

Sea-level response to melting of Antarctic ice shelves on multi-centennial time scales with the fast Elementary Thermomechanical Ice Sheet model (f.ETISh v1.0)

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Abstract. The magnitude of the Antarctic ice sheet's contribution to global sea-level rise is dominated by the potential of its marine sectors to become unstable and collapse as a response to ocean (and atmospheric) forcing. This paper presents Antarctic sea-level response to sudden atmospheric and oceanic forcings on multi-centennial time scales with the newly developed *fast Elementary Thermomechanical Ice Sheet* (f.ETISh) model. The f.ETISh model is a vertically integrated hybrid ice sheet/ice shelf model with vertically-integrated thermomechanical coupling, making the model two-dimensional. Its marine boundary is represented by two different flux conditions, coherent with power-law basal sliding and Coulomb basal friction. The model has been compared to existing benchmarks.

Modelled Antarctic ice sheet response to forcing is dominated by sub-ice shelf melt and the sensitivity is highly dependent on basal conditions at the grounding line. Coulomb friction in the grounding-line transition zone leads to significantly higher mass loss in both West and East Antarctica on centennial time scales, leading to 1.5 m sea level rise after 500 year for a limited melt scenario of 10 m a^{-1} under freely-floating ice shelves, up to 6 m for a 50 m a^{-1} scenario. The higher sensitivity is attributed to higher ice fluxes at the grounding line due to vanishing effective pressure.

Removing the ice shelves altogether results in a disintegration of the West Antarctic ice sheet and (partially) marine basins in East Antarctica. After 500 years, this leads to a 5 m and a 16 m sea level rise for the power-law basal sliding and Coulomb friction conditions at the grounding line, respectively. The latter value agrees with simulations by DeConto and Pollard (2016) over a similar period (but with different forcing and including processes of hydro-fracturing and cliff failure).

The chosen parametrizations make model results largely independent of spatial resolution, so that f.ETISh can potentially be integrated in large-scale Earth system models.

1 Introduction

Projecting future sea-level rise (SLR) requires ice sheet models capable of exhibiting complex behaviour at the contact of the ice sheet with the atmosphere, subglacial environment and the ocean. Some of these interactions demonstrate non-linear behaviour due to feedbacks, leading to self-amplifying ice mass change. For instance, surface mass balance interacts with ice sheets through a powerful melt–elevation feedback, invoking non-linear response as a function of equilibrium line altitude, such

as a positive feedback on ablation that can be expected as the ice-sheet surface becomes lower (Levermann and Winkelmann, 2016). This feedback is also the main reason for the threshold behaviour of the Greenland ice sheet on multi-millennial time scales (e.g., Ridley et al., 2010). Typical for these self-amplifying effects is that they work both ways: the melt–elevation feedback equally allows for ice sheets to grow rapidly once a given threshold in positive accumulation is reached, resulting in hysteresis (Weertman, 1976).

Another powerful feedback relates to the contact of ice sheets (especially marine ice sheets with substantial parts of the bedrock lying below sea level) with the ocean. Mercer (1978) and Thomas (1979) identified marine ice sheet instability for ice sheets where the bedrock dips deeper inland from the grounding line (retrograde bed slopes), so that increased (atmospheric/oceanic) melting leads to recession of the grounding line. This would result in the glacier becoming grounded in deeper water with greater ice thickness. Since ice thickness at the grounding line is a key factor in controlling ice flux across the grounding line, thicker ice grounded in deeper water would result in increased ice discharge, and further retreat within a positive feedback loop. Early numerical ice sheet models failed to reproduce this feedback due to the lack of physical complexity (e.g., neutral equilibrium; Hindmarsh, 1993) and the poor spatial resolution to resolve the process of grounding line migration (Vieli and Payne, 2005; Pattyn et al., 2006). A major breakthrough was provided by an analysis of grounding line dynamics based on boundary layer theory (Schoof, 2007a, b, 2011), mathematically confirming the earlier findings by Weertman (1974) and Thomas (1979), i.e. that grounding line positions are unstable on retrograde bedrock slopes in absence of (ice shelf) buttressing. Schoof (2007a) showed that numerical ice-sheet models need to evaluate membrane stresses across the grounding line, hence resolving them on a sufficiently fine grid of less than a kilometre, which was further confirmed by two ice sheet model intercomparisons (Pattyn et al., 2012, 2013). Since then several marine ice sheet models of the Antarctic ice sheet have seen the light, with varying ways of treating the grounding line, i.e. by increasing locally spatial resolution at the grounding line (Favier et al., 2014; Cornford et al., 2015), by making use of local interpolation strategies at the grounding line (Feldmann et al., 2014; Feldmann and Levermann, 2015; Golledge et al., 2015; Winkelmann et al., 2015) or by parametrizing grounding line flux based on boundary layer theory (Pollard and DeConto, 2009; Pollard et al., 2015; DeConto and Pollard, 2016).

Other feedbacks relate ice sheet dynamics to basal sliding through thermo-viscous instabilities, which may lead to limit-cycle behaviour in ice sheets (Payne, 1995; Pattyn, 1996) as well as ice stream development in absence of strong basal topographic control (Payne and Dongelmans, 1997; Payne et al., 2000; Hindmarsh et al., 2009). More elaborate subglacial water flow models have since been developed, exhibiting similar feedback mechanisms in ice discharge (Schoof, 2010). For marine portions of ice sheets, the major subglacial constraint is governed by till deformation and observations have led to new insights in subglacial till deformation based on Coulomb friction controlled by subglacial water pressure (Tulaczyk et al., 2000a, b). In contact with the ocean, subglacial water pressure may therefore stem from the depth of the bed below sea level, which led to new characterizations of grounding line dynamics (Tsai et al., 2015).

In this paper, I present a new ice sheet model that reduces the three-dimensional nature of ice sheet flow to a two-dimensional problem, while keeping the essential (or elementary) characteristics of ice sheet thermomechanics and ice stream flow. Processes controlling grounding line motion are adapted in such a way that they can be represented at coarser resolutions. This

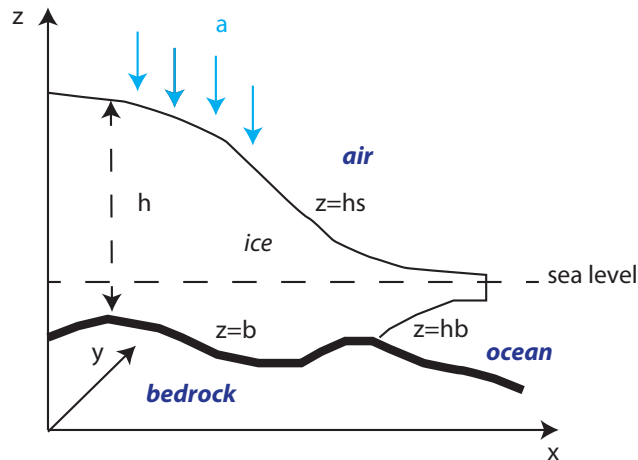


Figure 1. General Cartesian geometry of the f.ETISh model.

way, the model can more easily be integrated within computational-demanding Earth-system models. A new grounding-line algorithm based on the zero effective pressure conditions reigning at the contact with the ocean has been implemented (Tsai et al., 2015), which leads to a more sensitive grounding-line response.

I start by giving a detailed overview of the model and its components. The initialisation procedure for the Antarctic ice sheet is then given, and finally, the sensitivity of the Antarctic ice sheet to sudden atmospheric and ocean warming is presented on centennial time scales. The appendices further describe results of known benchmarks for grounded ice flow (Huybrechts et al., 1996; Payne et al., 2000) and marine ice sheet dynamics (Pattyn et al., 2012).

2 Model description

The model consists of diagnostic equations for ice velocities, and three prognostic equations for the temporal evolution of ice thickness, ice temperature, and bedrock deformation beneath the ice. Prescribed boundary fields are equilibrium bedrock topography, basal sliding coefficients, geothermal heat flux, and sea level. Present-day mean surface air temperatures and precipitation are derived from data assimilation within climate models. Ablation is determined from a Positive Degree-Day model. A list of model symbols is provided in Tables 1–3. A general overview of the Cartesian geometry used is given in Fig. 1.

For the coupled ice sheet/ice shelf system the surface elevation h_s is defined as

$$h_s = \max \left[b + h, \left(1 - \frac{\rho_i}{\rho_w} \right) h + z_{sl} \right], \quad (1)$$

Symbol	Description	Units	Value
\dot{a}	Surface mass balance (SMB)	m a^{-1}	
A	Glen's flow law factor	$\text{Pa}^{-n} \text{a}^{-1}$	
A_b, A'_b	Basal sliding factor in power-law sliding	$\text{Pa}^{-m} \text{m a}^{-1}$	
A_{froz}	Basal sliding factor for frozen conditions	$\text{Pa}^{-m} \text{m a}^{-1}$	10^{-10}
b	Bedrock elevation	m	
b_f	Buttressing factor		0–1
c_p	Specific heat of ice	$\text{J kg}^{-1} \text{K}^{-1}$	2009
C_r	Calving rate	m a^{-1}	
C_s	Friction coefficient in Schoof (2007a)	$\text{Pa m}^{-m_s} \text{a}^{m_s}$	$A'_b{}^{-m_s}$
c_0	Till cohesion	Pa	0
d	Diffusion coefficient of grounded ice sheet flow	$\text{m}^2 \text{a}^{-1}$	
D	Flexural rigidity of lithosphere	N m	10^{25}
E_f	Adjustment factor in Arrhenius equation		0.1–1
F_{melt}	Adjustment factor for sub-shelf melt rates		0.125–1
f_g	Fractional area of shelf grid cell in contact with bed		0–1
g	Gravitational acceleration	m s^{-2}	9.81
G	Geothermal heat flux	W m^{-2}	
h	Ice thickness	m	
h_b	Bottom of ice sheet/ice shelf	m	
h_e	Subgrid ice thickness on ice shelf edge	m	
h_g	Interpolated ice thickness at grounding line	m	
h_{max}	Maximum neighbouring ice thickness	m	
h_s	Ice sheet surface	m	
h_w	Water column thickness under ice shelf	m	
K	Thermal conductivity	$\text{J m}^{-1} \text{s}^{-1} \text{K}^{-1}$	2.1
L_w	Flexural length scale of the lithosphere		
m	Exponent in basal sliding law		2
m_s	Basal sliding exponent in Schoof (2007a)		$1/m$
M	Basal melting rate under ice shelves	m a^{-1}	
n	Glen's flow law exponent		3
n_x, n_y	Outward pointing normal vectors in x and y		
O_b	Optimization parameter for Coulomb friction law		
P	Precipitation rate (accumulation)	m a^{-1}	

