



Liquid-water content and water distribution of wet snow using electrical monitoring.

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Abstract:

Snow exists in a wide range of temperatures and around its melting point snow becomes a three-phase material. A better understanding of wet snow and the first starting point of water percolation in the seasonal snowpack is essential for snow pack stability, snow melt run-off and remote sensing. In order to induce and measure precisely the liquid water and the corresponding dielectric properties inside a snow sample, an experimental setup was developed. Using microwave heating at 18 kHz allows the use of dielectric properties of ice to enable heat to be dissipated homogeneously through the entire volume of snow. A desired liquid water content inside the snow sample could then be created and analysed in a micro-computer tomography. Based on the electrical monitoring a promising perspective for retrieving water content and water distribution in the snowpack is given. The heating process and extraction of water content are mainly dependent on the morphological properties of snow, the temperature and the liquid water content. The experimental observation can be divided in three different heating processes affecting the dielectric properties of snow for different densities: (1) dry snow heating process up to 0 °C indicating a temperature and snow structure dependency of the dielectric property of snow; (2) wet snow heating at stagnating temperature of 0°C and the presence of uniformed distributed liquid water changes the dielectric properties. The presence of liquid water decreases the impedance of the snow sample until water starts to percolate; and (3) the start of water percolation is between 5-12 water volume fraction depending on the



31 snow density and confirms the literature findings. The onset of water percolation
32 initiated an inhomogeneity in snow and water distribution, strongly affecting the
33 dielectric properties of the snow. These findings are pertinent to the interpretation of
34 the snow melt run-off of spring snow. These laboratory measurements allow to find
35 the narrow range of the starting point of water percolation in coarse-grained snow and
36 to extract the corresponding dielectric properties which is important for remote
37 sensing.



38 **1. Introduction**

39 Snow, a sintered porous material made of ice grains, has a complex porous
40 microstructure and consist of a continuous ice structure at temperature below zero
41 degrees (Löwe et al., 2011). Reaching the melting point, snow becomes a three-
42 component mixture of ice, water and air. A detailed understanding of the influence of
43 liquid water on the snow microstructure is essential. It influences radar and microwave
44 attenuation, sub-surface exploration, remote sensing, radar altimetry, electrical
45 grounding, atmospheric electrical fields and electrostatic charging by precipitation and
46 blown particles (Mellor, 1977). Liquid water in snow is also a critical factor for
47 estimating the hazard of wet snow avalanches and the transmission of melt-water
48 through a snow-pack (Evans, 1965; Reiweger et al., 2015).

49 Estimating liquid water content is difficult even for experienced observers (Martinec,
50 1991; Fierz and Föhn, 1994), partly because water flow through snow varies both
51 spatially and temporally (e.g. Colbeck 1979; Marsh, 1988; Conway and Benedict,
52 1994). Introduction of liquid water into snow changes morphological (Brun, 1989;
53 Coléou and Lesaffre, 1998; Raymond and Tusima, 1979; Brun, 1989; Marsh, 1987;
54 Colbeck, 1997; Marshall et al., 1999; Jordan et al., 2008) and mechanical properties
55 of snow (Techel et al., 2011; Colbeck, 1982). When liquid water occurs for the first
56 time in the seasonal snowpack, much water can be hold as small grains cause high
57 capillary forces. After a couple of melt-freeze cycles smaller grains disappear and less
58 melt-water is held immobile in the snow matrix (Yamaguchi et al., 2010). This delays
59 water runoff during the early stages of snowpack melt-out and snow can retain liquid
60 water (Colbeck, 1972; Linsley et al, 1949). Reaching a saturation point, the liquid water
61 is then released suddenly. The transition point where the liquid water starts to
62 percolate in the snow sample is important because it dominates the spring runoff
63 period in many regions.

64 Measuring the liquid water content non-destructively and homogeneously in larger
65 snow samples (in centimetre regime) is very challenging. The small amount of liquid
66 water present and the sensitivity of the snow to the various processes to induce a
67 defined liquid water content makes the measurements hard. Radiative absorption or
68 snow melting in a room at 0°C induces a temperature gradient from the surface to the
69 core of the snow sample leading to an inhomogeneous liquid-water content



70 distribution. The direct supply of liquid water causes percolation in preferential
 71 selected channels. In both cases, the water distribution is not homogeneous and the
 72 exact extraction of the starting point of water percolation is not possible. In contrast,
 73 Coléou and Lesaffre (1998) performed experiments by slowly saturate a snow sample
 74 fully with water and afterwards drained out to find the starting point of water
 75 percolation. They approached the water retention curve of snow (Yamaguchi et al.,
 76 2010) from the right side. In these experiments water percolation was initiated at
 77 around 5-14 % of mass volume for snow density between 350 kg m^{-3} and 680 kg m^{-3}
 78 (Coléou and Lesaffre, 1998).

79 Another way to induce a homogeneous liquid-water content into the snow without
 80 destroying the snow sample is microwave heating (Brun, 1989; Camp and LaBrecque,
 81 1992). In this case, the water retention curve of snow (Yamaguchi et al., 2010) is
 82 approached from the left side. A uniform electric field oscillating at an appropriate
 83 frequency excites the dielectric properties of ice enabling heat to be dissipated through
 84 the whole volume of snow (Mellor, 1977; Brun, 1989; Camp and LaBrecque, 1992).
 85 The dielectric properties of the ice depend on the frequency, temperature and snow
 86 density. The applied field results in a displacement of charged particles in the
 87 insulating material, giving rise to induced dipoles. The permanent dipoles of the water
 88 molecule respond to the electric field, which results in a temperature increase of the
 89 material. The heat absorption by the ice phase is uniform and the absorbed energy
 90 depends only on the imaginary part ε'' of permittivity (Polder and Van Santen, 1946).

91 Dielectric properties of dry snow are closely related to solid ice. The ideal relaxation-
 92 frequency of ice is at 7.5 kHz (Auty and Cole, 1952). However, the relaxation
 93 frequency of dry snow lies between 10 and 100 kHz depending on the snow density
 94 and temperature (Bader and Kuroiwa, 1962; Polder and Van Santen, 1946; Evans,
 95 1965). The presence of liquid water strongly affects the dielectric properties of the wet
 96 snow sample (Sweeny and Colbeck, 1974; Ambach and Denoth, 1980, Camp and
 97 LaBrecque, 1992). A wide spectrum of frequencies has been explored to determine
 98 the free water content of water in snow (Ambach and Denoth, 1975; Boyne and Fisk,
 99 1987; Brun, 1989; Denoth et al., 1984; Denoth and Foglar, 1986; Perla, 1990; Camp
 100 and LaBrecque, 1992). As long as the liquid water phase remains discontinuous on
 101 the ice matrix (Brun E., 1989), the dielectric properties of the wet snow sample are



102 homogenous over the whole sample and the amount of liquid water can be estimated
103 (Ambach and Denoth, 1972, Koch et al., 2014). At the point where the liquid water
104 starts to percolate, an inhomogeneous distribution of water and ice starts to build up
105 in the total snow sample and locally affects the dielectric properties of the sample.
106 Work by Camp and LaBrecque (1992) showed that dielectric heating at 20 kHz is a
107 useful means of modifying the water content from 0 to 30% by weight.

