

1 **Abstract** When black carbon (BC) is mixed internally with other atmospheric particles,
2 the BC light absorption effect is enhanced. This study explicitly resolved the optical
3 properties of coated BC in snow based on the core/shell Mie theory and the snow, ice,
4 and aerosol radiative model (SNICAR). Our results indicated that the BC coating effect
5 enhances the reduction in snow albedo by a factor ranging from 1.1–1.8 for a
6 nonabsorbing shell and 1.1–1.3 for an absorbing shell, depending on the BC
7 concentration, snow grain radius, and core/shell ratio. We developed parameterizations
8 of the BC coating effect for application to climate models, which provides a convenient
9 way to accurately estimate the climate impact of BC in snow. Finally, based on a
10 comprehensive set of in situ measurements across the Northern Hemisphere, we
11 determined that the contribution of the BC coating effect to snow light absorption
12 exceeds that of dust over northern China. Notably, high enhancements of snow albedo
13 reduction due to the BC coating effect were found in the Arctic and Tibetan Plateau,
14 suggesting a greater contribution of BC to the retreat of Arctic sea ice and Tibetan
15 glaciers.

16

1 **1 Introduction**

2 Snow is the most reflective natural substance on the surface of Earth and covers
3 more than 30% of the global land area (Cohen and Rind, 1991). Snow albedo feedback
4 is considered one of the major energy balance factors of the climate system. Previous
5 observations have revealed that light-absorbing particles (LAPs; e.g., black carbon
6 (BC), organic carbon (OC), and mineral dust) within snow may reduce snow albedo
7 and enhance the absorption of solar radiation (Hadley and Kirchstetter, 2012). As a
8 result, LAPs play a major role in the alteration of snow morphology and snowmelt
9 processes and therefore yield important effects on local hydrological cycles and global
10 climate (Qian et al., 2009).

11 Given the importance of the climate feedback caused by LAPs in snow, studies
12 have developed snow radiative models and sought to improve our understanding of the
13 influence of LAP-contaminated snow on climate. For example, Warren and Wiscombe
14 (1980) developed a radiative forcing model based on the Mie theory and the δ -
15 Eddington approximation and reported that snow albedo at visible wavelengths could
16 be reduced by 5%–15% with 1000 ng g⁻¹ BC in snow. Flanner et al. (2007) established
17 a more comprehensive snow albedo model (the snow, ice, and aerosol radiation model;
18 SNICAR) for a multilayer snowpack based on the two-stream radiative transfer solution.
19 In addition to BC, the SNICAR model also considers the potential effects of dust
20 particles and volcanic ash on snow albedo. Recently, studies have indicated that the
21 mixing state of BC and snow could effectively alter snow albedo (Liou et al., 2011,

1 2014; Flanner et al., 2012; Liu et al., 2012; He et al., 2017, 2018a, b, c). Moreover, the
2 snow grain shape exerts an important influence on snow albedo (Kokhanovsky and
3 Zege, 2004). Nonspherical snow grains attain a lower albedo reduction than that due to
4 spherical snow grains (He et al., 2018c; Dang et al., 2016).

5 Although efforts have been made to optimize snow albedo models, current models
6 still suffer from major limitations. Studies have demonstrated that when BC in the
7 atmosphere is coated with other aerosols, this greatly enhances light absorption via a
8 lensing effect over uncoated BC, as investigated via model simulations (e.g., Jacobson
9 2001; Matsui et al., 2018) and experimental measurements (e.g., Cappa et al., 2012;
10 Peng et al., 2016). Moreover, coated BC has been observed to persist for only a few
11 hours after emission in certain regions (Moteki et al., 2007; Moffet and Prather, 2009).
12 Global aerosol models that simulate microphysical processes have revealed that most
13 BC is mixed with other particles within 1–5 days (Jacobson, 2001) at all altitudes
14 (Aquila et al., 2011). However, it remains uncertain whether coated BC occurs in real
15 snowpacks because the coating materials (e.g., salts and OC) other than BC may
16 dissolve during wet deposition. A recent study observing the individual particle
17 structure and mixing states between glaciers–snowpacks and the atmosphere based on
18 field measurements and laboratory transmission electron microscopy (TEM) and
19 energy dispersive X-ray spectrometry (EDX) instrument analysis (Dong et al., 2018)
20 has provided an answer. It was found that salt-coated BC was still observed in real
21 snowpacks despite its lower proportion than that in the atmosphere due to the

1 dissolution effect during snow precipitation. Regarding OC, the above study did not
2 observe reduced OC components in LAPs. More notably, it was also determined that
3 the proportion of coated BC was even higher in snowpacks than that in the atmosphere.
4 All of the above observation results demonstrate that coated BC particles occur in real
5 snowpacks and are even more common than those occurring in the atmosphere. Hence,
6 the climate impacts of BC must be evaluated within the context of the BC coating effect
7 on light absorption enhancement.

8 Although the BC coating effect on light absorption enhancement in the atmosphere
9 has been broadly acknowledged, little research has been carried out on snow albedo.
10 Flanner et al. (2007) developed the first radiative transfer model to investigate the
11 coating effect on snow albedo, thereby employing sulfate as BC particle coating
12 material with a constant absorption enhancement factor of ~ 1.5 . Subsequently, Wang et
13 al. (2017) considered a similar constant light absorption enhancement factor in their
14 spectral albedo model for dirty snow (SAMDS). However, the above factor varies with
15 the optical properties of different coating materials, core/shell ratio, wavelength, and
16 other parameters in real environments (Lack and Cappa, 2010; Liu et al., 2017). For
17 example, Liu et al. (2017) reported that the core/shell ratio notably controls light
18 absorption enhancement. You et al. (2016) suggested that light absorption enhancement
19 is highly correlated with visible or near-infrared (NIR) wavelengths and coating
20 material. Furthermore, a core/shell Mie theory-based simulation study (Lack and Cappa,
21 2010) found that the attained light absorption enhancement was smaller for mildly

1 absorbing coatings (e.g., OC) than that attained for nonabsorbing coatings (e.g., sulfate).
2 Hence, the use of a constant enhancement factor may result in biased simulation
3 estimates, which prevents us from obtaining a better understanding of the hydrological
4 and climate impacts of BC in snow.

5 In this study, we apply the core/shell Mie theory to calculate the optical properties
6 of coated BC considering both mildly absorbing OC and nonabsorbing sulfate and
7 incorporate these results into the SNICAR model to evaluate the influence on snow
8 albedo. Parameterizations of the BC coating effect are then developed for application
9 in other snow albedo and climate models. Finally, we estimate the enhancement of snow
10 albedo reduction and the associated radiative forcing due to the BC coating effect across
11 the Northern Hemisphere by combining model simulations with in situ observations of
12 the BC and OC concentrations in snow.

13 **2 Methods**

14 **2.1 Modeling**

15 **2.1.1 Optical parameter calculations for snow coated in BC**

16 Figure 1a and 1c show schematics of light absorption by externally and internally
17 mixed particles (EMPs and IMPs, respectively). EMPs are particles not coated in BC
18 mixed with other particles, while IMPs include BC, which is assumed to be the core
19 material coating particles and acts as a shell (Kahnert et al., 2012). Regarding the
20 nonabsorbing shell, the overall light absorption includes contributions of the BC core
21 and absorption enhancement due to the lensing effect, while regarding the absorbing

1 shell, the shell itself also contributes to light absorption. The lensing effect indicates
2 that when BC is coated with a nonabsorbing shell (or an absorbing shell), the shell acts
3 as a lens and focuses more photons onto the core than would reach it otherwise so that
4 the light absorption effect of the BC core is enhanced (Bond et al., 2006).

5 To evaluate the BC coating effect on snow albedo, it is necessary to determine the
6 optical parameters of coated BC. The refractive index (RI) of BC was assumed to be
7 $1.95-0.79i$ following Lack and Cappa (2010), which is consistent with the original
8 SNICAR model (Flanner et al., 2007). Two types of particle shells (nonabsorbing and
9 absorbing) were considered. The nonabsorbing shell was represented with sulfate, and
10 its RI was set to be $1.55-10^{-6}i$ following the atmospheric study of Bond et al. (2006).
11 The absorbing shell was represented with OC, which is a major light-absorbing particle
12 in snow (Wang et al., 2013). The RI of OC varies with the wavelength. Here, a fixed
13 mass absorption coefficient (MAC) for OC of $0.3 \text{ m}^2 \text{ g}^{-1}$ at 550 nm, a real RI value of
14 1.55, and a particle diameter of 200 nm were assumed, following the observations of
15 Yang et al. (2009) and the study of Lack and Cappa (2010). The uncertainty in snow
16 albedo considering the BC coating effect due to the OC MAC will be discussed in
17 Section 3.4. Based on the Mie theory, an imaginary RI value of $-1.36 \times 10^{-2}i$ at 550 nm
18 was calculated. Subsequently, wavelength-dependent imaginary RI values (Figure S1)
19 were derived according to an absorption angstrom exponent (AAE) of -6 (Sun et al.,
20 2007).

21 In regard to a core/shell-structured particle, the core and shell diameters refer to

1 the BC core diameter and the whole-particle diameter, respectively. The BC diameter
2 usually ranges from ~50–120 nm in the atmosphere (Corbin et al., 2018) and are
3 typically larger by ~20 nm in snow due to the removal process via wet deposition
4 (Schwarz et al., 2013). Therefore, we assumed that the BC diameter in snow was 100
5 nm with a fixed monodisperse size distribution. The uncertainty in snow albedo of the
6 BC coating effect due to the BC size distribution will be described in Section 3.4. The
7 shell diameter was assumed to range from 110 to 300 nm based on Bond et al. (2006).
8 The above core and shell diameters, RI, and wavelength were then applied in a Mie
9 model to derive the optical parameters of core/shell particles, including the single
10 scatter albedo (SSA), asymmetry factor (g), and extinction cross-section (Q_{ext}). The
11 mass extinction coefficient (MEC) of core/shell particles was calculated based on Q_{ext}
12 and the density, given as 1.8 g cm^{-3} for BC (Bond et al., 2006), 1.2 g cm^{-3} for sulfate,
13 and 1.2 g cm^{-3} for OC (Turpin and Lim, 2001).

14 **2.1.2 Snow albedo calculations**

15 We simulated snow albedo with the SNICAR model (Flanner et al., 2007), which
16 calculates the radiative transfer in a snowpack based on the theory of Warren and
17 Wiscombe (1980) and a two-stream multilayer radiative approximation (Toon et al.,
18 1989). Here, we summarize only the model features in SNICAR that are crucial to our
19 study. The SNICAR model allows for a vertical multilayer distribution of snow
20 properties, LAPs, and heating throughout the snowpack column. The input optical
21 parameters (MEC, SSA, and g) of snow grains and BC were calculated offline with the

1 Mie theory. SNICAR provides snow albedo changes due to uncoated and sulfate-coated
2 BC particles, in addition to dust particles and volcanic ash (for further details, please
3 refer to Flanner et al., 2007).

