Response to Reviewer 1

We thank Reviewer 1 for their thoughtful and helpful review of our paper. The Reviewer's comments are shown in blue, followed by our detailed responses, shown in black text.

1. *What could be the impact of Piso on the recrystallization mechanisms? For instance, could it slow down the texture evolution, and the disappearance of the M2 pole? There exist very few work about it, I could just find the paper of Jones and Chew (J. Phys. Chem, 1983) that show the variation of the minimum creep rate with hydrostatic pressure... not sure it helps!*

There is some work on the effect of pressure (P) on creep behavior. Cole (1996) and Rigsby (1958) show there is very little effect of pressure on dislocation glide in single crystals, and Durham et al. (1983) show little effect of pressure on tertiary creep of polycrystalline ice. We have just completed some repeat experiments of the -10°C experiments in Qi et al. (2017), but at a confining pressure of 20MPa (the Qi et al. (2017) experiments are conducted for a confining pressure of 10MPa). The peak stresses and shape of the stress-strain curve through tertiary creep are very similar at the two different pressures. Jones and Chew (1983) showed a change in minimum strain rate related to changes in pressure; it is difficult to evaluate this reported effect, however, as insufficient details are provided in the paper about how the load was applied and how the load was adjusted to give equivalent differential stresses for all experiments. Indeed, in all previous experiments, investigating the effect of pressure on deformation, except those in Durham et al. (1983) and in our own experiments, the axial stress is measured external to the pressure vessel and is likely to be subject to significant uncertainties, including the friction of the deformation piston which must pass through a sliding pressure seal. The measured stress in those studies thus may not be the stress on the sample, and since the stress exponent is relatively large (3 to 4), errors in stress measurement will significantly influence the measured strain rates. The wide range of experiments carried out by Bill Durham from the early 1980s to the 2010s (and now by us, using the same apparatus), where the load cell is located inside the pressure medium and unaffected by seal friction, do not show any significant effect of pressure on creep at low pressures (Durham pers comm). At high pressures, and more specifically at high differential stresses (~>50MPa), the style of deformation changes (Golding, Durham and Prior in prep) from homogenous deformation to localized ductile shear (Golding et al., 2010, 2012). That is not relevant to the experiments presented here, nor to natural terrestrial ice deformation where P would rarely exceed 50 MPa and high differential stresses are only found near the margins of ice sheets, where P is low (Bons et al. 2018).

We do not think including an extensive discussion of possible pressure effects on deformation in the paper is valuable since all experiments were conducted at the same confining pressure. We have included a statement in section 4.2: "All previous shear experiments have been at ambient pressure. Durham et al. (1983) show that there is minimal effect of confining pressure on the tertiary creep of ice."

2. *M index is never used (or did I miss something?)...*

The J- and M-indexes are illustrated in Figure 4 for all samples.

3. Could you expect any post-dynamic evolution of texture and grain size, especially in the case of PIL135 and PIL144? Therefore how caution should you be to use those results at the same level as the one from other experiments?

After each experiment run, retracting the deformation piston and depressurizing the pressure vessel usually took a couple of minutes. The sample was then removed from the apparatus and transferred to the -30°C freezer. The indium jacket was peeled off of the sample in the freezer, which took another couple of minutes. The length and width of the samples were measured in the freezer. The samples were briefly exposed to room temperature air for about 30 s while they were photographed, then returned to the freezer. Samples were then quenched in liquid nitrogen by lowering them slowly into a liquid nitrogen storage dewar. The samples remained in liquid nitrogen until they were removed for EBSD analyses. The maximum total time from the end of an experiment to the time the sample was quenched in liquid nitrogen is ~ 15 minutes.

Static annealing of the microstructures after the sample is unloaded is always a potential issue in deformation experiments. Repeat EBSD measurements of deformed ice samples after fixed thermal annealing times (Hidas et al., 2017) show some microstructural changes, but the changes that occur in one hour (or less) at relatively warm temperatures (-2°C, -5°C) are limited to relatively minor static recovery. Thus, the 15 mins our samples spend prior to quenching is unlikely to have affected the microstructures of our samples significantly. More specifically, the observed CPOs of our samples should represent those that existed at the end of deformation experiments. Hidas et al. (2017) also show no significant grain growth in pre-deformed samples over the time scales of our sample extraction process. Experiments on samples with initially undeformed but very fine grains (~10 μm initial size) show insignificant grain growth (Becroft, 2015) on the same time scales.

We have added a statement into section 2.2: "The maximum time between the end of an experiment and the sample being quenched in liquid nitrogen is ~15minutes. Microstructural changes on this timescale are likely to be limited to minor static recovery (Hidas et al., 2017), with no significant change in CPO or distributions of grain size."

4. You mention very often the elongation of the c-axis clustering. This elongation is not observed by Bouchez and Duval 1982 (later referred to as BD82), neither in natural ice from Hudleston (1977 or 2015 review paper), and not even in the deeper part of ice cores where shear is strong (as for instance bottom of Talos Dome ice core, Montagnat et al. 2012). We do not observe it neither in our recent torsion exp, going to gamma=2 (Journaux et al. AGU2017)... Therefore couldn't it result from the specific geometry of your test? It could be link to an extension component, cf Kamb 1972? The same remarks hold for the specific anisotropy of a-axis orientations on which I would be very careful before exploiting it too far in the conclusion...

In Figure 5 of (Bouchez and Duval, 1982), samples E1 and E3 both shows an elongation in the c-axis clusters. Although these can be seen in the original data they are clearer when the data are

reoriented so that pole to the shear plane is in the center of the stereonet. The re-plotting of the BD82 data that we used in our analysis is shown below. We have similar analyses for all the data we extract from the literature (from both experiments and natural ice) and it may be useful to show these as an extra resource. The c-axis cluster elongation is common to all the experiments where a large piece of ice is sheared, except one experiment in BD82 (E2) and one part of one experiment in Wilson and Peternell, 2012) (2-52 zone 2). Unpublished shear experiments from the Hobart lab all show elongated c-axis clusters (Adam Treverrow, pers. comm.), as do all samples from a new set of ~ 20 experiments (conducted at temperatues of - 7°C to -20°C, for shear strains of 0.2 to 0.6) from John Platt and Tom Mitchell. (We recently conducted EBSD on the Platt and Mitchell samples at the University of Otago). The elongation in the c-axis clusters does not occur in the syn-microscopic experiments (Burg et al., 1986), but the kinematic boundary conditions of these experiments are very different, with a sample thickness that is less than the grain size. We are intrigued that the Reviewer does not observe elongation in their recent experiments. We look forward to seeing these data and discussing this issue with the Reviewer in more detail. In the meantime, in the paper, we factually state: "this elongation has been observed in many previous studies (Kamb, 1972; Bouchez and Duval, 1982; Li et al., 2000;Wilson and Peternell, 2012)".
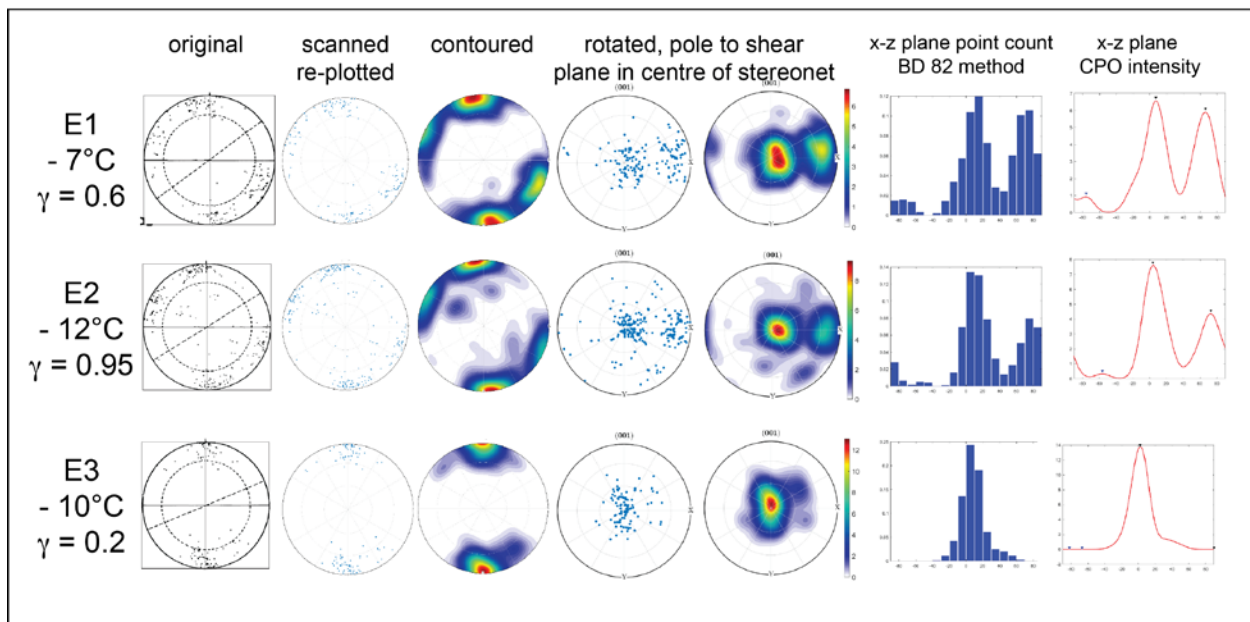

Figure R1. Replotting of the orientation data of Bouchez and Duval (1982) with MTEX toolbox.

The c-axis elongation may well be due to a component of sample elongation perpendicular to shear: we have already included this possibility in section 4.2: "Li et al. (2000) attributed this elongation to extensional deformation in the shear plane normal to the shear direction, due to the flattening of the sample during shear deformation." It is important to note that this flattening occurs in situations where there is zero normal stress perpendicular to the shear plane (Li et al., 2000) as well as when there is a compressional component normal to the shear plane (e.g. in our experiments). We are not totally convinced that this kinematic explanation is

sufficient; the statement we make in section 4.7, that "elongation of c-axis clusters remains a bit of an enigma" reflects our current level of understanding.

We agree that the c-axis cluster elongation we observed in our experiments is uncommon in naturally deformed ice samples. In section 4.4. we state: "The key difference between these single-cluster CPOs in natural samples and those generated in experiments is that the experimental samples all have an elongated c-axis cluster, whereas the naturally deformed samples mostly do not." In section 4.7 we state: "Furthermore, there are examples of symmetrical (not elongated) c-axis clusters in naturally deformed samples demonstrably related to shear (Hudleston, 1977)". To make this clearer we have added a statement into section 4.4, where the Hudleston data are discussed: "Hudleston (1977) did not observe elongated c-axis clusters. "

Since a-axis orientations have never been documented for sheared ice samples before, they are useful for future comparisons with naturally and experimentally deformed ice. We agree that it is not necessary to push the interpretation of these data too far at present, so we only described our observations in the conclusions section.

> 5. *I am not sure to understand the interest of pole figures made by taking one point per grain. First because it does not include information about grain size, that is otherwise directly integrated, and second because it could induce a bias in case of a non normal distribution (and it is the case I think, regarding your microstructure). Then, since intragranular misorientations are strong, it can induce another bias depending on the selected point inside the grain... I understand it in order to compare to "old" texture measurements that were done manually, but since the info is included into the "full" texture, not sure it is really interesting...*

The one point per grain (OPPG) stereonets are based on the average orientation of each grain, so the results are not biased by intragranular misorientations. The Reviewer is correct about OPPG stereonets not including information on grain size; they magnify the contributions of finer grains to the CPOs. Differences between OPPG and all data plots may relate to different CPOs in different grain size fractions. The primary reason we show OPPG stereonets (as pointed out by the Reviewer) is that these allow a better comparison to older manual measurements of c-axis orientations (until recently, for all published data). Since those OPPG stereonets do not take up a lot of space in the figures, we have included them for the reasons stated.

> 6. *In paragraph 2.5, about grain size measurement. How does it take into account the grain shape anisotropy? Such a method seems to be well adapted for a microstructure that evolves in staying "self-similar", but it is not the case at all, since the shape anisotropy (and the distribution of grain size) evolves with strain. Maybe you could just mention such a limitation? In the same idea, there is no mention of the fact that you are using a 2D technique to observe and evaluate grains that have a true 3D structures (with anisotropy). We all do that, of course, but the impact is different when a microstructure is relatively equiaxed, and remain so, or not. In particular, by doing so, we are totally unable to distinguish a small new grain from a cut piece of a highly serrated large grain... It therefore makes it complicated to distinguish nuclei (cf l. 13 of p.8). Again, you are*

using a "mean grain size", in the case of a non normal distribution, this mean has a weak meaning. Wouldn't a median + quartile representation be more adapted, in order, for instance to follow the evolution of the grain size distribution with strain?

Our grain size measurement does not take grain shape into account. By using an equivalent diameter as the grain size, we minimized the influence of grain shape on the measurement of grain size. This is fairly standard practice in the microstructural community (Berger et al., 2011; Cross et al., 2017; Heilbronner and Kilian, 2017). Grains are not strongly shaped so we do not think that ignoring shape factors will affect measured distributions of grain size significantly.

The Reviewer is correct that this is a 2D technique. As the Reviewer suggested, we have added a sentence on the limitation of this grain size measurement in the Methods section: "Note that grain size determined this way represents the size of a 2D cross section of a 3D grain."

Most recrystallized grain size distributions are skewed (log(d) tends to be normally distributed). We agree that for such non-normal distributions, the mean is not a good scalar representation of the distribution. Therefore, we also presented the "peak grain size" based on the grain size distribution in Figures 5, 6 and 7. Many other studies, however, present the mean --- so the mean values here give a comparison for those studies. There is a particular issue in the "ice world" in that many grain sizes are calculated as the mean area (by counting the number of grains in a given area of a thin section). The grain area distribution is highly skewed. More important than the scalar representations of grain size are the measured distributions presented in figures 5, 6 and 7.

7. *You refer to SGB, that you assume to be numerous and to evolve with strain. Honestly, this is hard to evaluate from the only figures 5 to 7, since there is no quantitative analyses of it. Relatively to some observations that I have done, I am even surprise not to see more of them, and I would be enable to say that there is a clear evolution with time. Couldn't you estimate, for instance, the Kernel Average Misorientation, and its evolution with time? (cf l.16 p 13 for instance).*

We did not assume that the number of subgrain boundaries evolves with strain (and do not say so in the paper). We have not presented data that show quantitatively the subgrain boundary density. In this paper we are trying to focus on the CPO and the minimal microstructural observations required to understand the CPOs. In the Results section, we simply described our observations: subgrain boundaries were observed, and subgrains (cells with at least one low-angle boundary segment) are of similar size to recrystallised grains (cells entirely surrounded by high-angle boundary segments). Subgrain boundaries (grey lines) can be seen in all of the EBSD maps in Figures 5, 6, and 7.

The Reviewer is correct, we do not have a quantitative measurement on the number or density of subgrain boundaries. As suggested, we have added the averaged kernel average misorientation (KAM) for each of the sections in Figures 5, 6 and 7. Averaged KAM provides a measurement of intragranular distortion. The values of averaged KAM do not show a trend with changing strain or temperature. It is not clear whether we should see any increase in KAM across the range of strains explored (between shear strains of 0.5 and 2.5). The presence of

low-angle (subgrain) boundaries is indicative of the operation of recovery processes. The decrease in grain size compared to the original grain size requires a nucleation process. The observation that cells with at least one subgrain boundary have similar sizes to grains surrounded entirely by high-angle grain boundaries is consistent with subgrain rotation recrystallization being a nucleation process. These processes can operate within an approximately steady-state microstructure. We might expect an increase in KAM in the first few percent of strain, but the data shown here are for much larger strains. Clearly, investigating and quantifying internal distortions of grains is an important thing to do, but beyond the scope of this paper. In the paper, we simply present microstructural evidence that is consistent with the operation of recovery and subgrain rotation. Our main focus is to present the CPO patterns and to establish a testable explanation.

