Sea ice floe size: its impact on pan-Arctic and local ice mass, and required model complexity

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Abstract
Sea ice is composed of discrete units called floes. The size of these floes can determine the nature and magnitude of interactions between the sea ice, ocean, and atmosphere including lateral melt rate, momentum and heat exchange, and surface moisture flux. Large-scale geophysical sea ice models employ a continuum approach and traditionally either assume floes adopt a constant size or do not include an explicit treatment of floe size. Observations show that floes can adopt a range of sizes spanning orders of magnitude, from metres to tens of kilometres. In this study we apply novel observations to analyse two alternative approaches to modelling a floe size distribution (FSD) within the state-of-the-art CICE sea ice model. The first model considered, the WIPoFSD (Waves-in-Ice module and Power law Floe Size Distribution) model, assumes floe size follows a power law with a constant exponent. The second is a prognostic floe size-thickness distribution where the shape of the distribution is an emergent feature of the model and is not assumed a priori. We demonstrate that a parameterisation of in-plane brittle fracture processes should be included in the prognostic model. While neither FSD model results in a significant improvement in the ability of CICE to simulate pan-Arctic metrics in a stand-alone sea ice configuration, larger impacts can be seen over regional scales in sea ice concentration and thickness. We find that the prognostic model particularly enhances sea ice melt in the early melt season, whereas for the WIPoFSD model this melt increase occurs primarily during the late melt season. We then show that these differences between the two FSD models can be explained by considering the effective floe size, a metric used to characterise a given FSD. Finally, we discuss the advantages and disadvantages to these different approaches to modelling the FSD. We note that the WIPoFSD model is less computationally expensive than the prognostic model and produces a better fit to novel FSD observations derived from 2-m resolution MEDEA imagery but is unable to represent potentially important features of annual FSD evolution seen with the prognostic model.

1 Introduction
The Arctic sea ice cover consists of contiguous pieces of sea ice referred to as floes (WMO, 2014). Floe size has a direct impact on several processes that are important to the evolution of the sea ice, including lateral melt rate (Steele, 1992; Bateson et al., 2020); momentum exchange between the sea ice, ocean, and atmosphere (Lüpkes et al., 2012; Tsamados et al., 2014); surface moisture flux over sea ice (Wenta and Herman, 2019); sea ice rheology i.e. the mechanical response of sea ice to stress (Feltham, 2005; Rynders, 2017; Rynders et al., 2020; Wilchinsky and Feltham, 2006); and the clustering of sea ice into larger agglomerates (Herman, 2012). Historically, continuum sea ice models such as CICE (Hunke et al., 2015) have assumed that floes are of a uniform size or do not explicitly consider floe size at all when evaluating sea ice thermodynamics (Bateson et al., 2020). In contrast, observations show that floe sizes can span a large range, from metres to tens of kilometres (Stern et al., 2018a). Model studies suggest that floe size has a non-negligible impact on sea ice extent and volume through changing lateral and total sea ice melt, particularly in areas where the sea ice cover largely consists of small floes (Bateson et al., 2020; Bateson, 2021a). Floe size has been found to be particularly important in the Marginal Ice Zone (MIZ); a province of sea ice cover...
influenced by waves and swell penetrating from the open ocean (Aksenov et al., 2017; Bateson et al., 2020; Roach et al., 2019). The MIZ is taken here as regions with sea ice concentration between 15 – 80 %, a definition commonly used due to an absence of observations of ocean surface waves in sea ice over the necessary spatial scales and timescales (Horvat et al., 2020; Strong et al., 2017).

Observations of the floe size distribution (FSD) are generally fitted to a truncated power law (Perovich and Jones, 2014; Rothrock and Thorndike, 1984; Stern et al., 2018a; Toyota et al., 2006), though the extent to which a power law is a good description of the FSD is disputed (Herman, 2010; Horvat et al., 2019; Herman et al., 2021). The exponents of power laws fitted to observations of the FSD show a large amount of variability, from -1.9 to -3.5 (see summary of observations in Stern et al., 2018a). Note that all power-law exponents stated in this study refer to the non-cumulative floe number density.

Observations show spatial and temporal variability of the FSD. Stern et al. (2018b) analysed satellite imagery collected over the Beaufort and Chukchi seas and reported an approximately sinusoidal seasonal cycle in the exponent with a minimum exponent of about -2.8 in August and a maximum exponent of about -1.9 in April in both 2013 and 2014 for floes larger than 2 km. Perovich and Jones (2014) also found evidence of seasonal variation in the exponent; aerial photographic imagery was analysed from the Beaufort Sea over the period June to September 1998 for floes between 10 m to 10 km in size. They noted a change in exponent from -3.0 over June and July to -3.2 in late August, coinciding with a high wind speed event driving fragmentation of floes under wind and ocean stress. The exponent then increased to slightly above -3.1 by September due to sea ice freeze-up and floe welding.

Modelling studies have been used to understand how the observed FSD shape and behaviours could emerge from relevant processes. These FSD models can be roughly divided into two different classes: (i) models where the general shape of the FSD is fixed (e.g. Bateson et al., 2020; Bennetts et al., 2017); (ii) models where the shape of the FSD emerges from the constituent sea ice dynamical-thermoodynamical processes (e.g. Roach et al., 2018, 2019; Zhang et al., 2016). Hybrid approaches have also been proposed, e.g. Boutin et al. (2020) allows the shape of the FSD to evolve in response to processes such as lateral melting, but resets the distribution to a power law after a wave break-up event. These modelling studies have incorporated one or several processes that have been observed to influence floe size: lateral melting and growth at the edges of floes (e.g. Perovich and Jones, 2014; Roach et al., 2018); break-up of sea ice floes into smaller pieces from ocean waves (e.g. Kohout et al., 2014); floes welding together in ocean freeze-up conditions (Roach et al., 2018); the formation mechanism of new floes (Roach et al., 2018); and rafting and ridging of floes during floe collisions (Horvat and Tziperman, 2015).

Satellite imagery of the Arctic sea ice cover, especially over the winter pack ice, shows linear features such as leads and fractures referred to as slip lines or linear kinematic features (Kwok, 2001; Schulson, 2001). These linear features have been found to intersect at acute angles, independent of the spatial scale, creating individual diamond shaped regions and floes over the sea ice cover (Schulson, 2004; Weiss, 2001). The similarity of these linear features to fracture patterns formed in laboratory studies of the shear rupture mechanism, where a crack forms once a large enough shear stress is imposed, has been used to argue that the shear rupture mechanism is responsible for the linear features seen in the pack ice (Weiss and Schulson, 2009).

A discrete element model of the sea ice incorporating compressive, tensile, and shear rupture failure mechanisms acting under wind stress has been shown to produce distributions of fractures that are comparable to the distribution of linear features seen in the Arctic pack ice (Wilchinsky et al., 2010). Perovich et al. (2001) observed that summer floe break-up of sea ice in the central Arctic in 1998 was driven by thermodynamic weakening of cracks and refrozen leads in the sea ice cover during a period when the dynamic forcing and internal sea ice stress was expected to be small. Similarly, Kohout et al. (2016) noted that at the onset of a wave break-up event in the Antarctic in September 2012, floes broke apart along ridges and existing weaknesses in the sea ice cover. These observations and model studies collectively suggest that brittle fracture processes impact floe size in winter and that the resulting pattern of linear features resulting from brittle fracture may also influence floe breakup in the subsequent melt season. However, models that simulate the FSD as emerging from the interaction of physical processes have not previously included in-plane brittle fracture, only wave-induced breakup of floes (Bateson, 2021a).
In this study we will consider the WIPOFSD model (Waves-in-Ice module and Power law Floe Size Distribution model) of Bateson et al. (2020) and the prognostic FSTD (Floe-Size-Thickness distribution model) of Roach et al. (2018, 2019). The WIPOFSD model represents the class of models where the shape of the FSD in the model is actively constrained according to observations, in this case by approximating the FSD as a power law. The prognostic model represents the model class where the shape of the distribution emerges primarily from parameterisations at the process level, though with some dependency on model structure such as how the FSD is discretised over floe size categories. These models present useful case studies to examine the advantages and disadvantages of different approaches to modelling the FSD and its impacts on sea ice. We introduce a new quasi-restoring brittle fracture scheme into the prognostic model, which crudely accounts for in-plane fracture processes in winter and melting of sea ice along existing cracks and other linear features over the subsequent melt season (Bateson, 2021a). We compare the performance of the prognostic model both with and without the brittle fracture scheme in simulating the shape of novel observations of the FSD and also assess the accuracy of a power-law fit to these observations. By examining the impact of the two FSD models on the sea ice mass balance, we consider whether either FSD model can improve the performance of CICE in our model configuration. The impact of both FSD models on key sea ice and MIZ metrics is investigated, including their interannual variability and spatial differences. Finally, we explore how differences in the impacts of the two models emerge and consider the implications of the results presented here for different strategies in modelling the FSD.

This paper is structured as follows. Section 2 describes the CICE model setup used in this study, the two FSD models, and new model components and modifications introduced in this study. Section 3 describes the methodology for this research, including a description of novel observations of the FSD and an overview of model experiments. Section 4 presents the results of the analysis and simulations, divided into 3 sub-sections: a comparison of the modelled FSD to observations; a comparison of model output to the observed sea ice extent and volume reanalysis; and a pan-Arctic comparison of the impacts of the two FSD models. Section 5 discusses the results and section 6 presents conclusions and summarises the study.

2 Model description

Here we will use the CPOM (Centre for Polar Observation and Modelling) version of the Los Alamos Sea Ice model v5.1.2, known as CICE (Hunke et al., 2015). In section 2.1.1, we will outline key details of CICE that are pertinent to this study. Within the CPOM-CICE setup, we use the prognostic mixed-layer model of Petty et al. (2014), and the form drag scheme of Tsamados et al. (2014). An overview of each of these model components are provided in sections 2.1.2 and 2.1.3, respectively. In section 2.1.4, we will outline how the standard CICE setup has been modified for use with FSD models. In section 2.2 and 2.3 we will provide an overview of the two FSD models considered here: a modified version of the prognostic FSD model of Roach et al. (2018), and a modified version of the WIPOFSD model of Bateson et al. (2020).

