# Projecting circum-Arctic excess ground ice melt with a sub-grid representation in the Community Land Model

3 Lei Cai<sup>1</sup>, Hanna Lee<sup>1</sup>, Kjetil Schanke Aas<sup>2</sup>, Sebastian Westermann<sup>2</sup>

4 <sup>1</sup>NORCE Norwegian Research Centre, Bjerknes Centre for Climate Research, 5008, Bergen, Norway

5 <sup>2</sup>Department of Geosciences, University of Oslo, Oslo, 0315, Norway

6 Correspondence to: Lei Cai (leca@norceresearch.no)

7 Abstract To address the longstanding underrepresentation of the influences of highly variable ground 8 ice content on the trajectory of permafrost conditions simulated in Earth System Models under a warming 9 climate, we implement a sub-grid representation of excess ground ice within permafrost soils using the 10 latest version of the Community Land Model (CLM5). Based on the original CLM5 tiling hierarchy, we 11 duplicate the natural vegetated landunit by building extra tiles for up to three cryostratigraphies with 12 different amounts of excess ice for each grid cell. For the same total amount of excess ice, introducing 13 sub-grid variability in excess ice contents leads to different excess ice melting rates at the grid level. In 14 addition, there are impacts on permafrost thermal properties and local hydrology with sub-grid 15 representation. We evaluate this new development with single-point simulations at the Lena river delta, 16 Siberia, where three sub-regions with distinctively different excess ice conditions are observed. A triple-17 landunit case accounting for this spatial variability conforms well to previous model studies for the Lena 18 river delta and displays a markedly different dynamics of future excess ice thaw compared to a single-19 landunit case initialized with average excess ice contents. For global simulations, we prescribed a tiling 20 scheme combined with our sub-grid representation to the global permafrost region using the dataset 21 "Circum-Arctic Map of Permafrost and Ground-Ice Conditions" (Brown et al., 1997). The sub-grid scale 22 excess ice produces significant melting of excess ice under a warming climate and enhances the 23 representation of sub-grid variability of surface subsidence on a global scale. Our model development 24 makes it possible to portray more details on the permafrost degradation trajectory depending on the sub-25 grid soil thermal regime and excess ice melting, which also shows a strong indication that accounting for 26 excess ice is a prerequisite of a reasonable projection of permafrost thaw. The modeled permafrost 27 degradation with sub-grid excess ice follows the pathway that continuous permafrost transforms into 28 discontinuous permafrost before it disappears, including surface subsidence and talik formation, which 29 are highly permafrost-relevant landscape changes excluded from most land models. Our development of 30 sub-grid representation of excess ice demonstrates a way forward to improve the realism of excess ice 31 melt in global land models, but further developments rely on additional global observational datasets on 32 both the horizontal and vertical distributions of excess ground ice.

# 33 1. Introduction

Permafrost soils are often characterized by different types of ground ice that can exceed the pore
space (Brown et al. 1997; Zhang et al., 1999). The presence of such "excess" ground ice can alter the

36 permafrost thermal regime and landscape structure. Widespread thawing of permafrost is expected in a 37 warmer future climate and modeling studies suggest large-scale degradation of near-surface permafrost 38 at the end of the 21st century (Lawrence et al., 2008 & 2011). Melting of ground ice due to active layer 39 thickening releases water in the form of surface and/or subsurface runoff, causing surface subsidence and 40 modifying the local hydrological cycle (West and Plug, 2008; Grosse et al., 2011; Kokelj et al., 2013; 41 Westermann et al., 2016). In addition to containing ground ice, some permafrost soils store massive 42 amounts of carbon, which could be released to the atmosphere in the form of greenhouse gases upon 43 thawing (Walter et al., 2006; Zimov et al., 2006; Schuur et al., 2008), possibly making a positive feedback 44 to amplify future climate change (Koven et al., 2011; Schaefer et al., 2014; Burke et al., 2013). The 45 existence of excess ice and its distribution in permafrost can significantly affect the rate of permafrost 46 thawing (Westermann et al., 2016; Nitzbon et al., 2020), and in turn, the rate of soil carbon release 47 (Hugelius et al., 2014; Schuur et al., 2015; Turetsky et al., 2019). Therefore, better projections of excess 48 ice melt are critical to improve our understanding of the impacts of permafrost thaw on corresponding 49 climatic impacts.

50 Previous studies address excess ice modeling on the local or regional scale, in which the small study 51 area makes it possible for detailed configurations of the cryostratigraphy of permafrost and excess ice 52 based on observations. Simulations for the Lena river delta have retrieved the permafrost thermal 53 dynamics fairly close to the observations with excess ice incorporated in the modeling (Westermann et 54 al., 2016). A two-tile approach allowing lateral heat exchange between two land elements demonstrated 55 that maintaining thermokarst ponds requires the heat loss from water to the surrounding land (Langer et 56 al., 2016). A similar tiling approach has been applied to projecting the landscape changes due to 57 permafrost thaw for ice-wedge polygons and peat plateaus with different features of ice melting and 58 surface subsidence (Aas et al., 2019; Nitzbon et al., 2019).

59 On the global scale, the land components of Earth System Models (ESMs) have significant 60 capabilities of representing key permafrost physics. In the Community Land Model (CLM), for example, 61 the representation of permafrost-associated processes has been continuously improving, By including 62 key thermal and hydrological processes of permafrost, the CLM version 4 (CLM4) has reasonably 63 reproduced the global distribution of permafrost (Lawrence et al., 2008; Lawrence et al., 2012; Slater 64 and Lawrence, 2013). Projections based on the CLM4 under its highest warming scenario (RCP8.5) have 65 shown over 50% degradation of near-surface permafrost by 2100 (Lawrence et al., 2012). Moreover, the 66 recently released CLM5 has more advanced representations of many biogeophysical and biogeochemical 67 processes (Lawrence et al., 2019). A refined soil profile and upgraded snow accumulation and 68 densification scheme in the CLM5 could contribute to simulating more realistic permafrost thermal 69 regimes, whereas upgrades on biogeochemistry improve simulations of soil carbon release in response 70 to permafrost thaw. In addition, an excess ice physics scheme has been implemented in CLM4.5 71 (CLM4.5 EXICE) by Lee et al. (2014), which allowed for the first-order simulation of surface 72 subsidence globally by modeling excess ice melt under a warming climate.

73 The homogeneous distribution of excess ice throughout the grid cell in CLM4.5 EXICE (Lee et al., 74 2014) could cause biases in thaw trajectories in the warming climate. In nature, excess ice forms in a 75 highly localized manner due to a variety of accumulation processes. For instance, segregated ice formed 76 during frost heave differs substantially in excess ice morphology from ice wedges that are formed from 77 repeated frost cracking and freezing of penetrating water. Field measurements illustrate that the depth 78 distribution of ground ice can vary substantially on the order to 10-50 meters horizontally and 0-10 meters 79 vertically (Pascale et al., 2008; Fritz et al., 2011). The horizontal grid spacing of ESMs, on the other hand, 80 usually ranges from one to two degrees (~100-200km horizontal scale), which makes it impossible to 81 represent localized excess ice. The mismatch in spatial scale between model and the real world raises 82 concerns for the reliability of excess ice modeling in ESMs. Aside from the homogenously, initialized 83 excess ice in the grid cell, CLM4.5 EXICE initializes excess ice in the same soil depths globally (below 84 1m), regardless of the varying active layer thickness in circum-Arctic permafrost areas (Lee et al., 2014). 85 Such deficiencies in excess ice parameterization hamper global projections of permafrost thaw including 86 excess ice with ESMs.

87 To narrow the gap between the high spatial variability of excess ice and the coarse grid spacing in 88 the ESMs, we applied a sub-grid approach in representing excess ice in permafrost soils within the CLM5 89 to investigate how presence and melting of excess ice affect land surface physics under a warming climate. 90 We conducted idealized single-point simulations to examine the robustness of model development. We 91 furthermore conducted global simulations using a first-order estimate for the spatial distribution of excess <del>92</del> ice and associated cryostratigraphies, aiming to present a model framework that can eventually bring the 93 modeling towards a higher accuracy. Due to the lack of information in global excess ice conditions, it is 94 not the aim of this study to accurately project excess ice melt and surface subsidence in the 21st century, 95 but rather to develop a functionable process within a land surface model on a global scale. The CLM5 96 with sub-grid excess ice representation developed through this study would be ready to serve as a proper 97 simulation tool on further advancing global excess ice modeling once new datasets become available.

## 98 2. Methodology

#### **2.1 Sub-grid representation of excess ice in the CLM5**

100 The CLM5 model utilizes a three-level tiling hierarchy to represent sub-grid heterogeneity of 101 landscapes, which are (from top to bottom) landunits, columns, and patches (Lawrence et al., 2019). 102 There is only one column (the natural soil column) that is under the natural vegetated landunit, which 103 represents soil including permafrost. In this study, we modify the CLM5 tiling hierarchy by duplicating 104 the natural vegetated landunit, making extra landunits for prescribing up to three different excess ice 105 conditions in permafrost (Figure 1). The original natural vegetated landunit is considered as "natural 106 vegetated with no excess ice" (hereafter no ice landunit), while we denote the additional landunits as 107 "natural vegetated with low content of excess ice" (hereafter the low ice landunit), "natural vegetated 108 with medium content of excess ice" (hereafter the mid ice landunit), and "natural vegetated with high 109 content of excess ice" (hereafter the high ice landunit). The sub-grid initial conditions of excess ice are

imported as part of the surface data, which includes the variables of volumetric excess ice contents,depths of the top and bottom soil layer of added excess ice, and the area weights of the four landunits.

112 We adopted the excess ice physics from CLM4.5\_EXICE (Lee et al., 2014), including 113 thermodynamic and hydrological processes. The added excess ice is evenly distributed within each soil 114 layer. Note that the original CLM5 model already represents the dynamics of pore ice. Our representation 115 of excess ice physics only addresses the ground ice bodies that exceed soil pore space. The volumetric 116 excess ice content in this study is defined as the ratio of the volume of excess ice in a soil layer to the 117 volume of the whole soil layer. For example, a 50% volumetric content of excess ice means the excess 118 ice body occupies 50% volume of a soil layer, while the rest of soil (and pore ice) occupies the other 50% 119 volume of the soil layer. If not otherwise notified, the parameter of volumetric ice content in this 120 manuscript refers only to that of excess ice bodies. After adding excess ice, the soil layer thickness 121 increases accordingly. Because ice density is considered constant, the increase of soil layer thickness is 122 linearly proportional to the volumetric content of excess ice. For example, adding an excess ice body 123 with a 50% volumetric excess ice content doubles the soil layer thickness of the corresponding soil layer. 124 The revised algorithm for thermal conductivity and heat capacity of soil involves the effects of added 125 excess ice, while the revised phase change energy equation allows excess ice to melt. The meltwater adds 126 to soil liquid water in the same soil layer, and it can move to the above layer if the original layer is 127 saturated. Such numerical implementation replicates how the melt excess ice eventually converts to 128 runoff and discharges from the soil in case of well-drained conditions. As excess ice melts, soil layer 129 thickness decreases, which corresponds to surface subsidence due to excess ice melt. In our model 130 parameterization, excess ice only melts and does not re-form since the applied excess ice physics does 131 not account for the different ice formation processes.

