

1 **Abstract.** When black carbon (BC) is internally mixed with other atmospheric particles,
2 BC light absorption is effectively enhanced. This study explicitly resolved ~~This study~~
3 ~~is the first to explicitly resolve the optical properties of coated BC in snow~~ the optical
4 ~~properties of coated BC in snow~~, based on core/shell Mie theory and a snow, ice, and
5 aerosol radiative model (SNICAR). Our results indicate that a ‘BC coating effect’
6 enhances the reduction of snow albedo by a factor of 1.1–1.8 for a non-absorbing shell
7 and 1.1–1.3 for an absorbing shell, depending on BC concentration, snow grain radius,
8 and core/shell ratio. We develop parameterizations of the BC coating effect for
9 application to climate models, which provides a convenient way to accurately estimate
10 the climate impact of BC in snow. Finally, based on a comprehensive set of in situ
11 measurements across the Northern Hemisphere, we find that the contribution of the BC
12 coating effect to snow light absorption has exceeded that of dust over northern China.
13 Notably, the high enhancements of snow albedo reductions by BC coating effect were
14 found in the Arctic and Tibetan Plateau, suggesting a greater contribution of BC to the
15 retreat of Arctic sea ice and Tibetan glaciers.

16

1 **1 Introduction**

2 Snow is the most reflective natural substance at Earth's surface and covers more
3 than 30% of global land area (Cohen and Rind, 1991). Snow albedo feedback is
4 considered one of the major energy balance factors of the climate system. Previous
5 observations have revealed that light-absorbing particles (LAPs; e.g., black carbon
6 (BC), organic carbon (OC), and mineral dust) within snow can reduce snow albedo and
7 enhance the absorption of solar radiation (Hadley and Kirchstetter, 2012). As a result,
8 LAPs play a significant role in altering snow morphology and snowmelt processes, and
9 therefore have important effects on local hydrological cycles and global climate (Qian
10 et al., 2009).

11 Given the importance of the climate feedback caused by LAPs in snow, studies
12 have developed snow radiative models and sought to improve our understanding of the
13 influence of LAP-contaminated snow on climate. For example, Warren and Wiscombe
14 (1980) developed a radiative forcing model based on Mie theory and δ -Eddington
15 approximation, and reported that snow albedo in visible wavelengths could be reduced
16 by 5%–15% when 1000 ng g^{-1} BC is present in snow. Flanner et al. (2007) developed
17 a more comprehensive snow albedo model (the snow, ice, and aerosol radiation model;
18 SNICAR) for multilayer snowpack using the two-stream radiative transfer solution. In
19 addition to BC, the SNICAR model also accounts for the potential effects of dust
20 particles and volcanic ash on snow albedo. Recently, some studies indicated that the
21 mixing state of BC and snow could effectively change snow albedo (Liou et al., 2011,

1 2014; Flanner et al., 2012; Liu et al., 2012; He et al., 2017, 2018a, b, c2011,-). Recent
2 Moreover, studies have indicated that snow grain shape also has an important influence
3 on snow albedo (Kokhanovsky and Zege, 2004). Nonspherical snow grains have
4 weaker albedo reduction than snow spheres (He et al., 2018cb; Dang et al., 2016).e.g.,
5 Dang et al., 2016).

6 Although efforts have been made to optimize snow albedo models, current models
7 still suffer from major limitations. Studies have indicated that when BC in the
8 atmosphere is coated with other aerosols it can significantly enhance light absorption
9 via a lensing effect compared with uncoated BC, as investigated using model
10 simulations (e.g., Jacobson 2001; Matsui et al., 2018) and experimental measurements
11 (e.g., Cappa et al., 2012; Peng et al., 2016). Moreover, coated BC has been observed to
12 exist for only a few hours after emission in some regions (Moteki et al., 2007; Moffet
13 and Prather, 2009). Global aerosol models that simulate microphysical processes have
14 indicated that most BC is mixed with other particles within 1–5 days (Jacobson, 2001)
15 at all altitudes (Aquila et al., 2011). However, a problem is that whether coated BC is
16 existed in real snowpack because the coating materials (e.g. salts and OC) of coated BC
17 may be dissolved during wet deposition. A recent study observing individual particle
18 structure and mixing states between the glacier–snowpack and atmosphere based on
19 field measurements and laboratory transmission electron microscope (TEM) and
20 energy dispersive X-ray spectrometer (EDX) instrument analysis (Dong et al., 2018)
21 told the truth. They found that the salt-coated BC werewas still observed in real

1 snowpack in spite of its lower proportion than that in the atmosphere due to the
2 dissolution effect within precipitating snow. For OC, that study didn't observe reduced
3 OC components in LAPs. More notably, that study further found that the proportion of
4 coated BC was even higher in snowpack than that in the atmosphere. All of the above
5 observation results demonstrated that the coated BC particles are existed in real
6 snowpack and even more common than that in the atmosphere. Hence, the climate
7 impacts of BC must be evaluated in the context of the effect of coating on light
8 absorption enhancement.

9 Although the BC coating effect on light absorption enhancement in the atmosphere
10 is broadly acknowledged, little research has been carried out on snow albedo. Flanner
11 et al. (2007) developed the first radiative transfer model to investigate the coating effect
12 on snow albedo, using sulfate as the BC particle coating with a constant absorption
13 enhancement factor of ~1.5. Subsequently, Wang et al. (2017) used a similar constant
14 light absorption enhancement factor for their spectral albedo model for dirty snow
15 (SAMDS). However, the factor varies with the optical properties of different coatings,
16 the core/shell ratio, wavelength, and other parameters in real environments (Lack and
17 Cappa, 2010; Liu et al., 2017). For example, Liu et al. (2017) reported that the core/shell
18 ratio is a key control on light absorption enhancement. You et al. (2016) suggested that
19 light absorption enhancement is highly correlated with visible or near-infrared (NIR)
20 wavelengths and coating material. Furthermore, a core/shell Mie theory simulation
21 (Lack and Cappa, 2010) found light absorption enhancement was smaller for mildly

1 absorbing coatings (e.g., OC) than non-absorbing coatings (e.g., sulfate). Hence, using
2 a constant enhancement factor will result in biased simulation estimates, against
3 refining our knowledge of the hydrological and climate impacts of BC in snow.

4 In this study we apply core/shell Mie theory to calculate the optical properties of
5 BC coated with both mildly absorbing OC and non-absorbing sulfate, and use these
6 results within a SNICAR model to evaluate the influence on snow albedo.
7 Parameterizations for the BC coating effect are then developed for application in other
8 snow albedo and climate models. Finally, we estimate the enhancements of snow albedo
9 reductions and associated radiative forcing by the BC coating effect across the Northern
10 Hemisphere, by combining model simulations with in situ observations of BC and OC
11 concentrations in snow.

12 **2 Methods**

13 **2.1 Modeling**

14 **2.1.1 Optical parameter calculations for coated BC**

15 Figure 1a and 1c shows schematics of light absorption by externally and internally
16 mixed particles (EMP and IMP, respectively). EMP refers to uncoated BC mixed with
17 other particles, while IMP refers to BC that is assumed to be a core coated by another
18 particle acting as a shell (Kahnert et al., 2012). For a non-absorbing shell, overall light
19 absorption includes contributions from the BC core and enhancement absorption from
20 a lensing effect, while for an absorbing shell, the shell itself also contributes to light
21 absorption. The lensing effect means that when BC is coated with the non-absorbing

1 shell (or the absorbing shell), the shell acts as a lens and focuses more photons onto the
2 core than would reach it otherwise, so that the light absorption by the BC core can be
3 enhanced (Bond et al., 2006).

4 To evaluate the BC coating effect on snow albedo, it is necessary to determine the
5 optical parameters of coated BC. The refractive index (RI) of BC was assumed to be
6 $1.95-0.79i$ following Lack and Cappa (2010), which is consistent with the original
7 SNICAR model (Flanner et al., 2007). Two types of particle shells (non-absorbing and
8 absorbing) were considered. The non-absorbing shell was represented using sulfate,
9 and its RI was assumed to be $1.55-10^{-6}i$ following the atmospheric study of Bond et al.
10 (2006). The absorbing shell was represented using OC, which is a major light-absorbing
11 particle in snow (Wang et al., 2013). The RI of OC varies with wavelength. Here, a
12 fixed mass absorption coefficient (MAC) for OC of $0.3 \text{ m}^2 \text{ g}^{-1}$ at 550 nm, a real RI of
13 1.55, and a particle diameter of 200 nm were assumed, ~~Here, a fixed mass absorption~~
14 ~~coefficient (MAC) for OC of $0.3 \text{ m}^2 \text{ g}^{-1}$ at 550 nm, a real RI of 1.55, and a particle~~
15 ~~diameter of 200 nm were assumed, following the observations of Yang et al. (2009) and~~
16 ~~the study of Lack and Cappa (2010) following Lack and Cappa (2010). The uncertainty~~
17 ~~of snow albedo of coated BC due to OC MAC will be discussed in Section 3.4.~~ Based
18 on Mie theory, an imaginary RI value of $-1.36 \cdot 10^{-2}i$ at 550 nm was calculated.
19 Subsequently, wavelength-dependent imaginary RI values (Figure S1) were derived
20 according to an absorption angstrom exponent (AAE) of -6 (Sun et al., 2007).

21 For a core/shell-structured particle, the core and shell diameters refer to the BC

1 core diameter and the whole particle diameter, respectively. BC diameters are usually
2 in the range of ~50–120 nm in the atmosphere (Corbin et al., 2018), and are typically
3 larger by ~20 nm in snow due to a removal process via wet deposition (Schwarz et al.,
4 2013). Therefore, we assumed the BC diameter in snow was 100 nm with a fixed
5 monodisperse size distribution. The uncertainty of snow albedo of coated BC due to
6 BC size distribution will be discussed in Section 3.4 ~~Therefore, we assumed the BC~~
7 ~~diameter in snow was 100 nm.~~ The shell diameter was assumed from 110 nm to 300
8 nm based on Bond et al. (2006). Core and shell diameters, RI, and wavelength were
9 then used in a Mie model to derive optical parameters of the core/shell particle,
10 including single scatter albedo (SSA), asymmetry factor (g), and extinction cross-
11 section (Q_{ext}). The mass extinction coefficient (MEC) of the core/shell particle was
12 calculated based on Q_{ext} and the density, given as 1.8 g cm^{-3} for BC (Bond et al., 2006),
13 1.2 g cm^{-3} for sulfate, and 1.2 g cm^{-3} for OC (Turpin and Lim, 2001).

14 **2.1.2 Snow albedo calculations**

15 We simulated snow albedo with the SNICAR model (Flanner et al., 2007), which
16 calculates the radiative transfer in snowpack based on the theory of Warren and
17 Wiscombe (1980) and a two-stream multilayer radiative approximation (Toon et al.,
18 1989). Here, we summarize only the model features in SNICAR that are crucial to our
19 study. SNICAR allows for a vertical multilayer distribution of snow properties, LAPs,
20 and heating throughout the snowpack column. Input optical parameters (MEC, SSA,
21 and g) of snow grains and BC were calculated off-line using Mie theory. SNICAR

1 provides albedo changes from uncoated and sulfate-coated BC on snow, as well as dust
2 particles and volcanic ash (for further details, see Flanner et al., 2007)._

3 In this study, we assumed a homogeneous semi-infinite snowpack and a solar
4 zenith angle of 49.5°, whose cosine value (0.65) represents the insolation-weighted
5 mean solar zenith cosine for sunlit Earth hemisphere (Dang et al., 2015). The snow
6 grain optical effective radius varied from 5400 to 1000 μm (with a 50- μm interval) to
7 characterize snow aging. Meanwhile, BC concentrations were assumed in the range of
8 0-1000 ng g^{-1} (with a 10- ng g^{-1} interval) to demonstrate clear to polluted snow, which
9 was based on the global field observations with BC concentrations in snowpack mostly
10 below 1000 ng g^{-1} (e.g. Doherty et al., 2010, 2014; Wang et al., 2013; Li et al., 2017,
11 2018; Pu et al., 2017; Zhang et al., 2017, 2018). These parameters are also applied for
12 parameterizations (see Section 2.3). In addition, we note the SNICAR used in this study
13 was default version that assumes BC-snow external mixing and snow spheres (Flanner
14 et al., 2007). Although the mixing state of BC and snow grains, and snow grain shape
15 can affect the snow albedo, the empirical parameterizations for the effect of BC
16 internally mixed with snow grains on snow albedo has been developed by He et al.
17 (2018cb), and the albedo of a snowpack consisting of nonspherical snow grains can be
18 mimicked by using a smaller grain of spherical shape (Dang et al. 2016). Therefore,
19 users can combine the empirical parameterizations by He et al. (2018cb) and Dang et
20 al. (2016) with the empirical parameterizations by us (see Section 2.3) to study the
21 effect of the internal mixing of BC with snow grains, snow grain shape, and coated BC

1 on snow albedo.

2 For SNICAR snow albedo simulations of uncoated BC, concentrations of both BC
3 and other particles were input directly. For coated BC, optical parameters (MEC, SSA,
4 and g) of IMP (calculated above) were first archived as lookup tables within SNICAR,
5 and then the concentration of IMP was input.

6 **2.2 Calculation of broadband snow albedo**

7 The spectral albedo (α_λ) was integrated over the solar spectrum ($\lambda = 300\text{--}2500$ nm)
8 and weighted by the incoming solar irradiance (S_λ) to calculate broadband snow albedo
9 ($\alpha_{\text{integrated}}$):

$$10 \quad \alpha_{\text{integrated}} = \frac{\int \alpha_\lambda S_\lambda d_\lambda}{\int S_\lambda d_\lambda} \quad (1)$$

11 The incoming solar irradiance was a typical surface solar spectrum for mid–high
12 latitudes from January to May, calculated with the Santa Barbara DISORT Atmospheric
13 Radiative Transfer (SBDART) model (Pu et al., 2019), which is one of the most widely
14 used models for radiative transfer simulations (for further details, see Ricchiazzi et al.
15 1998).

16 **2.3 Parameterizations**

17 In the original SNICAR model, the BC coating effect is simply parameterized with
18 an absorption enhancement of ~ 1.5 (Flanner et al., 2007). However, the effect of BC
19 coating on snow albedo is widely variable and dependent on BC concentration,
20 core/shell ratio, snow grain size, and the type of particle shell (see Section 3.3). In view

1 of this complexity, more explicit parameterizations were developed in this study:

$$2 \quad E_{\alpha, \text{integrated}} = \frac{\alpha_{\text{int, integrated}}}{\alpha_{\text{ext, integrated}}} \quad (2)$$

3 where $\alpha_{\text{ext, integrated}}$ and $\alpha_{\text{int, integrated}}$ are broadband snow albedos for EMP and
4 IMP, respectively. Following a previous empirical formulation (Hadley and Kirchstetter,
5 2012), $E_{\alpha, \text{integrated}}$ was parameterized as

$$6 \quad E_{\alpha, \text{integrated, para}} = a_0 \times (C_{BC})^{a_1} + a_2 \quad (3)$$

$$7 \quad a_1 = b_0 \times (\log_{10}(R_{\square f} / 50))^{b_1} \quad (4)$$

8 where $E_{\alpha, \text{integrated, para}}$ is the parameterized $E_{\alpha, \text{integrated}}$, C_{BC} is the BC
9 concentration, and $R_{\square f}$ represents the snow grain radius. The terms a_0 , a_1 , a_2 , b_0 ,
10 and b_1 are the empirical coefficients and dependent on the core/shell ratio and the type
11 of particle shell. To enhance the precision, parameterizations were divided into two
12 groups: the first to account for relatively clean snow (with BC concentrations $< 200 \text{ ng}$
13 g^{-1}) and the second for relatively polluted snow ($200 \text{ ng g}^{-1} < \text{BC concentrations} < 1000$
14 ng g^{-1}). ~~We note that if BC concentration is larger than 1000 ng g^{-1} , the parameterization~~
15 ~~for relatively polluted snow is also applicable with a small negative bias based on the~~
16 ~~results of Section 3.5.~~

17 **2.4 Calculation of in situ snow albedo and radiative forcing**

18 In situ broadband clear-sky ($\alpha_{\text{integrated}}^{\text{clear, in-situ}}$) and cloudy-sky ($\alpha_{\text{integrated}}^{\text{cloudy, in-situ}}$) albedos
19 were calculated separately based on in situ snow-LAP parameters and SBDART
20 simulated clear-sky and cloudy-sky incoming solar irradiance. ~~by We assuming~~

1 assumed a semi-infinite snowpack due to limited snow depth measurements. BC and
 2 OC concentrations were collected from in situ field measurements (e.g. Doherty et al.,
 3 2010, 2014; Wang et al., 2013; Li et al., 2017, 2018; Pu et al., 2017; Zhang et al., 2017,
 4 2018). The snow grain radius of 100 (1000) μm was assumed for fresh (old) snow,
 5 which is comparable to previous observations of snow grain sizes at mid to high
 6 latitudes in winter (Wang et al., 2017; Shi et al., 2020). The value of solar zenith angle
 7 was calculated based on the longitude, latitude, and sampling time at each sampling
 8 site. The in situ all-sky albedo ($\alpha_{\text{integrated}}^{\text{all-sky,in-situ}}$) was then calculated using weighted
 9 clear-sky and cloudy-sky albedos depending on cloud fraction (CF), given as:

$$10 \quad \alpha_{\text{integrated}}^{\text{all-sky,in-situ}} = \text{CF} \times \alpha_{\text{integrated}}^{\text{cloudy,in-situ}} + (1 - \text{CF}) \times \alpha_{\text{integrated}}^{\text{clear,in-situ}} \quad (5)$$

11 In situ radiative forcing by LAPs was calculated by multiplying the derived
 12 broadband albedo reduction by the downward shortwave flux at the snow surface (Dang
 13 et al., 2017). We point out that the radiative forcing was calculated using the January-
 14 February average solar radiation for NA and NC, while April-May average solar
 15 radiation for the Arctic and TP according to the periods of field campaigns. In this study,
 16 we mainly estimate the relative impact of internal mixing to external mixing on snow
 17 albedo and radiative forcing, which is hence not influenced by the chosen solar
 18 radiation. We used the downward solar radiation in January (March) and March (May)
 19 for fresh snow and old snow at the mid-latitude (Arctic) sampling sites, respectively,
 20 consistent with the study of Dang et al. (2017). Figure S2 shows the spatial distributions
 21 of solar flux and cloud fraction, which were obtained from the Clouds and the Earth's

1 Radiant Energy System (CERES)

2 (<https://ceres.larc.nasa.gov/products.php?product=SYN1deg>).

