



1 **An empirical algorithm to map perennial firn aquifers, ice slabs,**
2 **and perched firn aquifers within the Greenland Ice Sheet**
3 **using satellite L-band microwave radiometry**
4

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18
19 **Abstract**

20 *Perennial firn aquifers are subsurface meltwater reservoirs formed from a water-saturated firn layer.*
21 *They have been observed within the percolation facies of glaciated regions experiencing intense*
22 *seasonal surface melting and high snow accumulation. Widespread perennial firn aquifers have*
23 *been identified within the Greenland Ice Sheet (GrIS) via field expeditions, airborne ice-penetrating*
24 *radar surveys, and satellite microwave sensors. In contrast, ice slabs are nearly-continuous ice*
25 *layers that form on spatial scales of kilometers as a result of surface and subsurface water-*
26 *saturated snow and firn layers sequentially refreezing following multiple melting seasons. They*
27 *have been observed within the percolation facies of glaciated regions experiencing intense*
28 *seasonal surface melting, but in areas where snow accumulation is at least ~25% lower as*
29 *compared to perennial firn aquifer areas. Widespread ice slabs have recently been identified within*
30 *the GrIS via field expeditions and airborne ice-penetrating radar surveys, specifically in areas where*
31 *perennial firn aquifers typically do not form. However, ice slabs have yet to be inferred from space.*
32 *Together, these two ice sheet features represent distinct, but related, sub-facies within the broader*
33 *percolation facies of the GrIS that can be defined primarily by differences in snow accumulation,*
34 *which influences the englacial hydrology and thermal characteristics of firn layers at depth.*

35 *Here, for the first time, we use enhanced-resolution vertically-polarized L-band brightness*
36 *temperature (T_V^B) imagery (2015-2019) generated using observations collected over the GrIS by*
37 *NASA's Soil Moisture Active Passive (SMAP) satellite to map both perennial firn aquifer and ice slab*
38 *areas as a continuous system over the percolation facies. We also map 'perched' firn aquifer areas,*
39 *which we define as areas where shallow water-saturated firn layers transiently form on top of buried*
40 *ice slabs, or other semi-impermeable layers within the snow and firn. An empirical algorithm*



41 *previously developed to map the extent of Greenland's perennial firn aquifers via fitting*
42 *exponentially decreasing temporal L-band signatures to a set of sigmoidal curves is recalibrated to*
43 *also map the extent of ice slab and perched firn aquifer areas using airborne ice-penetrating radar*
44 *surveys collected by NASA's Operation Ice Bridge (OIB) campaigns (2010-2017). Our SMAP-derived*
45 *maps show that between 2015 and 2019, perennial firn aquifer areas extended over ~64,000 km², ice*
46 *slab areas extended over ~76,000 km², and perched firn aquifer areas extended over ~37,000 km².*
47 *Combined together, these three sub-facies are the equivalent of ~24% of the percolation facies of*
48 *the GrIS. As Greenland's climate continues to warm, and seasonal surface melting increases in*
49 *extent, intensity, and duration, quantifying the possible rapid expansion of each of these sub-facies*
50 *using satellite L-band microwave radiometry has significant implications for understanding ice*
51 *sheet-wide variability in englacial firn hydrology resulting in meltwater-induced hydrofracturing and*
52 *accelerated ice flow as well as high-elevation run-off that can impact the mass balance and stability*
53 *of the GrIS.*

54

55 **1 Introduction**

56 The recent launch of several satellite L-band microwave radiometry missions by NASA (Aquarius mission,
57 Levine, et al., 2007; Soil Moisture Active Passive (SMAP) mission, Entekhabi et al., 2010) and ESA (Soil
58 Moisture and Ocean Salinity (SMOS), Kerr et al., 2010) has provided a new Earth-observation tool
59 capable of detecting stored meltwater ~tens of meters to kilometers beneath the surface of ice sheets.
60 Jezek et al. (2015) recently demonstrated that in the high-elevation (~3500 m.a.s.l.) dry snow facies of the
61 Antarctic Ice Sheet, meltwater stored in subglacial Lake Vostok can be detected ~4000 m beneath the ice
62 sheet surface. Subglacial lakes represent radiometrically cold subsurface meltwater reservoirs. Upwelling
63 L-band emissions from the radiometrically warm bedrock underlying the subglacial lakes are effectively
64 blocked by high reflectivity and attenuation at the interface between bedrock and the overlying lake bottom.
65 This results in a lower observed microwave brightness temperature (T^B) at the ice sheet surface as
66 compared to other dry snow facies areas where bedrock contributes to L-band emissions depth-integrated
67 over the entire ice sheet thickness.

68 Similar to subglacial lakes, perennial firn aquifers also represent radiometrically cold subsurface
69 meltwater reservoirs (Miller et al., 2020) formed from a ~4 m-25 m thick water-saturated firn layer (Koenig
70 et al., 2014; Montgomery et al., 2017; Chu et al., 2018). They have been observed via field expeditions and
71 airborne ice-penetrating radar surveys in the lower-elevation (< ~2000 m.a.s.l.) percolation facies of the
72 Greenland Ice Sheet (GrIS), at depths from between ~1 m and 40 m beneath the ice sheet surface (Miège
73 et al. 2016), and in areas that experience intense seasonal surface melting (>650 mm yr⁻¹) during the
74 melting season and high snow accumulation (>800 mm yr⁻¹) during the freezing season (Forster et al.,
75 2014). High snow accumulation in perennial firn aquifer areas thermally insulates water-saturated firn layers
76 from the cold atmosphere allowing seasonal meltwater to be stored in liquid form if the overlying seasonal
77 snow layer is sufficiently thick (Kuipers Munneke et al., 2014). Koenig et al. (2014) estimated that the



78 volumetric fraction of meltwater stored within the pore space of Greenland's perennial firn aquifers just prior
79 to melt onset ranges from between ~10% and 25%, which limits the upward propagation of electromagnetic
80 energy from greater depths within the ice sheet. Large volumetric fractions of meltwater within the firn pore
81 space results in high reflectivity and attenuation at the interface between water-saturated firn layers and
82 the overlying refrozen firn layers, and between glacial ice or a semi-impermeable layer and the overlying
83 water-saturated firn layers. Upwelling L-band emissions from deeper glacial ice and the underlying bedrock
84 are effectively blocked.

85 While perennial firn aquifers are radiometrically cold, the slow refreezing of deeper firn layers
86 saturated with large volumetric fractions of meltwater represents a significant source of latent heat that is
87 continuously released throughout the freezing season. Refreezing of seasonal meltwater by the descending
88 winter cold wave (Pfeffer et al., 1991), and the subsequent formation of embedded ice structures (i.e.,
89 horizontally-oriented ice layers and ice lenses, and vertically-oriented ice pipes; Benson et al., 1960;
90 Humphrey et al., 2012; Harper et al., 2012) within the upper snow and firn layers represents a secondary
91 source of latent heat. These heat sources help maintain meltwater at depth. Perennial firn aquifer areas
92 are radiometrically warmer than other percolation facies areas where the single source of latent heat is via
93 refreezing of seasonal meltwater. This results in a higher observed T^B at the ice sheet surface during the
94 freezing season as compared to other percolation facies areas where seasonal meltwater is fully refrozen
95 and stored exclusively as embedded ice.

96 Many open questions remain about Greenland's perennial firn aquifers, regarding initial formation,
97 extent, depth, flow characteristics, timescales of refreezing and/or englacial drainage, and connections to
98 the subglacial hydrological system. Seasonal surface melting over the GrIS has increased in extent,
99 intensity, and duration since the beginning of the satellite era (Steffen et al., 2004; Tedesco et al., 2008;
100 Tedesco et al., 2011; Nghiem et al., 2012; Tedesco et al., 2016; Tedesco and Fettweis, 2020; Cullather et
101 al., 2020). If this trend continues (Franco et al., 2013; Noël et al., 2021), subsequent increases in the
102 volume of meltwater stored within Greenland's perennial firn aquifers will increase the possibility of
103 crevasse-deepening via meltwater-induced hydrofracturing (Alley et al., 2005; van der Veen, 2007),
104 especially if crevasse fields laterally expand into perennial firn aquifer areas as a result of accelerated ice
105 flow (Colgan et al., 2016). Meltwater-induced hydrofracturing is an important component of supraglacial
106 lake drainage during the melting season (Das et al., 2008; Stevens et al., 2015) leading to at least temporary
107 accelerated flow velocities (Zwally et al., 2002; Joughin et al., 2013; Moon et al., 2014) and mass balance
108 changes (Joughin et al., 2008). Greenland's firn perennial aquifers may also support meltwater-induced
109 hydrofracturing, even during the freezing season (Poinar et al., 2017; 2019).

110 Recently, mapping the extent of Greenland's perennial firn aquifers from space was demonstrated
111 using satellite L-band microwave radiometry (Miller et al., 2020). Exponentially decreasing temporal L-band
112 signatures observed in enhanced-resolution vertically-polarized L-band brightness temperature (T_V^B)
113 imagery (2015-2016) generated using observations collected over the GrIS by the microwave radiometer
114 on the SMAP satellite (Brodzik et al., 2019) were correlated with a single year of perennial firn aquifer



115 detections (2016) identified via the Center for Remote Sensing of Ice Sheets (CReSIS) Multi-Channel
116 Coherent Radar Depth Sounder (MCoRDS) flown by NASA's Operation Ice Bridge (OIB) campaigns (Miège
117 et al. 2016; Rodriguez-Morales et al, 2014). An empirical algorithm to map extent was developed by fitting
118 temporal L-band signatures to a set of sigmoidal curves derived from the continuous logistic model.

119 The relationship between the radiometric, and thus the physical, temperature of perennial firn
120 aquifer areas, as compared to other percolation facies areas, forms the basis of the empirical algorithm.
121 Miller et al. (2020) hypothesized that the dominant control on the relatively slow exponential rate of T_V^B
122 decrease over perennial firn aquifer areas is physical temperature versus depth. L-band emissions from
123 the radiometrically warm upper snow and firn layers decrease during the freezing season as embedded ice
124 structures slowly refreeze at increased depths below the ice sheet surface. In the percolation facies,
125 refreezing of seasonal meltwater results in the formation of an intricate network of embedded ice structures
126 that are large (~10-100 cm long, ~10-20 cm wide; Jezek et al., 1994) relative to the L-band wavelength
127 (~21 cm). Embedded ice structures induce strong volume scattering (Rignot et al., 1993; Rignot 1995) that
128 decreases T^B (Zwally, 1977; Swift et al. 1985; Jezek et al., 2018).

129 Ice slabs are ~1 m–16 m thick nearly-continuous ice layers that form on spatial scales of kilometers
130 as a result of surface and subsurface water-saturated snow and firn layers sequentially refreezing following
131 multiple melting seasons (Machguth et al., 2016; McFerrin et al., 2019). Over time, they become dense low-
132 permeability solid-ice layers overlying deeper permeable firn layers. Similar to perennial firn aquifers, ice
133 slabs have been observed via field expeditions and ice-penetrating airborne radar surveys in the lower-
134 elevation (< ~2000 m.a.s.l.) percolation facies of the GrIS. They form at depths from between ~1 m and 20
135 m beneath the ice sheet surface. Particularly in areas that experience intense seasonal surface melting
136 (>600 mm yr⁻¹) during the melting season, and lower snow accumulation (<600 mm yr⁻¹) during the
137 freezing season as compared to perennial firn aquifer areas (McFerrin et al., 2019). Lower snow
138 accumulation in ice slab areas results in a seasonal snow layer that is insufficiently thick to thermally
139 insulate water-saturated firn layers and seasonal meltwater is instead stored as embedded ice. Refreezing
140 of seasonal meltwater by the descending winter cold wave, and the subsequent formation of ice slabs as
141 well as other embedded ice structures within the upper snow and firn layers is the single source of latent
142 heat in ice slab areas. While ice slab areas are radiometrically warmer than other percolation facies areas
143 with a lower volumetric fraction of embedded ice, they are radiometrically colder than perennial firn aquifer
144 areas. This results in a lower observed T^B at the ice sheet surface during the freezing season.

145 Consistent with recent seasonal surface melting trends, meltwater run-off has accelerated to
146 become the dominant mass loss mechanism over the GrIS (van den Broeke et al., 2016). However,
147 significant uncertainty remains in meltwater run-off estimates in the percolation facies as a result of the lack
148 of knowledge of heterogeneous infiltration processes within the snow and firn layers (Pfeffer and Humphrey,
149 1996), the depths to which meltwater can descend beneath the ice sheet surface (Humphrey et al., 2012),
150 and the formation of englacial firn hydrological features (Benson et al., 1960; Humphrey et al., 2012; Forster
151 et al., 2014), especially ice layers and ice slabs (Machguth et al., 2016, McFerrin et al., 2019; Culberg et



152 al., 2021). A notable example of this lack of knowledge is the identification by Forster et al., (2014) of
153 widespread perennial firn aquifers within the percolation facies of the GrIS via airborne ice-penetrating radar
154 surveys collected by NASA's OIB campaigns (2010-2014; Rodriguez-Morales et al, 2014) that store large
155 volumes (~140 Gt; Koenig et al., 2014) of meltwater that was previously unknown. The mapped extent
156 (2010-2014) shown in Forster et al., (2014) can be distinctly observed in 1978 enhanced resolution Ku-
157 band radar backscatter imagery (Long and Drinkwater, 1994) collected by the radar scatterometer on
158 NASA's first Earth-observing satellite - the Seasat-A mission (Jones et al., 1982). This suggests that
159 Greenland's perennial firn aquifers have likely existed undetected in the deeper firn layers of the percolation
160 facies for decades. Meltwater storage in both solid (i.e., embedded ice structures) and liquid (i.e., perennial
161 firn and perched firn aquifers) form can buffer meltwater run-off in the percolation facies (Harper et al.,
162 2012). However, the formation of near-surface ice layers and ice slabs reduces the pore space within the
163 upper snow and firn layers and facilitates lateral meltwater flow with minimum vertical percolation into the
164 deeper firn layers, thus enhancing meltwater run-off downslope towards the periphery. Lateral meltwater
165 flow across ice layers overlying deeper permeable firn layers was first postulated by Müller (1962). The
166 theory was then further developed by Pfeffer et al., (1991) as an end-member case for meltwater run-off,
167 with the other end member case being lateral meltwater flow across superimposed ice in the wet snow
168 facies and/or across glacial ice in the ablation facies. McFerrin et al., (2019) recently identified widespread
169 near-surface ice slabs within the percolation facies of the GrIS via airborne ice-penetrating radar surveys
170 collected by NASA's OIB campaigns (2010-2014; Rodriguez-Morales et al, 2014). Lateral meltwater flow
171 and high-elevation (~1850 m.a.s.l) meltwater run-off across the identified ice slabs was also observed in
172 visible satellite imagery collected by the NASA-USGS Landsat 7 mission (e.g. Goward et al., 2001). This
173 was also observed during the anomalous 2012 melting season (McFerrin et al., 2019) during which
174 seasonal surface melting extended over ~99% of the GrIS (Nghiem et al., 2012)

175 In this study, we use enhanced-resolution L-band T_V^B imagery (2015-2019) generated using
176 observations collected over the GrIS by the microwave radiometer on the SMAP satellite (Brodzik et al.,
177 2019) to map ice sheet-wide englacial firn hydrological features within the percolation facies. First, we adapt
178 our empirical algorithm to map the extent of Greenland's perennial firn aquifers (Miller et al., 2020). We
179 correlate exponentially decreasing temporal L-band signatures with five years of perennial firn aquifer
180 detections (2010-2014) identified via the CReSIS Accumulation Radar (AR) flown by NASA's OIB
181 campaigns (Miège et al. 2016), and three years of additional detections (2015-2017) more recently
182 identified via MCoRDS (Miller et al., 2020). Next, we extend our empirical algorithm to also map the extent
183 of ice slab and perched firn aquifer areas. We identify distinct temporal L-band signatures in T_V^B time series
184 over ice slab detections (2010-2014) recently identified via AR (McFerrin et al., 2019). Similar to temporal
185 L-band signatures over perennial firn aquifer areas, temporal L-band signatures over ice slab areas are
186 exponentially decreasing during the freezing season, however, the rate of T_V^B decrease is slightly more
187 rapid. We correlate these relatively rapidly exponentially decreasing temporal L-band signatures with five
188 years of AR-derived ice slab detections. Additionally, we correlate exponentially decreasing temporal L-



189 band signatures with AR- and MCoRDS-derived detections where perennial firn aquifer and ice slab areas
190 overlap. We identify these transitional areas as perched firn aquifer areas. We infer that, in these areas,
191 shallow water-saturated firn layers transiently form on top of buried ice slabs or other semi-impermeable
192 layers, such as spatially coherent melt layers that form in the higher elevations ($> \sim 2000$ m.a.s.l.) of the
193 percolation facies and the dry snow facies that were recently identified via AR (Culberg et al., 2021).
194 Perched firn aquifers likely form during some melting seasons as a result of interannual variability in surface
195 melting and snow accumulation, and the formation of englacial firn hydrological features. Finally, we re-
196 calibrate the sigmoidal curves to map the extent of perennial firn aquifer, ice slab, and perched firn aquifer
197 areas over the percolation facies of the GrIS

198

199 **2 Methods**

200 **2.1 The Soil Moisture Active Passive (SMAP) Mission**

201 The key science objectives of NASA's SMAP mission (<https://smap.jpl.nasa.gov/>) are to map terrestrial soil
202 moisture and freeze/thaw state over Earth's land surfaces from space. However, the global L-band T^B
203 observations collected by the SMAP satellite also have many cryospheric applications. Mapping ice sheet-
204 wide englacial firn hydrological features over Earth's polar ice sheets represents an interesting analog and
205 an innovative extension of the science objectives. Measurements of moisture (i.e., defined in this study in
206 terms of the volumetric fraction of meltwater within the upper snow and firn layers of the percolation facies)
207 and freeze-thaw state (i.e., defined in this study in terms of the firn saturation parameter (see Section 2.4.3)
208 and the refreezing rate parameter (see Section 2.4.4)) are critical to understanding the hydrospheric state
209 over Earth's polar ice sheets. Perennial firn aquifers, ice slabs, and perched firn aquifers represent recently
210 identified components of the hydrosphere that are capable of storing large volumes of meltwater in both
211 solid and liquid form that can initiate meltwater-induced hydrofracturing and accelerated ice flow as well as
212 high-elevation run-off, and impact the mass balance and stability of the GrIS. Critically, the majority of
213 meltwater is stored at depths that only L-band satellite microwave sensors (i.e., radiometers, radar
214 scatterometers, and synthetic aperture radars) are capable of detecting.

