



# A local model of snow-firn dynamics and application to Colle Gnifetti site

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**Abstract.** The regulating role of glaciers on catchment run-off is of fundamental importance in sustaining people living in low lying areas. The reduction in glacierized areas under the effect of climate change disrupts the distribution and amount of run-off, threatening water supply, agriculture and hydropower. The prediction of these changes requires models that integrate hydrological, nivological and glaciological processes. In this work we propose a local model that combines the nivological and glaciological scales, developed with the aim of a subsequent integration in hydrological distributed models. The model was derived from mass balance, momentum balance and rheological equations and describes the formation and evolution of the snowpack and the firn below it. The model was applied at the site of Colle Gnifetti (Monte Rosa massif, 4400–4550 m a.s.l.). We obtained an average net accumulation of  $0.26 \cdot 10^3 \text{ kg m}^{-2} \text{ y}^{-1}$  to be compared with the observed net annual accumulation that increases from about  $0.15 \cdot 10^3 \text{ kg m}^{-2} \text{ y}^{-1}$  to about  $1.2 \cdot 10^3 \text{ kg m}^{-2} \text{ y}^{-1}$  moving from the north facing to the south facing slope. The model results confirm the strong influence of wind on snow accumulation and densification, observed also from ice cores. The conserved precipitation is made up mainly of snow deposited between May and September, when temperatures above melting point are also observed. Even though the variability of annual snow accumulation is not well reproduced by the model, the modelled and observed firn densities show a good agreement up to the depth reached by the model with the available input data.

## 1 Introduction

Glacier ice covers almost 16 million  $\text{km}^2$  of the Earth's surface, of which it is estimated that only 3 % is retained by the mountains outside the polar region (Benn and Evans, 2010). Despite this small percentage the amount of water stored in mountain glaciers plays a key role in sustaining people living in low lying areas (Adhikary, 1993), influencing run-off on a wide range of temporal and spatial scales (Jansson et al., 2003; Huss et al., 2010). Storing water coming from precipitation in winter and delaying the time in which it reaches the river network, they sustain streamflow in hotter and drier periods when precipitation is lacking and when it is most needed for agriculture and as drinking water (Fountain and Tangborn, 1985; Hagg et al., 2007). Jost et al. (2012) found in upper Columbia river basin (Canada) covered for only 5 % by glaciers, that ice melt contributes up to 25 % and 35 % to streamflow respectively in August and September and between 3 % and 9 % to total streamflow. In high mountain river basins of the northern Tien Shan (Central Asia), with areas of glaciation higher than



25 30–40 %, glacier melt contribution is 18–28 % of annual run-off but it can increase to 40–70 % during summer (Aizen et al., 1996).

The reduction of glacier volume observed over the past 150 years (Vaughan et al., 2013; Hock et al., 2019) will result in a change in the present distribution and amount of water storage and release with implications in all aspects of watershed management (Hock et al., 2005) with consequent high economic impacts (Huss et al., 2010). The prediction of these changes is  
 30 therefore fundamental in order to assess and reduce their impacts, optimizing consequently the management of water resources. To accomplish this task, models that integrate hydrological, nivological and glaciological components and that consider a variable glacier extension and the transient response of glacier to climate change are required (Luo et al., 2013).

Despite their importance, fully integrated glacio-hydrological catchment models are not common in literature (Wortmann et al., 2019). A keyword search in Scopus carried out the 7<sup>th</sup> of August 2020 produced 21803 results using only the keyword  
 35 “hydrological modelling” that reduced to 288 adding the keyword “glacier”. The combination of “hydrological modelling” and “glacier mass balance” produced 65 results and the combination of “hydrological modelling” with “glacier mass balance” and “glacier dynamics” 11 results. Some examples of glacio-hydrological models are provided by the works of Huss et al. (2010); Naz et al. (2014); Seibert et al. (2018) and Wortmann et al. (2019).

Wortmann et al. (2019) grouped the main problems of glacio-hydrological models in two categories: integration and scale.  
 40 With integration problems they refer to the simplified or absent description of the remaining catchment hydrology in models that describe in detail glacier processes. The decrease in the fraction of ice covered areas requires a proper description of both components also in basins that in the present are highly glacierized. Another aspect is the integration of nivological and glaciological components: a joint simulation of glacier mass balance and snow accumulation and melt is required in order to avoid inconsistencies (Jost et al., 2012; Naz et al., 2014). The problems of scale arise from the different resolutions  
 45 required by glacial, nivological and hydrological processes. Physically based models that consider all glacier processes (mass balance, subglacial drainage and ice flow dynamics) are often too computationally expensive to be used in a combined glacio-hydrological model that considers the entire catchment. In addition they are characterized by a complexity higher than the one of many semi-distributed hydrological models. It is therefore necessary to develop glacier models with a degree of complexity similar to the one of hydrological models but that are still able to reproduce the important processes (Seibert et al., 2018).

50 In the present work we give our contribution proposing a local model that integrates the nivological and glaciological components and that could be potentially integrated in a hydrological model. The model follows the transformation of snow into firn and glacier ice under the influence of temperature, precipitation and wind speed. It consists of six differential equations derived from mass balance, momentum balance and rheological equations that estimate the snowpack and firn characteristics (depth and density of snow and firn, depth of water and ice inside the snowpack). The equations that describe the snowpack  
 55 are derived from the work of De Michele et al. (2013) and later Avanzi et al. (2015), modified in order to take into account the contribution of wind erosion and the mass exchange between snow and firn. To model the firn component, the densification model proposed by Arnaud et al. (2000) was used. In order to test the model a high altitude site, Colle Gnifetti, belonging to the Monte Rosa massif was chosen. Due to the lack of precipitation data a simple procedure to reconstruct them using two lower altitude stations is also proposed.



60 The manuscript is organized in the following way: we provide the model in Sec. 2; illustrate the case study in Sec. 3; give the results in Sec. 4 and discussion in Sec. 5. The conclusions are given in Sec. 6.

## 2 Methodology

In this section, firstly the snowpack model, proposed by De Michele et al. (2013) and later modified by Avanzi et al. (2015), with the addition of the contribution of wind to snow transport is illustrated and secondly the model with the integration of  
 65 snow and firn processes is presented.

### 2.1 Snow model

The snowpack is modelled, according to De Michele et al. (2013) and Avanzi et al. (2015), as a mixture of dry and wet constituents. The solid deformable skeleton, composed by snow grains and pores, has a total volume  $V_S$  with unitary area, height  $h_S$ , mass  $M_S$  and density  $\rho_S$ . The liquid water inside the pores has a volume  $V_W$  with unitary area, height  $h_W$ , mass  
 70  $M_W$  and constant density  $\rho_W = 1000 \text{ kg m}^{-3}$ . The iced water inside the pores due to refreezing has a volume  $V_{MF}$  with unitary area, height  $h_{MF}$ , mass  $M_{MF}$  and constant density  $\rho_i = 917 \text{ kg m}^{-3}$ . It is also possible to define the bulk snow density ( $\rho$ ), snow water equivalent ( $SWE$ ) and volumetric liquid water content ( $\theta_W$ ) as  $\rho = (\rho_S h_S + \rho_W h_W + \rho_i h_{MF})/h$ ,  $SWE = (\rho h)/\rho_W$  and  $\theta_W = h_W/h$  where  $h$  is the height of the snowpack equal to  $h = h_S + \langle h_{MF} + h_W - \phi h_S \rangle$  (Avanzi et al., 2015) in which  $\langle \rangle$  are the Macaulay brackets that provide the argument if this is positive and zero otherwise and  $\phi$  is the  
 75 porosity.

The model solves the mass balance for the dry and liquid mass of the snowpack and the momentum balance and rheological equation for the solid deformable skeleton, resulting in four Ordinary Differential Equations (ODEs) in the variables  $h_S$ ,  $h_W$ ,  $h_{MF}$  and  $\rho_S$ . The mass fluxes considered are (1) solid precipitation events, snow melt and wind erosion for the dry snow mass, (2) rain events, snow melt, melt-freeze inside the snowpack and run-off for the liquid mass and (3) melt-freeze for the mass  
 80 of ice. The dry snow density is obtained considering (1) a densification due to overburden stress, (2) a densification due to drifting snow compaction and (3) a densification due to addition of new mass. Accordingly, the following system is obtained (see Appendix A for the derivation of the system and the detailed description of the terms in the equations):

$$\frac{dh_S}{dt} = -\frac{h_S}{\rho_S} \frac{d\rho_S}{dt} + \frac{\rho_{NS}}{\rho_S} s - (I \cdot a)(T_A - T_\tau) - \frac{Q}{\rho_S} \quad (1a)$$

$$\frac{dh_W}{dt} = r + \frac{\rho_S}{\rho_W} (I \cdot a)(T_A - T_\tau) + (I^* \cdot e \cdot a)(T_A - T_\tau) - \alpha \cdot K_W \quad (1b)$$

$$85 \quad \frac{dh_{MF}}{dt} = -\frac{\rho_W}{\rho_i} (I^* \cdot e \cdot a)(T_A - T_\tau) \quad (1c)$$

$$\frac{d\rho_S}{dt} = (c \cdot A_1 \cdot U) \rho_S \exp(-B \cdot (T_\tau - T_S) - A_2 \cdot \rho_S) + \frac{\rho_{NS} - \rho_S}{h_S} s \quad (1d)$$

In Eq. (1a),  $\rho_{NS}$  is the density of fresh snow ( $\text{kg m}^{-3}$ ),  $s$  is the solid precipitation rate ( $\text{m h}^{-1}$ ),  $a$  is a calibration parameter ( $\text{m h}^{-1} \text{ } ^\circ\text{C}^{-1}$ ),  $T_A$  and  $T_\tau$  are the air temperature and the threshold temperature for melting ( $^\circ\text{C}$ ),  $I$  is the product of a binary