8. *part 4.3 About the ' angle, well, I have quite a lot to say (sorry...). First, does it really make sense to compare an evaluation of this angle performed based on very different materials, from experiments with very different conditions? In particular, if I want to separate the two population of M1 and M2 orientation, I aim to take into account not only the visible angle between the 2 poles, but also the number of orientations on each pole (some kind of "weighted angle"). Why? Because in some cases there remain so few orientations in the M2 pole, that the separation is doubtful (and strongly dependent on the measurement technique). For instance, my interpretation of the gamma = 2 texture in BD82 is that there is no more M2 (or too few to be considered, and this was also the interpretation of BD82). Therefore, in this case, the phi angle has not meaning. I would do the same interpretation on your figure 2d at -20 and -30C. Then, from my point of view, figure 8 is highly confusing. (a) you compare experiments made in drastically different conditions. For instance Burg et al. worked on thin plates of ice, with very few grains, and strong boundary conditions effects are expected. Kamb added some axial compression at different levels, Hudleston samples are from natural fault... (b) the weakness of the model used by Llorens et al. is also hidden in the figure. This model, by construction (because it requires non basal prismatic and pyramidal slip system to accommodate the deformation) is unable to stabilise the M1 pole to the vertical, as it is observed naturally or in the laboratory. Although the angle can be small between this pole and the vertical, it persists and the main reason is a non adapted representation of the mechanisms that are accommodating basal slip. Even when adding some representation of subgrain mechanisms can't they correct this bias. But when plotting only the phi angle, this problem is hidden, and the interpretation can be biased... Well, I am not sure that this phi angle evolution is so necessary to the interpretation of your results, and maybe this one would be clearer without trying to fit all other existing data???*

It is true that focusing on the single angle phi is a simplification. However for the experimental data and the one data set on natural ice we can plot on here (Hudleston, 1977), the primary maximum is, within error, normal to the shear plane, so the angle between the two maxima becomes a useful parameter. Using a simple parameter phi makes it easier for readers to understand our paper, which is the same approach used in Kamb (1972) and Bouchez and Duval (1982). It is directly analogous to measuring the opening angle in open cone (small circle) CPOs

from axial deformation experiments (e.g., in Qi et al. (2017)). Understanding the relationship of these angles to strain and deformation conditions might lead to a better understanding of the underlying physical processes.

The Reviewer is correct to state that there are some difficulties, some of which are already stated in the text. For example, we state: "The most likely explanation is that the data in Fig. 8 represent experiments with subtly different kinematics (deviations from perfect simple shear) and contains data from experiments conducted across a range of strain rates (or stresses)." We agree that it is rather too problematic to include the see-through experiments of Burg et al. (1986); these data have numerous attributes that do not match other experiments and undoubtedly relate to the very specific boundary conditions of those experiments. We have removed the Burg et al. (1986) data from the figure and related discussion from the text. All of the experimental data and those from natural samples remaining on the plot are dominated by simple shear deformation (the Kamb data we use are those from simple shear-dominated experiments, as are the Wilson and Peternell data). In reality, we need sets of experiments for constant temperature and strain rate (or stress) where only the shear strain varies to verify the pattern of this plot. In the meantime, we believe it is useful to show the plot as is.

Numerical models provide a tool that allows for scaling to slower (natural) strain rates, which can be incorporated into larger scale ice sheet models. For this reason, the comparison of laboratory experiments with model outputs is important. We can use the differences between model outputs and observations of natural ice to discover what is missing or incorrect in numerical codes, or what might be a result of a boundary condition in an experiment. Importantly, we can also use such comparisons to design better experiments. Picking values of the phi parameter from models is problematic, because, as the Reviewer states, the main cluster of c axes is oblique to the shear plane normal. We have tried to be as clear as possible on this point in the text. Nevertheless, we can extract two clusters from these models, and the evolution of the angle between them provides insight into what processes might be going on in the samples.

9. *Part 4.5 Here, again is evoked the increase of subgrain boundary and lattice rotation effect without it being really quantified... It is therefore not so straighforward to assess an evolution from GBM to lattice rotation dominating process during recrystallization.*

Here we reiterate that we do not state that subgrain boundaries become more prevalent with strain and the KAM data we have now included support this. Our focus is on the balance between lattice rotation and GBM as a way to explain the CPO evolution. In this context, we state that rotation is controlled by a set of processes including dislocation glide, recovery, subgrain rotation, and grain boundary sliding. We accept that unpacking the details of this and quantifying this balance is rather difficult. Again, this is another aspect for which modeling approaches are important.

10. *Part 4.6 This paragraph is, to my point of view, giving a quite simplistic explanation for CPO development. It has been shown in ice and other materials, for quite some time now, that stress and strain field heterogeneities prevent from making a clear distinction between grains "well oriented" and grain "badly oriented" (see e.g. Grennerat et al.*

Our explanation is deliberately simplistic as we want to present a broad hypothesis that can be tested further. Our approach follows that of Alley (1992) and is influenced by a much larger set of experiments in which samples were deformed via axial shortening (the data in Qi et al. (2017) comprises a small part of this data set), wherein low temperatures and/or high strain rates yield clustering of c-axes parallel to shortening, and high temperatures and/or low strain rates yield an open cone fabric (small circle). In axial shortening, rotation yields the cluster fabric, and the open cone comprises grains with high resolved shear stresses. So, the rationale for assigning the possible relative importance of rotation and GBM to the observed CPOs is clear. Simple shear is more difficult to treat in this way, as the outcome of rotation (to c axes perpendicular to shear plane) coincides with one of the orientations of high resolved shear stress. In axial experiments we would predict an evolution of cone angles with strain. As yet there are no data on cone angles as a function of strain, except for experiments conducted for high temperatures and low strain rates (Jacka and Maccagnan, 1984; Montagnat et al., 2015; Piazolo et al., 2013; Vaughan et al., 2017), wherein the cone angle remains approximately constant as a function of strain. We have now conducted lower-temperature axial compression experiments to increasing strains, but have not yet acquired the microstructural data.

We agree with all of the Reviewer's comments related to kink bands in ice. It is notable that we do not observe kink structures in these shear experiments. In contrast, kinks are common in axial compression experiments at similar temperatures and strain rates to ours, and in shear experiments at lower temperatures (equivalent to the -20C and -30C experiments here) (Craw, 2018; Seidemann et al., 2018) and the kinking influences the recrystallization behavior (Seidemann et al., 2018).

We agree that internal distortion is not a proxy for dislocation density. We have removed "(a proxy for dislocation density)" in section 4.6 page 13.

This is the first-time that a-axes have been measured in experimentally sheared ice samples. In our experiments, for large strains, the a axes are parallel to the shear direction. If this were generally true it has important implications for the interpretation of CPOs of naturally deformed ice: a axes could be used to suggest shear directions. We therefore think it is important to include this section.

We thank the Reviewer for sharing their recent experimental observations. Besides the difference in deformation kinematics - ours were simple shear with a small component of compression, and the Reviewer's were (we think, from the description) perfect simple shear --- other conditions may affect the distribution of a-axes. For example, in our high temperature (-5°C) experiments, a axes do not align parallel to shear until high strains. The Reviewer mentioned that her experiments were conducted at high temperatures. We guess, because the experiments were at atmospheric pressure, that stresses (and thus strain rates) will be necessarily lower than in our experiments, which has a similar effect to being at higher temperature (Hirth and Tullis, 1992; Qi et al., 2017; Tullis et al., 1973). It is possible that temperature, and its effect on deformation and recrystallization processes, is a key control on the distributions of a axes. To solve this problem, we believe it is important to publish the a-axis distributions we have observed, and encourage others, including the Reviewer's group, to do the same.

We added citations for Gow and Williamson (1970), Herron and Langway (1982) and Herron et al. (1985) to the first sentence of this subsection.

> *12. Conclusion: From the remark about paragraph 4.7, I would suggest not to mention the point 4 of the conclusion, since it has not been shown that the observed results are not related to the specific experimental conditions used here. To turn this observation into a generic tool to interpret natural texture appears to me a little too fast...*

We did not include any statements on the interpretation of natural CPO using this observed a-axes clustering. This observation is new and will be worth testing by other researchers. So we think it is important to keep it here.

> *13. Similar remarks would hold also for the point 5, and the mentioning of the elongation of c-axis cluster that has not been observed in previous work (for instance Bouchez and Duval 1982).*

The elongation of the c –axis clusters is very common in shear experiments and is present in all of our results. Irrespective of the explanation, this is a factual observation and like the a-axis clustering should be reported as a conclusion.

14. About point 6, please refer to my comment on subgrain observations that are very weak in this paper. In order to be able to provide some info about subgrain size, one would need a measurement of this size, or at least a proxy, and it is not given in this work.

It is true that we do not provide a measurement of subgrain size. In a simple bulk measurement subgrain sizes will always come out smaller than grain sizes (Trimby et al., 1998). For the microstructural data presented here, a statistical subgrain size value measured using a low misorientation cut off will be essentially the same as the grain size, but that number will not be particularly meaningful, since subgrains only occur in one out of ~ 100 grains. In this case, the qualitative observation that the subgrains are of similar size to recrystallized grains is still useful.

15. Point 7, a similar remark holds here too since, in order to link what the author calls "high Schmid-factor grains" to GBM, one would need to show that there exist a relation between the Schmid factor and the grain size, or grain shape for instance (if grain size or shape is taken as a proxy of GBM). And this is not provided here. And the last sentence appears speculative too, since, to be able to discriminate the nucleation mechanisms, one would need to be able to observe nuclei! But, because of the 2D observation tool used here, one cannot distinguish small new grains from cut part of a serrated grain boundary. On top of that, nucleation by bulging could very well occur, but one would not observe it by only looking at 2D microstructure at the end of the test. Therefore, the only qualitative observation of subgrain boundaries is not enough to discriminate the nucleation mechanism. So this could be your interpretation, or assumption, but to my point of view this is not shown by the results presented here.

We agree with the Reviewer that without establishing a relationship between Schmid factor and grain size, it is not a good idea to conclude this way. Therefore, we removed "high Schmid-factor grains", so that the sentences reads "…a balance of the rates of lattice rotation due to dislocation slip and growth of grains by strain-induced GBM."

Distinguishing nucleation mechanisms is always difficult. We agree that ruling out bulging is very difficult and we have removed the implication that we can rule it out in the text.

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Response to Reviewer 2

We thank Reviewer 2 for their thoughtful review. We present our detailed responses (shown in black text) to the Reviewer's comments (shown in blue).

1. *During the sample preparation, when the samples are cooled to -60°C for the welding of the indium jacket, is there any possibility for the thermal/confinement stresses to alter the microstructure as it would relate to the grown-in dislocation density?*

Each experimental sample, including the undeformed one published in Qi et al. (2017), were stored in liquid nitrogen before microstructural characterization in the SEM. No thermal-stress-related microstructure was observed in these samples. Transferring the sample from the -30°C freezer to the -60°C alcohol bath for welding is a modest temperature change compared to immersing a sample from the freezer in liquid nitrogen. Thus, transferring the sample from the -30°C freezer to -60°C alcohol should not induce any observable alterations to the microstructure.

Moreover, after welding the jacket, each sample was placed into the apparatus and maintained at the temperature and pressure of the deformation experiment for >1h, so that if any dislocations were produced during welding, those dislocations would be relaxed before deformation started.

2. *From looking at Figure 1, I am perplexed as to how the piston is able to translate laterally while also remaining rigid and in-line with the axis of compression? Could you please explain?*

As illustrated in the figure below, as the driving piston moves vertically up, the bottom 45°-cut piston moves sideways, because the ice sample is weaker than the pistons and the boundary between the assembly and the driving piston allows lateral movement. This design for shear deformation is widely used in rock deformation studies (e.g., Schmid et al., 1987, JSG; Dell'angelo and Tullis, 1989, Tectonophysics). We have modified Figure 1 to include this information.

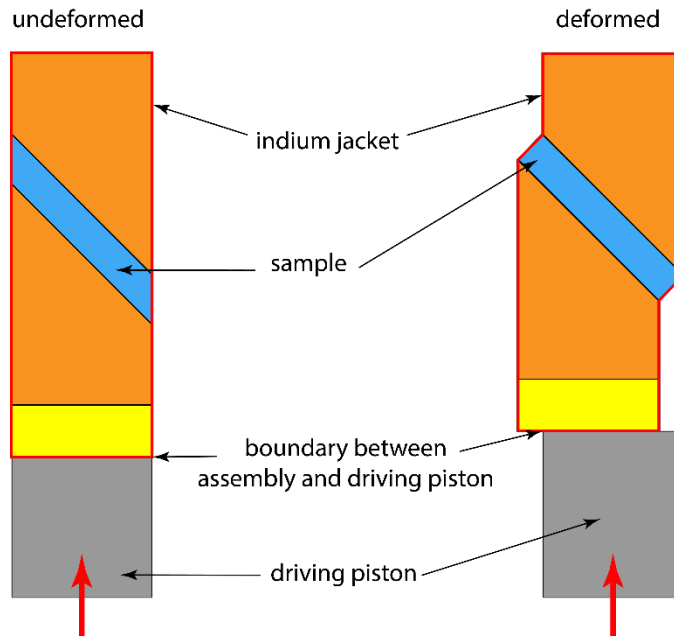Figure R1. Schematic drawing illustrating the movement of the pistons during deformation.

3. *Could you include the data (via personal communication) related to the flow law of the indium jacket and perhaps also the company/supplier that is used? Such that these experiments could be repeated?*

We can share W. Durham's indium data with you. But as the data belong to Durham, we think it is not appropriate to publish it in our paper.
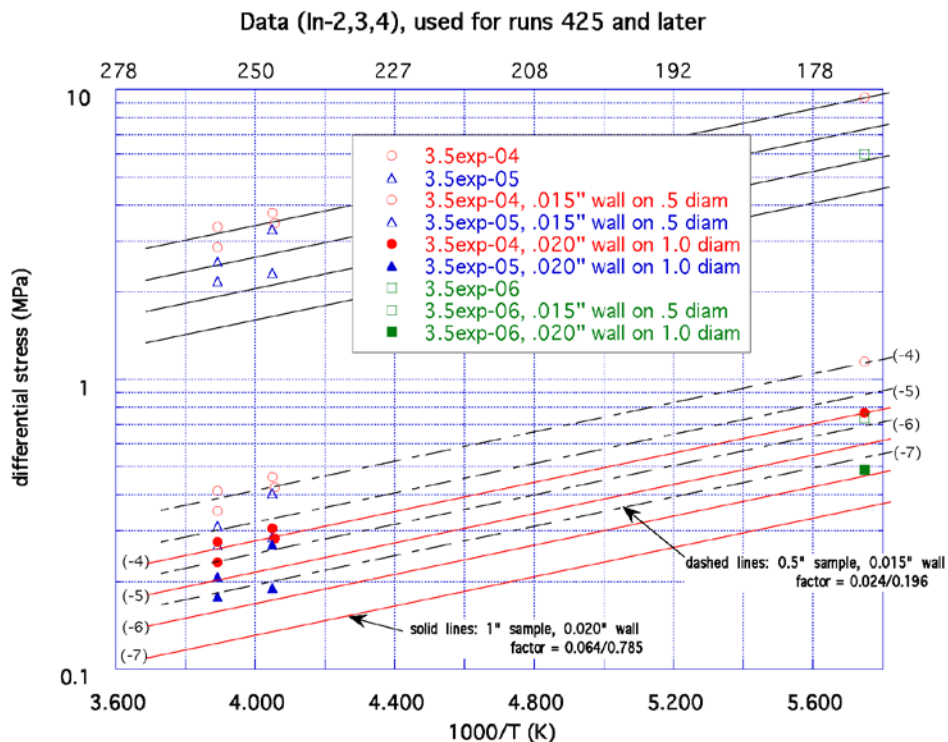
Figure R2. Plot of differential stress vs. temperature for indium. Data from W. Durham.

We added a citation (Jacka and Maccagnan, 1984) here as suggested.

