Convolutional Neural Network and Long Short-Term Memory Models for Ice-Jam Prediction

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10 Abstract. In cold regions, ice-jam events result in severe flooding due to a rapid rise in water levels upstream of the 11 jam. These floods threaten human safety and damage properties and infrastructures as the floods resulting from ice-12 jams are sudden. Hence, ice-jam prediction tools can give an early warning to increase response time and minimize 13 the possible corresponding damages. However, ice-jam prediction has always been a challenging problem as there is 14 no analytical method available for this purpose. Nonetheless, ice jams form when some hydro-meteorological 15 conditions happen, a few hours to a few days before the event. Ice-jam prediction problem can be considered as a 16 binary multivariate time-series classification. Deep learning techniques have been widely used for time-series 17 classification in many fields such as finance, engineering, weather forecasting, and medicine. In this research, we 18 successfully applied Convolutional Neural Network (CNN), Long Short-Term Memory (LSTM), and combined 19 Convolutional-Long Short-Term Memory (CNN-LSTM) networks for ice-jam prediction for 150 rivers in Quebec. 20 The hydro-meteorological variables (e.g., temperature, precipitation, and snow depth) along with the corresponding 21 jam or no-jam events are used as the inputs to the models. We hold out 10% of the data for testing. And we applied 22 100 re-shuffling and splitting iterations with 80 % of the remaining data for training and 20% for validation. The 23 results show that the CNN-LSTM model yields the best results in the validation and testing with F1 scores of 0.82 and 24 0.92, respectively. This demonstrates that CNN and LSTM models are complementary, and a combination of them

25 further improves classification.

26 1 Introduction

27 Predicting ice-jam events gives an early warning of possible flooding, but there is no analytical solution to predict 28 these events due to the complex interactions between involved hydro-meteorological variables (e.g., temperature, 29 precipitation, snow depth, and solar radiation). To date, a small number of empirical and statistical prediction methods 30 such as threshold methods, multi-regression models, logistic regression models, and discriminant function analysis 31 have been developed for ice jams (Barnes-Svarney and Montz, 1985; Mahabir et al., 2006; Massie et al., 2002; White, 32 2003; White and Daly, 2002, January; Zhao et al., 2012). However, these methods are site-specific with a high rate of 33 false-positive errors (White, 2003). The numerical models developed for ice-jam prediction (e.g., ICEJAM (Flato and 34 Gerard, 1986, cf.; Carson et al., 2011), RIVJAM (Beltaos, 1993), HEC-RAS (Brunner, 2002), ICESIM (Carson et al., 35 2001 and 2003), and RIVICE (Lindenschmidt, 2017)) show limitations in predicting ice-jam occurrence. This is 36 because mathematical formulations in these models are complex which need many parameters that are often 37 unavailable as they are challenging to measure in ice conditions. Hence, many simplifications corresponding to these

- parameters may degrade model accuracy (Shouyu & Honglan, 2005). A detailed overview of the previous models for
 ice-jam prediction based on hydro-meteorological data are presented in Madaeni et al. (2020).
- 40 Prediction of ice-jam occurrence can be considered as a binary multivariate time-series classification (TSC) problem
- 41 when the time series of various hydro-meteorological variables (explained later) can be used to classify jam or no jam
- 42 events. Time-series classification (particularly multivariate) has been widely used in various fields, including
- 43 biomedical engineering, clinical prediction, human activity recognition, weather forecasting, and finance. Multivariate
- 44 time-series provide more patterns and improve classification performance compared to univariate time-series (Zheng
- 45 et al., 2016). Time-series classification is one of the most challenging problems in data mining and machine learning.
- 46 Most existing TSC methods are feature-based, distance-based, or ensemble methods (Cui et al., 2016). Feature
- 47 extraction is challenging due to the difficulty of handcrafting useful features to capture intrinsic characteristics from
- 48 time-series data (Karim et al., 2019; Zheng et al., 2014, June). Hence, distance-based methods work better in TSC
- 49 (Zheng et al., 2014, June). Among the hundreds of methods developed for TSC, the leading classifier with the best
- 50 performance was ensemble nearest neighbor with dynamic time warping (DTW) for many years (Fawaz et al., 2019,
- 51 July; Karim et al., 2019).
- 52 In the k-nearest neighbors (KNN) classifier, the given test instance is classified by a majority vote of its k closest
- 53 neighbors in the training data. The KNN classifier needs all the data to make a prediction which requires high memory.
- 54 Hence, it is computationally expensive and could be slow if the database is large, and sensitive to irrelevant features
- 55 and the scale of the data. Furthermore, the number of neighbors to include in the algorithm should be carefully selected.
- 56 The KNN classifier is very challenging to be used for multivariate TSC. The dynamic time warping is a more robust
- 57 alternative for Euclidean distance (the most widely used time-series distance measure) to measure the similarity
- 58 between two given time series by searching for an optimal alignment (minimum distance) between them (Zheng et
- 59 al., 2016). However, the combined KNN with DTW is time-consuming and inefficient for long multivariate time-
- 60 series (Lin et al., 2012; Zheng et al., 2014, June). The traditional classification and classic data mining algorithms
- 61 developed for TSC have high computational complexity or low prediction accuracy. This is due to the size and inherent
- 62 complexity of time series, seasonality, noise, and feature correlation (Lin et al., 2012).
- 63 There are some machine learning methods available for TSC such as KNN and support vector machine (SVM).
- However, the focus of this research is on the deep learning models that have greatly impacted sequence classification
 problems and they can also be used for multivariate TSC with good performance. Deep learning methods are able to
- 66 consider two-dimensionality in multivariate time-series and their deeper architecture could further improve the
- 67 classification especially for complex problems, which is why their results are more accurate and robust than other
- 68 methods (Wu et al., 2018a, April). However, they are more time consuming and difficult to interpret.
- 69 Deep learning is a type of neural networks that uses multiple layers where nonlinear transformation is used to extract
- 70 higher-level features from the input data. Although deep learning in recent years showed promising performance in
- 71 various fields such as image and speech recognition, document classification, and natural language processing, only a
- few studies employed deep learning for TSC (Gu et al., 2018; Fawaz et al., 2019, July). Various studies show that
- 73 deep neural networks significantly outperform the ensemble nearest neighbor with DTW (Fawaz et al., 2019, July).
- 74 The main benefit of deep learning networks is automatic feature-extraction, which reduces the need for expert

- knowledge of the field and removes engineering bias in the classification task (Fawaz et al., 2019) as the probabilistic
- 76 decision (e.g., classification) is taken by the network.
- 77 The most widely used deep neural networks for TSC are Multi-Layer Perceptron (MLP; i.e., fully connected deep
- 78 neural networks), Convolutional Neural Networks (CNNs), and Long Short-Term Memory (LSTM). The application
- 79 of CNNs for TSC has recently become more and more popular, and different types of CNN are being developed with
- 80 superior accuracy for this purpose (e.g., Cui et al., 2016). Zheng et al. (2014, June) and Zheng et al. (2016) introduce
- 81 a Multi-Channels Deep Convolutional Neural Network (MC-DCNN) for multivariate TSC, where each variable (i.e.,
- 82 univariate time series) is trained individually to extract features and finally concatenated using an MLP to perform
- 83 classification (Fig. 1). They showed that their model achieves a state-of-the-art performance both in efficiency and
- 84 accuracy on a challenging dataset. The drawback of their model and similar architectures (e.g., Devineau et al., 2018,
- 85 May) is that they do not capture the correlation between variables as the feature extraction is carried out separately for
- 86 each variable.



