Dear editor,

Thank you very much for your valuable review and point-by-point comments. We have revised the manuscript carefully following your comments and suggestions. The revised manuscript and the supplemental material with marked changes are included as follow.

Sincerely,
Lei Cai, on behalf of all coauthors.

Projecting circum-Arctic excess ground ice melt with a sub-grid representation in the Community Land Model

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Abstract To address the longstanding underrepresentation of the influences of highly variable ground ice content on the trajectory of permafrost conditions simulated in Earth System Models under a warming climate, we implement a sub-grid representation of excess ground ice within permafrost soils using the latest version of the Community Land Model (CLM5). Based on the original CLM5 tiling hierarchy, we duplicate the natural vegetated landunit by building extra tiles for up to three cryostratigraphies with different amounts of excess ice for each grid cell. For the same total amount of excess ice, introducing sub-grid variability in excess ice contents leads to different excess ice melting rates at the grid level. In addition, there are impacts on permafrost thermal properties and local hydrology with sub-grid representation. We evaluate this new development with single-point simulations at the Lena river delta, Siberia, where three sub-regions with distinctively different excess ice conditions are observed. A triple-landunit case accounting for this spatial variability conforms well to previous model studies for the Lena river delta and displays a markedly different dynamics of future excess ice thaw compared to a single-landunit case initialized with average excess ice contents. For global simulations, we prescribed a tiling scheme combined with our sub-grid representation to the global permafrost region using presently available circum-Arctic ground ice data~~using the dataset "Circum-Arctic Map of Permafrost and Ground-Ice Conditions" (Brown et al., 1997)~~. The sub-grid scale excess ice produces significant melting of excess ice under a warming climate and enhances the representation of sub-grid variability of surface subsidence on a global scale. Our model development makes it possible to portray more details on the permafrost degradation trajectory depending on the sub-grid soil thermal regime and excess ice melting, which also shows a strong indication that accounting for excess ice is a prerequisite of a reasonable projection of permafrost thaw. The modeled permafrost degradation with sub-grid excess ice follows the pathway that continuous permafrost transforms into discontinuous permafrost before it disappears, including surface subsidence and talik formation, which are highly permafrost-relevant landscape changes excluded from most land models. Our development of sub-grid representation of excess ice demonstrates a way forward to improve the realism of excess ice melt in global land models, but further developments require substantially improved ~~rely on additional~~ global observational datasets on both the horizontal and vertical distributions of excess ground ice.

1. Introduction

Permafrost soils are often characterized by different types of ground ice that can exceed the pore space (Brown et al. 1997; Zhang et al., 1999). The presence of such "excess" ground ice can alter the permafrost thermal regime and landscape structure. Widespread thawing of permafrost is expected in a warmer future climate and modeling studies suggest large-scale degradation of near-surface permafrost at the end of the 21st century (Lawrence et al., 2008 & 2011). Melting of ground ice due to active layer thickening releases water in the form of surface runoff, subsurface flow, or both, causing ~~in the form of surface and/or subsurface runoff, causing~~ surface subsidence and modifying the local hydrological cycle (West and Plug, 2008; Grosse et al., 2011; Kokelj et al., 2013; Westermann et al., 2016). In addition to containing ground ice, some permafrost soils store massive amounts of carbon, which could be released to the atmosphere in the form of greenhouse gases upon thawing (Walter et al., 2006; Zimov et al., 2006; Schuur et al., 2008), possibly making a positive feedback to amplify future climate change (Koven et al.,

2011; Schaefer et al., 2014; Burke et al., 2013). The existence of excess ice and its distribution in permafrost can significantly affect the rate of permafrost thawing (Westermann et al., 2016; Nitzbon et al., 2020), and in turn, the rate of soil carbon release (Hugelius et al., 2014; Schuur et al., 2015; Turetsky et al., 2019). Therefore, better projections of excess ice melt are critical to improve our understanding of the impacts of permafrost thaw on corresponding climatic impacts.

Previous studies address excess ice modeling on the local or regional scale, in which the small study area makes it possible for detailed configurations of the cryostratigraphy of permafrost and excess ice based on observations. Simulations for the Lena river delta have retrieved the permafrost thermal dynamics fairly close to the observations with excess ice incorporated in the modeling (Westermann et al., 2016). A two-tile approach allowing lateral heat exchange between two land elements demonstrated that maintaining thermokarst ponds requires the heat loss from water to the surrounding land (Langer et al., 2016). A similar tiling approach has been applied to projecting the landscape changes due to permafrost thaw for ice-wedge polygons and peat plateaus with different features of ice melting and surface subsidence (Aas et al., 2019; Nitzbon et al., 2019).

On the global scale, the land components of Earth System Models (ESMs) have significant capabilities of representing key permafrost physics. In the Community Land Model (CLM), for example, the representation of permafrost-associated processes has been continuously improved~~ving~~. By including key thermal and hydrological processes of permafrost, the CLM version 4 (CLM4) has reasonably reproduced the global distribution of permafrost (Lawrence et al., 2008; Lawrence et al., 2012; Slater and Lawrence, 2013). Projections based on the CLM4 under its highest warming scenario (RCP8.5) have shown over 50% degradation of near-surface permafrost by 2100 (Lawrence et al., 2012). Moreover, the recently released CLM5 has more advanced representations of many biogeophysical and biogeochemical processes (Lawrence et al., 2019). A refined soil profile and upgraded snow accumulation and densification scheme in the CLM5 could contribute to simulating more realistic permafrost thermal regimes, whereas upgrades on biogeochemistry improve simulations of soil carbon release in response to permafrost thaw. In addition, an excess ice physics scheme has been implemented in CLM4.5 (CLM4.5_EXICE) by Lee et al. (2014), which allowed for the first-order simulation of surface subsidence globally by modeling excess ice melt under a warming climate.

The homogeneous distribution of excess ice throughout the grid cell in CLM4.5_EXICE (Lee et al., 2014) could cause biases in thaw trajectories in the warming climate. In nature, excess ice forms in a highly localized manner due to a variety of accumulation processes. For instance, segregated ice formed during frost heave differs substantially in excess ice morphology from ice wedges that are formed from repeated frost cracking and freezing of penetrating water. Field measurements illustrate that the depth distribution of ground ice can vary substantially on the order to 10-50 ~~meters~~ metres horizontally and 0-10 metrce~~r~~s vertically (Pascale et al., 2008; Fritz et al., 2011). The horizontal grid spacing of ESMs, on the other hand, usually ranges from one to two degrees (~100-200 km horizontal scale), which makes it impossible to represent localized excess ice. The mismatch in spatial scale between model and the real world raises concerns for the reliability of excess ice modeling in ESMs. Aside from the homogenously

-initialized excess ice in the grid cell, CLM4.5_EXICE initializes excess ice in the same soil depths globally (below 1m), regardless of the varying active layer thickness in circum-Arctic permafrost areas (Lee et al., 2014). Such deficiencies in excess ice parameterization hamper global projections of permafrost thaw including excess ice with ESMs.

To narrow the gap between the high spatial variability of excess ice and the coarse grid spacing in the ESMs, we applied a sub-grid approach in representing excess ice in permafrost soils within the CLM5 to investigate how presence and melting of excess ice affect land surface physics under a warming climate. We conducted idealized single-point simulations to examine the robustness of model development~~. We~~, and furthermore conducted global simulations using a first-order estimate for the spatial distribution of excess ice and associated cryostratigraphies. ~~, aiming to present a model framework that can eventually bring the modeling towards a higher accuracy.~~ Due to the lack of information in global excess ice conditions, it is not the aim of this study to accurately project excess ice melt and surface subsidence in the 21st century, but rather to develop and present a functionable process within a land surface model that can eventually bring permafrost thaw modeling towards a higher degree of accuracy on a global scale. The CLM5 with sub-grid excess ice representation developed through this study would be ready to serve as a proper simulation tool on further advancing global excess ice modeling once new datasets become available.

2. Methodology

2.1 Sub-grid representation of excess ice in the CLM5

The CLM5 model utilizes a three-level tiling hierarchy to represent sub-grid heterogeneity of landscapes, which are (from top to bottom) landunits, columns, and patches (Lawrence et al., 2019). There is only one column (the natural soil column) that is under the natural vegetated landunit, which represents soil including permafrost. In this study, we modify the CLM5 tiling hierarchy by duplicating the natural vegetated landunit, making extra landunits for prescribing up to three different excess ice conditions in permafrost (Figure 1). The original natural vegetated landunit is considered as "natural vegetated with no excess ice" (hereafter no ice landunit), while we denote the additional landunits as "natural vegetated with low content of excess ice" (hereafter the low ice landunit), "natural vegetated with medium content of excess ice" (hereafter the mid ice landunit), and "natural vegetated with high content of excess ice" (hereafter the high ice landunit). The sub-grid initial conditions of excess ice are imported as part of the surface data, which includes the variables of volumetric excess ice contents, depths of the top and bottom soil layer of added excess ice, and the area weights of the four landunits.

We adopted the excess ice physics from CLM4.5_EXICE (Lee et al., 2014), including thermodynamic and hydrological processes. The added excess ice is evenly distributed within each soil layer. ~~Note that~~Whereas the original CLM5 model already represents the dynamics of pore ice~~. Our~~, our representation of excess ice physics only addresses the ground ice bodies that exceed soil pore space. The volumetric excess ice content in this study is defined as the ratio of the volume of excess ice in a soil

layer to the volume of the whole soil layer. For example, a 50% volumetric content of excess ice means the excess ice body occupies 50% volume of a soil layer, while the rest of soil (and pore ice) occupies the other 50% volume of the soil layer. If not otherwise notified, the parameter of volumetric ice content in this manuscript refers only to that of excess ice bodies. After adding excess ice, the soil layer thickness increases accordingly. Because ice density is considered constant, the increase of soil layer thickness is linearly proportional to the volumetric content of excess ice. For example, adding an excess ice body with a 50% volumetric excess ice content doubles the soil layer thickness of the corresponding soil layer. The revised algorithm for thermal conductivity and heat capacity of soil involves the effects of added excess ice, while the revised phase change energy equation allows excess ice to melt. The meltwater adds to soil liquid water in the same soil layer, and it can move to the above layer if the original layer is saturated. Such numerical implementation replicates how the melt excess ice eventually converts to runoff and discharges from the soil in case of well-drained conditions. As excess ice melts, soil layer thickness decreases, which corresponds to surface subsidence due to excess ice melt. In our model parameterization, excess ice only melts and does not re-form since the applied excess ice physics does not account for the different ice formation processes.

Aside from sub-grid tiles for excess ice, we acknowledge that the version upgrade from CLM4.5 to CLM5 as the base model modifies the results of excess ice melt compared to the results from Lee et al. (2014). By default, CLM5 represents soil with a 25-layer profile, for which the top 20 hydrologically active layers cover 8.5 metrees of soil. There are additional 10 soil layers and it is 4.7 metrees deeper compared to the default hydrologically active soil layer profile in CLM4.5, not to mention the substantially more complex biogeophysical processes (Lawrence et al., 2019). Therefore, we developed the sub-grid representation of excess ice within the framework of the latest version of CLM. The duplicated landunits prolong computation time by roughly 10% compared to the original CLM5. We are, therefore, confident that our model development is highly efficient in addressing the sub-grid excess ice and subsequent permafrost thaw.

We examined the sensitivity of sub-grid excess ice initialization by conducting idealized experiments (see supplemental material). For overall the same amount of excess ice in one grid cell located in the same depth, a higher volumetric excess ice content along with a smaller area weight results in a later start of excess ice melt and a smaller melting rate. The different melting features from different sub-grid distribution of excess ice then leads to different hydrological impacts to the permafrost soil. The idealized experiments in this way verify the necessity of involving sub-grid configuration of excess ice to the CLM that is with a typical horizontal grid spacing of 1-2 degrees. More details are available in the supplemental material.

Commented [LC1]: We have added some stuff about the sensitivity test in the supplemental material.

2.2 Single-point simulations for the Lena river delta, Siberia

We conduct single-point simulations for the Lena River delta and compare the CLM5 model results to reference simulations with the CryoGrid3 model for the same location (Westermann et al., 2016). Abundant background information is available on the soil and ground ice dynamics from both observation and modeling, making the Lena river delta a suitable location to further evaluate our model

development. The Lena river delta can be broadly categorized into three different geomorphological units that have distinctively different subsurface cryostratigraphies of excess ice (Schneider et al., 2009; Ulrich et al., 2009). In the eastern and central part of the river delta, ground ice has been accumulated in the comparatively warm Holocene climate. The subsurface sediments (hereafter denoted as "Holocene ground ice terrain") are generally super-saturated with wedge ice that can extend up to 9 metrcers underground with the volumetric contents of total ground ice (pore ice + excess ice) ranging from 60-80% (Schwamborn et al., 2002; Langer et al., 2013). On the other hand, higher excess ice contents are found in Pleistocene sediments in the Lena River Delta (hereafter the "Yedoma Ice complex"), which are characterized by Yedoma type ground ice (Schirrmeister et al., 2013), which can reach depths of up to 20-25 metrcers deep and volumetric contents of total ground ice as high as 90% (Schwamborn et al., 2002; Schirrmeister et al., 2003 and 2011). Finally, the Northwestern part of the delta features sandy sediments and is characterized by low excess ice contents (hereafter denoted the "no excess ice terrain"; Rachold and Grigoriev, 1999; Schwamborn et al., 2002).

