New insights into the drainage of inundated ice-wedge polygons using fundamental hydrologic principles

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Abstract. The pathways and timing of drainage from the inundated centers of ice-wedge polygons in a warming climate have important implications for carbon flushing, advective heat transport, and transitions from methane to carbon dioxide dominated emissions. In this research, we perform (1) a rigorous model sensitivity analysis that expands on previously published indications of polygon drainage characteristics and (2) a calibration to field data identifying necessary model

- 5 refinements. This research provides intuition on inundated polygon drainage by presenting the first in-depth analysis of drainage within a polygon based on hydrogeological first principles. We use a recently developed analytical solution to provide a baseline for the effects of polygon aspect ratios (radius to thaw depth) and hydraulic conductivity anisotropy (horizontal to vertical hydraulic conductivity) on drainage pathways and temporal depletion of ponded water from inundated ice-wedge polygon centers. By varying the polygon aspect ratio, we evaluate the relative effect of polygon size (width), inter-annual
- 10 increases in active layer thickness, and seasonal increases in thaw depth on drainage. The results of our sensitivity analysis rigorously confirm a previous analysis indicating that most drainage through the active layer occurs along an annular region of the polygon center near the rims. This has important implications for transport of nutrients (such as dissolved organic carbon) and advection of heat towards ice-wedge tops. We also provide a comprehensive investigation of the effect of polygon aspect ratio and anisotropy on drainage timing and patterns expanding on previously published research. Our results indicate that
- 15 polygons with large aspect ratios and high anisotropy will have the most distributed drainage, while polygons with large aspect ratios and low anisotropy will have their drainage most focused near their periphery and will drain most slowly. Polygons with small aspect ratios and high anisotropy will drain most quickly. To build confidence in the conclusions of the sensitivity analysis, we verify the model through a calibration to a season of field measurements. Due to the parsimony of the model, providing the potential that it could fail, we identify the minimum necessary refinements that allow the model to match water
- 20 levels measured in a low-centered polygon. We find that (1) the measured precipitation must be increased by a factor of around 2.2 and (2) the vertical soil hydraulic conductivity must decrease with increasing thaw depth. Model refinement (1) accounts for runoff from rims into the ice-wedge polygon pond during precipitation events and (2) accounts for the decreasing permeability of deeper soil layers. Our results, based on parametric investigation of idealized scenarios, provide a baseline for further research considering the geometric and hydraulic complexities of ice-wedge polygons. The calibration to field measurements
- supports the validity of the model indicating that it is able to represent ice-wedge polygon drainage dynamics.

1 Introduction

Polygonal tundra occurs in continuous permafrost landscapes lacking exposed bedrock or active sedimentation (Brown et al., 1997; Mackay, 2000). Estimates of its spatial extent vary from around 250,000 km² (Minke et al., 2007), or approximately the

- 30 size of England , to 2.6 million km², or approximately 30% of the Arctic land surface (Mackay, 1972). This terrain is rich in organic carbon (Tarnocai et al., 2009; Hugelius et al., 2014) which is poised for release to the atmosphere as carbon dioxide or methane under a warming climate, and may cause a significant feedback to climate change (Schuur et al., 2008). Depressions in the microtopography of polygonal tundra collect water from precipitation and snowmelt events, resulting in a slow-release from the landscape through the thawed subsurface to surface water drainage networks. This process has important implications
- 35 for the leaching of dissolved organic carbon from active layer soils and for advective heat transfer through the subsurface. The role that polygonal tundra regions play in global terrestrial biogeochemical feedbacks as the Arctic warms necessitates a greater understanding their hydrologic flow regimes.

Polygonal tundra forms in cold environments by the cyclic process of vertical cracking of frozen ground due to thermal contraction, water infiltration into these cracks, freezing of this infiltrated water, and subsequent re-cracking. Over many cycles,

- 40 this process leads to the growth of subsurface ice-wedges connected in polygonal patterns known as ice-wedge polygons (Liljedahl et al., 2016). Ice-wedge polygons vary in size from several meters to a few tens of meters in diameter and develop over time frames of hundreds to thousands of years (Leffingwell, 1915; Lachenbruch, 1962; Mackay, 2000; Abolt and Young, 2020). Thermal expansion of the ice and soil during summer months often results in warping the soil strata, forming parallel rims on both sides of the ice-wedge and a trough directly above the ice-wedge (refer to Figure 1). Ice-wedge polygons with
- 45 well-formed rims and troughs with a distinct, central topographic depression are referred to as low-centered polygons (as opposed to high-centered or transition polygons). Ponding occurs frequently in the centers because the rims can trap water during snowmelt or precipitation events. This ponded water subsequently drains through the subsurface to the troughs (Helbig et al., 2013; Koch et al., 2018; Wales et al., 2020).

Recent observational studies have shaped our current conceptualization of low-centered polygonal tundra hydrology (Boike et al., 2008; Helbig et al., 2013; Koch et al., 2014; Liljedahl et al., 2016; Koch, 2016; Koch et al., 2018) indicating a system of inundated polygonal centers surrounded by elevated rims that prevent surface water from flowing overland into surrounding trough ponds. This land formation results in standing water over the polygon centers, reduces immediate landscape runoff from precipitation events, and increases evaporation (Liljedahl et al., 2016). Additionally, the elevated ponded water in polygon centers produces hydrological gradients that result in sustained outward flow through the subsurface under the rims, a process

55 that has been observed at several field sites (Helbig et al., 2013; Liljedahl and Wilson, 2016; Koch, 2016; Wales et al., 2020). This lateral flow controls landscape redistribution of water during the summer months (Helbig et al., 2013), governs ponded water budgets (Koch et al., 2014; Koch, 2016), and makes up a notable portion of regional river discharge (King et al., 2020). The manner and timing with which polygonal tundra landscapes transition from inundated to drained conditions has important

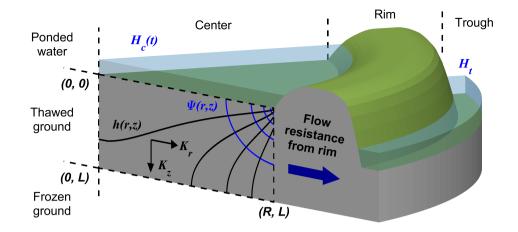


Figure 1. Pie-wedge schematic diagram of 3D-axisymmetric analytical model of inundated low-centered polygon drainage. The diagram represents an idealized *pie wedge* slice of a low-centered polygon including a wedge of the ponded center, rim, and trough. Equipotential hydraulic head lines are denoted as h(r,z) and streamlines as $\Psi(r,z)$. *L* is the depth of the thawed soil layer and *R* is the radius of the polygon center. The ponded water height $(H_c(t))$ and trough water level (H_t) are noted.

implications for (1) transitions from atmospheric emissions of methane to carbon dioxide (Conway and Steele, 1989; Moore
and Dalva, 1997; Zona et al., 2011; Zhu et al., 2013; O'Shea et al., 2014; Throckmorton et al., 2015; Wainwright et al., 2015; Lara et al., 2015; Vaughn et al., 2016), (2) dissolved organic carbon emissions to surface waters (Zona et al., 2011; Abnizova et al., 2012; Laurion and Mladenov, 2013; Larouche et al., 2015; Plaza et al., 2019), (3) biological succession (Billings and Peterson, 1980; Jorgenson et al., 2015; Wolter et al., 2016), and (4) ground surface deformation (Mackay, 1990, 2000; Raynolds et al., 2014; Nitzbon et al., 2019).

- The microtopographic features of polygonal tundra result in pronounced fine-scale spatial gradients in thermal and hydrologic conditions (Boike et al., 2008; Zona et al., 2011; Helbig et al., 2013) leading to sharply contrasting biogeochemical conditions (Newman et al., 2015; Norby et al., 2019). Standing water in polygonal centers shows distinctly different chemistry compared to surface water in troughs and ponds (Zona et al., 2011; Koch et al., 2014, 2018) which has been attributed to shallow subsurface flow from centers to troughs (Koch, 2016). For example, Koch et al. (2014) observed high nutrient concentrations
- 70 in troughs adjacent to centers with low concentrations, indicating drainage from the latter to the former. Given that the icewedge polygon can be considered the fundamental hydrologic landscape unit that initiates landscape-scale surface/subsurface flow and discharge, understanding their characteristic drainage pathways and residence times provides a basis to quantify the transport of terrestrially sourced dissolved organic carbon to surface waters. This is important for carbon emissions because dissolved organic carbon in surface waters can be mineralized and released to the atmosphere (Raymond et al., 2013).
- Although there have been numerous field observations of inundated low-centered polygon drainage to troughs (Helbig et al., 2013; Koch et al., 2014; Wales et al., 2020), the research here is, to our knowledge, the first in-depth investigation into the

relative pathways and timing associated with inundated ice-wedge polygon drainage based on hydrologic first principles. Aside from the field tracer experiments of Wales et al. (2020), previous research has primarily focused on 1D vertical hydrothermal effects within ice-wedge polygons (Atchley et al., 2015; Harp et al., 2016; Atchley et al., 2016) or polygonal tundra surface

80 hydrology (Boike et al., 2008; Jan et al., 2018a, b). Other researchers have investigated the hydrology of multiple polygons without investigating the drainage pathways within individual ice-wedge polygons (Cresto-Aleina et al., 2013; Nitzbon et al., 2019, 2020). While basic hydrology dictates that ice-wedge polygon geometry and heterogeneity will explicitly govern subsurface drainage pathways and duration, to date, a rigorous hydrological investigation of this process has not been presented.

The geometric shape of low-centered polygons along with soil hydraulic properties (for example, hydraulic conductivity)

- 85 affects the distribution of hydraulic heads that control the pathways and timing of inundated ice-wedge polygon drainage. In this paper, we use a recently developed model (Zlotnik et al., 2020) based on hydrogeological first principles (Harr, 1962; Cedergren, 1968; Freeze and Cherry, 1979; Bear, 1979) to understand and gain intuition into the effects of geometry and hydraulic properties on inundated ice-wedge polygon drainage. We investigate the pathways and timing of inundated polygon drainage using a 3D-axisymmetric analytical solution of groundwater heads. This approach idealizes the thawed subsurface of
- 90 an inundated low-centered polygon as a thin cylinder overlain with an initial height of ponded water that drains through the cylindrical thawed soil layer to the surrounding trough (outer vertical boundary; an annular ring defined by a line from (R, 0) to (R, L) in Figure 1). The depth (L) and radius (R) of the thawed soil layer of the polygon center and horizontal (radial) and vertical hydraulic conductivity are parameters of the solution. It is important to note that we are focusing on the drainage of inundated low-centered polygons here, and that biogeochemical investigations suggest that the drainage of non-inundated
- 95 low-centered, transition, and high-centered polygons may have different characteristics (Heikoop et al., 2015; Newman et al., 2015; Wainwright et al., 2015; Wales et al., 2020).

The analysis of the model enhances our intuition into the pathways and timing of inundated ice-wedge polygon drainage for polygons with different geometries and degrees of anisotropy. Varying the geometry of the cylinder not only allows us to capture relative differences in drainage between different sized polygons (in other words, polygons with different radii)

- 100 but also seasonal and inter-annual variations in polygon thaw-layer depths within a single polygon (in other words, as the thawed soil layer increases during the summer or as the active layer increases from year to year). By allowing for different effective hydraulic conductivities between the horizontal and vertical directions, we can evaluate the effects of preferential flow directions on drainage. In addition to geologic layering, processes such as frost heave and horizontal ice lens thaw can result in preferential horizontal flow in cold climates (Mackay, 1981; Matsuoka and Moriwaki, 1992; Wales et al., 2020). It
- 105 has also been observed that high hydraulic conductivity peat layers overlying lower hydraulic conductivity mineral soil results in horizontal watershed drainage (McDonnell et al., 1991; Brown et al., 1999; Quinton and Marsh, 1999). Helbig et al. (2013) found that in polygonal tundra, the peat layer quickly redistributed precipitation events across the subsurface topography from the rims to the centers and troughs. Vertical cracks, voids left from decayed roots, and animal burrows can result in preferential vertical flow. The cylindrical geometry and anisotropy are not intended to cover all potential variations in ice-wedge polygons,
- 110 but rather provide base cases where those variations will cause deviations around the idealizations considered here.

