Towards ice thickness inversion: an evaluation of global DEMs in the glacierized Tibetan Plateau

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Abstract. Accurate estimates of regional ice thickness, which are generally produced by ice-thickness inversion models, are crucial for assessments of available freshwater resources and sea level rise. Digital elevation model (DEM) derived from surface topography of glaciers is a primary data source for such models. However, the scarce in situ measurements of glacier surface elevation limit the evaluation of DEM uncertainty. Hence the influence of DEM uncertainty on ice-thickness modelling remains unclear over the glacierized area of the Tibetan Plateau (TP). Here, we examine the performance of six widely used and mainly global-scale DEMs: AW3D30 (30 m), SRTM-GL1 (30 m), NASADEM (30 m), TanDEM-X (90 m), SRTM v4.1 (90 m) and MERIT (90 m) over the glacierized TP by comparing with ICESat-2 laser altimetry data while considering the effects of glacier dynamics, terrain factors, and DEM misregistration. The results reveal NASADEM as the best performer in vertical accuracy, with a small mean error (ME) of 0.9 m and a root mean squared error (RMSE) of 12.6 m, followed by AW3D30 (2.6 m ME and 11.3 m RMSE). TanDEM-X also performs well (0.1 m ME and 15.1 m RMSE), but suffers from serious errors and outliers on steep slopes. SRTM-based DEMs (SRTM-GL1, SRTM v4.1, and MERIT) (13.5-17.0 m RMSE) had an inferior performance to NASADEM. Errors in the six DEMs increased from the south-facing to the north-facing aspect and become larger with increasing slope. Misregistration of the six DEMs relative to ICESat-2 footprint in most glacier areas is small (less than one grid spacing). Then, the influence of six DEMs on four ice-thickness models: GlabTop2, Open Global Glacier Model (OGGM), Huss-Farinotti (HF), Ice Thickness Inversion Based on Velocity (ITIBOV) is intercompared. The results show that GlabTop2 is sensitive to the accuracy of both elevation and slope, while OGGM and HF are less sensitive to DEM quality and resolution, and ITIBOV is the most sensitive to slope accuracy. Considering the necessity of DEMs with consistent acquisition dates, NASADEM is the best choice for ice-thickness estimates over the whole TP. Our assessment first figures out the performances of mainly global DEMs over the glacierized TP. This study not only avails the glacier thickness estimation with ice thickness inversion models but also offers references for other cryosphere studies using DEM.
1 Introduction

The Tibetan Plateau (TP), which includes the Pamir, Hindu Kush, Karakoram, Himalaya, and Tibet regions, covers an area of ~3 million km$^2$ and has a mean elevation of more than 4000 m a.s.l. (Fig. 1). It accounts for more than 82% of the Earth’s land surface area above 4000 m a.s.l. (Fielding et al., 1994), and is often referred to as the Third Pole of Earth or the Asian Water Tower (Yao et al., 2012) due to its high elevation and abundant water resources in the form of glaciers, snow, permafrost, lakes, and rivers. The TP has a glacierized area of ~8.3×10$^4$ km$^2$ (RGI Consortium, 2017) with an ice volume of ~6.2×10$^3$ km$^3$ (Farinotti et al., 2019), mainly distributed in the Karakoram and Himalaya regions.

Ice thickness is a crucial parameter for assessing the contribution of glaciers to global sea level rise (Kraaijenbrink et al., 2017), quantifying regional water availability (Huss and Hock, 2018; Immerzeel et al., 2020), and evaluating cryosphere-related hazards (Linsbauer et al., 2016; Zheng et al., 2021). In the TP, owing to the lack of in-situ ice thickness measurements (Welty et al., 2020), regional glacier thickness is mainly estimated by ice-thickness inversion models (ITIMs) using open-access digital elevation models (DEMs) (Farinotti et al., 2009; Farinotti et al., 2019; Frey et al., 2014). The DEM is a fundamental part of most regional ITIMs (Farinotti et al., 2017), and is often used to determine center flow lines (Maussion et al., 2019), shear stress (Frey et al., 2014; Wu et al., 2020), apparent mass balance (Farinotti et al., 2009), and for ice-thickness interpolation (Huss and Farinotti, 2012). In addition to its use in ITIMs, the DEM has been an essential input for a wide range of TP glaciology studies, such as glacier inventory (Bhambri et al., 2011; Frey et al., 2012; Ke et al., 2016; Mölg et al., 2018), glacier mass change (Brun et al., 2017; Shean et al., 2020; Zhou et al., 2018), glacier related disasters (Allen et al., 2019; Kääb et al., 2018; Zhang et al., 2019) and projections of glacier or glacial lake evolution (Kaser et al., 2010; Kraaijenbrink et al., 2017; Zheng et al., 2021). The uncertainty in the DEMs can lead to different ITIM outcomes (Frey and Paul, 2012; Fujita et al., 2017; Furian et al., 2021; Kääb, 2005), especially for those ITIMs in which the DEM is a crucial input. For example, the sensitivity of the glacier bed topography (GlabTop) model to slope increases for shallower slopes (Paul and Linsbauer, 2012), and an overestimate of slope by ~10% would result in an underestimation of ice thickness of ~32% (Linsbauer et al., 2012). Therefore, the DEM grid resolution could influence the thickness estimation from GlabTop, more detailed slope information could be provided by higher resolution DEM. Localized elevation errors and data gaps could affect the estimated ice thickness by 5–25% (Huss and Farinotti, 2012). In conclusion, DEM errors influence the determination of model physics and the final model outcomes. Therefore, it is imperative to choose a suitable DEM source for regional glacier thickness modelling (Koldtoft et al., 2021). Farinotti et al. (2017 and 2021) intercompare the performance of most ITIMs and suggest that consideration of the uncertainty in the input data could improve the model output. However, to our knowledge, the uncertainty in different open access DEMs and their influence on various ITIM outputs over the TP has not been evaluated.

