



# 1 Convolutional Neural Network and Long Short-Term Memory 2 Models for Ice-Jam Prediction

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9

10 **Abstract.** In cold regions, ice-jam events result in severe flooding due to a rapid rise in water levels upstream of the  
11 jam. These floods threaten human safety and damage properties and infrastructures as the floods resulting from ice-  
12 jams are sudden. Hence, the ice-jam prediction tools can give an early warning to increase response time and minimize  
13 the possible corresponding damages. However, the ice-jam prediction has always been a challenging problem as there  
14 is no analytical method available for this purpose. Nonetheless, ice jams form when some hydro-meteorological  
15 conditions happen, a few hours to a few days before the event. The ice-jam prediction problem can be considered as  
16 a binary multivariate time-series classification. Deep learning techniques have been successfully applied for time-  
17 series classification in many fields such as finance, engineering, weather forecasting, and medicine. In this research,  
18 we successfully applied CNN, LSTM, and combined CN-LSTM networks for ice-jam prediction for all the rivers in  
19 Quebec. The results show that the CN-LSTM model yields the best results in the validation and generalization with  
20 F1 scores of 0.82 and 0.91, respectively. This demonstrates that CNN and LSTM models are complementary, and a  
21 combination of them further improves classification.

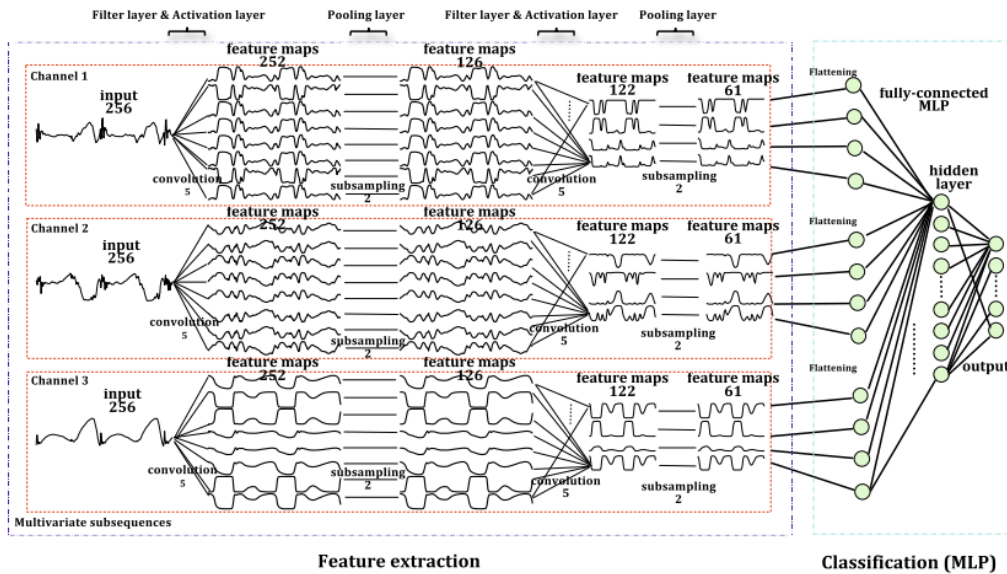
## 22 **1 Introduction**

23 Predicting ice-jam events gives an early warning of possible flooding, but there is no analytical solution to predict  
24 these events due to the complex interactions between involved hydro-meteorological variables. To date, a small  
25 number of empirical and statistical prediction methods that have been developed (threshold methods, multi-regression  
26 models, logistic regression models, and discriminant function analysis) for ice jams are site-specific with a high rate  
27 of false-positive errors (White, 2003). The numerical models developed for ice-jam prediction (e.g., ICEJAM (Flato  
28 and Gerard, 1986, cf.; Carson et al., 2011), RIVJAM (Beltaos, 1993), HEC-RAS (Brunner, 2002), ICESIM (Carson  
29 et al., 2001 and 2003), and RIVICE (Lindenschmidt, 2017)) show limitations in predicting ice-jam occurrence. This  
30 is because mathematical formulations in these models are complex which need many parameters that are often  
31 unavailable as they are challenging to measure in ice conditions. Hence, many simplifications corresponding to these  
32 parameters may degrade model accuracy (Shouyu & Honglan, 2005). A detailed overview of the previous models for  
33 ice-jam prediction based on hydro-meteorological data are presented in Madaeni et al. (2020).

34 Prediction of ice-jam occurrence can be considered a binary multivariate time-series classification (TSC) model when  
35 the time series of various hydro-meteorological variables (explained later) can be used to classify to jam or no jam.  
36 Time-series classification (particularly multivariate) has been widely used in various fields, including biomedical  
37 engineering, clinical prediction, human activity recognition, weather forecasting, and finance. Multivariate time-series



38 provide more patterns and improve classification performance compared to univariate time-series (Zheng et al., 2016).  
39 Time-series classification is one of the most challenging problems in data mining and machine learning.  
40 Most existing TSC methods are feature-based, distance-based, or ensemble methods (Cui et al., 2016). Feature  
41 extraction is challenging due to the difficulty of handcrafting useful features to capture intrinsic characteristics from  
42 time-series data (Karim et al., 2019; Zheng et al., 2014, June). Hence, distance-based methods work better in TSC  
43 (Zheng et al., 2014, June). Among the hundreds of developed methods for TSC, the leading classifier with the best  
44 performance was ensemble nearest neighbor with dynamic time warping (DTW) for many years (Fawaz et al., 2019,  
45 July; Karim et al., 2019).  
46 In the k-nearest neighbors (kNN) classifier, the given test instance is classified by a majority vote of its k closest  
47 neighbors in the training data. The kNN needs all the data to make a prediction which requires high memory. Hence,  
48 it is computationally expensive and could be slow if the database is large, and sensitive to irrelevant features and the  
49 scale of the data. Furthermore, the number of neighbors to include in the algorithm should be wisely selected. The  
50 kNN is very challenging to be used for multivariate TSC. The dynamic time warping is a more robust alternative for  
51 Euclidean distance (the most widely used time-series distance measure) to measure the similarity between two given  
52 time series by searching for an optimal alignment (minimum distance) between them (Zheng et al., 2016). However,  
53 the combined kNN with DTW is time-consuming and inefficient for long multivariate time-series (Lin et al., 2012;  
54 Zheng et al., 2014, June). The traditional classification and classic data mining algorithms developed for TSC have  
55 high computational complexity or low prediction accuracy. This is due to the size and inherent complexity of time  
56 series, seasonality, noise, and feature correlation (Lin et al., 2012).  
57 Deep learning is a type of neural network that uses multiple layers of nonlinear information to extract higher-level  
58 features from the input data. Although deep learning in recent years showed promising performance in various fields  
59 such as image and speech recognition, document classification, and natural language processing, only a few studies  
60 employed deep learning for TSC (Gu et al., 2018; Fawaz et al., 2019, July). Various studies show that deep neural  
61 networks significantly outperform the ensemble nearest neighbor with DTW (Fawaz et al., 2019, July). The main  
62 benefit of deep learning networks is automatic feature-extraction, which reduces the need for expert knowledge of the  
63 field and removes engineering bias in the classification task (Fawaz et al., 2019) as the probabilistic decision (e.g.,  
64 classification) is taken by the network.  
65 The most widely used deep neural networks for TSC are Multi-Layer Perceptron (MLP; i.e., fully connected deep  
66 neural networks), Convolutional Neural Networks (CNNs), and Long Short-Term Memory (LSTM) .  
67 The application of CNNs for TSC has recently become more and more popular, and different types of CNN are being  
68 developed with superior accuracy performance for this purpose (e.g., Cui et al., 2016). Zheng et al. (2014, June) and  
69 Zheng et al. (2016) introduce a Multi-Channels Deep Convolutional Neural Network (MC-DCNN) for multivariate  
70 TSC, where each variable (i.e., univariate time series) is trained individually to extract features and finally  
71 concatenated using an MLP to perform classification (Fig. 1). Their results show that their model achieves a state-of-  
72 the-art performance both in efficiency and accuracy on a challenging dataset. The drawback of their model and similar  
73 architectures (e.g., Devineau et al., 2018, May) is that they do not capture the correlation between variables as the  
74 feature extraction is carried out separately for each variable.