The objective of our sensitivity analysis is to provide a new perspective on inundated polygon hydrogeology indicating the effects of polygon geometry and hydraulic conductivity anisotropy on drainage pathways and timing. Although the simplifications of the model may limit its applicability to some scenarios, they allow general intuitive insights to be drawn which would be obfuscated without them. The findings here provide a basis to quantify and understand deviations from our idealized scenarios.

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Finally, to build confidence in our sensitivity analysis, we demonstrate that the model is able to accurately simulate icewedge polygon drainage by performing a calibration to field measurements over an entire thaw season. We calibrate the model parameters to fit water levels measured in the center of a low-centered polygon within the Barrow Environmental Observatory near Utgiagyik, Alaska. We force the model with measured trough water levels, precipitation, thaw depth, and evapotranspiration. The goodness-of-fit of initial calibration efforts indicated that the model was unable to capture the polygon-

- center water level trends (i.e., the model was falsified). However, by considering (1) increased precipitation and (2) a thaw 120 depth dependent (and therefore time-variable) vertical hydraulic conductivity, the model produces a good fit to the water levels. Model refinement (1) accounts for pond accumulation due to runoff from surrounding microtopographic highs (e.g., rims) while (2) accounts for the decreasing hydraulic conductivity of deeper tundra soil layers. The calibration indicates the minimum refinements necessary to a hydrology model to capture ice-wedge polygon drainage dynamics and indicates the
- 125 important factors in this process. This calibration, based on transient boundary conditions, provides confidence in the physical meaningfulness of the steady-state snapshots presented in the sensitivity analysis.

Methods 2

2.1 Model overview

We use recently developed 3D-axisymmetric analytical solutions, derived and validated in Zlotnik et al. (2020) and described 130 in Appendix A, of hydraulic heads and the stream function in the thawed soil layer below a polygon center (dashed rectangle in Figure 1) to investigate inundated low-centered polygon drainage pathways. To generalize the results concerning polygon center and trough ponded heights, we use non-dimensional forms of the hydraulic head and stream function (refer to equation A7 and A8). The non-dimensional hydraulic heads and stream function are independent of time, representing the relative pattern of hydraulic heads and stream function throughout the drainage process. The dimensional values at different times would indicate 135 the change in the absolute magnitude of these patterns as the drainage process proceeds. To evaluate drainage pathways, we plot flow nets, as illustrated in Figure 1, composed of lines of equal non-dimensional hydraulic head $(h^*(r^*, z^*))$, referred to as equipotentials, and contours of the stream function $(\Psi^*(r^*, z^*))$ as a function of radius and depth. The stream function contours are referred to as *streamlines* and are used here to identify steady drainage pathways.

Non-dimensional hydraulic head lines are drawn from 0.05 to 0.95 by increments of 0.1. Dimensional heads (h(r, z, t)) can be obtained from the non-dimensional heads $(h^*(r^*, z^*))$ using the ponded height of water in the polygon center $H_c(t)$ and the 140 height of water in the trough H_t as

$$h(r,z,t) = H_t + (H_c(t) - H_t)h^*(r^*, z^*), \ r^* = \frac{r}{L}\sqrt{\frac{K_z}{K_r}}, \ z^* = \frac{z}{L},$$
(1)

where r^* and z^* are non-dimensional radius and depth, respectively, L is the polygon thaw depth, and K_r and K_z are the radial (horizontal) and vertical hydraulic conductivity, respectively (refer to Figure 1).

- We use a Robin boundary condition (a third-type boundary condition allowing both head and flux to be specified) for the outer vertical boundary. This allows the model to represent the resistance of drainage under the rim due to elevated frozen ground and due to the accumulation of fine soil particles at the soil/water interface of the trough (Koch et al., 2018). The resistance to drainage below the polygon rim and across the soil/water interface into the trough is represented by a hydraulic conductance $\kappa = k/l$, where k is the hydraulic conductivity and l is the thickness of the drainage interface (refer to equation A3).
- We normalize the stream function $\Psi(r^*, z^*)$ from 0 to 1, and similar to heads, plot stream function contours (streamlines) from 0.05 to 0.95 by increments of 0.1. The region between any two adjacent streamlines conveys 10% of the drainage, while the two remaining regions (less than 0.05 and greater than 0.95), convey 5% of the drainage each. To make quantitative comparisons of the relative spread of drainage between polygons, we calculate the percent of each polygon volume accessed by 95% of the drainage (polygon volume with non-dimensional stream function > 0.05).
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5 The change in non-dimensional ponded water height in the polygon center due solely to drainage (the depletion curve) over time can be expressed by a simple exponential decay function as

$$H_c^*(t) = e^{-t/t_L}$$
(2)

where t_L is the characteristic time of drainage (refer to equation A11), defined as the time when the ponded height is 1/e times, or ~37% of, its original height $H_{c,0}$. The dimensional ponded height $H_c(t)$ can be obtained as

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$$H_c(t) = H_t + (H_{c,0} - H_t)H_c^*(t).$$
 (3)

As described in Zlotnik et al. (2020), for the calibration, temporally changing trough water levels, precipitation, evapotranspiration, and thaw depth are accounted for by running the model in a piecewise fashion.

2.2 Sensitivity analysis parameter ranges

We selected aspect ratio and anisotropy scenarios based on existing literature and observations. While a pan-Arctic survey 165 of ice-wedge polygon diameters does not to our knowledge currently exist, researchers have provided general characteristics based on extensive observations. Leffingwell (1915) states that ice-wedge polygons have an estimated average diameter of around 15 m. Liljedahl et al. (2016) indicate that low-centered polygons (including rims) can have diameters from 5-30 m. Abolt et al. (2018) state that polygonal formations in ice-wedge tundra are 10-30 m in diameter. Based on digital elevation models, Abolt et al. (2019) calculate that the mean polygon diameter near Utqiaġvik, Alaska is around 15 m with 5th and 95th

170 percentiles of approximately 8 and 33 m, respectively. Using a similar analysis on data from Prudhoe Bay (Abolt and Young, 2020), the mean polygon diameter is around 13 m with 5th and 95th percentiles of approximately 7 and 30 m, respectively.

Maximum thaw depths are increasing throughout the Arctic (Jorgenson et al., 2006). Deeper thaw depths may ultimately result in low-centered polygon transition to high-centered polygons, at which time polygon-center inundation will cease to occur due to rim collapse. Therefore, there is a practical limit to the thaw depth of interest in our analysis. Lewkowicz (1994)

- 175 reported that active layer thickness varied from 40 to 90 cm within the polygonal tundra of Fosheim Peninsula, Ellesmere Island, Canada in 1994. Shiklomanov et al. (2010) reported that polygonal tundra at several study sites near Utqiaġvik, Alaska monitored from 1995 to 2009 had active layer thicknesses from 17 to 47 cm. Based on extensive ground-penetrating radar surveys near Utqiaġvik, Alaska in 2013, Jafarov et al. (2017) document that average active layer thickness was 41 cm with a standard deviation of 9 cm. Even for polygons with substantial active layer thickness, it is important to understand the change
- 180 in drainage throughout the season by evaluating early-season thaw depths, which are captured in our analysis by larger aspect (i.e., radius to thaw depth) ratios.

Based on these considerations, we evaluate aspect ratios from 2.5 to 20. For example, given a thaw depth of 1 m, an aspect ratio of 2.5 would represent a 2.5 m radius polygon center, while an aspect ratio of 20 would represent a 20 m radius polygon center, more than covering the observed range. To consider cases with thinner thawed soil layers, larger aspect ratios can be used. For example, given a thaw depth of 0.5 m, an aspect ratio of 20 would represent a polygon with a 10 m radius center.

Comprehensive measurements of hydraulic conductivity anisotropy are lacking from ice-wedge polygons. Based on tracer arrival times, Wales et al. (2020) estimated horizontal conductivities of approximately 0.7 to 84 m d⁻¹ for a low-centered polygon and 0.01 to 0.3 m d⁻¹ for a high-centered polygon. Wales et al. (2020) stated that these are considered lower bound estimates of horizontal conductivity since, based solely on breakthrough times, the approach is unable to isolate horizontal

- and vertical flow effects on arrival times. Beckwith et al. (2003) performed laboratory measurements of anisotropy on small samples from peat soils where horizontal conductivities were around 6-7 m d⁻¹ and vertical conductivities were around 0.2-0.4 m d⁻¹ indicating preferential horizontal flow. The soil samples used in Beckwith et al. (2003) were from peat bogs in England, and therefore would not have been subjected to similar freeze-thaw dynamics as contemporary polygon soils, which would presumably lead to even greater preferential horizontal flow. Therefore, these estimates may provide a lower bound estimate
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for Arctic peat horizontal hydraulic conductivity. Based on the existing literature and above considerations, we considered hydraulic conductivities from 0.005-5 m d⁻¹, primarily focusing on anisotropic values from 0.1 to 100. These values allow us to investigate the relative effects of anisotropy on the drainage pathways and timing using hydraulic conductivities consistent with currently available measurements.

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A physical interpretation of our selected values of anisotropy can be obtained by considering that ice-wedge polygon soils or typically layered and that the horizontal and vertical hydraulic conductivities can therefore be considered as *effective* properties. As such, the effective horizontal hydraulic conductivity captures parallel flow dominated by the higher conductivity layers and the effective vertical hydraulic conductivity captures flow in series across multiple layers and is dominated by the lower conductivity layers. Therefore, an anisotropy of 100 would *effectively* capture layers with 2 orders of magnitude difference in hydraulic conductivity, while an anisotropy of 0.1 would capture the hypothetical scenario where vertical cracks or burrows result in preferential vertical flow. Given the current lack of direct measurements of ice-wedge polygon anisotropy,

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we cover a broad range of possible scenarios.

The hydraulic conductivity of the interface between soil and open water can be half that of the rest of the soil due to the accumulation of fines (Koch et al., 2018). The hydraulic conductance under the rim may also impede drainage due to a raised permafrost table following the surface topography. Note that while the raised permafrost table under the rim will constrict flow

- and alter drainage pathways, hydrologic first principles indicate that this effect will be restricted to the region of the model near the rim. This is analogous to the effect of a partially penetrating well on flow in an aquifer, which dissipates quickly and is non-existent by a lateral distance of 1.5 to 2 times the aquifer thickness for isotropic aquifers (Bear, 1979). This effect will diminish with increasing aspect ratio and decreasing anisotropy, and will not alter the qualitative insights drawn from the relative comparison of drainage pathways in our analysis. It is conceivable that early in the thaw season the permafrost table
- 215 under the rim could extend above the center ground surface within the vertical interval of the center pond. In this case, there will likely be very little drainage occurring associated with a very small discharge conductance. Although the conductance of the outer interface (defined as κ above) can therefore influence drainage, a preliminary analysis indicated that in most cases, its effect on drainage was significantly less than that of aspect ratio and anisotropy (Zlotnik et al., 2020). Therefore, we chose to use a default value for κ in all cases (unless otherwise specified) of 5 d⁻¹.
- In practice, the water level in troughs (H_t in equations 1 and 3) will vary throughout the thaw season, affecting the magnitude of heads in the soil of the polygon center and drainage times. As the non-dimensional heads are relative to H_t (refer to equation A7), its value does not affect our relative comparisons of drainage patterns (which are based on non-dimensional heads that are normalized from 0 to 1). The value of H_t will affect our comparisons of drainage time, but in a systematic, interpretable manner. For example, a higher H_t will compress the exponential curve defined by equation 3 upwards, while a lower H_t will stretch the exponential curve downwards. In cases where H_t is below the polygon-center ground surface, the
 - solution is valid until H_c reaches the ground surface, at which time the ponded center has completely drained. Therefore, to isolate our analysis to aspect ratio and anisotropy, we have set H_t in all cases equal to the polygon-center ground surface.

We have neglected the effects of evaporation and precipitation as they will not affect the drainage patterns we present (based on non-dimensional heads) and their effect on drainage timing (based on non-dimensional depletion curves) is straightforward,

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on non-dimensional heads) and their effect on drainage timing (based on non-dimensional depletion curves) is straightforward,
 shifting the non-dimensional exponential drainage curve upwards or downwards. In other words, using non-dimensional variables is a powerful approach to gain intuition into the fundamentals of inundated ice-wedge polygon drainage irrespective of variable magnitude.