4 In this study, we assumed a homogeneous semi-infinite snowpack and a solar
5 zenith angle of 49.5° , whose cosine value (0.65) represents the insolation-weighted
6 mean solar zenith cosine in the sunlit Earth hemisphere (Dang et al., 2015). The snow
7 grain optical effective radius was varied from 50 to 1000 μm (at 50- μm intervals) to
8 characterize snow aging. Moreover, the BC concentration was assumed to range from
9 0-1000 ng g^{-1} (at 10- ng g^{-1} intervals) to simulate clear to polluted snow, which was
10 based on global field observations of the BC concentration in snowpacks mostly below
11 1000 ng g^{-1} (e.g., Doherty et al., 2010, 2014; Wang et al., 2013; Li et al., 2017, 2018;
12 Pu et al., 2017; Zhang et al., 2017, 2018). These parameters were also applied in the
13 subsequent parameterizations (please refer to Section 2.3). In addition, we note that the
14 SNICAR model adopted in this study is the default version assuming BC-snow external
15 mixing and spherical snow grains (Flanner et al., 2007). Although the mixing state of
16 BC and snow grains and the snow grain shape affect the snow albedo, empirical
17 parameterizations describing the effect of BC internally mixed with snow grains on
18 snow albedo were developed by He et al. (2018c), and the albedo of a snowpack
19 consisting of nonspherical snow grains was simulated with smaller spherical grains
20 (Dang et al. 2016). Therefore, users may combine the empirical parameterizations
21 developed by He et al. (2018c) and Dang et al. (2016) with our empirical

1 parameterizations (please refer to Section 2.3) to study the effect of the internal mixing
2 of BC with snow grains, snow grain shape, and coated BC particles on snow albedo.

3 Regarding the SNICAR snow albedo simulations considering uncoated BC
4 particles, the concentrations of both BC and the other particles were directly input.
5 Regarding coated BC particles, the optical parameters (MEC, SSA, and g) of IMPs (as
6 calculated above) were first archived as lookup tables within the SNICAR model, and
7 the IMP concentration was then input.

8 **2.2 Calculation of the broadband snow albedo**

9 The spectral albedo (α_λ) was integrated over the solar spectrum ($\lambda = 300\text{--}2500$ nm)
10 and weighted based on the incoming solar irradiance (S_λ) to calculate the broadband
11 snow albedo ($\alpha_{\text{integrated}}$):

$$12 \quad \alpha_{\text{integrated}} = \frac{\int \alpha_\lambda S_\lambda d_\lambda}{\int S_\lambda d_\lambda} \quad (1)$$

13 The considered incoming solar irradiance was the typical surface solar spectrum
14 for mid–high latitudes from January to May, calculated with the Santa Barbara Discrete
15 Ordinate Radiative Transfer Atmospheric Radiative Transfer (SBDART) model (Pu et
16 al., 2019), which is one of the most widely applied models in radiative transfer
17 simulations (for further details, please refer to Ricchiazzi et al. 1998).

18 **2.3 Parameterizations**

19 In the original SNICAR model, the BC coating effect is simply parameterized with
20 an absorption enhancement factor of ~ 1.5 (Flanner et al., 2007). However, the BC

1 coating effect on snow albedo widely varies and depends on the BC concentration,
 2 core/shell ratio, snow grain size, and type of particle shell (please refer to Section 3.3).
 3 In view of this complexity, more explicit parameterizations were developed in this
 4 study:

$$5 \quad E_{\alpha, \text{integrated}} = \frac{\alpha_{\text{int, integrated}}}{\alpha_{\text{ext, integrated}}} \quad (2)$$

6 where $\alpha_{\text{ext, integrated}}$ and $\alpha_{\text{int, integrated}}$ are the broadband snow albedos for EMPs
 7 and IMPs, respectively. Following a previous empirical formulation (Hadley and
 8 Kirchstetter, 2012), $E_{\alpha, \text{integrated}}$ was parameterized as:

$$9 \quad E_{\alpha, \text{integrated, para}} = a_0 \times (C_{BC})^{a_1} + a_2 \quad (3)$$

$$10 \quad a_1 = b_0 \times (\log_{10}(R_{ef}/50))^{b_1} \quad (4)$$

11 where $E_{\alpha, \text{integrated, para}}$ is the parameterization of $E_{\alpha, \text{integrated}}$, C_{BC} is the BC
 12 concentration, and R_{ef} is the snow grain radius. The terms a_0 , a_1 , a_2 , b_0 , and b_1
 13 are empirical coefficients depend on the core/shell ratio and type of particle shell. To
 14 enhance the precision, the above parameterizations were divided into two groups: the
 15 first to consider relatively clean snow (at a BC concentration $< 200 \text{ ng g}^{-1}$) and the
 16 second to consider relatively polluted snow ($200 \text{ ng g}^{-1} < \text{BC concentration} < 1000 \text{ ng}$
 17 g^{-1}).

18 **2.4 Calculation of the in situ snow albedo and radiative forcing**

19 In situ broadband clear-sky ($\alpha_{\text{integrated}}^{\text{clear, in-situ}}$) and cloudy-sky ($\alpha_{\text{integrated}}^{\text{cloudy, in-situ}}$) albedos
 20 were separately calculated based on corresponding in situ snow-LAP parameters and

1 SBDART simulated clear- and cloudy-sky incoming solar irradiance levels,
 2 respectively. We assumed a semi-infinite snowpack due to the limited available snow
 3 depth measurements. The BC and OC concentrations were collected from in situ field
 4 measurements (e.g., Doherty et al., 2010, 2014; Wang et al., 2013; Li et al., 2017, 2018;
 5 Pu et al., 2017; Zhang et al., 2017, 2018). A snow grain radius of 100 (1000) μm was
 6 assumed for fresh (old) snow, which is comparable to previous observations at mid-
 7 high latitudes in winter (Wang et al., 2017; Shi et al., 2020). The value of the solar
 8 zenith angle was calculated based on the longitude, latitude, and sampling time at each
 9 sampling site. The in situ all-sky albedo ($\alpha_{\text{integrated}}^{\text{all-sky,in-situ}}$) was then calculated based on
 10 weighted clear- and cloudy-sky albedo values depending on the cloud fraction (CF),
 11 given as:

$$12 \quad \alpha_{\text{integrated}}^{\text{all-sky,in-situ}} = \text{CF} \times \alpha_{\text{integrated}}^{\text{cloudy,in-situ}} + (1 - \text{CF}) \times \alpha_{\text{integrated}}^{\text{clear,in-situ}} \quad (5)$$

13 The in situ radiative forcing due to LAPs was calculated by multiplying the derived
 14 broadband albedo reduction by the downward shortwave flux at the snow surface (Dang
 15 et al., 2017). We note that the radiative forcing was calculated with the January-
 16 February average solar radiation in NA and NC and the April-May average solar
 17 radiation in the Arctic and TP according to the periods of corresponding field campaigns.
 18 In this study, we mainly estimated the relative impacts of internal and external mixing
 19 on snow albedo and radiative forcing, which are hence not influenced by the chosen
 20 solar radiation level. Figure S2 shows spatial distributions of the solar flux and cloud
 21 fraction, which were obtained from the Clouds and the Earth's Radiant Energy System

1 (CERES) (<https://ceres.larc.nasa.gov/products.php?product=SYN1deg>).

2 **3 Results and discussion**

3 **3.1 Impact on particle light absorption**

4 Figure 1b and 1d show the light absorption enhancement and E_{abs} , respectively,
5 due to coated BC particles. E_{abs} is defined as the ratio of the light absorption due to
6 coated (LA_{int}) and uncoated BC particles (LA_{ext}) ($E_{\text{abs}} = \frac{LA_{\text{int}}}{LA_{\text{ext}}}$). Based on Bond et al.
7 (2006), we show the most common core/shell ratios (the ratio of the diameter of the
8 whole particle to that of the BC core) of 1.2, 1.5, 2.0, and 2.5 in real environments to
9 represent the thickness of shells, and we considered detailed core/shell ratios ranging
10 from 1.1 to 3.0 (at intervals of 0.1) in the parameterizations (see Section 3.5). E_{abs} varies
11 with the wavelength and increases with the core/shell ratio, in contrast to the default
12 E_{abs} value employed in the original SNICAR model, which remains constant. Regarding
13 nonabsorbing shells, the light absorption of IMPs is higher than that of EMPs across all
14 wavelengths (300–1400 nm). Regarding absorbing shells, E_{abs} is similar to that of
15 nonabsorbing shells in the NIR range but decreases in the visible (VIS) light and
16 ultraviolet (UV) light ranges, which indicates that absorbing shells reduce whole-
17 particle light absorption and negatively contribute to E_{abs} . This occurs because
18 compared to the nonabsorbing shell, the absorbing shell, although it absorbs additional
19 incident photons, causes fewer photons to reach the core, so that the photons absorbed
20 by the lensing effect and BC core are reduced. In this case, the number of additional
21 photons absorbed by the shell is smaller than the number of fewer photons absorbed by

1 the lensing effect and BC core, causing the total absorption of absorbing shell-coated
 2 BC particles to be lower than that of nonabsorbing shell-coated BC particles (Lack and
 3 Cappa, 2010). Furthermore, the absorbing shell reduces E_{abs} to <1 in the UV range at
 4 high core/shell ratios, suggesting that the lensing effect on absorption at these
 5 wavelengths does not match the BC core absorption reduction, resulting in fewer
 6 photons reaching the core, which is similar to the results reported by Lack and Cappa
 7 (2010).

8 **3.2 Impact on the spectral snow single-scattering properties and albedo**

9 In a real snowpack, BC effectively enhances the snow single-scattering co-albedo
 10 $(1-\omega)$, but its effect on other snow optical parameters, such as the asymmetry factor
 11 and extinction efficiency, is negligible (He et al., 2017). Therefore, we focus our
 12 discussion on the coating-induced enhancement of the snow single-scattering co-albedo
 13 $(E_{1-\omega})$, snow albedo (E_{α}) , and snow albedo reduction $(E_{\Delta\alpha})$. $E_{1-\omega}$ is defined as the ratio
 14 of the snow single-scattering co-albedo due to coated BC particles $(1-\omega_{\text{int}})$ to that due
 15 to uncoated BC particles $(1-\omega_{\text{ext}})$ ($E_{1-\omega} = \frac{1-\omega_{\text{int}}}{1-\omega_{\text{ext}}}$). Similar definitions were adopted for
 16 E_{α} ($E_{\alpha} = \frac{\alpha_{\text{int}}}{\alpha_{\text{ext}}}$) and $E_{\Delta\alpha}$ ($E_{\Delta\alpha} = \frac{\Delta\alpha_{\text{int}}}{\Delta\alpha_{\text{ext}}}$), where α_{int} and α_{ext} are the snow albedo values
 17 due to coated and uncoated BC particles, respectively, and $\Delta\alpha_{\text{int}}$ and $\Delta\alpha_{\text{ext}}$ are the
 18 snow albedo reductions due to coated and uncoated BC particles, respectively.

19 Figure 2 shows the variation in $1-\omega$ and $E_{1-\omega}$ depending on the BC concentration,
 20 core/shell ratio, and coating material. Regarding either the nonabsorbing or absorbing
 21 shell, $1-\omega_{\text{int}}$ is usually higher than $1-\omega_{\text{ext}}$ in the VIS range, while the coating effect

1 exerts little impact at wavelengths > 1200 nm because the optical properties of snow
2 are mainly affected by LAPs in the VIS range but primarily by snow itself at
3 wavelengths > 1200 nm. In addition, $E_{1-\omega}$ increases with increasing core/shell ratio, and
4 the wavelength with the maximum $E_{1-\omega}$ value depends on the BC concentration and
5 core/shell ratio. Moreover, the absorbing shell reveals a negative impact on $E_{1-\omega}$ over
6 the nonabsorbing shell, especially in the UV range.