132 Aside from sub-grid tiles for excess ice, we acknowledge that the version upgrade from CLM4.5 to 133 CLM5 as the base model modifies the results of excess ice melt compared to the results from Lee et al. (2014). By default, CLM5 represents soil with a 25-layer profile, for which the top 20 hydrologically 134 135 active layers cover 8.5 meters of soil. There are additional 10 soil layers and it is 4.7 meters deeper 136 compared to the default hydrologically-active soil layer profile in CLM4.5, not to mention the 137 substantially more complex biogeophysical processes (Lawrence et al., 2019). Therefore, we developed 138 the sub-grid representation of excess ice within the framework of the latest version of CLM. The 139 duplicated landunits prolong computation time by roughly 10% compared to the original CLM5. We are, 140 therefore, confident that our model development is highly efficient in addressing the sub-grid excess ice 141 and subsequent permafrost thaw.

# 142 2.2 Single-point simulations for the Lena river delta, Siberia

We conduct single-point simulations for the Lena River delta and compare the CLM5 model results to reference simulations with the CryoGrid3 model for the same location (Westermann et al., 2016). Abundant background information is available on the soil and ground ice dynamics from both observation and modeling, making the Lena river delta a suitable location to further evaluate our model development. The Lena river delta can be broadly categorized into three different geomorphological units

148 that have distinctively different subsurface cryostratigraphies of excess ice (Schneider et al., 2009; Ulrich 149 et al., 2009). In the eastern and central part of the river delta, ground ice has been accumulated in the 150 comparatively warm Holocene climate. The subsurface sediments (hereafter denoted as "Holocene 151 ground ice terrain") are generally super-saturated with wedge ice that can extend up to 9 meters 152 underground with the volumetric contents of total ground ice (pore ice + excess ice) ranging from 60-153 80% (Schwamborn et al., 2002; Langer et al., 2013). On the other hand, higher excess ice contents are 154 found in Pleistocene sediments in the Lena River Delta (hereafter the "Yedoma Ice complex"), which 155 are characterized by Yedoma type ground ice (Schirrmeister et al., 2013), which can reach depths of up 156 to 20-25 meters deep and volumetric contents of total ground ice (Schwamborn et al., 2002; Schirrmeister 157 et al., 2003 and 2011). Finally, the Northwestern part of the delta features sandy sediments and is 158 characterized by low excess ice contents (hereafter denoted the "no excess ice terrain"; Rachold and 159 Grigoriev, 1999; Schwamborn et al., 2002).

160 We determine the area weights of excess ice landunits in one single point based on the spatial pattern 161 of three subregions (Fedorova et al., 2015). The cryostratigraphy and the volumetric contents of excess 162 ice strictly follow those in Westermann et al. (2016). Note that the excess ice initialization scenario in 163 Westermann et al. (2016) does not necessarily represent the realistic excess ice condition for the Lena 164 river delta. The purpose of applying the same excess ice cryostratigraphy as in Westerman et al. (2016) 165 is to evaluate our model development by addressing intercomparisons between model results. Meanwhile, 166 we did not customize soil properties for different landunits as in Westermann et al. (2016), as our model 167 development does not support varying soil properties for different sub-grid landunits. We also directly 168 apply the snow accumulation physics in the CLM rather than customizing the snow density. By default, 169 the current model does not form thermokarst lakes as the meltwater from excess ice melt becomes surface 170 runoff and is removed from the grid cell. To apply the sub-grid representation, we initialize the case with 171 three landunits (the triple-landunit case) that respectively represent the three terraces in the Lena river 172 delta. We also initialize an "average ice single-landunit" case without the sub-grid representation of 173 excess ice. The excess ice amount for each soil layer in the average ice single-landunit case is initially 174 the same as that in the triple-landunit case. The volumetric content of excess ice is determined by spatial 175 averaging those for three excess ice landunits in the triple-landunit case. Detailed information on the 176 applied excess ice conditions for both cases is listed in Table 1.

177 We employed the single-point forcing data from in Westermann et al. (2016) for the Lena river delta 178 from 1901 to 2100, which is based on the CRU-NCEP (http://dods.extra.cea.fr/data/p529viov/cruncep/) 179 data set for the historical period (1901-2005) and the CCSM4 model output under the RCP4.5 scenario 180 for the projected period (2006-2100), but downscaled with in-situ observations. We run 100-year spin-181 up simulations in order to stabilize the permafrost thermal regime after adding excess ice. Spin-up 182 simulations are produced by running the model with cycled 1901-1920 climatological data. The purpose 183 of spin-up simulations is to stabilize ground temperatures and volumes of excess ice bodies. The 100-184 year length for spin-up is sufficient, as the model is run in Satellite Phenology (SP) mode that does not 185 involve slowly evolving biogeochemical processes such as soil carbon accumulation. Moreover, we 186 address idealized single-point simulations for additional permafrost locations with both continental and maritime climate that showcase the difference to Lee et al. (2014), the results of which are included inthe Supplementary material.

# 189 2.3 Global simulations of excess ice melt

190 The information available for the spatial distribution of excess ice and associated cryostratigraphies 191 on the global scale is generally not as detailed as in the Lena river delta due to the lack of observations. 192 For our global simulations we employ the widely used "Circum-Arctic Map of Permafrost and Ground-193 Ice Conditions" (hereafter the CAPS data; Brown et al., 2002) as data source, while we translate the 194 ground ice condition in the CAPS data to different excess ice stratigraphies as model input data. The 195 CAPS permafrost map categorizes the global permafrost area into classes coded by three factors (i) 196 permafrost extent (c = continuous, d = discontinuous, s = sporadic, and i = isolated), (ii) visible ground 197 ice content (h = high, m = medium, and l = low), and (iii) terrain and overburden (f = lowlands, highlands,198 and intra- and intermontane depressions characterized by thick overburden cover, and r = mountains, 199 highlands ridges, and plateaus characterized by thin overburden cover and exposed bedrock), resulting 200 in more than 20 different varieties in permafrost characteristics (Figure 2). For the simulations, we only 201 use the CAPS distinction between the three classes: high, medium and low ice contents. We qualitatively 202 categorize excess ice types with typical cryostratigraphies for which observations are available, 203 recognizing that this is a crude first-guess of the global distribution of ground ice which needs to be be 204 improved in future studies.

205 The high ice CAPS classes (e.g. chf, chr, and dhf) in central and eastern Siberia, as well as in Alaska, 206 partly coincide with Yedoma regions (Kanevskiy et al., 2011; Grosse et al., 2013). The cryostratigraphy 207 of the high ice landunit is therefore broadly oriented at the excess ice contents and distribution in intact 208 Yedoma, which is characterized by massive ice wedges leading to typical average volumetric content of 209 total ground ice in the range from 60% to 90% (Schwamborn et al., 2002; Kanevskiy et al., 2011). We 210 therefore set the volumetric content of excess ice in the high ice landunit to 70%, and we put excess ice 211 in all the soil layers between 0.2 meters below the active layer and the bottom of hydrologically-active 212 soil layer (8.5 meters). The onset depth of the excess ice just below the active layer is based on the 213 assumption of active ice aggradation which occurs at or below the permafrost table, e.g. the formation of 214 wedge or segregation ice. Initializing high content excess ice throughout the whole soil layer imitates the 215 cryostratigraphy of Yedoma type ice, while a certain amount of high ice landunit locates out of the 216 observed Yedoma regions (Schuur et al., 2015). The effects, limitations, and potential improvements of 217 this initialization scenario will be mentioned in the discussion section. For the low ice landunit, we 218 assume both a significantly lower volumetric excess ice content and a smaller vertical extent of the excess 219 ice body. The volumetric excess ice content is set to 25%, and we add excess ice at soil layers within 0.2 220 to 1.2 meters below the active layer, which in particular represents sediments with segregated ice (e.g. 221 Cable et al., 2018), but also accounts for a wide range of different excess ice conditions found throughout 222 the permafrost domain. For the mid ice landunit, we set the volumetric excess ice content to 45% and 223 put excess ice within 0.2 to 2.2 meters below the active layer, making the volumetric excess ice content 224 and vertical extent of which in between those for the low and high ice landunits. The cryostratigraphies

225 determine that excess ice melt in the low ice landunit can result in a maximum of 0.36 meters of surface 226 subsidence, while excess ice melt in the medium ice landunit can result in a maximum of 1.78 m of 227 surface subsidence. For the high ice landunit, the surface subsidence can be more than 10 meters if all 228 excess ice melts, which is expected to vary in space because of the different active layer thickness. For 229 all three landunits, the active layer thickness is determined by the soil temperature profile by the end of 230 the spinup in a no ice case, which is the simulation by the original CLM5 model without excess ice 231 incorporated. Non-permafrost regions in the CAPS data are assigned the no ice landunit for 100% of 232 their area. We emphasize that the prescribed cryostratigraphies are a first-order approximation that can 233 by no means represent the wide variety of true ground ice conditions found in the permafrost domain. 234 Nevertheless, this makes it possible to gauge the effect of excess ice melt on future projections of the 235 permafrost thermal regime, when compared to "traditional" reference simulations without excess ice.

236 We design a tiling scheme prescribing the assignment of landunits for each CAPS class based on 237 previous observations and empirical estimates (Table 2). All CAPS classes in this study are categorized 238 into three levels of volumetric ice content (5%, 15%, and 25%) that are converted from the ranges (<10%, 239 10-20%, and >20%) in the original CAPS data. The goal of our tiling scheme is to determine a 240 combination of area weights of three excess ice landunits for each CAPS class, making the spatially 241 averaged volumetric content of excess ice the same as that for the CAPS class. We assume that all CAPS 242 classes have the same area fraction (20%) of the low ice landunit, and the CAPS classes with a higher 243 ice content are due to the existence of the landunits with a higher content excess ice. We make this 244 assumption based on previous studies that the segregated ice is widely distributed in permafrost. 245 Observational studies have found segregated ice bodies in various continuous permafrost regions across 246 the circum-arctic including West Central Alaska (Kanevskiy et al., 2014), Nunavik, Canada (Calmels 247 and Allard, 2008), and Svalbard (Cable et al., 2018). In discontinuous permafrost regions, segregated ice 248 bodies also commonly exist underneath Palsas and Lithasas, including Fennoscandia (Seppälä, 2011), 249 Altai and Sayan, Russia (Iwanhana et al., 2012), Himalayas (Wünnemann et al., 2008), and Mongolia 250 (Sharkhuu et al., 1999). The volumetric content of visible segregated ice bodies mentioned above ranges 251 widely from 10-50% (Gilbert et al., 2016).