108 The objective of this paper is to present an experimental setup to allow standardized
109 studies to extract the starting point of water percolation depending on snow density
110 and dielectric properties. We developed a dielectric heating device at 18 kHz, similar
111 to the work by Brun (1989) and Camp and LaBrecque (1992), to find the narrow range
112 of the starting point of water percolation in coarse-grained snow. We improved the
113 suggested power measurements by improving the measurement of phase to be more
114 sensitive in the control of water content. Our technique of monitoring the voltage,
115 current and phase shift at the two copper plates makes it possible to study the
116 dielectric properties of the snow as the water content changes. In particular, at
117 temperature close to the melting point the surface properties of the ice change
118 markedly affecting the dielectric properties. Additionally, with the well-controlled
119 electrical heating the exact water content of water percolation of different kind of snow
120 densities and surface-to-volume ratio can be extracted. We analysed three regimes:
121 (1) dry snow heating showing the fraction of energy absorption of the snow, (2)
122 producing wet snow to investigate the starting point of water percolation based on the
123 electrical properties and density of the snow. Additionally, primarily quantifying of the
124 water content in three-dimensional space without destroying the snow structure are
125 analyzed using micro computed tomography (micro-CT); (3) water percolation
126 affecting the overall impedance of the snow sample.

127 **2. Experimental setup**

128 The experimental setup is shown schematically in Fig. 1 and a photo of the
129 experimental setup is shown in Fig. 2. The device consists of three functional blocks:
130 (1) low voltage circuit to generate the sinusoidal signal and amplify the energy output,
131 (2) high voltage circuit to transform the low primary voltage to a high secondary
132 voltage, and (3) design of the sample holder between the high voltage capacitor plates.



133 The core of the snow heater is a Red Pitaya STEM 125-14 using for signal generation
 134 and data acquisition, and is controlled via Standard Commands Programmable
 135 Instruments SCPI in Matlab. The low voltage sinusoidal input signal with a frequency
 136 of 18 kHz is generated by a high-speed digital to analog converter and is amplified
 137 afterwards to stabilizes the electrical potential in the circuit. A step-up transformer
 138 transforms the low primary voltage to a high secondary voltage of around 350 V
 139 applied to two copper plates inducing the dielectric heat into the snow sample. The
 140 surface of the copper plates is electrically insulated to prevent Joule heating of the
 141 snow sample. The snow sample was placed into a polyoxymethylene (POM) ring
 142 (diameter = 60 mm, distance = 13 mm) and inserted between the two capacitor plates.
 143 The snow sample and the capacitor are thermally insulated with extruded polystyrene
 144 foam (XPS) with a thickness of 120 mm to prevent radial conductive and convective
 145 heat losses.

146 The applied sinusoidal waveforms of voltage $U(t)$ to the copper-plates is attached to a
 147 differential probe and is measured galvanic sorted with a 100-fold attenuation. The
 148 current $I(t)$ from the plate is measured via a shunt resistor. The phase shift $\varphi(t)$
 149 between the sinusoidal waveforms of voltage and current is measured between the
 150 circuit's input and circuit's output signal. An input protection circuit prevent the analog
 151 to digital converter from damage in case of a short circuit. The voltage connection
 152 between the low and high voltage part is measured via a shunt resistor. This
 153 connection defines the star point of the circuit and makes sure that the second part of
 154 the circuit doesn't thrift away. It is the only star point preventing the circuit from circular
 155 currents. A negative temperature coefficient element is placed one centimetre inside
 156 the snow sample to measure the temperature. A low pass filter is applied to block the
 157 noise of the capacitor.

158 The total power $P_{\text{RMS}}(t)$ between the two copper-plates is calculated based on the root-
 159 mean-squared voltage $U_{\text{RMS}}(t)$, current $I_{\text{RMS}}(t)$ and the measured phase difference $\varphi(t)$

$$160 \quad P_{\text{RMS}}(t) = U_{\text{RMS}}(t) \cdot I_{\text{RMS}}(t) \cdot \cos\varphi(t) \quad (1)$$

161 The impedance $R_{\text{RMS}}(t)$, describing the resistant of the snow sample, between the two
 162 copper-plates is given by



$$R_{RMS}(t) = \frac{U_{RMS}(t)}{I_{RMS}(t)} \quad (1)$$

The uncertainties of the temperature $T(t)$, current $I_{RMS}(t)$, voltage $U_{RMS}(t)$, phase shift $\varphi(t)$, total power consumed $P(t)$, and density of the snow measured by weighting are: ± 0.05 °C, ± 0.01 mA, ± 0.5 V, ± 2 degrees, ± 0.005 W and ± 20 kg m⁻³.

2.1 Tomography experiments

A cooled micro-computer tomograph (CT; Scanco Medical μ -CT80) at a cold laboratory temperature of -5 °C was used to visually quantify the water content in three-dimensional space without destroying the snow structure. The scanned image had a volume of 200 x 200 x 20 voxels (3.6 mm x 3.6 mm x 0.36 mm) with a nominal voxel resolution of 18 μ m. The grey scale resolution for each voxel was 16 bit and a Gaussian filter ($\sigma = 1.4$, support = 3) was applied to reconstruct the micro-CT images. The volume was segmented to a binary image by classifying each voxel by ice or air. The threshold for the segmentation process was chosen such as that the manually measured density did not deviate more than 12 % from the CT-density in the segmentation process (Riche and Schneebeli, 2013). Each scan took around 2.7 h. Absorption by water and ice are almost identical (Lieb-Lappen et al., 2017), and are hardly to separate in the segmentation process. Therefore, the water creation on the snow surface was extracted by superposition of two micro-CT scans. One scan was taken before the heating process and the second one afterwards. Before the second micro-CT scan, the wet snow sample was shock frozen at -30 °C to preserve the snow structure. This allowed us to easily visualize and to extract the water creation on the surface of the ice matrix with an uncertainty of 4 %.

