially uniform and freeze earlier, making the variations in relative permittivity of the soil relatively constant.

In SWE retrieval, the snow-soil rough surface scattering and the forest effects on transmission and backscattering give bias in radar measurements. It is important to evaluate the magnitudes of these effects and how such bias in radar measurements vary with time.

3.3.2 Seasonal variability

Temporal change in snowpack properties have important implications for radar backscatter, in particular: 1) snow mass change, 2) metamorphism of snow microstructure, and 3) liquid water content and refreeze (ice lenses). High temporal resolution (hourly) measurement of snow mass accumulation and ablation using snow pillows, e.g. SNOTEL (Yan et al., 2018), or passive gamma radiation SWE sensors (Smith et al., 2017) provide excellent evaluation data to test SWE retrieval algorithms. However, such point measurements of SWE are spatially limited and seasonal variability in SWE is more commonly estimated through depth measurements, at a point using an acoustic sounder or spatially distributed from lidar, and periodically measured or modelled snow density. Uncertainties in modelled snow densities commonly dominate uncertainties in measured depth (Raleigh and Small, 2017).

Seasonal change in snow microstructural properties can strongly influence scattering of radar backscatter, especially in snowpacks of which depth hoar is a significant component. Constraining the proportions of snowpacks that have different scattering properties (e.g. surface hoar, wind slab, consolidated layers, indurated hoar or depth hoar) is required to prevent the retrieval of SWE from backscatter becoming an ill-posed problem. Frequent (weekly) objective profiles in snow pits (section 5.3) are optimal, however, in lieu of in-situ pit measurements, thermistors situated at different heights above the ground that

become sequentially buried in accumulating snow allow calculation of temperature gradients within the snowpack. Consistent temperature gradients can be used as a proxy for likely snow crystal type (Domine et al., 2008): rounded (<10° C m^{-1}), facets (10-20° C m^{-1}), depth hoar (>20° C m^{-1}). Where internal snowpack temperatures are not available, 2 m air temperatures and near surface soil temperatures can provide a bulk estimates of snow temperature gradients.

Profiles of liquid water content (LWC) are measured in-situ through insertion of dialectic devices (Denoth, 1994; Sihvola and Tiuri, 1986) into a snowpit wall. LWC can also be retrieved through non-invasive techniques using only GPS signal attenuation (Koch et al., 2019) or electrical self-potential (Thompson et al., 2016). Where mid-winter melt events are observed, either directly from LWC measurements or via inference from meteorological inputs, the chances increase of ice lens formation within the snowpack, which an important consideration for SAR backscatter retrievals. Snow wetness affects the radar backscattering (Stiles and Ulaby, 1980). The dielectric constants of wet snow have been modelled as a function of snow wetness (Ulaby and Long, 2015).

4 Characterization of snowpack properties using radar measurements

4.1 Describing the retrieval problem

In early studies, empirical models were proposed for SWE retrieval (Ulaby and Stiles, 1980; Drinkwater et al., 2001). These are unsuited for all snow types—e.g., ephemeral, prairie, maritime, and mountain snow, etc. (Sturm et al., 1995). Later investigators applied multiple channel measurements to determine snow parameters (Shi and Dozier, 2000; Rott et al., 2010). Recent algorithms (Cui et al., 2016; Xiong and Shi, 2017; Lemmetyinen et al., 2018; Zhu et al., 2018; King et al., 2019) are based on physical models in which RTM are used. Physical model-based retrieval algorithms consist of three parts: 1) a physical model of snow volume scattering, 2) estimation of a priori parameters, and 3) a cost-function inversion of the physical model to obtain SWE. An important limitation historically has been that there are fairly few in situ and airborne datasets on which to evaluate retrieval algorithms. This limitation is rapidly being overcome by recent observations, as described in section 3.2. In this section, we will describe the estimation of *a priori* parameters and SWE retrieval procedures.

Volume scattering of snowpack is a function of parameters including SWE, density, snow microstructure, and stratigraphy. Paramount for the success of the retrieval is the ability to predefine or constrain some of these unknown parameters, in particular the parameters that are used to characterize the snow microstructure. Based on the RTM, volume scattering is a function of snow depth, density, snow microstructure and layering structure (Rott et al., 2010; Zhu et al., 2018; King et al., 2018). A challenge is the non-uniqueness in inversion as different combinations of SWE and parameters of snow microstructure can give similar backscattering (Tsang et al., 2004; King et al., 2018). *A priori* estimates of parameters of snow microstructure can be used to improve the accuracy of retrieval by constraining the cost function with estimated statistical uncertainties.

Assuming normal distributions for the errors in forward simulations and observations of backscatter, the cost function of a maximum likelihood estimate for SWE and snow microstructure can be formulated as follows:

$$F = \left\{ \sum_{i=1}^{N} \frac{w_i}{2s_i^2} \left(\sigma_i^{obs} - \sigma_i^{model}(SWE, x) \right)^2 + \frac{w_x}{2s_x^2} (x - \bar{x})^2 \right\} \quad (3)$$

685 where σ_i^{obs} are radar observations from the ith channel, and N is the total number of channels for measurements. In CoReH2O, $N=4$ for VV and VH polarizations of X- and Ku-band. The backscattering predictions of snowpack are given by σ_i^{model}. In the above, s_i^2 are the error standard deviations of the radar measurements. The parameter x is related to snow microstructure, such as single scattering albedo, correlation length, and grain size. s_x^2 is the variance of *a priori* constraint. In Cui et al. (2016) and Zhu et al. (2018), s_i are assumed to be 0.5, which are based on the error standard deviations of radar measurements. w_i

690 and w_x are the weighting factors in the retrieval. Dual frequency retrievals are using either X- (9.6GHz) and Ku-band of 17.2 GHz as in CoReH2O or dual Ku-band of 13.6 GHz and 17.2 GHz as currently being proposed (see Section 6). However, cross polarizations have not been fully utilized and algorithms have been using the two co-polarizations of the dual frequency measurements. The two frequency measurements exploit the frequency dependence of volume scattering in snow. The two parameters that strongly influence the backscattering measurements are SWE and snow grain size. Then the problem becomes

695 retrieval of two parameters from two measurements.

The proposed algorithm in equation (3) has built off the CoReH2O (Rott etal 2010,approach. Such physical based retrieval approaches are quite general with (i) matching the data to the physical models , and (ii) a priori constraints on parameters. The actual implementation can have wide varieties of options and the importance is the validation against datasets of tower

700 and airborne measurements. Since the 2012 CoREH2O ESA report, there have been significant airborne and ground campaigns, as shown in Tables 2 and 3 providing much more data than were available prior to CoReH2O. In Section 4.3 , we will describe three algorithms that have been used successfully (Lemmetyinen et al., 2018; King et al., 2019, Zhu et al., 2018, Zhu etal 2021) . In particular , we will describe in more details the algorithm in Zhu etal 2018, Zhu etal 2021, and describe the validations with a series of tower and airborne measurements. In the CoREH2O cost function, there are several parameters

705 that require a priori estimates. The algorithm in Zhu etal 2018 , 2021 is more closely related to the NASA SMAP radar algorithm, by using regression to electromagnetic model simulations over a wide range of parameters, the number of parameters is significantly reduced. The strategy of this approach is to reduce the burden of a priori estimates of parameters for every scene. Nevertheless, it is important to stress that algorithms are still maturing.

710 **4.2 Constraining the retrieval problem with prior information**

Some of the challenges in retrieving snow properties from radar measurements can be addressed by using so-called "prior information". Prior information introduced in a retrieval problem or can be thought of in a Bayesian sense as discussed by Pulliainen (2006), or as "regularization". The cost function (equation 3) applies prior information as described in section 4.1, where x represented a snow microstructure related metric for which prior information is applied based on the final term on the

715 right of equation 3. More generally, priors could be applied to multiple terms in the retrieval problem including SWE, as done

in the proposed CoReH2O algorithm (ESA et al., 2012), or in a multi-layer sense, as illustrated for passive microwave remote sensing by Pan et al. (2017).

The degree to which prior information is applied to a problem can be thought of as a spectrum: the most minimal use of prior information is to remove the prior from the objective function but to specify a range of possible values for each prior, such as done by Thompson and Kelly (2021a). Specification of a prior on either grain size or single-scattering albedo can be considered moderate use of a priori information. The CoReH2O mission proposal specified an algorithm with prior on effective grain radius and SWE (ESA et al., 2012), building from the approach of the GlobSnow data product (Luojus et al., 2021). Cui et al. (2016) similarly specified priors for both optical thickness (an analog for SWE) and single-scattering albedo (an analog for microstructure). Zhu et al. (2018) built from the approach of Cui et al. by requiring only a single prior on single-scattering albedo. The algorithm of Zhu et al. requires only a "classification" of high or low single-scattering albedo. Maximal use of a priori information would be to use a dynamic simulation of snow microstructure processes to inform the retrieval. The model could be run "offline" and provide information on microstructure, or radar observations could be assimilated directly as done by Bateni et al. (2013, 2015).

Several studies have attempted to characterize the required precision of the priors on microstructure. ESA et al. (2012) found that an effective grain radius would need to be known with 15% of the true value. Rutter et al. (2019) similarly showed that microstructure would need to be known to within 10-15% in order to accurately retrieve SWE for field data in a tundra snow environment. These requirements are daunting. However, other approaches have indicated that microstructure information may not be required to be so precise. Thompson and Kelly (2021a) showed a successful inversion of SWE from in situ radar measurements in a prairie snow environment using a cost function specified with only minimal prior information (as defined the previous paragraph). The algorithm of Zhu et al. (2018) requires only the specification of whether the single scattering albedo is high or low: i.e. because the specification of a priori information is changed from a continuous to a categorical problem, the burden of a high precision prior is much alleviated. Bateni et al. (2013, 2015) demonstrated that maximal use of prior information in the context of an assimilations scheme could provide prior information from weather data and snow physics to successfully estimate SWE. Thus, even though the radiative transfer equations are highly sensitive to microstructure, and sensitivity analysis would indicate that priors must be specified to high precision, successful SWE inversions have been demonstrated without high precision priors. In the following subsections we review two ways of specifying prior information.

4.2.1 Leveraging snowpack information and snow classes

The simplest approach to specifying microstructure prior information for global SWE retrievals is to recognize the differences in snow types globally. The classification of Sturm et al. (1995) and Sturm and Liston (2021) specify differences in snow texture based upon temperature, precipitation and wind speed. Wind speed is mediated in many environments primarily by forest canopy height, and thus these three indicators can be specified by available land cover and meteorological information,

globally. Clearly defined physical processes such as vapor flux driven by temperature gradient link these three meteorological quantities to observable snow properties, such as the number of layers, vapor transport through the snowpack, and microstructure properties such as grain size. Sturm and Liston (2021) specify seven snow classes: tundra, boreal forest, prairie, montane forest, maritime and ephemeral globally at approximately 300 m spatial resolution. The relevance to microstructure properties is clear: tundra snow (e.g.) has far larger snow crystal size in its depth hoar layers than do taiga snow. In order for retrieval algorithms to leverage the predicted snow class to define *a priori* estimates to guide SWE retrievals, objective microstructure information would need to be specified for each snow class. The updated snow class of Sturm and Liston (2021) and the maturity of the methods to objectively measure microstructure described in section 3.3 have now made this a possibility that will guide SWE retrieval efforts from radar measurements in the future.

4.2.2 Snow microstructural models

4.2.2.1 Background

Across the electromagnetic spectrum, the interaction of radiation with snow cover is mediated by snow microstructure (West et al., 1993; Wiscombe and Warren, 1980; Nolin and Dozier, 2000). However, due to differing penetration depths, visible and near-infrared measurements are sensitive to grain size at the surface, whereas microwave measurements are sensitive to grain size at depth (Hall et al., 1986). The sensitivity of radar measurements to microstructure properties has been demonstrated by both models (Xu et al., 2012; Proksch et al., 2015a) and experiments (King et al., 2015; Rutter et al., 2019). Algorithms to retrieve SWE from radar backscatter typically solve for both SWE and some measure of snow microstructure (e.g. single-scattering albedo, correlation length) and regularization terms or prior information on microstructure is often included in the retrieval cost function (as described in the previous section; see Rott et al., 2010). In addition to important advances in measuring snow microstructure in the field, as described in previous sections, new work to simulate the evolution of snow grain size has indicated great potential for improving radar retrieval algorithms of SWE. In the cost function of retrieval algorithm, the *a priori* estimate term is $\frac{w_x}{2s_x^2}(x - \bar{x})^2$ with grain size being the most important *a priori* parameter.

To prevent confusion, it is important to begin with clear definitions for snow microstructure. Snow is a continuous, granular, bonded medium, composed of irregularly-shaped ice crystals, water vapor, liquid water, and void areas. The term "microstructure" commonly refers to snow grain size, shape, bonding, and distribution. Snow microstructure evolves both vertically within a snowpack and temporally throughout the snow season (as well as exhibiting significant horizontal spatial variability). The dendritic forms of new snowflakes sublimate, leading to a wide range of rounded or faceted shapes, depending on snowpack conditions. For many years, snow microstructure was referenced by the term "grain size". However, because "grain size" is an imprecise term, and because several metrics of snow microstructure play a role in radar backscatter, we will here simply refer to "snow microstructure" to encompass all measures of the snow medium; see Mätzler (2002) for a formal description of the various microstructural quantities. The most important and objective measure of snow microstructure is the snow specific surface area (SSA), which is often defined as the surface area of the ice-air interface to the mass of a control

volume of snow. SSA provides an objective measure that explains much of the microwave scattering processes. However, microwave interaction with microstructure cannot be entirely summarized by SSA; instead, radiative transfer is controlled by the spatial autocorrelation function (SAF) of the ice-air interface (Löwe and Picard, 2015). In the random medium model, the microstructure is described by a correlation function (Mätzler, 2002). In the bicontinuous medium model and the spherical scatterers models with stickiness, spatial correlation functions (SAF) have also been derived and have been related to the grain size and the aggregation parameter or the stickiness parameter (Chang et al., 2016). Thus, all microstructure characterizations in electromagnetic models can be related through the SAF. The SSA is a measure of the SAF at only the shortest spatial lags (e.g. ~10 µm); radar waves also respond to SAF at longer lags, (~100s µm). The SAF can be estimated using laboratory methods, such as micro-CT. Grain shape can play an important role in scattering, especially for the cross-polarization radar terms (Yueh et al., 2009). In summary, SSA has emerged as a practical and important microstructural property that both explains much variability in microwave scattering and can be measured in the field.

4.2.2.2 Microstructure evolution schemes: how they work

SSA evolves based on well-understood physical properties, providing a source of information to better inform SWE retrieval from Ku-band radar. Accurately modelling snow microstructure is not trivial, but decades of pioneering work by Colbeck (1982), Sturm (1989), Brun (1989), Brun et al. (1992), and Jordan (1991), among others, led to the development of snow metamorphism laws rooted in mass and energy conservation. The gravitational settling and metamorphism laws govern the temporal evolution of snow microstructure and its mechanical (e.g., snow stratification and shear stresses) and thermal (e.g., albedo and emissivity) properties. The metamorphism laws describe three types of grain growth mechanisms including: kinetic growth, equilibrium growth, and melt metamorphism (Lehning et al., 2002; Huang et al., 2012); kinetic and equilibrium growth are sometimes called constructive and destructive metamorphism, respectively.

Destructive metamorphism describes movement of water vapor from small grains with high curvature to larger grains with lower curvature. As a result, small grains and dendritic branches of large snow crystals evaporate and form larger and more spherical crystals. Constructive metamorphism is primarily driven by temperature gradients within the snowpack, resulting in direct vapor transport from warmer to colder surfaces. Sturm and Benson (1997) documented these processes in the Arctic. The snowpack temperature gradient, in turn, is simply the difference in temperature between the ground and the air, divided by the snowpack depth; typically snow covers insulate the ground, leading to soil being warmer than the ground. When snow is wet, the growth rate accelerates, compared with dry snow conditions. These fundamental physical processes have been explored for decades and solutions to the governing equations exist in a range of physical models.

4.2.2.3 Microstructure simulation accuracy

Snow microstructure model accuracy has improved significantly in recent decades, driven by improvements of field measurements and model techniques. Morin et al. (2013) used objective field-based measurements of snow specific surface area using the DUFISS instrument to evaluate the many-layer CROCUS snow model. Figure 11 clearly shows that the model captured the seasonal evolution of SSA. The r^2 fit values between observations and simulations ranged from 0.6 to 0.74.

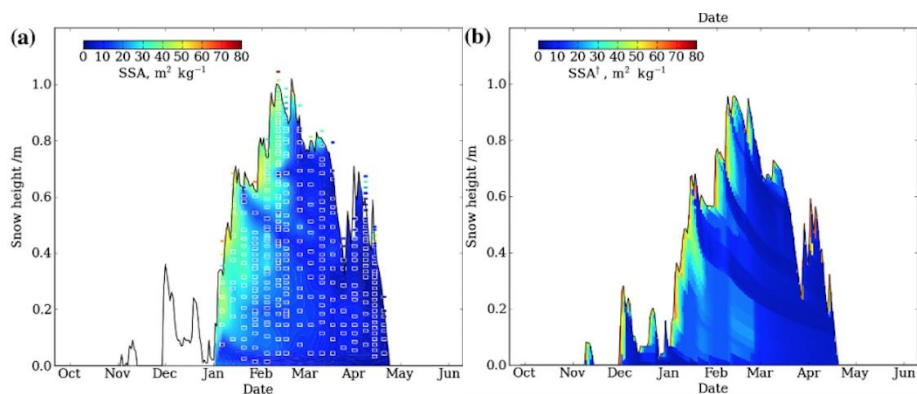



Figure 11: Observed and interpolated SSA observations (a) and SSA simulations (b). From Morin et al. (2013). The small white marks are the observations.