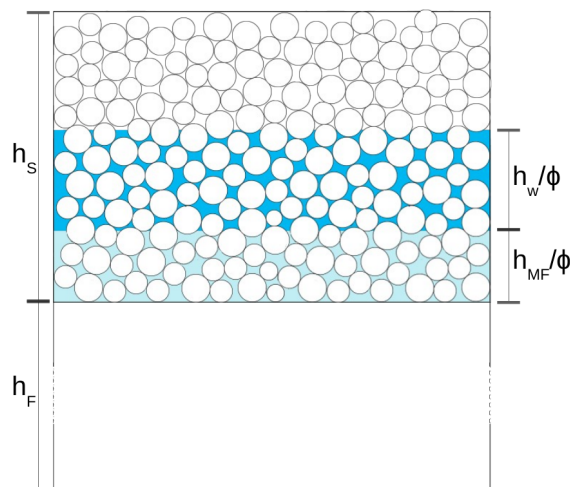
function equal to 1 if  $T_A \geq T_\tau$  and of a function of  $h_S$ , namely  $\frac{h_S}{h_S+k}$ , which tends to 0 with  $h_S$ , with  $k = 0.01$  m (Avanzi et al., 2015) and  $Q$  is the mass of snow eroded by wind ( $\text{kg m}^{-2} \text{h}^{-1}$ ). In Eq. (1b),  $r$  is the liquid precipitation rate ( $\text{m h}^{-1}$ ),  $e$  is a calibration parameter,  $I^*$  is equal to  $\frac{h_W}{h_W+k}$  if  $T_A < T_\tau$  and to  $\frac{h_{MF}}{h_{MF}+k}$  if  $T_A > T_\tau$  (Avanzi et al., 2015),  $\alpha = 1.9692 \cdot 10^9 \text{ m}^{-1} \text{h}^{-1}$  (DeWalle and Rango, 2008) and  $K_W$  is the intrinsic permeability of water in snow ( $\text{m}^2$ ). In Eq. (1d),  $c = 0.10 \cdot 3600 \text{ s h}^{-1}$ ,  $A_1 = 0.0013 \text{ m}^{-1}$ ,  $A_2 = 0.021 \text{ m}^3 \text{kg}^{-1}$ ,  $B = 0.08 \text{ K}^{-1}$  (Liston et al., 2007),  $U$  is the wind speed contribution ( $\text{m s}^{-1}$ ) and  $T_S$  is the average snow temperature ( $^\circ\text{C}$ ) obtained assuming thermal equilibrium between the constituents and a bilinear profile of temperature through depth (see De Michele et al. (2013) for further details).

With respect to the model by De Michele et al. (2013) and Avanzi et al. (2015), the version presented in this work includes the effect of wind both on mass balance and densification. This is important when the model is applied to high altitude sites: Haeberli and Alean (1985), in fact, suggested that a major part of the decrease of accumulation with altitude in the Alps, that occurs above about 3500 m a.s.l., may be due to wind effects.

In analogy with solid transport, snow is mobilized only when wind velocity at the surface exceeds a given threshold that depends on physical proprieties of the surface snowpack (Li and Pomeroy, 1997). Once transport begins, snow can travel in two main modes: saltation and suspension (Déry and Taylor, 1996; Pomeroy et al., 1997).

The total snow transport  $Q$  is computed by the model with the following assumptions: (1) only snow erosion occurs and no deposition of snow eroded in other positions is present; (2) measured wind speed is always referred to 10 m height, i.e. the height of the snow on the ground is neglected; (2) wind cannot erode snow that experienced a temperature greater than  $0^\circ\text{C}$  for the presence of ice crusts or wet layers following Vionnet et al. (2018). These last two assumptions allow to compute the series of total snow transport  $Q$  decoupled from the snow model since knowledge of snow height is not required.

To implement the routine, we proceeded as explained in the following. When the first solid precipitation event occurs in a time step, the amount of new snow on the ground at the end of the time step,  $S_A$  ( $\text{kg m}^{-2} \text{h}^{-1}$ ), is obtained subtracting from the mass of solid precipitation the snow transport calculated for that time step, where snow transport is zero if the wind speed is lower than the threshold wind speed. This value is saved along with the time of deposition and  $\rho_{NS}$  of the event. During the subsequent steps, the threshold is recomputed updating the average temperature and the time since deposition and the theoretical snow transport for the time step is obtained. The actual snow transport is then obtained considering four different situations: (1) a new snow event occurs in the time step. In this case  $S_A$  is moved into a vector  $\mathbf{S}_R$  with its time of deposition and  $\rho_{NS}$ . If  $Q < \rho_{NS} \cdot s$  then  $S_A$  is recomputed as  $\rho_{NS} \cdot s - Q$ , vice versa previously deposited events are eroded as in step (4); (2)  $T_A > 0^\circ\text{C}$ . In this case  $S_A$  and  $Q$  are set to  $0 \text{ kg m}^{-2} \text{h}^{-1}$  and all the old snow events memorized in  $\mathbf{S}_R$  are removed; (3)  $T_A < 0^\circ\text{C}$  and  $Q < S_A$ . In this case  $S_A$  is set to  $S_A = S_A - Q$ ; (4)  $T_A < 0^\circ\text{C}$  and  $Q > S_A$ . In this case, if  $\mathbf{S}_R$  has no elements,  $Q$  is set equal to  $S_A$  and  $S_A$  to  $0 \text{ kg m}^{-2} \text{h}^{-1}$ , otherwise the difference between  $Q$  and  $S_A$  is subtracted from the most recent event in  $\mathbf{S}_R$ , given that wind speed is higher than the threshold recomputed with the characteristics of that event, and this event is removed from  $\mathbf{S}_R$ . This is repeated until an event in  $\mathbf{S}_R$  that cannot be eroded by wind is encountered or the total amount of snow eroded in that time step reaches  $Q$ . In the latter case the actual transport is  $Q$  while in the former  $Q$  is given by the total amount of snow eroded before reaching the non erodible layer. The new  $S_A$  is the amount of snow associated with the last event considered.



**Figure 1.** A column of snow and firn.

## 2.2 Model of snow-firn dynamics

125 The model is composed of two layers: the snowpack (see Sec. 2.1) and the firn. The firn is modelled as a single impermeable layer of volume  $V_F$  with unitary area, height  $h_F$ , mass  $M_F$  and density  $\rho_F$  (Fig. 1). The amount of water percolation inside the firn, neglected in this version of the model, varies greatly depending on the type of glacier. At high altitudes, where maximum temperatures are rarely positive, the effects of percolation due to melting are limited (Smiraglia et al., 2000); at the cold site of Colle Gnifetti, where the model was applied, percolation occurs only in the few centimetres below the surface and it does not  
 130 involve previous year layers (Alean et al., 1983).

In order to separate snow from firn we refer to its original definition that defines firn as snow that has survived one melt season (Cuffey and Paterson, 2010).

### 2.2.1 Equations of the model

The model consists of six ODEs: the four equations of the snow model with in addition the mass balance and momentum  
 135 balance of firn. The mass variation of firn is obtained considering firn melt, the effects of precipitation on firn and the transformation of snow in firn at the end of each water year. The firn densification rate is obtained considering a densification due to overburden stress and a densification due to addition of new mass. Accordingly, the resulting system is as follows (see



Appendix A for the derivation of the system and the detailed description of the terms in the equations):

$$\frac{dh_S}{dt} = -\frac{h_S}{\rho_S} \frac{d\rho_S}{dt} + \frac{\rho_{NS}}{\rho_S} s - (I \cdot a)(T_A - T_\tau) - \frac{Q}{\rho_S} - \sum_i \frac{h_S}{dt} \delta(t - t_i) \quad (2a)$$

$$140 \quad \frac{dh_W}{dt} = r + \frac{\rho_S}{\rho_W} (I \cdot a)(T_A - T_\tau) + (I^* \cdot e \cdot a)(T_A - T_\tau) - \alpha \cdot K_W - \sum_i \frac{h_W}{dt} \delta(t - t_i) \quad (2b)$$

$$\frac{dh_{MF}}{dt} = -\frac{\rho_W}{\rho_i} (I^* \cdot e \cdot a)(T_A - T_\tau) - \sum_i \frac{h_{MF}}{dt} \delta(t - t_i) \quad (2c)$$

$$\frac{dh_F}{dt} = -\frac{h_F}{\rho_F} \frac{d\rho_F}{dt} - (I_F \cdot a)(T_A - T_\tau) \delta(h_S) + \frac{\rho_W}{\rho_F} r \delta(h_S) \langle T_\tau - T_A \rangle + \sum_i \frac{\rho}{\rho_F} \frac{h}{dt} \delta(t - t_i) \quad (2d)$$

$$\frac{d\rho_S}{dt} = (c \cdot A_1 \cdot U) \rho_S \exp(-B \cdot (T_\tau - T_S) - A_2 \cdot \rho_S) + \frac{\rho_{NS} - \rho_S}{h_S} s \quad (2e)$$

$$\frac{d\rho_F}{dt} = \left. \frac{d\rho_F}{dt} \right|_{comp} + \sum_i \frac{\rho - \rho_F}{h_F} \left( \frac{h}{dt} \right) \delta(t - t_i) \quad (2f)$$

145 The last terms in Eqs. (2a–2c) move, at the end of each melt season, the remaining snowpack (if present) in the firm layer;  $t_i$  is the time instant at the end of water year  $i$  and  $\delta(\cdot)$  is the Dirac delta function equal to 1 when the argument is 0 and 0 otherwise. In Eq. (2d),  $I_F$  is the product of a binary function equal to 1 if  $T_A \geq T_\tau$  and of a function of  $h_F$ , namely  $\frac{h_F}{h_F + k}$ , which tends to 0 with  $h_F$ , with  $k$  specified above.