215 Previous and current satellite microwave radiometer, radar scatterometer, and synthetic aperture
216 radar missions that operate in the frequency range between 37 GHz (Ka-band) and 5.3 GHz (C-band) have
217 provided a multi-decadal (1978-present) record of multi-frequency T^B and radar backscatter observations
218 over Earth's polar ice sheets since the beginning of the satellite era. The most common geophysical
219 parameter mapped over ice sheets using these observations is the extent of seasonal surface melting. The
220 key difference between L-band and higher frequency satellite microwave sensors is penetration depth.
221 When the snow and firn layers are saturated with meltwater during the melting season, the penetration
222 depth of both L-band and higher frequency satellite microwave sensors is less than ~a meter. When surface
223 and subsurface water-saturated snow and firn layers and embedded ice structures subsequently refreeze,
224 the penetration depth of higher frequency satellite microwave sensors ranges from between ~centimeters
225 and meters. During the freezing season, water-saturated snow and firn layers either completely refreeze



226 (i.e., ice layers, ice slabs, spatially coherent melt layers) or underlay the refrozen upper snow and firn layers
227 of the percolation facies and descend to depths ranging from between ~1 m and 40 m (Miège et al., 2016)
228 beneath the ice sheet surface (i.e., perennial and perched firn aquifers). While the upper surface of stored
229 meltwater in some perennial and perched firn aquifers may remain at depths that are shallow enough to be
230 directly detected by C-band satellite microwave sensors, the mean depth just prior to melt onset (~22 m;
231 Miège et al., 2016) is too deep to be detected at this wavelength. L-band satellite microwave sensors can
232 detect perennial firn aquifers from as much as an order of magnitude deeper than can be observed by C-
233 band satellite microwave radiometers. Deep enough to directly detect the upper surface of stored meltwater
234 over the entire depth range mapped by airborne ice-penetrating radar surveys over the GrIS.

235

236 **2.1 SMAP Enhanced-Resolution L-band T^B Imagery**

237 NASA's SMAP satellite was launched 31 January 2015 and carries a microwave radiometer that operates
238 at a frequency of 1.41 GHz (L-band) (Enkentabi et al., 2010). It is currently collecting observations of
239 vertically and horizontally-polarized T^B over Greenland. The surface incidence angle is ~40°, and the
240 radiometric accuracy is ~1.3 K (Piepmeier et al., 2017).

241 The Scatterometer Image Reconstruction (SIR) algorithm was developed to reconstruct coarse
242 resolution satellite scatterometry imagery on a higher spatial resolution grid (Long et al., 1993; Early and
243 Long, 2001). The SIR algorithm has been adapted for coarse resolution satellite microwave radiometry
244 imagery (Long and Daum, 1998; Long and Brodzik, 2016; Long et al., 2019). The microwave radiometer
245 form of the SIR algorithm (rSIR) exploits the measurement response function (MRF) for each observation,
246 which is a smeared version of the antenna pattern. Using the overlapping MRFs, the rSIR algorithm
247 reconstructs T^B from the spatially filtered low-resolution sampling provided by the observations. In effect, it
248 generates an MRF-deconvolved T^B image. Combining multiple orbital passes increases the sampling
249 density, which improves both the accuracy and resolution of SMAP enhanced-resolution T^B imagery (Long
250 et al., 2019).

251 Over Greenland, the rSIR algorithm combines satellite orbital passes that occur between 8 a.m.
252 and 4 p.m. local time-of-day to reconstruct SMAP enhanced-resolution T^B imagery twice-daily (i.e., morning
253 and evening orbital pass interval, respectively). T^B imagery is projected on a Northern Hemisphere (NH)
254 Equal-Area Scalable Earth Grid (EASE-Grid 2.0; Brodzik et al., 2012) at a 3.125 km rSIR grid cell spacing.
255 The effective resolution for each grid cell is dependent on the number of observations used in the rSIR
256 reconstruction and is coarser than the rSIR grid cell spacing. While the effective resolution of conventionally
257 processed SMAP T^B imagery posted on a 25 km grid is ~30 km, the effective resolution of SMAP enhanced-
258 resolution T^B imagery posted on a 3.125 km grid is ~18 km, an improvement of ~60% (Figs. 1; 2) (Long et
259 al., 2020).

260 For our analysis of the percolation facies, we use SMAP enhanced-resolution T_V^B imagery over the
261 GrIS. Compared to the horizontally-polarized channel, the vertically-polarized channel exhibits decreased
262 sensitivity to variability in the volumetric fraction of meltwater, which is attributed to reflection coefficient

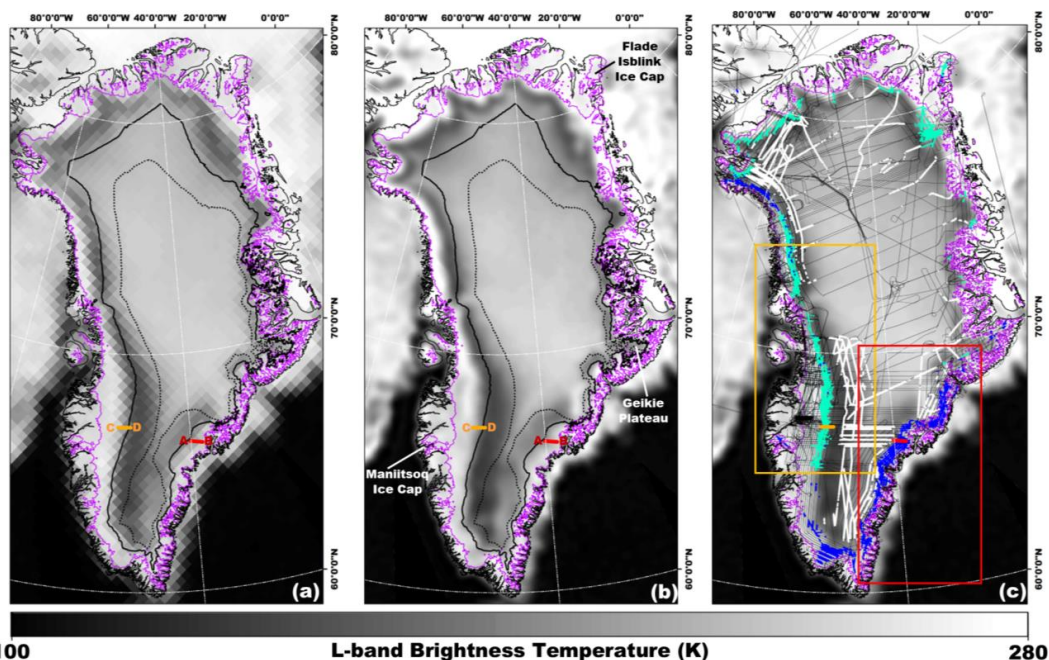


263 differences between channels (Miller et al., 2020). Using the vertically polarized channel also results in a
264 reduced chi-squared error statistic when fitting T_V^B time series to the sigmoid function (see Section 2.4.5).
265 We construct T_V^B imagery that alternate morning and evening orbital pass observations annually, beginning
266 and ending just prior to melt onset. The Greenland Ice Mapping Project (GIMP) Land Ice and Ocean
267 Classification Mask and Digital Elevation Model (Howat et al., 2014) are projected on a NH EASE-Grid 2.0
268 at a 3.125 km rSIR grid cell spacing. T_V^B imagery between 1 April 2015 and 31 March 2019 are ice sheet-
269 masked, and an elevation for each rSIR grid cell is calculated.
270

271 **2.2 Airborne Ice-Penetrating Radar Surveys**

272 Miller et al., (2020) calibrated the empirical algorithm to map the extent of Greenland's perennial firn
273 aquifers by correlating a single year of exponentially decreasing temporal L-band signatures (2015-2016)
274 with coincident perennial firn aquifer detections (2016) identified via MCoRDS. Here, we extend and expand
275 the calibration of our adapted empirical algorithm to include four years of exponentially decreasing temporal
276 L-band signatures (2015-2019) correlated with eight years of perennial firn aquifer detections (2010-2017)
277 and five years of ice slab detections (2010-2014) identified via AR and MCoRDS (Fig. 1c). Our multi-year
278 calibration technique projects perennial firn aquifer and ice slab detections on three separate NH EASE-
279 Grids 2.0 at an rSIR grid cell spacing of 3.125 km, consistent with the rSIR grid cell spacing of the SMAP
280 enhanced-resolution L-band T_V^B imagery. Interannual variability is not resolved in this study, however, it will
281 be explored further in future work.

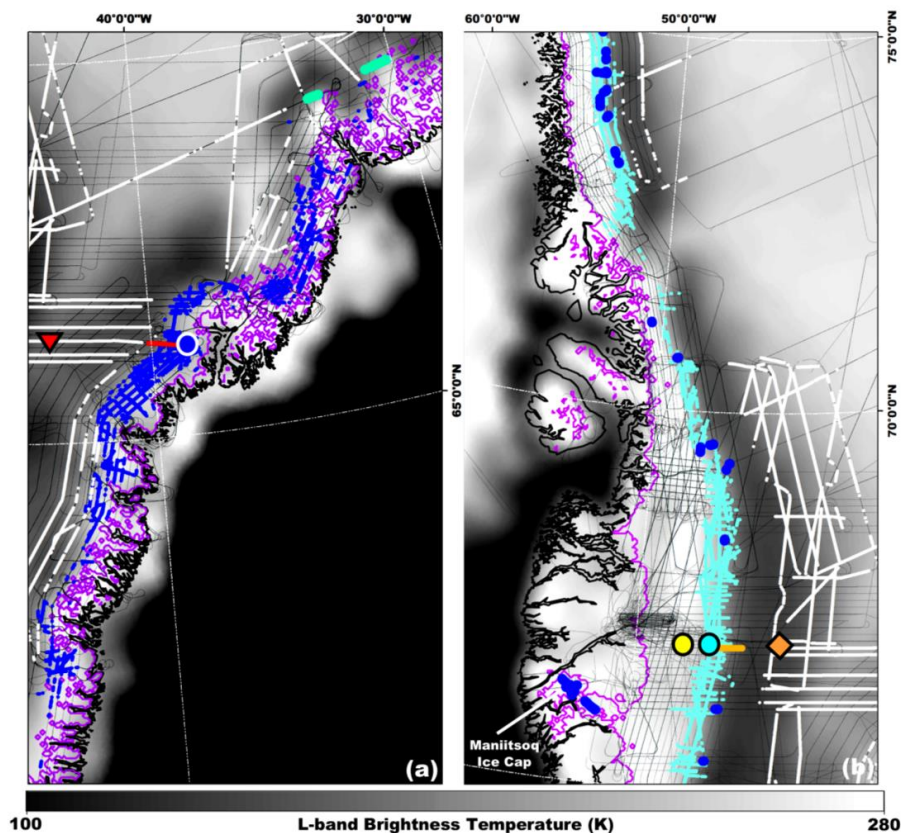
282 An advantage of the multi-year calibration technique as compared to the single-coincident year
283 calibration technique (Miller et al., 2020) is that it increases the number of rSIR grid cells that can be
284 assessed. It also provides repeat targets that can account for variability in the dielectric and geophysical
285 properties that seasonally influence the radiometric temperature and temporal L-band signatures in stable
286 perennial firn aquifer, ice slab, and perched firn aquifer areas. Uncertainty is introduced by correlating
287 exponentially decreasing temporal L-band signatures with AR- and MCoRDS-derived detections that are
288 not coincident in time. The multi-year calibration technique assumes the extent of each area remains stable,
289 which is not necessarily the case as climate extremes (Cullather et al., 2020) can influence each of these
290 sub-facies. The assumption of stability neglects boundary transitions in the extent of perennial firn aquifer
291 areas associated with refreezing of shallow water-saturated firn layers, englacial drainage of meltwater into
292 crevasses at the periphery (Poinar et al., 2017; Poinar et al, 2019), and transient upslope expansion
293 (Montgomery et al., 2017). Once formed, ice slabs are essentially permanent features within the upper
294 snow and firn layers of the percolation facies until they are compressed into glacial ice. However, they may
295 transition into superimposed ice at the lower boundary of ice slab areas or rapidly expand upslope,
296 particularly following extreme melting seasons (McFerrin et al., 2019). By our definition, perched firn
297 aquifers are transient features. Thus, we simply consider our mapped extent a high-probability area for the
298 preferential formation of each of these sub-facies within the broader percolation facies, with continued
299 presence dependent on seasonal surface melting and snow accumulation in subsequent years.



300
301

302 **Figure 1**

303 (a) Gridded (25 km), and (b) enhanced-resolution (3.125 km) L-band T_V^B imagery generated using
304 observations collected 15 April 2016 by the microwave radiometer on the SMAP satellite during the evening
305 orbital pass interval over Greenland (Brodzik et al., 2019). The solid black line is the 2000 m.a.s.l. contour,
306 and the black dotted line is the 2500 m.a.s.l. contour (Howat et al., 2014). The purple line is the ice sheet
307 extent (Howat et al., 2014). The black peripheral line is the coast of Greenland and adjacent Ellesmere
308 Island (Wessel and Smith, 1996). The whiter regions of higher T_V^B over the high-elevation (> ~2500 m.a.s.l.)
309 interior are the dry snow facies. The darker grey regions of lower T_V^B are the percolation facies, including
310 ice slabs and perched firn aquifer areas. The whiter regions of higher T_V^B over the coastal areas, peripheral
311 ice caps (e.g., Maniitsoq and Flade Isblink) and nearby islands are perennial firn aquifers, superimposed
312 or glacial ice, land, or spatially integrated L-band emissions. The whiter regions of higher T_V^B outside the ice
313 sheet extent are sea ice. (c) The SMAP enhanced-resolution L-band T_V^B imagery is overlaid with AR- and
314 MCoRDS-derived 2010-2017 perennial firn aquifer (blue shading; Miège et al., 2016), 2010-2014 ice slab
315 (cyan shading; McFerrin et al., 2019), and 2012 spatially coherent melt layer (white shading; Culberg et al.,
316 2021) detections along OIB flight lines (black lines). Overlapping perennial firn aquifer and ice slab
317 detections are interpreted as perched firn aquifer areas. The red and orange boxes in (c) are zoom areas
318 over south eastern Greenland (Fig. 2a), and south western Greenland (Fig. 2b), respectively. The red line
319 is AR radargram profile along perennial firn aquifer transect A-B (Fig. 3a). The orange line is AR radargram
320 profile along ice slab transect C-D (Fig. 3b).



