1	Estimation of subsurface porosities and thermal conductivities of polygonal tundra by
2	coupled inversion of electrical resistivity, temperature, and moisture content data
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17 Abstract

18 Studies indicate greenhouse gas emissions following permafrost thaw will amplify current rates of 19 atmospheric warming, a process referred to as the permafrost carbon feedback. However, large 20 uncertainties exist regarding the timing and magnitude of the permafrost carbon feedback, in part 21 due to uncertainties associated with subsurface permafrost parameterization and structure. 22 Development of robust parameter estimation methods for permafrost-rich soils is becoming urgent 23 under accelerated warming of the Arctic. Improved parameterization of the subsurface properties 24 in land system models would lead to improved predictions and reduction of modeling uncertainty. 25 In this work we set the groundwork for future parameter estimation (PE) studies by developing 26 and evaluating a joint PE algorithm that estimates soil porosities and thermal conductivities from 27 time-series of soil temperature and moisture measurements, and discrete in-time electrical 28 resistivity measurements. The algorithm utilizes the Model Independent Parameter Estimation and 29 Uncertainty Analysis toolbox and coupled hydro-thermal-geophysical modeling. We test the PE 30 algorithm against synthetic data, providing a proof-of-concept for the approach. We use specified

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44 **1. Introduction**

45 Subsurface soil property parametrization contributes to a wide uncertainty range in projected 46 active layer depth and in simulated permafrost distribution in the Northern Hemisphere when 47 predicted using Land System Models (Koven et al., 2015; Harp et al., 2016). Reduction of this 48 uncertainty is becoming urgent with recent accelerated thawing of permafrost (Biskaborn et al., 49 2019). Warming permafrost leads to increased infrastructure maintenance costs (Hjort et al., 2018), 50 has a positive feedback on global climate change (McGuire et al., 2018), and increases the 51 probability of the potential hazards for human health (Schuster et al., 2018). Better subsurface soil 52 property parametrizations in Land System Models requires the development of methods that can 53 robustly estimate these soil properties including porosity and thermal conductivity of peat and 54 mineral layers.

subsurface porosities and thermal conductivities and coupled models to setup a synthetic state,

perturb the parameters, then verify that our PE method is able to recover the parameters and

synthetic state. To evaluate the accuracy and robustness of the approach we perform multiple tests

for a perturbed set of initial starting parameter combinations. In addition, we varied types and

quantities of data to better understand the optimal dataset needed to improve the PE method. The

results of the PE tests suggest that using multiple types of data improve the overall robustness of

the method. Our numerical experiments indicate that special care needs to be taken during the field

experiment setup so that (1) the vertical distance between adjacent measurement sensors allows

the signal variability in space to be resolved and (2) longer time interval between resistivity

snapshots allows signal variability in time to be resolved.

55 Direct measurements of subsurface soil properties are labor intensive, destructive, and not always 56 feasible (Smith and Tice, 1988; Kern, 1994; Boike and Roth, 1997; Yoshikawa et al., 2004). While 57 soil sample analysis can provide critical information on soil properties at a fine scale, this 58 information is limited to sparsely sampled locations. Multiple methods used in the laboratory to 59 measure soil properties by using soil cores extracted from the field site are well summarized by 50 Nicolsky et al., (2009), but logistical and economic burden typically do not allow these 59 measurements to be made in the field. Inverse modeling serves as an alternative approach to recover soil properties using a combination of indirect and direct measurements and physics-basednumerical models.

64 Different inverse modeling frameworks have been developed to estimate soil thermal properties using physical-based models and time-series of ground temperature data. Some earlier studies 65 66 used heat equation models without phase change (Beck et al., 1985; Allifanov et al., 1996). More 67 recent works include phase change, which is an important component of the energy balance in 68 permafrost-affected soils (e.g. Nicolsky et al., 2007; 2009, Tran et al., 2017). Nicolsky et al., 69 (2007; 2009) used an optimization based inverse method and a variational data assimilation 70 method to estimate soil properties. In particular, Nicolsky et al., (2007; 2009) used measured 71 subsurface temperatures to inversely estimate thermal conductivities, porosities, freezing point 72 temperatures, and unfrozen water coefficients, pointing out that sensitivity analyses (i.e. 73 perturbation of the parameter values) are required in order to robustly establish a set of estimated 74 parameters. Harp et al., (2016) used an ensemble-based method to evaluate the uncertainty of 75 projections of permafrost conditions in a warming climate due to uncertainty in subsurface 76 properties. Atchley et al., (2015) used data calibration to estimate hydrothermal properties of soils. 77 All these methods used ground temperatures alone to estimate soil properties and 1D soil columns 78 assuming a 1D soil structure.

79 Recently, Tran et al., (2017) used a coupled hydrological-thermal-geophysical modeling approach 80 to estimate soil organic content. The approach was based on coupling the 1D Community Land 81 Model (CLM4.5; Oleson et al., 2013) that simulates surface-subsurface water, heat and energy 82 exchange and the 2D Boundless Electrical Resistivity Tomography (BERT) forward model 83 (Rücker et al., 2006). The simulated 1D snapshots of the subsurface temperature, liquid water and 84 ice content from the CLM model were explicitly linked to soil electrical resistivities via petrophysical relationships which were then used as input to BERT's forward model to calculate 85 86 apparent resistivities. Their inverse modeling framework aims to minimize the misfit between 87 calculated and measured data, including soil temperature, liquid water content and apparent 88 resistivity. Here we modify and extend this approach to 2D by using the Advanced Terrestrial 89 Simulator (ATS) model, which was specifically developed to study fine-scale hydrothermal 90 processes of permafrost-affected soils. In addition, instead of estimating organic content of the soil 91 as in Tran et al., (2017), we estimate porosities and thermal conductivities of peat (organic) and 92 mineral layers across a 2D transect within polygonal tundra.