Table 1. Model symbols, units and nominal values

Symbol	Description	Units	Value
p_w	Subglacial water pressure	Pa	
P_w	Point load on bedrock		
q	Exponent in Coulomb friction law		0–1
q_b	Bedrock load	Pa	
q_g	Ice flux at the grounding line	$\text{m}^2 \text{a}^{-1}$	
Q_o	Numerical coefficient in Tsai et al. (2015)		0.61
r	Scaling factor in sliding law		0–1
R	Gas constant	$\text{J kg}^{-1} \text{mol}^{-1}$	8.314
S	Surface melt rate	m a^{-1}	
T	Mean ice column temperature	K	
T_m	Pressure melting temperature	K	
T_{oc}	Ocean temperature	$^{\circ}\text{C}$	
T_r	Temperature at which basal sliding starts	$^{\circ}\text{C}$	
T_s	Surface temperature	K	
T^*	Homologous temperature	K	
ΔT	Background temperature forcing	$^{\circ}\text{C}$	
δT	Scaling factor in mass balance forcing	$^{\circ}\text{C}$	10
u	Horizontal ice velocities in x direction	m a^{-1}	
u_b	Basal velocity in x direction	m a^{-1}	
u_g	Velocity at the grounding line (Schoof, 2007a; Tsai et al., 2015)	m a^{-1}	
u_0	Limit velocity in Coulomb friction law	m a^{-1}	100
v	Horizontal ice velocities in y direction	m a^{-1}	
v_b	Basal velocity in y direction	m a^{-1}	
\mathbf{v}	Vertical mean horizontal velocity	m a^{-1}	
\mathbf{v}_b	Horizontal basal velocity	m a^{-1}	
\mathbf{v}_d	Horizontal deformational velocity	m a^{-1}	
w_b	Lithospheric deflection		
w_c	Weighting factor in calving law		0–1
w_p	Response to point load on bedrock		
x, y	Orthogonal horizontal coordinates	m	
z	Vertical elevation, increasing upwards from reference plane	m	
z_{sl}	Sea level elevation	m	0

Table 2. Model symbols, units and nominal values (continued)

Symbol	Description	Units	Value
β^2	Basal friction coefficient		
γ	Atmospheric lapse rate	$^{\circ}\text{C m}^{-1}$	0.008
Δ	Grid cell size, equal in x and y directions	m	
$\dot{\epsilon}_0$	Minimum strain rate in effective viscosity	a^{-1}	10^{-20}
η	Effective viscosity	Pa a	
κ	Thermal diffusivity	$\text{m}^2 \text{s}^{-1}$	1.1487×10^{-6}
λ_p	Scaling factor in pore water pressure		
ρ_b	Bedrock density	kg m^{-3}	3370
ρ_i	Ice density	kg m^{-3}	910
ρ_w	Sea water density	kg m^{-3}	1028
ϕ	Till friction angle	deg	
ϕ_{\min}	minimum till friction angle	deg	8–12
ϕ_{\max}	maximum till friction angle	deg	30
σ_b	Standard deviation of bedrock variability		
Θ	Buttressing at grounding line		[0, 1]
θ	Ice temperature	K	
θ_b	Basal temperature	K	
θ_b^s	Basal temperature of the ice shelf	K	
τ_b	Basal drag	Pa	
τ_c	Coulomb stress	Pa	
τ_d	Driving stress	Pa	
τ_f	Free-water tensile stress	Pa	
τ_{xx}, τ_{yy}	Longitudinal stress in x and y	Pa	
τ_w	Relaxation time for lithospheric response	a	3000
ζ	Scaled vertical coordinate		[0, 1]

Table 3. Model symbols, units and nominal values (continued)

where h is the ice thickness, b is the bedrock elevation, z_{sl} is the sea-level height with respect to the chosen datum, ρ_i and ρ_w are the ice and seawater density, respectively. It follows that the bottom of the ice sheet equals $h_b = h_s - h$, and that $h_b = b$ holds for the grounded ice sheet.

2.1 Ice velocities

5 2.1.1 Approximations

The ice sheet/ice shelf model has several modes of operation, depending on the boundary conditions that are applied. The most elementary flow regime of the grounded ice sheet is according to the Shallow-Ice approximation (SIA; Hutter, 1983), extended with either a Weertman-type (or power-law) function or a linear/plastic Coulomb friction law for basal sliding. Ice shelf flow is governed by the Shallow-Shelf approximation (SSA; Morland, 1987; MacAyeal, 1989), defined by zero basal drag and
 10 extended by a water-pressure condition at the seaward edge. The transition between both systems is given by a flux-condition at the grounding line (Pollard and DeConto, 2009, 2012a), either derived from boundary layer theory based on SSA (SGL; Schoof, 2007a) or given by a flux-condition based on Coulomb friction at the grounding line (TGL; Tsai et al., 2015).

A second mode of operation is the hybrid mode, in which the flow regime of the grounded ice sheet is governed by a combination of SIA, responsible for ice-deformational flow, and SSA for basal sliding (Bueler and Brown, 2009; Martin et al.,
 15 2011; Winkelmann et al., 2011). The hybrid model is used in combination with power-law sliding or linear/plastic Coulomb friction underneath the ice sheet. All components of the flow model are detailed in the sections below.

2.1.2 Shallow-Ice Approximation (SIA)

The Shallow-Ice approximation (SIA; Hutter, 1983) is commonly used in ice sheet modelling. This approximation is valid for ice sheets of small aspect ratios $h \ll L$, where L is the horizontal length scale of the ice sheet domain, and further characterized
 20 by a low curvature and low sliding velocities. The approximation is, however, not valid near grounding lines nor for ice shelf flow, for which other approximations are applied (see below). According to SIA, the vertical mean horizontal velocity in an ice sheet is given by

$$\mathbf{v}_{\text{SIA}} = \mathbf{v}_b + \frac{2A}{n+2} h |\tau_d|^{n-1} \tau_d, \quad (2)$$

where $\tau_d = -\rho_i g h \nabla h_s$ is the driving stress, A is the flow parameter in Glen's flow law (with $n = 3$), $\mathbf{v}_b = (u_b, v_b)$ is the basal sliding velocity and $\mathbf{v}_{\text{SIA}} = (u, v)$ is the vertical mean horizontal velocity according to SIA. The flow parameter A is a
 25 function of ice temperature (see Sect. 2.4).

2.1.3 Hybrid Shallow-Shelf/Shallow-Ice approximation (HySSA)

The flow velocity in an ice shelf or an ice stream characterized by low drag is derived from the Stokes equations (Stokes, 1845) by neglecting vertical shear terms and by integrating the force balance over the vertical. The resulting equations are (Morland, 1987; MacAyeal, 1989):

$$5 \quad 2 \frac{\partial}{\partial x} \left(2\eta h \frac{\partial u}{\partial x} + \eta h \frac{\partial v}{\partial y} \right) + \frac{\partial}{\partial y} \left(\eta h \frac{\partial u}{\partial y} + \eta h \frac{\partial v}{\partial x} \right) - \tau_{b_x} = -\tau_{d_x}, \quad (3)$$

$$2 \frac{\partial}{\partial y} \left(2\eta h \frac{\partial v}{\partial y} + \eta h \frac{\partial u}{\partial x} \right) + \frac{\partial}{\partial x} \left(\eta h \frac{\partial v}{\partial x} + \eta h \frac{\partial u}{\partial y} \right) - \tau_{b_y} = -\tau_{d_y}, \quad (4)$$

where

$$10 \quad \eta = \frac{A^{-1/n}}{2} \left[\left(\frac{\partial u}{\partial x} \right)^2 + \left(\frac{\partial v}{\partial y} \right)^2 + \frac{\partial u}{\partial x} \frac{\partial v}{\partial y} + \frac{1}{4} \left(\frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right)^2 + \varepsilon_0^2 \right]^{(1-n)/2n}, \quad (5)$$

and where $\tau_{d_x} = \rho_i g h (\partial h_s / \partial x)$ (similar for τ_{d_y}). $\varepsilon_0 = 10^{-20}$ is a small factor to keep η finite, hence to prevent singularities when velocity gradients are zero. For the ice shelf, $\tau_b = 0$, while for the grounded ice sheet the basal drag is a function of the friction at the base. The SSA stress-equilibrium equations (3) and (4) require boundary conditions to be specified along the contour which defines the boundary to the ice-shelf domain, which is taken as the edge of the computational domain, irrespective of whether or not calving is considered. Dynamic conditions (specification of stress) are applied at this seaward edge, so that the vertically-integrated pressure balance then reads

$$2\eta h \left[\left(2 \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) n_x + \frac{1}{2} \left(\frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right) n_y \right] = n_x \frac{1}{2} \rho_i g h^2 \left(1 - \frac{\rho_i}{\rho_w} \right), \quad (6)$$

$$20 \quad 2\eta h \left[\left(2 \frac{\partial v}{\partial y} + \frac{\partial u}{\partial x} \right) n_y + \frac{1}{2} \left(\frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right) n_x \right] = n_y \frac{1}{2} \rho_i g h^2 \left(1 - \frac{\rho_i}{\rho_w} \right), \quad (7)$$

where n_x, n_y are the outward-pointing normal vectors in the x and y direction, respectively.

The ice shelf velocity field is needed for determining the effect of buttressing in the grounding line flux conditions (see below), as well as for the thickness evolution of the ice shelf. For the purpose of buttressing, velocity gradients downstream

from the grounding line are used to determine the longitudinal stretching rate, which is compared to the stretching rate of a freely-floating ice shelf to determine a so-called buttressing factor.

Both SIA and SSA velocities are combined to obtain the velocity field of the grounded ice sheet according to the hybrid model (HySSA; Bueler and Brown, 2009). While Bueler and Brown (2009) use a weighing function to ensure a continuous solution of the velocity from the interior of the ice sheet across the grounding line to the ice shelf, Winkelmann et al. (2011) have demonstrated that a simple addition (for the grounded ice sheet velocities) still guarantees a smooth transition. Thus basal velocities for the grounded ice sheet are SSA velocities $\mathbf{v}_b = \mathbf{v}_{\text{SSA}}$ and

$$\mathbf{v} = \mathbf{v}_{\text{SIA}} + \mathbf{v}_{\text{SSA}} \quad (8)$$

for the velocity field in the grounded ice sheet. In the ice shelf, the SIA velocity is kept zero throughout.

10 2.1.4 Power-law basal sliding

Basal sliding is introduced as a Weertman sliding law, i.e.,

$$\mathbf{v}_b = A'_b |\tau_b|^{m-1} \tau_b, \quad (9)$$

where τ_b is the basal shear stress ($\tau_b \sim \tau_d$ for SIA), A'_b is a basal sliding factor, and m is the basal sliding law exponent. The basal sliding factor A'_b is temperature dependent and allows for sliding within a basal temperature range between -3 and 0°C .