321

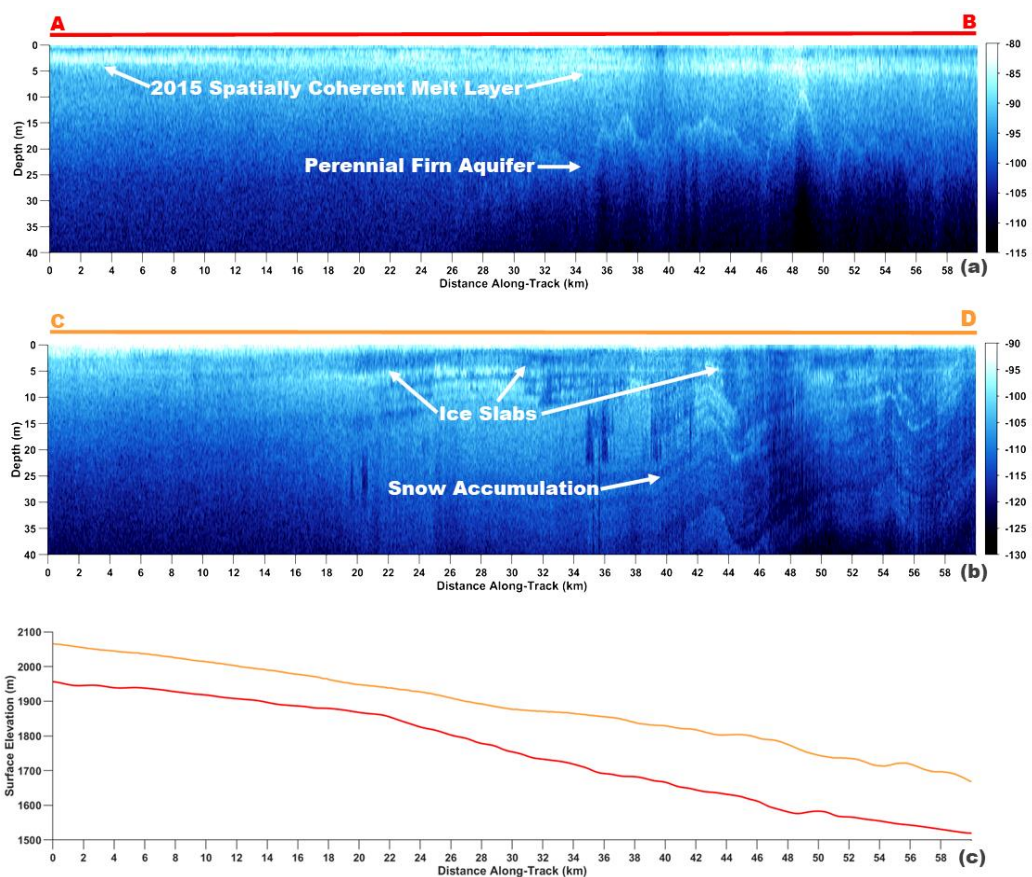
322 **Figure 2**

323 *Enhanced-resolution (3.125 km) L-band T_V^B imagery generated using observations collected 15 April 2016*
324 *by the microwave radiometer on the SMAP satellite during the evening orbital pass interval over (a) south*
325 *eastern Greenland (Fig. 1c; zoom area in red box), and (b) south western Greenland (Fig. 1c; zoom area*
326 *in orange box) (Brodzik et al., 2019). The purple line is the ice sheet or ice cap extent (Howat et al., 2014).*
327 *The black peripheral line is the coast (Wessel and Smith, 1996). (c) The SMAP enhanced-resolution L-*
328 *band T_V^B imagery is overlaid with AR- and MCoRDS-derived 2010-2017 perennial firn aquifer (blue shading;*
329 *Miège et al., 2016), 2010-2014 ice slab (cyan shading; McFerrin et al., 2019), and 2012 spatially coherent*
330 *melt layer (white shading; Culberg et al., 2021) detections along OIB flight lines (black lines). Overlapping*
331 *perennial firn aquifer and ice slab detections are interpreted as perched firn aquifer areas. The red line is*
332 *AR radargram profile along perennial firn aquifer transect A-B (Figs. 1; 3a). The orange line is AR radargram*
333 *profile along ice slab transect C-D (Figs. 1; 3b). The blue circle is a perennial firn aquifer area (Figs. 3a;*
334 *4a). The cyan circle is a perched firn aquifer area (Figs. 3b; 4b). The orange diamond is a percolation facies*
335 *area (Fig. 4c). The red triangle is a high-elevation (~2500 m.a.s.l.) percolation facies area (Fig. 4d). The*
336 *yellow circle is a superimposed ice area (Fig. 4e).*



337 Annual perennial firn aquifer and ice slab detections that may introduce significant uncertainty into
338 the multi-year calibration technique include those following the 2010 melting season, which was
339 exceptionally long (Tedesco et al., 2010), the anomalous 2012 melting season (Nghiem et al., 2012), and
340 the 2015 melting season which was especially intense in western and northern Greenland (Tedesco et al.,
341 2016). Following these extreme melting seasons, significant changes in the dielectric and geophysical
342 properties likely occurred across large portions of the GrIS, including perennial firn aquifer recharging
343 resulting in increases in meltwater volume and decreases in the depth to the upper surface of stored
344 meltwater. The formation of expansive near-surface ice slabs (McFerrin et al., 2019) likely resulted in the
345 formation of more extensive perched firn aquifers during subsequent melting seasons. The upper snow and
346 firn layers of the dry snow facies and percolation facies were also saturated with relatively large volumetric
347 fractions of meltwater as compared to the negligible to limited volumetric fractions of meltwater that
348 percolates during more typical seasonal surface melting on the GrIS. Seasonal meltwater was refrozen into
349 spatially coherent melt layers following the 2010 and 2012 melting seasons (Culberg et al., 2021) as well
350 as following the 2015 and 2018 melting seasons (i.e., identified as part of the temporal L-band signature
351 analysis in this study; see Section 2.4.2).

352 As compared to ice slabs, which are dense low-permeability solid-ice layers, spatially coherent melt
353 layers are a network of embedded ice structures primarily consisting of discontinuous horizontally-oriented
354 ice layers and ice lenses sparsely connected via vertical-oriented ice pipes (Culberg et al., 2021). Ice slabs
355 are relatively thick (~1 m – 16 m) and form in the high-elevation percolation facies (~2100 m.a.s.l.) at depths
356 of between ~1 m and 20 m beneath the ice sheet surface following intense seasonal surface melting over
357 multiple melting seasons (McFerrin et al., 2019). Spatially coherent melt layers are relatively thin (~0.02 cm
358 - 2 m) and can rapidly form across the entire high-elevation dry snow facies (~3200 m.a.s.l.; Nghiem et al.,
359 2012) at depths of less than ~1 m beneath the ice sheet surface following a single extreme melting season.
360 They can further merge together into thicker solid-ice layers following multiple extreme melting seasons
361 (Culberg et al., 2021). Similar to ice slabs, the formation of spatially coherent melt layers reduces the pore
362 space within the upper snow and firn layers and may also facilitate lateral meltwater flow with minimum
363 vertical percolation into the deeper firn layers, thus enhancing meltwater run-off from significantly higher
364 elevations downslope towards the periphery on accelerated time scales. The formation of spatially coherent
365 melt layers overlying deeper perennial firn aquifers (e.g., Fig. 3a) will limit or terminate gravity-driven
366 meltwater drainage and seasonal recharging (Fountain and Walder, 1998), which may eventually
367 completely refreeze stored meltwater into decimeters thick solid-ice layers overlying deeper glacial ice.
368 Spatially coherent melt layers are exceptionally bright in AR radargrams (e.g., Fig 3a). The large dielectric
369 contrast between the spatially coherent melt layer and the overlying, underlying, and interior snow and firn
370 layers results in high reflectivity at the interfaces. However, electromagnetic energy still propagates
371 downward through the high reflectivity layer into the deeper firn layers. Culberg et al., 2021) recently
372 demonstrated mapping the extent of the spatially coherent melt layer formed following the anomalous 2012
373 melting season (Nghiem et al., 2012) via AR (Figs. 1c; 2).



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Figure 3

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AR radargram profile (Rodríguez-Morales et al, 2014) (a) along perennial firn aquifer transect A-B (red line, Figs. 1; 2a) that was collected on 22 April 2017, and (b) ice slab transect C-D (orange line, Figs. 1; 2b) that was collected on 5 May 2017. (c) The corresponding perennial firn aquifer transect A-B elevation profile (red line), and ice slab transect C-D elevation profile (orange line). The exceptionally bright upper surface-parallel reflector in (a) is interpreted as a spatially coherent melt layer that formed following the 2015 melting season. The bright lower reflector in (a) is interpreted as the upper surface of meltwater stored within a perennial firn aquifer. Thick dark surface-parallel regions of low-reflectivity in (b) are interpreted as ice slabs. Alternating sequences of bright and dark surface-parallel reflectors in (b) are interpreted as seasonal snow accumulation layers. A first maximum after maximum gradient re-tracker is used to identify the surface return in each profile. Each profile is flattened so that the depth axis is measured relative to the local elevation. Corresponding elevation profiles in (c) are calculated by subtracting the radar-measured flight clearance over the ice sheet from the aircraft's global positioning system altitude measurements that were coincidentally collected along each transect.



389 AR and MCoRDS (Rodriguez-Morales et al, 2014) were flown over the GrIS on a P-3 aircraft in
390 April and May between 2010 and 2017. The AR instrument operates at a center frequency of 750 MHz with
391 a bandwidth of 300 MHz, resulting in a range resolution in firn of 0.53 m (Lewis et al., 2015). The collected
392 data have an along-track resolution of ~30 m with 15 m spacing between traces in the final processed
393 radargrams. At a nominal flight altitude of 500 m above the ice sheet surface, the cross-track resolution
394 varies between 20 m for a smooth surface, to 54 m for a rough surface with no appreciable layover. The
395 MCoRDS instrument operated at three different frequency configurations: (1) a center frequency of 195
396 MHz with a bandwidth of 30 MHz (2010-2014, 2017, 2018), (2) a center frequency of 315 MHz with a band
397 width of 270 MHz (2015), and (3) a center frequency of 300 MHz with a bandwidth of 300 MHz (2016). The
398 vertical range resolution in firn for each of these frequency configurations is 5.3 m, 0.59 m, and 0.53m,
399 respectively (CReSIS, 2016). The collected data have an along-track resolution of ~25 m with 14 m spacing
400 between traces in the final processed radargrams. At the same nominal flight altitude of 500 m, the cross-
401 track resolution varies between 40 m for a smooth surface in the highest bandwidth configuration, to 175
402 m for a rough surface with no appreciable layover in the lowest bandwidth configuration.

403 The multi-year calibration technique uses perennial firn aquifer detections previously identified
404 along OIB flight lines via AR (2010-2014) and MCoRDS (2015-2017) radargram profiles and the
405 methodology described in Miège et al. (2016). Bright lower reflectors that undulate with the local
406 topographic gradient underneath which reflectors are absent in the percolation facies are interpreted as the
407 upper surface of meltwater stored within perennial firn aquifers (e.g., Fig. 3a). The large dielectric contrast
408 between refrozen and water-saturated firn layers results in high reflectivity at the interface. However, the
409 presence of meltwater increases attenuation, limiting the downward propagation of electromagnetic energy
410 through the water-saturated firn layer. The total number of AR derived perennial firn aquifer detections is
411 ~325,000, corresponding to a total extent of ~98 km². The analysis assumes a smooth surface, which is
412 typical of much of the percolation facies, and a grid cell size of 15 m x 20 m. The total number of MCoRDS-
413 derived perennial firn aquifer detections is ~142,000, corresponding to a total extent of ~80 km². This also
414 assumes a smooth surface, and a grid cell size of 14 m x 40 m. The combined total number of grid cells
415 (~467,000) and total extent (~178 km²) is significantly larger than the total number of MCoRDS-derived grid
416 cells (~78,000) and total extent (~44 km²) calculated for 2016 (Miller et al., 2020). Perennial firn aquifer
417 detections are mapped in western, southern, and south and central eastern Greenland as well as the
418 Maniitsoq and Flade Isblink Ice Caps (Figs. 1c; 2a). We project AR- and MCoRDS-derived perennial firn
419 aquifer detections on the NH EASE-Grid 2.0 at an rSIR grid cell spacing of 3.125 km. Each rSIR grid cell
420 has an extent of ~10 km². The total number of rSIR grid cells with at least one perennial firn aquifer detection
421 is ~800, corresponding to a total extent of ~8000 km². However, given the limited AR and MCoRDS grid
422 cell coverage, less than ~1% of the rSIR grid cell extent has radargram coverage. As compared to the total
423 number of MCoRDS-derived perennial firn aquifer detections (~780) calculated for 2016 (Miller et al., 2020),
424 the total number of rSIR grid cells with at least one detection is only increased by ~20 for the multi-year
425 calibration technique, corresponding to an increased total extent of ~200 km².



426 We also use ice slab detections previously identified along OIB flight lines via AR (2010-2014)
 427 radargram profiles and the methodology described in McFerrin et al. (2019) in the multi-year calibration
 428 technique. Thick dark surface-parallel regions of low-reflectivity in the percolation facies are interpreted as
 429 ice slabs (Fig. 3b). The large dielectric contrast between ice slabs and the overlying and underlying snow
 430 and firn layers results in high reflectivity at the interfaces. However, electromagnetic energy is not scattered
 431 or absorbed within the homogeneous ice slab, it instead propagates downward through the layer and into
 432 the deeper firn layers. The total number of AR-derived ice slab detections is ~505,000, corresponding to a
 433 total extent of ~283 km². Ice slab detections are mapped in western, central and north eastern, and northern
 434 Greenland as well as the Flade Isblink Ice Cap (Figs. 1c; 2b). We project the AR-derived ice slab detections
 435 on the NH EASE-Grid 2.0 at an rSIR grid cell spacing of 3.125 km. The total number of rSIR grid cells with
 436 at least one ice slab detection is ~2000, corresponding to a total extent of ~20,000 km². However, less than
 437 ~2% of the rSIR grid cell extent has radargram coverage.

438 We detect perched firn aquifer areas by comparing the AR- and MCoRDS-derived perennial firn
 439 aquifer and ice slab detections projected on the NH EASE-Grid 2.0 and then identify overlapping rSIR grid
 440 cells. The total number of AR-derived perched firn aquifer detections is ~75,000, corresponding to a total
 441 extent of ~23 km². The total number of MCoRDS-derived perched firn aquifer detections is ~20,
 442 corresponding to a near-negligible extent (~0.006 km²). Perched firn aquifer detections are mapped in
 443 western, and central eastern Greenland as well as the Flade Isblink Ice Cap (Figs. 1c; 2b).

444 The total number of rSIR grid cells with at least one perched firn aquifer detection is ~200,
 445 corresponding to a total extent of ~2000 km². However, similar to the other sub-facies, less than ~1% of
 446 the rSIR grid cell extent has radargram coverage. The total number of AR- and MCoRDS-derived perennial
 447 firn aquifer, ice slab, and perched firn aquifer detections that we project on three separate NH EASE-Grids
 448 2.0, the associated total number of rSIR grid cells that we use in the calibration of our adapted empirical
 449 algorithm, and the coverage of detections and rSIR grid cells over each of the three sub-facies within the
 450 broader percolation facies are summarized in Table 1.

