Reply to editor's and reviewers' comments

Arctic sea ice-free season projected to extend into fall

Marion Lebrun, Martin Vancoppenolle, Gurvan Madec, and François Massonnet

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0. Comments of the Editor

Comments to the Author:
Dear Marion, dear all,

I have now received two reviews of your re-submitted manuscript "Arctic sea ice-free season projected to extend into fall". Based on these reviews, I must ask for another round of major revisions to address in particular reviewer 1's concerns regarding this study.

I understand the reviewers major concerns as follows, and would like to ask you to address these concerns adequately in a revised version:

1. Why does R increase substantially in CMIP5 simulations throughout the 21st century? While you give some plausible argumentation, it seems straightforward (at least from the outside) to examine your justification from the available model output, and be it just from IPSL-CM. Showing that your argumentation is reflected by the model's behaviour would greatly strengthen its credibility.

2. Why is R different on interannual compared to longer time scales? Again, you provide some justification, but should have all available data to show this on actual ESM output.

3. Please provide more detail on the quantification of the feedback factor for winter, and ideally show that it holds in more complex models, too.

Overall, I like the approach of "we have a result from complex models -> we examine a hypothesis and show that this hypothesis holds in a simple model". However, as it seems doable with reasonable effort to also go the final step of "we show that this hypothesis also holds in relation to ESM output", I would like to ask you to go this extra step before I can accept this study.

Please get in touch any time if further questions should come up.

All the best,

Dirk

Our answer to the Editor's comments

Dear Editor, dear Dirk,

Thanks a lot for the time spent on our manuscript and your willingness to improve it and make it more convincing.

As we explained to you in a separate email, it is very difficult to go further into #1 and #2 than we did in the paper because of the lack of sufficient output in CMIP5. We were seeing your points #1 and #2 as work perspectives. Hence, we tried to focus on being more convincing on #3.

Our main job was to introduce an exhaustive analysis of both winter and summer feedbacks, based on the framework of Goosse et al. (2018). In our view, the review process had the positive impact to enforce the changes that led to the new analysis, which we find more convincing.

We provide a point-by-point answer to your comments below.

Best regards,

Marion Lebrun, Martin Vancoppenolle, Gurvan Madec and François Massonnet.

—

1. Why does R increase substantially in CMIP5 simulations throughout the 21st century? While you give some plausible argumentation, it seems straightforward (at least from the outside) to examine your justification from the available model output, and be it just from IPSL-CM…

> Unfortunately it is not straightforward: we would need daily output of the ice-ocean energy fluxes, which none of the models (including ours) does provide. The lack of such detailed output explains why the 1D model was used. We make that point clear in the revised manuscript (see 1st sentence of second paragraph of Section 3.4).

1. (continued) … Showing that your argumentation is reflected by the model's behaviour would greatly strengthen its credibility.

The only arguments we can come up with are (i) the asymmetric SST response in IPSL-CM, (ii) that all models agree with each other and with the 1D model in terms of freeze-up amplification. We cannot provide stronger evidence for now.

2. Why is R different on inter-annual compared to longer time scales? Again, you provide some justification, but should have all available data to show this on actual ESM output.

Unless we are wrong, to prove why the short-term effect is opposite to the long-term effect, we need both daily output and to de-activate ice dynamics, which needs re-running GCM and takes (a lot of) time.

3. Please provide more detail on the quantification of the feedback factor for winter, and ideally show that it holds in more complex models, too.

Since this was the only item that we could address in detail, we worked hard to improve that part.

1. We now use the newly developed feedback framework of Goosse et al (2018) to discuss changes in ice seasonality. This greatly simplifies the mathematical developments and better frames the discussion, we believe. The 1D response to the radiative forcing perturbation is now split into feedback and reference responses, for which we give analytical formulations (Appendix A).

2. Winter and summer processes are now discussed with equal weight (both in Appendix A and Section 3.4).

3. We show that the R-coefficient is nearly equal to the summer feedback factor and explain why.

The abstract and conclusions were nearly entirely rewritten. We also thrived to clarify what was actually shown in the manuscript and what was left unexplained.

REVIEWER #1

General comments.

The authors have clarified some of their reasoning in the paper and provided more arguments for the changes in ice retreat and advance timing. However, ***there is no new analysis in the study.*** *This is disappointing. I think that there are many interesting elements to the work presented here but feel that* ***the authors have not dug in deeply enough to understand these elements.*** *Because of this, I believe that the important* ***new material in the study is modest*** *- basically that solar heating occurring over the summer is slow to be released during the fall freeze-up and delays the ice advance. This is based on simulations with a simple single column model and* ***only limited results on this mechanism*** *(just the SST annual cycle)* ***are shown from the coupled simulations****. There are* ***a number of questions that remain regarding the changes in ice retreat and advance timing as outlined in the major comments below****. I would encourage the authors to address some aspects of these questions and thereby* ***provide more insights on why the trend in ice advance timing exceeds the ice retreat trends in the 21st century*** *(as raised in my original review). I recommend another round of major revisions and would encourage some new analysis to address these comments.*

We thank the reviewer for his/her time, critical attitude and willingness to improve our paper.

We have done our best to address the reviewer's concerns. Generally speaking we focussed our actions on: (i) clarifying in the manuscript as to why a priori obviously doable analyses were not done, (ii) being as rigorous a we could on the analyses shaping ice seasonality mechanisms in the 1D model, (iii) being as clear as possible as to what was actually shown in the manuscript and what was left unexplained.

(i) That the reviewer suggests we have not dug in deeply enough probably stems from the fact that the reviewer thinks all diagnostics are available to address all questions regarding sea ice seasonality, but unfortunately it is not the case. Indeed, the energetic budget of the ice-free ocean, when available, is only provided with a monthly basis, which is insufficient to attribute changes in the date of ice advance. For the same reason it is not possible to clarify why the short and long-term responses differ and, as the reviewer, we are also not entirely satisfied with the absence of more conclusive evidence.

Action: This absence of key diagnostics explains why we cannot disentangle mechanisms and why we use of a 1D model. That this was not clear from the revised manuscript is entirely our fault. In the newly revised manuscript, we thrived to more clearly explain why we cannot answer those two critical questions with CMIP5 outputs and why we use a 1D model, which allows to isolate the thermodynamic response of ice seasonality to warming (see first § of 3.4). We also make that absence of diagnostics in the conclusion (see our point 4). The abstract hopefully synthesises an improved state of things.

(ii) That we should provide more insights on why the trend in ice advance timing exceeds the ice retreat trends in the 21st century, was addressed by providing expanded analyses of the mechanisms of changes of date of ice retreat and advance.

Action: A detailed feedback analysis of changes in ice retreat and advance date, based on the feedback framework recently introduced by Goosse et al. (2018) was performed. It remarkably does not change our results, but provides a much clearer framework to discuss changes in ice seasonality. The response of ice retreat and advance dates to radiative forcing perturbation is now split into the response to changes into « reference » (forced) and feedback contributions.

The new analysis includes a detailed account for the winter mechanisms, presented on the same level and same degree of detail as the summer mechanisms.

The new presentation of ice seasonality drivers is more general, clearer and not significantly longer than previously presented calculations.

Appendix A and Section 3.4 were thoroughly revised, being nearly entirely rewritten. The Appendix figures A1-A2 are entirely new, and there is also a new Figure 5.

In the new framework, we find that R is directly connected and even nearly equal to the summer feedback factor. We provide details as to why in the newly revised manuscript.

Note that the new equation for changes in ice advance date (16) is formally different but strictly equivalent to the one presented in the previous manuscript. The fundamental results of analysis are not changed.

(iii) We have tried to highlight the novel material presented in the study. We hope the reviewer now fully perceives what is new in our manuscript:

1. Our paper is the first study of the future ice seasonality with CMIP5 output over the entire Arctic and multiple models.
2. We use newly developed methods (the R diagnostics introduced are new).
3. The result that all models consistently show an ice-free season extending into fall on the long-term for all models is new.
4. That this long-term response is consistent with the basic thermodynamics of the ice-ocean system is new as well.
5. That the long-term and short-term responses differ is new as well.
6. The feedback analysis from the 1D model is new as well.

That we leave open questions is to be expected since this is the first study addressing mechanisms of ice seasonality in response to climate change.

We may have missed existing references that have explicitly addressed points 1-6, or any of these points individually, and we are ready to properly cite these works as they ought to.

Action: We further clarify our contribution in the abstract, introduction and conclusions. We also clarify the questions left open in the abstract and in the conclusion.

Major comments

1a. The discrepancies between the long-term and short-term variations in ice retreat and advance timing are interesting but not at all explored in the study. The authors offer a number of possibilities for why there might be this difference, with references to previous work, but nothing is conclusive or backed up by analysis.
1b. More analysis on what drives the ice retreat timing, ice advance timing and how this varies across timescales would be useful.

Answer (1a): To provide better mechanistic evidence as to why the short-term effect is opposite to the long-term effect, one would need (1) daily output of ice-ocean surface energy budget and (2) integrations with disabled sea-ice dynamics, in order to eliminate that source of variability. Neither (1) nor (2) is available from CMIP5. While this analysis could technically be done with the IPSL model, it would take far too much resources and time. It is therefore out of the scope for this study.

Action (1a):

We clearly acknowledge that it is hard to investigate with available CMIP5 output why the long-term response differs from the short-term one, and leave that as an open question. In Section 3.4, we add:

> *CMIP5 does not offer sufficient diagnostics to study this response in detail, in particular lacking a daily description of the surface energy budget. This is why we used a 1D thermodynamic model …*

In the conclusion, we add:

> *Thermodynamic processes neither do explain the inter-annual variations in ice seasonality, nor the transient path towards the long-term response, which are both consistently simulated features among CMIP5 models.*

Answer and action (1b): As described in the general comment, we provide more analyses of what drives the ice retreat timing, ice advance timing based on the feedback framework of Goosse et al (2018).

2. The authors provide results from the 0-layer thermodynamic model but with very little comparison to the coupled climate simulations. The 0-layer model excludes many factors (not just dynamics). For example, in the coupled model solar energy can penetrate through leads and ice so will not have such an abrupt transition as in the 0-layer model and the surface fluxes will affect the atmospheric state and feed back onto the surface fluxes, among others.

I'd suggest that more analysis is done with the coupled model to assess whether the 0-layer model results are indeed the dominate process occurring in the coupled runs, how things change with time scale, etc.. For example, on Figure 6b, why are the solar and net heat fluxes for IPSL not shown in addition to the SST? Do these look similar to the 0-layer model in Fig 6a? Do they change on inter-annual versus longer timescales (see 1 above)? Making more comparisons between the 0-layer results and the coupled model would help to strengthen the paper. It could also help to answer why the simple mechanism at work in the 0-layer model does not act on short timescales in the coupled modeling systems (again, see 1 above).

Answer: (see general comment). 1) We agree with the reviewer that it would be interesting to bridge the gap between the 0-layer model and GCM by formally studying how the surface fluxes compare. Unfortunately, the CMIP5 models and specifically the IPSL model did not provide daily outputs of the surface energy balance. Now this daily resolution is critical to the study the thermodynamic component of ice retreat and advance. So, while the reviewer's comment is well-founded, it is not possible to address it with more details than what is in the current manuscript, that is, by deducing the thermodynamics from the timings of ice retreat and advance.

2) That the SM0L model is simple is clear. As for penetration of solar radiation before ice retreat, such heat is used to melt bottom ice and not to warm the mixed layer in CMIP5 models, whereas it is used to melt ice from the surface in the SM0L model which could change the trend in ice retreat date. Such changes are part of the many differences between the 1D model and the CMIP5 models. Using the SM0L was motivated by the fact that it is the simplest ice-ocean model, and that models with SM0L thermodynamics cannot really be distinguished from others (e.g. Massonnet et al., 2018).

Action: 1) We clearly acknowledge that it is hard to investigate with available CMIP5 output why the long-term response differs from the short-term one, and leave that as an open question.

In Section 3.4, we add:

> *CMIP5 does not offer sufficient diagnostics to study this response in detail, in particular lacking a daily description of the surface energy budget. This is why we used a 1D thermodynamic model …*

In the conclusion, we add:

> *Thermodynamic processes neither do explain the inter-annual variations in ice seasonality, nor the transient path towards the long-term response, which are both consistently simulated features among CMIP5 models.*

2) In Section 2.4, we add:

> *We argue that the Semtner zero-layer approach is appropriate to study the response of CMIP5 models to warming, as the CMIP5 models with more complicated thermodynamics cannot be distinguished from those using the Semtner 0-layer approach (Massonnet et al., 2018).*

3. The 0-layer model results provide a reason why the ice advance timing is delayed but do not clearly indicate why (at least to me) it would be delayed more relative to retreat timing in the 21st century. Some physical arguments for why this occurs are suggested on lines 309-321. However, there is no analysis to back them up. It would be useful to assess some of these factors in the coupled model simulations to determine their influence, relative magnitude, etc. A clearer reason with corroborating material as to why Rlong increases to greater than one (which is one of the main conclusions of the manuscript) would be useful. I think that this could be done without drastically inflating the manuscript, especially if it is just to show support for the mechanisms that are already speculated in the manuscript.

Answer. We addressed this comment with new material. We analyse changes with the feedback framework of Goosse et al (2018) and now study the winter feedback with the same level of complexity as the summer one. R is expressed as a function of feedback factors and it is explained why it is greater than 1. See also answer to your general comment. We cannot back up the transition from the short-term to the long-term response because of the lack of sufficient diagnostics. We provide more arguments in the general answer to the Editor.

Minor comments.

Line 54: Wording/typo – need to include "be" in the sentence

Done.

Line 72-73: Wording needs to be revised ("in accord the observed in situ increase …")

Reworded into « in accord with the observed in situ increase… »

Line 109-112: It might also be good to say what the caveats are from a forced model. For example, the surface state doesn't feedback to the atmosphere which can affect the processes that drive changes in ice advance and retreat timing.

Thanks. Added « A caveat of forced-atmosphere simulations is the absence of feedback from the see ice/ocean surface state onto atmospheric dynamics, which can affect the processes that drive changes in ice advance and retreat timing. »

Section 3.1. You should mention here that there is an inherent discrepancy in comparing observations, which are influenced by internal variability, to a multi-model mean.

Added: « One should remind that as reality is a single realization of internal climate variability (REF), a model-observation comparison of this kind is intrinsically limited. »

Section 3.1. Last sentence: It would be useful to mention that the Barents Sea is subject to internally-generated decadal scale variations driven by ocean heat transport anomalies (for example see Yeager et al., 2015) which could explain some of the discrepancies between observations and models in that region.

Lines 244-245. It should be mentioned that internal variability may also play some role here in the discrepancy between the climate model and satellite data.

Both points were treated together. Thanks for recommending the Yeager reference. We added *“One should remind that as reality is a single realization of internal climate variability (Notz, 2015), a model-observation comparison of this kind is intrinsically limited. This could be of particular relevance in the Barents Sea, which is subject to internally-generated decadal scale variations driven by ocean heat transport anomalies (Yeager et al., 2015). »*

Lines 361-362. “This points to dynamical processes as most likely drivers …” I believe that you are making this argument because of the results from the 0-layer model. However, as mentioned above, the 0-layer model is missing many things in addition to dynamics. For example, the coupling to the atmosphere, which will change atmospheric conditions and fluxes could play an importan[t role].

We reworded into: « This points to transport processes (involving the atmosphere, sea ice, ocean, working individually or synergetically) as most likely drivers, »

REVIEWER #2

We thank the reviewer for his/her time and comments that improve our paper.

Main comments

1. CMIP5 model trends and R-values vary quite a bit spatially (Fig. 4,5 and S4). While this is not the main focus of the study, the manuscript would be improved by discussing the CMIP5 model differences instead of relating them generally to mean state errors. While the selected CMIP5 models may all produce mostly positive R-values, the large spatial differences between individual models indicate that the multi-model mean obscures a substantial amount of variability.