Use of microstructure simulations to constrain SWE retrievals require the additional step of coupling the microstructure simulation scheme and the RTM. Such studies have been explored more extensively in the context of passive microwave remote sensing (Kontu et al., 2017; Langlois et al., 2012; Larue et al., 2018). Exploring the accuracy of a coupled radar backscatter and snow physics model is an area for future work.

4.2.2.4 Implications for microwave remote sensing retrieval

Given the advances in microstructure modelling skill, retrieval of SWE from radar backscatter stands to benefit from incorporation of prior information on snow microstructure provided by snow physics models. Prior information could be provided in at least two ways. First, the radar backscatter could be assimilated directly into a coupled snow physics and RTM. This approach has been shown to be effective in assimilating passive microwave radiance. Assimilating backscatter has been demonstrated by Bateni et al. (2013, 2015) in the context of assimilating in situ backscatter observations. The second way that models could provide information to constrain SWE retrievals would be simply as a regularization term. In other words, the simulation model can produce a single estimate of a microstructure parameter such as SSA and the cost function could incorporate this as *a priori* information in Bayesian retrieval (as shown in equation 3 above).

4.2.2.5 Challenges and Future Work

In actual implementation of retrieval algorithms for global monitoring, there are needs of auxiliary information and *a priori* parameters. There are also needs on how to combine all these *a priori* information effectively in a retrieval algorithm. Computational efficiency needs to be achieved so that the retrieval algorithm can be operated in real time. Nonetheless with advances in computational resources, and examples of complex ground-processing segments from recent satellite missions, it can be envisioned that the latest advances in snow physics modeling and knowledge of microstructure can be applied to a future global satellite mission.

There are challenges associated with coupling snow physical models and RTMs. First, SWE simulations from snow physical models are often inaccurate, due to biases in the precipitation forcing. This happens mostly when information from weather stations is not available, and snow models must rely on atmospheric reanalysis data that are subject to biases, especially in the

840   precipitation amounts (Lindsay et al., 2014; Wrzesien et al, 2019b). Recent modelling work in Grand Mesa, CO shows however that biases in the simulations and analysis of higher resolution (~ 1km) numerical weather prediction models are significantly reduce leading to modelled SWE within ±10% of the observations (Cao and Barros, 2020). Changes in SWE have an immediate effect on several other snow properties, particularly snow microstructure, a critical parameter in radiative transfer models. Second, in snow physical models, SWE is inversely related to the grain size. When SWE decreases, temperature gradients

845   increase and grain growth is accelerated. In radiative transfer models, radar backscattering increase with SWE and with grain size. Backscattering is directly proportional to SWE and grain size. In SWE retrieval, SWE and grain size are independent parameters. When SWE increases and if the grain size stays constant, radar backscattering increases. However, in snow physical models, when SWE decreases, grain size increases and radar backscattering can increase or decrease due to the combined effects of SWE and grain size. This ambiguity emerges due to the nature of SWE, microstructure and backscatter

850   relations. An ongoing study has found that even for small changes in simulated SWE (+/- 10%), snow microstructure is affected enough to mislead the retrieval algorithm and deteriorate the SWE retrievals even further (Merkouriadi et al., accepted). These challenges can be addressed by introducing appropriate physical constraints to the retrieval algorithms.

There are multiple areas where simulations must continue to improve, including demonstrating skill in the context of varying degrees of forest cover. Additionally, most simulations focus on estimation of SSA. While SSA has been shown to be an

855   adequate summary of radiative transfer properties most of the time for visible and near-infrared remote sensing of clean snow, this is not the case in the microwave spectrum. To couple SSA to input to the RTMs, SSA must be related to SAF correlation length. Another subject of study is to use micro-CT to extract more information such as to relate to SAF. There are potentially useful synergies to be explored with retrieval of surface microstructure from visible and near-infrared measurements, in the context of radar retrievals of SWE. The retrieval algorithm shown earlier requires a classification rather than a precise value

860   of grain size. Thus, the study of the error tolerance for estimations of SSA should also be pursued. Retrievals using a two-layer physics model are the next step (King et al., 2018). Significant effort will be needed to address the question of how many layers are necessary to capture small changes in snowpack backscatter behavior and SWE, and how to solve the inverse problem in multi-layered snowpacks the number of and vertical structure of which changes in time.

4.3 Solving the retrieval problem: algorithms

865   Since the 2012 CoREH2O ESA report, there have been significant airborne and ground campaigns as shown in Tables 2 and 3 providing much more data than were available prior to CoReH2O. There presently four physical physical model-based retrieval algorithms that have been applied successfully (Lemmetyinen et al., 2018; Zhu et al., 2018, King et al., 2019). All four algorithms utilize the frequency dependence of snow volume scattering for X-band and the two Ku-bands. The importance

is the validation of the algorithms against the tower measurements listed in table 2 and the airborne measurements listed in Table 3.

Lemmetyinen et al. (2018) used a SWE retrieval scheme using both radar and radiometry measurements. The retrieval is based on the model of the expanded Microwave Emission Model for Layered Snowpack (MEMLS3&a) for simulation of both radar and radiometry observations (Proksch et al., 2015a). In the algorithm, the snow microstructure is represented by the effective correlation length, which is first retrieved with radiometry and in situ snow depth measurements. Then, retrieved correlation lengths are applied to constrain the SWE retrieval with radar observations. The algorithm has been validated with the Finnish NoSREx tower dataset listed in Table 2.

King et al. (2019) used a SWE retrieval algorithm which is a coupling of snow physics model, snow hydrology model and the physical model of predictions by SMRT (Picard etal 2018) based on two-layer snow modelling for dual Ku-band radar observations. The two-layer model accounts for the small grain size of new fallen snow versus the larger grain size beneath the new fallen snow. . The correlation length is based on *a priori* information from the snow physics model. The ancillary configuration parameters and *a priori* parameters of snowpack for the retrieval are provided by the snow hydrology model and the snow physics model. Ensembles are created and the minimization of the cost function is exercised using equation (3) with the uncertainties defined for the a priori parameters.   The algorithm was applied to SWE retrieval from data taken in the tundra environment from 2012-2013 of SnowSAR over TVC listed in Table 3. It is presently being applied to the UMass Ku-InSAR data taken over TVC in 2018-2019 as listed in Table 3

Recently, Thompson and Kelly (2021a) applied a new algorithm using no prior information in the cost function, in which an iterative search algorithm was run using the MEMLS 3&a model (Proksch et al., 2015a). They applied the algorithm in both one- and two- layer model on Canadian prairie snowpacks near agricultural fields. They were successfully able to retrieve SWE from in situ radar measurements.

4.4 Steps of Retrieval Algorithm and results

We next describe the third algorithm in Zhu etal 2018 and Zhu etal 2021 in more details. The algorithm has been applied and validated with 7 data sets in Tables 2 and 3. The results will be summarized at the end of this section. It is presently being applied to two more airborne datasets (Table 3) : SnowSAR 2017 over GrandMesa and UMass Ku-INSAR of TVCEXp in 2018-2019. The algorithm has similarities to the SMAP radar retrieval algorithm which has been applied to 6 months of SMAP radar globally from Jan 2015 to July 2015. An essence of the SMAP radar algorithm (Kim etal 2017) is to use regressions and classifications to reduce the backscattering sigma0 to be dependent on only three parameters: soil moisture, rms height of roughness and volumetric water content (VWC)

The SWE retrieval algorithm has three distinct features: 1) surface scattering are subtracted from radar observations; 2) the bicontinuous-DMRT model is used to derive regressions to simplify the dependence on parameters with the result that the copolarizations at X band and Ku band depend on only two parameters: SWE and scattering albedo. and 3) classification of snowpack into two classes (low albedo and high albedo) to mitigate the non-unique inversion problem. The detailed flow diagrams are in Zhu etal 2018. In Figure 12, we give a simplified flow diagram

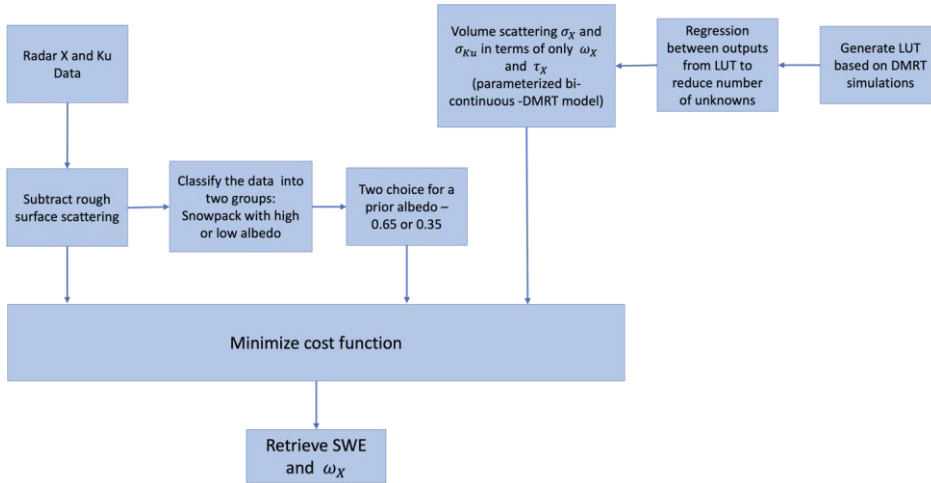



Figure 12: Simplified flow diagram of the algorithm; two measurements to retrieve two parameters with a prior binary choice of albedo. No prior estimate of SWE.

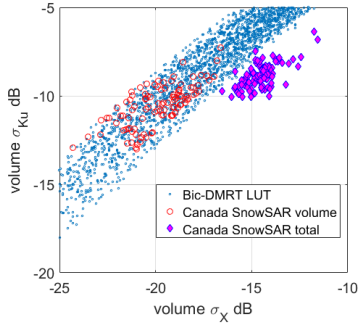
4.4.1 Steps of Retrieval algorithms

925

Figure 13: Canadian SnowSAR measurements compared with the Bic-DMRT LUT. Figure from Zhu et al. (2018).

step 1,: Subtraction of rough surface scattering : The rough surface contributions are subtracted from the radar measurements. The subtraction procedure is as described in 3.1.2 with several options. We show the case the SnowSAR data collected from the 2013 Canadian TVC campaign (King et al., 2018; Zhu et al., 2018) in Figure 13. SnowSAR flights were performed on

930 April 8 and 9, 2013 crossing each of the TVC sites. The SnowSAR collected data are shown in purple dots. The bicontinuous-DMRT simulations LUT are shown in blue dots. The SAR data show a bias when compared with X- and Ku-band DMRT simulations. The bias is attributed to the contributions from surface scattering . Since there are no measurements on the underlying soil in the 2013 Canadian TVC campaign, rough surface scattering are determined by differences between radar observations and snow volume scattering calculated based on snowpit measurements.. The rough surface bias in the Ku-band

935 data are 1 to 2 dB while, in the X-band data, the bias is about 4 to 6 dB, which indicates that the surface scattering has more influence at X-band. After subtraction of surface scattering from the SnowSAR data, the result SnowSAR data, shown in red dots, are assumed to contain only the volume scattering component. The red dots volume scattering components of the SnowSAR data fall into the range covered by the bicontinuous DMRT simulations. The dynamic range of SAR data is also larger with this subtraction.

940 Step 2, Regression training to reduce number of parameters: Regression trainings are applied to treduce the number of unknowns (Cui et al., 2016; Zhu et al., 2018; Zhu et al.,2021). Look-up table (LUT) are generated based on bicontinuous DMRT simulations of multiple scattering of snow volume scattering for various snow properties of snow depth, density, snow microstructure as represented by the kc and b parameters in the bicontinuous model . The output-dependent variables for the LUT are backscatter at X and Ku (σ_X and σ_{Ku}), the effective single scattering albedo at X and Ku (ω_X and ω_{Ku}), and optical

945 thickness at X and Ku (τ_X and τ_{Ku}) for X- and Ku-bands. Regression trainings are performed for $(i)\omega_X$ versus ω_{Ku} and (ii) τ_X versus τ_{Ku} to utilize the frequency dependence of scattering between the X- and Ku-bands.

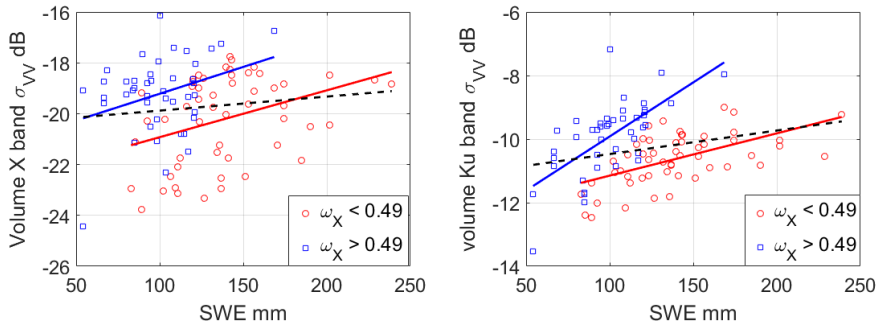
In Zhu et al. (2018), there are two trained relations that are derived from regressions. . The first regression trained relation is to train the multiple scattering solutions into effective first order solutions , $\sigma = A + B \log(\sigma^{1st})$, where σ is multiple volume scattering of snow and σ^{1st} is the first-order scattering. The coefficients A and B are given in Zhu et al. (2018) for X- and Ku-

950 bands. In the second regression trained relations, the relations between albedo at X- and Ku-band and between optical thickness at X- and Ku-band are trained to give $\omega_{Ku}(\omega_X)$ and $\tau_{Ku}(\tau_X)$. After these two sets of training, we then $\sigma^{1st} = 0.75 cos\theta_t \omega(1 - exp(-2\tau/cos\theta_t))$ (Cui et al., 2016; Zhu et al., 2018) and the regression relations, $\sigma_X = A_X + B_X \log(0.75 cos\theta_t \omega_X(1 - exp(-2\tau_X/cos\theta_t)))$ and $\sigma_{Ku} = A_{Ku} + B_{Ku} \log(0.75 cos\theta_t \omega_{Ku}(\omega_X)(1 - exp(-2\tau_{Ku}(\tau_X)/cos\theta_t)))$. The results and advantages of these regression trainings are that the multiple volume scattering at X and Ku bands, σ_X and σ_{Ku} , now only

955 depend on two parameters, ω_X and τ_X. The approach is labelled a "parameterized bicontinuous-DMRT model" (Cui etal 2016, Zhu etal 2018, Zhu etal 2021) .

Sep 3: Classification of data:

Following the strategy of SMAP radar retrieval, classification is performed. We use the dataset from the Canadian SnowSAR 2013 campaign as an example. The *a priori* information are obtained from co-located ground measurements. The

960 backscattering σ are classified into two groups: snowpack with high albedo and snowpack with low albedo. The threshold $\omega_X = 0.49$ is the average of all *a priori* albedos. Figure 14 shows that the sensitivities of backscatter to SWE are enhanced by classification of snowpack based on *a priori* scattering albedo. The classification scheme accounts for the heterogeneity of snow cover of varying grain sizes and SSAs from location to location.

965 **Figure 14: volume scattering of the Canada SnowSAR data as a function of SWE based on the retrieved scattering albedo ω_X at (a, left) X-band and (b, right) Ku-band. Radar observations are from a single flight. *A priori* estimates are used to classify ω_X into two classes. They are plotted by different coloured markers. The black dashed curve is the regression line of all Canada SnowSAR data. The blue and red solid curves are the regression lines for backscatter with ω_X larger and smaller than 0.49, respectively. Figure from Zhu et al. (2018).**

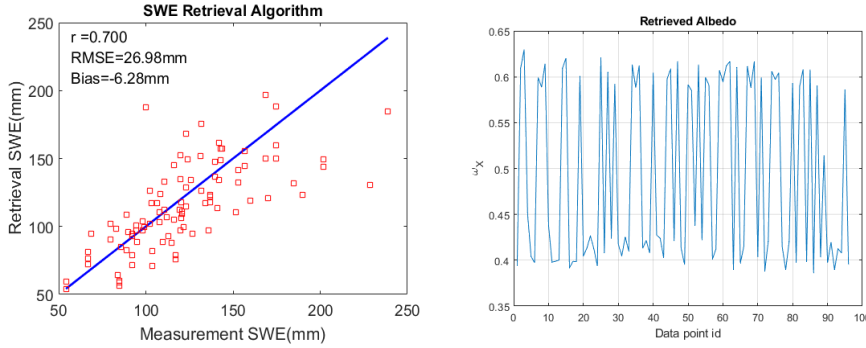



Figure 15: (a, left) SWE retrieval performance and (b, right) Scattering albedo retrieval using Canadian SnowSAR 2013 X- and Ku-band radar data. The figures are from Zhu et al. (2018) and Zhu, 2021.

Step 4, a priori estimates , binary choices and cost function minimization

A priori estimates of parameters are applied to determine the mean, the weight, and the uncertainty $\frac{w_p}{2s_p^2}(\omega_X - \overline{\omega}_X)^2$ of the cost function. *A priori* information can be obtained from co-located field stations or historical ground measurement data (Rott et al., 2010; Cui et al., 2016; Zhu et al., 2018In parametrizing microstructure, the snow grain size, correlation length (Proksch et al., 2015a) or scattering albedo (Cui et al., 2016; Zhu et al., 2018) are used.