Currently, open-access DEMs covering the whole TP are mainly created by stereo mapping sensors such as ALOS AW3D30 (Tadono et al., 2015), C- or X-band interferometry synthetic aperture radar (InSAR) such as TanDEM-X, and SRTM-C based products such as NASADEM (Crippen et al., 2016). Shadows and the layover effect of InSAR technology (González and Fernández, 2011), along with the deficient orientation of photogrammetrically stereo images (Mukherjee et al., 2013) or low
stereo-correlation (Hugonnet et al., 2021) propagated during DEM production, may introduce errors and voids. Filling these voids with other data could result in increased uncertainty (Liu et al., 2019). Additionally, the rugged terrain of glaciers and the low contrast of snow cover can often lead to geometric distortion and missing data (Reuter et al., 2007; Takaku et al., 2020). Estimates of the accuracy of DEMs in different terrains and landforms, and for different vegetation coverage and land use have been conducted outside the TP using Global Navigation Satellite Systems (GNSS) measurements or high-resolution DEMs (González-Moradas and Viveen, 2020; Grohmann, 2018; Hawker et al., 2019; Uuemaa et al., 2020). The performance of specific DEMs varied in these studies, indicating that the local terrain and land cover influenced the DEM accuracy. In the TP, glaciers are distributed across different climatic zones and have a wide range of elevations with rugged and complicated terrain (Fielding et al., 1994; Thompson et al., 2018). GNSS measurements are not accessible for most glaciers, and publicly available DEM with high resolution is also of limitation due to its long temporal coverage (Shean, 2017). The assessment of DEM accuracy in specific regions with limited GNSS measurements or high-resolution DEM is insufficient to determine the performance of global DEMs across the whole glacierized TP.

Liu et al. (2019) evaluated the performance of seven public freely-accessed DEMs over the TP with sparse ICESat altimetry data and suggested that AW3D30 has a high degree of accuracy. However, ICESat data with a footprint of 70 m (larger than the resolution of their estimated DEMs) could result in intra-pixel errors in steep slopes (Uuemaa et al., 2020). Besides, glacial regions were not considered in their studies, due to the variations of glaciers over time. Misregistration among DEMs, which may lead to evaluation bias (Han et al., 2021; Hugonnet et al., 2021; Van Niel et al., 2008), was also neglected. Bearing these issues in mind, and considering the limitations of optics sensors in rugged terrain and the glacier accumulation area (Chen et al., 2021), it is clear that a further assessment of the performance of AW3D30 over glacier area is required. Recently, TanDEM-X (released in 2017) and NASADEM (released in 2020) have been reported to have large improvements in accuracy relative to previous DEM products for various land-cover types (Wessel et al., 2018), floodplain sites (Hawker et al., 2019), slightly undulating terrain (Altunel, 2019), and mountain environments (Gdulová et al., 2020). Nonetheless, their performance over the rugged and glacierized TP remains unclear.

The purpose of this study is to evaluate the optimal DEM to use for regional ice thickness estimation over the TP. We first evaluated the performance of six widely used DEMs: AW3D30, SRTM-GL1, NASADEM, TanDEM-X, SRTM v4.1, and MERIT which are derived from different sensors and have different resolutions, against ICESat-2 data which has been proven to have high vertical accuracy and resolution (Brunt et al., 2019, 2021; Li et al., 2021), but with sparse tracks (Fig. 1). The elevation differences between these DEMs and the ICESat-2 are systematically analyzed concerning aspect, slope, elevation, and glacier zones. The influence on the accuracy assessment from the glacier elevation changes, terrain and misregistration among DEMs is then quantified. Finally, we compare the performance of ice thickness modelled by using the six DEMs against in situ measurements of ice thickness by ground penetrating radar (GPR).
Figure 1. Location of the TP and its ICESat-2 reference ground tracks (RGTs). a) ICESat-2 tracks over the TP covering with glaciers. b) Location of ground penetrating radar (GPR) profiles over the Chhota Shigri Glacier which is used as an example. c) Relative location of six beams when Advanced Topographic Laser Altimeter System (ATLAS) has backward orientation. The distance between RGTs is 28.8 km. d) Percentage of ICESat-2 data in different months from October 2018 to November 2020. The boundary of the TP is derived from SRTM above 2500 m.a.s.l. (Zhang et al., 2013).

2 Data and Methods

2.1 Descriptions of ICESat-2 elevation data referenced

ICESat-2, a follow-on mission to the Ice, Cloud, and land Elevation Satellite (ICESat), was launched on 15 September 2018, with the goal of acquiring Earth’s geolocated surface elevation that referenced to the WGS84 ellipsoid at the photon level. ICESat-2 ATLAS (Advanced Topographic Laser Altimeter System) emits a pulse every 0.7 m along the track covering a horizontal circular area with 0.5 m in vertical extent and ~17 m diameter. This design diameter value varied due to the photo-counting lidar technology and potentially the atmospheric conditions (Magruder et al., 2020). ICESat-2 ATL03 and ATL06 product both can be used as elevation reference. ATL03 product has a spacing of ~0.7m and can provide more terrain details
than ATL06 product. In this study, considering the resolution of global DEM and compute cost, we select the ICESat-2 Level-3A land-ice ATL06 product as an elevation reference. ATL06 heights are median-based heights derived from a linear-fit model over each segment corrected for first-photon bias and transmit-pulse shape. The segment has a length of 40 m centered on reference points at 20-m intervals along the track. The ATL06 product has better than 5 cm height accuracy and better than 20 cm surface measurement precision in the Antarctic (Brunt et al., 2019,2020; Li et al., 2021) and Qilian Shan (Zhang et al., 2020). The product also contains land background points. The RGI6.0 glacier inventory (RGI Consortium, 2017) was used to extract points falling on glaciers (Fig. 2).

ICESat-2 ATL06 data covering the TP from October 2018 to November 2020 was downloaded from https://earthdata.nasa.gov/ (Fig. 1). There are 2436 files containing about 100 GB of data in total. The fields: Location (latitude, longitude), surface elevation (h_li), elevation uncertainty (h_li_sigma) and quality (atl06_quality_summary) were used. By combining the quality field (atl06_quality_summary=0) (Smith et al., 2019) with the glacier inventory, a total of 3.5 million points out of 0.16 billion records over the TP were selected (Fig. 1). The slope, aspect and elevation value of the cell center of the DEMs were extracted for the ICESat-2 footprints.
**Figure 2.** Flow chart showing the targets and methods used in this study including accuracy evaluation of DEMs and their effects on ice-thickness inversion models. The $w_1$, $w_2$, $w_3$ and $w_4$ denote the weight of each modelled ice thickness, $i$ from 1 to 6 denotes six different DEMs, and the number 1–4 denotes the four ice thickness inversion models.

2.2 Descriptions of global-scale DEMs evaluated

Six global-scale DEMs were selected for evaluating their influences on ITIMs, based on popularity, data source, resolution and sensor type (optics or SAR) (Table 1).

1) **ALOS World 3D - 30 m (AW3D30)** is acquired by the optics stereo sensor loaded on the Advanced Land Observing Satellite (ALOS) which operated from 2006 to 2011 with a horizontal resolution of 30 m. Approximate 10% of global land area, mainly in tropical rainforest areas and the polar areas, has voids mostly due to cloud or snow/ice covers constatation in source imageries. Data gaps are filled with SRTM, ASTER GDEM v3, ArcticDEM v3, and TanDEM-X 90 (Takaku et al., 2020). After filling gaps, the accuracies in void-filled and void-free areas are nearly consistent (Takaku et al., 2020). Data was available at https://www.eorc.jaxa.jp/ALOS/en/aw3d30/index.htm after user registration.