3 **3 Results and discussion**

4 **3.1 Impact on particle light absorption**

5 ~~Figure 1b and 1d shows the light absorption enhancement, E_{abs} for coated BC. E_{abs}~~
6 ~~is defined as the ratio of the light absorption for an internal mixture coated (LA_{int}) versus~~
7 ~~external mixture uncoated BC (LA_{ext}), of BC ($E_{\text{abs}} = \frac{LA_{\text{int}}}{LA_{\text{ext}}}$). Figure 1b and 1d shows~~
8 ~~light absorption ratios (light absorption enhancement, E_{abs}) for IMP versus EMP.~~

9 Based on Bond et al. (2006), we show the most common core/shell ratios (the ratio of
10 the diameter of the whole particle to the BC core) of 1.2, 1.5, 2.0, and 2.5 in real
11 environments to represent the thickness of shells, and we used detailed core/shell ratios
12 from 1.1 to 3.0 (in intervals of 0.1) for parameterizations (see Section 3.5). E_{abs} varies
13 with the wavelength and increases with core/shell ratio, in contrast to the default E_{abs}
14 value used in the original SNICAR model, which remains constant. For a non-absorbing
15 shell, the light absorption of IMP is larger than EMP across all wavelengths (300–1400
16 nm). For an absorbing shell, E_{abs} is similar to the non-absorbing shell in NIR, but
17 becomes smaller in visible (VIS) light and ultra-violet (UV), which implies the
18 absorbing shell reduces whole-particle light absorption and contributes negatively to
19 E_{abs} . ~~This is because compared with non-absorbing shell, A plausible explanation is that~~
20 ~~the absorbing shell although shell absorbs additional –incident photons, but causesing~~
21 ~~fewer to reach the core, so that the photons absorbed by the lensing effect and the BC~~

1 core will be reduced. In such a case, the additional photons absorbed by the shell are
 2 fewer than the reduced number of photons absorbed by the lensing effect and the BC
 3 core, causing that the total absorption by absorbing shell coated BC will be smaller than
 4 non-absorbing shell coated BC (Lack and Cappa, 2010). Furthermore, the absorbing
 5 shell reduces E_{abs} to <1 in UV at high core/shell ratios, implying that the lensing effect
 6 absorption at those wavelengths cannot recover the BC core absorption reduction,
 7 resulting in fewer photons reaching the core, which is similar to the results by Lack and
 8 Cappa (2010).

9 **3.2 Impact on spectral snow single-scattering properties and albedos**

10 In real snowpack, BC can effectively enhance snow single-scattering co-albedo
 11 $(1-\omega)$, but its effect on other snow optical parameters, such as the asymmetry factor
 12 and extinction efficiency, is negligible (He et al., 2017). Therefore, we focus our
 13 discussion on coating-induced enhancement of snow single-scattering co-albedo ($E_{1-\omega}$),
 14 snow albedo (E_{α}), and snow albedo reduction ($E_{\Delta\alpha}$). The $E_{1-\omega}$ is defined as the ratio of
 15 snow single-scattering co-albedo with coated BC ($1-\omega_{\text{int}}$) versus that with uncoated BC
 16 $(1-\omega_{\text{ext}})$, ($E_{1-\omega} = \frac{1-\omega_{\text{int}}}{1-\omega_{\text{ext}}}$). Similar definitions were used for E_{α} ($E_{\alpha} = \frac{\alpha_{\text{int}}}{\alpha_{\text{ext}}}$) and $E_{\Delta\alpha}$
 17 ($E_{\Delta\alpha} = \frac{\Delta\alpha_{\text{int}}}{\Delta\alpha_{\text{ext}}}$), where α_{int} and α_{ext} are snow albedos with coated and uncoated BC,
 18 and $\Delta\alpha_{\text{int}}$ and $\Delta\alpha_{\text{ext}}$ are snow albedo reductions due to coated and uncoated BC.

19 Figure 2 shows the varied $1-\omega$ and $E_{1-\omega}$ depending on different BC concentrations,
 20 core/shell ratios, and coating materials. For either non-absorbing shell or absorbing
 21 shell, $1-\omega_{\text{int}}$ is usually larger than $1-\omega_{\text{ext}}$ in VIS (Figures 2a versus 2b, 2d versus 2e),

1 ~~andwhile t~~The coating effect ~~is distinct in UV and VIS but~~ has little impacts at
2 ~~wavelength > 1200 nm, (Figures 2e and 2f),~~ which is due to that the optical properties
3 ~~of snow is effectively affected by LAPs in UV and VIS, but primarily by snow itself at~~
4 ~~wavelength > 1200 nm. In addition, $E_{1-\omega}$ increases with increased core/shell ratios, and~~
5 ~~the wavelength of maximum $E_{1-\omega}$ value is dependent on BC concentrations and~~
6 ~~core/shell ratios. In addition, when wavelength $> \sim 500$ nm, both BC concentration and~~
7 ~~core/shell ratio have distinct impacts on $E_{1-\omega}$, but when wavelength $< \sim 500$ nm, $E_{1-\omega}$ is~~
8 ~~mainly affected by core/shell ratio. Moreover, absorbing shell shows a negative impact~~
9 ~~for $E_{1-\omega}$ compared with non-absorbing shell, especially in UV.~~

10 Snow albedo is effectively affected by various factors, such as snow grain size,
11 LAP content, solar zenith angle, which has been widely discussed and verified through
12 model simulation and experimental measurements by previous studies (e.g. Warren and
13 Wiscombe, 1980; Hadley and Kirchstetter, 2012; Wang et al., 2017). In this study, we
14 mainly focus on the coating effect of BC on snow albedo. Figure 3 shows the spectral
15 snow albedos for coated (α_{int}) and uncoated BC (α_{ext}), and the ratios (E_{α}) of α_{int}
16 versus α_{ext} . In consistent with $1-\omega$, the impact of coating effect on snow albedo mainly
17 presents at wavelength $< \sim 1200$ nm (Figures 3a versus 3b, 3d versus 3e), where the
18 higher the BC concentration is (or the larger the core/shell ratio is), the larger the
19 difference of snow albedos between snow albedos for uncoated and coated BC is.
20 Hadley and Kirchstetter (2012) also found a smaller snow albedo for internal mixed
21 particles relative to that for external mixed particles. This phenomenon is also obvious

1 on E_{α} , which decreases with increased BC concentration and core/shell ratios in VIS
2 and NIR (Figure 3c and 3f). For a given BC concentration and core/shell ratio, E_{α}
3 generally decreases with the wavelength from UV to VIS, then increases from VIS to
4 NIR, which is corresponding to the results of E_{abs} and $E_{1-\omega}$. On the other hand, the E_{α}
5 for non-absorbing and absorbing shell is comparable with each other at wavelength $>$
6 ~ 800 nm. However, when wavelength $< \sim 800$ nm, E_{α} for absorbing shell is larger than
7 that for non-absorbing shell and the difference increases with the decreased wavelength
8 and increased core/shell ratio. Moreover, for absorbing shell, the snow albedo for
9 coated BC is higher than that for uncoated BC at $< \sim 350$ nm at large core/shell ratios,
10 which are due to that the light absorption by internal mixed particles for absorbing shell
11 is smaller than that by external mixed particles at those wavelengths as discussed in
12 Section 3.1. These results indicate that the material of particle shell also plays an
13 important role for snow albedo in UV and VIS. We noted that the solar radiative flux is
14 very small at wavelengths < 350 nm, so that the coating effect at those wavelengths
15 may have little contributions to total light absorption and broadband snow albedos, but
16 which may potentially influence the photochemical reactions in snowpack (Grannas et
17 al., 2007).

18 Furthermore, Figure 4 shows the spectral snow albedo reductions caused by coated
19 ($\Delta\alpha_{\text{int}}$) and uncoated BC ($\Delta\alpha_{\text{ext}}$), and the ratios ($E_{\Delta\alpha}$) of $\Delta\alpha_{\text{int}}$ versus $\Delta\alpha_{\text{ext}}$.
20 Generally, $\Delta\alpha_{\text{int}}$ is larger than $\Delta\alpha_{\text{ext}}$, and core/shell ratio dominates the variations of
21 $E_{\Delta\alpha}$ across the wavelengths of 300-1400 nm, while the impact of BC content mainly

1 focuses on 500-1000 nm. In consistent with $E_{1-\omega}$ and E_{α} , the impact of the material of
2 particle shell is negligible at wavelength $> \sim 800$ nm, but the $E_{\Delta\alpha}$ for absorbing shell is
3 smaller than that for non-absorbing shell at wavelength $< \sim 800$ nm. Moreover, the $E_{\Delta\alpha}$
4 is < 1 for absorbing shell at wavelength $< \sim 350$ nm at large core/shell ratios. It is
5 interesting that the coating effect still has an obvious impact on snow albedo reduction
6 at wavelength $> \sim 1200$ nm, which is different with $E_{1-\omega}$ and E_{α} .

7 ~~has a clear influence on $E_{1-\omega}$ and E_{α} in UV and VIS, but affects $E_{\Delta\alpha}$ across all~~
8 ~~wavelengths (Figure 2). The core/shell ratio makes a positive contribution to $E_{1-\omega}$ and~~
9 ~~$E_{\Delta\alpha}$, and a negative contribution to E_{α} . The BC concentration makes a positive~~
10 ~~contribution to $E_{1-\omega}$ and a negative contribution to $E_{\Delta\alpha}$ and E_{α} . For a given BC~~
11 ~~concentration and core/shell ratio, $E_{1-\omega}$ and $E_{\Delta\alpha}$ decrease, and E_{α} increases, with longer~~
12 ~~wavelength from UV to VIS. In addition, the absorbing shell shows a negative influence~~
13 ~~for $E_{1-\omega}$ and $E_{\Delta\alpha}$, but positive for E_{α} compared with a non-absorbing shell, particularly~~
14 ~~under UV. Moreover, for an absorbing shell, $E_{1-\omega}$ and $E_{\Delta\alpha}$ are < 1 , and E_{α} is > 1 at~~
15 ~~approximately < 350 nm in the case of high core/shell ratios because of lower light~~
16 ~~absorption by IMP than EMP at those wavelengths.~~

17 **3.3 Impact on broadband snow single-scattering properties and albedos**

18 Compared with spectral optical properties, our broadband results have wider
19 implications for the research community. Figure 5 shows the spectrally weighted $1-\omega$
20 for coated ($1-\omega_{\text{int, integrated}}$) and uncoated BC ($1-\omega_{\text{ext, integrated}}$), and the ratios ($E_{1-\omega, \text{ integrated}}$)
21 of $1-\omega_{\text{int, integrated}}$ versus $1-\omega_{\text{ext, integrated}}$. In general, $1-\omega_{\text{int, integrated}}$ is larger than $1-\omega_{\text{ext}}$,

1 integrated, and $E_{1-\omega, \text{integrated}}$ increased with BC concentration and core/shell ratio, but is
 2 little affected by snow grain size. $E_{1-\omega, \text{integrated}}$ is in a range of 1.0 to ~ 1.35 and 1.0 to
 3 ~ 1.23 for non-absorbing and absorbing shell, respectively, with BC concentrations
 4 within 1000 ng g^{-1} and core/shell ratios of 1.2-2.5. For a given BC concentration and
 5 core/shell ratio, $E_{1-\omega, \text{integrated}}$ for non-absorbing shell is larger than that for absorbing
 6 shell. In addition, $E_{1-\omega, \text{integrated}}$ of the original SNICAR model is closed to that of non-
 7 absorbing shell at a core/shell ratio of 1.5.

8 Figure 6 6a and b shows the spectrally weighted snow albedo for coated ($\alpha_{\text{int, integrated}}$)
 9 and uncoated BC ($\alpha_{\text{ext, integrated}}$), and the ratios ($E_{\alpha, \text{integrated}}$) of $\alpha_{\text{int, integrated}}$ versus $\alpha_{\text{ext,}}$
 10 ~~integrated. E_{α} ($E_{\alpha, \text{integrated}}$).~~ Generally, $\alpha_{\text{int, integrated}}$ is smaller than $\alpha_{\text{ext, integrated}}$ by 0 to
 11 ~~$\times \times \times 0.069$ (0 to $\times \times \times 0.051$), and $E_{\alpha, \text{integrated}}$ varies varied from 1 to ~ 0.903 (1 to ~ 0.924)~~
 12 for non-absorbing (absorbing) shell with BC concentrations from 0 to 1000 ng g^{-1} , snow
 13 grain radius from $100 \mu\text{m}$ to $500 \mu\text{m}$, and core/shell ratios from 1.2 to 2.5. $E_{\alpha, \text{integrated}}$
 14 shows a decreased trend with increased BC concentration, core/shell ratio and snow
 15 grain size. In addition, the difference between $\alpha_{\text{ext, integrated}}$ and $\alpha_{\text{int, integrated}}$ (or $E_{\alpha, \text{integrated}}$)
 16 ~~$E_{\alpha, \text{integrated}}$~~ for non-absorbing shell is larger (or smaller) than that for absorbing shell.
 17 If considering these coating effects in real environments. For example, in clean snow,
 18 such as North American with a typical BC concentration of $\sim 50 \text{ ng g}^{-1}$ (Doherty et al.,
 19 2014), the difference between $\alpha_{\text{ext, integrated}}$ and $\alpha_{\text{int, integrated}}$ ~~$E_{\alpha, \text{integrated}}$~~ is in a range of
 20 ~~$\times \times \times 0.002$ - $\times \times \times 0.017$ 0.979 - 0.998 and $\times \times \times 0.001$ - $\times \times \times 0.012$ 0.985 - 0.998~~ for non-
 21 absorbing and absorbing shell, respectively, with core/shell ratios of 1.2-2.5 and snow

1 grain radius of 100-500 μm . In contrast, in polluted snow, such as Northeastern China,
 2 BC concentration is typically $\sim 1000 \text{ ng g}^{-1}$ in industrial regions. the difference between
 3 $\alpha_{\text{ext, integrated}}$ and $\alpha_{\text{int, integrated}}$ $E_{\alpha, \text{integrated}}$ ranges from ~~XXX0.008-XXX0.069~~ and
 4 ~~XXX0.007-XXX0.051~~ 0.903 to 0.991 and 0.924 to 0.992 for non-absorbing and
 5 absorbing shell, respectively, lower than the results in clean snow. The results show
 6 that the impact of coating effect on snow albedo can leads the snow albedo reduced by
 7 $\sim 2\%$ in clean snow and $\sim 10\%$ in polluted snow for ~~internal mixed particles~~
 8 ~~relative coated BC to than that for external mixed particles uncoated BC~~. In addition, the
 9 sensitivity of $E_{\alpha, \text{integrated}}$ to BC decreases with increasing BC concentration due to the
 10 nonlinear effect of BC on snow albedo (Flanner et al., 2007). For example, the
 11 difference of $E_{\alpha, \text{integrated}}$ is 0.009 (0.006) between BC concentrations of 100 and 200 ng g^{-1} ,
 12 but only 0.003 (0.002) between BC concentrations of 900 and 1000 ng g^{-1} at a
 13 core/shell ratio of 2.5 and snow grain radius of 200 μm for non-absorbing shell
 14 (absorbing shell). We note again that the original SNICAR model only reflects the
 15 impact of coating effect on snow albedo at an intermediate core/shell ratio of ~ 1.5 .