In the implementation of Zhu et al. 2018 and Zhu etal 2021 algorithm, the co-polarization of X-band (9.6 GHz) and Ku-band (17.2 GHz) are utilized in the cost function below.

$$F = \text{MIN}\left\{ \frac{w_X}{2s_X^2}\left(\sigma_{X,VV}^{obs} - \sigma_{X,VV}^{obs,bg} - \sigma_{X,VV}^{model}(\tau_X, \omega_X)\right)^2 + \frac{w_{Ku}}{2s_{Ku}^2}\left(\sigma_{Ku,VV}^{obs} - \sigma_{Ku,VV}^{obs,bg} - \sigma_{Ku,VV}^{model}(\tau_X, \omega_X)\right)^2 + \frac{w_p}{2s_p^2}(\omega_X - \overline{\omega}_X)^2 \right\} \quad (4)$$

where the two unknown parameters to be retrieved are the scattering albedo at X-band (ω_X) and the optical thickness at X-band (τ_X). The input parameters are: $\sigma_{X,VV}^{obs}$ and $\sigma_{Ku,VV}^{obs}$ are radar observations at X and Ku band, $\sigma_{X,VV}^{obs,bg}$ and $\sigma_{Ku,VV}^{obs,bg}$ are background scattering, and $\overline{\omega}_X$ is a priori scattering albedo and in the Zhu etal 2018 and Zhu etal 2021 algorithm, $\overline{\omega}_X$ is based on a binary choice. In this minimization problem of the current implementation, there is no a priori estimate on SWE. The only a priori estimate is on the $\overline{\omega}_x$ and the choice is binary, either 0.65 or 0.35. If better estimation of $\overline{\omega}_X$ can be obtained by ground measurements, snow physical model (Xiong and Shi, 2017), or passive observations (Zhu et al., 2021), the retrieval performance can be improved. In equation (4) w_X, w_{Ku}, w_p, and s_p are user defined parameters. While $s_X, s_{Ku} = 0.5\ dB$ are instrument parameters.

995 The cost function of equation (4) with least squares is applied to the SAR data at X- and Ku-bands in 6. In this example, s_x is set to 0.1, and the weight factors are set to be unity We apply the two channel observations to retrieve the two parameters, ω_X and τ_X. Then using retrieved ω_X and τ_X the SWE is obtained by the relation $SWE = a(1 - \omega_X)\tau_X$, where a = 9745 (Cui etal 2016, Zhu et al., 2018, Zhu etal 2021).

1000

Results of Retrieval

 Figure 15 (a) shows the performance of the retrieval algorithm. The retrieval results have RMSE of ~27 mm of SWE, a correlation of 0.7, and a bias of 6.3 mm. The results show that the retrieval algorithm is particularly successful for SWE values below 150 mm. The performance satisfies requirements from the CoREH2O are the RMSE is less than 30 mm for SWE below
1005 300mm and the RMSE is less than 10% of SWE for SWE above 300 mm. In Figure 15(b), the retrieved scattering albedo ω_X ~~are~~ is also shown.

In the equation of cost function, the weight w_x is the measure attached to the *a priori* parameter. In the example of Figure 15, w_x is set to be 1. In Zhu et al. (2018), we have studied the retrieval performance variation by reducing w_x. The performance is still acceptable down to $w_x = 0.14$ with RMSE equal to 40 mm. Next, we study the performance with variations in surface
1010 scattering subtractions was also studied by adding noise to the best guess of surface scattering in Zhu et al. (2018). At the best guess with 0% noise, the RMSE of SWE is 27 mm. The RMSE of SWE retrieval increases with noise increase. However, even with 50% additional noise (absolute error of 3 dB in surface scattering), the performance has RMSE of 45 mm.

In Figure 16, we show 3 dimensional plots of the sigma0 at ~~X band and~~ Ku Band against the two variables of retrieved
1015 scattering albedo and retrieved SWE, along with a three-dimensional fitted plane for two domains: single-scattering albedo>0.49 and <0.49, respectively. The orientation of the two planes indicates that there is a larger dependence on single-scattering albedo for the data with single-scattering albedo>0.49. Thus, the data support that sigma0 is a function of both SWE and single-scattering albedo. ~~The results show the strong correlation of sigma0 when plotted against two variables.~~ On the other hand, Figure 17 shows the ~~2D~~ two-dimensional plot of sigma0 against the single variable of retrieved ~~swe~~SWE, and the
1020 two-dimensional fitted line for all of the data. This further illustrates the point shown in Figure 14: a scatterplot of SWE vs sigma0 alone is not expected to capture the full relationship between the two variables.~~.~~
~~The correlation of sigma0 is much weaker when plotted against one variable.~~ The results show the importance of plotting sigma0 versus two independent variables of swe and scattering albedo.

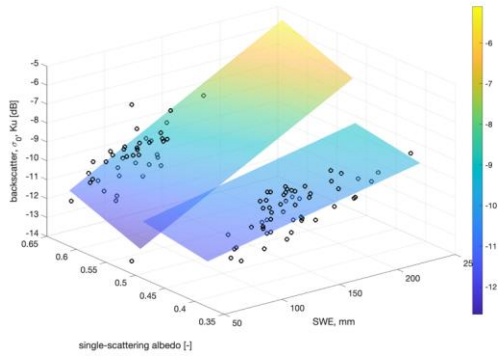
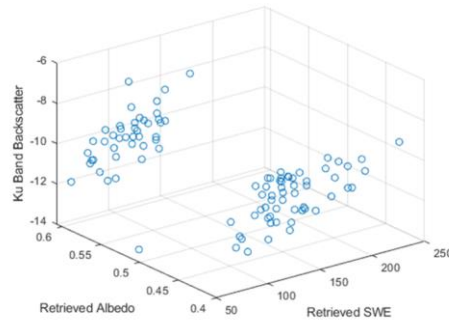
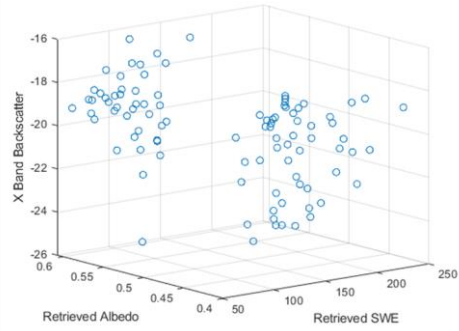



Figure 16: ~~(a, left)~~ 3-dimensional plot of the sigma0 when plotted against two variables at ~~X band (b, right) 3-dimensional plot of the sigma0 when plotted against two variables at~~ **Ku band** (black circles) along with a linear least-squares fits of sigma0 to two variables SWE and single-scattering albedo (surfaces). The surface color indicates sigma0 value in dB.

1030

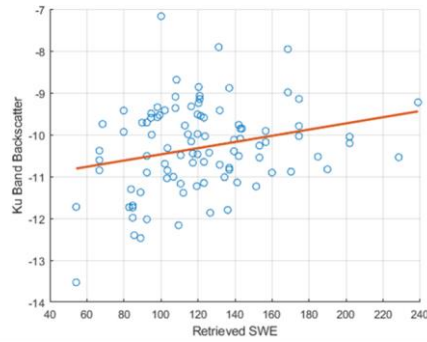
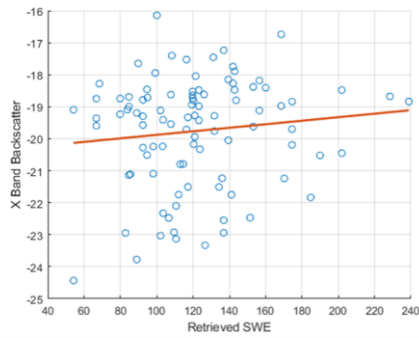
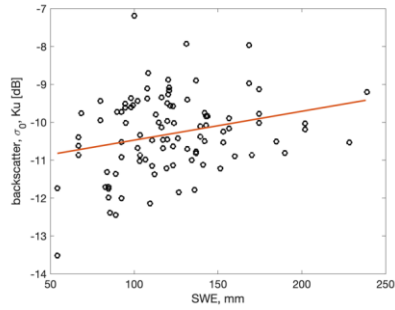



Figure 17: ~~(a, left) 2~~2D~~-dimensional~~ plot of sigma0 against the single variable of ~~retrieved SWE at X band (b, right) 2D plot of sigma0 against the single variable of retrieved~~ SWE at Ku band. The line represents a least squares linear fit between the two variables.

1035   The Zhu etal 2018 and Zhu etal 2021 have been applied to a total of 7 data sets of airborne and tower measurements as listed in Table 2 and Table 3. The performance of the retrieval algorithms for the 7 datasets and summarized in Table 4. The RMSE are generally good.

Dataset	Data Type	RMSE (mm)	Bias (mm)	SWE Range (mm)	Mean SWE (mm)	Location	Data Points

Canada SnowSAR 2013	Airborne	26.98	-6.28	50~250	127.14	Trail Valley Creek, Canada	103
Finland SnowSAR 2011		17.47	-6.12	90~150	123.6	Sodankylä, Finland	5
Finland SnowSAR 2012		24.23	-7.09	50~160	112.64	Sodankylä, Finland	28
NoSREx 2009-2010	Tower	26.30	14.50	60~200	121.69	Sodankylä, Finland	666
NoSREx 2010-2011		17.05	−0.70	40~140	72.34	Sodankylä, Finland	721
NoSREx 2012-2013		31.71	1.54	50~200	129	Sodankylä, Finland	686
SnowEX UWScat 2017		52.30	-38.01	440~7600	568.77	Grand Mesa, USA	4

1040

Table 4: Summary of validations of the dual frequency algorithm at 9.6GHz and 17.2 GHz (Zhu et al., 2018 and Zhu et al., 2021) against 7 datasets of airborne and tower measurements. Details of the 7 datasets are listed in Table 2 and 3.

~~summary of validations of the Zhu etal 2018 and Zhu etal 2021 algorithm against 8 datasets of airborne and tower~~
1045 ~~measurements. Details of the 7 datasets are listed in Table 2 and 3.~~

4.4.4 Future work

In the Zhu et al. (2018) algorithm illustrated above, a single layer is used. A multilayer snow model should also be considered.
1050 Studies have already been conducted using a two-layer model (King et al., 2018; King et al., 2019; Rutter et al., 2019) to account for small grain size in the upper layer and a larger grain size for the bottom layer (depth hoar). Accuracy requirements of *a priori* estimates to achieve desired retrieval skill have not yet been quantified. Future work should include systematic usage of cross polarizations in the retrieval algorithms. The inclusion of cross polarizations is important for deep snow layers

as the co-polarization K-band backscatter saturate for SWE larger than 300 mm. The Ku band cross polarization saturation can be shown using bi-continuous DMRT. The data for deep snow cross polarization at Ku band is quite limited.

5 Improving SWE retrieval estimations via synergy with other datasets

In satellite remote sensing, with the vast amount of satellite data, there can be data fusion of synergistic use of other data sets to refine the retrieval algorithms and improve the SWE estimations. The combined active and passive microwave remote sensing using data of the same frequencies has been an active area of research. Recent work shows the use of C-band Sentinel-1 data to retrieve SWE for deep snow layers. Interferometry and tomography are also studied for future launches of complementary missions. P-band GNSS-R has also been proposed for satellite retrieval of SWE.

5.1 Passive microwave

GCOM (Global Change Observation Mission) was launched in 2012 and carries the AMSR2 (Advanced Microwave Scanning Radiometer 2) instrument, measuring microwave brightness temperatures at 6 frequencies. The channels at 18.7 GHz and 36.5 GHz with both V and H polarizations have been used to retrieve global SWE. The spatial resolutions are coarse and are respectively at 22 km by 14 km for 18.7 GHz and 12 km by 7 km for 36.5 GHz. With overlapping footprints, interpolations algorithms have been applied (Long and Brodzik, 2016) to downscale resolution to 3 km. Uncertainty increases when downscaling resolution increases. Because the passive emissivity is related to the radar bistatic scattering (Tsang et al., 1982), the brightness temperatures are related to the radar backscattering cross sections. Since SAR observations (< 500 m) have much finer spatial resolutions than passive radiometry, a synergy is to use SAR at the X- and Ku-bands to downscale coarse resolution passive data or SWE products (Takala et al., 2011) to finer spatial resolutions using data assimilation or other algorithms.

Several other methods have been explored to combine the active and passive microwave observations to retrieve SWE. In Hallikainen et al. (2003), satellite microwave observations were used to demonstrate its feasibility to retrieve SWE by using passive-only, active-passive, and active-only algorithms in sub-arctic snow in Finland. Tedesco and Miller (2007) evaluated SWE retrieval performances by using active (Ku-band) and passive (X-band) microwave observations. Recently, Bateni et al. (2015) conducted SWE retrieval studies using passive (Ku- and Ka-bands) and active (L- and Ku-bands) ground-based microwave observations. The SWE retrieval was obtained within a data assimilation framework by comparing simulated microwave observations against the corresponding observations at multiple frequencies.

In the study of Lemmetyinen et al. (2018), the correlation length of snowpack is derived by matching both active and passive microwave observations against the simulations of the MEMLS3&a model (Proksch et al., 2015a) with ancillary data from snowpit measurements and weather stations. Next, the correlation length is used for the active radar algorithm to retrieve SWE. The derived correlation length from both active and passive data demonstrates an improvement of the SWE retrieval performance over the SWE retrieval with the active-only algorithm. Cao and Barros (2020) used a multilayer snow hydrology

1085 model coupled to MEMLS3&a to investigate the signature of the variability of snow physics on the microwave behavior at seasonal scales. They ound that a combined approach using active microwave sensing in the accumulation season and passive sensing in the melting season would yield in the best sensitivity to capture the temporal evolution of seasonal SWE by taking optimal advantage of microwave hysteresis (Ulaby et al., 1981, Kelly and Chang, 2003). The generalization of this approach to available active and passive microwave measurements with large resolution gap poses a significant challenge

1090 Recently, passive observations have been used to enhance the performance of the active algorithm (Zhu et al., accepted). The active-only algorithm was described earlier by using a cost function between simulated and observed radar observations as a function of the two parameters of scattering albedo and optical thickness. In this enhancement, passive observations at Ku- and Ka-bands at the collocated and coincident snow scene are used to determine the range of the scattering albedo. The bicontinuous DMRT model is applied for both passive and active model simulations. X- and Ku-band radar data are then used

1095 with the determined scattering albedo to obtain SWE. This active and passive combined method is applied to the NoSREx dataset. Comparison statistics show that the combined active-passive method has improved performance over the active-only method. The retrieval does not require *a prior* information and ancillary data from ground measurements.

5.2 C-band SAR

C-band radar can be used to detect wet snow by the strong decrease in backscatter (Stiles and Ulaby, 1980). Studies have
1100 shown contrasting results regarding the potential for SWE and snow depth retrieval but reviewing the literature on this topic is outside the scope of this manuscript. We here highlight that some recent studies have demonstrated the possibility of snow depth estimation for deep snow using C-band radar at cross-pol, thus making C-band possibly synergistic with the higher frequency approaches most applicable to shallower snow depths that are the focus of this manuscript.

1105 Lievens et al. (2019, 2021) developed an empirical change detection algorithm that was used to estimate snow depth at 1-km spatial resolution from S1 observations over all northern hemisphere mountain ranges (Lievens et al., 2019) and, with algorithm improvements, at sub-kilometer resolution over the European Alps (Lievens et al., 2021). The algorithm relies on the ratio of cross- to co-pol backscatter. Here, 300-m retrievals based on the S1 change detection approach are shown for Idaho, Montana and Wyoming, US. Figure 18 (a) shows a density plot, comparing weekly S1 retrievals for the periods between August and
1110 March from 2017 to 2020 with in situ measurements from 203 available SNOTEL sites. Figure 18 (b) shows the MAE relative to the snow depth (in %), illustrating that for shallow snowpacks (< 1 m) the MAE is on average ~50% with large variance. From a 1-m depth onwards, the relative average MAE remains constant at ~30%. Figure 18 (c) compares time series of snow depth retrievals and measurements for six selected SNOTEL sites. The ESA Sentinel-1 mission is the first C-band radar constellation that measures consistently (not regularly tasked) with the exact same orbit revisited every 6 days. Such consistent
1115 observation scenario benefits the change detection approach and could explain why limited success has been found with other C-band systems that must be tasked. The recent snow depth retrieval results from C-band SAR over mountainous regions with

deep snow indicate a strong complementarity with applications at higher frequencies – for example, Ku-band is much more sensitive to shallow snow, while C-band performs better in relative terms for deep snow.

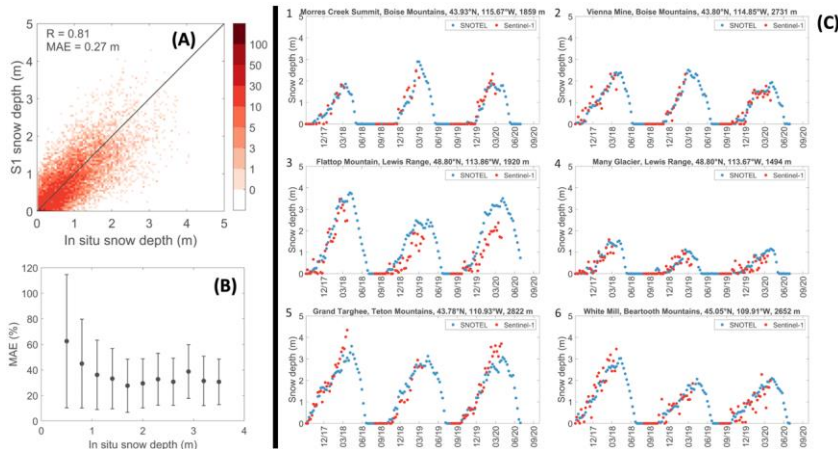



Figure 18: Snow depth retrieval from Sentinel-1, 2017-2020 in Idaho, Montana, and Wyoming. (a) Density plot of weekly 300-m resolution S1 snow depth retrievals, and coincident SNOTEL observations from 203 sites. (b) The corresponding mean and standard deviation of the absolute error between S1 retrievals and in situ measurements, stratified by the measured snow depth. (c) Time series comparison between snow depth from S1 and SNOTEL in situ measurements at six locations for three winter seasons. Note that the analysis includes snow-free conditions but excludes wet snow conditions as detected with the S1 algorithm (Lievens et al., submitted).