3. Method

The phenomena involved in microwave heating of snow are volumetrically absorption of electromagnetic energy to achieve self-heating uniformly and rapidly, which is characterized by the density of the snow. The dielectric power absorption P is equal to the total power consumed P_{RMS} , given by:

$$P = 2 \cdot \pi \cdot f \cdot E^2 \varepsilon_0 \cdot \varepsilon_s''(f, \rho_s, T_s) \cdot A \cdot d = P_{RMS} \quad (3)$$



191 where f is the frequency, $E = U/d$ the electric field, $\epsilon_0 = 8.85 \cdot 10^{-12}$ the electric field
 192 constant, ϵ_s'' the imaginary part of the complex dielectric constant of snow, A the
 193 capacitors surface area and d the distance between the two copper-plates.
 194 Rearranging Eq. (3) the imaginary part of the complex dielectric constant of dry snow
 195 is given by

$$196 \quad \epsilon_s''(f, \rho_s, T_s) = \frac{P_{\text{RMS}}}{2 \cdot \pi \cdot f \cdot E^2 \cdot \epsilon_0 \cdot A \cdot d} \quad (4)$$

197 which depends on the frequency f , snow density ρ_s , and snow temperature T_s .

198 The heating efficiency is an important factor to evaluate the heating process. It is
 199 defined as the ratio of energy absorbed by the heated sample to that radiated from the
 200 microwave source [Ali, 2016] given by:

$$201 \quad \eta = \frac{Q_{\text{setup}} - Q_{\text{sample}}}{Q_{\text{setup}}} = 1 - \frac{m_s c_p (T_1 - T_0)}{\int_0^{t_1} P_{\text{RMS}}(t) dt} \quad (5)$$

202 where m_s is the mass of the snow sample, c_p the specific heat capacity, T_0 and T_1 the
 203 initial temperature and melting temperature at 0 °C, and t_1 the time until temperature
 204 reached 0 °C.

205 The liquid water mass fraction for each timestep t , is calculated by the fraction of the
 206 measured dissipated latent heat and total latent heat needed for the phase change:

$$207 \quad x_{\text{mass}}(t) = \frac{\int_{t_1}^t \eta \cdot P_{\text{RMS}}(t) dt}{h_{\text{latent}} m_s} \quad (6)$$

208 where $h_{\text{latent}} = 334 \text{ kJ kg}^{-1}$ is the latent heat for the phase change from ice to water and
 209 t_1 the time step where the snow sample reached 0 °C.

210 The liquid water volume fraction is given by [Coléou and Lesaffre, 1998]:

$$211 \quad x_{\text{vol}}(t) = \frac{x_{\text{mass}} \cdot \rho_s}{\rho_i - \rho_s} \cdot \frac{\rho_i / \rho_w}{1 - x_{\text{mass}}} \quad (7)$$



212 where ρ_s , ρ_i and ρ_w are the snow, ice (917 kg m^{-3}) and water (999.9 kg m^{-3}) density.
 213 The uncertainties of x_{mass} and x_{vol} are 10 % due to the uncertainty of the power (± 0.005
 214 W) and density measurement ($\pm 20 \text{ kg m}^{-3}$).

215 4. Results

216 Deionized water with a conductivity of $\approx 0.2 \mu\text{S cm}^{-1}$ was used to produce natural
 217 identical snow (Schleef et al., 2014) in a cold laboratory at -20°C . The produced snow
 218 was sieved into sample holders (mesh size: $2 \times 2 \text{ mm}$) and was sintered at a
 219 temperature of -2°C for two to five days to allow the snow crystals to form a uniform
 220 grain size. A hydraulic press compressed the snow to densities between 400 and 600
 221 kg m^{-3} to represent snow packs in spring (Bartelt and Lehning, 2002). We analysed in
 222 total seven different snow samples.

223 The measured electrical properties between the two copper-plates were strongly
 224 influenced by the temperature, water content, and density of the snow sample. The
 225 higher the snow density and the water content in the snow was, the stronger the
 226 measured electrical properties were affected, shown in Table 1. Figure 3 shows a
 227 typical measured temperature $T(t)$, current $I_{\text{RMS}}(t)$, voltage $U_{\text{RMS}}(t)$, and phase shift $\phi(t)$
 228 profile of a heating process for snow density of (a) 438 kg m^{-3} , (b) 539 kg m^{-3} , (c) 612
 229 kg m^{-3} , and (d) 917 kg m^{-3} . The temperature profile shows the characteristic of the
 230 snow heating process increasing from -1°C up to 0°C . Afterwards the temperature
 231 stagnates at 0°C and the supplied energy was used for the phase change from ice to
 232 liquid water. The current profile has a different behaviour. It shows a slightly linear
 233 increase until the snow sample reached a temperature of 0°C . Afterwards the incline
 234 of the current curve further increased reaching the highest current of 1.7 mA, 2.6 mA,
 235 3.8 mA, and 4.3 mA at around 80 min, 60 min, 55 min, and 9 min for snow with
 236 densities of 438 kg m^{-3} , 539 kg m^{-3} , 612 kg m^{-3} , and 917 kg m^{-3} . After this maximum
 237 the current started to decrease with time. The voltage and phase shift showed a mirror
 238 inverted behaviour to the current profile. Both parameters decreased with time and
 239 increased afterwards again. At the beginning a phase shift of 55.9° , 52.8° , 50° , and
 240 46.9° were measured with the lowest phase shift of 41.3° , 35.2° , 31.5° , and 22.4° for
 241 snow densities of 438 kg m^{-3} , 539 kg m^{-3} , 612 kg m^{-3} , and 917 kg m^{-3} .



242 The snow temperature, density and water content strongly affected the impedance
 243 and the total power consumed by the snow sample. The impedance decreased with
 244 increasing temperature, water content, and density, vice versa for the total power
 245 consumed, shown in Table 2. Figure 4 shows a typical calculated total power $P_{\text{RMS}}(t)$
 246 and impedance $R_{\text{RMS}}(t)$ profile compared with the measured temperature profile of a
 247 heating process for snow density of (a) 438 kg m^{-3} , (b) 539 kg m^{-3} , (c) 612 kg m^{-3} , and
 248 (d) 917 kg m^{-3} . The impedance had the same profile behaviour like the phase shift
 249 starting with $368.4 \text{ k}\Omega$, $275.5 \text{ k}\Omega$, $213.5 \text{ k}\Omega$, and $123.1 \text{ k}\Omega$ reaching a minimum of
 250 $197.4 \text{ k}\Omega$, $127.3 \text{ k}\Omega$, $87.3 \text{ k}\Omega$, and $73.5 \text{ k}\Omega$ after 80 min, 60 min, 55 min, and 9 min for
 251 snow density of 438 kg m^{-3} , 539 kg m^{-3} , 612 kg m^{-3} , and 917 kg m^{-3} . The total power
 252 consumption profile was mirror inverted. It started with 0.17 W , 0.25 W , 0.33 W , and
 253 0.63 W and reached a maximum of 0.41 W , 0.69 W , 1.04 W , and 1.24 W after 80 min,
 254 60 min, 55 min, and 9 min for snow density of 438 kg m^{-3} , 539 kg m^{-3} , 612 kg m^{-3} , and
 255 917 kg m^{-3} .