Modeling the full, continuous 2D transect allows us to simulate lateral hydro-thermal fluxes not possible with individual 1D columns known to be important in polygonal tundra (Abolt et al, 2018, Liljedahl et al, 2016). At each grid cell in the transect, a physical state develops during the ATS simulation (temperature, saturation, etc.) that is then used to calculate heterogeneous electrical resistivities via petrophysical relations. This allows more realistic simulated apparent resistivities that include the effects of lateral hydrothermal connectivity within the transect.

99 Through this approach, we develop a parameter estimation (PE) algorithm that aims to estimate 100 porosities and thermal conductivities in permafrost-affected soils through joint inversion of 101 hydrothermal and geophysical measurements, including ground temperature, saturation, and 102 apparent resistivity. Our main objective then is to evaluate which types and number of 103 measurements are necessary to constrain the inversion to yield a robust and accurate prediction of 104 subsurface porosities and thermal conductivities. The inverse modeling framework couples the 105 state-of-the-art hydrothermal permafrost simulator ATS, electrical resistivity software package 106 BERT and the Model Independent Parameter Estimation and Uncertainty Analysis toolbox (PEST) 107 software package (Doherty, 2001). We progressively test the accuracy and robustness of the 108 method using a series of synthetic problems by: 1) increasing the complexity of the meteorological 109 data used to drive the coupled thermo-hydro-geophysical model and 2) testing the inclusion of 110 individual and combinations of several available measurement types on the accuracy and 111 robustness of inversions. The results of this work can be used to better understand challenges 112 associated with subsurface porosity and thermal conductivity estimation. Additionally, we used 113 findings from this study to suggest how data should be collected to improve the accuracy of the 114 estimated soil properties and to optimize the total number of measurements needed to make a 115 robust subsurface PE.

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117 **2. Methods**

We estimate the soil properties of porosity and soil grain thermal conductivity for peat and mineral layers of a 2D transect within polygonal tundra. Our PE approach is summarized in Figure 1. Given specified "true" values of these parameters, we used the ATS version 0.86 model to solve for a transient, spatially distributed hydro-thermal state characterized by temperature and liquid and ice saturations. ATS is a 3D-capable coupled surface and groundwater flow and heat transport model representing the soil physics needed to capture permafrost dynamics, including flow of unfrozen 124 water in variably-saturated, partially-frozen, non-homogeneous soils (Painter et al., 2016). Given 125 this hydrothermal state, we calculate resistivity values at every grid cell via petrophysical 126 relationships, and run the forward modelling component of the BERT software package (Rücker 127 et al., 2006) to simulate resistance and related apparent resistivity values that would be measured 128 with ground-coupled electrodes and an ERT acquisition system.



Figure 1. Schematics of the parameter estimation algorithm. The algorithm starts with initial guesses on porosities and thermal conductivities $\{\phi, k\} = \{\phi_m, \phi_p, k_m, k_p\}$ for the peat and mineral layers. The coupled ATS-BERT forward model then simulates temperature (*T*), liquid water saturation (*s*_l), ice saturation (*s*_i), and apparent resistivities (ρ_a), which are passed to the cost function. If the cost function is small enough, $\{\phi, k\}$ are considered to be the estimated parameters. If not, the values of the $\{\phi, k\}$ are updated according to the Levenberg-Marquardt (LM) minimization algorithm and passed back to the ATS-BERT model.

138 2.1 ATS-BERT Model

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139 To set up the synthetic model, we used digital elevation data of a transect through ice-wedge

140 polygonal tundra at the Barrow Environmental Observatory (BEO), at Utqiagvik, Alaska (Fig. 2).

Our study includes an 11 m section covering a single polygon with an ice-wedge on each side. In this study we do not explicitly assign ice properties for the ice-wedges. Instead, we model bulk porosities and effective thermal conductivities that can be associated with peat and mineral layers of the entire transect.

145 In Figure 2A, we present the computational mesh representing the cross-section of the polygonal 146 tundra that ATS is run on. The thickness of the peat layer corresponds to observations at the site, 147 with a thick peat layer on the sides (troughs) and a thinner layer in the middle of the low-centered 148 polygon. A mineral layer was assigned below the peat layer across the transect. We initially 149 designated six synthetic direct temperature and soil moisture measurement locations within the 150 active layer area, the maximum thaw layer from the ground surface to the top of the permafrost, 151 similar to the sensor setup at the site (Dafflon et al., 2017). The average active layer depth is about 152 38cm, as it can be seen from the ground temperatures simulated for the synthetic model run with 153 actual meteorological data in Figure 2B. The linear white region on Fig. 2B indicates the bottom 154 of the active layer within the transect (0° C). Then we added four more synthetic direct 155 measurement locations below the active layer to evaluate the effect of their inclusion on PE 156 accuracy and robustness. All observation locations are represented as stars on Figure 2A 157 corresponding to the locations of the collected daily averaged temperature and soil moisture 158 timeseries. The temperature and soil moisture timeseries were recorded at depths of 5, 20, 60, and 159 80 cm below the surface.

160 The setup of the ATS model followed a standard procedure described in several studies (Atchley 161 et al., 2015; Painter et al., 2016; Jafarov et al., 2018). Typically, we set up the model in several 162 steps: 1) initialization of the water table, 2) introduction of the energy equation to establish 163 antecedent permafrost, and 3) spinup of the model with simplified and actual meteorological data 164 from the BEO station. We spun up the model until the active layer achieved cyclical equilibrium. The overall depth of the modeling domain is 50 m. We set the bottom boundary to a constant 165 166 temperature of T=263.55K and set zero heat and zero mass flux boundary conditions on the vertical 167 sides. A seepage face was imposed at 4 cm below the surface on each side of the domain to allow 168 drainage to the trough network to prevent water from pooling at the surface, as is typical of partially 169 degraded polygonal ground (Liljedahl et al, 2016). We use two types of meteorological datasets 170 as surface boundary condition drivers for the ATS model: simplified (sinusoidal air temperature, 171 constant precipitation, and constant radiative forcing) and actual weather data from the BEO site.

