

Response review by Martin Truffer (Referee)

This paper presents models of recent thinning and grounding line retreat of the glaciers feeding the Dotson and Crosson ice shelves. The models are also used to address possible future scenarios for this system of glaciers. The paper is hugely relevant. While a lot of attention is currently focused on the neighboring Thwaites Glacier it can easily be forgotten that the Pope/Smith/Kohler glaciers have undergone some of the largest changes observed anywhere on the planet. In addition, it has the potential to affect ice evolution in the larger area, as thinning can spread inland rapidly and lead to divide migration, with consequences for this entire sector of the ice sheet.

I do recommend publication in TC for this paper, but I also have a few general comments that I hope will be useful.

Thank you for the careful read and helpful comments; we have incorporated them as described below.

1) Generally, the paper could do a better job in outlining what works well in these models and what doesn't. This could be accomplished by a slight reorganisation of the Discussion and some expansion of the Conclusions. Otherwise, it is easy to read this paper and get sidetracked by model-data mismatches. This starts with Figure 1: Fig. 1b-d show velocity model-data mismatches that are quite large. It is easy for a reader to then be skeptical of any conclusion reached in the paper. I suggest that the paper first emphasises the conclusions that are most solidly supported and then discusses all the qualifications. For example, continued mass loss over the next century of order >6 mm sea level seem inescapable. Grounding line position is fiendishly difficult to get right and varies a lot between models. Etc.

It is certainly a challenge to distill the most valuable aspects of the modeling. Following this comment, we restructured the text at several places so as to try to emphasize the most strongly supported conclusions while still presenting the necessary caveats, which involved four main changes:

- 1. We have switched figure 1 to be data only and have removed the panels of modeled speed since the changes in velocity can also be gathered from later figures.*
- 2. For the discussion, we have tried to emphasize the comparison to observed grounding-line positions, because this comparison is the main tool by which we evaluate the effects of different model parameters upon the results. We moved the discussion century-scale simulations to immediately follow this section, since the grounding-line comparison provides the necessary framework for understanding which of those longer-term simulations we consider most likely. (see sections 4.1 and 4.2 of the revised manuscript)*

3. *To begin the comparison with ice velocities and thinning, we explicitly acknowledge the substantial mismatch, but emphasize that the mismatch nevertheless allows us to learn about what important processes the model might be missing and in what direction it may err.*
4. *We have expanded the conclusions section to reflect these most inescapable aspects of the model simulations.*

2) What is the criterion for the choice of models for the prognostic simulation? It seems like you don't hold much faith in some of these. Could you more clearly outline, which range is most realistic, given the model performance over the period of observations. *We chose which models to run with three criteria: 1. All the runs were 1Obs so as to have the most realistic melt rates. 2. The simulations with substantial retreat were all represented and 3. We spanned even some simulations without much retreat, in case retreat eventually continued beyond the time span of the short simulations. We have added a brief mention of this in the methods "were chosen to represent a range of retreat rates, some realistic and some slower than observed, and all used realistic melt rates." and a reminder in the results "chosen to represent a range of retreat scenarios with realistic melt intensity."*

We have also changed the discussion to start by explicitly reminding the reader that we only consider 3/6 of these simulations to be reasonable matches to observations. The new pieces of text are:

*"The centennial-scale simulations can be broadly categorized that emulate observed grounding-line retreat (i.e. display more than 35 km of retreat) and those that retreat less than observations. Those simulations that emulate retreat (2, 4, and 19 in **Error! Reference source not found.**) all continue to produce retreat into the future."*

and

"Thus, these three simulations suggest that these glaciers will likely contribute 6 mm of sea-level rise over the coming century, even if shelf-integrated melt rates remain at about their levels in recent years."

3) I would love to see a bit more discussion on initialization. You generally do a good job outlining the challenges. Is there a way to assess how important the initial temperature distribution is? You make a steady state calculation here; if I read it correctly. For example, when you invert for flow rate factors over the ice shelf, how does that compare to the derived temperature distribution? Also, one measure of success for initialization is to look at thinning rates. How well do the models do with that?

Yes, it is indeed a steady state calculation. We frame the inversion in terms of the enhancement factor, so the most straightforward measure of how close this is to the temperature distribution is to look at where these values are close to one. The initial inversion results over the shelves (prior to relaxation) were previously published (Lilien

et al., 2018, figure 5); generally, the enhancement factor is ~ 1.5 or less, with the temperature being largely sufficient to capture the 1996 velocities (though greater enhancement was needed to accurately model the velocities in the 2010s). However, this does not necessarily imply that the modeled temperature is correct, and it may just be a weak sensitivity of the modeled velocities to the viscosity. Regardless, it appears that temperature alone does reasonably well on the shelves. We have added “this initial set of inversions is also described in Lilien et. al, 2018, where plots of the inferred enhancement are shown”.

It is a much tougher question to assess whether the temperature distribution of grounded ice is sufficiently uncertain to adversely affect our results, as we may have compensating errors between the temperature distribution and basal slipperiness field. While some previous work has simultaneously inferred ice viscosity and basal slipperiness, we choose not to do so due to the potential for non-unique inference of the fields. While thinning rates may theoretically indicate something about model initialization accuracy, in practice they can simply indicate something about the accuracy of ice-thickness measurements. For example, even if a model had “true” basal friction and effective viscosity but had a 40-m error in bed elevation, we would expect substantial thinning/thickening for mass conservation. We have added a paragraph describing this assessment: “While it is difficult to assess whether the model accurately represents the true temperature, enhancement, and basal slipperiness fields, modeled thinning rates at the end of relaxation give an indication of model self-consistency. Conversely, the total change in surface height during relaxation gives a misfit between the model and available data (though in part that relaxation may be compensating for errors in the data). Here, relaxation resulted in local changes of up to 100 m near Kohler Glacier’s grounding line and changes of at most 50 m elsewhere. While most of the change during relaxation can potentially be attributed to errors in ice thickness caused by uncertainty in the bed elevation, the large change on Kohler likely indicates that the surface elevations were also incorrect in that area. Because determining the surface elevations at initialization required some extrapolation using longer term thinning rates (see Lilien et al., 2018 for details), this misfit is not surprising and may reflect a change in the spatial pattern of thinning during 1996-2003. At the end of the relaxation, thickness change rates were reduced to $<10 \text{ m a}^{-1}$, which is smaller than the observed rate of thickness change, except on Kohler Glacier where $\sim 30 \text{ m a}^{-1}$ of thickening persisted. While this is still a large rate of elevation change on Kohler, we were forced to choose between accepting Kohler’s unrealistic imbalance and possibly relaxing away the real imbalance on Smith and Pope. The potential effects of the resultant transients upon the modeled retreat of Kohler are revisited in Section Error! Reference source not found..”

4) How is calving at the ice shelf front handled?

Because the calving fronts have remained conveniently near the ends of their embayments, we do not explicitly model calving but simply use a sea-pressure boundary condition at the end of the embayment. We recognize that this of interest for readers, and have added: “Calving was not explicitly modeled, but instead ocean pressure was applied on the downstream boundary at the mouth of the ice shelves’ embayments where ice is

allowed to flow out. This boundary condition would remain accurate for an advance since ice tongues extending beyond embayment walls do not provide additional back stress, but, if substantial ice loss caused the calving front to retreat behind the embayment walls, it could potentially result in underestimating ice loss during retreat.”

5) Could you comment a bit more on the choice of multiplying observed melt rates rather than multiplying parameters as in prior studies (line 224-230). What are the benefits of this choice?

The main benefit is preventing unrealistically large losses during a ramp-in period, while the primary drawback is the requirement to have the data available to constrain these rates. We do not want to elaborate too much here since there is a full paragraph in the discussion, but have added the brief description “but this choice was mainly made to limit melt rates to realistic values during the period with observations”

6) Parts of the discussion on weakening (l.383-394) reads a bit odd in the sense that it sounds like you discuss weakening of margins as a possible cause. But what would cause weakening in the first place? Ice doesn't just get 5 deg warmer or more anisotropic; there would have to be some other driver. So weaker margins could lead to an amplification of an otherwise triggered change. Some rewording would clarify that. *Indeed there needs to be a trigger, and the wording was ambiguous in this section. We have rephrased at several points, and it now reads: “While snapshot inversions for ice-shelf viscosity in 1996, 2011, and 2014 indicate some weakening of Crosson Ice Shelf (Lilien et al., 2018), this weakening cannot be definitively identified as having been caused by a particular process (e.g. loss of a pinning point or rifting). Thus, we are unable to identify if the weakening of the margins was triggered by grounding-line retreat itself or was externally triggered and helped initiate grounding-line retreat. We consider it unlikely, regardless of their trigger, that”*

7) Figures are a bit hard to read with small fonts, at least on a printed out copy. I would prefer a Figure 1 that is more of an overview. In particular, having results in there already (velocities) is actually distracting

We agree that these are hard to read in the version online. Font sizes were all in line with the publisher recommendations when the figures were produced, but shrunk substantially due to different margin widths between the template files and what is expected for final, published versions, and also due to shrinking by the publisher after submission in order to fit logos at the top of each page for the discussion version. We apologize for the difficulty in reading them, but have left the font sizes as-is for resubmission since we expect the problem to be remedied by using the full-size figures at production.

We have changed figure 1 to be data alone.

8) This is a bit of a repeat of comment 1): What should the reader take away from figures such as Fig. 7? I can look at it and say that this model is terrible: on Pope the largest thinning is off by a factor of 2 in the best case. Similar things could be said for

grounding line positions and velocities. But that is obviously not your main point. Help the reader a bit in what you consider the successes and challenges of this modeling effort. I think a bit of a restructure of Discussions would go a long ways here.

Addressed along with comment 1.

Small edits:

I.30: I would say 'peaked temporarily'. There is no reason that this would have to remain a one-time occurrence.

Done

I.175: I think this is not quite correct. The effective pressure assumption here essentially implies infinite hydraulic conductivity (a flat water table). The implication is that any sort of pressure gradient that is required to drain subglacial water means that water pressure further away from the grounding line needs to be higher, which extends Coulomb like deformation inland. Therefore the model is likely to underestimate inland velocity response.

Yes, this is probably a better description of the assumption, and one of multiple reasons that this parameterization may underestimate Coulomb-like behavior. We have changed the text to:

"This assumption is valid for infinite hydraulic conductivity, while in reality inland water pressures may be higher due to finite hydraulic conductivity, which would lead to this parameterization underestimating the extent of Coulomb-like behavior"

I.203: ... comparison BETWEEN modeled ...

Fixed

I.277: ... compared TO the observed ...

Fixed

I.324/25: Why those particular choices (see also comment 2) above)

We elaborate more elsewhere as described above, but here we have added "chosen to represent a range of retreat scenarios with realistic melt intensity"

I.445: to -> from

Fixed

I.449: Where is the Haynes Glacier (maybe show in Fig. 1?)

Since it is mostly clipped from figure 1, we have instead specified in the text that we refer to loss of buttressing at the outer right corner of Crosson.

I.463: There are A variety ...

Fixed

I.509: error -> errors

Fixed

I.516-519: Also, hydraulic gradients would lead to lower effective pressure inland, as per comment above.

Changed to “ignoring hydraulic gradients and limiting Coulomb (plastic) behavior to near the grounding line”

I.526: .. as much AS the ...

Fixed

I.526: How do you know that?

We have made this more tentative: “it is possible bed errors alone could change the timing of retreat by as much as the model-data mismatch.”

I.530: its -> it

Done

I.531: ... we did NOT have ...

Fixed

I.567: 'relatively modest' is in the eye of the beholder, you're describing some major changes here with global impacts from a single basin

Changed to: “modest compared to some other Antarctic catchments”

Conclusions could be expanded a bit.

Done. Changes are described in response to General Comment 1.

I.759: one of the 'thin for 2Obs' should be 'thick for 1Obs'

Thanks

Response to anonymous reviewer #2

General Comments

In this paper, the authors present the results of from a model of the Smith, Pope, and Kohler glaciers using varying sub-shelf melt forcings and marginal shelf weakening. The experimental design is thoughtfully considered and thorough, with a large number of combinations of model setups tested. Any limitations to the model are also thoroughly discussed at the end of the paper. After backtesting the model over the previous 25 years and comparing to observations, the model is run forward in time to predict the retreat of the grounding lines of Smith, Pope, and Kohler glaciers over the next century. The authors find that the glaciers are likely to contribute at least 6mm of sea level rise

over the next 100 years. They also predict that Smith glacier could retreat to the ice divide with the Thwaites glacier catchment within the next 100 years, further undermining the ice sheet in the Thwaites drainage. This is an interesting and important result that will likely be of special interest to the broader community of researchers studying the Amundsen Sea region of the Antarctic Ice Sheet.