2) **TanDEM-X 90 m DEM** (hereafter TanDEM-X) is a product derived from the first bistatic X band SAR mission of the world which took place from 2014 to 2016 (Bachmann et al., 2021). It is a pixel-reduced product of the global TanDEM-X DEM with a pixel spacing of 0.4 arcseconds (12 m). The official reported absolute vertical and horizontal accuracy is better than 10 m at the 90% confidence level. It is noted that the current release is a non-edited version: areas with outliers, noise and voids remain. The original data was collected during different seasons and years, and the influence of ablation and accumulation of glaciers should also be noted. Data was acquired from https://download.geoservice.dlr.de/TDM90/.

3) **NASADEM** is a new product released in 2020, which is derived by reprocessing the original SRTM signal data using updated interferometric unwrapping algorithms and auxiliary data, such as ICESat, to reduce voids and improve vertical accuracy (Crippen et al., 2016). Remnant voids are filled mainly by Global Digital Elevation Model (GDEM) v3 data. This data was downloaded from https://search.earthdata.nasa.gov/.

4) **SRTM-GL1 (30 m)** is an extensively used DEM in ITIMs. The first open-access ice-thickness database of global glaciers also adopted SRTM-GL1 as its DEM source (Farinotti et al., 2019). Voids were primarily filled by ASTER GDEM2.

5) **SRTM v4.1**, with a spatial resolution of 90 m, is produced by the method proposed by Reuter et al. (2007), including merging tiles, filling small holes iteratively and interpolating across the holes using a range of methods, according to the size of the hole, and the land type surrounding it (https://cgiarcsi.community/data/srtm-90m-digital-elevation-database-v4-1/). SRTM v4.1 was also used to compare against the performance of SRTM-GL1 to estimate the influence of resolution.

6) **MERIT** is also widely used with a spatial resolution of 90 m. It was developed by removing absolute bias, stripe noise, speckle noise, and tree height bias from the existing spaceborne DEMs (SRTM3 v2.1 and AW3D30 v1) using multiple satellite datasets and filtering techniques (Yamazaki et al., 2017). Its accuracy was significantly improved, especially in
flat regions (Yamazaki et al., 2017). The overall accuracy is similar to TanDEM-X in floodplain sites (Hawker et al. 2019), but lower in short vegetation. The dataset was downloaded from http://hydro.iis.u-tokyo.ac.jp/~yamadai/MERIT_DEM/. SRTM v4.1 and MERIT were selected to compare with TanDEM-X, and simultaneously estimate the influence of DEM resolution on ITIMs.

Elevation of ICESat-2 data, NASADEM_SHHPv001 and TanDEM-X is based on WGS84 ellipsoid reference, and elevation of the other four DEMs is based on EGM96 geoid (Table 1). The function of geoidheight provided by MATLAB was used to calculate geoid height to unify their references.
Table 1 Details of the selected DEMs.

<table>
<thead>
<tr>
<th>Item</th>
<th>Version</th>
<th>Acquisition time</th>
<th>Reference</th>
<th>Release time</th>
<th>Resolution (m)</th>
<th>Sensor type</th>
<th>Source</th>
</tr>
</thead>
</table>
2.3 Ice thickness inversion method

Tiles of six DEMs (AW3D30, TanDEM-X, NASADEM, SRTM-GL1, SRTM v4.1, and MERIT) were used to form a mosaic of terrain data covering the whole TP. Four ice-thickness inversion models (GlabTop2, HF, OGGM, ITBOV) were used to estimate the glacier thickness. The Chhota Shigri Glacier located in western Himalaya with available GPR data (Fig.1) was selected as an example to evaluate the influence of DEM uncertainty on the ITIMs. Full details of the ITIMs are given below:

GlabTop (Glacier bed topography) is based on the theory that glacier thickness is mainly determined by the slope of the terrain (Linsbauer et al., 2009, 2012; Paul and Linsbauer, 2012). It is assumed that the glacier is an ideal plastic fluid, with bottom slip being ignored. Based on the empirical relationship between mean shear stress along the centrelines and the range of glacier elevation (Haeberli and Hoelzle, 1995) (Eq. 1), the actual basal shear stress $\tau$ can be determined.

$$\tau = 0.005 + 1.598 \Delta H - 0.435 \Delta H^2$$

where $\Delta H$ is the elevation range of the glacier. The ice thickness $h$ can then be determined from Eq. (2)

$$h = \frac{\tau}{f \rho g \sin \alpha}$$

where $f$ is the shape factor, $\rho$ is glacier density (850±60 kg/m$^3$) (Huss, 2013), $g$ is the acceleration due to gravity (9.8 m/s$^2$) and $\alpha$ is the slope. Glabtop2 is an automated method for calculating ice thickness, similar to GlabTop, but avoids digitizing the branch lines. For details refer to Frey et al. (2014).

HF (Huss- Farinotti) model is based on the mass balance principle which relates the surface mass balance of the glacier ($b$) to the ice flux and variation in the glacier thickness. Given the ice flux, ice thickness can be calculated according to Glen's ice flow law (Farinotti et al., 2009a; Huss and Farinotti, 2012).

$$h = \sqrt[2n+2]{q(1-fs/l) \frac{n+2}{2A \left( f \rho g \sin \alpha \right)^{n}}}$$

where $h$ is the mean elevation of band thickness, $q$ is the ice flux, $fs/l=0.8$ is the basal slip correction factor, $n=3$ is the exponent of flow law, $\rho$ is glacier density (850±60 kg/m$^3$), $g$ is the acceleration due to gravity (9.8 m/s$^2$), $f=0.8$ is the valley shape factor (Cuffey and Paterson, 2010) and $A$ is the Glen flow rate factor (3.24×10$^{24}$ Pa$^{-3}$ s$^{-1}$) (Cuffey and Paterson, 2010; Gantayat et al., 2014).

This method defines a new variable $\tilde{b} = \tilde{b} - \rho g \frac{\partial h}{\partial t}$, where $\tilde{b}$ is the apparent mass balance, $\tilde{b}$ is the glacier surface mass balance, and $\frac{\partial h}{\partial t}$ is the glacier surface elevation change. $\tilde{b}$ is linearly related to the elevation. In the absence of mass balance data and thickness change data on the surface of a glacier, the ice flux $q$ can be obtained by estimating $\tilde{b}$, which is determined from Huss and Farinotti et al. (2012). Ice thickness in each elevation band can then be determined by substituting into Equation (3).
Finally, $h$ is extrapolated, in combination with the slope, to obtain the distributed ice thickness, according to the parameters in Huss and Farinotti (2012).