In Eq. (2f), the densification due to compaction ( $\left. \frac{d\rho_F}{dt} \right|_{comp}$ ) is obtained adopting the model of Arnaud et al. (2000) with  
 150 some of the modifications proposed by Bréant et al. (2017). Accordingly,

$$\left. \frac{d\rho_F}{dt} \right|_{comp} = \begin{cases} \gamma \frac{\max(P, 10^4 \text{ Pa})}{(\rho_F/\rho_i)^2} \left( 1 + \frac{0.5}{6} - \frac{5}{3} \frac{\rho_F}{\rho_i} \right) \rho_i & \rho_F/\rho_i \leq D_0 \\ 5.3A \cdot ((\rho_F/\rho_i)^2 D_0)^{1/3} \left( \frac{a_c}{\pi} \right)^{1/2} \left( \frac{4\pi \cdot P \cdot \rho_i}{3a_c \cdot Z \cdot \rho_F} \right)^3 \rho_i & D_0 < \rho_F/\rho_i \leq D_c \\ 2A \cdot \frac{\rho_F(1 - \rho_F/\rho_i)}{\rho_i(1 - (1 - \rho_F/\rho_i)^{1/3})^3} \left( \frac{2(P - P_b)}{3} \right)^3 \rho_i & D_c < \rho_F/\rho_i \leq 0.95 \\ \frac{9}{4}A \cdot (1 - \rho_F/\rho_i)(P - P_b)\rho_i & \rho_F/\rho_i > 0.95 \end{cases} \quad (3)$$

In the first stage,  $P$  is the overburden pressure (Pa) and  $\gamma = \gamma' \exp\left(-\frac{Q_1}{R_G(T_F + 273.15)}\right)$  in which  $R_G$  is the gas constant,  $Q_1$  an activation energy equal to  $48 \cdot 10^3 \text{ J mol}^{-1}$ ,  $\gamma'$  a parameter (estimated in Sec. 4.2) and  $T_F$  is the average temperature of firm ( $^\circ\text{C}$ ). In the second stage,  $A = A_0 \exp\left(-\frac{Q_2}{R_G(T_F + 273.15)}\right)$  with  $A_0 = 2.84 \cdot 10^{-11} \text{ Pa}^{-3} \text{ h}^{-1}$ ,  $a_c$  is the average contact area,  
 155  $Z$  is the number of particle contacts (see Appendix A for the expression of  $a_c$  and  $Z$ ),  $Q_2$  is an activation energy and  $D_0$  is the relative density at the transition between the first stage and the second stage. The value of  $Q_2$  was set to  $60 \cdot 10^3 \text{ J mol}^{-1}$ , as in the model of Arnaud et al. (2000), since it is the typical activation energy associated with self-diffusion of ice. However, at warmer temperature (i.e. higher than  $-10 \text{ }^\circ\text{C}$ ) a higher activation energy is required to best fit density profiles with firm densification models (Cuffey and Paterson, 2010; Arthern et al., 2010; Jacka and Jun, 1994). A discussion of the thermal  
 160 variation of the creep parameter and the impact of the different sintering mechanisms on it can be found in Bréant et al. (2017). Lastly, in the third stage,  $P_b$  is the pressure inside the bubbles equal to  $P_b = P_c \frac{(\rho_F/\rho_i)(1 - D_c)}{D_c \cdot (1 - \rho_F/\rho_i)}$  with  $D_c$  and  $P_c$  the relative density and pressure at the transition between second and third stage.



The model of Arnaud et al. (2000) was chosen because it explicitly represents stress, it models non-steady conditions and it includes a more physical description of densification. Nevertheless, the model can be implemented also with a different  
 165 firm densification model, given that it represents non steady conditions. In particular, the model of Arnaud et al. (2000), that was developed for polar sites, may not be suitable for temperatures too close to 0 °C. Anyway, the possibility to apply a firm densification model developed for polar sites also to warmer firm of mountain glaciers, possibly with some modifications, is shown in Huss (2013) where the model of Herron and Langway (1980), developed for the Greenland ice sheet, was recalibrated and adapted for temperate/polythermal firm.

## 170 2.2.2 Temperature profile

The energetic description of the volume was simplified assuming the constituents in thermal equilibrium and assuming a bilinear profile of temperature through depth. Temperature was assumed to vary linearly from surface temperature  $T_0$  to the mean annual firm temperature (MAFT) at the depth  $z_M$  at which seasonal variation of temperature is negligible. At depths higher than  $z_M$ , temperature was kept constant and equal to MAFT. In cold glaciers the value of MAFT is close to the mean  
 175 annual air temperature (MAAT) when melt water percolation is limited (Suter et al., 2001) while in temperate glaciers it is equal to the melting temperature (Cuffey and Paterson, 2010). Surface temperature was fixed equal to  $T_A$  if  $T_A < 0^\circ\text{C}$  and zero elsewhere. Already Huss (2013) assumed a bilinear profile of temperature in order to study temperate firm densification, fixing  $z_M$  to 5 m since it is the typical penetration of winter air temperature.

## 2.3 Numerical model

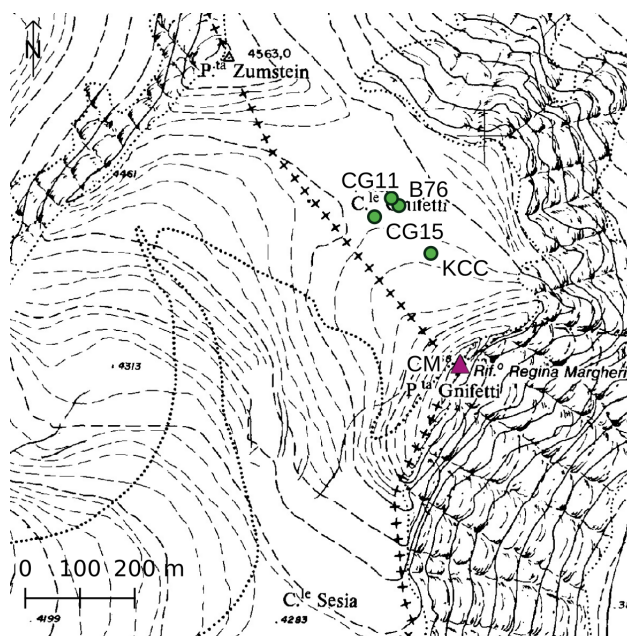
180 The model was solved using the forward Euler finite-difference scheme with a fixed time step,  $\Delta t$ , of one hour. To compute the last terms in Eqs. 1d and 2f, also when  $h_S$  and  $h_F$  are zero, these terms were calculated, following De Michele et al. (2013), as  $\frac{\rho_{NS}(t)-\rho_S}{h_S(t)+s(t)\Delta t} s(t)$  and  $\frac{\rho(t)-\rho_F}{h_F(t)+h(t)\Delta t} \frac{h(t)}{\Delta t}$ . The model requires the calibration of the two parameters governing the rate of melting of firm and snow and the refreezing inside the snowpack, namely  $a$  and  $e$ . If data are available, a different value for  $a$  could be calibrated for firm and snow.

## 185 3 Study area and data

### 3.1 Study area

The site of Colle Gnifetti (CG) is part of the summit ranges of the Monte Rosa massif, Swiss/Italian Alps. It is the uppermost part of the accumulation area of Grenzgletscher and it forms a saddle that lies between Signalkuppe (4554 m a.s.l.) and Zumsteinspitze (4563 m a.s.l.) at an altitude of 4400–4550 m a.s.l. (Lüthi and Funk, 2000) (Fig. 2). The glacier at Colle  
 190 Gnifetti has a thickness between 60 and 120 m and a MAFT of  $-14^\circ\text{C}$  (Wagenbach et al., 2012). The regime is that of a high altitude site, i.e. nearly persistent sub-zero air temperature, a high precipitation total and high wind speed (Suter et al., 2001).





**Figure 2.** The site of Colle Gnifetti and the location of the ice cores considered in the present work. Source of the basemap: Piedmont Geoportal

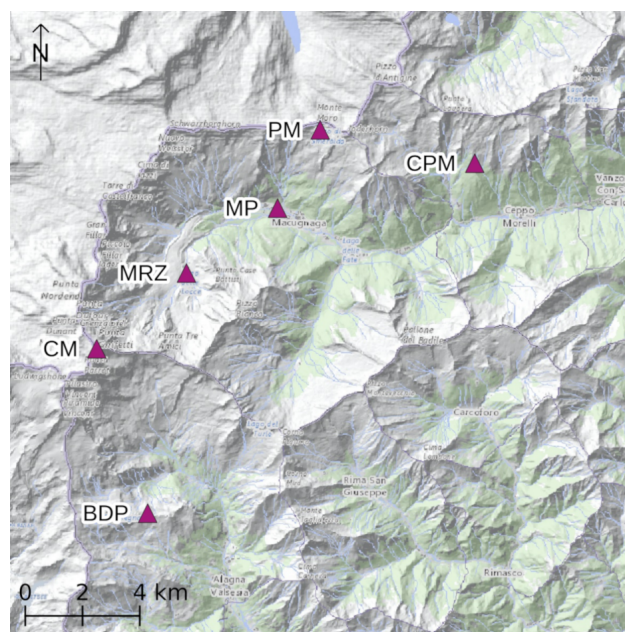
A mean annual precipitation of  $2.7 \cdot 10^3 \text{ kg m}^{-2} \text{ y}^{-1}$  with an interannual variability of  $0.8 \cdot 10^3 \text{ kg m}^{-2} \text{ y}^{-1}$  (Mariani et al., 2014) was estimated for the period 1961–1993 from a core extracted at upper Grenzgletscher (Eichler et al., 2000).

Even though the site is characterized by high precipitation totals, accumulation in the saddle is considerably lower and highly variable over the glacier surface due to wind erosion, with values ranging from about  $0.15 \cdot 10^3 \text{ kg m}^{-2} \text{ y}^{-1}$  to  $1.2 \cdot 10^3 \text{ kg m}^{-2} \text{ y}^{-1}$  depending on the wind exposure (Alean et al., 1983; Lüthi and Funk, 2000; Licciulli et al., 2020). Alean et al. (1983) measured the accumulation at CG between 17 August 1980 and 23 July 1982 with a network of 30 stakes. For the period between 14 August 1981 and 23 July 1982 the mass balance was negative in all the stakes due to wind erosion, while the net accumulation of water year 1980–1981 varied between  $+0.04 \cdot 10^3 \text{ kg m}^{-2} \text{ y}^{-1}$  and  $+1.18 \cdot 10^3 \text{ kg m}^{-2} \text{ y}^{-1}$  with the highest values on south facing slopes. This occurs because the enhanced melting and refreezing causes the formation of wet layers and ice crusts and because higher temperatures are associated with a faster densification and both these aspects reduce the possibility of wind to erode snow. This results also in the fact that almost all the snow that survives the melt season comes from summer events (Bohleber et al., 2018; Schöner et al., 2002).

### 3.2 Data collection

All meteorological data belong to Arpa Piemonte stations (Fig. 3) and they are summarized in Table 1. Information about installed instruments can be found at <https://www.arpa.piemonte.it>. Hourly data of air temperature and average wind speed at Capanna Regina Margherita (CM) were used as input for the model, daily data at Macugnaga Pecetto (MP) and Macugnaga





**Figure 3.** Location of the meteorological stations used: Capanna Regina Margherita (CM), Macugnaga Rifugio Zamboni (MRZ), Macugnaga Pecetto (MP), Ceppo Morelli (CPM), Passo del Moro (PM) and Bocchetta delle Pisse (BDP). Source of the basemap: Arpa Piemonte Geoportal

Rifugio Zamboni (MRZ) were used to reconstruct precipitation series at Colle Gnifetti, hourly data of air temperature along with daily data at Macugnaga Rifugio Zamboni were used to calibrate the parameter  $a$  and hourly and daily air temperature data at Macugnaga Pecetto, Passo del Moro (PM), Bocchetta delle Pisse (BDP) and Ceppo Morelli (CPM) were used to infill missing temperature data at Capanna Regina Margherita. In order to compute the snow transport, we considered the average wind speed instead of maximum wind speed, to avoid overestimation due considering a wind speed equal to the maximum one during all the hour.