451

452 **Table 1.** *The total number of airborne ice penetrating radar survey detections (2010-2017), the associated*
 453 *total number of rSIR grid cells, and the coverage of detections and rSIR grid cells over perennial firn aquifer,*
 454 *ice slab, and perched firn aquifer areas.*

	Detections	Coverage (km ²)	rSIR Grid Cells	Coverage (km ²)
Perennial Firn Aquifers	~467,000	~178	~80	~8000
Ice Slabs	~505,000	~283	~2000	~20,000
Perched Firn Aquifers	~75,000	~23	~200	~2000

455

456



457 **2.4 Empirical Algorithm**

458 **2.4.1 Greenland's Ice Facies**

459 Greenland's ice facies (i.e., dry snow facies - percolation facies - wet snow facies - ablation facies) were
460 first described in detail by Benson et al., (1960), and were shown to represent the GrlS's response to
461 climate. Evolution of the boundaries of Greenland's ice facies are often used as an indicator of climate
462 change. Early studies using field-based (Jezek et al., 1994; Zabel et al., 1995), airborne (Swift et al., 1985;
463 Bindschadler et al., 1987; Rignot et al., 1993; Jezek et al., 1993), and satellite (Fahnestock et al., 1993;
464 Long and Drinkwater, 1994; Parrington, 1998) synthetic aperture radars and radar scatterometers operating
465 at frequencies between Ku-band (13 GHz) and P-band (0.4 GHz) have demonstrated the exceptional
466 capabilities of microwave sensors for mapping Greenland's ice facies. Early airborne studies using C-band
467 microwave radiometry (Swift et al., 1985), and more recent studies using L-band microwave radiometry
468 (Jezek et al. 2018) have demonstrated similar capabilities. In this study, we extend these capabilities to
469 include satellite L-band microwave radiometry. We delineate the boundaries of the percolation facies
470 relative to the adjacent dry snow facies (i.e., where negligible seasonal surface melting occurs) and wet
471 snow facies (i.e., where snow layers are fully water-saturated during the melting season and subsequently
472 refreeze as superimposed ice overlying deeper glacial ice). And, we further identify sub-facies (i.e.,
473 perennial firn aquifer, ice slabs, and perched firn aquifers) within the broader percolation facies that are
474 currently experiencing rapid expansion (McFerrin et al., 2019; Culberg et al., 2021) as Greenland's climate
475 continues to warm (Hanna et al., 2013; Cullather et al., 2020) and seasonal surface melting increases in
476 extent, intensity, and duration (Steffen et al., 2004; Tedesco e al., 2008; Tedesco et al., 2011; Nghiem et
477 al., 2012; Tedesco et al., 2016; Tedesco and Fettweis, 2020; Tedesco and Fettweis, 2020). Higher
478 frequency microwave sensors provide shallower penetration depths, and an increased sensitivity to snow
479 grain size, layering, embedded ice structures (Long and Drinkwater, 1994; Drinkwater et al., 2001) and
480 stored meltwater (Jezek et al., 1993; Miller, 2019) within the upper snow and firn layers of the percolation
481 facies. Lower frequencies provide deeper penetration depths and a range of sensitivities to embedded ice
482 structures (Jezek et al., 1993; Jezek et al., 2018) and stored meltwater (Miller et al., 2020) in the deeper
483 firn layers.

484

485 **2.4.2 Temporal L-band signatures over the percolation facies**

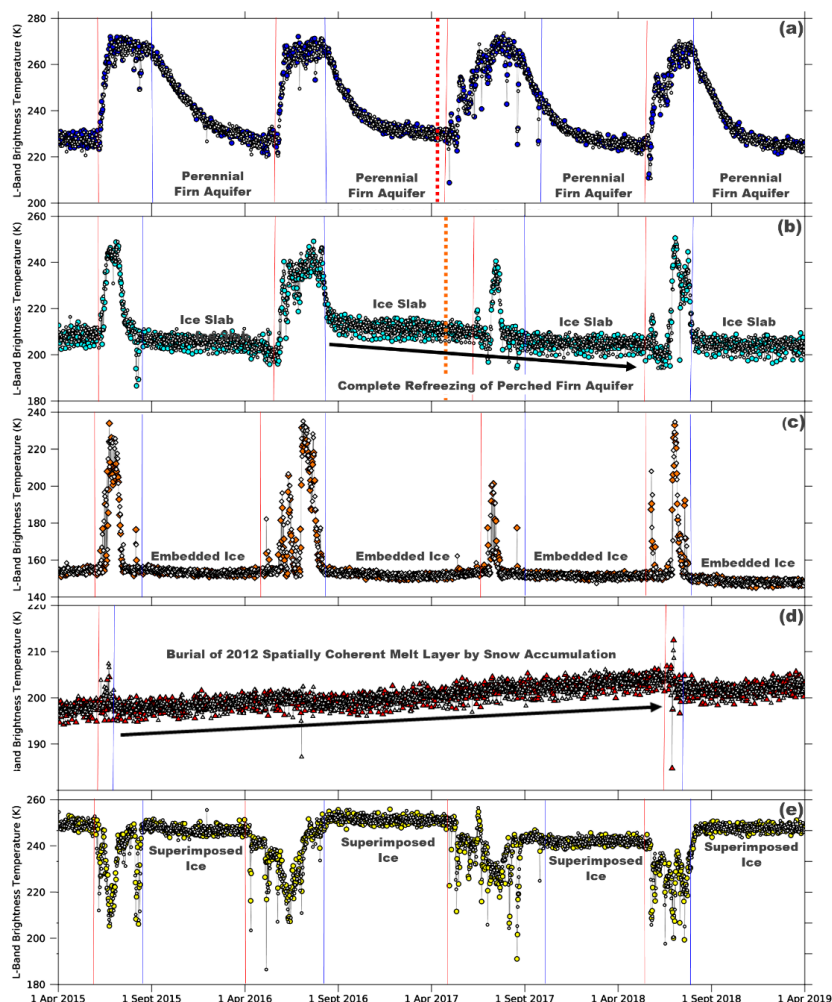
486 Microwave brightness temperature (T^B) expresses the satellite-observed magnitude of thermal emission
487 and is influenced by the observation geometry as well as the dielectric and geophysical properties of the
488 ice sheet (Ulaby et al., 2014). The most significant geophysical property influencing T^B is the volumetric
489 fraction of meltwater within the snow and firn pore space (Mätzler and Hüppi, 1989). During the melting
490 season, the upper snow and firn layers of the percolation facies are saturated with large volumetric fractions
491 of meltwater that percolates vertically into the deeper firn layers (Benson, 1960; Humphrey et al., 2012).
492 Increases in the volumetric fraction of meltwater results in rapid relative increases in the imaginary part of



493 the complex dielectric constant (Tiuri et al., 1984), with corresponding increases in T^B . This increase is
494 attributed to a decrease in volume scattering, and penetration depth. The L-band penetration depth can
495 rapidly decrease from ~tens to hundreds of meters, to less than ~a meter, dependent on the local snow
496 and firn conditions, and englacial firn hydrological features. Surface and subsurface water-saturated snow
497 and firn layers and embedded ice structures subsequently refreeze. During the freezing season, decreases
498 in the volumetric fraction of meltwater results in rapid relative decreases in the imaginary part of the complex
499 dielectric constant, with corresponding decreases in T^B . This increase is attributed to an increase in volume
500 scattering, and penetration depth. The L-band penetration depth increases back to ~tens to hundreds of
501 meters on variable time scales.

502 We analyze melting and freezing seasons in temporal L-band signatures exhibited in T_V^B time series
503 (1 April 2015 - 31 March 2019) over and near AR- and MCoRDS-derived perennial firn aquifer, ice slab,
504 and perched firn aquifer detections projected on NH EASE-Grids 2.0 (Fig. 4). We project ice surface
505 temperature data calculated using thermal infrared brightness temperature collected by the Moderate
506 Resolution Imaging Spectroradiometer (MODIS) on the Terra and Aqua satellites (i.e., Hall et al., 2012) on
507 coincident NH EASE-Grids 2.0 at a 3.125 km rSIR grid cell spacing. We then derive melt onset and surface
508 freeze-up dates (2015-2019) for each rSIR grid cell using the methodology described in Miller et al., (2020).
509 We set a threshold of ice surface temperature $>-1^\circ\text{C}$ for meltwater detection (Nghiem et al., 2012),
510 consistent with the $\pm 1^\circ\text{C}$ accuracy of the ice surface temperature data. For temperatures that are close to
511 0°C , ice surface temperatures are closely compatible with contemporaneous NOAA near-surface air
512 temperature data (Shuman et al., 2014). Melt onset and surface freeze-up dates are overlaid on T_V^B time
513 series to partition the melting and freezing seasons. Melt onset dates occur between ~April and July, and
514 surface freeze-up dates occur between ~July and September. The melting season increases in duration
515 moving downslope from the dry snow facies, and ranges from a single day in the highest elevations (>2500
516 m) of the percolation facies, to ~150 days in the ablation facies. Similarly, the associated freezing season
517 decreases in duration moving downslope and ranges from between ~215 days and 365 days.

518 Over perennial firn aquifer areas (e.g., Figs. 1c; 2a; 4a), T_V^B is radiometrically warm during the
519 melting season. Vertically percolating meltwater and gravity-driven meltwater drainage seasonally
520 recharges perennial aquifers at depth (Fountain and Walder et al., 1998). Maximum values range from
521 between ~200 K and 275 K during seasonal surface melting. Temporal L-band signatures exhibit increases
522 on time scales of ~days to weeks following the melt onset date, and melting seasons range from between
523 ~75 and 100 days. T_V^B remains radiometrically warm during the freezing season as a result of latent heat
524 continuously released by the slow refreezing of the deeper firn layers that are saturated with large
525 volumetric fractions of meltwater (Miller et al, 2020). Minimum values range from between ~180 K and 250
526 K following the surface freeze-up date. L-band emissions from the radiometrically warm upper snow and
527 firn layers decrease during the freezing season as embedded ice structures slowly refreeze at increased
528 depths below the ice sheet surface (Miller et al., 2020). Temporal L-band signatures exhibit exponential
529 decreases on time scales of ~months that approach and sometimes achieve relatively stable T_V^B values,



530

531 **Figure 4**

532 *Temporal L-band signatures that alternate morning (white symbols) and evening (colored symbols) orbital*
533 *pass interval enhanced-resolution T_V^B generated using observations collected over the GrIS by the*
534 *microwave radiometer on the SMAP satellite (Brodzik et al., 2019) over (a) perennial firn aquifer area (blue*
535 *circles; Figs. 2a; 3a), (b) perched firn aquifer area (cyan circles; Figs. 2b; 3b), (c) percolation facies area*
536 *(orange diamonds; Fig 2b), (d) high-elevation (~2500 m.a.s.l.) spatially coherent melt layer area (red*
537 *triangles; Fig. 2a), and (e) superimposed ice area (yellow circles; Fig. 2b). Melt onset (red lines) and surface*
538 *freeze-up (blue lines) dates are derived from thermal infrared T^B collected by MODIS on the Terra and*
539 *Aqua satellites (Hall et al, 2012). AR radargram profile along perennial firn aquifer transect A-B (red dashed*
540 *line; Figs. 1; 2a; 3a) that was collected on 22 April 2017, and ice slab transect C-D (orange dashed line;*
541 *Figs. 1; 2b; 3b) that was collected on 5 May 2017.*



542 and freezing seasons range from between ~265-290 days. T_V^B often decreases by more than ~50 K during
543 the freezing season (e.g., Fig. 4a), representing the descent of the upper surface of stored meltwater by
544 ~tens of meters (Miège et al., 2016).

545 Over ice slab and perched firn aquifer areas (e.g., Figs. 1c; 2b; 5b), T_V^B is typically radiometrically
546 colder than over perennial firn aquifer areas during the melting season. The presence of dense low-
547 permeability solid-ice layers (e.g., Fig. 3b) reduces the snow and firn pore space available to store seasonal
548 meltwater at depth. Meltwater may alternatively run-off downslope towards the wet snow facies. Maximum
549 values range from between ~170 K and 260 K during seasonal surface melting. Temporal L-band signatures
550 exhibit increases on time scales of ~days to weeks following the melt onset date, and melting seasons
551 range from between ~60 and 90 days. T_V^B is also typically radiometrically colder than over perennial firn
552 aquifer areas during the freezing season as a result of the absence of meltwater stored at depth (i.e. ice
553 slab areas), or the presence of limited volumetric fractions of meltwater stored at depth in shallow water-
554 saturated firn layers (i.e. perched firn aquifer areas). Minimum values range from between ~130 K and 240
555 K following the surface freeze-up date. Temporal L-band signatures exhibit exponential decreases on time
556 scales of ~weeks to months that often achieve relatively stable T_V^B values, and freezing seasons range from
557 between ~275-305 days. Exponentially decreasing temporal L-band signatures sometimes transition to
558 linearly decreasing on time scales of ~years following the surface freeze-up date (e.g., between
559 ~September 2016 and May 2018 in Fig. 4b). We infer this indicates the formation and subsequent refreezing
560 of a shallow perched firn aquifer on top of a buried ice slab or other semi-impermeable layer. As compared
561 to the large T_V^B decreases in percolation facies areas, T_V^B decreases over perched firn aquifer areas are as
562 small as ~a few K annually, which represents the descent of the upper surface of stored meltwater by
563 ~meters rather than by ~tens of meters.

564 Over other percolation facies areas, where seasonal meltwater is fully refrozen and stored
565 exclusively as embedded ice (e.g., Fig. 4c), T_V^B is typically radiometrically colder than over perennial firn
566 aquifer, ice slab, and perched firn aquifer areas during the melting season. Maximum values range from
567 between ~150 K and 200 K during seasonal surface melting. Temporal L-band signatures exhibit increases
568 on time scales of ~days to weeks following the melt onset date, and melting seasons range from between
569 ~1 and 60 days. T_V^B is also typically radiometrically cold during the freezing season. Minimum values range
570 from between ~130 K and 180 K following the surface freeze-up date. Temporal L-band signatures exhibit
571 exponential decreases on time scales of ~days to weeks and achieve relatively stable T_V^B values, and
572 freezing seasons range from between ~305-364 days. However, over the highest elevations (> ~2500
573 m.a.s.l.) of the percolation facies approaching the dry snow line, where seasonal surface melting and the
574 formation of embedded ice structures is limited, T_V^B remains radiometrically warm during the freezing
575 season. Minimum values range from between ~180 K and 220 K following the surface freeze-up date. We
576 infer T_V^B decreases, sometimes step-responses exceeding ~10 K, that follow the surface freeze-up date
577 (e.g., between April 2018 and September 2018 in Fig. 4c) are a result of an increase in volume scattering
578 from newly formed embedded ice structures within a spatially coherent melt layer. We also infer that



579 temporal L-band signatures that increase several K on time scales of ~years (e.g., between ~April 2015
580 and April 2018 in Fig. 4c) indicate the burial of spatially coherent melt layers formed following the 2010,
581 2012, 2015, and 2018 melting seasons by snow accumulation.

582 Exponentially decreasing temporal L-band signatures transition smoothly between perennial firn
583 aquifer, ice slab, perched firn aquifer, and other percolation facies areas – there are no distinct temporal L-
584 band signatures that delineate boundaries between these sub-facies. Boundary transitions between other
585 facies, however, are delineated both above and below the percolation facies. Over the dry snow facies
586 (e.g., Fig. 4d), T_V^B is radiometrically warm during the melting and freezing seasons. Values range from
587 between ~200 K and 240 K. While T_V^B is known to be relatively stable in the dry snow facies, temporal L-
588 band signatures that increase on time scales of ~years are observed throughout this region at elevations
589 as high as Summit Station (~3200 m.a.s.l.), similar to those observed in the highest elevations (> ~2500
590 m.a.s.l.) of the percolation facies. We infer increasing temporal L-band signatures indicate the burial of the
591 spatially coherent melt layer formed following the anomalous 2012 melting season (Nghiem et al., 2012) by
592 snow accumulation (Culberg et al., 2021). Over the wet snow facies (e.g., Fig. 4e), where seasonal
593 meltwater is fully refrozen and stored as superimposed ice, T_V^B is radiometrically warm during the melting
594 season. Maximum values range from between ~230 K and 250 K during seasonal surface melting. As
595 compared to the percolation facies, where temporal L-band signatures exhibit rapid increases following
596 melt onset, temporal L-band signatures reverse and exhibit decreases on time scales of ~days to weeks,
597 and melting seasons that range between ~90-120 days. We infer these reversals are the result of high
598 reflectivity and attenuation at the fully water-saturated snow layer and/or at the wet, rough superimposed
599 ice-air interface. Meltwater runs-off superimposed ice downslope towards the ablation facies in the wet
600 snow facies. T_V^B remains radiometrically warm during the freezing season. Minimum values range from
601 between ~230 K and 250 K following seasonal surface melting. Temporal L-band signatures exhibit
602 increases on time scales of ~days that achieve relatively stable T_V^B values, and freezing seasons range
603 from between ~245 and 275 days.

604 The MODIS-derived total number of days in the melting and freezing seasons estimated from melt
605 onset and surface freeze-up dates, the SMAP-derived maximum and minimum vertically-polarized L-band
606 brightness temperature, and the time scales of exponential decrease following the surface freeze-up date
607 estimated for each T_V^B time series for rSIR grid cells over perennial firn aquifer, ice slab, perched firn aquifer,
608 and other percolation facies areas as well as for the dry snow facies, and the wet snow facies are
609 summarized in Table 2.

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616 **Table 2.** The MODIS-derived total number of days in the melting and freezing seasons (2015-2019), the
 617 SMAP-derived maximum vertically-polarized L-band brightness temperature ($T_{V,max}^B$), the minimum
 618 vertically-polarized L-band brightness temperature ($T_{V,min}^B$), and the time scale scales of exponential
 619 decrease following the surface freeze-up date (1 April 2015 - 31 March 2019) for perennial firn aquifer, ice
 620 slab, perched firn aquifer, and other percolation facies areas as well as for the dry snow facies and the wet
 621 snow facies.