17 Figure 7 shows the spectrally weighted snow albedo reductions by coated ($\Delta\alpha_{\text{int, integrated}}$)
 18 and uncoated BC ($\Delta\alpha_{\text{ext, integrated}}$), and the ratios ($E_{\Delta\alpha, \text{integrated}}$) of $\Delta\alpha_{\text{int, integrated}}$
 19 versus $\Delta\alpha_{\text{ext, integrated}}$. Different from $E_{\alpha, \text{integrated}}$, $E_{\Delta\alpha, \text{integrated}}$ is dominated by core/shell
 20 ratio, but little dependent on snow grain size (Figures 7c and 6f). In addition, $E_{\Delta\alpha, \text{integrated}}$
 21 presents a slight decreased trend with increased BC concentration. Comparing Figure

1 7c and f, we find that the material of particle shell presents a distinct impact on $E_{\Delta\alpha}$,
2 $E_{\Delta\alpha, \text{integrated}}$ mostly falls in a range of 1.11 to ~ 1.80 (1.10 to ~ 1.33) for non-
3 absorbing (absorbing) shell with core/shell ratios from 1.2 to 2.5. Our results were
4 comparable with the previous study that the snow albedo reduction of BC-snow internal
5 mixing is larger than external mixing by a factor of 0.2-1.0 (He et al., 2018cb). On the
6 other hand, the $E_{\Delta\alpha, \text{integrated}}$ from the original SNICAR model only shows a small
7 variation of 1.23–1.31. This is similar to a non-absorbing shell with a core/shell ratio
8 of ~ 1.5 , which implies the original SNICAR model only reflects a coating effect on
9 snow albedo reduction at an intermediate core/shell ratio and may lead to possible
10 biases of -10% to 50% in snow albedo reduction calculation.

11 ~~Core/shell ratios dominate variations in spectrally weighted $E_{1-\omega, \text{integrated}}$, $E_{\alpha, \text{integrated}}$~~
12 ~~and $E_{\Delta\alpha, \text{integrated}}$ (Figure 3). Snow grain size and BC concentration show a~~
13 ~~negative contribution to $E_{\alpha, \text{integrated}}$, but barely affect $E_{\Delta\alpha, \text{integrated}}$. However, the type of~~
14 ~~particle shell has a significant impact on $E_{1-\omega, \text{integrated}}$, $E_{\alpha, \text{integrated}}$, and $E_{\Delta\alpha, \text{integrated}}$.~~
15 ~~Compared with $E_{1-\omega, \text{integrated}}$ and $E_{\alpha, \text{integrated}}$, $E_{\Delta\alpha, \text{integrated}}$ has a more direct influence on~~
16 ~~radiative forcing and climate change. $E_{\Delta\alpha, \text{integrated}}$ largely falls within a range of 1.11 to~~
17 ~~~ 1.80 for a non-absorbing shell, which exceeds the values for an absorbing shell (1.10~~
18 ~~to ~ 1.33) by a factor of 1.0–1.35 (with BC concentrations within 1000 ng g^{-1} , a snow~~
19 ~~grain radius of 100–500 μm , and core/shell ratios from 1.2 to 2.5). Our results were~~
20 ~~comparable with the previous study that the snow albedo reduction of BC-snow internal~~
21 ~~mixing is larger than external mixing by a factor of 0.2–1.0 (He et al., 2018b). In~~

1 ~~contrast~~On the other hand, the $E_{\Delta\alpha, \text{integrated}}$ from the original SNICAR model only shows
2 ~~a small variation of 1.23–1.31. This is similar to a non-absorbing shell with a core/shell~~
3 ~~ratio of ~1.5, which implies the original SNICAR model only reflects a coating effect~~
4 ~~on snow albedo reduction at an intermediate core/shell ratio and may lead to possible~~
5 ~~biases of ~10% to 50% in snow albedo reduction calculation.~~

6 **3.4 Uncertainties**

7 Although the imaginary RI value of OC has been theoretically calculated (Section
8 2.1), we note that in real snowpack there is large uncertainty because the types and
9 optical properties of OC varies spatially and temporally due to different emission
10 sources and photochemical reactions in the atmosphere (e.g. Lack and Cappa, 2010).
11 To address this issue, we tested the degree of influence of imaginary RI on $E_{\alpha, \text{integrated}}$,
12 and $E_{\Delta\alpha, \text{integrated}}$ values by increasing and decreasing the calculated imaginary RI by 50%
13 (Figure S1), which studies have shown to be plausible (e.g., Lack et al., 2012). We find
14 imaginary RI uncertainty to be $\pm 1\%$ for $E_{\alpha, \text{integrated}}$ and $\pm 5\%$ for $E_{\Delta\alpha, \text{integrated}}$.

15 In addition, observations show large variation in the size distribution of
16 atmospheric and snow BC particles (Schwarz et al., 2013), which can affect snow
17 optical properties and albedo (He et al., 2018). Therefore, we examined the effects of
18 BC particle size on $E_{\alpha, \text{integrated}}$ and $E_{\Delta\alpha, \text{integrated}}$ with two additional BC diameters of 50
19 nm and 150 nm, which are within observed size ranges (Schwarz et al., 2013) and are
20 comparable to BC particle sizes used in other studies (e.g. He et al., 2018**b**). We find
21 the uncertainty attributed to BC diameter is $\pm 1\%$ for $E_{\alpha, \text{integrated}}$ and $\pm 13\%$ for $E_{\Delta\alpha, \text{integrated}}$.

1 integrated. According to Equation 2, the uncertainty for $E_{\alpha, \text{integrated}}$ is equivalent to that for
2 snow albedo and the uncertainty for $E_{\Delta\alpha, \text{integrated}}$ is equivalent to that for snow albedo
3 reduction. ThereforeOverall, the total uncertainty related to imaginary RI and BC
4 diameter is $\pm 1.4\%$ for $E_{\alpha, \text{integrated}}$ (snow albedo) and $\pm 13.9\%$ for $E_{\Delta\alpha, \text{integrated}}$ (snow
5 albedo reduction).

6 Another important issue is that in real environments, BC mixtures with other
7 species are likely much more complex than uniform coatings on spheres, hence a core-
8 shell assumption seems somewhat dubious. –However, a recent study observing
9 individual particle structure and mixing states between the glacier–snowpack and
10 atmosphere (Dong et al., 2018) found that fresh BC particles are generally characterized
11 with fractal morphology, which has a large quantity in the atmosphere. In contrast, in
12 the snowpack, aged BC particles dominated the BC content and the mixing states of
13 aged BC particles change largely to the internal mixing forms with BC as the core. This
14 process is characterized by the initial transformation from a fractal structure to spherical
15 morphology and the subsequent growth of fully compact particles during the transport
16 and deposition process. Therefore, a core-shell assumption for coated BC in snowpack
17 seems to be plausible. In addition, most field measurements can not capture the explicit
18 structure of coated BC due to limited observation methods (e.g. Doherty et al., 2010,
19 2014; Wang et al., 2013; Li et al., 2017, 2018; Pu et al., 2017; Zhang et al., 2017, 2018),
20 therefore even if a model for explicit BC structure was developed, researchers are hard
21 to use it for studying the effect of coated BC on snow albedo reductions at present.

1 Moreover, a core-shell assumption for coated BC in the atmosphere has been widely
2 applied by most global climate models (e.g. Jacobson, 2001; Bond et al. 2013), so that
3 our parameterizations for coated BC in snowpack can be easily linked to them. In
4 summary, we indicate that a core-shell assumption for coated BC in snowpack is
5 plausible and practical for field observations and model simulations at present in despite
6 of the possible uncertainties. However, with the developments of measurement methods
7 and climate models, building a more explicit structure for coated BC in snowpack is
8 actually needed in the future.

9 **3.5 Parameterizations of the coating effect**

10 Figure 874 compares parameterized $E_{\alpha, \text{integrated, para}}$ with SNICAR-modeled $E_{\alpha, \text{integrated}}$,
11 and Tables S1 and S2 list the empirical coefficients (see Section 2.3) derived
12 from nonlinear regression processes. This parameterization is under the assumptions of
13 semi-infinite snowpack, BC-snow external mixing, and spherical snow grains as
14 mentioned in Section 2. Generally, $E_{\alpha, \text{integrated, para}}$ and $E_{\alpha, \text{integrated}}$ show a strong
15 correlation, with $R^2 = 0.988$ (0.986) for a non-absorbing shell and $R^2 = 0.987$ (0.986)
16 for an absorbing shell in relatively clean (polluted) snow, and root mean squared errors
17 of $1.81 \cdot 10^{-3}$ ($4.70 \cdot 10^{-3}$) and $1.41 \cdot 10^{-3}$ ($3.76 \cdot 10^{-3}$), respectively. Biases for $E_{\alpha, \text{integrated, para}}$
18 are smallest for intermediate BC concentrations ~~and snow grain radius~~, but
19 become relatively larger at extremely low or high values, due mainly to processes
20 within the nonlinear regression method. In addition, the snow grain size has small
21 impacts on the accuracy of parameterized results, so that the parameterizations can be

1 applied in either fresh snow or old snow types. Overall, the $E_{\alpha, \text{integrated}}$ can be well
2 reproduced by $E_{\alpha, \text{integrated, para}}$ and the parameterizations are applicable in various snow
3 pollution conditions with BC concentrations from 0-1000 ng g⁻¹, core/shell ratios from
4 1.1 to 3.0, and different coating materials (non-absorbing and absorbing shell). We note
5 that if BC concentration is larger than 1000 ng g⁻¹, the parameterization for relatively
6 polluted snow is also applicable with a small negative ~~-(positive)~~ bias. Overall, the $E_{\alpha,$
7 integrated can be well reproduced by $E_{\alpha, \text{integrated, para}}$ for both a non-absorbing and absorbing
8 shell under the conditions of both relatively clean and polluted snow.

9 Therefore, other studies can estimate the coating effect of BC on snow albedos
10 and radiative forcing very conveniently by combining the original SNICAR or other
11 snow radiative forcing model with our new parameterizations, which ~~can~~ may reduce
12 snow albedo simulation bias. ~~For example, Wang et al. (2017) compared observations~~
13 ~~and model simulations of snow albedo reduction in northern China. They found~~
14 ~~simulated results overestimated snow albedo by -0.06 in polluted snow, despite~~
15 ~~considering the effects of all LAP types (BC, OC, and dust), snow grain type, and snow~~
16 ~~depth. However, if the coating effect is taken into account and the new~~
17 ~~parameterizations are applied (according to their measured LAPs and snow parameters),~~
18 ~~the difference between simulation and observation is reduced to -0.02, thereby~~
19 ~~improving the simulation. Furthermore~~ On the other hand, although most global climate
20 models (GCMs) account for coated BC in the atmosphere, ~~although most global~~
21 climate models (GCMs) account for internal mixing of atmospheric BC, they barely

1 consider the coating effect for BC in snow (Bond et al., 2013).— In —addition, different
2 GCMs apply different types of snow radiative transfer models, which means that one
3 physical mechanism responsible for the BC coating effect in snow cannot be suitable
4 for all GCMs. Hence, our parameterizations isare good for the climate models to have
5 an option for BC coating effects in snow~~In this case our parameterizations are~~
6 ~~particularly helpful, as they are easily used in any GCM and improve understanding of~~
7 ~~how BC in snow influences local hydrological cycles and global climate.~~

8 **3.6 Measurement-based estimate of coating effect**

9 To evaluate the coating effect of BC on both snow albedo and radiative forcing in
10 real snowpack, we collected in situ measurements of BC and OC concentrations in
11 snow (Figure [895](#)) during field campaigns in the Arctic in spring 2007–2009 (Doherty
12 et al., 2010), North America in January–March 2013 (Doherty et al., 2014), northern
13 China in January–February 2010 and 2012 (Ye et al., 2012; Wang et al., 2013), and the
14 Tibetan Plateau in spring 2010 and 2012 (Wang et al., 2013; Li et al., 2017, 2018; Pu
15 et al., 2017; Zhang et al., 2017, 2018). Measurements are separated into four
16 geographical regions (Figure [895c](#)): the Arctic, North America (NA), northern China
17 (NC), and the Tibetan Plateau (TP). An absorbing shell of OC was assumed in measured
18 snowpack, which is plausible because previous studies have found that OC is the
19 dominant coating in the atmosphere (e.g., Cappa et al., 2012) and snow (Dong et al.,
20 2018). The OC/BC mass ratio is generally from 1 to 10, with the corresponding
21 core/shell ratio from 1.3 to 2.5 (Figure [895b](#)). The average core/shell ratio was highest

1 (2.45) in the TP, followed by 1.92 and 1.81 in the Arctic and NC, respectively, and
2 lowest (1.31) in NA (Figure 895d). These results reveal the BC coating effect had a
3 larger impact on snow albedo in the TP than in other regions. In this study, the
4 assumption that all measured OC resides as coating on BC particles were mainly used
5 to show the upper bound of coating effect on snow albedo reduction, which was
6 comparable with the previous studies (e.g. He et al. 2018c).

7 Figure 910 shows the statistics for snow albedo reductions and radiative forcing
8 in different regions for fresh snow (snow grain radius =100 μm) and old snow (snow
9 grain radius =1000 μm). The spatial distributions of snow albedo reductions and
10 radiative forcing are presented in Figure S3 and S4. Briefly, the TP snowpack suffers
11 the highest snow albedo reduction (0.066), and the regional average snow albedo
12 reductions are lower in NC (0.055), NA (0.009), and the Arctic (0.007) for fresh snow
13 in the case of external mixing (Figure 10a). Accordingly, the regional average radiative
14 forcing is 11.63, 4.42, 0.97, and 0.56 W m^{-2} in TP, NC, NA, and the Arctic (Figure
15 910b). In the case of internal mixing, the regional average snow albedo reductions are
16 0.084, 0.065, 0.011, and 0.009 in TP, NC, NA, and the Arctic, with the corresponding
17 radiative forcing of 14.84, 5.51, 1.11, and 0.69 W m^{-2} . Figure 101 shows the
18 comparisons of internal mixing to external mixing. Figure 6 presents the coating effect
19 on snow albedo reduction and radiative forcing based on measured BC in real snowpack,
20 and Figures S3–S5 show spatial distributions and statistics. For fresh snow, we find that
21 EMP-coated BC results in greater snow albedo reductions compared with EMP-uncoated

1 BC by factors of 1.27, 1.19, 1.13, and 1.23 in the TP, NC, NA, and the Arctic,
2 respectively (Figures 1016a and 101b). Correspondingly, we find that ~~HMP~~ the coating
3 effect leads radiative forcing by 1.27, 1.20, 1.14, and 1.22 for these same regions. The
4 highest (lowest) enhancement was found in the TP (NA), which corresponds to the
5 highest (lowest) OC/BC mass ratio and core/shell ratio in the TP (NA). For old snow_{5,2}
6 the regional average snow albedo reductions are 0.17 (0.21), 0.14 (0.17), 0.028 (0.033)
7 and 0.022 (0.027) in TP, NC, NA, and the Arctic for external (internal) mixing (Figure
8 910c). The corresponding radiative forcing are 38.2 (47.6), 19.2 (22.7), 4.6 (5.2) and
9 3.6 (4.6) W m⁻² (Figure 910d). The enhancement of snow albedo reductions due to the
10 BC coating effect are 1.24, 1.15, 1.13, and 1.23 in TP, NC, NA, and the Arctic,
11 respectively (Figure 101c). The corresponding radiative forcing reductions are 1.24,
12 1.16, 1.14, and 1.22 (Figure 101d). The enhancement shows a slight decrease with
13 snowpack aging, which is consistent with the results in Figure 73. Of note, we found
14 the contribution of coating effect to light absorption has exceeded dust over most areas
15 of northern China after comparing with previous studies of dust in snow (Wang et al.,
16 2013, 2017; Pu et al., 2017), which further demonstrated the critical role of BC coatings
17 in snow albedo evaluation.

18 In contrast to previous studies, we note that enhanced light absorption in snow
19 from the BC coating effect should be taken into account, especially in the Arctic and
20 the TP. Arctic sea ice has shown a sharp decline in recent decades (Ding et al., 2019),
21 and climate models predict a continued decreasing trend (Liu et al., 2020) that is likely

1 to perturb the Earth system and influence human activities (Meier et al., 2014). Multi-
2 model ensemble simulations indicate that greenhouse gases cannot fully explain this
3 decline, and recent studies have proposed that BC deposition in snow and sea ice is an
4 important additional contributor (e.g., Ramanathan and Carmichael, 2008).
5 Furthermore, the TP holds the largest ice mass outside polar regions, and acts as a water
6 ‘storage tower’ for more than 1 billion people in South and East Asia. Tibetan glaciers
7 have rapidly retreated over the last 30 years (Yao et al., 2012), raising the possibility
8 that many glaciers and their fresh water supplies could disappear by the middle of the
9 21st century. Observed evidence suggests that BC deposition is a significant
10 contributing factor to this retreat (Xu et al., 2009), but quantitatively modeling the effect
11 of BC on glacier dynamics is a challenge, partly because of incomplete radiative
12 transfer mechanisms within models. Due to the significant contribution of BC to
13 retreating Arctic sea ice and Tibetan glaciers, and the strong enhancement of light
14 absorption by coated BC, the coating effect must now be considered in climate models
15 that are designed to accurately reconstruct both the historical record and future change.