7 Snow albedo is notably influenced by various factors, such as the snow grain size,
8 LAP content, and solar zenith angle, which has been widely examined and verified
9 through model simulations and experimental measurements in previous studies (e.g.,
10 Warren and Wiscombe, 1980; Hadley and Kirchstetter, 2012; Wang et al., 2017). In this
11 study, we mainly focus on the BC coating effect on snow albedo. Figure 3 shows the
12 spectral snow albedo values due to coated (α_{int}) and uncoated BC particles (α_{ext}) and
13 the ratios (E_{α}) of α_{int} to α_{ext} . Consistent with $1-\omega$, the impact of the coating effect
14 on snow albedo is mainly observed at wavelengths $< \sim 1200$ nm (Figures 3a versus 3b,
15 and Figures 3d versus 3e), where the higher the BC concentration is (or the higher the
16 core/shell ratio is), the larger the difference in snow albedo between uncoated and
17 coated BC particles. Hadley and Kirchstetter (2012) also found a lower snow albedo
18 due to internally mixed particles than that due to externally mixed particles. This
19 phenomenon is also obvious for E_{α} , which decreases with increasing BC concentration
20 and core/shell ratio in the VIS and NIR ranges (Figure 3c and 3f, respectively). At a
21 given BC concentration and core/shell ratio, E_{α} generally decreases with the

1 wavelength from the UV range to the VIS range and then increases from the VIS range
2 to the NIR range, which corresponds to the E_{abs} and $E_{1-\omega}$ results. In contrast, the E_{α}
3 values considering the nonabsorbing and absorbing shells are comparable at
4 wavelengths $> \sim 800$ nm. However, when the wavelength $< \sim 800$ nm, E_{α} considering
5 the absorbing shell is higher than that considering the nonabsorbing shell, and the
6 difference increases with decreasing wavelength and increasing core/shell ratio.
7 Moreover, regarding the absorbing shells, the snow albedo due to coated BC particles
8 is higher than that due to uncoated BC particles at $< \sim 350$ nm at high core/shell ratios
9 because the light absorption of internally mixed particles with absorbing shells is lower
10 than that of externally mixed particles at the same wavelengths, as previously described
11 in Section 3.1. These results indicate that the material of the particle shell also plays an
12 important role in snow albedo in the UV and VIS ranges. We note that the solar radiative
13 flux is very low at wavelengths < 350 nm, so that the coating effect at these wavelengths
14 may contribute little to the total light absorption and broadband snow albedo but may
15 potentially influence the photochemical reactions in a snowpack (Grannas et al., 2007).

16 Furthermore, Figure 4 shows the spectral snow albedo reduction caused by coated
17 ($\Delta\alpha_{\text{int}}$) and uncoated BC particles ($\Delta\alpha_{\text{ext}}$) and the ratio ($E_{\Delta\alpha}$) of $\Delta\alpha_{\text{int}}$ to $\Delta\alpha_{\text{ext}}$.
18 Generally, $\Delta\alpha_{\text{int}}$ is larger than $\Delta\alpha_{\text{ext}}$, and the core/shell ratio dominates the variation
19 in $E_{\Delta\alpha}$ across all wavelengths from 300-1400 nm, while the impact of the BC content
20 is mainly manifested from 500-1000 nm. Consistent with $E_{1-\omega}$ and E_{α} , the impact of the
21 material of the particle shell is negligible at a wavelength $> \sim 800$ nm, but $E_{\Delta\alpha}$ for the

1 absorbing shell is lower than that for the nonabsorbing shell at a wavelength $< \sim 800$
2 nm. Moreover, $E_{\Delta\alpha}$ is < 1 for the absorbing shell at wavelengths $< \sim 350$ nm and high
3 core/shell ratios. It is noteworthy that the coating effect still yields an obvious impact
4 on snow albedo reduction at wavelengths $> \sim 1200$ nm, which is different from $E_{1-\omega}$ and
5 E_{α} .

6 **3.3 Impact on the broadband snow single-scattering properties and albedo**

7 Compared to the spectral optical properties, our broadband results have wider
8 implications for the research community. Figure 5 shows the spectrally weighted $1-\omega$
9 due to coated ($1-\omega_{\text{int, integrated}}$) and uncoated BC particles ($1-\omega_{\text{ext, integrated}}$) and the ratio
10 ($E_{1-\omega, \text{ integrated}}$) of $1-\omega_{\text{int, integrated}}$ to $1-\omega_{\text{ext, integrated}}$. In general, $1-\omega_{\text{int, integrated}}$ is larger than
11 $1-\omega_{\text{ext, integrated}}$, and $E_{1-\omega, \text{ integrated}}$ increases with the BC concentration and core/shell ratio
12 but is little affected by the snow grain size. $E_{1-\omega, \text{ integrated}}$ ranges from 1.0 to ~ 1.35 and
13 1.0 to ~ 1.23 for the nonabsorbing and absorbing shells, respectively, with the BC
14 concentration lower than 1000 ng g^{-1} at core/shell ratios ranging from 1.2-2.5. At a
15 given BC concentration and core/shell ratio, $E_{1-\omega, \text{ integrated}}$ considering the nonabsorbing
16 shell is higher than that considering the absorbing shell. In addition, $E_{1-\omega, \text{ integrated}}$
17 determined with the original SNICAR model, is close to that considering the
18 nonabsorbing shell at a core/shell ratio of 1.5.

19 Figure 6 shows the spectrally weighted snow albedo due to coated ($\alpha_{\text{int, integrated}}$) and
20 uncoated BC particles ($\alpha_{\text{ext, integrated}}$) and the ratio ($E_{\alpha, \text{ integrated}}$) of $\alpha_{\text{int, integrated}}$ to $\alpha_{\text{ext,}}$
21 integrated . Generally, $\alpha_{\text{int, integrated}}$ is lower than $\alpha_{\text{ext, integrated}}$ by 0 to 0.069 (0 to 0.051), and

1 $E_{\alpha, \text{integrated}}$ ranges from 1 to ~ 0.903 (1 to ~ 0.924) considering the nonabsorbing
2 (absorbing) shell at BC concentrations from 0 to 1000 ng g^{-1} , with the snow grain radius
3 ranging from 100 to $500 \mu\text{m}$, and the core/shell ratio ranging from 1.2 to 2.5. $E_{\alpha, \text{integrated}}$
4 exhibits a decreasing trend with increasing BC concentration, core/shell ratio and snow
5 grain size. In addition, the difference between $\alpha_{\text{ext, integrated}}$ and $\alpha_{\text{int, integrated}}$ (or $E_{\alpha, \text{integrated}}$)
6 for the nonabsorbing shell is larger (or smaller) than that for the absorbing shell. If
7 considering these coating effects in real environments, e.g., in clean snow, such as in
8 North America at a typical BC concentration of $\sim 50 \text{ ng g}^{-1}$ (Doherty et al., 2014), the
9 difference between $\alpha_{\text{ext, integrated}}$ and $\alpha_{\text{int, integrated}}$ ranges from 0.002-0.017 and 0.001-
10 0.012 considering the nonabsorbing and absorbing shells, respectively, at core/shell
11 ratios from 1.2-2.5 and snow grain radii from 100-500 μm . In contrast, in polluted snow,
12 such as in northeastern China, the BC concentration is typically $\sim 1000 \text{ ng g}^{-1}$ in
13 industrial regions. The difference between $\alpha_{\text{ext, integrated}}$ and $\alpha_{\text{int, integrated}}$ ranges from
14 0.008-0.069 and 0.007-0.051 considering the nonabsorbing and absorbing shells,
15 respectively. These results indicate that the impact of the coating effect on snow albedo
16 may lead to a reduction in snow albedo by $\sim 2\%$ in clean snow and $\sim 10\%$ in polluted
17 snow due to coated BC particles below the snow albedo due to uncoated BC particles.
18 In addition, the sensitivity of $E_{\alpha, \text{integrated}}$ to BC decreases with increasing BC
19 concentration due to the nonlinear effect of BC on snow albedo (Flanner et al., 2007).

20 Figure 7 shows the spectrally weighted snow albedo reduction due to coated ($\Delta\alpha_{\text{int,}}$
21 integrated) and uncoated BC particles ($\Delta\alpha_{\text{ext, integrated}}$) and the ratio ($E_{\Delta\alpha, \text{integrated}}$) of $\Delta\alpha_{\text{int,}}$

1 integrated to $\Delta\alpha_{\text{ext, integrated}}$. In contrast to $E_{\alpha, \text{ integrated}}$, $E_{\Delta\alpha, \text{ integrated}}$ is dominated by the
2 core/shell ratio but slightly depends on the snow grain size (Figures 7c and 6f,
3 respectively). In addition, $E_{\Delta\alpha, \text{ integrated}}$ exhibits a slight decreasing trend with increasing
4 BC concentration. Comparing Figure 7c and f, we find that the particle shell material
5 exerts a distinct integrated impact on $E_{\Delta\alpha}$. $E_{\Delta\alpha, \text{ integrated}}$ mostly ranges from 1.11 to ~1.80
6 (1.10 to ~1.33) for the nonabsorbing (absorbing) shells at core/shell ratios from 1.2 to
7 2.5. Our results are comparable to those of a previous study in which the snow albedo
8 reduction due to BC/snow internal mixing was larger than that due to external mixing
9 by a factor of 0.2-1.0 (He et al., 2018c). However, the $E_{\Delta\alpha, \text{ integrated}}$ value retrieved from
10 the original SNICAR model demonstrates only a small variation from 1.23–1.31. This
11 is similar to the nonabsorbing shell at a core/shell ratio of ~1.5, which suggests that the
12 original SNICAR model only reflects the coating effect on snow albedo reduction at an
13 intermediate core/shell ratio, which may lead to possible biases ranging from -10% to
14 50% in snow albedo reduction calculations.

15 **3.4 Uncertainties**

16 Although the imaginary RI value of OC has been theoretically calculated (Section
17 2.1), we note that in a real snowpack, there exists a high uncertainty because the types
18 and optical properties of OC vary spatially and temporally due to different emission
19 sources and photochemical reactions in the atmosphere (e.g., Lack and Cappa, 2010).
20 To address this issue, we tested the degree of influence of the imaginary RI value on
21 the $E_{\alpha, \text{ integrated}}$, and $E_{\Delta\alpha, \text{ integrated}}$ values by increasing and decreasing the calculated

1 imaginary RI value by 50% (Figure S1), which studies have revealed to be plausible
2 (e.g., Lack et al., 2012). We found the imaginary RI uncertainty to be $\pm 1\%$ for $E_{\alpha, \text{integrated}}$
3 and $\pm 5\%$ for $E_{\Delta\alpha, \text{integrated}}$.