Despite the observational evidence of C-band cross-polarization sensitivity to deep snow, the underlying physical scattering mechanisms, and the associated impacts of snow properties, are still not fully understood. Snow crystals can form larger-scale clusters that are more similar in size compared to the C-band wavelength. Snow crystals are highly anisotropic (irregular in shape), that, in principle, results in a stronger scattering in cross-polarization. Thus, we would expect that snow microstructure plays a role in governing C-band response to SWE. Other contributions to snow scattering at C-band that can be investigated are larger-scale contrasts in snow density (incl. between snow layers) and the formation of ice layers with rough boundaries in deep snowpack. Recent progress in snow radiative transfer modelling is addressing the anisotropic shape of snow crystals and the clustering of crystals (Zhu et al., accepted) using a bicontinuous model that introduces a two-parameter correlation function (Ding et al., 2010) and show that large clustering of grains can cause cross-polarization signals from volume scattering that are in the range observed by S1, and that the volume scattering signal at cross-polarization can dominate over surface scattering for large snow depths. This hypothesized mechanism may explain why cross-polarized C-band radar is sensitive to SWE (Lievens et al., 2019), while co-pol is relatively insensitive to SWE (Naderpour et al., 2022). Further field-based studies of the

investigations of the effects of microstructure on C-band radar signals are ongoing. More work is needed to improve our understanding of the physical mechanisms that cause C-band sensitivity to snow mass.

5.3 Phase-based approaches

Approaches to estimating snow characteristics using microwave remote sensing almost invariably make use of some combination of the radar cross section σ^0, sensitivity to polarization, and frequency dependence; the techniques previously mentioned are all based on microwave scattering, which focus on the amplitude response. Approaches that use the signal phase, related to the electrical path length and time-of-flight information, while more challenging, can provide additional information about the snowpack, which is synergistic with the Ku-band backscatter approach that is the focus of this paper. These approaches provide independent information about snow properties through travel-time through layers, and information about where within the snowpack the major sources of amplitude (e.g. layer boundaries) are originating. The additional information could be used to improve the accuracy of the backscattering retrievals. Three techniques are described: 1) ultra-wideband radar, 2) tomography, and 3) interferometry.

5.3.1 Ultra-wideband radar

The range resolution of a radar system is inversely proportional to the bandwidth. Ultra-wideband radar can be used to resolve reflections from different depths within the snowpack. This not only provides insight into which locations within the snowpack are contributing most to the backscatter but also estimates the depth-dependent refractive index of snow, which can be used to independently estimate snow depth, SWE, and stratigraphy. However, the ultra-wideband radar technology does not have a straightforward path to space, due to bandwidth and frequency allocation limitations. Ultra-wideband approaches have been demonstrated for decades from the ground, using broadband radar at nadir incidence angles to estimate depth and SWE (for a review, see Marshall and Koh, 2008), using L-band GPR systems (Lundberg et al., 2000; McGrath et al., 2019) and at higher microwave frequencies (Gubler and Hiller, 1984); multi-channel L-band radar has recently been used to map density profiles in polar firn (Meehan et al., 2021). Nadir ultra-wideband FM-CW radar (2-18 GHz) has been flown from an aircraft platform with success in the polar regions as part of NASA Operation IceBridge, mapping snow depth on sea ice and stratigraphy in firn on the ice sheets (Panzer et al., 2013; Arnold et al., 2019). More recently, airborne FM-CW experiments have been done over seasonal snow in the mountains (Yan et al., 2017), with additional efforts being carried out at the University of Alabama in developing airborne tomography mountain applications (Taylor et al., 2020).

5.3.2 Tomography

Recently, Synthetic Aperture Radar (SAR) Tomography (TomoSAR) has been used in monitoring the snowpack from X-band to Ku-band (Laurent et al. 2015, Wiesmann et al. 2019, Rekioua et al. 2017, and Xu et al. 2018 & 2020). This technique provides unique access to the structure of the imaged scene, and in the case of snowpack, it enables the separation of multiple snow layers as well as the detection of and compensation for soil and vegetation layers. Polarimetric capabilities can be used

to decompose the backscattered signal into volumetric and surface scattering components, and to distinguish between snow, soil, and vegetation. Some ground-based field experiments have been carried out that demonstrate the focused image recovery of the layering structure of the snowpack with different densities, for example in a recent experiment (Xu et al., 2018) at Fraser Experimental Forest, Colorado, at X and Ku-bands (9.6, 13.5, 17.2 GHz). In Figure 19, we show the results of tomography carried at three frequencies for hh polarization. The tomograms demonstrate the layer structure and frequency dependence. The ability to identify snow layers and density changes are expected to significantly improve SWE retrieval.

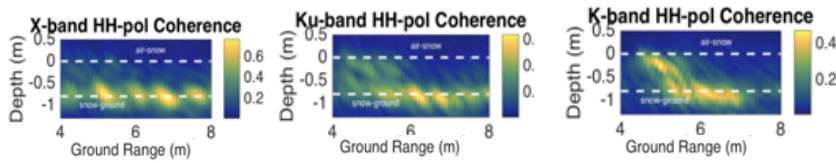



Figure 19:TomoSAR coherence images for hh polarization at 9.6 GHz , 13.5 GHz and 17.2 GHz at Fraser, Co sites.

5.3.3 Interferometry

Interferometry can be used to measure differential path length and changes in the electromagnetic path length in signals interacting with the seasonal snowpack. This technique has been proposed in several studies, both at high frequency with single-pass InSAR for mapping the snow surface, to measure snow depth (Moller et. al, 2017), and at low frequency with repeat-pass InSAR to measure changes in snow depth or SWE (Guneriussen et al., 2001; Deeb et al., 2011; Lei et al., 2016). Interferometry can be performed either between two observations separated in space (Figure 20 (A)), or by repeat observations after changes in snow occur (Figure 20 (B)). Although phase measurements are not absolute measurements (modulo 2π), there are a number of methods, including phase unwrapping, the use of a surface DEM, and modelled and measured SWE change, that can be used to resolve the ambiguity.

For the first approach (standard cross-track interferometry), using a high microwave frequency or in wet snow where the penetration depth would be limited, we can assume the majority of the signal comes from the snow surface, and the snow surface topography can be mapped. When this is differenced from a snow surface at a different time, a snow depth change can be estimated spatially. This implementation of interferometry is achieved through the introduction in the system of a second antenna separated from the transmitting antenna by the baseline B. Such an antenna can be passive, receiving the signal of a common transmitter antenna, and the phase difference between the two antennas is measured. The scattering phase center and the interferometric correlation magnitude can be measured, which are both sensitive to the frequency and polarization combinations as well as the snowpack physical characteristics (e.g. Rott et al., 2021).

In the second approach, a low microwave frequency in dry snow can be used, where we can assume the majority of the signal comes from the snow-ground interface (Figure 20 (B)). In this case, changes in the time of flight, or electromagnetic path length, to the snow-ground interface are caused by changes in snow depth and SWE. A time series of InSAR observations at L-band can thus potentially be used to estimate changes in snow depth and SWE. This technique was tested during the NASA SnowEx 2020 and 2021 experiments (Marshall et al., 2021). In addition, a similar approach with P-band has been demonstrated from tower-based platforms, using existing transmitted signals (Shah et al., 2017). This bistatic approach shows great promise for a much lower cost satellite system, as only a receiver is required.

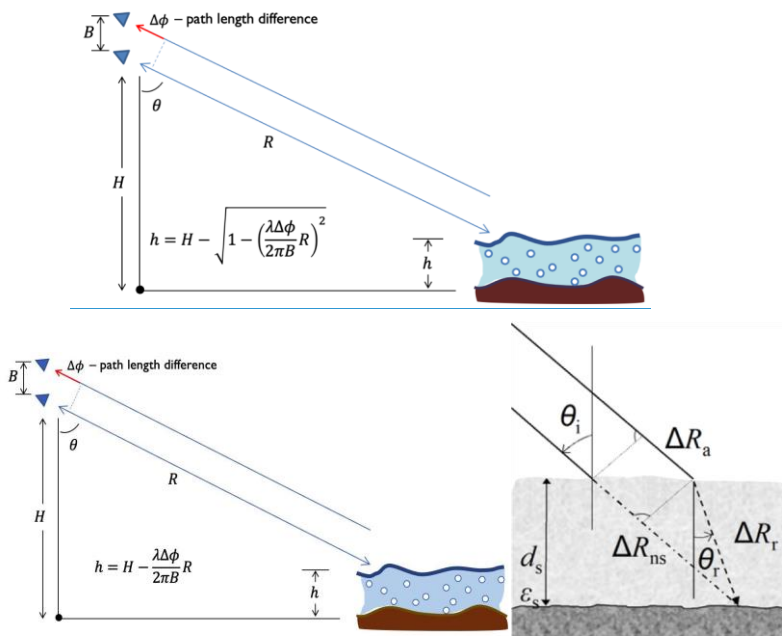



Figure 20: (A, left) Illustration of single-pass InSAR for mapping the snow surface. Using measured phase, $\Delta\phi$, simple trigonometric calculations are used to estimate the relative height, h, of the scattering phase center compared to the reference height, H. (B, right) When the phase center is below the snow surface, refraction in snow must also be taken into account. At low microwave frequencies (e.g. L-band) in dry snow, the phase center is often the snow-ground interface, and due to the slower electromagnetic velocity in snow, phase changes are related to changes in snow depth and density.

InSAR has been used for characterizing the volume scattering components of forests (e.g. Kugler et al., 2015), where a vertical profile of the volume density can be estimated (Reigber and Moreira, 2000; Tebaldini and Rocca, 2011). While most of this

development has been done at low-frequencies for vegetation, a scaling of the volume characteristics of snow with frequency
has been equally promising (Lei et al., 2016), especially at Ku- and Ka-band.

In Section 6, the planned TSMM mission will be described. With the interferometry set up as described in , we can explore possible configurations, such as the baseline B, of launching a companion satellite with receive-only, receiving the complex scattered electric field signal from the snow medium. Such a companion would be able to complement the planned baseline TSMM observations with additional measures of reflectivity, interferometric phase, and correlation magnitude that could all be used to better characterize the snow volume.

6 Planning a Satellite Mission

The earliest synthetic aperture radar (SAR) satellite missions were focused on C-band (~~Envisat~~ERS-1, Radarsat-1). Missions developed during recent decades extended the frequency range to L- (e.g. PALSAR) and X-band (e.g. TERRASAR-X), with planned missions at the P- (ESA-Biomass), and L- and S-bands (NASA-ISRO SAR mission). Spaceborne scatterometer missions such as QuikScat have illustrated the wide-ranging contributions of measurements at Ku-band to applications spanning the cryosphere (Kwok, 2007; Swan and Long, 2012), biosphere (Frolking et al., 2006), and ocean (Bourassa et al., 2010). Ku-band cloud radar measurements have made significant contributions to precipitation-related fields through missions like CloudSat (Stephens et al., 2002) and GPM (Skofronick-Jackson et al., 2017). ~~To date, however, there have been no SAR missions at Ku-band.~~

The potential for Ku-band radar to retrieve snow water equivalent (SWE) was explored as part of the NASA Snow and Cold Land Processes Mission and supporting Cold Land Processes Experiment (Yueh et al., 2009; Cline et al., 2009). The ESA COld REgions Hydrology High-resolution Observatory (CoReH2O; X- and Ku-bands; Rott et al., 2010; ESA et al., 2012) completed Phase A in 2013, but was not selected for implementation. CLPX and CoReH2O science and mission development activities played a major role in motivating the significant progress achieved over the past decade in measuring, understanding, and modelling the Ku-band radar response to SWE, snow microstructure, and snow wet/dry state (as assessed in previous sections of this review). Given this collective progress, satellite mission concept reviews following the completion of CoReH2O Phase A further emphasized the potential for Ku-band SAR measurements to address a broad set of user requirements related to seasonal snow mass.

Supported by these studies and continued analysis of experimental ground-based and airborne campaigns (See Section 4; King et al., 2018; Lemmetyinen et al., 2018; Zhu et al., 2018), a Ku-band SAR mission was selected as the most feasible approach to meet the operational requirements (wide swath/rapid revisit/short latency) of Environment and Climate Change Canada (ECCC) for spaceborne measurements sensitive to SWE. Since 2018, ECCC and the Canadian Space Agency (CSA) have partnered to advance the scientific and technical readiness of the "Terrestrial Snow Mass Mission" (TSMM), a Ku-band radar satellite with the primary science objectives focused on the provision of climate services related to seasonal snow, and

1245 improved operational environmental prediction including streamflow. The TSMM development effort is underpinned by engagement with Canadian industry, academia, and international partners.

Table 5: Summary of CoReH2O and TSMM missions.

	CoReH2O	**TSMM**
Frequencies	X band 9.6 GHz Ku band 17.2GHz	Ku band 13.5GHz Ku band 17.25GHz
Polarizations	VV, VH	VV, VH
Level 1 SAR image resolution	50m	Low resolution: 250m High resolution: 50m
Spatial Resolution of product	100m-500m	500m
Temporal	3 days repeat for Phase 1	5 days, Canada and other snow-covered area
Accuracy Requirements in SWE	3 cm RMSE, SWE <30 cm 10% for SWE > 30 cm	3 cm RMSE (non-alpine) 25% (alpine)
NES0	X band VV <-23dB & VH <-28dB Ku band VV<-29dB & VH<-25dB	13.5 GHz VV&VH < -26 dB 17.2 GHz VV&VH < -25 dB
Accuracy in σ_0	Stability <0.5 dB Abs. accuracy <1 dB	Stability <0.5 dB Abs. accuracy <1 dB (13.5 GHz) and <0.5 dB (17.2GHz)
Incident angle	$30 - 45°$	$23 - 50°$

Because TSMM is the first spaceborne Ku-band SAR mission of its typean 'Explorer' mission concept was developed by
1250 industrial partners in Canada to advance technological innovation and prove the scientific viability using a 'design-to-cost' approach. The resulting 'TSMM-Explorer' concept meets ECCC science requirements through dual frequency (13.5 and 17.25 GHz) Ku-band radar measurements at 500-m spatial resolution, with a 50-m spatial resolution mode across a 30 km swath available for specific regions (e.g. mountains areas) and targeted events (e.g. periods of high flood risk). An imaging swath of 250 km combined with a duty cycle of approximately 25% meets the requirement to image all of Canada and other global
1255 snow-covered areas every 7 days.

In the CoReH2O proposal, the dual frequencies were in the X-band at 9.6 GHz and the Ku-band at 17.2 GHz. ~~Based on the ground-based measurements and the airborne measurements, the Ku-band at 17.2 GHz has a dynamic range from -16 dB to~~

6 dB and shows good correlation with SWE. The X-band at 9.6 GHz has co-polarization dynamic range from -20 dB to -14 dB. The theoretical predictions of rough surface scattering at X-band, depending on penetration through the snow layer are from -20 dB to -12 dB. In TSMM, the X-band (9.6 GHz) is not chosen and is replaced by a low Ku-band at 13.5 GHz. Table shows a comparison between CoREH2O and the current TSMM concept. The TSMM frequencies were selected to fully exploit the frequency dependence of snow volume scattering through thedifferential sensitivities at 13.5 and 17.25 GHz to both SWE and snow microstructure. The dual frequencies will help address the ill-posed nature of retrieving SWE from a single Ku-band radar measurement (see Section 4c). The change in the lower frequency of CoReH2O (9.6 GHz) to TSMM (13.5 GHz) will result in less sensitivity to the underlying rough surface scattering effect, but sensitivity to deep snow will be reduced without the X-band measurement. Further study is needed in fine-grained mountain snowpacks to better understand the limits of sensitivity to deep snow at Ku-band. It is also possible to explore the use of cross-polarization at Ku-band for larger snow depth beyond 1 meter.

The approach to optimally integrate spaceborne radar measurements with state-of-the-art modelling systems is currently under development at ECCC. For applications which require a SWE retrieval, the radar backscatter measurements will be combined with snow property initial conditions (including snow microstructure; see Section 4) produced by an advanced version of the ECCC operational land surface model forced with short-range meteorological forecasts and precipitation analyses. Importantly, in areas without radar coverage (e.g. due to swath gaps) or where the radar-derived SWE retrieval is highly uncertain (e.g. due to wet snow or dense forest cover), the SWE analyses will be determined by numerical outputs from the land surface model. In this way, the remote sensing information is combined with modelling to create seamless coverage both in space and time, with minimized uncertainty. Another goal is to assimilate the Ku-band radar measurements directly in ECCC prediction systems without a SWE retrieval. For land surface data assimilation needs, the Ku-band backscatter will be directly assimilated, again with the land surface model providing the required ancillary information. This approach is analogous to how L-band radiometer measurements from the SMOS and SMAP missions have improved soil moisture analysis at ECCC through radiance-based assimilation (Carrera et al., 2019). Work remains to fully implement a forward radar model coupled with the physical snow model, building on recent developments in this field (Bateni et al., 2015; Merkouriadi et al., 2021).