2.1 Description of Standard Model Physics

2.1.1 Standard CICE model

CICE is a continuum numerical model of sea ice that has been designed for use within fully coupled climate models. The model consists of several different components designed to simulate the evolution of sea ice on the geophysical scale including sea ice and snow thermodynamics, sea ice dynamics, a sea ice thickness distribution, and advection. Sea ice melt is subdivided into three separate components within CICE: melt from the upper surface of the sea ice floe (top melt), melt from the bottom surface of the floe (basal melt), and melt from the sides of the floe (lateral melt). Full details of CICE can be found within Hunke et al. (2015). An overview of lateral melt treatment within CICE is presented here. The lateral melt volume is explicitly calculated within CICE:

\[
\frac{1}{A} \frac{dA}{dt} = \frac{\pi}{\alpha_{\text{shape}}A} w_{\text{lat}}. \tag{1}
\]

\(A\) represents the sea ice area fraction, such that the term on the left-hand side, \(\frac{1}{A} \frac{dA}{dt}\), represents the fractional rate of sea ice area loss due to lateral melt (units of \(s^{-1}\)). The rate of sea ice volume loss from lateral melt is the product of \(\frac{1}{A} \frac{dA}{dt}\) with the sea ice
area and mean thickness. \( \alpha_{\text{shape}} \) and \( L \) are the constant floe shape and diameter parameters, set to 0.66 and 300 m in standard CICE. \( w_{\text{lat}} \) is the lateral melt rate (units of m s\(^{-1}\)); it is a function of the elevation of the sea surface temperature above freezing for standalone CICE. The lateral heat flux, \( F_{\text{lat}} \), is calculated from the volume of lateral melt. The melting or freezing potential at the surface ocean-sea ice interface, \( F_{\text{frzmlt}} \), is calculated in CICE as the product of the difference in sea surface temperature from freezing, the specific heat capacity and density of the surface ocean, and the surface mixed-layer depth. The magnitude of \( F_{\text{frzmlt}} \) is capped at a fixed value. Following CICE sign conventions, a negative value for \( F_{\text{frzmlt}} \) corresponds to melting of sea ice. The following condition applies to the lateral and basal flux during periods of melt:

\[
|F_{\text{bot}} + F_{\text{basal}}| \leq |F_{\text{frzmlt}}|.
\]

(2)

Here \( F_{\text{bot}} \) is the net downward heat flux from the sea ice to the ocean. Where the melting potential is exceeded, \( F_{\text{bot}} \) and \( F_{\text{basal}} \) are both reduced by a common factor such that the condition set by Eq. (2) is satisfied.

### 2.1.2 The mixed-layer model

A modified version of the prognostic mixed-layer model of Petty et al. (2014) is used rather than a constant prescribed mixed-layer depth. This allows us to better account for ocean mixed-layer properties in determining lateral and basal melt rates, which are both important for FSD evolution (e.g. Bateson et al., 2020). The mixed layer model is a bulk mixed-layer model and avoids the complexity and computational expense of a full ocean model. In this model, the mixed-layer temperature, salinity, and depth are all evaluated prognostically. The deep ocean below the mixed layer is restored to observations, and the model is zero-dimensional i.e. defined for each model grid cell without lateral interactions between grid cells. Full details of the original scheme are available in Petty et al. (2014). The original Petty et al. (2014) mixed-layer model was set-up and tested for the Southern Ocean where the stronger winds and waves, weaker upper ocean stratification, and larger extent of the MIZ enables a high wind power input leading to a much deeper mixed-layer when compared to the Arctic. Here we adopt several adjustments to the mixed-layer model made by Tsamados et al. (2015) to ensure reasonable performance of the mixed-layer model in the Arctic. The three-component model of surface layer, mixed layer, and deep ocean is replaced with a two-component model, with just a mixed layer and deep ocean. In addition, the mixed-layer temperature and salinity are restored to the 10 m depth temperature and sea surface salinity from a monthly climatology reanalysis dataset.

### 2.1.3 Form drag scheme

Recent versions of CICE include an implementation of the form drag scheme (Hunke et al., 2015) following Tsamados et al. (2014), which aims to better describe the turbulent momentum and heat exchange between the sea ice, ocean, and atmosphere by accounting for the topography of the sea ice. The scheme of Tsamados et al. (2014) replaces the constant drag coefficients in CICE with explicit representations of both form drag and skin drag terms, \( C_a \), the updated expression for the atmospheric neutral drag coefficient, can be calculated in terms of contributions from specific spatial features of the sea ice cover:

\[
C_a = C_a^{\text{skin}} + C_a^{\text{frd}} + C_a^{\text{floe}} + C_a^{\text{pond}}.
\]

(3)

\( C_a \), the updated expression for the ocean neutral drag coefficient, can similarly be calculated as:

\[
C_w = C_w^{\text{skin}} + C_w^{\text{frd}} + C_w^{\text{floe}}.
\]

(4)

Here \( C^{\text{skin}} \) refers to the skin drag term, and \( C^{\text{frd}} \), \( C^{\text{floe}} \) and \( C^{\text{pond}} \) refer to form drag terms for ridges and keels, floe edges, and melt pond edges respectively. Tsamados et al. (2014) outline the following expression for \( C^{\text{floe}} \) in the case of surface momentum exchange over the sea ice-atmosphere interface with a reference height of 10 m:

\[
C_a^{\text{floe}} = \frac{1}{2} \alpha_{\text{shape}} \frac{H_f}{L} \frac{H_f}{\kappa_{\text{floe}}} \left[ \ln \left( \frac{H_f}{\kappa_{\text{floe}}} \right) \right]^2.
\]

(5)

Here \( \alpha_{\text{shape}} \) is a local form drag coefficient, taken to be constant. \( \alpha_{\text{shape}} \) is a geometrical parameter to account for the shape of the floes. The ratio \( \frac{H_f}{\kappa_{\text{floe}}} \) takes the value 0.2. \( L \) is the average floe diameter. \( \kappa_{\text{floe}} \) is the roughness length of water upstream of
the floe, given by 3.27 x 10^4 m (Hunke et al., 2015). \( H_f \) is the freeboard of the floe i.e. the distance between the upper surface of the floe and the sea surface. To calculate \( C_{\text{floe}}^{f,\text{free}} \), the form drag of sea ice floes at the sea ice-ocean interface, \( H_f \) in Eq. (5) is replaced with \( D \), the draft. \( D \) is defined as the distance between the lower surface of the floe and the sea surface. \( S_e \) is the sheltering function and is calculated as a function of sea ice area fraction, \( A \), using an approximation from Lüpkes et al. (2012):

\[
S_e = 1 - e^{-s_I (1-A)}.
\]  

(6)

\( s_I \) is the floe sheltering attenuation coefficient, with \( s_I = 11 \) as per Lüpkes et al. (2012).

### 2.1.4 Modifications to standard CICE to incorporate FSD effects

The CPOM-CICE setup has been adapted to represent the impact of the FSD on the sea ice cover via both the lateral melt rate and floe edge contribution to form drag. Eq. (1), used to calculate the fraction of sea ice area lost due to lateral melting, is modified to:

\[
\frac{1}{\bar{A}} \frac{dA}{dt} = \pi \frac{L}{a_{\text{shape}} 1_{\text{eff}}} \omega_{\text{lat}}.
\]  

(7)

\( L \), the constant floe diameter, has been replaced by \( l_{\text{eff}} \), the effective floe size. \( l_{\text{eff}} \) is the floe diameter that has the same perimeter per unit sea ice area as a given FSD (Bateson et al., 2020). Eq. (5), the expression for the floe edge contribution to form drag at the sea ice-atmosphere interface, has also been modified:

\[
C_{\text{floe}}^{f,\text{free}} = \frac{1}{2} \frac{c_f}{a_{\text{shape}}} \left( \frac{S_e}{l_{\text{eff}}} \right)^2 \left( \frac{H_f}{\zeta_{\text{max}}} \right)^2 \left( \frac{10}{\zeta_{\text{max}}} \right)^2.
\]  

(8)

The equivalent expression at the sea ice-ocean interface is modified similarly. \( l_{\text{eff}} \) is used here since it characterises the average floe length scale.

### 2.2 The prognostic FSD model

#### 2.2.1 Prognostic model overview

The prognostic FSD model used here has been adapted from the version presented by Roach et al. (2018). At the core of the prognostic FSD model is the joint floe size-thickness probability distribution (FSTD), \( f(r, h) \, dr \, dh \). This describes the fraction of a grid cell covered by floes with a radius between \( r \) and \( r + dr \) and thickness between \( h \) and \( h + dh \). Processes that change floe size represented in this model include lateral melting and freezing, wave-induced breakup of floes, and welding together of floes. The model also allows the formation of new floes, complete melt out of existing floes, and advects the FSTD between grid cells. The parameterisation introduced in Roach et al. (2019) to determine the size of newly formed floes from the local wave conditions has also been included in the setup used here. A full description of the original prognostic floe size-thickness distribution model is presented in Roach et al. (2018) with details of the wave-dependent floe formation parameterisation available in Roach et al. (2019). Note that the in-wave scheme used by Roach et al. (2018) has been adapted here to calculate \( H_\text{max} \), the spectral height parameter, and \( \lambda_p \), the wavelength corresponding to the peak wave energy, within the sea ice-covered grid cells for use with the wave-dependent floe formation parameterisation. We also introduce a novel treatment of brittle fracture to the prognostic model. This brittle fracture scheme is described in section 2.2.2.

For the prognostic FSD model \( l_{\text{eff},n} \), the effective floe size for the \( n \)th sea ice thickness category, is calculated in terms of \( L(r, h) \), the modified areal FSTD, where the integral of \( L(r, h) \) over the range \( r_{\text{min}} \) to \( r_{\text{max}} \) is 1 i.e. the distribution is normalised per thickness category:

\[
l_{\text{eff},n} = \frac{2}{\int_{r_{\text{min}}}^{r_{\text{max}}} r^{-1} L(r, n) \, dr}.
\]  

(9)

A representative \( l_{\text{eff}} \) for the full FSTD is then calculated as the area-weighted average of \( l_{\text{eff},n} \) across the thickness categories.

#### 2.2.2 The brittle fracture scheme

In a brittle fracture event cracks can propagate and, where they exceed a critical speed, become unstable and branch. Individual
branches and fractures can also merge, with the lifetime of the fracture determining the size of the subsequent fragment that forms. The branching results in a hierarchical process, with several levels of branches forming from the same central fissure (Åstrom et al., 2004; Kekäläinen et al., 2007). Idealised models of brittle fracture show that the fragment size distribution adopts a power law with an exponent of -2 and an upper cut-off determined by an exponential in the square of the fragment size (Gherardi and Lagomarsino, 2015).