4 In addition, observations have demonstrated large variations in the size
5 distribution of atmospheric and snowpack BC particles (Schwarz et al., 2013), which
6 may affect the snow optical properties and albedo (He et al., 2018b). Therefore, we
7 examined the effects of the BC particle size on $E_{\alpha, \text{integrated}}$ and $E_{\Delta\alpha, \text{integrated}}$ with two
8 additional BC particle diameters of 50 and 150 nm, which occur within the observed
9 size ranges (Schwarz et al., 2013) and are comparable to the BC particle sizes adopted
10 in other studies (e.g., He et al., 2018b). We find that the uncertainty attributed to the BC
11 particle diameter is $\pm 1\%$ for $E_{\alpha, \text{integrated}}$ and $\pm 13\%$ for $E_{\Delta\alpha, \text{integrated}}$. According to Equation
12 2, the uncertainty in $E_{\alpha, \text{integrated}}$, is equivalent to that in the snow albedo, and the
13 uncertainty in $E_{\Delta\alpha, \text{integrated}}$, is equivalent to that in the snow albedo reduction. Therefore,
14 the total uncertainty related to the imaginary RI value and BC particle diameter is $\pm 1.4\%$
15 for $E_{\alpha, \text{integrated}}$ (snow albedo) and $\pm 13.9\%$ for $E_{\Delta\alpha, \text{integrated}}$ (snow albedo reduction).

16 Another important issue is that in real environments, BC mixtures containing other
17 species are likely much more complex than are uniform coatings on spheres. Hence, a
18 core-shell assumption seems somewhat dubious. However, a recent study observing the
19 individual particle structure and mixing states between glaciers–snowpacks and the
20 atmosphere (Dong et al., 2018) has found that fresh BC particles are generally
21 characterized by a fractal morphology, which abundantly occur in the atmosphere. In

1 contrast, in a snowpack, aged BC particles dominated the BC content, and the mixing
2 states of aged BC particles largely changed to internal mixing forms with BC at the
3 core. This process was characterized by the initial transformation from a fractal
4 structure to a spherical morphology and the subsequent growth of fully compact
5 particles during the transport and deposition process. Therefore, a core-shell
6 assumption for coated BC particles in a snowpack seems to be plausible. In addition,
7 most field measurements have not captured the explicit structure of coated BC particles
8 due to the limited observation methods (e.g., Doherty et al., 2010, 2014; Wang et al.,
9 2013; Li et al., 2017, 2018; Pu et al., 2017; Zhang et al., 2017, 2018); therefore, even if
10 a model of the explicit BC structure was developed, researchers experience difficulties
11 studying the effect of coated BC particles on snow albedo reduction at present.
12 Moreover, a core-shell assumption for coated BC particles in the atmosphere has been
13 widely applied in most global climate models (e.g., Jacobson, 2001; Bond et al. 2013),
14 so our parameterizations describing coated BC particles in a snowpack may be easily
15 linked to these models. In summary, we indicate that a core-shell assumption describing
16 coated BC particles in a snowpack is plausible and practical for field observations and
17 model simulations at present despite possible uncertainties. However, with the
18 development of measurement methods and climate models, a more explicit structure
19 characterizing coated BC particles in a snowpack is actually needed in the future.

20 **3.5 Parameterizations of the coating effect**

21 Figure 8 compares parameterized $E_{\alpha, \text{integrated, para}}$ values to SNICAR-modeled $E_{\alpha,}$

1 integrated values, and Tables S1 and S2, respectively, list the empirical coefficients (please
2 refer to Section 2.3) derived from the nonlinear regression process. This
3 parameterization is applicable under the assumptions of a semi-infinite snowpack, BC-
4 snow external mixing, and spherical snow grains, as mentioned in Section 2. Generally,
5 $E_{\alpha, \text{integrated, para}}$ and $E_{\alpha, \text{integrated}}$ exhibit a strong correlation, with $R^2 = 0.988$ (0.986) for
6 the nonabsorbing shell and $R^2 = 0.987$ (0.986) for the absorbing shell in relatively clean
7 (polluted) snow, and root mean squared errors of 1.81×10^{-3} (4.70×10^{-3}) and
8 1.41×10^{-3} (3.76×10^{-3}), respectively. The biases in $E_{\alpha, \text{integrated, para}}$ are the lowest at
9 intermediate BC concentrations but become relatively high at extremely low or high
10 concentrations, mainly due to processes within the nonlinear regression method. In
11 addition, the snow grain size exerts a limited impact on the accuracy of the
12 parameterized results so that these parameterizations can be applied to either fresh or
13 old snow types. Overall, the integrated E_{α} value is suitably reproduced by $E_{\alpha, \text{integrated, para}}$,
14 and the parameterizations are applicable under various snow pollution conditions
15 at BC concentrations ranging from 0-1000 ng g⁻¹, core/shell ratios ranging from 1.1 to
16 3.0, and different coating materials (nonabsorbing and absorbing shells). We note that
17 if the BC concentration is higher than 1000 ng g⁻¹, the parameterization describing
18 relatively polluted snow is also applicable with a low negative bias.

19 Therefore, future studies may estimate the BC coating effect on snow albedo and
20 radiative forcing very conveniently by combining the original SNICAR model or other
21 snow radiative forcing models with our new parameterizations, which may reduce the

1 snow albedo simulation bias. However, although most global climate models (GCMs)
2 account for coated BC particles in the atmosphere, they barely consider the BC coating
3 effect in snow (Bond et al., 2013). In addition, different GCMs apply varying types of
4 snow radiative transfer models, which indicates that one physical mechanism
5 describing the BC coating effect in snow may not be suitable for all GCMs. Hence, our
6 parameterizations are suitable for climate models and provide an option to capture BC
7 coating effects in snow.

8 **3.6 Measurement-based estimate of the coating effect**

9 To evaluate the BC coating effect on both the snow albedo and radiative forcing
10 in a real snowpack, we collected in situ measurements of BC and OC concentrations in
11 snow (Figure 9) during field campaigns in the Arctic in the spring from 2007–2009
12 (Doherty et al., 2010), in North America from January–March 2013 (Doherty et al.,
13 2014), in northern China from January–February 2010 and 2012 (Ye et al., 2012; Wang
14 et al., 2013), and on the Tibetan Plateau in the spring of 2010 and 2012 (Wang et al.,
15 2013; Li et al., 2017, 2018; Pu et al., 2017; Zhang et al., 2017, 2018). The measurements
16 were separated into four geographical regions (Figure 9c): the Arctic, North America
17 (NA), northern China (NC), and the Tibetan Plateau (TP). An absorbing shell consisting
18 of OC was assumed in the measured snowpack data, which is plausible because
19 previous studies have found that OC is the dominant coating in the atmosphere (e.g.,
20 Cappa et al., 2012) and snow (Dong et al., 2018). The OC/BC mass ratio generally
21 ranges from 1 to 10, with the corresponding core/shell ratio ranging from 1.3 to 2.5

1 (Figure 9b). The average core/shell ratio was the highest (2.45) on the TP, followed by
2 values of 1.92 and 1.81 in the Arctic and NC, respectively, and was the lowest (1.31) in
3 NA (Figure 9d). These results reveal that the BC coating effect exerted a larger impact
4 on snow albedo on the TP than that in the other regions. In this study, the assumption
5 that all measured OC occurs as a coating on BC particles was mainly adopted to reveal
6 the upper bound of the coating effect on snow albedo reduction, which is comparable
7 to previous studies (e.g., He et al. 2018c).

8 Figure 10 shows statistics of the snow albedo reduction and radiative forcing in
9 the different regions for fresh snow (snow grain radius =100 μm) and old snow (snow
10 grain radius =1000 μm). Spatial distributions of the attained snow albedo reduction and
11 radiative forcing are shown in Figures S3 and S4, respectively. Briefly, the TP
12 snowpack suffers the highest snow albedo reduction (0.066), and the regional average
13 snow albedo reduction is lower in NC (0.055), NA (0.009), and the Arctic (0.007) for
14 fresh snow in the case of external mixing (Figure 10a). Accordingly, the regional
15 average radiative forcing is 11.63, 4.42, 0.97, and 0.56 W m^{-2} on the TP, NC, NA, and
16 the Arctic, respectively (Figure 10b). In the case of internal mixing, the regional average
17 snow albedo reduction is 0.084, 0.065, 0.011, and 0.009 on the TP, NC, NA, and the
18 Arctic, respectively, with corresponding radiative forcings of 14.84, 5.51, 1.11, and
19 0.69 W m^{-2} , respectively. Figure 11 shows a comparison of internal mixing to external
20 mixing. In fresh snow, we find that coated BC particles result in greater snow albedo
21 reductions than those due to uncoated BC particles by factors of 1.27, 1.19, 1.13, and

1 1.23 on the TP, NC, NA, and the Arctic, respectively (Figures 11a and 11b, respectively).
2 Correspondingly, we find that the coating effect yields radiative forcing values of 1.27,
3 1.20, 1.14, and 1.22, respectively, in these regions. The largest (smallest) enhancement
4 was found on the TP (NA), which corresponds to the highest (lowest) OC/BC mass
5 ratio and core/shell ratio on the TP (NA). In regard to old snow, the regional average
6 snow albedo reduction is 0.17 (0.21), 0.14 (0.17), 0.028 (0.033) and 0.022 (0.027) on
7 the TP, NC, NA, and the Arctic, respectively, for external (internal) mixing (Figure 10c).
8 The corresponding radiative forcings are 38.2 (47.6), 19.2 (22.7), 4.6 (5.2) and 3.6 (4.6)
9 W m^{-2} , respectively (Figure 10d). The enhancement of snow albedo reduction due to
10 the BC coating effect is 1.24, 1.15, 1.13, and 1.23 on the TP, NC, NA, and the Arctic,
11 respectively (Figure 11c). The corresponding radiative forcing reduction is 1.24, 1.16,
12 1.14, and 1.22, respectively (Figure 11d). The enhancement exhibits a slight decrease
13 with snowpack aging, which is consistent with the results shown in Figure 7. Notably,
14 we found that the contribution of the coating effect to light absorption exceeded that of
15 dust over most areas of northern China after comparison to previous studies of dust in
16 snow (Wang et al., 2013, 2017; Pu et al., 2017), which further demonstrated the critical
17 role of the BC coating effect in snow albedo evaluation.

18 In contrast to previous studies, we note that an enhanced light absorption in snow
19 due to the BC coating effect should be considered, especially in the Arctic and TP.
20 Arctic sea ice has sharply declined in recent decades (Ding et al., 2019), and climate
21 models predict a continued decreasing trend (Liu et al., 2020) that is likely to perturb

1 the Earth system and influence human activities (Meier et al., 2014). Multimodel
2 ensemble simulations have indicated that greenhouse gases cannot fully explain this
3 decline, and recent studies have proposed that BC deposition in snow and sea ice is an
4 important additional contributor (e.g., Ramanathan and Carmichael, 2008).
5 Furthermore, the TP holds the largest ice mass outside the polar regions and acts as a
6 water storage tower for more than 1 billion people in South and East Asia. Tibetan
7 glaciers have rapidly retreated over the last 30 years (Yao et al., 2012), raising the
8 possibility that many glaciers and their freshwater supplies could disappear by the
9 middle of the 21st century. Observed evidence has suggested that BC deposition is a
10 major contributing factor to this retreat (Xu et al., 2009), but the quantitative modeling
11 of the BC effect on glacier dynamics is a challenge, partly because of the incomplete
12 radiative transfer mechanisms within current models. Due to the notable contribution
13 of BC to the retreat in Arctic sea ice and Tibetan glaciers and the strong enhancement
14 of light absorption due to coated BC particles, the coating effect must now be
15 considered in climate models that are designed to accurately reconstruct both historical
16 records and future changes.