We followed your comment, without going towards of a listing of individual model differences, because then one could then wonder why we do not discuss individual models for all explored diagnostics.

Action. Section 2.2, we add:

The spatial distribution of ice seasonality diagnostics varies among models, reflecting a possible dependence on the mean state or differences in the treatment of ice dynamics.

In Section 3.1, we add:

Simulated trends by the mean of selected CMIP5 models are comparable with observations, in terms of ice retreat date (-4.4 ± 3.5 days / decade), ice advance date (5.9 ± 3.3 days / decade) and ice-free season duration (10.3 ± 6.3 days / decade), yet substantial inter-model spread exists (Fig. 3). Individual models show larger errors (Fig. S4 to compare with Fig.3), to be related notably with mean state issues. One common location where trends are underestimated is the North Atlantic region, in particular Barents Sea, which arguably reflects a weak meridional oceanic heat supply (Serreze et al., 2016). One should remind that as reality is a single realization of internal climate variability (Notz, 2015), a model-observation comparison of this kind is intrinsically limited. This could be of particular relevance in the Barents Sea, which is subject to internally-generated decadal scale variations driven by ocean heat transport anomalies (Yeager et al., 2015).

2. I suggest changing the header of the "Conclusions" section to "Summary and Discussion" for this manuscript. I understand and appreciate the authors' desire to connect the key points of the manuscript to broader implications. However, I maintain from my original comments that "Conclusions" should focus on the findings of the study, which have been shown in the results section. For example, the connections drawn in lines 363-367 should either be done as "discussion" or introduced in Section 3.5. They should not be introduced for the first time as conclusions.

We followed your comment.

Furthermore, since the authors hope to keep lines 368-380, I suggest limiting this part of the discussion to two distinct topics: (1) photosynthetic organisms and (2) shipping. These two examples are the most clearly impacted by the authors' conclusions (a greater change in ice advance versus retreat) out of those listed.

Following your comment, we remove « affects travel and hunting habits of coastal human communities (Huntington et al, 2017) ».

Other comments

Lines 54-55: The distinction between melt season and open water season has improved in this submission.

Thanks!

Line 78: The phrase "for sure" is too informal. I recommend saying "... and this is true in the Alaskan Arctic where they have been analyzed."

Thanks, we followed your comment.

Line 132: Figure S2 is more useful than the original Table S1 and should continue to be included in the supplementary material. To bolster this point, I recommend that the authors add additional text near line 132 describing why the interpolation error analysis using satellite observations is expected to be similar in the CMIP5 models.

Thanks, we reworded the group of sentences into *« These biases were determined from an analogous processing of satellite records. Dates of ice retreat and advance were derived from a daily interpolation of monthly averaged concentration fields, and subsequently compared to direct retrievals based on daily resolved concentration fields (see Fig S2). The identified biases apply to CMIP5 records, because errors stem from the processing of data, and do not depend on the type of data used (satellite or CMIP5). »*

Line 139: "Tangible" not the correct word here. Perhaps the word "visible" instead?

Thanks, your suggestion was followed.

Lines 175-177: It would be clearer to describe when exactly each timescales is used. It is too easy for the reader to mistakenly connect ***Rshort with 36 years and Rlong with 200 years.***

Thanks for insisting. We clarified into: "*For computations of Rlong and Rshort we use a reference period of 36 years. 36 years is the length of the available observation period and is close to the standard 30 years used in climate sciences. In one occasion (Table 1), we use 200 years as a reference period. 200 years is the total amount of years we can use to qualify changes and the most representative of a long climate change simulation. "*

Lines 203-206: At this location, the manuscript would benefit from a more substantial explanation of model differences.

We have considered your comment with greatest care. It is hard to find consistent patterns among the models, in terms of ice advance and retreat dates. It is also hard to disentangle these changes because of the lack of detailed enough diagnostics in CMIP5. Finally, discussing individual models here would also question why we do not do it elsewhere.

Action: we add a few more details on the inter-model differences in the second paragraph of Section 3.1:

> *« Simulated trends by the mean of selected CMIP5 models are comparable with observations, in terms of ice retreat date (-4.4 ± 3.5 days / decade), ice advance date (5.9 ± 3.3 days / decade) and ice-free season duration (10.3 ± 6.3 days / decade, Fig. 3). Individual models show larger errors (Fig. S4 to compare with Fig.3), to be related notably with mean state issues, or to the spread in the strength of strong oceanic currents, in the North Atlantic and the North Pacific.. One common location where trends are underestimated is the North Atlantic region, in particular Barents Sea, which arguably reflects a weak meridional oceanic heat supply (Serreze et al., 2016). One should remind that as reality is a single realization of internal climate variability (Notz, 2015), a model-observation comparison of this kind is intrinsically limited. This could be of particular relevance in the Barents Sea, which is subject to internally-generated decadal scale variations driven by ocean heat transport anomalies (Yeager et al., 2015). »*

Line 222: As far as I understand, the last paragraph was about satellite observations, but the topic sentence of this paragraph seems to be making a conclusion about the R-values of the CMIP5 models, which haven't been discussed yet. I recommend taking out the word "thus" or rephrasing this sentence.

Thanks for noting this subtle but important point. We removed « thus ».

Line 261: It would be clearer if there was a sentence here signalling that in the next section you will explore this mechanism (in addition to the header of Section 3.4).

Thanks for this piece of advice. We added « In the next section, we will study the link between ice retreat and advance in more detail. »

Lines 283-284: Please clarify if the 100-200% statistic refers to 100-200% of the winter contribution.

This comment is obsolete because of changes added to Section 4 following the comments of Reviewer #1.

Lines 309-310: Points (i)-(iii) seem to provide arguments for progressive emergence found in the 1-D model that are applicable to the CMIP5 models. If this is true, the sentence, "There are physical arguments…in the course of this century," should explain this instead of mentioning only the 1-D model.

This comment is obsolete due to changes in the conclusions.

Line 357: The phrase "turns up" is too informal. Perhaps the word "appears" instead?

Thanks, suggestion followed.

Arctic sea ice-free season projected to extend into fall

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Abstract

The recent Arctic sea-ice reduction comes with an increase in the ice-free season duration, with comparable contributions of earlier ice retreat and later advance. CMIP5 models all project that the trend towards later advance should progressively exceed and ultimately double the trend towards earlier retreat, causing the ice-free season to shift into fall. We show that such shift is a basic feature of the thermodynamic response of seasonal ice to warming. The detailed analysis of an idealised thermodynamic ice-ocean model stresses the role of two seasonal amplifying feedbacks. The summer feedback generates a 1.6-day later advance in response to a 1-day earlier retreat. The underlying physics are the property of the upper ocean to absorb solar radiation more efficiently than it can release heat right before ice advance. The winter feedback is comparatively weak, prompting a 0.3-day earlier retreat in response to a 1-day shift towards later advance. This is because a shorter growth season implies thinner ice, that subsequently faster melts away. However, the winter feedback is dampened by the relatively long ice growth period and by the inverse relationship between ice growth rate and thickness. At inter-annual time-scales, the thermodynamic response of ice seasonality to warming is obscured by inter-annual variability. Nevertheless, on the long term, because all feedback mechanisms relate to basic and stable elements of the Arctic climate system, there is little inter-model uncertainty on the projected long-term shift into fall of the ice-free season.

1. Introduction

Arctic sea ice has strikingly declined in coverage (Cavalieri and Parkinson, 2012), thickness (Kwok and Rothrock, 2009; Renner et al., 2014; Lindsay and Schweiger, 2015) and age (Maslanik et al., 2011) over the last four decades. CMIP5 global climate and Earth System Models simulate and project this decline to continue over the 21st century (Massonnet et al., 2012; Stroeve et al., 2012) due to anthropogenic CO_2 emissions (Notz and Stroeve, 2016), with a loss of multi-year ice estimated for 2040-2060 (Massonnet et al., 2012), in the case of a business-as-usual emission scenario.

Less Arctic sea ice also implies changes in ice seasonality, which are important to investigate because of socio-economic (e.g., on shipping, Smith and Stephenson, 2013) and ecosystem implications. Indeed, the length of the Arctic sea ice season exerts a first-order control on the light reaching phytoplankton (Arrigo and van Dijken, 2011; Wassmann and Reigstad, 2011, Assmy et al., 2017) and is crucial to some marine mammals, such as walruses (Laidre et al., 2015) and polar bears (Stern and Laidre, 2016), who use sea ice as a living platform.

Various seasonality diagnostics are discussed in the sea ice literature and definitions as well as approaches vary among authors. The open water season duration can be diagnosed from satellite ice concentration fields, either as the number of ice-free days (Parkinson et al., 2014), or as the time elapsed between ice retreat and advance dates, corresponding to the day of the year when ice concentration exceeds or falls under a given threshold (Stammerjohn et al., 2012; Stroeve et al., 2016). The different definitions of the length of the open water season can differ in subtleties of the computations (notably filtering) and may not always entirely be consistent and comparable. In addition, the melt season duration, distinct from the open water season duration, has also been analysed from changes in passive microwave emission signals due to the transition from a dry to a wet surface during melting (Markus et al., 2009; Stroeve et al., 2014).

As for changes in the Arctic open water season duration, satellite-based studies indicate an increase by >5 days per decade over 1979-2013 (Parkinson, 2014) due to earlier ice retreat and later advance (Stammerjohn et al., 2012; Stroeve et al., 2016). There are regional deviations in the contributions to a longer open water season duration, most remarkably in the Chukchi and Beaufort Seas where later ice advance takes over (Johnson and Eicken, 2016; Serreze et al., 2016), which has been attributed to increased oceanic heat advection from Bering Strait (Serreze et al., 2016). Such changes in the seasonality of Arctic ice-covered waters reflect the response of the ocean surface energy budget to warming. Indeed, warming and ice thinning imply earlier surface melt onset and ice retreat (Markus et al., 2009; Stammerjohn et al., 2012; Blanchard-Wrigglesworth et al., 2010). Besides, a shift towards later ice advance, tightly co-located with earlier retreat is observed, especially where negative sea-ice trends are large (Stammerjohn et al., 2012; Stroeve et al., 2016). This has been attributed to the ice-albedo feedback, namely to the combined action of (i) earlier ice retreat, implying lower surface albedo and (ii) higher annual solar radiation uptake by the ocean. Such mechanism (Stammerjohn et al., 2012) explains the ongoing delay in ice advance of a few days per decade from the estimated increase in solar absorption (Perovich et al., 2007), in accord with the observed in situ increase in the annual SST maximum (Steele et al., 2008; Steele and Dickinson, 2016).

The observed increase in the ice-free season duration should continue over the next century, as projected by the CESM-Large Ensemble (Barnhart et al., 2016), but this signal is obscured by important levels of internal variability. Other CMIP5 ESMs likely project a longer ice-free season as well, and this is true in the Alaskan Arctic where they have been analysed (Wang and Overland, 2015). In both these studies, the simulated future increases in the ice-free season duration are dominated by the later ice advance. Such behaviour remains unexplained and should be investigated from a larger set of models and regions.

In the present study, we aim at better quantifying the potential changes in Arctic sea ice seasonality and understanding the associated mechanisms. We first revisit the ongoing changes in Arctic sea ice retreat and advance dates using satellite passive microwave records, both at inter-annual and multi-decadal time scales. We also analyse, for the first time over the entire Arctic, all CMIP5 historical and RCP8.5 simulations covering 1900-2300 and study mechanisms at play using a one-dimensional ice-ocean model.

2. Methods

We analyse the recent past and future of sea ice seasonality by computing a series of diagnostics based on satellite observations, Earth System Models and a simple ice-ocean model.

2.1 Data sources

Passive microwave sea ice concentration (SIC) retrievals, namely the GSFC Bootstrap SMMR-SSM/I quasi-daily time series product, over 1980-2015 (Comiso, 2000, updated 2015), are used as an observational basis. We also use CMIP5 Earth System Model historical simulations and future projections of SIC. Because of high inter-annual variability in ice advance and retreat dates and because some models lose multi-year ice only late into the 21st century, we retain the 9 ESMs simulations that pursue RCP8.5 until 2300 (first ensemble member, Table 1). Analysis focuses on 1900-2200, combining historical (1900-2005) and RCP8.5 (2005-2200) simulations. 2200 corresponds to the typical date of year-round Arctic sea ice disappearance (Hezel et al., 2014). We also extracted the daily SST output from IPSL-CM5A-LR. All model outputs were interpolated on a 1° geographic grid.

To investigate how mean state biases may affect ESM simulations, we also included in our analysis a 1958-2015 forced-atmosphere ISPL-CM simulation, i.e. an ice-ocean simulation that was performed with the NEMO-LIM 3.6 model (Rousset et al., 2015), driven by the DFS5 atmospheric forcing (Dussin et al., 2015). NEMO-LIM 3.6 is very similar to the ice-ocean component of IPSL-CM5A-LR, except that (i) horizontal resolution is twice as high (1° with refinement near the poles and the equator) and (ii) a weak sea surface salinity restoring is applied. Such a simulation, not only performs generally better than a free-atmosphere ESM run in terms of seasonal ice extent (Fig S1; Uotila et al., 2017), but also has year-to-year variations in phase with observations, a feature that is intrinsically not captured in a coupled ESM. However, a caveat of forced-atmosphere simulations is the absence of feedback from the sea ice/ocean surface state onto atmospheric dynamics, which can affect the processes that drive changes in ice advance and retreat timing.

2.2 Ice seasonality diagnostics

We use slightly updated computation methods for ice retreat (d_r) and advance (d_a) dates, as compared with previous contributions (Parkinson, 1994; Stammerjohn et al., 2012; and Stroeve et al., 2016). Ice retreat date (d_r) is defined as the first day of the year where SIC drops below 15%, whereas ice advance date (d_a) is the first day of the year where SIC exceeds this threshold (Stroeve et al, 2016). The choice of the SIC threshold has no significant impact on the results. All previous studies recognise that a typical 5-day temporal filtering on the input ice concentration is required to get rid of short-term dynamical events (Stammerjohn et al., 2012; Stroeve et al., 2016). By contrast, we use 15 days, in order to get rid of most short-term dynamical ice events, which barely affects trends in d_r and d_a (see Table S1). Another important issue is the reference time axis, which varies among authors. To circumvent the effect of the d_a discontinuity between Dec 31 and Jan 1, we define the origin of time on Jan 1, and count d_a negatively if it falls between Jul 1 and Dec 31. Jul 1 is a safe limit, because there is no instance of ice advance date between early June and late July in the satellite record or in CMIP5 simulations. The length of the ice-free season is defined as the period during which SIC is lower than 15%.

The same seasonality diagnostics are computed from model outputs. Yet, since the long-term ESM simulations used here only have monthly SIC outputs, we compute the ice seasonality diagnostics based on monthly SIC fields linearly interpolated daily. Such operation drastically reduces error dispersion but introduces a small systematic bias on d_r (early bias) and d_a (late bias), on the order of 5 ± 5 (6) days. These biases were determined from an analogous processing of satellite records. Dates of ice retreat and advance were derived from a daily interpolation of monthly averaged concentration fields, and subsequently compared to direct retrievals based on daily resolved concentration fields (see Fig S2). The identified biases apply to CMIP5 records, because errors stem from the processing of data, and do not depend on the type of data used (satellite or CMIP5). These small systematic biases in model ice retreat and advance dates likely contributes to the mean model bias compared to satellite data (Table 1, Fig. 1), but remains small compared to the long-term signals analysed throughout this paper.