2.3 Acquisition of field data used in calibration

The measured data used in the calibration were collected during the thaw season of 2013 from June 16 to September 18 from a low-centered polygon within the Barrow Environmental Observatory near Utqiaġvik, Alaska (Figure 2). We used water levels collected by Liljedahl and Wilson (2016) and precipitation collected by Hinzman et al. (2014). We determined thaw depths from thermal transects collected by Romanovsky et al. (2017). We obtained evapotranspiration data from NASA's Global Land Data Assimilation System (GLDAS) (Rodell et al., 2004).

2.4 Calibration approach

240 We performed nonlinear least-squares calibrations using a Levenberg-Marquardt approach (Transtrum et al., 2011). The objective function is the sum-of-squared errors (SSE) between the measured and simulated polygon-center water levels expressed

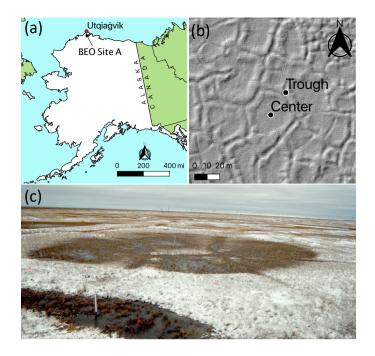


Figure 2. (a) Map, (b) hillshade relief with well locations, and (c) photo of the Barrow Environmental Observatory (BEO) Site A near Utqiagvik, Alaska. Photo courtesy of Bob Busey.

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$$SSE(\theta) = \sum_{i=0}^{N} (H_c(t_i, \theta) - H_c^m(t_i))^2,$$
(4)

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where θ is a vector of model parameters and $H_c^m(t_i)$ is the measured polygon-center water level at the *i*th time. We present three calibration cases including (1) a base case (model setup similar to the validation in Zlotnik et al. (2020)), (2) precipitation multiplied by a calibrated factor, and (3) a depth-dependent vertical hydraulic conductivity ($K_z = f(D)$). Depending on the calibration case, θ contains different parameters.

In calibration case 1, θ includes parameters K_r , K_z , κ , and $H_{c,0}$. Based on field observations and the validation in Zlotnik et al. (2020), we constrain K_z to be less than K_r using a meta-parameter \mathcal{F}_{K_z} as $K_z = K_r \sigma(\mathcal{F}_{K_z})$ where σ is the sigmoid function defined as $\sigma(x) = 1/(1 + \exp(x))$.

In calibration case 2, we add a precipitation multiplier M_P to case 1, where $\hat{P} = M_P P$ and \hat{P} is the augmented precipitation accounting for runoff from microtopographic highs.

In calibration case 3, we add vertical hydraulic conductivity as a super-elliptical function of thaw depth to calibration case 2 as $K_z(D) = K_z^{min} + (K_z^{max} - K_z^{min})(1 - D_{norm}^a)^{1/a}$, $D_{norm} = \frac{D - D^{min}}{D^{max} - D^{min}}$, where K_z^{max} and K_z^{min} are the maximum 255 and minimum values of K_z , respectively, D^{max} and D^{min} are the maximum and minimum values of D during the thaw season, respectively, and a is the super-elliptical shape parameter that controls curvature. K_z^{max} is constrained to be positive using a meta-parameter $\mathcal{F}_{K_z^{max}}$ and the softplus function as $K_z^{max} = log(1 + \exp(\mathcal{F}_{K_z^{max}}))$. We ensure that $K_z^{min} \leq K_z^{max}$ using a meta-parameter $\mathcal{F}_{K_z^{min}}$ as $K_z^{min} = K_z^{max} \sigma(\mathcal{F}_{K_z^{min}})$. We ensure that the shape parameter *a* is restricted between 0.5 and 1.5 using a meta-parameter \mathcal{F}_a as $a = 0.5 + 1.5\sigma(\mathcal{F}_a)$. The constrained super-elliptical function allows the calibration to identify a general nonlinear decrease in vertical hydraulic conductivity with increasing thaw depth.

3 Results

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We present drainage flow nets for various aspect ratios and anisotropy values, polygon-center ponded height depletion curves, and maps of the percent of the thawed soil accessed by 95% of the drainage flow and depletion characteristic times as a function of aspect ratio and anisotropy. We compare the effect of aspect ratio on drainage pathways in an isotropic and a highly anisotropic ($K_r/K_z = 100$) polygon. The drainage pathways are also evaluated for various anisotropies holding the aspect 265 ratio constant. We present a global perspective of the combined effects of aspect ratio and anisotropy on the focusing/spreading of the drainage flow by mapping the percent of the polygon thawed soil volume that is accessed by 95% of the drainage flow. We evaluate the effect of aspect ratio and anisotropy on drainage time by plotting the polygon-ponded water height depletion curves. Similar to accessed volume, we provide a global perspective on the combined effects of aspect ratio and 270 anisotropy on drainage time by mapping the depletion characteristic time. We illustrate the counteracting effects of aspect ratio and anisotropy on drainage pathways by showing two, although geometrically and hydrologically dissimilar, mathematically equivalent solutions of drainage. We verify the model through calibration to water-level measurements, identifying refinements necessary for hydrologic models to match field observations of polygon drainage.

3.1 Drainage pathways

- The relative effect of aspect ratio on drainage pathways when the hydraulic conductivities are isotropic $(K_r/K_z = 1)$ is shown 275 in Figure 3. Under isotropic hydraulic conductivities, results show that the drainage pathway for high aspect ratio polygons will be predominantly isolated to an annular region at the periphery of the polygon center. As the aspect ratio decreases (in other words, as the thawed region of the polygon subsurface becomes deeper with respect to its width), the portion of the polygon accessed by drainage increases. For an aspect ratio of 20 (Figure 3a), 95% of the drainage is focused within around 280 6% of the polygon volume, while for an aspect ratio of 2.5 (Figure 3d), the drainage is spread over around 33% of the polygon volume. The spreading (increase in the accessed volume) occurs along the radial direction, where the horizontal extent of the accessed volume moves towards the middle of the polygon center (r = 0), while the vertical extent is nearly unchanged. The results in Figure 3 indicate that throughout the thaw season as the thaw depth increases, or over successive years as the active layer thickens, the drainage path will spread out towards the middle of the polygon center. Similarly, Figure 3 can be used to evaluate drainage pathways of polygons of different widths but similar thaw depths. In this context, Figure 3 indicates that
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The effect of anisotropy on drainage pathways when the aspect ratio is held constant (R/L = 10) is shown in Figure 4. As anisotropy increases (i.e., greater preferential horizontal flow), the region accessed by drainage flow becomes larger. Similar to a decreasing aspect ratio (smaller and/or more deeply thawed polygons) in Figure 3, increasing anisotropy leads to a larger

wider polygons will have more focused drainage, while drainage for smaller polygons will be more dispersed.

Variable Aspect Ratio/Isotropic Hydraulic Conductivity

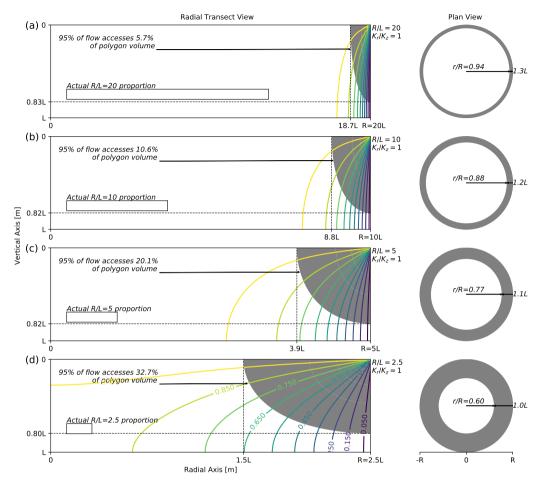


Figure 3. Effect of polygon aspect ratio on polygon drainage with isotropic hydraulic conductivity. Plots along the left contain polygon radial transect head contours (colored lines) and filled stream tubes (grey regions) for several polygon aspect ratios (radius/thickness). The grey shaded region denotes the portion of the transect accessed by 95% of the flow. The plots along the right contain corresponding grey rings indicating the surface area where 95% of the polygon flow infiltrates. Each plot along the left contains a rectangle drawn to the actual proportions for the given polygon aspect ratio. In all cases, the anisotropy (horizontal/vertical conductivity) is fixed at unity.

radial extent of the accessed region, while the vertical extent is nearly unaffected. When the vertical conductivity is ten times the horizontal (Figure 4a), only around 3% of the polygon volume is accessed by 95% of the drainage. If horizontal conductivity

Fixed Aspect Ratio/Variable Anisotropy

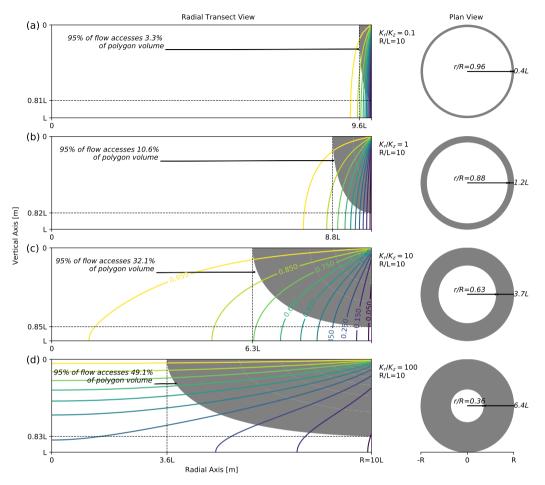


Figure 4. Effect of hydraulic conductivity anisotropy on polygon drainage. Plots along the left contain polygon radial transect head contours (colored lines) and filled stream tubes (grey regions) for several anisotropies (horizontal/vertical conductivity). The grey shaded region denotes the portion of the transect accessed by 95% of the flow. The plots along the right contain corresponding grey rings indicating the surface area where 95% of the polygon flow infiltrates. Each plot along the left contains a rectangle drawn to the actual proportions for the given polygon aspect ratio. In all cases, the polygon aspect ratio (radius/thickness) is fixed at 10.

is 100 times vertical conductivity (Figure 4d), around 49% is accessed. These results indicate that anisotropy has a significant impact on ice-wedge polygon drainage pathways.

Variable Aspect Ratio/High Anisotropy

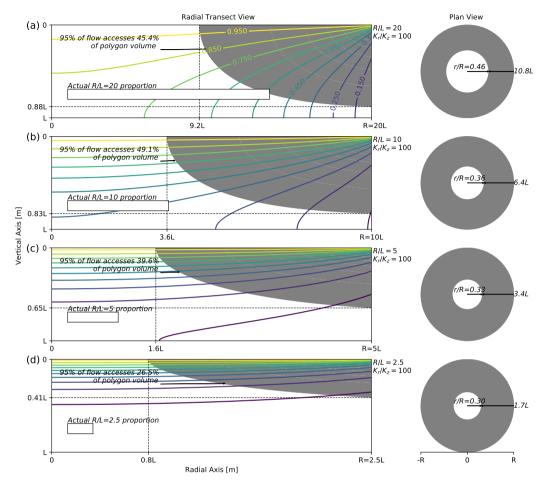


Figure 5. Effect of polygon aspect ratio on polygon drainage with high hydraulic conductivity anisotropy ($K_r/K_z = 100$). Plots along the left contain polygon radial transect head contours (colored lines) and filled stream tubes (grey regions) for several polygon aspect ratios (radius/thickness). The grey shaded region denotes the portion of the transect accessed by 95% of the flow. The plots along the right contain corresponding grey rings indicating the surface area where 95% of the polygon flow infiltrates. Each plot along the left contains a rectangle drawn to the actual proportions for the given polygon aspect ratio. In all cases, the anisotropy (horizontal conductivity/vertical conductivity) is fixed at 100.