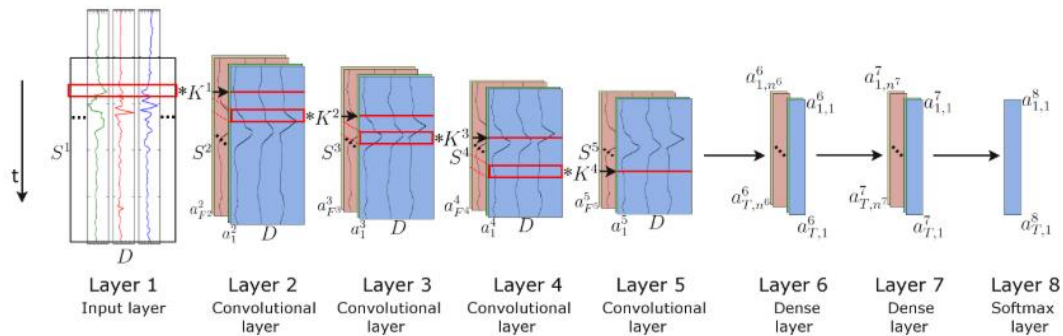


75

76 **Figure 1. A 2-stages MC-DCNN architecture for activity classification. This architecture consists of three channels input,**  
77 **two filter layers, two pooling layers, and two fully-connected layers (after Zheng et al., 2014, June).**

78 Brunel et al. (2019) present CNNs adapted for TSC in cosmology using 1D filters to extract features from each channel  
79 over time and a 1D convolution in depth to capture the correlation between the channels. They compared the results  
80 from LSTMs with CNNs, which shows that CNNs give better results than LSTMs. Nevertheless, both deep learning  
81 approaches are very promising.

82 The combination of CNNs and LSTM units has already yielded state-of-the-art results in problems requiring  
83 classification of temporal information such as human activity recognition (Li et al., 2017; Mutegeki and Han, 2020,  
84 February), text classification (Luan and Lin, 2019; March, She and Zhang, 2018, December; Umer et al., 2020),  
85 video classification ( Lu et al., 2018 and Wu et al., 2015, October), sentiment analysis (Ombabi et al., 2020; Sosa,  
86 2017; Wang et al., 2016, August; Wang et al., 2019), typhoon formation forecasting (Chen et al., 2019), and  
87 arrhythmia diagnosis (Oh et al., 2018). In this architecture, convolutional operations capture features and LSTMs  
88 capture time dependencies on extracted features. Ordóñez and Roggen (2016) propose a deep convolutional LSTM  
89 model (DeepConvLSTM) for activity recognition (Fig. 2). Their results are compared to the results from standard  
90 feedforward units showing that DeepConvLSTM reaches a higher F1 score and better decision boundaries for  
91 classification. Furthermore, they noticed that the LSTM model gives promising results with relatively small datasets.  
92 Furthermore, LSTMs present a better performance in capturing longer temporal dynamics, whereas the convolution  
93 filters can only capture the temporal dependencies dynamics within the length of the filter.



94

95 **Figure 2. The architecture of the DeepConvLSTM framework for activity recognition (after Ordóñez and Roggen, 2016).**

96 The objective of this research is to develop deep learning models to predict breakup ice-jam events to be used as an  
97 early warning system of possible flooding. Deep learning methods are promising to address the requirements of ice-  
98 jam predictions. Hence, we developed three deep learning models; a CNN, an LSTM, and a combined CN-LSTM  
99 (Convolutional-Long Short-Term Memory) for ice-jam predictions and compared the results. The previous studies  
100 show that these models show good capabilities in capturing features and the correlation between features (through  
101 convolution units) and time dependencies (through memory units) that will be later used for TSC. The combined CN-  
102 LSTM can reduce errors by compensating for the internal weaknesses of each model. In the CN-LSTM model, CNNs  
103 capture features, then the LSTMs give the time dependencies on the captured features.

## 104 2 Material and Methods

### 105 2.1 Input data and study area

106 It is known that specific hydro-meteorological conditions lead to the ice-jam occurrence (Turcotte and Morse, 2015,  
107 August and White, 2003). For instance, breakup ice jams occur when a period of intense cold is followed by a rapid  
108 peak discharge resulting from spring rainfall and snowmelt runoff (Massie et al., 2002). The period of intense cold  
109 can be represented by the changes in Accumulated Freezing Degree Days (AFDD). The sudden spring runoff increase  
110 is not often available at the jam location and can be represented by liquid precipitation and snow depth some days  
111 before the ice-jam occurrence (Zhao et al., 2012). Prowse and Bonsal (2004) and Prowse et al. (2007) evaluate various  
112 hydroclimatic explanations for river ice freeze-up and breakup, concluding that shortwave radiation is the most critical  
113 factor influencing the mechanical strength of ice and consequently the possibility of breakup ice jams to occur.  
114 Turcotte and Morse (2015, August) explain that Accumulated Thawing Degree Day (ATDD), an indicator of warming  
115 periods, partially covers the effect of shortwave radiation. In the previous studies of ice-jam and breakup predictions,  
116 discharge and changes in discharge, water level and changes in water level, AFDD, ATDD, precipitation, solar  
117 radiation, heat budget, and snowmelt or snowpack are the most readily used variables (Madaeni et al., 2020).

118 The inputs we used in this study are historical ice-jam or no ice-jam occurrence (Fig. 2) as well as hydro-  
119 meteorological variables including liquid precipitation (mm), min and max temperature (°C), AFDD (from August



120 1st; °C), ATDD (from January 1st; °C), snow depth (cm) and net radiation ( $W m^{-2}$ ) in all rivers in Quebec. The net  
121 solar radiation, the total energy available to influence the climate, is calculated as the difference between incoming  
122 and outgoing energy. If the median temperature is greater than 1, the precipitation is considered liquid precipitation.  
123 The source, time period, and spatial resolution of the input variables are presented in Table 1. The “NaN” precipitation  
124 values get 0 values.

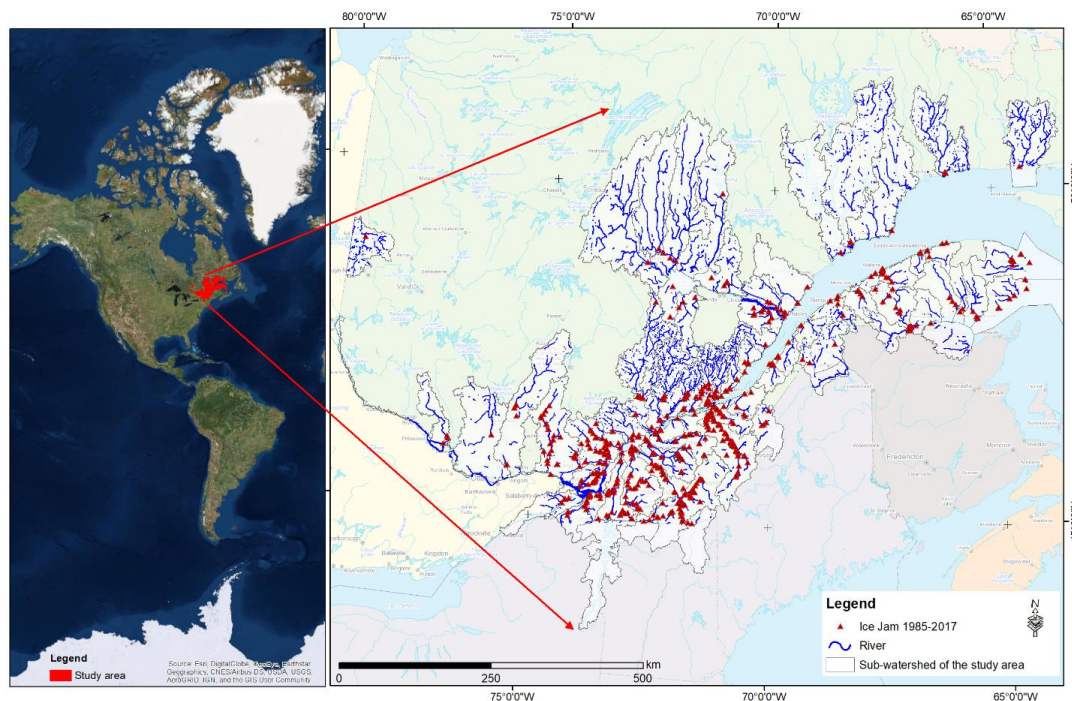
125 The ice-jam database is provided by the Quebec Ministry of Public Security (MSPQ; Données Québec, 2021) for  
126 150 rivers in Quebec, mainly in the St. Lawrence basin. The database comes from the digital or paper event reports  
127 by local authorities under the jurisdiction of the MSPQ from 1985 to 2014. Moreover, some other data of this database  
128 are provided by the field observations from the Vigilance / Flood application from 2013 to 2019. It contains 995  
129 recorded jam events that are not validated and contain many inaccuracies, mainly in the toponymy of the rivers,  
130 location, dating, and the redundancy of jam events.

131 The names of the watercourse of several ice jams are not given or completely wrong or affected by a typo or an  
132 abbreviation. The toponymy of the rivers was corrected using the National Hydrographic Network (NHN; National  
133 Hydrographic Network - Natural Resources Canada (NRCan)), the Geobase of the Quebec hydrographic network  
134 (National Hydro Network - NHN - GeoBase Series - Natural Resources Canada), and the Toporama Web map service  
135 (The Atlas of Canada - Toporama - Natural Resources Canada) of the Sector of Earth Sciences.

