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Reassessing seasonal sea ice predictability of the Pacific-Arctic sector using

2	a Markov model
3	Yunhe Wang ^{1,4} , Xiaojun Yuan ² , Haibo Bi ^{1,3,4} , Mitchell Bushuk ⁵ , Yu Liang ^{1,6} ,
4	Cuihua Li ² , Haijun Huang ^{1,3,4,6}
5	¹ CAS Key Laboratory of Marine Geology and Environment, Institute of Oceanology,
6	Chinese Academy of Sciences, Qingdao, China.
7	² Lamont-Doherty Earth Observatory of Columbia University, New York, USA.
8	³ Laboratory for Marine Geology, Qingdao National Laboratory for Marine Science
9	and Technology, Qingdao, China.
10	⁴ Center for Ocean Mega-Science, Chinese Academy of Sciences, Qingdao, China.
11	⁵ National Oceanic and Atmospheric Administration/Geophysical Fluid Dynamics
12	Laboratory, Princeton, New Jersey, USA
13	⁶ University of Chinese Academy of Sciences, Beijing, China
14	Corresponding author: Xiaojun Yuan (xyuan@ldeo.columbia.edu)

15 Abstract

In this study, a regional linear Markov model is developed to assess seasonal sea ice 16 predictability in the Pacific-Arctic sector. Unlike an earlier pan-Arctic Markov model 17 that was developed with one set of variables for all seasons, the regional model 18 consists of four seasonal modules with different sets of predictor variables, 19 accommodating seasonally-varying driving processes. A series of sensitivity tests are 20 performed to evaluate the predictive skill in cross-validated experiments and to 21 determine the best model configuration for each season. The prediction skill, as 22 23 measured by the sea ice concentration (SIC) anomaly correlation coefficient (ACC) 24 between predictions and observations, increased by 32% in the Bering Sea and 18% in the Sea of Okhotsk relative to the pan-Arctic model. The regional Markov model's 25 skill is also superior to the skill of an anomaly persistence forecast. SIC trends 26 27 significantly contribute to the model skill. However, the model retains skill for detrended sea ice extent predictions up to 7 month lead times in the Bering Sea and 28 the Sea of Okhotsk. We find that subsurface ocean heat content (OHC) provides a 29 crucial source of prediction skill in all seasons, especially in the cold season, and 30 adding sea ice thickness (SIT) to the regional Markov model has a substantial 31 contribution to the prediction skill in the warm season but a negative contribution in 32 the cold season. The regional model can also capture the seasonal reemergence of 33 predictability, which is missing in the pan-Arctic model. 34

35 **1 Introduction**

Sea ice acts as a major component of the Arctic climate system through 36 37 modulating the radiative flux, heat, and momentum exchanges between the ocean and the atmosphere (Peterson et al., 2017; Porter et al., 2011; Smith et al., 2017). Sea ice 38 39 also modulates sea surface salinity, which is one of the key drivers for thermohaline circulations (Sévellec et al., 2017). The rapid retreat of Arctic sea-ice extent in the 40 past few decades has been considered a key indicator of climate change (Koenigk et 41 al., 2016; Swart, 2017). The decreasing Arctic sea ice extent contributes to polar 42 temperature amplification (Kim et al., 2016; Screen and Francis, 2016), an increase in 43 wintertime snowfall over Siberia, northern Canada, and Alaska (Deser et al., 2010), 44 45 polar stratospheric cooling (Screen et al., 2013; Wu et al., 2016), and potentially contributes to a weakening of the mid-latitude jet (Francis and Vavrus, 2012) and 46 increased frequency of cold Northern Hemisphere midlatitude winter events (Cohen et 47 al., 2020; Meleshko et al., 2018). 48

49 The rapid retreat of summer Arctic sea ice extent has also created more commercial opportunities in the newly opened Arctic waters. The Northwest Passage 50 (through northern Canada) and the Northern Sea Route (north of Russia) could offer 51 faster and less expensive shipping between the Pacific and Atlantic (Smith and 52 53 Stephenson, 2013). Information on the Arctic marine accessibility and ice-free season duration in the marginal ice zone would enable planning of merchant shipping, 54 conservation efforts, resource extraction, and fishing activities. The growing polar 55 ecotourism industry could also benefit from shrinking sea-ice cover. Therefore, 56 57 increased efforts have been devoted to developing Arctic sea-ice forecast systems in recent decades. 58

59 Substantial efforts have gone toward developing both statistical and dynamical sea 60 ice prediction models. Dynamic models numerically solve equations that govern the 61 sea ice physics using sea-ice, ocean, and/or atmospheric conditions to initialize the 62 models for each season (Bushuk et al., 2019; Bushuk et al., 2020; Bushuk et al., 2021; 63 Dai et al., 2020; Msadek et al., 2014). Numerous studies using fully coupled general

circulation models (GCMs) have quantified the seasonal prediction skill of pan-Arctic 64 sea ice extent (SIE) and have found forecast skill for detrended pan-Arctic SIE at lead 65 times of 1 to 6 months (Blanchard-Wrigglesworth et al., 2015; Day et al., 2014b; 66 Guemas et al., 2016a; Peterson et al., 2015; Sigmond et al., 2013). Bushuk et al. 67 (2017a) evaluated regional Arctic sea ice prediction skill in a Geophysical Fluid 68 69 Dynamics Laboratory (GFDL) seasonal prediction system. They found skillful detrended regional SIE predictions, and found that skill varied strongly with both 70 71 region and season.

72 On the other hand, statistical methods are also appealing for seasonal sea ice 73 predictions (Petty et al., 2017). Statistical models capture relationships between sea 74 ice and oceanic, atmospheric, or time-lagged sea ice predictor. Recently, statistical methods have been used to provide sea ice field predictions using numerous 75 techniques such as linear Markov model (Chen and Yuan, 2004; Yuan et al., 2016), 76 vector autoregressive model (Wang et al., 2019a; Wang et al., 2016), deep neural 77 78 network (Andersson et al., 2021; Chi and Kim, 2017; Wang et al., 2017), Bayesian 79 logistic regression (Horvath et al., 2020), and the combination of complex networks 80 and Gaussian process regression model (Gregory et al., 2020). In some cases, statistical models provide better performance than dynamical models (Hamilton and 81 Stroeve, 2016). For example, Yuan et al. (2016) showed that a linear Markov model 82 has skillful sea ice concentration (SIC) predictions up to 9-month lead times in many 83 regions of the Arctic and that this statistical model consistently captured more sea ice 84 prediction skill than NOAA/NCEP Climate Forecast System (CFSv2) and the 85 Canadian seasonal and interannual prediction system at the seasonal time scale. The 86 87 Markov model prediction skill also exhibits strong regional and seasonal dependence. Two common characteristics of sea ice predictability emerged from both dynamic 88 (e.g. CFSv2 and GFDL climate models) and statistical models (e.g. linear Markov 89

models, and linear regression models). First, low prediction skill occurs in the Pacific
sector of the Arctic, particularly in the Bering Sea and the Sea of Okhotsk, compared

with other Arctic regions (Bushuk et al., 2017a; Yuan et al., 2016). Many factors may

93 lead to this low predictability. Bushuk et al. (2017a) suggest that less persistent sea ice anomalies in the North Pacific sector possibly lead to less predictability in the region 94 by the GFDL dynamical model. The Markov model of Yuan et al. (2016) was built in 95 multivariate empirical orthogonal functions (MEOF) space in the pan-Arctic and the 96 leading modes are dominated by the large long-term trend and strong climate 97 variability in the Atlantic sector (Figure 1). So the signal of sea ice variability in the 98 Pacific sector could be under-represented in the model. Therefore, it is necessary to 99 100 evaluate the sea ice predictability in the Pacific sector with a new regional model.

Second, many studies have shown evidence for an Arctic sea ice spring 101 102 predictability barrier that causes forecasts initialized prior to May to be less skillful 103 and imposes a relatively sharp limit on regional summer sea ice prediction skill (Bushuk et al., 2017a; Day et al., 2014b; Yuan et al., 2016). Spring sea ice variability 104 105 is complicated by surface melt ponds. The sea ice driven processes in spring could be different from those in other seasons. The spring barrier may result from a sharp 106 107 increase in predictability at melt onset, when sea-ice-albedo feedback acts to enhance 108 and persist the preexisting export-generated mass anomaly (Bushuk et al., 2020). In addition, summer initialization months have little sea ice coverage and have little 109 intrinsic memory of sea ice and, therefore, require another source of memory to 110 provide winter SIE prediction skill. 111

112 Actually, re-emergence mechanisms can provide sources of sea ice predictability on time scales from a few months to 1 year (Blanchard-Wrigglesworth et al., 2011). 113 114 The re-emergence mechanism mainly relies on the persistence of some sea-ice related variables such as sea ice thickness (SIT) and ocean temperature. Previous studies have 115 116 shown that summer sea surface temperature (SST) anomalies can provide a significant source of SIE predictability in the ice growth season (Blanchard-Wrigglesworth et al., 117 118 2011; Bushuk and Giannakis, 2017; Cheng et al., 2016; Dai et al., 2020). Initializing the upper ocean heat content (OHC) in a seasonal prediction system can also yield 119 120 remarkable regional skill for winter sea ice (Bushuk et al., 2017a). Moreover, assimilating SIT data can slightly improve the SIC forecast and particularly benefit 121 the sea ice prediction in summer, which is attributed to the long-lived SIT anomalies 122 and their impact on summer sea ice (Blockley and Peterson, 2018; Bushuk et al., 123

2017b; Guemas et al., 2016b; Xie et al., 2016). Because sea ice is closely coupled 124 with the atmosphere and the ocean, the sea ice predictability is provided by the 125 intrinsic memory of sea ice and its related variables, and accurate initial conditions are 126 of importance for sea ice predictions (Blanchard-Wrigglesworth et al., 2011; Guemas 127 et al., 2016b). Current climate models used for sea ice predictions are usually 128 initialized using various atmospheric and oceanic variables, such as SIC, SIT, OHC, 129 SST, surface air temperature (SAT), or other data from existing reanalysis (Bushuk et 130 al., 2017a; Dai et al., 2020; Kimmritz et al., 2019; Yuan et al., 2016). 131