We determine the area weights of excess ice landunits in one single point based on the spatial pattern of three subregions (Fedorova et al., 2015). The cryostratigraphy and the volumetric contents of excess ice strictly follow those in Westermann et al. (2016). Notinge that the excess ice initialization scenario in Westermann et al. (2016) does not necessarily represent the realistic excess ice condition for the Lena river delta., tThe purpose of applying the same excess ice cryostratigraphy as in Westermman et al. (2016) is to evaluate our model development by addressing intercomparisons between model results. Meanwhile, we did not customize soil properties for different landunits as in Westermann et al. (2016), as our model development does not support varying soil properties for different sub-grid landunits. We also directly apply the snow accumulation physics in the CLM rather than customizing the snow density. By default, the current model does not form thermokarst lakes as the meltwater from excess ice melt becomes surface runoff and is removed from the grid cell. To apply the sub-grid representation, we initialize the case with three landunits (the triple-landunit case) that respectively represent the three terraces in the Lena river delta. We also initialize an "average ice single-landunit" case without the sub-grid representation of excess ice. The excess ice amount for each soil layer in the average ice single-landunit case is initially the same as that in the triple-landunit case. The volumetric content of excess ice is determined by spatial averaging those for three excess ice landunits in the triple-landunit case. Detailed information on the applied excess ice conditions for both cases is listed in Table 1.

We employed the single-point forcing data from in Westermann et al. (2016) for the Lena river delta from 1901 to 2100, which is based on the CRU-NCEP (http://dods.extra.cea.fr/data/p529viov/cruncep/) data set for the historical period (1901-2005) and the CCSM4 model output under the RCP4.5 scenario for the projected period (2006-2100), but downscaled with in-situ observations. We run 100-year spin-up simulations in order to stabilize the permafrost thermal regime after adding excess ice. Spin-up simulations are produced by running the model with cycled 1901-1920 climatological data. The purpose of spin-up simulations is to stabilize ground temperatures and volumes of excess ice bodies. The 100-year length for spin-up is sufficient, as the model is run in Satellite Phenology (SP) mode that does not involve slowly evolving biogeochemical processes such as soil carbon accumulation. Moreover, we

address idealized single-point simulations for additional permafrost locations with both continental and maritime climate that showcase the difference to Lee et al. (2014), the results of which are included in the Supplementary material.

2.3 Global simulations of excess ice melt

The information available for the spatial distribution of excess ice and associated cryostratigraphies on the global scale is generally not as detailed as in the Lena river delta due to the lack of observations. For our global simulations we employ the widely used "Circum-Arctic Map of Permafrost and Ground-Ice Conditions" (hereafter the CAPS data; Brown et al., 2002) as data source, while we translate the ground ice condition in the CAPS data to different excess ice stratigraphies as model input data. The CAPS permafrost map categorizes the global permafrost area into classes coded by three factors (i) permafrost extent (c = continuous, d = discontinuous, s = sporadic, and i = isolated), (ii) visible ground ice content (h = high, m = medium, and l = low), and (iii) terrain and overburden (f = lowlands, highlands, and intra- and intermontane depressions characterized by thick overburden cover, and r = mountains, highlands ridges, and plateaus characterized by thin overburden cover and exposed bedrock), resulting in more than 20 different varieties in permafrost characteristics (Figure 2). For the simulations, we only use the CAPS distinction between the three classes: high, medium and low ice contents. We qualitatively categorize excess ice types with typical cryostratigraphies for which observations are available, recognizing that this is a crude first-guess of the global distribution of ground ice which needs to be be improved in future studies.

The high ice CAPS classes (e.g. chf, chr, and dhf) in central and eastern Siberia, as well as in Alaska, partly coincide with Yedoma regions (Kanevskiy et al., 2011; Grosse et al., 2013). The cryostratigraphy of the high ice landunit is therefore broadly oriented at the excess ice contents and distribution in intact Yedoma, which is characterized by massive ice wedges leading to typical average volumetric content of total ground ice in the range from 60% to 90% (Schwamborn et al., 2002; Kanevskiy et al., 2011). We therefore set the volumetric content of excess ice in the high ice landunit to 70%, and we put excess ice in all the soil layers between 0.2 metrcers below the active layer and the bottom of hydrologically -active soil layer (8.5 metrcers). The onset depth of the excess ice just below the active layer is based on the assumption of active ice aggradation which occurs at or below the permafrost table, e.g. the formation of wedge or segregation ice. Initializing high ~~content~~ excess ice content throughout the whole soil layer imitates the cryostratigraphy of Yedoma type ice, while ~~a certain amount~~roughly 65% of the high ice landunit ~~locates~~ is located out of the observed Yedoma regions (Schuur et al., 2015). The effects, limitations, and potential improvements of this initialization scenario will be mentioned in the discussion section. For the low ice landunit, we assume both a significantly lower volumetric excess ice content and a smaller vertical extent of the excess ice body. The volumetric excess ice content is set to 25%, and we add excess ice at soil layers within 0.2 to 1.2 metrcers below the active layer, which in particular represents sediments with segregated ice (e.g. Cable et al., 2018), but also accounts for a wide range of different excess ice conditions found throughout the permafrost domain. For the mid ice landunit, we set the volumetric excess ice content to 45% and put excess ice within 0.2 to 2.2 metrcers below the

active layer, making the volumetric excess ice content and vertical extent of which in between those for the low and high ice landunits. The cryostratigraphies determine that excess ice melt in the low ice landunit can result in a maximum of 0.36 metrcers of surface subsidence, while excess ice melt in the medium ice landunit can result in a maximum of 1.78 m of surface subsidence. For the high ice landunit, the surface subsidence can be more than 10 metrcers if all excess ice melts, which is expected to vary in space because of the different active layer thickness. For all three landunits, the active layer thickness is determined by the soil temperature profile by the end of the spinup in a no ice case, which is the simulation by the original CLM5 model without excess ice incorporated. Non-permafrost regions in the CAPS data are assigned the no ice landunit for 100% of their area. We emphasize that the prescribed cryostratigraphies are a first-order approximation that can by no means represent the wide variety of true ground ice conditions found in the permafrost domain. Nevertheless, this makes it possible to gauge the effect of excess ice melt on future projections of the permafrost thermal regime, when compared to "traditional" reference simulations without excess ice.

We design a tiling scheme prescribing the assignment of landunits for each CAPS class based on previous observations and empirical estimates (Table 2). All CAPS classes in this study are categorized into three levels of volumetric ice content (5%, 15%, and 25%) that are converted from the ranges (<10%, 10-20%, and >20%) in the original CAPS data. The goal of our tiling scheme is to determine a combination of area weights of three excess ice landunits for each CAPS class, making the spatially averaged volumetric content of excess ice the same as that for the CAPS class. We assume that all CAPS classes have the same area fraction (20%) of the low ice landunit, and the CAPS classes with a higher ice content are due to the existence of the landunits with a higher content excess ice. We make this assumption based on previous studies that the segregated ice is widely distributed in permafrost. Observational studies have found segregated ice bodies in various continuous permafrost regions across the circum-arctic including West Central Alaska (Kanevskiy et al., 2014), Nunavik, Canada (Calmels and Allard, 2008), and Svalbard (Cable et al., 2018). In discontinuous permafrost regions, segregated ice bodies also commonly exist underneath Palsas and Lithasas, including Fennoscandia (Seppälä, 2011), Altai and Sayan, Russia (Iwanhana et al., 2012), Himalayas (Wünnemann et al., 2008), and Mongolia (Sharkhuu et al., 1999). The volumetric content of visible segregated ice bodies mentioned above ranges widely from 10-50% (Gilbert et al., 2016).

Given the tiling scheme prescribed above, all CAPS classes are assigned a 20% area of low ice landunit. Correspondingly, the CAPS classes with 15% volumetric ice content are assigned another 14% area weight for mid ice landunit on top of the CAPS classes with 5% volumetric ice content, while the CAPS classes with 25% volumetric ice are assigned another 22% area for high ice landunit on top of the CAPS classes with 15% volumetric ice content. The classes of "chf" and "chr" are the exceptions as their corresponding regions are typically with the landscape of Yedoma and/or or ice wedge polygonal tundra or both (Kanevskiy et al., 2011; Gross et al., 2013). We therefore assign only the low and high ice landunits for these two CAPS classes. Summing up the landunit fractions for all the CAPS grid cells within each CLM grid cell obtains the area weights on the grid level that are stored in the surface data file. Figure 3 shows a schematic plot for the initialization scenario and the area covered by different

excess ice landunits as the result of sub-grid excess ice initialization in the global simulation case. Note that excess ice for some regions (e.g. Southern Norway and the Alps) can completely melt out during the spinup period since the CLM initial condition prescribes overly warm (non-permafrost) soil temperature for these regions.

In this study, we define the grid cells or ~~/~~landunits with permafrost as the ones having at least one hydrologically active soil layer that has been frozen in the last consecutive 24 months. In this case, we define ~~permafrost degradation~~fully degraded permafrost when all landunits in one grid ~~point are with~~cell have an active layer thickness of more than 6.5 metrc~~er~~s, , recognizing that in reality permafrost at many localities may continue to exist at greater depths.. We also prepare a "grid-average ice case" by applying the same total amount of excess ice as in the sub-grid ice case in each soil layer, but using only one landunit instead of three that account for the sub-grid variability of excess ice. The volumetric content of excess ice in the single landunit is calculated as the spatial average of those in the three landunits in the triple-landunit case. This grid-average ice case provides a reference to evaluate the effects of the sub-grid excess ice representation on the global scale. Finally, we simulate a reference case without excess ice, denoted the "no ice case" in the following. Details on the three cases for the global simulations are listed in Table 3. All global cases are forced by the 3rd version of Global Soil Wetness Project forcing data (GSWP3; Kim et al., 2012), running in the Satellite Phenology (SP) mode. The International Land Atmosphere Model Benchmarking (ILAMB; Collier et al., 2018) project has indicated the superior performance of GSWP3 data forcing the CLM5 in the SP-only mode (http://webext.cgd.ucar.edu/I20TR/_build_090817_CLM50SPONLY_CRUNCEP_GSWP3_WFDEI/index.html). We conducted a 100-year spin-up using the 1901-1920 climatology before conducting historical period simulations covering 1901-2005. The anomaly forcing under the RCP8.5 scenario on top of the 1982-2005 climatology forces simulations in the projected period.

3. Result

3.1 Excess ice melt simulations for Lena River delta cryostratigraphies

By the end of the spinup in the triple-landunit case, the active layer thickness is 0.85 m, 0.55 m, and 0.45 m for the ice-poor terrain, the Holocene ice wedge terrain, and the Yedoma ice complex, respectively. On the other hand, the active layer thickness for the average ice single-landunit case is 0.85 m, which is the same as in the no excess ice terrain in the triple-landunit case. For the average ice single-landunit case, a small amount of excess ice (24kg ~~/m^2~~m^{-2}) melts during the spinup period, resulting in 2.6 cm surface subsidence throughout the grid.

For the Yedoma ice complex, very little excess ice melt in the 1950s, and it stabilizes afterwards until the late 2000s when substantial ice melt and surface subsidence starts to ~~happen~~occur. For the Holocene ground ice terrain, there is no excess ice melt before the late 2010s. By the year 2100, the Yedoma ice complex has exhibited nearly 4 metrc~~er~~s of surface subsidence, while the Holocene ground ice terrain has about 0.6 metrc~~er~~s of surface subsidence (Figure 4). For the average ice single-landunit case, the noticeable excess ice melt and surface subsidence starts in the late 2010s, which creates about

0.5 metrcers of surface subsidence by 2100. The magnitude of surface subsidence in the average ice single-landunit case is lower than both the Holocene ground ice terrain and the Yedoma ice complex in the triple-landunit case.

On the grid scale, the total excess ice melt is higher in the average ice single-landunit case than in the triple-landunit case (Figure 5). By the year 2100, the average ice single-landunit case has about 30 kg ~~/m^2~~ m^{-2} more excess ice melt than the triple-landunit case. The difference in excess ice on the grid level results from the different volumetric content of excess ice caused by the spatial averaging. In this way, the sub-grid representation of excess ice can potentially also provide more detailed and realistic representation of model variables on the grid level. This is particularly important for the CLM5, which serves as the land component in Earth System Models, which requires the coupling between interacting components on the grid level.