Figure 1. A 2-stages MC-DCNN architecture for activity classification. This architecture consists of three channels input, two filter layers, two pooling layers, and two fully-connected layers (after Zheng et al., 2014, June).

- 90 Brunel et al. (2019) present CNNs adapted for TSC in cosmology using 1D filters to extract features from each channel
- 91 over time and a 1D convolution in depth to capture the correlation between the channels. They compared the results
- 92 from LSTMs with CNNs, which shows that CNNs give better results than LSTMs. Nevertheless, both deep learning
- 93 approaches are very promising.
- 94 The combination of CNNs and LSTM units has already yielded state-of-the-art results in problems requiring
- 95 classification of temporal information such as human activity recognition (Li et al., 2017; Mutegeki and Han, 2020,

96 February), text classification (Luan and Lin, 2019; March, She and Zhang, 2018, December; Umer et al., 2020), 97 video classification (Lu et al., 2018 and Wu et al., 2015, October), sentiment analysis (Ombabi et al., 2020; Sosa, 98 2017; Wang et al., 2016, August; Wang et al., 2019), typhoon formation forecasting (Chen et al., 2019), and 99 arrhythmia diagnosis (Oh et al., 2018). In this architecture, convolutional operations capture features and LSTMs 100 capture time dependencies on extracted features. Ordóñez and Roggen (2016) propose a deep convolutional LSTM 101 model (DeepConvLSTM) for activity recognition (Fig. 2). Their results are compared to the results from standard 102 feedforward units showing that DeepConvLSTM reaches a higher F1 score and better decision boundaries for 103 classification. Furthermore, they noticed that the LSTM model gives promising results with relatively small datasets. 104 Furthermore, LSTMs present a better performance in capturing longer temporal dynamics, whereas the convolution 105 filters can only capture the temporal dependencies dynamics within the length of the filter.



106

107 Figure 2. The architecture of the DeepConvLSTM framework for activity recognition (after Ordóñez and Roggen, 2016).

This project is a part of a project called DAVE, which aims to develop a tool to provide regional ice jam watches and warnings, based on the integration of three aspects: the current conditions of the ice cover; hydro-meteorological patterns associated with breakup ice jams; and channel predisposition to ice-jam formation. The outputs of the previous tasks will be used to develop an ice-jam monitoring and warning module and transfer the knowledge gained to endusers to better manage the risk of ice jams.

113 The objective of this research is to develop deep learning models to predict breakup ice-jam events to be used as an 114 early warning system of possible flooding. While most TSC research in deep learning is performed on 1D channels 115 (Hatami et al., 2018, April), we propose deep learning frameworks for multivariate TSC for ice-jam prediction. 116 Through our comprehensive literature review, we noticed that CNN (e.g., Brunel et al., 2019; Cui et al., 2016; 117 Devineau et al., 2018, June; Kashiparekh, 2019, July; Nosratabadi et al., 2020; Yan et al., 2020; Yang et al., 2015, 118 June; Yi et al., 2017; Zheng et al., 2016), LSTM (e.g., Fischer and Krauss, 2018; Lipton et al., 2015; Nosratabadi et 119 al., 2020; Torres et al., 2021), and a combined CNN-LSTM (e.g., Karim et al., 2017; Livieris et al., 2020; Ordóñez 120 and Roggen, 2016; Sainath et al., 2015, April; Xingjian et al., 2015) have been widely used for TSC. There are 121 numerous applications of CNN, LSTM, and their hybrid versions applied in hydrology (Althoff et al., 2021; Apaydin 122 et al., 2020; Barzegar et al., 2021, 2020; Kratzert et al., 2018; Wunsch et al., 2020; Zhang et al., 2018). Although deep 123 learning methods seem to be promising to address the requirements of ice-jam predictions, none of these methods yet

124 have been explored for ice jam prediction.

Hence, we developed three deep learning models; a CNN, an LSTM, and a combined CNN-LSTM for ice-jam

126 predictions and compared the results. The previous studies show that these models show good capabilities in capturing

127 features and the correlation between features (through convolution units) and time dependencies (through memory

128 units) that will be later used for TSC. The combined CNN-LSTM can reduce errors by compensating for the internal

- 129 weaknesses of each model. In the CNN-LSTM model, CNNs capture features, then the LSTMs give the time
- 130 dependencies on the captured features.
- 131 Furthermore, we also developed some machine learning methods as simpler methods for ice-jam prediction. And their
- results are compared with results from the developed deep learning models.

133 2 Materials and Methods

134 **2.1 Data and study area**

135 It is known that specific hydro-meteorological conditions lead to ice-jam occurrence (Turcotte and Morse, 2015, 136 August and White, 2003). For instance, breakup ice jams occur when a period of intense cold is followed by a rapid 137 peak discharge resulting from spring rainfall and snowmelt runoff (Massie et al., 2002). The period of intense cold 138 can be represented by the changes in Accumulated Freezing Degree Days (AFDD). The sudden spring runoff increase 139 is not often available at the jam location and can be represented by liquid precipitation and snow depth some days 140 before ice-jam occurrence (Zhao et al., 2012). Prowse and Bonsal (2004) and Prowse et al. (2007) evaluate various 141 hydroclimatic explanations for river ice freeze-up and breakup, concluding that shortwave radiation is the most critical 142 factor influencing the mechanical strength of ice and consequently the possibility of breakup ice jams to occur. 143 Turcotte and Morse (2015, August) explain that Accumulated Thawing Degree Day (ATDD), an indicator of warming 144 periods, partially covers the effect of shortwave radiation. In the previous studies of ice-jam and breakup predictions, 145 discharge and changes in discharge, water level and changes in water level, AFDD, ATDD, precipitation, solar 146 radiation, heat budget, and snowmelt or snowpack are the most readily used variables (Madaeni et al., 2020). 147 The inputs we used in this study are historical ice-jam or no ice-jam occurrence (Fig. 3) as well as hydro-