In order to investigate the potential impact of in-plane brittle fracture processes on the FSD, the prognostic model has been modified to include a quasi-restoring brittle fracture scheme, which applies a conditional restoring to the FSD towards the theoretical distribution produced by idealised models of brittle fracture i.e. a power law with an exponent of -2. In this scheme brittle fracture can transfer sea ice area fraction from a larger floe size category to the adjacent smaller category. In addition, the following condition must be fulfilled:

\[
\ln n_i - \ln n_{i-1} > -2.
\]

Here \( n \) and \( d \) refer to the floe number density and diameter at the midpoint of category \( i \) respectively. This condition means that the restoring scheme only applies where the slope between adjacent categories in log-log space is greater (more positive) than -2. The sea ice area fraction transferred in a single timestep between two adjacent categories is \( C_{bf}a_i \) where \( a_i \) is the area fraction of the larger category. \( C_{bf} \), the restoring constant, is calculated as:

\[
C_{bf} = \frac{\tau}{\Delta t}.
\]

Here \( \tau \) is the restoring timescale, and \( \Delta t \) is the model timestep. Figure 1 provides a visual summary of the quasi-restoring scheme. The motivation for this scheme is to impose a restoring tendency on the FSD to the predicted shape of the distribution if it were acting only under brittle fracture. The transfer of sea ice area fraction is only allowed in one direction from larger to adjacent smaller categories since floes cannot unfracture. This process is conservative in sea ice area i.e. the reduction in floe area in the larger category will be matched by an increase in floe area in the smaller category.

A value for the restoring timescale, \( \tau \), needs to be determined. There are two mechanisms through which brittle fracture can impact the sea ice cover. Fracture events occur regularly through autumn, winter and spring within the pack ice to form linear features like leads, which subsequently freeze up again. These linear features are then vulnerable to increased thinning and melting, increasing the likelihood of break-up along these features during late spring and summer as the sea ice retreats. It is this second mechanism that is of more relevance when considering the impacts of the FSD on the seasonal retreat of the Arctic sea ice. The timescale for a crack or linear feature in the sea ice to fully melt through is taken to be of the order of 1 month. For simplicity, \( \tau \) is here set to 30 days.

There are limitations associated with this approach. The use of a constant restoring timescale means that the strength of the impact of brittle fracture processes on the FSD is assumed to be the same everywhere and at all times. However, the brittle fracture-derived mechanisms operate over different timescales and scale with different properties. In addition, the brittle fracture approach assumes transfer of sea ice area fraction only between adjacent categories, whereas physically a larger floe can break down into floes of any smaller size.

### 2.3 The WIPoFSD model

The WIPoFSD model used in this study has been adapted from the version presented Bateson et al. (2020), which in turn was based on the coupled ocean–waves–in–ice model NEMO–CICE–WIM developed at the UK National Oceanography Centre (NOC). The NEMO–CICE–WIM model approximates the shape of the FSD as a multiple-exponent truncated power law with coefficients depending on ice fraction; in this study we use a constant exponent as per Bateson et al. (2020). The WIPoFSD model fits the number-weighted FSD, \( N(x) \), where \( x \) is the floe diameter, to a power law distribution:

\[
N(x|d_{\text{min}} \leq x \leq l_{\text{var}}) = Cx^\alpha.
\]

\( N \) has units of reciprocal metres, all floe size variables have units of metres, and \( \alpha \), the power law exponent, is dimensionless.
\( l_{\text{var}} \), the variable FSD tracer, evolves in each grid cell as a function of physical processes between the upper and lower floe diameter cut-offs, \( d_{\text{max}} \) and \( d_{\text{min}} \) respectively. The model is initiated with \( l_{\text{var}} \) set to \( d_{\text{max}} \) in all grid cells where sea ice is present. \( \mathcal{C} \) is calculated so that the total floe area is equal to the total sea ice area. The model parameterises the role of four processes in the evolution of the FSD: lateral melting, wave-induced break-up, winter growth, and advection. A full description of how these processes are represented within the WIPoFSD model is available in Bateson et al. (2020); a summary has also been provided here in Appendix A.

The version of the WIPoFSD model used here includes a modified lateral melting scheme to that presented in Bateson et al. (2020). In the WIPoFSD model, processes are parameterised in terms of how they impact \( l_{\text{var}} \) and useful properties such as \( l_{\text{eff}} \) can easily be calculated from \( l_{\text{var}} \). The appeal of this approach is its simplicity. The broader impacts of a power-law distribution on the sea ice cover can be explored whilst also including spatial and temporal variability of the FSD within the model. For mechanical processes such as wave break-up, the use of \( l_{\text{var}} \) is particularly suitable. It marks a transition from a regime where flocs are being broken up to a regime where the number of flocs is increasing due to the break-up of larger flocs. For thermodynamic processes it makes less intuitive sense. It is not possible to define two clear regimes; instead, flocs across the distribution reduce in diameter by the same magnitude in response to a lateral melting event. Here, we have modified the lateral melting scheme to calculate the change in \( l_{\text{eff}} \) rather than \( l_{\text{var}} \), since it is possible to calculate exactly how \( l_{\text{eff}} \) would change in response to a given perturbation of the FSD. Whilst it is not possible to capture cumulative changes to the FSD due to the constraints of having a fixed exponent power-law distribution with a lower floe size limit, it is possible to approximate how the effective floe size, \( l_{\text{eff}} \), will change over one timestep by integrating across the exact updated FSD after a lateral melting event. The updated effective floe size, \( l_{\text{eff,new}} \), can then be calculated as follows:

\[
\left[ l_{\text{eff,new}} \right] = \frac{\left[ l_{\text{var}} \right]^{\frac{3 + \alpha}{2}} - \left[ d_{\text{min}} \right]^{\frac{3 + \alpha}{2}}}{\left( \frac{3 + \alpha}{2} \right)} A_{\text{old}} \left( \frac{\left[ l_{\text{var}} \right]^{\frac{2 + \alpha}{2}} - \left[ d_{\text{min}} \right]^{\frac{2 + \alpha}{2}}}{\left( \frac{2 + \alpha}{2} \right)} \right) + \Delta l \left[ \frac{\left[ l_{\text{var}} \right]^{\frac{1 + \alpha}{2}} - \left[ d_{\text{min}} \right]^{\frac{1 + \alpha}{2}}}{\left( \frac{1 + \alpha}{2} \right)} \right]^{-1}
\]

(13)

Here \( \Delta l \) is the length of lateral melting experienced by each floe edge and \( A_{\text{old}} \) and \( A_{\text{new}} \) refer to the sea ice area fraction before and after the lateral melting event, respectively. \( l_{\text{var,new}} \) can then be calculated from \( l_{\text{eff,new}} \) using a Newton-Raphson iterative scheme. A full derivation of Eq. (13) and description of the iterative scheme can be found in Appendix B.

3 Methodology

3.1 Sea ice simulations

All simulations in this study are initiated with an ice-free Arctic on 1st January 1980 and evaluated over a 37-year period until 31st December 2016. The first ten years of these simulations are taken as spin-up, with timeseries presented over the period 1990-2016. Averages are calculated over the period 2000-2016, taken as representative of the current climatology. The CPOM version of CICE is run over a pan-Arctic domain with a 1° tripolar (129x104) grid. Sections of the Hudson Bay and Canadian Archipelago are not included within the model domain. Surface forcing is obtained from 6-hourly NCEP-2 reanalysis fields (Kanamitsu et al., 2002). The mixed-layer properties are restored over a timescale of 5 days to a monthly climatology reanalysis at 10 m depth taken from the MyOcean global ocean physical reanalysis product (MYO reanalysis; Ferry et al., 2011). The deep ocean is restored after detrainment from the mixed layer over a timescale of 90 d to the winter climatology (for this we take the mean conditions on 1 January from 1993 to 2010) from the MYO reanalysis. The minimum mixed-layer depth is set to 10 m. \( H_s \), the significant wave height (m), and \( T_p \) the peak wave period (s), of ocean surface wave fields are obtained from the ERA-Interim reanalysis dataset (Dee et al., 2011). The forcings are updated at 6 h intervals, but only for locations where the sea ice is at less than 1% sea ice concentration. The general CPOM-CICE setup used for all simulations in this study has several further differences to CICE version 5.1.2, in addition to those described in section 2, based on recent work by Schröder et al. (2019). The maximum meltwater added to melt ponds is reduced from 100% to 50%. This produces a more realistic distribution of melt ponds (Rösel et al., 2012). Snow erosion, to account for a redistribution of snow based on wind fields, snow density, and surface topography, is parameterised...
based on Lecomte et al. (2015) with the additional assumptions described by Schröder et al. (2019). The “bubbly” conductivity formulation of Pringle et al. (2007) is also included, which results in larger thermal conductivities for cooler ice. The longwave emissivity is increased from 0.95 to 0.976. The following parameters are modified from the default values used in Tsamados et al. (2014): atmospheric background drag coefficient, ocean background drag coefficient, ridge impact parameter, and keel impact parameter of the form drag parameterisation. They are set to 0.001, 0.0005, 0.1 and 0.5 respectively. Schröder et al. (2019) discuss how these changes increase ice drift over level ice and reduce it over ridged ice leading to more realistic ice drift patterns.

A total of five different simulations are used here; a summary of these simulations is presented in Table 1. The reference simulation, ref, sets \( l_{eф} \) to a fixed value of 300 m. The prognostic FSD setup, \( \text{prog-best} \), uses the standard 12 floe size categories outlined in Roach et al. (2018) and the 5 standard CICE thickness categories (Hunke et al., 2015). Apart from the modifications outlined in section 2.2.2 – 2.2.4, prognostic model setup and parameter choices are identical to Roach et al. (2011). The simulation using the WIPoFSD model, \( \text{WIPo-best} \), uses an identical setup to that in Bateson et al. (2020), but now incorporating the updated lateral melting scheme described in section 2.3. For the WIPoFSD model parameters, \( d_{\text{max}} \) is set to the standard value used by Bateson et al. (2020) of 30 km. The minimum floe size that can be resolved in \( \text{prog-best} \) is 5.375 m and hence \( d_{\text{min}} \) will be set to the same value. \( \alpha \) is set to -2.56, the average value across the three locations represented in the novel FSD observations that will be discussed in Sect. 3.2. This means that parameter or model choices for both \( \text{WIPo-best} \) and \( \text{prog-best} \) have been selected to produce a best fit to the same set of observations. Two additional simulations are performed using the prognostic model to compare against observations of the FSD. These two simulations will include a total of 16 floe size categories using Gaussian spacing rather than the standard 12. The prognostic model produces an unphysical increase or ‘uptick’ in the largest few categories, at least partially a result of having a fixed maximum floe size in the model (Roach et al., 2018). By using 16 floe size categories rather than 12, the largest 4 floe size categories that include this ‘uptick’ will fall outside the range of floe sizes included in the comparison to observations. The first of these additional prognostic simulations, \( \text{prog-16} \), is otherwise identical to \( \text{prog-best} \). The second, \( \text{prog-16-nof} \), excludes the brittle fracture scheme described in section 2.2.3. Figure 2 presents an example of the model output from \( \text{prog-16-nof} \), showing the perimeter density distribution within the MIZ for April, June, and August, averaged over 2000-2016. Figure 2 demonstrates how the “uptick” is confined to the largest 3–4 floe size categories.