I recommend that the paper be accepted for publication subject to the following comments/corrections.

We thank the reviewer for the careful read and comments. Specific points are addressed below.

Specific Comments

P. 2, lines 40-41: If the grounding line is retreating to deeper seabed, the warm water will need to flow down over the shallower seabed to get to it, meaning that the grounding line is no more vulnerable to warm ocean water than it was before. Do you mean that the grounding line is more vulnerable to melting due to the reduction in the freezing point with depth?

There are several reasons besides freezing-point depression that deepening a grounding line can increase melt rates. First, at the shallowest point in the bathymetry, shallowing draft thickens the water column and permits greater access of water to contact the ice. Recent modeling shows that the ice-bottom topography plays an important role in how water accesses the cavity (Goldberg et al., 2019). Moreover, deeper grounding lines generally imply greater sub-shelf area below any given depth, again creating more potential melt independent of the local melting point (this is stated directly in Jenkins et al., 2018, which we cite at this point in the text). We believe the statement is well supported, and have left it as-is.

P. 7, line 212: It would be interesting to know how the Cryo2 melt rates compare to flux divergence melt rates for the 2010-2016 period. Have you looked into this?

We have looked into this on a shelf-averaged scale for Dotson, where they agree within error ($7.7 \pm 1.3 \text{ m yr}^{-1}$ vs. $6.1 \pm 0.7 \text{ m yr}^{-1}$). We have added mention in the text that agree to within errors.

P. 8, line 277: “5-km retreat” looks more like ~1km retreat to me.

We are guessing that this is a typo, and the reviewer meant 10-km retreat. Regardless, it is a good catch. Depending on the exact flowline used, it ranges from ~5-12 km; since the flowline used in the figures has it near 10 km, we have switched it to 10 km here.

P. 9, line 308: Referral to Figure 4a-c, but control melt results aren’t shown.

This referred to an earlier version of the figure where we had included more different simulations that were subsequently removed for readability. We have deleted the reference.

P. 9, line 314: Referral to Figure 5a-c to see stabilization after 5 year forced ungrounding, but the first five years of grounding line retreat are covered by the figure label (especially for Smith).

Yes, the label was poorly placed. We have moved the figure label to make this visible.

P. 9, lines 314-315: “retreat subsequently ensues on each of the three glaciers...” This doesn’t appear to be true for S2016 melt on Pope or Kohler.

Good point, the text was in error. We have fixed this to only reference Smith glacier.

P. 10, lines 320-322: “...by the end of the 50-year simulations...” To my eye, the only one that consistently approximates the J2010 free GL results is J2010 5-yr GL.

Our language was imprecise. We have made this a simple, quantitative statement to avoid the ambiguity. It is now “leaving the grounding lines within 5 km of their 2014 positions”

P. 10, line 335: Define “significant” (>40km?)

We added >50 km as a parenthetical. At several points in the text, we switched the language from “significant” to “substantial” to avoid implications of statistical significance.

P. 11, line 357: “...those with the J2010 melt parameterization...” (with the exception of the control melt-scaling)

Another good catch. We have rephrased to “J2010 melt parameterization with 1Obs or 2Obs melt, irrespective of marginal weakening”

P. 11, lines 375-378: “While our rescaling...” What does this mean for Cryo2 melt rates from 1996-2010? The Cryo2 melt distribution also doesn’t allow the ice shelf to deepen into melt as you go back in time – does this mean that melt rates near the grounding line would be comparatively high for the Cryo2 distribution in 1996?

The rates used to force the model are low there because the areas of high melt in 2010-2016 are generally in newly ungrounded area. We have changed the text to clarify how this mismatch in timing and forcing are affect the results. It now reads:

“The stable grounding-line position found by forcing the model with Cryo2 melt (Gourmelen et al., 2017) may result from underestimation of melt near the grounding line in 1996, either due to the difficulty of using satellite altimetry to infer melt rates in an area not in hydrostatic equilibrium (Fricker and Padman, 2006; Rignot, 1998) or due to a change in distribution of melt between 1996 and 2010. Since melt rates were inferred over 2010-2016, if melt were highest near the grounding line in 1996 but subsequently the area of peak melt moved upstream, the 2010-2016 rates may be much lower those in 1996 near the grounding line at that time. This mismatch in observation time and model forcing could have then resulted in the model never beginning to retreat into areas of concentrated melt. Moreover, even once retreat was triggered, the inferred melt rate beneath areas that ungrounded during 2010-2016 mixes periods of no melt and more intense melt, thus causing underestimation of the annual-average melt during the periods when the ice was ungrounded.”

P. 12-13, Section 4.1.2: Should at least part of this be in the Results section?

While the thinning plots contain some model results, because the results section focuses on the effect of input parameters on model output as opposed to comparison with data, we would like to leave this section in the discussion. Moving it to the results would require breaking it up amongst a number of different sections and lose the coherence of a single discussion of thinning rates.

P. 13, lines 423-425: It looks like the SSA simulations thin too little for all three glaciers upstream of their grounding lines.

This is perhaps a question of what “reasonably well” means, so we have eliminated that phrasing and incorporated this point. The relevant text now reads: “In general, the shallow-shelf simulations approximately match the pattern of observed surface change downstream of the grounding line, but show too little thinning upstream (Error! Reference source not found.b-d).”

Figure 2: You say “shelf total melt rates are most sensitive to melt rates between ~250 and 600 meters.” Why not choose two depths where the PDF values are equal, e.g. ~250 and ~800m?

Yes, this is probably more appropriate. It has been changed to “between ~250 and 800m” where the PDF values are approximately 0.014.

Table 1: Simulation number 8 has an asterisk indicating that the retreat was entirely forced, but in Figure 5 we can see that the retreat continues beyond the 18y grounding line for Smith glacier.

It was not our intention for the asterisk to indicate that, but we see how that was unclear from the table caption. We have added an additional note in the table on the simulations that continued retreating beyond the period of explicit forcing. The caption now indicates “The last column indicates whether the Smith Glacier grounding line retreated over 15 km within the simulation, with starred entries indicating that retreat was explicitly forced. Daggers indicate that some grounding-line retreat continued beyond the period of explicit forcing.”

Figure 4: The important first 5 years of grounding line retreat are covered by the plot labels for Smith and Kohler glaciers. Similar for Figure 5.

Labels have been moved on both figures.

Technical Corrections

P. 2, lines 49-50: I found this wording confusing – it sounds like “committed” is a verb. Maybe reword it?

Changed to “Modeling of the grounded portion of the Smith, Pope, Kohler catchment indicates that these glaciers are committed to further retreat on decadal timescales”

P. 4, line 121: “allows us to”

Fixed

P. 5, line 155: "We ran a suite"

Fixed

P. 6, line 178: I think this should say something like "...errors due to the assumption are alleviated through choice of the sliding coefficient..."

This alternative phrasing is a bit overly optimistic. We are confident that there is compensation, but whether that results in a model that is closer to reality is not clear.

P. 7, line 232: Perhaps a matter of taste, but I like the word "margins" more than "edge." Edge makes me think of the calving front.

Changed

P. 8, line 279: 20011 → 2011

Fixed

P. 10, line 321: should say "...using all four melt distributions...?"

Fixed

P. 10, line 329: I think the referral to Figure 6 is repetitive, given that the whole paragraph is referring to the figure. You could make it a referral to Figures 6c-d if you want to be specific.

Switched to 6c-d

P. 11, line 374: mix → mixes

Fixed

P. 11, line 379: instantiate → induce (or trigger)?

Changed to "induce"

P. 12, line 391: "simulations with marginal"

Fixed

P. 12, line 401: indicate → indicates

Fixed

P. 12, line 405: 19 → 21

Good catch, fixed

P. 14, line 458: across → along?

Fixed

P. 14, line 463: "There is a variety..."

Fixed the missing “a”, but left the verb as “are” since both “is” and “are” are grammatical here.

P. 14, line 470: complicate → complicates
Fixed

P. 14, lines 482-483: The way this is worded makes it sound like it was the SSA simulations that required HPC. Maybe say “... allowing the use of local workstations rather than requiring high-performance computing resources.”
Indeed, this phrasing is much clearer.

P. 15, line 509: have → “has” or “may have”
Fixed

P. 15, line 528: “not be an indication” ?
Changed to “not indicate”

P. 16, line 531: “we did not have” Figure 1: I assume there should be a box showing the study area on the map of Antarctica – I can’t see one on my printed copy.
Yes, thank you. There seems to have been an error in PDF conversion that we did not catch.

Figure 3, line 759: “thick for 1Obs, thin for 2Obs.”
Fixed

Figure 5, line 779: double periods
Fixed

Figure 5, line 782-782: “Color of the line indicates year” already stated in line 781.
Thanks, fixed.

Figure 6: Axis labels are overlapping for 6a and 6c.
Fixed.

Figure 6, line 790: “difference...result” → “difference . . . results” or “differences . . . result”
Corrected to “differences . . . result”

Melt at grounding line controls observed and future retreat of Smith, Pope, and Kohler Glaciers

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Abstract

Smith, Pope, and Kohler Glaciers and the corresponding Crosson and Dotson Ice Shelves have undergone speedup, thinning, and rapid grounding-line retreat in recent years, leaving them in a state likely conducive to future retreat. We conducted a suite of numerical model simulations of these glaciers and compared the results to observations to determine the processes controlling their recent evolution. The model simulations indicate that the state of these glaciers in the 1990s was not inherently unstable, i.e. that small perturbations to the grounding line would not necessarily have caused the large retreat that has been observed. Instead, sustained, elevated melt at the grounding line was needed to cause the observed retreat. Weakening of the margins of Crosson Ice Shelf may have hastened the onset of grounding-line retreat but is unlikely to have initiated these rapid changes without an accompanying increase in melt. In the simulations that most closely match the observed thinning, speedup, and retreat, modeled grounding-line retreat and ice loss continue unabated throughout the 21st century, and subsequent retreat along Smith Glacier's trough appears likely. Given the rapid progression of grounding-line retreat in the model simulations, thinning associated with the retreat of Smith Glacier may reach the ice divide and undermine a portion of the Thwaites catchment as quickly as changes initiated at the Thwaites terminus.

1 Introduction

Glaciers along the Amundsen Sea Embayment (ASE) have long been thought to be vulnerable to catastrophic retreat (Hughes, 1981), and the major ice streams in the region have recently undergone significant speedup and grounding-line retreat (Mouginot et al., 2014; Rignot et al., 2014; Scheuchl et al., 2016). Largely due to synchronicity between variability in ocean temperature and glacier response, ocean-induced melting is thought to be the primary driver of these changes (Jenkins et al., 2010; Joughin et al., 2012). Oceanographic observations (Assmann et al., 2013) and modeling (Thoma et al., 2008) indicate that variable transport of warm circumpolar deep water (CDW) onto the continental shelf has caused ~~substantial~~ variability in sub-shelf melt over the past two decades, with melt thought to have ~~temporarily peaked in the early 2010s~~ (Jenkins et al., 2018). Melt rates influence the large-scale flow of ice streams by affecting ice-shelf thickness; thinner ice shelves provide less buttressing to ice upstream, and ice is forced to flow faster to increase strain-rate dependent stresses in the ice. Ice-flow modeling (e.g., Joughin et al., 2014) and glaciological observations (e.g., Rignot et al., 2014) suggest that the retreat of Thwaites and perhaps Pine Island

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36 Glacier, the largest glaciers along the ASE, will continue under all realistic melt scenarios (Favier et al., 2014; Joughin
37 et al., 2010).

38

39 Despite their lower ice discharge relative to Thwaites and Pine Island Glaciers, Smith, Pope and Kohler Glaciers (see
40 Figure 1 for an overview of the area) have gained attention as some of the most rapidly changing outlets along the
41 Amundsen Sea Embayment (Mouginot et al., 2014). These glaciers, and the Crosson and Dotson Ice Shelves
42 downstream, have undergone >30 km of grounding-line retreat in recent decades (Rignot et al., 2014; Scheuchl et al.,
43 2016), leaving their grounding lines positioned more than 1 km below sea level, where they are vulnerable to warm
44 ocean waters (Jenkins et al., 2018; Thoma et al., 2008). By contrast, the Thwaites grounding line sits approximately
45 50 km downstream of the deepest portions of its basin (Rignot et al., 2014) and the Pine Island grounding line has
46 held a steady position on the retrograde slope at the seaward end of its overdeepening from 2009-2015 (Joughin et al.,
47 2016). Thus, the positioning of Smith Glacier's grounding line in the deep portion of its trough suggests that it is in a
48 more advanced stage of retreat than its larger neighbors. Indeed, Smith Glacier comprises one of the most extensive
49 instances of modern glacier retreat and can serve as an important example of a marine ice-sheet basin in an advanced
50 state of collapse.