Compared to Westermann et al. (2016), the CLM5 with sub-grid excess ice simulates slightly less (~ 20% less) surface subsidence by 2100 for both the central delta and ice complex. We consider this a good agreement as we do not expect a closer fit of the model results due to substantial differences in the model physics (for example, the Cryogrid3 simulations in Westermann et al. (2106) lack a representation of the subsurface water cycle). What is in common between these two studies is the earlier start of excess ice melt and more surface subsidence in the ice complex than in the central delta. The CLM5 with sub-grid excess ice also exhibits the varying active layer thickness with different excess ice conditions as Cryogrid3 does. These results suggest that the new model development enables small-scale variability in excess ice melt and subsequent impacts in agreement with previously published modeling efforts.

3.2 Global projection of permafrost thaw and excess ice melt

Single-point simulations have shown that the varying excess ice cryostratigraphies for different landunits result in sub-grid variabilities of excess ice melt and surface subsidence under the warming climate. The same features remain in the sub-grid ice case within the global simulations that excess ice in the low ice landunit can completely melt out throughout the circum-Arctic permafrost region by the end of the 21st century (Figure 6). The modeled magnitude of surface subsidence is similar to the ~10 cm surface subsidence observed in Barrow and West Dock in the early 21st century (Shiklomanov et al., 2013; Streleskiy et al., 2017). The magnitude of surface subsidence is also comparable to the 1-4 cm decade^{-1} surface subsidence rate on average over the North Slope of Alaska observed by satellite measurements since the 1990s (Liu et al., 2010). In comparison, the absence of surface subsidence for Arctic Alaska modeled by Lee et al. (2014) is due to an overly deep (1 m deep) excess ice initialization depth. By the year 2100, most ice in the medium ice landunit melts away in the sub-arctic region, while there is less ice melt in the colder regions such as the North Slope of Alaska and the central Siberia. The high ice landunit has the greatest surface subsidence among the three because of its high excess ice content, leading to 2-5 metrcers of surface subsidence by the year 2100.

The existence of excess ice modulates the thermal regime of permafrost soil and is a major control on permafrost degradation trajectories in a warming climate. Permafrost with excess ice consistently exhibits delayed permafrost degradation compared to the no ice case (Figure 7). For the no ice case

modeled by the original CLM5, more than half of the permafrost area undergoes degradation by the end of the 21st century. By 2100, the only areas where permafrost remains are the North Slope of Alaska, Northern Canada, and the majority of the land area in Northern Siberia. The areas with remaining permafrost in the year 2100 under the RCP8.5 scenarios are substantially larger compared to the CLM4 simulations, in which nearly all permafrost in Eurasia becomes degraded (Lawrence et al., 2012). For the grid-average ice case, the presence of excess ice stabilizes the permafrost thermal regime and thus sustains a larger permafrost area on a global scale in the simulation. For example, permafrost areas in some subarctic regions in the eastern and western Siberia, as well as part of the Arctic coastal regions in Yukon Territory, Canada, remain in the grid-average ice case by 2100. Compared to the grid-average ice case, even more permafrost areas are sustained in the sub-grid ice case, most of which are located in southern Siberia. In the subarctic regions in Alaska and Northwest Canada as well as part of the central Siberia, permafrost degradation is delayed from the 2040s in the grid ice case to the 2080s in the sub-grid ice case. We emphasize that permafrost is only sustained according to the accepted temperature-based definition (ground material at temperature below zero for two consecutive years), but excess ice continuously melts in this process, which energetically is a different mode of permafrost degradation, similar to a negative mass balance of glaciers and ice sheets.

In the sub-grid ice case, the landunits with high excess ice contents lead to more grid ~~points~~ cells for which permafrost conditions remain in the year 2100 compared to the grid-average ice case. On the other hand, permafrost with excess ice only covers a fraction of a grid ~~point~~cell. Among the permafrost degradation trajectories in the three global simulation cases (Figure 8), the sub-grid ice case can provide a more detailed picture on the timing of permafrost degradation. Grid cells become 'partially degraded permafrost' if landunits with excess ice still contain permafrost, which phenomenologically is a more realistic representation that also makes it possible to represent the permafrost distribution in the discontinuous and sporadic permafrost zones. On the other hand, only "fully degraded permafrost" and "remaining permafrost" can be distinguished for the no ice and grid-average ice case. Under the warming climate in the 21st century, the existence of excess ice, especially the high content of excess ice, has a stabilizing effect on soil temperature that delay the disappearance of permafrost on the sub-grid level. Therefore, by the year 2100, there are regions with partially degraded permafrost in between intact and degraded permafrost (Figure 8). For example, in western Siberia, the Pacific coastal area of eastern Siberia, Northwestern Canada, and along the Brooks Range in Alaska, taliks form for landunits with low excess ice contents which leads to partially degraded permafrost regions. Therefore, permafrost degradation exhibits a gradual transition from continuous to discontinuous permafrost, and to non-permafrost regions. Some of these regions also encounter substantial surface subsidence in the high ice landunit (> 5 m) (Figure 6).

We further compare the total permafrost area (defined as landunits with active layer thickness < 6.5 metrc~~er~~s) in the three cases throughout time. The differences in permafrost area increase from the grid-average ice case and sub-grid ice case to the no ice case at a rate of 1000 km^2 per year until 2050 (Figure 9). After 2050, the area difference of permafrost in the grid-average ice case and no ice cases rapidly increases, which reaches nearly one million km^2 by 2100. In the sub-grid ice case, the rate of increase

remains relatively unchanged after 2050, resulting in an about 0.2 million km^2 larger permafrost area than that in the no ice case.

4. Discussion

The aim of the sub-grid excess ice representation in the CLM5 is to facilitate long-term global projection of excess ice melt and surface subsidence in the permafrost regions. Results from idealized sensitivity experiments (see supplemental material) implies that overly low volumetric content of excess ice, such as the grid-average ice case in this study and that in Lee et al. (2014), result in overly early start of excess ice melt and an overly high melting rate. It is because the higher content of excess ice covering a smaller area takes longer to absorb enough latent heat of fusion from the atmosphere before it can start melting. A good model performance in this way relies not only on the updated sub-grid representation of excess ice in the global land model, but also on retrieving accurate initial conditions of excess ice distribution. However, , ~~but~~ the corresponding observational data for both~~-~~ background excess ice conditions and model evaluation is sparse, considering especially that drastic excess ice melt as modeled until 2100 is only observed in few locations today (e.g. Günther et al., 2015). In the following, we discuss the challenges and limitations of the sub-grid excess ice framework, and how this sub-grid representation can potentially help the development of other CLM components.

Both single-point and global test simulations in this study have shown that excess ice melts under a warming climate is sensitive to its initialization depth. The active-layer-dependent excess ice initialization in this study in the global simulation (sub-grid excess ice case) yields excess ice melt and surface subsidence rates in the early 2000s that are comparable to observations. The lower depths of the assumed excess ice body control the termination of excess ice melt which at the same time determines the onset of talik formation in many permafrost areas. Due to the scarcity of observational data, it is unclear to what extent the cryostratigraphies assumed in our tiling scheme can reproduce the true vertical extent of excess ice bodies at least in a statistical sense. Even so, we manage to make the prescribed excess ice condition as close to the previous results as possible. Firstly, our tiling scheme on the large scale strictly follows the CAPS data (Brown et al., 2002) in terms of the volumetric excess ice content. Furthermore, statistics by Zhang et al. (2000) suggest the ranges of the vertical extent of ice-rich permafrost of 0-2 metrc~~e~~rs and 2-4 metrc~~e~~rs respectively for the CAPS classes with low (5%) and medium (15%) ice content. Comparatively, the vertical extents permafrost with excess ice prescribed by our tiling scheme are respectively 1.36 metrc~~e~~rs and 3.78 metrc~~e~~rs for the same CAPS classes, both of which lie within the ranges in Zhang et al. (2000). The vertical extent of ice-rich permafrost for the high ice landunit is much higher than that (4-6 metrc~~e~~rs) in Zhang et al. (2000), but the unmelted part of the ice bodies does not strongly affect the overall rate of excess ice melt, although the remaining ice can slightly change soil temperature and moisture of the surrounding permafrost. We therefore imply that our high ice landunit initialization would not induce a strong bias in excess ice melt projection in the 21st century.

Commented [LC2]: We have added discussions on the model's sensitivity.

Due to the lack of excess ice datasets and observational evidence, our projections of excess ice melt and surface subsidence likely have biases that arise from the need to make empirical estimates and simplifications for the excess ice initialization scenarios in the global simulation cases. ~~involve empirical estimates and simplifications, which could bring biases to the projection of excess ice melt and surface subsidence.~~ For example, as the CAPS data is mostly based on visible ice bodies (i.e., not pore ice) (Heginbottom et al., 1995), we used the reported volumetric ground ice content in the CAPS data to approximate the volumetric content of excess ice during model initialization.~~We apply the volumetric content of ground ice in the CAPS data approximately as the volumetric content of excess ice during initialization as the CAPS data is mostly based on visible ice bodies (Heginbottom et al., 1995), not to mention~~further the determination of volumetric contents of excess ice for three landunits also results from sparse observations and empirical estimates. The prescribed excess ice cryostratigraphies ignore ice morphology and the variation of volumetric content of excess ice with soil depth, regarding excess ice as homogeneous within each assigned sub-grid ice content type (low, mid, or high) (Figure 3, upper panel).~~"ice cubes"~~. For the high ice landunit, we simplify the cryostratigraphy initialization to Yedoma type ice, which prescribes overly thick excess ice bodies out of the Yedoma regions (Schurr et al., 2015). A deficiency in the current version of source code prevents us from initializing ~~disables us to initialize~~ non-Yedoma wedged ice for the high ice landunit where it occurs outside ~~out~~ of the Yedoma region. Future versions of our model development will have more freedom in the stratigraphic configuration of excess ice~~excess ice stratigraphy configuration~~, which will make~~makes~~ it possible to prescribe different cryostratigraphies of the same landunit (e.g. the high ice landunit) for different locations. ~~Furthermore, excess ice stratigraphy.~~ Because of the above shortcomings in the excess ice initialization, we do not expect the modeled excess ice melt in this study to be an adequate representation of reality~~yet,~~. However, direct ingestion of new or improved ~~while~~improved observational data sets of excess ice contents and cyostratigraphies would likely ~~could be directly ingested to~~ yield ~~improved~~ more accurate results. However, a spatially distributed global dataset with quantitative information on excess ice stratigraphies does not exist at present. We emphasize that for a better projection of excess ice melt, more observational data of excess ice distribution and surface subsidence is required to further evaluate and validate the new model implementation of excess ice. On the regional scale, Jorgenson et al. (2008) presented a permafrost map of total ground ice volume for the uppermost 5 metrer~~s~~ of permafrost based on both observations and estimates for Alaska. In addition, O'Neill et al. (2019) compiled permafrost maps for Northern Canada by paleographic modeling, mapping the abundances of three types of excess ice respectively. Further improvements of model results depend on additional observationally constrained datasets of excess ice conditions on the global scale.

The area weights of the excess ice landunits (Table 2) in the global simulation are obtained from the higher-resolution CAPS points located within a CLM grid cell. However, complex landscape development, such as thermokarst ponds, requires knowledge of the metrer~~-~~scale distribution, for example the extent and geometry of individual ice wedges (Langer et al., 2016; Nitzbon et al., 2019), which cannot be represented with the still coarse-scale excess ice classes from the CAPS map. One possible solution to represent this could be to include another layer of sub-grid tiles below the CLM landunit level, where the individual tiles can interact laterally. This would allow for the representation of

small-scale permafrost features within a large-scale landunit with a given excess ice content. An example of how this could work is given by Aas et al. (2019) who simulated both polygonal tundra and peat plateaus with a two-tile interactive setup. This is also similar to the recent representation of hillslope hydrology by Swenson et al. (2019), where sub-grid tiles (on the column level in CLM) were used to represent different elements in a representative hillslope. In the future development of CLM, this could be part of a more generic tiling system where lateral heat and mass fluxes could be switched on and off to represent a wide range of land surface processes that are currently ignored or parameterized in LSMs. Fisher and Koven (2020) have discussed the challenges and opportunities in such an adaptive and generic tiling system. We would also advocate for enhancing current tiling schemes in such a direction, which could substantially improve the realism in the representation of permafrost landscapes in LSMs. However, the success of such a tiling approach will rely heavily on the availability of adequate observational data, further highlighting the need for observational efforts and close collaboration between field scientists and modelers.