The ice seasonality diagnostics and their spatial distribution are reasonably well captured by the mean of selected CMIP5 models over the recent past (Fig. 2). The spatial distribution of ice seasonality diagnostics varies among models, reflecting a possible dependence on the mean state or differences in the treatment of ice dynamics. Larger errors in some individual models (Fig. S3) are associated with an inaccurate position of the ice edge. Overall, ESMs tend to have a shorter open water season than observed (Fig 2a-c and S3), which is visible in the North Atlantic and North Pacific regions and can be related to the systematic bias due to the use of interpolated monthly data, but also to the tendency of our model subset to overestimate sea ice. Such an interpretation is supported by (i) the visibly better consistency of the simulated ice seasonality diagnostics with observations in the forced-atmosphere ISPL-CM simulation than in IPSL-CM5A-LR and (ii) by the fact that models with simulated ice extent rather close to observations over the recent past (CESM, CNRM or MPI; Massonnet et al., 2013) are more in line with observed seasonality diagnostics than the other models (Fig. 2 and S3).

2.3. Trends in ice advance and retreat dates, and related diagnostics

Trends in ice retreat and advance dates were calculated for each satellite or model pixel, from the slope of a least-square fit over a given period, using years where both d_r and d_a are defined. If the number of years used for calculation of the trend is less than 1/3 of the considered period, a missing value is assigned. 1/3 compromises between spatial and temporal coverage of the considered time-series (see Tab. S1).

To describe the relative contribution of ice advance and retreat dates to changes in open water season duration, we introduce a first diagnostic, termed the *long-term ice advance vs. retreat amplification coefficient* ($R_{a/r}^{long}$). $R_{a/r}^{long}$ is defined as minus the ratio of trends in ice advance to trends in ice retreat dates. The sign choice for $R_{a/r}^{long}$ is such that positive values arise for concomitant long-term trends toward later ice advance and earlier retreat. $R_{a/r}^{long}$ gives synthetic information about trends in ice advance and retreat dates within a single diagnostic. For example, $R_{a/r}^{long} > 0$ means that a trend towards earlier retreat ($d_r < 0$) occurs concurrently with a trend towards later advance ($d_r > 0$). Strictly speaking $R_{a/r}^{long} > 0$ could also indicate later retreat and earlier advance (i.e. a reduction of open water season duration), which does not happen in a warming climate. Moreover, by definition, $R_{a/r}^{long} > 1$ if the long-term trend in ice advance date exceeds the long-term trend in retreat date in a particular pixel, otherwise $R_{a/r}^{long} < 1$. Note that for $R_{a/r}^{long}$ to be meaningful, we restrict computations to pixels where trends in both d_r and d_a are significant at a specified confidence level. $p=0.05$, i.e a 95% confidence interval gives the most robust value but heavily restricts the spatial coverage, especially for CMIP5 outputs. By contrast, $p=0.25$, i.e. a 75% confidence interval slightly expands coverage, but loses some robustness.

In order to study the shorter-term association between retreat and ice advance, we introduce a second diagnostic, termed the *short-term ice advance vs retreat amplification coefficient* ($R_{a/r}^{short}$). $R_{a/r}^{short}$ is defined by applying the same reasoning to inter-annual time scales, as minus the linear regression coefficient between detrended ice advance and retreat dates. $R_{a/r}^{short}$ gives information on how anomalies in ice advance date scale with respect to anomalies in retreat dates over the same year, regardless of the long-term trend. Such definition warrants comparable interpretation for $R_{a/r}^{short}$ and $R_{a/r}^{long}$. In a warming climate, $R_{a/r}^{short} > 0$ indicates concomitant anomalies towards earlier retreat and later advance, and $R_{a/r}^{short} > 1$ indicates that anomalies in advance date are larger than in retreat date.

For computations of $R_{a/r}^{long}$ and $R_{a/r}^{short}$ we use a reference period of 36 years. 36 years is the length of the available observation period and is close to the standard 30 years used in climate sciences. In one occasion (Table 1), we use 200 years as a reference period. 200 years is the total amount of years we can use to qualify changes and the most representative of a long climate change simulation.

All trends and ice advance vs. retreat amplification coefficients given in the rest of the text are median (± inter-quartile range), taken over the seasonal ice zone. We use non-parametric statistics because the distributions are not Gaussian.

2.4 1D model

We use the Semtner (1976) zero-layer approach for ice growth and melt above an upper oceanic layer taking up heat, whereas snow is neglected. The model simplifies reality by assuming constant mixed-layer depth, no horizontal advection in ice and ocean, and no heat exchange with the interior ocean. The ice-ocean seasonal energetic cycle is computed over 300 years, using climatological solar, latent and sensible heat fluxes and increasing downwelling long-wave radiation, to represent the greenhouse effect. Ice retreat and advance dates are diagnosed from model outputs (see Appendix A for details). We argue that the Semtner (1976) zero-layer approach is appropriate to study the response of CMIP5 models to warming, as the CMIP5 models with more complicated thermodynamics cannot be distinguished from those using the Semtner 0-layer approach (Massonnet et al., 2018).

3. Link between earlier ice retreat and later ice advance in observations and models

3.1 Trends in ice advance and retreat date in observations and models

Over 1980-2015, the ice-free season duration has increased by 9.9 ± 10.6 days / decade, with nearly equal contributions of earlier ice retreat (-4.8 ± 7.7 days / decade) and later ice advance (4.9 ± 5.8 days /decade, median based on satellite observation, updated figures, see Table S1). Variability is high however. Significant trends in both d_r and d_f at the 95% confidence level are found over a relatively small fraction (22%) of the seasonal ice zone (Fig. 3), independently of the details of the computation (Tab. S1). The patterns of changes are regionally contrasted, and Chukchi Sea is the most notable exception to the rule, where later ice advance clearly dominates changes in the ice-free season (Serreze et al., 2016, Fig. 3).

Simulated trends by the mean of selected CMIP5 models are comparable with observations, in terms of ice retreat date (-4.4 ± 3.5 days / decade), ice advance date (5.9 ± 3.3 days / decade) and ice-free season duration (10.3 ± 6.3 days / decade, Fig. 3). Individual models show larger errors (Fig. S4 to compare with Fig.3), to be related notably with mean state issues, or to the spread in the strength of strong oceanic currents, in the North Atlantic and the North Pacific. One common location where trends are underestimated is the North Atlantic region, in particular Barents Sea, which arguably reflects a weak meridional oceanic heat supply (Serreze et al., 2016). One should remind that as reality is a single realization of internal climate variability (Notz, 2015), a model-observation comparison of this kind is intrinsically limited. This could be of particular relevance in the Barents Sea, which is subject to internally-generated decadal scale variations driven by ocean heat transport anomalies (Yeager et al., 2015).

3.2 Earlier sea ice retreat implies later ice advance

In terms of mean state and contemporary trends, models seem realistic enough for an analysis of changes at pan-Arctic scales but might be less meaningful at regional scales. We first study the contemporary link between earlier retreat and ice advance by looking at the sign of $R_{a/r}$'s in contemporary observations and models. Because $R_{a/r}^{long}$ is a ratio of significant trends, and because all models have regional differences as to where trends are significant, we base our analysis on individual models.

Based on observations (Fig. 4), we find positive values of $R_{a/r}^{long}$ in more than 99% of grid points in the studied zone, provided that computations are restricted where trends on ice retreat and advance dates are significant at a 95% level (N=5257). In a warming climate, Positive $R_{a/r}^{long}$ values mean concomitant and significant trends towards earlier retreat and later advance, whereas missing values reflect either that the trends are not significant or that the point is out of the seasonal ice zone. $R_{a/r}^{short}$ (Fig. 6) is generally smaller (0.21 ± 0.27) than $R_{a/r}^{long}$ (0.71 ± 0.42, 95% confidence level), and also positive in most pixels (87% of 23475 pixels).

CMIP5 models are ~~thus~~ consistent with the robust link between earlier ice retreat and later advance dates found in observations (Stammerjohn et al., 2012; Stroeve et al., 2016). More generally, we find a robust link between earlier retreat and later advance in all cases: both $R_{a/r}$'s are virtually always positive for short and long-term computations, from observations and models (Fig. 4, 5) over the three analysed periods (1980-2015 for observations and models, 2015-2050 and 2050-2085 for models only) and regardless of internal variability (Fig S5 and S6). This finding expands previous findings from satellite observations using detrended time series (Stammerjohn et al., 2012; Serreze et al, 2016; Stern and Laidre, 2016), in particular the clear linear correlation found between detrended ice retreat and ice advance dates (Stroeve et al., 2016). Following these authors, we attribute the strong earlier retreat / later ice advance relationship as a manifestation of the ice-albedo feedback: earlier ice retreat leads to an extra absorption of heat by the upper ocean. This heat must be released back to the atmosphere before the ice can start freezing again, leading to later ice advance. Such mechanism, also supported by satellite SST analysis in the ice-free season (Steele et al., 2008; Steele and Dickinson, 2016), explains the sign of the changes in ice advance date. However, it does not explain the relatively larger magnitude of the trends in ice advance date as compared with trends in ice retreat date, studied in the next section.

3.3 Increasingly late ice advance dominates future changes in open water season

We now focus on the respective contribution of changes in retreat and ice advance dates to the increasingly long open water season, by analysing the magnitude of $R_{a/r}^{long}$. Contemporary values of $R_{a/r}^{long}$ match between model and observations but not spatially (Fig. 4). Over 1980-2015 the simulated $R_{a/r}^{long}$ (CMIP5 mean) is slightly higher (1.1 ± 0.7) than the observational value (0.7 ± 0.4). Since none of the models positions the sea ice edge correctly everywhere, it is not surprising that the spatial distribution and the modal $R_{a/r}^{long}$ differs among models and between models and observations. The fact that, by definition, satellite data only sample one realization of internal variability could contribute to the discrepancy as well. In support of these two arguments, the forced-atmosphere ISPL-CM simulation better simulates the spatial distribution of $R_{a/r}^{long}$ (see Fig. S7), which underlines the role of mean state errors.

As far as future changes are concerned, all models show a qualitatively similar evolution (Fig. 1 and S5). Projected changes in ice retreat and ice advance dates start by approximately 2000 and continue at a nearly constant pace from 2040 until 2200. By 2040, the trend in ice advance date typically becomes larger than the trend in ice retreat date, as indicated by the corresponding mean $R_{a/r}^{long}$=1.8 ± 0.4 over 2000-2200 (Table 1).

To further understand these contrasting trends between ice retreat and ice advance dates, we mapped $R_{a/r}^{long}$, over 2015-2050 and 2050-2085. We find that, in the course of the 21st century, trends in retreat and ice advance date become significant over increasingly wide regions. The overall $R_{a/r}^{long}$ value increases, as illustrated in Fig. 4. This behaviour is found independent of the considered model and of the internal variability (Fig. S5 and S6).

This finding expands the recent analyses of the CESM Large-Ensemble project (Barnhart et al., 2016); and of Alaskan Arctic sea ice in CMIP5 models, finding faster ice coverage decrease in fall than in spring (Wang and Overland, 2015). Both studies propose that the extra heat uptake in the surface ocean due to an increased open water season as a potential explanation. As suggested earlier, this indeed explains why $R_{a/r}^{long}$ would be positive but does not explain the amplified delay in ice advance date, that is, why $R_{a/r}^{long}$ would be > 1. We are now addressing this question.

3.4 A thermodynamic mechanism for an amplified delay in ice advance date

The reason why $R_{a/r}^{long}$ becomes > 1 by 2040 is related to the asymmetric response of ice-ocean thermodynamics to warming: the upper ocean absorbs solar radiation about twice as efficiently as it can release heat right before ice advance. That summer feedback processes dominate is enabled by a relatively weak winter feedback (between later ice advance and earlier retreat the next year).

To come to this statement, CMIP5 diagnostics proved helpless, as they do not offer sufficient diagnostics to study this response in detail, in particular lacking a daily description of the surface energy budget. This is why we used a 1D thermodynamic model of sea ice growth and melt in relation with the upper ocean energy budget (Semtner, 1976), to study the idealised thermodynamic response of seasonal ice to a radiative forcing perturbation. Without any particular tuning, the 1D model simulations feature an evolution that is similar to the long-term behaviour of CMIP5 models (Fig. 1b), with trends in ice advance date (8 days/decade) of larger absolute magnitude than trends in retreat date (−5 days/decade), giving a corresponding value of $R_{a/r}^{long} = 1.9$. All figures fall within the CMIP5 envelope (Tab. 1).

As explained above, the seasonal relationships between ice advance and retreat dates are underpinned by atmosphere-ice-ocean feedbacks. The non-radiative feedback framework of Goosse et al. (2018, see Appendix A for details) clarifies the study of these relationships. Changes in dates of ice retreat (Δd_r) and advance (Δd_a) in response to a radiative forcing perturbation are split into reference and feedback response terms:

$$\begin{cases} \Delta d_r = \Delta d_r^{ref} - \lambda_w \Delta \mathrm{d}_a, \\ \Delta d_a = \Delta d_a^{ref} - \lambda_s \Delta \mathrm{d}_r. \end{cases}$$

The sign convention for the feedback terms is such that the link between earlier retreat ($\Delta d_r < 0$) and later advance ($\Delta d_a > 0$) gives positive feedback factors. The feedback response refers to the change in d_r (resp. d_a) that can solely be attributed to the change in d_a (resp. d_r). It is expressed using a feedback factor λ_w (resp. λ_s) related to winter (resp. summer) feedback processes. The reference response Δd_r^{ref} (resp. Δd_a^{ref}) is that of a virtual system in which the feedback would be absent. Expressions for the reference and feedback response terms, as well as for feedback factors stem from physical analysis, detailed in Appendix A.

According to this analysis, feedbacks between the dates of retreat and advance dominate the thermodynamic response of ice seasonality (Fig. 5): the reference response to the applied perturbation of 0.1 $W/m^2/yr$ is -0.2 d/yr of earlier retreat and 0.1 d/yr of later advance.

Ice growth and melt processes generate a relatively weak *winter* amplifying feedback of ice advance date onto ice retreat date: a shorter growth season implies thinner ice, that subsequently faster melts away. The winter feedback factor is (see Appendix A for derivation)

$$\lambda_w = \frac{1}{2} \cdot \left(\frac{d_r - d_h}{d_h - d_a} \right),$$

where d_h is the date of maximum ice thickness, is solely function of the ice growth and melt seasonal parameters. λ_w has a rather stable value of 0.31 ± 0.04 over the 127 years of simulated seasonal ice. This value of λ_w indicates a feedback response in ice retreat date of about ~1/3 of the change towards later ice advance the previous fall. λ_w is < 1 for two reasons. First the melt season is shorter than the growth season (Perovich et al., 2003), hence changes in ice advance date translate into weaker changes in ice retreat date. Second, the ice growth rate is larger for thin than for thick ice (Maykut, 1986), hence the maximum winter ice thickness does not decrease due to later advance as much as if the growth rate was constant.

Energetics of the summer ice-free ocean generate a *summer* amplifying feedback of ice retreat date onto ice advance date, much stronger than the winter feedback. The summer feedback factor is (see Appendix A for derivation)

$$\lambda_s = -\frac{\langle Q_+ \rangle}{\langle Q_- \rangle},$$

where $\langle Q_+ \rangle$ and $\langle Q_- \rangle$ are the absolute values of average net positive (negative) atmosphere-to-ocean heat fluxes during the ice free-period. 1D model diagnostics give an average value of 1.63 ± 0.18 for λ_s, meaning that earlier retreat implies a feedback delay in ice advance of ~1.6 times the initial change in ice retreat date. Physically, the strength of the summer feedback is in direct relation with the ice-free upper ocean energy budget and the evolution of SST. $\langle Q_+ \rangle$ mostly corresponds to net solar flux, typically 150 W/m^2, and is typically larger than $\langle Q_- \rangle$, which corresponds to the net non-solar, mostly long-wave heat flux, at freezing temperatures, typically 75-150 W/m^2 (See Appendix B). Hence, after ice retreat, the SST rapidly increases due to solar absorption into the mixed layer and then decreases much slower until freezing, due to non-solar ocean-to-atmosphere fluxes (Fig. 7a), an evolution that is similar to a recent satellite-based analysis (Steele and Dickinson, 2016). In other words, the energy excess associated with later retreat, stored into the surface ocean, takes extra time to be released before ice advance.