51

52 Modeling of the grounded portion of the Smith, Pope, Kohler catchment indicates that these glaciers are committed
53 to further retreat on decadal timescales (Goldberg et al., 2015). However, this modeling was focused on transient
54 calibration and did not assess causes of retreat or examine likely changes over periods longer than 30 years. Additional
55 modeling work shows that the ice-shelf response is highly sensitive to the sub-shelf melt rates, which, when
56 determined from an ocean model, are in turn highly dependent on how well the bathymetry is resolved (Goldberg et
57 al., 2019). Regardless of the initial cause of retreat, the ice shelves are unsustainable at present melt rates, and Dotson
58 Ice Shelf may melt through in the next 50 years (Gourmelen et al., 2017). The ice presently within the Smith, Pope,
59 Kohler drainage could raise global mean sea level by a relatively modest 6 cm (Fretwell et al., 2012), but thinning can
60 lead to drainage capture and therefore increased loss of ice volume. Thus, due to a shared divide, rapid thinning could
61 potentially hasten the collapse of the larger reservoir of ice in the neighboring Thwaites catchment.

62

63 Although there is evidence of increased transport of warm ocean waters beneath these ice shelves, the complex nature
64 of ice-sheet dynamics involves the responses to past and present forcing. Present observations represent a combination
65 of adjustment to past imbalance and response to recent melt (e.g., Jenkins et al., 2018). In the case of Smith, Pope,
66 and Kohler Glaciers, multiple lines of evidence suggest that retreat began before widespread satellite observations
67 were first acquired (Gourmelen et al., 2017; Konrad et al., 2017; Lilien et al., 2018), though the exact cause and timing
68 of retreat initiation are unknown. Separating the effects of different forcings is key to understanding the extent to
69 which continued forcing is required to sustain retreat. Since future forcing is uncertain, identifying whether retreat is
70 inevitable within the expected range of ocean warming is particularly valuable. Because of the short length of the
71 satellite record, separating the compounded influence of the possible drivers of retreat is difficult with observations

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alone, and numerical ice-flow models are an important tool for identifying plausible scenarios that could have resulted in the observed changes to ice thickness, velocity, and grounding-line position.

Here, we describe a suite of model simulations designed to investigate which processes control the ongoing retreat of Smith, Pope, and Kohler Glaciers. Our modeling experiments tested the effects of melt distribution, melt intensity, basal resistance, and marginal buttressing on speedup, thinning, and grounding-line position. We compared these modeled changes to remotely sensed observations in order to determine which processes have driven retreat over the last two decades. After comparing the modeled velocity, surface elevation, and grounding-line position to observations, we ran a subset of the simulations for a longer duration to investigate the sensitivity of the future evolution of this system to a range of forcing.

Simulations of Antarctic ice streams generally require a melt forcing to determine the mass balance of the bottom of the ice shelves. Spatially well-resolved sub-shelf melt rates have only recently been measured for ice shelves in the ASE (Gourmelen et al., 2017; Shean et al., 2017), and these observations are limited by their brief record and low temporal resolution. Thus, use of these high-resolution melt rates as inputs to prognostic ice-flow models that extend further into the past or into the future requires extrapolation. To avoid such extrapolation, models are usually forced with simple, often solely depth-dependent, parameterizations of melt (e.g., Favier et al., 2014; Joughin et al., 2010). Significant progress has been made in coupling state-of-the-art ice and ocean models (e.g., De Rydt and Gudmundsson, 2016; Jordan et al., 2018), though to our knowledge only one study has applied a fully coupled model with moving grounding line to the geometry of a real glacier (Seroussi et al., 2017). Coupled simulations capture spatial and temporal variability in melt rates but require substantial high-performance computing resources. Moreover, modeled sub-shelf melt rates are highly sensitive to the sub-shelf bathymetry (Goldberg et al., 2019), which is difficult to measure or infer due to the ice and ocean cover. Because these coupled ice-ocean models require additional development and substantial high-performance computing resources, and are sensitive to uncertain bathymetry, they are not yet readily available for assessing sensitivity to a suite of forcings.

While ocean forcing is thought to be the primary driver of retreat along the ASE, a glacier's sensitivity to sub-shelf melt is modulated by additional processes. Grounding-line retreat exposes additional and, for a retrograde bed, deeper sub-shelf area to melt, potentially increasing the integrated melt rate without any change in ocean heat content (De Rydt et al., 2014). Additionally, ungrounding on a retrograde bed causes ice-flow speeds to increase due to the nonlinear dependence of ice velocity on ice thickness. These feedbacks cause some grounding-line positions to be inherently unstable, such that upstream perturbations to those grounding-line positions can lead to self-sustaining retreat (e.g., Schoof, 2007). Changes to the effective viscosity of ice shelves, such as weakening from mechanical damage, fabric development, or higher ice temperatures, can reduce the shelf's ability to transmit stresses and thus reduce buttressing in the same manner as a decrease in the shelf's cross sectional area (e.g., Borstad et al., 2016). Observations (Macgregor et al., 2012) and inverse modeling (Lilien et al., 2018) suggest that changes to viscosity have indeed played a role in the speedup of Crosson Ice Shelf, and model sensitivity studies suggests that weakening

111 of several key regions of the ice shelves, particularly the shear margins or near the grounding line, would significantly
112 alter ice discharge (Goldberg et al., 2016, 2019). While some other processes, such as loss of terminal buttressing due
113 to retreat of the neighboring Haynes Glacier, may have destabilized Crosson Ice Shelf, changes to melt, marginal
114 weakening, and feedbacks between ungrounding and increased ice-flow speeds represent the most likely drivers of
115 retreat in this system.

116 2 Methods

117 We conducted a suite of prognostic numerical model simulations of Smith, Pope, and Kohler Glaciers, primarily using
118 a shallow-shelf (SSA) model implemented in the finite element software package Elmer/Ice (Gagliardini et al., 2013;
119 Zwinger et al., 2007). The shallow-shelf equations describe ice flow in two dimensions under the assumptions that the
120 ice is thin relative to its extent and that ice velocity is uniform with depth (i.e., the model is depth-averaged); while a
121 simplification, these assumptions are generally applicable to ice streams (MacAyeal, 1989) and have been applied to
122 other glaciers in the ASE (e.g., Favier et al., 2014; Joughin et al., 2014). To validate the use of these simplified ice
123 physics, we performed one simulation using a state-of-the-art full-Stokes (FS) ice-flow model, also implemented in
124 Elmer/Ice. In slower flowing regions where our inversion results show that internal deformation comprises a
125 significant portion of motion, incorporating the variation of velocity with depth may be important. The full-Stokes
126 simulation allows us to identify potential drawbacks of applying the simplified shallow-shelf model to this particular
127 system of glaciers.

128 2.1 Model setup

129 The model domain extended from the ice divide (determined from the measured velocity field) to the seaward edge
130 of the ice shelves' embayment (see Figure 1 for the extent of the domain). For all simulations, the horizontal mesh
131 resolution was 300 m near the grounding line and 3 km elsewhere. The full-Stokes domain was extruded to 9 vertical
132 layers, with 5 layers concentrated in the bottom third of the ice, giving an effective resolution of 20 to 500 m depending
133 on ice thickness and depth within the ice column. This resolution is generally considered sufficient to accurately
134 capture grounding-line dynamics (Pattyn et al., 2013), and sensitivity to mesh resolution is explored further in the
135 supplementary materials. The upper ice surface at initialization was found by adjusting a high-quality reference digital
136 elevation model (DEM) mosaic, derived from WorldView/GeoEye stereo imagery, to match expected conditions in
137 1996. This adjustment used thinning rates found from ICESat-1, the Airborne Topographic Mapper from NASA's
138 Operation IceBridge, and WorldView/GeoEye stereo DEMs (further description of the determination of this surface
139 can be found in Lilien et al., 2018). The bed elevations were determined from all publicly available airborne radio
140 echo sounding data, anisotropically interpolated to 1-km posting so as to weight measurements along flow more
141 heavily than those across flow; details can be found in Medley et al. (2014) and the supplementary materials to Joughin
142 et al. (2014). The advantage to this method of interpolation is that it is free of assumptions related to a particular state
143 of mass balance, unlike mass-conservation methods. The lower ice surface was then determined using the bed
144 elevations beneath grounded ice and using an assumption of hydrostatic equilibrium downstream of the 1996

Deleted: 1996 calving front. For the majority of

146 grounding line. Firn-air content for the hydrostatic calculation was found by comparing coincident ice-thickness and
147 surface-elevation measurements over the ice shelves (supplementary materials of Lilien et al., 2018).

148

149 All model simulations were initialized to best match the transient state of these ice streams in 1996, the earliest year
150 with relatively complete maps of ice velocity in this area. The velocity measurements were acquired by
151 the European Remote-Sensing Satellites (ERS-1 and 2) and processed using a combination of interferometry and
152 speckle tracking (Joughin, 2002). Model initialization consisted of an iterative process using a full-Stokes,
153 diagnostic thermomechanical model in Elmer/Ice. We iterated between updating the temperature field and using
154 inverse procedures to infer the basal shear stress of grounded ice and the enhancement factors over floating ice.

155 These inferred fields minimized the misfit between modeled velocity and the measurements from 1996, (this initial
156 set of inversions is also described in Lilien et. al, 2018, where plots of the inferred enhancement are shown). In order
157 to minimize transient effects of data errors while capturing the real transient state of these ice streams in 1996, the
158 model was briefly relaxed by running forward in time for one year under constant forcing, and with the grounding-
159 line fixed in place. Then, the inversions were repeated to infer the final inputs for the forward model. Further details
160 of inversion procedures, temperature initialization, and relaxation are provided in supplementary materials.

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162 While it is difficult to assess whether the model accurately represents the true temperature, enhancement, and basal
163 slipperiness fields, modeled thinning rates at the end of relaxation give an indication of model self-consistency.
164 Conversely, the total change in surface height during relaxation gives a misfit between the model and available data
165 (though in part that relaxation may be compensating for errors in the data). Here, relaxation resulted in local changes
166 of up to 100 m near Kohler Glacier's grounding line and changes of at most 50 m elsewhere. While most of the
167 change during relaxation can potentially be attributed to errors in ice thickness caused by uncertainty in the bed
168 elevation, the large change on Kohler likely indicates that the surface elevations were also incorrect in that area.
169 Because determining the surface elevations at initialization required some extrapolation using longer term thinning
170 rates (see Lilien et al., 2018 for details), this misfit is not surprising and may reflect a change in the spatial pattern of
171 thinning during 1996-2003. At the end of the relaxation, thickness change rates were reduced to $<10 \text{ m a}^{-1}$, which is
172 smaller than the observed rate of thickness change, except on Kohler Glacier where $\sim 30 \text{ m a}^{-1}$ of thickening
173 persisted. While this is still a large rate of elevation change on Kohler, we were forced to choose between accepting
174 Kohler's unrealistic imbalance and possibly relaxing away the real imbalance on Smith and Pope. The potential
175 effects of the resultant transients upon the modeled retreat of Kohler are revisited in Section 4.3.1.

176 2.2 Prognostic simulations

177 We ran a suite of more than 20 ice-flow model simulations for at least 23 years, all beginning in model-year 1996.
178 These relatively brief simulations enabled comparison with observations, and 6 of these simulations were subsequently
179 run over 100 years to investigate the future evolution of these glaciers. Those 6 simulations were selected after the
180 full suite of shorter runs and were chosen to represent a range of retreat rates, some realistic and some slower than
181 observed, but all using realistic melt rates. Table 1 summarizes the inputs for all model runs, indicating the model

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physics, run length, melt distribution and intensity, and any other forcing as described below. In all model simulations, time stepping used a backwards-difference formula with timestep size of 0.05 years. Calving was not explicitly modeled, but instead ocean pressure was applied on the downstream boundary at the mouth of the ice shelves' embayments where ice is allowed to flow out. This boundary condition would remain accurate for an advance since ice tongues extending beyond embayment walls do not provide additional back stress, but, if substantial ice loss caused the calving front to retreat behind the embayment walls, it could potentially result in an underestimate of ice loss during retreat.