17 **4 Conclusions**

18 This study evaluated the BC coating effect on snow albedo and radiative forcing
19 by combining the core/shell Mie theory and snow-albedo SNICAR model. We found
20 that the coating effect enhances snow albedo reduction by a factor of 1.11–1.80 for the
21 nonabsorbing shell and 1.10–1.33 for the absorbing shell at BC concentrations below

1 1000 ng g⁻¹, a snow grain radius ranging from 100–500 μm, and a core/shell ratio
2 ranging from 1.2–2.5. The core/shell ratio plays a dominant role in snow albedo
3 reduction. Furthermore, the absorbing shell causes a smaller snow albedo reduction
4 than that caused by the nonabsorbing shell because of the lensing effect, whereby the
5 absorbing shell reduces photon absorbance in the BC core. Our results effectively
6 considered the complex enhancement of snow albedo reduction due to the coating effect
7 in real environments.

8 Parameterizations describing the coating effect were further developed for
9 application in snow albedo and climate models. The parameterized and simulated
10 results exhibit strong correlations in both clean and polluted snowpacks. The root mean
11 squared error of the parameterized $E_{\alpha, \text{integrated, para}}$ values is small (1.41×10^{-3}). A list of
12 empirical coefficients for parameterizations was provided suitable for most seasonal
13 snowpack field cases, with BC concentrations lower than 1000 ng g⁻¹, snow grain sizes
14 ranging from 50–1000 μm, and core/shell ratios ranging from 1.1 to 3.0. We
15 demonstrated that these parameterizations could reduce the simulation bias regarding
16 local experiments in snow albedo models and, more importantly, could be applied to
17 GCMs to improve our understanding of how BC in snow affects local hydrological
18 cycles and the global climate.

19 Based on a comprehensive set of field measurements across the Northern
20 Hemisphere, the BC coating effect in real snowpacks was evaluated by assuming the
21 presence of an absorbing OC shell. The enhancement of snow albedo reduction ranged

1 from 1.13–1.27, and the enhancement of radiative forcing was 1.14–1.27, which
2 exceeds the contribution of dust to snow light absorption over most areas of northern
3 China. Notably, the greatest enhancements were detected on the Tibetan Plateau and in
4 the Arctic, which may likely contribute to further Arctic sea ice and Tibetan glacier
5 retreat. Our findings indicated that the coating effect must be considered in future
6 climate models, in particular to evaluate the climate on the Tibetan Plateau and Arctic
7 more accurately.

1 **Conflict of interest**

2 The authors declare that they have no conflict of interest.

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9 **Author contributions**

10 X Wang and W Pu invited the project. W Pu and X Wang designed the study. W
11 Pu wrote the paper with contributions from all co-authors. TL Shi processed and
12 analyzed the data.

13

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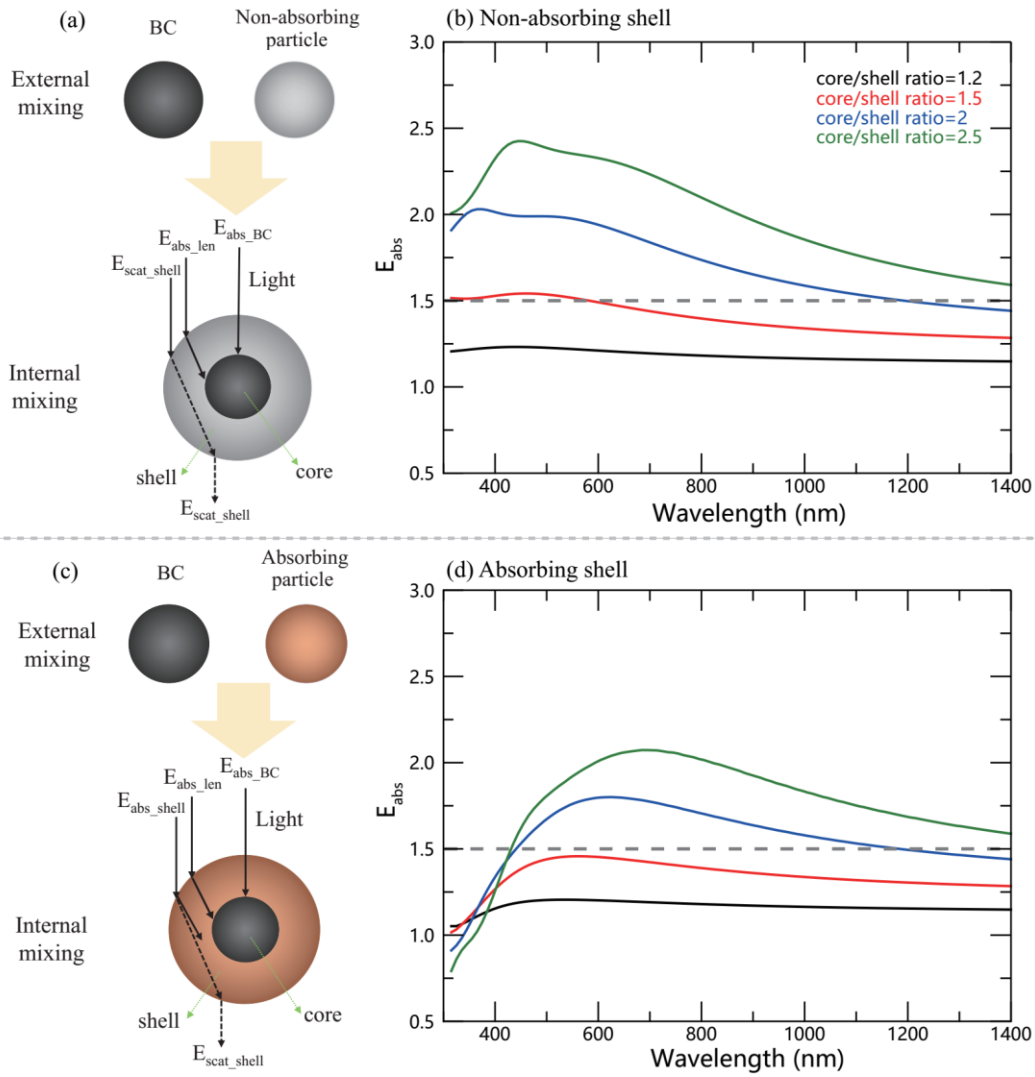
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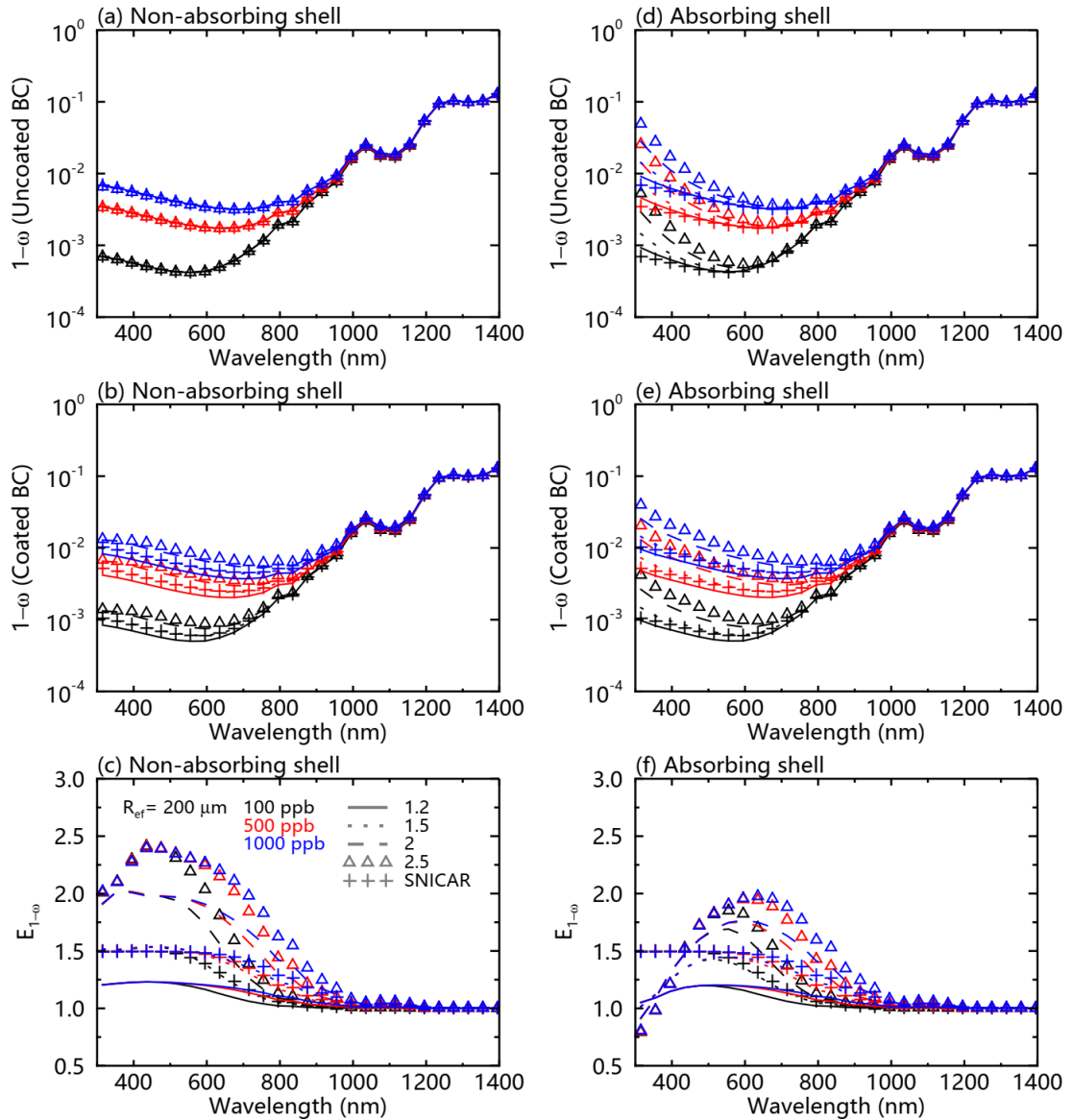
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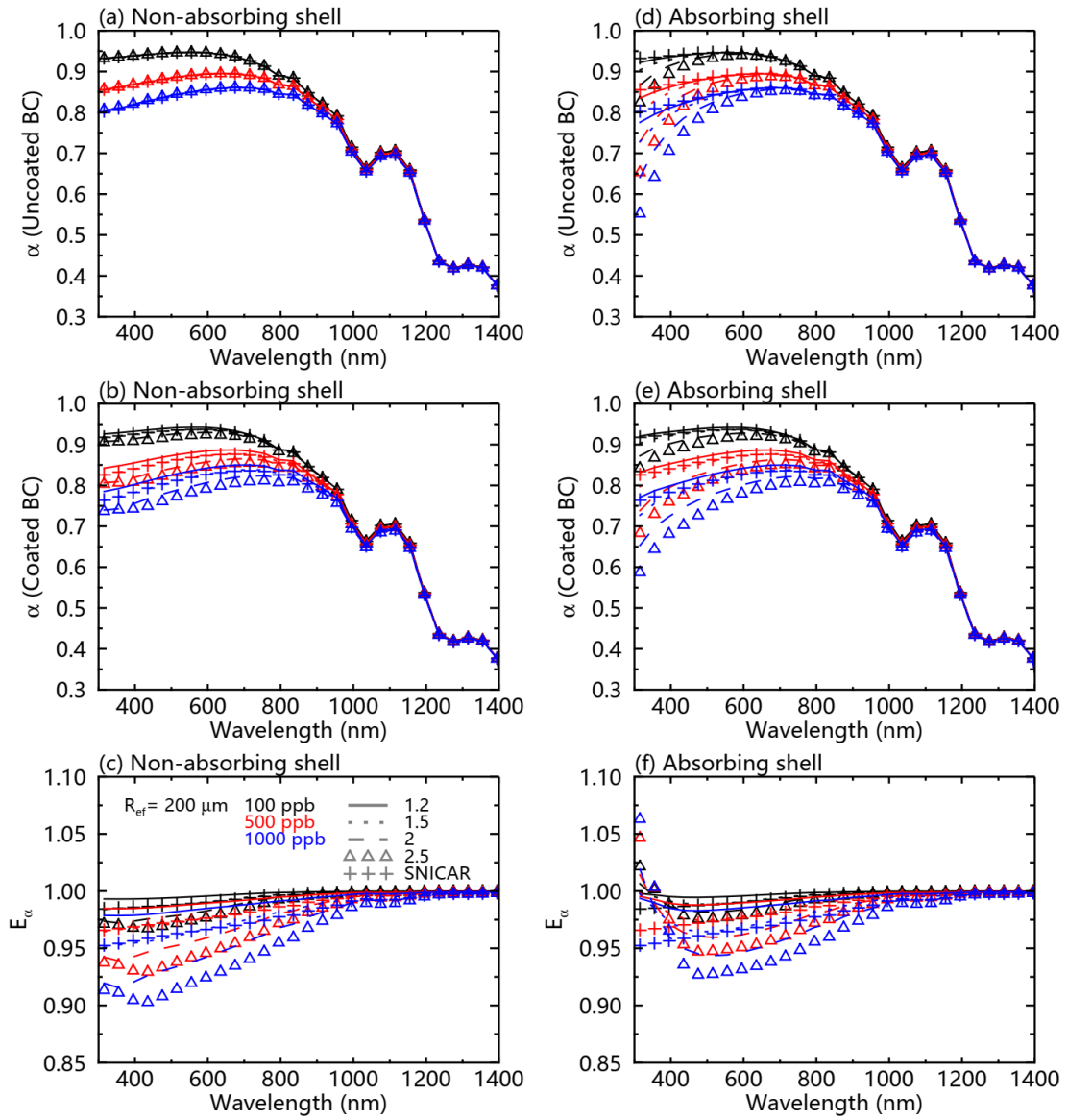
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Figure 1. Schematic diagrams showing the light absorption of an external mixture and internal mixture of BC considering (a) a nonabsorbing particle and (c) an absorbing particle. Additionally, the enhancement of light absorption due to the internal mixture (E_{abs}) is compared to that due to the external mixture of BC with (b) nonabsorbing and (d) absorbing particles. The internal mixed particle was assumed to be a core/shell structure with a black carbon (BC) core.