In practise, keeping only the dominant term, $R^{long}_{a/r}$ (the seasonality of the system) reduces to the summer feedback factor:

$$R^{long}_{a/r} \approx \lambda_s, \quad (4)$$

$R^{long}_{a/r}$ appears to vary little among CMIP5 models and even the 1D model. Why this could be the case is because the winter and summer feedback factors are controlled by very basic physical processes of the Arctic ice-ocean-climate system, and therefore feature relatively low uncertainty levels. Celestial mechanics, ubiquitous clouds and near-freezing temperatures provide strong constraints on the surface radiation balance, hence on the summer feedback factor, that all models likely capture. All models also include the growth and melt season asymmetry and the growth-thickness relationship (see Massonnet et al., 2018) at the source of the relatively weak winter feedback. In IPSL-CM5A-LR, the sole model for which we could retrieve daily SST (Fig. 7b), the evolution of the summer SST in seasonally ice-free regions features a rapid initial increase followed by slow decrease, an indication that the mechanism we propose is sensible.

3.5 Inter-annual variability and extra processes add to the purely thermodynamic response

The CMIP5 response of ice seasonality differs from the idealised thermodynamic response in two notable ways. First, $R_{a/r}^{long}$>1 only clearly emerges by 2040 in CMIP5 models. Second, $R_{a/r}^{long}$ is typically <1 over the recent past (1980-2015) from the satellite record (Fig. 4). This must be due to the contribution of processes absent from the 1D model.

As to why the 1D response would emerge in the course of this century, there are a series of potential reasons that we cannot disentangle with the limited available CMIP5 outputs. (i) The contribution of the sub-surface ocean to the surface energy budget, neglected in the 1D approach, is likely larger today than in the future Arctic. Over the 21st century, the Arctic stratification increases in CMIP5 models (Vancoppenolle et al., 2013; Steiner et al., 2014), whereas the oceanic heat flux convergence should decrease (Bitz et al, 2005). (ii) The solar contribution to the upper ocean energy budget is smaller today than in the future, as the date of retreat falls closer to the summer solstice. (iii) The surface energy budget is less spatially coherent today than in the future, when the seasonal ice zone moves northwards. The solar radiation maximum drastically changes over 45 to 65°N but has small spatial variations above the Arctic circle (Peixoto and Oort, 1992). Note that in some specific regions, $R_{a/r}^{long}$ is already >1, in particular in Chukchi Sea, but this has been associated to the summer oceanic heat transport through Bering Strait (Serreze et al., 2016) which is a localized event, that does not explain why $R_{a/r}^{long}$ would globally become >1 in the future.

The aforementioned processes, ignored in the 1-D model may explain why $R_{a/r}^{long}$> 1 would emerge by mid-century, but internal variability, also absent in the 1-D model, should also be considered (Barnhart et al., 2016). It is remarkable that $R_{a/r}^{short}$ is < 1 both from satellite records and from CMIP5 model simulations, for all periods and models considered (Fig. 6). This suggests that the ice advance amplification mechanism is not dominant at inter-annual time scales. Indeed, based on inter-annual satellite time series, the standard deviation of ice retreat (STD=21.6 days) and advance dates (STD=14.3 days) is high (Stroeve et al., 2016) and the corresponding trends over 1980-2015 are not significant. Conceivably, atmosphere, ocean and ice horizontal transport, operating at synoptic to inter-annual time scales, obscure the simple thermodynamic relation between the ice retreat and advance dates found in the 1D model. For instance, the advection of sea ice on waters with temperature higher than the freezing point would imply earlier ice advance. Altogether, this highlights that the ice advance amplification mechanism is a long-term process and stress the importance of the considered time scales and period as previous studies have already shown (Parkinson et al., 2014; Barnhart et al., 2016).

4. Summary and discussion

The analysis presented in this paper, focused on changes in sea ice seasonality and the associated driving mechanisms, raised the following new findings:

1. All CMIP5 models consistently project that the trend towards later advance progressively exceeds and ultimately doubles the trend towards earlier retreat over this century, causing the ice-free season to shift into fall.
2. The long-term shift into fall of the ice-free season is a basic feature of the thermodynamic response of seasonal ice to warming.
3. The thermodynamic shift into fall of the ice-free season is caused by the combination of relatively strong summer and relatively weak winter feedback processes.
4. Thermodynamic processes only explain the long-term response of ice seasonality, not the inter-annual variations, nor the delayed emergence of the long-term response, which are both consistently simulated features among CMIP5 models.

A central contribution of this paper is the detailed study of the mechanisms shaping the thermodynamic response of sea ice seasonality to radiative forcing in the Semtner (1976) ice-ocean thermodynamic model, using the non-radiative feedback framework of Goosse et al. (2018). The low seawater albedo as compared with ice and the enhanced solar radiation uptake by the ocean had previously been put forward to explain the increase in the length of the open water season (Stammerjohn et al., 2012). Our analysis completes this view. Extra solar heat reaching the ocean due to earlier ice retreat is absorbed at a higher rate than it can be released until ice advance. This provides a powerful feedback at the source of the shift into fall of the open water season. In addition, the link between later advance and earlier retreat the next spring is weak, because of the damping effects of the long ice growth period and of the inverse relationship between growth rate and ice thickness. All of those processes are simple enough to be captured by most of the climate models, which likely explains why the different models are so consistent in terms of future ice seasonality.

The link between earlier ice retreat and later advance is found in both satellite retrievals and climate projections, regardless of the considered period and time scale, expanding findings from previous works (Stammerjohn et al., 2012; Serreze et al, 2016; Stern and Laidre, 2016; Stroeve et al., 2016) and further stressing the important control of thermodynamic processes on sea ice seasonality. Yet, two notable features are in contradiction with the thermodynamic response of seasonal ice to warming. First, the long-term response of ice seasonality to warming only appears by mid-century in CMIP5 simulations, when changes in the ice-free season emerge out of variability (Barnhart et al., 2016). Second, changes in ice retreat date are larger than changes in ice advance date at inter-annual time scales. Transport or coupling processes (involving the atmosphere, sea ice, ocean) are the most likely drivers but their effect could not be formally identified because of the lack of appropriate diagnostics in CMIP5. Such setup, with a long-term control by thermodynamic processes has other analogues in climate change studies (Bony et al., 2004; Kröner et al., 2017; Shepherd, 2014), ~~The suggested increase in the ice-free season and shift into fall are to be put in the context of broader seasonal changes in the climate system. Global warming induces changes in the seasonal cycle of surface temperature (Thomson, 1995), both in terms of amplitude and phase (Dwyer et al., 2012), in relation with the surface energy fluxes and the presence of sea ice (Dwyer et al., 2012; Donohoe and Battisti, 2013).~~

As the Arctic sea ice seasonality is a basic trait of the Arctic Ocean, a shift of the Arctic sea ice-free season would also have direct ecosystem and socio-economic impacts. The shift in the sea ice seasonal cycle will progressively break the close association between the ice-free season and the seasonal photoperiod in Arctic waters, a relation that is fundamental to photosynthetic marine organisms existing in present climate (Arrigo and van Dijken, 2011). Indeed, because the ice advance date is projected to overtake the onset of polar night (Fig. 1), typically by 2050, changes in the photoperiod are at this point solely determined by the ice retreat date, and no more by advance date. The duration of the sea ice season also ~~affects travel and hunting habits of coastal human communities (Huntington et al, 2017) and~~ restricts the shipping season (Smith and Stephenson, 2013; Melia et al., 2017). The second clear implication of the foreseen shift of the Arctic open water season is that the Arctic navigability would expand to fall, well beyond the onset of polar night, supporting the lengthening of the shipping season mostly by later closing dates (Melia et al., 2017).

Better projecting future changes in sea ice and its seasonality is fundamental to our understanding of the future Arctic Ocean. Detailed studies of the drivers of sea ice seasonality, in particular the upper ocean energy budget, the role of winter and summer feedbacks and the respective contribution of thermodynamic and dynamic processes are possible tracks towards reduced uncertainties. Further knowledge can be acquired from observations (e.g. Steele and Dickinson, 2016) and Earth System Model analyses, for which the expanded set of ice-ocean diagnostics expected in CMIP6, including daily ice concentration fields (Notz et al., 2016) will prove instrumental.

Code, data and sample availability

Scripts available upon request.

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Appendices

Appendix A: Upper ocean energetics and ice seasonality in the 1D ice-ocean model

To characterize the purely thermodynamic response of seasonal ice to a radiative forcing perturbation, we use the Semtner (1976) zero-layer approach for ice growth and melt above an upper oceanic layer taking up heat. Snow is neglected. The ice model equations for surface temperature (T_{su}) and ice thickness (h) read:

$$Q_{atm}(T_{su}) = Q_c(T_{su}), \quad (1)$$

$$\rho L \frac{dh}{dt} = Q_{atm}(T_{su}) + Q_w. \quad (2)$$

where $Q_{atm} = Q_0 + Q_{sol}(1 - \alpha_i) - \epsilon\sigma T_{su}^4$, with Q_0 the sum of downwelling longwave, latent and sensible heat fluxes, Q_{sol} the incoming solar flux, $\alpha_i = 0.64$ the ice albedo, $\epsilon = 0.98$ the emissivity and $\sigma = 5.67 \times 10^{-8}$ W/m^2/K^4 the Stefan-Boltzmann constant. Q_c is the heat conduction flux in the ice (> 0 downwards), Q_w is the ocean-to-ice sensible heat flux at the ice base, $\rho = 900$ kg/m^3 is ice density and $L = 334$ kJ/kg is the latent heat of fusion. Once the ice thickness vanishes, the water temperature T_w in a $h_w = 30$ m-thick upper ocean layer follows:

$$\rho_w c_w \frac{\partial T_w}{\partial t} h_w = Q_0 + Q_{sol}(1 - \alpha_w)[1 - exp(-\kappa h_w)] - \epsilon\sigma T_w^4. \quad (3)$$

$\rho_w = 1025$ kg/m^3 is water density, $c_w = 4000$ J/kg/K is water specific heat, $\kappa_w = 1/30$ m^{-1} is the solar radiation attenuation coefficient in water. Ice starts forming back once T_w returns to the freezing point $T_f = -1.8$°C.

The atmospheric solar (Q_{sol}) and non-solar (Q_0) heat fluxes are forced using the classical standard monthly mean climatologies, typical of Central Arctic conditions (Fletcher, 1965). We impose $Q_w = 2$ W/m^2 following Maykut and Untersteiner (1971). We add a radiative forcing perturbation $\Delta Q = 0.1$ W/m^2 to the non-solar flux each year to simulate the greenhouse effect. Ice becomes seasonal after 127 years. The model is run until there is no ice left, which takes 324 years.

The following diagnostics of the ice-ocean seasonality (see Fig. A1) are derived from 1D model outputs:

- d_r (*ice retreat date*): the first day with $T_w > T_f = -1.8°C$;

- d_a (*ice advance date*): the last day with $T_w > T_f = -1.8°C$;

Two other markers of the ice-ocean seasonality prove useful and were also diagnosed:

- d_T (*maximum water temperature date*): the last day with $Q > 0$.

- d_h (*maximum thickness date*): the date of maximum ice thickness.

The simulated trend towards later ice advance is on average 1.9 times the trend towards earlier retreat, a value consistent with the CMIP5 value. An advantage of the 1D model is that the required diagnostics to investigate the ice seasonality drivers are easily available.

Nevertheless, the response of ice seasonality is not straightforward, because there are feedbacks between ice retreat and advance dates. First, later advance delays ice growth, reduces the winter maximum thickness, and, in turn, implies earlier retreat. Second, earlier retreat adds extra solar heat to the upper ocean, delaying ice advance. To understand the changes in ice seasonality and attributing their causes, we apply the non-radiative feedback framework introduced by Goosse et al. (2018).

A.1 Analysis framework

We split the changes in ice retreat (Δd_r) and advance (Δd_a) dates in response to a radiative forcing perturbation into *reference* and *feedback* contributions (Goosse et al., 2018):

$$\begin{cases} \Delta d_r = \Delta d_r^{ref} - \lambda_w \Delta d_a, \\ \Delta d_a = \Delta d_a^{ref} - \lambda_s \Delta d_r. \end{cases} \quad (4)$$

The reference response in ice retreat date to the perturbation (Δd_r^{ref}) is defined using a virtual reference system where winter feedbacks (from d_a onto d_r) would not operate. The feedback response (Δd_r^{fb}) is the total minus the reference response and is assumed proportional to the change in ice advance date (Δd_a). Equivalently it is the part of the total change in d_r that can solely be linked to changes in d_a in the previous fall. The feedback factor λ_w quantifies the strength of this link. The sign convention is such that concomitant later advance ($\Delta d_a > 0$) and earlier retreat ($\Delta d_r > 0$) give a positive feedback factor. The definitions for the feedback and reference response terms in ice advance date are similar, but the summer feedback factor λ_s quantifies the link between earlier retreat and later advance in the same year.

A.2 Winter response

To formulate what determines the changes in ice retreat date, we focus on the ice season (Fig. A1) and use the maximum ice thickness to connect d_a to d_r. The ice thickness increases from zero on $d = d_a$ until a maximum h^{max} reached when $d = d_h$. Stefan's law of ice growth (Stefan, 1890) gives

$$h^{max} \approx \sqrt{-\frac{2k\langle T_{su}\rangle}{\rho L}.(d_h - d_a)}, \tag{5}$$

where $\langle T_{su}\rangle$ is the surface temperature averaged over $[d_a, d_h]$, i.e. over the ice growth period. Stefan's law is not exact but precise enough, reproducing the simulated annual values of h^{max} within 2±2% of the 1D model simulation over the 197 years of seasonal ice. The other advantage of Stefan's ice thickness is to be differentiable. Defining $v = k/(\rho L h^{max})$, the change in ice thickness due to the radiative forcing perturbation is, after linearisation,

$$\Delta h^{max} = v.\langle T_{su}\rangle.\left[\Delta d_a - \Delta d_h + (d_a - d_h)\frac{\Delta\langle T_{su}\rangle}{\langle T_{su}\rangle}\right]. \tag{6}$$

Now, to connect the maximum ice thickness to the ice retreat date, we consider the melt season. The ice melts from h^{max} on $d = d_h$ until ice thickness vanishes on $d = d_r$. Hence

$$h^{max} = \langle m \rangle . (d_r - d_h), \quad (7)$$

where $\langle m \rangle$ is the average melt rate, assumed to be negative.

We now combine growth and melt seasons and eliminate h^{max}. Differentiating (7), then injecting Δh^{max} from (6) and dividing by $\langle m \rangle$, we get:

$$\frac{\Delta\langle m \rangle}{\langle m \rangle} . (d_r - d_h) + \Delta d_r - \Delta d_h = \frac{v.\langle T_{su} \rangle}{\langle m \rangle} . \left[\Delta d_a - \Delta d_h + (d_a - d_h) \frac{\Delta\langle T_{su} \rangle}{\langle T_{su} \rangle} \right]. \quad (8)$$

Using Stefan's law (equation 5) to replace h^{max} in the definition of v, the first factor on the right-hand side of (8) can be rewritten as:

$$\frac{v.\langle T_{su} \rangle}{\langle m \rangle} = -\frac{1}{2} . \left(\frac{d_r - d_h}{d_h - d_a} \right) \equiv -\lambda_w .$$

(9)

Substituting (9) into (8) and rearranging terms gives the desired decomposition between reference and feedback responses:

$$\Delta d_r = \Delta d_r^{ref} - \lambda_w \Delta d_a, \quad (10)$$

where the reference response gathers all terms independent on Δd_a:

$$\Delta d_r^{ref} = (1 - \lambda_w)\Delta d_h + (d_r - d_h) . \left(\frac{\Delta\langle T_{su} \rangle}{2\langle T_{su} \rangle} - \frac{\Delta\langle m \rangle}{\langle m \rangle} \right). \quad (11)$$

The terms on the right-hand side reflect the contributions of (i) changes in the date of maximum thickness, (ii) changes in surface temperature and (iii) changes in surface melt rate. The feedback term in (10) isolates the contribution of changes in ice advance date and λ_w now clearly appears as a feedback factor. To compute the forced and feedback terms from model output, the annual time series of $\langle T_{su} \rangle$, $\langle m \rangle$ and d_h were extracted from model outputs.