172 The actual meteorological data were collected starting on January 1, 2015 and include air 173 temperature, rain and snow precipitation, humidity, long and shortwave radiation, and wind speed. 174 We created a synthetic truth by designating porosities and soil grain thermal conductivities $\{\phi, k\}$ 175 of peat and mineral soil as parameters in the forward model. The resulting temperature (T), liquid 176 and ice-water saturations (s_l, s_i) , and apparent resistivities (ρ_a) were collected as the true state. 177 Critical for these simulations is the calculation of the thermal conductivities of the bulk soil; 178 calculated in ATS using Kersten numbers to interpolate between saturated frozen, saturated 179 unfrozen, and fully dry states (Painter et al., 2016) where the thermal conductivities of each end-180 member state is determined by the thermal conductivity of the components (soil grains, air, water, 181 or liquid) weighted by the relative abundance of each component in the cell (Johansen, 1977; 182 Peters-Lidard et al, 1998; Atchley et al., 2015). Thermal conductivities of water, ice, and air are 183 considered constant, leaving soil grain thermal conductivity as the remaining parameter to be 184 estimated. The equation to calculate saturated, frozen thermal conductivity ($\kappa_{sat,f}$) has the 185 following form:

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$$\kappa_{sat,f} = \kappa_{sat,uf} \cdot \kappa_i^{\phi} \cdot \kappa_w^{-\phi}, \tag{1}$$

187 where $\kappa_{sat,uf}$, κ_i , κ_w are thermal conductivities for saturated unfrozen, ice, and liquid water, 188 respectively, and ϕ is porosity.

The freezing characteristic curve is thermodynamically derived using a Clapeyron relation and the unfrozen water retention curve, as described in Painter and Karra (2014) and Painter et al., (2016). In Figure 3 we present liquid and ice saturations for one realization of the model for winter (January) and summer (August) times of the year. The ice saturation is high below the active layer all year long and lowest within the active layer in the summer. The peat layer holds more water; therefore, ice concentration is higher than in the mineral layer in the winter. The liquid saturation plot shows that by the end of the summer, the peat layer is drier than the mineral layer.

196 We sequentially couple the ATS and BERT numerical models via petrophysical relationships used 197 by Tran et al. (2017) and based on Archie (1942) and Minsley et al. (2015). In that approach, the 198 electrical resistivity (ρ) is determined as a function of soil characteristics, temperature, porosity, 199 liquid water saturation, fluid conductivity, and ice content:

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$$\rho = 1/(\phi^{d}[s_{l}^{n}\sigma_{w} + (\phi^{-d} - 1)\sigma_{s}] \cdot [1 + c(T - 25)]), \qquad (2)$$

- where σ_w is the fluid electrical conductivity, σ_s is soil/sediments electrical conduction, *n* is a saturation index, *d* is a cementation index, and *c* is a temperature compensation factor accounting for deviations from $T = 25^{\circ}C$.
- The ice content is linked to water content through the liquid-water saturation and to σ_w , which is influenced by the concentration of Na⁺ and Cl⁻ ions and the ice/liquid fraction. Here σ_w has the following form:
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$$\sigma_{w} = \sum_{i=1}^{n_{ion}} F_{c} \beta_{i} |z_{i}| C_{i(S_{f_{i}=0})} S_{f_{w}}^{-\alpha}$$
(3)

208 Where F_c is Faraday's constant, β_i and z_i the ionic mobility and valence respectively, C_i is the 209 concentration of i^{th} ion, α is factor influencing how the liquid water salinity increases when the 210 fractions of liquid in ice-liquid water S_{fw} decreases. S_{fw} is defined as:

- 211 $S_{f_w} = s_l / (s_l + s_i)$ (4)
- Both s_l and s_i are simulated by ATS. Note that ϕ in eq. (2) is an estimated parameter (see Figure 1). In this study we assume that $n, d, \sigma_s, \alpha, F_c, \beta_{Na^+}, \beta_{Cl^-}, C_{Na^+}$, and C_{Cl^-} parameters used
- in equations (2) and (3) are known (see Tran et al., 2017) and focus on the robustness of the PE algorithm in estimating porosity and thermal conductivity.
- 216 The 2D resistivity data inferred from ATS simulations and petrophysical relationships gets
- 217 passed to BERT which simulates resistances that are then converted to the apparent resistivities
- 218 (ρ_a). The ρ_a values correspond to an acquisition along an 11 m long transect using a 0.5 m
- electrode spacing and a Schlumberger configuration with a total of 138 measurements (see Fig.
- 220 2B). This configuration implies that the measurements are mostly sensitive to the electrical
- 221 resistivity in the top few meters.
- 222 Since BERT and ATS operate on different unstructured meshes, we wrote a function that
- interpolates the values between the two meshes. Note that the ATS mesh is 50m deep. We
- 224 calculate ρ by using corresponding outputs from the ATS model and the petrophysical
- 225 relationships and then interpolated these values on a mesh defined in BERT and adapted to the
- acquisition geometry. BERT's mesh consists of a finely resolved mesh (11m wide by 4.5m
- deep) embedded within a coarser outer mesh that is about 120m wide and 85m deep. We link
- 228 hydrological variables with electrical resistivities in the fine mesh. The coarse mesh is used to
- reduce the effect of boundaries. It extends until the change in the electrical resistivity between
- two neighboring cells is negligible.



Figure 2. The (vertically exaggerated) 2D transect used by the ATS model. A) The unstructured mesh where green represents the peat layer and brown represents the mineral soil layer. Black stars represent the 6 sensors recording temperature and soil moisture content within the active layer. Red stars represent the 4 sensors recording temperature and soil moisture content below the active layer. B) Ground temperature distribution simulated by the ATS model, corresponding to the time of maximum active layer depth. Here the depth of the active layer corresponds to the distance above the white linear feature (i.e., 0°C) dividing the thawed and frozen regions of the ground. The light blue dots represent the location of the electrodes in this setup.

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Figure 3. The 2D transect used by the ATS model. The rows from top to bottom correspond to ice saturation and liquid, respectively. The columns from left to right indicate one-day snapshots taken in the middle of the winter and the day of maximum active layer depth in summer.