### 3.2 Novel observations of the FSD

To assess the performance of the two alternative FSD models, we consider a new observational dataset that has not been used to motivate the development of either FSD model. These novel FSD observations have been produced by Byoungjun Hwang and Yanan Wang as part of the NERC funded project ‘Towards a marginal Arctic sea ice cover’ (NE/R000654/1). The observations consist of 41 separate samples over the period 2000-2014, covering three months, May – July, and collected from three regions: the Chukchi Sea (70 N, 170 W); the East Siberian Sea (82 N, 150 E); and the Fram Strait (84.9 N, 0.5 E). The raw floe size data has been retrieved using the algorithm described in Hwang et al. (2017) from the GFL HRVI (Global Fudicials Library high-resolution visible-band image) imagery that has been declassified by the MEDEA group (Kwok and Untersteiner, 2011). This has been made available publicly as LIDPs (Literal Image Derived Products) at 1 m resolution (available at http://gfl.usgs.gov/). The total image size varies between observations, but generally has length dimensions of 5 – 20 km. The resolution of the imagery was reduced from 1 m to 2 m prior to processing by the algorithm. For the first step of processing the raw floe size data, consisting of a list of individual floe sizes, are sorted into the Gaussian-distributed floe size categories used within the prognostic model for ease of comparison. Any floes that exceed the upper diameter cut-off of the largest category, 1892 m, will be discarded from the analysis. This step is necessary because the presence of a single large floe, comparable to the image size, can cause a large perturbation across the distribution reported for that location. Instead, only floe size categories that are small enough to consistently be populated by multiple floes across all sampled images are retained. A lower floe diameter cut-off of 104.8 m is also applied to this analysis, taken to be the smallest...
floe size that can be reliably resolved by the methodology and resolution used. The limiting factor on the smallest resolved floe size is the ability to resolve gaps between floes. Once floes outside the range of 104.8 m to 1892 m in diameter have been discarded, the total area of remaining floes is calculated and taken to be the total sea ice area for normalising the reported perimeter density (perimeter per unit sea ice area). The average normalised perimeter density for each floe size category is then reported at the mid-point of that category. The floe perimeter density distribution, $P_{FSD}(x)$, is considered in this study rather than the floe number or area distribution since it is the perimeter that has been identified as most relevant to the impact of the FSD on sea ice when considering lateral melt (Bateson et al., 2020). It is defined here as:

$$P_{FSD} = \frac{\int_{x_{\text{min}}}^{x_{\text{max}}} \rho_{FSD}(x) \, dx}{x_{\text{max}} - x_{\text{min}}}$$

(14)

Here $x_{\text{min}}$ and $x_{\text{max}}$ refer to the minimum and maximum floe diameters respectively within an FSD. $P_{FSD}$ is the perimeter density across the whole distribution, calculated as the total perimeter divided by the total area of all floes in the distribution.

The concept of perimeter density is not novel to this study e.g. Roach et al. (2019), Bateson et al. (2020).

To compare model output to the observations of the FSD, two sample years will be selected for each location: Chukchi Sea, May – June 2006 (4 LIDPs), May 2014 (4 LIDPs); East Siberian Sea, June 2001 (3 LIDPs), June – July 2013 (2 LIDPs); Fram Strait, June 2001 (6 LIDPs), June 2013 (2 LIDPs). These specific years have been selected as they all include at least two separate LIDP-derived floe size observations. Perimeter density distributions from the prognostic model are reported as an average over one or two months for the relevant region. The months selected for this average are chosen to minimise the difference between the mean day of collection for observations and median day of the model output. Figure 3 shows the specific areas over which the FSD is averaged. Each case study area consists of a set of 5 x 5 grid cells that includes the location where the observations were drawn from.

3.3 Observations of sea ice extent and volume

We use sea ice concentration products from the Bootstrap algorithm version 3 (Comiso, 1999) and NASA Team algorithm version 1 (Cavalieri et al., 1996). Comparisons will focus on the pan-Arctic extent rather than the spatial distribution of sea ice concentration due to the high uncertainty in summer and MIZ of satellite-derived concentration products (Meier and Notz, 2010). We use the sea ice volume product from PIOMAS, the Pan-Arctic Ice Ocean Modelling and Assimilation System (Zhang and Rothrock, 2003). Whilst the PIOMAS volume product is a reanalysis and does not incorporate direct observations of the sea ice thickness, this product is often used to test model performance in simulating the total Arctic sea ice volume due to the challenges in estimating sea ice thickness from radar altimetry and limited availability of in-situ thickness measurements.

4. Results

4.1 A comparison to observations of the FSD

The observations described in section 3.2 can be used to test how well both the prognostic FSD model and a power-law fit capture the shape of the observed FSD for mid-sized floes. Figure 4 compares FSD observations, a power-law fit, and prognostic model output from both the prog-16 (with brittle fracture) and prog-16-nobf (without brittle fracture) simulations for each selected case study region and time period described in section 3.2. The results in Fig. 4 show that prog-16-nobf performs poorly in capturing the behaviour of the FSD for mid-sized floes. The perimeter density distribution predicted by the prognostic model for each category is in general multiple orders of magnitude from the observed value. In particular, the slope of the distribution is much steeper (more negative) for the model output than observations. Figure 4 also shows that prog-16 significantly improves the shape of the emergent perimeter density distribution for the floe size range considered compared to prog-16-nobf. The updated model performs particularly well in the East Siberian Sea and Fram Strait but less well in the Chukchi Sea, as shown in panels a and b in Fig. 4. Overall, the inclusion of the quasi-restoring brittle fracture scheme represents a significant improvement in the ability of the prognostic model to capture the shape of the FSD for mid-sized floes. It should be noted that these comparison tests do not include floes smaller than 100 m in the comparison, which are particularly important for determining the impact of the FSD on the sea ice mass balance.
It is worth commenting briefly on how the brittle fracture scheme can improve model performance compared to observations, given it is a counterintuitive result that increasing floe break-up would produce a shallower slope in perimeter density. As discussed in section 3.2, the largest floe size categories in the prognostic model are excluded from the comparison to observations to exclude the non-physical ‘uptick’ that forms (Fig. 2). Whilst a reduction in ice area fraction in the largest category and an increase in the smallest category can be expected, the change in ice area fraction in the remaining categories depends precisely on the balance between ice area fraction lost from that category and ice area fraction gained from the adjacent larger category.

4.2 A comparison to observations of sea ice extent and volume

In this section the CICE simulations prog-best and WIPO-best, summarised in Table 1, will be compared against observations or reanalysis of the sea ice cover. Both of these simulations have been optimised against the FSD observations presented in section 4.1. The prog-best simulation includes the brittle fracture scheme described in section 2.2.2 and the exponent selected for the WIPO-best simulation is the average fitted exponent across the FSD observations. These two simulations, alongside the ref simulation that applies a constant floe size, will be tested against observations by considering the following metrics: the performance of the simulations in capturing the annual and interannual variability of the sea ice extent and volume; the performance of the simulations in capturing interannual trends in the sea ice extent and volume; and whether the inclusion of either FSD model reduces known model bias in the sea ice area fraction.

Figure 5 shows timeseries for the total Arctic sea ice extent and volume in March and September over 1990 – 2016 for ref, WIPO-best, prog-best alongside observations (extent) or reanalysis (volume) over the same period. These plots show that the inclusion of either FSD model does not improve the ability of the CICE model to simulate either the annual or interannual variability in sea ice extent and volume. The differences between the simulations are significantly smaller than the difference between ref and the observations / reanalysis in both March and September. Figure 6 shows the percentage difference in the March and September sea ice extent and volume over 1990 – 2014 relative to the climatological mean for each simulation over the same period. This metric is also plotted for the observations and reanalysis. Clear negative trends in the March volume and September volume and extent can be seen. Figure 6 shows that ref already performs well in capturing these observed trends, particularly in September, without the addition of an FSD model. However, the addition of either FSD model does not improve the ability of CICE in simulating these trends.

Previous studies, e.g. Bateson et al. (2020) and Roach et al. (2018), show that the largest impacts of including an FSD model occur within the MIZ. Figure 7 compares timeseries from 1990 – 2016 for the MIZ and pack ice extent in both March and September for each of ref, prog-best, and WIPO-best in addition to the satellite-derived observations. Figure 7 shows that all three simulations generally simulate both the MIZ and pack ice extent within observational uncertainty, though this is partly due to the large differences in MIZ and pack ice extent between the two observational products. The simulations are unable to replicate a negative trend in March pack extent shown within both observations. prog-best produces both a higher MIZ extent and variability on average in March compared to ref but a lower extent in September. In comparison, WIPO-best shows a reduced MIZ extent throughout the year compared to ref. In September, all three simulations produce very similar pack extents, but in March there is a moderate reduction for prog-best and a small reduction for WIPO-best relative to ref. Overall, inclusion of FSD processes within CICE results in changes to extent metrics of order 1 x 10^7 km^2.

4.3 Comparing the two FSD models

In this section, the prog-best and WIPO-best simulations will be compared directly, considering several metrics including total sea ice extent and volume, and spatial difference plots for area fraction, thickness, and l_eff. The aim of this comparison is to understand the differences in the impacts of the two alternative FSD models and how these differences emerge.