136 Several ice jams are placed on the banks at a small distance (less than 20 m) from the polygon of the river. In this  
137 case, the location of the ice jam is moved inside the river polygon. In other cases, the ice-jam point is posed further  
138 on the flooded shore at a distance between 20 and 200 m. This has been corrected based on images with very high  
139 spatial resolution, the sinuosity and the narrowing of the river, the history of ice jams at the site in question, and the  
140 press archives. In addition, some ice jams were placed too far from the mentioned river due to a typo in entering their  
141 coordinates. A single-digit correction in longitude or latitude returned the jam to its exact location. There are certain  
142 cases where the date of jam formation is verified by searching the press archives, notably when the date of formation  
143 is missing or several jams with the same dates and close locations in a section of a river are present.

144 The ice jam database contains many duplicates. This redundancy can be due to merging two data sources, the double  
145 entry during ice-jam monitoring, or recording an ice jam for several days. The duplicates are removed from the  
146 database. The corrected ice-jam database contains 850 jams for 150 rivers, mainly in southern Quebec (Fig. 3). The  
147 ice jams formed in November and December (freeze-up jams) are removed to only include breakup jams (from January  
148 15th) in the modelling as these two types of jams are formed due to different processes. The final breakup ice-jam  
149 database that used in this study includes 504 jam events.





150

151 **Figure 3. Study area and historic ice-jam locations recorded in Quebec from 1985-2017.**

152 **Table 1. Hydro-meteorological data used as the input to the model.**

Data	Source	Duration	Spatial resolution
<b>Min and Max temperature*</b>	Daily Surface Weather Data (Daymet; Thornton et al., 2020)	1979-2019	1 km
<b>Liquid precipitation</b>	Canadian Precipitation Analysis (CaPA; Mahfouf et al., 2007)	2002-2019	10-15km
<b>Liquid precipitation</b>	North American Regional Reanalysis (NARR; Mesinger et al., 2006)	1979-2001	30 km
<b>Infrared radiation emitted by the atmosphere</b>	North American Regional Reanalysis (NARR)	1979-2019	30 km
<b>Infrared radiation emitted from the surface</b>	North American Regional Reanalysis (NARR)	1979-2019	30 km
<b>Snow depth</b>	North American Regional Reanalysis (NARR)	1979-2019	30 km

153

\* The average was used to derive the AFDD and the ATDD.

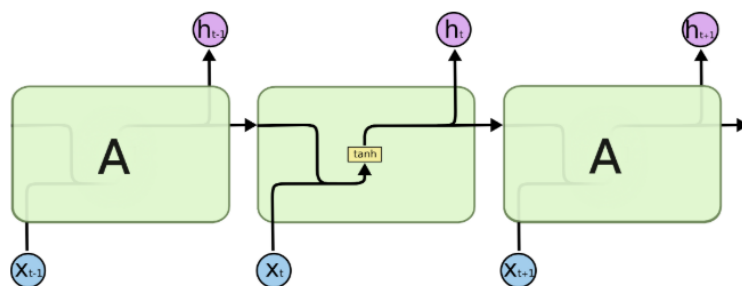
154

155 **2.2 Deep learning models for time-series classification (TSC)**

156 The most popular deep neural networks for TSC are MLP, CNNs, and LSTM. Despite their power, however, MLP  
 157 has limitations that each input (i.e., time-series element) and output are treated independently, which means that the  
 158 temporal or space information is lost (Lipton et al., 2015). Hence, an MLP needs some temporal information in the  
 159 input data to model sequential data such as time series (Ordóñez and Roggen, 2016). In this regard, Recurrent Neural  
 160 Networks (RNNs) are specifically adapted to sequence data through the direct connections between individual layers  
 161 (Jozefowicz et al., 2015). Recurrent Neural Networks perform the same repeating function with a straightforward



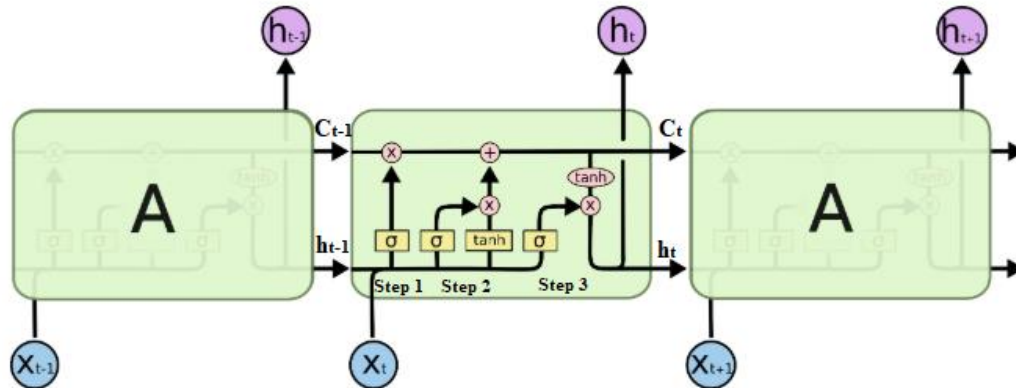
162 structure, e.g., a single tanh (hyperbolic tangent) layer, for every input of data ( $x_t$ ), while all the inputs are related to  
163 each other with their hidden internal state, which allows it to learn the temporal dynamics of sequential data (Fig. 4).



164  
165 **Figure 4. An RNN with a single tanh layer, where A is a chunk of the neural network,  $x_t$  is input data, and  $h_t$  is output data**  
166 **(after Olah, 2015).**

167 Recurrent Neural Networks were rarely used in TSC due to their significant problems. Recurrent Neural Networks  
168 mainly predict output for each time-series element, they are sensitive to the first examples seen, and it is also  
169 challenging to capture long-term dependencies due to vanishing gradients, exploding gradients, and their complex  
170 dynamics (Devineau et al., 2018, June; Fawaz et al., 2019).

171 Long short-term memory RNNs are developed to improve the performance of RNNs by integrating a memory to  
172 model long-term dependencies in time-series problems (Brunel et al., 2019; Karim et al., 2019). Long short-term  
173 memory networks do not have the problem of exploding gradients. LSTMs have four interacting neural network layers  
174 in a very special way (Fig. 5). An LSTM has three gates (sigmoid layers;  $\sigma$ ) to control how much of each component  
175 should be let through by outputting numbers between zero and one. The input to an LSTM goes through three gates  
176 (“forget”, “input”, and “output gates”) that control the operation performed on each LSTM block (Ordóñez and  
177 Roggen, 2016). The first step is the “forget gate” layer that gets the output of the previous block ( $h_{t-1}$ ), the input for  
178 the current block ( $x_t$ ), and the memory of the previous block ( $C_{t-1}$ ) and gives a number between 0 and 1 for each  
179 number in the cell state ( $C_{t-1}$ ; Olah, 2015). The second step is called the “input gate” with two parts, a sigmoid layer  
180 that decides which values to be updated and a tanh layer that creates new candidate values for the cell state. These two  
181 new and old memories will then be combined and control how much the new memory should influence the old  
182 memory. The last step (output gate; step 3 in Fig. 5) gives the output by applying a sigmoid layer deciding how much  
183 new cell memory goes to output, and multiply it by tanh (giving values between  $-1$  and  $1$ ).



184

185 **Figure 5. Structure of LSTM block with four interacting layers (adopted from Olah, 2015).**

186 Recently, convolutional neural networks challenged the assumption that RNNs (e.g., LSTMs) have the best  
187 performance when working with sequences. Convolutional neural networks show state-of-the-art performance in  
188 sequential data such as speech recognition and sentence classification, similar to TSC (Fawaz et al., 2019).

189 Convolutional neural networks are the most widely used deep learning methods in TSC problems (Fawaz et al., 2019).  
190 They learn spatial features from raw input time series using filters (Fawaz et al., 2019). Convolutional neural networks  
191 are robust and need a relatively small amount of training time comparing with RNNs or MLPs. They work best for  
192 extracting local information and reducing the complexity of the model.

193 A CNN is a kind of neural network with at least one convolutional layer (or filter). A CNN usually involves several  
194 convolutional layers, activation functions, and pooling layers for feature extraction following by dense layers (or  
195 MLP) as a classifier (Devineau et al., 2018, June). The reason to use a sequence of filters is to learn various features  
196 from time series for TSC. A convolutional layer consists of a set of learnable filters that compute dot products between  
197 local regions in the input and corresponding weights. With high-dimensional inputs, it is impractical to connect  
198 neurons to all neurons in the previous layer. Therefore, each neuron in CNNs is connected to only a local region of  
199 the input, namely the receptive field, which equals the filter size (Fig. 5). This feature reduces the number of  
200 parameters by limiting the number of connections between neurons in different layers. The input is first convolved  
201 with a learned filter, and then an element-wise nonlinear activation function is applied to the convolved results (Gu et  
202 al., 2018). The pooling layer performs a downsampling operation such as maximum or average, reducing the spatial  
203 dimension (Fig. 6). One of the most powerful features of CNNs is called weight or parameter sharing, where all  
204 neurons share filters (weights) in a particular feature map (Fawaz et al., 2019) to reduce the number of parameters.