252 Given the tiling scheme prescribed above, all CAPS classes are assigned a 20% area of low ice 253 landunit. Correspondingly, the CAPS classes with 15% volumetric ice content are assigned another 14% 254 area weight for mid ice landunit on top of the CAPS classes with 5% volumetric ice content, while the 255 CAPS classes with 25% volumetric ice are assigned another 22% area for high ice landunit on top of the 256 CAPS classes with 15% volumetric ice content. The classes of "chf" and "chr" are the exceptions as their 257 corresponding regions are typically with the landscape of Yedoma and/or ice wedge polygonal tundra 258 (Kanevskiy et al., 2011; Gross et al., 2013). We therefore assign only the low and high ice landunits for 259 these two CAPS classes. Summing up the landunit fractions for all the CAPS grid cells within each CLM 260 grid cell obtains the area weights on the grid level that are stored in the surface data file. Figure 3 shows 261 a schematic plot for the initialization scenario and the area covered by different excess ice landunits as 262 the result of sub-grid excess ice initialization in the global simulation case. Note that excess ice for some

regions (e.g. Southern Norway and the Alps) can completely melt out during the spinup period since the
 CLM initial condition prescribes overly warm (non-permafrost) soil temperature for these regions.

265 In this study, we define the grid eells/landunits with permafrost as the ones having at least one 266 hydrologically active soil layer that has been frozen in the last consecutive 24 months. In this case, we 267 define permafrost degradation when all landunits in one grid point are with active layer thickness more 268 than 6.5 meters. We also prepare a "grid-average ice case" by applying the same total amount of excess 269 ice as in the sub-grid ice case in each soil layer, but using only one landunit instead of three that account 270 for the sub-grid variability of excess ice. The volumetric content of excess ice in the single landunit is 271 calculated as the spatial average of those in the three landunits in the triple-landunit case. This grid-272 average ice case provides a reference to evaluate the effects of the sub-grid excess ice representation on 273 the global scale. Finally, we simulate a reference case without excess ice, denoted the "no ice case" in 274 the following. Details on the three cases for the global simulations are listed in Table 3. All global cases 275 are forced by the 3<sup>rd</sup> version of Global Soil Wetness Project forcing data (GSWP3; Kim et al., 2012), 276 running in the Satellite Phenology (SP) mode. The International Land Atmosphere Model Benchmarking 277 (ILAMB; Collier et al., 2018) project has indicated the superior performance of GSWP3 data forcing the 278 CLM5 in the SP-only mode 279 (http://webext.cgd.ucar.edu/I20TR/\_build\_090817\_CLM50SPONLY\_CRUNCEP\_GSWP3\_WFDEI/in 280 dex.html). We conducted a 100-year spin-up using the 1901-1920 climatology before conducting 281 historical period simulations covering 1901-2005. The anomaly forcing under the RCP8.5 scenario on 282 top of the 1982-2005 climatology forces simulations in the projected period.

# 283 3. Result

# 284 3.1 Excess ice melt simulations for Lena River delta cryostratigraphies

By the end of the spinup in the triple-landunit case, the active layer thickness is 0.85 m, 0.55 m, and 0.45 m for the ice-poor terrain, the Holocene ice wedge terrain, and the Yedoma ice complex, respectively. On the other hand, the active layer thickness for the average ice single-landunit case is 0.85 m, which is the same as in the no excess ice terrain in the triple-landunit case. For the average ice single-landunit case, a small amount of excess ice  $(24kg/m^2)$  melts during the spinup period, resulting in 2.6 cm surface subsidence throughout the grid.

291 For the Yedoma ice complex, very little excess ice melt in the 1950s, and it stabilizes afterwards 292 until the late 2000s when substantial ice melt and surface subsidence starts to happen. For the Holocene 293 ground ice terrain, there is no excess ice melt before the late 2010s. By the year 2100, the Yedoma ice 294 complex has exhibited nearly 4 meters of surface subsidence, while the Holocene ground ice terrain has 295 about 0.6 meters of surface subsidence (Figure 4). For the average ice single-landunit case, the noticeable 296 excess ice melt and surface subsidence starts in the late 2010s, which creates about 0.5 meters of surface 297 subsidence by 2100. The magnitude of surface subsidence in the average ice single-landunit case is lower 298 than both the Holocene ground ice terrain and the Yedoma ice complex in the triple-landunit case.

299 On the grid scale, the total excess ice melt is higher in the average ice single-landunit case than in 300 the triple-landunit case (Figure 5). By the year 2100, the average ice single-landunit case has about 30 301 kg/m<sup>2</sup> more excess ice melt than the triple-landunit case. The difference in excess ice on the grid level 302 results from the different volumetric content of excess ice caused by the spatial averaging. In this way, 303 the sub-grid representation of excess ice can potentially also provide more detailed and realistic 304 representation of model variables on the grid level. This is particularly important for the CLM5, which 305 serves as the land component in Earth System Models, which requires the coupling between interacting 306 components on the grid level.

307 Compared to Westermann et al. (2016), the CLM5 with sub-grid excess ice simulates slightly less 308 ( $\sim 20\%$  less) surface subsidence by 2100 for both the central delta and ice complex. We consider this a 309 good agreement as we do not expect a closer fit of the model results due to substantial differences in the 310 model physics (for example, the Cryogrid3 simulations in Westermann et al. (2106) lack a representation 311 of the subsurface water cycle). What is in common between these two studies is the earlier start of excess 312 ice melt and more surface subsidence in the ice complex than in the central delta. The CLM5 with sub-313 grid excess ice also exhibits the varying active layer thickness with different excess ice conditions as 314 Cryogrid3 does. These results suggest that the new model development enables small-scale variability in 315 excess ice melt and subsequent impacts in agreement with previously published modeling efforts.

## 316 **3.2** Global projection of permafrost thaw and excess ice melt

317 Single-point simulations have shown that the varying excess ice cryostratigraphies for different 318 landunits result in sub-grid variabilities of excess ice melt and surface subsidence under the warming 319 climate. The same features remain in the sub-grid ice case within the global simulations that excess ice 320 in the low ice landunit can completely melt out throughout the circum-Arctic permafrost region by the 321 end of the  $21^{st}$  century (Figure 6). The modeled magnitude of surface subsidence is similar to the ~10 cm 322 surface subsidence observed in Barrow and West Dock in the early 21st century (Shiklomanov et al., 323 2013; Streleskiy et al., 2017). The magnitude of surface subsidence is also comparable to the 1-4 cm 324 decade<sup>-1</sup> surface subsidence rate on average over the North Slope of Alaska observed by satellite 325 measurements since the 1990s (Liu et al., 2010). In comparison, the absence of surface subsidence for 326 Arctic Alaska modeled by Lee et al. (2014) is due to an overly deep (1 m deep) excess ice initialization 327 depth. By the year 2100, most ice in the medium ice landunit melts away in the sub-arctic region, while 328 there is less ice melt in the colder regions such as the North Slope of Alaska and the central Siberia. The 329 high ice landunit has the greatest surface subsidence among the three because of its high excess ice 330 content, leading to 2-5 meters of surface subsidence by the year 2100.

The existence of excess ice modulates the thermal regime of permafrost soil and is a major control on permafrost degradation trajectories in a warming climate. Permafrost with excess ice consistently exhibits delayed permafrost degradation compared to the no ice case (Figure 7). For the no ice case modeled by the original CLM5, more than half of the permafrost area undergoes degradation by the end of the 21<sup>st</sup> century. By 2100, the only areas where permafrost remains are the North Slope of Alaska, Northern Canada, and the majority of the land area in Northern Siberia. The areas with remaining 337 permafrost in the year 2100 under the RCP8.5 scenarios are substantially larger compared to the CLM4 338 simulations, in which nearly all permafrost in Eurasia becomes degraded (Lawrence et al., 2012). For the 339 grid-average ice case, the presence of excess ice stabilizes the permafrost thermal regime and thus 340 sustains a larger permafrost area on a global scale in the simulation. For example, permafrost areas in 341 some subarctic regions in the eastern and western Siberia, as well as part of the Arctic coastal regions in 342 Yukon Territory, Canada, remain in the grid-average ice case by 2100. Compared to the grid-average ice 343 case, even more permafrost areas are sustained in the sub-grid ice case, most of which are located in 344 southern Siberia. In the subarctic regions in Alaska and Northwest Canada as well as part of the central 345 Siberia, permafrost degradation is delayed from the 2040s in the grid ice case to the 2080s in the sub-346 grid ice case. We emphasize that permafrost is only sustained according to the accepted temperature-347 based definition (ground material at temperature below zero for two consecutive years), but excess ice 348 continuously melts in this process, which energetically is a different mode of permafrost degradation, 349 similar to a negative mass balance of glaciers and ice sheets.

350 In the sub-grid ice case, the landunits with high excess ice contents lead to more grid points for 351 which permafrost conditions remain in the year 2100 compared to the grid-average ice case. On the other 352 hand, permafrost with excess ice only covers a fraction of a grid point. Among the permafrost degradation 353 trajectories in the three global simulation cases (Figure 8), the sub-grid ice case can provide a more 354 detailed picture on the timing of permafrost degradation. Grid cells become 'partially degraded 355 permafrost' if landunits with excess ice still contain permafrost, which phenomenologically is a more 356 realistic representation that also makes it possible to represent the permafrost distribution in the 357 discontinuous and sporadic permafrost zones. On the other hand, only "fully degraded permafrost" and 358 "remaining permafrost" can be distinguished for the no ice and grid-average ice case. Under the warming 359 climate in the 21st century, the existence of excess ice, especially the high content of excess ice, has a 360 stabilizing effect on soil temperature that delay the disappearance of permafrost on the sub-grid level. 361 Therefore, by the year 2100, there are regions with partially degraded permafrost in between intact and 362 degraded permafrost (Figure 8). For example, in western Siberia, the Pacific coastal area of eastern 363 Siberia, Northwestern Canada, and along the Brooks Range in Alaska, taliks form for landunits with low 364 excess ice contents which leads to partially degraded permafrost regions. Therefore, permafrost 365 degradation exhibits a gradual transition from continuous to discontinuous permafrost, and to non-366 permafrost regions. Some of these regions also encounter substantial surface subsidence in the high ice 367 landunit (> 5 m) (Figure 6).

We further compare the total permafrost area (defined as landunits with active layer thickness < 6.5 meters) in the three cases throughout time. The differences in permafrost area increase from the gridaverage ice case and sub-grid ice case to the no ice case at a rate of 1000 km<sup>2</sup> per year until 2050 (Figure 9). After 2050, the area difference of permafrost in the grid-average ice case and no ice cases rapidly increases, which reaches nearly one million km<sup>2</sup> by 2100. In the sub-grid ice case, the rate of increase remains relatively unchanged after 2050, resulting in an about 0.2 million km<sup>2</sup> larger permafrost area than that in the no ice case.