16 **4 Conclusions**

17 This study evaluated the effect of BC coating on snow albedo and radiative forcing
18 by combining core/shell Mie theory and the snow-albedo model SNICAR. We found that
19 the coating effect ~~reduces~~enhances snow albedo reduction by a factor of 1.11–1.80 for
20 a non-absorbing shell and 1.10–1.33 for an absorbing shell, when BC concentrations
21 are within 1000 ng g^{-1} , the snow grain radius is $100\text{--}500 \mu\text{m}$, and the core/shell ratio is

1 1.2–2.5. The core/shell ratio plays a dominant role in reducing snow albedo.
2 Furthermore, an absorbing shell causes a smaller snow albedo reduction than a non-
3 absorbing shell because of a lensing effect, whereby the absorbing shell reduces photon
4 absorbance in the BC core. Our results can effectively account for the complex
5 enhancement of snow albedo reduction due to coating effect in real environments.

6 Parameterizations for the coating effect are further developed for use in snow
7 albedo and climate models. Parameterized and simulated results show strong
8 correlations for both clean and polluted snowpack. The root mean squared error of
9 parameterized $E_{a, \text{integrated, para}}$ is low ($1.41 \cdot 10^{-3}$). A list of empirical coefficients for
10 parameterizations is provided for most seasonal snowpack field cases, with BC
11 concentrations within 1000 ng g^{-1} , snow grain sizes from ~~5100~~– $1000 \mu\text{m}$, and core/shell
12 ratios from 1.1 to 3.0. We demonstrate that parameterizations can reduce simulation
13 bias for local experiments in snow albedo models and, more importantly, can be applied
14 to GCMs to improve our understanding of how BC in snow affects local hydrological
15 cycles and global climate.

16 Based on a comprehensive set of field measurements across the Northern
17 Hemisphere, the BC coating effect in real snowpack was evaluated by assuming the
18 presence of an absorbing OC shell. The enhancement of snow albedo reduction was
19 ~~1.133–1.273~~ and enhancement of radiative forcing was ~~1.1435~~– 1.274 , which exceeds
20 the contribution of dust to snow light absorption over most areas of northern China. Of
21 note, the greatest enhancements were detected on the Tibetan Plateau and in the Arctic,

- 1 which will likely contribute to further Arctic sea ice and Tibetan glacier retreat. Our
- 2 findings indicate that the coating effect must be considered in future climate models, in
- 3 particular to more accurately evaluate the climate of the Tibetan Plateau and the Arctic.

1 **Conflict of interest**

2 The authors declare that they have no conflict of interest.

3 **Acknowledgments**

4 This research was supported jointly by [the National Science Fund for](#)
5 [Distinguished Young Scholars \(42025102\)](#), the National Key R&D Program of China
6 (2019YFA0606801), ~~the~~ the National Natural Science Foundation of China ([42075061](#),
7 41975157 and 41775144), and the China Postdoctoral Science Foundation
8 (2020M673530).

9 **Author contributions**

10 X Wang and W Pu invited the project. W Pu and X Wang designed the study. W
11 Pu wrote the paper with contributions from all co-authors. TL Shi processed and
12 analyzed the data.

1 **References**

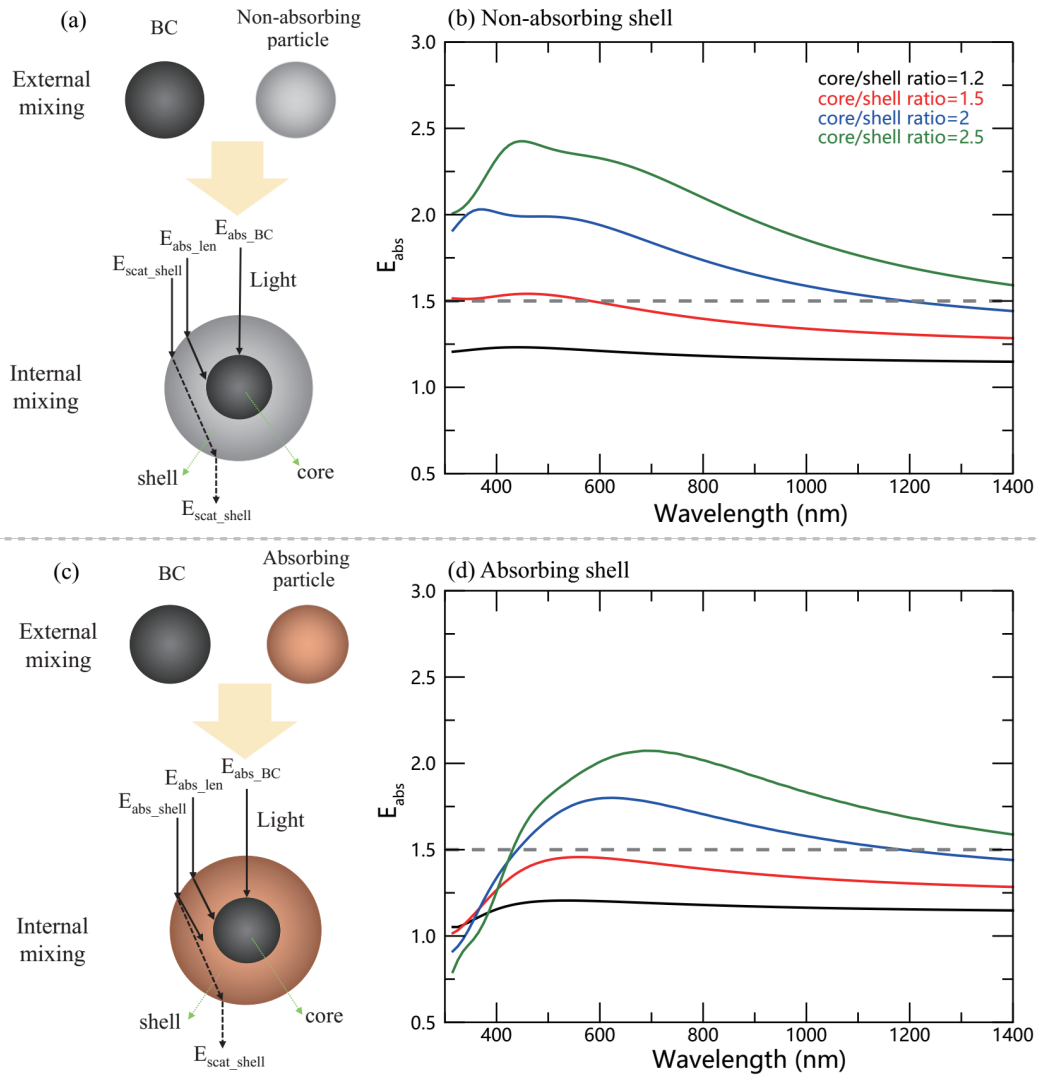
- 2 Aquila, V., Hendricks, J., Lauer, A., Riemer, N., Vogel, H., Baumgardner, D., Minikin,
3 A., Petzold, A., Schwarz, J., and Spackman, J.: MADE-in: A new aerosol
4 microphysics submodel for global simulation of insoluble particles and their
5 mixing state, *Geosci. Model Dev.*, 4, 325-355, 2011.
- 6 Bond, T. C., Habib, G., and Bergstrom, R. W.: Limitations in the enhancement of
7 visible light absorption due to mixing state, *J. Geophys. Res.-Atmos.*, 111, D20,
8 2006.
- 9 Bond, T. C., Doherty, S. J., Fahey, D. W., Forster, P. M., Berntsen, T., DeAngelo, B.
10 J., Flanner, M. G., Ghan, S., Karcher, B., Koch, D., Kinne, S., Kondo, Y., Quinn,
11 P. K., Sarofim, M. C., Schultz, M. G., Schulz, M., Venkataraman, C., Zhang, H.,
12 Zhang, S., Bellouin, N., Guttikunda, S. K., Hopke, P. K., Jacobson, M. Z., Kaiser,
13 J. W., Klimont, Z., Lohmann, U., Schwarz, J. P., Shindell, D., Storelvmo, T.,
14 Warren, S. G., and Zender, C. S.: Bounding the role of black carbon in the climate
15 system: A scientific assessment, *J. Geophys. Res.-Atmos.*, 118, 5380-5552, 2013.
- 16 Cappa, C. D., Onasch, T. B., Massoli, P., Worsnop, D. R., Bates, T. S., Cross, E. S.,
17 Davidovits, P., Hakala, J., Hayden, K. L., Jobson, B. T., Kolesar, K. R., Lack, D.
18 A., Lerner, B. M., Li, S. M., Mellon, D., Nuaaman, I., Olfert, J. S., Petaja, T.,
19 Quinn, P. K., Song, C., Subramanian, R., Williams, E. J., and Zaveri, R. A.:
20 Radiative Absorption Enhancements Due to the Mixing State of Atmospheric
21 Black Carbon, *Science*, 337, 1078-1081, 2012.
- 22 Cohen, J., and Rind, D.: The effect of snow cover on the climate, *J. Climate*, 4, 689-
23 706, 1991.
- 24 Corbin, J. C., Pieber, S. M., Czech, H., Zanatta, M., Jakobi, G., Massabò, D., Orasche,
25 J., El Haddad, I., Mensah, A. A., and Stengel, B.: Brown and black carbon emitted
26 by a marine engine operated on heavy fuel oil and distillate fuels: optical
27 properties, size distributions, and emission factors, *J. Geophys. Res.-Atmos.*, 123,
28 6175-6195, 2018.
- 29 [Dang, C., Brandt, R. E., and Warren, S. G.: Parameterizations for narrowband and
30 broadband albedo of pure snow and snow containing mineral dust and black
31 carbon, *J Geophys Res-Atmos*, 120, 5446-5468, 2015.](#)
- 32 Dang, C., Fu, Q., and Warren, S. G.: Effect of Snow Grain Shape on Snow Albedo, *J.*
33 *Atmos. Sci.*, 73, 3573-3583, 2016.
- 34 Dang, C., Warren, S. G., Fu, Q., Doherty, S. J., and Sturm, M.: Measurements of light -
35 absorbing particles in snow across the Arctic, North America, and China: effects
36 on surface albedo, *J. Geophys. Res.-Atmos.*, 122, 10149-10168, 2017.
- 37 Ding, Q., Schweiger, A., L'Heureux, M., Steig, E. J., Battisti, D. S., Johnson, N. C.,
38 Blanchard-Wrigglesworth, E., Po-Chedley, S., Zhang, Q., and Harnos, K.:
39 Fingerprints of internal drivers of Arctic sea ice loss in observations and model
40 simulations, *Nat. Geosci.*, 12, 28-33, 2019.
- 41 Doherty, S. J., Warren, S. G., Grenfell, T. C., Clarke, A. D., and Brandt, R. E.: Light-

- 1 absorbing impurities in Arctic snow, *Atmos. Chem. Phys.*, 10, 11647-11680, 2010.
- 2 Doherty, S. J., Dang, C., Hegg, D. A., Zhang, R., and Warren, S. G.: Black carbon and
3 other light-absorbing particles in snow of central North America, *J. Geophys.*
4 *Res.-Atmos.*, 119, 12807-12831, 2014.
- 5 [Dong, Z., Kang, S., Qin, D., Shao, Y., Ulbrich, S., and Qin, X.: Variability in individual
6 particle structure and mixing states between the glacier–snowpack and atmosphere
7 in the northeastern Tibetan Plateau, *The Cryosphere*, 12, 3877-3890, 2018.](#)
- 8 [Flanner, M. G., Liu, X., Zhou, C., Penner, J. E., and Jiao, C.: Enhanced solar energy
9 absorption by internally-mixed black carbon in snow grains, *Atmos Chem Phys*,
10 12, 4699-4721, 2012.](#)
- 11 Flanner, M. G., Zender, C. S., Randerson, J. T., and Rasch, P. J.: Present-day climate
12 forcing and response from black carbon in snow, *J. Geophys. Res.*, 112, D11, 2007.
- 13 [Grannas, A. M., Jones, A. E., Dibb, J., Ammann, M., Anastasio, C., Beine, H. J., Bergin,
14 M., Bottenheim, J., Boxe, C. S., Carver, G., Chen, G., Crawford, J. H., Domine,
15 F., Frey, M. M., Guzman, M. I., Heard, D. E., Helmig, D., Hoffmann, M. R.,
16 Honrath, R. E., Huey, L. G., Hutterli, M., Jacobi, H. W., Klan, P., Lefer, B.,
17 McConnell, J., Plane, J., Sander, R., Savarino, J., Shepson, P. B., Simpson, W. R.,
18 Sodeau, J. R., von Glasow, R., Weller, R., Wolff, E. W., and Zhu, T.: An overview
19 of snow photochemistry: evidence, mechanisms and impacts, *Atmos Chem Phys*,
20 7, 4329-4373, 2007.](#)
- 21 Hadley, O. L., and Kirchstetter, T. W.: Black-carbon reduction of snow albedo, *Nat.*
22 *Clim. Change*, 2, 437-440, 2012.
- 23 He, C. L., Takano, Y., Liou, K. N., Yang, P., Li, Q., Chen, F., He, C., Takano, Y., Liou,
24 K. N., and Yang, P.: Impact of Snow Grain Shape and Black Carbon-Snow
25 Internal Mixing on Snow Optical Properties: Parameterizations for Climate
26 Models, *J. Climate*, 30, 10019-10036, 2017.
- 27 ~~He, C. L., Liou, K. N., and Takano, Y.: Resolving Size Distribution of Black Carbon
28 Internally Mixed With Snow: Impact on Snow Optical Properties and Albedo,
29 *Geophys. Res. Lett.*, 45, 2697-2705, 2018.~~ [He, C. L., Flanner, M. G., Chen, F.,
30 Barlage, M., Liou, K. N., Kang, S. C., Ming, J., and Qian, Y.: Black carbon-
31 induced snow albedo reduction over the Tibetan Plateau: uncertainties from snow
32 grain shape and aerosol-snow mixing state based on an updated SNICAR model,
33 *Atmos Chem Phys*, 18, 11507-11527, 2018a.](#)
- 34 [He, C. L., Liou, K. N., and Takano, Y.: Resolving Size Distribution of Black Carbon
35 Internally Mixed With Snow: Impact on Snow Optical Properties and Albedo,
36 *Geophys. Res. Lett.*, 45, 2697-2705, 2018b.](#)
- 37 [He, C. L., Liou, K. N., Takano, Y., Yang, P., Qi, L., and Chen, F.: Impact of Grain
38 Shape and Multiple Black Carbon Internal Mixing on Snow Albedo:
39 Parameterization and Radiative Effect Analysis, *J Geophys Res-Atmos*, 123,
40 1253-1268, 2018c.](#)
- 41
- 42 Jacobson, M. Z.: Strong radiative heating due to the mixing state of black carbon in