In this study, we develop a regional linear Markov model for the seasonal 132 prediction of SIC in the Pacific sector with a focus on understanding unique sea ice 133 driving processes in different seasons. We follow the framework of the pan-Arctic 134 linear Markov model (Yuan et al., 2016). Unlike the pan-Arctic model that was 135 developed with one set of variables (SIC, SAT, SST) for all seasons and the entire 136 Arctic region, the regional model consists of four modules with seasonal dependent 137 138 variables, which isolate the dominant processes for each targeted season. Regional relevant predictors are evaluated. New variables, including surface net radiative flux, 139 140 turbulent heat flux, and pressure and wind fields, as well as SIT and OHC, are introduced to the model experiments. Sea ice predictability is assessed at grid points 141 and over all seasons, and subsequently compared with the pan-Arctic model and other 142 dynamic models. 143

144 **2 Data and methodology**

145 **2.1 Data**

Building on the extensive literature studying the predictability and variability of sea ice (Bushuk and Giannakis, 2017; Bushuk et al., 2020; Guemas et al., 2016a; Horvath et al., 2021; Lenetsky et al., 2021; Yuan et al., 2016), we firstly chose many kinds of oceanic and atmospheric variables and examined their correlations with SIC. The results show that SIC is highly related to OHC in the upper 300 m, SIT, SST, SAT, surface net radiative flux, surface net turbulent heat flux, geopotential height and wind vector at different levels including 850 to 200 hPa. Due to the barotropic

nature of the polar troposphere (Chen, 2005; Ting, 1994) and the low correlation
between sea level pressure and SIC, we chose geopotential height and wind vector at
850 hPa to define the low-level atmospheric circulation, whose interaction with sea
ice is stronger relative to that in higher levels. Therefore, we choose to define the
atmosphere-ice-ocean coupled Arctic climate system with 9 variables: SIC, OHC in
the upper 300 m, SIT, SST, SAT, surface net radiative flux, surface net turbulent heat
flux, 850 hPa geopotential height, and 850 hPa wind vector.

Monthly SICs in 25 km \times 25 km grids are obtained from the National Snow and 160 Ice Data Center (NSIDC) from 1979 to 2020 (Comiso, 2017). The dataset is generated 161 from brightness temperatures derived from Nimbus-7 Scanning Multichannel 162 163 Microwave Radiometer (SMMR), Defense Meteorological Satellite Program (DMSP) -F8, -F11, and -F13 Special Sensor Microwave/Imager (SSM/I), and DMSP-F17 164 Special Sensor Microwave Imager/Sounder (SSMIS) using the bootstrap algorithm. 165 Monthly SITs are from the Pan-Arctic Ice-Ocean and Assimilating System (PIOMAS) 166 167 model data. PIOMAS is a sea ice-ocean reanalysis product that compares reasonably well to available satellite, aircraft, and in situ SIT measurements (Schweiger et al., 168 169 2011). The system applies a 12-category SIT and enthalpy distribution (Zhang and Rothrock, 2003) and is driven by NCEP/NCAR reanalysis atmospheric forcing 170 171 including 10-m surface winds and 2-m SAT.

All atmospheric variables and SST with a spatial resolution of $1^{\circ} \times 1^{\circ}$ are from the 172 latest European Centre for Medium-Range Weather Forecasts (ECMWF) reanalysis 173 product ERA5 (Hersbach et al., 2020) and are applied to represent the conditions of 174 175 the atmosphere and ocean. ERA5 is produced using the version of ECMWF's Integrated Forecast System (IFS), CY41R2, based on a hybrid incremental 4D-Var 176 system, with 137 hybrid sigma/pressure (model) levels in the vertical direction, with 177 the top-level at 0.01 hPa. The OHC used here is global ocean and sea-ice reanalysis 178 (ORAS5: Ocean Reanalysis System 5) monthly mean data and is developed by the 179 European Centre for Medium-Range Weather Forecasts (ECMWF) OCEAN5 ocean 180 analysis-reanalysis system (Zuo et al., 2019). ORAS5 includes five ensemble 181

members and covers the period from 1979 onwards. It is regarded as a global eddy-

183 permitting ocean ensemble reanalysis product. Both the forcing fields and

184 observational datasets are updated in ORAS5.

185 **2.2 The model**

The idea of using a Markov model for climate prediction is to build multivariate 186 models, aiming to capture the co-variability in the atmosphere-ocean-sea ice coupled 187 system instead of linearly regressing on individual predictors. Yuan et al. (2016) 188 applied this statistical approach to predict SIC in the Arctic at a seasonal timescale 189 and showed that the Lamont statistical model outperformed the NOAA CFSv2 190 operational model and the Canadian Seasonal to Interannual Prediction System in sea 191 ice prediction. They used MEOF as the building blocks of the model to filter out 192 incoherent small-scale features that are basically unpredictable. Similar Markov 193 models were also developed to study ENSO predictability (Cañizares et al., 2001; Xue 194 et al., 2000) and for East Asian monsoon forecasts (Wu et al., 2013). The success of 195 196 the Markov model is attributed to the dominance of several distinct modes in the coupled atmosphere-ocean-sea ice system and to the model's ability to pick up these 197 modes. 198

Here we focus on the atmosphere-ocean-sea ice interactive processes that are 199 unique to the Pacific sector and develop a regional linear Markov model for the 200 seasonal prediction of SIC. The model consists of four modules with seasonally 201 202 dependent variables. The model domain extends from 40°N to 84°N in latitude and from 120°E to 240°E in longitude (Figure 1). To reduce model dimensions, we 203 204 remove land grid cells, mostly open water grid cells and mostly 100% ice cover grid cells from the sea ice field. The mostly open water cells are defined by the grids 205 where SIC \geq 15% only occurred less than 4% of the total all-season time series (492) 206 months), and mostly ice covered cells are defined by the grids where SIC \geq 95% for 207 208 more than 96% of total time series. SIC at the rest grid cells ranges from 0 to 100%.

209 Our model is constructed in the MEOF space. The base functions of the model's spatial dependence consist of the eigenvectors from the MEOF, while the temporal 210 evolution of the model is a Markov process with its transition functions determined 211 from the corresponding principal components (PCs). We use only several leading 212 MEOF modes, which greatly reduce model space and filter out unpredictable small-213 214 scale features. This method of reducing model dimension has been successfully used in earlier Antarctic and Arctic sea ice predictability studies (Chen and Yuan, 2004; 215 216 Yuan et al., 2016).

We preselect SIC, OHC, SIT, SST, SAT, surface net radiative flux, surface net 217 turbulent heat flux, and geopotential height and winds at 850 hPa to represent 218 different sea ice-driving processes in the Pacific sector. We create anomaly time 219 series for all variables from 1979 to 2020 by subtracting climatologies of the same 220 period from monthly mean data. A normalization is applied to the time series at each 221 222 grid point for all variables. To emphasize sea ice variability in the model construction, we weight SIC by 2 and other variables by 1, although the final model skill is not very 223 224 sensitive to this choice of weight. The weighted variables are stacked up into a single 225 matrix V(n, m), where n is the number of grid points of all fields and m is the length of the time series. We then decompose V into eigenvectors (spatial patterns) E and 226 their corresponding PCs (time series) **P**: 227

228

$$\boldsymbol{V} = \boldsymbol{E}\boldsymbol{P}^T, \tag{1}$$

where the columns of E are orthogonal and the columns of P are orthonormal; the
superscript T denotes matrix transpose. It greatly reduces the model space by
truncating (1) to the several leading modes. The Markov model is computed using the
single-step correlation matrix, that is, a transition matrix A that satisfies the following
linear relation:

234 $\boldsymbol{P}_{i+1} = \boldsymbol{A}\boldsymbol{P}_i + \boldsymbol{e}_i, \qquad (2)$

where *i* denotes the *i*th month and e_i is the error in the model fit. Transition **A** is calculated by multiplying (2) with P_i^T

237
$$\boldsymbol{P}_{i+1}\boldsymbol{P}_i^T = \boldsymbol{A}\boldsymbol{P}_i\boldsymbol{P}_i^T + \boldsymbol{e}_i\boldsymbol{P}_i^T, \qquad (3)$$

For the best model fit, e_i and P_i^T should have no correlation. Thus

239
$$\boldsymbol{A} = (\boldsymbol{P}_{i+1}\boldsymbol{P}_i^T)(\boldsymbol{P}_i\boldsymbol{P}_i^T)^{-1}.$$
 (4)

A is constructed to be seasonally-dependent because of the strong seasonality of SIC
and related variables. Thus (4) is applied to 12 subsets of PCs to obtain different
transition matrices for each of the 12 calendar months.

After the Markov model is formulated, the SIC prediction can be generated 243 through the following eight steps: 1) to examine which variables have the highest 244 prediction potential in the Pacific sector, we create 10 climate variable combinations 245 representing different driving processes. 2) The PCs corresponding to each initial 246 multivariate space are calculated by the MEOF equation (1). 3) Transition matrices, 247 A, for each calendar month are calculated by equation (4). 4) The predictions of the 248 PCs are made by truncating to the first several modes and applying the appropriate 249 transition matrices at different lead times. "Lead time" refers to the number of months 250 prior to the target month that the forecast was initialized. For example, lead-1 251 252 prediction of January SIE is based on December data. 5) The predicted PCs are combined with the respective eigenvectors to produce a spatially-resolved SIC 253 anomaly prediction for each variable combination. 6) We evaluate the prediction skill 254 measured by the SIC anomaly correlation coefficient (ACC), percentage of grid points 255 with significant ACC (PGS), and root mean square error (RMSE) using cross-256 validated model experiments to identify the superior model for each season. 7) The 257 complete SIC anomaly prediction can then be generated by combining predicted PCs 258 259 by the corresponding optimal model in each season with eigenvectors. We differentiate the seasons as follows: winter (December through February), spring 260 (March through May), summer (June through August), and autumn (September 261 through November). 8) The predicted SIC anomalies are divided by weight value 2, 262 multiplied by standard deviation, and added the climatology to generate the complete 263 prediction field. 264

To determine model variables and the number of modes to be used in the model, 265 we evaluate the prediction skill at all grid points and all seasons in a cross-validated 266 fashion for the period 1980-2020, by calculating the ACC and RMSE between 267 predictions and observations. Notably, the dramatic declining trend in SIC prohibits 268 us to use the first half of the time series for training the model and the second half of 269 270 the time series to validate the model since the climate system mean state has changed dramatically over the last four decades. Another cross-validation scheme (Barnston 271 272 and Ropelewski, 1992) is jackknifing, where one case is withheld from the regression development in the Markov model as an independent sample for testing. Thus, we 273 built a Markov model for each month with a 1-yr moving window of data removal, 274 and then used this window of predictions to evaluate the model performance. Here, 275 we subtract one-year data from PCs and recalculate the transition matrix in equation 276 (4); then twelve-month predictions are generated for that year. This procedure is 277 repeated for each year of the time series. Such a cross-validated experimental design 278 reduces artificial skill without compromising the length of the time series. 279

The long-term trend is an essential part of the Arctic sea ice variability. A substantial declining trend exists in Arctic SIC, particularly in the Barents Sea, the Kara Sea, the Beaufort Sea, and the Chukchi Sea (Figure 1). However, outside of the Arctic Basin, the long-term trends are relatively weak in the Pacific sector. As the trends are parts of the total variability, we retain the SIC trends in anomalies while building the model and then conduct a post prediction evaluation of the impact of trends on the model skill.