The proposed decomposition (10) is supported by analysis: the sum of calculated reference and feedback responses (black dashed line in Fig. A2a) matches the total change in ice retreat date as diagnosed from model output (yellow line in Fig. A2a).

A.3 Summer forced and feedback responses.

The link between ice advance date and the previous ice retreat date stems from the conservation of energy in the ice-free upper ocean. Once ice disappears on $d = d_r$, the upper ocean takes up energy (see Figure A1). The surface ocean temperature T_w increases from the freezing point until a maximum, reached on $d = d_T$. Then the upper ocean starts losing energy, and T_w decreases, reaching the freezing point at the date of ice advance d_a. Over this temperature path, the energy gain from d_a to d_T must equal the energy loss from d_T to d_a:

$$\langle Q_+ \rangle (d_T - d_r) = -\langle Q_- \rangle (d_a - d_T), \qquad (12)$$

where $\langle Q_+ \rangle$ is the average net heat flux from the atmosphere to the upper ocean over $[d_r, d_T]$ and $\langle Q_- \rangle$ is the average net heat flux over $[d_{max}, d_a]$. Defining

$$\lambda_s = -\frac{\langle Q_+ \rangle}{\langle Q_- \rangle}, \qquad (13)$$

and rearranging terms in (12), we relate d_a to d_r via surface energy fluxes:

$$d_a = -\lambda_s d_r + d_T(1 + \lambda_s). \qquad (14)$$

By differentiating this expression, we get the sought decomposition between reference and feedback responses:

$$\Delta d_a = \Delta d_a^{ref} - \lambda_s \Delta d_r. \qquad (15)$$

The reference response groups all terms independent of Δd_r:

$$\Delta d_r^{ref} = -d_r \Delta \lambda_s + \Delta d_T + \Delta(\lambda_s d_T). \qquad (16)$$

The terms on the right-hand side reflect the contributions of (i) changes in energy fluxes, (ii) change in the date of maximum water temperature, and (iii) non linearities between both. The feedback term in (15) isolates the contribution of changes in ice retreat date and λ_s clearly now appears as a feedback factor. To compute the reference and feedback terms from the 1D model output, the annual time series of $\langle Q_+ \rangle$, $\langle Q_- \rangle$ and d_T were extracted.

Analysis supports the proposed decomposition: the sum of calculated feedback and reference responses (black dashed curve in Fig. A2a) is equal to the total response diagnosed from model outputs (yellow curve in Fig. A2a).

A.4 Analysis

Forced and feedback responses clarify the drivers of the shift into fall that characterises the thermodynamic response of ice seasonality to the perturbation of the radiative forcing. The response of the system is dominated by changes in ice advance date, which are by far dominated by the feedback response (0.8 d/yr), much larger than the reference response (0.1 d/yr, see Fig. A2a). The summer feedback factor λ_s, equal on average to 1.63, largely amplifies changes in retreat date. The positive sign of λ_s indicates that earlier retreat implies later advance. Why $\lambda_s > 1$ is because positive heat fluxes into the ocean $\langle Q_+ \rangle$ are typically larger than the heat losses $\langle Q_- \rangle$ that follow the ocean temperature maximum. Hence it takes more time for the surface ocean to release the extra energy than it takes to absorb it.

The response of ice retreat date, following **winter** processes, is characterised by roughly equal contributions of reference (-0.2 d/yr) and feedback (-0.3 d/yr) responses. The feedback factor λ_w is equal to 0.31 on average, hence changes in d_a imply changes in d_r of smaller magnitude. The positive sign means that later advance implies earlier retreat. Why $\lambda_w < 1$ is because of two robust features of the ice seasonal cycle that dampen the impact of changes in d_a on d_r. First the melt season is shorter than the growth season, hence changes in ice advance date translate into weaker changes in ice retreat date. Second, the ice growth rate is larger for thin than for thick ice, hence the maximum winter ice thickness does not decrease due to later advance as much as if the growth rate was constant. (The $1/h$ dependence in growth rate explains the extra 0.5 factor in λ_w).

Now considering the ice *advance vs. retreat amplification coefficient*, it can be expressed as a function of feedback and reference responses:

$$R \equiv -\frac{\Delta d_a}{\Delta d_r} = \lambda_s + \frac{\Delta d_a^{ref}}{\Delta d_r}. \qquad (17)$$

R and its two contributors are depicted in Fig. A2b. Summer feedbacks largely dominate R, such that $R \approx \lambda_s$ is a reasonable approximation.

Let us finally note that both feedback factors are determined by fundamental physical features of ice-ocean interactions, likely going beyond climate uncertainties. The winter feedback is determined by the shape of the seasonal cycle and the non-linear dependence of ice growth rate, which are likely invariant across models. As for the summer feedback, the scaling detailed in Appendix 2, indicates that the related feedback factor is constrained by celestial mechanics, ubiquitous clouds and near-freezing temperatures. This likely contributes to the low level of uncertainty in R among the different climate models.

Appendix B: scaling of the ice-free ocean energy budget

1D model results show a direct link between, on the one hand, the ratio of long-term trends in ice advance and retreat date ($R^{long}_{a/r}$), and the energetics of the ice-free ocean on the other hand:

$$R^{long}_{a/r} \approx \lambda_s = -\langle Q_+ \rangle / \langle Q_- \rangle ,$$

where $\langle Q_+ \rangle$ and $\langle Q_- \rangle$ are the average net positive (negative) atmosphere-to-ocean heat fluxes during the ice free-period. CMIP5 and 1D model results suggest that over long-time scales, this ratio is stable and does not vary much among models, with values ranging from 1.5 to 2. Why this ratio would be so invariable is because celestial mechanics, ubiquitous clouds and near-freezing temperatures provide strong constraints on the radiation balance, which dominates the surface energy budget.

Assuming that non-solar components cancel each other, the mean heat gain is mostly solar:

$$\langle Q_+ \rangle = \langle Q_{sol}(1-\alpha_w)[1-exp(-\kappa h_w)] \rangle_{early\ ice-free\ season},$$

where the mean is taken over the first part of the ice-free period, typically covering July or June. Of remarkable importance is that the magnitude of clear-sky solar flux above the Arctic Circle deviates by less than 20 W/m^2, both in space and time, around the summer solstice (see, e.g., Peixoto and Oort, 1992). Assuming summer cloud skies would remain the norm, we take 150 W/m^2 as representative for $\langle Q_+ \rangle$.

The mean heat loss is mostly non-solar:

$$\langle Q_- \rangle = \langle Q_{lw} - \epsilon\sigma T_w^4 + Q_{sh} + Q_{lh} \rangle_{late\ ice-free\ season},$$

and corresponds to the second part of the ice-free period, typically covering August to October. Downwelling long-wave radiation flux Q_{lw} corresponds to cloud skies at near freezing temperatures, for which 250 W/m^2 seems reasonable (Perssonn et al., 2002). The thermal emission would be that of the ocean, a nearly ideal black body, at near-freezing temperatures, and should not depart much from 300 W/m^2. The sensible (Q_{sh}) and latent (Q_{lh}) heat fluxes are relatively more uncertain. In current ice-covered conditions, turbulent fluxes imply a net average heat loss, typically smaller than 10 W/m^2 (Personn et al., 2002). Over an ice-free ocean however, turbulent heat losses would obviously increase, in particular through the latent heat flux, but also become more variable at synoptic time scales. Assuming that turbulent heat fluxes would in the future Arctic compare to what they are today in ice-free ocean regions of the North Pacific, we argue that they would correspond to a 25 W/m^2 heat loss, definitely not exceeding 100 W/m^2 (Yu et al., 2008).

Taken together, these elements give an estimated R value ranging from 1 to 2, where uncertainties on the dominant radiation terms of the energy budget are small and inter-model differences in turbulent heat fluxes would be decisive in determining the actual value of the ratio.

Author Contribution

All authors conceived the study and co-wrote the paper. ML and MV performed analyses.

Competing contribution

The authors declare that they have no conflict of interest.

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References

Arrigo, K. R. and van Dijken, G. L.: Secular trends in Arctic Ocean net primary production, J. Geophys. Res., 116(C9), C09011, doi:10.1029/2011JC007151, 2011.

Assmy, P., Fernández-Méndez, M., Duarte, P., Meyer, A., Randelhoff, A., Mundy, C. J., Olsen, L. M., Kauko, H. M., Bailey, A., Chierici, M., Cohen, L., Doulgeris, A. P., Ehn, J. K., Fransson, A., Gerland, S., Hop, H., Hudson, S. R., Hughes, N., Itkin, P., Johnsen, G., King, J. A., Koch, B. P., Koenig, Z., Kwasniewski, S., Laney, S. R., Nicolaus, M., Pavlov, A. K., Polashenski, C. M., Provost, C., Rösel, A., Sandbu, M., Spreen, G., Smedsrud, L. H., Sundfjord, A., Taskjelle, T., Tatarek, A., Wiktor, J., Wagner, P. M., Wold, A., Steen, H. and Granskog, M. A.: Leads in Arctic pack ice enable early phytoplankton blooms below snow-covered sea ice, Scientific Reports, 7, srep40850, doi:10.1038/srep40850, 2017.

Barnhart, K. R., Miller, C. R., Overeem, I. and Kay, J. E.: Mapping the future expansion of Arctic open water, Nature Clim. Change, 6(3), 280–285, doi:10.1038/nclimate2848, 2016.

Bitz, C. M., Holland, M. M., Hunke, E. C. and Moritz, R. E.: Maintenance of the Sea-Ice Edge, J. Climate, 18(15), 2903–2921, doi:10.1175/JCLI3428.1, 2005.

Blanchard-Wrigglesworth, E., Armour, K. C., Bitz, C. M. and DeWeaver, E.: Persistence and Inherent Predictability of Arctic Sea Ice in a GCM Ensemble and Observations, J. Climate, 24(1), 231–250, doi:10.1175/2010JCLI3775.1, 2010.

Bony, S., Dufresne, J.-L., Treut, H. L., Morcrette, J.-J. and Senior, C.: On dynamic and thermodynamic components of cloud changes, Climate Dynamics, 22(2–3), 71–86, doi:10.1007/s00382-003-0369-6, 2004.

Cavalieri, D. J. and Parkinson, C. L.: Arctic sea ice variability and trends, 1979–2010, The Cryosphere, 6(4), 881–889, doi:10.5194/tc-6-881-2012, 2012.

Collins, W. J., Bellouin, N., Doutriaux-Boucher, M., Gedney, N., Halloran, P., Hinton, T., Hughes, J., Jones, C. D., Joshi, M., Liddicoat, S., Martin, G., O'Connor, F., Rae, J., Senior, C., Sitch, S., Totterdell, I., Wiltshire, A. and Woodward, S.: Development and evaluation of an Earth-System model – HadGEM2, Geosci. Model Dev., 4(4), 1051–1075, doi:10.5194/gmd-4-1051-2011, 2011.

Comiso, Josephino `Joey`: Bootstrap Sea Ice Concentrations from Nimbus-7 SMMR and DMSP SSM/I-SSMIS, Version 2, , doi:10.5067/J6JQLS9EJ5HU, 2000.

Dufresne, J.-L., Foujols, M.-A., Denvil, S., Caubel, A., Marti, O., Aumont, O., Balkanski, Y., Bekki, S., Bellenger, H., Benshila, R., Bony, S., Bopp, L., Braconnot, P., Brockmann, P., Cadule, P., Cheruy, F., Codron, F., Cozic, A., Cugnet, D., Noblet, N. de, Duvel, J.-P., Ethé, C., Fairhead, L., Fichefet, T., Flavoni, S., Friedlingstein, P., Grandpeix, J.-Y., Guez, L., Guilyardi, E., Hauglustaine, D., Hourdin, F., Idelkadi, A., Ghattas, J., Joussaume, S., Kageyama, M., Krinner, G., Labetoulle, S., Lahellec, A., Lefebvre, M.-P., Lefevre, F., Levy, C., Li, Z. X., Lloyd, J., Lott, F., Madec, G., Mancip, M., Marchand, M., Masson, S., Meurdesoif, Y., Mignot, J., Musat, I., Parouty, S., Polcher, J., Rio, C., Schulz, M., Swingedouw, D., Szopa, S., Talandier, C., Terray, P., Viovy, N. and Vuichard, N.: Climate change projections using the IPSL-CM5 Earth System Model: from CMIP3 to CMIP5, Clim Dyn, 40(9–10), 2123–2165, doi:10.1007/s00382-012-1636-1, 2013.

Dussin, R., B. Barnier and L. Brodeau, *The making of Drakkar forcing set DFS5.* Tech. report DRAKKAR/MyOcean Report 01-04-16, LGGE, Grenoble, France. (2016).

Fletcher, J. O., The heat budget of the Arctic Basin and its relation to climate, Rep. R-444-PR, RAND Corp., Santa Monica, Calif., (1965).

Gent, P. R., Danabasoglu, G., Donner, L. J., Holland, M. M., Hunke, E. C., Jayne, S. R., Lawrence, D. M., Neale, R. B., Rasch, P. J., Vertenstein, M., Worley, P. H., Yang, Z.-L. and Zhang, M.: The Community Climate System Model Version 4, J. Climate, 24(19), 4973–4991, doi:10.1175/2011JCLI4083.1, 2011.

Giorgetta Marco A., Jungclaus Johann, Reick Christian H., Legutke Stephanie, Bader Jürgen, Böttinger Michael, Brovkin Victor, Crueger Traute, Esch Monika, Fieg Kerstin, Glushak Ksenia, Gayler Veronika, Haak Helmuth, Hollweg Heinz-Dieter, Ilyina Tatiana, Kinne Stefan, Kornblueh

Luis, Matei Daniela, Mauritsen Thorsten, Mikolajewicz Uwe, Mueller Wolfgang, Notz Dirk, Pithan Felix, Raddatz Thomas, Rast Sebastian, Redler Rene, Roeckner Erich, Schmidt Hauke, Schnur Reiner, Segschneider Joachim, Six Katharina D., Stockhause Martina, Timmreck Claudia, Wegner Jörg, Widmann Heinrich, Wieners Karl-H., Claussen Martin, Marotzke Jochem and Stevens Bjorn: Climate and carbon cycle changes from 1850 to 2100 in MPI-ESM simulations for the Coupled Model Intercomparison Project phase 5, Journal of Advances in Modeling Earth Systems, 5(3), 572–597, doi:10.1002/jame.20038, 2013.

Goosse, H., Kay, J. E., Armour, K. C., Bodas-Salcedo, A., Chepfer, H., Docquier, D., Jonko, A., Kushner, P. J., Lecomte, O., Massonnet, F., Park, H.-S., Pithan, F., Svensson, G. and Vancoppenolle, M.: Quantifying climate feedbacks in polar regions. *Nature Communications, 9(1), doi:10.1038/s41467-018-04173-0*, 2018.

Hezel, P. J., Fichefet, T. and Massonnet, F.: Modeled Arctic sea ice evolution through 2300 in CMIP5 extended RCPs, The Cryosphere, 8(4), 1195–1204, doi:10.5194/tc-8-1195-2014, 2014.

Huntington, H. P., Gearheard, S., Holm, L. K., Noongwook, G., Opie, M. and Sanguya, J.: Sea ice is our beautiful garden: indigenous perspectives on sea ice in the Arctic, in Sea Ice, edited by D. N. Thomas, pp. 583–599, John Wiley & Sons, Ltd., 2017.

Johnson, M. and Eicken, H.: Estimating Arctic sea-ice freeze-up and break-up from the satellite record: A comparison of different approaches in the Chukchi and Beaufort Seas, Elem Sci Anth, 4(0), doi:10.12952/journal.elementa.000124, 2016.