5. *In Section 3.4, please comment on the skewed distribution of grain sizes. Is this lognormal? As would be expected? Was this distribution used for calculating the mean? How was the anisotropy in the elongated grains accounted for?*

For most samples, the distribution is lognormal. A lognormal distribution of grain size was expected, because our previous compression experiments found roughly the same distribution. Moreover log normal distributions of dynamically recrystallized grain size in rocks and metals are very common. The distribution was not used to calculate the mean grain size, but was used to identify the "peak" grain size. Using an equivalent radius to calculate grain size, the influence of anisotropic grain shapes is minimized.

6. *Discussion Section. Although I appreciate the detail of this section, it seems to me that it could be more concise, such that the most relevant findings and results are more impactful.*

We have shortened the discussion section by about half a page.

7. *In Section 4.1, should any consideration be given to the recrystallized grains experiencing primary creep in this scenario?*

The terms "primary creep", "secondary creep" and "tertiary creep" are used to describe the behavior of the bulk of a material. In tertiary (approximately steady-state) creep, dynamic recrystallization and grain growth are balanced. Recrystallized grains with lower dislocation densities than other grains are produced at all times. But researchers do not generally consider these recrystallized grains to be under primary creep, because the bulk material is in the tertiary creep stage.

8. *Page 11, line 30, replace "in" with "are".*

Changed as suggested.

9. *Line 13-14, Page 13, please add a citation for this statement.*

We added a citation (Steinbach et al., 2017) as suggested.

10. *Regarding GBS mentioned in Section 4.6, was there any evidence of this in the observed microstructure? Quadruple points? If not, how would this be incorporated into models for ice if it has yet to be directly observed?*

GBS is always a tricky process to infer because, unlike dislocation creep, it does not leave clear microstructural signatures, or its characteristic microstructures have not yet been identified. Furthermore it is unlikely that basal-slip accommodated GBS dominates the deformation at the high stresses explored in our experiments, in which dislocation creep is likely also occurring.

Our EBSD maps contain numerous examples of quadruple junctions and near-quadruple junctions. Similar observations have been used to infer GBS in other materials (Negrini et al., 2018) but the issue is complex (Kellermann-Slotemaker and De Bresser, 2006) and needs a more systematic investigation to be useful in these experiments. The microstructures of the samples deformed at -20°C and -30°C are very similar to those in the recrystallized portions of samples deformed by Craw et al. (2018). In the Craw et al. work, the (natural) samples had much larger original grains, and explaining the CPOs of the porphyroclasts and recrystallized grains is much, much easier if GBS is allowed. We cannot prove that GBS is occurring in our experiments, but we can infer it is active based on extrapolation of existing flow laws for GBS to the conditions of our experiments, and that it will then influence the evolution of the CPO. Modelling GBS allows us to explore its potential effects on CPO in a more rigorous way. Another indication that GBS is likely is that peak stresses at a given strain rate are grain size-dependent (Qi et al. 2017). Grain size sensitivity, with strain rate increasing with decreasing grain size, requires grain boundary sliding (Langdon, 2006) for kinematic reasons, irrespective of whether sliding is accommodated by diffusional or dislocation processes. As we have evidence that there is grain size sensitivity (and thus a component of GBS) at the (larger) starting grain size (Qi et al. 2017), it is likely that GBS becomes even more important as the grain size is reduced with strain.

11. Conclusions Section. Could also be more concise. (e.g. no need to summarize the method and/or results before presenting a conclusion)

We consolidated this section as suggested. The summary of the experimental methods a was removed.

12. Figure 3b – and with regard to Question 2: : :Am I correct to interpret the increase in the shear stress in these tests as related to the piston becoming displaced and the onset of frictional effects? If not, could you further explain the cause of the increase in the shear stress?

The raw data are illustrated in Figure 3a. The stress is roughly stable with increasing strain in the raw data, which suggests there is no onset of an additional frictional force. In Figure 3b, the increase in the stress is due to the application of the area correction. As shear strain increases, the piston becomes displaced (see Figure R1 above), and the area of the sample that is in contact with both top and bottom pistons decreases.

However, after consulting with experimentalists who are more familiar with the direct shear method (Greg Hirth and Leif Tokle), we decide to remove panel b from Figure 3. They have concluded for a large data set on other earth materials that stress is transferred across the whole cross sectional area up to high strain and that the area correction is not needed. The observation that the grain sizes of our samples do not change much with increasing strain, especially in the -20 and -30°C experiments, suggests that the stresses in our experiments are roughly constant with increasing strain at strains > 0.2. This confirms that an area correction is not necessary.

13. Figures 5,6,7 – It's not clear to me what is being indicated with the blocky black arrow on the left of these maps. Is this a transverse view/map?

These black arrows mark the shear direction. These figures are transverse view, which we called it shear plane, as illustrated in Figure 1. You can see the black arrows in Figures 1 and 2. In the captions of Figures 5, 6 and 7, we mentioned that: "The shear direction on the top side is up, as shown by the black arrow."

14. Figure 10 – Is it possible to also quantify the Key Processes related to the Final microstructure? Such that these 2-D characteristics could be identified with an automated algorithm? Perhaps see Lehto et al. 2016, Characterization of local grain size variation of welded structural steel, as a good starting point. It seems that there needs to be a better method of identifying and/or quantifying the differences in these microstructural regimes.

Thank you for suggesting Lehto et al. 2016. It is a very interesting paper, but beyond the scope of the discussion in our paper. In our paper, we are focusing on the observed transition in the CPO patterns. We use microstructural evidence to support our explanation of CPO formation, but at the current stage it is very difficult to quantify the contributions from different recrystallization processes. We have considered kernel average misorientation and subgrain boundary density, but neither of them is a good proxy for a recrystallization mechanism. This is an area of future research for our groups.

15. Lastly, after reading Maurine Montagnat's insightful comments pertaining to this manuscript, I would have to agree that it is difficult to ascertain with any certainty the nucleation mechanisms responsible for recrystallization from a 2-D post-mortem analysis alone.

Yes. There are difficulties in determining the nucleation mechanism from a 2D section. We have removed the sentence related to the nucleation process in the conclusion section.

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Negrini, M., Smith, S.A., Scott, J.M. and Tarling, M.S., 2018. Microstructural and rheological evolution of calcite mylonites during shear zone thinning: Constraints from the Mount Irene shear zone, Fiordland, New Zealand. Journal of Structural Geology, 106, pp.86-102.

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Schmid, S.M., Panozzo, R. and Bauer, S., 1987. Simple shear experiments on calcite rocks: rheology and microfabric. Journal of structural Geology, 9(5-6), pp.747-778.

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Crystallographic preferred orientations of ice deformed in direct-shear experiments at low temperatures

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Abstract. We sheared synthetic polycrystalline ice at temperatures of -5, -20 and $-30°$C, to different shear strains, up to $\gamma = 2.6$ (equivalent to an extrusion of 150%). Cryo-electron backscatter diffraction (EBSD) analysis shows that basal intra-crystalline slip planes become preferentially oriented parallel to the shear plane, in all experiments. This is visualized as a primary cluster of crystal c-axes (the c-axis is perpendicular to the basal plane) perpendicular to the shear plane. In all except the two highest-strain experiments at $-30°$C, a secondary cluster of c-axes is observed, at an angle to the primary cluster. With increasing strain, the primary c-axis cluster strengthens. With increasing temperature, both clusters strengthen. In the $-5°$C experiments, the angle between the two clusters reduces with strain. The c-axis clusters are elongated perpendicular to the shear direction. This elongation increases with increasing shear strain and with decreasing temperature. Highly curved grain boundaries are more prevalent in samples sheared at higher temperatures. At each temperature, the proportion of curved boundaries decreases with increasing shear strain. Subgrains are observed in all samples. Microstructural interpretations and comparisons of the data from experimentally sheared samples with numerical models suggest that the observed crystallographic orientation patterns result from a balance of the rates of lattice rotation (during dislocation creep) and growth of grains by strain-induced grain boundary migration (GBM). GBM is faster at higher temperatures and becomes less important as shear strain increases. These observations and interpretations provide a hypothesis to be tested in further experiments and using numerical models, with the ultimate goal of aiding the interpretation of crystallographic preferred orientations in naturally deformed ice.

1 Introduction

Polycrystalline ice 1h deformed in the laboratory (e.g., Kamb, 1972; Li et al., 2000; Wilson et al., 2014; Qi et al., 2017) and in nature (e.g., Gow and Williamson, 1976; Hudleston, 1977; Thorsteinsson et al., 1999; Treverrow et al., 2016; Weikusat

et al., 2017) develops strong crystallographic preferred orientations (CPO, often called crystal orientation fabric, COF, in the glaciological literature), usually presented as the preferred orientation of ice [0001] axes, i.e., c axes. As single crystals of ice are most easily deformed by glide on the (0001) plane, i.e., the basal plane (Nakaya, 1958; Wakahama, 1967; Duval et al., 1983), the manner in which the c axes are aligned affects the flow strength for a given applied deformation kinematics, for example, simple shear versus uniaxial compression (e.g., Shoji and Langway, 1988; Azuma, 1995; Li et al., 1996; Duval et al., 2010; Budd et al., 2013). The development of a CPO is commonly used to explain the accelerating strain rate that occurs after secondary creep (Cuffey and Paterson, 2010, pp. 53-55). The occurrence of strong CPOs in ice has led to the use of enhancement factors (Jacka and Maccagnan, 1984; Budd and Jacka, 1989; Li et al., 1996) to relate laboratory flow laws for isotropic ice (Glen, 1955, 1975; Goldsby and Kohlstedt, 2001) to the flow of ice in glaciers and ice sheets where a strong CPO is likely (e.g., Russell-Head and Budd, 1979; Thorsteinsson et al., 1999). Thus, understanding the formation and evolution of CPOs during deformation is crucial to our ability to predict rates of flow of ice sheets and glaciers as ice temperature rises in a warming world (Houghton, 1996) and as stress boundary conditions change, for example, during ice shelf thinning and collapse (e.g., Scambos et al., 2004; Joughin et al., 2014). Furthermore, the CPO controls elastic anisotropy in ice and, through this, the anisotropy of sound wave velocity (Kohnen and Gow, 1979; Diez et al., 2015; Vaughan et al., 2017). Seismic data can be used to constrain bulk CPOs (e.g., Bentley, 1972; Smith et al., 2017; Kerch et al., 2018) and understanding how CPOs relate to deformation kinematics and conditions is valuable in limiting the range of possible CPO solutions in a field seismic experiment (Picotti et al., 2015; Vélez et al., 2016).

Many laboratory experiments demonstrate the development of a CPO in polycrystalline ice. The vast majority of these experiments are on ice samples deformed in uniaxial compression to relatively small maximum strains (axial strains up to ∼0.3) (e.g., Jacka and Maccagnan, 1984; Jacka and Li, 2000; Wilson et al., 2014; Qi et al., 2017; Vaughan et al., 2017). However, most deformation in ice sheets and glaciers is dominantly simple shear (Cuffey and Paterson, 2010) and CPOs developed in compression and simple shear are not equivalent (Alley, 1992). Shear experiments on polycrystalline ice are limited to relatively high temperatures and mostly relatively low shear strains (Kamb, 1972; Bouchez and Duval, 1982; Li et al., 2000; Wilson and Peternell, 2012). Only four published shear experiments (Bouchez and Duval, 1982; Wilson and Peternell, 2012) achieve shear strains greater than 0.5 at temperatures ≤ -10°C, with the coldest experiment conducted at -15°C. Shear experiments at colder conditions (Wilson and Peternell, 2012) have not achieved shear strains >0.12. The majority of laboratory shear experiments have been conducted at temperatures of -5°C or warmer.

In this contribution, we adapt the direct shear method, applied in rock deformation studies (e.g., Schmid et al., 1987; Dell'angelo and Tullis, 1989; Zhang and Karato, 1995; Heilbronner and Tullis, 2006; Kohlstedt and Holtzman, 2009) to polycrystalline ice. By confining our samples with gas pressure, we are able to apply relatively high differential stresses without causing brittle fracture of the samples, allowing us to shear ice to large strains at much lower temperatures than have been applied before. The objective of this paper is to explore the effects of shear strain and temperature on the CPOs and microstructures of ice deformed in shear, and to explore the implications for understanding the development of CPO in ice and the associated evolution of its mechanical behavior.

2 Methods

2.1 Sample preparation and deformation assembly

To prepare polycrystalline ice samples with a controlled initial microstructure, we adopted the flooding and freezing procedure developed by Durham et al. (1983) and Stern et al. (1997). Ice cubes made from deionized water were crushed in a blender into ice powders. These powders were then sieved at -30 to $-20°C$ to sizes between 0.18 and 0.25 mm for "standard-ice" samples (Durham et al., 1983). The sieved seed-ice grains were packed into stainless-steel cylindrical molds with an inside diameter of 25.4 mm and capped with double-o-ring-sealed stainless-steel end plugs, to a porosity of $\sim 40\%$. Air was then evacuated from the pores in the packed powder, while the molds containing the powders were equilibrated at $0°C$ in an ice-water bath. Degassed, deionized water (at $0°C$) was then introduced into the evacuated powders in the molds. Flooded sample molds were inserted into vertical holes in a large styrofoam block so that the mold bottoms rested on a copper plate at the bottom of a freezer maintained at $-30°C$. This ensured that the water in the saturated powders froze from the bottom up, excluding bubbles from the samples. After freezing overnight, ice samples were gently pressed out of the mold with an arbor press.

A 4 to 6 mm-thick slice was cut from the cylinders at $45°$ to the cylinder axis. Both surfaces were shaved to ensure they were flat and parallel to each other. These surfaces were then polished on 180-grit sandpaper. See Fig. 1(a) for a picture of a prepared sample. The initial sample thickness, h_0, was measured with a micrometer. The ice sample was placed between two $45°$-cut aluminum or wood cylindrical pistons, as illustrated in Fig. 1(b). To prevent slippage between the ice and the pistons, 180-grit sandpaper was glued onto the cut surfaces of the pistons with epoxy. Ice samples and pistons were enclosed in an indium tube with an inner diameter of 25.4 mm, which was then encapsulated in another indium tube with an inner diameter of 26.9 mm, with the bottom of the tube "welded" to a 12.7 mm-thick stainless-steel spacer (here "welded" means the indium tube was melted against the copper-plated steel spacer with a soldering iron). The total thickness of the two indium jackets is 1.4 mm. The bottom of a steel semi-internal force gauge was welded to the top of the outer indium jacket, with a 19.1 mm-thick zirconia spacer placed between the force gauge and sample to thermally isolate the ice from the welding area. During welding, the sample assembly was immersed in an alcohol bath at $\sim -60°C$, leaving only the small area to be welded above the bath.

2.2 Deformation Experiments

Samples were deformed in direct shear at a confining pressure $P = 20$ MPa at three different temperatures, $T = -5, -20$ and $-30°C$, in a cryogenic gas-medium apparatus (Durham et al., 1983; Heard et al., 1990), as illustrated in Fig. 1(c). Pressure and temperature were maintained constant to ± 0.5 MPa and $\pm 0.5°C$, respectively. Before deformation, each sample was allowed to equilibrate at the deformation pressure and temperature for about 1 h. Deformation experiments were performed at a constant axial displacement rate of 5.08×10^{-4} mm/s. Experiments were terminated at different shear strains. After each run, the indium jackets were carefully peeled off, and then the deformed sample was photographed and placed into a long-term storage dewar filled with liquid nitrogen. The final sample thickness, h_1, was estimated from a photo, and we noted whether the sample thickness was constant along the length of the sample. The horizontal shift of the edge of the sample, synthetic to the imposed shear direction, l, was measured with a ruler (see Fig. 1(f)). The maximum time between the end of an experiment and the

sample being quenched in liquid nitrogen is ~15 minutes. Microstructural changes on this timescale are likely to be limited to minor static recovery (Hidas et al., 2017), with no significant change in CPO or distributions of grain size.