256 The heating efficiency was affected by heat loss at the wall and decreases with higher
 257 snow density. The microwave power did not directly penetrate into the snow samples
 258 but also through the air space of the pores. As a result, the reflection of microwave
 259 power on the interface, which was caused by the relative permittivity mismatch
 260 between the air and the sample led to limited heating efficiency. As the frequency of
 261 18 kHz was in the range of the optimal snow heating frequency between 10 and 100
 262 kHz depending on the snow density (Bader and Kuroiwa, 1962; Polder and Van
 263 Santen, 1946; Evans, 1965), the efficiency of the heating samples was usually higher
 264 for lower density. This effect is confirmed by Fig. 5 showing the heating efficiency and
 265 the complex dielectric constant of dry snow at $T = 0 \text{ }^{\circ}\text{C}$ for various snow sample. The
 266 error bars indicate the measured uncertainty of the experimental setup. Ice had the
 267 lowest heating efficiency with the highest extracted permittivity value of $\epsilon_i'' = 30.65$,
 268 similar to literature values of $\epsilon_i'' = 30.93$ at 18 kHz [Fujita et al., 2000].

269 The start of water percolation was between 5 - 12 water volume fraction depending on
 270 the snow density. Dense snow absorbed more microwave energy leading to higher
 271 liquid water content in a snow sample in a short time. The temporal evolution of the
 272 liquid water mass and volume fraction based on the measured power for the different
 273 snow samples (Fig. 6) increased with time and the influence of snow density was



274 observed. At the maximum of consumed power $P_{\text{RMS}}(t)$ a water mass and volume
 275 fraction of 7.1 and 6.1, 6.7 and 8.8, 8.7 and 15.4, and 0.4 and 0 for snow density of
 276 (a) 438 kg m^{-3} , (b) 539 kg m^{-3} , (c) 612 kg m^{-3} , and (d) 917 kg m^{-3} was reached. Table
 277 3 shows the estimated water mass and volume fraction and time of the different snow
 278 sample at the reversal point of the measured power, indicating the start of water
 279 percolation.

280 The created water led to a stronger rounding of the ice crystals and the effect of fast
 281 wet snow metamorphism was observed where a growth in size of snow crystals was
 282 identified (Colbeck and Davidson, 1973). Figure 7 shows preferential spots of water
 283 accumulation inside the snow structure. Blue indicates the ice structure and orange
 284 shows the water part. The snow sample with an initial density of around 682 kg m^{-3}
 285 was heated to induce a volume water content of 16 %. A volume water content of
 286 around 13.3 % was extracted from the difference in the micro-CT scans before and
 287 after the experiments. This rounding effect is also shown in an insight in the snow
 288 heating process by a microscopy image illustrated in Fig. 8. The photography on the
 289 left shows a snow structure of dry snow before and on the right after the experimental
 290 run.

291 4. Discussion

292 Our major experimental results are summarized in Fig. 4 and 6, and in Table 2 and 3.
 293 The dominant sources of absolute errors in the measurement of the water mass and
 294 volume fraction in the snow were the snow density and the inaccuracy in the power
 295 measurement. Especially, at snow densities below 450 kg m^{-3} this might cause
 296 deviations of $\pm 1 \%$ in the water mass and volume fraction measurement. However, at
 297 higher snow densities the relative errors were considerably less.

298 The snow structure and the water content had a major impact on the electrical
 299 properties showing the same behaviour like in the work of Camp and LeBraque (1992).
 300 In both works the electrical power increased with increasing water content and drops
 301 at one point again. Based on the findings we divided the heating process in three
 302 areas, shown in Fig. 9:



303 **(1) Dry snow:** The heating process up to 0 °C indicated a temperature and snow
304 structure dependency on the measured values. As snow temperature reached the
305 melting point, the surface properties of the ice structure changed markedly and
306 affected the electrical properties. The vibration and the mobility of protons enhanced
307 and influenced the electrical conductivity leading to a decrease of the impedance.
308 Further, at higher density the structural connections between ice crystals were less
309 destructed by the pore volumes. This allowed a higher rate of flow of electric charge
310 leading to a higher electric current. Additionally, the electrical potential between the
311 two copper-plates was less affected by the pore volume leading to a more stable
312 voltage and smaller phase shift between voltage and current. As a result, the electrical
313 conductivity increased resulting in a lower impedance and a higher electrical energy
314 transfer.

315 **(2) Wet snow:** Snow was becoming a particularly complicated medium because the
316 introduction of liquid water caused rapid changes of the important material properties.
317 The temperature stagnated at 0°C and the presence of uniformed distributed liquid
318 water changed the dielectric properties of the snow sample. Additionally, the liquid
319 water layer at the surface allowed the mobility of protons resulting in stronger rate of
320 flow of electric charge and therefore enhanced the electrical conductivity. This reduced
321 the impedance of the two-phase material significantly leading to a decrease of the
322 impedance and phase shift, and an increase in electric current and power.

323 **(3) Water percolation:** The water started to percolate and liquid water accumulated
324 at the bottom of the sample holder. The missing water in the upper part of the sample
325 holder treasured up at the bottom of the sample holder and left empty spots at the top
326 where the density decreased locally. The snow probe was not homogeneous anymore
327 leading to a decrease in the electrical conductivity. As a result, the impedance
328 increased again and the electric power decreased. First camera picture of water
329 percolation after an experimental run is shown in Fig. 10. The sample holder was
330 aligned vertically between the capacitor plates. Water percolated in the upper part of
331 the sample and accumulated at the bottom of the sample holder leading to an
332 inhomogeneous mixture of the sample. This inhomogeneous mixture changed the
333 dielectric properties of the complete sample and affected the heating process. After



334 this state the relative error of the water mass and volume fraction calculation
335 increased.

336 Based on the findings, water percolation occurred over a narrow range of values in
337 coarse-grained snow (see Table 3) and was initiated at around 5-8 % of the mass
338 volume (see Table 3). For high snow densities where the surface-to-volume ratios
339 were small, our results were lower than found by Coléou and Lesaffre (1998).
340 Following reasons are: (1) they approached the retention curve of snow (Yamaguchi
341 et al., 2010) from the opposite site and therefore the physical processes were different,
342 (2) they fully saturated the snow sample for about 5 minutes. Therefore, the surface
343 tension of water had an additional effect, like a suction effect, holding more water in
344 the pore space. In our approach water could not be held immobile as the percolation
345 started earlier at the smooth ice surface.