- 148 meteorological variables including liquid precipitation (mm), min and max temperature (°C), AFDD (from August 149 1st; °C), ATDD (from January 1st; °C), snow depth (cm) and net radiation (W m⁻²) in 150 rivers in Quebec. The net 150 solar radiation, the total energy available to influence the climate, is calculated as the difference between incoming
- 151 and outgoing energy. If the median temperature is greater than 1, the precipitation is considered liquid precipitation.
- 152 The statistics of hydro-meteorological data used in the models are presented in Table 1. The source, time period, and
- 153 spatial resolution of the input variables are shown in Table 2.
- 154 Ice-jam database is provided by the Quebec Ministry of Public Security (MSPQ; Données Québec, 2021) for 150
- rivers in Quebec, mainly in the St. Lawrence basin. The database comes from the digital or paper event reports by
- 156 local authorities under the jurisdiction of the MSPQ from 1985 to 2014. Moreover, some other data of this database
- 157 are provided by the field observations from the Vigilance / Flood application from 2013 to 2019. It contains 995
- 158 recorded jam events that are not validated and contain many inaccuracies, mainly in the toponymy of the rivers,
- 159 location, dating, and the redundancy of jam events.

- 160 The names of the watercourse of several recorded jams are not given or completely wrong or affected by a typo or an
- 161 abbreviation. The toponymy of the rivers was corrected using the National Hydrographic Network (NHN; National
- 162 Hydrographic Network Natural Resources Canada (NRCan)), the Geobase of the Quebec hydrographic network
- 163 (National Hydro Network NHN GeoBase Series Natural Resources Canada), and the Toporama Web map service
- 164 (The Atlas of Canada Toporama Natural Resources Canada) of the Sector of Earth Sciences.
- 165 Several ice jams are placed on the banks at a small distance (less than 20 m) from the polygon of the river. In this
- 166 case, the location of the ice jam is moved inside the river polygon. In other cases, ice-jam point is posed further on the
- 167 flooded shore at a distance between 20 and 200 m. This has been corrected based on images with very high spatial
- 168 resolution, the sinuosity and the narrowing of the river, the history of ice jams at the site in question, and the press
- 169 archives. In addition, some ice jams were placed too far from the mentioned river due to wrong recorded coordinates
- 170 in the database. A single-digit correction in longitude or latitude returned the jam to its exact location. There are certain
- 171 cases where the date of jam formation is verified by searching the press archives, notably when the date of formation
- 172 is missing or several jams with the same dates and close locations in a section of a river are present.
- 173 The ice jam database contains many duplicates. This redundancy can be due to merging two data sources, the double
- 174 entry during ice-jam monitoring, or recording an ice jam for several days. The duplicates are removed from the
- 175 database. The corrected ice-jam database contains 850 jams for 150 rivers, mainly in southern Quebec (Fig. 3). The
- 176 ice jams formed in November and December (freeze-up jams) are removed to only include breakup jams (from January
- 177 15th) in the modelling as these two types of jams are formed due to different processes. The final breakup ice-jam
- 178 database that used in this study includes 504 jam events.



180 Figure 3. Study area and historic ice-jam locations recorded in Quebec from 1985-2017.

Statistics	Liquid P (mm)	Tmin (°C)	Tmax (°C)	Net radiation (W m- 2)	ATDD (°C)	AFDD (°C)	Snowdepth (cm)
min	0.00	-40.00	-25.97	-67.77	0.00	-2109.33	0.00
max	50.87	12.05	27.48	222.69	280.82	-35.41	121.86
average	1.04	-9.41	0.98	59.75	8.83	-898.48	15.99

181 Table 1. Statistics of hydro-meteorological variables used in the models.

-7.73

182 183 median

Table 2. Source, duration, and spatial resolution of hydro-meteorological data used in the models.

1.68

Data	Source	Duration	Spatial
			resolution
Min and Max temperature*	Daily Surface Weather Data (Daymet; Thornton et al., 2020)	1979-2019	1 km
Liquid precipitation	Canadian Precipitation Analysis (CaPA; Mahfouf et al.,	2002-2019	10-15km
	2007)		
Liquid precipitation	North American Regional Reanalysis (NARR; Mesinger et	1979-2001	30 km
	al., 2006)		
Infrared radiation emitted by	North American Regional Reanalysis (NARR)	1979-2019	30 km
the atmosphere			
Infrared radiation emitted	North American Regional Reanalysis (NARR)	1979-2019	30 km
from the surface			
Snow depth	North American Regional Reanalysis (NARR)	1979-2019	30 km

59.41

1.27

-890.74

11.50

184 * The average was used to derive the AFDD and the ATDD.

0.00

186 2.2 Machine learning models for TSC

- 187 The common machine learning techniques that have been used for TSC are SVM (Rodríguez and Alonso, 2004; Xing
- and Keogh, 2010), KNN (Li et al., 2013; Xing and Keogh, 2010), decision tree (DT; Brunello et al., 2019; Jović et al.,
- 189 2012, August), and multilayer perceptron (MLP; del Campo et al., 2021; Nanopoulos et al., 2001). For more
- 190 information about these machine learning models refer to the mentioned literature above. We do not explain these
- 191 models and their applications in TSC, as they are not the focus of this study.
- 192 We developed the mentioned machine learning methods and compared their results with the results of deep learning
- 193 models. After some trials and errors, the parameters that are changed from the default values for each machine learning
- 194 model are as follows. We developed an SVM with a polynomial kernel with a degree of 5 that can distinguish curved
- 195 or nonlinear input space. The KNN is used with 3 neighbors used for classification. The decision tree model is applied
- 196 with all the default values. The shallow MLP is used with 'lbfgs' solver (which can converge faster and perform better
- 197 for small datasets), alpha of 1e-5, and 3 layers with 7 neurons in each layer.

198 **2.3 Deep learning models for TSC**

- 199 The most common and popular deep neural networks for TSC are MLPs, CNNs, and LSTMs (Brownlee, 2018; and
- 200 Torres et al., 2021). Despite their power, however, MLP has limitations that each input (i.e., time-series element) and
- 201 output are treated independently, which means that the temporal or space information is lost (Lipton et al., 2015).
- 202 Hence, an MLP needs some temporal information in the input data to model sequential data such as time series
- 203 (Ordóñez and Roggen, 2016). In this regard, Recurrent Neural Networks (RNNs) are specifically adapted to sequence
- 204 data through the direct connections between individual layers (Jozefowicz et al., 2015). Recurrent Neural Networks
- 205 perform the same repeating function with a straightforward structure, e.g., a single tanh (hyperbolic tangent) layer, for
- 206 every input of data (xt), while all the inputs are related to each other with their hidden internal state, which allows it
- 207 to learn the temporal dynamics of sequential data (Fig. 4).