2.3 Data processing

The raw data, i.e., time, axial displacement and load, were processed to obtain shear strain, shear strain rate and stress data. In our experiments, assuming samples were deformed in simple shear, i.e., no flattening of the samples occurred and there was no deformation of the pistons, the calculated shear strain rate, $\dot{\gamma}_{\text{calc}}$, is given by $\dot{\gamma}_{\text{calc}} = \frac{\sqrt{2}v_{\text{ax}}}{h_0}$, where v_{ax} is the axial displacement rate. The calculated shear strain is given by $\gamma_{\text{calc}} = \dot{\gamma}_{\text{calc}} \times t_t$, where t_t is the total elapsed time of deformation. However, since samples shortened slightly in the axial direction and the wooden pistons were also slightly deformed, the calculated shear strains and shear strain rates sometimes deviated from the actual values for the samples. Moreover, some samples exhibit lateral bulging (Fig. 1(g)), the measurement of which provides an estimate of the degree of axial shortening, $\varepsilon_{\text{axial}}$. Thus, we measured the shear strain directly from the deformed samples and determined the shear strain rate from the measured shear strain. The shear strain of each sample is determined from the displacement measured on the sample by

$$\gamma_{\text{meas}} = \frac{\sqrt{2}l}{h_0}. \tag{1}$$

The measured strain rate of each sample is given by,

$$\dot{\gamma}_{\text{meas}} = \frac{\gamma_{\text{meas}}}{t_t}. \tag{2}$$

For the samples with $\gamma_{\text{meas}} \gg \varepsilon_{\text{axial}}$, the values of γ_{meas} and γ_{calc} are very close in value.

Shear stress is calculated from the measured axial load, F_{ax},

$$\tau_{\text{raw}} = \frac{1/\sqrt{2}F_{\text{ax}}}{A_{s0}}, \tag{3}$$

where $A_{s0} = \frac{\sqrt{2}}{4}\pi \times 25.4^2$ mm^2 is the initial area of the shear surface. The strength of the indium jackets at a given temperature and strain rate, based on an indium flow law (W. Durham, personal communication), was subtracted from τ_{raw},

$$\tau_{\text{cor}} = \tau_{\text{raw}} - \tau_{\text{in}} \tag{4}$$

Note that the shear stress and shear strain rate in our experiments have the following relationship with the von Mises equivalent stress, σ, and von Mises equivalent strain rate, $\dot{\varepsilon}$

$$\tau = \frac{\sigma}{\sqrt{3}}, \quad \dot{\gamma} = \sqrt{3}\,\dot{\varepsilon}. \tag{5}$$

As illustrated in Fig. 1(d) for a typical stress-strain curve, with increasing shear strain, shear stress increases to a peak at a strain of 0.05 to 0.15 (equivalent to an axial strain of 0.03 to 0.09) and then decreases. Data collected for the peak stress are used to characterize the mechanical behavior of ice with an initial, isotropic microstructure. This is equivalent to using the minimum strain rate in creep tests (e.g., Jacka and Maccagnan, 1984). The magnitude of the stress drop, $\Delta\tau$, is the difference

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in stress between the peak stress and where the slope of the stress-strain curve approaches zero, as illustrated in Fig. 1(d). The stress data at higher shear strains are affected by non-coaxial alignment of the pistons and bending moments on the internal force gauge, and are not as robust as the peak-stress data. Summary data are presented in Table 1.

2.4 Collection of orientation data with electron backscatter diffraction (EBSD)

Samples were prepared for EBSD analysis in a scanning-electron microscope (SEM) at the University of Otago, following the procedure described in Prior et al. (2015). During preparation, a sample was either kept in a cryogenic dewar (at $\leq -190°$C) or in an insulated transfer box (at $\leq -120°$C). The deformation pistons were carefully separated from the ice sample with a razor blade. The sample was mounted on a copper ingot, with a surface parallel to the shear plane facing up (see Fig. 1(e)). Mounting, polishing and analysis were performed in the same way as reported previously (Qi et al., 2017). Crystallographic orientation maps of all samples were obtained from the shear plane, with step sizes summarized in Table 2.

2.5 Microstructural analyses

Orientation data obtained from diffraction data were processed using HKL Channel5 software, including removal of single mis-indexed points, and assigning the average orientation of neighboring pixels to un-indexed points. Grains were constructed from processed orientation data using the MTEX toolbox (Bachmann et al., 2011). Grain boundaries were drawn where neighboring pixel misorientations exceeded $10°$. No extrapolation of orientation data was applied in MTEX, since the data were already processed by the HKL Channel5 software. Grain size was determined as the equivalent diameter of a circle with the area of each grain in cross section. Note that grain size determined this way represents the size of a 2D cross section of a 3D grain. In the analysis of the average grain size for a map, grains containing no more than 5 pixels or lying on the edge of the map were excluded.

To quantify the intragranular misorientations for each sample, averaged kernel average misorientation (KAM) was used. For each data point, KAM was calculated as the average value for misorientations with each nearest neighbor. Then KAMs for all data points were averaged for the whole section, which produced the averaged KAM for a sample. The unit of values of averaged KAM is radian.

Orientation distributions were generated from either the complete set of orientation data or a subset of data with one point per grain using the MTEX toolbox in MATLAB (Bachmann et al., 2010; Mainprice et al., 2015). The manner in which an orientation distribution was generated is specified in the figure captions. To quantify the strength of the CPOs, both the J-index (Bunge, 1982) and the M-index (Skemer et al., 2005) were used. From uniformly-distributed orientations to a single-crystal orientation, the J-index, based on a calculated orientation distribution function, increases from 0 to infinity, while the M-index, based on the distribution of random-pair misorientation axes, increases from 0 to 1.

Since the CPOs of sheared ice are often characterized by double clusters of c axes (e.g., Kamb, 1972; Hudleston, 1977; Bouchez and Duval, 1982; Jackson, 1999), an angle φ was used to quantify the relative orientation between the two clusters. We adopted the same approach as previously described by Bouchez and Duval (1982). As illustrated in Fig. 2(b), in the stereonets, an angle from $-90°$ to $+90°$ was defined on the shear plane (green circle). At a given angle, two great circles with

10° between them (red circles) were drawn perpendicular to the shear plane. The number of data points that lie between these two great circles were counted. The normalized counts were then plotted as the frequency at this angle on a histogram. The angle φ was defined as that between the two peaks on the histogram (Fig. 2(c)).

3   Results

3.1   Starting material

The starting materials were the same as described in Qi et al. (2017). The undeformed samples of standard ice have a homogeneous foam texture, with polygonal grains and straight grain boundaries. The mean grain size is $\sim$0.23 mm. The initial crystallographic orientation is approximately random with an M-index of 0.0026. The averaged KAM is about 0.01. There is almost no subgrain boundaries within the grains.

3.2   Mechanical data

As illustrated in Fig. 1(f) and (g), the deformed samples exhibit some flattening normal to the imposed shear direction. As listed in Table 1, the measured thicknesses for deformed samples are very similar to the initial values. No slip between pistons and samples was observed. Based on these observations, the maximum flattening (axial strain) in our samples is $\sim$19% in sample PIL145 (Table 1). This amount of axial strain is small relative to the shear strain, and does not affect significantly the strain ellipsoid nor the passive rotation of material lines (Sanderson and Marchini, 1984).

Graphs of shear stress plotted against shear strain (hereafter "stress" and "strain" for brevity) are presented in Fig. 3. Key parameters (e.g., peak stress) extracted from the experimental data are presented in Table 1. All the curves for experiments with aluminum pistons show a rapid stress rise to a peak stress at an approximate strain of $\gamma = 0.1\pm0.06$, followed by a steep drop to a more slowly changing stress with increasing strain. The curves for experiments with wooden pistons have different shapes around the peak stresses, and smaller drops following the peak stresses. Two of the experiments with wooden pistons (PIL82 and PIL91) have complicated double peaks near the peak stresses. In all experiments except for PIL82 and PIL135, the stress slowly decreases with increasing strain, following the steep drop after the peak stress. In PIL82, the stress increases slowly after a sharp drop at $\gamma \approx 0.2$. In PIL135, with increasing strain, the stress increases slightly and plateaus at $0.8 < \gamma < 1.9$, decreases at $1.9 < \gamma < 2.5$, and increases suddenly at $\gamma > 2.5$, which corresponds with the 45°-cut piston touching the metal cylindrical sleeve in the bore of the pressure vessel. In PIL144, the stress continues to decrease until a strain of $\sim$1.2, and increases slowly thereafter. At a strain of $\sim$1.8, there is an upward perturbation in stress followed by a decrease in stress. In both PIL135 and PIL144, the perturbation in stress at a strain of 1.8 to 1.9 is probably related to the changes in kinematics due to the changes in the assembly geometry with increasing strain. PIL144 is the one sample for which the final sample thickness is not uniform along its length.

3.3 Crystallographic preferred orientations

In this subsection, CPOs in samples deformed at different temperatures to different shear strains are described, as illustrated in Fig. 4. The CPOs of -5 and $-20°$C samples are all characterized by two clusters of c axes. The primary cluster (M1) is normal to the imposed shear plane at all strains. The secondary cluster (M2) lies in the profile plane antithetic to the imposed shear direction. The CPOs of $-30°$C samples are characterized by one broad cluster of c axes close to the normal to the imposed shear plane. In all samples, c-axis clusters are elongated in the direction sub-perpendicular to the shear direction. At the same temperature, the CPO strength characterized by J- and M-indexes generally increases with increasing strain, with the exception of sample PIL87, which has a relatively small number of grains in the data set.

3.3.1 $-5°$C series

The CPOs of $-5°$C samples are all characterized by two tight clusters of c axes. The angle between the two clusters decreases with increasing strain, as presented in Fig. 4(d). The secondary cluster is weaker (exhibits a lower value of multiples of uniform density, MUD) than the primary cluster, except for sample PIL87, which has a small number of grains in the data set. The elongation of the clusters is clearer in the higher-strain samples. The secondary cluster is stronger (exhibits a higher MUD value) in the stereonets plotted with all orientation data than it is in the stereonets plotted with one point per grain. The secondary cluster generally weakens (has a lower MUD value) with increasing strain in the stereonets plotted with one point per grain.

The CPOs of all $-5°$C samples feature girdles of $\langle 11\bar{2}0 \rangle$ axes (a axes) and $\langle 10\bar{1}0 \rangle$ axes (poles to m planes) in the shear plane, and weaker girdles of a axes and poles to m planes normal to the secondary c-axis clusters. a axes in the three samples with lower strains have dominant clusters normal to the shear direction in the shear plane. In the sample with the highest strain (PIL94, $\gamma = 1.5$), the dominant cluster of a axes is parallel to the shear direction. The distributions of the poles to m planes are similar to the distributions of a axes in all samples, except in the sample with the lowest strain (PIL91, $\gamma = 0.62$), where there is an additional cluster subparallel to the shear direction.

3.3.2 $-20°$C series

The CPOs of $-20°$C samples (Fig. 4) are also characterized by two clusters of c axes. The angle between the two clusters increases slightly with increasing strain. The secondary cluster is weaker (has a lower MUD value) than the primary cluster. The elongation of the clusters is clearer in the higher-strain sample. The secondary cluster is stronger (has a higher MUD value) in the stereonets plotted with all orientation data than it is in the stereonets plotted with one point per grain. The secondary cluster also weakens (obtains a lower MUD value) with increasing strain.

In both samples, the CPO features broad girdles of a axes and poles to m planes in the shear plane. The distributions of a axes and poles to m planes exhibit maximum intensities subparallel to the shear direction in the shear plane. a axes and poles to m planes are more tightly clustered in the higher-strain sample.

3.3.3 −30°C series

The CPOs of −30°C samples (Fig. 4) are characterized by one broad cluster of c axes close to the normal to the imposed shear plane. In the lowest-strain sample, the primary cluster is $\sim 10°$ oblique to the shear-plane normal. This probably relates to this sample fracturing on a plane slightly oblique to the shear plane when removed from the deformation piston and being analyzed on this oblique surface. This primary cluster is asymmetric with a large number of c axes distributed broadly in the quadrant antithetic to the shear direction. In the samples with lower strains (PIL142 and PIL143), the elongation of the primary cluster is more extensive in the stereonets plotted with one point per grain. In the sample with the lowest strain (PIL143, $\gamma = 0.65$), a weak secondary cluster is observed close to the primary cluster. This secondary cluster is stronger than the primary cluster in the stereonet plotted with one point per grain.

The CPOs of all −30°C samples feature broad girdles of a axes and poles to m planes subparallel to the shear plane, and clusters of a axes and poles to m planes subparallel to the shear direction. In the sample with the lowest strain (PIL143, $\gamma = 0.65$), a axes and poles to m planes are less strongly clustered.

3.4 Microstructure

In this subsection, microstructures in samples deformed at different temperatures to different shear strains are described. For a given temperature, as strain increases, the fraction of lobate grain boundaries decreases and the fraction of straight grain boundaries increases. In all samples, the distributions of grain size are skewed, with a peak at finer grain sizes and a long tail extending to coarser grain sizes. The values for averaged KAM of all samples lie in the range of 0.008 to 0.013, with no obvious correlation with increasing strain or decreasing temperature.

3.4.1 −5°C series

The microstructures of all samples deformed at −5°C (Fig. 5(a)) are characterized by lobate grain boundaries and irregular grain shapes. In the sample with the lowest strain (PIL91, $\gamma = 0.62$), the grain boundaries are highly lobate. Preferred orientations of grain shape are not well-developed. Intragranular distortion and subgrain boundaries are widely observed in all samples. In all samples, most grains have c axes sub-perpendicular to the shear plane (grains with reddish colors). In the samples with lower strains (PIL91, 82 and 87), the distribution is based on a very limited number of grains, leading to uncertainties in the mean grain size. Peak grain sizes (the grain size at the peak frequency of the distribution) for all samples are between 40 and 80 μm.

3.4.2 −20°C series

The microstructures of both samples deformed at −20°C (Fig. 6(a)) are characterized by slightly curved grain boundaries. In both samples, preferred orientations of grain shapes are not well-developed. Intragranular distortion and subgrain boundaries are observed. In the sample with lower strain (PIL145, $\gamma = 1.1$), grains with basal planes oblique to the shear plane (with other than reddish color) are widely observed. In the sample with higher strain (PIL144, $\gamma = 2.2$), the map is dominated by grains

with basal planes subparallel to the shear surface (grains with reddish colors). The mean grain size decreases slightly with increasing strain. Peak grain sizes for both samples are 80 μm.

3.4.3 $-30°$C series

The microstructures of all samples deformed at $-30°$C (Fig. 7(a)) are characterized by straight and slightly curved grain boundaries and polygonal grain shapes. In the two samples with lower strains (PIL143, $\gamma = 0.65$ and PIL142, $\gamma = 1.4$), preferred orientations of grain shapes are not well-developed. In the sample with the highest strain (PIL135, $\gamma = 2.6$), there is a grain shape preferred orientation, with long axes subparallel to the shear direction. Intragranular distortion and subgrain boundaries are observed in all samples. The subgrains are developed preferentially in larger grains and the shapes and sizes of the subgrains are similar to those of the small grains. In the sample with the lowest strain (PIL143, $\gamma = 0.65$), intragranular distortion is more evident and more subgrains are observed than in the sample with the highest strain (PIL135, $\gamma = 2.6$). In all samples, there are a range of grain orientations as shown by multiple colors on the map. In the two samples with lower strains (PIL143, $\gamma = 0.65$, and PIL142, $\gamma = 1.4$), the mean grain size is 78 μm, while in the sample with the highest strains (PIL135, $\gamma = 2.6$), the mean grain size is larger, 101 μm. Peak grain sizes for all samples are between 40 and 60 μm.