	Melting Season (days)	Freezing Season (days)	$T_{V,max}^B$ (K)	$T_{V,min}^B$ (K)	Exponential Decrease (time scale)
Perennial Firn Aquifers	~75 - 100	~265 - 290	~200 - 275	~180 - 250	~weeks - months
Ice Slabs / Perched Firn Aquifers	~60 - 90	~275 - 305	~170 - 260	~130 - 240	~days - Weeks
Percolation Facies	~1 - 60	~305 - 364	~150 - 200	~130 - 220	~days
Dry Snow Facies	-	365	~200 - 240	~200 - 240	-
Wet Snow Facies	~90 - 120	~245 - 275	~230 - 250	~230 - 250	-

622

623 **2.4.3 L-band geophysical-brightness temperature model**

624 Based on our analysis of $T_{V,max}^B$ and $T_{V,min}^B$ values in temporal L-band signatures over the percolation facies,
 625 we derive a ‘firn saturation’ parameter using the simple two-layer L-band geophysical-brightness
 626 temperature model described in Ashcraft and Long (2006). The firn saturation parameter is similar to the
 627 ‘melt intensity’ parameter derived in Hicks and Long (2011) that uses enhanced resolution vertically-
 628 polarized Ku-band radar backscatter imagery (2003) collected by the SeaWinds radar scatterometer that
 629 was flown in tandem on NASA’s Quick SCATterometer (QuikSCAT) satellite (Tsai et al., 2000) and JAXA’s
 630 Advanced Earth Observing Satellite 2 (ADEOS-II) (Freilich et al., 1994). We use the firn saturation
 631 parameter to estimate the maximum seasonal volumetric fraction of meltwater within the saturated upper
 632 snow and firn layers of the percolation facies using $T_{V,max}^B$ and $T_{V,min}^B$ values extracted from T_V^B time series
 633 (1 April 2015 - 31 March 2019). We calculate the firn saturation parameter for each rSIR grid cell within the
 634 ice sheet-masked extent of the GrIS as part of our adapted empirical algorithm (see Section 2.4.5).

635 We first describe the geophysical model as follows. We assume a base layer underlying a water-
 636 saturated firn layer with a given depth and volumetric fraction of meltwater. Each of the layers is
 637 homogenous. We next describe T_V^B from the geophysical model (Eq. 1). The ice sheet is discretely layered
 638 (i.e., two-layers; the base layer, and the water-saturated firn layer) to calculate T_V^B at an oblique incidence
 639 angle. Emissions from the base layer are a function of both the macroscopic roughness and the dielectric
 640 properties of the layer. They occur in conjunction with volume scattering at depth, and are locally dependent



641 on englacial firn hydrological features, including embedded ice structures, spatially coherent melt layers,
642 ice slabs, and perennial and perched firn aquifers. Reflectivity at depth (i.e., at the base layer-water-
643 saturated firn layer interface), and at the ice sheet surface (i.e., at the water-saturated firn layer-air interface)
644 is neglected. The contribution from each layer is individually calculated.

645 The two-layer L-band geophysical-brightness temperature model is represented analytically by
646

$$647 T_{V,max}^B = T(1 - e^{-\kappa_e d \sec \theta}) + T_{V,min}^B e^{-\kappa_e d \sec \theta}, \quad (\text{Eq. 1})$$

648

649 where $T_{V,max}^B$ is the maximum vertically-polarized L-band brightness temperature at the ice sheet
650 surface, $T_{V,min}^B$ is the minimum vertically-polarized L-band brightness temperature emitted from the base
651 layer, T is the physical temperature of the water-saturated firn layer, θ is the transmission angle, κ_e is the
652 extinction coefficient, and d is depth.

653 We invert Eq. 1 and solve for the firn saturation parameter (ξ)

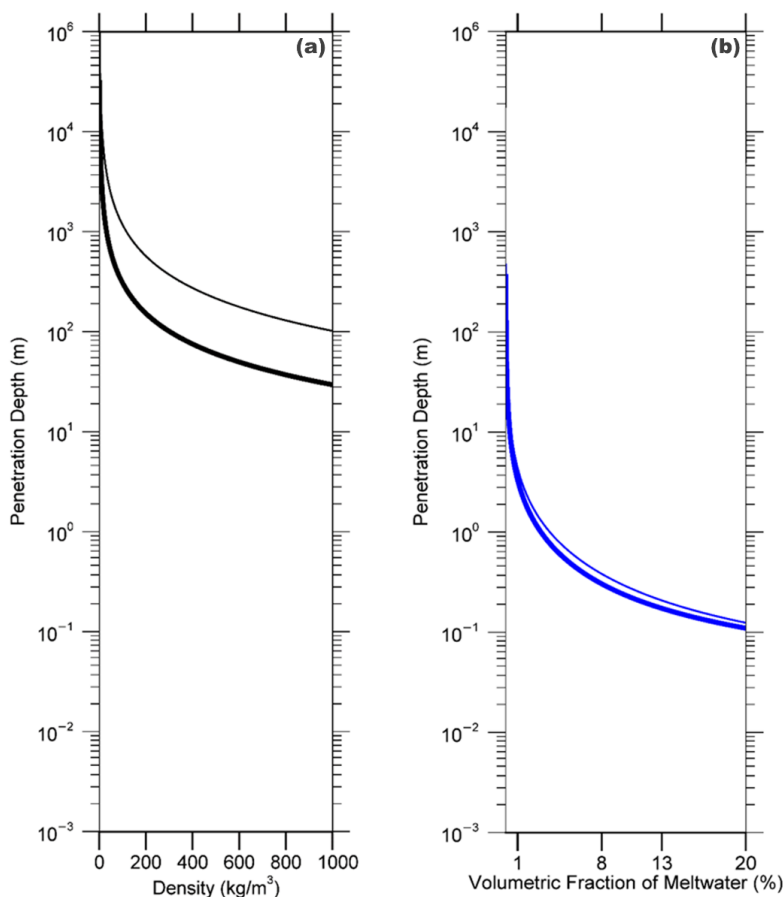
654

$$655 \xi = \ln \left(\frac{T_{V,max}^B - T}{T_{V,min}^B - T} \right) \cos \theta, \quad (\text{Eq. 2})$$

656

657 where $\xi = \kappa_e d$. The maximum vertically-polarized L-band brightness temperature asymptotically approaches
658 the physical temperature of the water-saturated firn layer as the extinction coefficient and the depth of the
659 water-saturated firn layer increases. The extinction coefficient is defined as the sum of the Raleigh
660 scattering coefficient (κ_s) and the absorption coefficient (κ_a). For water-saturated firn, absorption dominates
661 over scattering, and increases in the extinction coefficient are controlled by the volumetric fraction of
662 meltwater (m_v). We assume that thicker water-saturated firn layers with larger volumetric fractions of
663 meltwater generate higher firn saturation parameter values. However, the thickness of the water-saturated
664 firn layer is limited by the L-band penetration depth. Theoretical L-band penetration depths calculated for a
665 water-saturated firn layer range from between ~10 m for small volumetric fractions of meltwater ($m_v < 1\%$),
666 and ~1 cm for large volumetric fractions of meltwater ($m_v = 20\%$) (Fig. 5). Large volumetric fractions of
667 meltwater results in high reflectivity and attenuation at the interface between water-saturated firn layers and
668 the overlying refrozen firn layers, and between glacial ice or a semi-impermeable layer and the overlying
669 water-saturated firn layers, and a radiometrically cold firn layer (e.g., Fig 5e).

670



671

672 **Figure 5**

673 *Theoretical L-band penetration depths for (a) refrozen, and (b) water-saturated firn. Penetration depths*
674 *($\frac{1}{\kappa_s + \kappa_a}$) are calculated as a function of the Raleigh scattering coefficient (κ_s ; Eq. 8) and the absorption*
675 *coefficient (κ_a ; Eq. 10), which are functions of the dielectric and geophysical properties of the GrlS. The*
676 *complex dielectric constant is calculated using the empirically derived models described in Tiuri et al.,*
677 *(1984). Refrozen firn penetration depths are calculated as a function of firn density (ρ_{firn}), and the curves*
678 *are plotted for snow grain radii (r) set to $r = 0.5$ mm (upper curve), and $r = 4$ mm (lower curve). Water-*
679 *saturated firn penetration depths are calculated as a function of the volumetric fraction of meltwater (m_v),*
680 *and the curves are plotted for firn density set to $\rho_{firn} = 400$ kg/m³ (upper curve), and $\rho_{firn} = 917$ kg/m³ (lower*
681 *curve). Given the complexity of modeling embedded ice structures, they are excluded from the penetration*
682 *depth calculation. Increases in the volumetric fraction of embedded ice in the firn will result in an increase*
683 *in volume scattering, which will decrease and compress the distance between the penetration depth curves*
684 *for both refrozen and water-saturated firn.*



685 **2.4.4 Continuous logistic model**

686 We adapt our previously developed empirical algorithm to map the extent of Greenland's perennial firn
 687 aquifers (Miller et al., 2020) to also map the extent of ice slab and perched firn aquifer areas. The empirical
 688 algorithm is derived from the continuous logistic model, which is based on a differential equation that models
 689 the decrease in physical systems as a function of time using a set of sigmoidal curves. These curves begin
 690 at a maximum value with an initial interval of decrease that is approximately exponential. Then, as the
 691 function approaches its minimum value, the decrease slows to approximately linear. Finally, as the function
 692 asymptotically reaches its minimum value, the decrease exponentially tails off and achieves stable values.
 693 We use the continuous logistic model to parametrize the refreezing rate within the saturated upper snow
 694 and firn layers of the percolation facies using T_V^B time series (1 April 2015 - 31 March 2019) that are
 695 partitioned using $T_{V,max}^B$ and $T_{V,min}^B$ values. We calculate the refreezing rate for each rSIR grid cell within the
 696 percolation facies extent as part of our adapted empirical algorithm (see Section 2.4.5).

697 The continuous logistic model is described by a differential equation known as the logistic equation
 698

$$699 \quad \frac{dx}{dt} = \zeta x(1 - x) \quad (\text{Eq. 3})$$

700

701 that has the solution

702

$$703 \quad x(t) = \frac{1}{1 + \left(\frac{1}{x_0} - 1\right)e^{-\zeta t}}, \quad (\text{Eq. 4})$$

704

705 where x_0 is the function's initial value, ζ is the function's exponential rate of decrease, and t is time. The
 706 function $x(t)$ is also known as the sigmoid function. We use the sigmoid function to model the exponentially
 707 decreasing temporal L-band signatures observed over the percolation facies as a set of decreasing
 708 sigmoidal curves.

709 We first normalize T_V^B time series for each rSIR grid cell

710

$$711 \quad T_{V,N}^B(t) = \frac{T_V^B(t) - T_{V,min}^B}{T_{V,max}^B - T_{V,min}^B}, \quad (\text{Eq. 5})$$

712

713 where $T_{V,min}^B$ is the minimum vertically-polarized L-band brightness temperature, and $T_{V,max}^B$ is the maximum
 714 vertically-polarized L-band brightness temperature. We then apply the sigmoid fit

715

$$716 \quad T_{V,N}^B(t \in [t_{max}, t_{min}]) = \frac{1}{1 + \left(\frac{1}{T_{V,N}^B(t_{max})} - 1\right)e^{-\zeta t}}. \quad (\text{Eq. 6})$$

717



718 $T_{V,N}^B(t \in [t_{max}, t_{min}])$ is the normalized vertically-polarized L-band brightness temperature on the time
719 interval $t \in [t_{max}, t_{min}]$, where t_{max} is the time the function achieves a maximum value, and t_{min} is the
720 time the function achieves a minimum value. The initial normalized vertically-polarized L-band brightness
721 temperature ($T_{V,N}^B(t_{max})$) is the function's maximum value. The final normalized vertically-polarized L-band
722 brightness temperature ($T_{V,N}^B(t_{min})$) is the function's minimum value. The function's exponential rate of
723 decrease represents the refreezing rate parameter (ζ). An example set of simulated sigmoidal curves is
724 shown in Fig. 6.

725

726 **2.4.5 SMAP-derived perennial firn aquifer, ice slab, and perched firn aquifer maps**

727 Our adapted empirical algorithm uses ice sheet-masked SMAP enhanced-resolution T_V^B imagery over the
728 GrIS that alternates morning and evening orbital pass observations annually, beginning and ending just
729 prior to melt onset. Our algorithm is implemented in two steps: (1) mapping the extent of the percolation
730 facies using the firn saturation parameter derived from the L-band geophysical-brightness temperature
731 model (see Section 2.4.3), and (2) mapping the extent of perennial firn aquifer, ice slab, and perched firn
732 aquifer areas over the percolation facies using the continuous logistic model (see Section 2.4.4) we
733 calibrate using airborne ice-penetrating radar detections projected on three separate NH EASE-Grids 2.0
734 (see Section 2.2).

735 Using Eq. 2, we first set a threshold for the firn saturation parameter (ξ_T) defined by the relationship
736

$$737 \xi_T = (\kappa_s + \kappa_a)d \leq \xi . \quad (\text{Eq. 7})$$

738

739 We calculate the Raleigh scattering coefficient (κ_s) in Eq. 7 using

740

$$741 \kappa_s = N_d \frac{8}{3} k_o^4 r^6 \left| \frac{\epsilon_r - 1}{\epsilon_r + 2} \right|^2 , \quad (\text{Eq. 8})$$

742

743 where N_d is the particle density, k_o is the wave number of the background medium of air, r is the snow
744 grain radius set to $r=2$ mm, and ϵ_r is the complex dielectric constant. The particle density is defined by

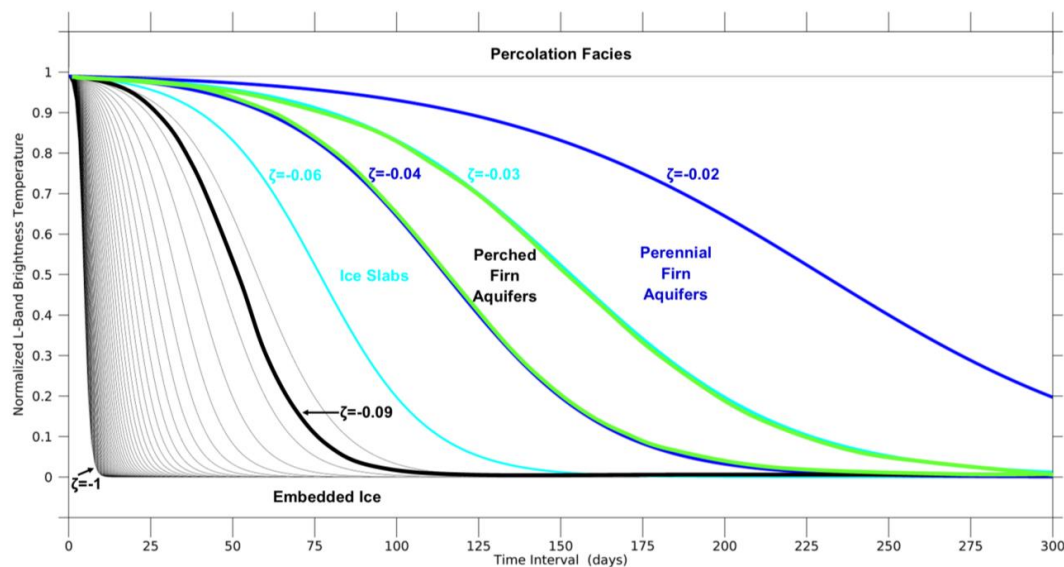
745

$$746 N_d = \frac{\rho_{firn}}{\rho_{ice}} \frac{1}{\frac{4}{3}\pi r^3} , \quad (\text{Eq. 9})$$

747

748 where ρ_{firn} is firn density, which we set to $\rho_{firn}=400$ kg/m³, and ρ_{ice} is ice density, which we set to $\rho_{ice}=917$
749 kg/m³. Our grain radius and firn density estimates are consistent with measurements within the upper snow
750 and firn layers of the percolation facies of south eastern Greenland at the Helheim Glacier field site (Fig.

751



752

753 **Figure 6**

754 *Example set of simulated sigmoidal curves that represent our model of the exponentially decreasing*
755 *temporal L-band signatures predicted over the percolation facies. The initial normalized vertically-polarized*
756 *L-band brightness temperature was fixed at a value of $T_{V,N}^B(t_{max}) = 0.99$, and the time interval was set to a*
757 *value of $t \in [t_{max}, t_{min}] = 300$ observations. The refreezing rate parameter was set to values between $\zeta =$*
758 *$[-1, 0]$ incremented by steps of 0.02. The blue lines correspond to the interval $\zeta \in [-0.04, -0.02]$ and*
759 *produce curves similar to those observed over perennial firn aquifer areas. The cyan lines correspond to*
760 *the interval $\zeta \in [-0.06, -0.03]$ and produce curves similar to those observed over ice slab areas. The green*
761 *lines correspond to the interval $\zeta \in [-0.04, -0.03]$ and produce curves similar to those observed over*
762 *perched firn aquifer areas. The black line is the observed lower bound ($\zeta = -0.09$) of the refreezing rate*
763 *parameter of partitioned T_V^B time series (1 April 2015 - 31 March 2019) iteratively fit to the sigmoid function*
764 *(see Section 3).*

765



766 2a; blue circle; Fig. 4a), where in situ perennial firn aquifer measurements have recently been collected
767 (Miller et al., 2017).