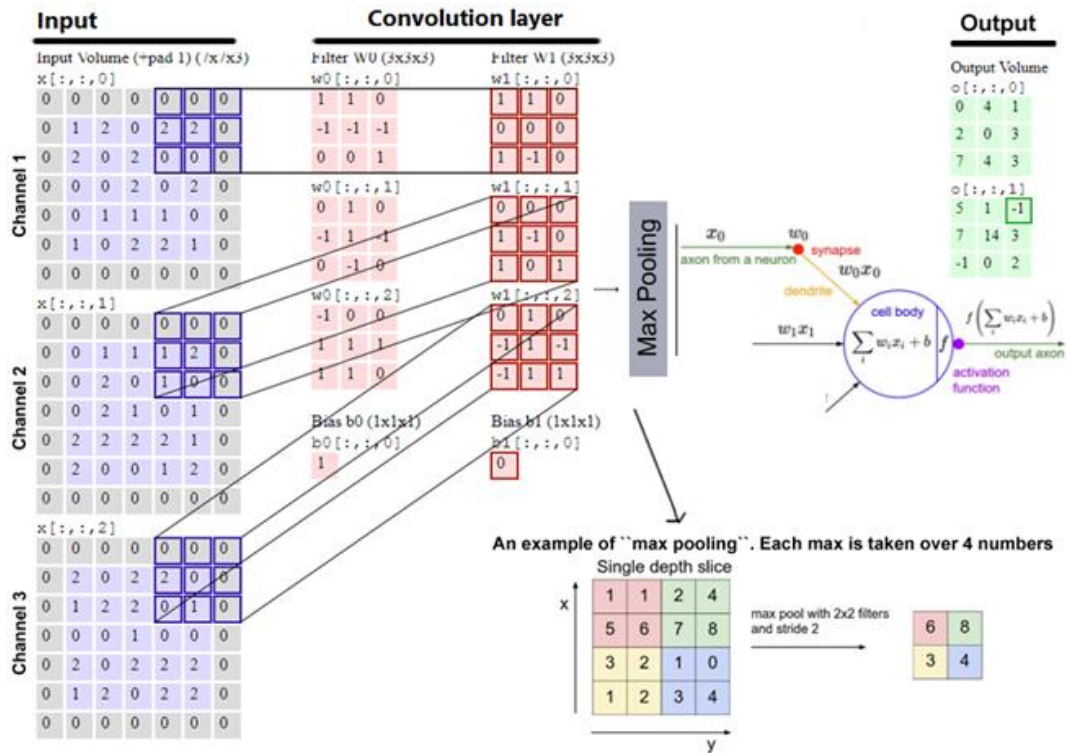


Figure 6. . A CNN Architecture for image classification (modified from Karpathy, 2017).

### 205 2.3 Model libraries

206 In an anaconda (Analytics, C., 2016) environment, Python is implemented CNN, LSTM, and CN-LSTM networks  
 207 for TSC. To build and train networks, the networks are implemented in Theano (Bergstra et al., 2010, June) using the  
 208 Lasagne (Dieleman et al., 2015) library. The other core libraries used for importing, preprocessing, training data, and  
 209 visualization of results are Pandas (Reback et al., 2020), NumPy (Harris et al., 2020), Scikit-Learn (Pedregosa et al.,  
 210 2011), and Matplotlib.PyLab (Hunter, J. D., 2007). Spyder (Raybaut, 2009) package of Anaconda is utilized as an  
 211 interface, or the command window can be used without any interface.

### 212 2.4 Preprocessing

213 The data is comprised of variables with varying scales, and the machine learning algorithms can benefit from rescaling  
 214 the variables to all have the same scale. Scikit-learn (Pedregosa et al., 2011) is a free library for machine learning in  
 215 Python that can be used to preprocess data. We examined Scikit-learn MinMaxScaler (scaling each variable between  
 216 0 and 1), Normalizer (scaling individual samples to the unit norm), and StandardScaler (transforming to zero mean  
 217 and unit variance separately for each feature). The results show that MinMaxScaler (Eq. (1)) works the best in our  
 218 models. The scaling of validation data is done with min and max from train data.



219 
$$X_{\text{scaled}} = \left( \frac{X - X_{\text{min}}}{X_{\text{max}} - X_{\text{min}}} \right), \quad (1)$$

220 For each jam or no jam event, we used 15 days of information before the event to predict the event on the 16th day.  
221 We generate a balanced dataset with the same number of jam and no-jam events (1008 small sequences totally),  
222 preventing the model from becoming biased to jam or no-jam events. The hydro-meteorological data related to no-  
223 jam events are constructed by extracting data from the reaches of no-jam records. We used ShuffleSplit subroutine  
224 from the Scikit-learn library, where the database was randomly sampled during each re-shuffling and splitting iteration  
225 to generate training and validation sets. We applied 100 re-shuffling and splitting iterations with 80 % of data for  
226 training and 20 % for validation. There are 806 and 202 small sequences with the size of (16, 7), 16 days of data for  
227 the seven variables; for training and validation, respectively. To examine models' generalization, we hold out 30 small  
228 sequences for testing and 80 % and 20 % of remaining data for training and validation, respectively.

## 229 **2.5 Training**

230 Training a deep neural network with an excellent generalization to new unseen inputs is challenging. As a benchmark,  
231 a CNN model with the parameters and layers similar to previous studies is developed. The model shows underfitting  
232 or overfitting with various architectures and parameters. To overcome underfitting, deeper models and more nodes in  
233 each layer are beneficial; however, overfitting is more challenging to overcome. The ice-jam dataset is small, which  
234 easily causes the network to memorize training examples and consequently results in overfitting, as a small dataset  
235 may not appropriately describe the relationship between input and output spaces.

### 236 **2.5.1 Overcome overfitting**

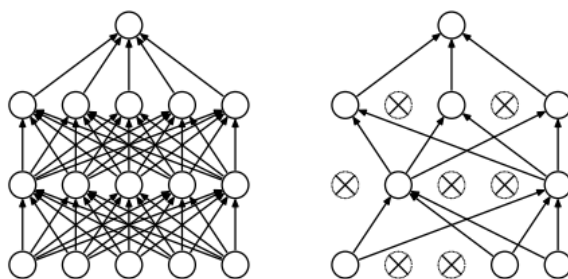
#### 237 **2.5.1.1 Noise layer**

238 The first approach to overcome overfitting is acquiring more data that is not possible with ice-jam records. Another  
239 popular approach to increase the number of samples is data augmentation, including cropping, rotating, blurring, color  
240 modification, and noise injection in image classification. Data augmentation can act as a regularizer, prevent  
241 overfitting, and improve performance in imbalanced class problems (Wong et al., 2016). However, the application of  
242 data augmentation in deep learning for time series classification still has not been studied thoroughly (Fawaz et al.,  
243 2019). To expand the size of the dataset, noise layers, as a simple form of random data augmentation, can be used.  
244 Over the training process, each time an input sample is exposed to the model, the noise layer creates new samples in  
245 the vicinity of the training samples resulting in various input data every time, increases randomness, making the model  
246 less prone to memorize training samples and learns more general features (resulting in better generalization).  
247 We added the Gaussian noise layer (from the Lasagne library), where the noise values are Gaussian-distributed with  
248 zero-mean and a standard deviation of 0.1 to the input. The noise layer is usually added to the input data but can also  
249 be added to other layers.



### 250 2.5.1.2 Dropout

251 The other approach to tackle overfitting is dropout (Srivastava et al., 2014). The dropout, the most successful method  
252 for neural network regularization, randomly sets inputs to zero (Fig. 7). To overcome overfitting and examine the  
253 effectiveness of dropout in our models, the dropout with the recommended rates of 0.1 for the input layer and between  
254 0.5 and 0.8 for hidden layers (Garbin et al., 2020) are applied in different layers of the models.



255

256 **Figure 7. A neural network with two hidden layers (left) and a neural network with dropout (right; after Srivastava et al.,**  
257 **2014).**

### 258 2.5.1.3 Early stopping

259 Early stopping is another efficient method to tackle overfitting via halting the training procedure where further  
260 training would decrease training loss, while validation loss starts to increase.

### 261 2.5.1.4 Batch normalization

262 As explained earlier, the input data is scaled separately for each feature to be between 0 and 1. However, in deep  
263 learning, the distribution of the input of each layer will be changed by updates to all the preceding layers, so-called  
264 internal covariate shift. Hence, hidden layers try to learn to adapt to the new distribution slowing down the training  
265 process. Batch normalization (Ioffe and Szegedy, 2015, June) is a recent method that provides any layer with inputs  
266 of zero mean and unit variance and consequently prevents internal covariate, solves exploding or vanishing gradient  
267 problems, allows the use of higher learning rates, improves the training efficiency, and speeds up the training. Batch  
268 normalization adjusts the value for each batch, results in more noise acting as a regularizer, similar to dropout, and  
269 thus reduces the need for dropout (Garbin et al., 2020). We performed batch normalization over each channel in  
270 different layers in our models to find its best locations through trial and error.