15 It further takes into account sub-grid sliding across mountainous terrain (Pollard et al., 2015):

$$A'_b = (1 - r)A_{\text{froz}} + rA_b, \quad (10)$$

where $r = \max[0, \min[1, (T^* - T_r)/(-T_r)]]$, A_{froz} is the sliding coefficient in case of frozen bedrock (chosen to be very small but different from zero to avoid singularities in the basal friction calculation), T^* is the temperature corrected for the dependence on pressure (see Sect. 2.4.3) and $T_r = \min[-3 - 0.2\sigma_b]$, where σ_b is the standard deviation of bedrock elevation within the grid cell (Pollard et al., 2015). Basal sliding factors A_b are either considered constant in space/time or are spatially varying and obtained through optimization methods (see Sect. 4.1). Basal velocities in the hybrid model are defined through a friction power law, where

$$\tau_b = \beta^2 \mathbf{v}_b = A_b'^{-1/m} |\mathbf{v}_b|^{1/m-1} \mathbf{v}_b. \quad (11)$$

2.1.5 Coulomb friction law

25 Basal friction within the HySSA equations can also be calculated based on a model for plastic till (Tulaczyk et al., 2000a). Several variations of a basal till model can be found in the literature (Schoof, 2006; Gagliardini et al., 2007; Bueler and Brown,

2009; Winkelmann et al., 2011). Deformation of saturated till is well modelled by a plastic (Coulomb friction) or nearly plastic rheology (Truffer et al., 2000; Tulaczyk et al., 2000a; Schoof, 2006). Its yield stress τ_c satisfies the Mohr–Coulomb relation:

$$\tau_c = c_0 + O_b \tan \phi (\rho_i g h - p_w), \quad (12)$$

where the term between brackets is the effective pressure of the overlying ice on the saturated till (Cuffey and Paterson, 2010), or the ice overburden pressure minus the water pressure p_w , c_0 is the till cohesion ($c_0 = 0$ is further considered), and ϕ is the till friction angle. The latter can be either taken as a constant value or vary as a function of bedrock elevation (Maris et al., 2014):

$$\phi = -\phi_{\min} \frac{b - z_{sl}}{10^3} + \left(1 + \frac{b - z_{sl}}{10^3}\right) \phi_{\max}, \quad (13)$$

and limited by $\phi = \phi_{\min}$ for $b - z_{sl} \leq -10^3$ m and $\phi = \phi_{\max}$ for $b - z_{sl} \geq 0$. O_b is a spatially-varying parameter used to optimize the basal friction field, in a similar way as A_b in Eq. (10). Without optimization, it takes the value of $O_b = 1$.

The most comprehensive approach to solve for the subglacial water pressure in Eq. (12) is due to Bueller and van Pelt (2015) by considering a hydrological model of subglacial water drainage within the till. However, Martin et al. (2011) propose to relate major till characteristics to bedrock geometry and allow till friction angle and basal water pressure to be a function of the bed elevation compared to sea level. This leads to zones of weak till and saturation in subglacial basins that are well below sea level (Martin et al., 2011; Maris et al., 2014). Following their analysis, the subglacial water pressure is defined by

$$p_w = 0.96 \lambda_p \rho_i g h. \quad (14)$$

Here, λ_p is a scaling factor such that the pore water pressure is maximal when the ice is resting on bedrock at or below sea level. Below sea level, the pores in the till are assumed to be saturated with water so λ_p is then equal to 1. The factor λ_p is scaled with the height above sea level up until 1000 m. At and above 1000 m, λ_p is equal to 0 (Maris et al., 2014). While there is no direct physical evidence for such water-pressure distribution in the interior of ice sheets, near grounding lines in direct contact with the ocean, subglacial water pressure of saturated till may also be approximated by (Tsai et al., 2015):

$$p_w = -\rho_w g (b - z_{sl}), \quad (15)$$

which is valid for $b - z_{sl} < 0$, otherwise $p_w = 0$. By definition, $p_w = \rho_i g h$ at the grounding line and underneath floating ice shelves, so that the effective pressure becomes zero. Bueller and Brown (2009) consider the pore water pressure locally as at most a fixed fraction (95%) of the ice overburden pressure $\rho_i g h$. Winkelmann et al. (2011) use a fraction of 0.96, which is applied in Eq. (14).

To link Coulomb friction to basal drag, the formulation proposed by Bueler and van Pelt (2015) is opted for, where τ_c and v_b combine to determine τ_b through a sliding law, i.e.,

$$\tau_b = \tau_c \frac{v_b}{|v_b|^{1-q} u_0^q}, \quad (16)$$

where $0 \leq q \leq 1$, and u_0 is a threshold sliding speed (Aschwanden et al., 2013). The Coulomb friction law, Eq. (16), includes the case $q = 0$, leading to the purely plastic (Coulomb) relation $\tau_b = \tau_c v_b / |v_b|$. At least in the $q \ll 1$ cases, the magnitude of the basal shear stress becomes nearly independent of $|v_b|$, when $|v_b| \gg u_0$. Equation (16) could also be written in a generic power-law form $\tau_b = \beta^2 |v_b|^{q-1} v_b$ with coefficient $\beta^2 = \tau_c / u_0^q$; in the linear case $q = 1$, $\beta^2 = \tau_c / u_0$ (Bueler and van Pelt, 2015).

Alternatively, both the power-law sliding law Eq. (9) and the Coulomb friction law Eq. (16) can be combined (Tsai et al., 2015; Asay-Davis et al., 2015), by taking the lowest friction value of both. Since at the grounding line basal sliding velocities are considered highest, this equally implies high basal drag in a traditional power-law sliding law. As a consequence, power law sliding/friction still leads to a relatively sharp transition in τ_b at the grounding line (Tsai et al., 2015). Coulomb basal conditions imply that basal drag vanishes towards the grounding line, thus ensuring a smooth transition between the ice stream and ice shelf. Expressing the basal traction as

$$\tau_b = \min \left[\beta^2 v_b, \frac{\tau_c v_b}{|v_b|^{1-q} u_0^q} \right] \quad (17)$$

ensures that it is continuous (though not differentiable) across the grounding line (Asay-Davis et al., 2015).

2.1.6 Grounding-line flux condition for power-law sliding (SGL)

Previous studies have indicated that it is necessary to resolve the transition zone/boundary layer at sufficiently fine resolution in order to capture grounding-line migration accurately (Durand et al., 2009; Pattyn et al., 2012, 2013; Pattyn and Durand, 2013; Durand and Pattyn, 2015). In large-scale models, this can lead to unacceptably small time-steps and costly integrations. Pollard and DeConto (2009, 2012a) incorporated the boundary layer solution of Schoof (2007a) directly in a numerical ice-sheet model at coarse grid resolution, so the flux, q_g , across model grounding lines is given by

$$q_g = \left[\frac{A(\rho_i g)^{n+1} (1 - \rho_i / \rho_w)^n}{4^n C_s} \right]^{\frac{1}{m_s+1}} \Theta^{\frac{n}{m_s+1}} h_g^{\frac{m_s+n+3}{m_s+1}}. \quad (18)$$

This yields the vertically averaged velocity $u_g = q_g/h_g$ where h_g is the ice thickness at the grounding line. Θ in Eq. (18) accounts for back stress at the grounding line due to buttressing by pinning points or lateral shear, and is defined as

$$\Theta = \frac{b_f \tau_{xx} + (1 - b_f) \tau_f}{\tau_f}, \quad (19)$$

where τ_{xx} is the longitudinal stress just downstream of the grounding line, calculated from the viscosity and strains in a preliminary SSA solution without constraints given by Eq. (18), and τ_f the free-water tensile stress defined by

$$\tau_f = \frac{1}{2} \rho_i g h \left(1 - \frac{\rho_i}{\rho_w} \right). \quad (20)$$

b_f is an additional buttressing factor to control the buttressing strength of ice shelves and varies between 0 (no buttressing) and 1 (full buttressing). As in Pollard and DeConto (2012a), C_s is Schoof's basal sliding coefficient and m_s the basal sliding exponent, so that C_s is related to the sliding coefficients A'_b by $C_s = A'_b{}^{-m_s}$, where $m_s = 1/m$. Grounding-line ice thickness h_g is linearly interpolated in space by estimating the sub-grid position of the grounding line between the two surrounding floating and grounded h -grid points. Therefore, the height above floatation is linearly interpolated on the Arakawa C-grid between those two points to where it is zero. Subsequently, the bedrock elevation is linearly interpolated to that location, and the floatation thickness of ice for that bedrock elevation and current sea level is obtained (Pattyn et al., 2006; Gladstone et al., 2010; Pollard and DeConto, 2012a). The velocity u_g is then calculated at the grounding-line points and imposed as an internal boundary condition for the flow equations, hence overriding the large-scale velocity solution at the grounding line. $u_g = q_g/h_g$ is imposed exactly at the u -grid grounding line point when the flux q_g is greater than the large-scale sheet-shelf equation's flux at the grounding line.

Equation (18) applies equally to the y direction, with v_g and τ_{yy} instead of u_g and τ_{xx} . Note that spatial gradients of quantities parallel to the grounding line, which are not included in Schoof's flow-line derivation of Eq. (18), are neglected here (Katz and Worster, 2010; Gudmundsson et al., 2012; Pattyn et al., 2013). This parametrization was also found to yield results comparable to SSA models solving transient grounding line migration at high spatial resolution of the order of hundreds of meters (Pattyn and Durand, 2013; Durand and Pattyn, 2015), despite the fact that Eq. (18) applies to steady-state conditions.

2.1.7 Grounding-line flux condition for Coulomb friction (TGL)

The grounding-line parametrization based on the boundary layer theory by Schoof (2007a) is invalid when Coulomb friction near the grounding line is considered and the effective stress tends to zero. However, Tsai et al. (2015) offers such a solution for vanishing Coulomb friction at the grounding line, and therefore independent of basal sliding coefficients:

$$q_g = Q_o \frac{8A(\rho_i g)^n}{4^n O_b \tan \phi} \left(1 - \frac{\rho_i}{\rho_w} \right)^{n-1} \Theta^{n-1} h_g^{n+2}, \quad (21)$$

where $Q_o \approx 0.61$ is a numerical coefficient determined from the boundary-layer analysis. The flux in the y direction is obtained in a similar fashion. As in Eq. (18), buttressing scales to the same power as $(1 - \rho_i/\rho_w)$, which is $n - 1$. The performance of both flux conditions is tested in Appendix C.