- 1 atmospheric aerosols, *Nature*, 409, 695-697, 2001.
- 2 Kahnert, M., Nousiainen, T., Lindqvist, H., and Ebert, M.: Optical properties of light
3 absorbing carbon aggregates mixed with sulfate: assessment of different model
4 geometries for climate forcing calculations, *Opt. Express*, 20, 10042-10058, 2012.
- 5 [Kokhanovsky, A. A., and Zege, E. P.: Scattering optics of snow, *Appl Optics*, 43, 1589-
6 1602, 2004.](#)
- 7 Lack, D. A., and Cappa, C. D.: Impact of brown and clear carbon on light absorption
8 enhancement, single scatter albedo and absorption wavelength dependence of
9 black carbon, *Atmos. Chem. Phys.*, 10, 4207-4220, 2010.
- 10 Lack, D. A., Langridge, J. M., Bahreini, R., Cappa, C. D., Middlebrook, A. M., and
11 Schwarz, J. P.: Brown carbon and internal mixing in biomass burning particles,
12 *PNAS*, 109, 14802-14807, 2012.
- 13 Li, X., Kang, S., He, X., Qu, B., Tripathee, L., Jing, Z., Paudyal, R., Li, Y., Zhang, Y.,
14 and Yan, F.: Light-absorbing impurities accelerate glacier melt in the Central
15 Tibetan Plateau, *Sci. Total Environ.*, 587, 482-490, 2017.
- 16 Li, X., Kang, S., Zhang, G., Qu, B., Tripathee, L., Paudyal, R., Jing, Z., Zhang, Y., Yan,
17 F., and Li, G.: Light-absorbing impurities in a southern Tibetan Plateau glacier:
18 Variations and potential impact on snow albedo and radiative forcing, *Atmos. Res.*,
19 200, 77-87, 2018.
- 20 Liu, D. T., Whitehead, J., Alfarra, M. R., Reyes-Villegas, E., Spracklen, D. V.,
21 Reddington, C. L., Kong, S. F., Williams, P. I., Ting, Y. C., Haslett, S., Taylor, J.
22 W., Flynn, M. J., Morgan, W. T., McFiggans, G., Coe, H., and Allan, J. D.: Black-
23 carbon absorption enhancement in the atmosphere determined by particle mixing
24 state, *Nat. Geosci.*, 10, 184-U132, 2017.
- 25 Liu, J., Wu, D., Liu, G., Mao, R., Chen, S., Ji, M., Fu, P., Sun, Y., Pan, X., and Jin, H.:
26 Impact of Arctic amplification on declining spring dust events in East Asia, *Clim.*
27 *Dyn.*, 54, 1913-1935, 2020.
- 28
- 29 [Liou, K. N., Takano, Y., and Yang, P.: Light absorption and scattering by aggregates:
30 Application to black carbon and snow grains, *J Quant Spectrosc Ra*, 112, 1581-
31 1594, 2011.](#)
- 32 [Liou, K. N., Takano, Y., He, C., Yang, P., Leung, L. R., Gu, Y., and Lee, W. L.:
33 Stochastic parameterization for light absorption by internally mixed BC/dust in
34 snow grains for application to climate models, *J Geophys Res-Atmos*, 119, 7616-
35 7632, 2014.](#)
- 36 [Liu, X., Zhou, C., Penner, J. E., and Jiao, C.: Enhanced solar energy absorption by
37 internally-mixed black carbon in snow grains, *Atmos. Chem. Phys.*, 12, 4699-
38 4721, <https://doi.org/10.5194/acp-12-4699-2012>, 2012.](#)
- 39 Matsui, H., Hamilton, D. S., and Mahowald, N. M.: Black carbon radiative effects
40 highly sensitive to emitted particle size when resolving mixing-state diversity, *Nat.*
41 *Commun.*, 9, 1-11, 2018.
- 42 Meier, W. N., Hovelsrud, G. K., Van Oort, B. E., Key, J. R., Kovacs, K. M., Michel,

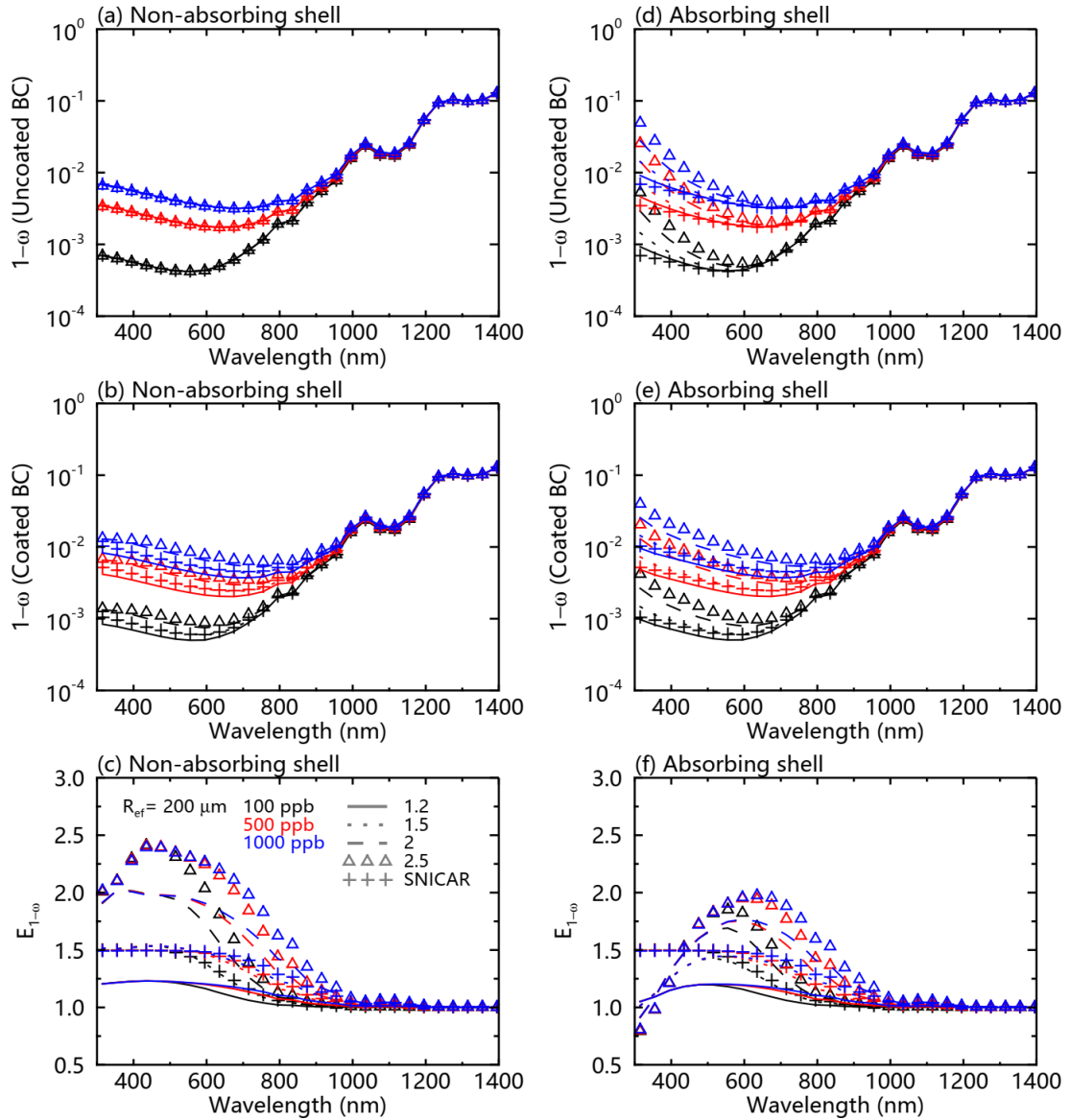
- 1 C., Haas, C., Granskog, M. A., Gerland, S., and Perovich, D. K.: Arctic sea ice in
2 transformation: A review of recent observed changes and impacts on biology and
3 human activity, *Rev. Geophys.*, 52, 185-217, 2014.
- 4 Moffet, R. C., and Prather, K. A.: In-situ measurements of the mixing state and optical
5 properties of soot with implications for radiative forcing estimates, *PNAS*, 106,
6 11872-11877, 2009.
- 7 Moteki, N., Kondo, Y., Miyazaki, Y., Takegawa, N., Komazaki, Y., Kurata, G., Shirai,
8 T., Blake, D. R., Miyakawa, T., and Koike, M.: Evolution of mixing state of black
9 carbon particles: Aircraft measurements over the western Pacific in March 2004,
10 *Geophys. Res. Lett.*, 34, L11803, 2007.
- 11 Peng, J. F., Hu, M., Guo, S., Du, Z. F., Zheng, J., Shang, D. J., Zamora, M. L., Zeng,
12 L. M., Shao, M., Wu, Y. S., Zheng, J., Wang, Y., Glen, C. R., Collins, D. R.,
13 Molina, M. J., and Zhang, R. Y.: Markedly enhanced absorption and direct
14 radiative forcing of black carbon under polluted urban environments, *PNAS*, 113,
15 4266-4271, 2016.
- 16 Pu, W., Wang, X., Wei, H., Zhou, Y., Shi, J., Hu, Z., Jin, H., and Chen, Q.: Properties
17 of black carbon and other insoluble light-absorbing particles in seasonal snow of
18 northwestern China, *The Cryosphere*, 11, 1213-1233, 2017.
- 19 Pu, W., Cui, J. C., Shi, T. L., Zhang, X. L., He, C. L., and Wang, X.: The remote sensing
20 of radiative forcing by light-absorbing particles (LAPs) in seasonal snow over
21 northeastern China, *Atmos. Chem. Phys.*, 19, 9949-9968, 2019.
- 22 Qian, Y., Gustafson, W. I., Leung, L. R., and Ghan, S. J.: Effects of soot-induced snow
23 albedo change on snowpack and hydrological cycle in western United States based
24 on Weather Research and Forecasting chemistry and regional climate simulations,
25 *J. Geophys. Res.-Atmos.*, 114, D3, 2009.
- 26 Ramanathan, V., and Carmichael, G.: Global and regional climate changes due to black
27 carbon, *Nat. Geosci.*, 1, 221-227, 2008.
- 28 Ricchiazzi, P., Yang, S., Gautier, C., and Sowle, D.: SBDART: A research and teaching
29 software tool for plane-parallel radiative transfer in the Earth's atmosphere, *Bull.*
30 *Amer. Meteor. Soc.*, 79, 2101-2114, 1998.
- 31 Schwarz, J. P., Gao, R. S., Perring, A. E., Spackman, J. R., and Fahey, D. W.: Black
32 carbon aerosol size in snow, *Sci. Rep.*, 3, 1356, 2013.
- 33 [Shi, T., Pu, W., Zhou, Y., Cui, J., Zhang, D., and Wang, X.: Albedo of Black Carbon-](#)
34 [Contaminated Snow Across Northwestern China and the Validation With Model](#)
35 [Simulation, *J. Geophys. Res.-Atmos.*, 125, e2019JD032065, 2020.](#)
- 36 Sun, H. L., Biedermann, L., and Bond, T. C.: Color of brown carbon: A model for
37 ultraviolet and visible light absorption by organic carbon aerosol, *Geophys. Res.*
38 *Lett.*, 34, L17813, 2007.
- 39 Toon, O. B., McKay, C. P., Ackerman, T. P., and Santhanam, K.: Rapid Calculation of
40 Radiative Heating Rates and Photodissociation Rates in Inhomogeneous Multiple-
41 Scattering Atmospheres, *J. Geophys. Res.-Atmos.*, 94, 16287-16301, 1989.
- 42 Turpin, B. J., and Lim, H. J.: Species contributions to PM_{2.5} mass concentrations:

- 1 Revisiting common assumptions for estimating organic mass, *Aerosol Sci. Tech.*,
2 35, 602-610, 2001.
- 3 Wang, X., Doherty, S. J., and Huang, J.: Black carbon and other light-absorbing
4 impurities in snow across Northern China, *J. Geophys. Res.-Atmos.*, 118, 1471-
5 1492, 2013.
- 6 Wang, X., Pu, W., Ren, Y., Zhang, X. L., Zhang, X. Y., Shi, J. S., Jin, H. C., Dai, M.
7 K., and Chen, Q. L.: Observations and model simulations of snow albedo
8 reduction in seasonal snow due to insoluble light-absorbing particles during 2014
9 Chinese survey, *Atmos. Chem. Phys.*, 17, 2279-2296, 2017.
- 10 Warren, S. G., and Wiscombe, W. J.: A Model for the Spectral Albedo of Snow. 2:
11 Snow Containing Atmospheric Aerosols, *J. Atmos. Sci.*, 37, 2734-2745, 1980.
- 12 Xu, B. Q., Cao, J. J., Hansen, J., Yao, T. D., Joswia, D. R., Wang, N. L., Wu, G. J.,
13 Wang, M., Zhao, H. B., Yang, W., Liu, X. Q., and He, J. Q.: Black soot and the
14 survival of Tibetan glaciers, *PNAS*, 106, 22114-22118, 2009.
- 15 [Yang, M., Howell, S. G., Zhuang, J., and Huebert, B. J.: Attribution of aerosol light
16 absorption to black carbon, brown carbon, and dust in China - interpretations of
17 atmospheric measurements during EAST-AIRE, *Atmos Chem Phys*, 9, 2035-2050,
18 2009.](#)
- 19 Yao, T. D., Thompson, L., Yang, W., Yu, W. S., Gao, Y., Guo, X. J., Yang, X. X.,
20 Duan, K. Q., Zhao, H. B., Xu, B. Q., Pu, J. C., Lu, A. X., Xiang, Y., Kattel, D. B.,
21 and Joswiak, D.: Different glacier status with atmospheric circulations in Tibetan
22 Plateau and surroundings, *Nat. Clim. Change*, 2, 663-667, 2012.
- 23 Ye, H., Zhang, R., Shi, J., Huang, J., Warren, S. G., and Fu, Q.: Black carbon in seasonal
24 snow across northern Xinjiang in northwestern China, *Environ. Res. Lett.*, 7,
25 044002, 2012.
- 26 You, R., Radney, J. G., Zachariah, M. R., and Zangmeister, C. D.: Measured
27 Wavelength-Dependent Absorption Enhancement of Internally Mixed Black
28 Carbon with Absorbing and Nonabsorbing Materials, *Environ. Sci. Technol.*, 50,
29 7982-7990, 2016.
- 30 Zhang, Y., Kang, S., Cong, Z., Schmale, J., Sprenger, M., Li, C., Yang, W., Gao, T.,
31 Sillanpää, M., and Li, X.: Light - absorbing impurities enhance glacier albedo
32 reduction in the southeastern Tibetan Plateau, *J. Geophys. Res.-Atmos.*, 122,
33 6915-6933, 2017.
- 34 Zhang, Y., Kang, S., Sprenger, M., Cong, Z., Gao, T., Li, C., Tao, S., Li, X., Zhong, X.,
35 and Xu, M.: Black carbon and mineral dust in snow cover on the Tibetan Plateau,
36 *The Cryosphere*, 12, 413-431, 2018.



1
2
3
4
5
6
7
8

Figure 1. Schematic diagrams showing the light absorption for an external mixture and internal mixture of BC, for (a) a non-absorbing particle and (c) an absorbing particle. Also shown is the enhancement of light absorption from the internal mixture (E_{abs}) compared to the external mixture of BC with (b) non-absorbing and (d) absorbing particles. The internal mixed particle was assumed to be a core/shell structure with a black carbon (BC) core.



1

2 **Figure 2.** Snow single-scattering co-albedo ($1-\omega$) as a function of wavelength, with
 3 different BC concentrations and core/shell ratios for (a) uncoated and (b) coated BC
 4 with an assumption of a non-absorbing shell. (d) and (e) are same as (a) and (b),
 5 respectively, but with an assumption of an absorbing shell. (c) shows the ratios of snow
 6 single-scattering co-albedo ($E_{1-\omega}$) for coated versus uncoated BC with an assumption
 7 of a non-absorbing shell. (f) is same as (c), but with an assumption of an absorbing shell.
 8 The snow grain radius was assumed to be 200 nm.