Most of the model simulations used a Coulomb-type sliding law proposed by Schoof (2005) and Gagliardini et al. (2007), which takes the form

$$\tau_b = CN \left(\frac{\chi u_b^m}{1 + \chi} \right)^{\frac{1}{m}} u_b \quad \text{Equation 1}$$

where τ_b is the basal shear stress, u_b the basal velocity, N the effective pressure, C proportional to the maximum bed slope, m the sliding law exponent, and $\chi = \frac{u_b}{C^m N^m A_c}$, where A_c is a coefficient that is determined using the inversion results. This sliding law was derived to represent sliding over a rigid bed with cavitation behind obstacles, but its high- and low-pressure limits make it suitable for describing Antarctic ice streams. At high effective pressure, generally found in slow-flowing regions that may be underlain by hard beds, the sliding law approximates Weertman (1957) sliding ($\tau_b \propto u_b^m$). At low effective pressures, this Equation 1 approaches Coulomb-type sliding ($\tau_b \propto CN$), which is thought to be appropriate for sliding over soft beds (e.g., Iverson et al., 1998; Tulaczyk et al., 2000) and hard beds where fast-sliding with cavitation takes place (Schoof, 2005). We take $m = 3$, and assume that the effective pressure is equal to the ice overburden minus the hydrostatic pressure. With this assumption, Coulomb-like behavior only occurs within several kilometers of the grounding line, with Weertman-like behavior farther inland (Joughin et al., 2019). This assumption is valid for infinite hydraulic conductivity, but realistic, finite hydraulic conductivity would cause higher water pressures inland, which would lead to this parameterization underestimating the extent of Coulomb-like behavior. However, this assumption is often employed (e.g., Morlighem et al., 2010), and because coupling to a hydrologic model is beyond the scope of this study, we retain the assumption here. To some extent, errors in the assumption compensated for in the solution for the sliding coefficient, C , though it may introduce errors as the basal shear stress is reduced too drastically in response to inland thinning. For comparison, we ran four additional simulations with a commonly used Weertman-type sliding law ($\tau_b = A_w u_b^m$), with A_w calculated from the same inversion results, again with $m = 3$.

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2.2.1 Melt sensitivity experiments

We explored the effect of a variety of plausible melt forcings on the evolution of Smith, Pope, and Kohler Glaciers. The forcings can be separated into melt intensity (i.e. shelf-integrated melt) and its spatial distribution; simulations were conducted varying the melt intensity and distribution independently to determine their relative importance in

controlling retreat. Because of their low computational expense, we used simple prescriptions of melt: three depth-dependent parameterizations (Favier et al., 2014; Joughin et al., 2010; Shean, 2016), all tuned to fit the melt-depth relationship of nearby Pine Island Glacier, and an interpolation from previously published high-resolution melt-rate estimates inferred from Cryosat-2 by assuming hydrostatic equilibrium (Gourmelen et al., 2017), which was extended to cover both ice shelves. Hereafter, we refer to these melt distributions as F2014, J2010, S2016, and Cryo2, respectively. The parameterizations are intended to span a reasonable range of likely melt distributions, and none of them were expected to match the Cryosat-inferred pattern of melt exactly. Any depth-dependent parameterization will fail to span the range of melt rates observed at a given depth. However, the depth-dependent parameterizations capture the general form of the Cryo2-inferred melt rates, despite not having been tuned to Crosson and Dotson Ice Shelves (Figure 2).

Melt rates inferred from Cryosat 2 are limited to areas that were floating during the period of 2010-2016, which potentially complicates forcing the model with the Cryo2 distribution. If additional area beyond what was afloat in 2016 were to unground in a model simulation, some extrapolation would be needed to apply a melt forcing to that area. For the minor extrapolation that was necessitated by the retreat in these simulations, we first smoothed the melt rates to 2-km resolution then used nearest-neighbor interpolation to extend the rates inland. However, during the first 25 years of the model simulations, these extrapolated values were not required, so the limited extent of the inferred melt rates does not affect comparison between modeled and observed retreat.

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During each timestep from model years 1996-2014, each melt distribution was re-scaled to match the time-varying shelf-total melt rate, as derived from flux divergence. Note that this scheme differs from prior studies (Favier et al., 2014; Joughin et al., 2010, 2014) that instead fix the parameterization for a particular run and accept the resulting temporal variation in melt rate as the depth of shelf's underside evolves. Comparative advantages and disadvantages of our approach are discussed in detail in section 4.4.2, but this choice was mainly made to limit melt rates to realistic values during the period with observations. The melt intensity was determined by linear interpolation between available measurements of shelf-total melt obtained from flux divergence measurements through time (Lilien et al., 2018). In general, this scheme requires adjusting the depth-dependent parameterizations down from the "1x" versions by a factor of 4-5; such scaling is unsurprising given the large differences between the Dotson and Crosson cavities and the Pine Island Glacier cavity for which the parameterizations were originally tuned. Though the Cryo2 rates agree to within errors with the flux divergence estimates over Dotson during 2010-2014 (Lilien et al., 2018), the forcing was scaled down by ~20% at the start of the simulations to match the relatively low melt rates in 1996. Through the simulations, the scaling factor for melt was generally increased to force the observed increases in melt. For the depth-dependent parameterizations, this increase was compounded by the need to compensate for the rapid decrease of ice-shelf draft due to intense melt at depth, which can result in the shelves "shallowing out" of high melt rates over most of their area. Thus, the scaling through time varied significantly based upon how quickly the ice-shelf draft shallowed and how much new area became exposed to the ocean and contributed to the shelf-total melt rate. After 2014, when melt-rate estimates are no longer available, the scaling was fixed to the value determined for 2014 and the

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Deleted: In general, this scheme requires adjusting the depth-dependent parameterizations down from the "1x" versions by a factor of 4-5, and the Cryo2 rates down by 20%, in order to match the relatively low melt rates 1996; such scaling is unsurprising given the large differences between the Dotson and Crosson cavities and the Pine Island Glacier cavity for which the parameterizations were originally tuned.

270 total melt rate was allowed to vary as in previous studies. For partially floating elements, melt was applied only over
271 the floating portion, and the model resolution employed avoided significant sensitivity to this choice (Seroussi and
272 Morlighem, 2018).

273

274 We also conducted simulations changing melt intensity to twice that observed (simulations 3, 11, 18, and 25 in Table
275 1). To vary the melt intensity, we again rescaled the parameterization at every timestep through 2014 in order to force
276 the total melt rate to match twice the observations. To distinguish these from what previous authors refer to as “1x”,
277 “2x”, and “4x”, we instead refer to the different intensities as “1Obs” and “2Obs”. It is important to note that in the
278 prior studies, “Nx” referred to scaling of the parameters, which, due to shallowing of the ice-shelf draft, could lead to
279 substantially less melt than N times the observations. Our scaling ensures that during the period of observations, 2Obs
280 actually doubled the shelf-wide integrated melt.

281 2.2.2 Marginal weakening experiments

282 We manually masked the areas within 10 km of the margins of Crosson and Dotson Ice Shelves and applied an ad-
283 hoc change to the depth-averaged enhancement factor over these areas to test the model’s sensitivity to marginal
284 weakening. These runs were conducted using the shallow-shelf model and used an enhancement factor of 4 (a 44%
285 reduction in B) to weaken the margins. These weakening experiments were done with all four melt distributions at
286 1Obs melt intensity. One additional simulation was run with an enhancement factor of 1.8 (a 17% reduction in B)
287 using the J2010 melt parameterization at 1Obs intensity (simulation 5 in Table 1). In order to test the effect of marginal
288 weakening in the absence of any increase in melt, an additional set of simulations were conducted fixing the melt
289 parameterization to its 1996 scaling and applying the enhancement factor of 4; these simulations again used each of
290 the four melt distributions at 1Obs intensity (simulations 4, 12, 19, and 26 in Table 1). We refer to these experiments
291 with weakened margins but fixed melt parameterization as “control melt” simulations (simulations 6, 13, 20, and 27
292 in Table 1).

293 2.2.3 Forced ungrounding experiments

294 Since model simulations cannot be expected to perfectly replicate observed grounding-line retreat, we ran an
295 additional suite of experiments to test the effect of the ungrounding itself on thinning and speedup. These simulations
296 allow us to assess whether feedbacks between ungrounding, thinning, and speedup may have caused the observed
297 retreat, and to separate errors in modeled grounding-line retreat rates from their effects on ice-flow speed and thinning.
298 To estimate the grounding-line position at times between the three available measurements (1996, 2011, and 2014),
299 we linearly interpolated the time of ungrounding along a suite of flowlines spaced approximately every kilometer
300 across flow, creating maps of the grounded area every 0.1 years. At each model timestep through a forcing period
301 (1996-2001 or 1996-2014 depending on the simulation), the grounding-line position was set to match the nearest
302 grounding map, without changing the ice geometry, (i.e. the basal shear stress was set to zero and melt was applied
303 under ungrounded area). We only forced retreat and not the re-advance of Kohler between 2011 and 2014 since forcing
304 re-advance is complicated by the changing geometry after the ice goes afloat. After the period of forced ungrounding

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306 finished, the grounding line was allowed to retreat freely based upon hydrostatic equilibrium. Simulations were
307 conducted with all four melt distributions at 1Obs intensity and with both 5 and 18 years of forced ungrounding
308 (simulations 7-8, 14-15, 21-22, 28-29 in Table 1).

309 3 Results

310 Model outputs are composed of the spatio-temporal evolution of a number of variables, notably ice velocity, ice
311 thickness, and grounding-line position. To distill this many-dimensional output into a manageable format, we focus
312 on comparing the changes to grounding-line position and ice-surface speeds along the centerlines of the three main
313 outlet glaciers under various forcings.

314 3.1 Melt variability

315 Figure 3 shows the results of the eight experiments designed to evaluate the melt intensity and distribution
316 (experiments 1-3, 10-11, 17-18, and 24-25 in Table 1). Collectively, the results show that grounding-line position and
317 the pattern of thinning are highly sensitive to the spatial distribution of melt. For the 1Obs experiments, there is <10
318 km of grounding-line retreat in the shallow-shelf simulations, and the retreat that does occur happens after model year
319 25. Amongst the 1Obs shallow-shelf simulations, only the one with J2010 melt shows more than 2 km of retreat,
320 during which time Smith Glacier's grounding line retreats by ~9 km. The full-Stokes simulation with 1Obs, however,
321 shows substantial (30 km) retreat along Smith Glacier during that time, in relatively good agreement with the
322 observations.

323
324 Over the first 25 years, retreat in the shallow-shelf models is generally confined to simulations with the 2Obs melt
325 forcing and is greatest with parameterizations that concentrate melt at depth. While the timing of retreat onset varies
326 with melt forcing, the 2Obs parameterizations generally yield similar retreat along Smith and Kohler glaciers (see
327 [observed change from 1996 to 2011 in Figure 3f](#)). An exception is the Cryo2 melt, which consistently produces the
328 least retreat. For Pope glacier with 2Obs forcing, the extent of the retreat varies greatly with melt distribution, ranging
329 from 0 to 18 km compared to the observed ~10-km retreat. Along Smith and Kohler Glaciers, simulations with the
330 J2010 distribution retreat most rapidly, followed by S2016, F2014, and Cryo2. Melt rates near the grounding line need
331 to reach some threshold before retreat commences; in the shallow-shelf model of Smith Glacier, retreat of the
332 grounding line does not begin unless melt rates of ~100 m a⁻¹ or higher are reached near the grounding line. Retreat
333 commences more easily in the full-Stokes model, requiring only ~50 m a⁻¹ of melt. The grounding-line retreat rate of
334 Pope Glacier, which has a slightly shallower (~750 m.b.s.l.) grounding line, has a less direct relationship with melt
335 distribution. While retreat initiates most quickly with the J2010 parameterization, it is eventually overtaken by retreat
336 with the S2016 and F2014 parameterizations (Figure 3c).

337 3.2 Marginal weakening

338 We ran nine simulations with weakened margins, and all displayed notable differences in grounding-line position and
339 speedup compared to the simulations with no weakening. Figure 4 shows the effects of weakening on grounding-line

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347 retreat and ice-flow speedup. The grounding-line positions of Smith and Pope Glaciers are sensitive to the shelf
 348 viscosity. With the J2010 melt parameterization, the retreat for Smith Glacier initiates ~10 years sooner with
 349 enhancement of 4 in the margins (Figure 4a-b). While this lag can lead to substantial differences in grounding-line
 350 position at any given time, the simulations with full-strength margins generally continue to retreat and reach that same
 351 state 10 years later. The notable exception is the simulation with the S2016 melt, which shows >10 km more
 352 grounding-line retreat when the margins are weakened (Figure 4a). Kohler Glacier's grounding line also retreats
 353 sooner with enhanced margins, but as retreat progresses grounding-line position does not differ by more than ~2 km
 354 from the unweakened case (Figure 4c). In the case of the S2016, F2014, and Cryo2 melt forcings, within 50 years,
 355 weakening of the margins causes grounding-line retreat on Pope and Kohler glaciers that did not take place even in
 356 100 years without marginal weakening (Figure 4a and c). Simulations with enhancement of 1.8 display approximately
 357 half as much change in the timing of retreat as an enhancement of 4 does (not shown). Effects of marginal strength on
 358 ice speeds differ markedly between the two ice shelves; Crosson/ Pope flows almost 50% faster in some regions
 359 (Figure 4d-e) when the margins are weakened while Dotson/Kohler speeds are nearly insensitive to the strength of the
 360 margins (Figure 4f).