4.3.1 Pan-Arctic extent and volume

Figure 8 shows the percentage difference in the sea ice extent and volume for both prog-best and WIPO-best relative to ref averaged over 2000 to 2016, indicating the impact of each FSD scheme compared to assuming a constant floe size. The
prognostic model produces a mean reduction in sea ice extent of just under 2% in June, compared to less than a 1% reduction with the WIPOFSD model; this reduction is just under 2% for both models in August. The average reduction in sea ice volume in September is 2.5% and 4% for WIPO-best and prog-best respectively relative to ref. The minimum reduction for the prognostic model is 1.5% in the spring months, compared to just 0.5% with the WIPOFSD model. The prognostic model also shows a larger interannual variability (indicated by the width of the ribbon) compared to the WIPOFSD model.

Figure 8 considers differences in the mean behaviour only, however the mean behaviour may obscure important trends. Figure 9 shows the percentage difference in total Arctic sea ice extent and volume for both prog-best and WIPO-best compared to ref from 1990 – 2016 in March and September. The differences are consistent with Fig. 8, with prog-best generally showing larger reductions than WIPO-best relative to ref other than for September extent. There is a possible positive trend for the difference in the March sea ice extent and a negative trend for the September sea ice extent for both prog-best and WIPO-best relative to ref, but this is inconclusive due to high interannual variability relative to the strength of the trend. More robust trends can be seen in the sea ice volume e.g. prog-best produces an average reduction in September volume of 2% compared to ref in the 1990s increasing to about a 5% reduction in the 2010s. A similar but weaker trend can be seen for WIPO-best relative to ref. The reduction in the March sea ice changes from about 1.1% in the 1990s to about 1.5% in the 2010s for prog-best relative to ref, whereas there is no evidence of any trend for WIPO-best relative to ref. Figure 8 shows that the interannual variability shown in Fig. 7 can be partly explained by long term trends, particularly for prog-best relative to ref.

4.3.2 Sea ice melt components

In WIPO-best and prog-best, floe size impacts the sea ice via two model components: form drag and lateral melt volume. Bateson et al. (2020) demonstrated that increases in the lateral melt with reductions in floe size were compensated by a reduction in the basal melt. This compensation effect was shown to primarily be a result of the physical reduction of sea ice area in locations of high basal melt. Figure 10 explores whether the same basal melt compensation effect is produced by the prognostic model. Figure 10 shows annual timeseries of the difference in the cumulative top, basal, lateral, and total melt for both prog-best and WIPO-best relative to ref averaged over 2000 – 2016. For both models a significant increase in lateral melt is compensated by a reduction in basal melt of similar magnitude, leading to only a small net increase in total melt. Whilst the increase in the lateral melt for prog-best is higher than for WIPO-best, both show an increase in the total melt of a small and similar magnitude. This suggests that any feedbacks on the total melt resulting from the decrease in area from enhanced lateral melt, such as the albedo feedback, are weak even for the prog-best simulation. The similar magnitude of change in the total melt also means that the results shown in Figs 8 and 9, where the sea ice volume is lower in both September and March for prog-best compared to WIPO-best, are unlikely to be driven by an increase in the total melt. Also shown in Fig. 10 is the difference in melt components for prog-best compared to WIPO-best. The difference in cumulative total melt peaks in July and then decreases and switches sign. This is consistent with Fig. 8, where prog-best shows a stronger reduction in sea ice extent in the early melt season compared to WIPO-best, but the reduction in extent in August is comparable.

4.3.3 Spatial distribution of ice area fraction, thickness, and effective floe size

Previous studies e.g. Bateson et al. (2020) and Roach et al. (2018), have shown large FSD model impacts locally even where pan-Arctic impacts are small. Figure 11 shows maps of differences in sea ice area fraction and thickness for both prog-best and WIPO-best relative to ref, and spatial distribution plots of $l_{eff}$ for both prog-best and WIPO-best. Results are presented for March, June, and September. The spatial pattern of the reduction in area fraction is similar for both prog-best and WIPO-best relative to ref but the magnitude is larger for the former in the early melt season. The region where $l_{eff}$ drops significantly below 280 m in WIPO-best is generally confined to the outer MIZ. For the prognostic model, $l_{eff}$ is generally well under 100 m across the MIZ. The distribution in $l_{eff}$ corresponds to the regions of largest reduction in sea ice area fraction for prog-best relative to ref in the early melt season. The reduction in sea ice area fraction in the September MIZ is comparable in magnitude for both prog-best and WIPO-best, which is consistent with the results presented in Figs 8 and 10. For prog-best, $l_{eff}$ is shown to increase within the MIZ over the course of the melt season from March to September, which can explain the different results
in the early and late melt season. *prog-best* shows an increase in the sea ice area fraction across much of the pack ice in September, with a particularly strong response in the central Beaufort Sea. This response is not seen with *WIPo-best* because the maximum $l_{\text{eff}}$ is 300 m for the selected model parameters i.e. the same as the fixed floe size in *ref*, whereas for *prog-best* it can be as high as 1700 m. For *prog-best* relative to *ref*, reductions in sea ice thickness persist through March and June across the central Arctic, but for *WIPo-best* differences only persist in locations that become marginal for at least some of the year and along the Canadian archipelago. In September, the reduction in thickness spans the full Arctic for *prog-best*, whereas differences are mostly confined to the outer MIZ for *WIPo-best*.

Figure 11 shows much higher spatial variability in $l_{\text{eff}}$ for *prog-best* compared to *WIPo-best*. Further analysis (not presented here) indicates the high spatial variability in $l_{\text{eff}}$ for the prognostic model cannot easily be attributed to a single process but is particularly sensitive to the floe formation mechanism, brittle fracture scheme, and welding, all processes not explicitly represented in the WIPoFSD model. Processes included in the WIPoFSD model, such as wave break up of floes and lateral melt, are not found to have a large impact on the spatial distribution of $l_{\text{eff}}$ within the prognostic model.

### 4.3.4 Standard deviation of sea ice area fraction, thickness, and effective floe size

Figure 11 is useful to understand the spatial distribution of the pan-Arctic changes in sea ice state shown in Fig. 8, but the inclusion of an FSD model may not only act to change the mean state of the sea ice but also the interannual variability. Figure 12 shows the standard deviation in sea ice area fraction and thickness for *ref*, the difference in standard deviation for area fraction, thickness, and $l_{\text{eff}}$ for *prog-best* and *WIPo-best* relative to *ref*. Changes to the standard deviation in area fraction have a low magnitude and are isolated rather than part of a more systematic change in behaviour. For the standard deviation in thickness, differences are again small and isolated in March, but larger changes can be seen within the September MIZ of up to 10 – 20%. These changes in thickness variability correspond to where the largest differences in sea ice thickness can be seen in Fig. 11 and are consistent with the high interannual variability of the reduction in sea ice volume suggested in Fig. 9. For *WIPo-best*, variability in $l_{\text{eff}}$ is generally only seen within the MIZ as $l_{\text{eff}}$ remains close to the maximum value within the pack ice. For *prog-best*, the standard deviation in $l_{\text{eff}}$ broadly correlates to the magnitude of $l_{\text{eff}}$ seen in Fig. 11. High interannual variability can be seen across the pack ice in both March and September for *prog-best*, suggesting that all locations experience some differences in the contributing processes to the emergent FSD year on year. These distinct patterns in interannual variability of $l_{\text{eff}}$ for *prog-best* and *WIPo-best* may therefore be a useful metric to measure in the Arctic to discriminate between the different approaches to modelling the FSD.

### 5. Discussion

#### 5.1 Inclusion of brittle fracture in FSD models

Observations of the sea ice cover suggest brittle fracture processes have a role in the evolution of the FSD (e.g. Perovich et al., 2001; Kohout et al., 2016). The inclusion of the quasi-restoring brittle fracture scheme into the prognostic FSD model significantly improved the simulated shape of the FSD for mid-sized floes of 100 m – 2000 m (Fig. 4). Considering the distributions presented in Fig. 4 for the standard prognostic model without brittle fracture, it does not obviously follow that a redistribution of sea ice area from larger categories to smaller categories would improve the shape of the distribution compared to the observations given the gradient is already too negative. However, the largest floe size categories in the prognostic model are excluded from the comparison to observations to exclude the non-physical ‘uptick’ that forms, as demonstrated in Fig. 2. The inclusion of brittle fracture acts to reduce the size of the uptick and redistributes sea ice area to mid-sized floe categories. There are two plausible factors that can produce this uptick: the truncation of the maximum possible floe size such that sea ice area accumulates in the largest category that would otherwise be distributed over several larger categories; and missing floe fragmentation processes in the prognostic model. The results presented in Fig. 4 provide evidence for the latter, but observations of floes above the range included in the 16-category prognostic model suggest the truncation effect also contributes.
Including brittle fracture leads to a better fit to observations in the Fram Strait and East Siberian Sea. However, improvements are less impressive for the Chukchi Sea site. This an illustrative example of the limitations of the brittle fracture scheme used here. To understand the difference in model performance at these sites, consider their locations shown in Fig. 3. Brittle fracture acts on the FSD at two of the three sites throughout the year, but only for part of the year for the Chukchi Sea since it fully transitions to an ice-free state over the melting season, unlike the other sites. \( \tau \) is not a restoring timescale in the traditional sense. \( \tau \) here represents the timescale for two neighbouring categories to reach an equilibrium state, but the prognostic FSD model consists of 16 categories for the simulations considered in Fig. 3. It would take several months for a starting state with all sea ice area in the largest floe size category to reach equilibrium across all floe size categories, a long enough lag to explain the different prognostic model performance for the Chukchi Sea.

Despite the limitations with the quasi-restoring brittle fracture scheme described here and in section 2.2.2, the results shown in Fig. 4 strongly suggest that brittle fracture or related fragmentation processes are required to capture the shape of the FSD for mid-sized floes, motivating the need to develop a physically derived brittle fracture parameterisation for FSD models.

### 5.2 Differences in the impacts of the FSD models and how they emerge

Focusing first on a pan-Arctic scale, Figures 5-7 do not provide any evidence that the inclusion of an FSD model improves the performance of CICE in simulating the aggregated Arctic sea ice extent and volume behaviours and trends against observations or reanalyses. This does not preclude either FSD model from being an important improvement to sea ice models; these improvements may be at a regional scale rather than at a pan-Arctic scale. As previously discussed, it is a significant challenge to obtain high accuracy observations of the sea ice concentration and thickness, and the use of the latter to validate models requires a careful use of case studies such as demonstrated by Schröder et al. (2019). Nevertheless, significant biases have been identified in coupled climate models in simulating the sea ice concentration (Ivanova et al., 2016) and CICE, in particular, has been shown to overpredict the sea ice concentration at the sea ice edge and underpredict the concentration within the pack ice (Schröder et al., 2019). In Bateson et al. (2020), the WIPoFSD model was found to provide a limited correction to this model bias. Similarly, Fig. 10 shows that the prognostic model produces a stronger correction to this model bias, driving reductions in sea ice area fraction in the MIZ and small increases in area fraction in the pack ice.