The Open Global Glacier Model (OGGM) is based on the same concept as HF, but has two main differences (Maussion et al., 2019). Firstly, the method described in Kienholz et al. (2014) is used to automatically obtain the middle streamlines and watershed division. Secondly, the apparent mass balance data are reconstructed from the local climatic dataset from variables such as precipitation and temperature.

The ice thickness inversion based on velocity (ITIBOV) model is inverted from the shallow ice approximation, it obtains the ice thickness by combining the surface velocity field with the Glen ice flow law (Gantayat et al., 2014; Glen, 1955):

$$h = \frac{n + 1}{2A} \frac{(1 - k)u_s}{(f \rho g \sin \alpha)^n}$$

(4)

where $h$ is ice thickness, $u_s$ is glacier surface velocity, and $k$ is the contribution ratio of basal slip velocity relative to the $u_s$.

We used the mean velocity over 1985-2019 from ITSLIVE dataset (Gardner, 2019 ) as the $u_s$ input. We assumed that basal slip only occurred during the warm seasons, and $k$ was calculated by dividing the annual glacier velocity by winter glacier velocity (Wu et al., 2020). Data from the Global Land Ice Velocity Extraction from Landsat 8 (GoLIVE) dataset with a date separation length of fewer than 96 days are used to estimate the monthly velocity (Fabnestock et al., 2016; Scambos, 2016), allowing the winter velocity (December, January and February) and annual mean velocity to be calculated. Basal factor $k$ was calculated as 0.80 (Fig. S1). The shared parameters, such as creep factor, shape factor and basal creep factor are same in all four models.

An ensemble of the output from different models can improve the modelled thickness (Farinotti et al., 2017; Farinotti et al., 2021). Therefore, after calculating the ice thickness from four models using different DEMs, we calculated an ensemble ice thickness using the same DEM but with different models. First, the ensemble ice thickness was the sum of the four models with weights $w_1$, $w_2$, $w_3$, and $w_4$, respectively. The sum of four weights equals 1. 70% of the GPR data are adopted as calibration data. 30% of the GPR results are adopted as validation data. Then, the four weights are iteratively changed to achieve the minimal mean absolute error between calibration data and model result. Finally, the MAE between ensemble ice thickness and validation data are calculated.

2.4 Accuracy assessment method

The error in the DEMs is considered to be the difference between the DEM elevation and the ICESat-2 measurement. To remove the influence of outliers, elevation differences outside four standard deviations were removed. Mean error (ME), mean absolute error (MAE), median error, root mean square error (RMSE), standard deviation (STD), and normalized median absolute deviation (NMAD) were calculated for the error assessments. NMAD and ME were used to assess the disturbance from extreme errors (Höhle and Höhle, 2009; Gdulová et al., 2020). When calculating the ME, the positive and negative biases
cancel each other, making the error smaller; therefore, the STD together with ME could be a complementary indicator for assessment.

\[
ME = \frac{1}{n} \sum_{1}^{n} (H_{DEM} - H_{ICESat-2})
\]  
\[
MAE = \frac{1}{n} \sum_{1}^{n} \text{abs}(H_{ICESat-2} - H_{DEM})
\]  
\[
RMSE = \sqrt{\frac{1}{n} \sum_{1}^{n} (H_{ICESat-2} - H_{DEM})^2}
\]  
\[
STD = \sqrt{\frac{1}{n-1} \sum_{1}^{n} (H_{ICESat-2} - H_{DEM} - ME)^2}
\]  
\[
NMAD = 1.4826 \times \text{median}(abs(H_{ICESat-2} - H_{DEM}))
\]

Glacier surface elevation changed at -21-17m/yr over the TP during 2000-2018 (Shean et al., 2020). Therefore, the disparity of acquiring date between ICESat-2 and six DEM (Table 1) could introduce large error due to the glacier dynamic. TanDEM-X and AW3D30 are acquired in different months and years (Table 1), it’s hard to analyse the impact of glacier dynamic on accuracy assessment. However, the other four DEMs are produced from NASA’s Shuttle Radar Topography Mission during the 11-day mission in February 2000. We selected ICESat-2 data acquired in February 2019 and 2020. Then the glacier elevation dynamic magnitude during February 2000 and February 2019/2020 are subtracted from the selected ICESat-2 elevation. The mean glacier elevation change data is adopted from Shean et al. (2020). By comparing the elevation from the four DEMs and adjusted ICESat-2, we could exactly know the impacts of glacier dynamic on accuracy assessment.

3. Results

3.1 Accuracy of DEMs

The four standard deviations (that is 4 std) was chosen to not only filter the differences between ICESat-2 and DEMs to exclude extreme outliers, but also keep most records in the further accuracy analysis. The ration of excluded outliers relative to the record of each DEM is less than 1%. Overall, there is no irregular deviation existed among these DEMs and ICESat-2 elevation after filtering (Fig. 3). The ICESat-2 vs DEMs values are distributed tightly around the fit line with a slope coefficient of 1, with no obvious differences among the R². NASADEM and TanDEM-X performed the best in terms of intercept and fit RMSE, with very little difference to the ICESat-2 data.
Figure 3. Differences between six DEMs and ICESat-2 elevation. a) AW3D30, b) SRTM-GL1, c) NASADEM, d) TanDEM-X, e) SRTM v4.1, and f) MERIT. The gradually lighter red lines denote the range within 6, 4 and 2 std of the mean. The text at the top left of each panel gives the fit results for data within 4 std of the mean. ‘Outlier’ denotes the proportion of outliers relative to the total records. ‘$R^2$’, ‘RMSE’, and ‘Intercept’ are fit results when the slope coefficient is set to 1. The elevation range was cut to 3500–6500 m, the range in which most elevations values are located, to show clearly the effect of using different multiples of the std from the mean.

Statistically, Median and ME differed little, which indicated that extreme values did not influence the ME much after the 4 std filter was applied (Fig. 4). STD was slightly larger than NMAD, especially for TanDEM-X, indicating larger discrepancies due to the DEM errors and noise (Höhle and Höhle, 2009). NASADEM performed better than the other two 30-m resolution DEMs in ME. AW3D30 behaved best in RMSE (11.3 m), MAE (8.2 m). SRTM-GL1 and NASADEM are both produced from the same original SAR data, but differ in RMSE (13.5 vs 12.6 m), MAE (10.0 vs 9.4 m), and ME (2.0 vs 0.9 m). The new algorithm and auxiliary data applied in NASADEM do indeed improve the absolute accuracy of the product over glacierized terrain. The quality of TanDEM-X was the best out of the 90-m resolution DEMs with the smallest RMSE (15.1 m), MAE (8.9 m), ME (0.1 m), and STD (15.1 m). SRTM v4.1 and MERIT are both error-reduced products from SRTM3 v2 (Reuter et al., 2007; Yamazaki et al., 2017), and they have similar ME (–1.5 m vs 2.6 m) and RMSE (17.0 m vs 15.6 m).
Figure 4. Overall difference (m) statistics between six DMEs and ICESat-2 elevation. a) 30-m-resolution DEMs, AW3D30, SRTM-GL1 and NASADEM. b) 90-m-resolution DEMs, TanDEM-X, SRTM v4.1 and MERIT. The vertical dash line denotes the mean elevation difference of each DEM between ICESat-2.