208

Figure 4. An RNN with a single tanh layer, where A is a chunk of the neural network, x is input data, and h is output data.

210 Recurrent Neural Networks were rarely used in TSC due to their significant problems. Recurrent Neural Networks

- 211 mainly predict output for each time-series element, they are sensitive to the first examples seen, and it is also
- 212 challenging to capture long-term dependencies due to vanishing gradients, exploding gradients, and their complex
- dynamics (Devineau et al., 2018, June; Fawaz et al., 2019).
- 214 Long short-term memory RNNs are developed to improve the performance of RNNs by integrating a memory to
- 215 model long-term dependencies in time-series problems (Brunel et al., 2019; Karim et al., 2019). Long short-term

- 216 memory networks do not have the problem of exploding gradients. The LSTMs have four interacting neural network
- 217 layers in a very special way (Fig. 5). An LSTM has three sigmoid (σ) layers to control how much of each component
- should be let through by outputting numbers between zero and one. The input to an LSTM goes through three gates
- 219 ("forget", "input", and "output gates") that control the operation performed on each LSTM block (Ordóñez and
- 220 Roggen, 2016). The first step is the "forget gate" layer that gets the output of the previous block (ht-1), the input for
- the current block (Xt), and the memory of the previous block (Ct-1) and gives a number between 0 and 1 for each
- number in the cell state (Ct-1; Olah, 2015). The second step is called the "input gate" with two parts, a sigmoid layer
- that decides which values to be updated and a tanh layer that creates new candidate values for the cell state. These two
- new and old memories will then be combined and control how much the new memory should influence the old
- memory. The last step (output gate) gives the output by applying a sigmoid layer deciding how much new cell memory
- 226 goes to output, and multiply it by tanh applied to the cell state (giving values between -1 and 1).



228 Figure 5. Structure of LSTM block with four interacting layers.

Recently, convolutional neural networks challenged the assumption that RNNs (e.g., LSTMs) have the best performance when working with sequences. The CNNs show state-of-the-art performance in sequential data such as speech recognition and sentence classification, similar to TSC (Fawaz et al., 2019).

The CNNs are the most widely used deep learning methods in TSC problems (Fawaz et al., 2019). They learn spatial features from raw input time series using filters (Fawaz et al., 2019). The CNNs are robust and need a relatively small amount of training time comparing with RNNs or MLPs. They work best for extracting local information and reducing the complexity of the model.

- A CNN is a kind of neural network with at least one convolutional (or filter) layer. A CNN usually involves several
- 237 convolutional layers, activation functions, and pooling layers for feature extraction following by dense layers (or
- MLP) as a classifier (Devineau et al., 2018, June). The reason to use a sequence of filters is to learn various features
- from time series for TSC. A convolutional layer consists of a set of learnable filters that compute dot products between
- 240 local regions in the input and corresponding weights. With high-dimensional inputs, it is impractical to connect
- 241 neurons to all neurons in the previous layer. Therefore, each neuron in CNNs is connected to only a local region of
- the input, namely the receptive field, which equals the filter size (Fig. 6). This feature reduces the number of

- 243 parameters by limiting the number of connections between neurons in different layers. The input is first convolved
- 244 with a learned filter, and then an element-wise nonlinear activation function is applied to the convolved results (Gu et
- 245 al., 2018). The pooling layer performs a downsampling operation such as maximum or average, reducing the spatial
- 246 dimension. One of the most powerful features of CNNs is called weight or parameter sharing, where all neurons share
- filters (weights) in a particular feature map (Fawaz et al., 2019) to reduce the number of parameters.



249 Figure 6. A convolution layer structure including two sets of filters.

248

251 2.4 Model libraries

In an Anaconda (Analytics, C., 2016) environment, Python is implemented to develop CNN, LSTM, and CNN-LSTM
networks for TSC. To build and train networks, the networks are implemented in Theano (Bergstra et al., 2010, June)
using the Lasagne (Dieleman et al., 2015) library. The other core libraries used for importing, preprocessing, training
data, and visualization of results are Pandas (Reback et al., 2020), NumPy (Harris et al., 2020), Scikit-Learn
(Pedregosa et al., 2011), and Matplotlib.PyLab (Hunter, J. D., 2007). Spyder (Raybaut, 2009) package of Anaconda

is utilized as an interface, or the command window can be used without any interface.

258 2.5 Preprocessing

- 259 The data is comprised of variables with varying scales, and the machine learning algorithms can benefit from rescaling
- the variables to all have the same scale. Scikit-learn (Pedregosa et al., 2011) is a free library for machine learning in
- 261 Python that can be used to preprocess data. We examined Scikit-learn MinMaxScaler (scaling each variable between
- 262 0 and 1), Normalizer (scaling individual samples to the unit norm), and StandardScaler (transforming to zero mean
- and unit variance separately for each feature). The results show that MinMaxScaler (Eq. (1)) leads to the most accurate
- results. The scaling of validation data is done with min and max from train data.

$$265 \qquad X_{\text{scaled}} = \frac{X - X_{\text{min}}}{X_{\text{max}} - X_{\text{min}}} \tag{1}$$

For each jam or no jam event, we used 15 days of information before the event to predict the event on the 16th day. We generate a balanced dataset with the same number of jam and no-jam events (1008 small sequences totally), preventing the model from becoming biased to jam or no-jam events. The hydro-meteorological data related to nojam events are constructed by extracting data from the reaches of no-jam records. To examine models' generalization,

- we hold out 10% of data for testing and 80 % and 20 % of remaining data for training and validation, respectively.
- 271 We used ShuffleSplit subroutine from the Scikit-learn library, where the database was randomly sampled during each
- 272 re-shuffling and splitting iteration to generate training and validation sets. We applied 100 re-shuffling and splitting
- iterations for training and validation. There are 726, 181, and 101 small sequences with the size of (16, 7), 16 days of
- 274 data for the seven variables; for training, validation, and test, respectively.

275 **2.6** Training

Training a deep neural network with an excellent generalization to new unseen inputs is challenging. As a benchmark, a CNN model with the parameters and layers similar to previous studies (e.g., Ordóñez and Roggen, 2016) is developed. The model shows underfitting or overfitting with various architectures and parameters. To overcome underfitting, deeper models and more nodes in each layer are beneficial; however, overfitting is more challenging to overcome. Ice-jam dataset for Quebec contains 1008 balanced sequence instances (with a length of 16), which is small for deep learning. The deep learning models often tend to overfit small datasets by memorizing inputs rather than training, as a small dataset may not appropriately describe the relationship between input and output spaces.