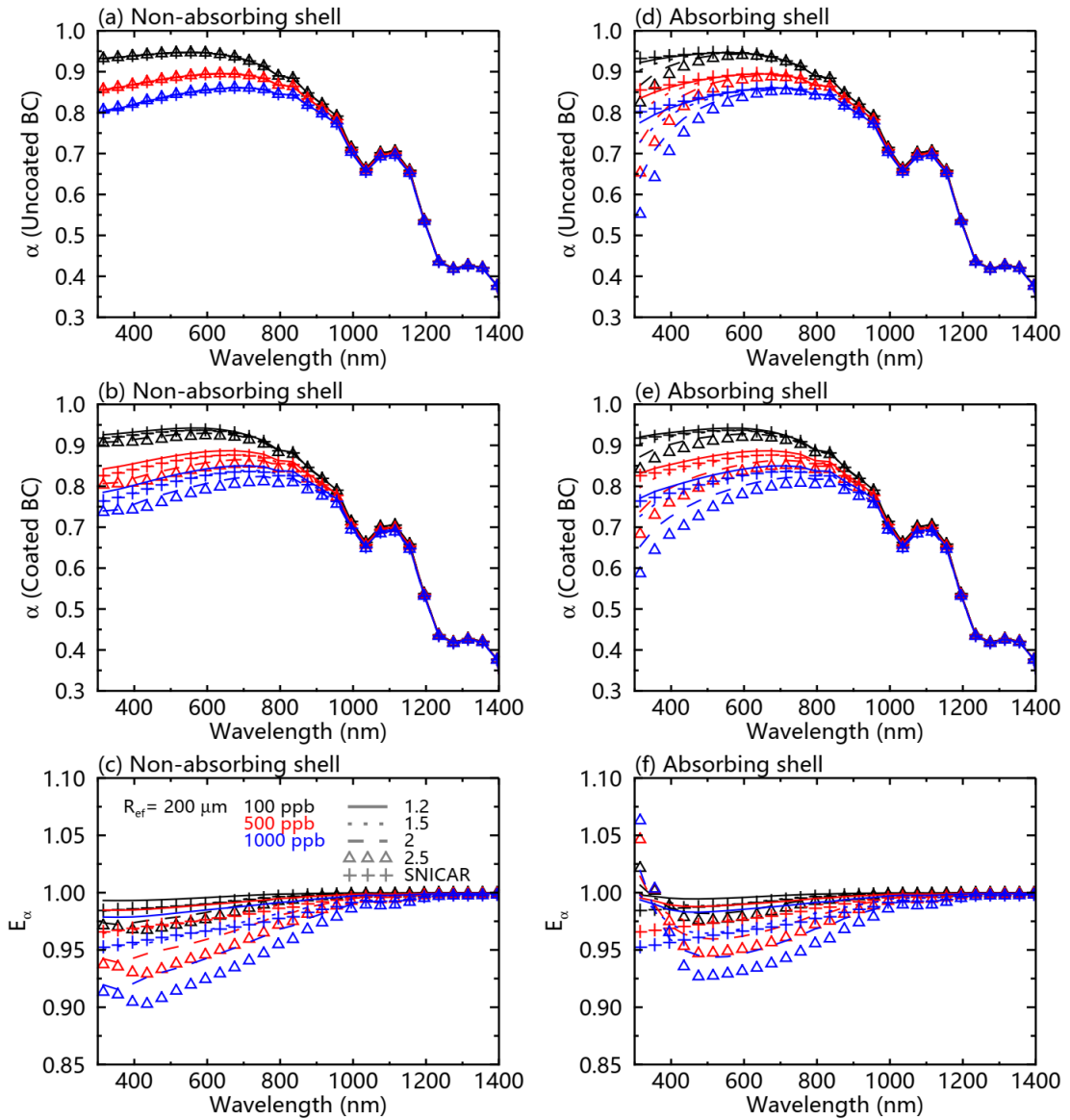
9

10

11

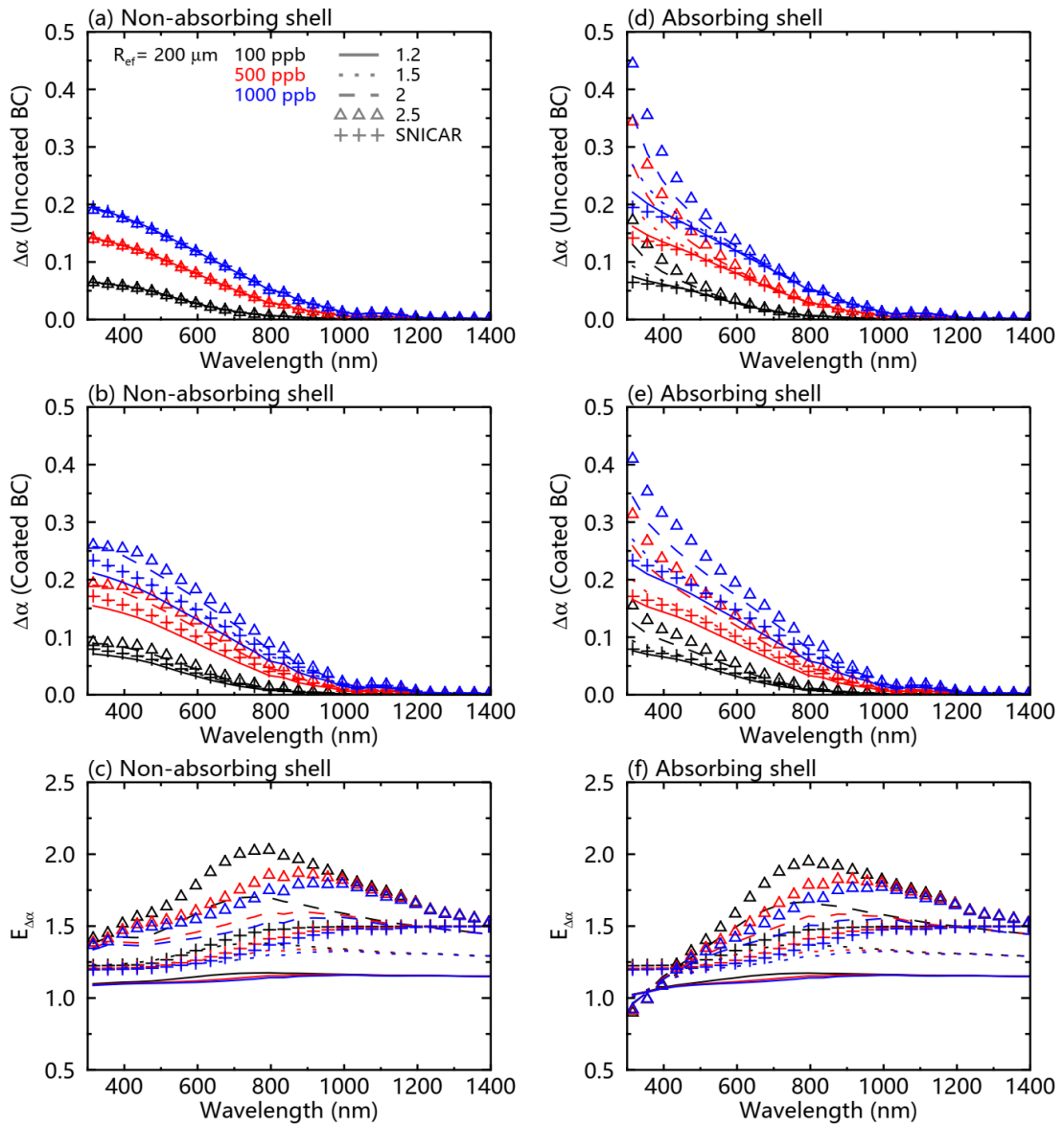
12

13



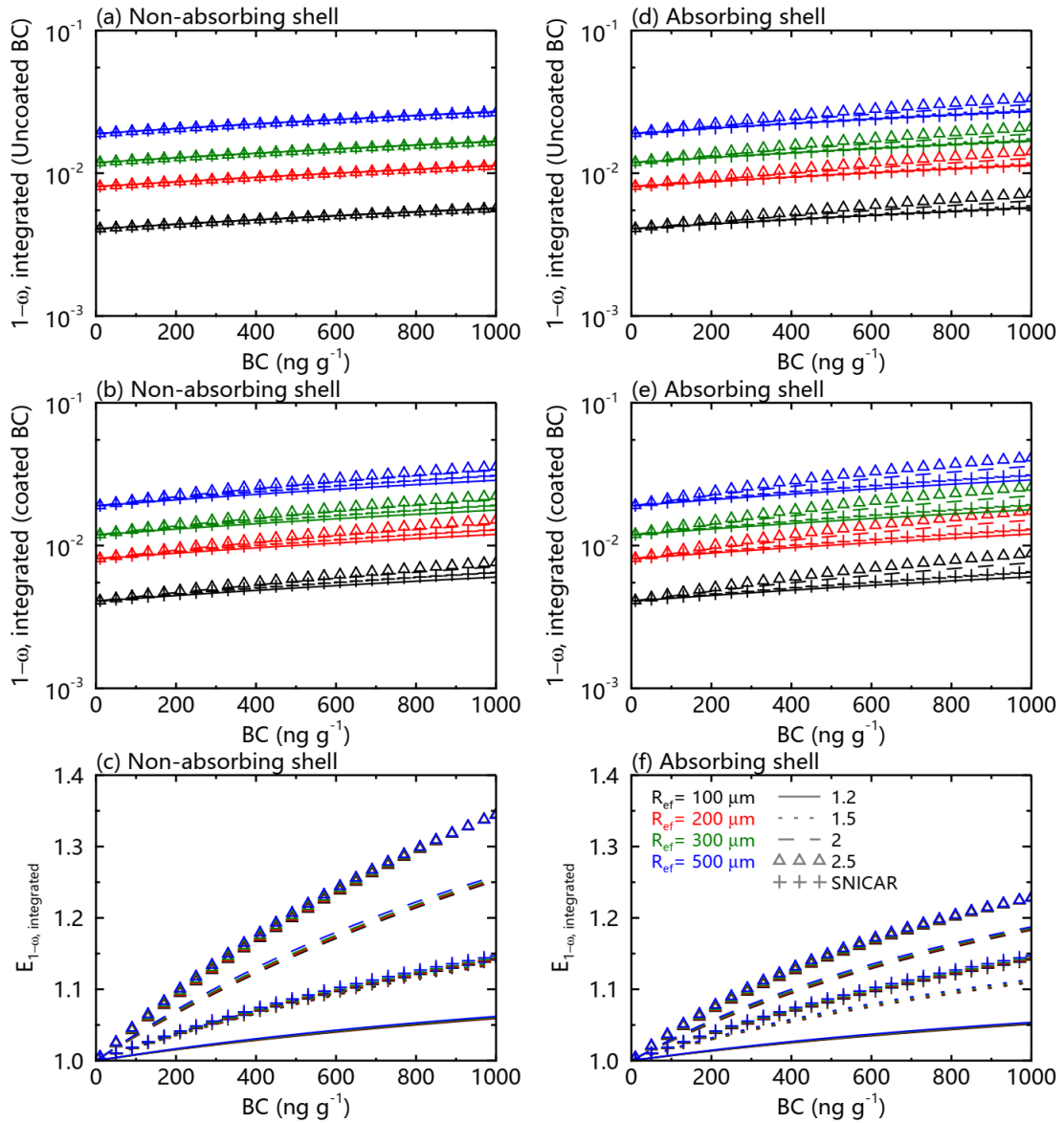
1
2
3

Figure 3. Same as Figure 2, but for snow albedo (α).



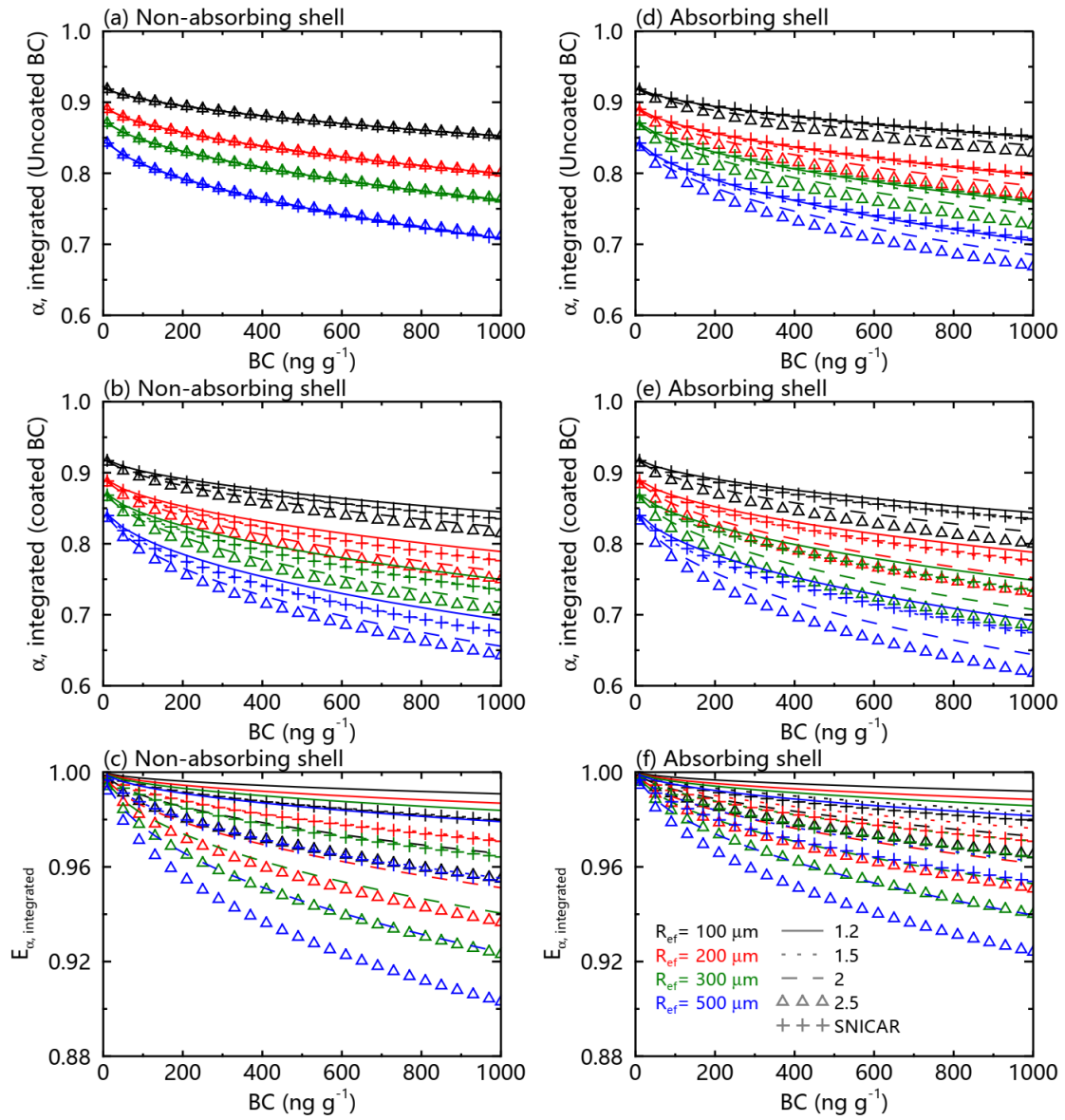
1
2
3

Figure 4. Same as Figure 2, but for snow albedo reduction ($\Delta\alpha$).



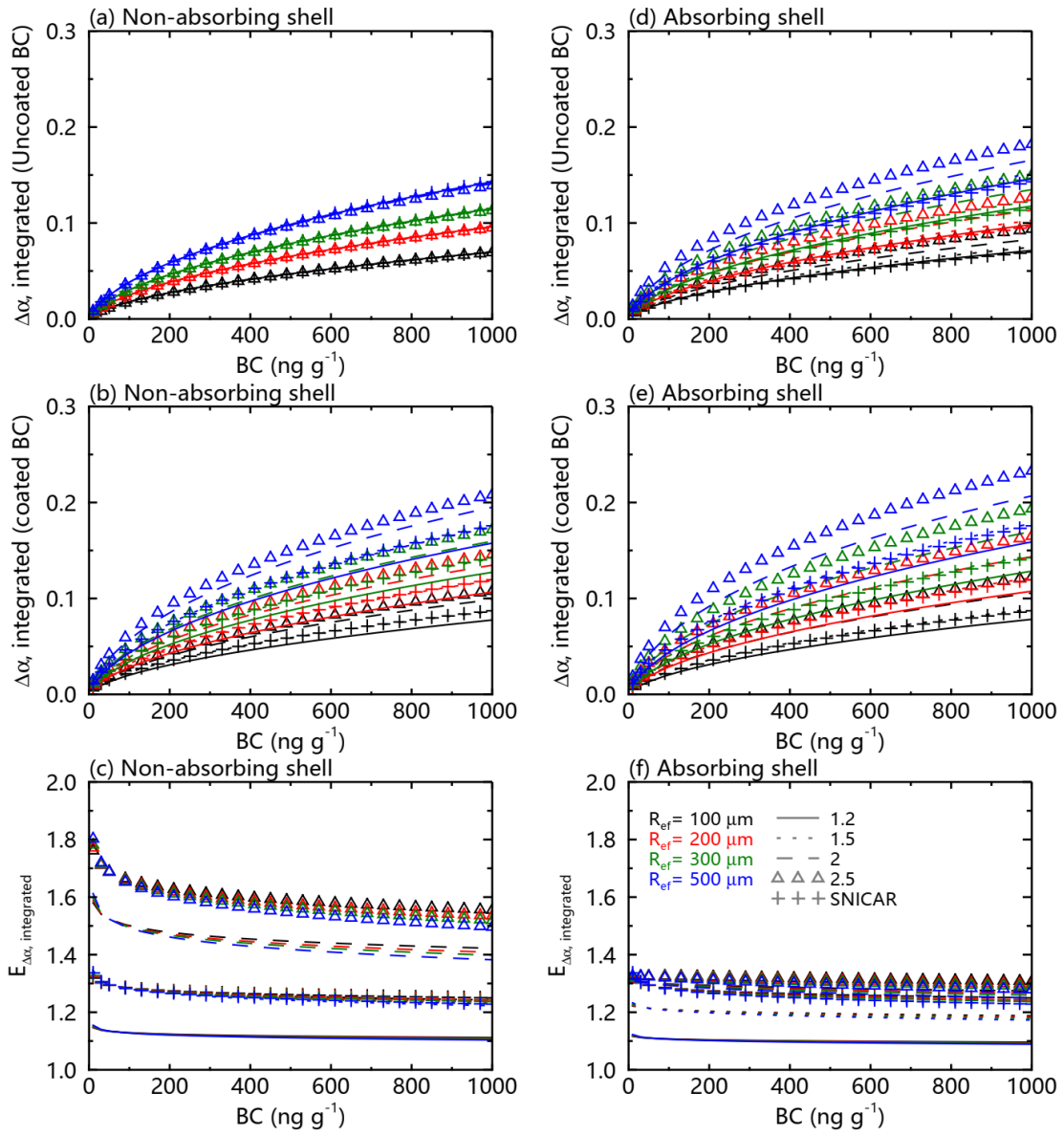
1
2
3
4
5
6
7
8
9

Figure 5. The spectrally weighted snow single-scattering co-albedo ($1-\omega_{\text{integrated}}$) over 300–2500 nm of a typical surface solar spectrum at mid–high latitude from January to May, for (a) uncoated and (b) coated BC with an assumption of a non-absorbing shell. (d) and (e) are same as (a) and (b), respectively, but with an assumption of an absorbing shell. (c) shows the ratios ($E_{1-\omega, \text{integrated}}$) of spectrally weighted snow single-scattering co-albedo for coated versus uncoated BC with an assumption of a non-absorbing shell. (f) is same as (c), but with an assumption of an absorbing shell.