The station of Capanna Regina Margherita, whose data were used to run the snow-firn model, was installed in 2002 by the Piedmont Region at the Regina Margherita Hut as part of a project that aimed to study the interaction between synoptic flow and orography. With its 4560 m of altitude it can be considered the highest meteorological station in Europe and its wind speed series can be considered representative of the synoptic conditions (Martorina et al., 2003). Due to its recent installation, the use of these data limits the length of the simulation and the number of cores with which our results can be compared. Nevertheless, we believe that, given the peculiar characteristics of the station, the use of these data may give added value to this study.

In Table 2 ice core data are reported (Fig. 2). KCC, CG11 and CG15 were used to validate the model and B76 was used as a reference steady-state depth-density profile while computing the value of parameter  $\gamma'$ .



**Table 1.** Meteorological data employed in the case study ( $p$  stands for precipitation,  $SD$  for snow depth,  $T_A$  air temperature,  $u$  average wind speed and  $s$  fresh snow). All stations belong to Arpa Piemonte network. Water years are identified by the first year, e.g. 2008 is water year 2008–2009.

Station name	Altitude (m a.s.l.)	UTM X WGS84 (m)	UTM Y WGS84 (m)	Variable	Aggregation	Period used
Macugnaga Pecetto (MP)	1360	419251	5091486	$p, SD, T_A, s$	Daily	1 October 2002– 30 September 2019
Macugnaga Rifugio Zamboni (MRZ)	2075	416068	5089214	$p, SD, T_A, s$	Daily	1 October 2007– 30 September 2019
Macugnaga Rifugio Zamboni (MRZ)	2075	416068	5089214	$T_A$	Hourly	Water year: 2008, 2009, 2011, 2014, 2016, 2017
Capanna Regina Margherita (CM)	4560	412930	5086564	$T_A, u$	Hourly	1 October 2002– 13 August 2013
Passo del Moro (PM)	2820	420739	5094227	$T_A$	Daily	1 October 2002– 30 September 2007
Passo del Moro (PM)	2820	420739	5094227	$T_A$	Hourly	November 2002, September 2007
Bocchetta delle Pisse (BDP)	2410	414709	5080807	$T_A$	Daily	1 October 2002– 30 September 2007
Bocchetta delle Pisse (BDP)	2410	414709	5080807	$T_A$	Hourly	November 2002, September 2007
Ceppo Morelli (CPM)	1995	426141	5093057	$T_A$	Daily	1 October 2002– 30 September 2007
Ceppo Morelli (CPM)	1995	426141	5093057	$T_A$	Hourly	November 2002, September 2007

### 3.3 Data handling

The model requires in input a continuous series of air temperature, precipitation and wind speed.

Following the comparison presented by Henn et al. (2013), to fill missing hourly temperature data at Capanna Margherita, MicroMet procedure (Liston and Elder, 2006) was adopted for gap smaller than 24 hours and a long-term lapse rate approach with five stations (CM, MP, CPM, PM, BDP) was adopted for longer gaps. In the period 1 October 2002–13 August 2013, 0.37 % of hourly temperature data were missing. After MicroMet procedure 0.23 % remained missing and were substituted with a long-term lapse rate approach.



**Table 2.** Ice core data employed in the case study.

Name	Drilling date	Mean annual accumulation ( $10^3 \text{ kg m}^{-2} \text{ y}^{-1}$ )	Data source
B76	1976	0.37	Gäggeler et al. (1983)
CG15	2015	0.45	Sigl et al. (2018)
CG11	2011	0.41	Ardenghi (2012)
KCC	2013	0.22	Licciulli et al. (2020)

To fill missing wind speed data, MicroMet procedure was used for gaps smaller than 24 hours. For gaps longer than 24 hours, the missing period was substituted with the corresponding measurement of another year. The year was chosen computing the frequency duration curve of wind speed for each year and selecting a year whose behaviour was similar to the average one. In the period 1 October 2002–13 August 2013, 1.3 % of data were missing, that reduced to 1.17 % after MicroMet procedure. Longer gaps were present in three years, namely 2002, 2007 and 2012. The sensitivity of the year chosen was tested computing the net accumulation for the three water years; the largest difference was obtained for water year 2011–2012 that showed a variability between  $0.44 \cdot 10^3$  and  $0.50 \cdot 10^3 \text{ kg m}^{-2} \text{ y}^{-1}$ .

Precipitation at CG was reconstructed starting from the corrected daily precipitation series at MP and MRZ. The corrected precipitation series at the two stations was obtained combining the information coming from precipitation series (measured by rain gauges) and fresh snow series (an estimation of snow fallen in the 24 hours before 8 AM of each day obtained from snow depth data). Precipitation data are provided both as the total precipitation fallen in the day and as the total precipitation fallen in the 24 hours before 9 AM; to better compare precipitation with fresh snow data, the latter was chosen. To obtain total precipitation, firstly the processed series of fresh snow in water equivalent, called  $s_w$ , was obtained as follows: (1) missing data of fresh snow in days with average daily air temperature greater than  $0^\circ \text{C}$  were set to zero (fresh snow reported at 8 AM was associated with the previous day temperature); (2) all other missing data were estimated from the difference between the previous and next non missing snow depth data; (3) fresh snow was transformed in water equivalent computing fresh snow density following Anderson (1976). Secondly, total and liquid precipitation series, called  $p$  and  $p_r$  respectively, were reconstructed as follows: (1) missing data of precipitation during days with average air temperature lower than  $0^\circ \text{C}$  were set to zero; (2) a first estimation of rain was obtained setting  $p_r$  equal to  $p - s_w$  if the difference was positive and zero otherwise and setting it missing if  $p$  or  $s_w$  were missing; (3) total precipitation  $p$  was recomputed summing  $p_r$  and  $s_w$ ; (4) every missing value of  $p$  in one station corresponding to a non missing value in the other one was substituted estimating an average increase of precipitation with altitude:

$$m_p = \frac{1}{n} \sum_{i=1}^n \frac{p_{i,MP} - p_{i,MRZ}}{z_{i,MP} - z_{i,MRZ}} \quad (4)$$



where  $z$  is the altitude and  $m_p$  was calculated considering only days with precipitation; (5) precipitation data still missing after these steps were set to zero; (6) rain was recomputed as in step 3.

In order to extrapolate precipitation at the altitude of CG, it is necessary to take into account that precipitation does not increase indefinitely with altitude but at one point along the slope it reaches a maximum, after which it starts decreasing. The altitude of maximum precipitation is the result of two opposite phenomena that are at the base of orographic precipitation: the enhanced moisture condensation due to air lifting and the exponential decrease in the amount of available moisture with height following Clausius–Clapeyron (Roe, 2005). We therefore decided to assume a linear increase of precipitation up to an altitude  $z_m$  and then to keep precipitation constant. Since studies about the altitude of maximum precipitation for the Monte Rosa massif were not found, the formula proposed by Alpert (1986) for a bell shaped mountain was adopted. The formula is derived from the continuity equation of water vapour and it links  $z_m$  to the mountain height  $H$  and the temperature lapse rate  $\Gamma$  as follows:

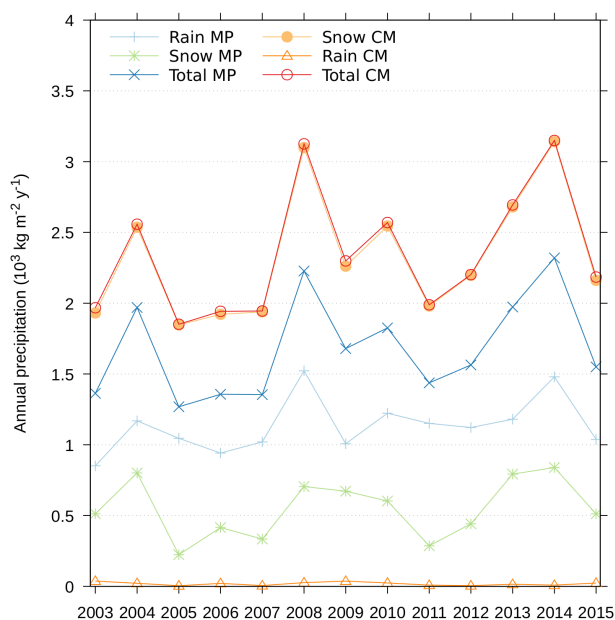
$$z_m = \frac{3H}{(4 - 0.12 \cdot \Gamma H + 0.0036 \cdot \Gamma^2 H^2)^{1/2} + 0.06 \cdot \Gamma H + 2} \quad (5)$$

In this case,  $H = 4634$  m and  $\Gamma = 0.0058$  °C m<sup>-1</sup> using the average value between CM and MP.

Given  $z_m$  and  $m_p$  (from Eq.4), precipitation at CG can be estimated for each day  $i$  from the series  $p$  of MP as follows:  $p_{i,CM} = p_{i,MP} + m_p(z_m - z_{MP})$  if  $p_{i,MP} > 0$  mm d<sup>-1</sup> and  $p_{i,CM} = 0$  mm d<sup>-1</sup> otherwise. Precipitation was then divided equally over the 24 hours and a threshold of 1 °C was chosen to distinguish between solid and liquid precipitation, since this is the value generally found in Europe (Jennings et al., 2018).