While the dual-frequency Ku-band TSMM-Explorer concept meets the requirements at ECCC for enhanced snow remote sensing, this approach alone cannot solve all snow-related observational needs. For instance, volume scattering will be negligible under wet snow conditions, hence the need to implement the approach outlined above to combine satellite and model-derived information during snow melt. There are, however, opportunities to further exploit the baseline TSMM-Explorer concept through the development of companion satellites. This could take the form of a similar mission concept to improve coverage and revisit (e.g. a small SAR constellation). Development of a companion receive-only satellite is more challenging but would deliver a greater reward through the potential for InSAR-based snow depth retrievals under wet snow conditions (as previously explored with airborne Ka-band measurements by Moller et al. (2017)). This InSAR approach, as described in Section 5.3, necessitates pushing the performance envelope of the TSMM-Explorer SAR (bandwidth, increased high resolution mode imaging) and spacecraft (maintenance of a very tight baseline, hence very precise orbit control) which

introduces cost and complexity to the current scope of the mission. Still, the potential benefits of an InSAR capability are notable, so further study of these options is encouraged.

With the industrial Phase 0 now complete, the TSMM-Explorer mission has advanced into a mission planning phase at CSA.
1295 Technical readiness is being advanced through industrial investment focused on the radar antenna technologies. Scientific readiness for the mission continues to be enhanced by community-wide progress in field techniques (e.g. quantitative snow microstructure measurements; Section 3.3)), physical snow modelling (Section 4.2), data assimilation, and multi-frequency radar analysis (Section 4.4). The analysis of tower and airborne Ku-band radar datasets in collaboration with international partners is ongoing. Future airborne data acquisition plans are under development, including through the NASA SnowEx
1300 program. Collectively, these efforts serve to advance the TSMM-Explorer mission specifically, and snow-radar science in general.

7 Summary and Perspectives

Freshwater delivered by seasonal snow melt is a commodity of the utmost importance for human health and well-being, supports ~~nearly all~~ many sectors of the economy, sustains ecosystems, and poses risks by contributing to floods and sustaining
1305 drought events (Barnett et al., 2005; Li et al., 2017; Qin et al., 2020). At present, information on water stored as seasonal snow is highly uncertain. Because of surface monitoring limitations, satellite measurements are critical, but current missions are inappropriate for determining snow mass with the spatial, temporal, and accuracy characteristics required to deliver climate services, effective water resource management, and skilful environmental prediction such as streamflow.

Over the last decade, X- and Ku-band radar remote sensing technologies have shown clear potential for monitoring SWE.
1310 Scattering models now provide understanding of the contributions of volume and surface scattering, and the complicating effects of forests. Snow physical models have significantly advanced, and are capable of providing the required snow microstructure information required for forward and inverse modeling . Tower and airborne radar measurements, supported by dramatic improvements in field-based quantitative characterization of snow microstructure have provided a small but rapidly growing range of datasets to support modeling and retrieval studies. In the coming years, there is a clear need for more
1315 experimental measurement campaigns to fill information gaps (such as the influence of vegetation, and sensitivity to deep snow) and evaluate new SWE retrieval frameworks.. There will be more studies on coupling snow physical models to radiative transfer models so that they can be more effectively combined in retrieval algorithms with computational efficiency for real time retrievals.

We anticipate the continued development of satellite missions with Ku-band radars, which could be followed by synergistic
1320 instruments supporting techniqus such as Ku-band interferometry and tomography.

8 Competing Interest

Ludovic Brucker is a member of the editorial board of The Cryosphere.

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Table of Abbreviations

AIEM	Advanced Integral Equation Model
Can-CSI	Canadian CoReH2O Snow and Ice Experiment
CASIX	Canadian Snow and Ice Experiment
CF	Coniferous Forests
CMIP6	Coupled Model Intercomparison Project
CoReH2O	Cold Regions Hydrology Observatory
DMRT	Dense Medium Radiative Transfer
DMRT-ML	Dense Medium Radiative Transfer – Multiple Layers
EM	Electromagnetic
ESA	European Space Agency
FMCW	Frequency Modulated Continuous Wave
GNSS-R	Global Navigation Satellite System Reflectometry
HUT	Helsinki University of Technology
InSAR	Interferometric SAR
Lidar	Light detection and ranging
LUT	Look-Up Table
LWC	Liquid Water Content
MEMLS	Microwave Emission Model of Layered Snowpacks
MIMICS	Michigan Microwave Canopy Scattering
NMM3D	Numerical solutions of Maxwell's Equations in 3-D
NoSREx	Nordic Snow Radar Experiment

	NWP	Numerical Weather Prediction
	POLSCAT	Polarimetric Scatterometer
	QCA	Quasi-Crystalline Approximation
	SAR	Synthetic Aperture Radar
1355	SMAP	Soil Moisture Active and Passive
	SMOS	Soil Moisture and Ocean Salinity
	SMP	Snow Micropenetrometer
	SMRT	Snow Microwave Radiative Transfer
	SSA	Specific Surface Area
1360	SWE	Snow Water Equivalent
	SWESARR	Snow Water Equivalent SAR and Radiometer
	RTE	Radiative Transfer Equation
	RTM	Radiative Transfer Model
	UAVSAR	Unoccupied Aerial Vehicle Synthetic Aperture Radar
1365	μ-CT	Micro computed tomography

References

Abaza, M., V. Fortin, E. Gaborit, S. Belair, and C. Garnaud. 2020. Assessing 32-Day hydrological ensemble forecasts in the Lake Champlain–Richelieu River watershed. Journal of Hydrologic Engineering. 10.1061/(ASCE)HE.1943-5584.0001983

1370 Anttila, K., Manninen, T., Karjalainen, T., Lahtinen, P., Riihelä, A., and Siljamo, N.: The temporal and spatial variability in submeter scale surface roughness of seasonal snow in Sodankylä Finnish Lapland in 2009–2010, Journal of Geophysical Research: Atmospheres, 119, 9236-9252, doi: 10.1002/2014jd021597, 2014.

Arnold E, Leuschen C, Rodriguez-Morales F, Li J, Paden J, Hale R, Keshmiri S (2019). CReSIS airborne radars and platforms for ice and snow sounding. Annals of Glaciology 1–10. https://doi.org/10.1017/aog.2019.37

1375 Attema, EPW and FT Ulaby , Vegetation modeled as a water cloud, Radio Science, vol. 13, pp357-364. 1978

Bader, H., Haefeli, R., Bucher, E., Neher, J., Eckel, C., and Thams, C.: Der Schnee und seine Metamorphose, Beitr. Geol. Schweiz, Geotechn. Ser. Hydrol, 3, 1-313, 1939.

Barnett, T. P., Adam, J. C., and Lettenmaier, D. P.: Potential impacts of a warming climate on water availability in snow-dominated regions, Nature, 438, 303 309, https://doi.org/10.1038/nature04141, 2005.

1380 Bateni, S. M., Huang, C., Margulis, S. A., Podest, E., and McDonald, K.: Feasibility of characterizing snowpack and the freeze–thaw state of underlying soil using multifrequency active/passive microwave data, IEEE Transactions on Geoscience and Remote Sensing, 51, 7, 4085-4102, 2013.

Bateni, S.M , S. A. Margulis, E. Podest and K. C. McDonald.: Characterizing Snowpack and the Freeze–Thaw State of Underlying Soil via Assimilation of Multifrequency Passive/Active Microwave Data: A Case Study (NASA CLPX

1385 2003), IEEE Transactions on Geoscience and Remote Sensing, vol. 53, no. 1, pp. 173-189, doi: 10.1109/TGRS.2014.2320264, 2015.

Bindlish, R., and Barros, A.P.: Sub-Pixel Variability of Remotely-Sensed Soil Moisture- An Intercomparison Study of SAR and ESTAR. *IEEE Transactions in Geoscience and Remote Sensing*, Vol. 40, 326-337, doi: 10.1109/36.992792, 2002.

Formatted: English (United States)

1390 Biskaborn, B.K., Smith, S.L., Noetzli, J. et al. Permafrost is warming at a global scale. Nat Commun 10, 264 (2019). https://doi.org/10.1038/s41467-018-08240-4

Bourassa, M. A., and McBeth Ford, K.: Uncertainty in scatterometer-derived vorticity. Journal of Atmospheric and Oceanic Technology, 27(3), 594-603, 2010.

Brun, E.: Investigation on wet-snow metamorphism in respect of liquid-water content. Annals of glaciology, 13, 22-26, 1989.

1395 Brun, E., David, P., Sudul, M., and Brunot, G.: A numerical model to simulate snow-cover stratigraphy for operational avalanche forecasting. Journal of Glaciology, 38(128), 13-22, 1992.

Cao, Y. and Barros, A.P.: Weather-Dependent Nonlinear Microwave behavior of Seasonal High-Elevation Snowpacks. *Remote Sensing*, 12,3422; doi:10.3390/rs12203422, 2020.

Carrera, M. L., Bilodeau, B., Bélair, S., Abrahamowicz, M., Russell, A., and Wang, X.: Assimilation of passive L-band
1400 microwave brightness temperatures in the Canadian land data assimilation system: Impacts on short-range warm season numerical weather prediction. Journal of Hydrometeorology, 20(6), 1053-1079, 2019.

Chabot, M., Lindsay, J., Rowlandson, T., and Berg, A.: Comparing the Use of Terrestrial LiDAR Scanners and Pin Profilers for Deriving Agricultural Roughness Statistics, Canadian Journal of Remote Sensing, 44, 1-16, doi: 10.1080/07038992.2018.1461559, 2018.

1405 Chang, T. C., Gloersen, P., Schmugge, T., Wilheit, T. T., and Zwally, H. J.: Microwave emission from snow and glacier ice. Journal of Glaciology, 16(74), 23-39, 1976.

Chang, W., Tan, S., Lemmetyinen, J., Tsang, L., Xu, X., and Yueh, S. H.: Dense media radiative transfer applied to SnowScat and SnowSAR. IEEE Journal of Selected Topics in Applied Earth Observations and Remote Sensing, 7(9), 3811-3825, 2014.

1410 Chang, W., Ding, K. H., Tsang, L., and Xu, X. (2016). Microwave scattering and medium characterization for terrestrial snow with QCA–Mie and bicontinuous models: Comparison studies. IEEE Transactions on Geoscience and Remote Sensing, 54(6), 3637-3648.

Chen, K. S., Wu, T. D., Tsang, L., Li, Q., Shi, J., and Fung, A. K.: Emission of rough surfaces calculated by the integral equation method with comparison to three-dimensional moment method simulations. IEEE Transactions on
1415 Geoscience and Remote Sensing, 41(1), 90-101, 2003.

Cline, D., Yueh, S., Chapman, B., Stankov, B., Gasiewski, A., Masters, D., ... and Mahrt, L.: NASA cold land processes experiment (CLPX 2002/03): Airborne remote sensing. Journal of Hydrometeorology, 10(1), 338-346, 2009.

Coccia, A., Trampuz, C., Imbembo, E., and Meta, A.: First results of snowSAR, the new X-and Ku-Band polarimetric airborne SAR sensor supporting the CoReH2O mission. In Workshop on Advanced RF Sensors and Remote Sensing
1420 Instruments, 2011.

Cohen, J., Lemmetyinen, J., Pulliainen, J., Heinilä, K., Montomoli, F., Seppänen, J., and Hallikainen, M. T.: The effect of boreal forest canopy in satellite snow mapping—A multisensor analysis. IEEE Transactions on Geoscience and Remote Sensing, 53(12), 6593-6607, 2015.

Colbeck, S. C.: An overview of seasonal snow metamorphism, Rev. Geophys., 20(1), 45– 61, doi:10.1029/RG020i001p00045,
1425 1982.

Cui, Y., Xiong, C., Lemmetyinen, J., Shi, J., Jiang, L., Peng, B. et al.: Estimating snow water equivalent with backscattering at X and Ku band based on absorption loss, Remote Sensing, 8(6), 505. doi:10.3390/RS8060505, 2016.

Dall, J.: InSAR Elevation bias caused by penetration into uniform volumes, IEEE Trans. Geosc. Remote Sensing, 45(7), 2319–2324, 2007.

1430

Deeb, E.J., R.R. Forster, and D.L. Kane, "Monitoring snowpack evolution using interferometric synthetic aperture radar on the North Slope of Alaska, USA," Int. J. Rem. Sens., 32(14) , 3985-4003, 2011.

Deems, J. S., Painter, T. H., and Finnegan, D. C.: Lidar measurement of snow depth: a review. Journal of Glaciology, 59(215), 467-479, 2013.

1435 Derksen, C., J. King, S. Belair, C. Garnaud, V. Vionnet, V Fortin, J. Lemmetyinen, Y. Crevier, P. Plourde, B. Lawrence, H. van Mierlo, G. Burbidge, and P. Siqueira. 2021. Development of the Terrestrial Snow Mass Mission. *International Geoscience and Remote Sensing Symposium*, July, 2021

Ding, K. H., Xu, X., and Tsang, L.: Electromagnetic scattering by bicontinuous random microstructures with discrete permittivities. IEEE Transactions on Geoscience and Remote Sensing, 48(8), 3139-3151, 2010.

1440 Drinkwater, M. R., Long, D. G., and Bingham, A. W.: Greenland snow accumulation estimates from satellite radar scatterometer data. Journal of Geophysical Research: Atmospheres, 106(D24), 33935-33950, 2001.

Deems, J. S., Painter, T. H., and Finnegan, D. C.: Lidar measurement of snow depth: a review. Journal of Glaciology, 59(215), 467-479, 2013.

De Lannoy, G., R. Reichle, P. Houser, K. Arsenault, N. Verhoest, and V. Pauwels. 2010. Satellite-scale snow water equivalent
1445 assimilation into a high-resolution land surface model. Journal of Hydrometeorology. 11: 352-369.

Denoth, A.: An Electronic Device for Long-Term Snow Wetness Recording, in: Annals of Glaciology, Vol 19, 1994 - Proceedings of the Symposium on Applied Ice and Snow Research, edited by: Jones, S. J., Annals of Glaciology, 104-106, 1994.

Deschamps-Berger, C., Gascoin, S., Berthier, E., Deems, J., Gutmann, E., Dehecq, A., Shean, D., and Dumont, M.: Snow
1450 depth mapping from stereo satellite imagery in mountainous terrain: evaluation using airborne laser-scanning data, The Cryosphere, 14, 2925–2940, https://doi.org/10.5194/tc-14-2925-2020, 2020

Domine, F., Albert, M., Huthwelker, T., Jacobi, H.-W., Kokhanovsky, A. A., Lehning, M., Picard, G., and Simpson, W. R.: Snow physics as relevant to snow photochemistry, Atmospheric Chemistry and Physics, 8, 171-208, 2008.

Elfouhaily, T. M., and Johnson, J. T.: A new model for rough surface scattering. IEEE transactions on geoscience and remote
1455 sensing, 45(7), 2300-2308, 2007.

ESA: Report for Mission Selection: CoReH2O, ESA SP-1324/2 (3 volume series), European Space Agency, Noordwijk, The

Netherlands, 2012.

https://earth.esa.int/eogateway/documents/20142/37627/CoReH2O-Report-for-Mission-Selection-An-Earth-Explorer-to-

observe-snow-and-ice.pdf

1460

Fassnacht, S. R., Stednick, J. D., Deems, J. S., and Corrao, M. V.: Metrics for assessing snow surface roughness from digital imagery, Water Resour. Res., 45, 6, doi: 10.1029/2008wr006986, 2009.

Ferrazzoli, P., and Guerriero, L.: Radar sensitivity to tree geometry and woody volume: A model analysis. IEEE Transactions on Geoscience and Remote Sensing, 33(2), 360-371, 1995.

1465 Fierz, C., Armstrong, R. L., Durand, Y., Etchevers, P., Greene, E., McClung, D. M., Nishimura, K., Satyawali, P. K., and Sokratov, S. A.: The International Classification for Seasonal Snow on the Ground, IHP-VII Technical Documents in Hydrology No.83, IACS Contribution No.1, UNESCO-IHP, Paris., 2009.

Gallet, J. C., Domine, F., Zender, C. S., and Picard, G.: Measurement of the specific surface area of snow using infrared reflectance in an integrating sphere at 1310 and 1550 nm. The Cryosphere, 3(2), 167-182, 2009.

1470

Ferrazzoli , L. Guerriero; G. SchiavonExperimental and model investigation on radar classification capability, IEEE Transactioons on Geoscience and Remote Sensing, vol. 37, No2, pp960-968, March 1999

Frolking, S., Milliman, T., McDonald, K., Kimball, J., Zhao, M., and Fahnestock, M.: Evaluation of the SeaWinds
1475 scatterometer for regional monitoring of vegetation phenology. Journal of Geophysical Research: Atmospheres, 111(D17), 2006.

Fung, A. K., Chen, K. S., and Chen, K. S.: Microwave scattering and emission models for users. Artech house. 2010.

Grünewald, T. Schirmer, M., Mott, R., and Lehning M.: Spatial and temporal variability of snow depth and ablation rates in a

small mountain catchment, The Cryosphere, 4, 215-225, 2010.

1480

Gu, W., Tsang, L., Colliander, A., and Yueh, S.: Wave Propagation in Vegetation Field Using a Hybrid Method. IEEE Transactions on Antennas and Propagation, vol. 69, No 10, pp 6752-6761 , October 2021.

Gu, W., Tsang, L., Colliander, A., and Yueh, S , Multifrequency Full-Wave Simulations of Vegetation Using a Hybrid Method, IEEE Transactsions on Microwave Theory and Techniques , vol. 70, No. 1, pp275-285 Jan 2022

Gubler, H., Hiller, M., 1984. The use of microwave FMCW radar in snow and avalanche research. Cold Reg. Sci. Technol. 9, 109–119.

Guneriussen, T., Hogda, K.A., Johnson, H., and Lauknes, I.: InSAR for estimating changes in snow water equivalent of dry snow, IEEE Trans. Geosc. Rem. Sens. 39(10), 2101-2108, 2001.