Kröner, N., Kotlarski, S., Fischer, E., Lüthi, D., Zubler, E. and Schär, C.: Separating climate change signals into thermodynamic, lapse-rate and circulation effects: theory and application to the European summer climate, Clim Dyn, 48(9–10), 3425–3440, doi:10.1007/s00382-016-3276-3, 2017.

Kwok, R. and Rothrock, D. A.: Decline in Arctic sea ice thickness from submarine and ICESat records: 1958–2008, Geophys. Res. Lett., 36(15), L15501, doi:10.1029/2009GL039035, 2009.

Laidre, K. L., Stern, H., Kovacs, K. M., Lowry, L., Moore, S. E., Regehr, E. V., Ferguson, S. H., Wiig, Ø., Boveng, P., Angliss, R. P., Born, E. W., Litovka, D., Quakenbush, L., Lydersen, C., Vongraven, D. and Ugarte, F.: Arctic marine mammal population status, sea ice habitat loss, and conservation recommendations for the 21st century, Conservation Biology, 29(3), 724–737, doi:10.1111/cobi.12474, 2015.

Lindsay, R. and Schweiger, A.: Arctic sea ice thickness loss determined using subsurface, aircraft, and satellite observations, The Cryosphere, 9(1), 269–283, doi:10.5194/tc-9-269-2015, 2015.

Markus, T., Stroeve, J. C. and Miller, J.: Recent changes in Arctic sea ice melt onset, freeze-up, and melt season length, J. Geophys. Res., 114(C12), C12024, doi:10.1029/2009JC005436, 2009.

Maslanik, J., Stroeve, J., Fowler, C. and Emery, W.: Distribution and trends in Arctic sea ice age through spring 2011, Geophys. Res. Lett., 38(13), L13502, doi:10.1029/2011GL047735, 2011.

Massonnet, F., Fichefet, T., Goosse, H., Bitz, C. M., Philippon-Berthier, G., Holland, M. M. and Barriat, P.-Y.: Constraining projections of summer Arctic sea ice, The Cryosphere, 6(6), 1383–1394, doi:10.5194/tc-6-1383-2012, 2012.

Massonnet, F., Vancoppenolle, M., Goosse, H., Docquier, D., Fichefet, T., and Blanchard-Wrigglesworth, E.: Arctic sea ice change tied to its mean state through thermodynamic processes, Nature Climate Change, 8(7), 599—603, 2018.

Maykut, G. A.: The surface heat and mass balance. In *The Geophysics of Sea Ice*, edited by N. Untersteiner, Plenum Press, New York, 146, 395-463, 1986.

Maykut, G. A. and Untersteiner, N.: Some results from a time-dependent thermodynamic model of sea ice, J. Geophys. Res., 76(6), 1550–1575, doi:10.1029/JC076i006p01550, 1971.

Melia, N., Haines, K., Hawkins, E. and Day, J. J.: Towards seasonal Arctic shipping route predictions, Environ. Res. Lett., 12(8), 084005, doi:10.1088/1748-9326/aa7a60, 2017.

Notz, D.: How well climate models must agree with observations. *Philos. Trans. R. Soc. A* **373**: 20140164. doi:10.1098/rsta.2014.0164, 2015.

Notz, D., Jahn, A., Holland, M., Hunke, E., Massonnet, F., Stroeve, J., Tremblay, B. and Vancoppenolle, M.: The CMIP6 Sea-Ice Model Intercomparison Project (SIMIP): understanding sea ice through climate-model simulations, Geosci. Model Dev., 9(9), 3427–3446, doi:10.5194/gmd-9-3427-2016, 2016.

Notz, D. and Stroeve, J.: Observed Arctic sea-ice loss directly follows anthropogenic CO2 emission, Science, aag2345, doi:10.1126/science.aag2345, 2016.

Parkinson, C. L.: Spatial patterns in the length of the sea ice season in the Southern Ocean, 1979–1986, J. Geophys. Res., 99(C8), 16327–16339, doi:10.1029/94JC01146, 1994.

Parkinson, C. L.: Global Sea Ice Coverage from Satellite Data: Annual Cycle and 35-Yr Trends, J. Climate, 27(24), 9377–9382, doi:10.1175/JCLI-D-14-00605.1, 2014.

Peixoto, J. P. and Oort, A. H.: Physics of Climate, 1992 ed., American Institute of Physics, New York., 1992.

Perovich, D. K., Grenfell, T. C., Richter-Menge, J. A., Light, B., Tucker, W. B. and Eicken, H.: Thin and thinner: Sea ice mass balance measurements during SHEBA, Journal of Geophysical Research: Oceans, 108(C3), doi:10.1029/2001JC001079, 2003.

Perovich, D. K., Light, B., Eicken, H., Jones, K. F., Runciman, K. and Nghiem, S. V.: Increasing solar heating of the Arctic Ocean and adjacent seas, 1979–2005: Attribution and role in the ice-albedo feedback, Geophys. Res. Lett., 34(19), L19505, doi:10.1029/2007GL031480, 2007.

Persson, P. O. G., Fairall, C. W., Andreas, E. L., Guest, P. S. and Perovich, D. K.: Measurements near the Atmospheric Surface Flux Group tower at SHEBA: Near-surface conditions and surface energy budget, Journal of Geophysical Research (Oceans), 107, 8045, doi:10.1029/2000JC000705, 2002.

Renner, A. H. H., Gerland, S., Haas, C., Spreen, G., Beckers, J. F., Hansen, E., Nicolaus, M. and Goodwin, H.: Evidence of Arctic sea ice thinning from direct observations, Geophys. Res. Lett., 41(14), 5029–5036, doi:10.1002/2014GL060369, 2014.

Rotstayn, L. D., Jeffrey, S. J., Collier, M. A., Dravitzki, S. M., Hirst, A. C., Syktus, J. I. and Wong, K. K.: Aerosol- and greenhouse gas-induced changes in summer rainfall and circulation in the Australasian region: a study using single-forcing climate simulations, Atmos. Chem. Phys., 12(14), 6377–6404, doi:10.5194/acp-12-6377-2012, 2012.

Rousset, C., Vancoppenolle, M., Madec, G., Fichefet, T., Flavoni, S., Barthélemy, A., Benshila, R., Chanut, J., Levy, C., Masson, S. and Vivier, F.: The Louvain-La-Neuve sea ice model LIM3.6: global and regional capabilities, Geosci. Model Dev., 8(10), 2991–3005, doi:10.5194/gmd-8-2991-2015, 2015.

Schmidt, G. A., Kelley, M., Nazarenko, L., Ruedy, R., Russell, G. L., Aleinov, I., Bauer, M., Bauer, S. E., Bhat, M. K., Bleck, R., Canuto, V., Chen, Y.-H., Cheng, Y., Clune, T. L., Del Genio, A., de Fainchtein, R., Faluvegi, G., Hansen, J. E., Healy, R. J., Kiang, N. Y., Koch, D., Lacis, A. A., LeGrande, A. N., Lerner, J., Lo, K. K., Matthews, E. E., Menon, S., Miller, R. L., Oinas, V., Oloso, A. O., Perlwitz, J. P., Puma, M. J., Putman, W. M., Rind, D., Romanou, A., Sato, M., Shindell, D. T., Sun, S., Syed, R. A., Tausnev, N., Tsigaridis, K., Unger, N., Voulgarakis, A., Yao, M.-S. and Zhang, J.: Configuration and assessment of the GISS ModelE2 contributions to the CMIP5 archive, J. Adv. Model. Earth Syst., 6(1), 141–184, doi:10.1002/2013MS000265, 2014.

Semtner, A. J.: A Model for the Thermodynamic Growth of Sea Ice in Numerical Investigations of Climate, J. Phys. Oceanogr., 6(3), 379–389, doi:10.1175/1520-0485(1976)006<0379:AMFTTG>2.0.CO;2, 1976.

Serreze, M. C., Crawford, A. D., Stroeve, J. C., Barrett, A. P. and Woodgate, R. A.: Variability, trends, and predictability of seasonal sea ice retreat and advance in the Chukchi Sea, J. Geophys. Res. Oceans, 121(10), 7308–7325, doi:10.1002/2016JC011977, 2016.

Shepherd, T. G.: Atmospheric circulation as a source of uncertainty in climate change projections, Nature Geoscience, 7(10), 703–708, doi:10.1038/ngeo2253, 2014.

Smith, L. C. and Stephenson, S. R.: New Trans-Arctic shipping routes navigable by midcentury, PNAS, 110(13), E1191–E1195, doi:10.1073/pnas.1214212110, 2013.

Stammerjohn, S., Massom, R., Rind, D. and Martinson, D.: Regions of rapid sea ice change: An inter-hemispheric seasonal comparison, Geophys. Res. Lett., 39(6), L06501, doi:10.1029/2012GL050874, 2012.

Steele, M., Ermold, W. and Zhang, J.: Arctic Ocean surface warming trends over the past 100 years, Geophys. Res. Lett., 35(2), L02614, doi:10.1029/2007GL031651, 2008.

Steele, M. and Dickinson, S.: The phenology of Arctic Ocean surface warming, J. Geophys. Res. Oceans, 121(9), 6847–6861, doi:10.1002/2016JC012089, 2016.

Stefan, J.: Uber die Theorie der Eisbildung, insbesondere uber Eisbildung im Polarmeer. *Ann. Phys. 3rd. Ser., 42*, 269-286, 1891.

Steiner, N. S., Christian, J. R., Six, K. D., Yamamoto, A. and Yamamoto-Kawai, M.: Future ocean acidification in the Canada Basin and surrounding Arctic Ocean from CMIP5 earth system models, J. Geophys. Res. Oceans, 119(1), 332–347, doi:10.1002/2013JC009069, 2014.

Stern, H. L. and Laidre, K. L.: Sea-ice indicators of polar bear habitat, The Cryosphere, 10(5), 2027–2041, doi:10.5194/tc-10-2027-2016, 2016.

Stroeve, J. C., Kattsov, V., Barrett, A., Serreze, M., Pavlova, T., Holland, M. and Meier, W. N.: Trends in Arctic sea ice extent from CMIP5, CMIP3 and observations, Geophys. Res. Lett., 39(16), L16502, doi:10.1029/2012GL052676, 2012.

Stroeve, J. C., Markus, T., Boisvert, L., Miller, J. and Barrett, A.: Changes in Arctic melt season and implications for sea ice loss, Geophysical Research Letters, 41(4), 1216–1225, doi:10.1002/2013GL058951, 2014.

Stroeve, J. C., Crawford, A. D. and Stammerjohn, S.: Using timing of ice retreat to predict timing of fall freeze-up in the Arctic, Geophys. Res. Lett., 43(12), 2016GL069314, doi:10.1002/2016GL069314, 2016.

Uotila, P., Iovino, D., Vancoppenolle, M., Lensu, M. and Rousset, C.: Comparing sea ice, hydrography and circulation between NEMO3.6 LIM3 and LIM2, Geosci. Model Dev., 10(2), 1009–1031, doi:10.5194/gmd-10-1009-2017, 2017.

Vancoppenolle, M., Bopp, L., Madec, G., Dunne, J., Ilyina, T., Halloran, P. R. and Steiner, N.: Future Arctic Ocean primary productivity from CMIP5 simulations: Uncertain outcome, but consistent mechanisms, Global Biogeochem. Cycles, 27(3), 605–619, doi:10.1002/gbc.20055, 2013.

Voldoire, A., Sanchez-Gomez, E., Mélia, D. S. y, Decharme, B., Cassou, C., Sénési, S., Valcke, S., Beau, I., Alias, A., Chevallier, M., Déqué, M., Deshayes, J., Douville, H., Fernandez, E., Madec, G., Maisonnave, E., Moine, M.-P., Planton, S., Saint-Martin, D., Szopa, S., Tyteca, S., Alkama, R., Belamari, S., Braun, A., Coquart, L. and Chauvin, F.: The CNRM-CM5.1 global climate model: description and basic evaluation, Clim Dyn, 40(9–10), 2091–2121, doi:10.1007/s00382-011-1259-y, 2013.

Wang, M. and Overland, J. E.: Projected future duration of the sea-ice-free season in the Alaskan Arctic, Progress in Oceanography, 136, 50–59, doi:10.1016/j.pocean.2015.01.001, 2015.

Wassmann, P. and Reigstad, M.: Future Arctic Ocean Seasonal Ice Zones and Implications for Pelagic-Benthic Coupling, Oceanography, 24(3), 220–231, doi:10.5670/oceanog.2011.74, 2011.

Wu, T., Song, L., Li, W., Wang, Z., Zhang, H., Xin, X., Zhang, Y., Zhang, L., Li, J., Wu, F., Liu, Y., Zhang, F., Shi, X., Chu, M., Zhang, J., Fang, Y., Wang, F., Lu, Y., Liu, X., Wei, M., Liu, Q., Zhou, W., Dong, M., Zhao, Q., Ji, J., Li, L. and Zhou, M.: An overview of BCC climate system model development and application for climate change studies, Acta Meteorol Sin, 28(1), 34–56, doi:10.1007/s13351-014-3041-7, 2014.

Yeager, S. G., A. R. Karspeck, and G. Danabasoglu (2015), Predicted slowdown in the rate of Atlantic sea ice loss, *Geophys. Res. Lett.*, *42*, doi:10.1002/2015GL065364.

Yu, L., X. Jin, and R. A. Weller, Multidecade Global Flux Datasets from the Objectively Analyzed Air-sea Fluxes (OAFlux) Project: Latent and sensible heat fluxes, ocean evaporation, and related surface meteorological variables. Tech. Report Woods Hole Oceanographic Institution, OAFlux Project Technical Report. OA-2008-01, 64pp. Woods Hole. Massachusetts (2008).

Tables and Figures

Table 1. Linear trends in ice retreat and advance dates over 2000-2200 (200 years), and long-term ice advance amplification ratios for the individual and mean CMIP5 models and for the 1D model. Trends and ratios are given as median ± interquartile range over the seasonal ice zone where trends are significant at a 95% confidence level (p = 0.05).

	r_r (days / decade)	r_a (days / decade)	$R^{long}_{a/r}$	*Reference*
CCSM4	-6.6 ± 2.1	13.4 ± 7.3	2.0 ± 0.6	*Gent et al.*, 2011
CNRM-CM5	-8.0 ± 2.8	13.5 ± 5.9	1.7 ± 0.3	*Voldoire et al.*, 2013
CSIRO-Mk3-6-0	-6.1 ± 3.3	10.4 ± 4.0	1.7 ± 0.6	*Rotstayn et al.*,2012
GISS-E2-H	-2.8 ± 0.6	5.1 ± 1.6	1.8 ± 0.4	*Schmidt et al.*,2014
MPI-ESM-LR	-8.6 ± 2.8	15.2 ± 8.1	1.8 ± 0.4	*Giorgetta et al.*, 2013
bcc-csm1-1	-5.2 ± 1.3	9.7 ± 2.6	1.9 ±0.4	*Wu et al.*, 2014
GISS-E2-R	-2.0 ± 0.4	3.4 ± 0.8	1.8 ± 0.3	*Schmidt et al.*, 2014
HadGEM2-ES	-9.1 ± 3.0	18.6 ± 7.6	1.9 ± 0.5	*Collins et al.*, 2011
IPSL-CM5A-LR	-5.7 ± 1.2	11.1 ± 3.8	1.9 ± 0.5	*Dufresne et al.*, 2013
MEAN CMIP5	- 6.0 ± 2.0	11.1 ± 4.6	1.8 ± 0.4	
1D model	- 3.1 ± n.a.	6.0 ± n.a.	1.9 ± n.a.	