361
 362 Although some of the simulations with weakened margins show more retreat, these simulations all are forced using
 363 the 1Obs melt intensity and thus incorporate the increases in melt observed between 1996 and 2014. In the "control
 364 melt" simulations with weakening but with the melt parameterization fixed at 1996 values, there is only minor
 365 grounding-line retreat over the 50-year duration of the simulations. If the weakening alone were sufficient to cause
 366 grounding-line retreat, we would expect to have seen retreat in these simulations.

367 3.3 Forced ungrounding

368 Figure 5 shows the results of the simulations in which the grounding line was forced to migrate at the rate observed.
 369 The forced ungrounding had differing effects depending on the melt distribution, and in some cases no subsequent
 370 grounding-line retreat ensued after the period of imposed ungrounding. In simulations with the 5-year forced
 371 ungrounding, the grounding line is able to stabilize temporarily (Figure 5a-c), though retreat subsequently ensues on
 372 Smith Glacier for the melt distributions that concentrate melt at depth (J2010, S2016). Ice-flow speeds on Pope and
 373 Kohler glaciers are relatively unaffected by the forced 5-year grounding-line retreat, but when forced through 2014
 374 (18 years) they display some speedup as well (Figure 5d and f). In the case of Smith Glacier, the effect of exposing
 375 additional area to melt and decreasing basal resistance results in substantial speedup near the grounding line that
 376 continued over 25 years following the period of forced ungrounding. For the 18-year forced-ungrounding simulations,
 377 little grounding-line retreat occurs on any of the glaciers in the subsequent 25 years, leaving the grounding lines within
 378 5 km of their 2014 positions.

379 3.4 Longer term simulations

380 Figure 6 shows the evolution of the ice volume and grounding-line position for the centennial-scale simulations,
 381 displaying sustained loss of ice volume through 2100 CE. These six simulations (simulations 2, 4, 10, 17, 19, 24 in

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Table 1) were simply extensions of model runs mentioned above, chosen to represent a range of retreat scenarios with realistic melt intensity; four used the different melt distributions at 1Obs intensity and no marginal weakening while two used the J2010 and S2016 melt distribution at 1Obs intensity with marginal weakening. Simulations with marginal weakening and/or the J2010 melt parameterization show continuing grounding-line retreat throughout the simulation (Figure 6c-d). In simulations with substantial (>50 km) of retreat, the grounding line of Smith Glacier eventually extends upstream of Kohler, and the grounding lines of these two glaciers merge. Even in these simulations with the most retreat, melt rates remain below 75 Gt a⁻¹ (within 25% of 2014 levels) for most of the 21st century before gradually increasing to 120 Gt a⁻¹ between 2080 and 2100, as more deep ice is exposed to melt. With these relatively modest melt rates, the overall contribution to sea-level rise still ranges from 6–to–10 mm by 2100 and Smith Glacier’s grounding line retreats by >80 km in the simulations with J2010 melt distribution. Despite continued loss of ice volume, substantial grounding-line retreat never initiates when using the F2014, S2016, or Cryo2 melt distributions with 1Obs intensity. Even in these simulations with little retreat, contributions to sea level exceed 2 mm by 2100.

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4 Discussion

We first evaluate how different parameter choices in the model affect its ability to reproduce the extensive grounding-line retreat between 1996 and 2014, then consider the implications for the future retreat of the system. We then discuss how model simulations compare to the observations of ice-flow speed and thinning from 1996–2018, and evaluate how necessarily subjective modeling choices may have affected these results.

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4.1 Conditions needed to match observed grounding-line retreat

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Here we assess how different model forcings affect the

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Deleted: <#>Grounding-line position

The extensive, observed 30-km retreat (Rignot et al., 2014; Scheuchl et al., 2016) provides a simple metric for whether model simulations match the data. Along the Smith centerline, the bed depth remains at around 1 km b.s.l. for the first 10 km upstream from the grounding line before deepening to close to 2 km b.s.l. over the following ~10 km (Figure 3f), and in many simulations the grounding line never retreats off this relatively flat, shallow portion of the bed. This geometry leads to an essentially bimodal distribution of grounding-line position along the Smith glacier centerline. Model simulations where the retreat reaches the retrograde slope past 10 km all reach >20 km of grounding-line retreat (Figure 3c). While only the full-Stokes simulation matches the timing of the observed retreat under 1Obs melt intensity, the stepped pattern of retreat is similar regardless of model physics (discussed more in Section 4.4.1). We partition the simulations into those that display 15 km or more grounding-line retreat on Smith glacier, regardless of the timing, and those that do not; those that display this large retreat are considered generally good matches to the observed grounding-line positions where ~30-km of retreat was observed. The simulations that matched this large retreat were: those with the J2010 melt parameterization with 1Obs or 2Obs melt, irrespective of marginal weakening; those with the S2016 or F2014 parameterization and 2Obs melt; and the simulation with the S2016 parameterization, 1Obs melt, and marginal enhancement of 4 (Table 1).

We find that grounding-line position is controlled by a combination of melt distribution, melt intensity, and marginal weakening, though melt near the grounding line (a product of melt distribution and intensity) is the primary driver of

438 retreat. This result confirms the conclusion of previous work that has also highlighted the importance of the melt
 439 distribution for determining ice-shelf stability (Gagliardini et al., 2010; Goldberg et al., 2019; Seroussi and Morlighem,
 440 2018). To match the observed grounding-line retreat using realistic (10Obs) melt intensity, the models suggest that melt
 441 must have been concentrated near the grounding line. Concentrated melt at depth is expected given that the warm,
 442 CDW which drives melt generally intrudes at depth (e.g., Jacobs et al., 2012). However, without elevated melt
 443 intensity (relative to 1996) or greater concentration of melt at the grounding line than considered by our melt forcings,
 444 the “control melt” simulations show that the modeled grounding-line positions of Smith, Pope, and Kohler glaciers
 445 would have remained stable for the 50 years following 1996.

447 The stable grounding-line position found by forcing the model with Cryo2 melt (Gourmelen et al., 2017) may result
 448 from underestimation of melt near the grounding line in 1996, either due to the difficulty of using satellite altimetry
 449 to infer melt rates in an area not in hydrostatic equilibrium (Fricker and Padman, 2006; Rignot, 1998), or due to a
 450 change in distribution of melt between 1996 and 2010. Since melt rates were inferred over 2010-2016, if melt were
 451 highest near the grounding line in 1996 but subsequently the area of peak melt moved upstream, the 2010-2016 rates
 452 may be much lower than those in 1996 near the grounding line at that time. This mismatch in observation time and model
 453 forcing could have then resulted in the model never beginning to retreat into areas of concentrated melt. Moreover,
 454 even once retreat was triggered, the inferred melt rate beneath areas that ungrounded during 2010-2016 mixes periods
 455 of no melt and more intense melt, thus causing underestimation of the annual-average melt during the periods when
 456 the ice was ungrounded. While our rescaling of parameterizations can increase the melt rates at the grounding line as
 457 the shelf-averaged ice draft decreases, the Cryo2 distribution does not allow the shelf to shallow out of melt, and so
 458 any underestimation of melt near the grounding line persists through the simulation. Thus, effective melt rates at the
 459 grounding line are lowest using the Cryo2 distribution, and they remain too low to induce retreat. Estimates of melt
 460 rates from ocean models should eventually provide a better option for forcing models, but computational constraints
 461 and poorly constrained cavity geometry prevent their widespread application at present (e.g., De Rydt and
 462 Gudmundsson, 2016).

464 It is possible that weakening of the margins of Crosson affected the timing of grounding-line retreat. Our model
 465 simulations applied an ad-hoc enhancement of 4 to the margins, which is akin to ~5° C of warming (Cuffey and
 466 Paterson, 2010), development of a relatively weak anisotropic fabric (Ma et al., 2010), or damage due to rifting (e.g.,
 467 Borstad et al., 2013). While snapshot inversions for ice-shelf viscosity in 1996, 2011, and 2014 indicate some
 468 weakening of Crosson Ice Shelf (Lilien et al., 2018), this weakening cannot be definitively identified as having been
 469 caused by a particular process (e.g., loss of a pinning point or rifting). Thus, we are unable to identify if the weakening
 470 of the margins was triggered by grounding-line retreat itself or was externally triggered and helped initiate grounding-
 471 line retreat. We consider it unlikely, regardless of their cause, that changes to the strength of the shelf were the primary
 472 cause of retreat since the simulations with marginal weakening but no increase beyond 1996 melt rates showed little
 473 retreat. Additionally, inversion results do not show significant weakening of Dotson Ice Shelf through this time (Lilien

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et al., 2018), suggesting that weakening was not the cause of Kohler Glacier's retreat even if it affected Pope and Smith Glacier, and thus does not explain widespread retreat in the area.

The modeled grounding-line positions demonstrate the stepwise nature of grounding-line retreat and highlight the complexity of assessing whether unstable retreat is taking place. Previous modeling has found that grounding lines tend to remain in relatively favorable positions for a period before abruptly retreating (e.g., Joughin et al., 2010), and the presence of grounding-line wedges at various points on the continental shelf indicate that retreat since the last glacial maximum followed a similar stepwise pattern with extended periods of stability (Graham et al., 2010; Smith et al., 2014). Similarly, exposure dating of glacial erratics along Pine Island Glacier indicate that during the Holocene it experienced long periods of slow retreat punctuated by decades or centuries of rapid thinning (Johnson et al., 2014). Our forced ungrounding experiments were designed to test whether the grounding line was situated such that some perturbation necessarily led to a continued step back to a new stable grounding-line position. While forced ungrounding for 5 years resulted in retreat of one simulation that otherwise remained stable (17 vs. 21 in Table 1), even with elevated melt intensity the grounding line was able to stabilize on the retrograde slopes under some melt distributions (Figure 5), at least over the period of our simulations. Additionally, regardless of melt distribution, little further retreat was found in the 25 years following 18 years of forced ungrounding (Figure 5). The re-stabilization of the retreated grounding line indicates that small perturbations do not necessarily lead to immediate retreat, although 25- to 50-year simulations may simply be too short to capture the retreat that may eventually ensue. These forced ungrounding experiments also serve as a check upon the low temporal resolution of the melt forcing; the shelf-total melt was linearly interpolated between measurements in 1996 and 2006, and a brief period of elevated melt could have perturbed the grounding line during a subset of that time. However, the simulations with 5 years of forced ungrounding suggest that such a perturbation would not have led to immediate and sustained grounding-line retreat. Rather, sustained high melt rates at the grounding line appear to be necessary to cause the continuing grounding-line retreat that has been observed.

4.2 Centennial simulations

The centennial-scale simulations can be broadly categorized as those that emulate observed grounding-line retreat (i.e., display more than 35 km of retreat) and those that retreat less than observations. Those simulations that emulate retreat (2, 4, and 19 in Table 1) all continue to produce retreat into the future. Even those simulations that do not capture the magnitude of recent retreat yield continuing mass loss resulting in over 2 mm of contribution to global mean sea level by 2100 (Figure 6). In the simulations with the 1Obs J2010 melt parameterization, nominally equivalent to no increase beyond 2014 melt forcing, ice losses exceed 8 mm sea-level equivalent and reaches 10 mm when marginal weakening is included. With the S2016 parameterization and marginal weakening, the grounding line also continues to retreat, albeit at a more moderate pace, and losses still reach 6 mm sea-level equivalent by 2100. This simulation with the S2016 forcing and marginal weakening is essentially a minimum loss scenario amongst simulations capable of producing the observed retreat; shelf-total melt rates after 2014 remain below 50 Gt a⁻¹, lower than observed in 2006-2014, yet grounding line retreat and sea-level contribution continue unabated. Thus, these three simulations suggest

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528 that these glaciers will likely contribute 6 mm of sea-level rise over the coming century, even if shelf-integrated melt
529 rates remain at about their levels in recent years. Moreover, the delayed grounding-line retreat compared to
530 observations suggests that these projections are more likely to underestimate than overestimate future ice loss. Given
531 the retreat produced by the simulations with the lowest melt, and grounding-line retreat rates suggest that these
532 simulations underestimate loss, it is unclear whether Smith Glacier could now reach a new stable configuration before
533 the grounding line recedes to the head of its trough.