Spatially, the ME in southeast Tibet is more positive than that in the Himalayas, and it is slightly negative in western Kunlun and the Karakoram mountains (Fig. 5a). It is worth noting that in the Himalayas and southeast Tibet, the ME of the other four DEMs is more positive than that of TanDEM-X and AW3D30. ME of TanDEM-X are mainly at ±5 m, but with some large values in several regions. SRTMGL-1, NASADEM, SRTM v4.1 and MERIT have the nearly same distribution of ME, and show negative ME values in the West Kunlun and Karakoram. ME of NASADEM is smaller than that of SRTM-GL1 in most regions of TP, but is bigger in West Kunlun and Karakoram. Overall, the STD of 30-m resolution DEMs is much better than
that of 90-m resolution DEMs (Fig. 5b). STD along the Hindu Kush-Himalaya and southeast Tibet was larger than that in other regions. Thereinto, STD in southeast Tibet was relatively larger (>12 m). Specifically, the STD of AW3D30 and NASADEM was minimum and share similar spatial distribution features. Relative to ME, the STD of NASADEM was improved over the most part of TP, compared with that of SRTM-GL1. This indicate that some disturbances from noise and errors may exist in the SRTM-GL1, SRTM v4.1 and MERIT in the West Kunlun and Karakoram. TanDEM-X performs well in overall statistics (Fig. 4b) and ME (Fig. 5a), but didn’t show large advantage and was even worse in STD in some areas. The STD and ME of SRTM v4.1 and MERIT are almost same in space (Fig. 5b), corresponding to their similar overall STD (both ~15 m) and ME (both ~2 m) values (Fig. 4b).

**Figure 5.** Aggregated spatial mean error (ME) (a) and standard deviation (STD) (b) between six DEMs and ICESat-2 elevation for 1°×1° cells across the TP. The cross symbol denotes that NASADEM performs better than SRTM-GL1 in ME or STD.
3.2 Differences between DEMs and ICESat-2 in aspect, slope and elevation

The influence of aspect is most apparent for SRTM-GL1, with a median value of about –5 m in the south aspect which increased in magnitude gradually towards the north aspect (~ 5 m). A similar pattern, but with a smaller amplitude for the NASADEM, TanDEM-X, MERIT (±1 m) and AW3D30 (0 – 2 m) (Fig.6a).

The median differences of the 30-m DEMs generally increased along the slope. However, for the 90-m DEMs, the difference increased with slope at first, but then decreased on steep slopes. NASADEM and TanDEM-X had minimum mean median values of about 0.9 and 1.2 m, respectively (Fig. 6b). For all DEMs, the spreads of differences become larger as the slope becomes steeper. This increase is most obvious for TanDEM-X and SRTM v4.1, with rates of 1.29 m/degree ($r=0.97$, $p<0.01$) and 1.11 m/degree ($r=0.89$, $p<0.01$). This indicated that errors of both DEMs suffered from serious slope effects. AW3D30 and NASADEM have a similar mean spread (19.2m vs 20.8m). On slopes of less than 20°, TanDEM-X has the best quality with a mean median value of -0.2 m and mean spread of 11.7 m, respectively. MERIT shows a slight advantage over SRTM v4.1 with a reduced spread for steep slopes. Overall, relative to the other DEMs, AW3D30 and NASADEM behave best against the slope in terms of spread and median value.

The differences for all DEMs generally decreased with elevation, with fluctuations around zero at very high elevations (Fig.6c). AW3D30 has a smaller difference at low elevation relative to NASADEM and SRTM-GL1. For NASADEM and SRTM-GL1, the differences along the elevations show the similar distribution and varied from –10 to 10 m over the range 4500–6500 m, where measurements are concentrated (Fig. 6d); However, NASADEM behave best out of six DEMs in the high elevation. The difference of TanDEM-X varied from around –5 to 5 m between 4500 and 6500 m. The SRTM v4.1 and MERIT differences changed almost similarly from –20 to 40 m, but show differences at the high elevation region.
Figure 6. Differences between six DEMs and ICESat-2 with terrain factors. (a) 5° aspect bin. (b) 2° slope bin. (c) 200 m elevation bin. (d) Percentage (%) of data in each aspect, slope and elevation bin.
3.3 Differences between DEMs and ICESat-2 in different glacier zones

Differences in different glacier zones were also estimated and are shown in Figure 7a-d. We divided it into four sub-zones using the maximal, median and minimum elevation from the RGI glacier inventory (Fig. 7e). Here we consider Zone 1 and Zone 4 to be the ablation area and accumulation area, respectively. Zone 2 and Zone 3 are transition areas. Crests of the probability distribution of differences located in the positive axis range in Fig. 7a move to the left in Fig. 7b–d. Correspondingly, ME, MAE and RMSE all decrease from Zone 1 (ablation area) to Zone 2 (transition area) (Fig. 7 and Table S1). Spatially, areas in the glacier terminus are subject to more melting (Brun et al., 2017) leading to this decrease. The ME of the SRTM based products SRTM-GL1, SRTM v4.1, NASADEM and MERIT are all around 10 m in Zone 1 and decreased similarly by 8.1, 7.6, 7.5 and 7.2 m towards Zone 2, respectively (Table S1). Temporally, the ME of the DEM acquired in earlier periods is bigger. The ME is 8.1 m for AW3D30, which was acquired in 2006–2011, bigger than that of TanDEM-X (3.9 m), which was acquired in 2010–2015.

ME, MAE and RMSE in Zone 3 and Zone 4, near or in the accumulation area, are almost all smaller than the corresponding values in Zone 1 (Fig. 7 and Table S1). ME of all DEMs decreased to negative values in Zone 3 and Zone 4. Usually, in the accumulation area, glaciers have a positive or less negative elevation change (Li and Lin, 2017; Maurer et al., 2019; Rankl and Braun, 2016), therefore, accumulation may be concerned with changes in Zone 3 and Zone 4. The observed shift in the ME from zone 1 to zone 4 is a sign of influence from thinning or accumulation between the time of collection of the six DEMs and the ICESat-2 data.