# 375 4. Discussion

The aim of the sub-grid excess ice representation in the CLM5 is to facilitate long-term global projection of excess ice melt and surface subsidence in the permafrost regions, but the corresponding observational data for model evaluation is sparse, considering especially that drastic excess ice melt as modeled until 2100 is only observed in few locations today (e.g. Günther et al., 2015). In the following, we discuss the challenges and limitations of the sub-grid excess ice framework, and how this sub-grid representation can potentially help the development of other CLM components.

382 Both single-point and global test simulations in this study have shown that excess ice melts under a 383 warming climate is sensitive to its initialization depth. The active-layer-dependent excess ice 384 initialization in this study in the global simulation (sub-grid excess ice case) yields excess ice melt and 385 surface subsidence rates in the early 2000s that are comparable to observations. The lower depths of the 386 assumed excess ice body control the termination of excess ice melt which at the same time determines 387 the onset of talik formation in many permafrost areas. Due to the scarcity of observational data, it is 388 unclear to what extent the cryostratigraphies assumed in our tiling scheme can reproduce the true vertical 389 extent of excess ice bodies at least in a statistical sense. Even so, we manage to make the prescribed 390 excess ice condition as close to the previous results as possible. Firstly, our tiling scheme on the large 391 scale strictly follows the CAPS data (Brown et al., 2002) in terms of the volumetric excess ice content. 392 Furthermore, statistics by Zhang et al. (2000) suggest the ranges of the vertical extent of ice-rich 393 permafrost of 0-2 meters and 2-4 meters respectively for the CAPS classes with low (5%) and medium 394 (15%) ice content. Comparatively, the vertical extents permafrost with excess ice prescribed by our tiling 395 scheme are respectively 1.36 meters and 3.78 meters for the same CAPS classes, both of which lie within 396 the ranges in Zhang et al. (2000). The vertical extent of ice-rich permafrost for the high ice landunit is 397 much higher than that (4-6 meters) in Zhang et al. (2000), but the unmelted part of the ice bodies does 398 not strongly affect the overall rate of excess ice melt, although the remaining ice can slightly change soil 399 temperature and moisture of the surrounding permafrost. We therefore imply that our high ice landunit 400 initialization would not induce a strong bias in excess ice melt projection in the 21st century.

401 Due to the lack of excess ice datasets and observational evidence, the excess ice initialization <del>402</del> scenarios in the global simulation cases, involve empirical estimates and simplifications, which could bring biases to the projection of excess ice melt and surface subsidence. We apply the volumetric content <del>403</del> 404 of ground ice in the CAPS data approximately as the volumetric content of excess ice during initialization 405 as the CAPS data is mostly based on visible ice bodies (Heginbottom et al., 1995), not to mention the 406 determination of volumetric contents of excess ice for three landunits also result from sparse observations 407 and empirical estimates. The prescribed excess ice cryostratigraphies ignore ice morphology and the 408 variation of volumetric content of excess ice with soil depth, regarding excess ice as homogeneous "iee 409 eubes", For the high ice landunit, we simplify the cryostratigraphy initialization to Yedoma type ice, 410 which prescribes overly thick excess ice bodies out of the Yedoma regions (Schurr et al., 2015). A 411 deficiency in the current version of source code disables us to initialize non-Yedoma wedged ice for the 412 high ice landunit out of the Yedoma region. Future versions of our model development will have more

freedom in excess ice stratigraphy configuration, which makes it possible to prescribe different 413 414 cryostratigraphies of the same landunit (e.g. the high ice landunit) for different locations. Furthermore, 415 excess ice stratigraphy. Because of the above shortcomings in the excess ice initialization, we do not 416 expect the modeled excess ice melt in this study to be an adequate representation of reality, yet, <del>417</del> whileimproved observational data sets of excess ice contents and cyostratigraphies eould be directly 418 ingested to yield improved results. However, a spatially distributed global dataset with quantitative 419 information on excess ice stratigraphies does not exist at present. We emphasize that for a better 420 projection of excess ice melt, more observational data of excess ice distribution and surface subsidence 421 is required to further evaluate and validate the new model implementation of excess ice. On the regional 422 scale, Jorgenson et al. (2008) presented a permafrost map of total ground ice volume for the uppermost 423 5 meters of permafrost based on both observations and estimates for Alaska. In addition, O'Neill et al. 424 (2019) compiled permafrost maps for Northern Canada by paleographic modeling, mapping the 425 abundances of three types of excess ice respectively. Further improvements of model results depend on 426 additional observationally constrained datasets of excess ice conditions on the global scale.

427 The area weights of the excess ice landunits (Table 2) in the global simulation are obtained from the 428 higher-resolution CAPS points located within a CLM grid cell. However, complex landscape 429 development, such as thermokarst ponds, requires knowledge of the meter-scale distribution, for example 430 the extent and geometry of individual ice wedges (Langer et al., 2016; Nitzbon et al., 2019), which cannot 431 be represented with the still coarse-scale excess ice classes from the CAPS map. One possible solution 432 to represent this could be to include another layer of sub-grid tiles below the CLM landunit level, where 433 the individual tiles can interact laterally. This would allow for the representation of small-scale 434 permafrost features within a large-scale landunit with a given excess ice content. An example of how this 435 could work is given by Aas et al. (2019) who simulated both polygonal tundra and peat plateaus with a 436 two-tile interactive setup. This is also similar to the recent representation of hillslope hydrology by 437 Swenson et al. (2019), where sub-grid tiles (on the column level in CLM) were used to represent different 438 elements in a representative hillslope. In the future development of CLM, this could be part of a more 439 generic tiling system where lateral heat and mass fluxes could be switched on and off to represent a wide 440 range of land surface processes that are currently ignored or parameterized in LSMs. Fisher and Koven 441 (2020) have discussed the challenges and opportunities in such an adaptive and generic tiling system. 442 We would also advocate for enhancing current tiling schemes in such a direction, which could 443 substantially improve the realism in the representation of permafrost landscapes in LSMs. However, the 444 success of such a tiling approach will rely heavily on the availability of adequate observational data, 445 further highlighting the need for observational efforts and close collaboration between field scientists 446 and modelers.

The more detailed simulation of permafrost degradation trajectory with a sub-grid representation of excess ice also builds more potential on better modeling the permafrost-carbon feedback with biogeochemistry activated (CLM5BGC). Excess ice stabilizes the permafrost thermal regime, therefore alter the rate of carbon releasing from the permafrost (Shuur et al., 2008). Improved projections of permafrost warming could also enhance modeling of vegetation type changes (e.g. shrub expansion) that

- determines the nitrogen uptake to the atmosphere (Loranty and Goetz, 2012). On the other hand, the
- possibility to simulate surface subsidence and excess ice meltwater formation also opens the possibility
- of a more accurate representation of wetland formation. The increase in the area of wetland and soil
- 455 moisture have an impact of the balance of CH<sub>4</sub> and CO<sub>2</sub> releasing from the permafrost as more organic
- 456 matter could decompose in an anaerobic pathway (Lawrence et al., 2015; Treat et al., 2015). Compared
- 457 to the parameterized inundated area simulation in the CLM5 (Ekici et al., 2019), a process-based wetland
- 458 physics scheme together with the sub-grid representation of excess ice in this study would substantially
- 459 contribute to the biogeochemical modeling over the circum-arctic area.

#### 460 5. Conclusion

This study develops a sub-grid representation of excess ice in the CLM5 and examines the impacts of the existence and melting of excess ice in the sub-grid scale in a warming climate. Extra landunits duplicated from the natural vegetated landunit in the CLM sub-grid hierarchy make it possible to prescribe up to three different excess ice conditions in each grid point with permafrost.

465 A test over the Lena river delta showcases that the sub-grid representation of excess ice can retrieve 466 the sub-grid variability of annual thaw-freeze state and the excess ice melt/surface, subsidence through 467 time. On the other hand, initializing excess ice homogeneously throughout the grid cell produces a 468 smaller stabilization effect of excess ice to the permafrost thermal regime and the local surface 469 subsidence under a warming climate. With a tiling scheme ingesting a global data set of excess ice 470 condition into the CLM surface data, our model development shows the capability of portraying more 471 details on simulating permafrost degradation trajectories. As excess ice thermally stabilizes the 472 permafrost on the sub-grid scale, permafrost degrades with a trajectory from continuous permafrost to 473 discontinuous permafrost, and finally to a permafrost-free area. The modeled global pattern of permafrost 474 therefore exhibits regions of discontinuous permafrost as the transition zone between the continuous 475 permafrost and degraded permafrost.

476 This study, for the first time, used an ESM to project excess ice melt/surface subsidence and 477 permafrost degradation with sub-grid variability. The approach of duplicating tiles at the landunit level 478 instead of the column level allows more freedom for further developments in this direction. Furthermore, 479 the new CLM tiling hierarchy has much more potential than representing more accurate excess ice 480 physics as examined in this study. Further advancing the excess ice modeling relies on additional 481 observational studies/datasets of the excess ground ice conditions on a global scale. The model 482 development in our study, therefore, lays the foundation for further advances focusing on excess ice 483 modeling and other processes in the CLM framework that could benefit from an improved sub-grid 484 representation.

485

# 486 Code/Data Availability

- 487 The original Community Land Model is available at <u>https://github.com/ESCOMP/ctsm</u>. The source code
- 488 of model development in this study is available from the corresponding author upon request.

#### 489 Author contributions

- 490 L.C conducted model development work and wrote the initial draft with additional contributions from
- 491 all authors. H.L, S.W, and K.S.A provided ideas and help during the process of model development. H.L
- 492 provided the code of excess ice physics in the earlier version of CLM. L.C prepared all figures.

#### 493 Acknowledgments

494 This study is funded by the Research Council of Norway KLIMAFORSK program (PERMANOR;
495 RCN#255331). K.S.A is supported by the Research Council of Norway EMERALD project
496 (RCN#294948). We thank Sarah Chadburn for helpful comments and suggestions in preparing this
497 manuscript.