The TGL flux condition can be used in conjunction with power-law basal sliding. Indeed, Tsai et al. (2015) have shown that the crossover from Coulomb to power-law roughly occurs at stresses $\gtrsim 100$ kPa, hence the Coulomb regime occurs within $\lesssim 17$ m above the floatation height. This is a very small height difference, which implies that in most cases —with exception of ice plains— a narrow Coulomb regime exists, within a grid cell of a continental-scale model.

2.2 Ice thickness evolution

Ice sheet thickness evolution is based on mass conservation, leading to the continuity equation. For the general ice sheet/ice shelf system, this is written as:

$$\frac{\partial h}{\partial t} = -\frac{\partial(uh)}{\partial x} - \frac{\partial(vh)}{\partial y} + \dot{a} - M, \quad (22)$$

where \dot{a} is the surface mass balance (accumulation minus surface ablation), and M is the basal melt rate (solely underneath ice shelves, as basal melt rates underneath the ice sheet are not accounted for). The treatments of the various local ice gains or losses (surface mass balance, etc.) are described in later sections. For the SIA model in the grounded ice sheet, Eq. (22) is written as a diffusion equation for ice thickness (Huybrechts, 1992):

$$\frac{\partial h}{\partial t} = \frac{\partial}{\partial x} \left(d \frac{\partial(h + h_b)}{\partial x} \right) + \frac{\partial}{\partial y} \left(d \frac{\partial(h + h_b)}{\partial y} \right) + \dot{a} - M, \quad (23)$$

where h_b is the bottom of the ice sheet (or the bedrock elevation b for the grounded ice sheet).

It is also ensured that thinning due to grounding line retreat does not exceed the maximum permissible rate, using theoretical knowledge of maximum possible stresses at the grounding line that is called the ‘maximum strain check’. Similar to Ritz et al. (2015), tensile stresses at the grounding line are ensured to not exceed those from buttressing by water alone, i.e., the free-water tensile stress, and calculate the maximum corresponding strain rate, expressed as a maximum thinning rate.

2.3 Calving and sub-shelf pinning

Ice-front calving is obtained from the large scale stress field (Pollard and DeConto, 2012a), based on the horizontal divergence of the ice-shelf velocities and which is similar to parametrizations used elsewhere (Martin et al., 2011; Winkelmann et al., 2011; Levermann et al., 2012). The calving rate C_r is defined as

$$C_r = 30(1 - w_c) + 3 \times 10^5 \max \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y}, 0 \right) \frac{w_c h_e}{\Delta} \quad (24)$$

where $w_c = \min(1, h_e/200)$ is a weight factor and h_e is the subgrid ice thickness within a fraction of the ice edge grid cell that is occupied by ice (Pollard and DeConto, 2012a), defined by

$$h_e = \max \left[h_{\max} \times \max \left(0.25, e^{-h_{\max}/100} \right), 30, h \right] \quad (25)$$

where a minimum ice thickness of 30 m avoids too thin ice shelves. The value of h_{\max} is defined as the maximum ice thickness of the surrounding grid cells (grounded or floating) that are not adjacent to the ocean (Pollard and DeConto, 2012a). The calving rate C_r is then subtracted from the basal melt rate M in Eq. (22).

Given the relatively low spatial resolution of a large-scale ice-sheet model, small pinning points underneath ice shelves due to small bathymetric rises scraping the bottom of the ice and exerting an extra back pressure on the ice shelf (Berger et al., 2016; Favier et al., 2016) are not taken into account. To overcome this a simple parametrization based on the standard deviation of observed bathymetry within each model cell was accounted for to introduce a given amount of basal friction of the ice shelf (Pollard and DeConto, 2012a). The fractional area f_g of ice in contact with sub-grid bathymetric high is defined as (modified from Pollard and DeConto, 2012a):

$$f_g = \max \left[0, 1 - \frac{h_w}{\sigma_b} \right] \quad (26)$$

where h_w is the thickness of the water column underneath the ice shelf and σ_b is the standard deviation of the bedrock variability (see above). This factor f_g is multiplied with β^2 in the basal friction. For the grounded ice sheet, $f_g = 1$; for the floating ice shelf in deeper waters, $f_g = 0$, so that the ice shelf does not experience any friction.

2.4 Ice temperature and rheology

2.4.1 Ice-sheet temperature

The diffusion–advection equation for an ice sheet is given by (Huybrechts, 1992):

$$\frac{\partial \theta}{\partial t} = \kappa \frac{\partial^2 \theta}{\partial z^2} - u \frac{\partial \theta}{\partial x} - v \frac{\partial \theta}{\partial y} + \frac{\Phi}{\rho_i c_p}, \quad (27)$$

where $\kappa = K/\rho_i c_p$ is the thermal diffusivity of ice, K is the thermal conductivity, c_p is the heat capacity of ice, θ is the ice temperature, and $\Phi = -\rho_i g (h_s - z) \nabla h_s \partial v_d / \partial z$ represents deformational heating, where v_d is the deformational velocity component ($v_d = v - v_b$). The basal boundary condition is given by

$$\frac{\partial \theta_b}{\partial z} = \frac{G + \tau_d v_b}{K}, \quad (28)$$

where G is the geothermal heat flux and the second term represents frictional heating at the base. The last term in Eq. (28) represents strain heating. Given the two-dimensional nature of the model, the temperature field employs shape functions for

vertical profiles of deformational velocity v_d , its vertical gradient, and the vertical velocity, based on SIA (Hindmarsh, 1999). Eq. 27 is then solved in scaled vertical coordinates $\zeta = (h_s - z)/h$, with $\zeta = 0$ at the surface and $\zeta = 1$ at the bottom of the ice sheet. The use of shape function allows for a faster calculation of the thermodynamic model. However, since this is an approximation compared to fully solving Eq. 27, the EISMINT-I benchmark experiments (Huybrechts et al., 1996) were performed and results are given in Appendix A.

2.4.2 Ice-shelf temperature

In ice shelves, a simple temperature model is adopted, considering the accumulation at the surface balanced by basal melting underneath an ice shelf and with only vertical diffusion and advection into play (Holland and Jenkins, 1999):

$$\theta(\zeta) = \frac{(T_s - \theta_b^s) \exp(\beta_1) + \theta_b^s - T_s \exp(\beta_2)}{1 - \exp(\beta_2)}, \quad (29)$$

where $\beta_1 = \dot{a}\zeta h/\kappa$, $\beta_2 = \dot{a}h/\kappa$, and θ_b^s is the ocean temperature at the base of the ice shelf, corrected for ice-shelf depth, i.e., $\theta_b^s = T_{oc} = -1.7 - 0.12 \times 10^{-3}h_b$ (Maris et al., 2014).

2.4.3 Thermomechanical coupling

The mean column temperature T is obtained by integrating θ from the base of the ice sheet to a given height in the ice column. Since most of the ice deformation is in the bottom layers of the ice sheet, the temperature closest to the bottom determines to a large extent the deformational properties. Compared to full thermomechanically-coupled ice sheet models, satisfactory results where obtained by considering a mean column temperature for the lower most 10-40% of the ice column. This fraction can also be regarded as an extra tuning parameter in an ensemble run, especially given the large uncertainties pertaining to geothermal heat flow underneath major ice sheets. The flow parameter A and its temperature dependence on temperature are specified as in Huybrechts (1992) and Pollard and DeConto (2012a):

$$A = E_f \times 5.47 \times 10^{10} \exp\left(\frac{-13.9 \times 10^4}{RT^*}\right) \quad \text{if } T^* \geq 263.15\text{K}, \quad (30)$$

$$A = E_f \times 1.14 \times 10^{-5} \exp\left(\frac{-6.0 \times 10^4}{RT^*}\right) \quad \text{if } T^* < 263.15\text{K}, \quad (31)$$

where $T^* = T - T_m$ is the homologous temperature, with $T_m = -8.66 \times 10^{-4}(1 - \zeta)h$ the pressure melting correction and R the gas constant. Units of A are $\text{Pa}^{-3} \text{yr}^{-1}$ corresponding to $n = 3$. The enhancement factor E_f is set to 1 for the main ice sheet model, and to $E_f = 0.5$ for ice shelves. The ratio of enhancement factors represent differences in fabric anisotropy between grounded and ice shelf ice (Ma et al., 2010). Verification of the thermomechanical coupling scheme using a vertical mean value of A follows the EISMINT-II benchmark experiments (Payne et al., 2000) and is detailed in Appendix B.

2.5 Bedrock deformation

The response of the bedrock to changing ice and ocean loads is solved through a combined time-lagged asthenospheric relaxation and elastic lithospheric response due to the applied load (Huybrechts and de Wolde, 1999; Pollard and DeConto, 2012a). The deflection of the lithosphere is given by

$$5 \quad D\nabla^4 w_b + \rho_b g w_b = q_b, \quad (32)$$

where D is the flexural rigidity of the lithosphere, and ρ_b is the bedrock density. The load is then defined by

$$q_b = \rho_i g h + \rho_w g h_w - \rho_i g h^{\text{eq}} - \rho_w g h_w^{\text{eq}}, \quad (33)$$

where h_w is the ocean column thickness, and h^{eq} and h_w^{eq} are the values of ice thickness and ocean column thickness in equilibrium, respectively, taken from modern observed fields. Equation (32) is solved by a Green's function (Huybrechts and de Wolde, 1999). The response to a point load P_w ($q_b \times \text{area}$) versus distance from the point load l is then given by

$$w_p(l) = \frac{P_w L_w^2}{2\pi D} \text{kei} \left(\frac{l}{L_w} \right), \quad (34)$$

where kei is a Kelvin function of zeroth order (defined as the imaginary part of a modified Bessel function of the second kind), and $L_w = (D/\rho_b g)^{1/4} \approx 132$ km is the flexural length scale. For any load, the different values of the point loads w_p are summed over all grid cells to yield $w_b(x, y)$. Finally, the actual rate of change in bedrock elevation is given by a simple relaxation scheme:

$$\frac{\partial b}{\partial t} = -\frac{1}{\tau_w} (b - b^{\text{eq}} + w_b), \quad (35)$$

where b is the actual bedrock elevation, b^{eq} is the elevation in equilibrium (taken from modern observed fields), and $\tau_w = 3000$ year (Pollard and DeConto, 2012a).

2.6 Numerical grid and solution

The ice sheet-shelf model uses a finite-difference staggered grid, where horizontal velocities (u, v) are calculated on two separate staggered Arakawa C-grids, as is usual for vector fields (Rommelaere and Ritz, 1996), while diffusion coefficients for the ice-sheet equation d are calculated on an Arakawa B-grid, staggered in both x and y direction, since these are scalar quantities (Fig. 2). The f.ETISh model uses no vertical coordinate, except for the temperature field calculation. Here, the scaled vertical coordinate system consists of 11 irregularly-spaced layers, with a minimum layer thickness of $\Delta\zeta = 0.015$ at the bottom. This way, the number of vertical layers can be greatly reduced, as most of the variability of the vertical temperature profile is situated close to the bed.