In terms of STD, NASADEM performed best in Zone 3 and Zone 4, with values ranging from 8.8 to 11.1 m (Table S1). AW3D30 had the best performance of all DEMs in Zone 1 and Zone 2, with an STD varying from 10.0 to 12.3 m. The STD of TanDEM-X was better than that of SRTM v4.1 and MERIT in Zone 1 and Zone 2, but was worse in Zone 3 and Zone 4.
Figure 7. Probability distribution of the difference between six DEMs elevation and ICESat-2 elevation in different glacier zones (a–d) that defined in panel (e).
3.4 Comparisons of ice thickness modelled by DEMs

The models are not adjusted independently according to the difference between the output and GPR results. Therefore, the results are not indicators of the performance of the models but rather references for examining the influence of different DEMs on specific ITIMs. The effects of the DEMs on the model outcomes are presented in Figure 8 and are quite obvious. Mean ice thickness differs, according to the DEM used, by up to 134%, 6%, 47% and 19% for GlabTop2, HF, ITIBOV and OGGM, respectively. The deepest ice thickness differs by up to 53%, 25%, 13% and 13% for GlabTop2, HF, ITIBOV and OGGM, respectively.

The mean ice thicknesses from GlabTop2 and ITIBOV using the 90-m DEMs (they are TanDEM-X, SRTM v4.1 and MERIT) are ~30 m less than those obtained from using 30-m DEMs (that is AW3D, SRTM-GL1 and NASADEM) (Fig. 8). GlabTop2, HF and OGGM using AW3D30, and ITIBOV using NASADEM output the maximal mean thickness. GlabTop2 and ITIBOV using TanDEM-X, OGGM and HF using SRTM-GL1 output the minimum mean thickness.

The influence of different DEMs on ITIMs can also be identified when making a comparison with the GPR results (Fig. 8 and Table 2). If the median error is used as the criterion, GlabTop2 and ITIBOV using NASADEM, HF using AW3D30, and OGGM using SRTM v4.1 achieved the relatively best simulation (Fig. 9). If RMSE was used, GlabTop2 using NASADEM, HF using SRTM-GL1, ITIBOV using AW3D30 and OGGM using TanDEM-X performed best (Table 2).

In different glacier zones, each DEM-model combination has its merits and weakness (Table 2). Totals of 8, 7, 3 and 2 output achieved the minimum RMSE in profiles (bold number in Table 2) by different ITIMs using AW3D30, NASADEM, TanDEM-X and SRTM-GL1, respectively. Overall, NASADEM and AW3D30 performed better in different glacier zones in all models.
**Figure 8.** Distribution of modelled ice thickness of Chhota Shigri Glacier (location shown in Fig.1) using AW3D30, SRTM-GL1, TanDEM-X, SRTM v4.1, NASADEM and MERIT. (a) Glabtop2; (b) HF; (c) ITBOV; (d) OGGM; (e) composite result. Mean (ME) and maximum (MAX) modelled ice thickness are given in each panel.

As similar to the procedure of Farinotti et al. (2017), results from the four models are further composed to achieve the minimum MAE between the modelled and GPR thicknesses (Fig. 8e). The weights for each model in ten experiments are shown in Table S2. After composition, the mean thickness using different DEMs ranged from 90 (acquired based on TanDEM-X) to 98 m (acquired based on AW3D30). NASADEM and AW3D30 achieved minimum MAE, which are 36.7m and 44.1m, respectively. The mean errors and median errors of all DEMs are at the range of ±10m, except for that of AW3D30 and TanDEM-X which is at a level of around 20m. The spreads of error of 30-m DEMs are 33% smaller than those of 90-m DEM. Error spread from NASAM was minimum (75.1m), followed by AW3D30 (77.3 m).

**Figure 9.** Point-by-point deviation comparison between the modelled and measured ice thickness from GlabTop2, HF, ITIBOV, OGGM and the composite result. In each group, the boxes are plotted in the order: AW3D30, SRTM-GL1, NASADEM, TanDEM-X, SRTM v4.1 and MERIT. Different models using the same DEM are aggregated by weights (labelled at the bottom) to achieve minimum mean absolute error.
Table 2 RMSE (m) of modelled ice thickness compared with ground penetrating radar (GPR) measurements on each profile. The location of profiles are shown in Figure 1. Bold numbers denote the best model performance on each profile using different DEMs.

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4. Discussion

4.1 Influence of glacier elevation change on the assessment of DEMs

The identified extreme outliers (Fig. 3) are mostly located in the glacier terminus, high elevation and high slope regions (Fig. 10a–b). Extreme glacier melt, such as in south-eastern Tibet, and surges, as observed in the Karakoram, can also lead to
dramatic elevation changes, resulting in large differences (Fig. 10c). This glacier elevation change effect is also reflected in the spatial distribution of difference (Fig. 5), elevation bins (Fig. 6c) and glacier zones (Fig. 7). The differences at lower elevations are positive, and generally decrease with elevation, consistent with the fact that glaciers melt at lower elevations and accumulate at higher elevations (Cuffey and Paterson, 2010). The differences in all DEMs with elevation and glacier zones comply with these features (Fig. 6c and Fig. 7). NASADEM was acquired in 2000 and TanDEM-X was acquired in 2010–2015, and the value of NASADEM is more positive than TanDEM-X in the ablation zone. The relatively more positive and larger values of ME and STD along the Hindu Kush-Himalaya, southern Tibet (Fig. 5) and negative ME values in the West Kunlun and Karakoram (Fig. 5) are also related to glacier elevation change (Hugonnet et al., 2021).
Figure 10. Distribution of excluded extreme outliers. The proportion of outliers accounting for the total number in slope bins (a) and each glacier Zone (b). Examples of locations of excluded points overlaid with glacier surface elevation change in the Karakoram (c) and southern TP (d). Locations of these two examples are labelled A and B in the central insert. Glacier elevation change data covering 2000–2019 is from Shean et al. (2020).

Table 3 Comparisons of differences between four SRTM based DEMs and ICESat-2 elevation over glacier zones before and after adjustment. ICESat-2 data acquired in February are used to calculate the differences. Glacier zones are defined according to Fig. 8e.

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<th>After (m)</th>
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</table>

After removing the glacier elevation change using the glacier elevation change dataset covering 2000–2018 (Shean et al., 2020), the mean difference in Zone 1 and Zone 2 decreased sharply by ~14 m and ~7 m for the SRTM based DEMs, respectively (Table 3). However, similar improvements are not obvious in Zone 3 and Zone 4. This may be related to the slight elevation change in the accumulation region (Brun et al., 2017; Shean et al., 2020), and high uncertainty due to steeper slopes and higher elevations (Fig. 6b–c). MAE, STD and RMSE all improved a lot in four regions after this adjustment.