4 Discussion

4.1 Mechanical evolution

The stress drop following the peak stress is usually attributed to grain-size reduction and/or geometric softening. Dynamic recrystallization often results in a grain-size reduction that is thought to cause weakening by increasing the strain-rate contribution of grain-size sensitive deformation mechanisms (e.g., Tullis and Yund, 1985; De Bresser et al., 2001). Geometric softening due to the development of a CPO also causes weakening (e.g., Hansen et al., 2012), particularly in a strongly viscously anisotropic material such as ice. As is evident from the microstructures and CPOs of deformed samples, both grain-size reduction and geometric softening occur in the experiments. It is difficult to separate the effects of the two processes in the type of experiments carried out in this study.

4.2 The orientation of the two c-axis clusters: comparison of experiments

In our experiments, the primary cluster of c axes is normal to the shear plane in all deformed samples. This statement is true for most other ice samples deformed dominantly by simple shear in the laboratory, for which CPOs with significant numbers of measured grains are published (Kamb, 1972; Bouchez and Duval, 1982; Li et al., 2000). Wilson and Peternell (2012) reported the primary cluster being slightly oblique to the imposed shear plane, but the sample images (Fig. 6a in Wilson and Peternell, 2012) show that shear zones developed oblique to the imposed shear plane and the c-axis cluster is sub-perpendicular to the shear zone boundaries. All previous shear experiments have been at ambient pressure. Durham et al. (1983) show that there is minimal effect of confining pressure on the tertiary creep of ice.

All c-axis clusters in our experiments are elongated in the direction sub-perpendicular to the shear direction. This elongation has been observed in many previous studies (Kamb, 1972; Bouchez and Duval, 1982; Li et al., 2000; Wilson and Peternell, 2012). Li et al. (2000) attributed this elongation to extensional deformation in the shear plane normal to the shear direction, due to the flattening of the sample during shear deformation.

The evolution of φ, the angle between the two c-axis clusters, with strain in our samples is compared with the results from previous experimental studies, with numerical models and with data from naturally deformed ice (Table 3 and Fig. 8). We have used the method described in Section 2.5 to measure φ for our own data and also to make comparable measurements using literature data. For data from the literature, we digitized c-axis orientations from published stereonets (Bouchez and Duval, 1982; Li et al., 2000; Wilson and Peternell, 2012; Hudleston, 1977; Jackson, 1999; Van der Veen and Whillans, 1994). The values of φ for experimental samples of Kamb (1972) are taken from that paper (Kamb published only contoured data); these angles were analyzed using a similar method to ours.

To our knowledge, Fig. 8 contains data from all published CPOs from experiments where simple shear is the dominant deformation kinematic. The values of φ are scattered between 30 and 80° for all experimental samples with double c-axis clusters. Single-cluster CPOs occur at shear strains above 1.4. Many individual data sets, including our data at −30°C and −5°C, reveal that φ decreases with shear strain. In our data, we observe that the trajectory of φ with strain occurs at lower φ values at −30°C than at −5°C, with the φ value of one of the −20°C data points lying between the −30°C and −5°C trajectories. The high-strain −20°C sample has a geometry suggesting that it departed from simple shear in a different way than the other samples (i.e., it was wedge-shaped after deformation: Table 1) and the resulting high φ value may be anomalous. The correlation of the position of the φ–strain trajectories and temperature is less clear in the broader literature data. There are a number of possible reasons. The most likely explanation is that the data in Fig. 8 represent experiments with subtly different kinematics (deviations from perfect simple shear) and contains data from experiments conducted across a range of strain rates (or stresses). At present, there are not enough experimental data to restrict the data set to samples with identical kinematics and strain rates. We would predict that, given identical kinematics and strain rates, the angle φ between the two clusters would decrease with increasing strain at any given temperature and that the φ–strain trajectory would shift to lower φ values with decreasing temperature.

Except for this study, a single-cluster distribution of c axes in experimentally sheared ice has only been observed by Li et al. (2000). In their study, the CPO with a single c-axis cluster occurs at a strain similar to the strain at which this CPO occurs in our experiments, but at a much warmer temperature ($T = -2$°C). Li et al. (2000) attributed the occurrence of this CPO to allowing free deformation of the samples in the direction perpendicular to the applied shear direction (i.e., flattening of the sample). Wilson and Peternell (2012) did not report a CPO with a single c-axis cluster at −2°C, even though their experiments were conducted using the same apparatus and kinematic constraints as those of Li et al. (2000). The experiments of Li et al. (2000) were conducted to higher shear strains than those of Wilson and Peternell (2012), and also to higher shear strains than our highest-strain experiment at −5°C. Allowing free deformation of the samples in the direction perpendicular to the applied shear direction may be important for explaining the single c-axis cluster (as suggested by Li et al., 2000). Our view, based on our study, is that the key element in generating a single c-axis cluster is high shear strain.

4.3 The orientations of the two *c*-axis clusters: comparison with models

The pattern of φ-strain trajectories in Fig. 8 is complicated. Individual φ-strain trajectories at one temperature do not match very simple models, such as one based on the evolution of the angle between the long axis of the strain ellipse and the shear direction, or the passive rotation of a line originally perpendicular to the shear plane (Fig. 8). Bouchez and Duval (1982) applied the two-dimensional kinematic model of Etchecopar (1977). Although this model roughly fits their three experimental data points, the predictions mirror the passive rotation of a line originally perpendicular to the shear plane and do not match the broad set of experimental data. Van der Veen and Whillans (1994) predict different φ-strain trajectories (Fig. 8) depending upon model parameters, most particularly how recrystallization is incorporated into the model. We think the balance between different recrystallization mechanisms may be critical to the manner in which the angle φ evolves. Modern, fast Fourier transform viscoplastic (VPFFT) models of intracrystalline deformation by dislocation glide (Lebensohn, 2001; Lebensohn et al., 2008) generate remarkably similar intragranular microstructures to those measured in ice deformation experiments to low strain (Grennerat et al., 2012; Montagnat et al., 2014; Piazolo et al., 2015), and would seem to be an excellent starting point for trying to understand the evolution of CPO and microstructure in ice during deformation. Llorens et al. (2016a, b, 2017) have coupled the full-field viscoplastic code to recrystallization codes within the ELLE modeling platform (Jessell et al., 2001) to predict microstructural and CPO evolution in ice to relatively high strains. The bulk CPOs produced by these models (Llorens et al., 2016a, b, 2017) and those produced by earlier viscoplastic self-consistent models (Castelnau et al., 1996, 1997) predict a single *c*-axis cluster in shear. The cluster is not perpendicular to the shear plane, but instead lies in an orientation antithetic to the shear direction with an angle to the shear plane normal that reduces with increasing shear strain (see Fig. 5(a)-(d) in Llorens et al., 2017). Localization occurs in these models (see Fig. 10 in Llorens et al., 2017), and the CPO patterns extracted from the localized zones of high strain rate have double *c*-axis clusters at low strains with φ reducing with increasing strain, ultimately generating a single *c*-axis cluster at high strain (see Fig. 5(i) in Llorens et al., 2017). As these CPOs match experimental results much better than bulk CPOs, we have extracted a data set of CPOs from the high-strain rate zones of two end member simple shear models from Llorens et al. (2017) to compare with experimental data. The data are for deformation without recrystallization (VPFFT only) from model experiment SSH0, and for deformation with 25 steps of recrystallization (grain boundary migration), including recovery driven by a reduction of the intra-granular stored energy for each increment of deformation, from model experiment SSH25, in Llorens et al. (2017). A selection of the *c*-axis stereonets from these model experiments are shown in Fig. 9; measured values of φ as a function of strain are shown in Fig 8. The main cluster of *c* axes from the high strain-rate localized zones (Fig. 9) is still oblique to the shear plane normal, although the angle of obliquity is much less than in the bulk CPO data from the same models (see Fig. 5(a) and (d) in Llorens et al., 2017). The φ-strain trajectories for these two end-member models bracket most of the experimental data and support the idea that the complexity in the pattern of φ-strain trajectories relates to the role of recrystallization.

Clearly more work is needed to integrate and reconcile the outcomes of laboratory experiments and numerical models. This is an important direction to pursue as, in general, we have more constraints from laboratory experiments than we do from naturally deformed samples to provide a quantitative test of models. Two key ideas arise from our work. Firstly, numerical

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models fail to predict a c-axis cluster that is always normal to the shear plane. A possible explanation is that the models do not include a key process that can affect grain orientations; grain boundary sliding (GBS) is a candidate process, and nucleation and/or preferential growth of grains with suitable orientations is another. Secondly, only the high-strain-rate zones of FFT-based models match broadly the experimental CPOs. An important focus for future research is to explore the balance of processes that occur in the high-strain-rate zones of models, and to see if we can re-parameterize the models accordingly or explore processes that enable the high strain-rate zone CPOs to propagate through a larger volume of the sample.

4.4 The orientations of the two c-axis clusters: comparison with natural samples

Many natural CPOs characterized by a single c-axis cluster occur, and some of these are attributed to shear deformation. It is difficult for us to make any comparison between CPOs in natural samples and experimental samples here, as many of the natural samples are not from areas with large-scale shear context (e.g., Treverrow et al., 2016). It is possible that these data represent CPOs in ice sheared to high shear strains. The key difference between these single-cluster CPOs in natural samples and those generated in experiments is that the experimental samples all have an elongated c-axis cluster, whereas the naturally deformed samples mostly do not.

Three studies of naturally deformed ice provide more context, because the shear zone geometries are constrained from field data. Hudleston (1977) presented a well-documented study on CPOs observed in a glacial shear zone, which were compared with the CPOs observed in experimental samples by Bouchez and Duval (1982). The ice studied by Hudleston (1977) was collected from a shaft in the Barnes Ice Cap where the temperature was nearly constant at $-10°C$, and where the shear kinematics and strains were constrained by classical methods of structural geology. Key elements of Hudleston's (1977) observations that match those from shear experiments are that (1) the primary cluster of c axes is close to normal to the shear plane at all shear strains; (2) the angle between two clusters, φ, decreases with increasing strain; and (3) CPOs with a single c-axis cluster occur at high strains. The transition between CPOs of double clusters and a single cluster occurs at shear strains between 1.1 and 2.7 (Bouchez and Duval, 1982), in good agreement with experimental data (Fig. 8). The φ–strain trajectory of this data set also fits within the range of experimental observations. Hudleston (1977) did not observe elongated c-axis clusters.

The CPOs of ice within the ice stream marginal shear zone reported by Jackson (1999) exhibit a wider range of φ than the CPOs of ice deformed in the laboratory, from a single c-axis cluster to double c-axis clusters with $\varphi \approx 90°$. Because measurements of shear strains are unavailable for these natural ice samples, the relationship between φ and strain cannot be determined. These CPOs are all likely to be from ice deformed to shear strains > 3. The occurrence of double clusters at these strains would not match the experimental data well and illustrates that there are probably significant complications in natural scenarios. Wilson and Peternell (2011) show CPOs with single and double c-axis clusters that they attributed to simple shear. The data of Wilson and Peternell (2011), however, cannot be related quantitatively to strain. One aspect that the data of Jackson (1999) and some of the data of Wilson and Peternell (2011) have in common with the experimental observations is that c-axis clusters are elongated. In the case of the data of Jackson (1999), it is notable that the elongation is perpendicular to the shear direction, as it is in all experiments.

4.5 Recrystallization processes

After deformation, all samples have significantly-altered microstructures, indicative of dynamic recrystallization. The mean grain sizes and the peak grain sizes in deformed samples are smaller than the initial grain size of 230 μm (Qi et al., 2017), indicating that nucleation is involved in the recrystallization process. The observation of subgrains within larger grains suggests that subgrain rotation recrystallization (polygonization) (e.g., Guillope and Poirier, 1979; Urai et al., 1986; Alley, 1992) is a possible nucleation mechanism.

At $-5°$C, the presence of highly curved and lobate grain boundaries suggests that the recrystallization process is dominated by strain-induced grain boundary migration (GBM) (Urai et al., 1986). As temperature decreases, the fraction of lobate grain boundaries decreases, suggesting that GBM contributes less to recrystallization, while the fraction of straight grain boundaries and polygonal grains increases, indicating that lattice rotation and subgrain rotation (polygonization) contribute comparatively more to recrystallization (Steinbach et al., 2017). At $-30°$C, the large number of small polygonal grains suggests that the recrystallization process is dominated by subgrain rotation recrystallization (e.g., Drury and Urai, 1990).

The microstructures of the samples evolve with increasing strain. At all temperatures, the fraction of curved grain boundaries decreases, with increasing strain, while the number of polygonal grains increases. This observation suggests that the transition of the dominant recrystallization process from GBM to lattice rotation also occurs with increasing strain.

4.6 Process control on CPO development

The transition from a double-cluster to a single-cluster distribution of c axes with increasing strain and/or decreasing temperature corresponds with the transition in the dominant recrystallization process. Qi et al. (2017) proposed that deformation by lattice rotation and recrystallization by grain boundary migration are the primary controls on CPO development. We extend this idea here to explain the CPOs that are formed in shear (Fig. 10). Fig. 10(c) explains how key processes (Fig. 10(a)) involved in deformation and recrystallization may effect CPO formation and evolution in shear.

The VPFFT models that yield the results shown in Fig. 9(a) simulate the effects of lattice rotation, with glide primarily on the basal plane. The VPFFT models predict that lattice rotation generates an initial CPO with c-axis clusters perpendicular to the shear plane and parallel to the shear direction. The cluster perpendicular to the shear plane strengthens rapidly with shear and migrates slowly in a direction antithetic to the shear-induced vorticity. The cluster parallel to the shear direction weakens and rotates rapidly in a direction synthetic to the shear-induced vorticity.

In the GBM process, grains with low dislocation density consume those with high dislocation density by migration of their mutual boundary (Urai et al., 1986). Grains poorly oriented for easy (basal) slip (i.e., that have low resolved shear stresses, or Schmid factors, on the basal plane) have to deform by slip on non-basal slip systems. As these dislocations are more difficult to glide, and there will be more than one interacting slip system, internal distortion tends to be higher in grains whose basal planes are in low-Schmid-factor orientations (Bestmann and Prior, 2003; Jansen et al., 2016; Vaughan et al., 2017). Grains in high-Schmid-factor orientations will grow at the expense of grains in low-Schmid-factor orientations (Fig. 10(a) and (c)). In

simple shear, high-Schmid-factor orientations on the basal plane occur where c axes are normal to the shear plane and parallel to the shear direction (Fig. 10(b)).

The subgrain rotation process is built into the VPFFT model (Fig. 9(a)). The process can be considered as kinematically indistinguishable from the lattice rotation process. The subgrain rotation process can lead to generation of new small grains, a nucleation process commonly called subgrain rotation recrystallization (Guillope and Poirier, 1979; Urai et al., 1986; Bestmann and Prior, 2003). Microstructural studies of rocks show that small recrystallized grains have CPOs that are randomly-dispersed equivalents of the stronger host-grain CPOs (Jiang et al., 2000; Bestmann and Prior, 2003; Storey and Prior, 2005). These observations are interpreted as the result of an increased contribution of GBS to deformation. Recent experiments, in which very coarse-grained ice is recrystallized (Craw et al., 2018) during deformation at $-30°$C, also reveal CPOs in recrystallized grains (with peak grain sizes of 125-175μm) that are randomly dispersed equivalents of the stronger CPOs in host grains (several mm grain size). These observations suggest that GBS can be an important process of deformation in ice (Goldsby and Kohlstedt, 2001). GBS may add a component of rotation around the vorticity axis (Fig. 10(c)), synthetic to shear (Cross et al., 2017).