283 **2.6.1** Overcome overfitting

- There are various methods to tackle the problem of overfitting, including acquiring more data, data augmentation (e.g., cropping, rotating, and noise injection), dropout (Srivastava et al., 2014), early stopping, batch normalization (Ioffe and Szegedy, 2015, June), and regularization. Acquiring more data is not possible with ice-jam records. We added the Gaussian noise layer (from the Lasagne library), where the noise values are Gaussian-distributed with zero-mean and a standard deviation of 0.1 to the input. The noise layers applied to the CNN and LSTM models significantly overcome the overfitting problem through data augmentation. However, the performance of the CNN-LSTM model dramatically deteriorates, including a noise layer (Fig. 7). Adding a noise layer to other layers does not improve any of the
- 291 developed models for ice-jam prediction.

292

293 Figure 7. Train and validation errors over epochs for CNN-LSTM model with a noise layer.

Early stopping is another efficient method that halts the training procedure where further training would decrease training loss, while validation loss starts to increase. Neural networks solve an optimization problem that requires a loss function to calculate the model error. The loss function is similar to an objective function for process-based hydrological models. Among the developed models, only LSTM needs early stopping at 40 epoch (Fig. 8). More

- 298 explanations about the other methods that are used in this study to overcome overfitting (e.g., batch normalization,
- and L2 regularization) can be found in the Appendix.

301 Figure 8. Train and validation errors over epochs for an LSTM model showing overfitting after 40 epochs.

302 **2.6.2 Model Hyperparameters**

303 Finding hyperparameter values in deep learning has been challenging due to the complex architecture of deep learning 304 models and a large number of parameters (Garbin et al., 2020). To find the best model architecture, we study the 305 performance of models with different layers and parameters such as number of noise, batch normalization, 306 convolutional, pooling, LSTM, dropout, and dense layers, as well as different pooling sizes and strides, different batch 307 sizes, various scaling of data (standardization and normalization), various filter sizes, number of units in LSTM and 308 dense layers, the type of the activation functions, regularization and learning rates, weight decay and number of filters 309 in convolutional layers. We also applied various combinations of these layers and parameters. The hyperparameters 310 are optimized through manual trial and error searches as grid search experiments suffer from poor coverage in 311 dimensions (Bergstra and Bengio, 2012) and manual experiments are much easier and more interpretable in 312 investigating the effect of one hyperparameter of interest. The optimized hyperparameters are presented in Table 3. 313 The most important parameters of the models are explained below and for more information about other parameters 314 readers are referred to the Appendix.

315 Table 3. Common values and selected values for different parameters of the models.

Parameter	Common values	Selected value
Mini-batch size	16, 32, 64	16
Number of convolution filters	32, 64, 128	128
Filter size	3, 5, 7	(5,1) and (5,3)
Number of LSTM units	32, 64, 128	128
Number of dense layer units	16, 32, 128, 256	32
Momentum in SGD	0.5, 0.99, 0.9	0.9

317 2.6.2.1 Number of layers

- 318 The depth is related to the sequence length (Devineau et al., 2018, May), as deeper networks need more data to provide
- 319 better generalization (Fawaz et al., 2019, July). In the previous studies of CNNs, there are usually one, two, or three
- 320 convolution stages (Zheng et al., 2014, June). We tried different numbers of CNN, LSTM, and dense layers and
- 321 selected three, two, and two such layers, respectively, as the sequence length in this study is small (16), and we could
- 322 not improve the model performance by merely adding more depth.

323 2.6.2.2 Number and size of convolution filters

- 324 Data with more classes need more filters and longer time series need longer filters to capture longer patterns and 325 consequently to produce accurate results (Fawaz et al., 2019, July). However, longer filters significantly increase the
- 326 number of parameters and potential for overfitting small datasets, while a small filter size risks poor performance. We
- 327 finally selected two convolutional layers with 1-D filters of (5, 1) and stride of (1, 1) to capture temporal variation for
- 328 each variable separately. Furthermore, one convolutional layer with 2-D filters of size (5, 3) and stride of (1, 1) is then
- 329 used to capture the correlation between variables via depth-wise convolution of input time-series. A big stride might
- 330
- cause the model to miss valuable data used in predicting and smoothing out the noise in the time series. The layers in
- 331 CNNs have a bias for each channel, sharing across all positions in each channel.

332 2.6.2.4 Adaptive learning rates

333 The adaptive learning rate decreases the learning rate and consequently weights over each epoch. We tried different 334 base learning and decay rates for each model and found that the learning rate significantly impacts the model 335 performance. Finally, we chose a base learning rate of 0.1, 0.01, and 0.001 for LSTM, CNN, and CNN-LSTM,

336 respectively. A decay rate of 0.8 was used for CNN and CNN-LSTM, while for the LSTM model, this rate was 0.95.

337 Table 4 shows the adaptive learning rates for CNN, LSTM, and CNN-LSTM calculated using Eq. (2) for each epoch.

338 adaptive learning rate = base learning rate \times decay^{epoch} (2)

339 The experiments show that the learning rate is the most critical parameter influencing the model performance. A small 340 learning rate can cause the loss function to get stuck in local minima, and a large learning rate can result in oscillations

- 341 around global minima without reaching it.
- 342 Our CNN-LSTM model is deeper than the other two models, and deeper models are more prone to a vanishing gradient 343 problem. To overcome the vanishing gradients, it is recommended that lower learning rates, e.g., lower than 1e-4, be
- 344 used. Interestingly, we found that our CNN-LSTM model works better with lower learning rates than the other two
- 345 models.
- 346

347 Table 4. The adaptive learning rate for 50 epochs.

	Learning rate			
Epochs	CNN	CNN- LSTM	LSTM	
1	0.008	8.00E-04	0.095	

2	0.006	6.40E-04	0.09
3	0.005	5.12E-04	0.086
4	0.004	4.10E-04	0.081
40	1.30E-06	1.33E-07	0.013
			-
50	1.40E-07	1.43E-08	-

349

363

350 2.6.5 Model evaluation

тр

351 The network on the validation set is evaluated after each epoch during training to monitor the training progress. During

352 validation, all non-deterministic layers are switched to deterministic. For instance, noise layers are disabled, and the 353 update step of the parameters is not performed.

354 The classification accuracy cannot appropriately represent the model performance for unbalanced datasets, as the

355 model can show a high accuracy by biasing towards the majority class in the dataset (Ordóñez and Roggen, 2016).