346 Although the micro-CT measurements (see Fig. 7) showed a snow sample after the
347 water percolation point, still preferential spots of water accumulation inside the snow
348 structure could be seen. Three interesting observations were visible after percolation:
349 (1) No water film around the snow structure but isolated smaller and larger water
350 accumulations were visible indicating that phase change from ice to water were
351 happening on preferential spots on the ice crystal. However, it has to mention that the
352 pixel resolution was too coarse to detect an additional thin water film around the snow
353 structure. The created water led to a stronger rounding of the ice crystals and the
354 dendritic structure further disappeared. Nevertheless, no big change in grain shape
355 was observable due to the high density. (2) The gravity had no influence on the
356 orientation of the accumulated water on the ice crystal. It is apparent that the water
357 was uniformly distributed on the single ice crystals. The water droplets were too small
358 to be distracted by the gravity. (3) Single water accumulation links between single
359 neighbouring ice crystals can be seen. The refreezing of the snow sample after the
360 experiment led to single crystals agglomeration and a growth in size of snow crystals
361 (Colbeck and Davidson, 1973).

362 The electrical heating procedure developed to incrementally melt snow in order to vary
363 the water content and to analyse the created water non-destructive in a micro-CT
364 worked very well. Improving the experimental setup that the frequency can be
365 increased to the GHz-MHz regime for a short period of time, the exact dielectric snow



property based on the snow morphology and water content can be extracted. This will allow to improve remote sensing and field measurements on the snow-water-equivalent (Ambach and Denoth, 1972, Koch et al., 2014).

5. Summary and Conclusion

We designed, fabricated, and tested an experimental setup for in-situ time-lapse nondestructive investigation of water percolation in snow using the electrical properties of snow. Frequency heating close to the relaxation frequency of ice was applied to slowly increase the water content uniformly in the snow sample until liquid water started to percolate. By measuring the temperature and the applied power, the water content in the snow sample at each timestep was deduced. This new instrument allows to elucidating the starting point of water percolation based on measured electrical and morphological properties of the snow. The setup and the obtained results can be used to precisely forecast the run-off time of different density snowpacks and to investigate the mechanical properties, water movements, surface friction, adhesion, and liquid-water measurements, for wet snow and ice.

The experimental observation showed three different heating processes affecting the dielectric properties of snow for different densities: (1) dry snow heating process up to 0 °C indicating a temperature and snow structure dependency of the dielectric property of snow. At warmer temperature, slightly higher complex dielectric constant were measured having higher discrepancy for more dense snow; (2) wet snow heating at stagnating temperature of 0°C and the presence of uniform distributed liquid water changes the dielectric properties and therefore reduces the impedance of the two-phase material significantly until the starting point of water percolation; and (3) the start of water percolation is between 5-12 water volume fraction depending on the snow density. After this point the snow sample has an inhomogeneous mixture where liquid water treasures up at the bottom of the sample holder and is leaving bigger pores in the upper part leading to an increase of overall impedance of the snow sample.

Our results and conclusions indicate that there is a need for additional validation. Specially, it would be crucial to not only look at the density but also at the specific surface area of the snow at a given density which also affects the capillary forces and



397 therefore the starting point of water percolation. Ideally, the entire snow sample will be
398 tomographically measured before the experiment to extract the morphological
399 parameters. The primarily micro-computer tomography (CT) result (Fig. 7) shows first
400 promising visualization of the preferred spots of liquid water in three-dimensional
401 space without destroying the snow structure. However, more detailed measurements
402 are needed to make stronger statements about preferential spots of water
403 accumulations inside the snow sample.

404

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Table 1: Density of the snow samples and the corresponding voltage U_{RMS} , current I_{RMS} , and phase shift φ_{RMS} at the start of the experiment (init), reaching 0 °C (dry-wet) and the point where the power is maximum (peak).

Density (kg m ⁻³)	U_{RMS} (V)			I_{RMS} (mA)			φ_{RMS} (°)		
	init	dry-wet	peak	init	dry-wet	peak	init	dry-wet	peak
427	325.5	325.6	326.9	0.81	0.82	1.21	57.4	57.3	48.7
438	332.6	327.2	328.0	0.90	0.90	1.66	55.9	55.7	41.4
465	328.0	328.3	328.1	1.14	1.16	1.83	52.2	52.2	40.6
465	329.4	330.1	329.9	1.10	1.13	1.81	52.4	52.1	40.7
539	339.1	329.3	327.8	1.23	1.29	2.58	52.8	51.0	35.2
612	331.3	332.0	327.0	1.55	1.65	3.76	49.5	48.8	31.5
917	336.5	327.9	313.8	2.73	3.41	4.27	46.9	34.5	22.4



Table 2: Density of the snow samples and the corresponding impedance U_{RMS} and power P_{RMS} at the start of the experiment (init), reaching 0 °C (dry-wet) and the point where the power is maximum (peak).

Density (kg m ⁻³)	R_{RMS} (kΩ)			P_{RMS} (W)		
	init	dry-wet	peak	init	dry-wet	peak
427	403.4	396.9	269.4	0.14	0.14	0.26
438	368.4	362.0	197.5	0.17	0.17	0.41
465	287.8	282.4	179.2	0.23	0.23	0.46
465	300.4	291.1	182.3	0.22	0.23	0.45
539	275.5	254.8	127.3	0.25	0.27	0.69
612	213.4	213.4	87.3	0.33	0.36	1.04
917	123.1	123.1	73.5	0.63	0.92	1.24

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549 **Table 3:** Density of the snow samples and the corresponding heating time and the
 550 water mass and volume fraction where water starts to percolate.

Density (kg m ⁻³)	Heating time (min)	Water mass fraction (%)	Water volume fraction (%)
427	94.5	4.1	3.3
438	81.1	6.4	5.2
465	51.2	4.3	4.1
465	55.2	4.6	4.2
539	58.2	5.8	7.3
612	54.5	7.5	12.9
917	8.79	0.3	0

551



552 **Figure captions:**

553 **Figure 1:** The experimental setup consisting of three functional blocks (1) low voltage
 554 circuit to generate the sinusoidal signal and amplify the energy output, (2) high voltage
 555 circuit to transform the low primary voltage to a high secondary voltage, and (3) design
 556 of the sample holder between the high voltage capacitor plates.

557 **Figure 2:** (Top) Illustration of the snow heating device. The setup includes a function
 558 generator, an audio amplifier and a plastic box with all the high voltage parts. The lid
 559 of the box is secured by a safety switch. (Bottom) An illustration of the inner part of the
 560 box is shown. It illustrates the high voltage parts with the 60 mm capacitor.
 561 Additionally, the CT sample holder with the 34 mm capacitor is shown.

562 **Figure 3:** Typical measured temperature $T(t)$, current $I_{RMS}(t)$, voltage $U_{RMS}(t)$, and
 563 phase shift $\phi(t)$ profile of a heating process for snow density of (a) 438 kg m^{-3} , (b) 539
 564 kg m^{-3} , (c) 612 kg m^{-3} , and (d) 917 kg m^{-3} .