Fig. 10(d) provides a schematic synthesis of the relationships of CPO patterns to temperature and shear strain as suggested by experimental data. The figure also attempts to explain the patterns in terms of the contributions of the processes outlined in the previous paragraphs. Both lattice rotation and GBM will generate initial CPOs with c-axis clusters perpendicular to the shear plane and parallel to the shear direction. Lattice rotation is likely the primary cause of rotation of the secondary cluster towards the primary cluster with increasing shear strain. The elongation of clusters perpendicular to the shear direction may relate to the deformation kinematics (Li et al., 2000), but may also relate to GBS-aided rotation around the vorticity axis synthetic to the shear direction. GBM will continue to favor growth of grains with c axes perpendicular to the shear plane and parallel to the shear direction throughout the deformation. Lattice rotation ensures that there is always a supply of grains with c axes perpendicular to the shear plane that can grow by GBM. Similarly, lattice rotation depletes the supply of grains with c axes parallel to the shear direction. Subgrain rotation recrystallization and GBS will contribute to the formation of the CPO by providing a wider range of crystal orientations, some of which can grow by GBM. If GBM is more effective than subgrain rotation recrystallization, re-population of grains with the secondary c-axis cluster subparallel to the shear direction will slow the rotation of the secondary cluster towards the primary cluster. As shear strain increases, the CPO becomes dominated by the primary c-axis cluster, so that there are fewer grains in low-Schmid-factor orientations. We suggest that this will reduce the number of grains with high dislocation density, effectively reducing the driving force for GBM. This would explain the decrease in microstructures indicative of GBM as shear strain increases. We suggest that GBM activity reduces with increasing shear strain as a result of a reduced driving force for boundary migration. As temperature decreases, the mobility of grain boundaries decreases, and the contribution of GBM reduces relative to lattice rotation, with two effects: the rotation of the secondary cluster as a function of strain is more effective at lower temperatures, and the c-axis clusters are broader at colder temperatures.

4.7 Determination of deformation geometry in natural ice: measuring a-axis orientations

Ice CPOs with a vertical c-axis cluster are common in nature (e.g., Gow and Williamson, 1976; Herron and Langway, 1982; Herron et al., 1985; Faria et al., 2014; Treverrow et al., 2016). Such CPOs could relate to vertical axial shortening or to shear with a horizontal shear plane. There is little intrinsic information in the c-axis distributions to enable distinction of these two interpretations. Elongated c-axis clusters and double c-axis clusters break the cylindrical symmetry expected for axial shortening (Wenk and Christie, 1991), and have symmetry consistent with shear. However, these are reported relatively rarely for natural ice samples (Jackson, 1999; Jackson and Kamb, 1997; Wilson and Peternell, 2011). Furthermore, there are examples of symmetrical (not elongated) c-axis clusters in naturally deformed samples demonstrably related to shear (Hudleston, 1977). Elongation of c-axis clusters remains a bit of an enigma.

Our experiments show that the a-axis (and pole to m-plane) distributions are not uniformly distributed in the planes perpendicular to c-axis clusters. In contrast, the a-axis distributions corresponding to CPOs with a single c-axis cluster formed in axial-compression experiments (e.g., the sample shown in Fig. 11 in Prior et al., 2015) are uniformly distributed within the plane perpendicular to c-axis cluster (Prior, unpublished data). Thus the distributions of a axes (and poles to m planes) in naturally deformed samples may help resolve their deformation kinematics with clustered a axes indicating shear. Furthermore, if collected natural samples are oriented, the a-axis data may constrain the shear direction. Our experiments suggest that at high shear strains, a axes and poles to m planes are oriented parallel to the shear direction.

4.8 Future directions

Fig. 10 provides a hypothesis to test in future laboratory experiments that can be subdivided on the basis of temperature, strain rate (stress) and kinematics. Exploring the role of initial grain size and chemistry will also be important. Because it is possible to use the direct shear method with a confining pressure, a wider range of temperatures and strain rates can be explored than has been achieved before this study. The direct shear approach has significant promise in expanding our understanding of sheared ice. However, control of sample kinematics (and through this, the details of strain rate) may be improved by adapting other rock deformation approaches, such as confined torsion (Paterson and Olgaard, 2000; Pieri et al., 2001; Covey-Crump et al., 2016). Comparison with numerical models (Llorens et al., 2017) gave excellent insights into how different processes interact. Areas of poor comparison between experiments and numerical models highlight deficiencies in our quantitative understanding of ice deformation and recrystallization. Future work should explore the parameter space within models to maximize the agreement with experimental observations, and needs to focus on adding processes that are currently not included in models. GBS is a key process that should be incorporated into models. Many aspects of numerical models are limited in terms of dimensions and/or kinematics, and designing experiments that match these limitations is also important.

Ultimately, both experimental work and modeling needs to be linked to natural deformation. The relationships of CPO and strain, quantified in the well-constrained study of natural ice deformation by (Hudleston, 1977), match well with the experimental observations, giving us and previous authors (Bouchez and Duval, 1982) confidence that the results of laboratory experiments are applicable to natural deformation. Studies comparable to Hudleston's are difficult undertakings. Overcoming

these difficulties, so that we have more samples of naturally deformed ice across strain gradients, with constraints on deformation conditions, is crucial to future development of this research direction.

5 Conclusions

1. Polycrystalline ice samples, sheared to different shear strains ($\sim$0.6 to 2.6) at -5, -20 and $-30°$C all develop a dominant, primary cluster of c axes perpendicular to the shear plane. The orientation of this primary cluster does not change as a function of strain.

2. In samples deformed to $\gamma = 0.6, 0.7, 1.4$ and 1.5 at $-5°$C, $\gamma = 1.1$ and 2.2 at $-20°$C and $\gamma = 0.65$ at $-30°$C, a secondary c-axis cluster develops in the profile plane, but rotates from the primary cluster in a direction antithetic to the shear-related rotation. The angle between the two clusters reduces with shear strain in the $-5°$C experiments. Samples deformed to $\gamma = 1.4$ and 2.6 at $-30°$C exhibit a single c-axis cluster.

3. Clusters of a axes and poles to the m plane form, parallel to each other, within great circles perpendicular to c-axis clusters. At $-5°$C, these clusters lie roughly in the shear plane and are perpendicular and parallel to the shear direction, becoming parallel to the shear direction at the highest strain ($\gamma = 1.4$). At -20 and $-30°$C, these clusters lie parallel to the shear direction.

4. With decreasing temperature, both c-axis clusters become more diffuse, and the distinction of two c-axis clusters becomes less clear. At all temperatures, cluster strength increases with increasing shear strain. c-axis clusters are elongated along great circles perpendicular to the shear direction. Elongation increases with increasing shear strain.

5. Lobate grain boundaries are more prevalent and more irregular in samples sheared at higher temperatures. At each temperature, the proportion of and irregularity of lobate boundaries decreases with increasing shear strain. At all strains, the majority of grains are substantially smaller than the starting grain size.

6. We used our data, published literature data, and comparisons of both with numerical models to interpret key processes that control the microstructures and the CPOs of ice during shear. We suggest that observed patterns result from a balance of the rates of lattice rotation due to dislocation slip and growth of grains by strain-induced GBM. GBM is faster at higher temperatures and becomes less important as shear strain increases.

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Table 1. Summary of experimental data.

Sample #	h_0 (mm)	h_1[1](mm)	piston type[2]	T (°C)	max ε_axial[3]	$\dot{\gamma}_\text{meas}$ (10^{-5} s^{-1})	γ_meas	τ_p[4](MPa)	γ_p	$\Delta\tau$[5](MPa)	$\gamma_{\Delta\tau}$
PIL82	6.35	n/a	w	−5.4	0.15	7.98	0.69	0.87	0.07	n/a[6]	n/a
PIL87	5.33	n/a	w	−5.6	0.15	10.8	1.4	1.40	0.13	n/a	n/a
PIL91	6.10	∼6.4	w	−5.6	0.10	17.8	0.62	1.54	0.09	n/a	n/a
PIL94	5.69	∼5.6	Al	−5.2	0.14	13.7	1.5	2.02	0.10	0.73	0.31
PIL135	5.33	∼4.8	Al	−30.5	n/a	12.5	2.6	7.03	0.16	1.43	0.38
PIL142	5.08	∼4.9	Al	−29.9	n/a	12.8	1.4	6.73	0.16	1.32	0.25
PIL143	5.08	∼5.0	Al	−30.6	n/a	14.6	0.65	6.81	0.10	1.32	0.26
PIL144	5.33	∼5.6[7]	Al	−20.4	0.15	11.9	2.2	4.60	0.13	1.50	0.38
PIL145	6.10	∼6.1	Al	−20.1	0.19	9.49	1.1	4.80	0.05	1.91	0.35

[1] h_1 is the estimated value of sample thickness from photos of each sample. This estimation is only accurate to within ∼10% of the value, due to the perspective and distortion in photos.

[2] w stands for wooden pistons. Al stands for aluminum pistons.

[3] max ε_axial is the maximum axial strain estimated from bulging of the samples.

[4] τ_p is peak stress corrected for the strength of the indium jacket. γ_p is the strain at which the peak stress was collected.

[5] $\Delta\tau$ is the magnitude of the stress drop following the peak stress. $\gamma_{\Delta\tau}$ is the approximate shear strain at which the sharp decrease in stress stops and stress becomes nominally constant.

[6] n/a stands for data not available.

[7] Sample has non-uniform thickness after deformation, i.e., is wedge-shaped. All other samples have uniform thicknesses.

Table 2. Summary of EBSD analyses.

Sample #	data for CPO			data for microstructure		
	section & step size (μm)	# indexed	# grains	section & step size (μm)	# indexed	# grains
PIL82	shear, 50	36522	3303	shear, 5	62636	84
PIL87	shear, 30	47261	1387	shear, 6	236617	259
PIL91	shear, 50	113899	10560	shear, 5	79486	225
PIL94	shear, 50	109767	8613	shear, 7	335313	1186
PIL135	shear, 20	732565	33828	shear, 5	454424	1282
PIL142	shear, 20	1131010	51529	shear, 5	425804	2016
PIL143	shear, 20	344083	18061	shear, 5	233143	1100
PIL144	shear, 30	416546	27738	shear, 10	317027	4045
PIL145	shear, 30	312157	21248	shear, 10	299413	3199

Table 3. The CPOs of sheared ice reported in the literature.

Reference	sample name	type[1]	# of c axes	φ	conditions
Jackson (1999)	Chaos-1	n	72	84°	Camp Chaos marginal shear zone, 300-m depth
	Chaos-2	n	139	57°	
	Chaos-3	n	85	58°	
	Chaos-4	n	43	56°	
	Lostlove-1	n	59	46°	Lost Love marginal shear zone, 300-m depth
	Dragonpad-1	n	54	single cluster	Dragon Pad marginal shear zone, 300-m depth
	Staging-1	n	87	42°	Staging area, 300-m depth
	Unicorn-1	n	22	51°	Unicorn Camp
	Fishhook-1	n	78	89°	Fishhook drill site
Hudleston (1977)	IV	n	80	44°	Shear zone in the Barnes Ice Cap, lower strain part of core
	V-IX	n	72-79	single cluster	Shear zone in the Barnes Ice Cap, higher strain part of core
	X	n	88	80°	Shear zone in the Barnes Ice Cap, lower strain part of core
	XI	n	93	40°	Shear zone in the Barnes Ice Cap, lower strain part of core
	XII	n	127	54°	Shear zone in the Barnes Ice Cap, lower strain part of core
Kamb (1972)	A10	e	462	79°	$T = -1.2°C$, $\dot{\gamma} = 0.2 \times 10^{-7}$ s^{-1}, $\gamma = 0.13$, $\varepsilon_{axial} = 0.13$
	A8	e	507	65°	$T = -1$ to $-2.5°C$, $\dot{\gamma} = 2.8 \times 10^{-7}$ s^{-1}, $\gamma = 0.12$-0.24
	A7	e	97	70°	$T = -2.5°C$, $\dot{\gamma} = 3.1 \times 10^{-7}$ s^{-1}, $\gamma = 0.05$, $\varepsilon_{axial} = 0.003$
	A6	e	252	63°	$T = -4°C$, $\dot{\gamma} = 1.1 \times 10^{-7}$ s^{-1}, $\gamma = 0.40$, $\varepsilon_{axial} = 0.01$
	A5	e	626	62°	$T = -2.5°C$, $\dot{\gamma} = 0.7 \times 10^{-7}$ s^{-1}, $\gamma = 0.27$, $\varepsilon_{axial} = 0.06$
	A3	e	136	68°	$T = -4°C$, $\dot{\gamma} = 1.4 \times 10^{-7}$ s^{-1}, $\gamma = 0.16$, $\varepsilon_{axial} = 0.05$
	A14	e	563	72°	$T = -1.2°C$, $\dot{\gamma} = 3.4 \times 10^{-7}$ s^{-1}, $\gamma = 0.15$, $\varepsilon_{axial} = 0.082$
	A13	e	576	54°	$T = -1°C$, $\dot{\gamma} = 8.9 \times 10^{-7}$ s^{-1}, $\gamma = 0.22$, $\varepsilon_{axial} = 0.42$
Bouchez and Duval (1982)	E1	e	147	60°	$T = -7°C$, $\dot{\gamma} = 1 \times 10^{-7}$ s^{-1}, $\gamma = 0.6$
	E2	e	208	69°	$T = -12°C$, $\dot{\gamma} = 1 \times 10^{-7}$ s^{-1}, $\gamma = 0.95$
	E3	e	100	35°	$T = -10°C$, $\dot{\gamma} = 1 \times 10^{-7}$ s^{-1}, $\gamma = 2$
	Etchecopar-a	m		60°	$\gamma = 0.7$
	Etchecopar-b	m		50°	$\gamma = 1.07$
	Etchecopar-c	m		40°	$\gamma = 1.43$
	Etchecopar-d	m		30°	$\gamma = 2.6$
	Etchecopar-e	m		20°	$\gamma = 2.9$
Van der Veen and Whillans (1994)	model 1	m		68°	$\gamma = \sqrt{3}\varepsilon = 0.87$
	model 1	m		68°	$\gamma = \sqrt{3}\varepsilon = 1.73$
	model 2	m		72°	$\gamma = \sqrt{3}\varepsilon = 0.52$
	model 2	m		58°	$\gamma = \sqrt{3}\varepsilon = 1.04$
	model 2	m		single cluster	$\gamma = \sqrt{3}\varepsilon = 1.56$
Li et al. (2000)	A2	e		single cluster	$T = -2°C$, $\tau = \sqrt{3/2} \times 0.2$ MPa $= 0.24$ MPa, $\gamma = 2.18$
	A5	e		single cluster	$T = -2°C$, $\tau = \sqrt{3/2} \times 0.3$ MPa $= 0.37$ MPa, $\gamma = 2.10$
	A6	e		single cluster	$T = -2°C$, $\tau = \sqrt{3/2} \times 0.4$ MPa $= 0.49$ MPa, $\gamma = 2.04$
Wilson and Peternell (2012)	2-66-center	e	387	61°	$T = -15°C$, $\tau = 0.4$ MPa, $\gamma = 1.0$, $\varepsilon_{axial} = 0.05$
	2-64-center	e	712	59°	$T = -10°C$, $\tau = 0.4$ MPa, $\gamma = 1.1$, $\varepsilon_{axial} = 0.18$
	2-41-zone2	e	274	64°	$T = -2°C$, $\tau = 0.4$ MPa, $\gamma = 1.1$, $\varepsilon_{axial} = 0.08$
	2-41-zone3	e	128	53°	$T = -2°C$, $\tau = 0.4$ MPa, $\gamma = 1.1$, $\varepsilon_{axial} = 0.08$
	2-52-zone2	e	103	50°	$T = -2°C$, $\tau = 0.4$ MPa, $\gamma = 0.95$, $\varepsilon_{axial} = 0.1$
	2-52-zone3	e	942	68°	$T = -2°C$, $\tau = 0.4$ MPa, $\gamma = 0.95$, $\varepsilon_{axial} = 0.1$
Llorens et al. (2017)	SSH0	m		66°	$\gamma = \sqrt{3}\varepsilon = 0.52$
		m		56°	$\gamma = \sqrt{3}\varepsilon = 1.04$
		m		single cluster	$\gamma = \sqrt{3}\varepsilon = 2.08$