### 271 2.5.1.5 Regularization

272 There are two general ways to keep a deep neural network simple and consequently prevent overfitting; through the  
273 number of weights and values of weights. The number of weights can be controlled by the number of layers and nodes  
274 optimized via the grid or random search. A network with large weights can be more complex and unstable as large  
275 weights increase loss gradients exponentially, resulting in exploding gradients that cause massive output changes with  
276 minor changes in the inputs. In turn, the exploding gradients can force the model loss and weights to “NaN” values  
277 (Brownlee, 2017).



278 The simplest and most common approach to keep the weights small is regularization methods that involve checking  
279 model weights and adding an extra penalty term to the loss function in proportion to the size of weights' size in the  
280 model. The two main methods used to calculate the size of the weights are L1 (the sum of the absolute values of the  
281 weights; Eq. (2)) and L2 or weight decay (the sum of the squared values of the weights; Eq. 3). In Eq. (2) and (3),  $\lambda$   
282 is a parameter that controls the importance of the regularization, and  $W$  is the network parameters. The L1  
283 regularization encourages weights to be 0.0 (causing underfitting) and very few features with non-zero weights, while  
284 L2 regularization forces the weights to be small rather than zero. Hence, L2 can predict more complex patterns when  
285 output is a function of all input features. We used an L2 regularization cost by applying a penalty to the parameters of  
286 all layers in the networks in CNN, LSTM, and CN-LSTM models.

$$287 \text{ Cost function} + \lambda \sum_{i=1}^n |w_i| \quad (2)$$

$$288 \text{ Cost function} + \lambda \sum_{i=1}^n w_i^2 \quad (3)$$

## 289 2.5.2 Architecture Tuning

290 Finding hyperparameter values in deep learning has been challenging due to the complex architecture of deep learning  
291 and a large number of parameters (Garbin et al., 2020). To find the best model architecture, we study the performance  
292 of models with different layers and parameters such as number of noise, batch normalization, convolutional, pooling,  
293 LSTM, dropout, and dense layers, as well as different pooling sizes and strides, different batch sizes, various scaling  
294 of data (standardization and normalization), various filter sizes, number of units in LSTM and dense layers, the type  
295 of the activation functions, regularization and learning rates, weight decay and number of filters in convolutional  
296 layers. We also applied various combinations of these layers and parameters.

### 297 2.5.2.1 Activation function

298 The activation function adds non-linearity to the network allowing the model to learn more complex relationships  
299 between inputs and outputs (Zheng et al., 2014, June). Each activation function that is used in deep learning has its  
300 advantages and disadvantages, and typical activation functions in deep learning are Rectified Linear Unit (ReLU; Eq.  
301 (4)), sigmoid (Eq. (5)), and hyperbolic tangent (tanh; Eq. (6); Fig. 8; Gu et al., 2018). In deep neural networks, adding  
302 more layers with certain activation functions results in the vanishing gradient problem where the gradients of the loss  
303 function become almost zero, causing difficulties in training. For instance, the sigmoid function maps a large input  
304 space into a small one between 0 and 1. Hence, when the input is very positive or very negative, the sigmoid function  
305 saturates (becomes very flat) and becomes insensitive to small changes in its input, causing the derivatives to disappear  
306 (Goodfellow et al., 2016). Therefore, in backpropagation, small derivatives are multiplied together, causing the  
307 gradient to decrease exponentially, propagating back to the first layer. This causes ineffective updates of weights and  
308 biases of the initial layers and consequently inaccuracy. Some solutions to overcome this problem include using  
309 specific activation functions like ReLU and tanh and using batch normalization layers to prevent the activation  
310 functions from becoming saturated. The ReLU recently drawn lots of attention and has been widely used in recent  
311 deep learning models (Gamboa, 2017). The advantage of ReLU over sigmoid and tanh is a better generalization,

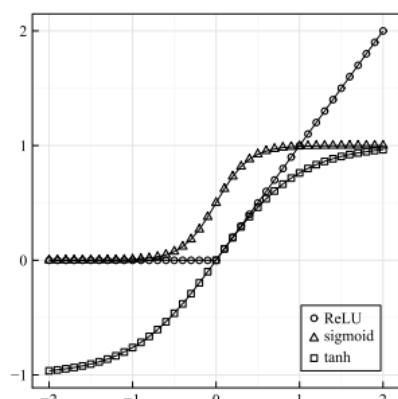


312 making the training faster and simpler. Hence, we investigated the performance of the model with ReLU, sigmoid, or  
 313 tanh activation functions in convolutional layers.

314  $ReLU(x) = \max(0, x)$  (4)

315  $Sigmoid(x) = \frac{1}{1+e^{-x}}$  (5)

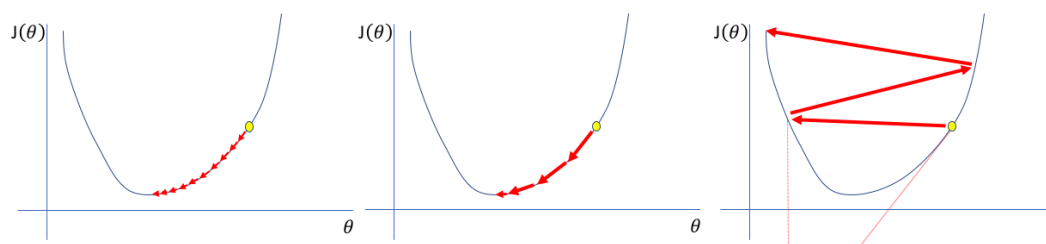
316  $\tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}$  (6)



317  
 318 **Figure 8. Illustration of sigmoid, tanh, and ReLU activation functions (after Zheng et al., 2016).**

319 **2.5.2.2 Learning rate**

320 To find the minimum cost function, a move in the negative direction of the gradient is required. This movement is  
 321 called the “learning rate,” which is the most significant hyperparameter in training a deep neural network. The model  
 322 error is calculated, and the errors corresponding to weights updated by the learning rate are backpropagated in the  
 323 network. A too-small learning rate needs many updates and epochs, reaching the minimum. On the other hand, a too-  
 324 large learning rate causes dramatic updates and leads to oscillations in loss over epochs. A good learning rate quickly  
 325 reaches the minimum point between 0.1 to 1e-6 on a log scale and can be found through a grid or random search (Fig.  
 326 9).



327  
 328 **Figure 9. Too small, good, and too large learning rates from left to right (after Jordan, 2018).**



### 329 2.5.2.3 Update expression

330 There are various algorithms to update the trainable parameters at each mini-batch. The parameter updating procedure  
331 includes feedforwarding, backpropagation, and applying gradients. We tried the Stochastic Gradient Descent (SGD)  
332 with Nesterov momentum, RMSProp, Adadelta, and Adam updates to update the parameters in Lasagne. The SGD  
333 with momentum updates the model weights by adding a momentum so that the overall gradient depends on the current  
334 and previous gradients, causing the weights to move in the previous direction without oscillation.

### 335 2.5.3 Network optimization

336 Training CNN involves global optimization by defining a loss expression to be minimized overtraining. For the  
337 classification task, the loss function of the models is calculated using categorical cross-entropy between network  
338 outputs and targets (Eq. (7)), where  $L$  is the loss,  $p$  is the prediction (probability),  $t$  is the target, and  $c$  is the number  
339 of classes. Then, the mean of the loss is computed over each mini-batch.

$$340 L = -\sum_{i=1}^c t_i \log(p_i) \quad (7)$$

### 341 2.5.4 Model evaluation

342 The network on the validation set is evaluated after each epoch during training to monitor the training progress. During  
343 validation, all non-deterministic layers are switched to deterministic. For instance, noise layers are disabled, and the  
344 update step of the parameters is not performed.

345 The classification accuracy cannot appropriately represent the model performance for unbalanced datasets, as the  
346 model can show a high accuracy by biasing towards the majority class in the dataset (Ordóñez and Roggen, 2016).  
347 While we built a balanced dataset (with the same number of jam and no jam events), randomly selecting test data and  
348 shuffling the inputs, and splitting data into train and validation sets can result in a slightly unbalanced dataset. In our  
349 case, the number of jams and no jams for train and validation and test sets is presented in Table 2. Therefore, the F1  
350 score (Eq. (8)), which considers each class equally important, is used to measure the binary classification accuracy.  
351 The F1 score, as a weighted average of the precision (Eq. (9)) and recall (Eq. (10)), has the best and worst scores of 1  
352 and 0, respectively. In Eqs. 9 and 10, TP, FP, and FN are true positive, false positive, and false negative, respectively.

353 **Table 2. The number of jam and no jam events in train and validation and test datasets.**

	Train and validation	Test
Jam	504	48
No jam	403	53

$$354 F1 = 2 \times \frac{\text{precision} \times \text{recall}}{\text{precision} + \text{recall}} \quad (8)$$

$$355 \text{Precision} = \frac{TP}{TP+FP} \quad (9)$$

$$356 \text{Recall} = \frac{TP}{TP+FN} \quad (10)$$





357 Although the model accuracy is usually used to examine the performance of deep learning models, the model size  
358 (i.e., number of parameters) provides a second metric, which represents required memory and calculations, to be  
359 compared among models with the same accuracy (Garbin et al., 2020).