498

# 499 Reference

- Aas, K. S., Martin, L., Nitzbon, J., Langer, M., Boike, J., Lee, H., Berntsen, T. K., and Westermann, S.:
  Thaw processes in ice-rich permafrost landscapes represented with laterally coupled tiles in a
  land surface model, The Cryosphere, 13, 591-609, 10.5194/tc-13-591-2019, 2019.
- Brown, J., Ferrians Jr, O., Heginbottom, J., and Melnikov, E.: Circum-Arctic map of permafrost and
   ground-ice conditions, US Geological Survey Reston, VA, 1997.
- Burke, E. J., Dankers, R., Jones, C. D., and Wiltshire, A. J.: A retrospective analysis of pan Arctic
  permafrost using the JULES land surface model, Climate Dynamics, 41, 1025-1038,
  10.1007/s00382-012-1648-x, 2013.
- Cable, S., Elberling, B., and Kroon, A.: Holocene permafrost history and cryostratigraphy in the High Arctic Adventdalen Valley, central Svalbard, Boreas, 47, 423-442, 10.1111/bor.12286, 2018.
- Calmels, F., and Allard, M.: Segregated ice structures in various heaved permafrost landforms through
  CT Scan, Earth Surface Processes and Landforms, 33, 209-225, 10.1002/esp.1538, 2008.

Collier, N., Hoffman, F. M., Lawrence, D. M., Keppel-Aleks, G., Koven, C. D., Riley, W. J., Mu, M.,
and Randerson, J. T.: The International Land Model Benchmarking (ILAMB) system: design,
theory, and implementation, Journal of Advances in Modeling Earth Systems, 10, 2731-2754,
2018.

- Ekici, A., Lee, H., Lawrence, D. M., Swenson, S. C., and Prigent, C.: Ground subsidence effects on
  simulating dynamic high-latitude surface inundation under permafrost thaw using CLM5,
  Geosci. Model Dev., 12, 5291-5300, 10.5194/gmd-12-5291-2019, 2019.
- 519 Fedorova, I., Chetverova, A., Bolshiyanov, D., Makarov, A., Boike, J., Heim, B., Morgenstern, A.,
  520 Overduin, P. P., Wegner, C., Kashina, V., Eulenburg, A., Dobrotina, E., and Sidorina, I.: Lena

- 521 Delta hydrology and geochemistry: long-term hydrological data and recent field observations,
  522 Biogeosciences, 12, 345-363, 10.5194/bg-12-345-2015, 2015.
- Fisher, R. A., and Koven, C. D.: Perspectives on the future of Land Surface Models and the challenges
   of representing complex terrestrial systems, Journal of Advances in Modeling Earth Systems,
   n/a, 10.1029/2018MS001453, 2020.
- Fritz, M., Wetterich, S., Meyer, H., Schirrmeister, L., Lantuit, H., and Pollard, W. H.: Origin and characteristics of massive ground ice on Herschel Island (western Canadian Arctic) as revealed by stable water isotope and Hydrochemical signatures, Permafrost and Periglacial Processes, 22, 26-38, 10.1002/ppp.714, 2011.
- Gilbert, G. L., Kanevskiy, M., and Murton, J. B.: Recent Advances (2008–2015) in the Study of Ground
  Ice and Cryostratigraphy, Permafrost and Periglacial Processes, 27, 377-389, 10.1002/ppp.1912,
  2016.
- Grosse, G., Romanovsky, V., Jorgenson, T., Anthony, K. W., Brown, J., and Overduin, P. P.:
  Vulnerability and feedbacks of permafrost to climate change, Eos, Transactions American
  Geophysical Union, 92, 73-74, 2011.
- Grosse, G., Robinson, J. E., Bryant, R., Taylor, M. D., Harper, W., DeMasi, A., Kyker-Snowman, E.,
  Veremeeva, A., Schirrmeister, L., and Harden, J.: Distribution of late Pleistocene ice-rich
  syngenetic permafrost of the Yedoma Suite in east and central Siberia, Russia, US Geological
  Survey Open File Report, 2013, 1-37, 2013.
- Günther, F., Overduin, P. P., Yakshina, I. A., Opel, T., Baranskaya, A. V., and Grigoriev, M. N.:
  Observing Muostakh disappear: permafrost thaw subsidence and erosion of a ground-ice-rich
  island in response to arctic summer warming and sea ice reduction, The Cryosphere, 9, 151-178,
  10.5194/tc-9-151-2015, 2015.
- Heginbottom, J.A., Dubreuil, M.A. and Harker, P.A.: Canada, Permafrost. National Atlas of Canada.
  Natural Resources Canada, 5th Edition, MCR, 4177, 1995.
- Hugelius, G., Strauss, J., Zubrzycki, S., Harden, J. W., Schuur, E. A. G., Ping, C. L., Schirrmeister, L.,
  Grosse, G., Michaelson, G. J., Koven, C. D., O'Donnell, J. A., Elberling, B., Mishra, U., Camill,
  P., Yu, Z., Palmtag, J., and Kuhry, P.: Estimated stocks of circumpolar permafrost carbon with
  quantified uncertainty ranges and identified data gaps, Biogeosciences, 11, 6573-6593,
  10.5194/bg-11-6573-2014, 2014.
- Kanevskiy, M., Shur, Y., Fortier, D., Jorgenson, M. T., and Stephani, E.: Cryostratigraphy of late
  Pleistocene syngenetic permafrost (yedoma) in northern Alaska, Itkillik River exposure,
  Quaternary Research, 75, 584-596, 10.1016/j.vgres.2010.12.003, 2011.
- Iwahana, G., Fukui, K., Mikhailov, N., Ostanin, O., and Fujii, Y.: Internal Structure of a Lithalsa in the
   Akkol Valley, Russian Altai Mountains, 23, 107-118, 10.1002/pp

- Jorgenson, M., Yoshikawa, K., Kanevskiy, M., Shur, Y., Romanovsky, V., Marchenko, S., Grosse, G.,
  Brown, J., and Jones, B.: Permafrost characteristics of Alaska, Proceedings of the Ninth
  International Conference on Permafrost, 2008, 121-122.p.1734, 2012.
- Kanevskiy, M., Jorgenson, T., Shur, Y., O'Donnell, J. A., Harden, J. W., Zhuang, Q., and Fortier, D.:
  Cryostratigraphy and Permafrost Evolution in the Lacustrine Lowlands of West-Central Alaska,
  Permafrost and Periglacial Processes, 25, 14-34, 10.1002/ppp.1800, 2014.
- 562 Kim, H., Yoshimura, K., Chang, E., Famiglietti, J., and Oki, T.: Century long observation constrained
  563 global dynamic downscaling and hydrologic implication, AGU Fall Meeting Abstracts, 2012.
- Kokelj, S. V., Lacelle, D., Lantz, T. C., Tunnicliffe, J., Malone, L., Clark, I. D., and Chin, K. S.: Thawing
  of massive ground ice in mega slumps drives increases in stream sediment and solute flux across
  a range of watershed scales, Journal of Geophysical Research: Earth Surface, 118, 681-692,
  10.1002/jgrf.20063, 2013.
- Koven, C. D., Ringeval, B., Friedlingstein, P., Ciais, P., Cadule, P., Khvorostyanov, D., Krinner, G., and
  Tarnocai, C.: Permafrost carbon-climate feedbacks accelerate global warming, Proceedings of
  the National Academy of Sciences, 108, 14769-14774, 2011.
- Langer, M., Westermann, S., Boike, J., Kirillin, G., Grosse, G., Peng, S., and Krinner, G.: Rapid
  degradation of permafrost underneath waterbodies in tundra landscapes—toward a
  representation of thermokarst in land surface models, Journal of Geophysical Research: Earth
  Surface, 121, 2446-2470, 2016.
- Langer, M., Westermann, S., Heikenfeld, M., Dorn, W., and Boike, J.: Satellite-based modeling of
  permafrost temperatures in a tundra lowland landscape, Remote Sensing of Environment, 135,
  12-24, https://doi.org/10.1016/j.rse.2013.03.011, 2013.
- Lawrence, D. M., Slater, A. G., Romanovsky, V. E., and Nicolsky, D. J.: Sensitivity of a model projection
  of near-surface permafrost degradation to soil column depth and representation of soil organic
  matter, Journal of Geophysical Research: Earth Surface, 113, 10.1029/2007JF000883, 2008.
- Lawrence, D. M., Oleson, K. W., Flanner, M. G., Thornton, P. E., Swenson, S. C., Lawrence, P. J., Zeng,
  X., Yang, Z. L., Levis, S., and Sakaguchi, K.: Parameterization improvements and functional
  and structural advances in version 4 of the Community Land Model, Journal of Advances in
  Modeling Earth Systems, 3, 2011.
- Lawrence, D. M., Slater, A. G., and Swenson, S. C.: Simulation of present-day and future permafrost and
  seasonally frozen ground conditions in CCSM4, Journal of Climate, 25, 2207-2225, 2012.
- Lawrence, D. M., Koven, C. D., Swenson, S. C., Riley, W. J., and Slater, A. G.: Permafrost thaw and
  resulting soil moisture changes regulate projected high-latitude CO2 and CH4 emissions,
  Environmental Research Letters, 10, 094011, 10.1088/1748-9326/10/9/094011, 2015.
- Lawrence, D. M., Fisher, R. A., Koven, C. D., Oleson, K. W., Swenson, S. C., Bonan, G., Collier, N.,
  Ghimire, B., van Kampenhout, L., Kennedy, D., Kluzek, E., Lawrence, P. J., Li, F., Li, H.,