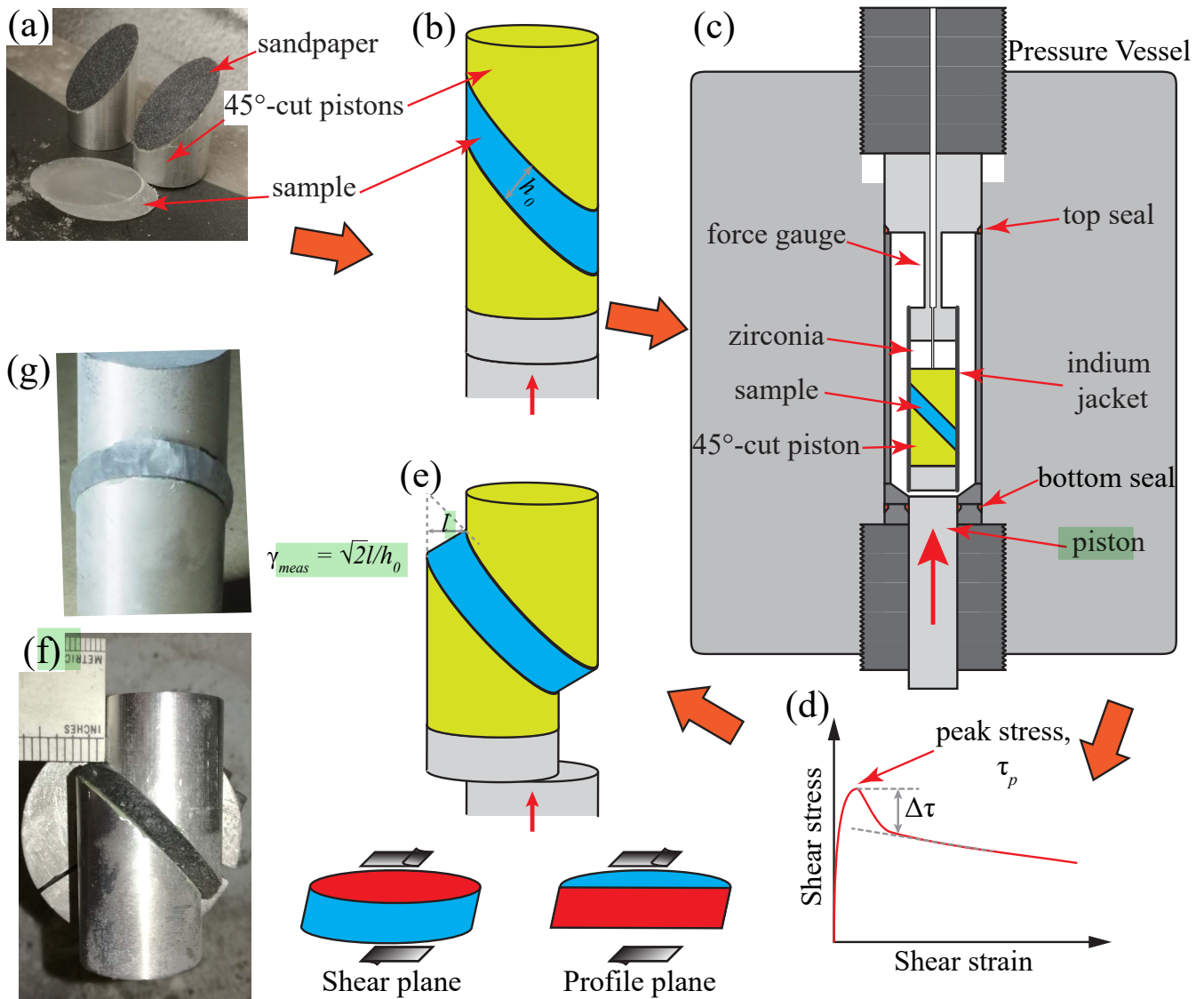[1] n stands for natural samples. e stands for experimental samples. m stands for models.

Figure 1. Figures illustrating the experimental procedure. Orange arrows indicate steps. (a) Photo of a sample and aluminum pistons. (b) Schematic drawing of the sample assembly before deformation. (c) Schematic drawing of the pressure vessel and the deformation assembly. (d) Schematic plot of a typical shear stress-shear strain curve during an experiment. Peak stress, τ_p, and stress drop, $\Delta\tau$, are marked on the curve. (e) Schematic drawing of the sample assembly after deformation. The two sub-drawings at the bottom denote the shear plane and the profile plane (in red). (f) and (g) Photos of deformed samples at different perspectives.

(a) shear plane ref. frame

+90°

top side shear

lower hemisphere

(b) Example data from *M. Jackson, PhD*

+90°

count of points between great circles plotted in the histogram

-90°

(c) Distribution of *c*-axes

φ

frequency

-90° angle +90°
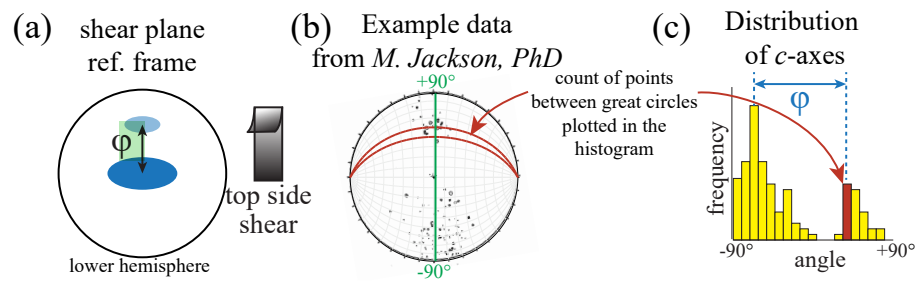
Figure 2. (a) Typical two-cluster distribution of c axes on the stereonets in shear plane reference frame. (b) A schematic drawing explaining the method used to quantify the distribution of c axes. (c) The distribution of c axes plotted in a histogram, illustrating the angle between the two clusters of c axes, φ.
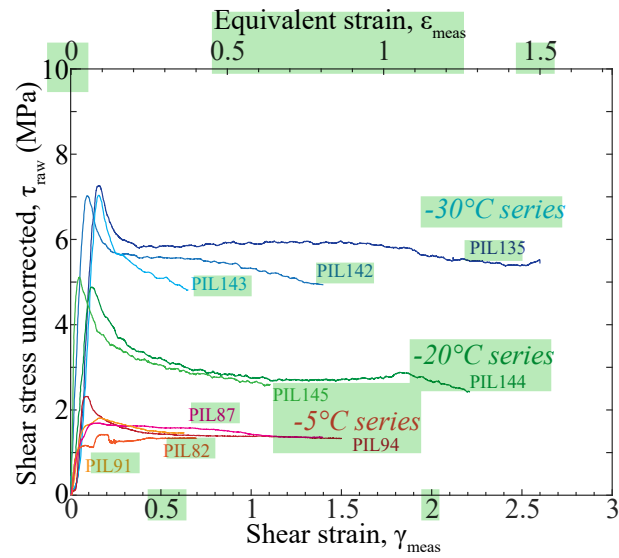
Figure 3. Plots of shear stress-shear strain curves for all experimental runs. The y-axis is the shear stress, τ_{raw}, calculated from the axial load. No correction has been applied for the change of area.
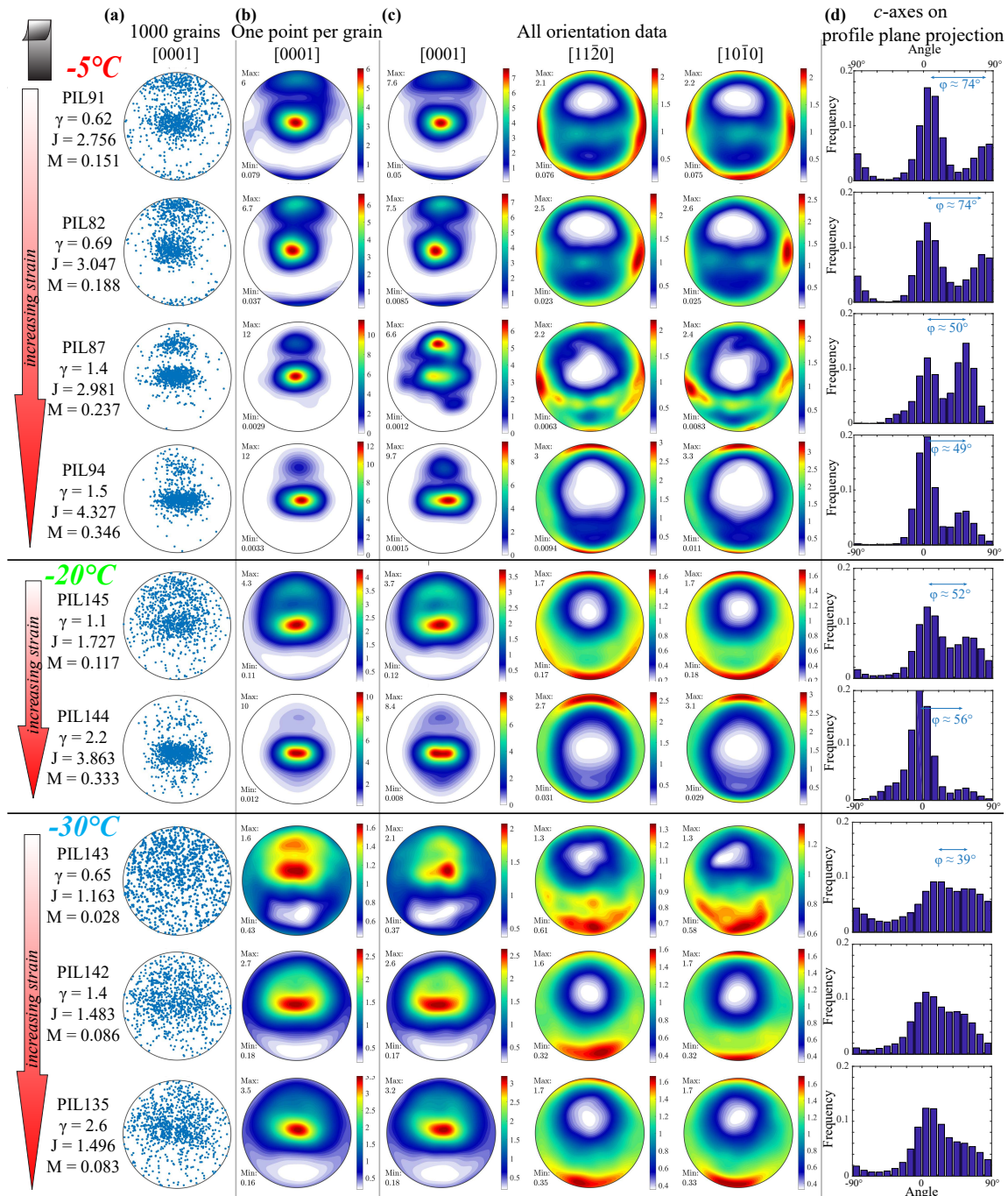
Figure 4. Analysis of crystallographic orientations on the shear plane of all deformed samples. Samples are grouped by their experimental temperatures. Groups are separated by black horizontal lines. All data are from shear plane. The shear direction is top side up, as illustrated by the bold black arrow. Step size is between 30 and 50 μm (see Table 2 columns 2-4). J- and M-indexes are calculated based on all orientation data. (a) Distributions of orientations of [0001] axes from 1000 randomly-selected grains. (b) Distributions of orientations of [0001] axes contoured on the basis of one point per grain. (c) Distributions of orientations of [0001], [11$\bar{2}$0] and [10$\bar{1}$0] contoured on the basis of all orientation data. The contours on each stereonet are colored by multiples of a uniform distribution (MUD), values of which are indicated in the color bar next to the stereonet. (d) Distributions of the [0001] axes on the great circle normal to the shear surface. The angle between the two clusters, φ, is presented on each histogram.
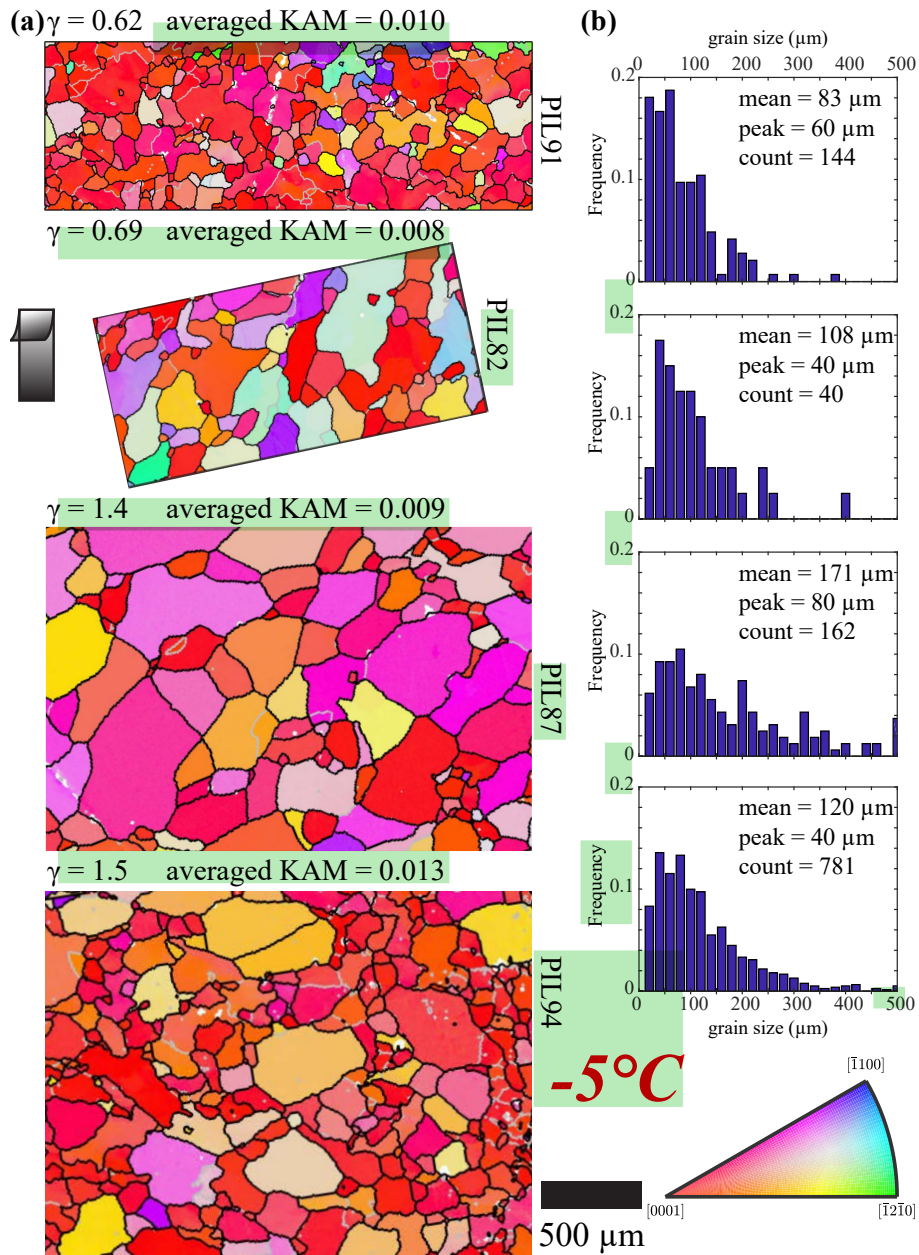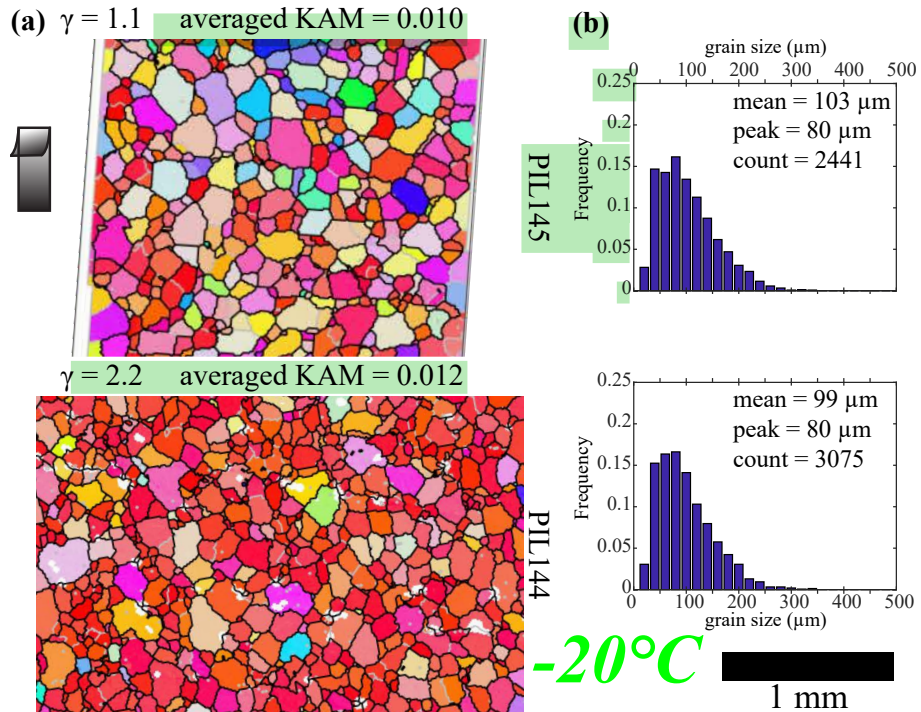
Figure 5. Microstructure of the shear planes of samples deformed at $-5°$. Strain increases from top to bottom. (a) Orientation maps colored by the crystallographic orientation normal to the shear surface according to the color map at bottom right. Step size is between 5 and 7 μm (see Table 2 columns 5-7). Grain boundaries, characterized by a misorientation of $10°$, are black, and sub-grain boundaries, characterized by a misorientation of $2°$, are gray. Un-indexed spots are white. The shear direction on the top side is up, as shown by the black arrow. (b) Distributions of grain size.
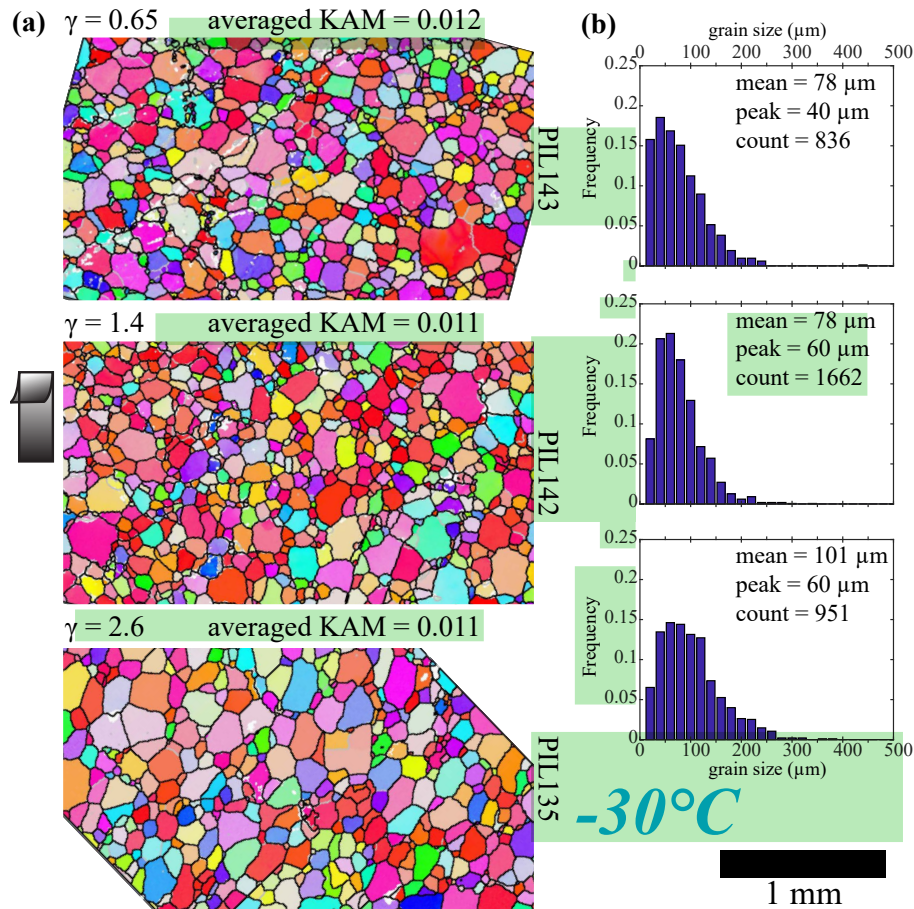
Figure 6. Microstructure of the shear planes of samples deformed at $-20°$. Strain increases from top to bottom. (a) Orientation maps colored by the crystallographic orientation normal to the shear plane according to the color map at bottom right. Step size is 10 μm (see Table 2, Columns 5-7). Grain boundaries, characterized by a misorientation of 10°, are black, and sub-grain boundaries, characterized by a misorientation of 2°, are gray. Un-indexed spots are white. The shear direction on the top side is up, as shown by the black arrow. (b) Distributions of grain size.