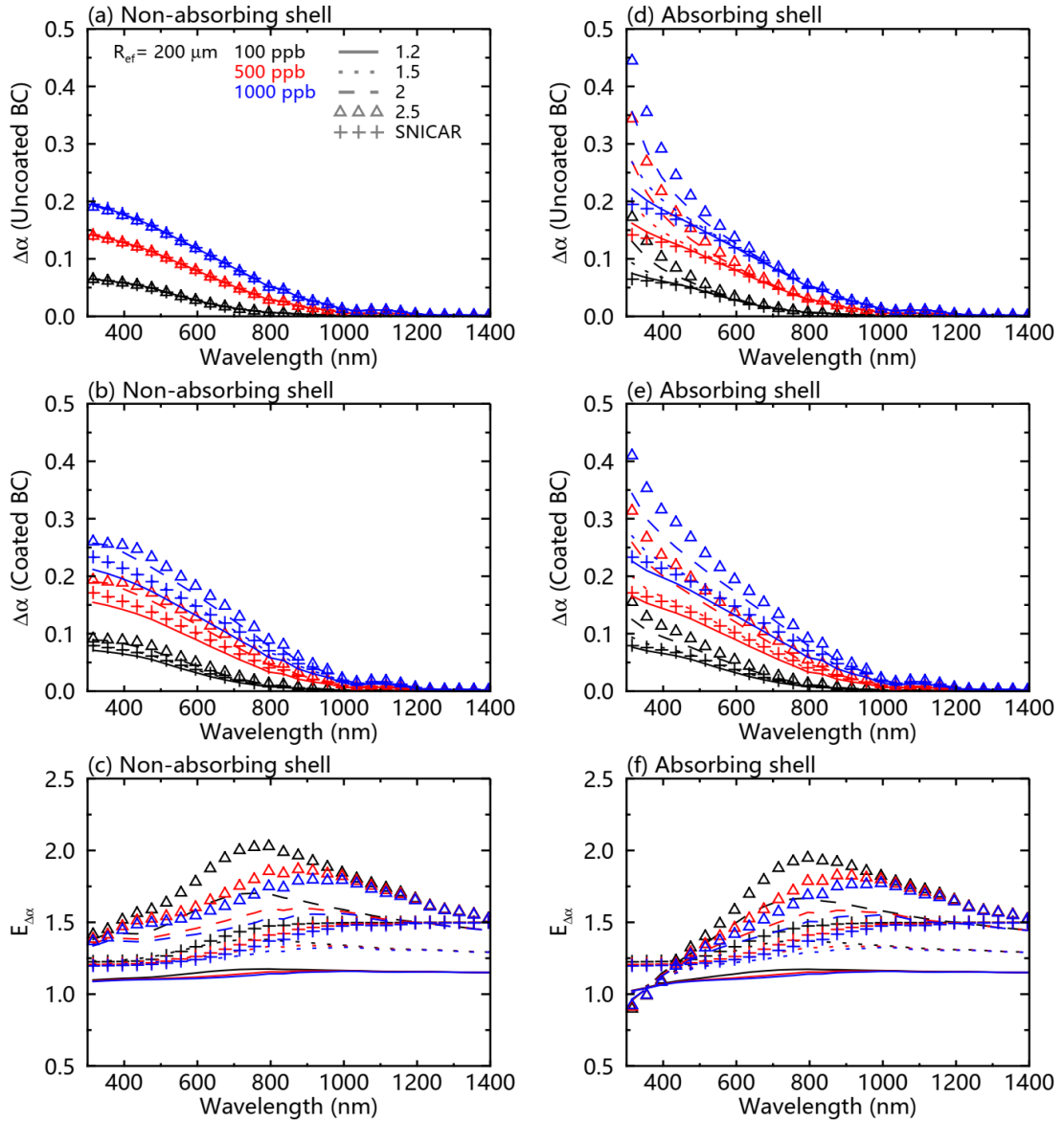
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2 **Figure 2.** Snow single-scattering co-albedo ($1-\omega$) as a function of the wavelength, at
3 different BC concentrations and core/shell ratios for (a) uncoated and (b) coated BC
4 particles under the assumption of a nonabsorbing shell. (d) and (e) are the same as (a)
5 and (b), respectively, but under the assumption of an absorbing shell. (c) shows the
6 ratios of the snow single-scattering co-albedo ($E_{1-\omega}$) for coated versus uncoated BC
7 particles under the assumption of a nonabsorbing shell. (f) is the same as (c) but under
8 the assumption of an absorbing shell. The snow grain radius was assumed to be 200 nm.

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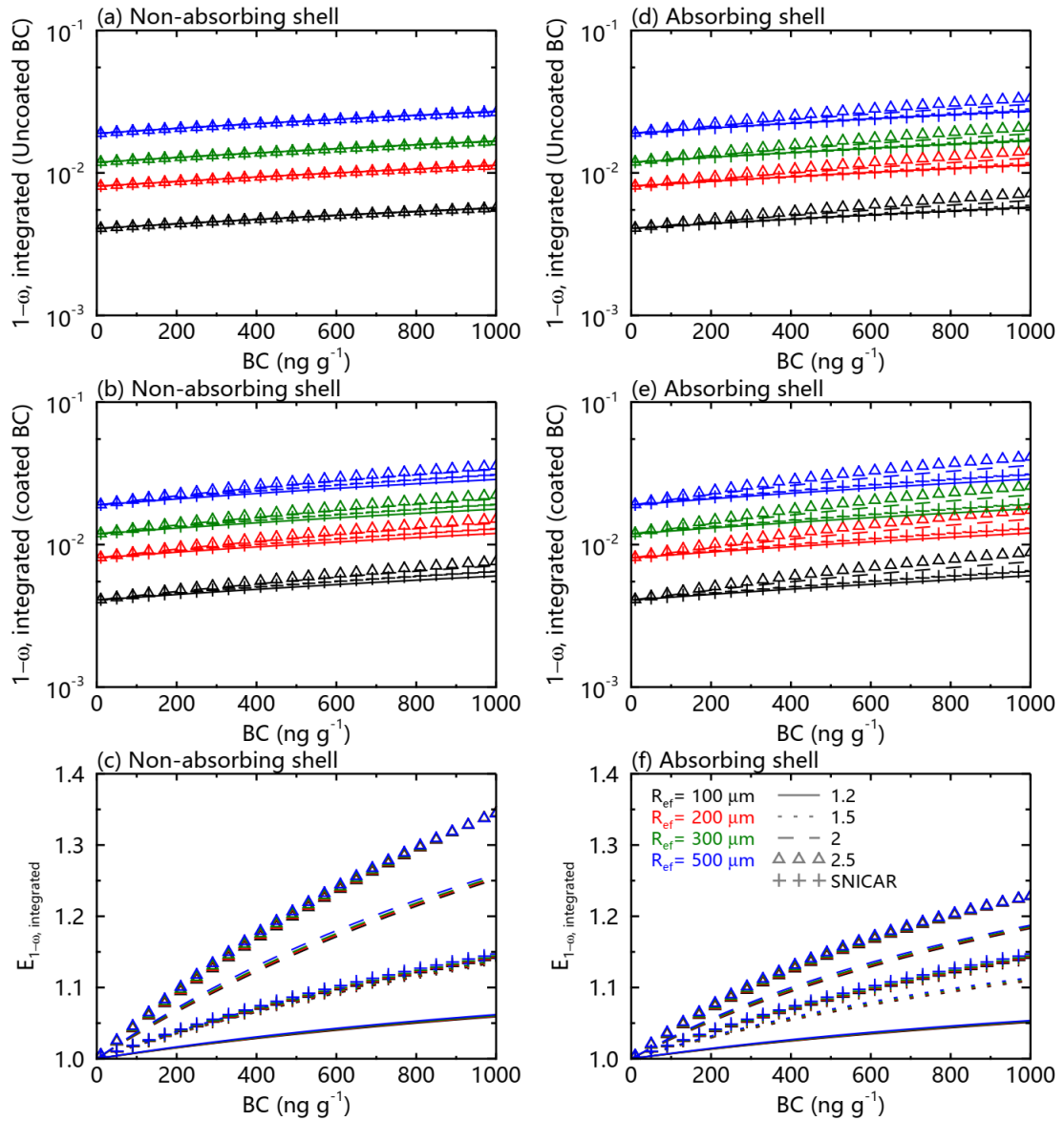
Figure 3. Same as Figure 2, but for the snow albedo (α).



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2 **Figure 4.** Same as Figure 2, but for the snow albedo reduction ($\Delta\alpha$).