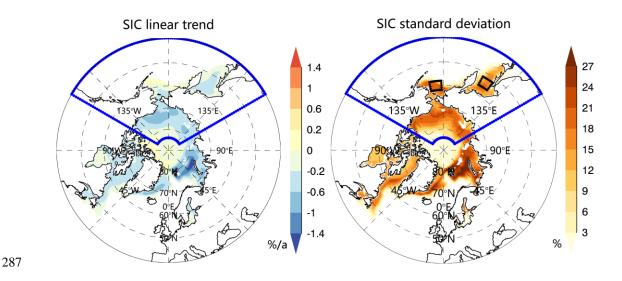


Figure 1. Arctic SIC trends (left) and standard deviation (right) computed using 288 SIC anomalies over all 12 months of the period 1979-2020. The Pacific-Arctic model 289 domain is enclosed by blue lines, which covers 40° - 84°N and 120° - 240°E. Two 290 focused areas marked in black boxes in the Bering Sea (between 58°- 62°N and 182°-291 192°E) and the Sea of Okhotsk (between 52°- 56°N and 144°-152°E) have large 292 standard deviations and are selected to evaluate the ACC skill improvement in the 293 294 regional model compared with the pan-Arctic Markov model developed by Yuan et al. (2016). 295

3 Model construction and assessments

297 **3.1 EOF analysis of Pacific SIC**

Before constructing the model, we first examine whether the EOF analysis can 298 isolate the regional and seasonal SIC variability in the Pacific-Arctic sector. Figure 2 299 shows the eigenvectors of the three leading EOF modes of SIC. The first mode of SIC 300 variability, accounting for 23% of the total variance, mainly shows a positive pattern 301 302 within the Arctic Basin from 1979 to 2002 and a negative pattern after 2003 with a record low in 2007 and 2012, representing the decreasing trend in summer and early 303 fall SIC. The declining trend is heavily loaded inside the Arctic Basin from the East 304 Siberian Sea to the Beaufort Sea. The second SIC mode (9% of total variance) 305 primarily captures out-of-phase SIC anomalies in the Bering Sea and the Sea of 306

Okhotsk and is associated with the Aleutian-Icelandic low seesaw, representing SIC 307 variability in cold seasons (Frankignoul et al., 2014). This pattern suggests 308 consistently positive SIC anomalies in the Bering Sea and negative anomalies in the 309 Sea of Okhotsk after 2004. The SIC variability in the central sector (approximately 310 60°-70°N) stands out in the third EOF mode (7% of the total variance), which is a 311 commonly observed feature in the region during spring and autumn. This finding 312 shows that the EOF (MEOF) analysis can well isolate the regional and seasonal SIC 313 314 variability including the trend in the Pacific-Arctic sector.

We further divided the SIC time series into four seasons and conducted EOF 315 analysis respectively. The results show that fewer modes can explain the dominant 316 317 SIC variance in autumn and summer benefiting from the large SIC variability and trend (Figure S1). For example, the leading 10 modes can explain 70% of the SIC 318 total variance in autumn and summer, while about 25 modes are needed for explaining 319 the same amount of variance in cold seasons. It turns out that the several leading 320 321 modes can explain the dominant SIC variability. This is an important premise to reduce the model dimension and, more importantly, to filter out incoherent small-322 scale features that are likely unpredictable. In addition, it is necessary to build the sea 323 ice prediction model for individual seasons because of the differences in seasonal 324 patterns of variability and the different number of leading modes required to capture 325 predictable variability. 326

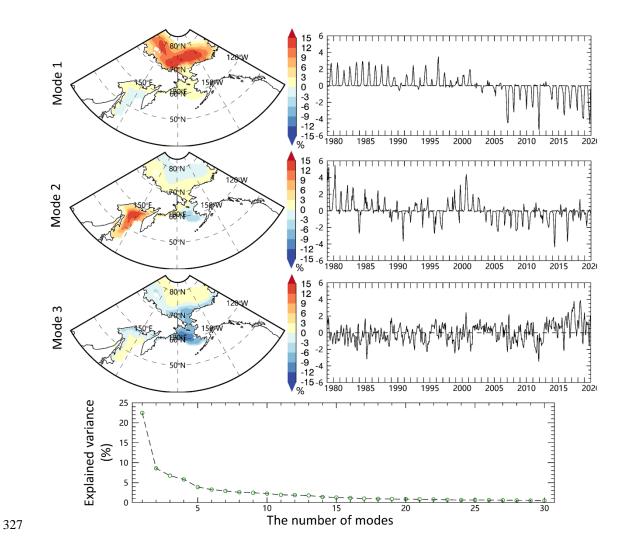


Figure 2. The eigenvectors and PCs of the three leading EOF modes of SIC in the Pacific-Arctic sector for the period 1979-2020. The bottom panel shows the explained variance as a function of the number of leading modes of SIC.

331 **3.2 Construct an optimal model for each season**

A practical issue in building a Markov model in MEOF spaces is which 332 333 combination of variables and number of leading modes to retain in the model. Using too few modes may miss some predictable signals, and too many may result in 334 overfitting and contaminate the model with incoherent small-scale features. To 335 determine optimal predictor variables and reasonable mode truncations, we calculate 336 the prediction skill from a series of cross-validated model experiments, which used 337 different numbers of modes and different variables. Table 1 shows the detailed 338 variable-combinations. Models V2-V4, V6-V8, and V10-V11 are weighted toward 339

thermodynamic processes, whereas V9 and V12 represent integration of

341 thermodynamic and dynamic processes.

Table 1. Variable combinations in cross-validated experiments. V1 represents the
No. 1 variable-combination. √ represents the variable included in the corresponding
combination.

	V1	V2	V3	V4	V5	V6	V7	V8	V9	V10	V11	V12
SIC	\checkmark											
ОНС		\checkmark		\checkmark								
SST			\checkmark	\checkmark						\checkmark	\checkmark	\checkmark
SIT					\checkmark							\checkmark
SAT						\checkmark						\checkmark
Surface net turbulent								\checkmark			\checkmark	\checkmark
heat flux												
Surface net radiative							\checkmark			\checkmark		\checkmark
flux												
850hPa GPH, U, V									\checkmark			\checkmark

The cross-validation scheme is carried out for the time series to produce 345 346 predictions at 1- to 12-month lead. The PGS and mean RMSE for each lead time in each season are calculated. To avoid missing predictable signals, we initially retain 347 large amounts of modes (up to 52) in the model and then narrow the range of mode 348 numbers to determine the best model configuration for each season. Figure S2 349 presents the PGS for each lead time for winter target months. It shows that the model 350 prediction skill in winter steeply decreases after 36 modes in most lead months. 351 Similarly, RMSE increases rapidly after 36 modes (Figure S3). This indicates that 352 including modes beyond mode 36 in winter, mainly representative of unpredictable 353 354 small-scale features, leads to the rapid decrease of predictive skill.

To select a model configuration that fits all lead times, we average the 12 panels in Figures S2 and S3, respectively, and display them in the first column of Figure S4. Similarly, predictive skills for other seasons are also examined. We further narrow the modes' range to display the predictive skill according to Figure S4 so that we can determine the optimal model more accurately (Figure 3). Generally, the model skills are better in summer and autumn than in winter and spring, and more modes are needed in the cold season to capture the predictable signal of SIC, which is likely due
to the weaker trends in these months. Models with high correlation also have smaller
RMSE but the RMSE differences between models are relatively small.



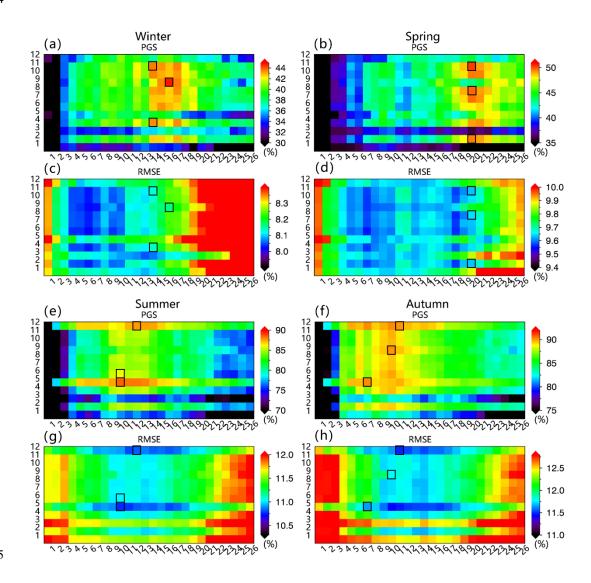




Figure 3. Mean PGS and mean RMSE between the observations and predictions in four seasons. (a) Mean PGS is obtained by averaging all lead months for winter predictions. The x-axis represents the number of MEOF modes, and the y-axis represents the combination of the variables corresponding to Table 1. (b, e, and f) are the same as (a) except for spring, summer, and autumn respectively. (c, d, g, and h) are the same as (a, b, e, and f) except for RMSE.