ICESat-2 data covering the period from October 2018 to October 2020 repeat every 91 days. Therefore, variations of ICESat-2 elevation data caused by glacier fluctuations have influenced the error statistics (Fig. 11a). Precipitation on the TP mainly occurs in June–August (Maussion et al., 2014). Hence, after precipitation accumulation on glaciers in spring and summer, the elevation increased, and the mean difference decreased. With little accumulation, the glacier melt and sublimate in autumn and winter (Li et al., 2018), the glacier surface elevation decreases; then the mean difference increases. However, the magnitude
of these changes is much smaller, at a level of fewer than 3 m (Fig. 11a), compared with the large ME, MAE and RMSE magnitude of most of the DEMs (with the exceptions of TanDEM-X and NASADEM) (Fig. 4). When taking all points from different seasons into consideration, the ICESat-2 dataset gives average elevation over the 2018-2020 period, the seasonal effects could also partly cancel each other out. If only the ICESat-2 data from February was used (Table 3), NASADEM and TanDEM-X still perform better than others. Therefore, we conclude that the seasonal fluctuations of ICESat-2 data have little influence on the assessments of the DEMs.
Figure 11. Influence on elevation differences between ICESat-2 and six DEMs from glacier elevation change and terrain factors. (a) Mean absolute difference between six DEMs and ICESat-2 in different seasons during 2018–2020. The spring, summer, autumn, and winter are defined as March–May, June–August, September–November and December–February,
respectively. The histogram at the bottom shows the percentage of the total number of points in each season. (b) Examples of elevation and shaded relief of six DEMs in the Shisha Pangma region. The rectangle denotes the area of interest.

4.2 Influence of terrain on the assessment of DEMs

The elevation differences have a strong dependence on terrain factors (Fig. 6a–b). The differences with aspect show contrasting features to the distribution of measurements in different aspects (Fig. 6d). The largest errors are concentrated in the north aspect, as was also reported in previous studies (Gorokhovich and Voustianiouk, 2006; Shortridge and Messina, 2011), in which they were attributed to the orientation of the sensor (Gdulová et al., 2020; Shortridge and Messina, 2011). However, here, the data from different sensors all show this aspect dependence, and we infer that it may be related to the accordant distribution of data in different slopes with aspect. There are many more measurements with steeper slopes in the north aspect, and fewer measurements with flatter slopes in the south aspect (Fig. 12). The error and spread become larger with steeper slopes (Fig. 7b), as also reported by Liu et al. (2019) and Uuemaa et al. (2020), which may be due to geometric deformation or shadow (Liu et al. 2019). Therefore, the error variation with aspect tends to be related to steeper slopes (Gdulová et al., 2020; Gorokhovich and Voustianiouk, 2006).

![Distribution of measurements in different aspects against the slope.](image)

Though points in the 55°–90° slope region account for a small fraction (Fig. 6d), almost half the points in the 55°–90° slope region are identified as extreme outliers (Fig. 10a). Differences also show large discrepancies for all DEMs in the steeply sloping regions where voids and large errors are frequent (Falorni, 2005). Steep slopes combined with low resolution led to
430 variations in the spread of differences in Fig. 6b. Spreads of differences were larger on steep slopes for the 90-m DEMs than those of the 30-m DEMs. Intra-pixel variation aggravates this effect in steeply sloping regions (Uuemaa et al., 2020), lower resolution or reduced pixel DEMs smooth the terrain details and lead to inaccurate elevation compared with the 20-m footprint of ICESat-2 points. The spread and the number of outliers gradually increased with the slope, especially for the TanDEM-X case (Fig. 7b). Using the terrain in the rugged Shishapangma region (Fig. 12b) as an example, we can see that the elevation from TanDEM-X suffers from serious errors along the ridge at high elevations with the output almost blurred. Even so, TanDEM-X still has overall accuracy advantages over SRTM v4.1 and MERIT, indicating the high quality of TanDEM-X in low relief regions (Fig. 7b).

4.3 Influence of misregistration on the assessment of DEMs

Six DEMs are produced from different sensors or by different methods. The pixel of different DEMs at the same location may mismatch each other. This misregistration among DEMs, which has been ignored in previous research (González-Moradas and Viveen, 2020; Liu et al., 2019), is an important error source when looking at DEM differences (Hugonnet et al., 2021; Van Niel et al., 2008). This study intends to give direct insights into the quality of uncorrected DEM products, so the misregistration problem was not tackled before the evaluations were carried out. However, the influence of misregistration was evaluated. According to the sinusoidal relationship between aspect and error differences between two DEMs (Van Niel et al., 2008), using the co-registration method in Nuth and Kääb (2011) and ICESat-2 points outside the glaciers, offset pixels relative to ICESat-2 in x- and y- direction at the 1°×1° grid scale were estimated by fitting method in MATLAB across the TP. Misregistration was found to be less than one grid spacing (Figure 13). The offset pixel of SRTM-GL1 relative to ICESat-2 is the largest; offset pixels of the other DEMs are all at less than 0.2 pixels. Considering that only the cell centre value was used, the sub-pixel shift may have little influence (Van Niel et al., 2008).
Figure 13. Distribution of offset pixels of DEMs relative to ICESat-2 on a 1°×1° grid. Only the grid squares with $R^2$ greater than 0.5 and the number of record greater than 1000 are considered.

4.4 Influence of DEMs on ice thickness estimated by ITIMs

Even with the same parameters, the same model using different DEMs have different outcomes (Figure 8 and 9). The uncertainty of DEM indeed influences the performance of the ITIMs. However, the different models have various levels of robustness to the quality of the input DEMs. Different DEMs resulted in differences in maximal and minimum mean ITIM ice thickness at a range of 3.6-32 m (Fig. 8).