246 **2.2 Parameter estimation using PEST**

To test if the known soil properties can be recovered by the PE approach, we start with randomly selected initial parameter guesses. We use a Latin Hypercube Sampling method to generate random initial guesses of porosity and thermal conductivities around the synthetic truth (McKay et al., 1979). Each parameter combination includes four parameters: porosity and thermal conductivity for peat and mineral soil layers. These parameters were chosen due to their strong controls on both hydrologic and thermal states (Atchley et al., 2015, Nicolsky et al., 2009). The rest of the hydrothermal properties are kept fixed. The inverse approach involves the minimization of a cost function expressed as the sum-of-squared differences between simulated values and synthetic measurements using the Levenberg-Marquardt (LM) algorithm (K. Levenberg, 1944; D. W. Marquardt 1963) implemented in the PEST software package (Doherty, 2001), which was used to handle all parameter estimation runs.

To estimate soil porosities and thermal conductivities, we minimize the cost function (*J*), which includes calculated and synthetic *T*, s_l , and ρ_a in the following form:

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$$J(\phi, k) = w_T \sum_{i}^{n_{sens}} \sum_{j}^{n_{days}} (T_{cj}^i - T_{sj}^i)^2 + w_s \sum_{i}^{n_{sens}} \sum_{j}^{n_{days}} (s_{l_{cj}}^i - s_{l_{sj}}^i)^2 + w_s \sum_{i}^{n_{sens}} \sum_{j}^{n_{sens}} \sum_{j}^{n_{sens}} (s_{l_{cj}}^i - s_{l_{sj}}^i)^2 + w_s \sum_{i}^{n_{sens}} \sum_{j}^{n_{sens}} \sum_{j}^{n_{sens}} (s_{l_{cj}}^i - s_{l_{sj}}^i)^2 + w_s \sum_{j}^{n_{sens}} \sum_{j}^{n_{$$

$$w_{\rho_{a}} \sum_{k}^{n_{snap}} \sum_{m}^{n_{meas}} \left(\rho_{a\,cm}^{k} - \rho_{a\,sm}^{k} \right)^{2}, \tag{5}$$

262 where subscripts c and s correspond to calculated and synthetic states of the system, and w_T , w_s , and w_{ρ_a} are the corresponding weights for the temperature, saturation and apparent resistivity 263 residuals. n_{sens} is the number of sensors, n_{days} is the number of days over which we collected the 264 data, n_{snap} is the number of ρ_a snapshots, and n_{meas} is the number of ρ_a measurements during 265 one snapshot. T_c and s_{l_c} are timeseries from multiple sensors collected daily from the beginning 266 267 of June till the end of September. ρ_a are apparent resistivity data snapshots taken at a certain day. 268 The number of apparent resistivity snapshots depends on the particular case, varying from one to 269 eight snapshots per year. The one-snapshot case corresponds to only one snapshot in the month 270 of August while the eight-snapshot case corresponds to a snapshot taken once per month from January till September. In addition, we tested the case where we collected eight daily ρ_a snapshots. 271 272 This was done to compare how different time spacing would affect the estimated properties.

273 The weights were chosen in order to scale the contribution of each type of residual so that 274 contributions to the cost function are evenly distributed across temperature, saturation, and 275 apparent resistivity residuals. For example, saturation residuals are on the order of a few tenths, 276 while apparent resistivity residuals can be tens of ohm-meters. The weights were selected based 277 on evaluating the individual contributions to the cost function for each measurement type on an 278 ensemble of simulations spanning the parameter ranges. The apparent resistivity residual weight (w_{ρ_a}) was set to one. The temperature and saturation residual weights $(w_T \text{ and } w_s)$ were then 279 280 modified so that each measurement type component in the cost function had roughly equivalent magnitude over most of the parameter space. This resulted in weights of $w_{\rho_a} = 1$, $w_T =$ 281 $\sqrt{2.5 \cdot 10^3}$, and $w_s = \sqrt{3.5 \cdot 10^5}$. 282

If the cost function satisfies a minimum criterion or the maximum allowed number of iterations, which we chose to be equal to 25, is reached, the PE terminates. The porosities and thermal conductivities corresponding to the minimum of the cost function, i.e., the parameters associated with the best fit between simulated and synthetic values, are considered the estimated parameter values as

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$$\{\phi, k\} = \underset{\substack{\phi_{\min} \le \phi \le \phi_{\max}, \\ k_{\min} \le k \le k_{\max}}}{\operatorname{argmin}} J(\phi, k).$$
(6)

Here $\{\phi, k\}$, are estimated porosities and thermal conductivities for peat and mineral soil.

Based on sensitivity analyses using simplified meteorological data, the cost function response surface was smooth and convex over the parameter ranges of interest. Therefore, we chose the LM approach because of its robust gradient-based optimization scheme that takes advantage of smooth convex response surfaces to quickly converge to minima.

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295 **2.3 Experiments**

296 To build an understanding of the inverse framework, we start with a simple setup and then 297 gradually add more complexity. First, we use simplified meteorological data where we assume 298 that air temperatures change according to a sinusoidal function and all other terms are constants. 299 Initially we start with 3 temperature and moisture content measurement locations within the peat 300 layer (refer to Figure 2A) and 1 ERT data snapshot. Then we increase the number of ERT data 301 snapshots up to 8 by adding snapshots once per month from January till August. Each ERT data snapshot calculated by BERT uses the set of daily averaged T and s_l simulated by ATS and 302 303 petrophysical relations (eqns. 2 and 3) which are varying over time. Then we increase the number 304 of sensors to 6 and add noise to the simulated data. Introduction of noise allows us to evaluate the 305 effect of measurement uncertainties that will be present in the actual application of the PE method. We added different levels of Gaussian noise to the synthetic measurements of T, s_l , and ρ_a in the 306 307 following way: 1% to T, 5% to s_l , and 10% to ρ_a . These levels of noise for the different types of 308 measurements are based on published literature and our own experience (Wang et al., 2018; 309 Dafflon et al., 2017). After that we substitute simplified meteorological data with actual data from 310 the BEO site to evaluate our PE method under realistic ground surface boundary conditions. In 311 this case we evaluate how much and what kind of data we need to robustly recover subsurface 312 porosities and thermal conductivities. To do this we test the inclusion of individual types of measurements in the cost function (equation 3) as well as all possible combinations of measurement types. We used different soil property ranges for the simplified and actual meteorological data PE runs which are summarized in Table 1. This was done to ensure that PE is able to recover different sets of parameters, and to test the consistency and effectiveness of the PE method. Finally, we compared the difference between estimated parameters for 8 ERT data snapshots collected once a month versus once a day for 8 days. Notation and a description of each run for simplified and actual meteorological data are summarized in Table 2.