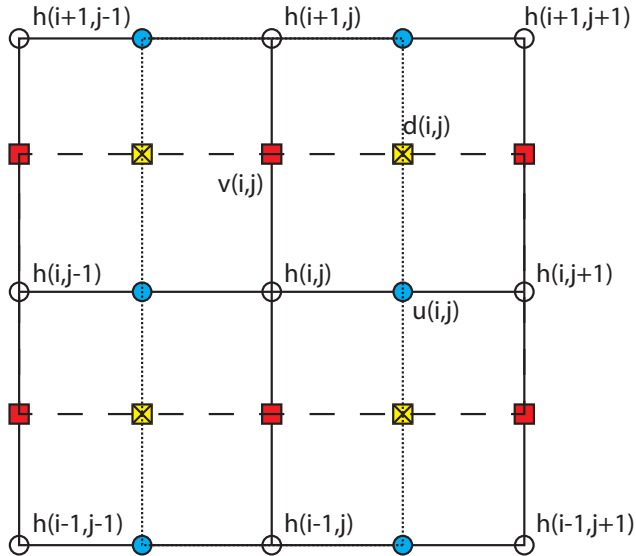


Figure 2. Staggered grids used in the model: the basic grid is the ice-thickness grid (shown in open circles). u and v velocities for the ice shelves (and ice streams) are calculated on two different staggered Arakawa C grids (filled circles and squares, respectively). Diffusion coefficients d in the ice-sheet equation are solved on an Arakawa B grid (crossed squares).

The SSA velocity field Eqs. (3–4) is solved as a sparse linear system where both u and v component are solved as once in one matrix \mathbf{A} with size $(2 \times N_x \times N_y)$ by $(2 \times N_x \times N_y)$:

$$\begin{pmatrix} \mathbf{A}_{ux} & \mathbf{A}_{vx} \\ \mathbf{A}_{uy} & \mathbf{A}_{vy} \end{pmatrix} \cdot \begin{pmatrix} \mathbf{u} \\ \mathbf{v} \end{pmatrix} = \begin{pmatrix} \mathbf{b}_x \\ \mathbf{b}_y \end{pmatrix} \quad (36)$$

where N_x, N_y are the number of grid points in the x, y direction, respectively. The submatrices $\mathbf{A}_{ux}, \mathbf{A}_{vx}$ contain the coefficients for the solution in the x direction for u and v , respectively. $\mathbf{A}_{uy}, \mathbf{A}_{vy}$ are defined in a similar way. Due to the dependence of the effective viscosity η on u, v , the solution requires a few iterations to reach convergence. A similar solution approach is taken for solving the continuity equation for ice thickness (Payne and Dongelmans, 1997), which was favoured over an Alternating Direct Implicit scheme used in several ice-sheet models (Huybrechts, 1992; Pollard and DeConto, 2012a).

The f.ETISH model is implemented in MATLAB[®]. Computational improvements involved the omission of all *for*-loops by using circular shifts (with exception of the time loop), thereby optimizing the use of matrix operations. The bulk of computational time is devoted to the solution of the sparse matrix systems, which are natively optimized in MATLAB[®] using multi-threading. A preconditioned conjugate gradient method is used for solving the ice sheet/ice shelf continuity equation. The velocity field in the hybrid model is solved using a stabilized bi-conjugate gradients method, which is also preconditioned and further initialized by the velocity field solution from the previous time step. Both numerical solvers are iterative and the

preconditioning limits the number of iterations to reach convergence. They are considerably faster compared to the direct solution.

The f.ETISH model is compared to other ice sheet models via a series of benchmarks, such as the EISMINT-I benchmark for isothermal ice-sheet models (Huybrechts et al., 1996, Appendix A), the EISMINT-II benchmark for thermomechanically-
 5 coupled ice sheet models (Payne et al., 2000, Appendix B), and the MISMIP experiments for marine ice-sheet models (Pattyn et al., 2012, Appendix C). Results show that the f.ETISH model is in close agreement with all of the benchmark experiments.

3 Input and climate forcing

3.1 Input data sets

For modelling the Antarctic ice sheet, the bedrock topography is based on the Bedmap2 data (Fretwell et al., 2013), from which
 10 ice thickness, present-day surface topography and grounding-line position are derived. Surface mass balance and temperatures are obtained from Van Wessem et al. (2014), based on the output of the regional atmospheric climate model RACMO2 for the period 1979–2011 and evaluated using 3234 *in situ* mass balance observations and ice-balance velocities.

For geothermal heat flux we employ a recent update of Fox-Maule et al. (2005) due to Purucker (2013). It is based on low-
 15 resolution magnetic observations acquired by the CHAMP satellite between 2000 and 2010, and produced from the MF-6 model following the same technique as described in Fox-Maule et al. (2005).

All datasets are resampled on the spatial resolution used for the experiments. The experiments shown in this paper employ a grid spacing of 25 (and in a few cases 40 or 16) km.

3.2 Atmospheric and ocean forcing

Atmospheric forcing is applied in a parametrized way, based on the observed fields of precipitation (accumulation rate) and
 20 surface temperature. For a change in background (forcing) temperature ΔT , corresponding fields of precipitation P and atmospheric temperature T_s are defined by (Huybrechts et al., 1998; Pollard and DeConto, 2012a)

$$T_s = T_s^{\text{obs}} - \gamma(h_s - h_s^{\text{obs}}) + \Delta T, \quad (37)$$

$$P = \dot{a}^{\text{obs}} \times 2^{(T_s - T_s^{\text{obs}})/\delta T}, \quad (38)$$

where $\gamma = 0.008^\circ\text{C m}^{-1}$ is the lapse rate and δT is 10°C (Pollard and DeConto, 2012a). The subscript ‘obs’ refers to the
 25 present-day observed value. Any forcing (increase) in background then leads to an overall increase in surface temperature corrected for elevation changes according to the environmental lapse rate γ . The parametrizations of T_s and P can easily be replaced by values that stem from GCMs, with appropriate corrections for surface elevation (e.g., de Boer et al., 2015).

Surface melt is parametrized using a positive degree-day model (Huybrechts and de Wolde, 1999). The total amount of positive degree days (PDD) is obtained as

$$\text{PDD} = \frac{1}{\sigma\sqrt{2\pi}} \int_0^A \left[\int_0^{\bar{T}+2.5\sigma} T \exp\left(-\frac{(T-\bar{T})^2}{2\sigma^2}\right) dT \right] dt, \quad (39)$$

where σ is taken as 5°C (Reeh, 1989) and \bar{T} is the mean annual temperature. The annual number of positive degree days represents a melt potential, used to melt snow and (superimposed) ice. This is determined by applying a seasonal cycle to the atmospheric temperatures with a double amplitude of 20°C , linearly increasing to 30°C at an elevation of 3000 m, and kept at 30°C at higher elevations (Pollard and DeConto, 2012a). The PDD melt potential is related to surface melt through a coefficient of 0.005 m of melt per degree day (Pollard and DeConto, 2012a). Although more complex schemes are often used, taking into account refreezing of percolating meltwater in the snow pack and melting of superimposed ice with different melt coefficients (Huybrechts and de Wolde, 1999), which is also confirmed by recent observations (Machguth et al., 2016), surface melt is rather limited for the present-day Antarctic ice sheet. Surface mass balance is then the sum of the different components, i.e., $\dot{a} = P - S$, where $S = 0.005 \times \text{PDD}$ is the surface melt rate.

Melting underneath the floating ice shelves is often based on parametrizations that relate sub-shelf melting to ocean temperature and ice-shelf depth (Beckmann and Goosse, 2003; Holland et al., 2008), either in a linear or a quadratic way (Martin et al., 2011; Pollard and DeConto, 2012a; de Boer et al., 2015; DeConto and Pollard, 2016). This leads to higher melt rates close to the grounding line, as the ice-shelf bottom is the lowest. While the adaptation by Holland et al. (2008) and Pollard and DeConto (2012a) is implemented in f.ETISH, only constant values of ice shelf melt were used in the experiments for this paper, scaled by a melt factor F_{melt} . This factor distinguishes protected ice shelves (Ross and Ronne-Filchner; Fig. 3), with a melt scaling factor of $F_{\text{melt}} = 0.125$, from all other ice shelves that have a scaling factor of $F_{\text{melt}} = 1$. A similar approach has been taken by many other ice-sheet models cited in de Boer et al. (2015).

20 4 Present-day Antarctic ice sheet simulation

4.1 Initialization

Model initialization to the modern Antarctic ice sheet geometry is based on the method by Pollard and DeConto (2012b) by optimizing basal sliding coefficients in an iterative fashion. This nudging scheme is applied to both the Weertman-type power law and the Coulomb friction law, so that it can be used in conjunction with the two types of grounding-line flux conditions. The model (with grounding lines and floating ice constrained as described above) is run forward in time, starting from modern observed bed and ice surface elevations and driven by the observed climatology (surface mass balance and temperature). Full thermomechanical coupling and temperature evolution, isostatic bedrock adjustment, calving and sub-grid ice-shelf pinning is equally considered. For the Weertman sliding law, basal sliding coefficients $A_b(x, y)$ are initialized with a constant value

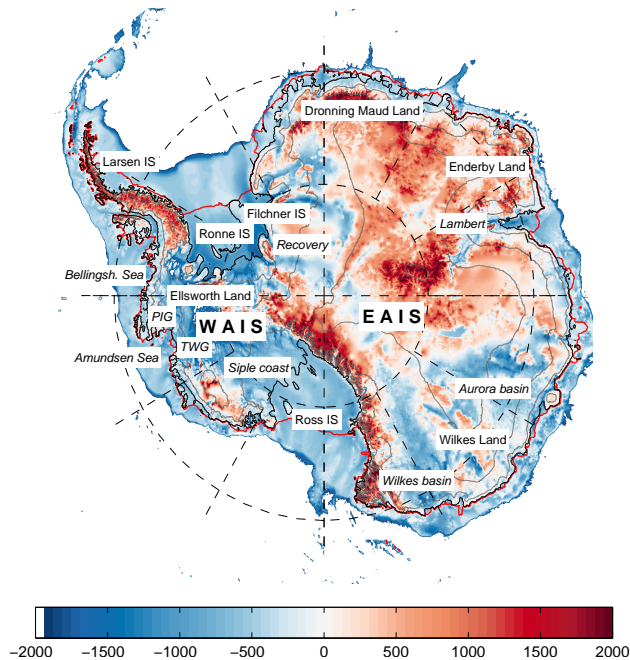


Figure 3. Bedrock topography (colour (m a.s.l.); Fretwell et al., 2013) and surface contours (grey; every 1000 m) of the Antarctic ice sheet, and ice sheet features mentioned in this paper. WAIS = West Antarctic ice sheet; EAIS = East Antarctic ice sheet; PIG = Pine Island Glacier; TWG = Thwaites Glacier; IS = ice shelf. Grounding lines are shown in black; ice shelf edges as a red line.