768 We calculate the absorption coefficient (κ_a) in Eq. 7 using

769

$$770 \kappa_a = -2k_o \Im\{\sqrt{\epsilon_r}\}, \quad (\text{Eq. 10})$$

771

772 where $\Im\{\}$ represents the imaginary part. We calculate the complex dielectric constant of the saturated firn
773 layer in Eq. 8 and Eq. 10 using the empirically derived models described in Tiuri et al., (1984). We set the
774 volumetric fraction of meltwater to $m_v=1\%$. We set the depth of the water-saturated firn layer in Eq. 7 to
775 $d=1$ m. These values are consistent with typical lower frequency (e.g., 37 GHz, 13.4 GHz, 19 GHz) passive
776 (e.g., Mote, et al. 1995; Abdalati and Steffen, 1997; Ashcraft and Long, 2006) and active (e.g., Hicks and
777 Long, 2011) microwave algorithms used to detect seasonal surface melting over the GrIS. Using the results
778 of Eq. 7, 8, 9, and 10, we calculate the firn saturation parameter threshold at $\xi_T=0.1$.

779 The first step in our adapted empirical algorithm is to map the extent of the percolation facies. For
780 each rSIR grid cell within the ice sheet-masked extent of the GrIS, we smooth the corresponding T_V^B time
781 series (1 April 2015 - 31 March 2019) using a 14-observation (1 week) moving window. We extract the
782 minimum vertically-polarized L-band brightness temperature ($T_{V,min}^B$), and the maximum vertically-polarized
783 L-band brightness temperature ($T_{V,max}^B$). We set the physical temperature of the water-saturated firn layer
784 to $T=273.15$ K, and the transmission angle to $\theta=40^\circ$. We then calculate the firn saturation parameter (ξ)
785 using Eq. 2. If the calculated firn saturation parameter exceeds the firn saturation parameter threshold, the
786 rSIR grid cell is converted to a binary parameter to map the total extent of the percolation facies.

787 We note that smoothing T_V^B time series will mask brief low-intensity seasonal surface melting that
788 occurs in the high-elevation ($> \sim 2500$ m) percolation facies, where seasonal meltwater is rapidly refrozen
789 within the colder snow and firn layers (e.g., Fig. 4d). Thus, the calculated firn saturated parameter will not
790 exceed the firn saturation parameter threshold, and these rSIR grid cells will be excluded from the algorithm.
791 The exclusion of rSIR grid cells in the high-elevation percolation facies is not expected to have a significant
792 impact on our results as our algorithm targets rSIR grid cells in areas that experience intense seasonal
793 surface melting. The exclusion of rSIR grid cells will, however, slightly underestimate the mapped
794 percolation facies extent.

795 The second step in our adapted empirical algorithm is to map the extent of perennial firn aquifer,
796 ice slab, and perched firn aquifer areas over the percolation facies. For each rSIR grid cell within the
797 mapped percolation facies extent, we normalize the corresponding T_V^B time series (1 April 2015 - 31 March
798 2019) using Eq. 5 ($T_{V,N}^B(t)$). We then extract the initial normalized vertically-polarized L-band brightness
799 temperature, ($T_{V,N}^B(t_{max})$) and the final normalized vertically-polarized L-band brightness temperature
800 ($T_{V,N}^B(t_{min})$), and partition $T_{V,N}^B(t)$ on the time interval $t \in [t_{max}, t_{min}]$. We smooth $T_{V,N}^B(t \in [t_{max}, t_{min}])$
801 using a 56-observation (4 week) moving window. The sigmoid fit is then iteratively applied using Eq. 6.



802 Smoothing reduces the chi-squared error statistic when fitting $T_{V,N}^B(t \in [t_{max}, t_{min}])$ to the sigmoid function.
803 We fix the initial normalized vertically-polarized L-band brightness temperature at $T_{V,N}^B(t_{max})=0.99$, which
804 provides a uniform parameter space in which the refreezing rate parameter (ζ) can be analyzed. Variability
805 in $T_{V,N}^B(t_{max})$ is controlled by the volumetric fraction of meltwater within the upper snow and firn layers of
806 the percolation facies, and is accounted for in the firn saturation parameter (ξ), which is analyzed separately.
807 $T_{V,N}^B(t \in [t_{max}, t_{min}])$ iteratively fit to the sigmoid function converge quickly (i.e., algorithm iterations $I \in [5,$
808 $15]$), and observations are a good fit (i.e., chi squared error statistic is $\chi^2 \in [0, 0.1]$).

809 Using the SMAP-derived $T_{V,N}^B(t_{max})$ and $T_{V,N}^B(t_{min})$, rather than the MODIS-derived initial
810 normalized vertically-polarized L-band brightness temperature at the surface freeze-up date ($T_{V,N}^B(t_{sfu})$),
811 and final normalized vertically-polarized L-band brightness temperature at the melt onset date ($T_{V,N}^B(t_{mo})$)
812 that were used in the empirical algorithm described in Miller et al., 2020 (e.g., Fig. 4), has several
813 advantages. The key advantage of this approach is that maps can be generated using T^B imagery
814 collected from a single satellite, which simplifies the adapted empirical algorithm. Another advantage is that
815 unlike T^B collected at shorter-wavelength thermal infrared frequencies (e.g., MODIS), T^B collected at
816 longer wavelength microwave frequencies (e.g., SMAP) is not sensitive to clouds, which eliminates
817 observational gaps and cloud contamination, and provides more accurate time series partitioning and more
818 robust curve fitting. The mapped extent of Greenland's perennial firn aquifers generated by our adapted
819 empirical algorithm and by our empirical algorithm (Miller et al., 2020) are consistent (see Section 3).

820 We calibrate our adapted empirical algorithm using the AR- and MCoRDS-derived perennial firn
821 aquifer (2010-2017), ice slab (2010-2014), and perched firn aquifer (2010-2017) detections projected
822 separately on three NH EASE-Grids 2.0. For each rSIR grid cell with at least one detection, we extract the
823 corresponding maximum vertically-polarized L-band brightness temperature ($T_{V,max}^B$), the minimum
824 vertically-polarized L-band brightness temperature ($T_{V,min}^B$), the firn saturation parameter (ξ), and the
825 refreezing rate parameter (ζ), and for each of the extracted SMAP-derived calibration parameters we
826 calculate the standard deviation (σ). Similar to Miller et al., 2020, thresholds of $\pm 2\sigma$ are set for each of the
827 extracted SMAP-derived calibration parameters in an attempt to eliminate peripheral rSIR grid cells near
828 the ice sheet edge and near the upper and lower boundaries of each sub-facies, where L-band emissions
829 can be influenced by morphological features, such as crevasses, superimposed and glacial ice, and
830 spatially integrated with emissions from rock, land, the ocean, and adjacent percolation facies and wet snow
831 facies areas. The SMAP-derived calibration parameter threshold intervals extracted from T_V^B time series
832 that we use to map perennial firn aquifer, ice slab, and perched firn aquifer areas are given in Table 3. We
833 apply the calibration to each rSIR grid cell within the percolation facies extent. If the extracted SMAP-
834 derived calibration parameters are within the threshold intervals, the rSIR grid cell is converted to a binary
835 parameter to map the total extent of each of these sub-facies.

836
837



838 **Table 3.** SMAP-derived calibration parameter threshold intervals (1 April 2015 - 31 March 2019) used for
 839 mapping perennial firn aquifer, ice slab, and perched firn aquifer areas.

	ξ	$T_{V,max}^B$ (K)	$T_{V,min}^B$ (K)	ζ
Perennial Firn Aquifers	0.2 – 4	200 – 275	180 – 250	-0.04 - -0.02
Ice Slabs	0.1 – 2	170 – 260	130 – 240	-0.03 - -0.06
Perched Firn Aquifers	0.2 - 1.2	200 – 260	180 – 240	-0.03 - -0.04

840

841 Iteratively applying the sigmoid fit to $T_{V,N}^B(t \in [t_{max}, t_{min}])$ over perched firn aquifer areas is a
 842 source of uncertainty in our adapted empirical algorithm. While the continuous logistic model is reasonable
 843 for the majority of exponentially decreasing temporal L-band signatures over the percolation facies, it is not
 844 optimal for exponentially decreasing temporal L-band signatures that transition to linearly decreasing on
 845 time scales of ~years following the surface freeze-up date. Especially multi-year linearly decreasing
 846 temporal L-band signatures over areas where perching occurs following intense seasonal surface melting
 847 and shallow water-saturated firn layers persist throughout the following freezing season as well as
 848 throughout weaker seasonal surface melting the following melting season (e.g., between ~September 2016
 849 and May 2018 in Fig. 4b). Although $T_{V,N}^B(t \in [t_{max}, t_{min}])$ over perched firn aquifer areas iteratively fit to
 850 the sigmoid function converge quickly (i.e., algorithm iterations $I \in [8, 15]$), and observations appear to be
 851 a good fit (i.e., chi squared error statistic is $\chi^2 \in [0.06, 0.1]$), simulated sigmoidal curves often
 852 asymptotically approach $T_{V,min}^B$ too quickly, which underestimates the refreezing rate parameter (ζ) to
 853 values outside the SMAP-derived calibration parameter threshold intervals. Perched firn aquifer areas may
 854 alternatively be mapped as ice slab areas or percolation facies areas, which will underestimate or
 855 overestimate the mapped extent of each of these sub-facies.

856 Miller et al., 2020 cited significant uncertainty in the SMAP-derived perennial firn aquifer extent as
 857 a result of the lack of a distinct temporal L-band signature delineating the boundary between perennial firn
 858 aquifer areas and adjacent percolation facies areas. In this study, similar uncertainty exists in the SMAP-
 859 derived perennial firn aquifer, ice slab, and perched firn aquifer extents. This uncertainty could, at least in
 860 part, be a result of the rSIR algorithm. An rSIR grid cell corresponds to the weighted average of T_V^B over
 861 SMAP's antenna footprint (Long et al., 2020). The weighting is the grid cell's spatial response function
 862 (SRF), which is ~18 km (i.e. the effective resolution) in diameter. The SRF is centered on the rSIR grid cell.
 863 Since the effective resolution (i.e., size of the 3 dB contour of the SRF) is less than the rSIR grid cell spacing,
 864 rSIR grid cell SRF's overlap and the grid cells T_V^B values are not statistically independent. This uncertainty,
 865 however, could also have a geophysical basis, as it is unlikely that the boundaries between sub-facies
 866 (perennial firn aquifers, ice slabs, and perched firn aquifers) as well as between facies (percolation facies,
 867 dry snow facies, wet snow facies) are distinct. The thickness of the water-saturated firn layer or ice slab
 868 may thin and taper-off at the periphery, and sub-facies and facies may become spatially scattered and



869 merge together. Over SMAP's ~18 km footprint, spatially integrated L-band emissions may also result in a
870 smooth transition between temporal L-band signatures.

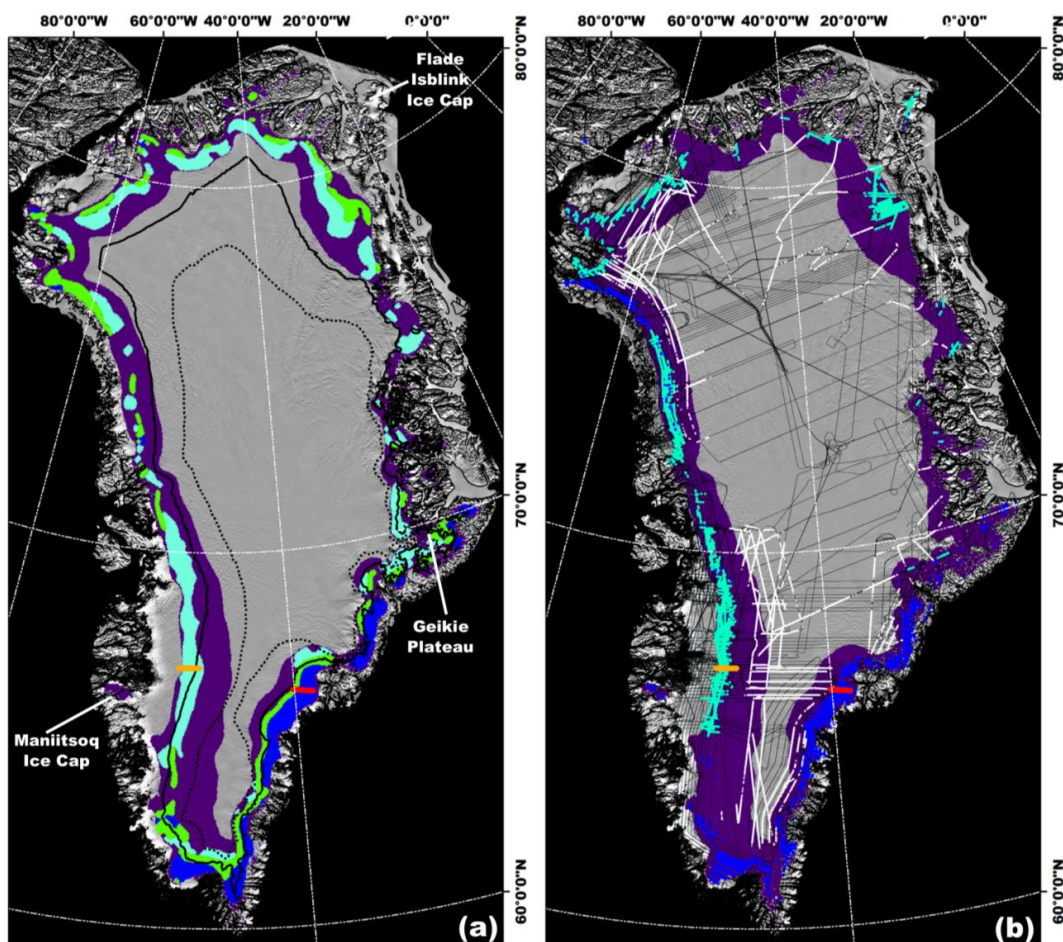
871 The limited extent (AR, 15 m x 20 m; MCoRDS, 14 m x 40 m) of the airborne ice-penetrating radar
872 detections as compared to the rSIR grid cell extent (3.125 km x 3.125 km) and the effective resolution (~18
873 km) of the SMAP enhanced-resolution T_V^B imagery is also cited in Miller et al., 2020 as a source of
874 uncertainty in the empirical algorithm. In this study, similar uncertainty exists in our adapted empirical
875 algorithm. The total rSIR grid cell extent with radargram coverage is less than 2%, which means that ~98%
876 of the total rSIR grid cell extent with radargram coverage, from which the SMAP-derived calibration
877 parameter threshold intervals are extracted, is unknown. Calculating the total rSIR grid cell extent where
878 detections are absent along OIB flight lines and statistically integrating this calculation into the multi-year
879 calibration technique may help reduce the uncertainty, particularly the significant uncertainty in the
880 interannual variability, which we have yet to resolve. A sensitivity analysis suggests that even small changes
881 in any of the SMAP-derived calibration parameter threshold intervals (i.e., several K for $T_{V,min}^B$, and $T_{V,max}^B$,
882 several tenths of a percentage point for ξ , and several hundredths of a percentage point for ζ) can result in
883 variability in the mapped extents of hundreds of square kilometers, and boundary transitions between
884 perennial firn aquifer, ice slab, and perched firn aquifer areas. Thus, the mapped extent of each of these
885 sub-facies of the broader percolation facies should simply be considered an initial result demonstrating the
886 potential of our adapted empirical algorithm for future work.

887
888

889 **3. Results and Discussion**

890 The SMAP-derived maximum vertically-polarized L-band brightness temperature values generated by our
891 adapted empirical algorithm range from between $T_{V,max}^B=150$ K and 275 K, and the minimum vertically-
892 polarized L-band brightness temperature values range from between $T_{V,min}^B=130$ K and 250. These values
893 are consistent with the range of $T_{V,max}^B$ and $T_{V,min}^B$ values given in the temporal L-band signature analysis
894 (Section 2.4.2; Table 2). Firn saturation parameter values range from between $\xi=0.1$ and 4.0. Refreezing
895 rate parameter values range from between $\zeta=-0.09$ and -0.01. The lower bound ($\zeta=-0.09$) of the refreezing
896 rate parameter observed over the percolation facies is significantly higher than the predicted lower bound
897 ($\zeta=-1$) in our example set of simulated sigmoidal curves (black line, Fig. 6).