The more detailed simulation of permafrost degradation trajectory with a sub-grid representation of excess ice also builds more potential on better modeling the permafrost-carbon feedback with biogeochemistry activated (CLM5BGC). Excess ice stabilizes the permafrost thermal regime, therefore alter the rate of carbon releasing from the permafrost (Shuur et al., 2008). Improved projections of permafrost warming could also enhance modeling of vegetation type changes (e.g. shrub expansion) that determines the nitrogen uptake to the atmosphere (Loranty and Goetz, 2012). On the other hand, the possibility to simulate surface subsidence and excess ice meltwater formation also opens the possibility of a more accurate representation of wetland formation. The increase in the area of wetland and soil moisture have an impact of the balance of CH_4 and CO_2 releasing from the permafrost as more organic matter could decompose in an anaerobic pathway (Lawrence et al., 2015; Treat et al., 2015). Compared to the parameterized inundated area simulation in the CLM5 (Ekici et al., 2019), a process-based wetland physics scheme together with the sub-grid representation of excess ice in this study would substantially contribute to the biogeochemical modeling over the circum-arctic area.

5. Conclusion

This study develops a sub-grid representation of excess ice in the CLM5 and examines the impacts of the existence and melting of excess ice in the sub-grid scale in a warming climate. Extra landunits duplicated from the natural vegetated landunit in the CLM sub-grid hierarchy make it possible to prescribe up to three different excess ice conditions in each grid ~~point~~ cell with permafrost.

A test over the Lena river delta showcases that the sub-grid representation of excess ice can retrieve the sub-grid variability of annual thaw-freeze state and the excess ice melt and ~~/~~surface subsidence through time. On the other hand, initializing excess ice homogeneously throughout the grid cell produces a smaller stabilization effect of excess ice to the permafrost thermal regime and the local surface subsidence under a warming climate. With a tiling scheme ingesting a global data set of excess ice condition into the CLM surface data, our model development shows the capability of portraying more details on simulating permafrost degradation trajectories. As excess ice thermally stabilizes the

permafrost on the sub-grid scale, permafrost degrades with a trajectory from continuous permafrost to discontinuous permafrost, and finally to a permafrost-free area. The modeled global pattern of permafrost therefore exhibits regions of discontinuous permafrost as the transition zone between the continuous permafrost and degraded permafrost.

This study, for the first time, used an ESM to project excess ice melt and ~~/~~surface subsidence and permafrost degradation with sub-grid variability. The approach of duplicating tiles at the landunit level instead of the column level allows more freedom for further developments in this direction. Furthermore, the new CLM tiling hierarchy has much more potential than representing more accurate excess ice physics as examined in this study. The accuracies of predicted excess ice melt and surface subsidence trends are limited at present by the available global-scale dataset and studies on excess ground ice conditions, thus further advancement of the excess ice modeling will rely ~~Further advancing the excess ice modeling relies~~ on ~~additional~~ new or improved observational studies or ~~/~~datasets of the excess ground ice conditions ~~on a~~at the global scale. The model development in our study, therefore, lays the foundation for further advances focusing on excess ice modeling and other processes in the CLM framework that could benefit from an improved sub-grid representation.

~~Code/Data Availability~~Source code and data availability

The original Community Land Model is available at https://github.com/ESCOMP/ctsm. The source code of model development in this study is available from the corresponding author upon request.

Author contributions

L.C conducted model development work and wrote the initial draft with additional contributions from all authors. H.L, S.W, and K.S.A provided ideas and help during the process of model development. H.L provided the code of excess ice physics in the earlier version of CLM. L.C prepared all figures.

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Reference

Aas, K. S., Martin, L., Nitzbon, J., Langer, M., Boike, J., Lee, H., Berntsen, T. K., and Westermann, S.: Thaw processes in ice-rich permafrost landscapes represented with laterally coupled tiles in a land surface model, The Cryosphere, 13, 591-609, 10.5194/tc-13-591-2019, 2019.

Brown, J., Ferrians Jr, O., Heginbottom, J., and Melnikov, E.: Circum-Arctic map of permafrost and ground-ice conditions, US Geological Survey Reston, VA, 1997.

Burke, E. J., Dankers, R., Jones, C. D., and Wiltshire, A. J.: A retrospective analysis of pan Arctic permafrost using the JULES land surface model, Climate Dynamics, 41, 1025-1038, 10.1007/s00382-012-1648-x, 2013.

Cable, S., Elberling, B., and Kroon, A.: Holocene permafrost history and cryostratigraphy in the High-Arctic Adventdalen Valley, central Svalbard, Boreas, 47, 423-442, 10.1111/bor.12286, 2018.

Calmels, F., and Allard, M.: Segregated ice structures in various heaved permafrost landforms through CT Scan, Earth Surface Processes and Landforms, 33, 209-225, 10.1002/esp.1538, 2008.

Collier, N., Hoffman, F. M., Lawrence, D. M., Keppel-Aleks, G., Koven, C. D., Riley, W. J., Mu, M., and Randerson, J. T.: The International Land Model Benchmarking (ILAMB) system: design, theory, and implementation, Journal of Advances in Modeling Earth Systems, 10, 2731-2754, 2018.

Ekici, A., Lee, H., Lawrence, D. M., Swenson, S. C., and Prigent, C.: Ground subsidence effects on simulating dynamic high-latitude surface inundation under permafrost thaw using CLM5, Geosci. Model Dev., 12, 5291-5300, 10.5194/gmd-12-5291-2019, 2019.

Fedorova, I., Chetverova, A., Bolshiyanov, D., Makarov, A., Boike, J., Heim, B., Morgenstern, A., Overduin, P. P., Wegner, C., Kashina, V., Eulenburg, A., Dobrotina, E., and Sidorina, I.: Lena Delta hydrology and geochemistry: long-term hydrological data and recent field observations, Biogeosciences, 12, 345-363, 10.5194/bg-12-345-2015, 2015.

Fisher, R. A., and Koven, C. D.: Perspectives on the future of Land Surface Models and the challenges of representing complex terrestrial systems, Journal of Advances in Modeling Earth Systems, n/a, 10.1029/2018MS001453, 2020.

Fritz, M., Wetterich, S., Meyer, H., Schirrmeister, L., Lantuit, H., and Pollard, W. H.: Origin and characteristics of massive ground ice on Herschel Island (western Canadian Arctic) as revealed by stable water isotope and Hydrochemical signatures, Permafrost and Periglacial Processes, 22, 26-38, 10.1002/ppp.714, 2011.

Gilbert, G. L., Kanevskiy, M., and Murton, J. B.: Recent Advances (2008–2015) in the Study of Ground Ice and Cryostratigraphy, Permafrost and Periglacial Processes, 27, 377-389, 10.1002/ppp.1912, 2016.

Grosse, G., Romanovsky, V., Jorgenson, T., Anthony, K. W., Brown, J., and Overduin, P. P.: Vulnerability and feedbacks of permafrost to climate change, Eos, Transactions American Geophysical Union, 92, 73-74, 2011.

Grosse, G., Robinson, J. E., Bryant, R., Taylor, M. D., Harper, W., DeMasi, A., Kyker-Snowman, E., Veremeeva, A., Schirrmeister, L., and Harden, J.: Distribution of late Pleistocene ice-rich syngenetic permafrost of the Yedoma Suite in east and central Siberia, Russia, US Geological Survey Open File Report, 2013, 1-37, 2013.

572 Günther, F., Overduin, P. P., Yakshina, I. A., Opel, T., Baranskaya, A. V., and Grigoriev, M. N.:
573 Observing Muostakh disappear: permafrost thaw subsidence and erosion of a ground-ice-rich
574 island in response to arctic summer warming and sea ice reduction, The Cryosphere, 9, 151-178,
575 10.5194/tc-9-151-2015, 2015.

576 Heginbottom, J.A., Dubreuil, M.A. and Harker, P.A.: Canada, Permafrost. National Atlas of Canada.
577 Natural Resources Canada, 5th Edition, MCR, 4177, 1995.

578 Hugelius, G., Strauss, J., Zubrzycki, S., Harden, J. W., Schuur, E. A. G., Ping, C. L., Schirrmeister, L.,
579 Grosse, G., Michaelson, G. J., Koven, C. D., O'Donnell, J. A., Elberling, B., Mishra, U., Camill,
580 P., Yu, Z., Palmtag, J., and Kuhry, P.: Estimated stocks of circumpolar permafrost carbon with
581 quantified uncertainty ranges and identified data gaps, Biogeosciences, 11, 6573-6593,
582 10.5194/bg-11-6573-2014, 2014.

583 Kanevskiy, M., Shur, Y., Fortier, D., Jorgenson, M. T., and Stephani, E.: Cryostratigraphy of late
584 Pleistocene syngenetic permafrost (yedoma) in northern Alaska, Itkillik River exposure,
585 Quaternary Research, 75, 584-596, 10.1016/j.yqres.2010.12.003, 2011.

586 Iwahana, G., Fukui, K., Mikhailov, N., Ostanin, O., and Fujii, Y.: Internal Structure of a Lithalsa in the
587 Akkol Valley, Russian Altai Mountains, 23, 107-118, 10.1002/pp

588 Jorgenson, M., Yoshikawa, K., Kanevskiy, M., Shur, Y., Romanovsky, V., Marchenko, S., Grosse, G.,
589 Brown, J., and Jones, B.: Permafrost characteristics of Alaska, Proceedings of the Ninth
590 International Conference on Permafrost, 2008, 121-122.p.1734, 2012.

591 Kanevskiy, M., Jorgenson, T., Shur, Y., O'Donnell, J. A., Harden, J. W., Zhuang, Q., and Fortier, D.:
592 Cryostratigraphy and Permafrost Evolution in the Lacustrine Lowlands of West-Central Alaska,
593 Permafrost and Periglacial Processes, 25, 14-34, 10.1002/ppp.1800, 2014.

594 Kim, H., Yoshimura, K., Chang, E., Famiglietti, J., and Oki, T.: Century long observation constrained
595 global dynamic downscaling and hydrologic implication, AGU Fall Meeting Abstracts, 2012.

596 Kokelj, S. V., Lacelle, D., Lantz, T. C., Tunnicliffe, J., Malone, L., Clark, I. D., and Chin, K. S.: Thawing
597 of massive ground ice in mega slumps drives increases in stream sediment and solute flux across
598 a range of watershed scales, Journal of Geophysical Research: Earth Surface, 118, 681-692,
599 10.1002/jgrf.20063, 2013.

600 Koven, C. D., Ringeval, B., Friedlingstein, P., Ciais, P., Cadule, P., Khvorostyanov, D., Krinner, G., and
601 Tarnocai, C.: Permafrost carbon-climate feedbacks accelerate global warming, Proceedings of
602 the National Academy of Sciences, 108, 14769-14774, 2011.

603 Langer, M., Westermann, S., Boike, J., Kirillin, G., Grosse, G., Peng, S., and Krinner, G.: Rapid
604 degradation of permafrost underneath waterbodies in tundra landscapes—toward a
605 representation of thermokarst in land surface models, Journal of Geophysical Research: Earth
606 Surface, 121, 2446-2470, 2016.

607 Langer, M., Westermann, S., Heikenfeld, M., Dorn, W., and Boike, J.: Satellite-based modeling of
608 permafrost temperatures in a tundra lowland landscape, Remote Sensing of Environment, 135,
609 12-24, https://doi.org/10.1016/j.rse.2013.03.011, 2013.

610 Lawrence, D. M., Slater, A. G., Romanovsky, V. E., and Nicolsky, D. J.: Sensitivity of a model projection
611 of near-surface permafrost degradation to soil column depth and representation of soil organic
612 matter, Journal of Geophysical Research: Earth Surface, 113, 10.1029/2007JF000883, 2008.

613 Lawrence, D. M., Oleson, K. W., Flanner, M. G., Thornton, P. E., Swenson, S. C., Lawrence, P. J., Zeng,
614 X., Yang, Z. L., Levis, S., and Sakaguchi, K.: Parameterization improvements and functional
615 and structural advances in version 4 of the Community Land Model, Journal of Advances in
616 Modeling Earth Systems, 3, 2011.

617 Lawrence, D. M., Slater, A. G., and Swenson, S. C.: Simulation of present-day and future permafrost and
618 seasonally frozen ground conditions in CCSM4, Journal of Climate, 25, 2207-2225, 2012.

619 Lawrence, D. M., Koven, C. D., Swenson, S. C., Riley, W. J., and Slater, A. G.: Permafrost thaw and
620 resulting soil moisture changes regulate projected high-latitude CO2 and CH4 emissions,
621 Environmental Research Letters, 10, 094011, 10.1088/1748-9326/10/9/094011, 2015.