Hall, D. K., Chang, A. T. C., and Foster, J. L.: Detection of the depth-hoar layer in the snow-pack of the Arctic coastal plain of Alaska, USA, using satellite data. Journal of Glaciology, 32(110), 87-94, 1986.

Hallikainen, M. T., Ulaby, F. T., and Van Deventer, T. E.: Extinction behavior of dry snow in the 18-to 90-GHz range. IEEE Transactions on Geoscience and Remote Sensing, (6), 737-745, 1987.

Hallikainen, M.T., Halme, P., Takala, M. and Pulliainen, J.,: Combined active and passive microwave remote sensing of snow in Finland. In IGARSS 2003. 2003 IEEE International Geoscience and Remote Sensing Symposium. Proceedings (IEEE Cat. No. 03CH37477) (Vol. 2, pp. 830-832). IEEE. 10.1109/IGARSS.2003.1293934, 2003.

Huang, S., Tsang, L., Njoku, E. G., and Chan, K. S.: Backscattering coefficients, coherent reflectivities, and emissivities of randomly rough soil surfaces at L-band for SMAP applications based on numerical solutions of Maxwell equations in three-dimensional simulations. IEEE Transactions on Geoscience and Remote Sensing, 48(6), 2557-2568, 2010.

Huang, S., and Tsang, L.: Electromagnetic scattering of randomly rough soil surfaces based on numerical solutions of Maxwell equations in three-dimensional simulations using a hybrid UV/PBTG/SMCG method. IEEE Transactions on Geoscience and Remote Sensing, 50(10), 4025-4035, 2012.

Huang, C., Margulis, S. A., Durand, M. T., & Musselman, K. N. (2012). Assessment of Snow Grain-Size Model and Stratigraphy Representation Impacts on Snow Radiance Assimilation: Forward Modeling Evaluation. IEEE Transactions on Geoscience and Remote Sensing, 50(11), 4551–4564. https://doi.org/10.1109/tgrs.2012.2192480.

Huang, H., Tsang, L., Njoku, E. G., Colliander, A., Liao, T. H., and Ding, K. H.: Propagation and scattering by a layer of randomly distributed dielectric cylinders using Monte Carlo simulations of 3D Maxwell equations with applications in microwave interactions with vegetation. IEEE Access, 5, 11985-12003, 2017.

Huang, H., Tsang, L., Colliander, A., and Yueh, S. H.: Propagation of Waves in Randomly Distributed Cylinders Using Three-Dimensional Vector Cylindrical Wave Expansions in Foldy–Lax Equations. IEEE Journal on Multiscale and Multiphysics Computational Techniques, 4, 214-226, 2019.

Ishimaru, A.: Wave propagation and scattering in random media (Vol. 2, pp. 336-393). New York: Academic press, 1978.

Johnson, J. T., Warnick, K. F., and Xu, P.: On the geometrical optics (Hagfors' law) and physical optics approximations for scattering from exponentially correlated surfaces. IEEE transactions on geoscience and remote sensing, 45(8), 2619-2629, 2007.

Jordan, R.: A one-dimensional temperature model for a snow cover: Technical documentation for SNTHERM. 89 (No. CRREL-SR-91-16). Cold Regions Research and Engineering Lab Hanover NH, 1991.

Karam M. A. , A. K. Fung, R. H. Lang and N. S. Chauhan, "A microwave scattering model for layered vegetation", *IEEE Trans. Geosci. Remote Sens.*, vol. 30, no. 4, pp. 767-784, Jul. 1992.

Kelly, R. E.J., and Chang, A.T.C.: Development of a Passive Microwave Global Snow Depth Retrieval Algorithm for Special Microwave Imager (SSM/I) and Advanced Microwave Scanning Radiometer- EOS (AMSR-E) data. Radio Science, Vol. 38, No.4, 8076, Doi: 10.1029/2002RS002648, 2003.

Kerbrat, M., Pinzer, B., Huthwelker, T., Gäggeler, H. W., Ammann, M., and Schneebeli, M.: Measuring the specific surface area of snow with X-ray tomography and gas adsorption: comparison and implications for surface smoothness. Atmospheric Chemistry and Physics, 8(5), 1261-1275, 2008.

Kim, S. B., Tsang, L., Johnson, J. T., Huang, S., van Zyl, J. J., and Njoku, E. G.: Soil moisture retrieval using time-series radar observations over bare surfaces. IEEE Transactions on Geoscience and Remote Sensing, 50(5), 1853-1863, 2012.

1535   Kim, S. B., Moghaddam, M., Tsang, L., Burgin, M., Xu, X., and Njoku, E. G.: Models of L-band radar backscattering coefficients over global terrain for soil moisture retrieval. IEEE Transactions on Geoscience and Remote Sensing, 52(2), 1381-1396, 2014.

Kim S. -B. et al., "Surface Soil Moisture Retrieval Using the L-Band Synthetic Aperture Radar Onboard the Soil Moisture Active–Passive Satellite and Evaluation at Core Validation Sites," in *IEEE Transactions on Geoscience and Remote*

1540   *Sensing*, vol. 55, no. 4, pp. 1897-1914, April 2017

Kim, R. S., Kumar, S., Vuyovich, C., Houser, P., Lundquist, J., Mudryk, L., ... and Wang, S.: Snow Ensemble Uncertainty Project (SEUP): Quantification of snow water equivalent uncertainty across North America via ensemble land surface modeling. The Cryosphere, 15(2), 771-791, 2021.

Kinar, N. J., and Pomeroy, J. W.: Measurement of the physical properties of the snowpack. Reviews of Geophysics, 53(2),

1545   481-544. doi:10.1002/2015RG000481, 2015.

King, J. M., Kelly, R., Kasurak, A., Duguay, C., Gunn, G., and Mead, J. B.: UW-Scat: A ground-based dual-frequency scatterometer for observation of snow properties. IEEE Geoscience and Remote Sensing Letters, 10(3), 528-532, 2012.

King, J., Kelly, R., Kasurak, A., Duguay, C., Gunn, G., Rutter, N., ... and Derksen, C.: Spatio-temporal influence of tundra

1550   snow properties on Ku-band (17.2 GHz) backscatter. Journal of Glaciology, 61(226), 267-279, 2015.

King, J., Derksen, C., Toose, P., Langlois, A., Larsen, C., Lemmetyinen, J. et al.: The influence of snow microstructure on dual-frequency radar measurements in a tundra environment, Remote Sensing of Environment, 215, 242-54. doi: 10.1016/j.rse.2018.05.028, 2018.

King, J., Derksen, C., Toose, P., Montpetit, B., and Siqueira, P.: Seasonal Ku-band (13.5 GHz) SAR measurements in a snow-

1555   covered tundra basin, The ASAR workshop 2019, Montreal, Canada, 2019.

Koch, F., Henkel, P., Appel, F., Schmid, L., Bach, H., Lamm, M., Prasch, M., Schweizer, J., and Mauser, W.: Retrieval of Snow Water Equivalent, Liquid Water Content, and Snow Height of Dry and Wet Snow by Combining GPS Signal Attenuation and Time Delay, Water Resour. Res., 55, 4465-4487, doi: https://doi.org/10.1029/2018WR024431, 2019.

Kontu, A., Lemmetyinen, J., Vehviläinen, J., Leppänen, L., and Pulliainen, J.: Coupling SNOWPACK-modeled grain size

1560   parameters with the HUT snow emission model. Remote sensing of environment, 194, 33-47, 2017.

Kugler, F., Lee, S. K., Hajnsek, I., and Papathanassiou, K. P. (2015). Forest height estimation by means of Pol-InSAR data inversion: The role of the vertical wavenumber. IEEE Transactions on Geoscience and Remote Sensing, 53(10), 5294-5311.

Kugler, F., Schulze, D., Hajnsek, I., Pretzsch, H., and Papathanassiou, K.: TanDEM-X Pol-InSAR performance for forest

1565   height estimation, IEEE Trans. Geosc. Rem. Sens., 52 (10), 6404 – _6421, 2014.

Kurt, S., and Tavli, B.: Path-Loss Modeling for Wireless Sensor Networks: A review of models and comparative evaluations. IEEE Antennas and Propagation Magazine, 59(1), 18-37, 2017.

Kwok, R. Near zero replenishment of the Arctic multiyear sea ice cover at the end of 2005 summer. Geophysical Research

1570   Letters, 34(5), 2007.

Langlois, A., Royer, A., Derksen, C., Montpetit, B., Dupont, F., and Goïta, K.: Coupling the snow thermodynamic model SNOWPACK with the microwave emission model of layered snowpacks for subarctic and arctic snow water equivalent retrievals. Water Resources Research, 48(12), 2012.

Larue, F., Royer, A., Sève, D. D., Roy, A., and Cosme, E.: Assimilation of passive microwave AMSR-2 satellite observations

1575   in a snowpack evolution model over northeastern Canada. Hydrology and Earth System Sciences, 22(11), 5711-5734, 2018.

Legagneux, L., Cabanes, A., and Dominé, F.: Measurement of the specific surface area of 176 snow samples using methane adsorption at 77 K. Journal of Geophysical Research: Atmospheres, 107(D17), ACH-5, 2002.

Lehning, M., Bartelt, P., Brown, B., Fierz, C., and Satyawali, P.: A physical SNOWPACK model for the Swiss avalanche

1580   warning: Part II. Snow microstructure. Cold regions science and technology, 35(3), 147-167, 2002.

Lei, Y., Siqueira, P., and Treuhaft, R.: A dense medium electromagnetic scattering model for the InSAR correlation of snow. Radio Science, 51(5), 461-480, 2016.

Leinss, S., Löwe, H., Proksch, H., and Kontu. A.: Modeling the evolution of the structural anisotropy of snow, The Cryosphere, 14, 51 –75 2020.

1585

Lemmetyinen, J., Pulliainen, J., Rees, A., Kontu, A., Qiu, Y., and Derksen, C.: Multiple-layer adaptation of HUT snow emission model: Comparison with experimental data. IEEE Transactions on Geoscience and Remote Sensing, 48(7), 2781-2794, 2010.

Lemmetyinen, J., Pulliainen, J., Kontu, A., Wiesmann, A., Mätzler, C., Rott, H., Volgmeier. Et al.: Observations of seasonal

1590   snow cover at X and Ku bands during the NoSREx campaign, EUSAR 2014; 10th European Conference on Synthetic Aperture Radar, 3-5 June 2014, Berlin Germany, 2014.

Lemmetyinen, J., Kontu, A., Pulliainen, J., Vehviläinen, J., Rautiainen, K., Wiesmann, A. et al. : Nordic snow radar experiment, Geosci. Instrum. Methods Data Syst, 5, 403–415. doi:10.5194/gi-5-403-2016, 2016.

Lemmetyinen, J., Derksen, C., Rott, H., Macelloni, G., King, J., Schneebeli, M., ... and Pulliainen, J.: Retrieval of effective

1595   correlation length and snow water equivalent from radar and passive microwave measurements. Remote Sensing, 10(2), 170, 2018.

Leppänen, M., Korpi, A., Yli-Pirilä, P., Lehto, M., Wolff, H., Kosma, V. M., ... and Pasanen, P.: Negligible respiratory irritation and inflammation potency of pigmentary TiO2 in mice. Inhalation toxicology, 27(8), 378-386, 2015.

Li, Q., Kelly, R., Lemmetyinen, J., and Pan, J.: Simulating the influence of temperature on microwave transmissivity of trees

1600   during winter observed by spaceborne microwave radiometer. IEEE Journal of Selected Topics in Applied Earth Observations and Remote Sensing, 13, 4816-4824, 2020.

Li, D., Wrzesien, M. L., Durand, M., Adam, J., and Lettenmaier, D. P.: How much runoff originates as snow in the western United States, and how will that change in the future?, Geophys Res Lett, 44, 6163–6172, https://doi.org/10.1002/2017gl073551, 2017.

1605 Liang, D., Xu, X., Tsang, L., Andreadis, K. M., and Josberger, E. G.: The effects of layers in dry snow on its passive microwave emissions using dense media radiative transfer theory based on the quasicrystalline approximation (QCA/DMRT). IEEE Transactions on Geoscience and Remote Sensing, 46(11), 3663-3671, 2008.

Liao, T.-H., Kim, S.-B., Tan, S., Tsang, L., Su, C., & Jackson, T. J. (2016). Multiple Scattering Effects With Cyclical Correction in Active Remote Sensing of Vegetated Surface Using Vector Radiative Transfer Theory. *IEEE Journal*

1610   *of Selected Topics in Applied Earth Observations and Remote Sensing*, 9(4), 1414–1429. https://doi.org/10.1109/jstars.2015.2505638

Lievens, H., Demuzere, M., Marshall, H. P., Reichle, R. H., Brucker, L., Brangers, I., … De Lannoy, G. J. M.: Snow depth variability in the Northern Hemisphere mountains observed from space. Nature Communications, 10(1), 1–12. https://doi.org/10.1038/s41467-019-12566-y, 2019.

1615 Lievens, H., Brangers, I., Marshall, H.-P., Jonas, T., Olefs, M. and De Lannoy, G. J. M.: Sentinel-1 snow depth retrieval at sub-kilometer resolution over the European Alps, The Cryosphere, 16, 159–177, 2022, https://doi.org/10.5194/tc-16-159-2022Lindsay, R., Wensnahan, M., Schweiger, A., and Zhang, J.: Evaluation of seven different atmospheric reanalysis products in the arctic, J. Clim., 27(7), 2588–2606, doi:10.1175/JCLI-D-13-00014, 2014.

Ling, H., Chou, R. C., and Lee, S. W.: Shooting and bouncing rays: Calculating the RCS of an arbitrarily shaped cavity. IEEE

1620   Transactions on Antennas and propagation, 37(2), 194-205, 1989.

Liston, G. E., and Sturm, M.: A snow-transport model for complex terrain. Journal of Glaciology, 44(148), 498-516, 1998.

Long, D. G., & Brodzik, M. J. (2016). Optimum Image Formation for Spaceborne Microwave Radiometer Products. *IEEE Transactions on Geoscience and Remote Sensing*, 54(5), 2763–2779. https://doi.org/10.1109/tgrs.2015.2505677

López-Moreno, J. I., Revuelto, J., Gilaberte, M., Morán-Tejeda, E., Pons, M., Jover, E., et al. (2014). The effect of slope aspect

1625   on the response of snowpack to climate warming in the Pyrenees. *Theoretical and Applied Climatology*, 117(1–2), 207–219. https://doi.org/10.1007/s00704-013-0991-0

Löwe, H., Riche, F., and Schneebeli, M.: A general treatment of snow microstructure exemplified by an improved relation for thermal conductivity. The Cryosphere, 7(5), 1473-1480. https://doi.org/10.5194/tc-7-1473-2013, 2013.

Formatted: English (United States)

Löwe, H. and Picard, G.: Microwave scattering coefficient of snow in MEMLS and DMRT-ML revisited: the relevance of sticky hard spheres and tomography-based estimates of stickiness, The Cryosphere, 9, 2101–2117, doi:10.5194/tc-9-2101-2015, 2015.

Lundberg, A., Thunehed, H., Bergström, J., 2000. Impulse radar snow surveys—influence of snow density. Nordic Hydrol. 31 (1), 1–14.

Lundquist, J., Hughes, M., Gutmann, E., and Kpnick, S.: Our skill in modleing mountain rain and snmow is bypassing the skill of our observational netwrks. Bull. American Meteorological Society, 2473-2490, DOI:10.1175/BAMS-D-19-0001.1, 2019.

Lundy, C. C., Edens, M. Q., and Brown, R. L.: Measurement of snow density and microstructure using computed tomography, Journal of Glaciology, 48, 312-316, doi: 10.3189/172756502781831485, 2002.

Luojus, K., J. Pulliainen, M. Takala, J. Lemmetyinen, C. Mortimer, C. Derksen, L. Mudryk, M. Moisander, P. Venäläinen, M. Hiltunen, J. Ikonen, T. Smolander, J. Cohen, M. Salminen, K. Veijola, and J. Norberg. 2021. GlobSnow v3.0 Northern Hemisphere snow water equivalent dataset. Scientific Data.

Manickam, S., and Barros, A.P.: Parsing Synthetic Aperture Radar Measurements of Snow in Complex Terrain: Scaling Behavior and Sensitivity to Snow Wetness and Landcover. *Remote Sensing*, *12*(3), 483; 10.3390/rs12030483, 2020.

Marsh, P., Bartlett, P., MacKay, M., Pohl, S., and Lantz, T.: Snowmelt energetics at a shrub tundra site in the western Canadian Arctic. Hydrological Processes, 24(25), 3603-3620, 2010.

Marshall, H.P. and Koh, G. (2008). FMCW radars for snow research. Cold Regions Science and Technology, 52(2):118-131

Marshall, H.P., Deeb, E., Forster, R., Vuyovich, C., Elder, K., Hiemstra, C., and Lund, J. (2021). L-band InSAR depth retrieval during the NASA SnowEx 2020 campaign: Grand mesa, Colorado. Proceedings of the IEEE International Geoscience and Remote Sensing Symposium (IGARSS). , 625-627.

Mätzler, C.: Improved Born approximation for scattering of radiation in a granular medium. Journal of Applied Physics, 83(11), 6111-6117, 1998.

Mätzler, C.: Relation between grain-size and correlation length of snow. Journal of Glaciology, 48(162), 461-466, 2002.