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The effect of aspect ratio on drainage pathways when the hydraulic conductivities are highly anisotropic $(K_r/K_z = 100)$ is shown in Figure 5. In this case, contrary to the isotropic case in Figure 3, as the aspect ratio decreases, the accessed volume generally decreases. However, the largest accessed volume is for an aspect ratio of 10 (Figure 5b), not 20 (Figure 5a). This

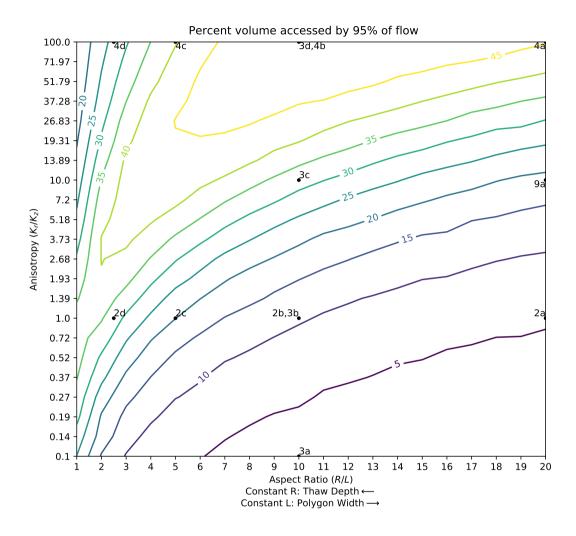


Figure 6. Contour map of the percent of the polygon access by 95% of the flow as a function of polygon aspect ratio and anisotropy. Locations associated with other figures are indicated by labeled points. By choosing a constant value for R (L = R/x), horizontal transects parallel to the x-axis represent the effect of thaw depth increasing from right to left, while they represent increasing polygon width from left to right for constant values of L (R = Lx). Note that $\kappa = 5$ day⁻¹ in these calculations, and therefore, the location associated with Figure 10b cannot be indicated.

nuance in the dependence of accessed volume to aspect ratio with high anisotropy is due to the competing effects of radial extension and vertical contraction of the accessed volume as aspect ratio decreases. By comparing Figures 3 and 5, it is also apparent that the volume accessed by drainage is generally larger with higher anisotropy.

- To gain a global perspective on the trends in drainage pathways with aspect ratio and anisotropy, Figure 6 maps the percent of the polygon accessed by 95% of the drainage as a function of aspect ratio and anisotropy. This illustrates the overall structure of the combined effect of aspect ratio and anisotropy on accessed volume (focused versus dispersed drainage). As indicated by the annotated points, the trend in accessed volume with respect to aspect ratio in Figure 3 is represented along the anisotropy=1 transect, while the trend in Figure 5 is represented by the anisotropy=100 transect. The trend in accessed volume with respect
- 305 to anisotropy in Figure 4 along the aspect ratio=10 transect is likewise indicated. There is a curved, spreading region of high accessed volume with increasing aspect ratio and anisotropy apparent in the contours of Figure 6. This curved feature represents the optimal balance of radial and vertical extension of the accessed volume region, as described in the previous paragraph. This structure explains the increasing accessed volume with decreasing aspect ratio in Figure 3 and the maximum accessed volume at an aspect ratio of 10 in Figure 5. The drainage flow is most spread out (largest accessed volume) when the aspect ratio is
- 310 large and the anisotropy is high (upper right of Figure 6). The drainage is the most focused (least accessed volume) when the aspect ratio is large and the anisotropy is low (lower right of Figure 6).

3.2 Ponded water depletion

Depletion curves for the non-dimensional ponded water height in the polygon center for various aspect ratios (at fixed high and low anisotropy) and anisotropies are shown in Figures 7a, b, and c, respectively. Note that since the depletion of the volume of ponded water is directly related to the ponded water height, the plots in Figure 7 can be used to obtain either, as indicated by the y-axis labels. As a point of reference between depletion curves, the characteristic time (the time when the height or volume

of ponded water reaches $1/e \approx 0.37$ its initial height or volume) is indicated.

It is apparent from these plots that small, deeply thawed (lower aspect ratio) polygons will drain faster than wide, shallowly thawed (high aspect ratio) polygons, while polygons with higher anisotropy will drain faster than those with lower anisotropy. 320 It is also apparent that the increase in drainage time with aspect ratio is nearly linear, while for anisotropy, it is exponential. This is further illustrated in Figure 8, where we plot the trend in characteristic times as a function of aspect ratio for various anisotropies (Figure 8a) and as a function of anisotropies for various aspect ratios (Figure 8b). Drainage time (represented by characteristic time) increases in a nearly linear fashion, particularly for high anisotropies, with slight upward curvature increasing for low anisotropies. The drainage time decreases in a nearly log-log fashion (exponentially) with increasing anisotropy with an identical trend for different aspect ratios.

- A global perspective on drainage timing trends, where characteristic time is mapped as a function of aspect ratio and anisotropy, is shown in Figure 9. The fastest (shortest) drainage times are achieved with a low aspect ratio and a high anisotropy, while the slowest (longest) drainage times are achieved with a high aspect ratio and low anisotropy. These trends indicate that given the same thawed soil layer thickness, wider polygons will drain more slowly than small polygons. Or, for polygons with
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similar aspect ratios, those with preferential horizontal flow will drain most quickly, while those with preferential vertical flow will drain most slowly.

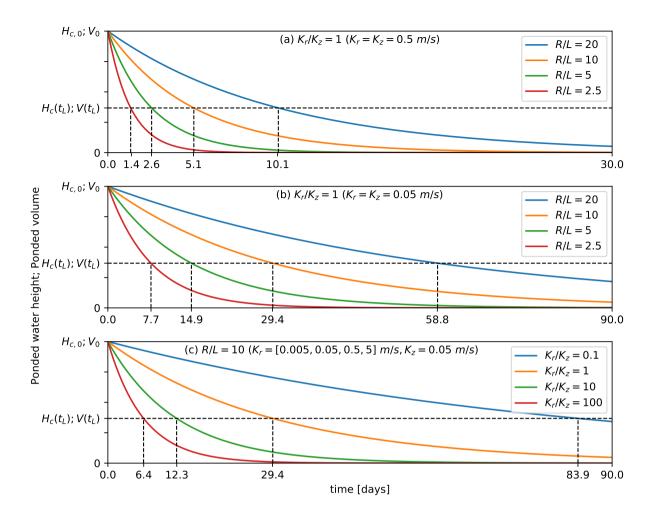


Figure 7. Depletion of ponded water height over time $(H_c(t))$ for (a,b) alternative polygon aspect ratios (radius/depth (R/L)) and (c) anisotropy (K_r/K_z) . Plots (a) and (b) have anisotropy fixed at unity with plot (a) having high conductivity $(K_r = K_z = 0.5 \text{ m/s})$ and plot (b) low conductivity $(K_r = K_z = 0.05 \text{ m/s})$. The aspect ratio is fixed at 10 in plot (c). The curves also describe the depletion of ponded water volume over time (V(t)). Dashed lines indicate the characteristic times (t_L) in each case. Note that the orange line in (b) and (c) are identical, R/L = 10 and $K_r/K_z = 1$.

3.3 Counteracting effect of aspect ratio and anisotropy

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It is important to note that aspect ratio and anisotropy have similar effects on drainage. Within the model used here, in a similar fashion to aspect ratio, anisotropy stretches the domain by multiplying the non-dimensional radius by $\sqrt{(K_z/K_r)}$ (refer to the definition of r^* in equation 1). As a result, the effect of increasing anisotropy in the analytical solution is mathematically equivalent to a decrease in aspect ratio. In the end, the equipotential heads and streamlines computed on stretched or compressed radial coordinates (r^*) are assigned back to non-modified radial coordinates (r). This would lead one to believe that it should

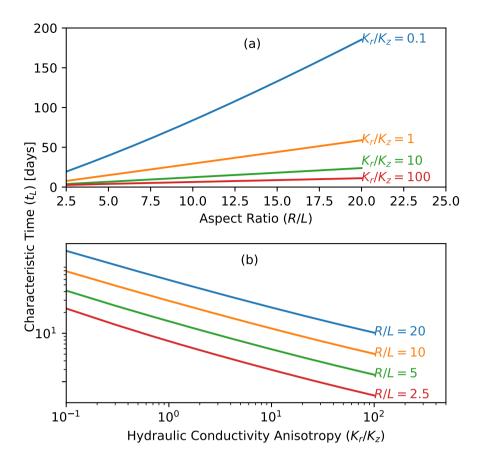


Figure 8. Characteristic time as a function of (a) polygon aspect ratio and (b) anisotropy. The $K_r/K_z = 1$ line in plot (a) corresponds to characteristic times in Figure 7b. Note that the trends in (a) are nearly linear and on natural scaled axes while the trends in (b) are also nearly linear on log transformed axes.

be possible to obtain two scenarios with different aspect ratios and anisotropies that produce the same mathematical solution. For example, doubling the aspect ratio should produce the mathematically identical effect as dividing the anisotropy by four.

340 However, this is not the case because the solution involves a Biot parameter (Bi) which defines the ratio of the ability for fluid to conduct across the drainage interface (the vertical outer boundary) relative to the internal hydraulic conductivity as

$$\mathrm{Bi} = \frac{\kappa L}{\sqrt{K_r K_z}},\tag{5}$$

where κ characterizes the hydraulic conductance across the outer vertical boundary of the model (refer to Appendix A for more details). A large Bi indicates that the outlet boundary interface of the model will not limit the drainage, while a small Bi
will result in outlet boundary interface limited drainage. Therefore, to obtain an identical mathematical drainage solution using different combinations of aspect ratio and anisotropy, one would also need to ensure that Bi is not modified in the process.

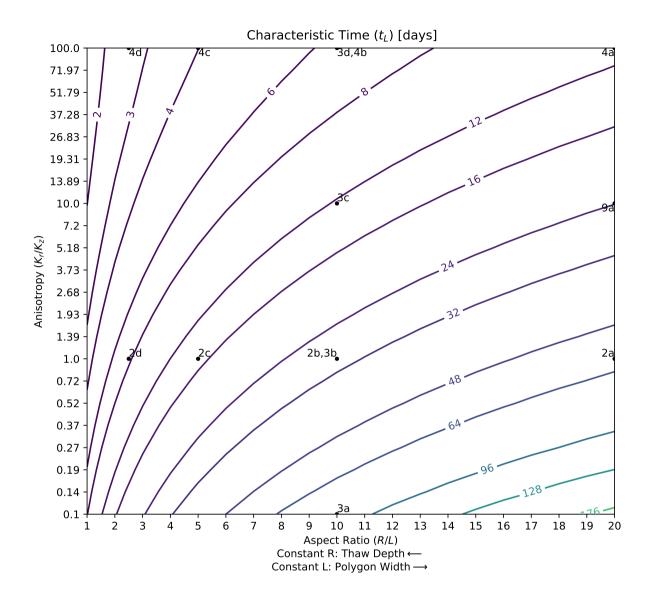


Figure 9. Contour map of the characteristic time of polygon drainage as a function of polygon aspect ratio and anisotropy. Locations associated with other figures are indicated by labeled points. By choosing a constant value for R (L = R/x), horizontal transects parallel to the x-axis represent the effect of thaw depth increasing from right to left, while they represent increasing polygon width from left to right for constant values of L (R = Lx). Note that $\kappa = 5$ day⁻¹ in these calculations, and therefore, the location associated with Figure 10b cannot be indicated.

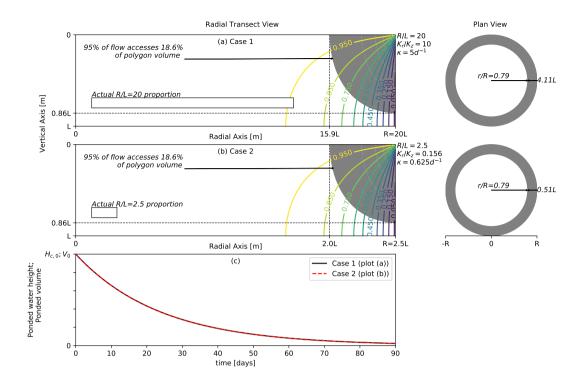


Figure 10. Attaining the same mathematical solution by modifying polygon aspect ratio (R/L), anisotropy (K_r/K_z) , and rim conductance (κ). The left plots of (a) and (b) contain polygon radial transect head contours (colored lines) and filled stream tubes (grey regions) for several polygon aspect ratios (radius/thickness). The grey shaded region denotes the portion of the transect accessed by 95% of the flow. The right plots of (a) and (b) contain corresponding grey rings indicating the surface area where 95% of the polygon flow infiltrates. Plots (a) and (b) contain a rectangle drawn to the actual proportions for the given polygon aspect ratio. The ponded water height/volume depletion curves for both cases are presented in (c).