622 Lawrence, D. M., Fisher, R. A., Koven, C. D., Oleson, K. W., Swenson, S. C., Bonan, G., Collier, N.,
623 Ghimire, B., van Kampenhout, L., Kennedy, D., Kluzek, E., Lawrence, P. J., Li, F., Li, H.,
624 Lombardozzi, D., Riley, W. J., Sacks, W. J., Shi, M., Vertenstein, M., Wieder, W. R., Xu, C.,
625 Ali, A. A., Badger, A. M., Bisht, G., van den Broeke, M., Brunke, M. A., Burns, S. P., Buzan,
626 J., Clark, M., Craig, A., Dahlin, K., Drewniak, B., Fisher, J. B., Flanner, M., Fox, A. M., Gentine,
627 P., Hoffman, F., Keppel-Aleks, G., Knox, R., Kumar, S., Lenaerts, J., Leung, L. R., Lipscomb,
628 W. H., Lu, Y., Pandey, A., Pelletier, J. D., Perket, J., Randerson, J. T., Ricciuto, D. M.,
629 Sanderson, B. M., Slater, A., Subin, Z. M., Tang, J., Thomas, R. Q., Val Martin, M., and Zeng,
630 X.: The Community Land Model Version 5: Description of New Features, Benchmarking, and
631 Impact of Forcing Uncertainty, 11, 4245-4287, 10.1029/2018ms001583, 2019.

632 Lee, H., Swenson, S. C., Slater, A. G., and Lawrence, D. M.: Effects of excess ground ice on projections
633 of permafrost in a warming climate, Environmental Research Letters, 9, 124006, 2014.

634 Liu, L., Zhang, T., and Wahr, J.: InSAR measurements of surface deformation over permafrost on the
635 North Slope of Alaska, Journal of Geophysical Research: Earth Surface, 115,
636 10.1029/2009jf001547, 2010.

637 Loranty, M. M., and Goetz, S. J.: Shrub expansion and climate feedbacks in Arctic tundra, Environmental
638 Research Letters, 7, 011005, 10.1088/1748-9326/7/1/011005, 2012.

639 Nitzbon, J., Langer, M., Westermann, S., Martin, L., Aas, K. S., and Boike, J.: Pathways of ice-wedge
640 degradation in polygonal tundra under different hydrological conditions, The Cryosphere, 13,
641 1089-1123, 10.5194/tc-13-1089-2019, 2019.

642 Nitzbon, J., Westermann, S., Langer, M., Martin, L. C. P., Strauss, J., Laboor, S., and Boike, J.: Fast
643 response of cold ice-rich permafrost in northeast Siberia to a warming climate, Nature
644 Communications, 11, 2201, 10.1038/s41467-020-15725-8, 2020.

645 O'Neill, H. B., Wolfe, S. A., and Duchesne, C.: New ground ice maps for Canada using a paleogeographic
646 modelling approach, The Cryosphere, 13, 753-773, 10.5194/tc-13-753-2019, 2019.

647 Pascale, G. P. D., Pollard, W. H., and Williams, K. K. J. J. o. G. R. A.: Geophysical mapping of ground
648 ice using a combination of capacitive coupled resistivity and ground-penetrating radar,
649 Northwest Territories, Canada, 113, 2008.

650 Rachold, V., and Grigoriev, M.: Russian-German Cooperation SYSTEM LAPTEV SEA 2000: The Lena
651 Delta 1998 Expedition, Berichte zur Polarforschung (Reports on Polar Research), 315, 1999.

652 Schaefer, K., Lantuit, H., Romanovsky, V. E., Schuur, E. A. G., and Witt, R.: The impact of the
653 permafrost carbon feedback on global climate, Environmental Research Letters, 9, 085003,
654 10.1088/1748-9326/9/8/085003, 2014.

655 Schirrmeister, L., Grosse, G., Schwamborn, G., Andreev, A. A., Meyer, H., Kunitsky, V. V., Kuznetsova,
656 T. V., Dorozhkina, M. V., Pavlova, E. Y., Bobrov, A. A., and Oezen, D.: Late Quaternary
657 History of the Accumulation Plain North of the Chekanovsky Ridge (Lena Delta, Russia): A
658 Multidisciplinary Approach, Polar Geography, 27, 277-319, 10.1080/789610225, 2003.

659 Schirrmeister, L., Grosse, G., Schnelle, M., Fuchs, M., Krbetschek, M., Ulrich, M., Kunitsky, V.,
660 Grigoriev, M., Andreev, A., Kienast, F., Meyer, H., Babiy, O., Klimova, I., Bobrov, A.,
661 Wetterich, S., and Schwamborn, G.: Late Quaternary paleoenvironmental records from the
662 western Lena Delta, Arctic Siberia, Palaeogeography, Palaeoclimatology, Palaeoecology, 299,
663 175-196, https://doi.org/10.1016/j.palaeo.2010.10.045, 2011.

664 Schirrmeister, L., Froese, D., Tumskoy, V., Grosse, G., and Wetterich, S.: Yedoma: Late Pleistocene ice-
665 rich syngenetic permafrost of Beringia, in: Encyclopedia of Quaternary Science. 2nd edition,
666 Elsevier, 542-552, 2013.

667 Schneider, J., Grosse, G., and Wagner, D.: Land cover classification of tundra environments in the Arctic
668 Lena Delta based on Landsat 7 ETM+ data and its application for upscaling of methane
669 emissions, Remote Sensing of Environment, 113, 380-391,
670 https://doi.org/10.1016/j.rse.2008.10.013, 2009.

671 Schuur, E. A., Bockheim, J., Canadell, J. G., Euskirchen, E., Field, C. B., Goryachkin, S. V., Hagemann,
672 S., Kuhry, P., Lafleur, P. M., and Lee, H.: Vulnerability of permafrost carbon to climate change:
673 Implications for the global carbon cycle, BioScience, 58, 701-714, 2008.

674 Schuur, E. A. G., McGuire, A. D., Schädel, C., Grosse, G., Harden, J. W., Hayes, D. J., Hugelius, G.,
675 Koven, C. D., Kuhry, P., Lawrence, D. M., Natali, S. M., Olefeldt, D., Romanovsky, V. E.,
676 Schaefer, K., Turetsky, M. R., Treat, C. C., and Vonk, J. E.: Climate change and the permafrost
677 carbon feedback, Nature, 520, 171, 10.1038/nature14338, 2015.

678 Schwamborn, G., Rachold, V., and Grigoriev, M. N.: Late Quaternary sedimentation history of the Lena
679 Delta, Quaternary International, 89, 119-134, https://doi.org/10.1016/S1040-6182(01)00084-2,
680 2002.

681 Seppälä, M.: Synthesis of studies of palsa formation underlining the importance of local environmental
682 and physical characteristics, Quaternary Research, 75, 366-370,
683 https://doi.org/10.1016/j.yqres.2010.09.007, 2011.

684 Sharkhuu, N.: Occurrence of frost heaving in the Selenge River Basin, Mongolia, 10, 187-192,
685 10.1002/(sici)1099-1530(199904/06)10:2<187::Aid-ppp294>3.0.Co;2-w, 1999.

686 Shiklomanov, N. I., Streletskiy, D. A., Little, J. D., and Nelson, F. E.: Isotropic thaw subsidence in
687 undisturbed permafrost landscapes, Geophysical Research Letters, 40, 6356-6361,
688 10.1002/2013gl058295, 2013.

689 Slater, A. G., and Lawrence, D. M.: Diagnosing present and future permafrost from climate models,
690 Journal of Climate, 26, 5608-5623, 2013.

691 Streletskiy, D. A., Shiklomanov, N. I., Little, J. D., Nelson, F. E., Brown, J., Nyland, K. E., and Klene,
692 A. E.: Thaw Subsidence in Undisturbed Tundra Landscapes, Barrow, Alaska, 1962–2015,
693 Permafrost and Periglacial Processes, 28, 566-572, 10.1002/ppp.1918, 2017.

694 Swenson, S. C., Clark, M., Fan, Y., Lawrence, D. M., and Perket, J.: Representing Intrahillslope Lateral
695 Subsurface Flow in the Community Land Model, Journal of Advances in Modeling Earth
696 Systems, 11, 4044-4065, 10.1029/2019MS001833, 2019.

697 Treat, C. C., Natali, S. M., Ernakovich, J., Iversen, C. M., Lupascu, M., McGuire, A. D., Norby, R. J.,
698 Roy Chowdhury, T., Richter, A., Šantrůčková, H., Schädel, C., Schuur, E. A. G., Sloan, V. L.,
699 Turetsky, M. R., and Waldrop, M. P.: A pan-Arctic synthesis of CH4 and CO2 production from
700 anoxic soil incubations, 21, 2787-2803, 10.1111/gcb.12875, 2015.

701 Turetsky, M. R., Abbott, B. W., Jones, M. C., Anthony, K. W., Olefeldt, D., Schuur, E. A., Koven, C.,
702 McGuire, A. D., Grosse, G., and Kuhry, P.: Permafrost collapse is accelerating carbon release,
703 Nature, 569, 32-34, 2019.

704 Ulrich, M., Grosse, G., Chabrillat, S., and Schirrmeister, L.: Spectral characterization of periglacial
705 surfaces and geomorphological units in the Arctic Lena Delta using field spectrometry and
706 remote sensing, Remote Sensing of Environment, 113, 1220-1235,
707 https://doi.org/10.1016/j.rse.2009.02.009, 2009.

708 Walter, K. M., Zimov, S. A., Chanton, J. P., Verbyla, D., and Chapin, F. S.: Methane bubbling from
709 Siberian thaw lakes as a positive feedback to climate warming, Nature, 443, 71-75,
710 10.1038/nature05040, 2006.

711 West, J. J., and Plug, L. J.: Time-dependent morphology of thaw lakes and taliks in deep and shallow
712 ground ice, Journal of Geophysical Research: Earth Surface, 113, 10.1029/2006jf000696, 2008.

713 Westermann, S., Langer, M., Boike, J., Heikenfeld, M., Peter, M., Etzelmüller, B., and Krinner, G.:
714 Simulating the thermal regime and thaw processes of ice-rich permafrost ground with the land-
715 surface model CryoGrid 3, Geosci. Model Dev., 9, 523-546, 10.5194/gmd-9-523-2016, 2016.

716 Wünnemann, B., Reinhardt, C., Kotlia, B. S., and Riedel, F.: Observations on the relationship between
717 lake formation, permafrost activity and lithalsa development during the last 20 000 years in the
718 Tso Kar basin, Ladakh, India, 19, 341-358, 10.1002/ppp.631, 2008.

719 Zhang, T., Barry, R. G., Knowles, K., Heginbottom, J. A., and Brown, J.: Statistics and characteristics
720 of permafrost and ground-ice distribution in the Northern Hemisphere, Polar Geography, 23,
721 132-154, 10.1080/10889379909377670, 1999.

722 Zhang, T., Heginbottom, J. A., Barry, R. G., and Brown, J.: Further statistics on the distribution of
723 permafrost and ground ice in the Northern Hemisphere, Polar Geography, 24, 126-131,
724 10.1080/10889370009377692, 2000.

725 Zimov, S. A., Schuur, E. A., and Chapin, F. S.: Permafrost and the global carbon budget, Science, 312,
726 1612-1613, 2006.

727

728 **Table 1: The excess ice initialization scenario in each of the three terraces (landunits) for the Lena**
729 **River delta, as well as that for the single-landunit excess ice initialization case.**
730

Depth (after adding ice)	Volumetric Ice content	Area weight
	No excess ice terrain	
N/A	0%	24.6%
	Holocene ground ice terrain	
0.9-9 m	65%	66.6%
	Yedoma ice complex	
0.6-20 m	90%	8.8%
	Average ice single-landunit case	
0.6-0.9 m	7.92%	100%
0.9-9 m	51.21%	100%
9-20 m	7.92%	100%

731

732

733 **Table 2: The tiling scheme prescribing area weights of landunits for each CAPS class. The detailed**
734 **CAPS classes are shown in Figure 2.**

Overall visible ground ice content for each CAPS point	Tiling scheme (area weights for each excess ice category)	Eligible CAPS types
5%	80% no excess ice; 20% Low	clf; clf; slf; ilf; clr; dlr; slr; ilr
15%	58% no excess ice; 20% Low; 22% Medium	cmf; dmf; smf; imf; dhr; shr; ihr
15%	66% no excess ice; 20% Low; 14% High	chr
25%	44% no excess ice; 20% Low; 22% Medium; 14% High	dhf; shf; ihf
25%	52% no excess ice; 20% Low; 28% High	chf

735 Note: For each class, the first letter is for the permafrost extent, the second for the excess ice content, and the third
736 for the terrain and overburden, following Brown et al. (2002).