Properties	Simplified mete	orological data	Actual meteorological data	
	peat	mineral	peat	Mineral
Porosity $[m^3 \cdot m^{-3}]$	0.8±1.9	0.6+0.25	0.6±1.9	0.4+0.25
Thermal conductivity, $[W m^{-1}K^{-1}]$	0.225±0.2	2.0±0.5	0.15±0.1	1.6±0.5

320 Table 1: Allowed range for the estimated parameters.

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322 Table 2: Description of all PE cases used in this study.

The numbers before *T* and s_l correspond to the number of sensors used. Number before ρ_a corresponds to the number of apparent resistivity snapshots used. *n* stands for noise added to the synthetic measurements. (S) corresponds to runs driven by simplified meteorological data. (s) represents daily ρ_a snapshots.

Case	Simplified meteo	orological data (S)	Actual meteorological data		
#	Case name Description		Case name	Description	
1	(S)3T3s _l 1 ρ_a	All data from #1 to #3 sensors, and 1 ρ_a snapshot	6T	Sensors from #1 to #6, temperature only	
2	(S)3 $T3s_l \delta \rho_a$	All data from #1 to #3 sensors, and 8 ρ_a snapshots	10 T	Sensors from #1 to #10, temperature only	
3	(S)6T6s _l 1 ρ_a	All data from #1 to #6 sensors, and 1 ρ_a snapshot	6 <i>s</i> _l	Sensors from #1 to #6, liquid saturation only	
4	(S)6 $T6s_l \delta \rho_a$	All data from #1 to #6 sensors, and 8 ρ_a snapshots	$1\rho_a$	1 ρ_a snapshot on month of August	
5	(S)6T6s _l 1 ρ_a +n	All data from #1 to #6 sensors, and 1 ρ_a snapshot with added noise	$6T1\rho_a$	Temperature sensors from #1 to #6, and 1 ρ_a snapshots	
6	(S) $\overline{6T6s_l 8\rho_a + n}$	All data from #1 to #6 sensors, and 8 ρ_a	$6s_l 1\rho_a$	Liquid saturation sensors from #1 to #6, and 1 ρ_a snapshots	

	snapshots noise	with	added		
7				6T6s _l	Temperature and liquid saturation sensors from #1 to #6
8				$3T3s_l 1\rho_a$	All data from #1 to #3 sensors, and 1 ρ_a snapshot
9				$3T3s_l 8\rho_a$	All data from #1 to #3 sensors, and 8 ρ_a snapshots
10				$6T6s_l 8\rho_a$	All data from #1 to #6 sensors, and 8 ρ_a snapshots
11				$6T6s_l 8\rho_a(s)$	All data from #1 to #6 sensors, and 8 ρ_a snapshots, taken every day
12				6Τ6s _l 1ρ _a	Special case, we moved sensors #4, #5 and #6 below the active layer depth (at 80cm depth), and 1 ρ_a snapshot
13				$10T10s_l1\rho_a$	All data from #1 to #10 sensors, and 1 ρ_a snapshot
14				$10TI0s_l 8\rho_a$	All data from #1 to #10 sensors, and 8 ρ_a snapshots

328 3. Results

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330 3.1 Simplified meteorological data

To evaluate the PE method performance driven by simplified meteorological data, we ran PE 331 332 experiments using 30 different random combinations of porosity and thermal conductivity values 333 as the initial starting point. We used 30 PE samples of $\{\phi, k\}$ starting points in the first experiment 334 $((S)3T3s_1 l \rho_a)$ to illustrate the overall performance of the parameter estimation using a large number of samples. After that, we did only five PE runs for the simplified meteorological data and 335 336 10 for all other runs with actual meteorological data. For all figures after Figure 4, for consistency 337 and clarity, we show results for only five PE runs per case. It is important to note that the number of samples that one needs to run to ensure the robust convergence of the estimated parameters 338 339 depends on the specifics of the corresponding case (i.e. experiment specific). If most of the LM 340 runs converge to the same set of parameters and have low cost function values, then that set of 341 runs most likely corresponds to the actual $\{\phi, k\}$. In Figure 4, the red triangles represent initial

342 guesses (parameter combinations) and the synthetic truth is indicated by the intersection of the two 343 dotted lines. Yellow lines connecting red triangles with white crosses represent the path that the 344 LM algorithm has taken from the initial guess to the estimated parameter combination (white 345 crosses, Fig. 4). The yellow dots along the yellow lines indicate the location at each LM iteration. 346 Figure 4 indicates that the method is able to recover porosities more robustly than thermal 347 conductivities, i.e. estimated porosities are similar to their true state. According to the liquid 348 saturation plot on Figure 3, liquid saturation of the mineral layer is quite dynamic and more 349 saturated in comparison to the peat layer. Nevertheless, thermal conductivity of the mineral layer 350 (k_m) corresponds to the highest mismatch. Three out of thirty inversions corresponding to k_m end up close to 1.4 $W m^{-1}K^{-1}$ (the true value is 2 $W m^{-1}K^{-1}$), suggesting those values do not 351 correspond to the 'truth', since most of the estimated values (27 cases) are concentrated around 352 353 the intersection of the dotted lines. The response surface for the corresponding cost function (eqn. 354 5) lies hereby in a flat, low-gradient region. The projections of the cost function response surfaces 355 corresponding to porosities (Figure 4A) has a better defined minimum, as opposed to projections 356 of the cost function response surfaces corresponding to thermal conductivities (Figure 4B), 357 indicating non-uniqueness of the estimated parameters. For this experiment, we used time-series 358 of T and s_1 only from the first 3 near-surface sensors (Figure 2A). All of these 3 sensors are located 359 in the peat layer, suggesting that using just near-surface sensors only from one upper layer might 360 not be enough to recover the deeper layer thermal conductivity.