898 The SMAP-derived perennial firn aquifer (blue shading), ice slab (cyan shading), perched firn
899 aquifer (green shading), and percolation facies (purple shading) extents (2015-2019) generated by our
900 adapted empirical algorithm are shown in Figs. 7a-9a, and are summarized in Table 4. The percolation
901 facies extent ($\sim 5.8 \times 10^5$ km²) generated by our adapted empirical algorithm is mapped at elevations
902 between ~500 m.a.s.l. and 3500 m.a.s.l., and extends over ~32 % of the GrIS extent ($\sim 1.8 \times 10^6$ km²). The
903 perennial firn aquifer extent (64,000 km²) is mapped at elevations between ~600 m.a.s.l and 2600 m.a.s.l.,
904 and extends over ~ 11% of the percolation facies extent and ~4% of the GrIS extent. High $T_{V,max}^B$, $T_{V,min}^B$,



905

906

Figure 7

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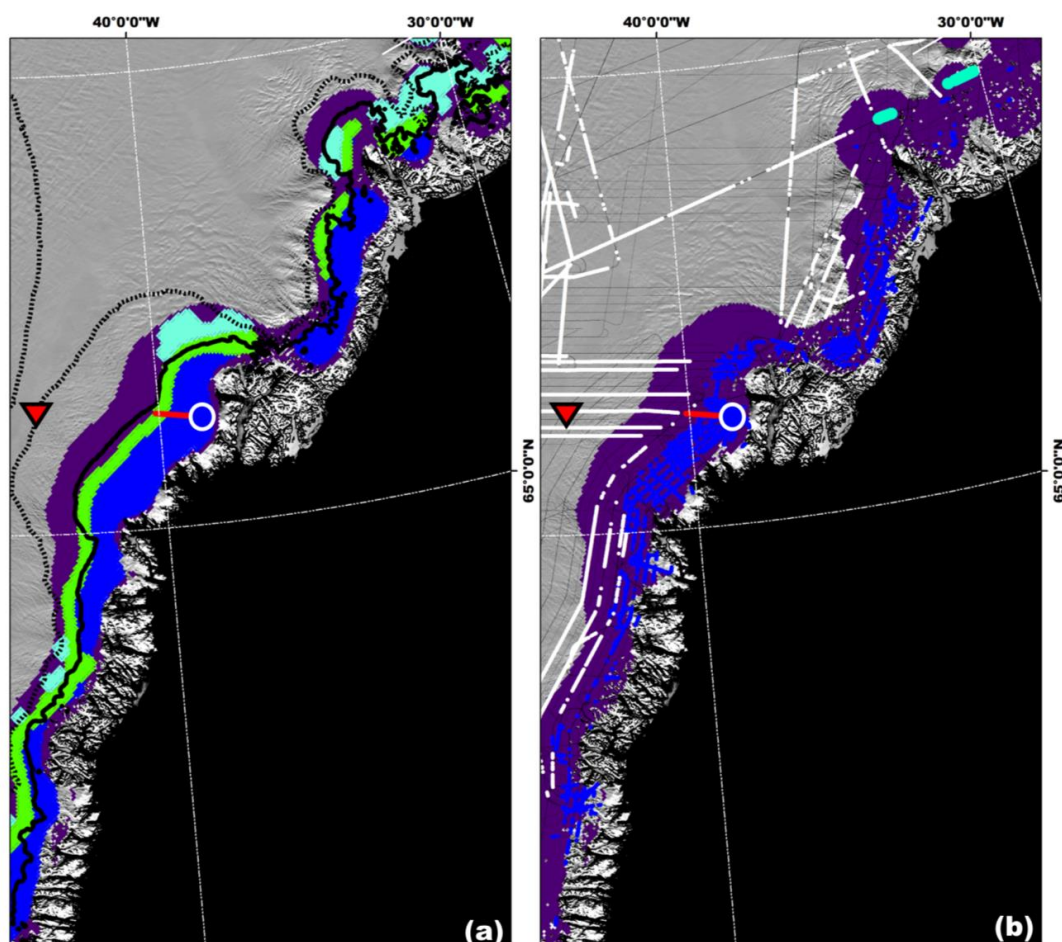
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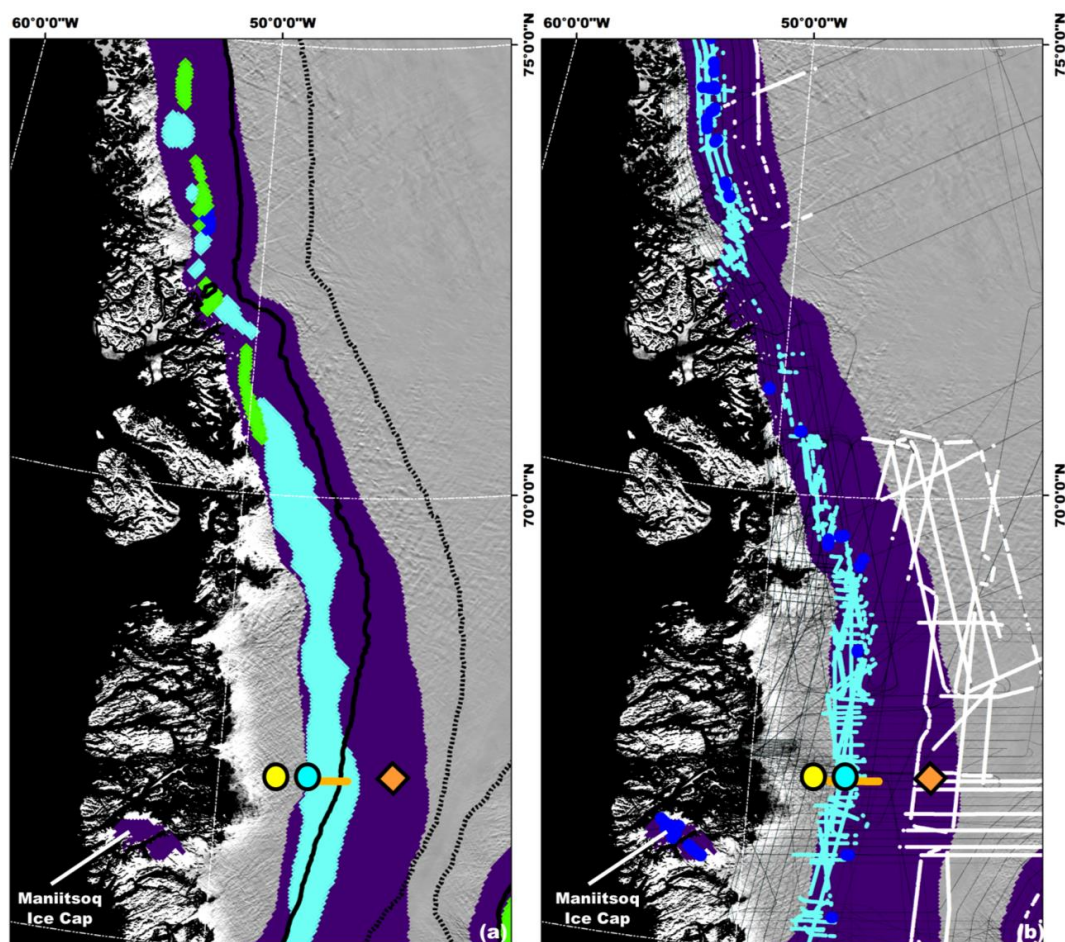
(a) The SMAP-derived perennial firn aquifer (blue shading), ice slab (cyan shading), perched firn aquifer (green shading), and percolation facies (purple shading) extents (2015-2019) generated by the adapted empirical algorithm overlaid on the 2015 MODIS Mosaic of Greenland image map (Haran et al., 2018). The black line is the 2000 m.a.s.l. contour, and the black dotted line is the 2500 m.a.s.l. contour (Howat et al., 2014). (b) The SMAP-derived extents are overlaid with AR- and MCoRDS-derived 2010-2017 perennial firn aquifer (blue shading; Miège et al., 2016), 2010-2014 ice slab (cyan shading; McFerrin et al., 2019), and 2012 spatially coherent melt layer (white shading; Culberg et al., 2021) detections along OIB flight lines (black lines). Overlapping perennial firn aquifer and ice slab detections are interpreted as perched firn aquifer areas. The red line is AR radargram profile along perennial firn aquifer transect A-B (Fig. 3a). The orange line is AR radargram profile along ice slab transect C-D (Fig. 3b).



918

919 **Figure 8**

920 (a) The SMAP-derived perennial firn aquifer (blue shading), ice slab (cyan shading), perched firn aquifer
921 (green shading), and percolation facies (purple shading) extents (2015-2019) generated by the adapted
922 empirical algorithm over south eastern Greenland (Fig. 1c; zoom area in red box) overlaid on the 2015
923 MODIS Mosaic of Greenland image map (Haran et al., 2018). The solid black line is the 2000 m.a.s.l.
924 contour, and the black dotted line is the 2500 m.a.s.l. contour (Howat et al., 2014). (b) The SMAP-derived
925 percolation facies extent is overlaid with AR- and MCoRDS-derived 2010-2017 perennial firn aquifer (blue
926 shading; Miège et al., 2016), 2010-2014 ice slab (cyan shading; McFerrin et al., 2019), and 2012 spatially
927 coherent melt layer (white shading; Culberg et al., 2021) detections along OIB flight lines (black lines).
928 Overlapping perennial firn aquifer and ice slab detections are interpreted as perched firn aquifer areas. The
929 red line is AR radargram profile along perennial firn aquifer transect A-B (Figs. 1; 3a). The blue circle is a
930 perennial firn aquifer area (Figs. 3a; 4a). The red triangle is a high-elevation (~2500 m.a.s.l.) percolation
931 facies area (Figs. 4d).



932

933 **Figure 9**

934 (a) The SMAP-derived perennal firn aquifer (blue shading), ice slab (cyan shading), perched firn aquifer
935 (green shading), and percolation facies (purple shading) extents (2015-2019) generated by the adapted
936 empirical algorithm over south western Greenland (Fig. 1c; zoom area in red box) overlaid on the 2015
937 MODIS Mosaic of Greenland image map (Haran et al., 2018). The solid black line is the 2000 m.a.s.l.
938 contour, and the black dotted line is the 2500 m.a.s.l. contour (Howat et al., 2014). (b) The SMAP-derived
939 percolation facies extent is overlaid with AR- and MCoRDS-derived 2010-2017 perennal firn aquifer (blue
940 shading; Miège et al., 2016), 2010-2014 ice slab (cyan shading; McFerrin et al., 2019), and 2012 spatially
941 coherent melt layer (white shading; Culberg et al., 2021) detections along OIB flight lines (black lines).
942 Overlapping perennal firn aquifer and ice slab detections are interpreted as perched firn aquifer areas. The
943 orange line is AR radargram profile along ice slab transect C-D (Figs 1; 3b). The cyan circle is a perched
944 firn aquifer area (Figs. 3b; 4b). The orange diamond is a percolation facies area (Fig. 4c). The yellow circle
945 is a superimposed ice area (Fig. 4e).



946 ξ , and ζ values within the perennial firn aquifer extent indicates the presence of thicker water-saturated
 947 firn layers with larger volumetric fractions of meltwater that are radiometrically warm during both the melting
 948 and freezing seasons and have extended refreezing rates. The ice slab extent (76,000 km²) is mapped at
 949 elevations between ~800 m.a.s.l and 2700 m.a.s.l., and extends over ~13 % of the percolation facies extent
 950 and ~4 % of the GrIS extent. As compared to perennial firn aquifer areas, decreased $T_{V,max}^B$, $T_{V,min}^B$, ξ and
 951 ζ values indicates the presence of thinner water-saturated firn layers with lower volumetric fractions of
 952 meltwater that are radiometrically colder and have slightly more rapid refreezing rates. The SMAP-derived
 953 perched firn aquifer calibration parameter intervals are within the perennial firn aquifer and the ice slab
 954 calibration parameter intervals (see Fig. 6, Table 3). The extents of these three sub-facies within the broader
 955 percolation facies are overlapping, such that perched firn aquifers typically represent the upper boundary
 956 of perennial firn aquifer areas that subsequently transition to percolation facies as well as the lower
 957 boundary of ice slab areas that subsequently transition to wet snow facies. However, in several areas in
 958 south and southeastern Greenland, the full progression of facies and sub-facies (dry snow facies -
 959 percolation facies - ice slab - perched firn aquifer - perennial firn aquifer – ablation facies) occur (e.g., Fig.
 960 7a). The perched firn aquifer extent (37,000 km²) is mapped at elevations between ~600 m.a.s.l and 2700
 961 m.a.s.l., and extends over ~30% of perennial firn aquifer extent, ~24% of ice slab extent, ~2% of the
 962 percolation facies extent, and less than ~1% of the GrIS extent. Combined together, the total extent
 963 (~140,000 km²) is the equivalent of ~24% of the percolation facies extent and 10% of the GrIS extent. This
 964 increases previous AR- and MCoRDS-derived elevation estimates upslope ~600 m.a.s.l. in both perennial
 965 firn aquifer areas (Miège et al., 2016) and ice slab areas (McFerrin et al., 2019). The highest perennial firn
 966 aquifer, ice slab, and perched firn aquifer elevations (>2500 m.a.s.l.) are mapped in southern Greenland
 967 and on the Geikie plateau, in central eastern Greenland.

968

969 **Table 4.** The SMAP-derived perennial firn aquifer, ice slab, and perched firn aquifer extents (2015-2019)
 970 over the percolation facies and the GrIS, and the elevation range at which they are mapped.

	Percolation Facies Extent (%)	Ice Sheet Extent (%)	Elevation Range (m.a.s.l.)
Perennial Firn Aquifers	11	4	600 – 2600
Ice Slabs	13	4	800 – 2700
Perched Firn Aquifers	5	<1	600 – 2700

971

972 Figs. 7b-9b shows perennial firn aquifers (blue shading), ice slabs (cyan shading), and spatially
 973 coherent melt layers (white shading) detected by airborne ice-penetrating radar surveys (2010-2017)
 974 overlaid on the SMAP-derived percolation facies extent (2015-2019). Perched firn aquifer areas are inferred
 975 where perennial firn aquifer and ice slab detections overlap. The SMAP-derived perennial firn aquifer extent
 976 mapped in southern, and south and central eastern Greenland is consistent with the AR- and MCoRDS-



977 geophysical derived perennial firn aquifer detections (2010-2017), except in north western Greenland
978 where perched firn aquifers are alternatively mapped. The SMAP-derived ice slab extent mapped in
979 western, central and north eastern, and northern Greenland is generally consistent with the spatial patterns
980 of the AR-derived ice slab detections (2010-2014), however, is significantly expanded upslope in each of
981 these areas. We note that the AR-derived ice slab detections are limited in space and time, particularly in
982 northern Greenland, with a time interval as large as nine years between the airborne ice penetrating radar
983 surveys and the SMAP enhanced-resolution T_V^B imagery used in the adapted empirical algorithm (i.e., 2010
984 to 2019). In western and northern Greenland, the 2015 melting season was especially intense (Tedesco et
985 al., 2016). And, in northern Greenland, the ablation facies have recently increased in extent (2010-2019;
986 Noël et al., 2019), and supraglacial lakes have recently advanced inland (2014-2019; Turton et al., 2021),
987 indicating a likely geophysical basis for the observed upslope expansion. In central and north eastern, and
988 northern Greenland, perched firn aquifers are often alternatively mapped. Additional smaller ice slab areas
989 are mapped in south and south eastern (Figs. 9a; 9b) Greenland. The scattered SMAP-derived perched
990 firn aquifer extent mapped in north western and central eastern Greenland is fairly consistent with the
991 sparse AR- and MCoRDS-derived perched firn aquifer detections (2010-2017), however, in central western
992 Greenland (Figs. 9a; 9b) ice slab areas are alternatively mapped. Expansive additional perched firn aquifer
993 areas are mapped in southern, and south and central eastern Greenland. These areas are often coincident
994 with spatially coherent melt layer detections, particularly in south eastern Greenland (Figs. 8a, 8b). Neither
995 perennial firn aquifer, ice slab, nor perched firn aquifer areas are mapped on the Maniitsoq and Flade Isblink
996 Ice Caps. Over these two small ice caps, L-band emissions spatially integrated with emissions from rock,
997 land, the ocean, and adjacent percolation facies and wet snow facies areas result in SMAP-derived
998 calibration parameter values outside the defined intervals for each of these sub-facies.