($A_b = 3 \times 10^{-9} \text{ m a}^{-1} \text{ Pa}^{-2}$) for the grounded ice sheet and a higher value ($A_b = 10^{-5} \text{ m a}^{-1} \text{ Pa}^{-2}$) underneath ice shelves and the ocean, to account for slippery saturated marine sediments in case of re-grounding. At intervals of Δt_{inv} years, at each grounded ice grid point, the local basal sliding coefficients $A_b(x, y)$ in Eq. (9) are adjusted by a multiplicative factor (Pollard and DeConto, 2012b):

$$5 \quad A_b^* = A_b \times 10^{\Delta z}, \quad (40)$$

where

$$\Delta z = \max \left[-1.5, \min \left(1.5, \frac{h_s - h_s^{\text{obs}}}{h_s^{\text{inv}}} \right) \right], \quad (41)$$

and where h_s^{obs} is the observed ice surface elevation and h_s^{inv} is a scaling constant. During the inversion procedure, basal temperature is still allowed to influence sliding. Adjusted $A_b^*(x, y)$ values are also not allowed to exceed $10^{-5} \text{ m a}^{-1} \text{ Pa}^{-2}$,
 10 representing the slipperiest deformable sediment. At the grounding line, observed surface velocities (Rignot et al., 2011) are

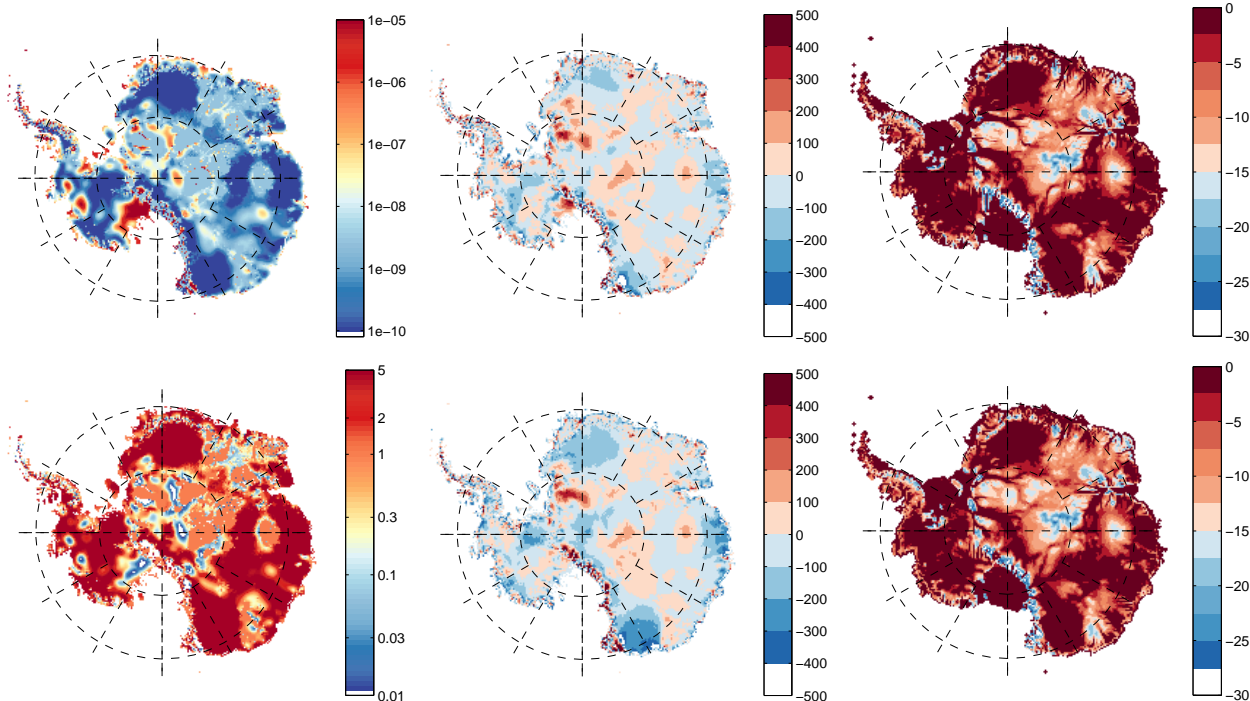


Figure 4. Top row: optimized basal sliding coefficients $A_b^*(x, y)$ after 80,000 years of integration (left); difference between optimized and observed surface elevation (center); basal temperature relative to pressure melting point (right). Bottom row: similar as top row but with optimized friction coefficients $O_b^*(x, y)$ according to the Coulomb friction law.

used to define the buttressing factors at the grounding line in the grounding-line flux condition. Values for A_b^* are only updated when $r > 0$ in Eq. (10), so that they are kept unchanged when ice is frozen to the bedrock.

In addition to Pollard and DeConto (2012b) we also introduce a regularization term that essentially smooths high-frequency noise in the basal sliding coefficients by using a Savitsky-Golay filter of degree 3, with a span of 160 km (surrounding influence matrix). The advantage of such filter is that it keeps lower-frequency variability intact while removing high-frequency noise. The filter is only applied for marine areas ($b - z_{sl} < 0$) as it improves the fit in these areas compared to the non-regularized case and guarantees a smooth transition between the inland bed and the more slippery ocean beds under present-day ice shelves.

For the Coulomb friction law, optimization starts with a constant field of $O_b = 1$. Eq. 40 then transforms to

$$O_b^* = O_b \times 10^{-\Delta z}. \quad (42)$$

10 Values of O_b are limited between 0.01 and 5 in order to keep $\tan \phi$ between physically plausible values.

Optimized basal sliding coefficients (Fig. 4) for the Antarctic ice sheet on a spatial resolution of 25 km were obtained after a forward integration of 80,000 years with $h_{inv} = 2000$ and $\Delta t_{inv} = 1000$ year. This results in a small difference (within

100 m) between the observed and the steady-state modelled topographic surface of the interior ice sheet (Fig. 4). The highest sliding coefficients are found in the marginal areas, especially in the Siple Coast sector, as well as under Pine Island and Thwaites Glaciers. Higher values are also encountered in the centre of the ice sheet, which is also obvious in other studies (Pollard and DeConto, 2012b; Bernales et al., 2016). These areas also show larger misfits (Fig. 4) and may be attributed to the

5 poor knowledge of bedrock topography, so that uncertainties are translated into a basal friction anomaly. The obtained patterns are in general agreement with the results from Pollard and DeConto (2012a, b), i.e., the largest errors are found around the major mountain ranges (e.g., Transantarctic Mountains), since outlet glaciers protruding through these mountain ranges are not well represented on coarser grid cells. However, this fit has been improved by including bedrock variability in determining basal sliding coefficients A'_b in Eq. (10) to allow for basal sliding of smaller outlet glaciers across mountain ranges.

10 The lower row of Fig. 4 displays the result for the Coulomb friction law, in combination with the grounding-line flux condition of Tsai et al. (2015). The pattern of optimized friction parameters is similar to the one obtained for Weertman sliding (but inverse, since it displays friction instead of sliding). The optimization results in a slightly larger misfit (especially near the Wilkes Basin in East Antarctica), and this may be attributed to the rather coarse approach taken here to account for the spatial distribution of subglacial water pressure and till friction angle.

15 The basal temperature fields (Fig 4) for both optimizations are quite similar and in general agreement with basal temperature fields from other Antarctic modelling studies. Differences can easily be attributed to the use of geothermal heat flow datasets, which has the largest impact on basal temperature distribution (Pattyn, 2010).

4.2 Model validation

Modelled velocities form an independent check of the model performance, since the optimized basal sliding coefficients are

20 obtained solely from the observed surface topography. The modelled flow field of the Antarctic ice sheet (Fig. 5) compares well to observations of surface velocities due to Rignot et al. (2011), such as the delineation of the different drainage basins and major ice streams discharging into the ice shelves. Some disagreement is found on glaciers discharging through the Transantarctic Mountains in the Ross ice shelf as well as glaciers near the Ellsworth Mountains discharging in the Ronne ice shelf. Those mismatches can be traced back to the difficulty in resolving those feature during the initialization process.

25 A direct comparison between the present-day velocity field (Rignot et al., 2011) and modelled velocities is shown in Fig. 5. The scatterplot shows a qualitatively good one-to-one fit for both the grounded ice sheet and the floating ice shelves. Quantitative error analysis shows a mean misfit of 11 m a^{-1} with a standard deviation of 190 m a^{-1} for the grounded ice flow, and a mean misfit of 97 m a^{-1} with a standard deviation of 1572 m a^{-1} for the floating ice shelves. The histogram comparison demonstrates a good overall fit of observed and modelled velocity magnitudes and the result is in line with other model studies

30 (e.g., Martin et al., 2011).