McGrath, D., Webb, R., Shean, D., Bonnell, R., H.P. Marshall, Painter, T., Molotch, N., Elder, K., Hiemstra, C., and Brucker, L. (2019). Spatially extensive ground-penetrating radar snow depth observations during NASA's 2017 SnowEx campaign: Comparison to in situ, airborne, and satellite observations. Water Resources Research, 55(11):10026-10036

Meehan, T. G., H.P. Marshall, Bradford, J. H., Hawley, R. L., Overly, T. B., Lewis, G., Graeter, K., Osterburg, E., and McCarthy, F. (2021). Historical surface mass balance reconstruction 1984-2017 from greentracs multi-o_set ground-penetrating radar. Journal of Glaciology, 67:219-228

Meloche, J., Royer, A., Langlois, A., Rutter, N., and Sasseville, V.: Improvement of microwave emissivity parameterization of frozen Arctic soils using roughness measurements derived from photogrammetry, International Journal of Digital Earth, 1-17, doi: 10.1080/17538947.2020.1836049, 2020.

Merkouriadi, I., Lemmetyinen, J., Liston G. E., and Pulliainen, J.: Challenges of assimilating active and passive microwave signatures with a physical model to estimate snow water equivalent. Water Resources Research, accepted, 2021.

Meta, A., Imbembo, E., Trampuz, C., Coccia, A., and De Luca, G.: A selection of meta sensing airborne campaigns at L-, X- and Ku-band. In 2012 IEEE International Geoscience and Remote Sensing Symposium (pp. 4571-4574). IEEE, 2012.

Meyer, J., Skiles, S. M., Deems, J., Bormann, K., and Shean, D.: Mapping snow depth and volume at the alpine watershed scale from aerial imagery using Structure from Motion. The Cryosphere Discussions, 1-17, 2021.

Mironov, V. L., Dobson, M. C., Kaupp, V. H., Komarov, S. A., and Kleshchenko, V. N.: Generalized refractive mixing dielectric model for moist soils. IEEE transactions on Geoscience and Remote sensing, 42(4), 773-785, 2004.

Moller, D., Andreadis, K. M., Bormann, K. J., Hensley, S., and Painter, T. H.: Mapping snow depth from Ka-band interferometry: Proof of concept and comparison with scanning lidar retrievals. IEEE Geoscience and Remote Sensing Letters, 14(6), 886-890, 2017.

Montpetit, B., Royer, A., Langlois, A., Cliche, P., Roy, A., Champollion, N., ... and Obbard, R.: New shortwave infrared albedo measurements for snow specific surface area retrieval. Journal of Glaciology, 58(211), 941-952, 2012.

Montomoli, F., Macelloni, G., Brogioni, M., Lemmetyinen, J., Cohen, J., and Rott, H.: Observations and simulation of multifrequency SAR data over a snow-covered boreal forest. IEEE Journal of Selected Topics in Applied Earth Observations and Remote Sensing, 9(3), 1216-1228, 2016.

Morin, S., Domine, F., Dufour, A., Lejeune, Y., Lesaffre, B., Willemet, J. M., ... and Jacobi, H. W.: Measurements and modeling of the vertical profile of specific surface area of an alpine snowpack. Advances in water resources, 55, 111-120, 2013.

Mousavi, S., De Roo, R., Sarabandi, K., and England, A. W.: Retrieval of Snow or Ice Pack Thickness Variation Within a Footprint of Correlation Radiometers. IEEE Geoscience and Remote Sensing Letters, 17(7), 1218-1222, 2019.

Mudryk, L., C. Derksen, P. Kushner, and R. Brown. 2015. Characterization of Northern Hemisphere snow water equivalent datasets, 1981–2010. Journal of Climate. 28: 8037-8051.

Mudryk, L., M. Santolaria-Otín, G. Krinner, M. Ménégoz, C. Derksen, C. Brutel-Vuilmet, M. Brady, and R. Essery. 2020. Historical Northern Hemisphere snow cover trends and projected changes in the CMIP-6 multi-model ensemble, The Cryosphere. 14, 2495–2514, DOI: 10.5194/tc-14-2495-2020.

Nagler, T., Roth, H., Ripper, E., Bippus, G., and Hetzenecker, M.: Advancements for snowmelt monitoring by means of Sentinel-1 SAR, Remote Sensing, 8, 348, 2016.

Natali, S.M., Watts, J.D., Rogers, B.M. et al. Large loss of CO_2 in winter observed across the northern permafrost region. Nat. Clim. Chang. 9, 852–857 (2019) doi:10.1038/s41558-019-0592-8

Nolin, A. W., and Dozier, J.: A hyperspectral method for remotely sensing the grain size of snow. Remote sensing of Environment, 74(2), 207-216, 2000.

Obu, J. S. Westermann, A. Bartsch, N. Berdnikov, H. Christiansen, A. Dashtseren, R. Delaloye, B. Elberling, B. Etzelmüller, A. Kholodov, A. Khomutov, A. Kääb, M. Leibman, A. Lewkowicz, S. Panda, V. Romanovsky, R. Way, A. Westergaard-Nielsen, T. Wu, J. Yamkhin, and D. Zou. 2019. Northern Hemisphere permafrost map based on TTOP modelling for 2000–2016 at 1 km2 scale, Earth-Science Reviews,193, 299-316,doi.org/10.1016/j.earscirev.2019.04.023, 2019.

Oh, Y., Sarabandi, K., and Ulaby, F. T.: An empirical model and an inversion technique for radar scattering from bare soil surfaces. IEEE transactions on Geoscience and Remote Sensing, 30(2), 370-381, 1992.

Oh, Y., and Kay, Y. C. (1998). Condition for precise measurement of soil surface roughness. IEEE transactions on geoscience and remote sensing, 36(2), 691-695, 1998.

Pan, J., M.T. Durand, B.J. Vander Jagt, and D. Liu. Application of a Markov Chain Monte Carlo algorithm for snow water equivalent retrieval from passive microwave measurements. Remote Sensing of Environment, 192, 150-165, 2017.

Panzer, B., D. Gomez-Garcia, Carl. Leuchen, J. Paden, F. Rodriguez-Morales, A. Patel, T. Markus, B. Holt, P. Gogineni. An ultra-wideband, microwave radar for measuring snow thickness on sea ice and mapping near-surface internal layers in polar firn. Journal of Glaciology, Vol. 59, No. 214, 2013 doi:10.3189/2013JoG12J128, 2013.

Peplinski, N. R., Ulaby, F. T., and Dobson, M. C.: Dielectric properties of soils in the 0.3-1.3-GHz range. IEEE transactions on Geoscience and Remote sensing, 33(3), 803-807, 1995.

Picard, G., Brucker, L., Roy, A., Dupont, F., Fily, M., Royer, A., and Harlow, C.: Simulation of the microwave emission of multi-layered snowpacks using the Dense Media Radiative transfer theory: the DMRT-ML model. Geoscientific Model Development, 6(4), 1061-1078, 2013.

Picard, G., Sandells, M., and Löwe, H.: SMRT: An active–passive microwave radiative transfer model for snow with multiple microstructure and scattering formulations (v1. 0). Geoscientific Model Development, 11(7), 2763-2788, 2018.

Pomeroy, J. W., D. M. Gray, and P. G. Landine (1993), The Prairie Blowing Snow Model: Characteristics, validation, operation, *J. Hydrol.*, 144, 164–192.

Pomeroy, J., R. Stewart, and P. Whitfield. 2016. The 2013 flood event in the South Saskatchewan and Elk River basins: Causes, assessment and damages. Canadian Water Resources Journal, 41:1-2, 105-117, DOI: 10.1080/07011784.2015.1089190

Proksch, M. et al.: MEMLS3&a: Microwave Emission Model of Layered Snowpacks Adapted to Include Backscattering, Geoscientific Model Development 8(8): 2611–26, 2015a.

Proksch, M., Löwe, H., and Schneebeli, M.: Density, specific surface area, and correlation length of snow measured by high-resolution penetrometry. Journal of Geophysical Research: Earth Surface, 120(2), 346-362, 2015b.

Proksch, M., Rutter, N., Fierz, C., and Schneebeli, M.: Intercomparison of snow density measurements: bias, precision, and vertical resolution, The Cryosphere, 10, 371-384, 2016.

Pulliainen, J. (2006). Mapping of snow water equivalent and snow depth in boreal and sub-arctic zones by assimilating space-borne microwave radiometer data and ground-based observations. *Remote Sensing of Environment*, *101*(2), 257 269. doi:10.1016/j.rse.2006.01.002

Pulliainen, J., Luojus, K., Derksen, C., Mudryk, L., Lemmetyinen, J., Salminen, M., ... and Norberg, J.: Patterns and trends of Northern Hemisphere snow mass from 1980 to 2018. Nature, 581(7808), 294-298, 2020.

Qin, Y., Abatzoglou, J. T., Siebert, S., Huning, L. S., AghaKouchak, A., Mankin, J. S., Hong, C., Tong, D., Davis, S. J., and Mueller, N. D.: Agricultural risks from changing snowmelt, Nat Clim Change, 10, 459–465, https://doi.org/10.1038/s41558-020-0746-8, 2020.

Raleigh, M. S., and Small, E. E.: Snowpack density modeling is the primary source of uncertainty when mapping basin-wide SWE with lidar, Geophys. Res. Lett., 44, 3700-3709, doi: https://doi.org/10.1002/2016GL071999, 2017.

Reigber, A., and Moreira, A.: First demonstration of airborne SAR tomography using multibaseline L-band data. IEEE Transactions on Geoscience and Remote Sensing, 38(5), 2142-2152, 2000.

Rekioua, B., Davy, M., Ferro-Famil, L., and Tebaldini, S.: Snowpack permittivity profile retrieval from tomographic SAR data. Comptes Rendus Physique, 18(1), 57-65, 2017.

Rott, H., Yueh, S. H., Cline, D. W., Duguay, C., Essery, R., Haas, C. et al.: Cold regions hydrology high-resolution observatory for snow and cold land processes, Proc. IEEE, 98(5), 752–765. doi: 10.1109/JPROC.2009.2038947, 2010.

Rott, H., Cline, D.W., Duguay, C., Essery, R., Etchevers, P., Macelloni, G., Hajnsek, I., Kern, M., Malnes, E., Pulliainen J., and Yueh, S.H.: CoReH2O, a Candidate ESA Earth Explorer Mission for snow and ice observations, Proc. of the Earth Observation and Cryosphere Science Conference, Frascati, Italy, Nov. 2012, *ESA SP-712*, European Space Agency, Noordwijk, The Netherlands, May 2013.

Rott, H., Scheiblauer, S., Wuite, J., Krieger, L., Floricioiu, D., Rizzoli, P., Libert, L., and Nagler, T.: Penetration of interferometric radar signals in Antarctic snow, The Cryosphere, 15, 4399–4419, 2021.

Roy, A., Leduc-Leballeur, M., Picard, G., Royer, A., Toose, P., Derksen, C., Lemmetyinen, J., Berg, A., Rowlandson, T., and Schwank, M.: Modelling the L-Band Snow-Covered Surface Emission in a Winter Canadian Prairie Environment, Remote Sensing, 10, 1451, 2018.

Rutter, N., Sandells, M. J., Derksen, C., King, J., Toose, P., Wake, L., ... and Sturm, M.: Effect of snow microstructure variability on Ku-band radar snow water equivalent retrievals. The Cryosphere, 13(11), 3045-3059, 2019.

Sandells, M., Löwe, H., Picard, G., Dumont, M., Essery, R., Floury, N., Kontu, A., Lemmetyinen, J., Maslanka, W., Morin, S., Wiesmann, A., and Mätzler, C.: X-Ray Tomography-Based Microstructure Representation in the Snow Microwave Radiative Transfer Model, in IEEE Transactions on Geoscience and Remote Sensing, doi: 10.1109/TGRS.2021.3086412, 2021.

Schneebeli, M., and Sokratov, S. A.: Tomography of temperature gradient metamorphism of snow and associated changes in heat conductivity, Hydrological Processes, 18, 3655-3665, doi: 10.1002/hyp.5800, 2004.

Shah, R., Xu, X., Yueh, S., Chae, C. S., Elder, K., Starr, B., and Kim, Y.: Remote sensing of snow water equivalent using P-band coherent reflection. IEEE Geoscience and Remote Sensing Letters, 14(3), 309-313, 2017.

Shi, J., and Dozier, J.: Estimation of snow water equivalence using SIR-C/X-SAR. II. Inferring snow depth and particle size, IEEE Transactions on Geoscience and Remote Sensing, 38(6), 2475–2488. doi: 10.1109/36.885196, 2000.

Shi, J., Xiong, C., and Jiang, L.: Review of snow water equivalent microwave remote sensing. Science China Earth Sciences, 59(4), 731-745, 2016.

Sihvola, A., and Tiuri, M.: Snow fork for field determniation of the density and wetness profiles of a snow pack, IEEE Transactions on Geoscience and Remote Sensing, 24, 717-721, 1986.

Skofronick-Jackson, G., Petersen, W. A., Berg, W., Kidd, C., Stocker, E. F., Kirschbaum, D. B., ... and Wilheit, T.: The Global Precipitation Measurement (GPM) mission for science and society. Bulletin of the American Meteorological Society, 98(8), 1679-1695, 2017.

Smith, C. D., Kontu, A., Laffin, R., and Pomeroy, J. W.: An assessment of two automated snow water equivalent instruments during the WMO Solid Precipitation Intercomparison Experiment, The Cryosphere, 11, 101-116, doi: 10.5194/tc-11-101-2017, 2017.

Sospedra-Alfonso, R. and Merryfield, W. (2017): Influences of temperature and precipitation on historical and future snowpack variability over the Northern Hemisphere in the Second Generation Canadian Earth System Model; Journal of Climate, v. 30, p. 4633–4656. doi:10.1175/JCLI-D-16-0612.1

Stephens, G. L., Vane, D. G., Boain, R. J., Mace, G. G., Sassen, K., Wang, Z., ... and CloudSat Science Team.: The CloudSat mission and the A-Train: A new dimension of space-based observations of clouds and precipitation. Bulletin of the American Meteorological Society, 83(12), 1771-1790, 2002.

Stiles, W. H., and Ulaby, F. T.: The active and passive microwave response to snow parameters: 1. Wetness. Journal of Geophysical Research: Oceans, 85(C2), 1037-1044, 1980.

Sturm, M.: The role of thermal convection in the heat and mass transport in the subarctic snow cover, (Doctoral dissertation). Retrieved from University of Alaska, 1989.

Sturm, M., Holmgren, J., and Liston, G. E.: A seasonal snow cover classification system for local to global applications. Journal of Climate, 8(5), 1261-1283, 1995.

Sturm, M., and Benson, C. S.: Vapor transport, grain growth and depth-hoar development in the subarctic snow. Journal of Glaciology, 43(143), 42-59, 1997.

Sturm, M., & Liston, G. E. (2021). Revisiting the Global Seasonal Snow Classification: An Updated Dataset for Earth System Applications. *Journal of Hydrometeorology*. https://doi.org/10.1175/jhm-d-21-0070.1

Sturm, M., Goldstein, M. A., and Parr, C.: Water and life from snow: A trillion dollar science question. Water Resources Research, 53(5), 3534-3544, 2017.

Sturm, M., and Holmgren, J.: An Automatic Snow Depth Probe for Field Validation Campaigns, Water Resour. Res., 54, 9695-9701, doi: 10.1029/2018wr023559, 2018.

Swan, A. M., and Long, D. G.: Multiyear Arctic sea ice classification using QuikSCAT. IEEE Transactions on Geoscience and Remote Sensing, 50(9), 3317-3326, 2012.

Takala, M., Luojus, K., Pulliainen, J., Derksen, C., Lemmetyinen, J., Kärnä, J. P., ... and Bojkov, B.: Estimating northern hemisphere snow water equivalent for climate research through assimilation of space-borne radiometer data and ground-based measurements. Remote Sensing of Environment, 115(12), 3517-3529, 2011.

Tan, S., Chang, W., Tsang, L., Lemmetyinen, J., and Proksch, M.: Modeling both active and passive microwave remote sensing of snow using dense media radiative transfer (DMRT) theory with multiple scattering and backscattering enhancement. IEEE Journal of Selected Topics in Applied Earth Observations and Remote Sensing, 8(9), 4418-4430, 2015.

Tan S. , C. Xiong, X. Xu and L. Tsang " Uniaxial Effective Permittivity of Anisotropic Bicontinuous Random Media Using NMM3D", IEEE Geoscience and Remote Sensing Letters, 2016

Tan, S., Zhu, J., Tsang, L., and Nghiem, S. V.: Microwave signatures of snow cover using numerical Maxwell equations based on discrete dipole approximation in bicontinuous media and half-space dyadic green's function. IEEE Journal of Selected Topics in Applied Earth Observations and Remote Sensing, 10(11), 4686-4702, 2017.

Tape, K. D., Rutter, N., Marshall, H. P., Essery, R., and Sturm, M.: Recording microscale variations in snowpack layering using near-infrared photography, Journal of Glaciology, 56, 75-80, doi: 10.3189/002214310791190938, 2010.

Taylor, D., Yan, J., O'Neill, C., Gogineni, S., Gurbuz, S., Aslan, B., Larson, J., Elluru, D., Kolpuke, S., Li, L., Mahjabeen, F., Nunn, J., Rahman, M., Reyhanigalangashi, O., Simpson, C., Thomas, R., Wattal, S., Blake, J., Boyle, C., Glidden, J., and Higgs, M.: Airborne dual-band microwave radar system for snow thickness measurement. In 2020 IEEE International Geoscience and Remote Sensing Symposium. IEEE, 2020.

Tebaldini, S., and Rocca, F.: Multibaseline polarimetric SAR tomography of a boreal forest at P-and L-bands. IEEE Transactions on Geoscience and Remote Sensing, 50(1), 232-246, 2011.

Tedesco, M. and Miller, J., : Observations and statistical analysis of combined active–passive microwave space-borne data and snow depth at large spatial scales. Remote Sensing of Environment, 111(2-3), pp.382-397. https://doi.org/10.1016/j.rse.2007.04.019, 2007.