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for peat and mineral soil layers. Yellow lines correspond to the paths taken by the LM algorithm. The white dots correspond to the estimated values. A) projection of the cost function with respect to porosities of peat and mineral layer. B) projection of the cost function with respect to thermal conductivities of peat and mineral layer. The color bar represents the cost function normalized by its maximum logarithmic value.

370 To illustrate the effect of noise on the robustness of the estimated parameters we used cases with 371 6 near-surface sensors (6T and $6s_1$), and a varying number of ERT snapshots driven with simplified 372 meteorological data. Similarly to the (S) $3T3s_1 l\rho_a$ case, (S) $6T6s_1 l\rho_a$ shows good convergence 373 for porosities and poor convergence for thermal conductivities with an averaged error of $0.1Wm^{-1}K^{-1}$ (Figure 5AB). Adding noise to the (S)6T6s_l1 ρ_a +n case slightly worsens the 374 estimated porosity values and significantly worsens k_m with root-mean-squared error (RMSE) 375 376 raising from 10% to more than 50% (Figure 5CD). Figure 5EF shows that increasing the number 377 of ERT snapshots from 1 to 8 per year (i.e. collected once per month from January till September) improves k_m estimates, allowing better convergence for four out of five samples to the synthetic 378 truth. If we compare all three cases on Figure 5 on how well they are able to estimate k_m , it is 379 clear from Figure 5D that for the case (S) $6T6s_l l\rho_a + n$ none of the k_m 's were correctly estimated, 380 whereas significantly improved k_m values were found by increasing the number of monthly ERT 381 382 snapshots (Figure 5F). Moreover, all except one estimated value showed a better match with its true value than the (S)6*T*6 $s_l l \rho_a$ case without any added noise. 383





Figure 5. Estimated properties from 5 inversions of the three different cases, where the "true" values are shown as a cross-section of the two dashed lines for the bulk porosities and effective thermal conductivities for peat and mineral soil layers. Yellow lines correspond to the paths taken by the LM algorithm. The white dots correspond to the estimated values. The rows from top to bottom correspond to cases (S)6T6s₁1 ρ_a , (S)6T6s₁1 ρ_a +n, and (S)6T6s₁8 ρ_a +n respectively. The columns from left to right correspond to the projection of the cost function with respect to porosities and thermal conductivities. The color bar represents the cost function normalized by its maximum logarithmic value.

393 In Figure 6, we summarize results of the five PE runs for each of the first six cases corresponding 394 to simplified meteorological data listed in Table 2. The first three matrix tables correspond to the 395 normalized RMSE values for each measurement type (ΔT , Δs_l , and $\Delta \rho_a$). The last two matrix tables correspond to the normalized Euclidian distances between the synthetic truth and estimated 396 397 parameter values of $\delta \phi$ and δk . We normalized the values in each matrix by dividing by the 398 maximum value from the corresponding matrix. The normalized values are marked with tildes 399 and range from 0 to 1, where values closer to 0 correspond to a better match and values closer to 400 1 correspond to a worse match. As shown above, the method is able to accurately estimate, both, 401 peat and mineral soil porosities as well as peat layer thermal conductivity (k_p) , but cannot always accurately estimate k_m . There is not much difference between cases (S)3T3s_l1 ρ_a and 402 403 (S)6T6s_l1 ρ_a except for a slight improvement in k_m , suggesting that the small vertical distance (10 404 cm) between sensors 1 and 4, 2 and 5, and 3 and 6 could be limit the recorded data variability, 405 leading to difficulties in the estimation of the k_m parameter. Since all 6 sensors lie within the 406 active layer, we added additional sensors below the active layer in the later experiments (red stars 407 in Figure 2A). The ϕ and k matrix tables show that increasing the number of monthly ERT 408 snapshots consistently improve the estimates of ϕ and k. This suggests that increasing the number 409 of monthly ERT snapshots can lead to improved convexity of the cost function (eqn.5).





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Figure 6. Five matrix tables presenting fitness metrics between synthetic model values and values obtained by the parameter estimation method using simplified meteorological data. Matrix tables from left to right correspond to the normalized root mean squared errors for temperatures, liquid water saturations, and apparent resistivities and to the normalized Euclidian distances between synthetic ("true") and estimated porosity, and thermal conductivity values. Each matrix value was normalized by dividing it by the matrix maximum value. The normalized values are indicated by tildes.

419 **3.2 Meteorological data from Utqiagvik (Barrow) site 2015**

After testing the PE method for the simplified meteorological data, we applied measured meteorological data from the BEO site for the year 2015. To better understand the importance of each measurement type and their combinations within the developed PE algorithm, we tested all of the scenarios corresponding to the 'actual meteorological data' column from Table 2. The results of these runs are summarized in the colored matrix tables in Figure 7. Since there are more than twice the number of actual meteorological cases than simplified meteorological cases, it is difficult to analyze all matrix tables at once.