565 **Figure 4:** Typical measured temperature $T(t)$, impedance $R_{RMS}(t)$ and power $P_{RMS}(t)$,
 566 profile of a heating process for snow density of (a) 438 kg m^{-3} , (b) 539 kg m^{-3} , (c) 612
 567 kg m^{-3} , and (d) 917 kg m^{-3} .

568 **Figure 5:** Heating efficiency and the complex dielectric constant of dry snow at $T = 0$
 569 $^{\circ}\text{C}$ for various snow sample.

570 **Figure 6:** The temporal evolution of the liquid water mass and volume fraction based
 571 on the measured power for snow density of (a) 438 kg m^{-3} , (b) 539 kg m^{-3} , (c) 612 kg
 572 m^{-3} , and (d) 917 kg m^{-3} .

573 **Figure 7:** 3D micro-computer tomography (CT) picture to visualize the water content
 574 in snow after water percolation. The scanned image has a volume of $200 \times 200 \times 20$
 575 voxels ($3.6 \text{ mm} \times 3.6 \text{ mm} \times 0.36 \text{ mm}$). Blue indicates the ice structure and orange shows
 576 the water part.

577 **Figure 8:** Photography under the microscope to illustrate the liquid water content in
 578 the wet snow sample: (left) snow structure of snow before the experimental run, (right)
 579 the same snow sample after 2 hours with an estimated liquid-water content of 12 wt%.



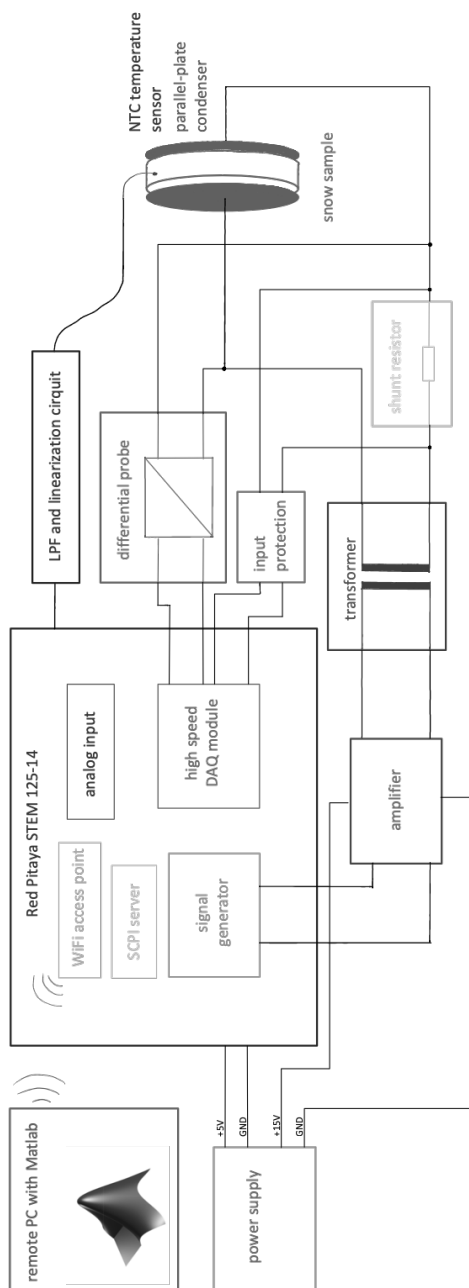
580 **Figure 9:** Dividing the heating process in three different processes: (1) dry snow
581 heating process up to 0 °C indicating a temperature and snow structure dependency
582 on the measured values; (2) wet snow heating at stagnating temperature of 0°C and
583 the presence of uniform distributed liquid water changes the dielectric properties of
584 the snow sample; and (3) starting point of water percolation in the snow sample
585 introducing an inhomogeneous mixture where liquid water treasures up at the bottom
586 of the sample holder and is leaving bigger pores in the upper part.

587 **Figure 10:** Visualization of water percolation after an experimental run. The sample
588 holder was aligned vertically between the capacitor plates. Water percolated in the
589 upper part of the sample and accumulated at the bottom of the sample holder leading
590 to an inhomogeneous mixture of the sample affecting the heating process of the
591 sample.