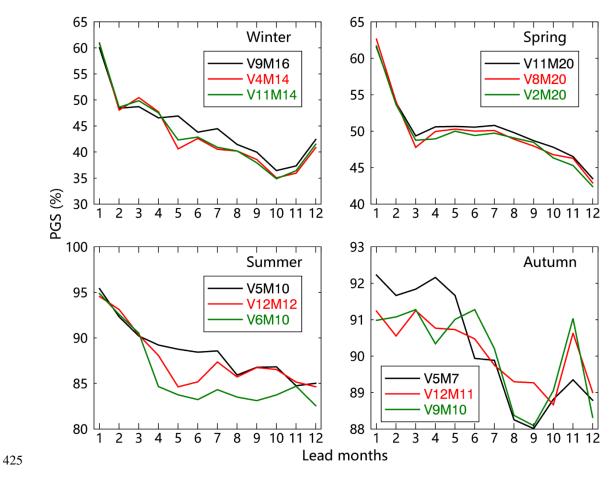
Based on the PGS and RMSE, we primarily chose three superior model 372 configurations marked by black boxes in Figure 3 for each season respectively. To 373 determine which model configuration produces the best prediction in each season, we 374 spatially average the SIC prediction skill from these superior models with 1- to 12-375 month leads (Figures 4 and 5). Figure 4 shows the cross-validation skill measured by 376 377 PGS. In general, the predictive skill in the warm season is higher than that in the cold season, although the RMSEs are also relatively large in the warm season (Figure 5). 378 379 The model prediction skills based on those superior model configurations have similar variability and magnitude in winter and spring respectively, while large differences of 380 that occur in the warm season, especially in autumn. It also shows that the model 381 prediction skill steeply decreases at the 2-month lead in winter and at the 2- and 3-382 month lead in spring. 383

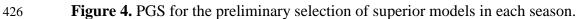
As a model construction principle, we choose the minimum number of variables and modes to achieve the same level of skill, avoiding possible overfitting. Based on the PGS and RMSE, we chose V9M16 as the best model in winter since it shows the highest PGS. Similarly, we chose V11M20 in spring and V5M10 in summer. In autumn, The model skill from V5 is obviously superior at 1-5 lead months, while V12 dominates prediction skill beyond the 8-month lead. We decided to choose V5M7 because it has a relatively higher mean skill and fewer variables and modes.

The contribution of different variables in ice prediction skill for each season is 391 also assessed. OHC contributes more model prediction skill than SST in all seasons 392 (Figure 3). The model built on the data matrix of SIC, OHC performs better in winter 393 394 and spring, which indicates that the OHC provides a considerable source of memory for SIC prediction skill in the cold season and plays a key role in the evolution of sea 395 ice conditions. The results are consistent with many previous studies (Bushuk et al., 396 2017a; Dai et al., 2020; Guemas et al., 2016b; Lenetsky et al., 2021). 850 hPa 397 geopotential height and winds can still contribute additional prediction skill in winter 398 since including OHC, geopotential height and winds slightly outperforms the case 399 without geopotential height and winds (Figure 4). 850 hPa GPH and wind not only 400

affect the heat and moisture transport by atmospheric circulation anomaly but also
drive sea-ice drift. For example, the dipole structure anomaly of the Arctic
atmospheric circulation shows strong meridionality and plays a profound role in seaice export/import, and heat and moisture transport through the Pacific-Arctic sector
(Wu et al., 2006).

Similarly, SST and turbulent heat flux also contribute additional skill in spring 406 although the contribution is minor (Figures 3 and 4). It is worth mentioning that the 407 variable such as SST with minor additional contributions to the model does not mean 408 that it is a minor contributor since the contributions from different variables to 409 prediction skill partially overlap. In addition, adding SIT to the model has a 410 411 substantial contribution to the prediction skill in the warm season, indicating that sea ice thickness is a key source of sea ice predictability within the Arctic Basin in the 412 warm season especially in summer, which is consistent with previous studies 413 (Blanchard-Wrigglesworth et al., 2011; Blockley and Peterson, 2018; Day et al., 414 415 2014a; Morioka et al., 2021; Tian et al., 2021; Yuan et al., 2016). However, SIT has a negative contribution to the prediction skill in the cold season (Figure 3). The 416 417 contributions of SIT to the prediction skill in autumn are very sensitive to the number of lead months that the skill steeply decreases beyond a 5-month lead (Figure 4). In 418 419 other words, the model didn't perform well in autumn prediction initialized in winter and spring. In addition, the surface net radiative flux also contributes to the model 420 skill in the cold season (Figure 3). Early studies suggested that the surface longwave 421 radiation plays an indispensable role in the polar climate system in the cold season 422 when shortwave radiation is at its annual minimum (Huang et al., 2015; Kapsch et al., 423 424 2013; Lee et al., 2017; Liu and Key, 2014; Luo et al., 2017; Wang et al., 2019b).





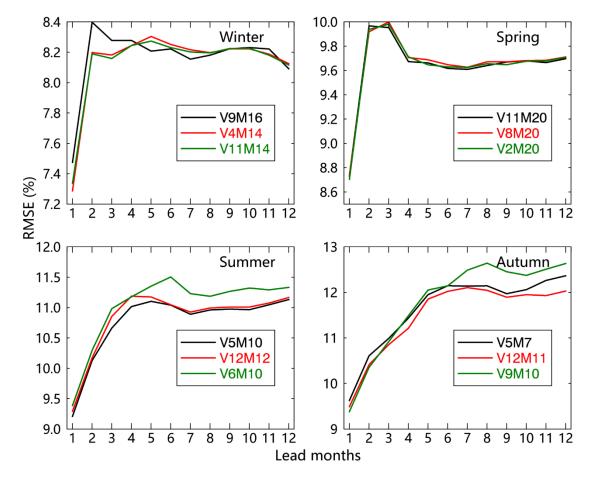


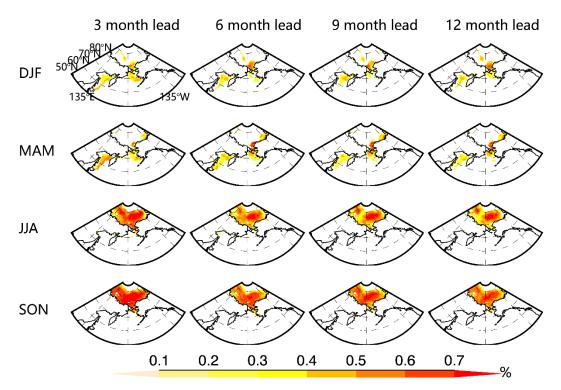


Figure 5. Same as Figure 4 but for RMSE.

429 **3.3 Assessment of model skill**

To test the forecast skill of the model, the SIC predictions were evaluated at each 430 grid cell and for all seasons using the ACC and RMSE between predicted and 431 observed anomalies, and the skill is presented at 3, 6, 9, and 12 lead months. In winter 432 (DJF), high forecast skill is concentrated in the Arctic marginal seas and peripheral 433 seas: the southern Chukchi Sea and Sea of Okhotsk (Figure 6). The skill is slightly 434 435 lower at a 12-month lead in the Sea of Okhotsk and a 9-month lead in the southern Chukchi Sea. Overall, the winter skill is roughly 0.4 in the Sea of Okhotsk and 0.5 in 436 the southern Chukchi Sea at up to 12-month leads. The spring (MAM) prediction skill 437 shows a similar pattern as that in winter but with a 0.1 increase in the ACC skill. The 438 southern Chukchi Sea and Bering Strait have higher skills than the Bering Sea. For 439 summer (JJA) predictions, the prediction skill is concentrated in the Arctic basin since 440 sea ice totally melts in the Arctic peripheral seas. The 3-month lead prediction has the 441

highest skill (>0.6) in most of the Arctic basin, while the lowest prediction skill (<0.5)
is found at a 12-month lead. The autumn (SON) prediction skill shows a similar
pattern as the summer skill but with higher correlations. In general, the model has
higher prediction skills for warm seasons, especially for autumn, than that for cold
seasons, while the lowest skill is in winter.



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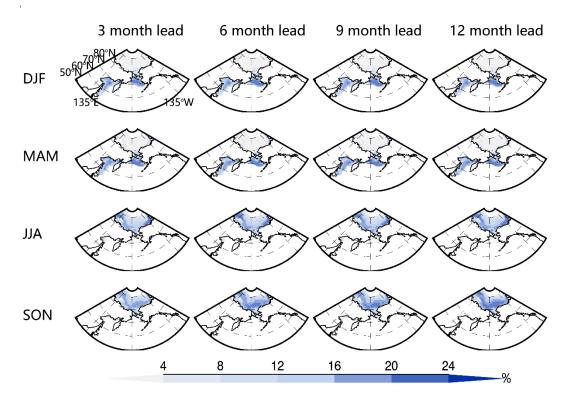
Figure 6. Cross-validated model skills measured by ACC between SIC
predictions and observation anomalies as a function of seasons and lead months. Only
the correlations that are significantly above the 95% confidence level based on a
Student's t test are included in the panels.

RMSEs are consistent with correlations: high correlations correspond to low 452 453 RMSEs, and vice versa, although minor inconsistencies occur in some seasons and 454 regions (Figure 7). The RMSE is large around the Arctic basin for the warm season and in the peripheral sea for the cold season where SIC has large variability. In the 455 456 cold season, the RMSE is larger in the Bering Sea than that in the Sea of Okhotsk. 457 The magnitudes of RMSE remain at roughly the same level from 3- to 12-month lead in most locations for all seasons. The marginal seas have larger RMSEs than the 458 central Arctic basin in both summer and autumn, while the error magnitudes in 459

460 autumn are slightly larger than those in summer but smaller than the SIC standard461 deviation across the Pacific sector (Figure 1).