### 3.4 Model's parameters

The parameter  $e$  requires data of snow density or snow water equivalent to be calibrated. Since they were not available, its value was set to 0.2, that is the median value obtained by Avanzi et al. (2015) for a Japanese site. The parameter  $a$  was calibrated running the snow model without the wind contribution at MRZ with an hourly time step. For each water year in Table 1 (i.e. 2008-2009, 2009-2010, 2011-2012, 2014-2015, 2016-2017 and 2017-2018) we estimated the parameter using least squares on daily snow depth data and minimizing the objective function with a population-evolution-based algorithm, namely SCE-UA (Shuffled Complex Evolution-University of Arizona) (Duan et al., 1992, 1993). To evaluate the model, for each calibrated parameter, we computed the NSE (Nash-Sutcliffe Efficiency) between observed and modelled snow depth for all water years except the one used to calibrate the parameter. The median value of  $a$  was selected and used in the snow-firn model. The parameter  $\gamma'$ , that governs firn densification rate, was estimated running the firn densification model in a steady-state condition (Bader, 1954), setting  $T_F = -14.1$  °C (Haeberli and Funk, 1991), the mean accumulation rate and surface density to the one of B76 ice core (see Table 2),  $D_0 = 0.56$  (Bréant et al., 2017),  $P_c = 740 \cdot 10^2$  Pa (Lüthi and Funk, 2000) and  $D_c = 0.85$  since the precise value is not known at CG (Lüthi and Funk, 2000). The other parameters of the snow-firn model that require to be specified are  $z_M$  and MAFT set to 5 m and  $-14.1$  °C (Haeberli and Funk, 1991) and the grain radius  $R$  that influences the threshold wind speed. It is defined as  $R = 3/(\rho_i SSA)$  where  $SSA$  is the specific surface area in m<sup>2</sup> kg<sup>-1</sup>.  $SSA$  was computed adopting the parametrization of Domine et al. (2007) for recent snow,  $SSA = -16.051 \ln(\rho_s \cdot 10^{-3}) + 7.01$ .



**Figure 4.** Annual precipitation at Macugnaga Pecetto (MP), obtained from the processed precipitation series, and at Capanna Margherita (CM), obtained from the reconstructed precipitation series.

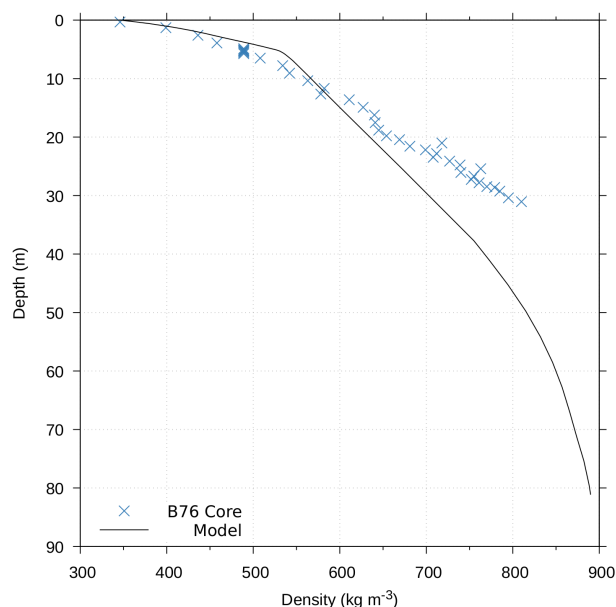
## 285 4 Results

### 4.1 Reconstructed precipitation at CM

From Eqs. (4, 5) we obtained  $m_p = 0.004 \text{ mm d}^{-1} \text{ m}^{-1}$  and  $z_m = 2547 \text{ m}$ . The altitude of maximum precipitation was found away from the crest as it is typical for large mountains (Roe, 2005). The reconstructed annual totals are reported in Fig. 4 subdivided in liquid and solid events. The average for the period 2003–2015 is  $2.35 \cdot 10^3 \text{ kg m}^{-2} \text{ y}^{-1}$  that can be confronted  
 290 with the average for the period 1961–1993 of  $2.7 \cdot 10^3 \text{ kg m}^{-2} \text{ y}^{-1}$  estimated from the upper Grenzgletscher core (see Section 3.1). An average annual precipitation of  $3.5 \cdot 10^3 \text{ kg m}^{-2} \text{ y}^{-1}$  and  $1.7 \cdot 10^3 \text{ kg m}^{-2} \text{ y}^{-1}$  would have been estimated using, respectively, the altitude of Capanna Margherita as  $z_m$  and the processed series of Macugnaga Pecetto not increased with altitude.

### 4.2 Parameters' estimation

295 We obtained a median value of the parameter  $a$  of  $3.84 \cdot 10^{-4} \text{ m h}^{-1} \text{ }^\circ\text{C}^{-1}$  with an average NSE of 0.71 in validation. The value is in the range obtained by Avanzi et al. (2014) for a selection of forty sites within the SNOTEL network. The estimated value of the parameter  $\gamma'$  is  $1.26 \text{ Pa}^{-1} \text{ h}^{-1}$  with the resulting profile reported in Fig. 5.



**Figure 5.** Firn densification model for steady-state conditions and density profile of B76 ice core.

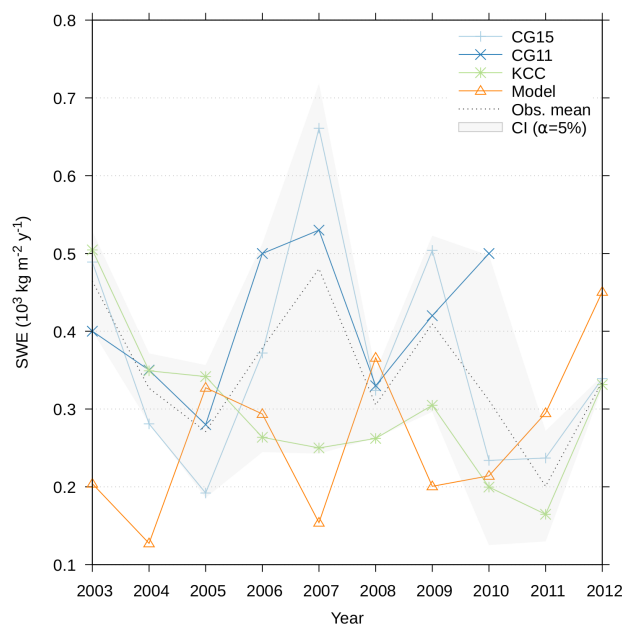
**Table 3.** Modelled and observed mean ( $\mu$ ) and standard deviation ( $\sigma$ ) of the accumulation rate for the period 2003–2012.

	$\mu$ ( $10^3 \text{ kg m}^{-2} \text{ y}^{-1}$ )	$\sigma$ ( $10^3 \text{ kg m}^{-2} \text{ y}^{-1}$ )
Model	0.26	0.10
CG11	0.41	0.09
KCC	0.30	0.09
CG15	0.36	0.15

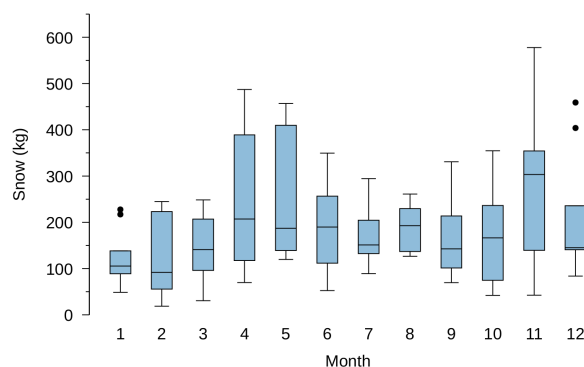
### 4.3 Snow accumulation

The annual accumulation obtained from the snow-firn model is reported in Fig. 6 along with the values retrieved from the three available ice cores, the average value of the observations and its 95% confidence interval. The Root Mean Square Error (RMSE) between the model and the average of the observations is equal to  $0.17 \cdot 10^3 \text{ kg m}^{-2} \text{ y}^{-1}$ , while the modelled and observed average annual accumulation and standard deviation are reported in Table 3.

In order to better understand the characteristics of the accumulation at CG the monthly box plot of solid precipitation, snow transport, monthly contribution to annual accumulation and number of hours with  $T_A > 0^\circ \text{C}$ , that in the model correspond to hours with melting, are provided in Figs. 7–10. Since snow is moved into firn at the end of September and wind is not allowed to erode firn, the fraction of conserved snow of September may be overestimated and the snow transport of October



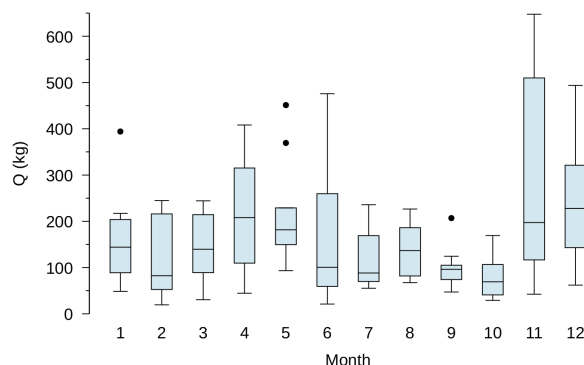
**Figure 6.** Annual accumulation modelled and retrieved from three ice cores. The average of the annual accumulations from ice cores and its 95% confidence interval are also reported.



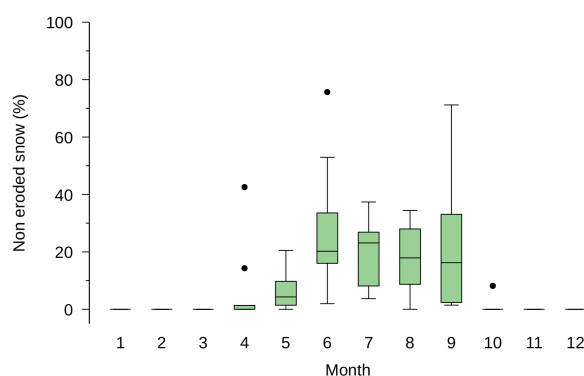
**Figure 7.** Box plot of monthly solid precipitation.

underestimated. We can see that annual accumulation is composed by snow deposited mainly between May and September, with July the month that in average contributes the most. The months in which solid precipitation is conserved are also the months in which temperature goes above the melting point; winter snow, instead, is completely removed.





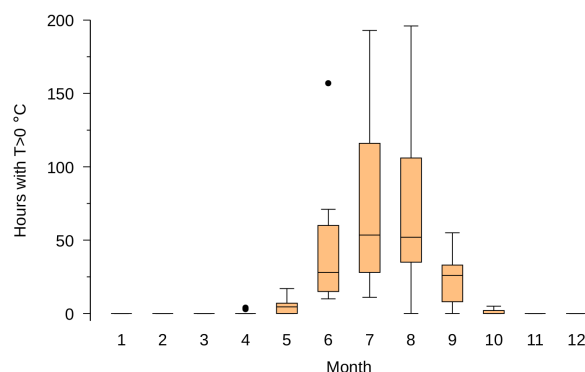
**Figure 8.** Box plot of monthly snow transport.