To compare the match between all estimated and observational values within a single plot wecalculated Euclidean norms for each case independently:

429
$$\Delta\left(\widetilde{\Delta T}, \widetilde{\Delta s}_{l}, \widetilde{\Delta \rho}_{a}\right)_{i} = \sqrt{\left(\frac{\Delta T_{i}}{\Delta T_{max}}\right)^{2} + \left(\frac{\Delta s_{l_{i}}}{\Delta s_{l_{max}}}\right)^{2} + \left(\frac{\Delta \rho_{a_{i}}}{\Delta \rho_{max}}\right)^{2}} \tag{7}$$

430
$$\Delta \left(\widetilde{\delta \phi}, \widetilde{\delta k} \right)_{i} = \sqrt{\left(\frac{\delta \phi_{i}}{\delta \phi_{max}} \right)^{2} + \left(\frac{\delta k_{i}}{\delta k_{max}} \right)^{2}} \tag{8}$$

431 The index *i* indicates hereby the case number (see Table 2). Then we applied k-means clustering 432 analysis to identify groups of cases with similar match between data and estimated parameters. 433 We divided all cases into four classes shown in Figure 8. Class I indicates the best cases that 434 provide an accurate parameter estimation as well as accurate matches with the synthetic "true" 435 measurements. Class II includes the cases that have accurate parameter estimates and less accurate 436 matches with the measurements. Class III indicates all cases that have less accurate parameter 437 estimates but accurate matches with the measurements. Finally, Class IV includes the cases that 438 showed the worst performance in terms of parameter estimates and the worst matches with the 439 measurements. We summarized the results from Figure 8 in Table 3.

Class I (see Table 3) suggest that sensors located below the active layer as well as increasing the number of sensors lead to more accurate parameter estimation. In contrast, Case #4 (corresponding to the one ERT snapshot, $1\rho_a$), suggests that already one ERT data snapshot could be enough for parameter estimation while Class II indicates that in general an increase of the numbers of monthly ERT snapshots is important for more accurate PE. However, increasing the number of monthly ERT snapshots leads to a less accurate match with measurements. These results are consistent with the results for simplified meteorological data with added noise (Figure 5).

- 447 Class III includes 6 cases suggesting that if we have only soil moisture data available for PE, then
- 448 we should expect less accurate soil property estimates. The last element in this class suggests that
- taking daily ERT snapshots improves the apparent resistivity match (Figure 7, resistivity table) but
- 450 does not improve $\{\phi, k\}$ estimates, where monthly ERT snapshots improve thermal conductivity
- 451 convergence.
- 452 Class IV once again clearly indicates that measurements obtained below the active layer provide
- 453 more accurate parameter estimates, however, they do not improve matches to measurements. This
- 454 is mainly due to significant mismatch with ρ_a , which can be seen from the $\Delta \rho_a$ matrix table on
- 455 Figure 8. At the actual site, the depth to the mineral soil can be deeper than 20 cm, not having
- 456 sensors lower than 20 cm limits therefore the amount of data that can help to improve the convexity
- 457 of the cost function in our case.

Class I	Class II	Class III	Class IV
$10T10s_l 1\rho_a$	$6T6s_l 8\rho_a$	6s _l	10T
$10T10s_l 8\rho_a$	$3T3s_l 8\rho_a$	$6s_l l \rho_a$	6T
$l\rho_a$		$6T1\rho_a$	
$6T6s_l 1\rho_a$		$3T3s_l 1\rho_a$	
		6T6s _l	
		$6T6s_l 8\rho_a(s)$	

458 **Table 3:** K-mean analysis of the accuracy for each 13 cases.

459

460 From Figure 8 and Table 3 we know that the 6T case has the worst performance in terms of 461 matching $\{\phi, k\}$. Similar to the experiments with simplified meteorological data, the main 462 difficulty for experiments with actual meteorological data is estimating thermal conductivity. The last matrix table (δk) on Figure 7 shows that $6T6s_l \delta \rho_a(s)$ has the highest maximum and mean 463 464 mismatch in thermal conductivity estimates. However, since ϕ estimates are a better match with 465 their corresponding "true" values, the case $6T6s_1 8\rho_a(s)$ falls into class III in Figure 8, as opposed 466 to case 6T, which falls into class IV. The highest mismatch in thermal conductivity values for the $6T6s_l \delta \rho_a(s)$ case suggests that collecting daily ERT snapshots improves the ρ_a match (Figure 7, 467 $\Delta \tilde{\rho}_a$ matrix table) but does not improve estimated parameters, where monthly ERT snapshots 468 469 improve thermal conductivity estimation.

470 To illustrate this, we plot values of estimated parameters and the corresponding response surfaces 471 of the cost function for cases $10T10s_l 8\rho_a$ and $6T6s_l 8\rho_a(s)$ on Figure 9. The PE method was able 472 to match 4 out of 5 estimates almost perfectly and missed the k_p for the $10T10s_l 8\rho_a$ case. The 473 corresponding cost function has a visible minimum and clear convexity. In contrast to this, the 474 $6T6s_l 8\rho_a(s)$ case completely missed 2 estimates by converging on values outside the boundaries, and 3 other estimates do not converge to the desired cross section as well. The contour lines suggest 475 476 that the corresponding response surfaces of the cost function do not have a well-defined global 477 minimum.

478

479 **4. Discussion**

480

The existence of multiple minima is common in inverse modeling and can lead to false convergence of the PE algorithm to physically non-realistic subsurface parameters (Nicolsky et al., 2007). This is one of the main reasons for using multiple initial guesses. If most of the inversions converge to a similar set of parameter estimates with the lowest cost function value, then that set of values is most likely the global minimum. Testing the PE algorithm using multiple starting points is a commonly used approach in evaluating the robustness of an inverse model (e.g. Hansen, 1998).

488 A potential strategy to improve the developed PE algorithms is to reduce the specified convergence 489 tolerance value (i.e. minimum condition, see Figure 1) or increase the allowable number of 490 iterations. However, this could lead to a significant increase in computational effort. In addition, 491 PEST provides multiple additional settings of inversion parameters to achieve a better 492 convergence. Parameter regularization is one of them. Regularization techniques have been 493 widely used in solving ill-posed inverse problems (Vogel, 2002). The overall idea is to constrain 494 the objective function by imposing additional priors on the estimated model parameters. We 495 recognize that including parameter regularization into the cost function may improve the 496 robustness of our method. However, inclusion of the regularization would require an extensive 497 exploration of the multiple regularization methods and values that could be applied to it, which is 498 beyond the scope of this paper. Here we illustrate that without using regularization it is possible to 499 achieve reasonable results by using the simple weighted cost function.