Generally, the outcome with GlabTop2 and ITBOV using 30-m DEMs is 51% and 43% better than with the 90-m DEMs in mean error, respectively. With GlabTop2, elevation data was used to determine not only the slope, but also the shear stress (Frey et al., 2014). An error of +5° in slope caused more than a −34.1 % difference in the output for slopes of less than 20°. Additionally, relative elevation errors had an enormous impact (Fig. 14 b). For glaciers with an elevation range of less than 400 m, which accounted for 41% of the total number and 5% of the total area over the TP, +10, +30, and +50 m errors in elevation range caused more than +2%, +6% and +10% differences in output. Such errors in elevation range had greater influence (Fig. 14b), especially for small glaciers, which have smaller elevation ranges. These two errors propagate and lead to a much larger overall error (Table 3). Thus, GlabTop2 using NASADEM and AW3D30 with best quantity as input achieved the best RMSE in comparison with GPR measurements. In contrast to the other ITIMs, the ITIBOV model directly estimated the ice thickness at each grid cell according to cell velocity information without interpolation. The slope sensitivity of ITIBOV is higher than that of GlabTop2, with an error of +5° in slope causing more than a −71.4% difference in the output for slopes
of less than 20° (Fig. 14a). The flatter the slope, the more sensitive the ITIBOV is to the slope error (Fig. 14a). Although along- and across-track slope data are provided in the ICESat-2 ATL06 product, they are incompatible with the slope estimated from DEMs due to their different data formats and algorithms used (Burrough and McDonell, 1998; Smith et al., 2019). Moreover, the surface terrain of glaciers changes with time due to accumulation, melting and motion (Dehecq et al., 2018; Shean et al., 2020). Nevertheless, the accuracy of the DEMs estimated here could also provide some information about slope accuracy. When the better accuracy of NASADEM and AW3D30 as input of ITIBOV led to the relatively best outcomes (Table 2).

For HF and OGGM, the modelled results did not show large differences when 30-m DEMs compared with 90-m resolution DEMs (Fig. 9): means that high spatial resolution improved the outcome little (Pelto et al., 2020). For the HF model, elevation data was used for convergence calculation of apparent mass balance and mean slope in elevation bins (Farinotti et al. 2009; Farinotti et al. 2019), whereas, for OGGM, it is used to extract flowlines, shear stress at flowlines and mass balance at an elevation (Maussion et al. 2019). These two models show good roughness to the input DEM (Fig. 14a). Although NASADEM and TanDEM-X had the large advantage of accuracy, the output of HF and OGGM using these two DEMs did not have much advantage over that using the other DEMs (Fig. 9). The STD of RMSE values for HF and OGGM using six DEMs are 6.2 and 4.9 m, respectively (Table 2). STD of mean ice thickness by HF and OGGM using six DEMs are 1.1 and 6.0 m (Fig. 8).

When the results from different models are ensembled, the influence of uncertainty and resolution in the input DEMs manifests (Fig. 9 and Table 2). The RMSE of ITIMs from 30-m DEMs was 16.8% less than that from 90-m DEMs. Models using AW3D30 and NASADEM, equipped with higher resolution and better accuracy, achieved the best outcomes. However, glacier surface elevation changes with climate, AW3D30 acquired in different years and seasons represents glacier terrain in different periods. This could result in the discord of the output of ITIMs in large-scale ice-thickness inversion. Above, we suggest NASADEM as the best input of ITIMs for ice-thickness estimates over the TP. This conclusion is of significance for ice thickness inversion models using DEMs in TP. However, it should be noted that the result may be not suitable for studies in other glacierized mountainous regions. Because various errors exist in DEMs, such as speckle noise, stripe noise and absolute bias; they behave differently across the Earth (Yamazaki et al., 2017; Takaku et al., 2020). But our method to assess the accuracy of DEMs is repeatable in different regions, combined with the recently released glacier elevation change data on Earth (Hugonnet et al., 2021). What’s more, benefiting from the high accuracy and dense coverage of ICESat-2 data, the quality of DEMs can also be improved as similar as the production of MERIT (Yamazaki et al., 2017). For example, the misregistration in DEMs could be corrected and terrain-related errors could be reduced by unitizing the relation of difference against slope, aspect and elevation in Fig. 6.
Figure 14. Sensitivity test of slope and elevation on ice-thickness inversion models. (a) Percentage difference of modelled ice thickness from GlabTop2, HF, ITIBOV and OGGM when there is $+5^\circ$ slope error; (b) Percentage difference of modelled ice thickness from GlabTop2 when the elevation range error is +10, +30 and +50 m for different elevation ranges.

5. Conclusions

In the present study, six DEMs (i.e. AW3D30, SRTM-GL1, NASADEM, TanDEM-X, SRTM-GL1 and MERIT) from different sensors with different spatial resolutions were evaluated using ICESat-2 data. The influence of glacier dynamics, terrain and misregistration on the DEM accuracy was analysed. Out of the three 30-m DEMs, NASADEM was the best performer in vertical accuracy with an ME of 0.9 m and an RMSE of 12.6 m. Out of the three 90-m DEMs, TanDEM-X performed best with an ME of 0.1 and an RMSE of 15.1 m. The quality of TanDEM-X was stable and unprecedented on shallow slopes, but suffered from serious problems on steep slopes, especially along the steep ridges. AW3D30 has similar accuracy to NASADEM, and is even better in STD, MAE and RMSE when not considering the effect of glacier dynamics. SRTM-based DEMs (i.e. SRTM-GL1, SRTM v4.1 and MERIT) (~15 m RMSE) were inferior to NASADEM. MERIT shows little improvement over SRTM v4.1 in glacierized terrain. The influence of glacier elevation change on the elevation difference is larger for DEMs acquired in earlier period, at low elevations and in the ablation region. However, this does not influence the conclusion that NASADEM performed the best, followed by TanDEM-X but with serious outliers in the high elevation region. For all the DEMs, the errors increased from the south-aspect slope to the north-aspect slope, controlled by the increasing
error with slope. Misregistration errors in the glacier region are within one grid spacing, and have little influence on the evaluation benefiting from the 20 m footprint of ICESat-2 relative to the 30- or 90-m resolution DEMs.

The influence of DEM accuracy on ice-thickness inversion models depends on the model properties. Generally, a higher resolution DEM was helpful for better model outcomes. The widely used GlabTop2 model is very sensitive to the accuracy of both elevation and slope; using NASADEM as the input, this model facilitated the best outcome. Although the OGGM and HF models are less sensitive to the quality of DEM, the use of NASADEM or AW3D30 was still beneficial. Among the four ice-thickness inversion models, ITIBOV was the most sensitive to slope accuracy. Ice-thickness inversion models using AW3D30 or NASADEM as input gave the best outcomes. These two DEMs also perform the best when four ice-thickness inversion results were aggregated by the minimum MAE optimization method.

Considering the influence of inconsistency in data acquisition time on generating glacier terrain, we suggest that NASADEM is the best choice for ice-thickness inversion models over the whole TP. AW3D30 could be a good substitute limited by its mixed acquiring dates. TanDEM-X is an appropriate alternative for glaciological research focusing on the flat glacier terminus, but it requires further improvement for use in steep terrain or ice-thickness inversion.

**Code/Data availability**


**Author contribution**

W.F Chen, T.D Yao and GQ. Zhang designed the outline of this study. W.F Chen processed the data and make all the figures. Fei Li estimate the ice thickness using OGGM. Guoxiong Zheng, Yushan Zhou and Fenglin Xu: review & editing. All authors contributed to writing the paper.
Competing interests

The authors declare that they have no conflict of interest.

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