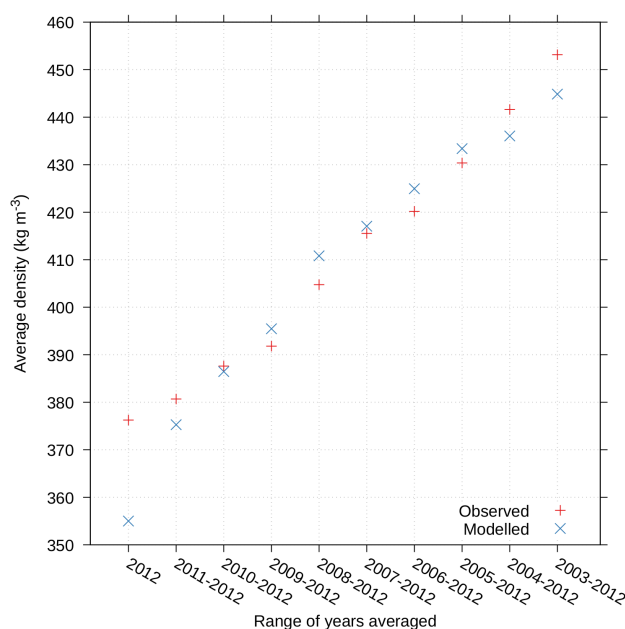
**Figure 9.** Box plot of monthly fraction of conserved solid precipitation.

#### 310 4.4 Firn density

The modelled firn density was confronted with the density estimated from KCC core (Fig. 11). Since the model returns the average density of all the firn column and not the density of each annual layer, to confront them the model was run for an increasing number of years and the corresponding observed density was obtained averaging the density of the layers deposited in the same range of years. The model was always run up to 13 August 2013, the KCC drilling date, in order to reproduce the same conditions experienced by the ice core. The RMSE is  $8.16 \text{ kg m}^{-3}$  with a maximum difference of about  $20 \text{ kg m}^{-3}$  corresponding to the average density of the layer deposited in 2012.



**Figure 10.** Box plot of monthly number of hours with above zero temperatures.



**Figure 11.** Observed and modelled average firn density. The range of years in the x-axis indicates the deposition year of the layers whose density was averaged. The firn densities, modelled and observed, are referred to August 2013.

## 5 Discussion

### 5.1 Snow accumulation

Snow accumulation at CG is characterized by a high spatial variability (Keck, 2001; Licciulli et al., 2020). The difference in net annual accumulation of CG11 and CG15, that are about 50 m apart, ranges from  $+0.13 \cdot 10^3 \text{ kg m}^{-2} \text{ y}^{-1}$  to  $-0.266 \cdot 10^3 \text{ kg m}^{-2} \text{ y}^{-1}$  in the period 2002–2012, while the one of CG15 and KCC, that are about 120 m apart, ranges between



+0.41 · 10<sup>3</sup> kg m<sup>-2</sup> y<sup>-1</sup> and -0.15 · 10<sup>3</sup> kg m<sup>-2</sup> y<sup>-1</sup>. The accumulation is strongly affected by surface topography that in turn is influenced by wind; this results in a quasi random spatial variation and a systematic temporal variation at a given location (Keck, 2001). Given the high variability in the accumulation rate, three ice cores may not be enough to fully represent the site, besides, ice core data are biased due to the fact they are drilled preferentially in the north flank, where accumulation and radiation are lower. While the modelled average annual accumulation is in the range of the ones estimated for the north flank of CG (Licciulli et al., 2020), the model is not able to reproduce the observed spatial variability. This would require to consider the effect of topography on wind speed and the spatial variation in solar radiation. Surface snow temperature was set equal to air temperature, instead of solving the full surface energy balance that would have required a higher availability of data; surface temperatures, in fact, may reach 0 °C also for air temperatures below 0 °C mainly when calm conditions are present or, on the contrary, melting may not occur during positive air temperatures particularly when wind is present (Keck, 2001).

In accordance with the box plot in Figs. 7–10, different works that studied ice cores drilled at CG report that snow accumulation is mainly made up by precipitation of the warm seasons (Wagenbach et al., 1988; Schöner et al., 2002; Bohleber et al., 2013, 2018). Also at Seserjoch (Colle Sesia in Fig. 2), 4300 m a.s.l., where snow height was measured between 1998 and 2000 by Suter et al. (2001), a main accumulation from about April to November, with practically no accumulation in high winter was observed. Figure 9 shows that the conserved fraction of solid precipitation reflects the number of hours with greater than zero temperature rather than the seasonality of precipitation. Accumulation is, in fact, mainly governed by wind erosion (Wagenbach et al., 1988) and the presence of wet layers or ice crusts as well as a faster compaction when temperatures are higher protect snow from wind erosion. This could lead, as already suggested by Alean et al. (1983), to a counterintuitive response in a scenario of greater temperatures, since the increased melting and the reduced fraction of solid events with respect to total precipitation will be accompanied by a reduced snow erosion. An increase of positive net balances may in turn influence ice avalanche activity. Future applications of the model may address the answer of the site in term of snow accumulation under scenarios of climate warming.

## 5.2 Firn density

The observed and modelled densities show a good agreement up to the densities reached by the model, even though to validate the ability of the model to reproduce firn densification up to glacier ice, a longer series of meteorological data is needed. The absence of snow density or water equivalent measures doesn't allow to validate the modelled surface snow density, whose underestimation may be the reason of the difference between observed and modelled density of 2012 firn layer. Surface density at CG is, in fact, difficult to measure and highly variable since it depends on aspect and wind exposure (Licciulli et al., 2020). Wind speed, in fact, affects snow and firn densification as well as snow accumulation when snow drift occurs (Keenan et al., 2020). Its influence was tested running the model neglecting wind contribution  $U$  in Eq. 1d, i.e. fixing its value to 1 m s<sup>-1</sup>, and extracting the same data of Fig. 11. An increase of RMSE from 8.16 kg m<sup>-3</sup> to 12.35 kg m<sup>-3</sup> was obtained with a systematic underestimation of average firn density.



## 6 Conclusions

In this study we have proposed a local model that combines snow and firn dynamics. It consists of six ODEs derived from the mass balance, momentum balance and rheological equations of snow and firn. The model has a parsimonious parametrization, with three parameters ( $a, e, \gamma'$ ) to be estimated. The model requires in input a series of hourly (or sub-hourly) series of precipitation, temperature and wind speed with which the series of snow, water and ice inside the snowpack and firn height along with dry snow and firn density are computed. The model was applied to the site of Colle Gnifetti (Monte Rosa massif, 4400–4550 m a.s.l.) for a period of 10 years. The application of the model to a high altitude site allowed us to explore two main problems: the low availability of measured data and the strong influence of wind on snow accumulation and densification. The modelled average net accumulation is equal to  $0.26 \cdot 10^3 \text{ kg m}^{-2} \text{ y}^{-1}$  against an average precipitation above  $2 \cdot 10^3 \text{ kg m}^{-2} \text{ y}^{-1}$ , with a monthly distribution of the conserved snow that reflects the number of melting events rather than the precipitation seasonality, as observed also from ice cores. The model is not able to reproduce the strong spatial variability of snow accumulation, that would probably require to take in consideration the influence of topography on wind speed and the spatial variation of solar radiation. The modelled density profile shows a good agreement with observed data, even though a longer time series is required to confirm this result for densities up to glacier ice density. The application of the model to other sites with a greater availability of data as well as a sensitivity analysis of the chosen parameters will be carried out for a more robust validation of the model along with the possibility to include it inside a distributed hydrological model.

## Appendix A: Complete description and derivation of the snow-firn model

### A1 Mass balance equations

The mass balance equations of snow ( $M_S$ ), liquid water in snow ( $M_W$ ), iced water in snow ( $M_{MF}$ ), and firn ( $M_F$ ) are as follows:

$$\frac{dM_S}{dt} = P_S - M - Q - E_S \quad (\text{A1a})$$

$$\frac{dM_W}{dt} = P_R + M + F - O - E_W \quad (\text{A1b})$$

$$\frac{dM_{MF}}{dt} = -F - E_{MF} \quad (\text{A1c})$$

$$\frac{dM_F}{dt} = -O_F + P_F + E_S + E_W + E_{MF} \quad (\text{A1d})$$

$P_S$  and  $P_R$  are the mass of solid and liquid precipitation events and they are equal to  $P_S = s \cdot \rho_{NS}$  and  $P_R = r \cdot \rho_W$ . Following Anderson (1976),  $\rho_{NS} = 50 \text{ kg m}^{-3}$  if the air temperature  $T_A < -15^\circ \text{C}$  and  $\rho_{NS} = 50 + 1.7 \cdot (T_A + 15)^{1.5} \text{ kg m}^{-3}$  otherwise.

$M$  is the snow melt mass flux that was computed with a temperature-index approach (Hock, 2003). Accordingly,  $M = (I \cdot a)(T_A - T_\tau)\rho_S$ .

$F$  is the melt freeze mass flux that was modelled with a coupled melt-freeze temperature-index approach. Accordingly,  $F = (I^* \cdot e \cdot a)(T_A - T_\tau)\rho_W$ .



The run-off  $O$  was modelled with a matrix flow approach and it is equal to  $O = \rho_W \alpha K_W$  where  $\alpha = \alpha' (5.47 \cdot 10^5 \text{ m}^{-1} \text{ s}^{-1})$  (DeWalle and Rango, 2008) with  $\alpha'$  a time conversion constant equal to  $3600 \text{ s h}^{-1}$ . Following Colbeck (1972),  $K_W$  was computed as  $K_W = K S^{*3}$  in which  $K$  is the intrinsic permeability of snow in  $\text{m}^2$  and  $S^*$  is the effective saturation degree of the mixture equal to  $S^* = (S_r - S_{r_i}) / (1 - S_{r_i})$  where  $S_{r_i}$  is the irreducible saturation degree equal to  $S_{r_i} = 0.02 \rho_S / (\rho_W \phi)$  (Kelleners et al., 2009) and  $S_r$  is the average saturation degree of the porous matrix equal to 1 when  $h_W \geq \phi h_S$  while  $S_r = h_W / (\phi h_S)$  otherwise (Avanzi et al., 2015). The intrinsic permeability is calculated using the parametrization proposed by Calonne et al. (2012) and it is equal to  $K = 3R^2 \exp(-0.013 \rho_S)$  in which  $R$  is the equivalent sphere radius defined as  $R = 3 / (SSA \rho_i)$  where  $SSA$  is the specific surface area in  $\text{m}^2 \text{ kg}^{-1}$  that was computed by Avanzi et al. (2015) adapting the formula proposed by Domine et al. (2007). Accordingly,  $SSA = -30.82 \ln(\rho_S \cdot 10^{-3}) - 20.60$ . When  $S_r > 0.5$ , to avoid numerical instability, the run-off was calculated with a kinematic wave approximation (De Michele et al., 2013) as  $\rho_W \theta_W h_W^{1.25}$ .