356 While we built a balanced dataset (with the same number of jam and no jam events), randomly selecting test data and

357 shuffling the inputs, and splitting data into train and validation sets can result in a slightly unbalanced dataset. In our

358 case, the number of jams and no jams for train and validation and test sets is presented in Table 5. Therefore, the F1

359 score (Eq. (3)), which considers each class equally important, is used to measure the accuracy of binary classification.

360 The F1 score, as a weighted average of the precision (Eq. (4)) and recall (Eq. (5)), has the best and worst scores of 1

361 and 0, respectively. In Eqs. 7 and 8, TP, FP, and FN are true positive, false positive, and false negative, respectively.

362 Table 5. The number of jam and no jam events in train and validation and test datasets.

	Train and validation	Test
Jam	456	48
No jam	451	53
$F1 = 2 \times \frac{1}{2}$	precision×reco precision+reco	all all

$$364 \quad Precision = \frac{TP}{TP + FP} \tag{4}$$

$$365 \quad Recall = \frac{TP}{TP + FN} \tag{5}$$

366 Although the model accuracy is usually used to examine the performance of deep learning models, the model size

367 (i.e., number of parameters) provides a second metric, which represents required memory and calculations, to be 368 compared among models with the same accuracy (Garbin et al., 2020).

369 After training the model, the well-trained network parameters are saved to a file and are later used for testing the

370 network generalization using a test dataset, which is not seen during training and validation.

371 2.7 Architecture of models

- 372 The architectures of CNN, LSTM, and CNN-LSTM models that are finally selected are presented in Figs. 9, 10, and
- 373 11, respectively. The layers, their output shapes, and their number of parameters are presented in Tables 6, 7, and 8
- 374 for CNN, LSTM, and CNN-LSTM models, respectively.
- 375 The CNN models often include pooling layers to reduce data complexity and dimensionality. However, it is not always
- necessary that every convolutional layer is followed by a pooling layer in the time-series domain (Ordóñez and
 Roggen, 2016). For instance, Fawaz et al. (2019, July) do not apply any pooling layers in their models for TSC. We
- Roggen, 2016). For instance, Fawaz et al. (2019, July) do not apply any pooling layers in their models for TSC. We tried max-pooling layers after different convolutional layers in CNN and CNN-LSTM networks and found that a
- 378 tried max-pooling layers after different convolutional layers in CNN and CNN-LSTM networks and found that a 379 pooling layer following only the last convolutional layer improves the performance of both models. This can be due
- pooling layer following only the last convolutional layer improves the performance of both models. This can be due to subsampling the time series and using time series with a length of 16 that reduces the need for reducing
- 381 dimensionality.

384 Figure 9. The architecture of the CNN model for ice-jam prediction (adapted after Ordóñez and Roggen, 2016).

387

388 Figure 11. The architecture of the CNN-LSTM model for ice-jam prediction (adapted after Ordóñez and Roggen, 2016).

389 Table 6. The layers, their output shapes, and their number of parameters for the CNN model.

Layers	Output shape	Number of parameters	
Input	(16, 1, 16, 7)	0	

GaussianNoise	(16, 1, 16, 7)	0
Conv2D	(16, 128, 16, 7)	640
BatchNorm	(16, 128, 16, 7)	512
Nonlinearity	(16, 128, 16, 7)	0
Conv2D	(16, 128, 16, 7)	81920
BatchNorm	(16, 128, 16, 7)	512
Nonlinearity	(16, 128, 16, 7)	0
Conv2D	(16, 128, 16, 7)	245888
MaxPool2D	(16, 128, 5, 2)	0
Dense	(16, 32)	40992
Dense	(16, 32)	1056
Softmax	(16, 2)	66

Table 7. The layers, their output shapes, and their number of parameters for the LSTM model.

Layers	Output shape	Number of parameters
Input	(16, 1, 16, 7)	0
GaussianNoise	(16, 1, 16, 7)	0
Dimshuffle	(16, 16, 1, 7)	0
BatchNorm	(16, 16, 1, 7)	64
LSTM	(16, 16, 128)	70272
BatchNorm	(16, 16, 128)	64
Nonlinearity	(16, 16, 128)	0
LSTM	(16, 16, 128)	132224
Reshape	(256, 128)	0
Dense	(256, 32)	4128
Dense	(256, 32)	1056
Softmax	(256, 2)	66
Reshape	(16, 16, 2)	0
Slice	(16, 2)	0

Table 8. The layers, their output shapes, and their number of parameters for the CNN-LSTM model.

Layers	Output shape	Number of parameters
Input	(16, 1, 16, 7)	0
Conv2D	(16, 128, 16, 7)	640
BatchNorm	(16, 128, 16, 7)	512
Nonlinearity	(16, 128, 16, 7)	0
Conv2D	(16, 128, 16, 7)	81920
BatchNorm	(16, 128, 16, 7)	512
Nonlinearity	(16, 128, 16, 7)	0
Conv2D	(16, 128, 16, 7)	245888
MaxPool2D	(16, 128, 5, 2)	0

Dimshuffle	(16, 5, 128, 2)	0
BatchNorm	(16, 5, 128, 2)	20
LSTM	(16, 5, 128)	197760
BatchNorm	(16, 5, 128)	20
Nonlinearity	(16, 5, 128)	0
LSTM	(16, 5, 128)	132224
Reshape	(80, 128)	0
Dense	(80, 32)	4128
Dense	(80, 32)	1056
Softmax	(80, 2)	66
Reshape	(16, 5, 2)	0
Slice	(16, 2)	0

395 3 Results and Discussion

396 3.1 Weight initialization

397 Among the various types of methods available in Lasagne for weight initialization, the GLOROT uniform (i.e., Xavier;

398 Glorot and Bengio, 2010, March) and He initializations (He et al., 2015), the most popular initialization techniques,

399 are used to set the initial random weights in convolutional layers. The results reveal that these methods yield almost

- 400 the same F1 scores. However, the histograms of F1 scores reveal that GLOROT uniform yields slightly better results
- 401 (Fig. 12).

402

403 Figure 12. Histograms of F1 score for CNN using He (left) and GLOROT uniform (right) weight initialization with 100 random train-validation splits.

405 **3.2 Model evaluation**

406 **3.2.1 Learning curves and F1 scores**

407 Line plots of the loss (i.e., learning curves), which are loss over each epoch, are widely used to examine the 408 performance of models in machine learning. Furthermore, line plots clearly indicate common learning problems, such 409 as underfitting or overfitting. The learning curves for CNN, LSTM, and CNN-LSTM models are presented in Fig. 13.