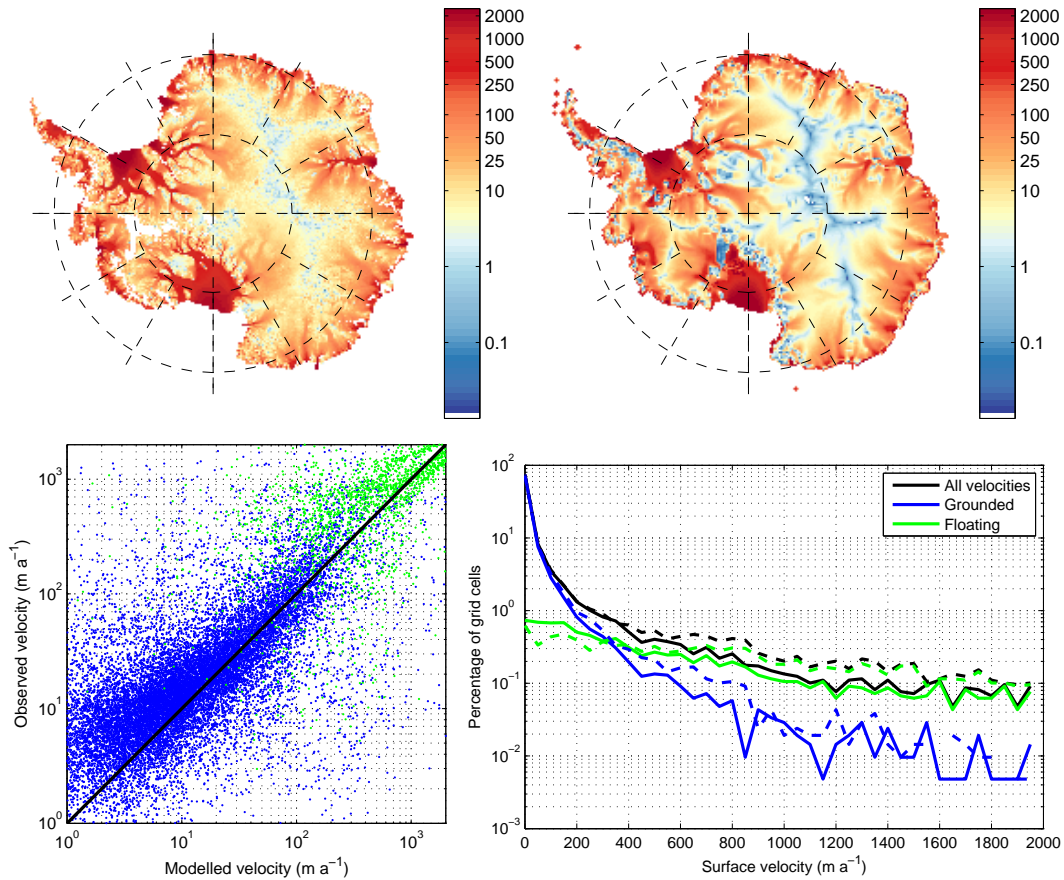


Figure 5. Observed (top left) and modelled (top right) ice sheet surface velocities after optimization; point-by-point scatterplot of modelled and observed (Rignot et al., 2011) ice sheet (blue) and ice shelf (green) velocities (bottom left); histogram of velocity distribution of observed (dashed) and modelled (solid) velocities. Each of the bins contains a velocity range of 50 m a^{-1} (bottom right).

5 Sensitivity experiments

5.1 Sensitivity to ice-shelf de-buttressing

Ice shelves are the prime gatekeepers of Antarctic continental ice discharge. The breakup of the Larsen B ice shelf (Fig. 3) and the subsequent speed-up of outlet glaciers that previously discharged into the ice shelf witness this important instability mechanism (Scambos et al., 2000, 2004). In West Antarctica, observational evidence (Rignot et al., 2014) as well as modelling studies (Favier et al., 2014; Joughin et al., 2014; Seroussi et al., 2014) show that the reduction in buttressing of ice shelves in the Amundsen Sea embayment may lead to significant inland ice mass loss, and that unstoppable retreat of the grounding line of Thwaites Glacier may already be on its way (Joughin et al., 2014).

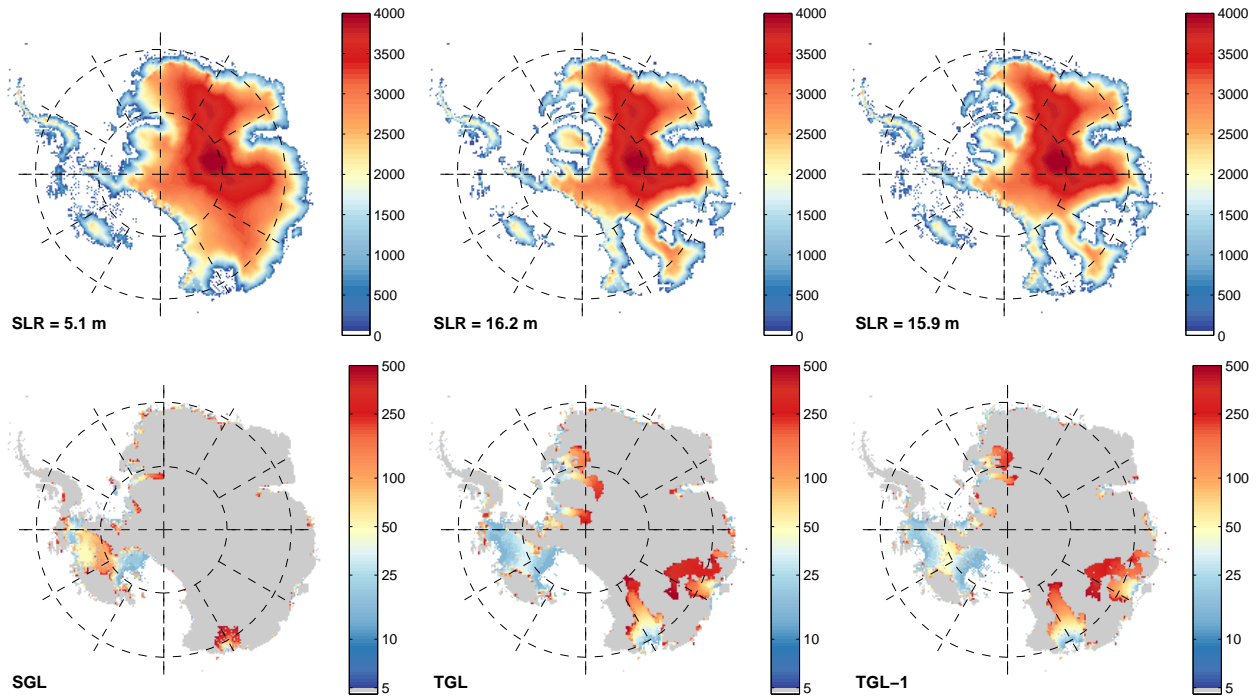


Figure 6. Top: Grounded ice sheet surface elevation (m a.s.l.), 500 years after sudden removal of all ice shelves. Bottom: grounding-line position in time according to the same experiment (colour scale is nonlinear and represents time in years) for the Weertman sliding law with SGL condition (left), Coulomb friction law with TGL condition (center), and Weertman sliding law with TGL condition (right). SLR denotes the contribution to sea level rise after 500 years.

Since ice shelf buttressing is a key element in the stability of the Antarctic ice sheet, a useful experiment to understand underlying model buttressing physics is the sudden removal of all floating ice shelves, starting from the initialized model state, and to let the model evolve over time. Over this period ice shelves were not allowed to regrow, which is equivalent to removing all floating ice at each time step. This experiment is carried out for three cases, i.e., (i) power-law sliding with the flux condition according to Schoof (2007a) (SGL), (ii) Coulomb friction with flux condition according to Tsai et al. (2015) (TGL), and (iii) power-law sliding with the TGL condition (TGL-1). All experiments result in a sudden ice-mass loss and grounding-line retreat, whereby the West Antarctic ice sheet collapses entirely in less than 200 years according to SGL and less than 100 years according to TGL, respectively (Fig. 6). Both TGL experiments lead to a similar mass loss (both in terms of timing and volume). Therefore, the decisive factor governing mass changes is the grounding-line flux condition and not the sliding/friction law that is employed for the grounded ice sheet.

For all experiments, grounding-line retreat starts in the marine sections discharging in the Ronne and Ross ice shelves. For the SGL experiment, the retreat from Ellsworth Land leads to thinning in the inland sectors of the Pine Island basin, which after >50 years triggers grounding-line retreat from Pine Island Glacier and subsequently Thwaites Glacier. Grounding-line

retreat then spreads rapidly towards the Ross sector of the West Antarctic ice sheet, leading to a complete disintegration of the ice sheet within 150 years. However, for both TGL experiments, initial grounding-line retreat also occurs in the Amundsen Sea sector, whereby the retreat is much faster and the ice sheet collapses within less than 100 years. Another major difference between SGL and TGL experiments is that the total SLR contribution for TGL is three times as large compared to SGL, i.e.,
5 ~ 16 m for TGL compared to ~ 5 m for SGL after 500 years. The extra mass loss is essentially located in the East Antarctic ice sheet, i.e., Wilkes and Aurora basins (Wilkes Land; Fig. 3), both losing substantial amounts of ice. Despite the presence of a sill at the outlet of Wilkes subglacial basin, grounding-line retreat occurs without invoking any other physical mechanism than the flux condition at the grounding line in combination with complete ice shelf collapse. These results contrast with Mengel and Levermann (2014) who require the removal of a specific coastal ice volume equivalent to 80 mm of SLR in order
10 to provoke an unstable grounding-line retreat within Wilkes basin.

The higher TGL grounding-line sensitivity must be sought in its underlying physics: at the grounding line the basal shear stress vanishes in a smooth way to reach zero exactly at the grounding line. As shown by Tsai et al. (2015), this is not the case for the SGL algorithm, where a sharp contrast between the inland non-zero basal shear stress and the ocean exists. This boundary becomes smoother with larger sliding velocities, leading to a larger transition zone (Pattyn et al., 2006; Gladstone et al.,
15 2012; Feldmann et al., 2014), but the transition jump does not vanish. The SGL condition at the grounding line is therefore a function of the friction coefficient A_b , while the TGL condition is related to a single parameter in the friction law, i.e., the till friction angle. The latter is also limited in its range, contrary to A_b ranging across several order of magnitude (from saturated till to nearly frozen bedrock). Furthermore, the TGL condition is a function of ice thickness h to a higher power compared to SGL. Since the TGL ice flux is larger than the SGL flux for similar conditions, the surface gradient at the grounding line is
20 generally higher, hence leading to higher driving stresses. These steeper surface slopes make the grounding line to retreat (and advance) more rapidly than with the power-law condition (SGL). The higher sensitivity for TSL is also demonstrated in the modified MISMIP experiments (Appendix C). Additionally, I carried out a series of sensitivity tests by fixing the value of the till friction angle at the grounding line ϕ , ranging from 10 to 60°. Only for $\phi \geq 50^\circ$ did the sensitivity decrease, but the amount of mass loss was still significantly higher than with the SGL condition.