However, given two solutions, this requires satisfying the conflicting conditions that $K_{z1}/K_{r1} = K_{z2}/K_{r2}$ and $K_{r1}K_{z1} = K_{r1}K_{r2}$ $K_{r2}K_{z2}$ (refer to equations 1 and 5), where subscripts 1 and 2 refer to the two solutions. Since these two constraints cannot be simultaneously met, κ or L must also be modified along with aspect ratio and anisotropy to achieve an identical mathematical solution of drainage. An example where identical mathematical solutions for drainage are obtained is provided in Figure 10, where the bottom plot is obtained by taking the properties of the top plot and dividing the aspect ratio by 8, dividing the anisotropy by 8^2 , and dividing κ by 8. While the solutions are mathematically identical, note that the axes in both plots are not to scale (actual proportions are provided as insets to the plots) and that there are differences in some relative dimensions indicated in the figure (for example, the relative width of the polygon volume accessed by 95% of the drainage flow is around 4L in the top case and around 0.5L in the bottom case).

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In the bottom plot in Figure 10, we demonstrate that despite these differences, the depletion curves are identical for both cases. This result is due to our choice to modify R to change the aspect ratio and modify K_r to change the anisotropy. If either L or K_z are chosen to modify the aspect ratio or anisotropy, respectively, the depletion curves would not necessarily be identical. For example, if L is multiplied by 8, K_z multiplied by 8², and κ divided by 8 (equivalent modifications to aspect ratio and anisotropy as above), the drainage flow net would still be mathematical equivalent, but the characteristic time would be 8 times shorter than in the original case (refer to equation A11). Therefore, while it is possible to obtain mathematically equivalent drainage patterns with counteracting modifications to aspect ratio, anisotropy, and outflow conductance, the temporal depletion will only be equivalent if R and K_r are used to modify the aspect ratio and anisotropy, respectively.

3.4 Calibration to field measurements

to Table 1) is extremely large and non-physical.

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We present the best-fit polygon-center water levels for the calibration cases along with the measured values in Figure 11. The two dominant drivers of the polygon-center water levels, the measured trough water level and precipitation, are shown for reference. Calibration case 1 (green line) is unable to match the high and low points of the water level measurements, and instead follows a more medial path over time (RMSE=1.42 cm; R²=0.49; refer to Table 1). This indicates that the measured precipitation alone is not able to account for the increased water levels after rain events. We also consider the calibration as
failed (the model as falsified (Popper, 2005)) because the calibrated value of the discharge conductance (κ = 835.3 d⁻¹; refer

Considering that precipitation will runoff from rims and collect in the polygon-center pond and that rain gauges may have undercatch issues (e.g., (Pollock et al., 2018)), we performed calibration case 2, also shown in Figure 11 (purple line), which includes a precipitation multiplier. Calibration case 2 significantly improves the fit (RMSE=0.89 cm; R^2 =0.80), but still has significant mismatch as the limitations of the model require the calibration to compromise between matching water levels at early and late times. As in calibration case 1, we also consider the model for calibration case 2 as falsified because the calibrated value of $\kappa = 1529.2 \text{ d}^{-1}$ is even larger than in case 1, and therefore even less physical.

The compromised fit in calibration case 2 indicated that the effective vertical hydraulic conductivity likely decreases as the thaw depth increases, which would be consistent with observations of reduced hydraulic conductivities at depth. In calibration case 3, we implemented vertical hydraulic conductivity as a function of thaw depth. This model refinement allowed the

calibration to achieve a good overall fit to the data (RMSE=0.37 cm; R^2 =0.96) as shown in Figure 11 (red line). K_r is well within the estimated limits of 0.7 to 84 m d⁻¹ based on a tracer test at a nearby low-centered polygon conducted by Wales et al. (2020). Based on a rim width of 1 meter, the discharge conductance of $\kappa = 3.3 \text{ d}^{-1}$ would correspond to a drainage boundary layer hydraulic conductivity of 3.3 m d⁻¹, which is also physically reasonable as opposed to the first two calibration estimates.

385 4 Discussion

Our analysis provides new insights into the relative effects of geometry and anisotropy on the manner in which inundated ice-wedge polygons retain and slowly release water from their centers to their troughs, which form the drainage network of

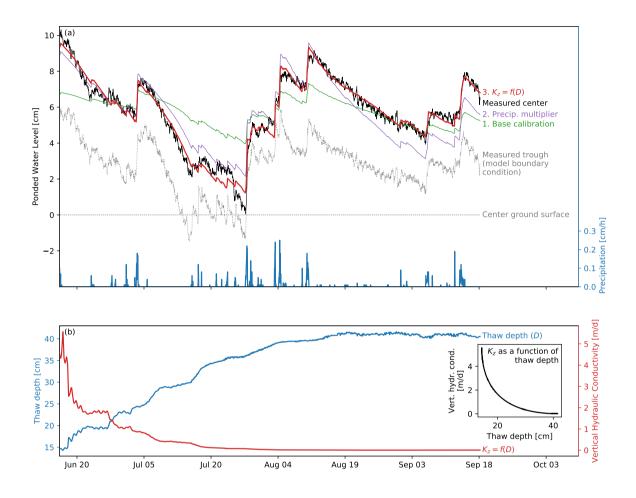


Figure 11. (a) Progression of center water-level calibration. The (1) base calibration, (2) calibration with a precipitation multiplier, and (3) calibration with vertical hydraulic conductivity as a function of thaw depth ($K_z = f(D)$). The measured polygon-center and trough water levels are plotted for reference. Precipitation is plotted on the right y-axis. (b) Measured thaw depth and calibrated vertical hydraulic conductivity as a function of thaw depth.

polygonal tundra landscapes. Using a mathematical representation of inundated ice-wedge polygon drainage (Zlotnik et al., 2020) based on extensive field observations (Helbig et al., 2013; Koch et al., 2014; Liljedahl and Wilson, 2016; Wales et al., 2020) and verified here through calibration to field measurements, we quantify the sensitivity of inundated ice-wedge polygon

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Table 1. Calibrated parameters values, root-mean-squared error (RMSE), and coefficient of determination (R^2) for calibration cases. Note that the coefficient of determination is equivalent to the Nash-Sutcliffe Efficiency here. Dashes indicate that the parameter was not part of the calibration.

		Calibration Case		
Parameter	Symbol	(1) Base	(2) Precip. mult.	$(3) K_z = f(D)$
Hor. Hydr. Cond. [m d^{-1}]	K_r	9.8	36.7	19.9
Vert. Hydr. Cond. $[m d^{-1}]$	K_z	1.02e-04	5.14e-04	_
Discharge conductance $[d^{-1}]$	κ	835.3	1529.2	3.3
Initial polygon-center water level [cm]	$H_c(t=0)$	6.58	8.66	9.12
Precipitation multiplier [–]	M_P	-	2.24	2.21
Min. Vert. Hydr. Cond. $[m d^{-1}]$	K_z^{min}	-	_	4.37e-03
Max. Vert. Hydr. Cond. $[m d^{-1}]$	K_z^{max}	-	_	5.57
Super-elliptical shape parameter [-]	a	-	-	0.50
Root-mean-squared error [cm]	RMSE	1.42	0.89	0.37
Coefficient of determination	R^2	0.49	0.80	0.96

drainage to representative polygon sizes, inter- and intra-annual changes in thaw depth, and preferential flow (hydraulic conductivity anisotropy).

4.1 Analysis implications

A key result of this study is that the geometry and anisotropy of the polygon subsurface have a significant effect on the region 395 of the polygon subsurface predominantly accessed by drainage flow and the time to transition from inundated to drained. Due to the geometry of inundated polygons, the primary drainage pathway is restricted to an annular, radially-peripheral region of the ice-wedge polygon center near the rim. As a result, the middle and lower portions of the polygon center are excluded from the majority of the drainage to varying degrees depending on the polygon geometry and anisotropy. Also, the majority of the ponded water will flow towards the rim of the polygon before infiltrating into the subsurface. Field observations have indicated not only the existence of intra-polygon biogeochemical diversity (Zona et al., 2011; Newman et al., 2015), but that, 400 based on mineral and nutrient loading, pervasive subsurface flow from centers to troughs exists (Koch et al., 2014). Based on our analysis, polygon geometry and anisotropy will have important effects on the biogeochemistry of polygons (Heikoop et al., 2015; Throckmorton et al., 2015; Newman et al., 2015; Wales et al., 2020; Plaza et al., 2019) affecting dissolved organic matter and mineral flushing from the subsurface of polygon centers to the surface waters of troughs. This is important not only simply concerning the discharge of dissolved organic matter from polygonal tundra landscapes, but also for the biogeochemical effects

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due to photolysis of dissolved organic matter newly exposed to sunlight (Laurion and Mladenov, 2013; Cory et al., 2014).

The potential that the annular, radially-peripheral region near the rims will be well flushed of nutrients, while the middle may not, indicates the need for additional field studies designed to measure the effects of anisotropy and preferential flow paths on thermal-hydrology and biogeochemistry. For isotropic cases, it should also be considered that the drainage will spread out

- 410 further towards the middle of the polygon center as the thaw season progresses and the thawed soil layer thickens (in other words, the aspect ratio decreases; Figures 3 and 5). However, with high anisotropy, the drainage still spreads out towards the polygon middle as the thaw season progresses (aspect ratio decreases), but the depth of the main drainage pathways contract towards the ground surface (Figure 5). Ultimately, the effect of this vertical contraction outweighs the lateral spreading, leading to a smaller region being accessed by drainage. Therefore, in the case of smaller and/or more deeply thawed (low aspect ratio)
- 415 polygons with high anisotropy, the region close to the surface will be flushed more than the deeper regions. Deeper nutrients that become available for transport because of recent thaw may still be less accessible to aqueous transport due to drainage pathways in polygons with high anisotropy. Field measurements of geochemical depth profiles in polygons support limited deep flushing. As reviewed in Newman et al. (2015), concentration increases of geogenic solutes and organic carbon with active layer depth are relatively common in polygonal terrain. It is unlikely that these sometimes large geochemical depth gradients would be
- 420 preserved with significant amounts of deep flushing. Inter-annual deepening of the active layer will lead to even more dramatic evolution in drainage patterns described above during the thaw season as the range of thaw depths encountered increases. This research reinforces the need for field studies on anisotropy and preferential flow in polygon landscapes to better understand the hydrologic transitions and feedbacks that will occur in a warming climate.

For a given thaw depth, advective heat transport will be more focused near the rim for larger polygons, and may result in
enhanced ice-wedge degradation (Wright et al., 2009). Based on the relative drainage pathways, advective heat transport will
be most pronounced in larger and/or shallower (large aspect ratio) polygons with low anisotropy (refer to Figures 3a and 4a).
Therefore, drainage events for wide, isotropic (or with preferential vertical flow) polygons may result in enhanced ice-wedge
top thawing, which would promote low- to high-centered polygon transition. The more spread out the drainage is throughout
the thawed soil layer, the less pronounced this effect may be (for example, wide polygons with high anisotropy as in Figures 5a
and b). However, small polygons with high anisotropy will restrict the drainage flow near the ground surface, potentially

reducing the advective transport of heat to the ice-wedge top as well (Figure 5d). Similarly, increasing seasonal thaw depth and inter-annual active layer thickness will lead to polygons with less focused advective heat transport towards ice-wedge tops, potentially providing a negative feedback on ice-wedge degradation. These results provide an additional perspective on ice-wedge degradation, complementing previous research that found that the process is also strongly controlled by geometry (Abolt et al., 2020) and hydrologic conditions (Nitzbon et al., 2019).