- 410 The LSTM model starts to overfit at epoch 40, so an early stopping is conducted. CNN-LSTM performs better than
- 411 the other two models, as its training loss is the lowest and is lower than its validation loss. Histograms of F1 scores
- 412 (Fig. 14 and Table 9) show that CNN-LSTM outperforms the other two models since it results in the highest average
- 413 and the highest minimum F1-scores for validation (0.82 and 0.75, respectively). Figure 13 shows that the training
- 414 error of CNN is lower than that of LSTM, which means that CNN trained better than LSTM model. However, it is not
- 415 true for the validation error. The reason that the validation error is less than the training error in the LSTM model can
- 416 be the employment of regularization methods as LSTM models are often harder to regularize, agreeing with previous
- 417 studies (e.g., Devineau et al., 2018, June).
- 418 The LSTM network is validated better than the CNN model since its average and minimum F1 scores for validation
- are better than the CNN model (by 1 % and 32 %, respectively), and also LSTM yielded no F1 scores below 0.74 (Fig.
 14 and Table 9).
- 421 As shown in Fig. 13, training loss is higher than validation loss in some of the results. There are some reasons
- 422 explaining that. Regularization reduces the validation loss at the expense of increasing training loss. The regularization
- 423 techniques such as noise layers are only applied during training, but not during validation resulting in more smooth
- 424 and usually better functions in validation. There is no noise layer in CNN-LSTM model that may cause a lower training
- 425 error than validation error. However, other regularization methods such as L2 regularization are used in all the models,
- 426 including the CNN-LSTM model.
- 427 Furthermore, the other issue is that batch normalization uses the mean and variance of each batch in training, whereas,
- 428 in validation, it uses the mean and variance of the whole training dataset. Plus, training loss is averaged over each
- 429 epoch, while validation losses are calculated after each epoch once the current training epoch is completed. Hence,
- 430 the training loss includes error calculations with fewer updates.
- 431 Among the developed machine learning models, SVM shows the best validation performance (Figure 15 and Table
- 432 10). However, F1 scores of deep learning models are much higher than those of machine learning models with an
- 433 average of 6% higher F1 score resulted from CNN-LSTM model compared to the SVM model (Tables 9 and 10).

Figure 13. Train and validation errors over epochs for CNN (left), LSTM (middle), and

CNN-LSTM (right) models with 100 random train-validation splits.

Figure 14. Histograms of F1 scores of validation for CNN (left), LSTM (middle), and

435 CNN-LSTM (right) models with 100 random train-validation splits.

Figure 15. Histograms of F1 scores of validation for SVM (top left), DT (top middle), KNN (top right), and MLP (bottom left) models with 100 random train-validation splits.

436

437 Table 9. F1 scores of validation for CNN, LSTM, and CNN-LSTM models with 100 random train-validation splits.

Models	F1 score			
	mean max m		min	
CNN	0.80	0.88	0.42	
LSTM	0.81	0.87	0.74	
CNN-LSTM	0.82	0.88	0.75	

Table 10. F1 scores of validation for SVM, DT, and KNN and MLP models with 100 random train-validation splits.

Models	F1 score		
	mean	max	min
SVM	0.76	0.82	0.69
DT	0.74	0.80	0.67

KNN	0.75	0.84	0.68
MLP	0.75	0.83	0.68

440 **3.2.2** Number of parameters and run time

The total number of parameters in CNN, LSTM, and CNN-LSTM networks are 371586, 207874, and 664746, respectively. The best performance has resulted from CNN-LSTM with the highest number of parameters. Even though the number of parameters for the LSTM model is less than CNN, the LSTM model shows better validation performance. Furthermore, the number of parameters in the CNN-LSTM model is much higher than the two other models, but the computation time is not much higher. All three models take less than 24 hours to train with 100 shuffle

- 446 splits for training and validation. The models are run on a CPU with four cores, 3.4 GHz clock speed, and 12 GB
- 447 RAM.
- 448 For all the machine learning models, it took a couple of minutes to train with 100 shuffle splits for training and

validation. Although, the training time for deep learning models is much higher than that of machine learning models,

450 the much better performance of deep learning models justifies their application in our cases.

451 **3.3 Order of input variables**

- 452 It is not clear that whether the order of input variables in the input file might influence multivariate TSC or not when 453 using 2-D filters and 2-D max-pooling layers. In the benchmark, we randomly used this order from left to right:
- 454 precipitation, minimum temperature, maximum temperature, net radiation, ATDD, AFDD, and snow depth. We
- 455 randomly changed this order and applied the new order: snow depth, maximum temperature, precipitation, AFDD, net
- 456 radiation, minimum temperature, and ATDD. Both models yielded the same average and minimum F1 scores, whereas
- 457 the maximum F1 score from the order in the benchmark model (0.88) is higher than that of the second-order (0.86).
- 458 Therefore, it can be concluded that the order does not significantly impact the results.

459 **3.4 Testing**

- 460 To examine the ability of the models to generalize to new unseen data, we randomly set aside 10% of data from
- training and validation for all the developed deep learning and machine learning models. We trained a CNN, an LSTM,
- 462 and a CNN-LSTM model, then the trained parameters are saved, and finally, the well-trained parameters are utilized
- 463 for testing. We trained an SVM, a DT, a KNN, and an MLP model and the models are saved and later used for testing.
- The test dataset is almost a balanced dataset with 101 samples with the size of (16, 7), including 48 jams and 53 no
- 465 jams.
- 466 The results of the test models show that CNN-LSTM model represent the best F1 score of 0.92 (Table 11). Tables 9
- 467 and 11 show that although LSTM has slightly better validation performance, CNN and LSTM models performed the
- 468 same in testing.
- 469 The results of machine learning models for testing presented in Table 12 indicate that among the machine learning
- 470 models KNN yields the best results with F1 scores of 78%. Tables 11 and 12 declare that deep learning models work

- 471 much better than machine learning models for testing with 14% comparing CNN-LSTM with KNN as the best deep
- 472 learning and machine learning models, respectively.
- 473

474 Table 11. Test F1 scores for LSTM, CNN, and CNN-LSTM models.

Models	F1 score
CNN	0.80
LSTM	0.80
CNN-LSTM	0.92

475 476

477 Table 12. Test F1 scores for SVM, DT, and KNN and MLP models.

Models	F1 score
SVM	0.75
DT	0.71
KNN	0.78
MLP	0.70

478

479 3.5 Model comparison

480 Multiple combined classifiers can be considered for pattern recognition problems to reduce errors as different 481 classifiers can cover internal weaknesses of each other (Parvin et al., 2011). The combined classifier may be less

482

accurate than the most accurate classifier. However, the accuracy of the combined model is always higher than the

483 average accuracy of individual models. Combining two models improved our results compared to convolution-only

484 or LSTM-only networks in both training and testing, supporting the previous studies (e.g., Sainath et al., 2015). It can

485 be because the CNN-LSTM model incorporates both the temporal dependency of each variable by using LSTM

486 networks and the correlation between variables through CNN models. The combined CNN-LSTM model efficiently

487 benefit from automatic feature learning by CNN plus the native support for time series by LSTM.