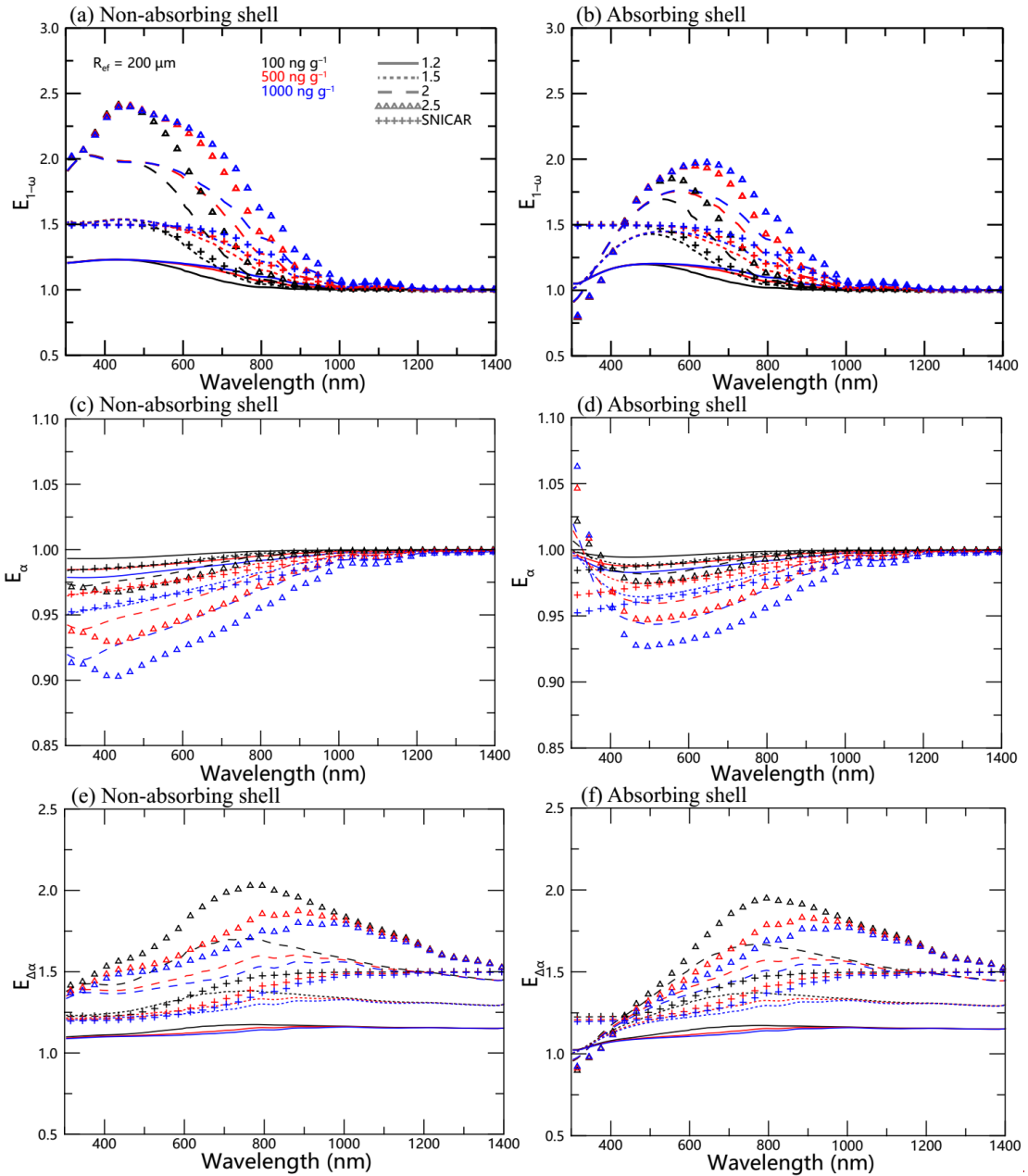
1
2
3

Figure 6. Same as Figure 5, but for snow albedo ($\alpha_{\text{integrated}}$).



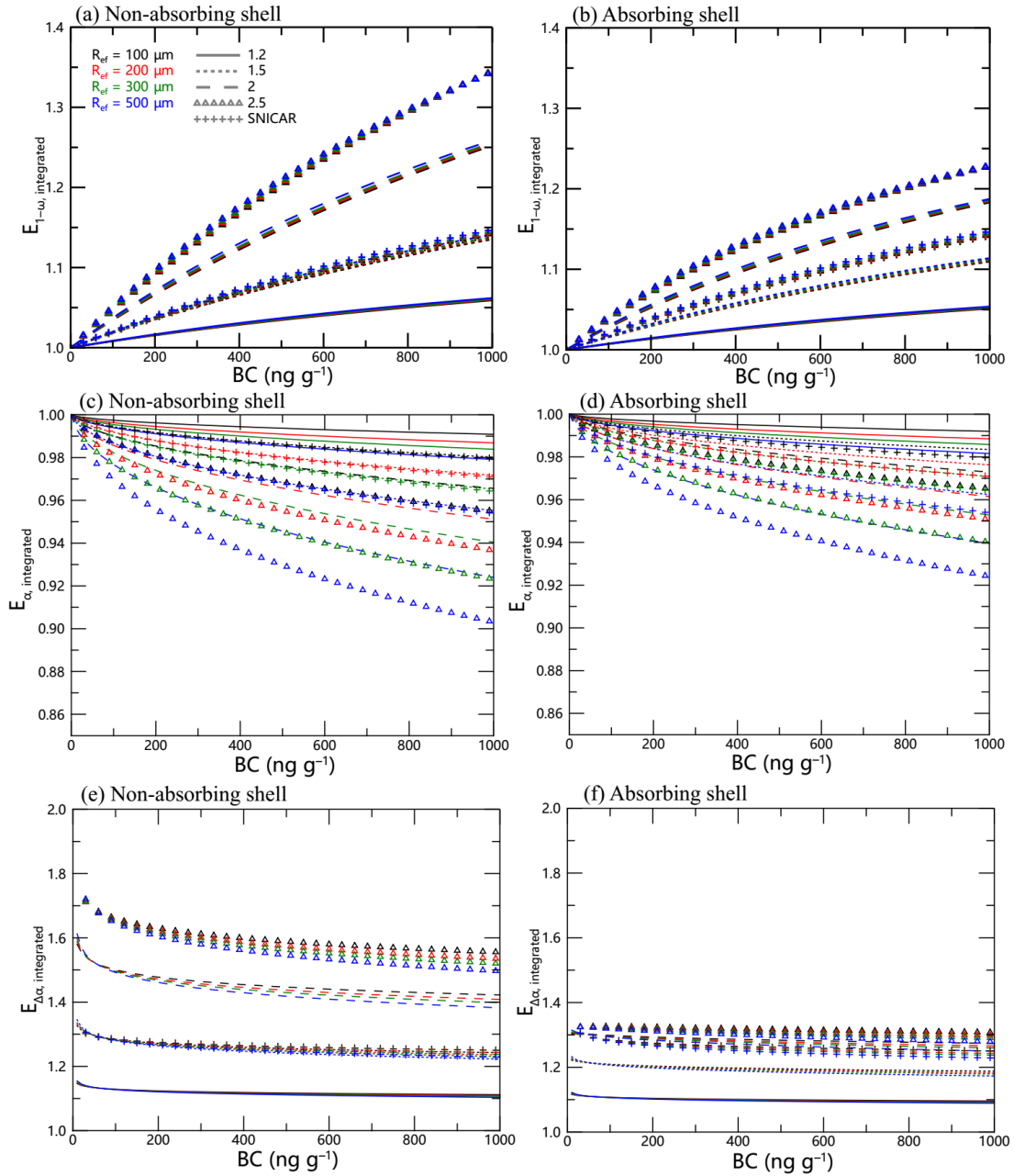
1
2
3

Figure 7. Same as Figure 5, but for snow albedo reduction ($\Delta\alpha_{\text{integrated}}$).



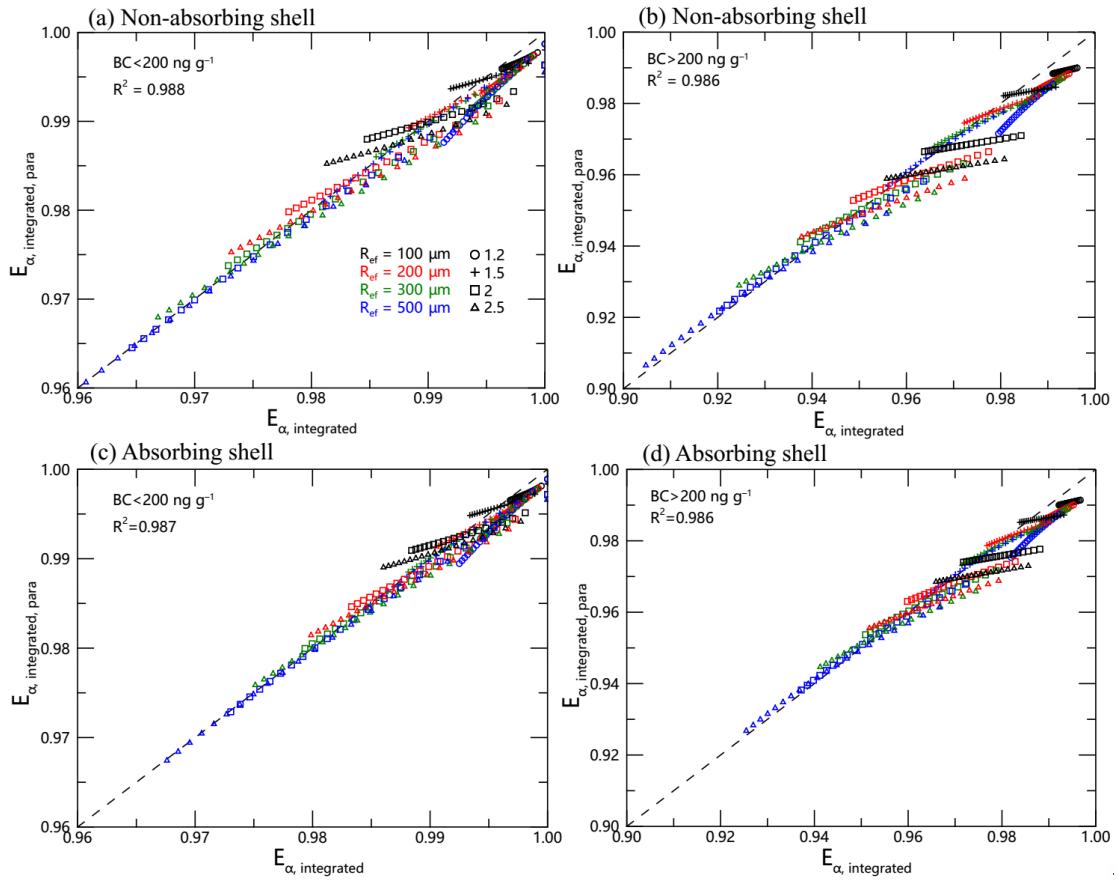
1
2
3
4
5
6
7
8

Figure 2. Ratios of snow single-scattering co-albedo ($E_{1-\omega}$) from an internal mixed particle to an external mixed particle as a function of wavelength, with different BC concentrations and core/shell ratios for (a) a non-absorbing shell, and (b) an absorbing shell. (c) and (d) Same as (a) and (b), but for snow albedo (E_{σ}). (e) and (f) Same as (a) and (b), but for snow albedo reduction ($E_{\Delta\sigma}$). The snow grain radius was assumed to be 200 nm.

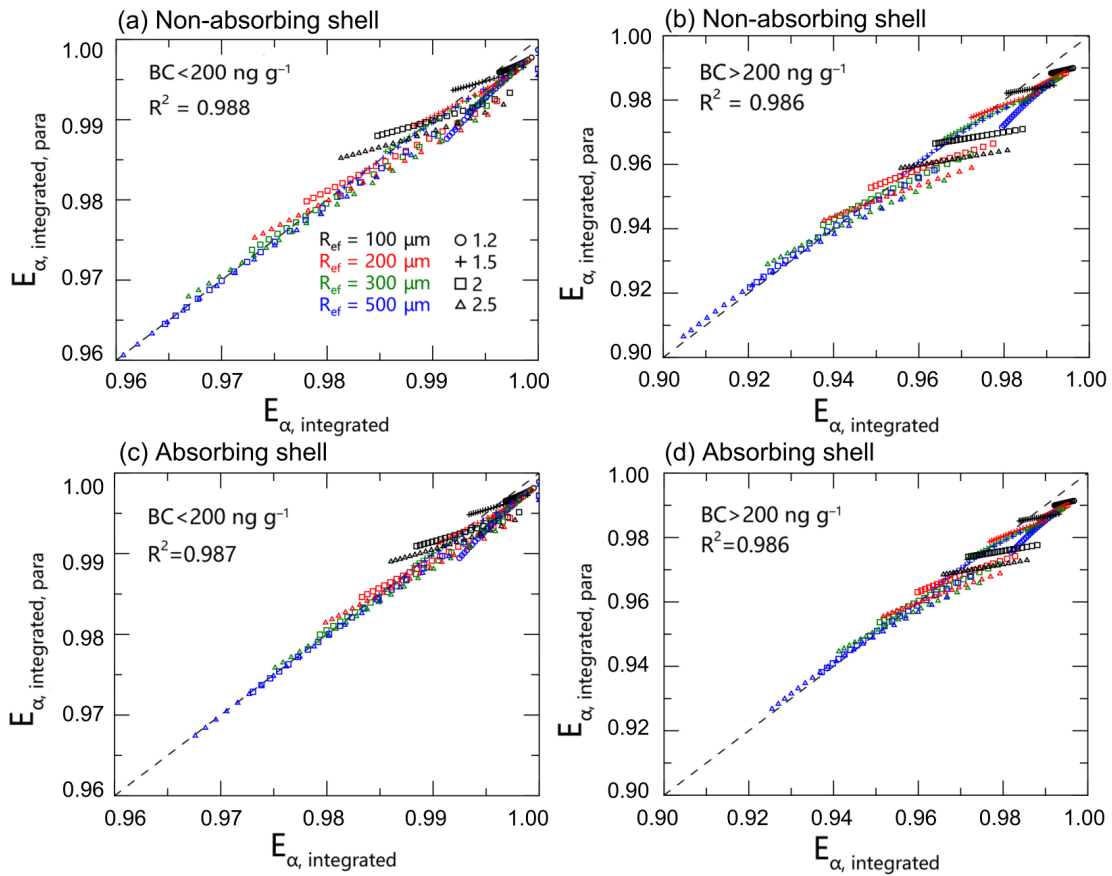


1
2
3
4
5
6
7
8

Figure 3. The spectrally weighted $E_{1-\omega}$ ($E_{1-\omega, \text{integrated}}$) over 300–1400 nm of a typical surface solar spectrum at mid-high latitude from January to May, for (a) a non-absorbing shell and (b) an absorbing shell as a function of black carbon (BC) concentration with different snow grain radii and core/shell ratios. (c) and (d) Same as (a) and (b), but for broadband snow albedo ($E_{\alpha, \text{integrated}}$). (e) and (f) Same as (a) and (b), but for broadband snow albedo reduction ($E_{\Delta\alpha, \text{integrated}}$).