Small polygons with deeply thawed soil layers (low aspect ratios) and high horizontal preferential flow (high anisotropy) have the potential to drain most quickly. Therefore, all other factors being equal, regions of polygonal tundra characterized by small, deeply thawed, anisotropic polygons will drain more quickly and consequently will have a greater potential for nutrient flushing, transition from methane to carbon dioxide atmospheric emissions, and biological succession than regions with large,

440 shallowly thawed, isotropic polygons. Concerning temporal changes during the thaw season, polygon pond depletion will slow down as the thaw depth increases, and this reduction will become more dramatic over the thaw season as inter-annual active-layer thickness increases. This implies that a thickening active layer due to warming trends may result in slower pond depletion. For a given location, factors such as regional flow patterns, large-scale topography, etc., will influence the region's

overall drainage timing. However, along with these other factors, our analysis indicates that aspect ratio will have a nearly

445 linear positive relationship while anisotropy will have an exponential negative relationship with drainage timing.

4.2 Model limitations

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The drainage pathways and timing presented here are based on hydrogeological first principles (Harr, 1962; Cedergren, 1968; Freeze and Cherry, 1979; Bear, 1979) using a generalization of ice-wedge polygon geometry and hydraulic properties that allow insights into drainage pathways and timing. The model captures the physical forces that ponded water exerts on a cylindrical porous disc with drainage allowed radially through its sides. While the cylindrical geometry and anisotropy considered here do not cover all potential variations present in ice-wedge polygons, the impact of those variations will cause deviations from the

- idealized scenarios considered here. For example, heterogeneities will warp the base case hydraulic head equipotentials and streamlines. The cylindrical idealization of ice-wedge polygon geometry will best approximate drainage in nearly symmetrical hexagonal ice-wedge polygons, while non-symmetric or square ice-wedge polygon drainage will deviate most from that shown
- 455 here. The model assumes uniform radial discharge around the periphery of the polygon center. Low points in the elevated frozen ground under the rim will lead to deviations from our results. Elevated frozen ground under the rim will also warp the streamlines upwards within a localized region near the rim, but this effect will dissipate a short distance into the polygon center.

In our analysis, we use idealized conceptualizations and dimensionless variables which allow hydrologic characteristics of drainage to be exposed in their most fundamental form. To clearly and concisely expose these characteristics, we neglect

460 factors such as evaporation, precipitation, and non-idealized polygon geometry. As a result, our analysis is not intended to provide predictive capability across all polygonal tundra scenarios, but to provide hydrologic intuition into the relative effects of geometry and anisotropy on inundated ice-wedge polygon drainage and timing.

As the analytical solution applies to ponded conditions, it does not apply to freeze-up at the end of the thaw season after the ponded water in the polygon center freezes. At this time, the active layer freezes simultaneously from the top and bottom and cryosuction draws water towards the freezing fronts. This redistribution of water affects ice-wedge polygon drainage and Wales et al. (2020) postulate that it may explain some of the observations of their tracer test. More complex models than applied here are required to capture the details of water redistribution during freeze-up (Painter, 2011; Atchley et al., 2016; Schuh et al., 2017).

Since the model is based on the saturated groundwater flow equation, in its current form it cannot be applied to non-inundated
low-centered polygons. Since it is based on having a ponded center, the model is also not applicable to high-centered polygons. However, a similar approach to that presented here could be taken with the unsaturated groundwater flow equation to capture these other polygon scenarios and types.

4.3 Relation to other mathematical analyses

As our analysis is the first detailed examination of inundated ice-wedge polygon drainage patterns, our results provide a new perspective to existing mathematical analyses. Much of the existing mathematical analyses investigate drainage from polygonal landscapes. For example, Cresto-Aleina et al. (2013) analyze low-centered polygonal landscape hydrology stochastically using percolation theory, a method that is not designed to investigate drainage pathways of individual polygons. Nitzbon et al. (2019, 2020) investigate the hydrology of polygonal tundra using a "tiled" approach that is also not designed to map individual ice-wedge polygon drainage pathways. In these cases, our analysis enhances our understanding by considering details that are

- 480 glossed over in these analyses for the sake of considering drainage from many polygons. Other research has focused on process-
- rich 1D analyses that are unable to consider lateral flow. For example, Atchley et al. (2015); Harp et al. (2016) and Atchley et al. (2016) use a process-rich, complex 1D model to calibrate and perform uncertainty and sensitivity analyses of thermalhydrology models of ice-wedge polygons. Our analysis augments these by providing insights into lateral fluid flow. Abolt et al. (2020) perform a sensitivity analysis of the thermal effects of ice-wedge thaw on individual polygons using a full-physics 485 thermal-hydrology model. Our analysis adds to this research by providing indications of the drainage patterns that would exist along with the thermal effects. Jan et al. (2020) calibrate a full-physics thermal-hydrology model of ice-wedge polygons using field data, but since the focus of their research is calibration, they do not investigate drainage pathways. As a result, our analysis provides new information that augments existing research, helps the Arctic hydrology research community gain an intuitive understanding of inundated ice-wedge polygon drainage, and provides new modeling and experimental research directions 490 based on the idealized base cases considered here.

4.4 **Calibration implications**

The calibration to field data builds confidence in our sensitivity analysis and helps identify factors which need to be considered by any hydrologic model to simulate drainage from an inundated polygon center. Using a parsimonious model, we were able to identify the refinements required in a polygon drainage model to capture center water levels. Using more complex models 495 would likely obfuscate the identification of these refinements. The final model formulation provides a fast model for predicting the manner and timing of polygon drainage driven by environmental factors. The calibration of the model, driven by transient boundary conditions, provides confidence in the real-world applicability of the sensitivity analysis based on comparisons of steady-state snapshots of the model.

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The first refinement is a precipitation multiplier and is based on a simple mass balance indicating that the measured precipitation cannot account for the total increase in ponded water levels after precipitation events. The second refinement is a thaw-depth dependent vertical hydraulic conductivity that accounts for the decreased hydraulic conductivity of deeper soil layers. This refinement accounts for the decrease in vertical hydraulic conductivities as the thaw depth increases and includes less hydraulically conductive soils. The final calibration provides a good match to measurements, with a sub-centimeter RMSE of 0.37 cm and an R^2 (equivalent to the Nash-Sutcliffe Efficiency here) of 0.96. A key insight from our research is that polygon 505 drainage models need to consider decreases in effective vertical hydraulic conductivity with increasing thaw depth. This research enhances our hydrologic understanding of an Arctic landscape that is undergoing rapid transition due to a warming climate. The hydrology of these landscapes has important implications concerning carbon transport and emissions, subsidence,

and Arctic shrubification, to name a few Arctic processes of concern.

5 Conclusions

- 510 Our results affirm that existing conceptualizations of polygon drainage need revisiting, as was implied by a preliminary analysis conducted by Zlotnik et al. (2020). Fundamental hydrological principles indicate that, due to low-centered polygon geometry and hydraulic properties, inundated polygon drainage flux will not be uniform throughout the thawed soil layer. This result indicates that while some portions of the polygon thaw layer will be well flushed, other portions will be poorly flushed. This has important implications for the aqueous transport of carbon and other dissolved nutrients from polygonal tundra. It also
- 515 indicates the potential for focused advective heat transport from the ponded water towards the ice-wedge tops, which could enhance ice-wedge degradation. Within this context, we provide the following conclusions:

- We provide rigorous confirmation that the majority of drainage from inundated ice-wedge polygon centers occurs along an annular region along their radial periphery; however, polygon geometry and hydraulic conductivity anisotropy significantly impact the drainage pathways, as originally postulated by Zlotnik et al. (2020). This implies that nutrient flushing and the advective thermal transfer will be focused along polygon edges, neglecting the polygon center. Additionally, our results indicate that:

- A combination of high aspect ratio (wide, shallow polygons) and high anisotropy (preferential horizontal flow) results in the greatest spreading of drainage flow towards the middle of the polygon center and the largest fraction of the polygon volume being accessed by drainage flow. In these cases, the nutrient flushing will be more uniform than other cases and advective heat transport towards the ice-wedge top will be less focused and therefore less able to thaw the ice-wedge top.
- A combination of high aspect ratio (wide, shallow polygons) and low anisotropy (preferential vertical flow) result in the greatest focusing of drainage flow and the smallest fraction of the polygon volume being accessed by drainage flow. In these cases, nutrient flushing will be more localized along the outer edge of the polygon (non-uniform) and the advective heat transport towards the ice-wedge tops most focused, likely resulting in greater degradation of ice-wedges than in other cases.
- Combinations of aspect ratio and anisotropy have counteracting effects of radial versus vertical extension/contraction of drainage pathways, producing non-monotonic relationships between aspect ratio/anisotropy and accessed volume (curved feature in accessed volume response surface in Figure 6). Therefore, the combined, non-linear effects of geometry and anisotropy on drainage patterns must be considered when evaluating nutrient flushing and advective heat transport.
- Polygon drainage time has an approximately positive linear relationship with aspect ratio; in other words, wide, shallow polygons drain slowly while small, deep polygons drain quickly. This implies that polygonal tundra with larger polygons may drain more slowly than tundra composed of smaller polygons.
- Polygon drainage time has a negative exponential relationship with anisotropy. In other words, increases in preferential horizontal flow lead to exponentially faster drainage. Therefore, polygonal tundra with greater preferential horizontal

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flow, due to more pronounced horizontal stratigraphy or ice lens development, will drain faster, while less horizontally stratified tundra, due to cryoturbation, for example, will drain more slowly.

A simple analytical solution based on hydrological first principles is able to capture ice-wedge polygon drainage dynamics over an entire thaw season. Consideration within the model of runoff from topographic highs (rims) during rain events and decreasing effective vertical hydraulic conductivity with increasing thaw depth are required to match field measurements. We were able to identify these necessary model components by using a parsimonious model that has the ability to fail.

Code availability. Matlab code of the analytical solution is available via Zlotnik et al. (2020) at http://www.mdpi.com/2073-4441/12/12/3376/s1.

Video supplement. A video illustrating the validation of the analytical solution to an inundated ice-wedge polygon drainage event in 2012 near Utqiagvik is available via Zlotnik et al. (2020) at http://www.mdpi.com/2073-4441/12/12/3376/s1.

Appendix A

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Here, we present the analytical solutions for hydraulic heads and stream function under the center of an inundated ice-wedge polygon and the depletion curve of the ponded water height due to drainage to the surrounding trough. For details on the derivations and validation of the model, refer to Zlotnik et al. (2020).

555 A1 Hydraulic head and stream function analytical solutions

We idealize the subsurface below the center region of a low-centered polygon as a thin cylinder with radius in the horizontal direction and length in the vertical direction (refer to Figure 1). Based on this approximation, the hydraulic heads (h(r, z, t)) in an inundated polygon will satisfy the following equation:

$$\frac{K_r}{r}\frac{\partial}{\partial r}\left(r\frac{\partial h}{\partial r}\right) + K_z\frac{\partial^2 h}{\partial z^2} = S_s\frac{\partial h}{\partial t}.$$
(A1)

560 However, considering that storativity is negligible given the vertical and horizontal scale of the domain, the right-hand term can be neglected as

$$\frac{K_r}{r}\frac{\partial}{\partial r}\left(r\frac{\partial h}{\partial r}\right) + K_z\frac{\partial^2 h}{\partial z^2} = 0,\tag{A2}$$

where h is the hydraulic head, r is the radial coordinate, z is the depth coordinate (positive in the downward vertical direction), K_r is the horizontal (radial) hydraulic conductivity, K_z is the vertical hydraulic conductivity, t is time, and S_s is specific 565 storage. The system is fully specified by ensuring that (BC1) the heads along the central vertical axis (h(0, z, t)) are finite, (BC2) the heads along the ground surface are equal to the height of ponded water in the polygon center ($h(r, 0, t) = H_c(t)$), (BC3) the change in heads along the outer vertical boundary is governed by the change in heads along the boundary and the height of water in the trough (H_t)

$$-K_r \frac{\partial h(R,z,t)}{\partial r} = \kappa (h(R,z,t) - H_t), \tag{A3}$$

570 (BC4) the bottom of the model has a zero head gradient

$$\frac{\partial h(r,L,t)}{\partial z} = 0, \ 0 < r < R,\tag{A4}$$

and (BC5) the change in volume of ponded water in the polygon center is related to the vertical head gradients along the ground surface,

$$\pi R^2 \frac{dH_c(t)}{dt} = 2\pi K_z \int_0^R \frac{\partial h(r,0,t)}{\partial z} r dr, \ H_c(0) = H_{c,0},$$
(A5)

575 where R is the radius of the polygon, L is the depth of the thawed subsurface of the polygon, $H_c(t)$ is the ponded water height in the center of the polygon at time t, H_t is the height of water in the trough, and κ characterizes the conductance to flow across the drainage interface to the trough (in our case, the hydraulic conductance of the soil layer under the rim).