462

463



464 Figure 7. Same as Figure 6 except for RMSEs. The color bar is in a unit of465 percentage.

Also, the model performance is further evaluated against anomaly persistence and 466 climatology. Averaged over the grid points in the model domain and over all seasons 467 for the period of 1980-2020, the regional Markov model's mean correlation is 468 manifestly higher, and the mean RMSE of the regional Markov model is much lower 469 than the climatology and anomaly persistence for all the lead months, especially from 470 2-month lead to 10-month lead (Figure 8). In addition, RMSE is not sensitive to the 471 lead months, showing the superiority of the regional model. These results suggest that 472 the regional Markov model can capture significantly more predictability beyond SIC 473 anomaly persistence. 474

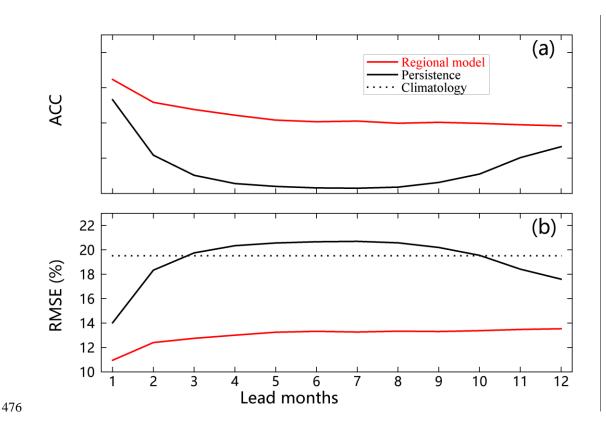
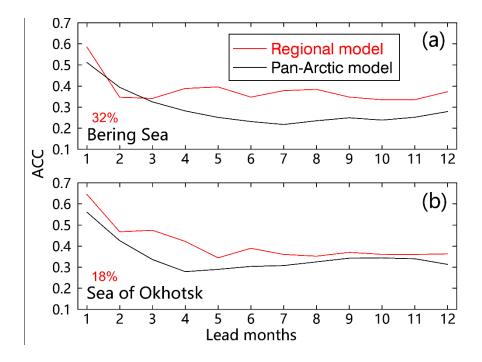


Figure 8. The prediction skill of the regional Markov model compared against that of anomaly persistence and climatology averaged over the model domain as a function of the number of month lead times.

To assess the regional model skill improvements from the pan-Arctic model 480 presented by Yuan et al. (2016), we calculated the ACC as a function of lead months 481 (Figure 9). Note that the ACC is calculated only in typical regions with large standard 482 deviations marked in Figure 1. The regional model evidently enhances the ACC skill 483 from the pan-Arctic model for the 4- to 12-month lead predictions in the Bering Sea 484 and the 1- to 7-month lead predictions in the Sea of Okhotsk. The mean ACC is also 485 increased by 32% in the Bering Sea and 18% in the Sea of Okhotsk. The prediction 486 skill of the regional Markov model within the Arctic basin also remains at the same 487 high level as that of the Pan-Arctic model (not shown), so significant skill 488 improvements occur in the peripheral sea of the Pacific sector. 489



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Figure 9. Cross-validated model skills of the regional Markov model vs. the Pan-Arctic Markov model. (a) The skills are measured by the ACC between predictions and observations with trends from 1980 to 2020 as a function of lead months in the Bering Sea. (b) is the same as (a) except for the Sea of Okhotsk. The red numbers in the bottom left of each panel represent the mean regional model skill improvements from the pan-Arctic model.

497 4 Discussion

498 **4.1 Contribution of linear trends to SIE prediction skill**

Sigmond et al. (2013) show that the linear trend in Arctic SIE dramatically 499 500 contributes to its forecast skill in the Canadian Seasonal to Interannual Prediction 501 System. Lindsay et al. (2008) show that their dynamic model prediction skill is much 502 lower when the trend is not included. They suggested that the trend accounts for 76% 503 of the variance of the pan-Arctic ice extent in September. The trend also contributes to the pan-Arctic prediction in the linear Markov model (Yuan et al., 2016). In the 504 505 Arctic, SIE has declined at -0.35 million square kilometers per decade during 1979-2020, which is significant at the 95% confidence level. The large SIC trend is mainly 506 in the Barents Sea and the Kara Sea, followed by the Chukchi Sea, while the mean 507 SIC trend in the Bering Sea and the Sea of Okhotsk is relatively weak (Figure 1). To 508

evaluate the contribution of long-term trends to the regional Markov model skill, we conducted post-prediction analysis on linear trends' contribution to the predictions skill of SIE in the Pacific-Arctic sector. We examine the time series of SIE in all calendar and lead months calculated by summing the Pacific-Arctic areas that have at least 15% SIC from observations and predictions. Monthly trends were removed from the predictions and observations, respectively. Then, the model skill is compared between the original SIE predictions and detrended SIE predictions.

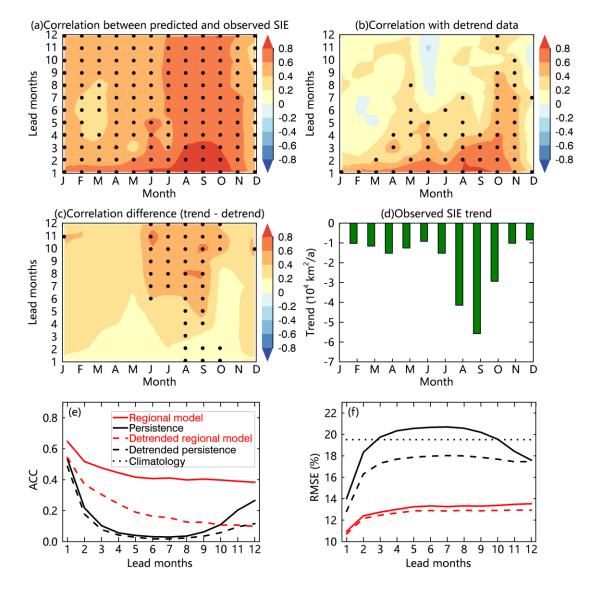


Figure 10. (a) The SIE forecast skill of the regional Markov model as a function of the calendar month and lead months. (b) The SIE forecast skill when monthly trends are removed from the predictions and observations respectively. The black dots in (a) and (b) represent the correlations that are significantly above the 95%

confidence level. (c) Difference between (a) and (b). The black dots in (c) indicate that the correlation differences are significant above the 95% confidence level. (d) Observed trends in SIE as a function of the calendar month. All monthly SIE trends are significantly above the 95% confidence level. (e, f) The prediction skill of the regional Markov model compared against that of anomaly persistence and climatology averaged over the model domain as a function of the number of month lead times.

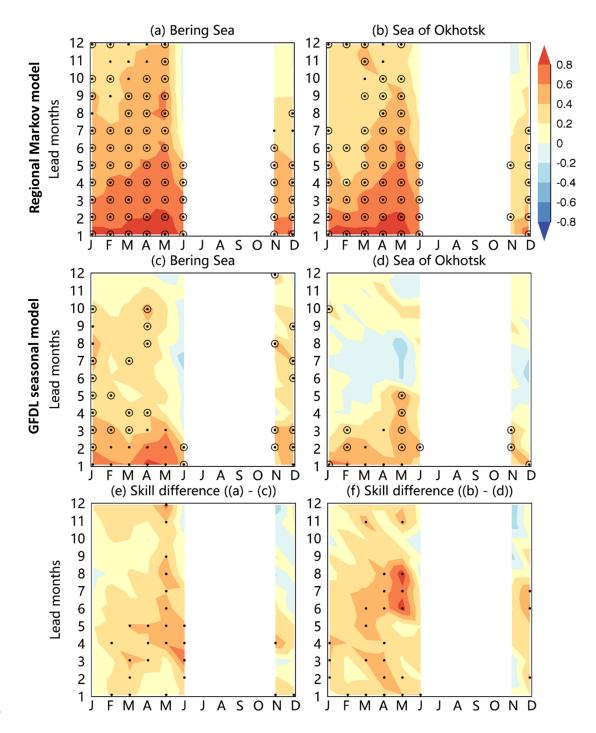
528 The model is skillful in predicting SIE from January to November at a 1-month lead (Figure 10a). The skill is particularly high for summer and autumn predictions, 529 where ACC is higher than 0.6 from July through November even at a 12-month lead. 530 531 The model skill is relatively low in May, especially at 4-8 lead months. This pattern is consistent with the seasonal variation of the model skill for SIC prediction presented 532 in Figure 6. After monthly trends are removed from predictions and observations 533 respectively, the model skill is significantly reduced for all seasons, especially for the 534 535 warm season at 6-12 months lead (Figure 10b, c). This is consistent with the seasonality of the observed trend (Figure 10d), which also peaks in late summer and 536 early fall. 537

Averaging the differences in Figure 10c over all lead times and predicted months, 538 539 the trend removal results in a mean reduction of 0.31 from the SIE forecast skill; a 53% reduction of the mean ACC. However, the model retains high prediction skill 540 (0.61) from January to November at 1-2 lead months, representing a 19% reduction 541 by the trend removal (Figure 10b), which shows the model's capability of capturing 542 543 sea ice internal variability. In addition, the trend is relatively large in the Chukchi Sea and weak outside of the Arctic Ocean. The model only reduces 13% of the mean ACC 544 from January to November at 1-2 lead months after the trend removal for the area 545 outside of the Arctic Ocean. Although linear trends contribute significantly to the 546 model skill, the regional Markov model's mean correlation is manifestly higher, and 547 the mean RMSE of the regional Markov model is much lower than the climatology 548

and anomaly persistence for all the lead months when the sea ice trend is removed(Figure 10e, f).

551 **4.2 Comparison with the GFDL model**

Yuan et al. (2016) showed that the pan-Arctic Markov model consistently 552 outperforms the NOAA/NCEP Climate Forecast System (CFSv2) and the Canadian 553 seasonal and interannual prediction system for sea ice seasonal predictions. Here the 554 555 regional Markov model is compared with the Geophysical Fluid Dynamics Laboratory Forecast-oriented Low Ocean Resolution (GFDL-FLOR) seasonal 556 prediction system (Bushuk et al., 2017a) in detrended SIE forecasts. The hindcast 557 model skills measured by the ACC for detrended SIE are high from both the regional 558 Markov model and GFDL model during January to June at a 1- to 3-month lead in the 559 Pacific sector (Figure 11). The regional Markov model skill is statistically significant 560 at lead times ranging from 1 to 6 months for target months of January-June in both the 561 Bering Sea and the Sea of Okhotsk. Below we highlight some key differences 562 563 between these two models in the Bering Sea and the Sea of Okhotsk.



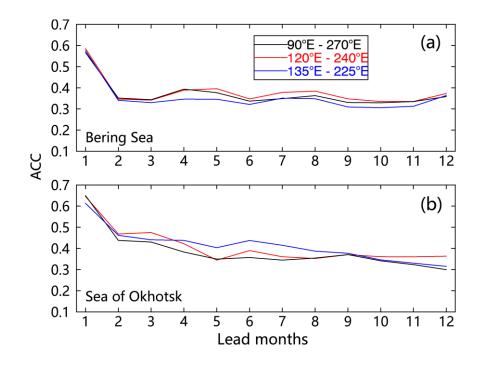
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Figure 11. (a, b) Hindcast model skill (ACC) for detrended regional SIE forecasts from 1982 to 2020 for the regional Markov model. (c, d) Same as (a, b) except for the GFDL seasonal prediction system. (e, f) is the skill difference between these two models. The black dots in (a-d) represent ACCs that are significantly above the 95% confidence level, and the circles in (a-d) indicate months in which the model's skill exceeds that of a persistence forecast. The black dots in (e-f) represent ACC differences that are significant above the 95% confidence level.