534
535 While the volume above floatation in the Smith, Pope, Kohler catchment is modest compared to some Antarctic
536 catchments, if thinning were to extend to the divide with the Thwaites catchment, additional losses could result. Due
537 to the extensive grounding-line retreat already undergone by Smith Glacier, the simulations with the J2010 melt
538 distribution suggest that substantial (>50 m) thinning could reach the divide shared with Thwaites by the end of the
539 21st century. This thinning could further contribute to the destabilization of the interior of Thwaites caused by changes
540 at Thwaites' terminus (Joughin et al., 2014). Because of their limited domain, our model simulations are unable to
541 assess the effects of divide migration on regional ice loss, and bed topography might isolate the loss to Smith's present
542 catchment. However, given the potential for divide migration, studies concerned with the stability of Thwaites Glacier
543 on timescales longer than ~100 years may underestimate ice loss if they do not account for potential drainage capture
544 by Smith Glacier.

545 4.3 Comparison to other observations

546 Here we assess how different model forcings affect the match between the simulations and the observations of thinning
547 and speed change. For all simulations, there are substantial differences between modeled and observed ice-flow speeds
548 and thinning rates, which need to be assessed carefully in order to understand the limitations of the model results. By
549 evaluating this mismatch, we can identify the direction in which the model simulations likely err and work to identify
550 processes that may be important for these glaciers but are not captured by our modeling results.

551 4.3.1 Ice surface elevation

552 In Figure 7, we compare modeled and measured ice-surface lowering. The comparison is confined to ice that was
553 grounded in 1996 since observations have greater signal-to-noise ratio over grounded ice; on grounded ice, all thinning
554 is expressed as surface lowering whereas on floating ice only ~10% of thinning is expressed at the surface.
555 Observations of surface lowering were derived from the various altimetry products described in section 2.1. The full-
556 Stokes simulation slightly overestimates thinning along Smith Glacier while producing thickening upstream of Kohler
557 Glacier's grounding line (Figure 7a). In general, the shallow-shelf simulations approximately match the pattern of
558 observed surface change downstream of the grounding line, but show too little thinning upstream (Figure 7b-d). Even
559 the simulations with IObs forcing that showed the most thinning slightly underestimate surface lowering. Part of this
560 difference may reflect errors in the bed elevation; if the true bed elevation were greater than estimated in the bed
561 product we used, a larger portion of dynamic thinning would have directly affected the surface height rather than
562 contributing to ice-draft shallowing. An additional portion of the model-data mismatch is likely due to timing of

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567 retreat; a delayed response of the model could lead to underprediction of surface lowering. Given that the shallow-
568 shelf simulations have delayed grounding-line retreat, it is unsurprising that they generally underestimate surface
569 change.

570

571 The thickening (or lack of thinning) on Kohler may result from difficulties in initiating a model of an out-of-balance
572 system. Melt and calving in 1996 were already larger than accumulation, likely due to elevated melt on Kohler (Lilien
573 et al., 2018), and it is possible that the relaxation of the model prior to the simulations dampened real surface changes
574 rather than artifacts from data errors in the Kohler drainage. Regardless of its cause, this discrepancy is transient and
575 surface lowering eventually propagates up the trunk of Kohler as in observations. However, this thickening on Kohler,
576 along with the shallow-shelf simulations' delayed grounding-line retreat and thinning, suggest that the simulations
577 may underestimate future ice loss.

578 4.3.2 Ice-flow speed

579 We compare the model results to velocity mosaics for 2006-2012, 2014, and 2016-2018. The 2007-2010 velocities
580 are derived from the Advanced Land Observation Satellite, processed using a combination of interferometry and
581 speckle tracking (Joughin, 2002). We used feature tracking of Landsat-8 imagery to obtain velocities for the 2014–
582 2015 austral summer. Velocity data for 2006 and 2011 are part of the NASA MEaSUREs dataset (Mouginot et al.,
583 2014). We determined the 2016–2018 velocity using speckle-tracking applied to data ~~from~~ Copernicus Sentinel-1A/B
584 data. These observations indicate speedup both near the grounding lines of Smith and Kohler Glaciers and farther out
585 on Crosson Ice Shelf (Mouginot et al., 2014). While the speedup near the grounding line is likely due a loss of basal
586 resistance as a result of ungrounding, the speedup of the outer shelf may be due to changes in shelf viscosity or loss
587 of buttressing at the ~~outer right corner of the ice shelf~~ due to the breakup of the Haynes glacier tongue (Lilien et al.,
588 2018).

589

590 The simulations indicate that ungrounding primarily affects speeds near the grounding line while speeds farther out
591 on the shelf remain constant or decrease (~~Figure 5~~). This heterogeneity results from buttressing; if the shelves were
592 spreading freely, a change in grounding-line speed would cause an equal change in the speed of the shelves.
593 Conversely, speedup of the outer portion of the ice shelves is likely a result of local changes to buttressing since
594 speedup is not observed in the region immediately upstream. The model experiments with weakened margins find
595 speedup along the Pope Glacier centerline on the outer portion of Crosson Ice Shelf (Figure 4d). While the modeled
596 speed changes in the simulations with weakening closely match the observed speeds 40-60 km from the 1996 calving
597 front, they show too little speedup closer to the front. This discrepancy ~~along the shelf~~ suggests that ~~part of the observed~~
598 changes in speed may be a result of forcing near the calving front, possibly associated with a loss of buttressing due
599 to the breakup of the Haynes glacier tongue around 2002 or the progressive rifting of this area. While the simulations
600 with weakened margins do not fully capture the observed velocity changes near the shelf margin, the marginal
601 weakening does cause the model to more accurately reproduce speedup of the bulk of Crosson Ice Shelf. There are ~~a~~
602 variety of possible reasons that the model does not capture the full spatial complexity of the observed speedup, for

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607 example weakening of the ice shelves, bed elevation errors, or inferred basal resistance being too low, and we cannot
608 identify a single cause.

609

610 For the grounded ice, the simulations tend to under predict speedup on Smith Glacier, while generally overpredicting
611 speed changes on Kohler Glacier. The timing of the speedup corresponds with the timing of rapid grounding-line
612 retreat, so the delay in modeled grounding-line retreat likely causes the delay in modeled speedup. The scarcity of
613 observations of grounding-line position and ice velocity earlier in the satellite records, complicates the interpretation.
614 Reliable grounding-line positions are unavailable between 1996 and 2011, and ice velocities are unavailable between
615 1996 and 2006. Substantial retreat occurred during this time period, and transient speedup could have occurred during
616 the gap in the observations.

617

618 4.4 Model limitations

619 We now evaluate effects that our choices in model complexity and melt forcing have on interpreting our results. In
620 addition, the relative insensitivity of the modeled retreat to our choice of sliding law and of the model resolution are
621 shown in supplementary materials.

622 4.4.1 Model complexity

623 Full-Stokes models require significantly greater computing resources than shallow-shelf models of similar resolution.
624 In the case of our simulations, the shallow-shelf simulations took ~1% of the CPU hours of an equivalent full-Stokes
625 simulation, allowing the use of local workstations rather than high-performance computing resources. Thus, using the
626 simplified physics of shallow-shelf models is desirable in cases where it is sufficient to capture the relevant processes.
627 While we find slower initiation of retreat with shallow-shelf than with full-Stokes models, after initialization the
628 pattern of retreat is similar between both classes of models.

629

630 Uncertainties in the model inputs, and necessary choices when initializing models, create significant spread in model
631 retreat rates that could explain the difference between full-Stokes and shallow-shelf simulations. For example, at Pine
632 Island Glacier, uncertainty in bed elevation propagates to uncertainty in the timing of retreat of around ± 5 -10 years
633 depending on assumptions about the spectrum of the bed roughness (Sun et al., 2014). Moreover, with idealized
634 geometry, L1L2 models, a class of depth-integrated models with slightly greater complexity than shallow-shelf
635 models, are more sensitive to high-frequency noise than full-Stokes models (Sun et al., 2014), suggesting the
636 possibility that the uncertainty in bedrock elevation may affect the full-Stokes and shallow-shelf models in different
637 ways.

638

639 The spacing of bed elevation measurements in our study region does not resolve detail with wavelengths of ~5 km
640 and below. In addition, noise with longer wavelengths may be present if there are systematic biases in the
641 measurements. Without constraints on this roughness, we cannot realistically assess how bed uncertainty may have

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649 affected the two types of models differently. However, comparison of observed and modeled grounding-line position
 650 and surface elevation suggest that errors in the bed dataset have indeed affected our results. The path of ungrounding
 651 of Smith Glacier for most model simulations progresses directly through an area that has been identified as having
 652 remained grounded through 2014 (Rignot et al., 2014; Scheuchl et al., 2016) despite the thinning rates in that area
 653 matching observations there. If the bed elevations were accurately captured by the bed product, accurately modeling
 654 thinning would be sufficient to accurately model retreat. By contrast, in an area where the bed is shallower than the
 655 bed product suggests, ungrounding would occur too early in the model and a greater portion of thinning would be
 656 expressed as ice-draft shallowing rather than surface lowering. Since the model finds ungrounding of a portion of
 657 Smith while approximately matching thinning rates there, it is likely that the bed is shallower there than the bed
 658 product indicates. Thus, we have strong evidence that ~~errors~~ in the bed elevation ~~may~~ have changed the ungrounding
 659 in our simulations, but we are unable to constrain the different ways this would have affected different simulations.

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 661 Limitations of the assumptions in the sliding law are another potential source of differences between the models.
 662 Recent work shows that alternatively parameterized versions of Equation 1 (regularized Coulomb friction) extend
 663 plastic behavior much farther inland to yield better agreement with observations on Pine Island Glacier (Joughin et
 664 al., 2019). The friction law in Equation 1 relies on a height-above-flotation parameterization for effective pressure,
 665 ~~ignoring hydraulic gradients and limiting~~ Coulomb (plastic) behavior to near the grounding line. Thus, the friction law
 666 used here may cause initially slow retreat in the shallow-shelf model to result in persistent differences from the full-
 667 Stokes model. Regularized Coulomb friction could potentially lead to faster modeled retreat rates in some simulations
 668 as plastic behavior follows the grounding line inland, thereby improving model data agreement beyond that found
 669 here.

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 671 Time to full relaxation in the model spin-up, differences in the inferred basal shear stress resulting from inversion
 672 procedure implementation, or different response to errors in surface elevation all may explain an additional portion of
 673 the difference between full-Stokes and shallow-shelf models. Assessing the effect of uncertainties in these parameters
 674 would require considerable investigation that is beyond the scope of this study. However, given that there are known
 675 errors in the bed topography, and that the unconstrained frequency of bed noise affects the models differently, ~~it is~~
 676 ~~possible~~ bed errors alone ~~could~~ change the timing of retreat by as much ~~as~~ the model-data mismatch. Thus, while the
 677 difference in timing between full-Stokes and shallow-shelf models might indicate substantially better full-Stokes
 678 performance for at least one of the three glaciers, it could also reflect the uncertainty and not ~~indicate~~ that one type of
 679 model is better suited to describing this system. Indeed, while the full-Stokes model better matches the timing of
 680 retreat on Smith Glacier, ~~it~~ finds thinning rates that are a poorer match to observations and does not do a better job
 681 than the shallow-shelf model at reproducing retreat on Pope or Kohler glaciers. Unfortunately, we did ~~not~~ have the
 682 computational resources for a suite of full-Stokes runs sufficient to make a robust comparison of relative performance.

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689 4.4.2 Melt forcing scheme

690 The application of the melt parameterizations in this study differs from previous work because, at each timestep where
 691 there are data, it rescales the parameterization so that model matches the observed shelf-wide integrated melt through
 692 time (Lilien et al., 2018). The primary advantage of this scheme is that it prevents the large, likely unrealistic changes
 693 to the shelf-total melt rate that occur as concentrated melt at depth causes the ice-shelf draft to shallow. We utilized
 694 this scheme primarily out of necessity; the grounding lines of Smith and Kohler Glaciers are sufficiently deep that
 695 without scaling the melt forcing, the shelf-total melt rates are drastically out of balance as simulations begin, and
 696 substantial retreat ensues before the shelf is able to shallow out of the intense melt, thus leading to sustained,
 697 unphysically high melt rates. On the other hand, the continuous-rescaling scheme dampens feedbacks between the
 698 grounding-line retreat and the melt rate. Whereas a fixed parameterization generally causes an initial increase in shelf-
 699 total melt in response to a retreat of the grounding line since greater sub-shelf area is exposed, this continuous-scaling
 700 scheme will reduce the scaling of the melt distribution in response to that retreat. The continuous-rescaling scheme
 701 may thus unrealistically dampen feedbacks leading to rapid retreat, since increasing exposure of sub-shelf area may
 702 truly increase the total melt rate if there is sufficient heat content in the nearby ocean. Because melt is not solely a
 703 function of depth, any depth-dependent melt parameterization faces tradeoffs between fidelity to observations and
 704 simplicity, but the scheme used here is a reasonable compromise for a study that needs quasi-realistic melt rates at the
 705 beginning of simulations to enable comparison between model and observations.