Using dimensionless coordinates and parameters defined as

$$r^* = \frac{r}{L}\sqrt{\frac{K_z}{K_r}}, \quad z^* = \frac{z}{L}, \quad R^* = \frac{R}{L}\sqrt{\frac{K_z}{K_r}}, \quad \text{Bi} = \frac{\kappa L}{\sqrt{K_r K_z}}, \tag{A6}$$

580 dimensionless solutions for hydraulic heads and the stream function can be obtained as

$$h^{*}(r^{*}, z^{*}) = \frac{h(r, z, t) - H_{t}}{H_{c}(t) - H_{t}} = 2\sum_{n=1}^{\infty} \frac{J_{1}(\lambda_{n}R^{*})}{\lambda_{n}R^{*}\left[J_{0}^{2}(\lambda_{n}R^{*}) + J_{1}^{2}(\lambda_{n}R^{*})\right]} \frac{\cosh(\lambda_{n}(1 - z^{*}))}{\cosh(\lambda_{n})} J_{0}(\lambda_{n}r^{*})$$
(A7)

and

$$\Psi^*(r^*, z^*) = \frac{\psi(r^*, z^*)}{\psi(R^*, 0)} = 2\sum_{n=1}^{\infty} \frac{J_1(\lambda_n R^*) J_1(\lambda_n r^*) r^*}{\lambda_n R^* [J_0^2(\lambda_n R^*) + J_1^2(\lambda_n R^*)]} \frac{\sinh(\lambda_n (1 - z^*))}{\cosh(\lambda_n)},\tag{A8}$$

respectively, where J_m , with m=0 or 1, is the Bessel function of the first kind of mth order and λ_n is the nth root of the equation

$$\lambda_n J_1(\lambda_n R^*) = \operatorname{Bi} J_0(\lambda_n R^*), \ n = 1, 2, \dots$$
(A9)

The solutions can be verified by direct substitution of equations A7 and A8 into the boundary value problem defined by equations A2 to A6.

A2 Ponded height depletion curve analytical solution

590 The ponded height depletion curve can be defined as

$$H_c(t) = H_t + [H_{c,0} - H_t]e^{-t/t_L},$$
(A10)

where t_L is the characteristic depletion time defined as

$$t_L = \frac{R^2}{2K_r LF(\mathrm{Bi}, R^*)},\tag{A11}$$

which is the time when $H_c(t)/H_{c,0} = 1/e$; in other words, when the ponded height is approximately 37% of its initial. The function $F(\text{Bi}, R^*)$ can be evaluated as

$$F(\mathbf{B}\mathbf{i}, R^*) = \int_{0}^{R^*} \frac{\partial h^*(r^*, 0)}{\partial z^*} r^* dr^* = 2 \sum_{n=1}^{\infty} \frac{\tanh(\lambda_n)}{\lambda_n \left[(\lambda_n / \mathbf{B}\mathbf{i})^2 + 1 \right]}.$$
 (A12)

The depletion curve can be expressed in non-dimensional terms as

$$H^*(t^*) = \frac{H_c(t) - H_t}{H_{c,0} - H_t} e^{-t^*},$$
(A13)

where non-dimensional time $t^* = t/t_L$. The solution can be verified by direct substitution of equation A10 into equation A5.

600 *Author contributions*. DH and VZ developed the conceptual model of inundated polygonal tundra hydrology. VZ derived the analytical solutions. VZ and DH encoded the analytical solutions. CA created Figure 1. DH created Figures 3-10. AA provided text for the Introduction and Discussion sections. EJ provided text for the discussion section. AA, BN, EJ, and CW provided critical reviews of the manuscript. CW secured funding.

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References

610

625

Abnizova, A., Siemens, J., Langer, M., and Boike, J.: Small ponds with major impact: The relevance of ponds and lakes in permafrost landscapes to carbon dioxide emissions, Global Biogeochemical Cycles, 26, 2012.

- Abolt, C. J. and Young, M. H.: High-resolution mapping of spatial heterogeneity in ice wedge polygon geomorphology near Prudhoe Bay, Alaska, Scientific Data, in revision, 2020.
 - Abolt, C. J., Young, M. H., Atchley, A. L., and Harp, D. R.: Microtopographic control on the ground thermal regime in ice wedge polygons, The Cryosphere (Online), 12, 2018.
- 615 Abolt, C. J., Young, M. H., Atchley, A. L., and Wilson, C. J.: Brief communication: Rapid machine-learning-based extraction and measurement of ice wedge polygons in high-resolution digital elevation models, The Cryosphere (Online), 13, 2019.
 - Abolt, C. J., Young, M. H., Atchley, A. L., Harp, D. R., and Coon, E. T.: Feedbacks between surface deformation and permafrost degradation in ice wedge polygons, Arctic Coastal Plain, Alaska, Journal of Geophysical Research: Earth Surface, 125, e2019JF005 349, 2020.
- Atchley, A. L., Painter, S. L., Harp, D. R., Coon, E. T., Wilson, C. J., Liljedahl, A. K., and Romanovsky, V. E.: Using field observations to
 inform thermal hydrology models of permafrost dynamics with ATS (v0. 83), Geoscientific Model Development, 8, 2701–2722, 2015.
 - Atchley, A. L., Coon, E. T., Painter, S. L., Harp, D. R., and Wilson, C. J.: Influences and interactions of inundation, peat, and snow on active layer thickness, Geophysical Research Letters, 43, 5116–5123, 2016.
 - Bear, J.: Hydraulics of groundwater New York, Mc GrawHill Inc, New York, 1979.

Beckwith, C. W., Baird, A. J., and Heathwaite, A. L.: Anisotropy and depth-related heterogeneity of hydraulic conductivity in a bog peat. I: laboratory measurements. Hydrological processes, 17, 89–101, 2003.

- Billings, W. and Peterson, K.: Vegetational change and ice-wedge polygons through the thaw-lake cycle in Arctic Alaska, Arctic and Alpine Research, 12, 413–432, 1980.
 - Boike, J., Wille, C., and Abnizova, A.: Climatology and summer energy and water balance of polygonal tundra in the Lena River Delta, Siberia, Journal of Geophysical Research: Biogeosciences, 113, 2008.
- 630 Brown, J., Ferrians Jr, O., Heginbottom, J., and Melnikov, E.: Circum-Arctic map of permafrost and ground-ice conditions, US Geological Survey Reston, VA, 1997.
 - Brown, V. A., McDonnell, J. J., Burns, D. A., and Kendall, C.: The role of event water, a rapid shallow flow component, and catchment size in summer stormflow, Journal of Hydrology, 217, 171–190, 1999.

Cedergren, H. R.: Seepage, drainage, and flow nets, John Wiley & Sons, New York, 1968.

- Conway, T. and Steele, L.: Carbon dioxide and methane in the Arctic atmosphere, Journal of Atmospheric Chemistry, 9, 81–99, 1989.
 Cory, R. M., Ward, C. P., Crump, B. C., and Kling, G. W.: Sunlight controls water column processing of carbon in arctic fresh waters, Science, 345, 925–928, 2014.
 - Cresto-Aleina, F., Brovkin, V., Muster, S., Boike, J., Kutzbach, L., Sachs, T., and Zuyev, S.: A stochastic model for the polygonal tundra based on Poisson-Voronoi diagrams, Earth System Dynamics, 4, 187–198, 2013.
- Freeze, R. A. and Cherry, J. A.: Groundwater, Prentice-Hall, Englewood Cliffs, New Jersey, 1979.
 Harp, D. R., Atchley, A. L., Painter, S. L., Coon, E. T., Wilson, C. J., Romanovsky, V. E., and Rowland, J. C.: Effect of soil property uncertainties on permafrost thaw projections: a calibration-constrained analysis, The Cryosphere, 10, 341–358, 2016.
 - Harr, M.: Groundwater and Seepage, McGraw-Hill, New York, 1962.

Heikoop, J. M., Throckmorton, H. M., Newman, B. D., Perkins, G. B., Iversen, C. M., Roy Chowdhury, T., Romanovsky, V., Graham, D. E.,

- 645 Norby, R. J., Wilson, C. J., et al.: Isotopic identification of soil and permafrost nitrate sources in an Arctic tundra ecosystem, Journal of Geophysical Research: Biogeosciences, 120, 1000–1017, 2015.
 - Helbig, M., Boike, J., Langer, M., Schreiber, P., Runkle, B. R., and Kutzbach, L.: Spatial and seasonal variability of polygonal tundra water balance: Lena River Delta, northern Siberia (Russia), Hydrogeology journal, 21, 133–147, 2013.
- Hinzman, L., Busey, B., Cable, W., and Romanovsky, V.: Surface meteorology, Barrow, Alaska, Area A, B, C and D, ongoing from 2012,
 Next Generation Ecosystem Experiments Arctic Data Collection, Oak Ridge National Laboratory, U.S. Department of Energy, Oak Ridge,
- Tennessee, USA. Data accessed on December 28, 2020 at https://doi.org/10.5440/1164893, 2014.
 - Hugelius, G., Strauss, J., Zubrzycki, S., Harden, J. W., Schuur, E., Ping, C.-L., Schirrmeister, L., Grosse, G., Michaelson, G. J., Koven, C. D., et al.: Estimated stocks of circumpolar permafrost carbon with quantified uncertainty ranges and identified data gaps, Biogeosciences, 11, 2014.
- 655 Jafarov, E., Parsekian, A., Schaefer, K., Liu, L., Chen, A., Panda, S., and Zhang, T.: Estimating active layer thickness and volumetric water content from ground penetrating radar measurements in Barrow, Alaska, Geoscience data journal, 4, 72–79, 2017.
 - Jan, A., Coon, E. T., Graham, J. D., and Painter, S. L.: A subgrid approach for modeling microtopography effects on overland flow, Water Resources Research, 54, 6153–6167, 2018a.
 - Jan, A., Coon, E. T., Painter, S. L., Garimella, R., and Moulton, J. D.: An intermediate-scale model for thermal hydrology in low-relief permafrost-affected landscapes, Computational Geosciences, 22, 163–177, 2018b.

660

- Jan, A., Coon, E. T., and Painter, S. L.: Evaluating integrated surface/subsurface permafrost thermal hydrology models in ATS (v0. 88) against observations from a polygonal tundra site, Geoscientific Model Development, 13, 2259–2276, 2020.
- Jorgenson, M. T., Shur, Y. L., and Pullman, E. R.: Abrupt increase in permafrost degradation in Arctic Alaska, Geophysical Research Letters, 33, 2006.
- 665 Jorgenson, M. T., Kanevskiy, M., Shur, Y., Moskalenko, N., Brown, D., Wickland, K., Striegl, R., and Koch, J.: Role of ground ice dynamics and ecological feedbacks in recent ice wedge degradation and stabilization, Journal of Geophysical Research: Earth Surface, 120, 2280– 2297, 2015.
 - King, T. V., Neilson, B. T., Overbeck, L. D., and Kane, D. L.: A distributed analysis of lateral inflows in an Alaskan Arctic watershed underlain by continuous permafrost, Hydrological Processes, 34, 633–648, 2020.
- 670 Koch, J. C.: Lateral and subsurface flows impact arctic coastal plain lake water budgets, Hydrological Processes, 30, 3918–3931, 2016. Koch, J. C., Gurney, K., and Wipfli, M. S.: Morphology-dependent water budgets and nutrient fluxes in Arctic thaw ponds, Permafrost and Periglacial Processes, 25, 79–93, 2014.
 - Koch, J. C., Jorgenson, M. T., Wickland, K. P., Kanevskiy, M., and Striegl, R.: Ice wedge degradation and stabilization impact water budgets and nutrient cycling in Arctic trough ponds, Journal of Geophysical Research: Biogeosciences, 123, 2604–2616, 2018.
- 675 Lachenbruch, A. H.: Mechanics of thermal contraction cracks and ice-wedge polygons in permafrost, vol. 70, Geological Society of America, 1962.
 - Lara, M. J., McGuire, A. D., Euskirchen, E. S., Tweedie, C. E., Hinkel, K. M., Skurikhin, A. N., Romanovsky, V. E., Grosse, G., Bolton, W. R., and Genet, H.: Polygonal tundra geomorphological change in response to warming alters future CO 2 and CH 4 flux on the Barrow Peninsula, Global Change Biology, 21, 1634–1651, 2015.
- 680 Larouche, J. R., Abbott, B. W., Bowden, W. B., and Jones, J. B.: The role of watershed characteristics, permafrost thaw, and wildfire on dissolved organic carbon biodegradability and water chemistry in Arctic headwater streams, Biogeosciences, 12, 4221–4233, 2015.