- 592 Lombardozzi, D., Riley, W. J., Sacks, W. J., Shi, M., Vertenstein, M., Wieder, W. R., Xu, C., 593 Ali, A. A., Badger, A. M., Bisht, G., van den Broeke, M., Brunke, M. A., Burns, S. P., Buzan, 594 J., Clark, M., Craig, A., Dahlin, K., Drewniak, B., Fisher, J. B., Flanner, M., Fox, A. M., Gentine, 595 P., Hoffman, F., Keppel-Aleks, G., Knox, R., Kumar, S., Lenaerts, J., Leung, L. R., Lipscomb, 596 W. H., Lu, Y., Pandey, A., Pelletier, J. D., Perket, J., Randerson, J. T., Ricciuto, D. M., 597 Sanderson, B. M., Slater, A., Subin, Z. M., Tang, J., Thomas, R. Q., Val Martin, M., and Zeng, 598 X.: The Community Land Model Version 5: Description of New Features, Benchmarking, and 599 Impact of Forcing Uncertainty, 11, 4245-4287, 10.1029/2018ms001583, 2019.
- Lee, H., Swenson, S. C., Slater, A. G., and Lawrence, D. M.: Effects of excess ground ice on projections
  of permafrost in a warming climate, Environmental Research Letters, 9, 124006, 2014.
- Liu, L., Zhang, T., and Wahr, J.: InSAR measurements of surface deformation over permafrost on the
  North Slope of Alaska, Journal of Geophysical Research: Earth Surface, 115,
  10.1029/2009jf001547, 2010.
- Loranty, M. M., and Goetz, S. J.: Shrub expansion and climate feedbacks in Arctic tundra, Environmental
  Research Letters, 7, 011005, 10.1088/1748-9326/7/1/011005, 2012.
- Nitzbon, J., Langer, M., Westermann, S., Martin, L., Aas, K. S., and Boike, J.: Pathways of ice-wedge
  degradation in polygonal tundra under different hydrological conditions, The Cryosphere, 13,
  1089-1123, 10.5194/tc-13-1089-2019, 2019.
- Nitzbon, J., Westermann, S., Langer, M., Martin, L. C. P., Strauss, J., Laboor, S., and Boike, J.: Fast
  response of cold ice-rich permafrost in northeast Siberia to a warming climate, Nature
  Communications, 11, 2201, 10.1038/s41467-020-15725-8, 2020.
- O'Neill, H. B., Wolfe, S. A., and Duchesne, C.: New ground ice maps for Canada using a paleogeographic
  modelling approach, The Cryosphere, 13, 753-773, 10.5194/tc-13-753-2019, 2019.
- Pascale, G. P. D., Pollard, W. H., and Williams, K. K. J. J. o. G. R. A.: Geophysical mapping of ground
  ice using a combination of capacitive coupled resistivity and ground-penetrating radar,
  Northwest Territories, Canada, 113, 2008.
- Rachold, V., and Grigoriev, M.: Russian-German Cooperation SYSTEM LAPTEV SEA 2000: The Lena
  Delta 1998 Expedition, Berichte zur Polarforschung (Reports on Polar Research), 315, 1999.
- Schaefer, K., Lantuit, H., Romanovsky, V. E., Schuur, E. A. G., and Witt, R.: The impact of the
  permafrost carbon feedback on global climate, Environmental Research Letters, 9, 085003,
  10.1088/1748-9326/9/8/085003, 2014.
- Schirrmeister, L., Grosse, G., Schwamborn, G., Andreev, A. A., Meyer, H., Kunitsky, V. V., Kuznetsova,
  T. V., Dorozhkina, M. V., Pavlova, E. Y., Bobrov, A. A., and Oezen, D.: Late Quaternary
  History of the Accumulation Plain North of the Chekanovsky Ridge (Lena Delta, Russia): A
  Multidisciplinary Approach, Polar Geography, 27, 277-319, 10.1080/789610225, 2003.

627	Schirrmeister, L., Grosse, G., Schnelle, M., Fuchs, M., Krbetschek, M., Ulrich, M., Kunitsky, V.,			
628	Grigoriev, M., Andreev, A., Kienast, F., Meyer, H., Babiy, O., Klimova, I., Bobrov, A.,			
629	Wetterich, S., and Schwamborn, G.: Late Quaternary paleoenvironmental records from the			
630	western Lena Delta, Arctic Siberia, Palaeogeography, Palaeoclimatology, Palaeoecology, 299,			
631	175-196, https://doi.org/10.1016/j.palaeo.2010.10.045, 2011.			
632	Schirrmeister, L., Froese, D., Tumskoy, V., Grosse, G., and Wetterich, S.: Yedoma: Late Pleistocene ice-			
633	rich syngenetic permafrost of Beringia, in: Encyclopedia of Quaternary Science. 2nd edition,			
634	Elsevier, 542-552, 2013.			
635	Schneider, J., Grosse, G., and Wagner, D.: Land cover classification of tundra environments in the Arctic			
636	Lena Delta based on Landsat 7 ETM+ data and its application for upscaling of methane			
637	emissions, Remote Sensing of Environment, 113, 380-391,			
638	https://doi.org/10.1016/j.rse.2008.10.013, 2009.			
639 640 641	<ul> <li>Schuur, E. A., Bockheim, J., Canadell, J. G., Euskirchen, E., Field, C. B., Goryachkin, S. V., Hagemann,</li> <li>S., Kuhry, P., Lafleur, P. M., and Lee, H.: Vulnerability of permafrost carbon to climate change: Implications for the global carbon cycle, BioScience, 58, 701-714, 2008.</li> </ul>			
642	Schuur, E. A. G., McGuire, A. D., Schädel, C., Grosse, G., Harden, J. W., Hayes, D. J., Hugelius, G.,			
643	Koven, C. D., Kuhry, P., Lawrence, D. M., Natali, S. M., Olefeldt, D., Romanovsky, V. E.,			
644	Schaefer, K., Turetsky, M. R., Treat, C. C., and Vonk, J. E.: Climate change and the permafrost			
645	carbon feedback, Nature, 520, 171, 10.1038/nature14338, 2015.			
646 647 648	Schwamborn, G., Rachold, V., and Grigoriev, M. N.: Late Quaternary sedimentation history of the Lena Delta, Quaternary International, 89, 119-134, https://doi.org/10.1016/S1040-6182(01)00084-2, 2002.			
649	Seppälä, M.: Synthesis of studies of palsa formation underlining the importance of local environmental			
650	and physical characteristics, Quaternary Research, 75, 366-370,			
651	https://doi.org/10.1016/j.yqres.2010.09.007, 2011.			
652 653	Sharkhuu, N.: Occurrence of frost heaving in the Selenge River Basin, Mongolia, 10, 187-192, 10.1002/(sici)1099-1530(199904/06)10:2<187::Aid-ppp294>3.0.Co;2-w, 1999.			
654	Shiklomanov, N. I., Streletskiy, D. A., Little, J. D., and Nelson, F. E.: Isotropic thaw subsidence in			
655	undisturbed permafrost landscapes, Geophysical Research Letters, 40, 6356-6361,			
656	10.1002/2013gl058295, 2013.			
657 658	Slater, A. G., and Lawrence, D. M.: Diagnosing present and future permafrost from climate models, Journal of Climate, 26, 5608-5623, 2013.			
659 660 661	<ul> <li>Streletskiy, D. A., Shiklomanov, N. I., Little, J. D., Nelson, F. E., Brown, J., Nyland, K. E., and Klene,</li> <li>A. E.: Thaw Subsidence in Undisturbed Tundra Landscapes, Barrow, Alaska, 1962–2015,</li> <li>Permafrost and Periglacial Processes, 28, 566-572, 10.1002/ppp.1918, 2017.</li> </ul>			

- Swenson, S. C., Clark, M., Fan, Y., Lawrence, D. M., and Perket, J.: Representing Intrahillslope Lateral
  Subsurface Flow in the Community Land Model, Journal of Advances in Modeling Earth
  Systems, 11, 4044-4065, 10.1029/2019MS001833, 2019.
- Treat, C. C., Natali, S. M., Ernakovich, J., Iversen, C. M., Lupascu, M., McGuire, A. D., Norby, R. J.,
  Roy Chowdhury, T., Richter, A., Šantrůčková, H., Schädel, C., Schuur, E. A. G., Sloan, V. L.,
  Turetsky, M. R., and Waldrop, M. P.: A pan-Arctic synthesis of CH4 and CO2 production from
  anoxic soil incubations, 21, 2787-2803, 10.1111/gcb.12875, 2015.
- 669 Turetsky, M. R., Abbott, B. W., Jones, M. C., Anthony, K. W., Olefeldt, D., Schuur, E. A., Koven, C.,
- McGuire, A. D., Grosse, G., and Kuhry, P.: Permafrost collapse is accelerating carbon release,
  Nature, 569, 32-34, 2019.
- Ulrich, M., Grosse, G., Chabrillat, S., and Schirrmeister, L.: Spectral characterization of periglacial
  surfaces and geomorphological units in the Arctic Lena Delta using field spectrometry and
  remote sensing, Remote Sensing of Environment, 113, 1220-1235,
  https://doi.org/10.1016/j.rse.2009.02.009, 2009.
- Walter, K. M., Zimov, S. A., Chanton, J. P., Verbyla, D., and Chapin, F. S.: Methane bubbling from
  Siberian thaw lakes as a positive feedback to climate warming, Nature, 443, 71-75,
  10.1038/nature05040, 2006.
- West, J. J., and Plug, L. J.: Time-dependent morphology of thaw lakes and taliks in deep and shallow
  ground ice, Journal of Geophysical Research: Earth Surface, 113, 10.1029/2006jf000696, 2008.
- Westermann, S., Langer, M., Boike, J., Heikenfeld, M., Peter, M., Etzelmüller, B., and Krinner, G.:
  Simulating the thermal regime and thaw processes of ice-rich permafrost ground with the landsurface model CryoGrid 3, Geosci. Model Dev., 9, 523-546, 10.5194/gmd-9-523-2016, 2016.
- Wünnemann, B., Reinhardt, C., Kotlia, B. S., and Riedel, F.: Observations on the relationship between
  lake formation, permafrost activity and lithalsa development during the last 20 000 years in the
  Tso Kar basin, Ladakh, India, 19, 341-358, 10.1002/ppp.631, 2008.
- Zhang, T., Barry, R. G., Knowles, K., Heginbottom, J. A., and Brown, J.: Statistics and characteristics
  of permafrost and ground-ice distribution in the Northern Hemisphere, Polar Geography, 23,
  132-154, 10.1080/10889379909377670, 1999.
- Zhang, T., Heginbottom, J. A., Barry, R. G., and Brown, J.: Further statistics on the distribution of
  permafrost and ground ice in the Northern Hemisphere, Polar Geography, 24, 126-131,
  10.1080/10889370009377692, 2000.
- Zimov, S. A., Schuur, E. A., and Chapin, F. S.: Permafrost and the global carbon budget, Science, 312,
  1612-1613, 2006.

# Table 1: The excess ice initialization scenario in each of the three terraces (landunits) for the Lena River delta, as well as that for the single-landunit excess ice initialization case.

698

Depth (after adding ice)	Volumetric Ice content	Area weight			
No excess ice terrain					
N/A	0%	24.6%			
Holocene ground ice terrain					
0.9-9 m	65%	66.6%			
Yedoma ice complex					
0.6-20 m	90%	8.8%			
Average ice single-landunit case					
0.6-0.9 m	7.92%	100%			
0.9-9 m	51.21%	100%			
9-20 m	7.92%	100%			

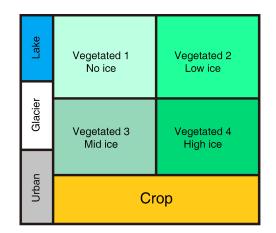
Overall visible ground ice content for each CAPS point	Tiling scheme (area weights for each excess ice category)	Eligible CAPS types
5%	80% no excess ice; 20% Low	clf; clf; slf; ilf; clr; dlr; slr; ilr
15%	58% no excess ice; 20% Low; 22% Medium	cmf; dmf; smf; imf; dhr; shr; ihr
15%	66% no excess ice; 20% Low; 14% High	chr
25%	44% no excess ice; 20% Low; 22% Medium; 14% High	dhf; shf; ihf
25%	52% no excess ice; 20% Low; 28% High	chf

# Table 2: The tiling scheme prescribing area weights of landunits for each CAPS class. The detailed CAPS classes are shown in Figure 2.