Notably, the skill from the regional Markov model is higher than that from the 572 GFDL seasonal prediction system during February to June at 3- to 6-month leads in 573 the Bering Sea and during December to June at 1- to 8-month leads in the Sea of 574 Okhotsk. In other words, the regional Markov model performs better in spring 575 prediction using winter observations for the Bering Sea and autumn observations for 576 the Sea of Okhotsk. Nevertheless, the regional Markov model slightly underperforms 577 the GFDL seasonal prediction system in predictions during November to December 578 579 using the previous winter and spring observations for the Bering Sea and using the previous winter observations for the Sea of Okhotsk. Overall, the regional Markov 580 model delivers skillful SIE predictions in seasonal ice zones of the Pacific sector up to 581 7 month lead times, an improvement from the 3 month leads displayed in the GFDL 582 seasonal prediction system. 583

584 **4.3 Sensitivity of model domain on the prediction skill**

We conducted a sensitivity analysis of the model domain on prediction skills in 585 586 the Bering Sea and the Sea of Okhotsk with the same model configuration and different sizes of the model domain. The model domain is defined by 90°E to 270°E, 587 120°E to 240°E and 135°E to 225°E respectively. The results show that the prediction 588 skill patterns based on three model domains show high similarity in the Bering Sea 589 and the skill based on the model domain (120°E to 240°E) is highest at all month 590 leads. The prediction skill in the Sea of Okhotsk based on the model domain (135°E 591 to 225°E) is highlighted at 5- to 8-month leads, but not well at 11- to 12-month leads. 592 Although the models with different sizes of model domain have different prediction 593 594 skills in the Bering Sea and the Sea of Okhotsk, the differences are not significant because all those model domains contain highly similar signals of climate variability. 595 Therefore, the regional model is not highly sensitive to the size of the model domain 596 within the Pacific-Arctic sector. 597



598

Figure 12. Cross-validated model skills of the regional Markov model with the same model configuration and different sizes of the model domain. (a) The skills are measured by the ACC between predictions and observations with trends from 1980 to 2020 as a function of lead months in the Bering Sea. (b) is the same as (a) except for the Sea of Okhotsk. The model is configured by V9M16 in winter, V11M20 in spring, V5M10 in summer, and V5M7 in autumn. The ACC values are averaged over the area marked in the black box in Figure 1.

606 **5 Conclusions**

Here, we developed a regional Markov model to predict SIC in the Pacific-Arctic 607 sector at the seasonal time scale. The model was constructed in the MEOF space so 608 that the model can capture the covariability of the North Pacific climate system 609 defined by 9 variables (SIC, OHC, SIT, SST, SAT, surface net radiative flux, surface 610 net turbulent heat flux, and geopotential height and winds at 850 hPa). Based on 611 cross-validation experiments, we selected model variables and mode truncations that 612 provided the best results in each season. These model configurations were V9M16 for 613 winter, V11M20 for spring, V5M10 for summer, and V5M7 for autumn. 614

The SIC prediction skill was evaluated at each grid cell and for all seasons using 615 ACC. The regional Markov model's skill is superior to the skill derived from anomaly 616 persistence, revealing the model's ability to capture more predictable SIC internal 617 variability than anomaly persistence. The winter skill is about 0.4 in the Sea of 618 Okhotsk and 0.5 in the northern Bering Sea at up to 12-month leads. The spring 619 prediction shows a similar pattern but with a 0.1 increase in the ACC skill. The model 620 skill in summer and autumn is more than 0.6 within the Arctic basin. Compared with 621 622 the pan-Arctic seasonal prediction model, the regional Markov model distinctly improves the SIC prediction skill in the peripheral seas of the Pacific-Arctic sector. 623 The regional model significantly enhances the correlation skill from the pan-Arctic 624 model for 4- to 12-month lead predictions in the Bering Sea and 1- to 7-month lead 625 predictions in the Sea of Okhotsk. The improvement is a 32% ACC increase in the 626 Bering Sea and 18% in the Sea of Okhotsk. In addition, similar to the pan-Arctic 627 Markov model, the regional model is not sensitive to the number of MEOF modes 628 retained, which indicates that the performance of this Markov model is robust. 629

The model retains prediction skill after sea ice trend is removed or not. However, 630 the detrended skill is notably lower, consistent with earlier sea ice prediction studies. 631 When sea ice time series includes the trend, the model can skillfully predict SIE from 632 633 January to November. The skill is particularly high for the predictions of summer and autumn sea ice at longer lead times, especially in July to November when the skill 634 is >0.6 even at a 12-month lead. Conversely, in May, the model skill is relatively low, 635 636 especially at 4-8 lead months. Trend removal from predictions and observations results in a 53% reduction of the mean ACC for the entire Pacific-Arctic sector. 637 However, the model only reduces 13% of the mean ACC from January to November 638 at 1-2 lead months after the trend removal in the Bering Sea and the Sea of Okhotsk. 639 This detrended analysis shows the model's capability of capturing sea ice internal 640 variability beyond linear trends. Furthermore, the regional Markov model improves 641 the detrended SIE prediction skill in the Pacific-Arctic sector to 7 month lead times 642 from the 3 month lead skill displayed in the GFDL-FLOR seasonal prediction system. 643

The following reasons contribute to the improvements. First, the dominant climate 644 variability in the northern mid-high latitudes mostly occurs in the Atlantic sector of 645 the Arctic and subarctic, which dictates the leading MEOF mode in the pan-Arctic 646 model. The unique characteristics of atmosphere-ocean-sea ice coupled relationships 647 in the Pacific sector may not be included in the leading MEOF decompositions of the 648 649 pan-Arctic climate system and thus are not correctly represented in the model. The regional model focuses on the Pacific-Arctic coupled atmosphere-ocean-sea ice 650 651 system and captures the dominant regional climate variability. Second, the Pacific sector of the Arctic needs a different set of variables to maximize the model's 652 predictability. We added OHC and SIT in the regional model, which provides a 653 654 crucial source of predictability in winter and summer months respectively. We also include 850 hPa GPH and winds to represent dynamic atmospheric processes in 655 656 winter and include turbulent heat flux to improve the model skill in spring. Finally, we constructed a superior model for each season, isolating the seasonally dominant 657 processes separately. 658

659 It was also found that more modes were needed in the cold season to capture the predictable signal of SIC. This suggests that sea ice in cold seasons has more 660 variability patterns compared with that in warm seasons, which may bring more errors 661 662 in prediction. SIC trends are strongest in the warm season months, which may contribute to the smaller number of modes required. In addition to the climate system 663 in the Arctic Basin, the coupled atmosphere-ocean-sea ice variability in the North 664 665 Pacific plays a more important role in the cold season and needs more modes to capture the covariability signals. 666

667

668 Data availability. The result data of this paper are available at Academic Commons,

669 Columbia's online research repository (https://doi.org/10.7916/4kpg-6904). The sea

670 ice concentration data are available at the National Snow and Ice Data Center

671 (NSIDC, https://nsidc.org/data/NSIDC-0079, last access: 1 July 2021, Comiso, 2017).

672 Monthly SIT from the Pan-Arctic Ice-Ocean and Assimilating System (PIOMAS) are

- available at the Polar Science Center (PSC)
- 674 (http://psc.apl.uw.edu/research/projects/arctic-sea-ice-volume-
- 675 <u>anomaly/data/model_grid</u>, last access: 1 July 2021, Zhang and Rothrock, 2003). The
- ocean heat content in the upper 300 m, sea surface temperature, surface air
- 677 temperature, surface net radiative flux, surface net turbulent heat flux, 850 hPa
- 678 geopotential height, and 850 hPa wind vector from ERA5 are available at the
- 679 ECMWF (<u>https://cds.climate.copernicus.eu/cdsapp#!/search?type=dataset</u>, last access:
- 680 1 July 2021, Hersbach et al., 2020).
- 681
- 682 *Supplement*. The supplement related to this article is available online at: **xxxx**.
- 683
- 684 Author contributions. YW, XY and HB conceived the idea for the protocol and
- experimental design. MB and HH provided primary support and guidance on the
- research. YW, YL and CL performed data processing. All authors drafted the
- 687 manuscript, and contributed to manuscript revision.
- 688
- 689 *Competing interests.* The authors declare that they have no conflict of interest.
- 690
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- 695 SIT from the Pan-Arctic Ice-Ocean and Assimilating System (PIOMAS) can be
- 696 obtained from the Polar Science Center (PSC)
- 697 (http://psc.apl.uw.edu/research/projects/arctic-sea-ice-volume-
- 698 <u>anomaly/data/model_grid</u>). The ocean heat content in the upper 300 m, sea surface
- 699 temperature, surface air temperature, surface net radiative flux, surface net turbulent
- heat flux, 850 hPa geopotential height, and 850 hPa wind vector from ERA5 can be

obtained from the ECMWF

702 (https://cds.climate.copernicus.eu/cdsapp#!/search?type=dataset).