999 We infer that the SMAP-derived perched firn aquifer extent represents L-band emissions from: (1)
1000 spatially expansive, relatively shallow water-saturated firn layers with lower volumetric fractions of
1001 meltwater as compared to perennial firn aquifer areas. These shallow water-saturated firn layers transiently
1002 form on top of buried ice slabs, spatially coherent melt layers, or other semi-impermeable layers that have
1003 previously formed within the upper snow and firn layers of the percolation facies, as shown in Figs. 7-8. Or,
1004 (2) spatially scattered deeper water-saturated firn layers with larger volumetric fractions of meltwater (i.e.,
1005 perennial firn aquifers) that are spatially integrated with L-band emissions from adjacent ice slabs,
1006 percolation facies, and/or wet snow facies areas. These areas are observed as shallow water-saturated firn
1007 layers with lower volumetric fractions of meltwater over SMAP's ~18 km footprint (i.e., the effective
1008 resolution). Or, (3) a combination of these englacial firn hydrological features, which is a likely scenario
1009 over many perched firn aquifers areas. This is particularly likely in north western Greenland, where airborne
1010 ice penetrating radar surveys consistently detect perennial firn aquifers; however, the SMAP-derived extent
1011 indicates perched firn aquifer areas (Fig. 7).

1012



1013 Shallow buried supraglacial lakes have recently been identified within the percolation facies of
1014 western, northern, and north and central eastern Greenland using airborne ice penetrating radar surveys
1015 (Koenig et al., 2015) and satellite synthetic aperture radar imagery (Miles et al., 2017; Schröder et al., 2020;
1016 Dunmire et al., 2021). These buried supraglacial lakes are within the SMAP-derived perennial firn aquifer,
1017 ice slab, and perched firn aquifer extents, however, they are not expected to significantly influence L-band
1018 emissions in these areas for two reasons: (1) as compared to SMAP's ~18 km footprint, the mean extent
1019 of buried supraglacial lakes is limited (less than ~1 km²), and they are sparsely distributed in perennial firn
1020 aquifer, ice slab, and perched firn aquifer areas (Dunmire et al., 2021). (2) Supraglacial lakes form during
1021 the melting season as a result of meltwater storage in topographic depressions at the ice sheet surface
1022 (Echelmeyer et al. 1991). Similar to subglacial lakes (Jezek et al., 2015) and perennial firn aquifers (Miller
1023 et al., 2020), supraglacial lakes represent radiometrically cold subsurface meltwater reservoirs. Upwelling
1024 L-band emissions from deeper firn layers, glacial ice, and the underlying bedrock are effectively blocked by
1025 high reflectivity and attenuation at the impermeable layer-lake bottom interface. This results in a low
1026 observed T_V^B at the upper surface of meltwater stored within supraglacial lakes. During the freezing season,
1027 the upper surface of meltwater stored within supraglacial lakes refreezes and forms a partial or solid-ice
1028 cap that is sometimes buried by snow accumulation (Koenig et al., 2015). Airborne ice penetrating radar
1029 surveys in April and May between 2009 and 2012 suggest the mean depth to the upper surface of meltwater
1030 stored within buried supraglacial lakes is ~2 m (Koenig et al., 2015). As previously noted, over perennial
1031 firn aquifer, ice slab, and perched firn aquifer areas, L-band emissions from the radiometrically warm upper
1032 snow and firn layers decrease on variable time scales during the freezing season as embedded ice
1033 structures slowly refreeze at increased depths below the ice sheet surface and induce strong volume
1034 scattering (Rignot et al., 1993; Rignot 1995). T_V^B can decrease by as much as ~50 K during the freezing
1035 season (e.g., Fig. 4a), representing the descent of the upper surface of stored meltwater by ~tens of meters
1036 (Miège et al., 2016). However, over buried supraglacial lakes, L-band emissions from the refreezing partial
1037 or solid-ice cap, which is smooth relative to the L-band wavelength (~21 cm), induce surface scattering. As
1038 a result, T_V^B decreases over buried supraglacial lakes are negligible. Thus, over SMAP's ~18 km footprint,
1039 water-saturated firn layers dominate L-band emissions over the percolation facies of the GrIS.

1040 The SMAP-derived perennial firn aquifer extent (~64,000 km²) generated by our adapted empirical
1041 algorithm and the multi-year (2010-2017) calibration technique is consistent with the extent (~66,000 km²)
1042 generated by the previously developed empirical algorithm and the single-coincident year (2016) calibration
1043 technique described in Miller et al., 2020. The SMAP-derived perennial firn aquifer extent is generally
1044 consistent with previous C-band (5.3 GHz) satellite radar scatterometer-derived perennial firn aquifer
1045 extents mapped using the Advanced SCATterometer (ASCAT) on the European Organization for the
1046 Exploitation of Meteorological Satellites (EUMETSAT) Meteorological Operational A (MetOp-A) satellite
1047 (2009-2016, ~52 000-153 000 km²; Miller, 2019), and the Active Microwave Instrument in radar
1048 scatterometer mode (ESCAT) on ESA's European Remote Sensing (ERS) satellite series (1992-2001,
1049 ~37 000-64 000 km²; Miller, 2019) as well as the C-band (5.4 GHz) synthetic aperture radar-derived extent



1050 mapped using ESA's Sentinel-1 satellite (2014-2019, ~54 000 km²; Brangers et al., 2020). The exception
1051 is the ASCAT-derived perennial firn aquifer extent (2012-2013, ~153,000 km²; Miller et al., 2019) mapped
1052 following the anomalous 2012 melting season (Nghiem et al., 2012) in which significant changes in the
1053 dielectric and geophysical properties that influence radar backscatter and the temporal C-band signatures
1054 occurred. The unreasonably expansive (i.e., more than twice the mean) mapped extent is a result of
1055 ASCAT'S shallow (~several meters) C-band penetration depth (Jezek et al., 1994), and the simple
1056 threshold-based algorithm that was not calibrated for an extreme melting season that included saturation
1057 of the upper snow and firn layers of the dry snow facies and percolation facies with relatively large
1058 volumetric fractions of meltwater (Miller et al., 2019). Water-saturated firn layers had extended refreezing
1059 rates, however, seasonal meltwater was not stored at depth. Spatially coherent melt layers were
1060 alternatively formed in many of the mapped areas (Culberg et al., 2021). The SMAP-derived ice slab extent
1061 (~76,000 km²) is also consistent with previous AR-derived ice slab extents (2010-2014, ~64,800 km²-69,400
1062 km²; McFerrin et al., 2019).

1063 Although we simply consider our mapped extents a high-probability area for preferential formation,
1064 the maps generated by our adapted empirical algorithm and the multi-year (2010-2017) calibration
1065 technique for individual years suggest interannual variability in perennial firn aquifer, ice slab, and perched
1066 firn aquifer extents, which is summarized in Table 5. Our results demonstrate reasonable sensitivity to
1067 variability in the dielectric and geophysical properties that influence the radiometric temperature and
1068 temporal L-band signatures, even during the extreme 2015 melting season (Tedesco et al., 2016).

1069

1070 **Table 5** *The SMAP-derived perennial firn aquifer, ice slab, and perched firn aquifer extents (2015-2019).*

	Perennial Firn Aquifer Extent (km ²)	Ice Slab Extent (km ²)	Perched Firn Aquifer Extent (km ²)
2015-2019	66,000	76,000	37,000
2015-2016	63,000	23,000	17,000
2016-2017	69,000	48,000	38,000
2017-2018	73,000	27,000	20,000
2018-2019	70,000	38,000	26,000

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1076 **5 Summary and Future Work**

1077 L-band satellite microwave sensors – including NASA’s L-band SMAP mission - represent a relatively new
1078 Earth-observation tool that has exceptional capabilities for cryospheric applications. Especially, mapping
1079 englacial and subglacial hydrological features at depths of ~tens to hundreds of meters beneath the surface
1080 of Earth’s polar ice sheets. In this study, for the first time, we have exploited this capability and demonstrated
1081 the novel use of the L-band microwave radiometer on NASA’s SMAP satellite for mapping perennial firn
1082 aquifers, ice slabs, and perched firn aquifers together as a continuous system over the percolation facies
1083 of the GrIS. We have also demonstrated that SMAP enhanced-resolution L-band T_V^B imagery can effectively
1084 resolve percolation facies features that are not effectively resolved in conventionally processed SMAP L-
1085 band T_V^B imagery (e.g., Fig. 1). We have adapted our previously developed empirical algorithm (Miller et
1086 al., 2020) by expanding our analysis of spatiotemporal differences in SMAP enhanced-resolution T_V^B
1087 imagery and temporal L-band signatures over the GrIS. We have used this analysis to derive a firn
1088 saturation parameter from a simple two-layer L-band geophysical-brightness temperature model. And, we
1089 have used the firn saturation parameter to map the extent of the percolation facies. We have found that by
1090 correlating maximum and minimum T_V^B values, the firn saturation parameter, and the refreezing rate
1091 parameter with perennial firn aquifer, ice slab, and perched firn aquifer detections identified via NASA’s OIB
1092 campaigns that we can calibrate our previously developed empirical algorithm (Miller et al., 2020) to map
1093 plausible extents.

1094 We note that significant uncertainty exists in the mapped extents as a result of (1) correlating the
1095 SMAP-derived parameters with airborne ice-penetrating radar detections that are not coincident in time, (2)
1096 the lack of a distinct temporal L-band signature delineating the boundary between each of the mapped sub-
1097 facies within the broader percolation facies, and (3) the much more limited extent of the airborne ice-
1098 penetrating radar detections as compared to the rSIR grid cell extent, as well as the effective resolution of
1099 the SMAP enhanced-resolution T_V^B imagery. Additional uncertainty exists in the perched firn aquifer extent
1100 as a result of fitting L-band signatures to the continuous logistic model, which is not optimal for these specific
1101 sub-facies.

1102 Miller et al., (2020) normalized SMAP enhanced-resolution T_V^B time series and converted the
1103 exponential rate of T_V^B decrease over perennial firn aquifer areas to a binary parameter to map extent. In
1104 this study, we have converted the SMAP-derived parameters to binary parameters to map the extent of
1105 perennial firn aquifer, ice slab, and perched firn aquifer areas. Moreover, we have included additional
1106 analysis of the spatiotemporal differences in maximum and minimum T_V^B values, the firn saturation
1107 parameter, and the refreezing rate parameter. We have shown that spatiotemporal differences in the
1108 SMAP-derived parameters are consistent with our assumption of spatiotemporal differences in the englacial
1109 hydrology and thermal characteristics of firn layers at depth. Particularly, our assumption that latent heat
1110 release influences temporal L-band signatures within the percolation facies of the GrIS. This includes
1111 continuous latent heat release via the slow refreezing of the deeper firn layers in perennial and perched firn
1112 aquifer areas that are saturated with large volumetric fractions of meltwater. And, latent heat release that



1113 occurs throughout the percolation facies via more rapid refreezing of seasonal meltwater by the descending
1114 winter cold wave, and the subsequent formation of embedded ice structures, including ice slabs and
1115 spatially coherent melt layers, within the upper snow and firn layers.

1116 Future work will focus on simulating maximum and minimum T_V^B , the firn saturation parameter, and
1117 the refreezing rate parameter as well as temporal L-band signatures observed over perennial firn aquifer,
1118 ice slab, and perched firn aquifer areas within the percolation facies of the GrIS for a wide range of
1119 geophysical properties. Significant interannual variability in the dielectric and geophysical properties that
1120 seasonally influence the radiometric temperature and temporal L-band signatures can occur, particularly
1121 following extreme melting seasons, such that it is critical that these properties are understood and
1122 considered in any given year. To better interannual variability as well as other geophysical properties, we
1123 will interpret our results together with climatological parameters, such as snow accumulation, liquid water
1124 content, temperature, and surface mass balance, and over the GrIS simulated using the Regional
1125 Atmospheric Climate Model (RACMO2.3p2; Noël et al., 2018). Additionally, we will simulate the distinct
1126 temporal L-band signatures observed over spatially coherent melt layers in the upper snow and firn layers
1127 of the dry snow facies and percolation facies of the GrIS recently identified via MCoRDS flown by NASA's
1128 OIB campaigns (Culberg et al., 2021) following the anomalous 2012 melting season (Nghiem et al., 2012)
1129 and as well as explore the potential for mapping the extent of these near-surface englacial hydrological
1130 features using satellite L-band microwave radiometry. Nghiem et al., (2003) previously demonstrated
1131 mapping spatially coherent melt layers that were formed following the anomalous 2002 melting season
1132 (Steffen et al., 2004) using similar signatures observed in Ku-band radar backscatter time series collected
1133 by the SeaWinds radar scatterometer that was flown on NASA's QuikSCAT satellite (Tsai et al., 2000).
1134 Combining multi-layer depth-integrated L-band geophysical-brightness temperature models (e.g., Jezek et
1135 al., 2015) that include embedded ice structure parametrizations (e.g., Jezek et al., 2018) with models of
1136 depth-dependent geophysical parameters can lead to an improved understanding of the extremely complex
1137 and very poorly described physics controlling L-band emissions over the percolation facies of the GrIS. For
1138 L-band emissions over perennial firn aquifer, ice slab, perched firn aquifer, and spatially coherent melt layer
1139 areas, the key geophysical parameters include atmospheric temperature forcing, physical temperature
1140 versus depth, latent heat, snow accumulation, the volumetric fraction and depth of meltwater, and the
1141 volumetric fraction and geometric configuration of embedded ice structures. The development of more
1142 sophisticated empirical algorithms that incorporate multi-layer depth-integrated L-band geophysical-
1143 brightness temperature models that are constrained by in situ measurements can help reduce the
1144 significant uncertainty in the current mapped extents, and provide more accurate boundaries delineating
1145 each of these sub-facies within the broader percolation facies that can be used to quantify variability in
1146 extent. As Greenland's climate continues to warm, and seasonal surface melting increases in extent,
1147 intensity, and duration, quantifying the possible rapid expansion of each of these sub-facies using satellite
1148 L-band microwave radiometry has significant implications for understanding ice sheet-wide variability in



1149 englacial firn hydrology resulting in meltwater-induced hydrofracturing and accelerated ice flow as well as
1150 high-elevation run-off that can impact the mass balance and stability of the GrIS.

1151 The results presented in this study demonstrate the outstanding potential of L-band satellite
1152 microwave sensors for mapping englacial firn hydrological features within the percolation facies of the GrIS
1153 that can be extended to forthcoming satellite missions, such as the NASA-ISRO SAR mission (NISAR),
1154 ESA's Copernicus Imaging Microwave Radiometer (CIMR) mission, ESA's Copernicus Radar Observation
1155 System for Europe in L-band (ROSE-L) mission, and candidate missions, such as ESA's Earth Explorer 10
1156 Cryorad mission.

1157

1158 **Data Availability**

1159 SMAP enhanced-resolution L-band T_V^B imagery (2015-2019) have been produced as part of the NASA
1160 Science Utilization of SMAP project and are available at <https://doi.org/10.5067/QZ3WJNOUZLFK> (Brodzik
1161 et al., 2019). The NASA MEaSURES Greenland Ice Mapping Project (GIMP) Land Ice and Ocean
1162 Classification Mask, Version 1, is available at <https://doi.org/10.5067/B8X58MQBFUPA> (Howat, 2017), and
1163 the Digital Elevation Model, Version 1, is available at <https://nsidc.org/data/nsidc-0645/versions/1> (Howat
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1165 resolution Geography Database <https://doi.org/10.1029/96JB00104> (Wessel and Smith, 1996). Ice surface
1166 temperature imagery (2015-2019) have been produced as part of the Multilayer Greenland Ice Surface
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1172 2019). OIB AR-derived spatially coherent melt layer detections (2017) are available at
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1174 Strength Profiles, Version 2, are available at, <https://doi.org/10.5067/OZY1XYHNIQNY> (Paden et al., 2018).
1175 NASA MEaSURES MODIS Mosaic of Greenland (MOG) 2015 Image Map, Version 2, is available at
1176 <https://nsidc.org/data/NSIDC-0547/versions/2> (Haran et al., 2018). SMAP-derived perennial firn aquifer, ice
1177 slab, and perched firn aquifer extents are available from JZM upon request.

1178

1179 **Author Contributions**

1180 JZM initiated the study, adapted the empirical model, performed the analyses, and wrote the manuscript.
1181 RC processed and interpreted the OIB AR radargram profiles. RC and DMS provided the spatially coherent
1182 melt layer detections. All authors participated in discussions and reviewed manuscript drafts.

1183

1184



1185 **Competing Interests**

1186 The authors declare that they have no conflict of interest.
1187

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1197

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