706 5 Conclusions

707 Using reasonable melt intensity distributed with simple, depth-dependent parameterizations, our model simulations
 708 are able to reproduce the recent speedup, thinning, and retreat of Smith, Pope, and Kohler Glaciers, albeit with some
 709 uncertainty in the timing. These simulations suggest that in 1996 Smith Glacier was in a state of precarious stability,
 710 but nonetheless elevated melt rates were needed to cause the observed grounding-line retreat. Even when shelf-
 711 integrated melt rates were increased, modeled retreat only occurred when that melt was concentrated near the
 712 grounding line and not farther out on the shelf. Explicit forcing of some retreat was also insufficient to cause the extent
 713 of grounding-line retreat that has been observed, as the grounding line was able to re-stabilize, at least temporarily,
 714 unless the melt was concentrated at depth. While weakening of the margins of Crosson Ice Shelf may have played a
 715 role in the speedup of the shelf or in the timing of grounding line retreat, it is unlikely that such a change precipitated
 716 the observed changes. Comparison to observations indicates that our model simulations underpredict the speedup and
 717 thinning of these glaciers, but despite this underprediction those model simulations that successfully reproduce recent
 718 grounding-line retreat continue to show grounding-line retreat into the future. We find that the rate of grounded ice
 719 loss is likely to grow in the coming decades as retreat progresses. These simulations indicate that >6 mm of sea-level
 720 contribution is likely by 2100, even if the total melt remains around current levels. By the end of our ~100-year
 721 simulations, thinning has extended to the ice divide separating Smith and Kohler from Thwaites Glacier, indicating
 722 the potential for Smith's retreat to hasten the destabilization of that larger catchment.

723 Acknowledgements

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While the volume above floatation in the Smith, Pope, Kohler catchment is relatively modest, if thinning were to extend to the divide with the Thwaites catchment, additional losses could result. Due to the extensive grounding-line retreat already undergone by Smith Glacier, the simulations with the J2010 melt distribution suggest that significant (>50 m) thinning could reach the divide shared with Thwaites by the end of the 21st century.

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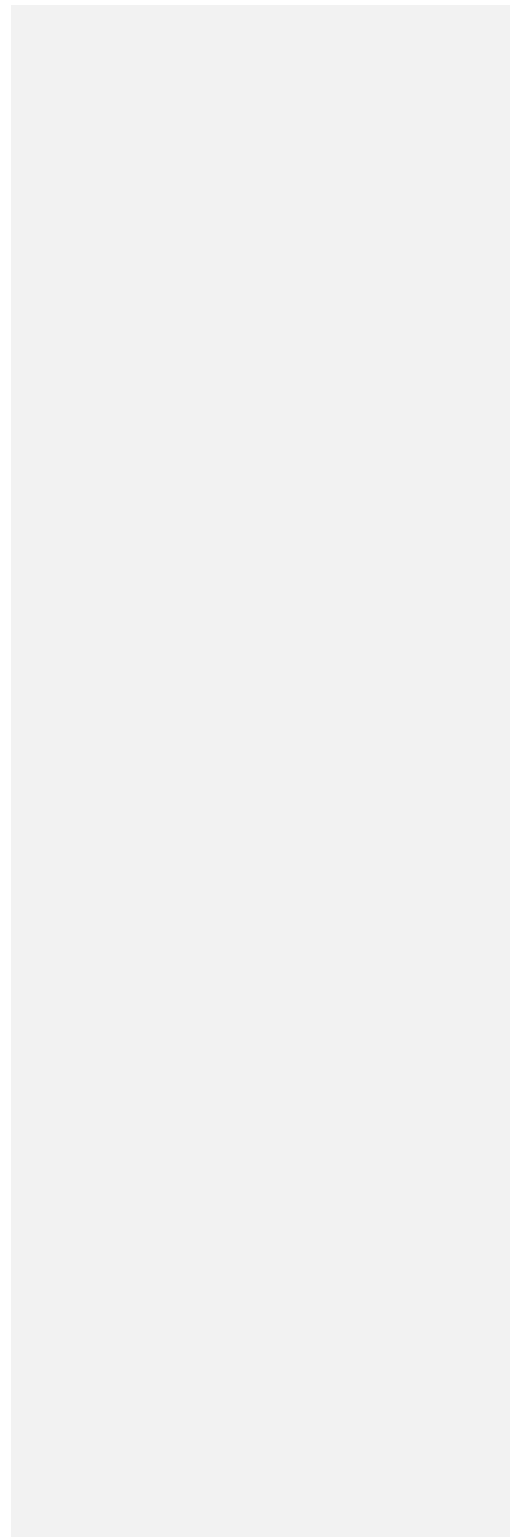
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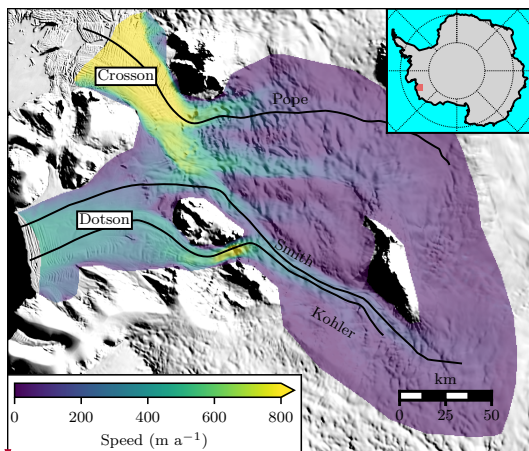
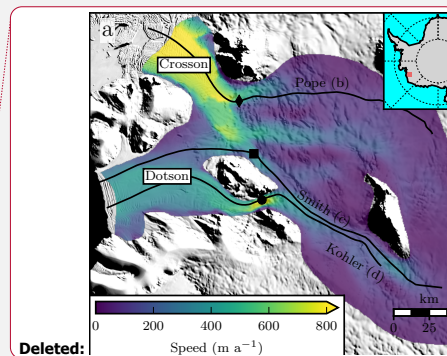


Figure 1. Study area. Colors show InSAR-derived velocities from 1996, plotted only over the area of the model domain. Black lines indicate flowlines for the three outlet glaciers. Inset shows location of study area.



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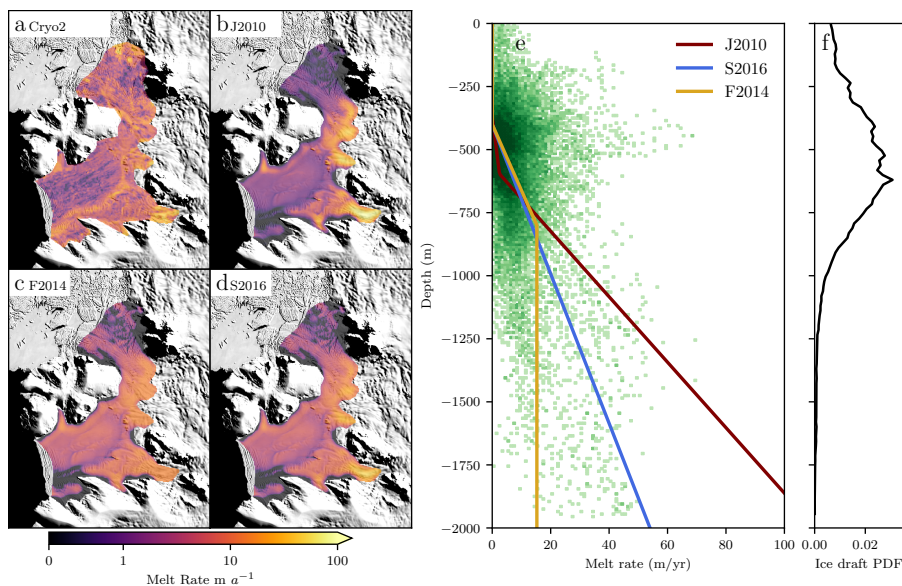


Figure 2. Melt forcings used for modeling. a-d. Distribution of melt rates at the beginning of simulations using Cryosat-inferred rates from Gourmelen et al. (2017), and parameterizations from Joughin et al. (2010), Favier et al. (2014), and Shean (2016) respectively. e. Scaled parameterizations (colored lines) plotted over green points showing Cryosat-derived distribution of melt. Darker colors indicate greater area with a given combination of depth and melt rate. f. PDF of depths; this indicates the total area at each depth, showing how shelf-total melt rates are most sensitive to melt rates between ~250 and 800 meters.

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	Model physics	Melt dist.	Melt intensity	Enhancement in margins	Forced ungrounding	Sliding Law	Sim. len. (years)	>15 km retreat
1	FS	J2010	1Obs	1	No	Schoof	23	Yes
2	SSA	J2010	1Obs	1	No	Schoof	104	Yes
3	SSA	J2010	2Obs	1	No	Schoof	25	Yes
4	SSA	J2010	1Obs	4	No	Schoof	104	Yes
5	SSA	J2010	1Obs	1.8	No	Schoof	50	Yes
6	SSA	J2010	Control	4	No	Schoof	50	No
7	SSA	J2010	1Obs	1	5 years	Schoof	50	Yes [‡]
8	SSA	J2010	1Obs	1	18 years	Schoof	50	Yes ^{*‡}
9	SSA	J2010	1Obs	1	No	Weertman	50	Yes
10	SSA	F2014	1Obs	1	No	Schoof	104	No
11	SSA	F2014	2Obs	1	No	Schoof	25	Yes
12	SSA	F2014	1Obs	4	No	Schoof	50	No
13	SSA	F2014	Control	4	No	Schoof	50	No
14	SSA	F2014	1Obs	1	5 years	Schoof	50	No [‡]
15	SSA	F2014	1Obs	1	18 years	Schoof	50	Yes [*]
16	SSA	F2014	1Obs	1	No	Weertman	50	No
17	SSA	S2016	1Obs	1	No	Schoof	104	No
18	SSA	S2016	2Obs	1	No	Schoof	25	Yes
19	SSA	S2016	1Obs	4	No	Schoof	104	Yes
20	SSA	S2016	Control	4	No	Schoof	50	No
21	SSA	S2016	1Obs	1	5 years	Schoof	50	Yes [‡]
22	SSA	S2016	1Obs	1	18 years	Schoof	50	Yes [*]
23	SSA	S2016	1Obs	1	No	Weertman	50	No
24	SSA	Cryo2	1Obs	1	No	Schoof	104	No
25	SSA	Cryo2	2Obs	1	No	Schoof	25	No
26	SSA	Cryo2	1Obs	4	No	Schoof	50	No
27	SSA	Cryo2	Control	4	No	Schoof	50	No
28	SSA	Cryo2	1Obs	1	5 years	Schoof	50	No [‡]
29	SSA	Cryo2	1Obs	1	18 years	Schoof	50	Yes [*]
30	SSA	Cryo2	1Obs	1	No	Weertman	50	No

Table 1. Summary of model inputs. Model physics and inputs are summarized in the first six columns. The last column indicates whether the Smith Glacier grounding line retreated over 15 km within the simulation, with starred entries indicating that retreat was explicitly forced. Daggers indicate that some grounding-line retreat continued beyond the period of explicit forcing.