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Figure 1

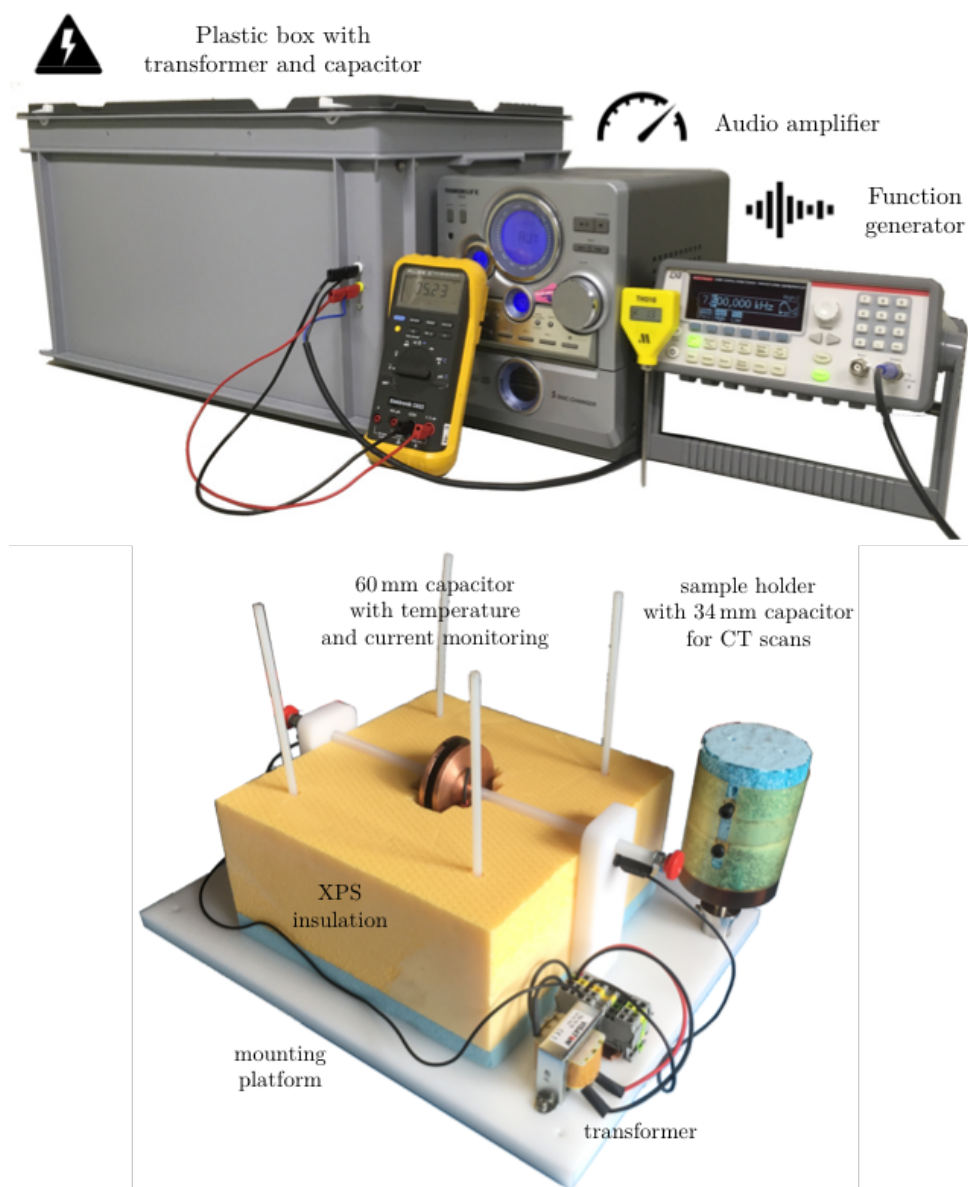


Figure 2

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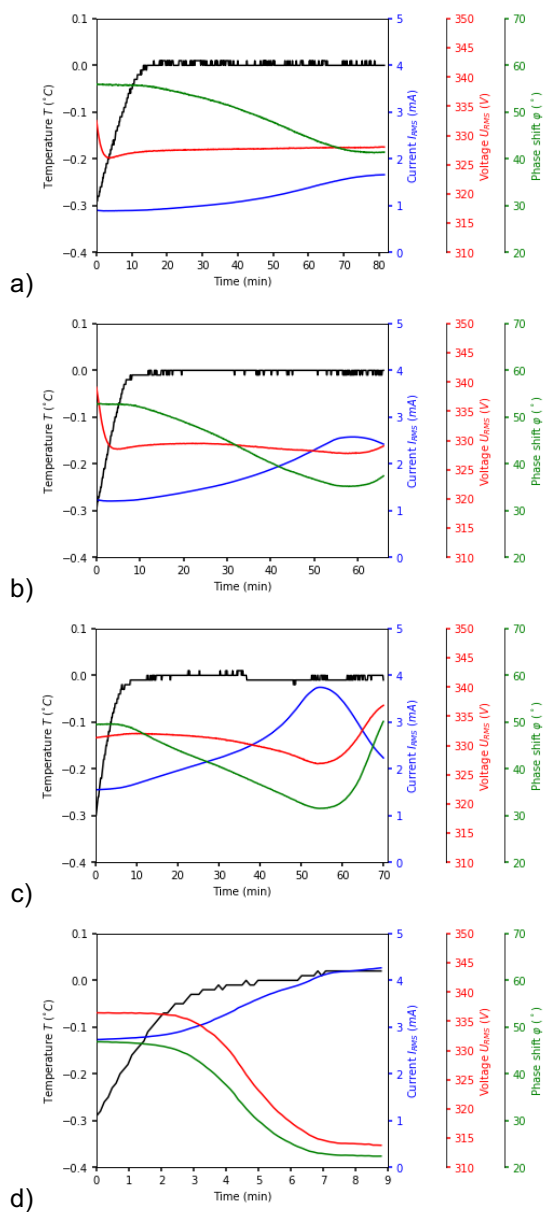