Laurion, I. and Mladenov, N.: Dissolved organic matter photolysis in Canadian arctic thaw ponds, Environmental Research Letters, 8, 035 026, 2013.

Leffingwell, E. d. K.: Ground-ice wedges: The dominant form of ground-ice on the north coast of Alaska, The Journal of Geology, 23,

685

635-654, 1915.

Lewkowicz, A. G.: Ice-wedge rejuvenation, fosheim peninsula, ellesmere Island, Canada, Permafrost and Periglacial Processes, 5, 251–268, 1994.

Liljedahl, A. K. and Wilson, C. J.: Ground Water Levels for NGEE Areas A, B, C and D, Barrow, Alaska, 2012-2014, Next Generation Ecosystem Experiments Arctic Data Collection, Oak Ridge National Laboratory, U.S. Department of Energy, Oak Ridge, Tennessee,

690 USA. Data accessed on February 8, 2020 at https://doi.org/10.5440/1183767, 2016.

- Liljedahl, A. K., Boike, J., Daanen, R. P., Fedorov, A. N., Frost, G. V., Grosse, G., Hinzman, L. D., Iijma, Y., Jorgenson, J. C., Matveyeva, N., et al.: Pan-Arctic ice-wedge degradation in warming permafrost and its influence on tundra hydrology, Nature Geoscience, 9, 312, 2016.
- Mackay, J.: Thermally induced movements in ice-wedge polygons, western Arctic coast: a long-term study, Géographie physique et Quaternaire, 54, 41-68, 2000.
- Mackay, J. R.: The world of underground ice, Annals of the Association of American Geographers, 62, 1–22, 1972.
 - Mackay, J. R.: Active layer slope movement in a continuous permafrost environment, Garry Island, Northwest Territories, Canada, Canadian Journal of Earth Sciences, 18, 1666–1680, 1981.
 - Mackay, J. R.: Some observations on the growth and deformation of epigenetic, syngenetic and anti-syngenetic ice wedges, Permafrost and Periglacial Processes, 1, 15–29, 1990.
- 700 Matsuoka, N. and Moriwaki, K.: Frost heave and creep in the Sør Rondane Mountains, Antarctica, Arctic and Alpine Research, 24, 271–280, 1992.
 - McDonnell, J., Owens, I. F., and Stewart, M.: A CASE STUDY OF SHALLOW FLOW PATHS IN A STEEP ZERO-ORDER BASIN 1, JAWRA Journal of the American Water Resources Association, 27, 679–685, 1991.
- Minke, M., Donner, N., Karpov, N. S., de Klerk, P., and Joosten, H.: Distribution, diversity, development and dynamics of polygon mires:
 examples from Northeast Yakutia (Siberia), Peatlands Internation, pp. 36–40, 2007.
 - Moore, T. and Dalva, M.: Methane and carbon dioxide exchange potentials of peat soils in aerobic and anaerobic laboratory incubations, Soil Biology and Biochemistry, 29, 1157–1164, 1997.
 - Newman, B. D., Throckmorton, H. M., Graham, D. E., Gu, B., Hubbard, S. S., Liang, L., Wu, Y., Heikoop, J. M., Herndon, E. M., Phelps, T. J., Wilson, C. J., and Wullschleger, S. D.: Microtopographic and depth controls on active layer chemistry in Arctic polygonal ground,
- 710 Geophysical Research Letters, 42, 1808–1817, 2015.
 - Nitzbon, J., Langer, M., Westermann, S., Martin, L., Aas, K. S., and Boike, J.: Pathways of ice-wedge degradation in polygonal tundra under different hydrological conditions, The Cryosphere, 13, 1089–1123, 2019.

Nitzbon, J., Westermann, S., Langer, M., Martin, L. C., Strauss, J., Laboor, S., and Boike, J.: Fast response of cold ice-rich permafrost in northeast Siberia to a warming climate, Nature Communications, 11, 1–11, 2020.

- 715 Norby, R. J., Sloan, V. L., Iversen, C. M., and Childs, J.: Controls on fine-scale spatial and temporal variability of plant-available inorganic nitrogen in a polygonal tundra landscape, Ecosystems, 22, 528–543, 2019.
 - O'Shea, S., Allen, G., Gallagher, M., Bower, K., Illingworth, S., Muller, J., Jones, B., Percival, C., Bauguitte, S., Cain, M., et al.: Methane and carbon dioxide fluxes and their regional scalability for the European Arctic wetlands during the MAMM project in summer 2012, Atmospheric Chemistry and Physics, 14, 13159–13174, 2014.

- 720 Painter, S. L.: Three-phase numerical model of water migration in partially frozen geological media: model formulation, validation, and applications, Computational Geosciences, 15, 69–85, 2011.
 - Plaza, C., Pegoraro, E., Bracho, R., Celis, G., Crummer, K. G., Hutchings, J. A., Pries, C. E. H., Mauritz, M., Natali, S. M., Salmon, V. G., et al.: Direct observation of permafrost degradation and rapid soil carbon loss in tundra, Nature Geoscience, 12, 627–631, 2019.
 - Pollock, M. D., O'Donnell, G., Quinn, P., Dutton, M., Black, A., Wilkinson, M., Colli, M., Stagnaro, M., Lanza, L., Lewis, E., et al.:
- Quantifying and mitigating wind-induced undercatch in rainfall measurements, Water Resources Research, 54, 3863–3875, 2018.
 Popper, K.: The logic of scientific discovery, Routledge, 2005.
 - Quinton, W. and Marsh, P.: A conceptual framework for runoff generation in a permafrost environment, Hydrological Processes, 13, 2563–2581, 1999.

Raymond, P. A., Hartmann, J., Lauerwald, R., Sobek, S., McDonald, C., Hoover, M., Butman, D., Striegl, R., Mayorga, E., Humborg, C., et al.: Global carbon dioxide emissions from inland waters, Nature, 503, 355–359, 2013.

Raynolds, M. K., Walker, D. A., Ambrosius, K. J., Brown, J., Everett, K. R., Kanevskiy, M., Kofinas, G. P., Romanovsky, V. E., Shur, Y., and Webber, P. J.: Cumulative geoecological effects of 62 years of infrastructure and climate change in ice-rich permafrost landscapes, Prudhoe Bay Oilfield, Alaska, Global change biology, 20, 1211–1224, 2014.

Rodell, M., Houser, P., Jambor, U., Gottschalck, J., Mitchell, K., Meng, C.-J., Arsenault, K., Cosgrove, B., Radakovich, J., Bosilovich, M., et al.: The global land data assimilation system, Bulletin of the American Meteorological Society, 85, 381–394, 2004.

- Romanovsky, V., Cable, W., and Dolgikh, K.: Subsurface temperature, moisture, thermal conductivity and heat flux, Barrow, Area A, B, C, D, Next Generation Ecosystem Experiments Arctic Data Collection, Oak Ridge National Laboratory, U.S. Department of Energy, Oak Ridge, Tennessee, USA. Data accessed on December 29, 2020 at https://doi.org/10.5440/1126515, 2017.
- Schuh, C., Frampton, A., and Christiansen, H. H.: Soil moisture redistribution and its effect on inter-annual active layer temperature and thickness variations in a dry loess terrace in Adventdalen, Svalbard, The Cryosphere, 11, 635, 2017.
 - Schuur, E. A., Bockheim, J., Canadell, J. G., Euskirchen, E., Field, C. B., Goryachkin, S. V., Hagemann, S., Kuhry, P., Lafleur, P. M., Lee, H., et al.: Vulnerability of permafrost carbon to climate change: Implications for the global carbon cycle, BioScience, 58, 701–714, 2008.

Shiklomanov, N. I., Streletskiy, D. A., Nelson, F. E., Hollister, R. D., Romanovsky, V. E., Tweedie, C. E., Bockheim, J. G., and Brown,

735

- Tarnocai, C., Canadell, J., Schuur, E. A., Kuhry, P., Mazhitova, G., and Zimov, S.: Soil organic carbon pools in the northern circumpolar permafrost region, Global biogeochemical cycles, 23, 2009.
- Throckmorton, H. M., Heikoop, J. M., Newman, B. D., Altmann, G. L., Conrad, M. S., Muss, J. D., Perkins, G. B., Smith, L. J., Torn, M. S., Wullschleger, S. D., et al.: Pathways and transformations of dissolved methane and dissolved inorganic carbon in Arctic tundra

watersheds: Evidence from analysis of stable isotopes, Global Biogeochemical Cycles, 29, 1893–1910, 2015.

Transtrum, M. K., Machta, B. B., and Sethna, J. P.: Geometry of nonlinear least squares with applications to sloppy models and optimization, Physical Review E, 83, 036 701, 2011.

Vaughn, L. J., Conrad, M. E., Bill, M., and Torn, M. S.: Isotopic insights into methane production, oxidation, and emissions in Arctic polygon tundra, Global change biology, 22, 3487–3502, 2016.

755 Wainwright, H. M., Dafflon, B., Smith, L. J., Hahn, M. S., Curtis, J. B., Wu, Y., Ulrich, C., Peterson, J. E., Torn, M. S., and Hubbard, S. S.: Identifying multiscale zonation and assessing the relative importance of polygon geomorphology on carbon fluxes in an Arctic tundra ecosystem, Journal of Geophysical Research: Biogeosciences, 120, 788–808, 2015.

J.: Decadal variations of active-layer thickness in moisture-controlled landscapes, Barrow, Alaska, Journal of Geophysical Research: Biogeosciences, 115, 2010.

⁷⁴⁵ Biog

Wales, N. A., Gomez-Velez, J. D., Newman, B. D., Wilson, C. J., Dafflon, B., Kneafsey, T. J., Soom, F., and Wullschleger, S. D.: Understanding the Relative Importance of Vertical and Horizontal Flow in Ice-Wedge Polygons, Hydrology and Earth System Sciences,

760 24, 1109–1129, 2020.

Wolter, J., Lantuit, H., Fritz, M., Macias-Fauria, M., Myers-Smith, I., and Herzschuh, U.: Vegetation composition and shrub extent on the Yukon coast, Canada, are strongly linked to ice-wedge polygon degradation, Polar Research, 35, 27489, 2016.

Wright, N., Hayashi, M., and Quinton, W. L.: Spatial and temporal variations in active layer thawing and their implication on runoff generation in peat-covered permafrost terrain, Water Resources Research, 45, 2009.

765 Zhu, X., Zhuang, Q., Gao, X., Sokolov, A., and Schlosser, C. A.: Pan-Arctic land–atmospheric fluxes of methane and carbon dioxide in response to climate change over the 21st century, Environmental Research Letters, 8, 045 003, 2013.

Zlotnik, V., Harp, D. R., and Abolt, C. J.: A Model of Ice Wedge Polygon Drainage in Changing Arctic Terrain, Water, 12, 3376, https://doi.org/doi:10.3390/w12123376, 2020.

Zona, D., Lipson, D., Zulueta, R., Oberbauer, S., and Oechel, W.: Microtopographic controls on ecosystem functioning in the Arctic Coastal

⁷⁷⁰ Plain, Journal of Geophysical Research: Biogeosciences, 116, 2011.