360 After training the model, the well-trained network parameters are saved to a file and are later used for testing the  
361 network generalization using a test dataset, which is not seen during training and validation.

## 362 **3 Results and Discussion**

### 363 **3.1 Hyperparameters optimization**

#### 364 **3.1.1 Batch size**

365 The inputs and corresponding targets are iterated in mini-batches for training and validation. Batch size significantly  
366 influences the training time (Fawaz et al., 2019, July), and the batch size of 32 is usually used in previous studies.  
367 However, we investigated batch sizes of 16, 32, and 64, and the mini-batches of 16 demonstrate to improve the results  
368 slightly.

#### 369 **3.1.2 Noise layers**

370 The performance of CNN and LSTM models developed for the ice-jam prediction problem is improved by adding a  
371 noise layer to the input, while the CN-LSTM model showed underfitting. Adding a noise layer to other layers does  
372 not improve any of the developed models for ice-jam prediction.

#### 373 **3.1.3 Dropout layer**

374 Adding dropout layers could not improve any developed models. This agrees with previous studies revealing that  
375 dropout does not work well with LSTMs (Zaremba et al., 2014) and CNNs, and dropout layers do not work when  
376 batch size is small (less than 256; Garbin et al., 2020). Furthermore, it is in agreement with Garbin et al. (2020) stating  
377 that utilizing batch normalization layers in a model reduces the need for dropout layers.

#### 378 **3.1.4 Number of layers**

379 The depth is related to the sequence length (Devineau et al., 2018, May), as deeper networks need more data to provide  
380 better generalization (Fawaz et al., 2019, July). In the previous studies of CNNs, there are usually one, two, or three  
381 convolution stages (Zheng et al., 2014, June). We tried different numbers of CNN, LSTM, and dense layers and  
382 selected three, two, and two such layers, respectively, as the sequence length in this study is small (16), and we could  
383 not improve the model performance by merely adding more depth.

#### 384 **3.1.5 Number and size of CN filters**

385 Fawaz et al. (2019, July) explain the number and length of filters used in CNNs. Data with more classes need more  
386 filters to classify the inputs accurately. Longer time series need longer filters to capture longer patterns and  
387 consequently to produce accurate results. However, longer kernels significantly increase the number of parameters



388 and increase the potential for overfitting small datasets, while a small kernel size risks poor performance. In our  
389 models, the optimum number of filters is attained to be 128 by searching among the typical number of filters (i.e., 32,  
390 64, and 128). The kernel sizes of 3, 5, and 7 are often applied in deep CNNs. We tried these filter sizes, and the best  
391 performance was achieved through using two convolutional layers with 1-D filters of (5, 1) with the stride of (1, 1) to  
392 capture temporal variation for each variable separately.  
393 Furthermore, one convolutional layer with 2-D filters of size (5, 3) with the stride of (1, 1) is then used to achieve the  
394 correlation between variables via depth-wise convolution of input time-series. A big stride might cause the model to  
395 miss valuable data used in predicting and smoothing out the noise in the time series. The layers in CNNs have a bias  
396 for each channel, sharing across all positions in each channel.

### 397 3.1.6 Padding

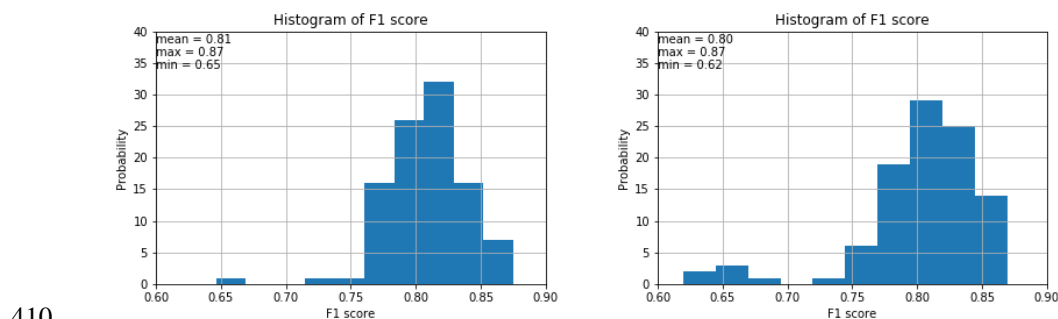
398 The convolution is applied where the input and the filter overlap. Hence, we pad the input by zeros with half the filter  
399 size on both sides. Using stride of 1 with “Pads = same” (in Lasagne) in the convolutional 2-D layers results in an  
400 output size equal to the input size for each layer.

### 401 3.1.7 Activation functions in CN layers

402 The experiments demonstrate that errors are very high using tanh, whereas ReLU and sigmoid show almost the same  
403 performance. As ReLU performs slightly better than sigmoid, we used ReLU in our models.

### 404 3.1.8 Weight initialization

405 Among the various types of methods available in Lasagne for weight initialization, the GLOROT uniform (i.e., Xavier;  
406 Glorot and Bengio, 2010, March) and He initializations (He et al., 2015), the most popular initialization techniques,  
407 are used to set the initial random weights in convolutional layers. The results reveal that these methods yield almost  
408 the same F1 scores. However, the histograms of F1 scores reveal that GLOROT uniform yields slightly better results  
409 (Fig. 10).



410

411 **Figure 10. Histograms of F1 score for CNN using He (left) and GLOROT uniform (right) weight initialization with 100**  
412 **random train-validation splits.**



413 **3.1.9 Number of LSTM units and their activation functions**

414 The optimal number of units in LSTM layers was found through a search over typical numbers of 32, 64, and 128.  
415 We found that 128 units yield the best results in our models. We used the default activation function of tanh in LSTM  
416 layers.

417 **3.1.10 Dense layer**

418 The dense layers with ReLU functions following by one dense layer with softmax function are applied after the  
419 feature learning and LSTM layers to perform classification. The common number of units in dense layers are 16, 32,  
420 128, and 256. We found that 32 gives the best results in our models. To output the binary classes from the network,  
421 softmax or sigmoid functions can be used. We applied softmax as it gives a probability for each class where their total  
422 sum is one.

423 **3.1.11 Adaptive learning rates**

424 The adaptive learning rate decreases the learning rate and consequently weights over each epoch. We tried different  
425 base learning and decay rates for each model and found that the learning rate significantly impacts the model  
426 performance. Finally, we chose a base learning rate of 0.1, 0.01, and 0.001 for LSTM, CNN, and CN-LSTM and,  
427 respectively. A decay rate of 0.8 was used for CNN and CN-LSTM, while for the LSTM model, this rate was 0.95.  
428 Table 3 shows the adaptive learning rates for CNN, LSTM, and CN-LSTM calculated using Eq. (11) for each epoch.

429 
$$\text{adaptive learning rate} = \text{base learning rate} \times \text{decay}^{\text{epoch}} \quad \text{Eq. (11)}$$

430 The experiments show that the learning rate is the most critical parameter influencing the model performance. A small  
431 learning rate can cause the cost function to get stuck in local minima, and a large learning rate can result in oscillations  
432 around global minima without reaching it.

433 Our CN-LSTM model is deeper than the other two models, and deeper models are more prone to a vanishing gradient  
434 problem. To overcome the vanishing gradients, it is recommended that lower learning rates, e.g., lower than  $1e-4$ , be  
435 used. Interestingly, we found that our CN-LSTM model works better with lower learning rates than the other two  
436 models.

437

438 **Table 3. The adaptive learning rate for 50 epochs.**

Epochs	Learning rate		
	CNN	CN-LSTM	LSTM
1	0.008	8.00E-04	0.095
2	0.006	6.40E-04	0.09
3	0.005	5.12E-04	0.086
4	0.004	4.10E-04	0.081
.	.	.	.
.	.	.	.
40	1.30E-06	1.33E-07	0.013



.	.	-
50	1.40E-07	1.43E-08

439

440 **3.1.12 Update expression**

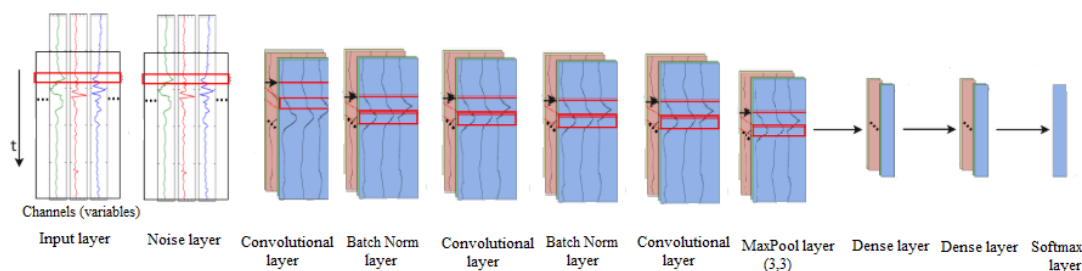
441 We found that SGD with momentum works better than other methods in our cases. The typical values for momentum  
 442 are 0.99, 0.9, and 0.5. We applied different values and found that 0.9 gives the best results in our models; this high  
 443 momentum results in larger update steps. It is recommended to scale the learning rate by “1 – momentum” for using  
 444 the high momentums, which gives 0.1. Interestingly, we already have applied the base learning rate of 0.1 for the  
 445 LSTM model chosen through trial and error (as explained earlier); however, smaller values are chosen for CNN and  
 446 CN-LSTM networks.