Figures 8-11, described in section 4.3, all highlight a key difference in the impact of the two FSD models. \textit{prog-best} produces a stronger reduction in sea ice area fraction relative to \textit{ref} in the early melt season but a more comparable reduction by August compared to \textit{WIPo-best}. This difference can be attributed to the different treatment of floe formation and growth processes between the two models. The WIPoFSD model uses a simple restoring approach that operates over a short timescale of 10 days, which is applied during conditions of freezing. This means that over winter \( \ell_{\text{eff}} \) will be at or close to its maximum value uniformly across the sea ice, except in locations at the outer sea ice edge that are exposed to wave break-up, as shown in Fig. 11. In comparison, the prognostic model aims to represent physically floe formation and growth processes such that the homogeneity produced after the freeze-up season with the WIPoFSD model is not seen with the prognostic model in Fig. 11. In the early melt season \( \ell_{\text{eff}} \) is particularly low across the MIZ due to wave activity in this region causing existing floes to fragment and new floes to form in the smallest size category. As the melting season proceeds, floes in the smallest floe size categories preferentially lose surface area and melt out in response to lateral melting, a behaviour that is also visible in Fig. 11 e.g. \( \ell_{\text{eff}} \) increases in the Fram Strait between March and June. This behaviour is not possible with the WIPoFSD model since it has a fixed exponent and minimum floe size. These results show the value of \( \ell_{\text{eff}} \) in being able to characterise and understand how the inclusion of either FSD model impacts the sea ice cover and in understanding how differences in these impacts emerge. These results also show the potential limitations of using a simplified FSD model such as the WIPoFSD model; even though a power law might in general be a good fit to the FSD over the melt season, there could still be important mechanisms and features of FSD impacts that it fails to properly capture.

In section 4.3.2 it was noted that the total cumulative melt is slightly higher for \textit{WIPo-best} compared to \textit{prog-best} despite the larger reduction in volume for \textit{prog-best} compared to \textit{WIPo-best} relative to \textit{ref} shown in Figs 8 and 9. Figure 10 also shows...
the lateral to basal melt ratio is higher for prog-best compared to WIPo-best; the change in this ratio may present an alternative explanation to explain the larger volume reduction produced by prog-best. Two floes of identical shape, diameter but different thickness will, under identical conditions, contribute the same sea ice volume to the total basal melt (provided the thinner floe does not melt out) whereas the thicker floe will contribute a greater volume to the total lateral melt, since lateral melt volume is proportional to thickness. Therefore, increasing the lateral melt contribution to the total melt increases the loss of thick ice in a given melt season, even if the total melt volume remains constant. Vertical sea ice growth rates are inversely proportional to the sea ice thickness, and hence whilst a system with an increased proportion of thin ice would produce a faster increase in sea ice volume during the early freeze-up season, the net vertical growth over the full Arctic winter season is relatively insensitive to initial sea ice thickness for areas of either thin or no sea ice cover. Instead, the peak sea ice volume that can be reached during a period of freeze-up is dependent on the area of thick sea ice, since thick ice can take several Arctic winters to form. This result shows that the inclusion of an FSD model can have important mechanistic impacts on sea ice evolution, even if the immediate change in pan-Arctic properties are small. Smith et al. (2021) recently demonstrated that the partitioning between lateral and basal melt can also have a large impact on open water formation, with implications for albedo feedback.

5.3 Advantages and disadvantages of FSD models

We have examined examples of two broad categories of FSD models where either the FSD shape is imposed or where the FSD shape emerges from parametrisations at process level. An important test for any FSD model is whether it simulates realistic FSD shape and variability. Figure 4 shows a power law produces a strong fit to observations of floes over a mid-sized (100 m – 2 km) range. The prognostic model with brittle fracture performed comparably to the power-law fit except in the Chukchi Sea. However, this comparison only included observations covering one quarter of the year and excluded floes smaller than about 100 m and larger than 2 km. Floes smaller than 100 m are particularly important for determining the impact of a given FSD on sea ice evolution (Bateson et al. 2020) and there is growing evidence that the power law may not hold across all floe sizes (Horvat et al., 2019) and that the power-law exponent changes significantly over an annual cycle (Stern et al., 2018b). In Bateson et al. (2020), it was found that imposing the annual cycle reported by Stern et al. (2018b) on the exponent only had a small impact on the sea ice state. The annual cycle imposed was taken as the mean from the Chukchi and Beaufort Seas only, so it is not sufficient evidence to conclude that a fixed exponent is a reasonable assumption. The WIPoFSD model is not computationally expensive; including the WIPoFSD model within CICE increases model run time by 30%. In comparison, the prognostic model is computationally expensive and is data intensive. The use of 12 floe size categories with the standard 5 thickness categories introduces a total of 60 floe size-thickness outputs to the model and simulation times increase by a factor of 2.1. Extending this to 16 floe size categories leads to a total of 80 categories and a further increase in simulation run time. The number of floe size-thickness categories can also make it difficult to diagnose and understand how changes to the sea ice state emerge in response to prognostic model processes. Identifying the mechanisms driving changes in sea ice state is more straightforward with the WIPoFSD model. Development of the prognostic model can also be more time intensive since each process requires either observations or lab-based studies to determine a suitable parameterisation to describe the physical process in the model.

A key advantage of the prognostic model approach is the shape of the FSD is an emergent feature of the model rather than imposed, avoiding the need to make assumptions about FSD shape or variability, notwithstanding the newly introduced brittle fracture scheme, which, as discussed above, requires further development. This also means the prognostic model can be used to understand the role of individual processes in determining the emergent FSD and can respond to future changes in the behaviour or strength of these processes. In section 5.2 it is shown how behaviours seen within the prognostic model such as the preferential melt out of smaller floes from the distribution or explicit simulation of floe formation and growth processes have impacts on the evolution of the sea ice cover. These impacts are not seen within the WIPoFSD model due to the restrictions of assuming a fixed FSD shape. Furthermore, the WIPoFSD model effectively operates by tuning model parameters to best capture observations of the FSD, however this tuning may not be appropriate over the full timescale of a simulation.
5.4 Limitations of these results

Whilst the parameters selected for the standard setup of the WIPoFSD model considered here were motivated as a best fit to observations, Bateson et al. (2020) demonstrated high sensitivity in the model response within the observational uncertainty of these parameters. For the prognostic model, the uncertainties are primarily associated with both the representation of existing processes and important processes not yet represented in the model. For example, Roach et al. (2019) demonstrated that using a full wave model coupled to CICE rather than the in-ice wave scheme used here approximately doubled the total lateral melt, though this was compensated by a reduction in basal melt of comparable magnitude. The use of a standalone sea ice model prevents the full representation of sea ice-ocean or atmosphere feedbacks. For example, Roach et al. (2019) found with a coupled sea ice-ocean model that their prognostic FSD setup produced an increase in lateral melt in the Arctic about 3–4 times higher than the reduction in basal melt, resulting in an approximately 20% increase in the total lateral and basal melt. Roach et al. (2019) do not identify the mechanism responsible for this increase, so it is not clear whether the FSD model setups used here would produce a similar response in a coupled CICE-NEMO setup. In addition, the role of the FSD is likely to be different for sea ice in the Southern Ocean. Several observational studies e.g. Alberello et al. (2019) show the presence of FSDs dominated by pancake ice floes smaller than 10 m. Sensitivity studies presented in Bateson et al. (2020) suggest that distributions dominated by such small floes can dramatically reduce the sea ice mass balance. Roach et al. (2019) apply a version of the prognostic model to both the Arctic and Antarctic (including a coupled wave model but not the brittle fracture scheme) and demonstrate a pan-Antarctic reduction in sea ice volume whereas in the Arctic there are regions of volume increase and decrease, with the latter found primarily in the MIZ.

6. Conclusion

We have compared two alternative methods to model the sea ice floe size distribution: a prognostic model where the shape of the FSD emerges from the model physics (Roach et al., 2018, 2019), and the WIPoFSD model where the shape of the FSD is constrained to a power law with a fixed exponent (Bateson et al., 2020). Observations of linear features in the winter pack ice (Kwok, 2001; Schulson, 2001) and the break-up of sea ice along these existing features over the subsequent melt season (Perovich et al., 2001; Kohout et al., 2016) motivated the inclusion of a quasi-restoring brittle fracture scheme within the prognostic FSD model. The inclusion of the brittle fracture scheme dramatically improved the performance of the prognostic model in simulating the shape of the perimeter density distribution of mid-sized floes compared to novel, high-resolution observations of the FSD, particularly in the Fram Strait and East Siberian Sea. Neither the inclusion of the WIPoFSD model or prognostic FSD model within CICE led to unequivocal improvement in simulating the observed sea ice extent and volume, though changes to the spatial distribution in sea ice area fraction were consistent with known model biases, particularly for the prognostic model. Clear differences were found between the models, particularly in terms of the strength of the early melt season and long-term trends in the sea ice volume for both March and September. The effective floe size, previously introduced as a useful way to characterise the FSD in Bateson et al. (2020), was found to be a useful tool in understanding how differences between the two models emerge. The faster retreat of sea ice in the early melt season for the prognostic model compared to the WIPoFSD model was attributed to the different model treatments of floe formation and growth in winter. The slower retreat in extent during the later melt season for the prognostic model was found to be a result of melt out of smaller floes, a feedback process not possible with the WIPoFSD model due to the restrictions on FSD shape. The difference in the response in the sea ice volume despite only small changes in the total sea ice melt was attributed to the impact of increased lateral to basal melt ratio on the sea ice thickness distribution and how that would influence sea ice growth. We discussed the advantages and disadvantages of the two approaches to modelling the FSD. The WIPoFSD model is more computationally efficient and a simple model to interpret. In addition, a power law fit using a single exponent averaged across all FSD observations produced a good fit to the observed FSD across all locations in the dataset considered here. However, some behaviours seen with the prognostic model could not be replicated by the WIPoFSD model due to restrictions on FSD shape. Furthermore, the prognostic model is better able to respond to regime change of the processes that...
Future work should focus on the development of a full physical treatment of the impact of brittle fracture on the FSD. Whilst the quasi-restoring scheme presented here is a useful tool to improve prognostic model performance and based on idealised models of brittle fracture, it makes use of significant assumptions that need to either be justified or improved upon. In addition, the results presented here highlight the need to collect further observations of the FSD. $l_{\text{eff}}$ has been shown to be a useful metric to characterise the FSD and its impact on the sea ice mass balance (see also Bateson et al., 2020). Horvat et al. (2019) demonstrated that it is possible to estimate the area-weighted floe size from satellite imagery, hence it is plausible that $l_{\text{eff}}$ could also be estimated from satellite imagery in a similar manner. This would present a way to observationally establish the spatial and temporal variability of the FSD. These observations can then provide further constraints for FSD models, which have previously been demonstrated to have high sensitivity to FSD parameters (Bateson et al., 2020) and how individual processes are represented or parameterised (Roach et al., 2019).