737

738 **Table 3: List of simulations conducted for this study.**

Cases	Description
	Single point cases for the Lena river delta
Triple-landunit case	Applying the sub-grid representation of excess ice. Three natural vegetated landunit initialized.
Average ice single-landunit case	Not applying the sub-grid representation of excess ice. Only one natural vegetated landunit initialized. The grid-mean excess ice content for each soil layer in the only landunit is calculated by spatially averaging those in different landunits in the triple-landunit case.
	Global simulation cases
No ice case	Not adding any excess ground ice (the original CLM5 simulation).
Sub-grid ice case	Applying the sub-grid representation of excess ice. A tiling scheme helps to "translate" excess ice conditions in the CAPS data to fit what the CLM5 requires.
Grid-average ice case	Not applying the sub-grid representation of excess ice. The grid-mean excess ice content for each soil layer is calculated by spatially averaging those in different landunits in the sub-grid ice case.

739

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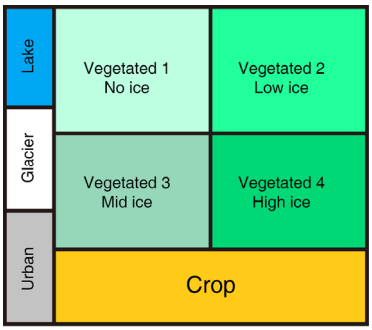
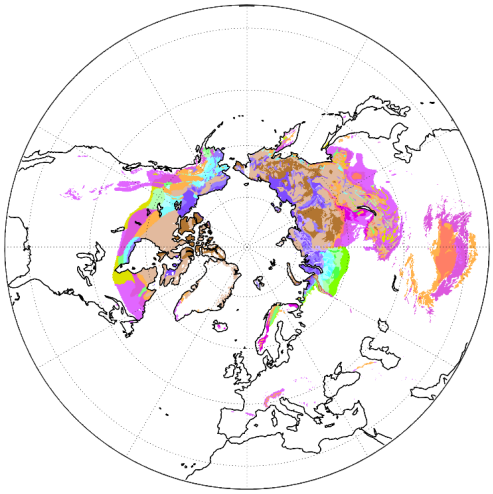


741

742 **Figure 1: Modification of the CLM5 tiling hierarchy on the landunit level containing four natural**
743 **vegetated landunits for different excess ice conditions.**

744



Permafrost area classification

Permafrost Extent	Ground Ice Content (percent by volume)				
	Lowlands, highlands, and intra-and intermontane depressions			Mountains, highlands, ridges, and plateaus	
	25%	15%	5%	15%	5%
Continous (100%)	chf	cmf	clf	chr	clr
Discontinous (70%)	dhf	dmf	dlf	dhr	dlr
Sporadic (30%)	shf	smf	slf	shr	slr
Isolated (5%)	ihf	imf	ilf	ihr	ilr

* Letter code naming: The first letter is for the permafrost extent, second for the ground excess ice concent, and the thrid for the terrain and overburden.

745

746 **Figure 2: Spatial distribution of excess ground ice in the Northern Hemisphere modified from**
747 **Brown et al. (2002). Compared to the original data, permafrost extents and ground ice contents**
748 **are converted to definite numbers (percentages) for model computation.**

749

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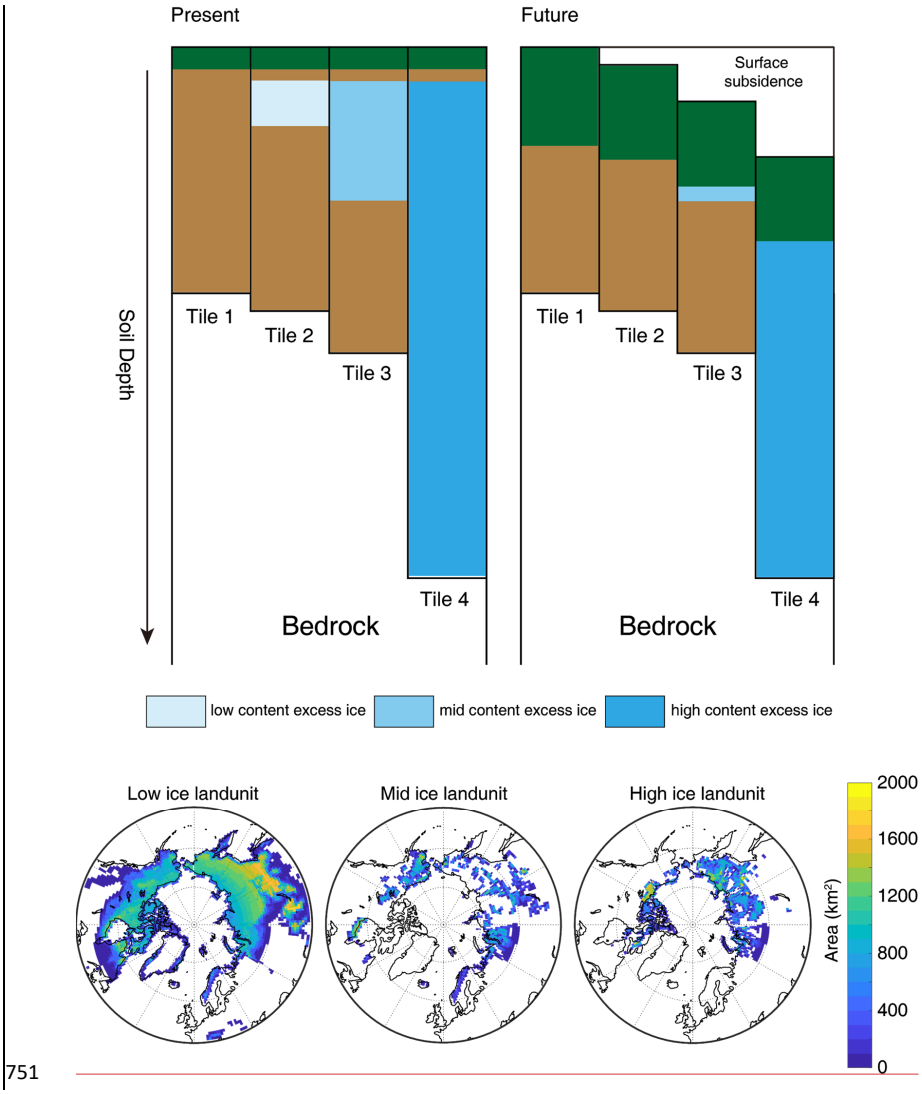
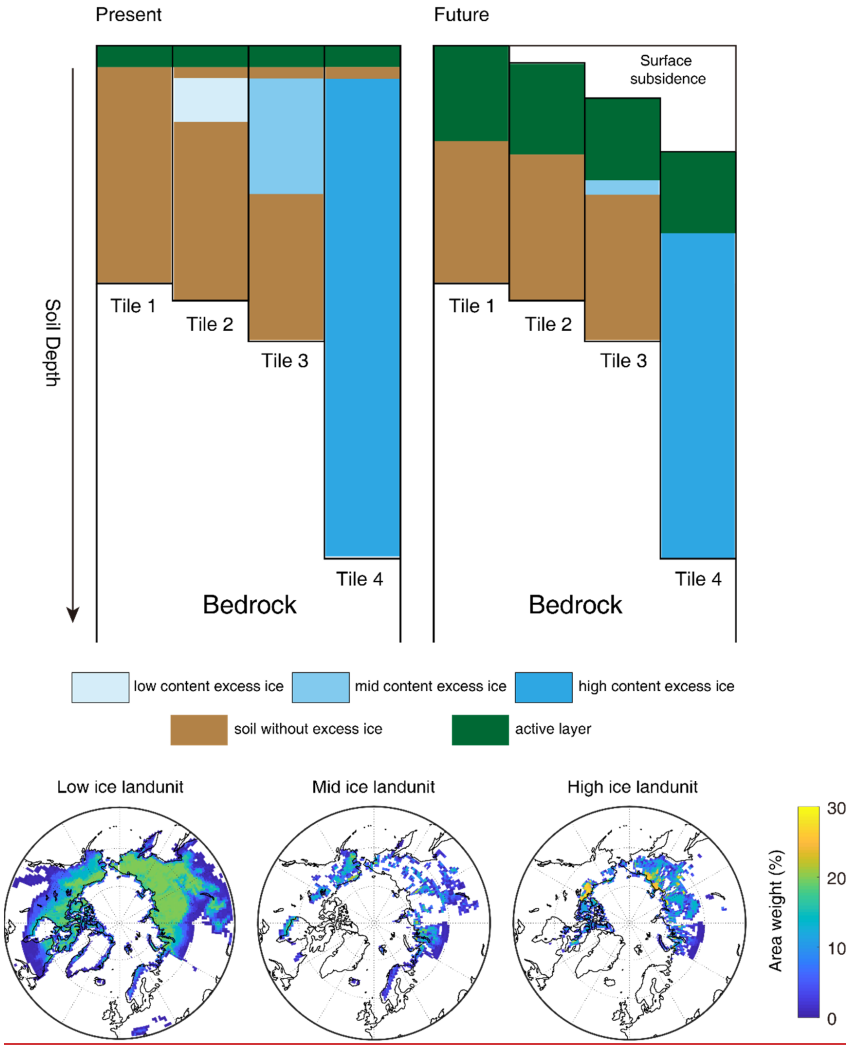

Present
Future
Surface subsidence
Soil Depth
Tile 1
Tile 2
Tile 3
Tile 4
Bedrock
low content excess ice
mid content excess ice
high content excess ice
Low ice landunit
Mid ice landunit
High ice landunit
Area (km²)
2000
1600
1200
800
400
0

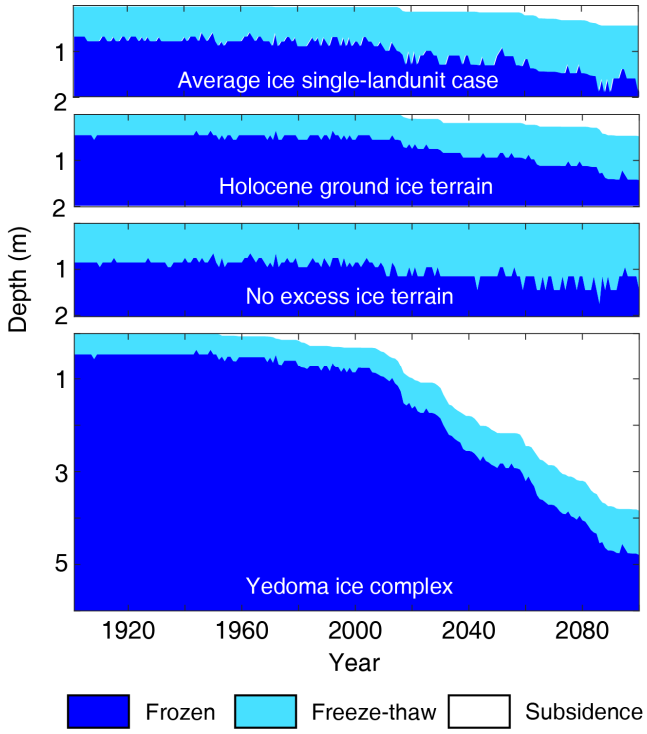
751



752

753 **Figure 3. Schematic representation of the sub-grid excess ice initialization scenario, and maps**
754 **showing the area weight (%) occupied by different excess ice landunits, i.e. the initial condition of**
755 **excess ice in the global simulation.**

756



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758 **Figure 4. Annual freeze-thaw state for the three terraces for the triple-landunit case, as well as for**
759 **the average ice single-landunit case.**