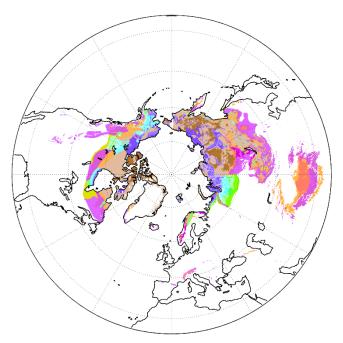
703 Note: For each class, the first letter is for the permafrost extent, the second for the excess ice content, and the third
704 for the terrain and overburden, following Brown et al. (2002).

706 Table 5: List of simulations conducted for this study.	706	Table 3: List of simulations conducted for this study.
--	-----	--

Cases	Description			
Single point cases for the Lena river delta				
Triple-landunit case	Applying the sub-grid representation of excess ice. Three natural vegetated landunit initialized.			
Average ice single- landunit case	Not applying the sub-grid representation of excess ice. Only one natural vegetated landunit initialized. The grid-mean excess ice content for each soil layer in the only landunit is calculated by spatially averaging those in different landunits in the triple-landunit case.			
Global simulation cases				
No ice case	Not adding any excess ground ice (the original CLM5 simulation).			
Sub-grid ice case	Applying the sub-grid representation of excess ice. A tiling scheme helps to "translate" excess ice conditions in the CAPS data to fit what the CLM5 requires.			
Grid-average ice case	Not applying the sub-grid representation of excess ice. The grid-mean excess ice content for each soil layer is calculated by spatially averaging those in different landunits in the sub-grid ice case.			



- 710 Figure 1: Modification of the CLM5 tiling hierarchy on the landunit level containing four natural
- 711 vegetated landunits for different excess ice conditions.



Permafrost area classification

	Ground Ice Content (percent by volume)				
Permafrost Extent	Lowlands, highlands, and intra-and intermontane depressions			Mountains, highlands, ridges, and plateaus	
	25%	15%	5%	15%	5%
Continous (100%)	chf	cmf	clf	chr	clr
Discontinous (70%)	dhf	dmf	dlf	dhr	dlr
Sporadic (30%)	shf	smf	slf	shr	slr
Isolated (5%)	ihf	imf	ilf	ihr	ilr

713

\* Letter code naming: The first letter is for the permafrost extent, second for the ground excess ice concent, and the thrid for the terrain and overburden.

714 Figure 2: Spatial distribution of excess ground ice in the Northern Hemisphere modified from

715 Brown et al. (2002). Compared to the original data, permafrost extents and ground ice contents

716 are converted to definite numbers (percentages) for model computation.

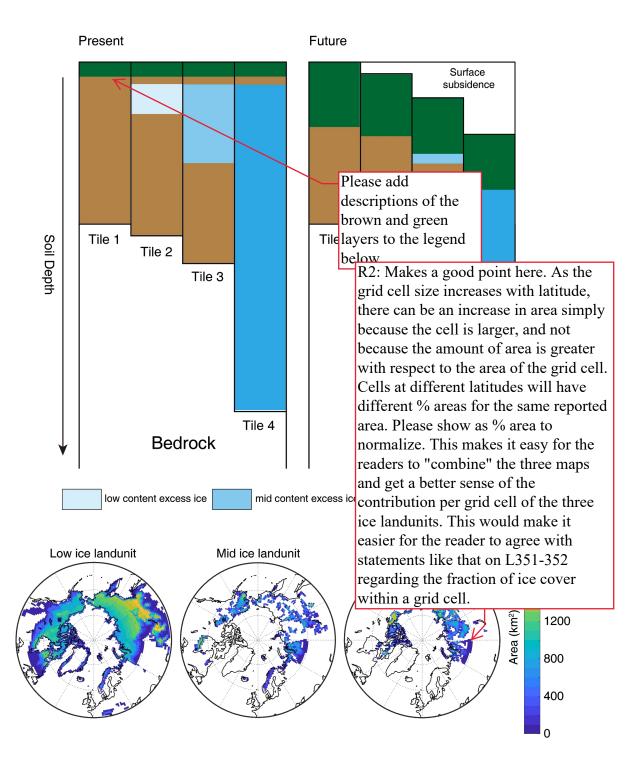


Figure 3. Schematic representation of the sub-grid excess ice initialization scenario, and maps
showing the area occupied by different excess ice landunits, i.e. the initial condition of excess ice in
the global simulation.

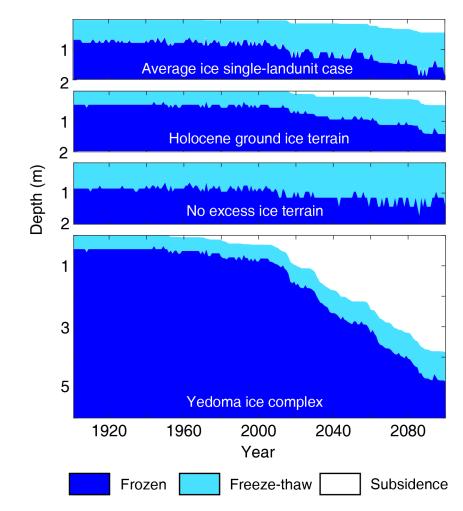


Figure 4. Annual freeze-thaw state for the three terraces for the triple-landunit case, as well as for

726 the average ice single-landunit case.

727

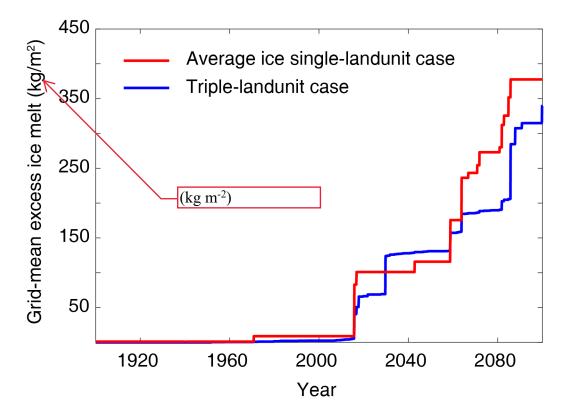


Figure 5. Grid-mean excess ice melt since 1900 for the single-point cases over the Lena river delta
with and without the sub-grid excess ice initialization.

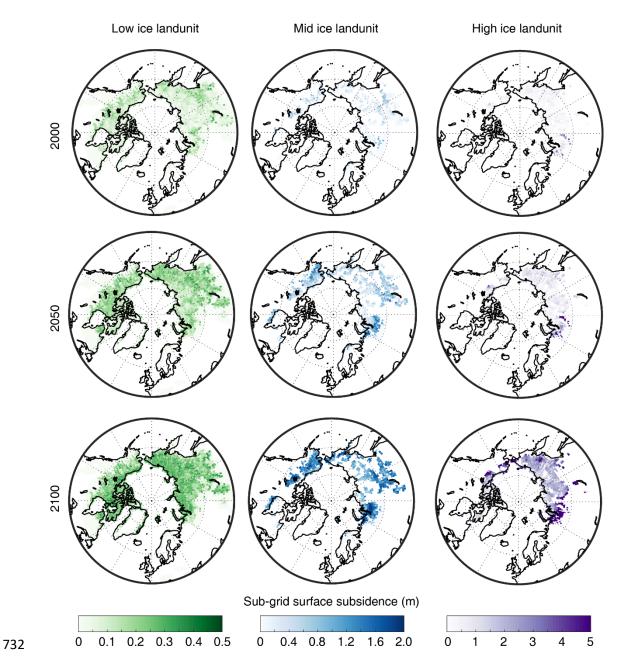


Figure 6. Maps showing sub-grid surface subsidence (m) in 2000, 2050, 2100 in the low, mid, and
high excess ice landunits in the sub-grid ice case.

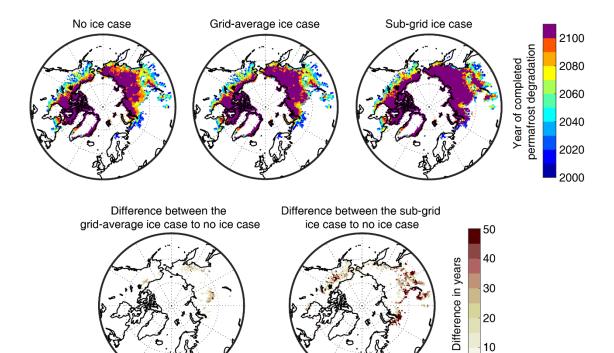
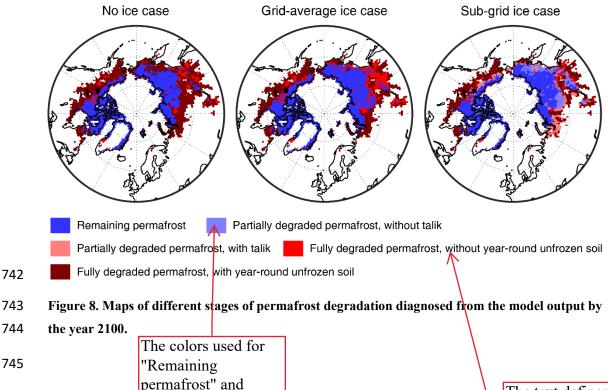


Figure 7. Maps showing the year of completed permafrost degradation (upper set of three maps),
as well as the differences between cases (lower set of two maps). The purple color indicates the
existence of permafrost in these grid points by 2100. The difference in years is provided only for
grid cell with completed permafrost degradation before 2100.



The colors used for "Remaining permafrost" and "partially degraded permafrost" are too close. Please better differentiate these two classes, and probably the others as well. As per our instructions to authors, you may find ColorBrewer 2.0 is useful for generating a helpful color scheme for these maps.

The text defines what fully degraded permafrost is, but please define somewhere what the difference is between "with" and "without" year-round frozen soil. In particular, as seasonal frost is expected within the entire model domain, how can there be year-round unfrozen soil? Probably best to define the 5 stages within one paragraph so that the reader has a clear understanding of the terminology.

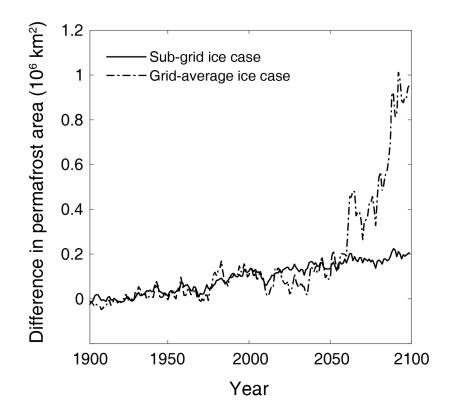


Figure 9. Difference in modeled permafrost area vsz time between the sub-grid ice case and no ice
case, as well as between the grid-average ice case and no ice case.