Appendices

Appendix A – Description of processes represented in the WIPOFSD model

The WIPOFSD model presented in Bateson et al. (2020) includes four mechanisms that can change $l_{\text{var}}$ and therefore the FSD. The first of these, lateral melting, is treated by assuming the reduction in $l_{\text{var}}$ from lateral melting is proportional to the reduction in the sea ice area fraction from lateral melting, $\Delta A_{\text{lim}}$:

$$l_{\text{var,final}} = l_{\text{var,initial}} \sqrt{1 - \frac{\Delta A_{\text{lim}}}{A}}. \quad (A1)$$

The second mechanism is the break-up of floes by waves. If a wave break-up event is identified, $l_{\text{var}}$ is then updated according to the following expression:

$$l_{\text{var}} = \max \left( d_{\text{min}}, \frac{\lambda_{W}}{2} \right). \quad (A2)$$

Here $\lambda_{W}$ is a representative wavelength, in units of metres. In order to calculate the value of $\lambda_{W}$ and to identify where the ocean surface conditions are sufficient to drive wave break-up, the WIPOFSD model uses a wave attenuation and floe breakup scheme adapted from the waves-ice model of the Nansen Environmental and Remote Sensing Centre (NERSC) Norway, details are given by Williams et al. (2013a, 2013b). The WIPOFSD model also uses a wave advection scheme developed by NOC in the NEMO-CICE-WIM model. Further details of how these schemes have been incorporated into the WIPOFSD model, and how break-up events are identified, are available in Bateson et al. (2020).

The WIPOFSD model treats floe growth using a simple floe restoring scheme. During periods where CICE identifies frazil ice growth i.e. when the freezing / melting potential is positive, $l_{\text{var}}$ is restored to its maximum value:

$$l_{\text{var,final}} = \min \left( d_{\text{max}}, l_{\text{var,initial}} + \frac{d_{\text{max}} d_{\text{t}}}{T_{\text{rel}}} \right). \quad (A3)$$

$T_{\text{rel}}$ is a relaxation timescale that represents how quickly floes would be expected to grow to cover the entire grid cell area. It is set to 10 days, taken as representative of the rapid increase in sea ice concentration during the early freeze-up season. In grid cells that newly transition to having a sea ice cover from an ice-free state, $l_{\text{var}}$ is initiated with the value $d_{\text{min}}$.

The fourth and final mechanism treated by the WIPOFSD model is advection. $l_{\text{var}}$ is transported using the horizontal remapping scheme with a conservative transport equation, the standard within CICE for ice area tracers (Hunke et al., 2015).

Since $l_{\text{var}}$ is not defined independently for each thickness category, the change in $l_{\text{var}}$ after advection and subsequent mechanical redistribution is calculated independently for each thickness category, with the net change in $l_{\text{var}}$ taken as the average across all the thickness categories.

Appendix B – The updated lateral melting scheme

A derivation is presented in this section of Eq. (13), the updated lateral melting scheme within the version of the WIPOFSD model used in this study. The floe number distribution can be written explicitly according to Eq. (12) and by evaluating the
constant, $C$, according to its definition as described in section 2.3:
\[ N(x \mid d_{\text{min}} \leq x \leq d_{\text{var}}) = \frac{(3 + \alpha)A_l^2}{\alpha_{\text{shape}}} \frac{x^{\alpha}}{[l_{3}^{\text{var}} - d_{3}^{\text{min}}]} \]  
(B1)

Bateson et al. (2020) derives an expression of $l_{\text{eff}}$ for this distribution:
\[ l_{\text{eff}} = \frac{(2 - \alpha)[l_{3}^{\text{var}} - d_{3}^{\text{min}}]}{(3 - \alpha)\{l_{4}^{\text{var}} - d_{4}^{\text{min}}]} \]  
(B2)

It is also possible to derive an expression for $l_{\text{eff}}$ after lateral melting. If floes experience an amount $\Delta l$ of lateral melting on each edge, the total diameter of each floe must decrease by $2\Delta l$. This changes the size of the floes but does not impact the shape of the number distribution i.e. floes of diameter $G$ prior to lateral melting and floes of diameter $G - 2\Delta l$ after lateral melting have the same number density, $N(G)$, where $N(x)$ is the number distribution prior to lateral melting. This description is true provided $d_{\text{min}} > 2\Delta l$ i.e. no floes are completely lost from the distribution due to lateral melting. The total perimeter after the lateral melting event, $P_{\text{lm}}$, can therefore be calculated as:
\[ P_{\text{lm}} = \int_{d_{\text{min}}}^{l_{\text{var}}} \pi (x - 2\Delta l)N(x) \, dx. \]  
(B3)

$N(x)$ in Eq. (B3) is the number FSID prior to lateral melting, and this equation holds provided $d_{\text{min}} > 2\Delta l$. This can then be evaluated as:
\[ P_{\text{lm}} = \frac{\pi(3 + \alpha)A_{\text{old}}^2}{\alpha_{\text{shape}}\{l_{1}^{\text{var}} - d_{1}^{\text{min}}]} \left[\frac{[l_{2}^{\text{var}} - d_{2}^{\text{min}}]}{2 + \alpha} + 2\Delta l\left[\frac{[l_{1}^{\text{var}} - d_{1}^{\text{min}}]}{1 + \alpha}\right]\right]. \]  
(B4)

The subscript for $A_{\text{old}}$ indicates that this is the sea ice area fraction before lateral melting. An expression for the total perimeter in terms of the new effective floe size, $l_{\text{eff,new}}$, can also be written using the updated sea ice area fraction after lateral melting, $A_{\text{new}}$:
\[ P_{\text{eff,new}} = \frac{A_{\text{new}}^2\pi}{\alpha_{\text{shape}}\l_{\text{eff,new}}}. \]  
(B5)

The two expressions for total perimeter after lateral melting can then be equated to give the updated effective floe size, $l_{\text{eff,new}}$:
\[ l_{\text{eff,new}} = \frac{[l_{3}^{\text{var}} - d_{3}^{\text{min}}]}{(3 + \alpha)A_{\text{old}}} \left\{\frac{[l_{4}^{\text{var}} - d_{4}^{\text{min}}]}{2 + \alpha} + 2\Delta l\left[\frac{[l_{1}^{\text{var}} - d_{1}^{\text{min}}]}{1 + \alpha}\right]\right\}^{-1}. \]  
(B6)

It is possible to calculate an analytical result for $A_{\text{new}}$ as a result of lateral melting of floes across the distribution, however CICE already accounts for changes to the sea ice area fraction. For internal model consistency, it is this internal CICE $A_{\text{new}}$ that will be used. In order to parameterise processes in terms of $l_{\text{eff}}$, a method is needed to calculate $l_{\text{var}}$ from $l_{\text{eff}}$. There is no analytical solution to this problem; instead a numerical approach must be used such as Newton-Raphson iteration:
\[ x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}, \]  
(B7)

where $x$ is $l_{\text{var}}$ and the function to solve is derived from the expression to calculate $l_{\text{eff}}$ for the power law distribution i.e.
\[ f(l_{\text{var}}) = 0 = \frac{(2 + \alpha)[l_{3}^{\text{var}} - d_{3}^{\text{min}}]}{(3 + \alpha)\{l_{4}^{\text{var}} - d_{4}^{\text{min}}]} - l_{\text{eff}}. \]  
(B8)

The iterative scheme can then be evaluated as:
\[ l_{\text{var,n+1}} = l_{\text{var,n}} - \frac{[l_{2}^{\text{var}} - d_{2}^{\text{min}}]}{\{l_{4}^{\text{var}} - d_{4}^{\text{min}}]} - l_{\text{eff}}\left[\frac{[l_{1}^{\text{var}} - d_{1}^{\text{min}}]}{(2 + \alpha)}\right]. \]  
(B9)

Note that, for simplicity, where $\alpha = -1, -2$ or -3, a value of 0.001 will be taken off. Whilst an exact solution is possible for these cases, this adds additional and unnecessary complexity to a scheme that is already an approximation. This scheme is evaluated until either $l_{\text{var,n+1}} - l_{\text{var,n}}$ is less than 0.01% of the change in $l_{\text{eff}}$ over a timestep or until a maximum of 50 iterations are
complete. In general, the threshold for convergence is achieved within 10 iterations, however where $l_{eff}$ and $l_{var}$ are close in value i.e. where $l_{var}$ is within a few metres of $d_{min}$, convergence can take longer than 50 iterations. These circumstances are associated with conditions of very low sea ice concentration, where the net error in the lateral melt volume calculation associated with the failure to reach the threshold condition for convergence is negligible.

Data Availability

Model output used in this paper is publicly available via the University of Reading research data archive (http://dx.doi.org/10.17864/1947.300; Bateson, 2021b). Output for the simulation prog-16-nofb can be found listed under chapter 6 as cice_cpom_prog_16cat_nofb. Output for the simulation prog-16 can be found listed under chapter 7 as cice_cpomProg_16cat. Output for the simulations ref, prog-best, and WIPo-best can be found listed under chapter 8 as cice_cpom_ref, cice_cpom_prog_best, and cice_cpom_WIPo_best respectively. Mask files defining the regions described in Fig. 3 can be found listed under chapter 6. Please contact the corresponding author to discuss access to model code.

Author Contributions

YW and BH produced the novel FSD observations from satellite imagery. AB completed the comparison of the novel FSD observations to model output, with support from YW, BH, DF, and DS. DS adapted the prognostic FSTD model of Roach et al. (2018) into the CPOM CICE stand-alone set-up. AB implemented the novel modifications described in this paper to the original FSD model setups. AB completed simulations and analysis under the supervision of DF and DS and with further support from YW, BH, JR, and YA. DS provided additional technical support. AB composed the paper with feedback and contributions from all authors.