760

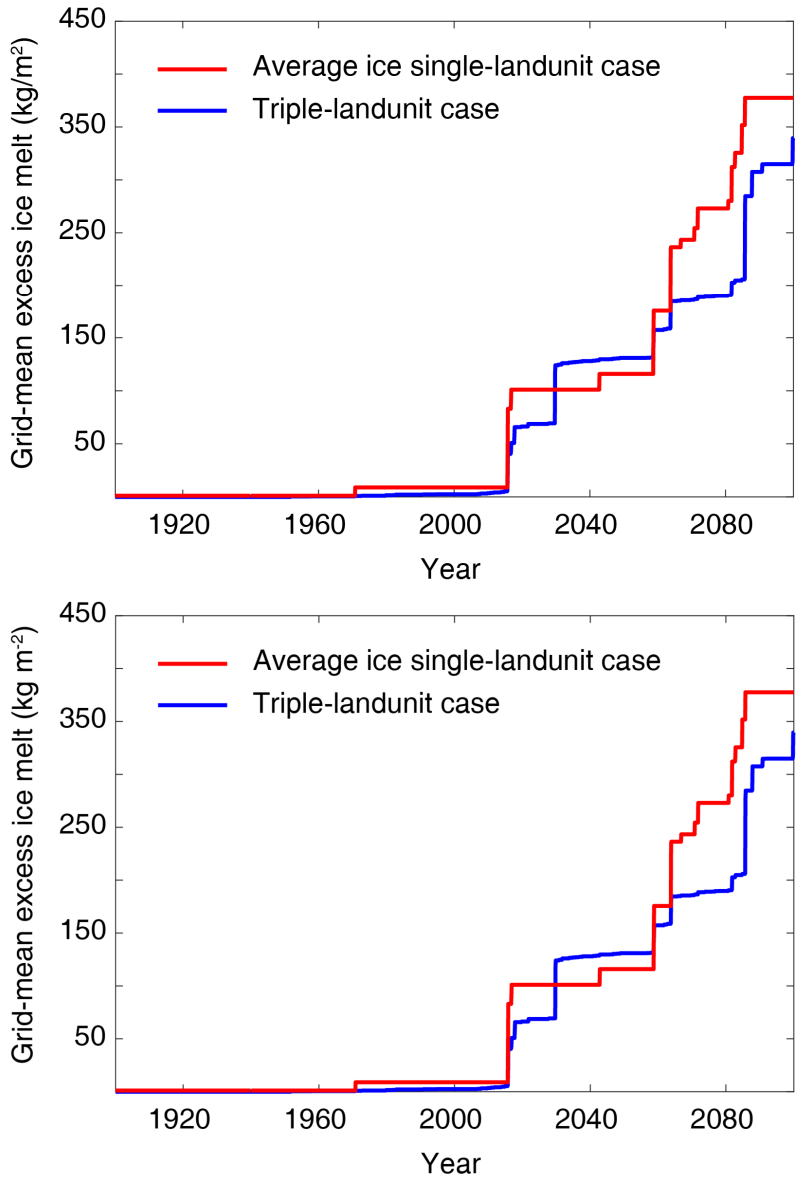
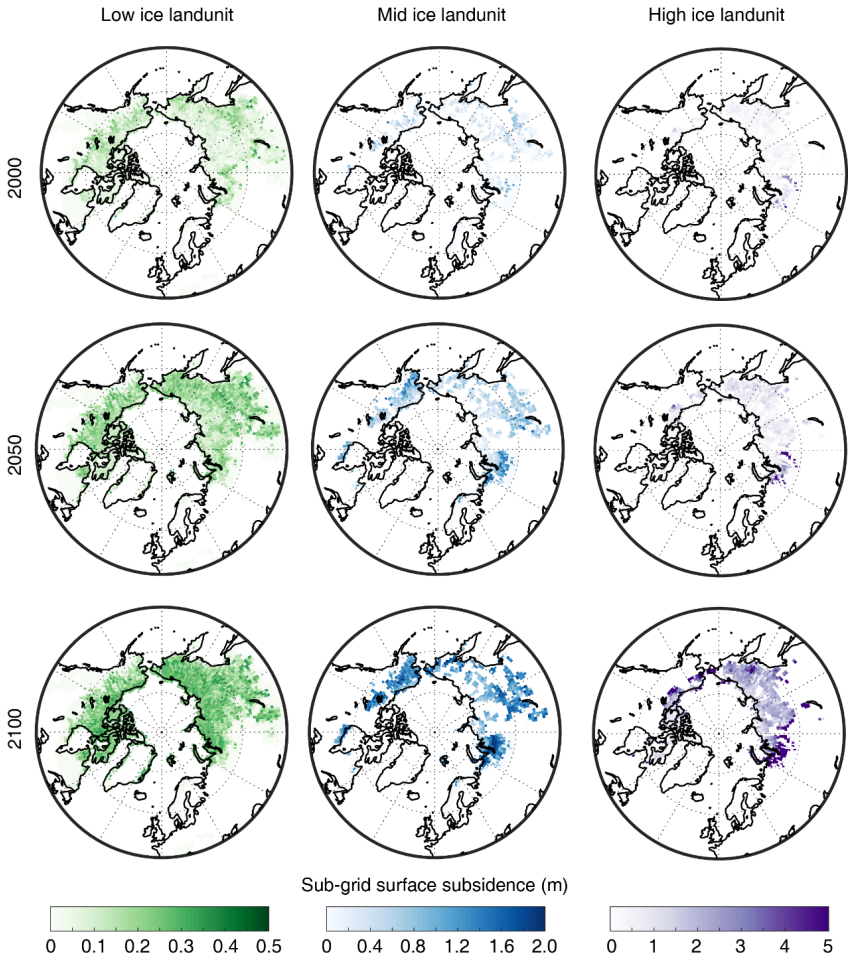


Figure 5. Grid-mean excess ice melt since 1900 for the single-point cases over the Lena river delta with and without the sub-grid excess ice initialization.



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767 **Figure 6. Maps showing sub-grid surface subsidence (m) in 2000, 2050, 2100 in the low, mid, and**
768 **high excess ice landunits in the sub-grid ice case.**

769

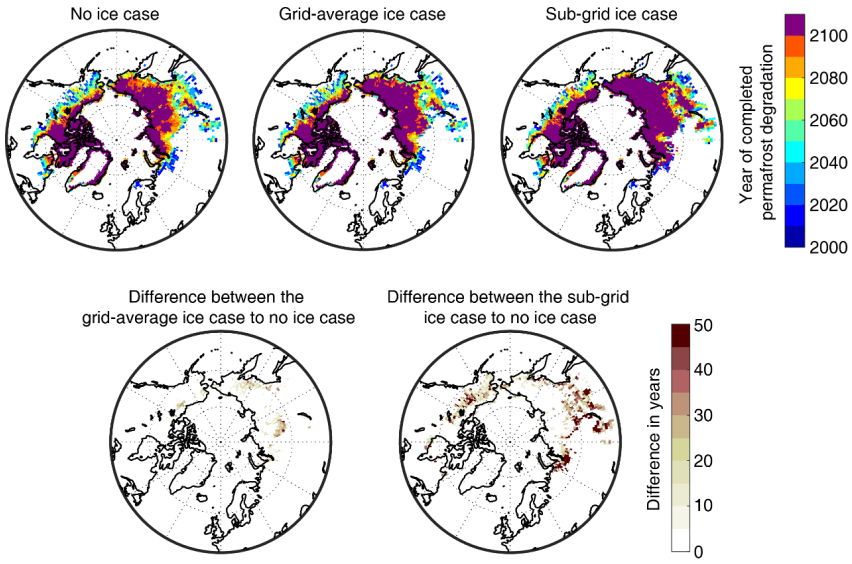


Figure 7. Maps showing the year of completed permafrost degradation (upper set of three maps), as well as the differences between cases (lower set of two maps). The purple color indicates the existence of permafrost in these grid ~~points~~ cells by 2100. The difference in years is provided only for grid cell with completed permafrost degradation before 2100.

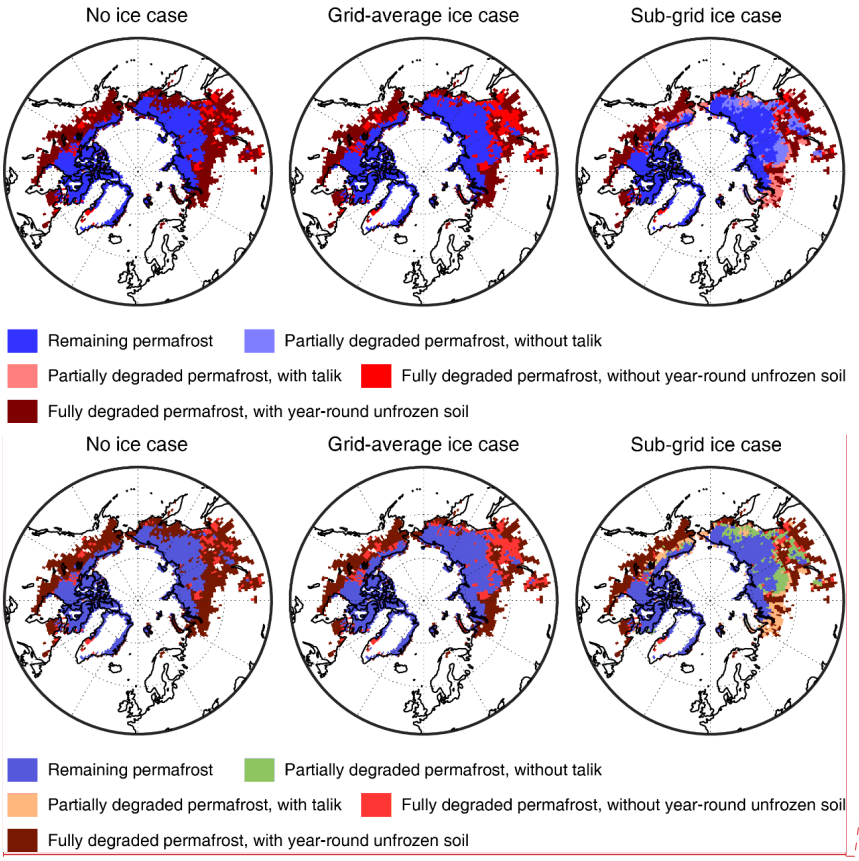
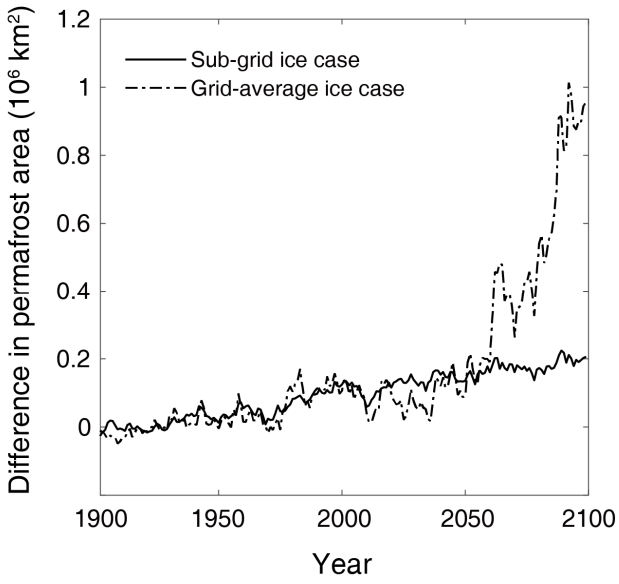


Figure 8. Maps of different stages of permafrost degradation diagnosed from the model output by the year 2100. "Year-round unfrozen soil"in the fully degraded permafrost region is defined as the part of degraded permafrost in which the soil temperature never decrease below 0 ℃ in any time of year, which is in the same manner as talik in the permafrost area.

Commented [LC3]: We have changed the colors to make them more distinct.



783

784 **Figure 9. Difference in modeled permafrost area ~~vs.~~versus time between the sub-grid ice case and**
785 **no ice case, as well as between the grid-average ice case and no ice case.**

786

Supplemental material for Projecting cCircum-Arctic eExcess gGround iIce mMelt with a sub-grid representation in the Community Land Model

S1. The sensitivity of excess ice melt and corresponding impacts to its sub-grid distribution

We design idealized single-grid simulation cases, aiming to examine the effects of incorporating excess ice at the sub-grid scale to soil physics, i.e. whether different sub-grid scale distributions of excess ice differ reasonably from each other during excess ice melt. The results of single-grid simulations help to verify if the sub-grid representation of excess ice shows more potential in modeling excess ice compared to its previous version, where excess ice is homogeneously distributed in the CLM grid cell (Lee et al., 2014). We employ the forcing data at the North Slope of Alaska (NSA; 70° N, 156° W) and to the Northeast of Yakutsk (Yakutsk; 63° N, 130° E) to represent the continental and maritime types of climate respectively in the circum-Arctic. They have the annual mean temperature and precipitation close to each other, while the seasonal variability in temperature is smaller in the North Slope of Alaska due to its adjacency to the Arctic Ocean (Bieniek et al., 2012).