Figure 3

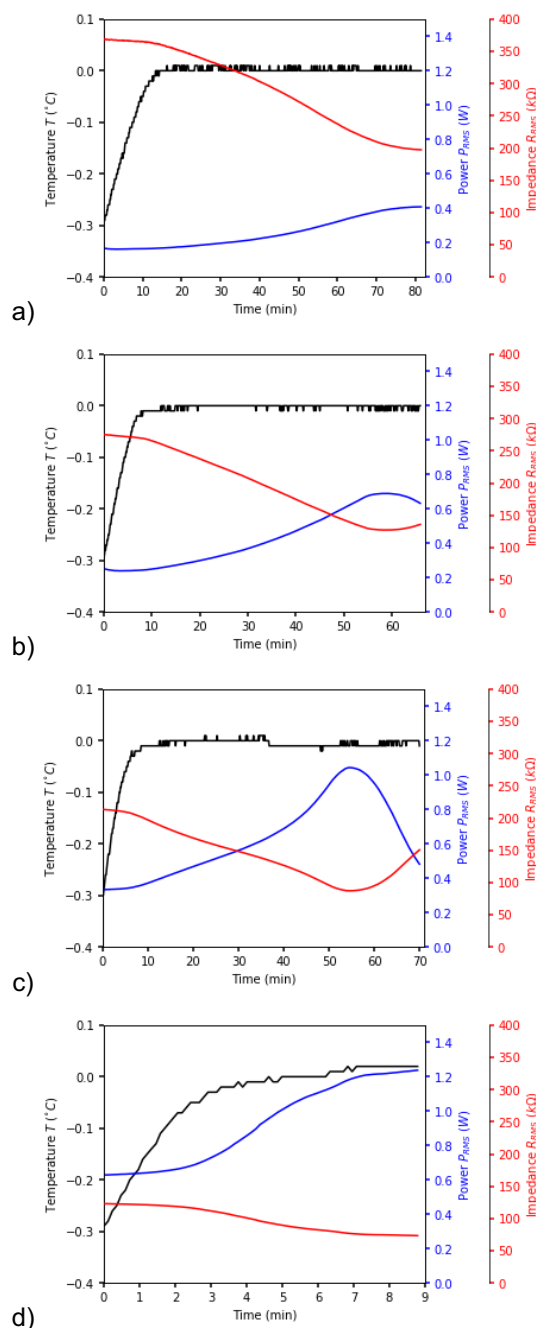


Figure 4

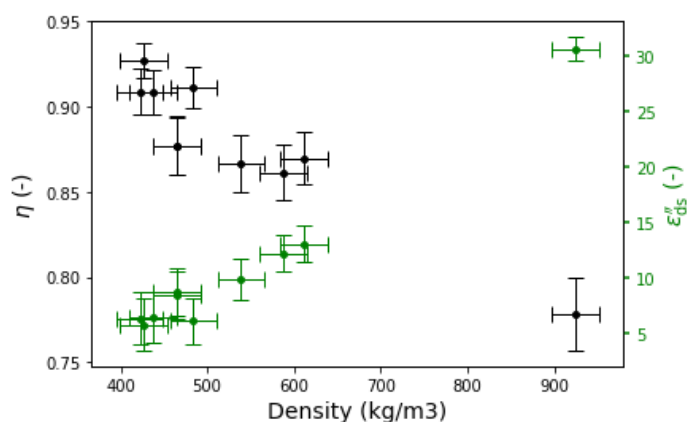


Figure 5

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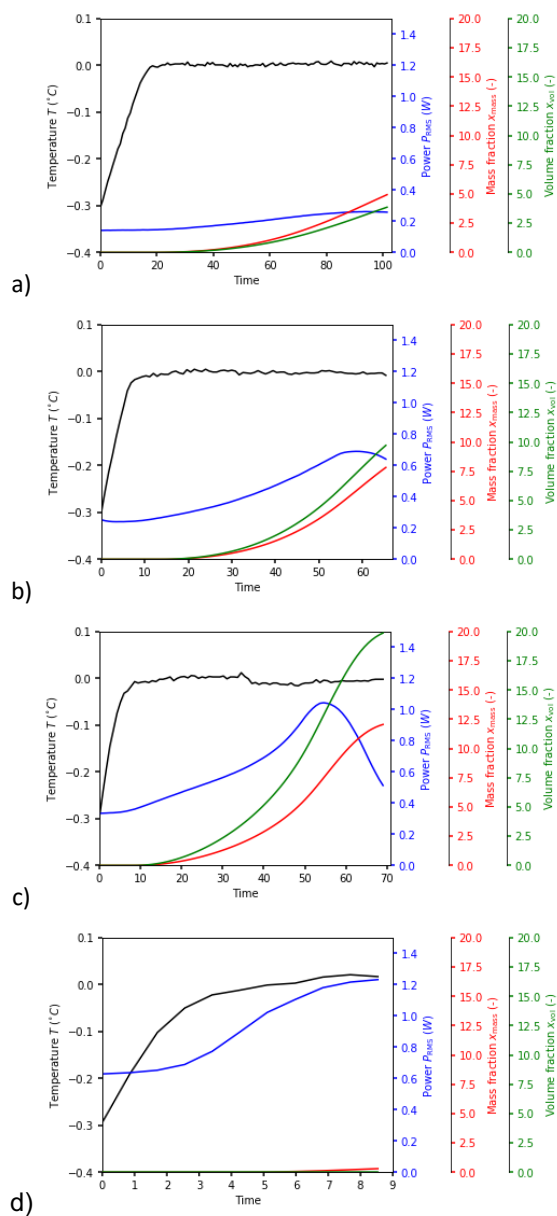


Figure 6

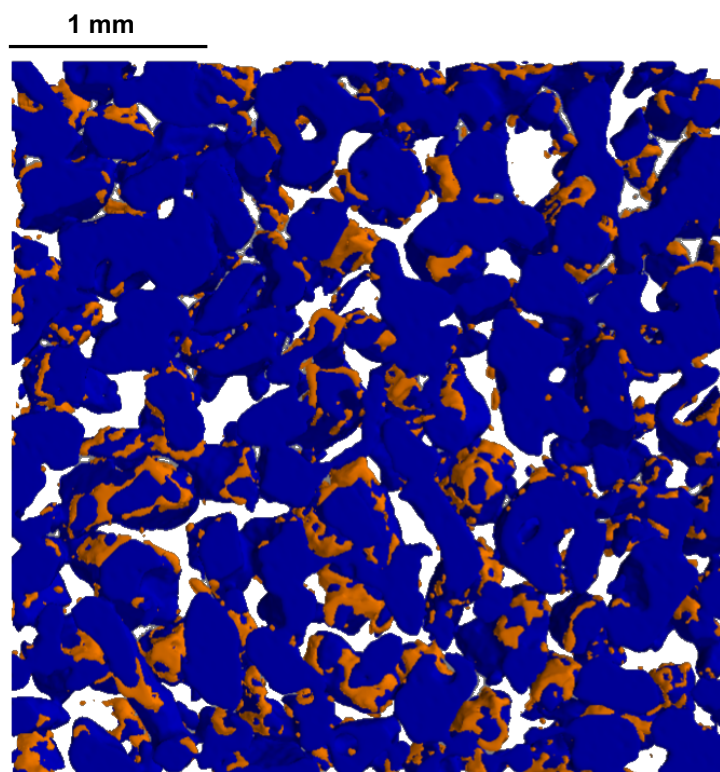
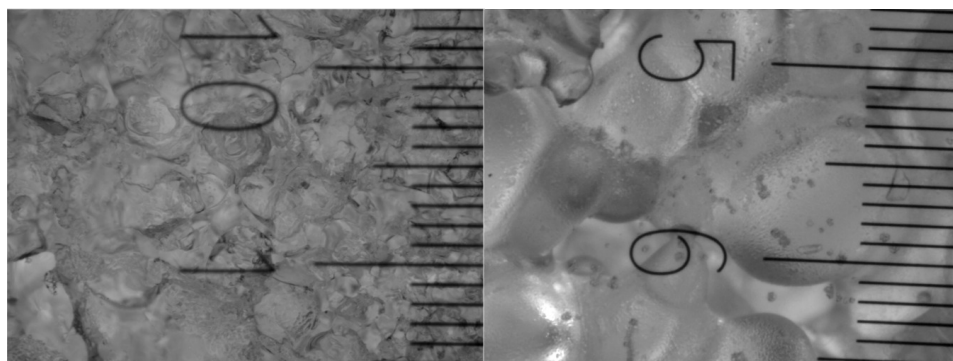


Figure 7

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Figure 8

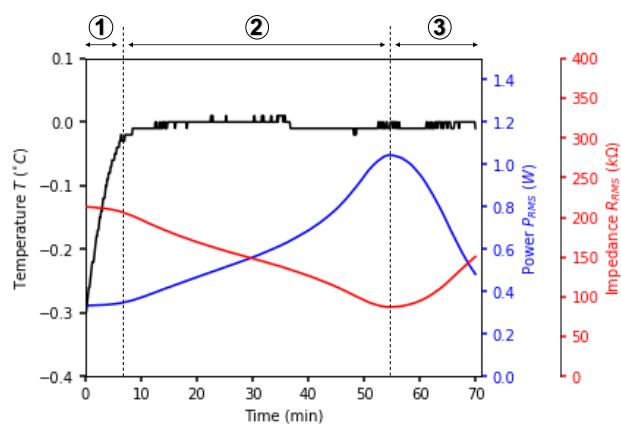


Figure 9

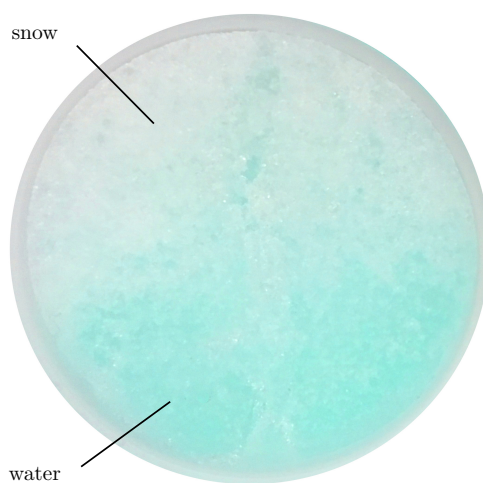


Figure 10

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