The firm melting  $O_F$ , that may occur only when the snowpack is absent, was modelled with a temperature-index approach and it is equal to  $O_F = (I_F \cdot a)(T_A - T_r) \rho_F \delta(h_S)$ .

$P_F$  is the effect of rain on firm that, when the snowpack is absent, causes an increase of  $M_F$  when  $T_A < 0^\circ \text{C}$  because rainfall is chilled to the firm temperature and a decrease when  $T_A > 0^\circ \text{C}$  because the energy supplied by rain will be used to melt ice. In the first case  $P_F = \rho_W \cdot r$  while in the second case  $P_F$  was set to zero due to its small contribution to mass balance (Doyle et al., 2015).

The terms  $E_S$ ,  $E_W$ ,  $E_{MF}$  move the mass of the snowpack still on the ground at the end of each melt season inside the firm and they are equal to  $E_j = \sum_i \rho_j \frac{h_j}{dt} \delta(t - t_i)$  with  $j = S, MF, W$ .

$Q$  is the mass of snow eroded by wind obtained from snow transport. The latter was computed adopting the parametrization proposed by Pomeroy et al. (1993) as the sum of a transport in saltation and a transport in suspension.

The saltation transport rate  $Q_{salt}$  ( $\text{kg m}^{-1} \text{ s}^{-1}$ ) occurs only when wind exceeds a given threshold and it is computed as follows:

$$Q_{salt} = \frac{0.68 \rho_a u_t^*}{u^* g} (u^{*2} - u_t^{*2}) \quad (\text{A2})$$

where  $\rho_a$  is the atmospheric density ( $\text{kg m}^{-3}$ ) and  $u^*$  and  $u_t^*$  are respectively the atmospheric friction velocity and the friction velocity applied to the snow surface at the transport threshold ( $\text{m s}^{-1}$ ). To move from the measured wind speed  $u$  to  $u^*$ , knowledge of the aerodynamic roughness height  $z_0$  is required. This passage is not straightforward since the value of  $z_0$  during blowing snow events is different from the one during non transport conditions and it depends on friction velocity (Pomeroy and Gray, 1990). In order to avoid an iterative procedure, we adopted the approximation proposed by Pomeroy and Gray (1990). Accordingly,  $u^* \approx 0.02264 u^{1.295}$  and  $z_0 = \frac{0.1203 u^{*2}}{2g}$  where  $u$  is 10 m wind speed ( $\text{m s}^{-1}$ ).

Suspension transport, that occurs only when particles are already in saltation, was computed as follows:

$$Q_{susp} = \frac{u^*}{\kappa} \int_{h^*}^{z_b} \eta(z) \ln\left(\frac{z}{z_0}\right) dz \quad (\text{A3})$$

where  $Q_{susp}$  is in  $\text{kg m}^{-1} \text{ s}^{-1}$ ,  $\kappa$  is the von Kármán constant equal to 0.4,  $h^*$  is the lower boundary for suspension equal to  $h^* = c_H u^{*1.27}$  (Pomeroy and Male, 1992) with  $c_H = 0.08436 \text{ m}^{-0.27} \text{ s}^{1.27}$ ,  $z_b$  is the top of the surface boundary-layer for



suspended snow and  $\eta(z)$  is the mass concentration of suspended snow ( $\text{kg m}^{-3}$ ) at height  $z$ . The mass concentration can be approximate as  $\eta(z) = \eta(z_r) \exp(-A_Q((B_Q u^*)^{-0.544} - z^{-0.544}))$  (Pomeroy and Male, 1992) where  $\eta(z_r)$  is the reference mass concentration for suspension set to  $0.8 \text{ kg m}^{-3}$  (Pomeroy and Male, 1992),  $A_Q$  is equal to  $1.55 \text{ m}^{0.544}$  and  $B_Q$  to  $0.05628 \text{ s}^{-0.544}$ .  $z_b$  was set to 5 m, since its value is typically between 5 m and 10 m (Déry and Taylor, 1996). The exact value is unimportant because of small mass fluxes at this height (Pomeroy et al., 1993). The snow erosion in the control volume of the model was set equal to the sum of these two transports.

The critical threshold, above which snow transport occurs, was computed adopting the formula proposed by He and Ohara (2017). Accordingly, the critical shear stress for snow movement can be computed as:

$$\tau_t = \frac{(8R \cdot C_g \cdot g)(\rho_S - \rho_a) \cos(\pi/3 - S) + (\pi C_c \varsigma) \left(\frac{C}{R^m} t_d\right)^{2/n} \left(\sin(\pi/3 + S) + \left(\frac{C}{R^m} t_d\right)^{1/n}\right)}{2(C_d \sin(\pi/3 - S) + C_l \cos(\pi/3 - S))} \quad (\text{A4})$$

where  $R$  is the grain radius (m),  $t_d$  is the time since deposition in seconds,  $C_c$ ,  $C_d$ ,  $C_g$  and  $C_l$  are dimensionless coefficients set to 1, 4,  $1.3\pi/6$  and 3.4 (He and Ohara, 2017),  $\varsigma$  is the stress caused by cohesion of ice computed as  $\varsigma = 1.51 \exp(0.44(T_A + 9)) + 6.8$  (Hosler et al., 1957) for temperatures between  $-20^\circ\text{C}$  and  $0^\circ\text{C}$  with  $\varsigma$  in  $\text{N m}^{-2}$  and  $T_A$  in  $^\circ\text{C}$  and  $S = \arcsin\left(\left(\frac{C}{R^m} t_d\right)^{1/n}\right)$ .  $C$ ,  $m$  and  $n$  are parameters that influence the rate of ice sintering, modelled following Maeno and Arakawa (2004). Accordingly,  $C = C_0 \exp\left(\frac{-Q_s}{R_G(T_A + 273.15)}\right)$  in which  $R_G$  is the gas constant and  $T_A$  is computed as the average air temperature since deposition,  $C_0 = 4.14 \cdot 10^{19} \text{ m}^3 \text{ s}^{-1}$  and  $Q_s = 1.965 \cdot 10^5 \text{ J mol}^{-1}$ . Finally,  $m$  and  $n$  are empirical parameters set to 2.9 and 5 respectively following the results of He and Ohara (2017). Once the critical shear stress is obtained it is possible to move to critical friction velocity as follows:  $u_t^* = \sqrt{\tau_t / \rho_a}$ .

Given that  $M_j = \rho_j h_j$  and  $\rho_k = \text{const}$  with  $j = S, MF, W$  and  $k = MF, W$ , after some algebra we can move from Eqs. A1a–A1d to Eqs. 2a–2d

## A2 Snow and firm densification

The densification of dry snow due to compaction was modelled adopting the formula proposed by Liston et al. (2007). Accordingly,

$$\frac{d\rho_S}{dt} = (c \cdot A_1 \cdot U) \rho_S \exp(-B \cdot (T_\tau - T_S) - A_2 \cdot \rho_S) \quad (\text{A5})$$

where  $c = 0.10 \cdot 3600 \text{ s h}^{-1}$ ,  $A_1 = 0.0013 \text{ m}^{-1}$ ,  $A_2 = 0.021 \text{ m}^3 \text{ kg}^{-1}$ ,  $B = 0.08 \text{ K}^{-1}$  and  $U$  is the wind speed contribution ( $\text{m s}^{-1}$ ). For wind speeds  $\geq 5 \text{ m s}^{-1}$ ,  $U = E_1 + E_2(1.0 - \exp(-E_3(u_2 - 5.0)))$  with  $E_1$ ,  $E_2$  and  $E_3$  equal to  $5.0 \text{ m s}^{-1}$ ,  $15.0 \text{ m s}^{-1}$  and  $0.2 \text{ m s}^{-1}$ , respectively, and  $u_2$  the wind speed at 2 m height. For wind speed  $< 5 \text{ m s}^{-1}$ ,  $U = 1 \text{ m s}^{-1}$ . Adding the densification due to mass variation (see De Michele et al. (2013)) the total densification rate can be computed as follows:

$$\frac{d\rho_S}{dt} = (c \cdot A_1 \cdot U) \rho_S \exp(-B \cdot (T_\tau - T_S) - A_2 \cdot \rho_S) + \frac{\rho_{NS} - \rho_S}{h_S} s \quad (\text{A6})$$

where we assumed that melting events and snow erosion occur at  $\rho_S = \text{const}$ .

The densification of firm due to compaction is obtained adopting the model of Arnaud et al. (2000) with some of the modifications proposed by Bréant et al. (2017). The model separates the densification of firm into three stages. The first stage is



governed by settling and it is modelled by Bréant et al. (2017) adapting the equation proposed by Alley (1987). The second stage, that starts when the relative density  $D = \rho_F / \rho_i$  equals  $D_0$ , is dominated by power law creep and it is modelled following  
 450 Arzt (1982) and Arzt et al. (1983). Grains are considered as spheres and each sphere is allowed to increase in radius around fixed centres. Starting from an initial radius  $l$ , the new radius  $l'$  (in units of the initial particle radius  $l$ ) is  $l'(D) = (D/D_0)^{1/3}$ . The growth of spheres increases the number of particle contacts  $Z$  from the initial value  $Z_0$  to  $Z(D) = Z_0 + b(l' - 1)$  in which  $b = 15.5$ . The overlap due to the growth of particles produces an excess volume of material. This excess is distributed uniformly around the portion of the surface of the spheres not in contact. From this excess volume, it is possible to calculate the  
 455 new radius  $l''$  as

$$l'' = l' + \frac{4Z_0(l' - 1)^2(2l' + 1) + b(l' - 1)^3(3l' + 1)}{12l'(4l' - 2Z_0(l' - 1) - b(l' - 1)^2)} \quad (\text{A7})$$

The average contact area (in unit of  $l^2$ ) can be obtained averaging over all of existing contacts:

$$a(D) = a(l'') = \frac{\pi}{3Zl'^2} (3(l''^2 - 1)Z_0 + l''^2 b(2l'' - 3) + b) \quad (\text{A8})$$

The value of  $Z_0$  for a given value of  $D_0$  is obtained, as proposed by Arnaud et al. (2000), assuming that the effective stress  
 460  $P^* = (4\pi P)/(a_c Z D)$  approaches  $P$  as  $D$  tends to 1. The third stage begins when pores start becoming isolated ( $D > D_c$ ) and densification is calculated considering the deformation of ice shells surrounding cylindrical pores (Wilkinson and Ashby, 1975). As for Eq. 2e, the total densification rate is obtained adding the densification due to new mass addition (Eq. 2f).