Figure 1. Evolution of the ice seasonality diagnostics (ice retreat date, blue; and ice advance date, orange): (a) CMIP5 median and interquartile range, with corresponding range of satellite derived-values (green rectangles 1980-2015) over the 70-80°N latitude band; (b) one-dimensional ice-ocean model results. The ice-free period (L_w), the photoperiod (L_p) and the average polar night (gray rectangle) are also depicted. Note that the systematic difference between observations and CMIP5 models is reduced when accounting for the systematic bias due to the daily interpolation of monthly means in CMIP5 models (See Methods and Tab. S2).

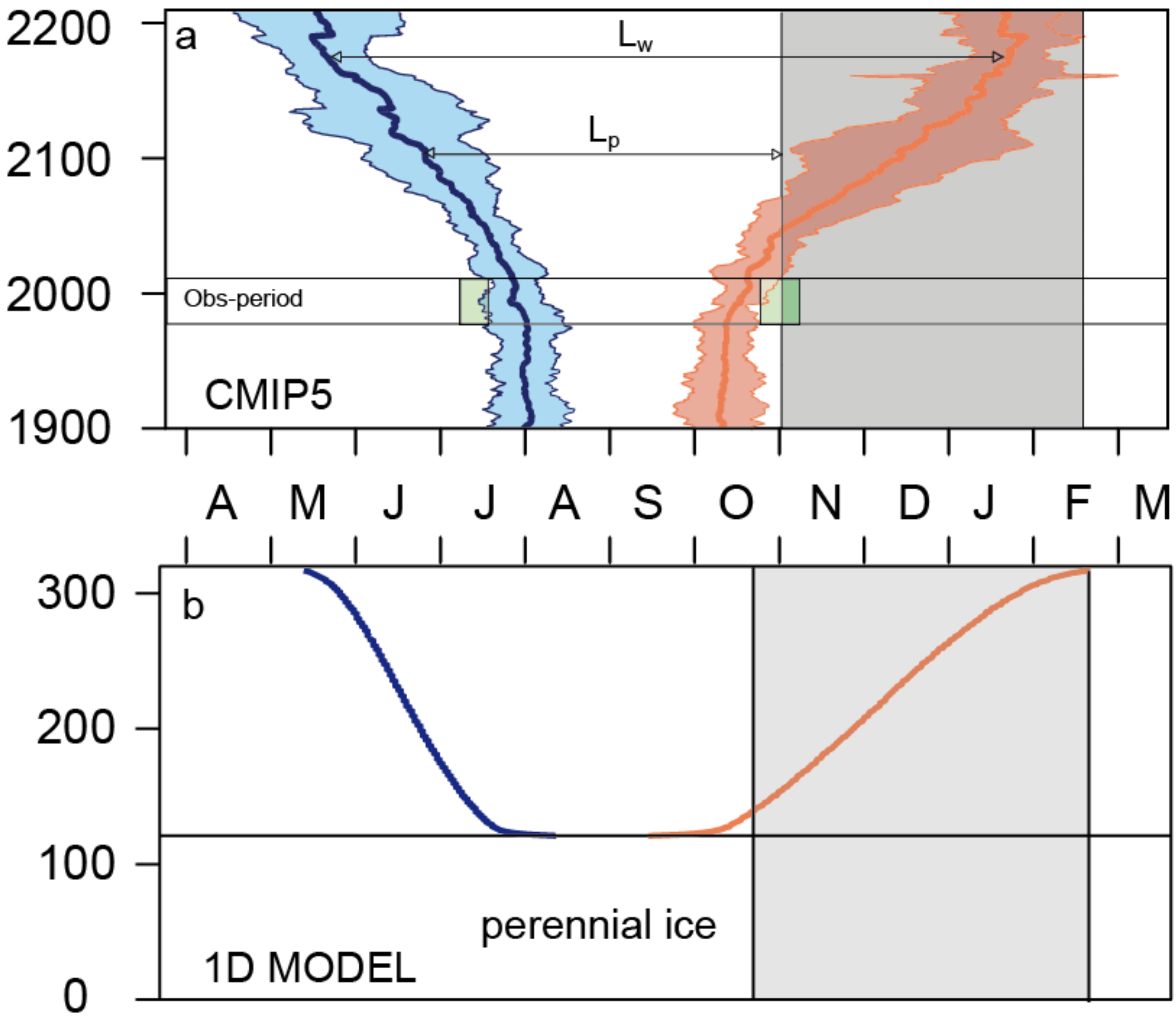

Figure 2. Maps and frequency histograms of (a,d) ice retreat date (b,e) ice advance date and (c,f) ice-free season length over 1980-2015 (36 years), based on (a,b,c) passive microwave satellite concentration retrievals (Comiso, 2000; updated 2015) and (d,e,f) daily concentration fields averaged over CMIP5 models. Median ± IQR refers to all points in the seasonal ice zone. See figure S3 for individual models.

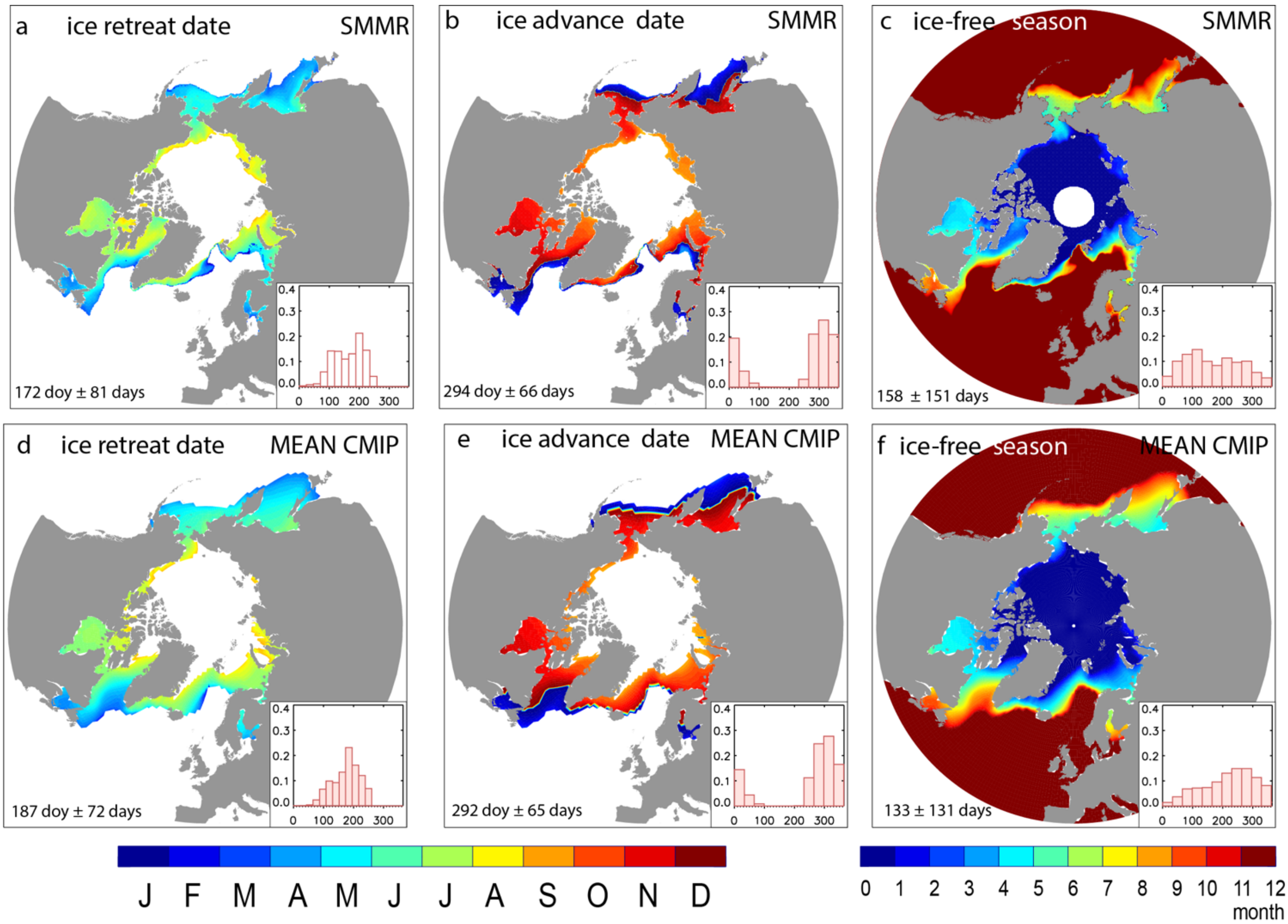

Figure 3. Maps and frequency histograms of linear trends (for hatched zones only) in (a,d) ice retreat date (b,e,) ice advance date and (c,f) ice-free season length over 1980-2015 (36 years), based on (a,b,c) passive microwave satellite concentration retrievals (Comiso, 2000; updated 2015); (d,e,f) he mean CMIP5 models. Hatching refers to the 95% confidence interval (p=0.05). Median ± IQR refers to significant pixels with at least 1/3 of the years with defined retreat and ice advance dates. See figure S4 for individual models.

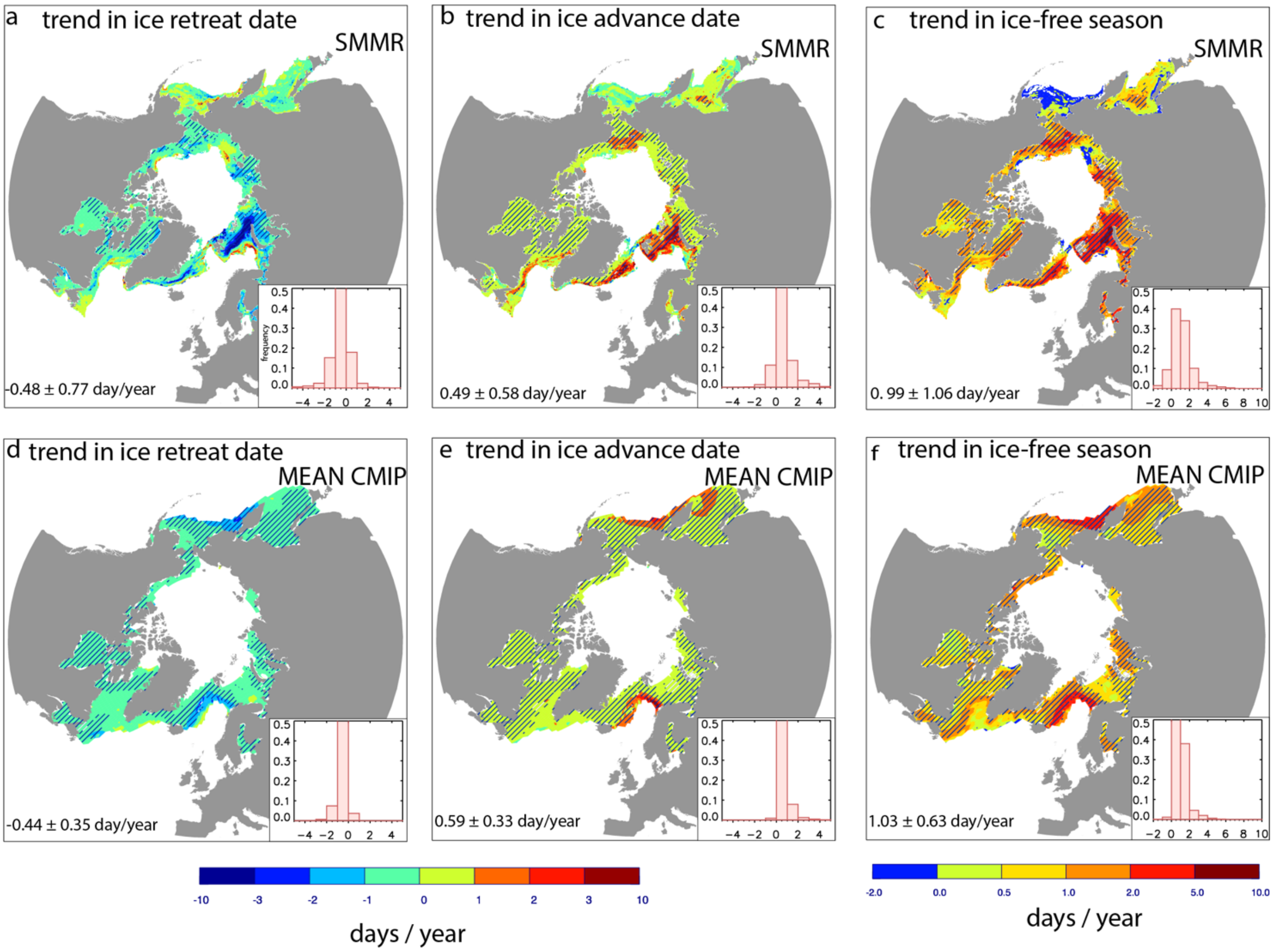

Figure 4. Long-term ice advance vs. retreat amplification coefficient from passive microwave ice concentration retrievals (SMMR; over 1980-2015); and for all individual models over 1980-2015, 2015-2050 and 2050-2085. We use a 75% (p=0.25) confidence interval for this specific computation. The same figures for p = 0.05 are available as Supplementary Material (Fig. S9).

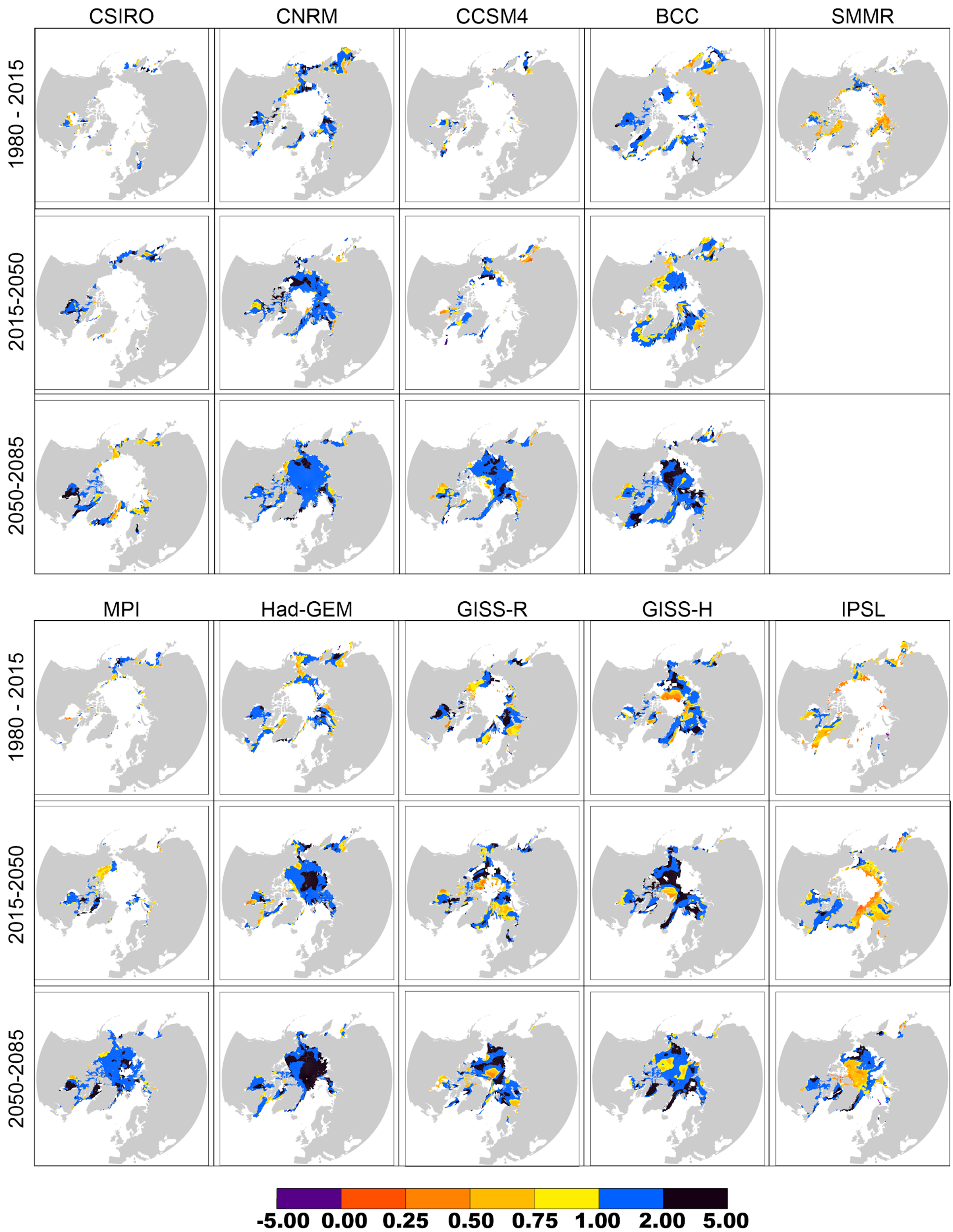

Figure 5. Schematics of the mechanisms shaping the thermodynamic response of sea ice seasonality to a radiative forcing perturbation. The numbers give annual averages simulated by the 1D model. Changes in ice retreat and advance dates are split between *reference (ref)* and *feedback (fb) responses.* See Appendix A for details of the computations.