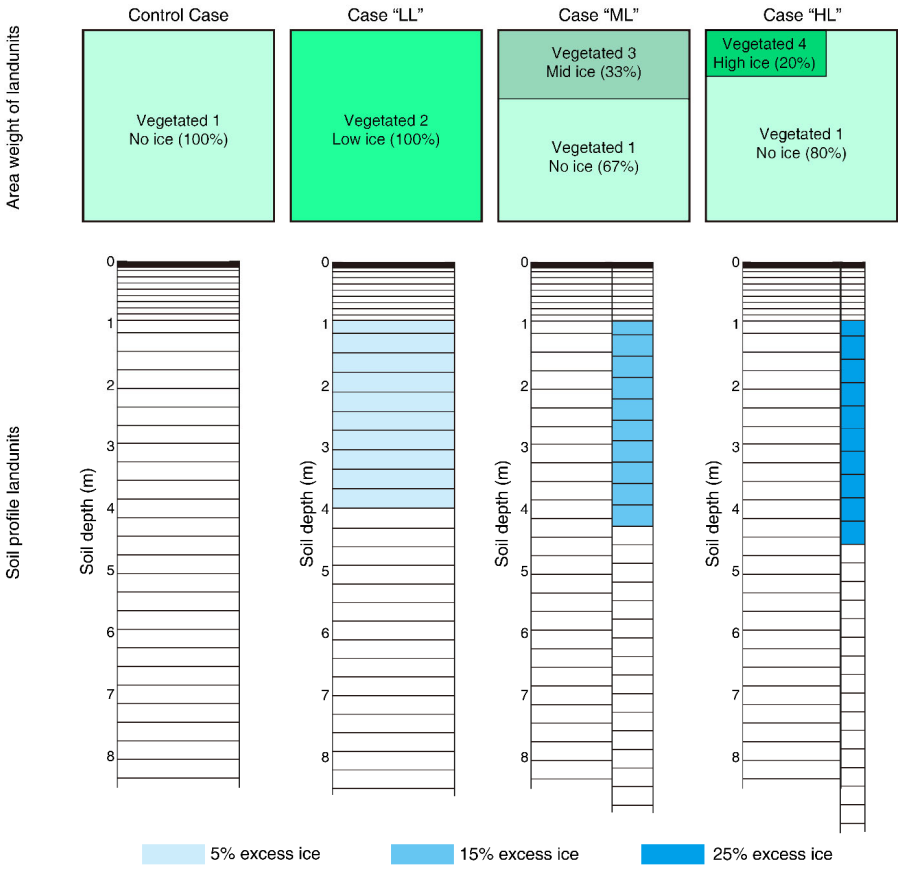


Figure S1: The schematic figure for the area weights (the percentage between parentheses) and soil profiles within the landunits in the four single-grid simulations. Besides the control case, three other cases are with the same amount of excess ice within the single grid. "LL", "ML", and "HL" are abbreviations for "Low ice Landunit", "Mid ice Landunit", and "High ice Landunit", representing the applied excess ice landunit in each case.

The grid-mean volumetric excess ice content is set to be 5%. We set up three excess ice cases with the same (or very close) grid-scale excess ice content but with different spatial variability. For each site, we design three cases, having a 100% area weight of 5% volumetric excess ice content (NSA_LL and Yakutsk_LL), a 33% area weight of 15% volumetric excess ice content (NSA_ML and Yakutsk_ML), and a 20% area weight of 25% volumetric excess ice content (NSA_HL and Yakutsk_HL), respectively (Figure S1). For all of the original soil layers between 1-4 meters, excess ice is incorporated homogeneously, which proportionally increases the soil thickness for these layers. The initialization depth of excess ice keeps the same as in Lee et al. (2014). Both locations we choose are with 100% natural soil and continuous permafrost to avoid the interference of model results by other landunit types from the source.

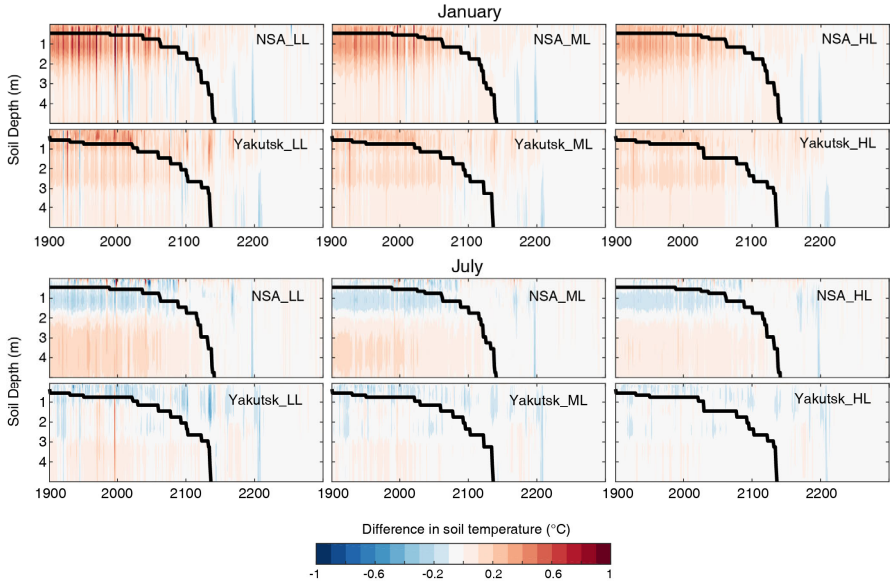


Figure S2: Soil temperature differences from excess ice cases to control cases (NSA_control and Yakutsk_control) for the depth of 0.005-5 meters in January and July. Black lines are the active layer depth deepening through time. The active layer depth is calculated from grid-scale soil temperature for each case.

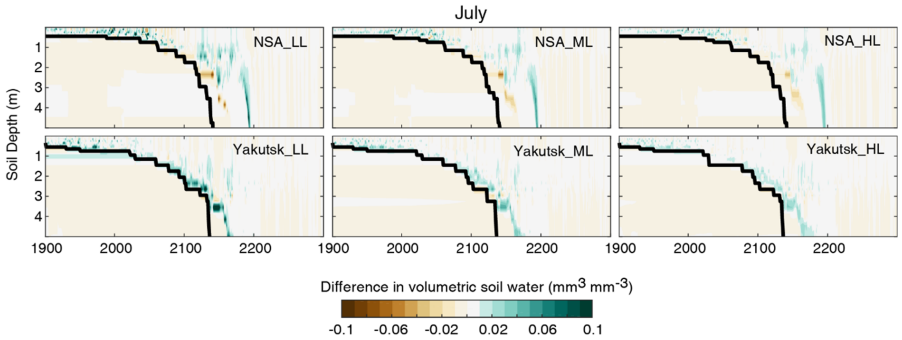


Figure S3: Soil moisture differences from excess ice cases to the corresponding control cases (NSA_control and Yakutsk_control) for the depth of 0.05-5 meters in July. Black lines are the active layer depth deepening through time. The active layer depth is calculated from grid-scale soil temperature for each case.

As a result, differences in soil temperature and moisture from excess ice cases to control cases in single-grid simulations quantitatively show the effects of excess ice and its melting. In the shallower layers (0-2 m), excess ice results in slightly higher soil temperature in January (winter) but lower soil temperature in July (summer) relative to control cases, reducing the magnitude of the seasonal cycle in soil temperature (Figure S2). In deeper layers (>2 m), the soil temperature in excess ice cases remains higher compared to control cases for both in summer and winter. The above responses in permafrost temperature results from the increases of specific heat and thermal conductivity of the soil layer after incorporating excess ice. As the climate warms and permafrost thaws, the meltwater discharges in the form of runoff, eventually bringing soil temperatures in excess ice cases closer to that in the control case. For soil moisture, the volumetric water content in July is higher in excess ice cases than control and is just above the permafrost table (Figure S3). As the active layer substantially deepens in the projected period for both sites, soil water in excess ice cases increases abruptly around 2180 for NSA while around 2150 for Yakutsk, indicating the degradation of permafrost in control cases. When permafrost degrades in the control case, the excess soil water in control cases starts to ~~of~~ runoff in the form of subsurface drainage, flushing out soil water and making the soil drier. Note that the subsurface drainage is unlikely to happen in reality since the permafrost at these two sites are much thicker than 10 m. Meanwhile, this has not occurred in excess ice cases yet, making the soil wetter in excess ice cases than in control cases. These responses in permafrost temperature and moisture after permafrost degradation are consistent with the results in Lee et al. (2014), suggesting that the excess ice physics developed in CLM4.5_EXICE performs reasonably in a sub-grid manner in CLM5. Among the three excess ice cases, the "LL" case shows the strongest responses in both soil temperature and soil water content. On the other hand, the effects of excess ice in soil temperature and moisture are weaker in the "ML" and "HL" cases, where the same amount of excess ice is distributed more localized within a fraction of the grid.

Both sites exhibit active layer depth of around 0.5 m by the end of the spinup and active layer thickness does not increase substantially during the historical period (Black lines in Figure S2 and S3). For this reason, excess ice is incorporated one meter below the surface. No excess ice, therefore, melts during either the spin-up or the historical period simulations. Excess ice starts to melt around the 2070s in NSA_LL, while the timing is delayed

for about 25 years in the other two cases for the same site (NSA_ML and NSA_HL; Figure S4). It is because the higher content of excess ice covering a smaller area takes longer to absorb enough latent heat of fusion from the atmosphere before it can start melting. Excess ice in NSA completely melts away in the 2170s and the exact timing of which varies slightly (< 5 years) between cases. In Yakutsk, excess ice starts to melt earlier, but with a slower rate compared to NSA. Similar to the NSA cases, Yakutsk_ML and Yakutsk_HL exhibit delays in the timing of excess ice melt compared to Yakutsk_LL. Excess ice in Yakutsk_LL completely melts in the 2170s, while the timings of excess ice melting in Yakutsk_ML and Yakutsk_HL is delayed for about 10 to 15 years, respectively (Figure S4).

Excess ice melting supplies extra water to subsurface water storage, increasing soil water and eventually converting to runoff. The increases in surface runoff correspond well in timing with excess ice melt (Figure S4). Earlier permafrost thaw timing in control cases causes an earlier increase in subsurface runoff and a decrease in the surface runoff than in excess ice cases. On the other hand, when the active layer depth reaches below the deepest soil layer in excess ice cases, more soil water from melt ice leads to the higher subsurface runoff compared to that in control cases. Among the three excess ice cases, the “LL” cases consistently exhibit the strongest and earliest responses in both surface and subsurface runoff as excess ice melts, being consistent with their earlier start of excess ice melt.

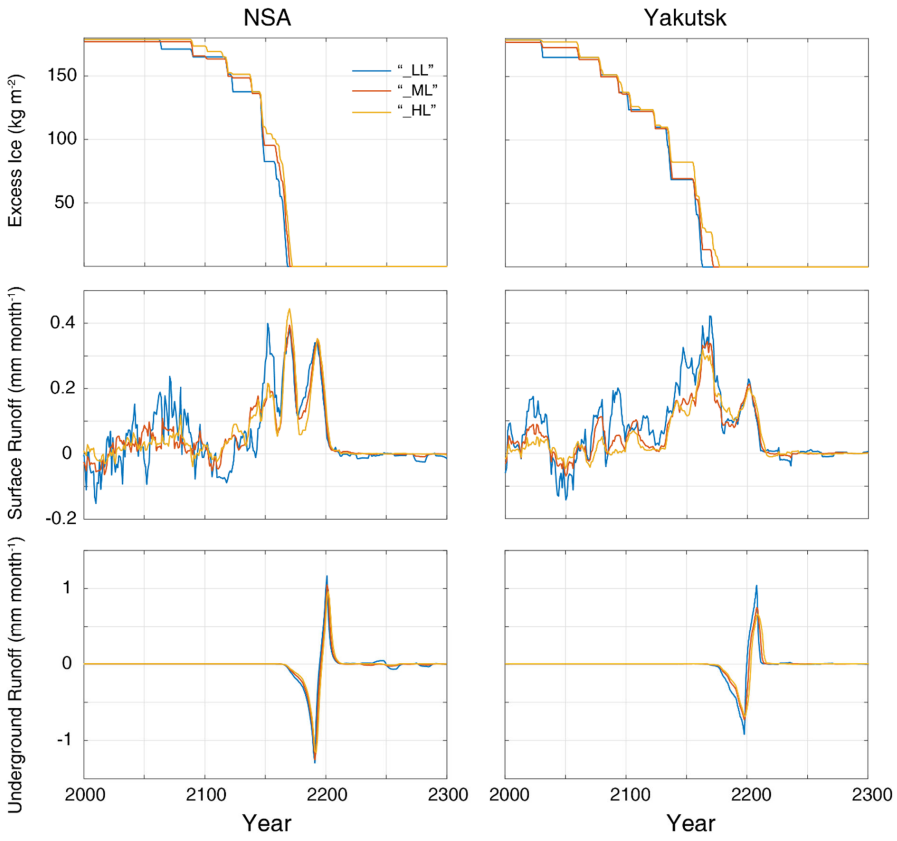


Figure S4: Time series of excess ice (kg ~~/m^3~~ m^{-2}), as well as the difference of surface runoff (mm ~~/~~month^{-1}) and subsurface drainage (mm/month) from the three excess ice cases to control cases. A 15-year moving average is applied before plotting both the surface and underground runoff.

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References

Bieniek, P. A., Bhatt, U. S., Thoman, R. L., Angeloff, H., Partain, J., Papineau, J., Fritsch, F., Holloway, E., Walsh, J. E., Daly, C., Shulski, M., Hufford, G., Hill, D. F., Calos, S., and Gens, R.: Climate Divisions for Alaska Based on Objective Methods, Journal of Applied Meteorology and Climatology, 51, 1276-1289, 10.1175/jamc-d-11-0168.1, 2012.

Lee, H., Swenson, S. C., Slater, A. G., and Lawrence, D. M.: Effects of excess ground ice on projections of permafrost in a warming climate, Environmental Research Letters, 9, 124006, 2014.