## Appendix B: List of all the symbols used





**Table B1.** List of the symbols used (from A to I)

Symbol	Description	Type	Unit
$A$	creep constant function of $T_F$	constant	$\text{Pa}^{-3} \text{h}^{-1}$
$A_0$	constant governing firn densification	constant	$\text{Pa}^{-3} \text{h}^{-1}$
$A_1$	constant governing snow densification	constant	$\text{m}^{-1}$
$A_2$	constant governing snow densification	constant	$\text{m}^3 \text{kg}^{-1}$
$A_Q$	constant governing the mass concentration of suspended snow	constant	$\text{m}^{0.544}$
$a$	degree hour parameter	<b>calibration parameter</b>	$\text{m h}^{-1} \text{ } ^\circ\text{C}^{-1}$
$a_c$	average contact area	variable	—
$B$	constant governing snow densification	constant	$\text{K}^{-1}$
$B_Q$	constant governing the mass concentration of suspended snow	constant	$\text{s}^{-0.544}$
$b$	parameter in firn densification	parameter	—
$C$	constant governing ice sintering function of $T_A$	constant	$\text{m}^3 \text{s}^{-1}$
$C_0$	constant governing ice sintering	constant	$\text{m}^3 \text{s}^{-1}$
$C_c, C_d, C_g, C_l$	coefficient governing cohesive force, drag, form and lift coefficient	parameter	—
$c$	constant governing snow densification	constant	$\text{s h}^{-1}$
$c_H$	coefficient influencing the lower boundary height for suspension	constant	$\text{m}^{-0.27} \text{s}^{1.27}$
$D$	relative firn density	variable	—
$D_0$	relative density between first and second stage of firn densification	here treated as constant	—
$D_c$	close-off density	here treated as constant	—
$E_1, E_2, E_3$	constants governing the influence of wind in snow densification	constant	$\text{m s}^{-1}$
$E_{MF}, E_S, E_W$	mass flux due to the transformation of snow in firn	variable	$\text{kg m}^{-2} \text{h}^{-1}$
$e$	melt-freeze factor	<b>calibration parameter</b>	—
$F$	melt freeze mass flux	variable	$\text{kg m}^{-2} \text{h}^{-1}$
$g$	gravitational acceleration	constant	$\text{m s}^{-2}$
$H$	mountain height	constant	$\text{m}$
$h$	snowpack height	variable	$\text{m}$
$h^*$	lower boundary for suspension	variable	$\text{m}$
$h_F$	firn height	variable	$\text{m}$
$h_{MF}$	height of ice inside the snowpack	variable	$\text{m}$
$h_S$	dry snow height	variable	$\text{m}$
$h_W$	height of water inside the snowpack	variable	$\text{m}$
$I, I^*, I_F$	multiplicative function	function	



**Table B2.** List of the symbols used (from K to R)

Symbol	Description	Type	Unit
$K$	intrinsic permeability of snow	variable	$\text{m}^2$
$K_W$	intrinsic permeability of water in snow	variable	$\text{m}^2$
$k$	constant	constant	$\text{m}$
$l', l''$	firm grain radius in units of the initial radius $l$	variable	—
$M$	snow melt mass flux	variable	$\text{kg m}^{-2} \text{h}^{-1}$
$M_F$	firm mass	variable	$\text{kg m}^{-2}$
$M_{MF}$	mass of ice inside the snowpack	variable	$\text{kg m}^{-2}$
$M_S$	dry snow mass	variable	$\text{kg m}^{-2}$
$M_W$	mass of water inside the snowpack	variable	$\text{kg m}^{-2}$
$MAAT$	mean annual air temperature	constant	$^{\circ}\text{C}$
$MAFT$	mean annual firm temperature	constant	$^{\circ}\text{C}$
$m$	parameter governing ice sintering	parameter	—
$m_p$	slope of the precipitation altitude relationship	parameter	$\text{mm d}^{-1} \text{m}^{-1}$
$n$	parameter governing ice sintering	parameter	—
$O$	run-off rate	variable	$\text{kg m}^{-2} \text{h}^{-1}$
$O_F$	firm melt mass flux	variable	$\text{kg m}^{-2} \text{h}^{-1}$
$P$	overburden pressure	variable	$\text{Pa}$
$P^*$	effective stress	variable	$\text{Pa}$
$P_b$	pressure in the bubbles	variable	$\text{Pa}$
$P_c$	atmospheric pressure at the close-off	here treated as constant	$\text{Pa}$
$P_F$	variation of mass due to rain on firm	variable	$\text{kg m}^{-2} \text{h}^{-1}$
$P_R$	mass flux of liquid precipitation	variable	$\text{kg m}^{-2} \text{h}^{-1}$
$P_S$	mass flux of solid precipitation	variable	$\text{kg m}^{-2} \text{h}^{-1}$
$p$	daily precipitation	variable	$\text{mm d}^{-1}$
$p_r$	reconstructed daily liquid precipitation	variable	$\text{mm d}^{-1}$
$Q$	snow erosion	variable	$\text{kg m}^{-2} \text{h}^{-1}$
$Q_1, Q_2, Q_s$	activation energy	constant	$\text{J mol}^{-1}$
$Q_{salt}$	snow transport in saltation	variable	$\text{kg m}^{-1} \text{s}^{-1}$
$Q_{susp}$	snow transport in saltation	variable	$\text{kg m}^{-1} \text{s}^{-1}$
$R$	grain radius	variable	$\text{m}$
$R_G$	gas constant	constant	$\text{J K}^{-1} \text{mol}^{-1}$
$r$	liquid precipitation rate	variable	$\text{m h}^{-1}$



**Table B3.** List of the symbols used (from S to Z)

Symbol	Description	Type	Unit
$S^*$	effective saturation degree of the snowpack	variable	—
$S_A$	mass of the most recent non eroded snow events	variable	$\text{kg m}^{-2} \text{h}^{-1}$
$\mathbf{S}_R$	vector of non eroded snow events	variable	$\text{kg m}^{-2} \text{h}^{-1}$
$S_r$	average saturation degree of the porous matrix	variable	—
$S_{r_i}$	irreducible saturation degree	variable	—
$SD$	observed snow depth	variable	m
$SSA$	specific surface area	variable	$\text{m}^2 \text{kg}^{-1}$
$SWE$	snow water equivalent	variable	m
$s$	solid precipitation rate	variable	$\text{m h}^{-1}$
$s_w$	solid precipitation rate in water equivalent	variable	$\text{mm d}^{-1}$
$T_0$	surface temperature	variable	$^{\circ}\text{C}$
$T_A$	air temperature	variable	$^{\circ}\text{C}$
$T_F$	average firn temperature	variable	$^{\circ}\text{C}$
$T_S$	average snow temperature	variable	$^{\circ}\text{C}$
$T_{\tau}$	threshold temperature for melting	here treated as constant	$^{\circ}\text{C}$
$t_d$	time since deposition	variable	s
$t_i$	time instant at the end of water year $i$	constant	h
$U$	wind speed contribution to snow densification	variable	$\text{m s}^{-1}$
$u$	10 m wind speed	variable	$\text{m s}^{-1}$
$u_2$	2 m wind speed	variable	$\text{m s}^{-1}$
$u^*$	atmospheric friction velocity	variable	$\text{m s}^{-1}$
$u_t^*$	critical friction velocity	variable	$\text{m s}^{-1}$
$V_F$	firn volume	variable	$\text{m}^3$
$V_{MF}$	volume of ice inside the snowpack	variable	$\text{m}^3$
$V_S$	dry snow volume	variable	$\text{m}^3$
$V_W$	volume of water inside the snowpack	variable	$\text{m}^3$
$Z$	number of particle contacts	variable	—
$Z_0$	initial number of particle contacts	constant	—
$z$	altitude	variable	m
$z_0$	aerodynamic roughness length	variable	m
$z_b$	top boundary for suspension	here treated as constant	m
$z_M$	maximum firn depth influenced by air temperature	here treated as constant	m
$z_m$	altitude of maximum precipitation	here treated as constant	m
$z_r$	reference height for mass concentration of suspended snow	constant	m



**Table B4.** List of the symbols used (Greek letters)

Symbol	Description	Type	Unit
$\alpha$	constant governing run-off rate	constant	$\text{m}^{-1} \text{s}^{-1}$
$\alpha'$	time conversion constant	constant	$\text{s h}^{-1}$
$\Gamma$	temperature lapse rate	parameter	$^{\circ}\text{C m}^{-1}$
$\gamma$	parameter function of $\gamma', T_F$	parameter	$\text{Pa}^{-1} \text{h}^{-1}$
$\gamma'$	parameter governing firm densification	<b>calibration parameter</b>	$\text{Pa}^{-1} \text{h}^{-1}$
$\Delta t$	time step	constant	h
$\delta$	Dirac delta function	function	
$\eta$	mass concentration of suspended snow	variable	$\text{kg m}^{-3}$
$\theta_W$	volumetric liquid water content	variable	—
$\kappa$	von Kármán constant	constant	—
$\rho$	bulk density of snow	variable	$\text{kg m}^{-3}$
$\rho_a$	atmospheric density	here treated as constant	$\text{kg m}^{-3}$
$\rho_F$	firm density	variable	$\text{kg m}^{-3}$
$\rho_i$	ice density	here treated as constant	$\text{kg m}^{-3}$
$\rho_{NS}$	fresh snow density	variable	$\text{kg m}^{-3}$
$\rho_S$	dry snow density	variable	$\text{kg m}^{-3}$
$\rho_W$	water density	here treated as constant	$\text{kg m}^{-3}$
$\varsigma$	stress due to ice cohesion	variable	Pa
$\tau_t$	critical shear stress for erosion	variable	Pa
$\phi$	porosity	variable	—



*Author contributions.* CDM and FB conceived the model. FB took care of data, and developed the case study. FB wrote a first draft of the  
465 manuscript. FB and CDM reviewed the manuscript.

*Competing interests.* No competing interests are present.

*Acknowledgements.* We would like to thank ARPA Piemonte for the meteorological data used in this study. Gratitude is also due to Josef Lier for KCC ice core data and to Pascal Bohleber for the information about Colle Gnifetti. One last thank you to Scenari Digitali and Rifugi Monterosa for additional information about Capanna Regina Margherita.



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