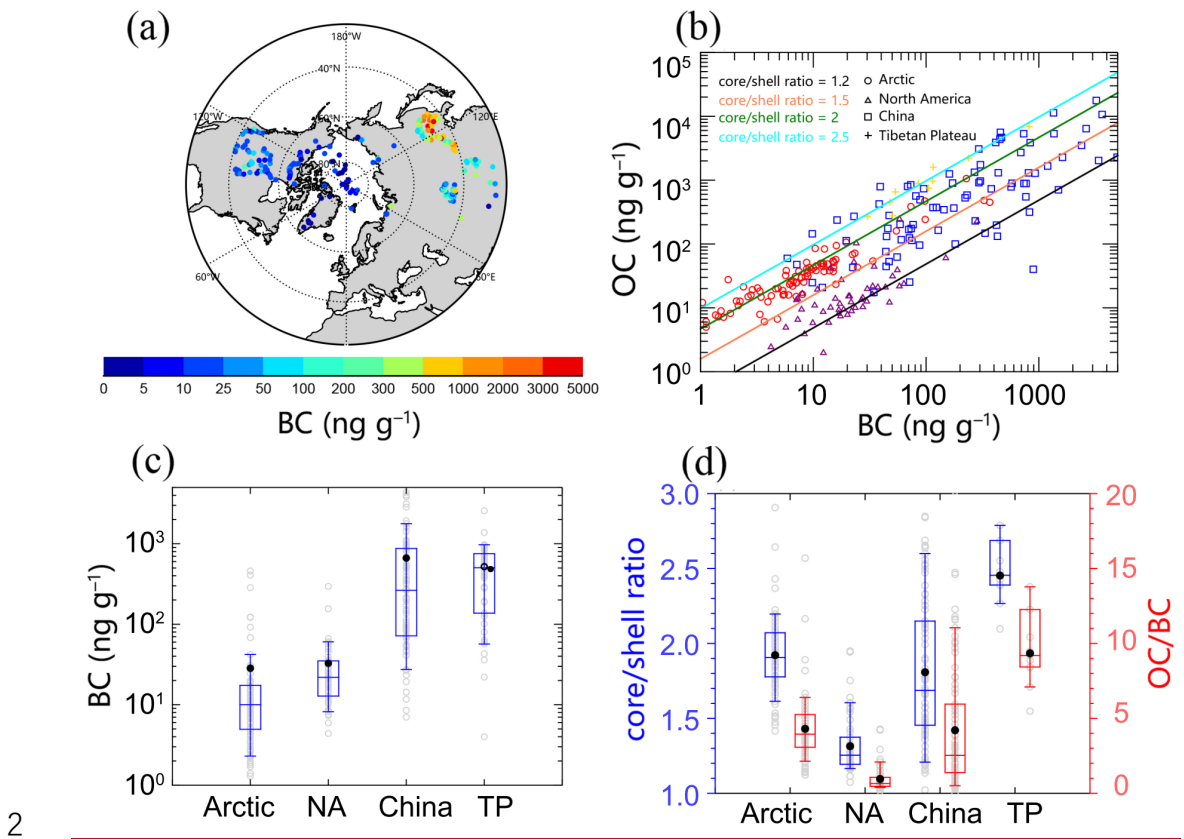
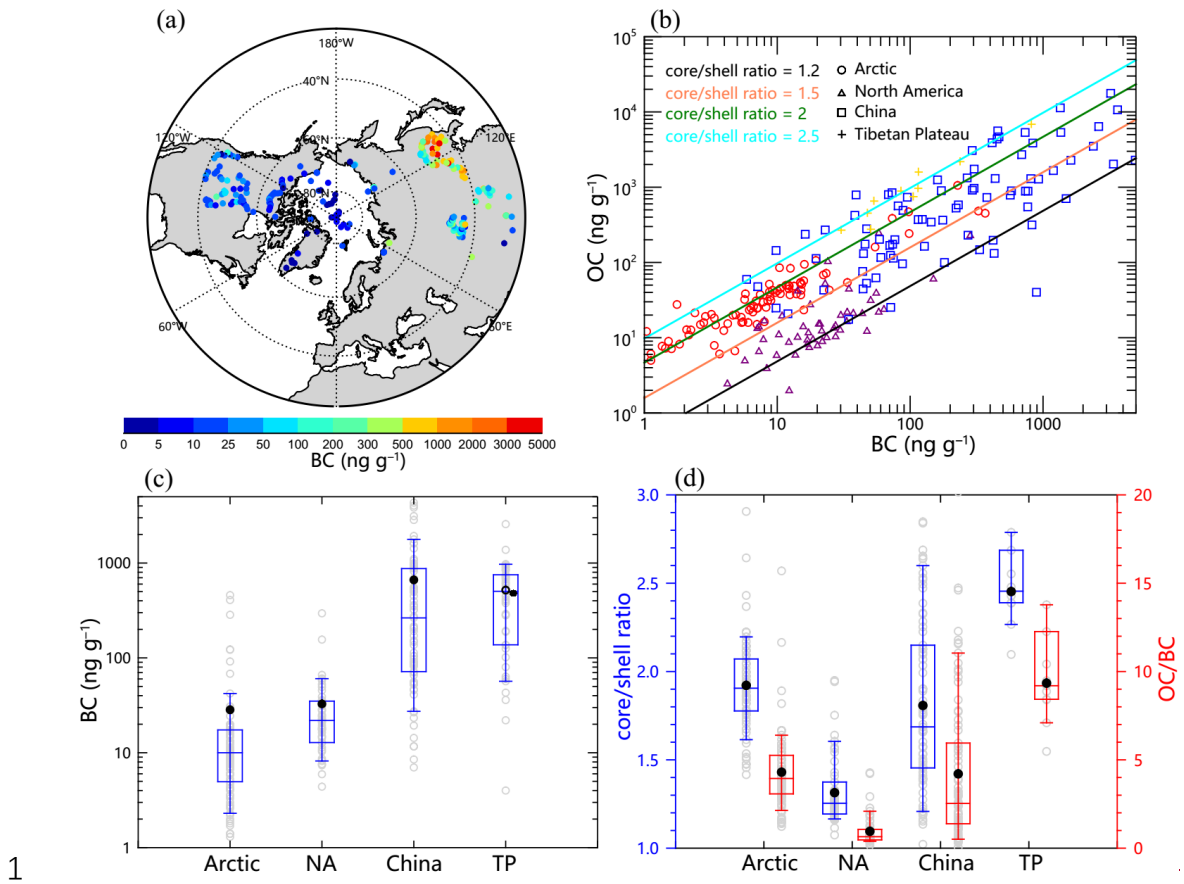


1



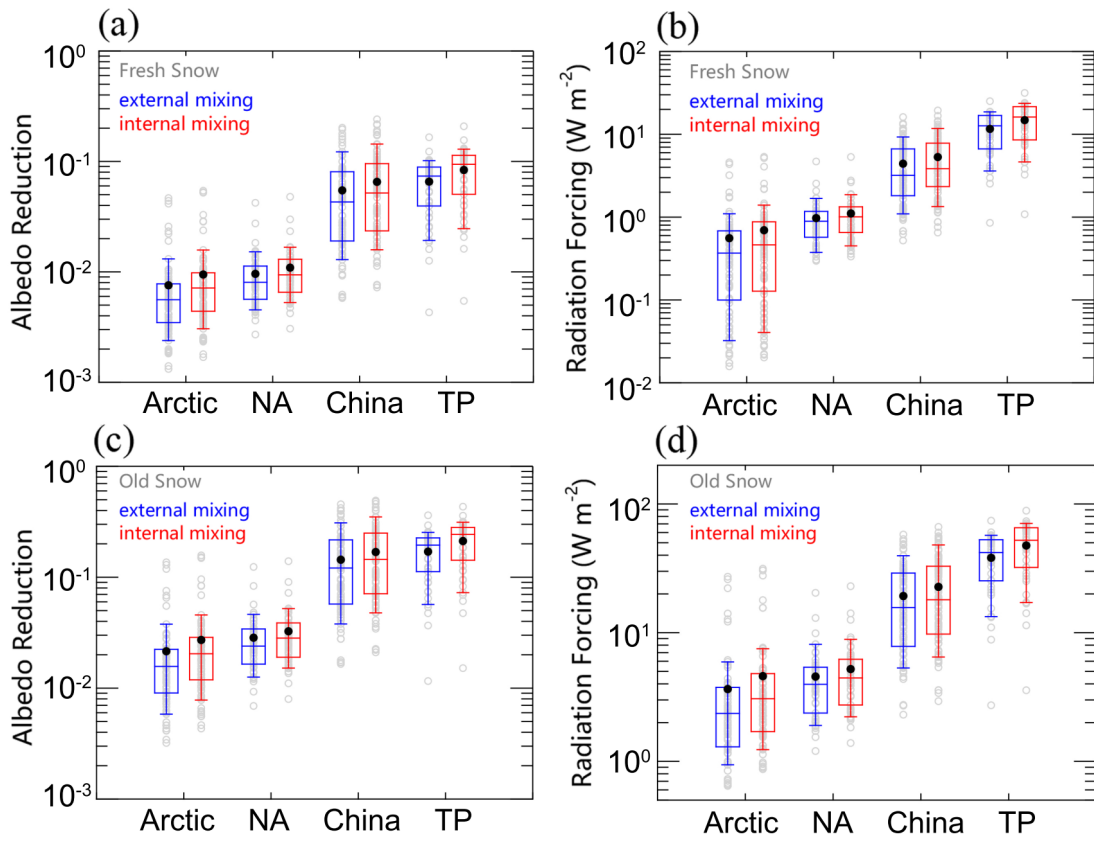
2

1 **Figure 84.** Comparisons of model calculated $E_{\alpha, \text{integrated}}$ and parameterized $E_{\alpha, \text{integrated}}$,
2 $_{\text{para}}$ for (a) relatively clean snow (BC concentration $< \underline{1000-200}$ ng g⁻¹), and (b) relatively
3 polluted snow (BC concentration $> \underline{1000-200}$ ng g⁻¹) for a non-absorbing shell. (c) and
4 (d) Same as (a) and (b), but for an absorbing shell.
5



3 **Figure 95.** (a) The spatial distribution of measured black carbon (BC) concentrations

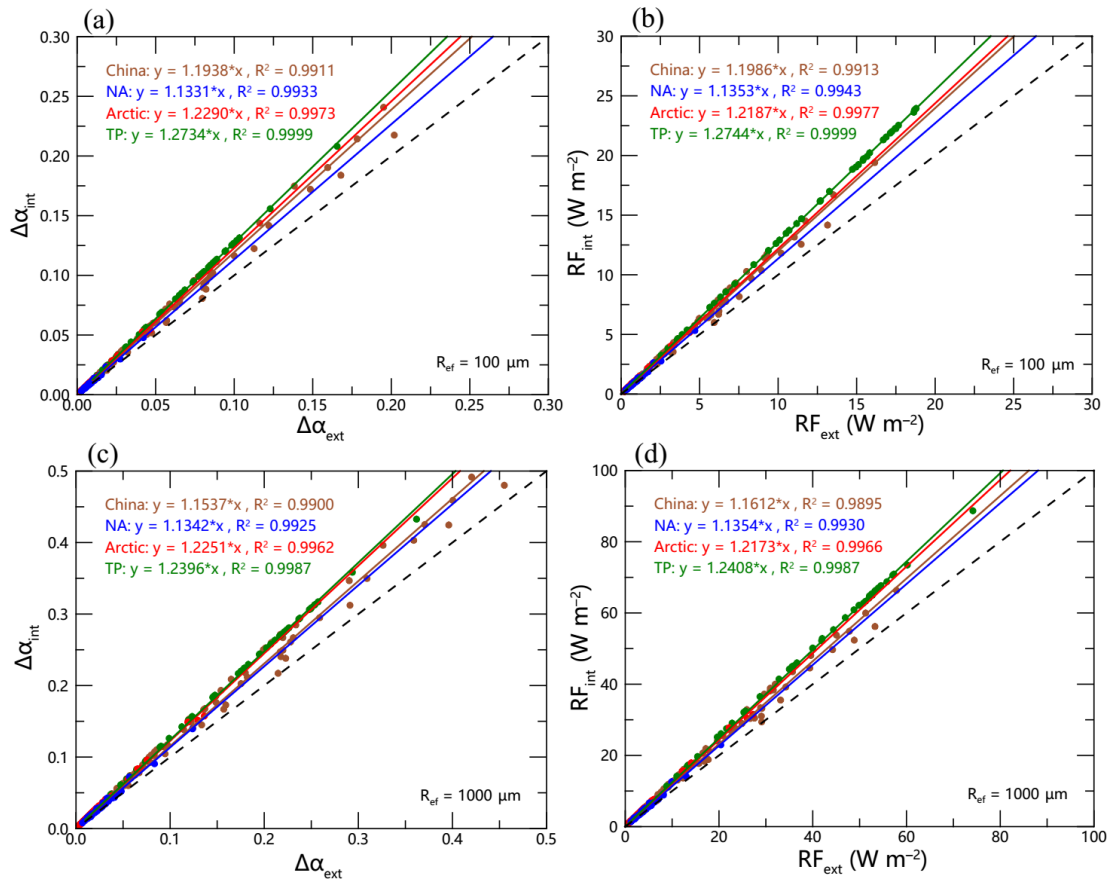
1 across the Northern Hemisphere. (b) Comparison of BC and organic carbon (OC)
2 concentrations in: the Arctic, North America (NA), northern China (NC) and the
3 Tibetan Plateau (TP). (c) Statistical plots of BC concentrations in different regions. The
4 boxes denote the 25th and 75th quantiles, the horizontal lines denote the 50th quantiles
5 (medians), solid dots denote averages, and whiskers denote the 10th and 90th quantiles.
6 In situ data is shown as gray circles. (d) Same as (c) but for a core/shell ratio and OC/BC
7 mass ratio, assuming a core/shell structure with a BC core and an absorbing OC shell.
8



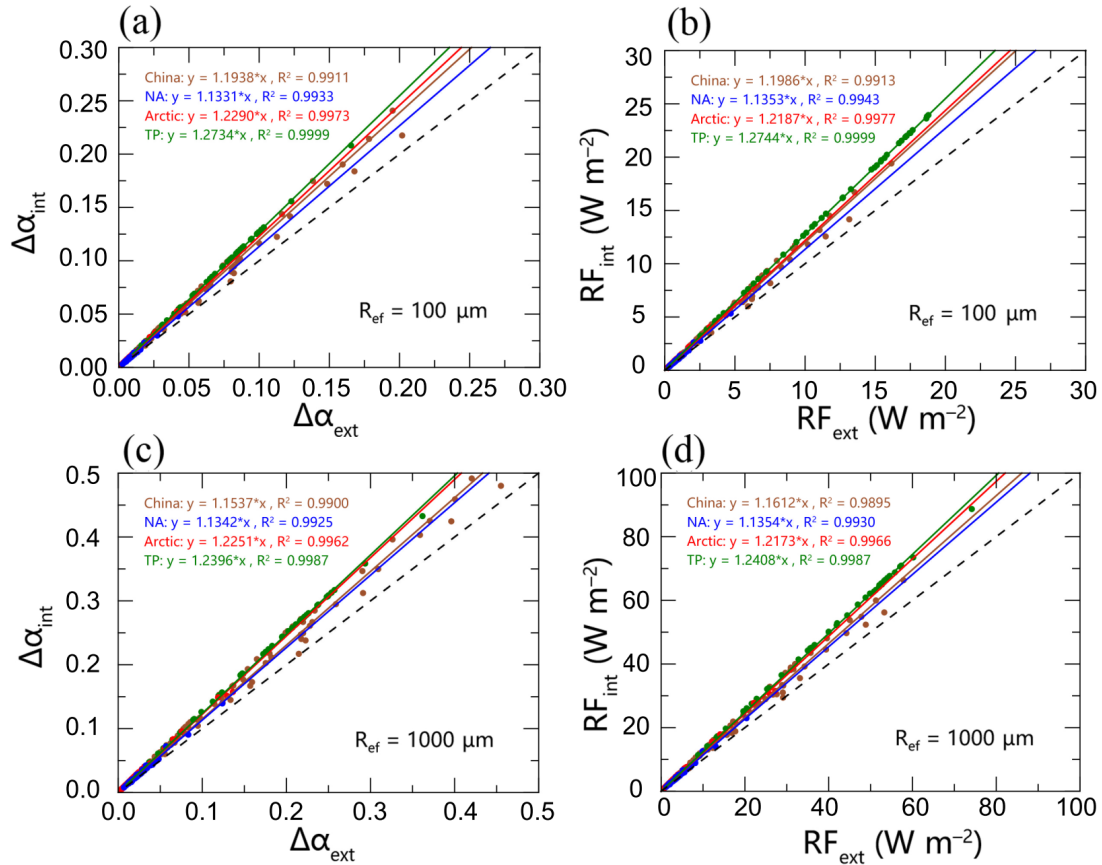
1
2
3
4
5
6
7

Figure 10. Statistical plots of (a) albedo reduction, and (b) radiative forcing, in different regions for fresh snow. (c) and (d) Same as (a) and (b), but for old snow. The boxes denote the 25th and 75th quantiles, horizontal lines denote the 50th quantiles (medians), solid dots denote averages, and whiskers denote the 10th and 90th quantiles. In situ data is shown as gray circles.

1



2



1

2 **Figure 116.** Comparisons of (a) the snow albedo reduction and (b) the radiative forcing
 3 by an internal mixed particle versus an external mixed particle, based on in situ
 4 measurements of fresh snow (assuming a snow grain radius of $100 \mu\text{m}$). (c) and (d)
 5 Same as (a) and (b), but for old snow and assuming a snow grain radius of $1000 \mu\text{m}$.

6

7