500 The good performance of the case with only one ERT snapshot $(1\rho_a)$ could be misleading due to 501 the design of this numerical experiment, i.e. we are using a synthetic "truth" produced by the same 502 model used in the inversion, which improves the convexity of the cost function and leads to a well 503 constrained unique minimum. However, in reality, collection of additional information, such as 504 organic layer thickness and temperature data, are extremely important and are required for model 505 calibration (Jafarov et al., 2012; Atchley et al., 2015). In addition, real ERT surveys can be 506 perturbed by noise and their interpretation may require site-specific petrophysical relationships as 507 opposed to the general petrophysical relationships used in this study. Therefore, we do not suggest 508 inversion based on one ERT snapshot without any additional data.

The $6T6s_l 8\rho_a(s)$ case, where all runs converge to different values of k_m , indicates that using certain combinations of datasets does not allow the inverse approach to properly recover k_m . It is likely that $6T6s_l 8\rho_a(s)$ does not capture much variability in soil temperatures and soil moisture, and therefore ERT snapshots do not have much variability as well. Once the cost function converges for one of the ERT snapshots, it immediately converges on the other daily snapshots due to their similarity. In fact, although $6T6s_l 8\rho_a(s)$ has a good accuracy with observations (see the $\Delta \tilde{\rho}_a$ matrix table in Figure 7), it is unable to recover the value of k_m .

We have shown that even in the ideal situation where we either generate observational data or use simplified meteorological data, we cannot always fit modeling results to observations. In reality, noise (e.g. the sensor's measuring resolution) influences the collected data. To investigate the impact of measurement noise, we introduced multiple levels of noise to the simplified meteorological data. The resulting PE showed that dealing with noisy data could be challenging (Figure 5). However, our results showed that adding monthly taken ERT snapshots into the cost function improves the overall PE accuracy.

The distance between sensors could be another source of uncertainty in the PE. As pointed out by Nicolsky et al., (2009), it is important to make sure that a vertical difference between adjacent measurements do not introduce additional noise that can mislead the minimization algorithm without providing new information. If sensors are close to each other, measurements might be the same or within the noise variability. In our setup the vertical distance between the first two rows of sensors is about 10cm. This could lead to small temperature variability between sensors. Indeed, providing greater vertical distance between sensors improved the PE accuracy. The Case #12 530 $(6T6s_l 1\rho_a)$ clearly illustrates this point, that by increasing the vertical distance between sensors 531 we can improve estimated parameter accuracy.

532 Combining hydrothermal observations from multiple depths with monthly ERT measurements 533 resulted in an improvement of the shape of the cost function and lead to better defined minima 534 (Figure 9). Increasing the number of the monthly ERT snapshots improved the accuracy of the 535 estimated parameters. In addition, we showed that having sensors below the active layer combined 536 with ERT snapshots shows the best accuracies, both, in terms of estimating parameters and 537 matching observations.

538

539 **5.** Conclusion

540 The overarching goal of this study was to develop and validate a parameter estimation algorithm 541 using a synthetic setup and a 2D coupled thermal-hydro-geophysical model based on a polygonal 542 tundra site within the Barrow Environmetal Observatory. Combining hydrothermal observations 543 from multiple depths with monthly ERT measurements resulted in an improved shape of the cost 544 function and led to better defined minima and improved accuracy of the estimated parameters. 545 This was presented in fitness matrices for six cases using simplified meteorological data. Similar 546 conclusion were found for inversion runs with actual meteorological data. It is important to note 547 that it was not only the number of ERT data snapshots that improved the robustness of the PE 548 method but rather the time frequency of the ERT data snapshots, i.e. monthly vs daily snapshots. 549 In addition, collecting data from several soil layers might improve the thermal conductivity 550 estimates for the corresponding soil layer. Our experiments show that robust PE can be achieved 551 not just by adding more sensors into the ground and increasing number of ERT snapshots, but also by optimally distributing those sensors within the transect (e.g., the $6T6s_l 1\rho_a$ case). Overall, the 552 553 inversion runs that we investigated consistently indicated that collecting data from multiple soils 554 layers, providing enough vertical separation between sensors, and collecting temporally diverse 555 ERT data should lead to robust parameter estimation. The exception from this conclusion is the 556 case $l\rho_a$, which showed robust parameter estimation due to specifics of the model setup. As discussed above, estimating porosities and thermal conductivities based on 1 ERT snapshot would 557 558 not be possible without additional information on the subsurface properties.

559 This work developed and demonstrated the feasibility of a PE algorithm that can be used to better 560 inform large-scale Land System Model subsurface parameterization. Here we demonstrated the 561 proof-of-concept of the PE method. Further improvements such as introduction of a PE 562 regularization parameter into the cost function and leveraging additional PEST capabilities could 563 improve method robustness. Finally, the PE method must still be tested using measured thermal-564 hydro-geophysical data from the BEO site.



565

Figure 7. Five matrix tables presenting fitness metrics between synthetic model values and values obtained by the parameter estimation method using meteorological data from the year 2015 from BEO site in Alaska. Matrix tables from left to right correspond to the normalized root mean squared errors for temperatures, liquid water saturations, and apparent resistivities, and to the normalized Euclidian distances between synthetic ("true") and estimated porosity, and thermal conductivity values. Each matrix value was normalized by dividing it by the matrix maximum value. The normalized values are indicated by tildes.

573



Figure 8. A k-means clustering analysis applied to the Euclidean norms of the normalized mean

576 differences of estimated soil properties and the corresponding fit between calculated and observed

577 values. Each color and marker represent a certain class as a result of the k-means clustering analysis.





Figure 9. Estimated properties from five inversions of the two different cases: $10T10s_18\rho_a$ (top) and 6T6s₁8 $\rho_a(s)$ (bottom). The "true" values are shown as a cross-section of the two dashed lines for the bulk porosities and effective thermal conductivities for peat and mineral soil layers. Yellow lines correspond to the paths taken by the LM algorithm. The white dots correspond to the estimated values. The columns from left to right correspond to the projection of the cost function with respect to porosities and thermal conductivities. The color bar represents the cost function normalized by its maximum logarithmic value.

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