447 **3.2 Architecture of models**

448 The architectures of CNN, LSTM, and CN-LSTM models that are finally selected are presented in Figs. 11, 12, and  
 449 13, respectively. The layers, their output shapes, and their number of parameters are presented in Tables 4, 5, and 6  
 450 for CNN, LSTM, and CN-LSTM models, respectively.

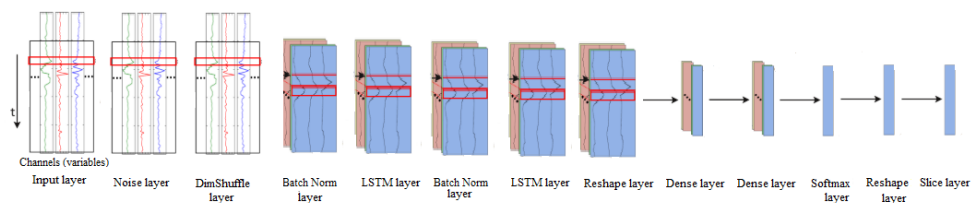
451 The ice-jam dataset for Quebec contains 1008 balanced sequence instances (with a length of 16), which is small for  
 452 deep learning. The deep learning models often tend to overfit small datasets by memorizing inputs rather than training.  
 453 The noise layers applied to the CNN and LSTM models significantly overcome the overfitting problem through data  
 454 augmentation. However, the performance of the CN-LSTM model dramatically deteriorates, including a noise layer  
 455 (Fig. 14; showing underfitting).

456 The CNN models often include pooling layers to reduce data complexity and dimensionality. However, it is not always  
 457 necessary that every convolutional layer is followed by a pooling layer in the time-series domain (Ordóñez and  
 458 Roggen, 2016). For instance, Fawaz et al. (2019, July) do not apply any pooling layers in their models for TSC. We  
 459 tried max-pooling layers after different convolutional layers in CNN and CN-LSTM networks and found that a pooling  
 460 layer following only the last convolutional layer improves the performance of both models. This can be due to  
 461 subsampling the time series and using time series with a length of 16 that reduces the need for reducing dimensionality.  
 462



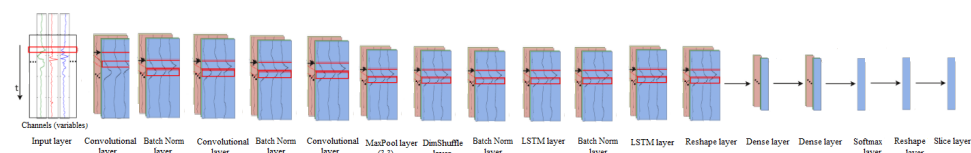
463

464 **Figure 11. The architecture of the CNN model for ice-jam prediction (adapted after Ordóñez and Roggen, 2016).**



465  
 466

Figure 12. The architecture of the LSTM model for ice-jam prediction (adapted after Ordóñez and Roggen, 2016).



467

468

Figure 13. The architecture of the CN-LSTM model for ice-jam prediction (adapted after Ordóñez and Roggen, 2016).

469

Table 4. The layers, their output shapes, and their number of parameters for the CNN model.

Layers	Output shape	Number of parameters
Input	(16, 1, 16, 7)	0
GaussianNoise	(16, 1, 16, 7)	0
Conv2D	(16, 128, 16, 7)	640
BatchNorm	(16, 128, 16, 7)	512
Nonlinearity	(16, 128, 16, 7)	0
Conv2D	(16, 128, 16, 7)	81920
BatchNorm	(16, 128, 16, 7)	512
Nonlinearity	(16, 128, 16, 7)	0
Conv2D	(16, 128, 16, 7)	245888
MaxPool2D	(16, 128, 5, 2)	0
Dense	(16, 32)	40992
Dense	(16, 32)	1056
Softmax	(16, 2)	66

470

471

Table 5. The layers, their output shapes, and their number of parameters for the LSTM model.

Layers	Output shape	Number of parameters
Input	(16, 1, 16, 7)	0
GaussianNoise	(16, 1, 16, 7)	0
Dimshuffle	(16, 16, 1, 7)	0
BatchNorm	(16, 16, 1, 7)	64
LSTM	(16, 16, 128)	70272
BatchNorm	(16, 16, 128)	64
Nonlinearity	(16, 16, 128)	0
LSTM	(16, 16, 128)	132224
Reshape	(256, 128)	0



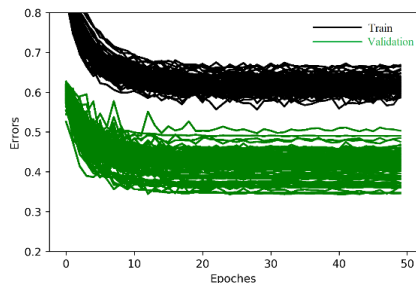
<b>Dense</b>	(256, 32)	4128
<b>Dense</b>	(256, 32)	1056
<b>Softmax</b>	(256, 2)	66
<b>Reshape</b>	(16, 16, 2)	0
<b>Slice</b>	(16, 2)	0

472  
 473

Table 6. The layers, their output shapes, and their number of parameters for the CN-LSTM model.

Layers	Output shape	Number of parameters
<b>Input</b>	(16, 1, 16, 7)	0
<b>Conv2D</b>	(16, 128, 16, 7)	640
<b>BatchNorm</b>	(16, 128, 16, 7)	512
<b>Nonlinearity</b>	(16, 128, 16, 7)	0
<b>Conv2D</b>	(16, 128, 16, 7)	81920
<b>BatchNorm</b>	(16, 128, 16, 7)	512
<b>Nonlinearity</b>	(16, 128, 16, 7)	0
<b>Conv2D</b>	(16, 128, 16, 7)	245888
<b>MaxPool2D</b>	(16, 128, 5, 2)	0
<b>Dimshuffle</b>	(16, 5, 128, 2)	0
<b>BatchNorm</b>	(16, 5, 128, 2)	20
<b>LSTM</b>	(16, 5, 128)	197760
<b>BatchNorm</b>	(16, 5, 128)	20
<b>Nonlinearity</b>	(16, 5, 128)	0
<b>LSTM</b>	(16, 5, 128)	132224
<b>Reshape</b>	(80, 128)	0
<b>Dense</b>	(80, 32)	4128
<b>Dense</b>	(80, 32)	1056
<b>Softmax</b>	(80, 2)	66
<b>Reshape</b>	(16, 5, 2)	0
<b>Slice</b>	(16, 2)	0

474



475

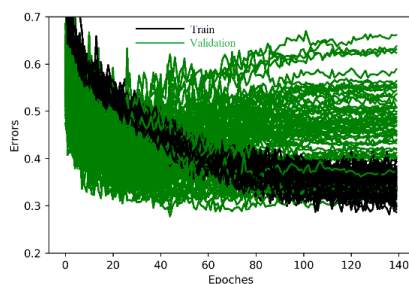
476 Figure 14. Train and validation errors over epochs for CN-LSTM model with a noise layer.





477 **3.3 Model evaluation**

478 LSTM needs only early stopping at 40 epoch among the developed models, as its validation error starts to increase,  
479 while its training error continues to decrease (Fig. 15). Hence, we set the number of epochs to 40 for the LSTM model.



480

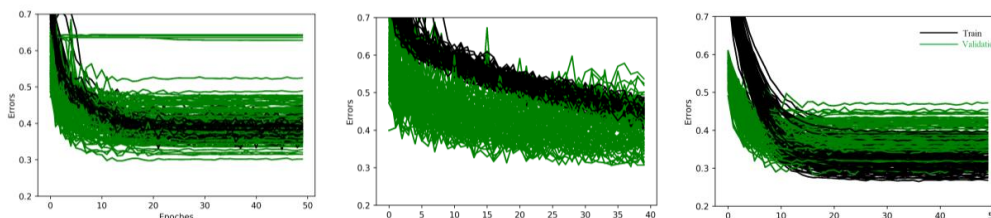
481 **Figure 15. Train and validation errors over epochs for an LSTM model showing overfitting after 40 epochs.**

482 **3.3.1 Learning curves and F1 scores**

483 Line plots of the loss (i.e., learning curves), which are loss over each epoch, are widely used to examine the  
484 performance of models in machine learning. Furthermore, line plots clearly indicate common learning problems, such  
485 as underfitting or overfitting. The learning curves for CNN, LSTM, and CN-LSTM models are presented in Fig. 16.  
486 The LSTM model starts to overfit at epoch 40, so an early stopping is conducted. CN-LSTM performs better than the  
487 other two models, as its training loss is the lowest and is lower than its validation loss. Histograms of F1 scores (Fig.  
488 16 and Table 7) show that CN-LSTM outperforms the other two models since it results in the highest average and the  
489 lowest F1-scores for validation (0.82 and 0.75, respectively). Figure 16 shows that training error of CNN is lower than  
490 that of LSTM, which means that CNN trained better than LSTM model. However, it is not true for the validation error.  
491 The LSTM network is validated better than the CNN model since its average and minimum F1 scores for validation  
492 are better than the CNN model (by 1 % and 32 %, respectively), and also LSTM yielded no F1 scores below 0.74 (Fig.  
493 17 and Table 7). This reveals that LSTM is showing underfitting.