Thompson, S. S., Kulessa, B., Essery, R. L. H., and Lüthi, M. P.: Bulk meltwater flow and liquid water content of snowpacks mapped using the electrical self-potential (SP) method, The Cryosphere, 10, 433-444, doi: 10.5194/tc-10-433-2016, 2016.

Thompson, A, R.E.J. Kelly (2019) Observations of coniferous forest at 9.6 and 17.2 GHz: Implications for SWE retrievals, *Remote Sensing*, 11(6), doi:10.3390/rs11010006

Thompson, A. and R.E.J. Kelly (2021a) Radar retrieval of snow water equivalent for mid-latitude agricultural sites, *Canadian Journal of Remote Sensing*. 47(1): 119-142. https://doi.org/10.1080/07038992.2021.1898938.

Thompson, A. and R.E.J. Kelly (2021b) Estimating wind slab thickness in a tundra snowpack, *Remote Sensing Letters*. 12:11, 1123-1135. https://doi.org/10.1080/2150704X.2021.1961174.

Treuhaft, R. N., Moghaddam, M., and van Zyl, J. J.: Vegetation characteristics and underlying topography from interferometric radar. Radio science, 31(6), 1449-1485, 1996.

Treuhaft, R. N., and Siqueira, P. R.: Vertical structure of vegetated land surfaces from interferometric and polarimetric radar. Radio Science, 35(1), 141-177, 2000.

Tsang, L., Blanchard, A. J., Newton, R. W., and Kong, J. A.: A simple relation between active and passive microwave remote sensing measurements of earth terrain. IEEE Transactions on Geoscience and Remote Sensing, (4), 482-485, 1982.

Tsang, L., Kong, J.A. and Shin, R.T. *Theory of microwave remote sensing*, Wiley, 1985.

Tsang, L., Ding, K. H., and Wen, B.: Dense media radiative transfer theory for dense discrete random media with particles of multiple sizes and permittivities. Progress in Electromagnetic Research, 6(5), 181-225, 1992.

Tsang, L. and J. A. Kong, Scattering of Electromagnetic Waves, Volume 3: Advanced Topics. New York, NY, USA, Wiley-Interscience, 2001.

Tsang, L., Kong, J. A., and Ding, K. H.: Scattering of electromagnetic waves: theories and applications (Vol. 27). John Wiley & Sons, 2004.

Tsang, L., Pan, J., Liang, D., Li, Z., Cline, D. W., and Tan, Y.: Modeling active microwave remote sensing of snow using dense media radiative transfer (DMRT) theory with multiple-scattering effects. IEEE Transactions on Geoscience and Remote Sensing, 45(4), 990-1004, 2007.

Tsang, L., Tan, S., Xiong, C., and Shi, J.: Optical and Microwave Modeling of Snow. Chapter 5, 85-138, Vol. 4, Comprehensive Remote Sensing: Water Cycle Components over Land. Elsevier., 2018.

Ulaby, F. T., and Stiles, W. H.: The active and passive microwave response to snow parameters: 2. Water equivalent of dry snow. Journal of Geophysical Research: Oceans, 85(C2), 1045-1049, 1980.

Ulaby, F. T., Moore, R. K., & Fung, A. K.: Microwave Remote Sensing: Active and Passive (Vol. 1, 456 p). Reading, MA: Addison-Wesley, 1981

Ulaby, F. T., Moore, R. K., and Fung, A. K.: Microwave remote sensing: Active and passive. Volume 3-From theory to applications, 1986.

Ulaby, F. T., Sarabandi, K., Mcdonald, K. Y. L. E., Whitt, M., and Dobson, M. C.: Michigan microwave canopy scattering model. International Journal of Remote Sensing, 11(7), 1223-1253, 1990.

Ulaby, F., and Long, D.: Microwave radar and radiometric remote sensing. Artech House, 2015.

Vander Jagt, B. J., Durand, M. T., Margulis, S. A., Kim, E. J., and Molotch, N. P.: The effect of spatial variability on the sensitivity of passive microwave measurements to snow water equivalent. Remote sensing of environment, 136, 163-179, 2013.

Vionnet, V., Fortin, V., Gaborit, E., Roy, G., Abrahamowicz, M., Gasset, N., and Pomeroy, J. W.: Assessing the factors governing the ability to predict late-spring flooding in cold-region mountain basins, Hydrol. Earth Syst. Sci., 24, 2141–2165, https://doi.org/10.5194/hess-24-2141-2020, 2020

Voronovich, A.: Small-slope approximation for electromagnetic wave scattering at a rough interface of two dielectric half-spaces. Waves in random media, 4, 337-367., 1994.

1870 Werner, C., Wiesmann, A., Strozzi, T., Schneebeli, M., and Mätzler, C.: The SnowScat ground-based polarimetric scatterometer: Calibration and initial measurements from Davos Switzerland. In 2010 IEEE International Geoscience and Remote Sensing Symposium (pp. 2363-2366). IEEE, 2010.

West, R., Tsang, L., and Winebrenner, D. P.: Dense medium radiative transfer theory for two scattering layers with a Rayleigh distribution of particle sizes. IEEE transactions on geoscience and remote sensing, 31(2), 426-437, 1993.

1875 Wiesmann, A., Mätzler, C., & Weise, T. (1998). Radiometric and structural measurements of snow samples. *Radio Science*, *33*(2), 273 289.

Wiesmann, A., Caduff, R., Werner, C., Frey, O., Schneebeli, M., Löwe, H., ... and Fehr, T.: ESA SnowLab Project: 4 Years of Wide Band Scatterometer Measurements of Seasonal Snow. In IGARSS 2019-2019 IEEE International Geoscience and Remote Sensing Symposium (pp. 5745-5748). IEEE, 2019.

1880 Wiscombe, W. J., and Warren, S. G.: A model for the spectral albedo of snow. I: Pure snow. Journal of Atmospheric Sciences, 37(12), 2712-2733, 1980.

Wood, A.W., T. Hopson, A. Newman, L. Brekke, J. Arnold, and M. Clark, 2016: Quantifying Streamflow Forecast Skill Elasticity to Initial Condition and Climate Prediction Skill. J. Hydrometeor., 17, 651–668, https://doi.org/10.1175/JHM-D-14-0213.1.

1885 Wrzesien, M. L., Pavelsky, T. M., Durand, M. T., Dozier, J., & Lundquist, J. D. (2019a). Characterizing biases in mountain snow accumulation from global data sets. Water Resources Research, 55, 9873–9891. https://doi.org/10.1029/2019WR025350

Wrzesien, M. L., Durand, M. T., & Pavelsky, T. M. (2019b). A Reassessment of North American River Basin Cool-Season Precipitation: Developments From a New Mountain Climatology Data Set. *Water Resources Research*, *55*(4), 3502–1890   3519. https://doi.org/10.1029/2018wr024106

Xiong, C., and Shi, J.: The potential for estimating snow depth with QuikScat data and a snow physical model, IEEE Geoscience and Remote Sensing Letters, 14(7), 1156–1160. doi: 10.1109/LGRS.2017.2701808, 2017.

Xiong, C., and Shi, J.: Seasonal snow water equivalent remote sensing by Ku band spaceborne scatterometers, In AGU Fall Meeting Abstracts (Vol. 2019, pp. C33E-1637), 2019.

1895 Xu, X., Tsang, L., and Yueh, S.: Electromagnetic models of co/cross polarization of bicontinuous/DMRT in radar remote sensing of terrestrial snow at X-and Ku-band for CoReH2O and SCLP applications. IEEE Journal of Selected Topics in Applied Earth Observations and Remote Sensing, 5(3), 1024-1032, 2012.

Xu, X., Baldi, C. A., De Bleser, J. W., Lei, Y., Yueh, S., and Esteban-Fernandez, D.: Multi-Frequency Tomography Radar Observations of Snow Stratigraphy at Fraser During SnowEx. In IGARSS 2018-2018 IEEE International Geoscience 1900   and Remote Sensing Symposium (pp. 6269-6272). IEEE, 2018.

Xu, X., Shen, H., Xu, H. and Tsang, L., 2020. Modeling Multi-Frequency Tomograms for Snow Stratigraphy. In IGARSS 2020-2020 IEEE International Geoscience and Remote Sensing Symposium (pp. 3436-3439). IEEE.

Yan, J. B., Gogineni, S., Rodriguez-Morales, F., Gomez-Garcia, D., Paden, J., Li, J., ... and Hale, R. D.: Airborne Measurements of Snow Thickness: Using ultrawide-band frequency-modulated-continuous-wave radars. IEEE 1905   Geoscience and Remote Sensing Magazine, 5(2), 57-76, 2017.

Yan, H., Sun, N., Wigmosta, M., Skaggs, R., Hou, Z., and Leung, R.: Next-Generation Intensity-Duration-Frequency Curves for Hydrologic Design in Snow-Dominated Environments, Water Resour. Res., 54, 1093-1108, doi: https://doi.org/10.1002/2017WR021290, 2018.

Yueh, S. H., Dinardo, S. J., Akgiray, A., West, R., Cline, D. W., and Elder, K.: Airborne Ku-Band Polarimetric Radar Remote 1910   Sensing of Terrestrial Snow Cover. IEEE Transactions on Geoscience and Remote Sensing, 47(10), 3347–3364. https://doi.org/10.1109/tgrs.2009.2022945, 2009.

Yueh, S. H., Shah, R., Xu, X., Stiles, B., and Bosch-Lluis, X.: A Satellite Synthetic Aperture Radar Concept Using P-Band Signals of Opportunity. IEEE Journal of Selected Topics in Applied Earth Observations and Remote Sensing, 14, 2796-2816, 2021.

1915 Zhang, G., and Tsang, L.: Application of angular correlation function of clutter scattering and correlation imaging in target detection. IEEE transactions on geoscience and remote sensing, 36(5), 1485-1493, 1998.

Zhu, J., Tan, S., King, J., Derksen, C., Lemmetyinen, J., and Tsang, L.: Forward and Inverse Radar Modeling of Terrestrial Snow Using SnowSAR Data, IEEE Transactions on Geoscience and Remote Sensing, 56(12), 7122-7132, doi:10.1109/TGRS.2018.2848642, 2018.

Zhu, J., Tan, S., Tsang, L., Kang, D.K., and Kim, E.: "Snow Water Equivalent Retrieval Using Active and Passive Microwave Observations." Water Resources Research 57, no. 7, July 2021.

Zhu, J, L. Tsang and TH Liao, 2021," Scattering from Random Rough Surfaces at X and Ku band for Global Remote
Sensing of Terrestrial Snow" IEEE International Symposium on Antennas and Propagation and USNC-URSI Radio Science
Meeting (APS/URSI), pp 1115-1116, Singapore, December 2021.

Zhu, J.: "Surface and Volume Scattering Model in Microwave Remote Sensing of Snow and Soil Moisture." Doctoral Dissertation, University of Michigan, Sept. 2021.

Zoughi, R., Wu, L.K., and Moore, R.K.: Identification of Major Backscattering Sources in Trees and Shrubs at 10 GHz. Remote Sensing of the Enviornment,19,269-290, doi: 10.1016/0034-4257(86)90057-X, 1986

Zuanon, N.: IceCube, a portable and reliable instrument for snow specific surface area measurement in the field, International Snow Science Workshop, Grenoble – Chamonix Mont-Blanc, 2013.

Zuniga, M. A., Habashy, T. M., and Kong, J. A.: Active remote sensing of layered random media. IEEE Transactions on Geoscience Electronics, 17(4), 296-302, 1979

Appendix A: Example protocol for measuring spatial variability of snow properties to support radar remote sensing

Geolocated measurements are vital to quantify variability of snowpack properties within sensor footprints (airborne or tower). Figure A1 (a) suggests an optimal configuration of snow depth and Snow MicroPenetrometer (SMP) measurements to create representative distributions of snowpack properties within airborne swaths. The main 222 m transect of snow depth and SMP profiles, located along an airborne swath centreline, has variable spacing (10^{-1}, 10^{0}, and 10^{1}m) on either side of a central pit to capture different horizontal length scales of variability. A shorter 22 m orthogonal transect with 10^{-1} and 10^{0} m spacing bisects the main transect at the central pit, and a spiral of snow depths extends from the central pit out to an 11 m radius (Figure A1 (a)). Measurements additional to the main transect allow omnidirectional analysis of snow depth variability and bi-directional analysis of snow microstructural properties, both of which may be influenced by dominant prevailing wind direction or irregular patterns of subnivean vegetation. Ideally, snow depths and positions are measured using automatic depth probes with integrated GPS providing position accuracy to ±2.5 m, e.g. Magnaprobes (Sturm and Holmgren, 2018). Where forest canopies obscure GPS satellite connection or snowpacks are deeper than 180 cm (current maximum magaprobe length), hand probes are used in measured grids arranged relative to a known absolute position. Accuracy of snow depths range from nearly 0 cm on hard ground to ~5 cm in soft subnivean vegetation. Where snowpit locations are not predetermined, measured snow depth distributions can be subsequently used to determine the location of snowpit(s) to match mean depth or multiple pits spanning interquartile ranges.
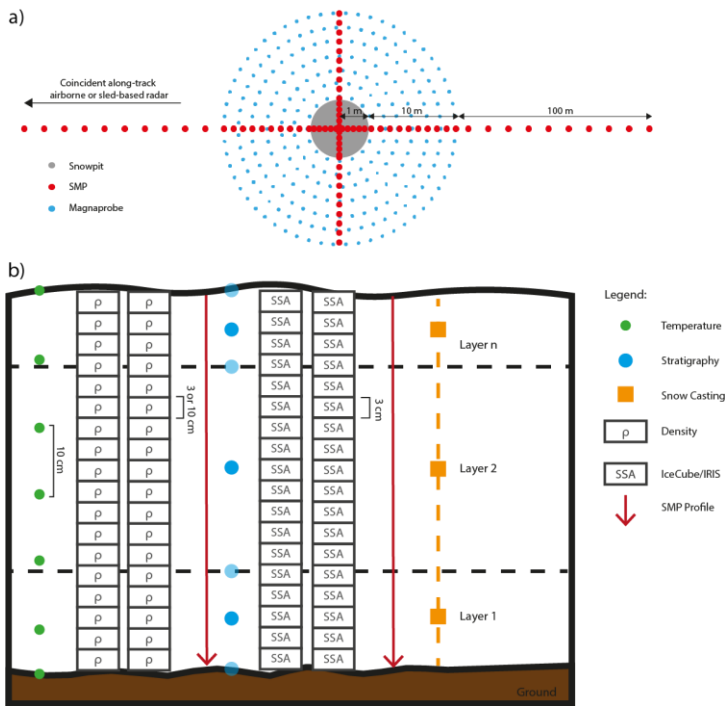
Figure A1: Optimal measurement configurations for evaluation of snow properties in sensor footprints.

One-dimensional (vertical) measurement of snowpack properties for SAR retrievals require objective measurements of snow
microstructure. SMP allows rapid (< 1 minute) force profile detection at millimetre resolution (Proksch et al., 2015b), which
is used to derive density, correlation length and Specific Surface Area (SSA); quantities directly or indirectly used by radiative
transfer models (Chang et al., 2016; Picard et al., 2018). The speed of data acquisition allows for SMP measurements to be
used in a distributed manner along transects, but SMP also supports other coincident snowpit measurements using different
techniques. Figure A1 (b) shows a schematic of optimal snowpit measurements. Double-sampled volumetric density
measurements, 100 cm^3 box-cutter with 3 cm vertical resolution for shallow snowpacks or 1000 cm^3 wedge-cutter with 10 cm
vertical resolution for deep snowpacks (Proksch et al., 2016), are averaged at each vertical position. Following principles
presented in Gallet et al. (2009), 3 cm vertical resolution double-sampled SSA measurements are made using an InfraRed
Integrating Sphere (IRIS) (Montpetit et al., 2012) or an A2 Photonic Sensors IceCube (Zuanon, 2013). Micro-CT analysis of
snow casts (Schneebeli and Sokratov, 2004; Lundy et al., 2002), consisting of entire profiles or samples of critical layers, are

1965   used as a benchmark for corroboration of all other measurements. However, in-practice, in-situ snow casting and subsequent cold-laboratory micro-CT analysis requires a much higher level of expertise and processing time than SMP or IRIS/IceCube measurements, meaning field application of micro-CT is often limited.

    Profiles of snow temperature using well-calibrated stem thermometers at 10 cm vertical resolution are important parameters for radiative transfer models, in conjunction with stratigraphic identification of snow layer boundaries and ice lenses using

1970   hand hardness. Visual identification of grain type (Fierz et al., 2009) using a hand lens or macroscope is an important complimentary measurement for layer classification and understanding the seasonal history of snowpack processes. However, using similar visual methods to quantify snow 'grain size' are too subjective to create a microstructural metric for further use in radiative transfer models. The SSA measurements provide much better accuracy for use in radiative transfer models.

    Near-infrared (NIR) photography allows two-dimensional analysis of layer boundary position (Tape et al., 2010) and layer

1975   thickness variability (Rutter et al., 2019) in snow trenches, quantifying spatial variability of stratigraphy around a single snowpit profile. It also enables measurements of layer boundary roughness, particularly of the snow-air and snow-ground interfaces. Other methods to characterise snow-air surface roughness use photographic image contrast analysis of dark boards placed behind snow (Fassnacht et al., 2009; Anttila et al., 2014) and subnivean roughness of areas cleared of snow using pin profilers, LiDAR scanning (Chabot et al., 2018; Roy et al., 2018) or structure from motion photogrammetry (Meloche et al.,

1980   2020). The subnivean roughness between snow and soil give significant contributions of rough surface scattering because of the contrast of dielectric constants between snow and soil.