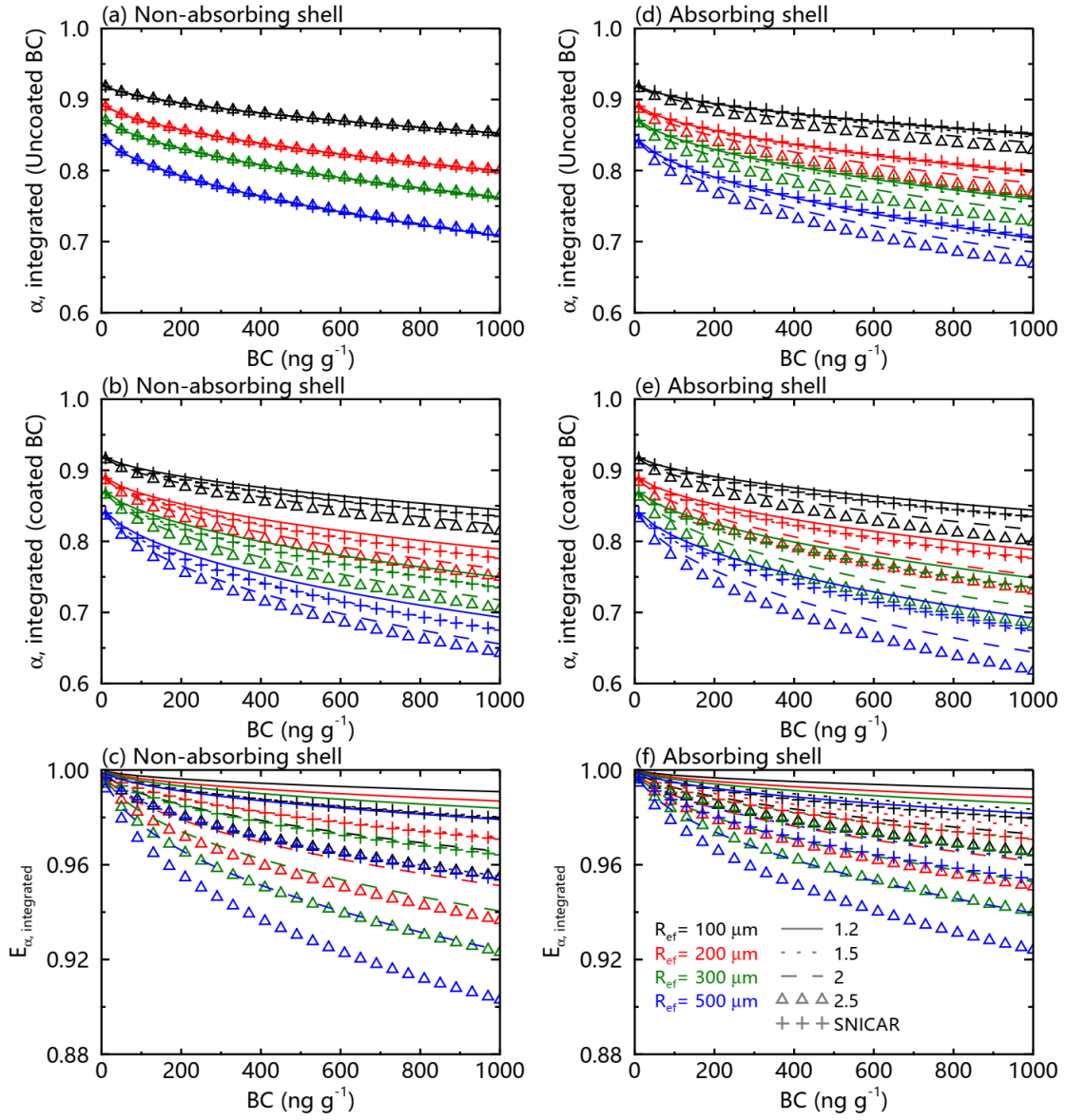
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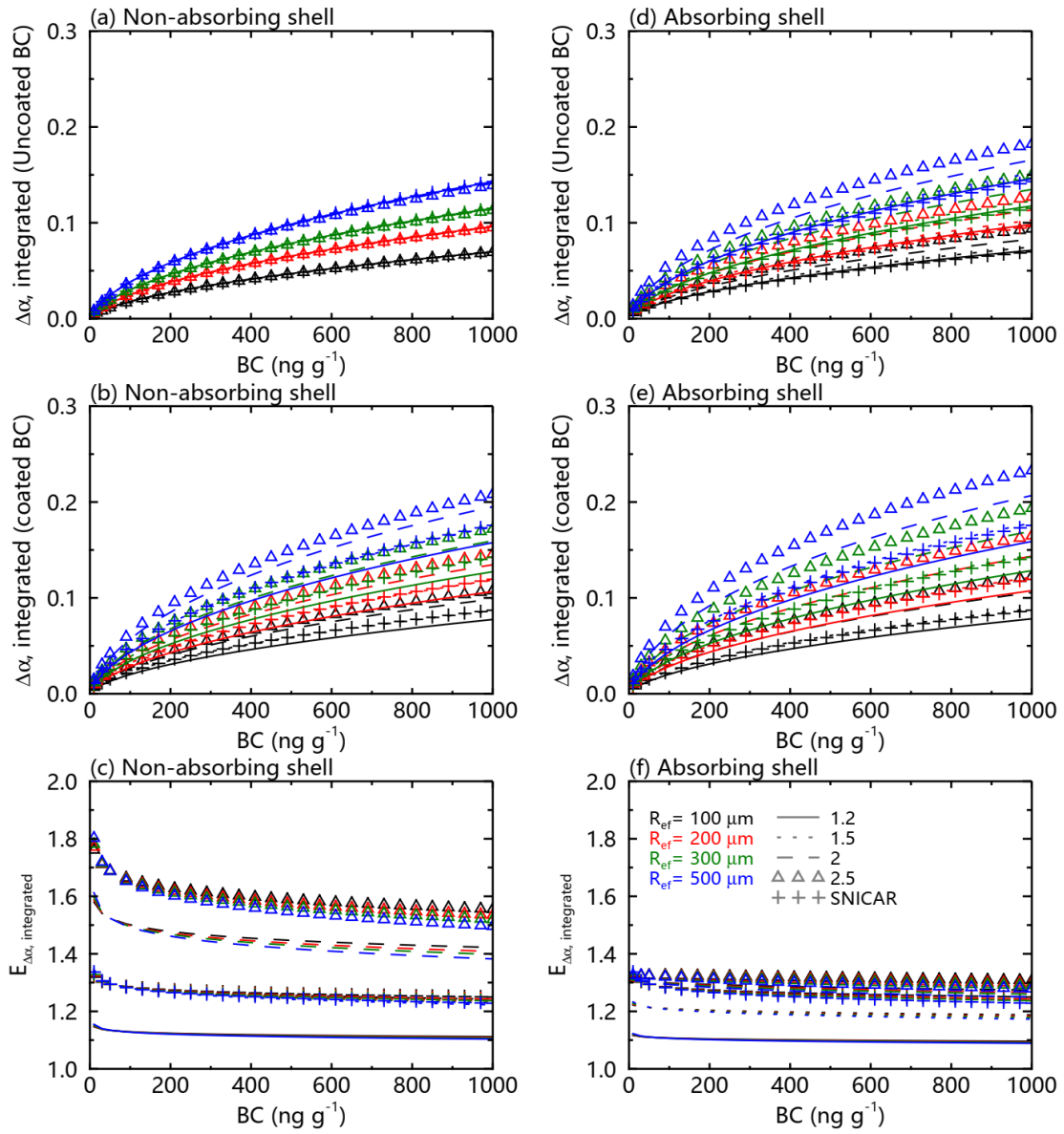
2 **Figure 5.** Spectrally weighted snow single-scattering co-albedo ($1-\omega_{\text{integrated}}$) from 300–
 3 2500 nm of the typical surface solar spectrum at mid–high latitudes from January to
 4 May for (a) uncoated and (b) coated BC particles under the assumption of a
 5 nonabsorbing shell. (d) and (e) are the same as (a) and (b), respectively, but under the
 6 assumption of an absorbing shell. (c) shows the ratios ($E_{1-\omega_{\text{integrated}}}$) of the spectrally
 7 weighted snow single-scattering co-albedo for coated versus uncoated BC particles
 8 under the assumption of a nonabsorbing shell. (f) is the same as (c) but under the
 9 assumption of an absorbing shell.

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Figure 6. Same as Figure 5, but for the snow albedo ($\alpha_{\text{integrated}}$).