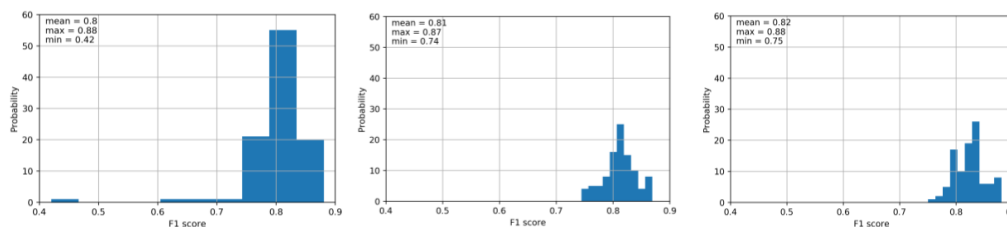
494 As shown in Fig. 16, training loss is higher than validation loss in some of the results. Some reasons are explaining  
495 that. Regularization reduces the validation and testing (i.e., evaluation) loss at the expense of increasing training loss.  
496 The regularization techniques such as noise layers are only applied during training, but not during evaluation resulting  
497 in more smooth and usually better functions in evaluation. There is no noise layer in CN-LSTM model that may caused  
498 a lower training error than validation error. However, other regularization methods such as L2 regularization are used  
499 in all the models, including the CN-LSTM model.

500 Furthermore, the other issue is that batch normalization uses the mean and variance of each batch in training, whereas,  
501 in evaluation, it uses the mean and variance of the whole training dataset. Plus, training loss is averaged over each  
502 epoch, while evaluation losses are calculated after each epoch once the current training epoch is completed. Hence,  
503 the training loss includes error calculations with fewer updates.



**Figure 16.** Train and validation errors over epochs for CNN (left), LSTM (middle), and CN-LSTM (right) models with 100 random train-validation splits.

504



**Figure 17.** Histograms of F1 scores of validation for CNN (left), LSTM (middle), and CN-LSTM (right) models with 100 random train-validation splits.

505

506 **Table 7.** F1 scores of validation for CNN, LSTM, and CN-LSTM models with 100 random train-validation splits.

Models	F1 score		
	mean	max	min
CNN	0.80	0.88	0.42
LSTM	0.81	0.87	0.74
CN-LSTM	0.82	0.88	0.75

507

### 508 3.3.2 Number of parameters and run time

509 The total number of parameters in CNN, LSTM, and CN-LSTM networks are 371586, 207874, and 664746,  
 510 respectively. The best performance has resulted from CN-LSTM with the highest number of parameters. Even though  
 511 the number of parameters for the LSTM model is less than CNN, the LSTM model shows better validation  
 512 performance. Furthermore, the number of parameters in the CN-LSTM model is much higher than the two other  
 513 models, but the computation time is not much higher. All three models take less than 24 hours to train with 100 shuffle  
 514 splits for training and validation. The models are run on a CPU with four cores, 3.4 GHz clock speed, and 12 GB  
 515 RAM.



### 516 3.4 Order of input variables

517 Although the order of input variables in the input file is important through using 2-D filters and 2-D max-pooling  
518 layers, there is no guideline for this order for multivariate TSC. In the benchmark, we randomly used this order from  
519 left to right: precipitation, minimum temperature, maximum temperature, net radiation, ATDD, AFDD, and snow  
520 depth. We randomly changed this order and applied the new order: snow depth, maximum temperature, precipitation,  
521 AFDD, net radiation, minimum temperature, and ATDD. Both models yielded the same average and minimum F1  
522 scores, whereas the maximum F1 score from the order in the benchmark model (0.88) is higher than that of the second-  
523 order (0.86). Therefore, it can be concluded that the order does not significantly impact the results.

### 524 3.5 Generalization

525 To examine the ability of the models to generalize to new unseen data, we randomly set aside 10 % of data from  
526 training and validation. We trained a CNN, an LSTM, and a CN-LSTM model, then the trained parameters are saved,  
527 and finally, the well-trained parameters are utilized for testing. The test dataset is almost a balanced dataset with 101  
528 samples with the size of (16, 7), including 48 jams and 53 no jams.

529 The results of the test models show that CN-LSTM models represent the best F1 score of 0.91 (Table 8). Tables 7 and  
530 8 show that although LSTM has slightly better validation performance, CNN works a little better in generalization by  
531 only 1 %. The better generalization of CNN can be because LSTM is a little underfitted as LSTM models are often  
532 harder to regularize, agreeing with previous studies (e.g., Devineau et al., 2018, June).

533 **Table 8. Test F1 scores for LSTM, CNN, and CNLSTM models.**

Models	F1 score
CNN	0.80
LSTM	0.79
CN-LSTM	0.91

534

### 535 3.6 Model comparison

536 Multiple combined classifiers can be considered for pattern recognition problems to reduce errors as different  
537 classifiers can cover internal weaknesses of each other (Parvin et al., 2011). The ensemble classifier may be less  
538 accurate than the most accurate classifier. However, the accuracy of the combined model is always higher than the  
539 average accuracy of individual models. Combining two models improved our results compared to convolution-only  
540 or LSTM-only networks in both training and generalization. It can be because the CN-LSTM model incorporates both  
541 the temporal dependency of each variable by using LSTM networks and the correlation between variables through  
542 CNN models.

543 The better generalization results from CNN compared to LSTM can be because of the ability of CNN to partially  
544 include both temporal dependency and the correlation between variables by using 1D and 2D filters, respectively,  
545 while LSTM is unable to incorporate the correlations between variables.



#### 546 **4 Conclusion**

547 This project is a part of a project called DAVE, which aims to develop a tool to provide regional ice jam watches and  
548 warnings, based on the integration of three aspects: the current conditions of the ice cover; hydrometeorological  
549 patterns associated with breakup ice jams; and channel predisposition to ice-jam formation. The outputs of the previous  
550 tasks will be used to develop an ice-jam monitoring and warning module and transfer the knowledge gained to end-  
551 users to manage the risk of ice jams better.

552 While most TSC research in deep learning is performed on 1D channels (Hatami et al., 2018, April), we propose deep  
553 learning frameworks for multivariate TSC for ice-jam prediction. The main finding from the comparison of results is  
554 that the CN-LSTM model is superior to the CNN-only and LSTM-only networks in both training and generalization  
555 accuracy, supporting the previous studies (e.g., Sainath et al., 2015). Though the LSTM network demonstrates quite  
556 good performance, the CNN model performed slightly better generalization, which agrees with previous studies (e.g.,  
557 Brunel et al., 2019).

558 To our best knowledge, this study is the first study introducing these deep learning models to the problem of ice-jam  
559 prediction. Even though our training data in supervised ice-jam prediction is small, the results reveal that deep learning  
560 techniques can give accurate results, which agrees with a previous study conducted by Ordóñez and Roggen (2016)  
561 in activity recognition. The excellent performance of CNN and CN-LSTM models may be partially due to the  
562 characteristic of CNN that decreases the total number of parameters which does training with limited training data  
563 easier (Gao et al., 2016, May) and including the correlation between involved variables. However, our models will be  
564 improved in the future by a larger dataset.

565 The developed models do not apply to freeze-up jams that occur in early winter and are based on different processes  
566 than breakup jams. We studied only break-up ice jams as usually they result in flooding and are more dangerous than  
567 freeze-up jams.

568 The hydro-meteorological variables are not the only drivers of ice-jam formation. The geomorphological indicators  
569 that control the formation of ice jams include the river slope, sinuosity, a barrier such as an island or a bridge,  
570 narrowing of the channel, and confluence of rivers. In the future, a geospatial model using deep learning will be  
571 developed to examine the impacts of these geospatial parameters on the ice-jam formation.

#### 572 **Author contribution**

573 Fatemehalsadat Madaeni designed and carried out the experiments under Kareem Chokmani and Saeid Homayouni  
574 supervision. Fatemehalsadat Madaeni developed the model code and performed the simulations using hydro-  
575 meteorological and ice-jam data provided and validated by Rachid Lhissou. Fatemehalsadat Madaeni wrote the bulk  
576 of the paper with conceptual edits from Kareem Chokmani and Saeid Homayouni. Yves Gauthier and Simon  
577 Tolszczuk-Leclerc helped in the refinement of the objectives and the revision of the methodological developments.



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