# Supplemental material for "Projecting Circum-Arctic Excess Ground Ice Melt with a sub-grid representation in the Community Land Model"

## S1. The sensitivity of excess ice melt and corresponding impacts to its sub-grid distribution

We design idealized single-grid simulation cases, aiming to examine the effects of incorporating excess ice at the sub-grid scale to soil physics, i.e. whether different sub-grid scale distributions of excess ice differ reasonably from each other during excess ice melt. The results of single-grid simulations help to verify if the sub-grid representation of excess ice shows more potential in modeling excess ice compared to its previous version, where excess ice is homogeneously distributed in the CLM grid cell (Lee et al., 2014). We employ the forcing data at the North Slope of Alaska (NSA; 70° N, 156° W) and to the Northeast of Yakutsk (Yakutsk; 63° N, 130° E) to represent the continental and maritime types of climate respectively in the circum-Arctic. They have the annual mean temperature and precipitation close to each other, while the seasonal variability in temperature is smaller in the North Slope of Alaska due to its adjacency to the Arctic Ocean (Bieniek et al., 2012).

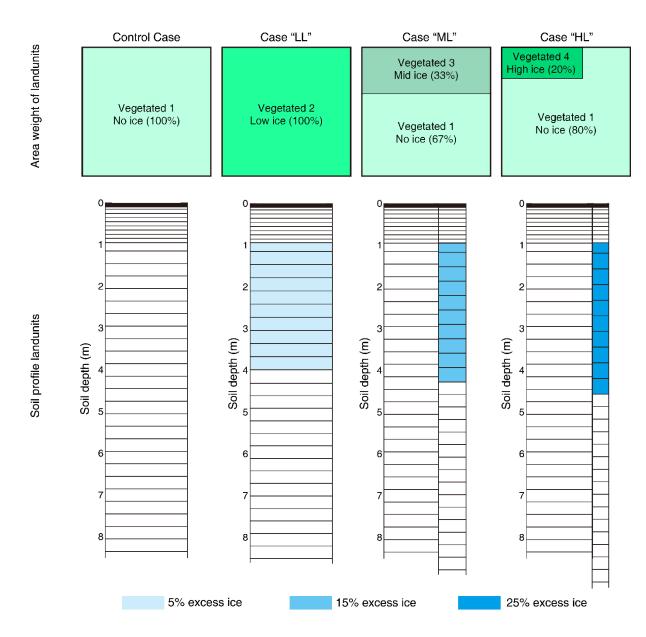


Figure S1: The schematic figure for the area weights (the percentage between parentheses) and soil profiles within the landunits in the four single-grid simulations. Besides the control case, three other cases are with the same amount of excess ice within the single grid. "LL", "ML", and "HL" are abbreviations for "Low ice Landunit", "Mid ice Landunit", and "High ice Landunit", representing the applied excess ice landunit in each case.

The grid-mean volumetric excess ice content is set to be 5%. We set up three excess ice cases with the same (or very close) grid-scale excess ice content but with different spatial variability. For each site, we design three cases, having a 100% area weight of 5% volumetric excess ice content (NSA\_LL and Yakutsk\_LL), a 33% area weight of 15% volumetric excess ice content (NSA\_ML and Yakutsk\_ML), and a 20% area weight of 25% volumetric excess ice content (NSA\_HL and Yakutsk\_HL), respectively (Figure S1). For all of the original soil layers between 1-4 meters, excess ice is incorporated homogeneously, which proportionally increases the soil thickness for these layers. The initialization depth of excess ice keeps the same as in Lee et al. (2014). Both locations we choose are with 100% natural soil and continuous permafrost to avoid the interference of model results by other landunit types from the source.

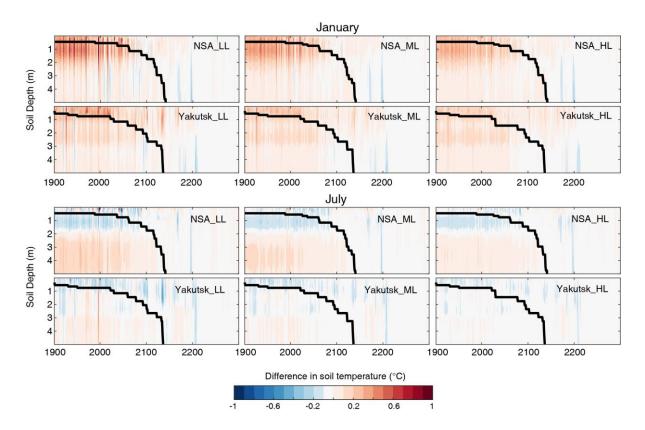


Figure S2: Soil temperature differences from excess ice cases to control cases (NSA\_control and Yakutsk\_control) for the depth of 0.005-5 meters in January and July. Black lines are the active layer depth deepening through time. The active layer depth is calculated from grid-scale soil temperature for each case.

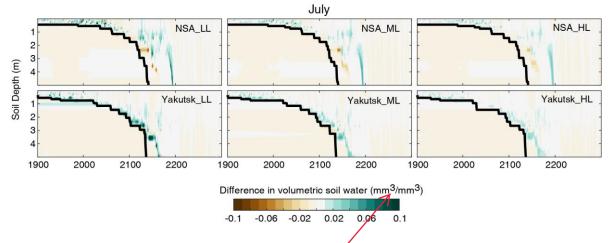


Figure S3: Soil moisture differences from excess ice cases to the corresponding control cases (NSA\_control and Yakutsk\_control) for the depth of 0.05-5 motors in July Plock lines are the active layer depth deepening (mm<sup>3</sup> mm<sup>-3</sup>) through time. The active layer depth is calculated from grad-scale son temperature for each case.

As a result, differences in soil temperature and moisture from excess ice cases to control cases in single-grid simulations quantitatively show the effects of excess ice and its melting. In the shallower layers (0-2 m), excess ice results in slightly higher soil temperature in January (winter) but lower soil temperature in July (summer) relative to control cases, reducing the magnitude of the seasonal cycle in soil temperature (Figure S2). In deeper layers (>2 m), the soil temperature in excess ice cases remains higher compared to control cases for both in summer and winter. The above responses in permafrost temperature results from the increases of specific heat and thermal conductivity of the soil layer after incorporating excess ice. As the climate warms and permafrost thaws, the meltwater discharges in the form of runoff, eventually bringing soil temperatures in excess ice cases closer to that in the control case. For soil moisture, the volumetric water content in July is higher in excess ice cases than control and is just above the permafrost table (Figure S3). As the active layer substantially deepens in the projected period for both sites, soil water in excess ice cases increases abruptly around 2180 for NSA while around 2150 for Yakutsk, indicating the degradation of permafrost in control cases. When permafrost degrades in the control case, the excess soil water in control cases starts of runoff in the form of subsurface drainage, flushing out soil water and making the soil drier. Meanwhile, this has not occurred in excess ice cases yet, making the soil wetter in excess ice cases than in control cases. These responses in permafrost temperature and moisture after permafrost degradation are consistent with the results in Lee et al. (2014), suggesting that the excess ice physics developed in CLM4.5\_EXICE performs reasonably in a sub-grid manner in CLM5. Among the three excess ice cases, the "LL" case shows the strongest responses in both soil temperature and soil water content. On the other hand, the effects of excess ice in soil temperature and moisture are weaker in the "ML" and "HL" cases, where the same amount of excess ice is distributed more localized within a fraction of the grid.

Both sites exhibit active layer depth of around 0.5 m by the end of the spinup and active layer thickness does not increase substantially during the historical period (Black lines in Figure S2 and S3). For this reason, excess ice is incorporated one meter below the surface. No excess ice, therefore, melts during either the spin-up or the historical period simulations. Excess ice starts to melt around the 2070s in NSA\_LL, while the timing is delayed for about 25 years in the other two cases for the same site (NSA\_ML and NSA\_HL; Figure S4). It is because the higher content of excess ice covering a smaller area takes longer to absorb enough latent heat of fusion from the

atmosphere before it can start melting. Excess ice in NSA completely melts away in the 2170s and the exact timing of which varies slightly (< 5 years) between cases. In Yakutsk, excess ice starts to melt earlier, but with a slower rate compared to NSA. Similar to the NSA cases, Yakutsk\_ML and Yakutsk\_HL exhibit delays in the timing of excess ice melt compared to Yakutsk\_LL. Excess ice in Yakutsk\_LL completely melts in the 2170s, while the timings of excess ice melting in Yakutsk\_ML and Yakutsk\_HL is delayed for about 10 to 15 years, respectively (Figure S4).

Excess ice melting supplies extra water to subsurface water storage, increasing soil water and eventually converting to runoff. The increases in surface runoff correspond well in timing with excess ice melt (Figure S4). Earlier permafrost thaw timing in control cases causes an earlier increase in subsurface runoff and a decrease in the surface runoff than in excess ice cases. On the other hand, when the active layer depth reaches below the deepest soil layer in excess ice cases, more soil water from melt ice leads to the higher subsurface runoff compared to that in control cases. Among the three excess ice cases, the "LL" cases consistently exhibit the strongest and earliest responses in both surface and subsurface runoff as excess ice melts, being consistent with their earlier

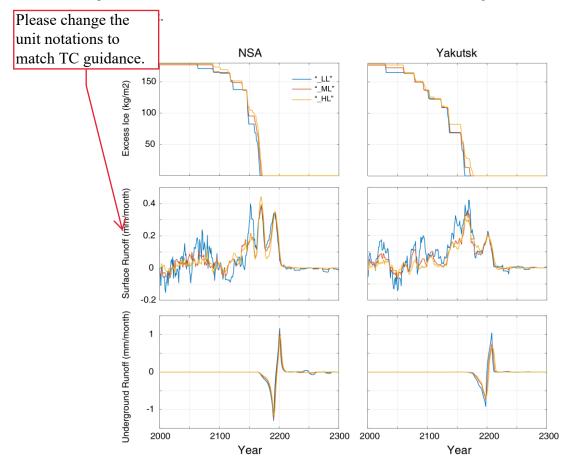


Figure S4: Time series of excess ice (kg/m<sup>2</sup>), as well as the difference of surface runoff (mm/month) and subsurface drainage (mm/month) from the three excess ice cases to control cases. A 15-year moving average is applied before plotting both the surface and underground runoff.

# References

- Bieniek, P. A., Bhatt, U. S., Thoman, R. L., Angeloff, H., Partain, J., Papineau, J., Fritsch, F., Holloway, E., Walsh, J. E., Daly, C., Shulski, M., Hufford, G., Hill, D. F., Calos, S., and Gens, R.: Climate Divisions for Alaska Based on Objective Methods, Journal of Applied Meteorology and Climatology, 51, 1276-1289, 10.1175/jamc-d-11-0168.1, 2012.
- Lee, H., Swenson, S. C., Slater, A. G., and Lawrence, D. M.: Effects of excess ground ice on projections of permafrost in a warming climate, Environmental Research Letters, 9, 124006, 2014.