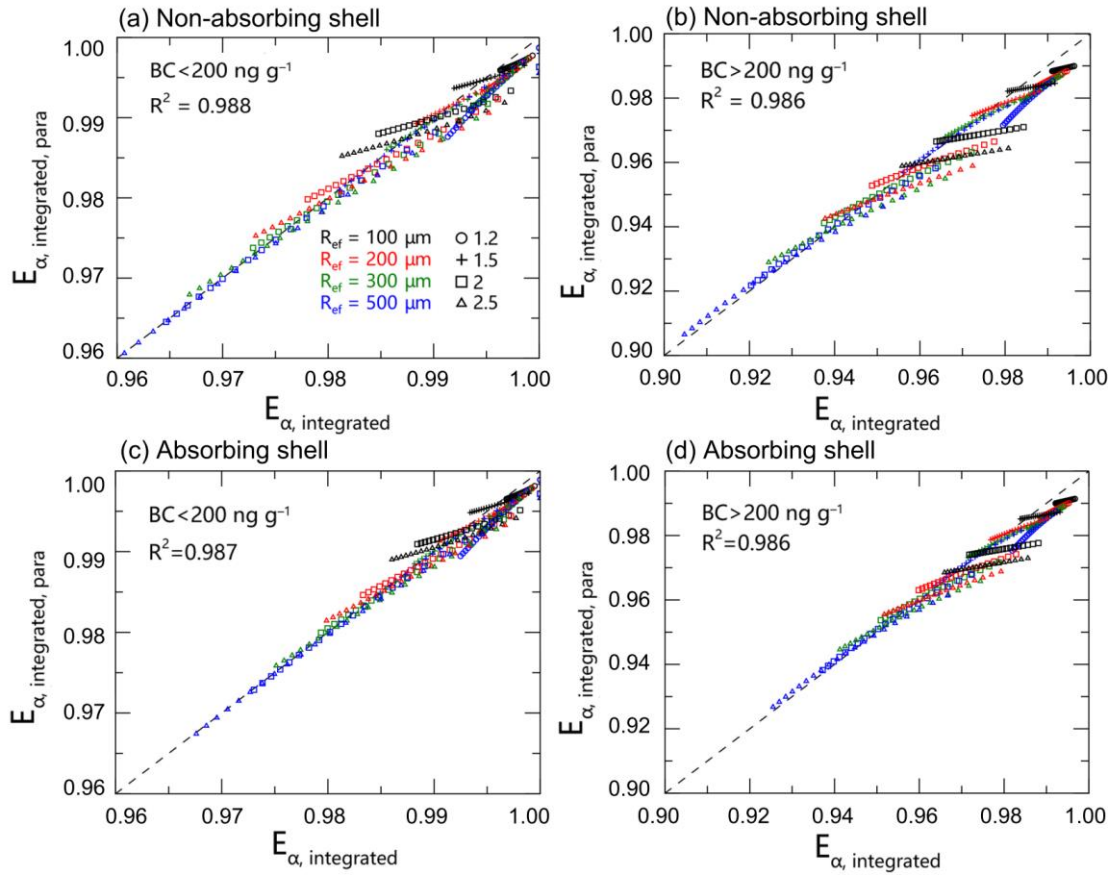


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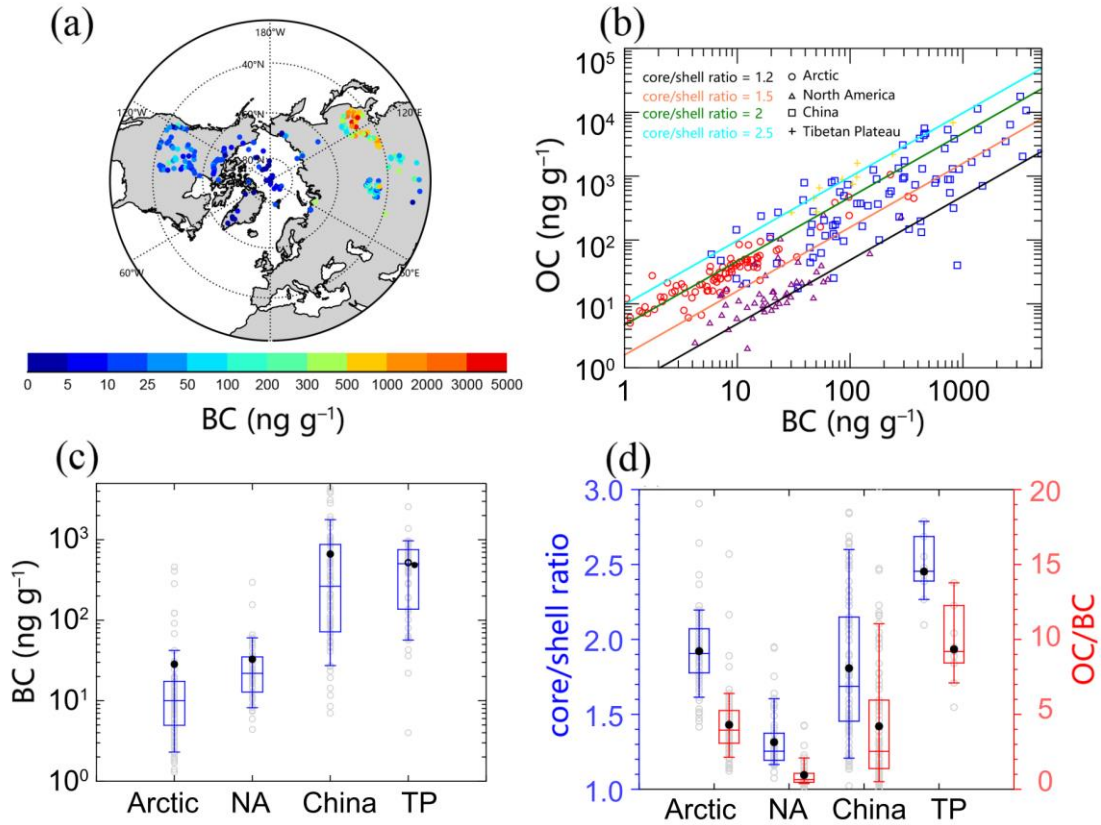
Figure 7. Same as Figure 5, but for the snow albedo reduction ($\Delta\alpha_{\text{integrated}}$).

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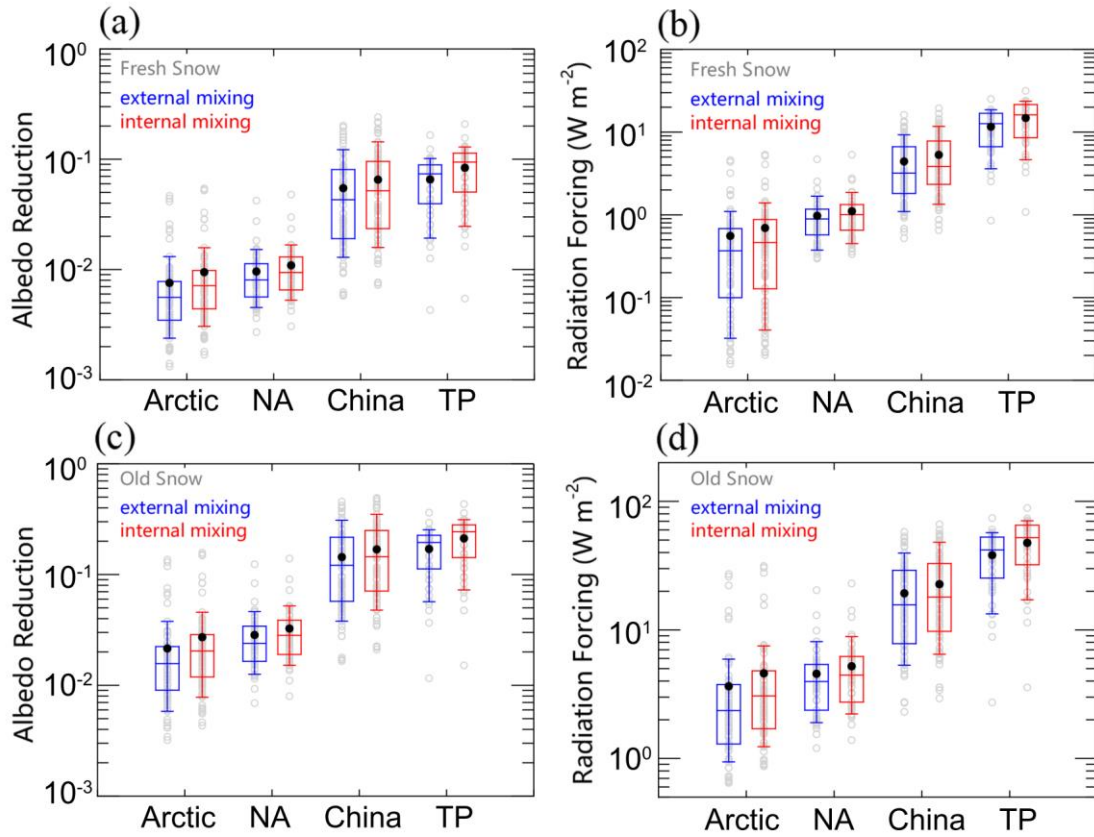
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Figure 8. Comparisons of model-calculated $E_{\alpha, \text{integrated}}$ and parameterized $E_{\alpha, \text{integrated, para}}$ values for (a) relatively clean snow (BC concentration $< 200 \text{ ng g}^{-1}$) and (b) relatively polluted snow (BC concentration $> 200 \text{ ng g}^{-1}$) for a nonabsorbing shell. (c) and (d) are the same as (a) and (b), respectively, but for an absorbing shell.



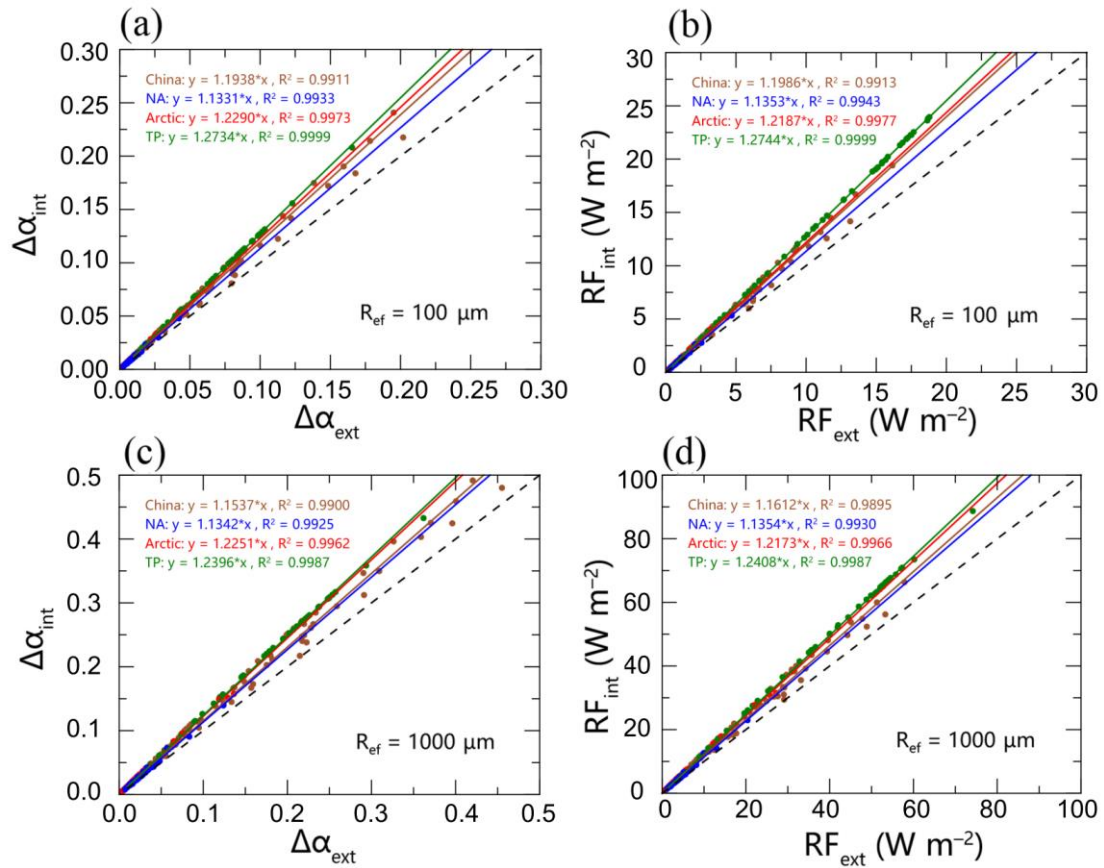
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 2 **Figure 9.** (a) Spatial distribution of the measured black carbon (BC) concentration
 3 across the Northern Hemisphere. (b) Comparison of the BC and organic carbon (OC)
 4 concentrations in the Arctic, North America (NA), northern China (NC) and the
 5 Tibetan Plateau (TP). (c) Statistical plots of the BC concentration in the different regions. The
 6 boxes denote the 25th and 75th quantiles, the horizontal lines denote the 50th quantiles
 7 (median values), the solid dots denote the average values, and the whiskers denote the
 8 10th and 90th quantiles. The in situ data are shown as gray circles. (d) is the same as
 9 (c) but for the core/shell ratio and OC/BC mass ratio, assuming a core/shell structure
 10 with a BC core and an absorbing OC shell.

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Figure 10. Statistical plots of (a) albedo reduction and (b) radiative forcing in the different regions for fresh snow. (c) and (d) are the same as (a) and (b), respectively, but for old snow. The boxes denote the 25th and 75th quantiles, the horizontal lines denote the 50th quantiles (median values), the solid dots denote the average values, and the whiskers denote the 10th and 90th quantiles. The in situ data are shown as gray circles.



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2 **Figure 11.** Comparisons of (a) snow albedo reduction and (b) radiative forcing via
 3 internally mixed particles versus external mixed particles based on in situ
 4 measurements of fresh snow (assuming a snow grain radius of $100 \mu\text{m}$). (c) and (d) are
 5 the same as (a) and (b), respectively, but for old snow and assuming a snow grain radius
 6 of $1000 \mu\text{m}$.