488 Although LSTM performed slightly better than CNN in validation, these models showed the same performance in

489 testing. The CNN is able to partially include both temporal dependency and the correlation between variables by using

490 1D and 2D filters, respectively. Although the LSTM is unable to incorporate the correlations between variables, it

491 gives promising results with relatively small dataset and captures longer temporal dynamics, while the CNN only

492 captures temporal dynamics within the length of its filters.

493 Even though our training data in supervised ice-jam prediction is small, the results reveal that deep learning techniques

494 can give accurate results, which agrees with a previous study conducted by Ordóñez and Roggen (2016) in activity

- 495 recognition. The excellent performance of CNN and CNN-LSTM models may be partially due to the characteristic of
- 496 CNN that decreases the total number of parameters which does training with limited training data easier (Gao et al.,

497 2016, May). However, our models will be improved in the future by a larger dataset.

- 498 Among the developed machine learning models, SVM showed the best performance in validation, whereas KNN
- 499 worked the best in testing. However, the performance of deep learning models is much better than machine learning

- 500 models in both validation and testing. The machine learning models do not consider correlations between variables.
- 501 However, it is not the only reason that deep learning models worked better than machine learning models. As the
- 502 LSTM also does not consider correlations between variables but worked better than machine learning models. Some
- 503 characteristics of developed deep learning models can explain their better performance compared to machine learning
- 504 models. For instance, deep learning models perform well for the problems with complex-nonlinear dependencies, time
- 505 dependencies, and multivariate inputs.
- 506 The developed CNN-LSTM model can be used for future predictions of ice jams in Quebec to provide early warning
- 507 of possible floods in the area by using historic hydro-meteorological variables and their predictions for some days in
- 508 advance.

509 **3.6 Discussion on the interpretability of deep learning models**

510 Even though the developed deep learning models performed pretty well in predicting ice jams in Quebec, the 511 interpretability of the results with respect to the physical processes of the ice jam is still essential. It is because although 512 deep learning models have achieved superior performance in various tasks, these really complicated models with a 513 large number of parameters might exhibit unexpected behaviours (Samek et al., 2017 & Zhang et al., 2021). This is 514 because the real-world environment is still much more complex. Furthermore, the models may learn some spurious 515 correlations in the data and make correct predictions with the 'wrong' reason (Samek and Müller, 2019). Hence, 516 interpretability is especially important in some real-world applications like flood and ice-jam predictions where an 517 error may cause catastrophic results. Also, interpretability can be used to extract novel domain knowledge and hidden 518 laws of nature in the research fields with limited domain knowledge (Alipanahi et al., 2015) like ice-jam prediction. 519 However, the nested non-linear structure and the "black box" nature of deep neural networks make interpretability of 520 their underlying mechanisms and their decisions a significant challenge (Montavon et al., 2018, Zhang et al., 2021 521 and Wojtas and Chen, 2020). That is why, interpretability of deep neural networks still remains a young and emerging

- 522 field of research. Nevertheless, there are various methods available to facilitate understanding of decisions made by a
- 523 deep learning model such as feature importance ranking, sensitivity analysis, layer-wise relevance propagation, and
- 524 the global surrogate model. However, the interpretability of developed deep learning models for ice-jam prediction is
- 525 beyond the scope of this study and it will be investigated in our future works.

526 **3.7 Model transferability**

- 527 The transferability of a model between river basins is highly desirable but has not yet been achieved because most 528 river ice-jam models are site specific (Mahabir et al., 2007). The developed models in this study can be used to predict 529 future ice jams some days before the event not only for Quebec but also for eastern parts of Ontario and western New 530 Brunswick. For other locations, the developed models can be transferred via re-training and a small amount of fine-531 tuning using labeled instances, rather than building from scratch. It is because the logic in the model may be 532 transferable to the other sites with small modifications. To transfer a model from one river basin to another, historic
- 533 records of ice jams and equivalent hydro-meteorological variables (e.g., precipitation, temperature, and snow depth)
- as inputs to the model must be available at each site.
- 535 4 Conclusion

- 536 The main finding from this project is that all the developed deep models performed pretty well and performed much
- 537 better than the developed machine learning models for ice-jam prediction in Quebec. The comparison of results show
- 538 that the CNN-LSTM model is superior to the CNN-only and LSTM-only networks in both validation and testing
- 539 accuracy, though the LSTM and CNN models demonstrate quite good performance.
- 540 To our best knowledge, this study is the first study introducing these deep learning models to the problem of ice-jam
- 541 prediction. The developed models are promising to be used to predict future ice jams in Quebec and in other river
- 542 basins in Canada with re-training and a small amount of fine-tuning.
- 543 The developed models do not apply to freeze-up jams that occur in early winter and are based on different processes
- 544 than breakup jams. We studied only breakup ice jams as usually they result in flooding and are more dangerous than
- 545 freeze-up jams. Furthermore, there is a lack of data availability for freeze-up ice jams in Quebec and only 89 records
- 546 of freeze-up jams are available which is too small.
- 547 The main limitation of this study is data availability as recorded ice jams are small which causes deep learning models
- 548 to easily overfit to small number of data. Another limitation of the presented work is the lack of interpretability of the
- 549 results with respect to the physical characteristics of the ice jam. This is a topic of future research and our next step is
- to explore that.
- 551 The hydro-meteorological variables are not the only drivers of ice-jam formation. The geomorphological indicators
- that control the formation of ice jams include the river slope, sinuosity, a barrier such as an island or a bridge,
- 553 narrowing of the channel, and confluence of rivers. In the future, a geospatial model using deep learning will be
- 554 developed to examine the impacts of these geospatial parameters on ice-jam formation.

555 Author contribution

- 556 Fatemehalsadat Madaeni designed and carried out the experiments under Karem Chokmani and Saeid Homayouni 557 supervision. Fatemehalsadat Madaeni developed the model code and performed the simulations using hydro-558 meteorological and ice-jam data provided and validated by Rachid Lhissou. Fatemehalsadat Madaeni wrote the bulk 559 of the paper with conceptual edits from Karem Chokmani and Saeid Homayouni. Yves Gauthier and Simon
- 560 Tolszczuk-Leclerc helped in the refinement of the objectives and the revision of the methodological developments.

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- 564 Climate Change Canada.

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