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711	References
712	
713	Andersson, T. R., Hosking, J. S., Perez-Ortiz, M., Paige, B., Elliott, A., Russell, C., Law, S., Jones, D.
714	C., Wilkinson, J., Phillips, T., Byrne, J., Tietsche, S., Sarojini, B. B., Blanchard-
715	Wrigglesworth, E., Aksenov, Y., Downie, R., and Shuckburgh, E.: Seasonal Arctic sea ice
716	forecasting with probabilistic deep learning, Nature Communications, 12,
717	https://doi.org/10.1038/s41467-021-25257-4, 2021.
718	Barnston, A. G. and Ropelewski, C. F.: Prediction of ENSO Episodes Using Canonical Correlation
719	Analysis, J. Clim., 5, 1316-1345, https://doi.org/10.1175/1520-
720	0442(1992)005<1316:poeeuc>2.0.co;2, 1992.
721	Blanchard-Wrigglesworth, E., Armour, K. C., Bitz, C. M., and DeWeaver, E.: Persistence and Inherent
722	Predictability of Arctic Sea Ice in a GCM Ensemble and Observations, J. Clim., 24, 231-250,
723	https://doi.org/10.1175/2010jcli3775.1, 2011.
724	Blanchard-Wrigglesworth, E., Cullather, R., Wang, W., Zhang, J., and Bitz, C.: Model forecast skill
725	and sensitivity to initial conditions in the seasonal Sea Ice Outlook, Geophys. Res. Lett., 42,
726	8042-8048, https://doi.org/10.1002/2015GL065860, 2015.
727	Blockley, E. W. and Peterson, K. A.: Improving Met Office seasonal predictions of Arctic sea ice using
728	assimilation of CryoSat-2 thickness, Cryosphere, 12, 3419-3438, https://doi.org/10.5194/tc-
729	12-3419-2018, 2018.
730	Bushuk, M. and Giannakis, D.: The Seasonality and Interannual Variability of Arctic Sea Ice
731	Reemergence, J. Clim., 30, 4657-4676, https://doi.org/10.1175/jcli-d-16-0549.1, 2017.
732	Bushuk, M., Msadek, R., Winton, M., Vecchi, G., Yang, X., Rosati, A., and Gudgel, R.: Regional
733	Arctic sea-ice prediction: potential versus operational seasonal forecast skill, ClDy, 52, 2721-
734	2743, https://doi.org/10.1007/s00382-018-4288-y, 2019.
735	Bushuk, M., Msadek, R., Winton, M., Vecchi, G. A., Gudgel, R., Rosati, A., and Yang, X.: Skillful
736	regional prediction of Arctic sea ice on seasonal timescales, Geophys. Res. Lett., 44, 4953-
737	4964, https://doi.org/10.1002/2017GL073155, 2017a.

738	Bushuk, M., Msadek, R., Winton, M., Vecchi, G. A., Gudgel, R., Rosati, A., and Yang, X.: Summer
739	Enhancement of Arctic Sea Ice Volume Anomalies in the September-Ice Zone, J. Clim., 30,
740	2341-2362, https://doi.org/10.1175/jcli-d-16-0470.1, 2017b.
741	Bushuk, M., Winton, M., Bonan, D. B., Blanchard-Wrigglesworth, E., and Delworth, T. L.: A
742	Mechanism for the Arctic Sea Ice Spring Predictability Barrier, Geophys. Res. Lett., 47,
743	https://doi.org/10.1029/2020gl088335, 2020.
744	Bushuk, M., Winton, M., Haumann, F. A., Delworth, T., Lu, F., Zhang, Y., Jia, L., Zhang, L., Cooke,
745	W., Harrison, M., Hurlin, B., Johnson, N. C., Kapnick, S. B., McHugh, C., Murakami, H.,
746	Rosati, A., Tseng, KC., Wittenberg, A. T., Yang, X., and Zeng, F.: Seasonal Prediction and
747	Predictability of Regional Antarctic Sea Ice, J. Clim., 34, 6207-6233,
748	https://doi.org/10.1175/jcli-d-20-0965.1, 2021.
749	Cañizares, R., Kaplan, A., Cane, M. A., Chen, D., and Zebiak, S. E.: Use of data assimilation via linear
750	low-order models for the initialization of El Niño-Southern Oscillation predictions, Journal of
751	Geophysical Research: Oceans, 106, 30947-30959, https://doi.org/10.1029/2000JC000622,
752	2001.
753	Chen, D. and Yuan, X.: A Markov model for seasonal forecast of Antarctic sea ice, J. Clim., 17, 3156-
754	3168, https://doi.org/10.1175/1520-0442(2004)017<3156:AMMFSF>2.0.CO;2, 2004.
755	Chen, T. C.: The structure and maintenance of stationary waves in the winter Northern Hemisphere,
756	Journal of the Atmospheric Sciences, 62, 3637-3660, https://doi.org/10.1175/jas3566.1, 2005.
757	Cheng, W., Blanchard-Wrigglesworth, E., Bitz, C. M., Ladd, C., and Stabeno, P. J.: Diagnostic sea ice
758	predictability in the pan-Arctic and US Arctic regional seas, Geophys. Res. Lett., 43, 11688-
759	11696, https://doi.org/10.1002/2016g1070735, 2016.
760	Chi, J. and Kim, Hc.: Prediction of Arctic Sea Ice Concentration Using a Fully Data Driven Deep
761	Neural Network, Remote Sensing, 9, https://doi.org/10.3390/rs9121305, 2017.
762	Cohen, J., Zhang, X., Francis, J., Jung, T., Kwok, R., Overland, J., Ballinger, T., Bhatt, U., Chen, H.,
763	and Coumou, D.: Divergent consensuses on Arctic amplification influence on midlatitude
764	severe winter weather, Nature Climate Change, 10, 20-29, https://doi.org/10.1038/s41558-
765	019-0662-y, 2020.
766	Comiso, J. C.: Bootstrap Sea Ice Concentrations from Nimbus-7 SMMR and DMSP SSM/I-SSMIS,
767	Version 3. NASA National Snow and Ice Data Center Distributed Active Archive Center,
768	Boulder, Colorado USA, 2017.
769	Dai, P., Gao, Y., Counillon, F., Wang, Y., Kimmritz, M., and Langehaug, H. R.: Seasonal to decadal
770	predictions of regional Arctic sea ice by assimilating sea surface temperature in the
771	Norwegian Climate Prediction Model, ClDy, 54, 3863-3878, https://doi.org/10.1007/s00382-
772	020-05196-4, 2020.
773	Day, J. J., Hawkins, E., and Tietsche, S.: Will Arctic sea ice thickness initialization improve seasonal
774	forecast skill?, Geophys. Res. Lett., 41, 7566-7575, https://doi.org/10.1002/2014gl061694,
775	2014a.
776	Day, J. J., Tietsche, S., and Hawkins, E.: Pan-Arctic and Regional Sea Ice Predictability: Initialization
777	Month Dependence, J. Clim., 27, 4371-4390, https://doi.org/10.1175/JCLI-D-13-00614.1,
778	2014b.
779	Deser, C., Tomas, R., Alexander, M., and Lawrence, D.: The seasonal atmospheric response to
780	projected Arctic sea ice loss in the late twenty-first century, J. Clim., 23, 333-351,
781	https://doi.org/10.1175/2009JCLI3053.1, 2010.

782	Francis, J. A. and Vavrus, S. J.: Evidence linking Arctic amplification to extreme weather in mid-
783	latitudes, Geophys. Res. Lett., 39, https://doi.org/10.1029/2012GL051000, 2012.
784	Frankignoul, C., Sennechael, N., and Cauchy, P.: Observed Atmospheric Response to Cold Season Sea
785	Ice Variability in the Arctic, J. Clim., 27, 1243-1254, https://doi.org/10.1175/jcli-d-13-
786	00189.1, 2014.
787	Gregory, W., Tsamados, M., Stroeve, J., and Sollich, P.: Regional September Sea Ice Forecasting with
788	Complex Networks and Gaussian Processes, Weather and Forecasting, 35, 793-806,
789	https://doi.org/10.1175/WAF-D-19-0107.1, 2020.
790	Guemas, V., Blanchard-Wrigglesworth, E., Chevallier, M., Day, J. J., Déqué, M., Doblas-Reyes, F. J.,
791	Fučkar, N. S., Germe, A., Hawkins, E., and Keeley, S.: A review on Arctic sea-ice
792	predictability and prediction on seasonal to decadal time-scales, QJRMS, 142, 546-561,
793	https://doi.org/10.1002/qj.2401, 2016a.
794	Guemas, V., Chevallier, M., Deque, M., Bellprat, O., and Doblas-Reyes, F.: Impact of sea ice
795	initialization on sea ice and atmosphere prediction skill on seasonal timescales, Geophys. Res.
796	Lett., 43, 3889-3896, https://doi.org/10.1002/2015gl066626, 2016b.
797	Hamilton, L. C. and Stroeve, J.: 400 predictions: The search sea ice outlook 2008–2015, Polar Geogr,
798	39, 274-287, https://doi.org/10.1080/1088937X.2016.1234518, 2016.
799	Hersbach, H., Bell, B., Berrisford, P., Hirahara, S., Horányi, A., Muñoz-Sabater, J., Nicolas, J.,
800	Peubey, C., Radu, R., and Schepers, D.: The ERA5 global reanalysis, QJRMS, 146, 1999-
801	2049, https://doi.org/10.1002/qj.3803, 2020.
802	Horvath, S., Stroeve, J., and Rajagopalan, B.: A linear mixed effects model for seasonal forecasts of
803	Arctic sea ice retreat, Polar Geogr, doi: 10.1080/1088937X.2021.1987999, 2021. 1-18,
804	https://doi.org/10.1080/1088937X.2021.1987999, 2021.
805	Horvath, S., Stroeve, J., Rajagopalan, B., and Kleiber, W.: A Bayesian Logistic Regression for
806	Probabilistic Forecasts of the Minimum September Arctic Sea Ice Cover, Earth and Space
807	Science, 7, https://doi.org/10.1029/2020ea001176, 2020.
808	Huang, Y., Dong, X., Xi, B., Dolinar, E. K., and Stanfield, R. E.: Quantifying the Uncertainties of
809	Reanalyzed Arctic Cloud and Radiation Properties using Satellite-surface Observations, ClDy,
810	30, 8007-8029, https://doi.org/10.1175/JCLI-D-16-0722.1, 2015.
811	Kapsch, M. L., Graversen, R. G., and Tjernström, M.: Springtime atmospheric energy transport and the
812	control of Arctic summer sea-ice extent, Nature Climate Change, 3, 744-748,
813	https://doi.org/10.1038/nclimate1884, 2013.
814	Kim, KY., Hamlington, B. D., Na, H., and Kim, J.: Mechanism of seasonal Arctic sea ice evolution
815	and Arctic amplification, The Cryosphere, 10, 2191-2202, https://doi.org/10.5194/tc-10-2191-
816	2016, 2016.
817	Kimmritz, M., Counillon, F., Smedsrud, L. H., Bethke, I., Keenlyside, N., Ogawa, F., and Wang, Y.:
818	Impact of Ocean and Sea Ice Initialisation On Seasonal Prediction Skill in the Arctic, Journal
819	of Advances in Modeling Earth Systems, 11, 4147-4166,
820	https://doi.org/10.1029/2019ms001825, 2019.
821	Koenigk, T., Caian, M., Nikulin, G., and Schimanke, S.: Regional Arctic sea ice variations as predictor
822	for winter climate conditions, ClDy, 46, 317-337, https://doi.org/10.1007/s00382-015-2586-1,
823	2016.
824	Lee, S., Gong, T., Feldstein, S. B., Screen, J. A., and Simmonds, I.: Revisiting the Cause of the 1989-
825	2009 Arctic Surface Warming Using the Surface Energy Budget: Downward Infrared