Competing interests

Daniel Feltham, David Schröder and Yevgeny Aksenov are members of the editorial board of the journal.

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A brief note on WIPoFSD model development: The WIPoFSD model code has been derived and modified from a scheme used within the coupled NEMO-CICE–WIM sea ice–ocean–waves interaction model developed by the L. Hosekova and Y. Aksenov at the National Oceanography Centre (NOC) in the EC FP7 project ‘Ships and Waves Reaching Polar Regions’ (SWARP) in 2014-2017 (https://cordis.europa.eu/project/id/607476; grant agreement 607476). The physics of waves–ice interactions in NOC–WIM model uses the framework of the waves–in–ice model of the Nansen Environmental and Remote Sensing Center (NERSC, Norway) by Williams et al. (2013a, b). Given the differences between the NERSC Arctic regional model setup (HYCOM ocean model with an early EVP sea ice rheology realisation and Semtner’s sea ice thermodynamics) and the global NOC–NEMO–CICE setup, the coding of the NOC–WIM model and all coupling with ocean and sea ice modules has been done completely from the start by NOC. During the course of the NOC–NEMO–CICE–WIM model development L.
Hosekova, advised by Y. Aksenov, has incorporated extra key processes in the model, including up-wind wave spectrum advection in the ice-covered areas, floe sizes evolution due to lateral floes melting, including renormalization algorithm with the Newton-Raphson method to compute mean from maximum floe sizes, freeze-up and floe sizes advection, and an optional choice of the multiple power law exponents for the PSD (Rynders, 2017); for these we also acknowledge contributions from G. Madec (IPSL) and A.J.G Nurser (NOC). The NOC–NEMO–CICE–WIM model includes the novel development of the combined EVP-collisional rheology (EVCP) (Feltham, 2005) coded in CICE by S. Rynders and advised by Y. Aksenov and D. Feltham (Rynders, 2017, Rynders et al., 2020). The NEMOv3.6–CICEv5.1–WIM model code (WIM – stands for waves in ice model) had been shared with the Centre for Polar Observations and Modelling (CPOM) at the University of Reading for the joint research under the UK Joint Marine Modelling Programme (the UK Joint Weather and Climate Research Programme – JWCRP).

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Figure 1: Diagram of the quasi-restoring brittle fracture scheme introduced to the prognostic FSD model. The diagram shows three adjacent pairs of floe size categories, where blue highlights the larger category and red the smaller category. The brittle fracture scheme only transfers sea ice area fraction from a larger category to the adjacent smaller category and only where the number density gradient between adjacent categories in log-log space is larger (more positive) than –2. The sea ice area fraction distributed is $C a_i$ where $a_i$ is the total sea ice area fraction in the larger category and $C$ is the restoring constant.
Figure 2: An example of prognostic model output from the prog-16-nofl simulation. Presented in the figure is the perimeter density distribution, \( km^{-2} \) for the April MIZ (red, cross, dashed), June MIZ (purple, diamond, dotted), and August MIZ (blue, triangle, long-dash) averaged over 2000 – 2016. Also highlighted in the figure by a blue transparent box is an artificial ‘uptick’, a non-physical feature of the model also reported by Roach et al. (2018a).
Figure 3: Boxes indicate the areas over which the prognostic model emergent FSD is averaged to represent the three locations included in the observational study. Each case study area spans a set of 5 x 5 grid cells that includes the site stated for collection of observations.
Figure 4: A comparison of the observations and prognostic model output for the perimeter density distributions for the Chukchi Sea in May – June 2006 (a) and May 2014 (b), the East Siberian Sea in June 2001 (c) and June – July 2013 (d), and the Fram Strait in June 2001 (e) and June 2013 (f). Observations are identified with pink or purple dashed lines. Output for prog-16 (light blue, solid, stars) and prog-16-nobf (dark blue, solid, crossed) is averaged across the relevant region identified in Fig. 3 over the stated month(s). The average power-law fit across all locations is also shown (red, solid). The floe size data used within this figure was produced by Byongjun Hwang using the methodology of Hwang et al. (2017). The exponent of the power-law fit was calculated by Yanan Wang using the methodology of Virkar and Clauset (2014). prog-16 performs particularly well in the Fram Strait and East Siberian Sea but less well for the Chukchi Sea. It represents a significant improvement to prog-16-nobf in all three locations.
Figure 5: The total Arctic sea ice March extent (a, top left), March volume (b, top right), September extent (c, bottom left), and September volume (d, bottom right) within the model domain over the period 1990 – 2016 for ref (red, circles), WIPo-best (blue, triangles), prog-best (yellow, cross) and observations / reanalysis (black). Sea ice concentration data is obtained from satellites using the Bootstrap (filled diamond, dashed) algorithm version 3 (Comiso, 1999) and the NASA Team (filled circle, solid) algorithm version 1 (Cavalieri et al., 1996). Sea ice volume data (filled diamond, dashed) is taken from PIOMAS (Zhang and Rothrock, 2003).
Figure 6: The % difference in the Arctic total sea ice March extent (a, top left), March volume (b, top right), September extent (c, bottom left), and September volume (d, bottom right) within the model domain over the period 1990 – 2014 relative to the simulated or observed climatological mean over the same period for \textit{ref} (red, circles), \textit{WIPo-best} (blue, triangles), \textit{prog-best} (yellow, cross) and observations / reanalysis (black). Sea ice concentration data is obtained from satellites using the Bootstrap (filled diamond, dashed) algorithm version 3 (Comiso, 1999) and the NASA Team (filled circle, solid) algorithm version 1 (Cavalieri et al., 1996). Sea ice volume data (filled diamond, dashed) is taken from PIOMAS (Zhang and Rothrock, 2003).
Figure 7: The total Arctic sea ice March MIZ extent (a, top left), March pack extent (b, top right), September MIZ extent (c, bottom left), and September pack extent (d, bottom right) over the period 1990 – 2016 for ref (red, circles, long dash), WIPo-best (blue, triangles, dotted), prog-best (yellow, cross, dot-dash) and observations (black). Sea ice concentration data is obtained from satellites using the Bootstrap (filled diamond, dashed) algorithm version 3 (Comiso, 1999) and the NASA Team (filled circle, solid) algorithm version 1 (Cavalieri et al., 1996). Sea ice volume data (filled diamond, dashed) is taken from PIOMAS (Zhang and Rothrock, 2003). The MIZ is here defined as the region with between 15% and 80% sea ice concentration. All three simulations generally lie within the range spanned by the observational products except for pack ice extent in March after 2010.
Figure 8: Difference in sea ice extent (solid, red ribbon) and volume (dashed, blue ribbon) of prog-best (a, left) and WIPo-best (b, right) relative to ref averaged over 2000 - 2016. The ribbon shows, in each case, the region spanned by the mean value plus or minus two times the standard deviation. Both prog-best and WIPo-best produce similar reductions in the August sea ice extent of just under 2 %, but the prognostic model produces a much larger reduction in the sea ice volume throughout the melting season.
Figure 9: The % difference in the Arctic total sea ice March extent (a, top left), March volume (b, top right), September extent (c, bottom left), and September volume (d, bottom right) over the period 1990 – 2016 for WIPo-best (red, circles, dashed), and prog-best (blue, triangles, dotted) relative to ref. Trends in the extent appear to be similar for both models, but the prognostic model shows stronger trends for both the March and September sea ice volume.
Figure 10: The top two plots show the difference in the cumulative lateral (pink ribbon, dotted), basal (grey ribbon, dot-dashed), top (green ribbon, dashed), and total (red ribbon, solid) melt averaged over 2000–2016 for prog-best (a, left) and WIPo-best (b, right) relative to ref. The ribbon shows, in each case, the region spanned by the mean value plus or minus twice the standard deviation. The bottom plot shows the difference in the cumulative lateral (orange, dotted), basal (red, dot-dashed), top (light blue, dashed), and total (dark blue, solid) melt averaged over 2000–2016 for prog-best relative to WIPo-best (c). prog-best shows a larger increase in the lateral melt compared to WIPo-best, but the change in the total melt is small and changes sign over the year.
Figure 11: Difference in the sea ice area fraction (a–c) and ice thickness (d–f) between prog-best (A, top) or WIPO-best (B, bottom) and ref and $l_{eff}$ (g–i) for prog-best (A, top) or WIPO-best (B, bottom) averaged over 2000–2016. Results are presented for March (a, d, g), June (b, e, h), and September (c, f, i). Values are shown only in locations where the sea ice concentration exceeds 5%. The inner (dashed black) and outer (solid black) extent of the MIZ averaged over the same period is also shown. Both prog-best and WIPO-best show a strong reduction in the MIZ area fraction and thickness relative to ref, but the magnitude of the changes is larger for prog-best.
Figure 12: Section A (top) shows the standard deviation of the sea ice area fraction (a, b) and thickness (c, d) in March (a, c) and September (b, d) for ref. Section B (bottom left) and C (bottom right) show difference plots in the standard deviation of the sea ice area fraction (a, b) and thickness (c, d) in March (a, c) and September (b, d) for prog-best and WIPo-best relative to ref respectively. In B and C, the standard deviation in $l_{eff}$ is also plotted for both March (e) and September (f). Values are shown only in locations where the sea ice concentration exceeds 5%. The inner (dashed black) and outer (solid black) extent of the MIZ averaged over the same period is also shown. Plots show that changes to the standard deviation in the sea ice area fraction and thickness are generally localised to the outer edge of the MIZ.
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<td>$l_{eff} = 300 \text{ m}$</td>
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<td>CPOM CICE including the prognostic FSD model setup but using 16 floe size categories.</td>
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<td>16 floe size categories following Gaussian spacing. Brittle fracture scheme, described in section 2.2.2, excluded from model.</td>
</tr>
<tr>
<td>prog-best</td>
<td>CPOM CICE including the standard prognostic FSD model setup.</td>
<td>12 floe size categories following Gaussian spacing.</td>
</tr>
<tr>
<td>WIPo-best</td>
<td>CPOM CICE including the WIPoFSD model, with WIPoFSD model parameters optimised against observations.</td>
<td>$d_{\text{min}} = 5.375 \text{ m}, d_{\text{max}} = 30,000 \text{ m}, \alpha = -2.56$</td>
</tr>
</tbody>
</table>

**Table 1:** A summary of the CPOM CICE simulations described in section 3.1. All simulations are initiated sea ice free on the 1st January 1980 and evaluated until 31st December 2016.