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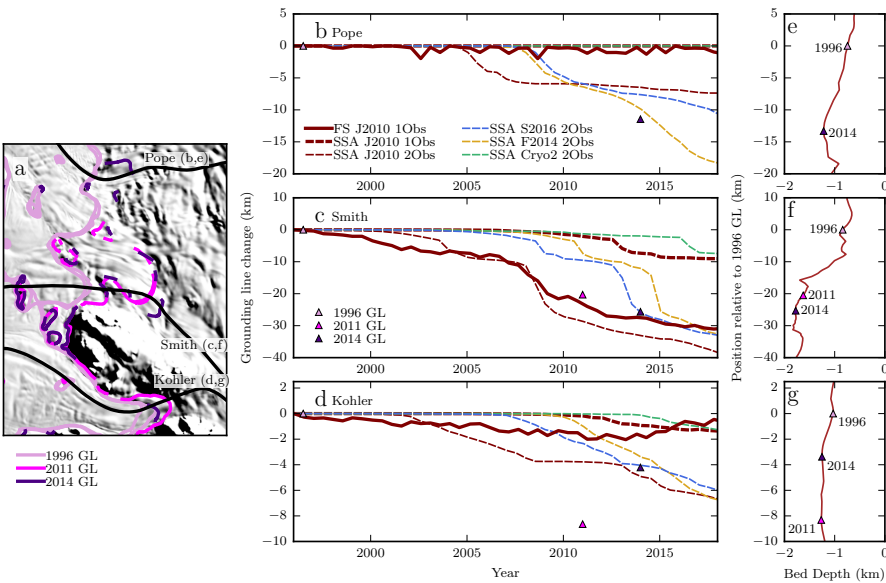


Figure 3. Sensitivity of change in grounding line position to melt distribution and intensity. **a.** Flowlines used for evaluation of grounding line retreat (black). Pink and purple lines indicate observed grounding line positions (Rignot et al., 2014; Scheuchl et al., 2016). **b-d.** Modeled and observed grounding line position along the centerlines of Pope, Smith, and Kohler Glaciers respectively for different model simulations. Zero indicates no change since 1996, negative values indicate retreat. Line colors indicate melt distribution: J2010 (maroon), S2016 (blue), F2014 (gold), and Cryo2 (green). Line thickness indicates melt intensity: thick for 1Obs, thin for 2Obs. Line style indicates full-Stokes (solid) or shallow-shelf model (dashed). Simulations that display less than 2 km of grounding-line retreat on all centerlines are not shown. Triangles indicate observations of grounding line position, with colors corresponding to lines in a. **e-g.** Bed elevations vs distance from 1996 grounding line along the centerlines of Pope, Smith, and Kohler Glaciers respectively. Vertical scale matches panels b-d. Purple triangles again indicate observed grounding line positions through time.

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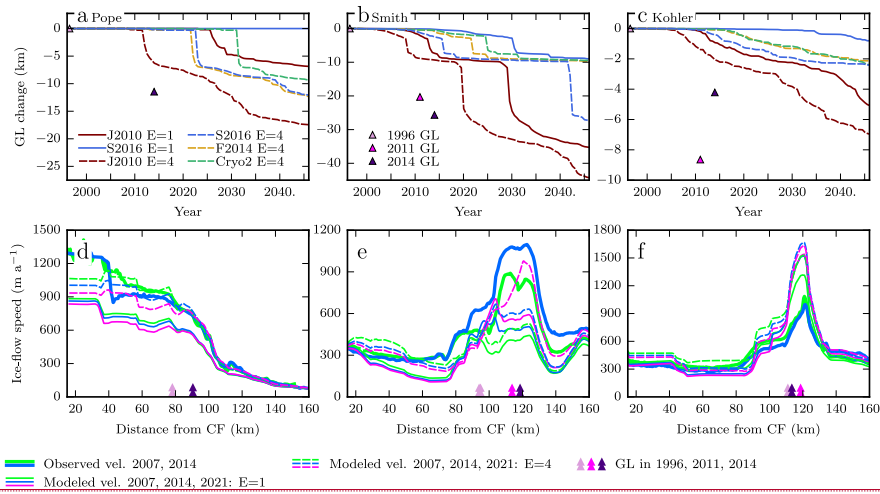
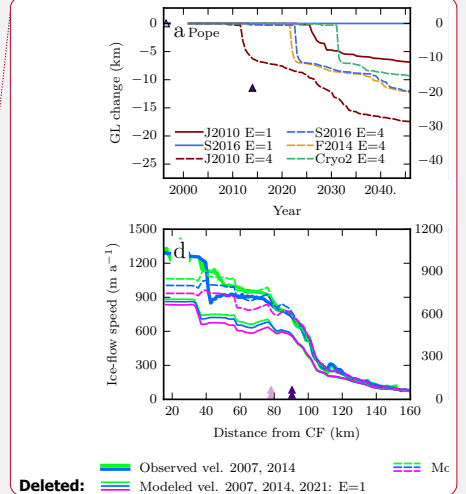


Figure 4. Effect of marginal weakening on grounding-line position and velocity. a-c. Modeled grounding-line position through time along Pope, Smith East, and Kohler along flowlines shown in Figure 1. All simulations used 10Obs melt intensity. Colors indicate the melt forcing as in Figure 3. Solid line indicates no weakening, and dashed line indicates 4x enhancement within 10 km of the ice-shelf margins. Triangles show observed grounding line position (Rignot et al., 2014; Scheuchl et al., 2016). **d-f.** Velocity along flowlines corresponding to upper panels, with all simulations now using the J2010 melt parameterization. Color of line indicates the year (blue for 2007, green for 2014, pink for 2021). Thick lines show observations. Thinner lines show model results (using the J2010 melt parameterization), with dashed and solid patterns corresponding to the upper panels. Arrows at bottom indicate observed grounding-line position through time.



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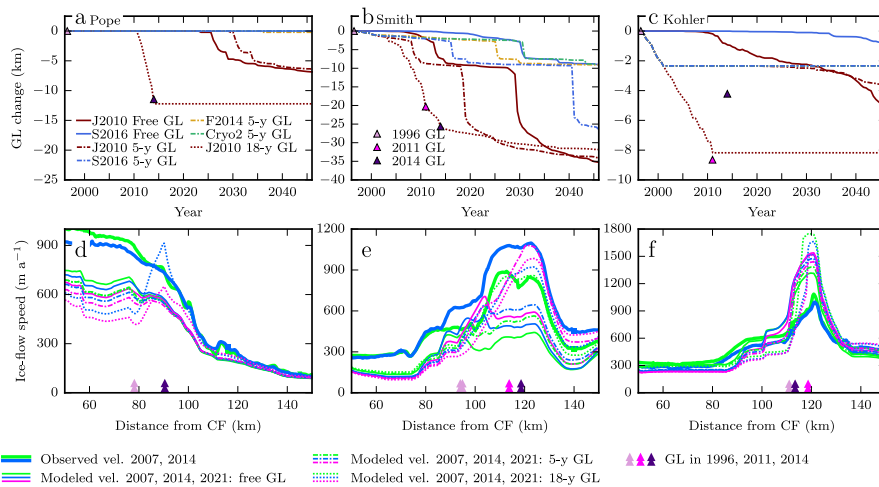
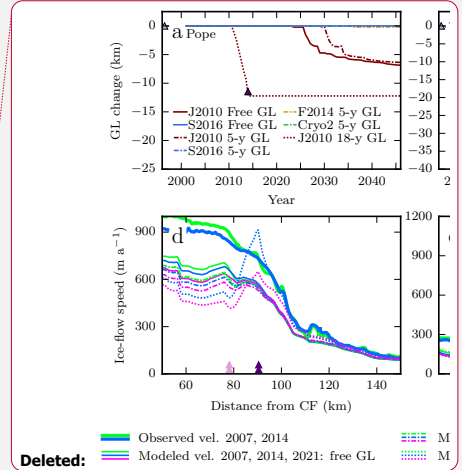


Figure 5. Grounding line and speed changes resulting from forced ungrounding. a-c. Modeled grounding-line positions along centerlines of Pope, Smith East, and Kohler centerlines, respectively, from Figure 1. All simulations used IObs melt intensity with no marginal enhancement. Line style indicates how the grounding line was treated: solid line for freely evolving grounding line, dashed line for forced ungrounding for 18 years (1996-2014), and dash-dot for forced ungrounding for 5 years only (1996-2001). Triangles indicate observed grounding-line positions through time (Rignot et al., 2014; Scheuchl et al., 2016). Simulations with no change in grounding-line position after the forced ungrounding are not shown. **d-e.** Observed and modeled ice speed along centerlines from upper panels, with line color indicating year as in Figure 4. Thick lines show observations. Thinner lines show model simulations (using J2010 melt distribution) with line style indicating ungrounding scheme as in a-c. Triangles at bottom indicate the observed grounding-line position in different years; the effect of forced ungrounding on modeled ice speed is generally restricted to the area around the grounding line where the surface remains relatively steep while basal resistance is removed.



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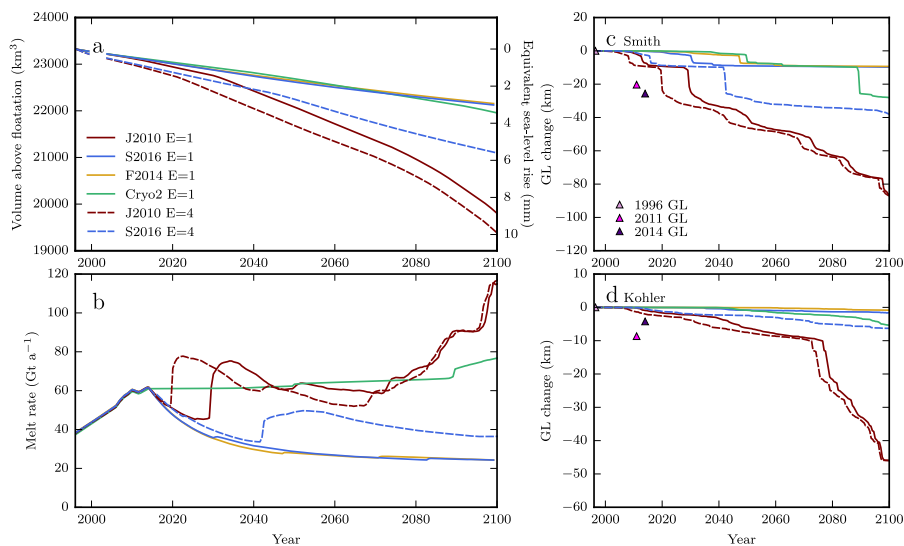
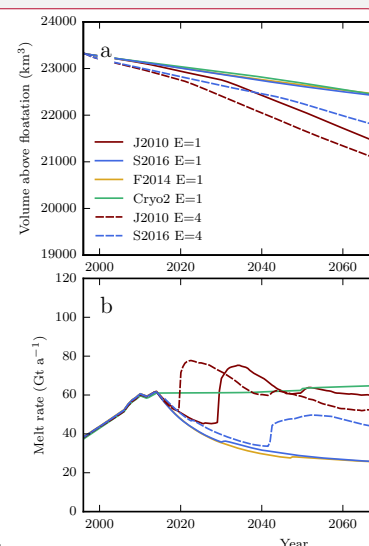


Figure 6. Results of centennial-scale model simulations. **a.** Volume above floatation in the Smith, Pope, Kohler catchment and equivalent sea-level rise through time for extended simulations. All runs use 1Obs melt intensity. Color of line indicates melt distribution as in previous figures. Solid line corresponds to shallow-shelf model, and dashed line shows shallow-shelf model with enhanced margins. The differences in volume during the period including forcing result from different ice-flow speeds causing different calving rates. **b.** Melt rate through time. Runs are forced to observations through 2014, so melt rates correspond through this period, then diverge since the scaling of the melt parameterization is fixed at the 2014 value. Note that melt rates do not directly cause loss of volume above floatation since some melt distributions cause melt of the shelves without substantial loss of grounded ice. **c-d.** Grounding-line position change through time along Smith and Kohler centerlines, respectively, from Figure 1. Purple triangles again show observed grounding-line positions through time (Rignot et al., 2014; Scheuchl et al., 2016).



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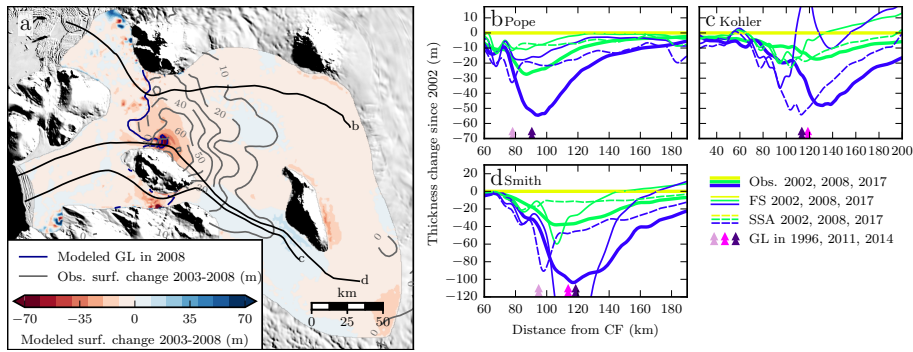


Figure 7. Modelled and observed thinning during the ICESat era (2003-2008). **a.** Spatial distribution of thinning using the shallow-shelf model with J2010 1Obs melt. Colors indicate modelled thickness change while grey contours indicate observations. Black lines show flowlines as in other figures. Thin, blue line shows the modelled grounding line in 2008. **b-e.** Thinning through time along flowlines. Color indicates the year. Thin lines show model, thick lines show data derived from Operation IceBridge altimetry, ICESat-1, and WorldView/GeoEye DEMs. Triangles indicate grounding-line position (Rignot et al., 2014; Scheuchl et al., 2016).