826	Radiation Dominates the Surface Fluxes, Geophys. Res. Lett., 44, 10654-10661,
827	https://doi.org/10.1002/2017GL075375, 2017.
828	Lenetsky, J. E., Tremblay, B., Brunette, C., and Meneghello, G.: Subseasonal Predictability of Arctic
829	Ocean Sea Ice Conditions: Bering Strait and Ekman-Driven Ocean Heat Transport, J. Clim.,
830	34, 4449-4462, https://doi.org/10.1175/jcli-d-20-0544.1, 2021.
831	Lindsay, R., Zhang, J., Schweiger, A., and Steele, M.: Seasonal predictions of ice extent in the Arctic
832	Ocean, Journal of Geophysical Research: Oceans, 113,
833	https://doi.org/10.1029/2007JC004259, 2008.
834	Liu, Y. and Key, J. R.: Less winter cloud aids summer 2013 Arctic sea ice return from 2012 minimum,
835	Environmental Research Letters, 9, 044002, https://doi.org/10.1088/1748-9326/9/4/044002,
836	2014.
837	Luo, B., Luo, D., Wu, L., Zhong, L., and Simmonds, I.: Atmospheric circulation patterns which
838	promote winter Arctic sea ice decline, Environmental Research Letters, 12, 1-13,
839	https://doi.org/10.1088/1748-9326/aa69d0, 2017.
840	Meleshko, V., Kattsov, V., Mirvis, V., Baidin, A., Pavlova, T., and Govorkova, V.: Is there a link
841	between Arctic sea ice loss and increasing frequency of extremely cold winters in Eurasia and
842	North America? Synthesis of current research, Russian Meteorology and Hydrology, 43, 743-
843	755, https://doi.org/10.3103/S1068373918110055, 2018.
844	Morioka, Y., Iovino, D., Cipollone, A., Masina, S., and Behera, S.: Summertime sea-ice prediction in
845	the Weddell Sea improved by sea-ice thickness initialization, Sci. Rep., 11,
846	https://doi.org/10.1038/s41598-021-91042-4, 2021.
847	Msadek, R., Vecchi, G. A., Winton, M., and Gudgel, R. G.: Importance of initial conditions in seasonal
848	predictions of Arctic sea ice extent, Geophys. Res. Lett., 41, 5208-5215,
849	https://doi.org/10.1002/2014gl060799, 2014.
850	Peterson, A. K., Fer, I., McPhee, M. G., and Randelhoff, A.: Turbulent heat and momentum fluxes in
851	the upper ocean under Arctic sea ice, Journal of Geophysical Research: Oceans, 122, 1439-
852	1456, https://doi.org/10.1002/2016JC012283, 2017.
853	Peterson, K. A., Arribas, A., Hewitt, H., Keen, A., Lea, D., and McLaren, A.: Assessing the forecast
854	skill of Arctic sea ice extent in the GloSea4 seasonal prediction system, ClDy, 44, 147-162,
855	https://doi.org/10.1007/s00382-014-2190-9, 2015.
856	Petty, A., Schröder, D., Stroeve, J., Markus, T., Miller, J., Kurtz, N., Feltham, D., and Flocco, D.:
857	Skillful spring forecasts of September Arctic sea ice extent using passive microwave sea ice
858	observations, Earth's Future, 5, 254-263, https://doi.org/10.1002/2016EF000495, 2017.
859	Porter, D. F., Cassano, J. J., and Serreze, M. C.: Analysis of the Arctic atmospheric energy budget in
860	WRF: A comparison with reanalyses and satellite observations, Journal of Geophysical
861	Research Atmospheres, 116, https://doi.org/10.1029/2011JD016622, 2011.
862	Sévellec, F., Fedorov, A. V., and Liu, W.: Arctic sea-ice decline weakens the Atlantic meridional
863	overturning circulation, Nature Climate Change, 7, 604-610,
864	https://doi.org/10.1038/NCLIMATE3353, 2017.
865	Schweiger, A., Lindsay, R., Zhang, J., Steele, M., Stern, H., and Kwok, R.: Uncertainty in modeled
866	Arctic sea ice volume, Journal of Geophysical Research-Oceans, 116,
867	https://doi.org/10.1029/2011jc007084, 2011.

868	Screen, J. A. and Francis, J. A.: Contribution of sea-ice loss to Arctic amplification is regulated by
869	Pacific Ocean decadal variability, Nature Climate Change, 6, 856-860,
870	https://doi.org/10.1038/NCLIMATE3011, 2016.
871	Screen, J. A., Simmonds, I., Deser, C., and Tomas, R.: The atmospheric response to three decades of
872	observed Arctic sea ice loss, J. Clim., 26, 1230-1248, https://doi.org/10.1175/JCLI-D-12-
873	00063.1, 2013.
874	Sigmond, M., Fyfe, J. C., Flato, G. M., Kharin, V. V., and Merryfield, W. J.: Seasonal forecast skill of
875	Arctic sea ice area in a dynamical forecast system, Geophys. Res. Lett., 40, 529-534,
876	https://doi.org/10.1002/grl.50129, 2013.
877	Smith, D. M., Dunstone, N. J., Scaife, A. A., Fiedler, E. K., Copsey, D., and Hardiman, S. C.:
878	Atmospheric response to Arctic and Antarctic sea ice: The importance of ocean-atmosphere
879	coupling and the background state, J. Clim., 30, 4547-4565, https://doi.org/10.1175/JCLI-D-
880	18-0100.1, 2017.
881	Smith, L. C. and Stephenson, S. R.: New Trans-Arctic shipping routes navigable by midcentury,
882	Proceedings of the National Academy of Sciences, 110, E1191-E1195,
883	https://doi.org/10.1073/pnas.1214212110, 2013.
884	Swart, N.: Natural causes of Arctic sea-ice loss, Nature Climate Change, 7, 239-241,
885	https://doi.org/10.1038/nclimate3254, 2017.
886	Tian, T., Yang, S., Karami, M. P., Massonnet, F., Kruschke, T., and Koenigk, T.: Benefits of sea ice
887	initialization for the interannual-to-decadal climate prediction skill in the Arctic in EC-Earth3,
888	Geoscientific Model Development, 14, 4283-4305, https://doi.org/10.5194/gmd-14-4283-
889	2021, 2021.
890	Ting, M. F.: MAINTENANCE OF NORTHERN SUMMER STATIONARY WAVES IN A GCM,
891	Journal of the Atmospheric Sciences, 51, 3286-3308, https://doi.org/10.1175/1520-
892	0469(1994)051<3286:monssw>2.0.co;2, 1994.
893	Wang, L., Scott, K. A., and Clausi, D. A.: Sea ice concentration estimation during freeze-up from SAR
894	imagery using a convolutional neural network, Remote Sensing, 9, 408,
895	https://doi.org/10.3390/rs9050408, 2017.
896	Wang, L., Yuan, X., and Li, C.: Subseasonal forecast of Arctic sea ice concentration via statistical
897	approaches, ClDy, 52, 4953-4971, https://doi.org/10.1007/s00382-018-4426-6, 2019a.
898	Wang, L., Yuan, X., Ting, M., and Li, C.: Predicting summer Arctic sea ice concentration intraseasonal
899	variability using a vector autoregressive model, J. Clim., 29, 1529-1543,
900	https://doi.org/10.1175/JCLI-D-15-0313.1, 2016.
901	Wang, Y., Yuan, X., Bi, H., Liang, Y., Huang, H., Zhang, Z., and Liu, Y.: The Contributions of Winter
902	Cloud Anomalies in 2011 to the Summer Sea-Ice Rebound in 2012 in the Antarctic, Journal
903	of Geophysical Research: Atmospheres, 124, 3435-3447,
904	https://doi.org/10.1029/2018JD029435, 2019b.
905	Wu, B., Wang, J., and Walsh, J. E .: Dipole Anomaly in the Winter Arctic Atmosphere and Its
906	Association with Sea Ice Motion, J. Clim., 19, 210-225, https://doi.org/10.1175/JCLI3619.1,
907	2006.
908	Wu, Q., Cheng, L., Chan, D., Yao, Y., Hu, H., and Yao, Y.: Suppressed midlatitude summer
909	atmospheric warming by Arctic sea ice loss during 1979-2012, Geophys. Res. Lett., 43, 2792-
910	2800, https://doi.org/10.1002/2016GL068059, 2016.

- 911 Wu, Q., Yan, Y., and Chen, D.: A linear Markov model for East Asian monsoon seasonal forecast, J. Clim., 26, 5183-5195, https://doi.org/10.1175/JCLI-D-12-00408.1, 2013. 912 Xie, J., Counillon, F., Bertino, L., Tian-Kunze, X., and Kaleschke, L.: Benefits of assimilating thin sea 913 914 ice thickness from SMOS into the TOPAZ system, Cryosphere, 10, 2745-2761, 915 https://doi.org/10.5194/tc-10-2745-2016, 2016. 916 Xue, Y., Leetmaa, A., and Ji, M.: ENSO prediction with Markov models: The impact of sea level, J. Clim., 13, 849-871, https://doi.org/10.1175/1520-0442(2000)013, 2000. 917 918 Yuan, X., Chen, D., Li, C., Wang, L., and Wang, W.: Arctic sea ice seasonal prediction by a linear 919 Markov model, J. Clim., 29, 8151-8173, https://doi.org/10.1175/JCLI-D-15-0858.1, 2016. 920 Zhang, J. L. and Rothrock, D. A.: Modeling global sea ice with a thickness and enthalpy distribution 921 model in generalized curvilinear coordinates, MWRv, 131, 845-861, 922 https://doi.org/10.1175/1520-0493(2003)131<0845:mgsiwa>2.0.co;2, 2003. 923 Zuo, H., Balmaseda, M. A., Tietsche, S., Mogensen, K., and Mayer, M.: The ECMWF operational 924 ensemble reanalysis-analysis system for ocean and sea ice: a description of the system and assessment, Ocean Sci., 15, 779-808, https://doi.org/10.5194/os-15-779-2019, 2019. 925
- 926