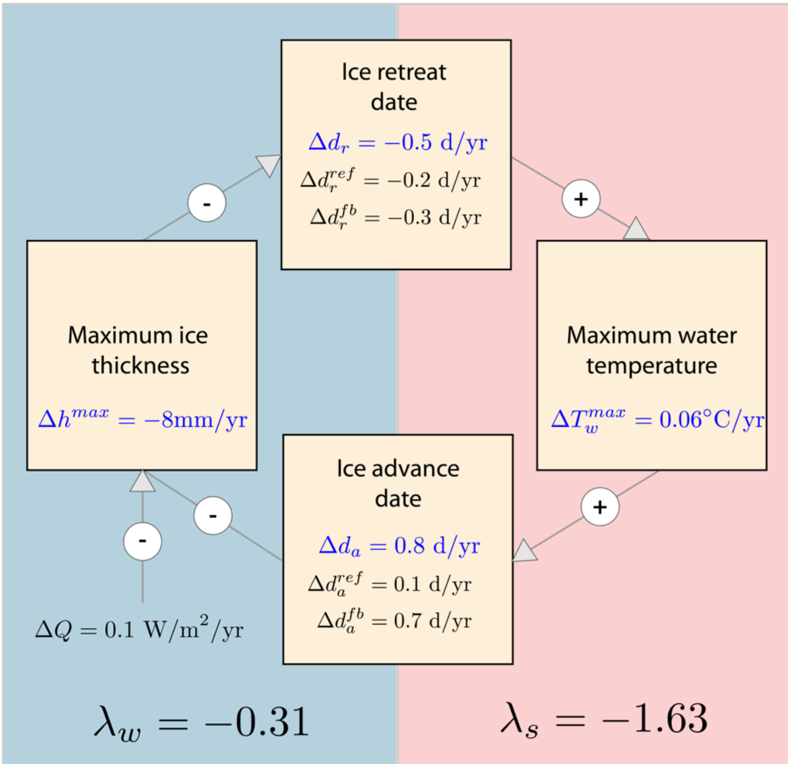

Figure 6. Short-term ice advance vs. retreat amplification coefficient from passive microwave ice concentration retrievals (SMMR; over 1980-2015); and for all individual models over 1980-2015, 2015-2050, 2050-2085.

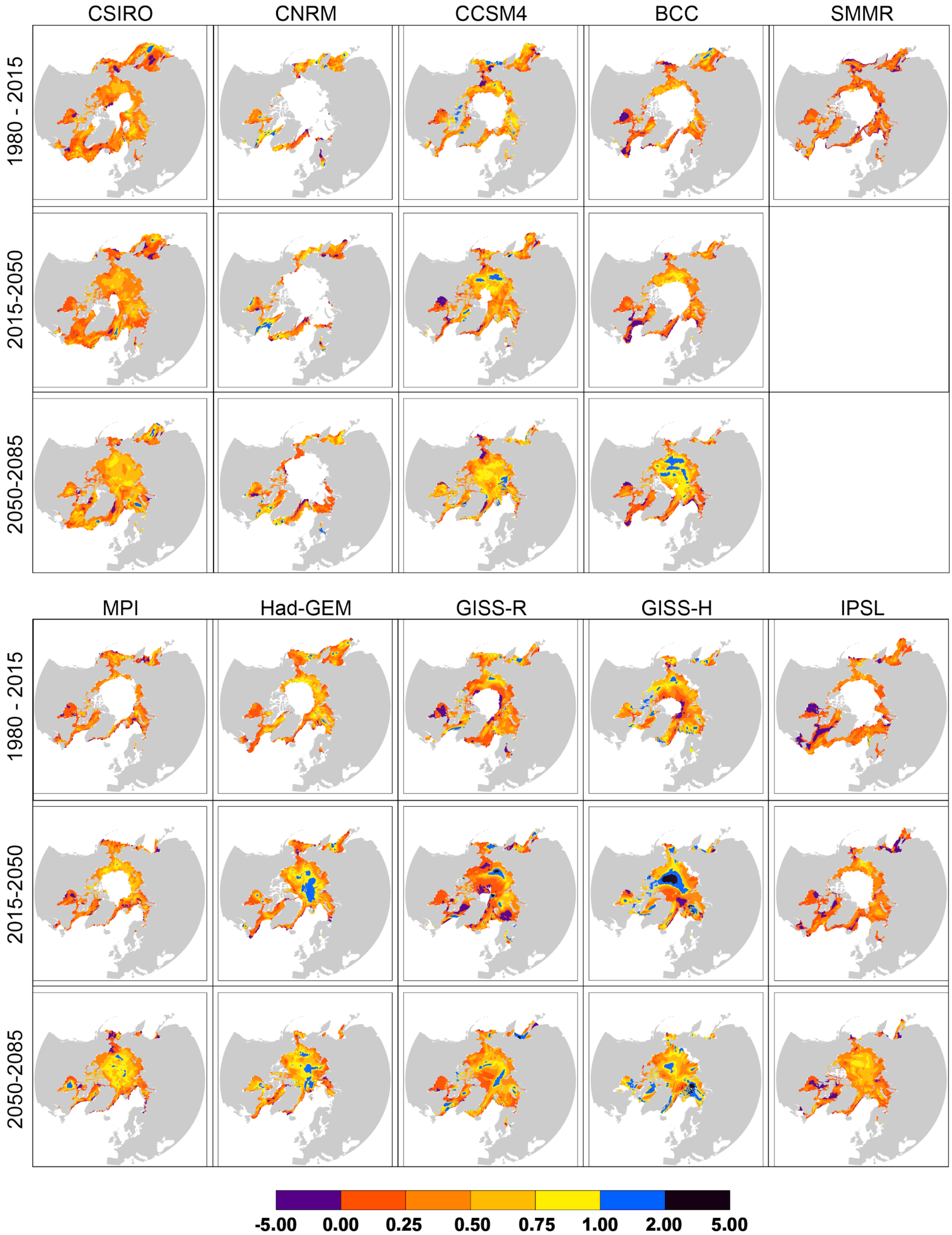

Figure 7. (Top) Energetics of ice retreat and advance in the simple model: net atmospheric (solid) and solar (yellow) heat fluxes to the ocean; SST (dash), depicted for years 150 and 210. **(Bottom)** Annual evolution of the simulated sea surface temperature, averaged over the seasonal ice zone, for two decades of reference (2015-2025, 2075-2085) as simulated by the IPSL_CM5A_LR model and showing the same temporal asymmetry as in the simple model.

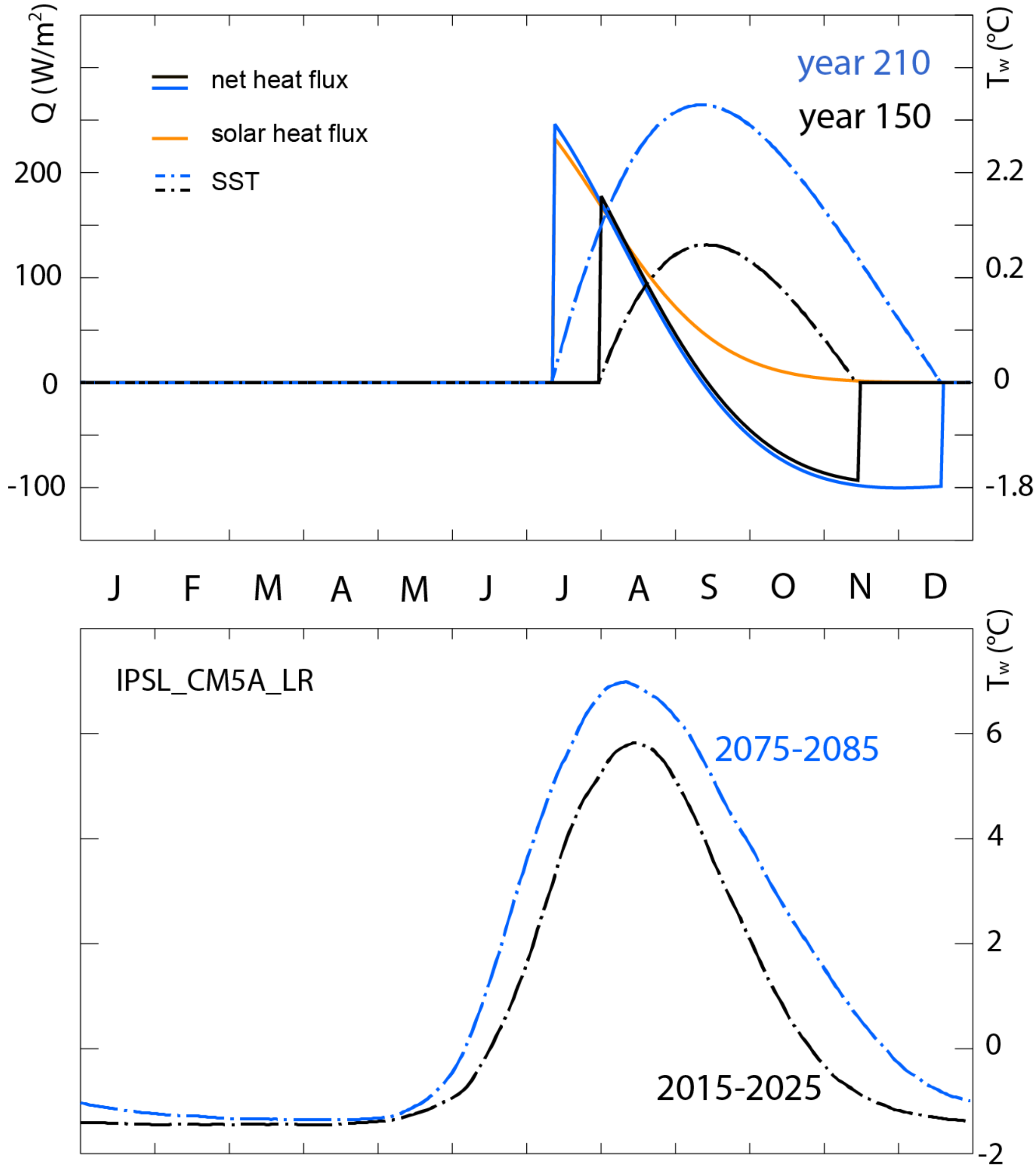

Figure A1. Schematic representation of the analysis framework applied to the 1D model outputs, illustrating the mechanisms of change in ice seasonality between a reference year (solid line/upper colors) and a subsequent year (dashed line/lower colors). Ice appears at the ice advance date (d_a). The ice thickness (h) increases until the date of maximum thickness (d_h) then decreases at an average melt rate $\langle m \rangle$. Once the ice thickness vanishes at the ice retreat date d_r, the sea water temperature T_w increases due to incoming heat flux $\langle Q_+ \rangle$, until the date of maximum temperature (d_T) and finally decreases due to the heat loss $\langle Q_- \rangle$.

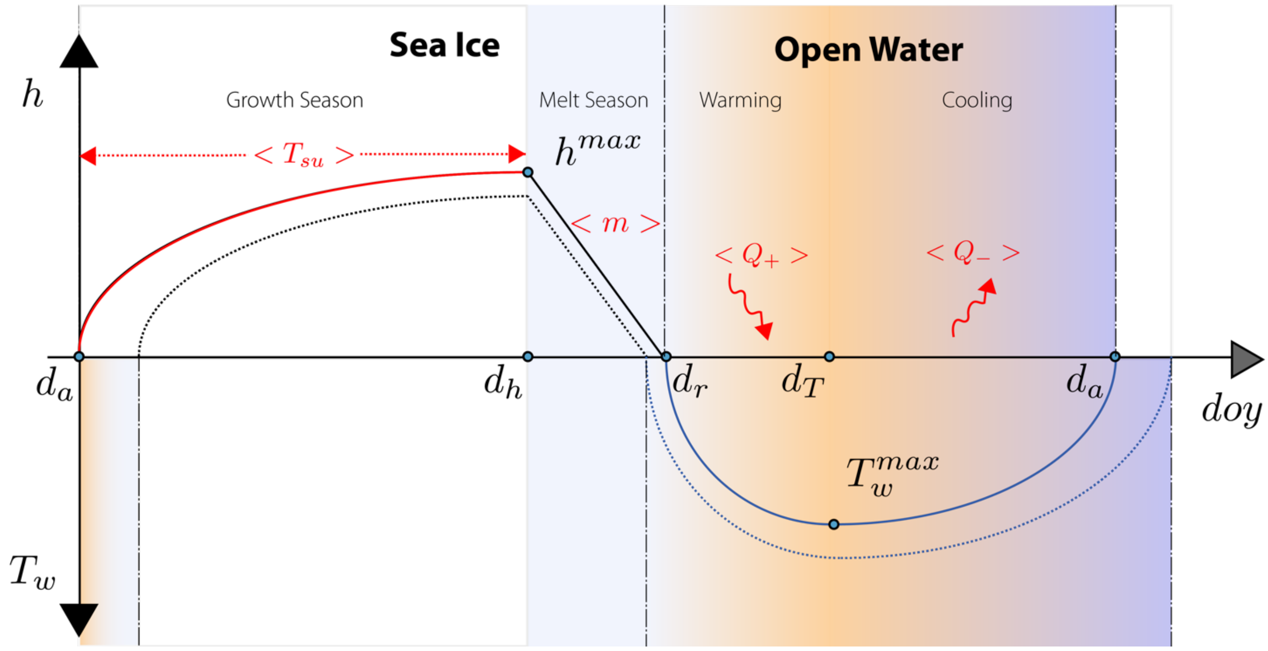

Figure A2. Thermodynamic response of sea ice seasonality to warming in the 1D model: (a) Evolution over the years of the annual contributors to changes in ice retreat and advance date, as simulated by the 1D model. The yellow line gives the total response Δd_r (resp. Δd_a) as diagnosed from model output. The blue curve gives the reference response Δd_r^{ref} (resp. Δd_a^{ref}) to the radiative forcing perturbation as calculated with eq. 11 (resp. 16). The red curve gives the feedback response Δd_r^{fb} (resp. Δd_a^{fb}), attributed to the feedback from d_a (resp. d_r), calculated with eq. 9 and 10 (resp. 13 and 15). The black dashed line testifies that the sum of reference and feedback responses matches the total. **(b) Evolution over the years of the simulated freeze-up amplification ratio in the 1D model.** The yellow curve gives the freeze-up amplification R, calculated as the ratio of the total response in d_a (Δd_a) divided by the total response in d_r (Δd_r), as diagnosed from the 1D model. The blue curve gives the contribution of the reference response to the freeze-up amplification ratio ($\Delta d_a^{ref}/\Delta d_r$). The red curve gives the contribution of the summer feedbacks ($\Delta d_a^{ref}/\Delta d_r = \lambda_s$). The black dashed line testifies that the sum of reference and feedback contributions matches the total.