Figure 7. Microstructure of the shear planes of samples deformed at $-30°$. (a) - (c) Orientation maps colored by the crystallographic direction normal to the shear plane. Color map is the same as in Fig. 5. Step size is 5 μm (see Table 2 columns 5-7). Grain boundaries, characterized by a misorientation of $10°$, are black, and sub-grain boundaries, characterized by a misorientation of $2°$, are gray. Un-indexed spots are white. The shear direction on the top side is up, as shown by the black arrow. Strain increases from panel (a) to (c). (e) - (h) Distributions of grain size. From top to bottom, histograms are ordered the same way as the orientation maps.
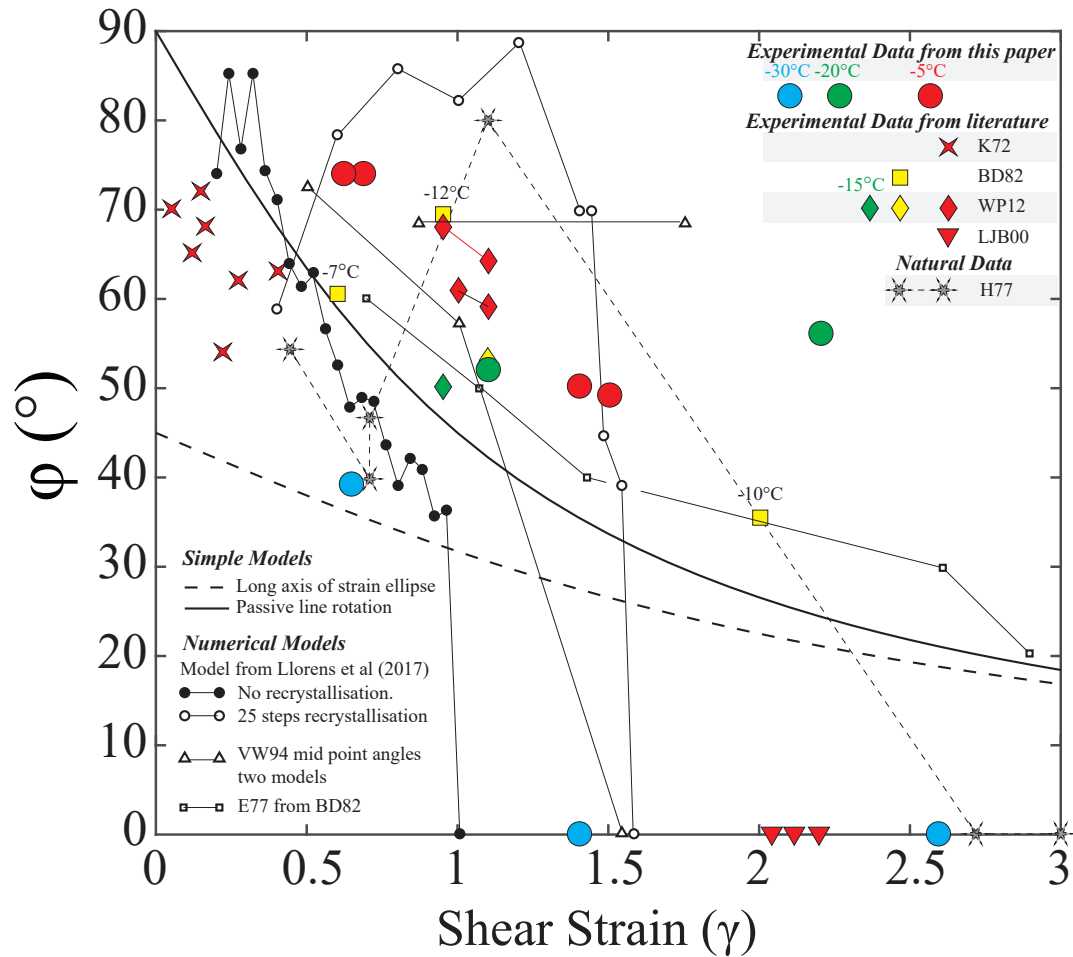
Figure 8. Plots of the angle between *c*-axis clusters, φ, for experiments from this study, experiments from the literature, data from natural shear zones, results of simple models, and results of numerical models. Experimental data: K72 = Kamb (1972); BD82 = Bouchez and Duval (1982); LJB00 = Li et al. (2000); WP12 = Wilson and Peternell (2012). Symbol colors broadly indicate deformation temperature and left-to-right position of symbols in legend indicates relative temperatures. Outcomes from published numerical models: VW94 = Van der Veen and Whillans (1994); E77 = the Etchecopar (1977) model as applied by Bouchez and Duval (1982). Models from Llorens et al. (2017) are explained in the text and CPOs from these are illustrated in Fig. 9. Data from natural shear zones: H77 = Hudleston (1977). Symbols tied by lines indicate they are from one sample.
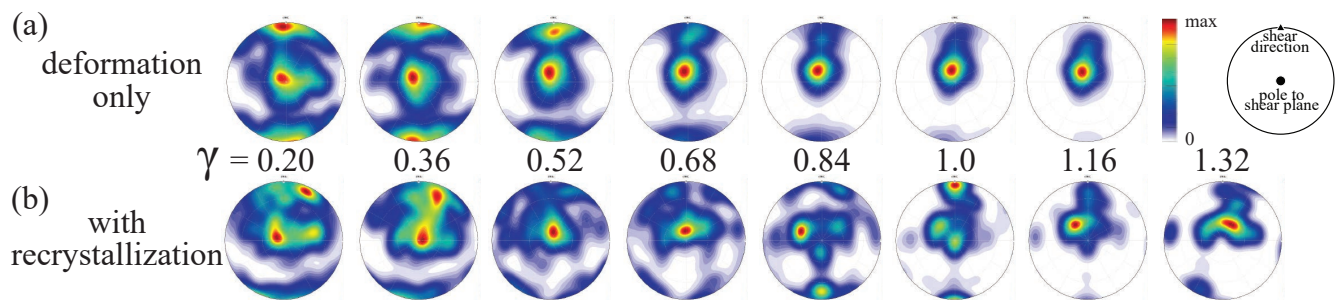
Figure 9. Lower-hemisphere, equal-area stereonets of c axes from numerical models described by Llorens et al. (2017). The data are extracted from high-strain-rate domains in the models, and are presented as a function of shear strain. The color contours of each stereonet are normalized to its own maximum. (a) Model SSH0: deformation with no recrystallization. (b) Model SSH25: deformation with recrystallization (strain-induced grain boundary migration) and recovery.
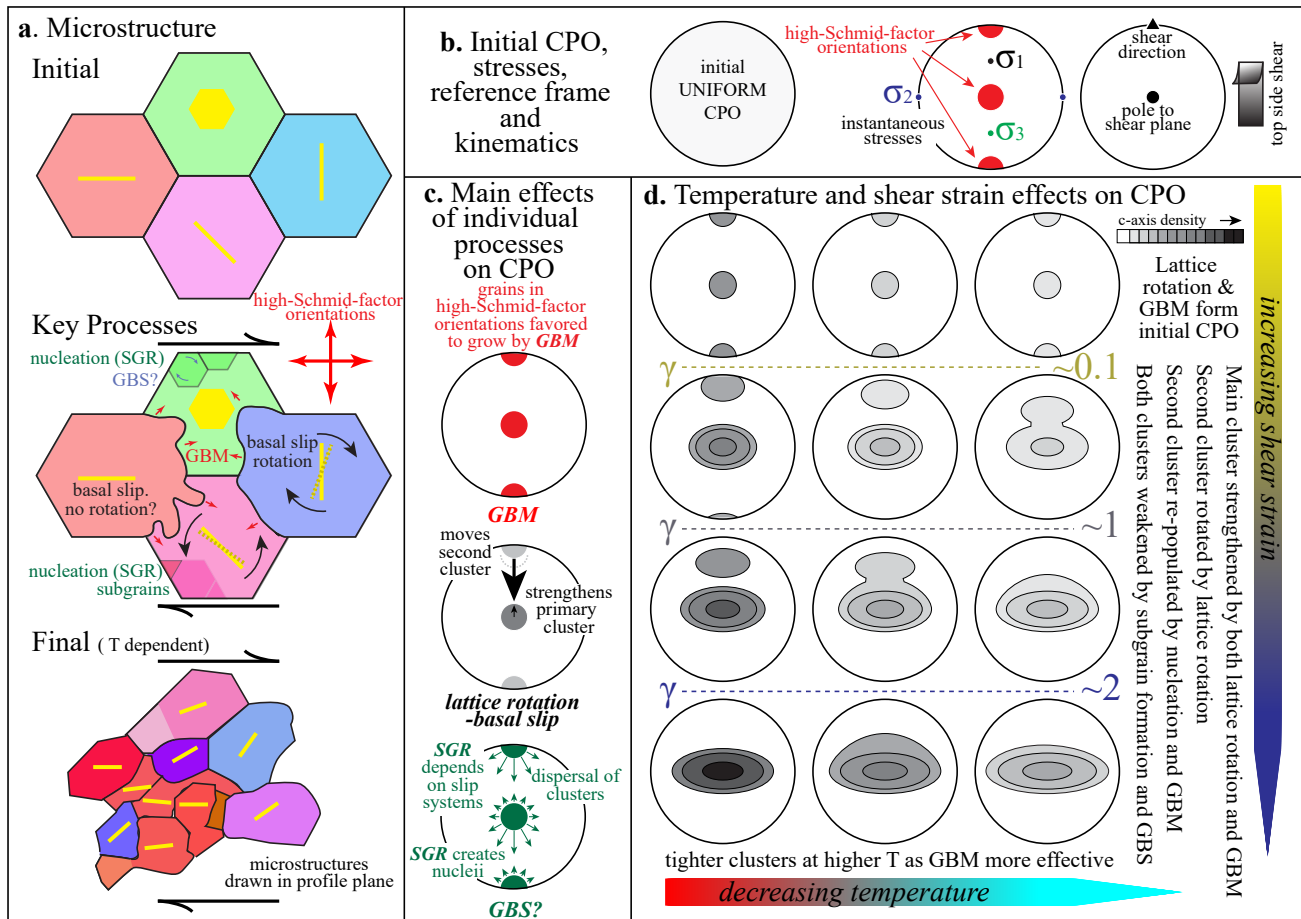
Figure 10. Schematic drawing for the development of CPOs in ice sheared in the laboratory. (a) The evolution of microstructure. Four hexagonal ice grains with different initial orientations of basal planes are used to represent the microstructure. (b) Initial CPO and the kinematics in the shear surface. σ_1 and σ_3 are the maximum and minimum deviatoric stresses (compressive positive), respectively. (c) The effects from CPO-formation mechanisms. (d) The development of CPOs with strain at different temperatures. SGR = subgrain rotation. GBM = grain boundary migration. GBS = grain boundary sliding.