25 5.2 Sensitivity to sub-shelf melt

Antarctic ice sheet sensitivity to sub-shelf melting is investigated with a multi-parameter/multi-resolution forcing ensemble over a period of 500 years. Atmospheric forcing includes changes in background temperature ΔT , ranging from 0 to +8.5°C, affecting both surface temperature, Eq. (37), and surface mass balance, Eq. (38), through the mass balance–elevation feedback. Surface melt is calculated with the PDD model, Eq. (39). Ocean forcing is based on constant forcing values of sub-shelf melting
30 ΔM , ranging from 0 to 50 m a⁻¹ underneath the freely floating ice shelves surrounding the Antarctic ice sheet, and between 0 and 6.25 m a⁻¹ for the Ronne-Filchner and Ross ice shelves (factor 8 less compared to the freely-floating ice shelves). Melting is only applied to fully floating grid cells, without taking into account the fractional area of grounded grid points that are actually afloat, as done in a few studies (Feldmann et al., 2014; Golledge et al., 2015). All forcings are applied as a sudden change in temperature/melt rate starting from the initialized model. A background run (without applying the forcing

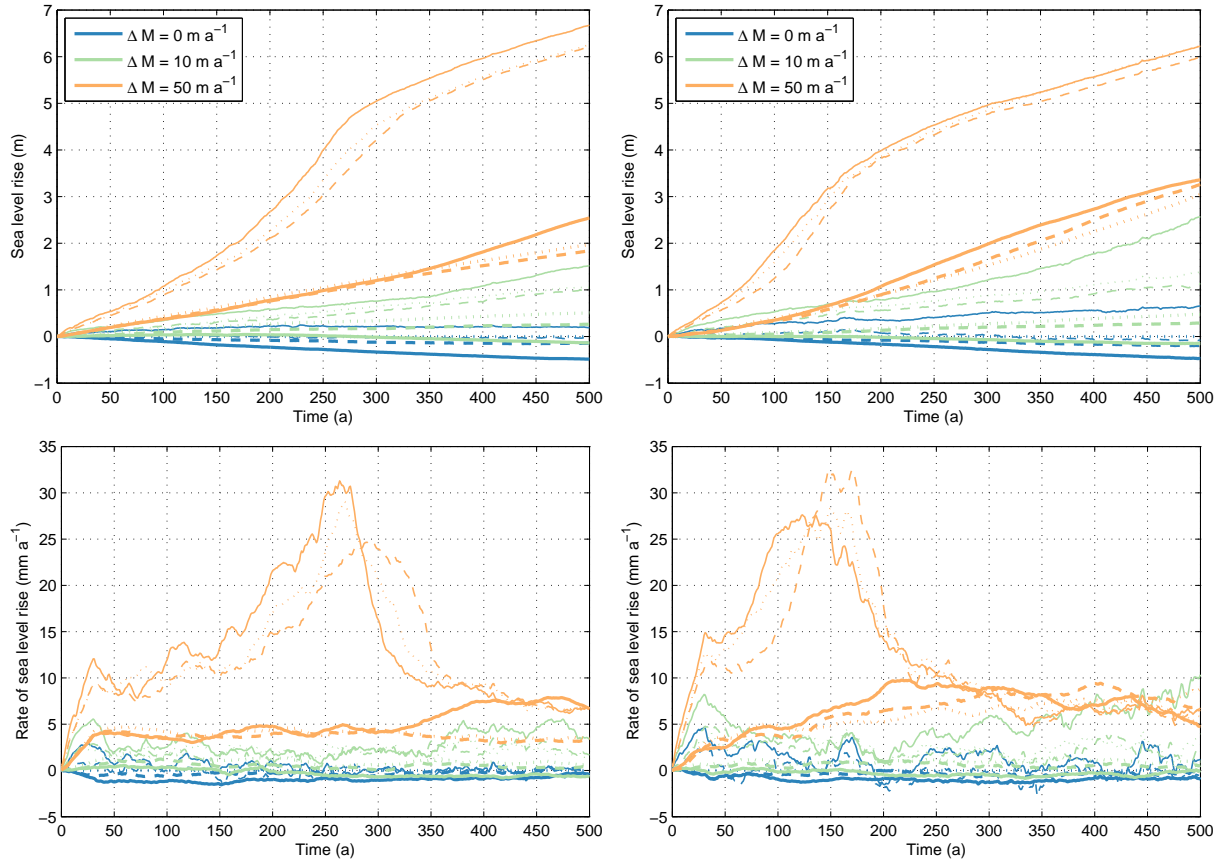


Figure 7. Evolution of sea-level contribution (top) and rate of sea-level rise (bottom) as a function of basal melting underneath ice shelves and background temperature change for the 25 km (left) and 40 km (right) spatial resolutions. Atmospheric temperature forcing is as follows: 0°C (dotted), 2.2°C (dashed), and 8.5°C (solid line). The thick lines correspond to the SGL grounding-line flux, while the thin lines correspond to the TGL flux.

anomaly) is also performed to determine the model drift on the different time scales. The experiments are run for different combinations of sudden changes in background temperature/basal melting rate underneath the ice shelves on a grid size of $\Delta = 25$ km (as well as on a $\Delta = 40$ km grid to test grid-size dependence). A few runs are performed on a grid size of $\Delta = 16$ km for comparison.

5 Sea-level contribution according to the forcing experiments and rate of change of sea level for the $\Delta = 25, 40$ km spatial resolutions are shown in Fig. 7. These are determined from the change in ice volume above floatation (Bindschadler et al., 2013; Nowicki et al., 2013). SLR according to the forcings ranges between -0.5 and 7 m after 500 years. It increases with increasing sub-shelf melt rates and slightly decreases with increasing atmospheric temperature forcing. The latter is due to higher precipitation rates in a warmer climate, leading to an increase in grounded ice mass. However, for larger atmospheric
10 forcing ($+8.5^{\circ}\text{C}$), mass loss is generally enhanced due to the dominance of surface melt and/or increase in ice flux with increased precipitation rates. The different curves in Fig. 7 are clustered according to sub-shelf melt rate, which is the most decisive process governing mass loss. Atmospheric forcing, however, has only a limited effect, probably because the time scale considered (500 years) is too short to relax the ice sheet to the imposed temperature and precipitation changes, and because weakening of ice shelves through hydro-fracturing is not taken into account. Model drift (zero forcing anomaly) is between 60
15 and 75 cm of sea level lowering over a period of 500 years, or 0.2–0.3% of the total Antarctic ice sheet volume per Century. This is comparable to other Antarctic model studies (e.g., Nowicki et al., 2013) and shows that the initialization is rather stable and close to steady-state.

The major differences in sea-level response are due to the treatment of grounding-line fluxes. As shown above, the TGL flux condition systematically leads to significant higher mass losses, making grounding-line migration a more sensitive process
20 (Sect. 5.1). The higher sensitivity leads to a rate of change in sea level of up to 30 mm a^{-1} . These high values correspond to periods when the marine ice sheet runs into a major instability (MISI). Note, however, that such rates are still significantly lower than those obtained during the ice-shelf removal experiment. For the SGL flux condition, these values are half as much, and major MISIs occur generally at a later stage during the model run. Compared to other studies (Golledge et al., 2015; Ritz et al., 2015; DeConto and Pollard, 2016), the TGL flux conditions puts sea-level contributions at the high end of the spectrum.

25 Only the higher melt-rate scenarios ($>10 \text{ m a}^{-1}$) produce significant MISIs over this time period. They first occur in the West Antarctic ice sheet (WAIS), starting from either Pine Island or Thwaites Glacier, progressing inland. Other MISI-prone areas are the Bellingshausen Sea (WAIS) and Wilkes basin (East Antarctic ice sheet – EAIS). Contrary to the de-buttressing experiment in Sect. 5.1, MISIs are not initially triggered in the Siple Coast area, nor through Ellsworth Land. This is probably due to the lower imposed melt rates, so that both Ronne and Ross ice shelves remain buttressed for a longer period of time.

30 The effect of spatial resolution on model result is summarized in Fig. 8 in addition to the data presented in Fig. 7. Coarser resolutions (40 km) give comparable results to the 25 km grid, especially for zero melt forcing and the highest melt forcing according to Coulomb-TGL. Those cases correspond to either absence of MISIs (low SLR) or complete disintegration of WAIS (high SLR). The main reason for this relatively good fit must be sought in the grounding line flux conditions (SGL and TGL) that make the model resolution-independent. Models that are not based on such heuristics have to resolve grounding
35 line migration at sub-kilometre resolutions (Pattyn et al., 2013; Pattyn and Durand, 2013). Differences in response (medium

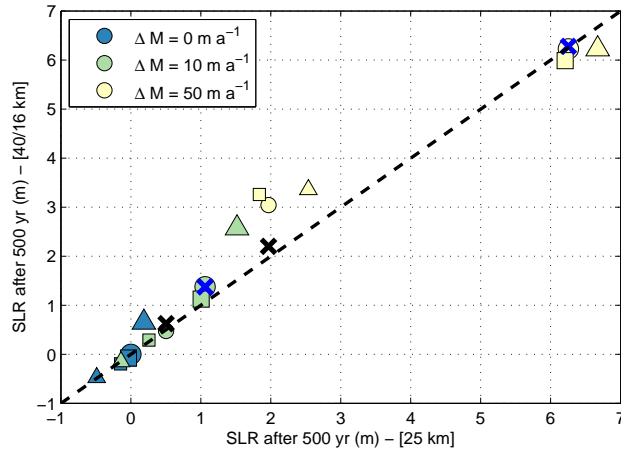


Figure 8. Comparison of sea-level contribution after 500 years as a function of model resolution (25 vs 40 km). Colours denote sub-shelf melt rates; shapes represent background temperature forcing: 0°C (circles), 2.2°C (squares), 8.5°C (triangles). Small markers denote the Weertman-SGL, while large markers Coulomb-TGL. Crosses are the comparison between 25 (x-axis) and 16 km (y-axis) for experiments without atmospheric forcing (only melt); Black = Weertman-SGL; Blue = Coulomb-TGL.

scenarios) are due to the precise timing of MISIs, that seems to be resolution dependent and some of the MISIs are not completed after 500 years (Fig. 7). However, a spatial resolution of 40 km generally remains to coarse, and results are much improved at 25 km. This is demonstrated by the comparison of 16 km to 25 km resolution for which obtained SLR is almost the same (crosses in Fig. 8), even for the medium scenarios. Nevertheless, it is expected that at very high spatial resolutions (<5 km), grounding-line retreat is influenced by bedrock irregularities as well as the presence of ice-shelf pinning points that are not always properly resolved at coarser resolutions. The parametrization of sub-grid processes, such as basal sliding in mountainous areas and sub-shelf pinning at sub-grid level, have to some extent reduced this dependency in the model, but differences remain.

In order to validate this claim, two more experiments were carried out to make comparison with an existing experimental result at high resolution possible (Cornford et al., 2016). Here, sub-shelf melting is taken as a function of ice thickness (Cornford et al., 2016), i.e.,¹

$$M = \max \left[\min \left(\frac{4}{7}(H - 100), 400 \right), 0 \right]. \quad (43)$$

It limits the melt rate between zero (for ice shelves thinner than 100 m) and 400 m a⁻¹ (for ice shelves thicker than 800 m). Results are shown in Fig. 9. The total contribution to SLR after 500 years in the SGL experiment (3.9 m) is comparable to the finest mesh experiment in Cornford et al. (2016). As expected, the TGL experiment gives a much higher mass loss due to its

¹In Cornford et al. (2016), the applied melt rate differs from its definition in the text; the correct melt rate is given in Eq. 43 (S. Cornford, personal communication, 2017).

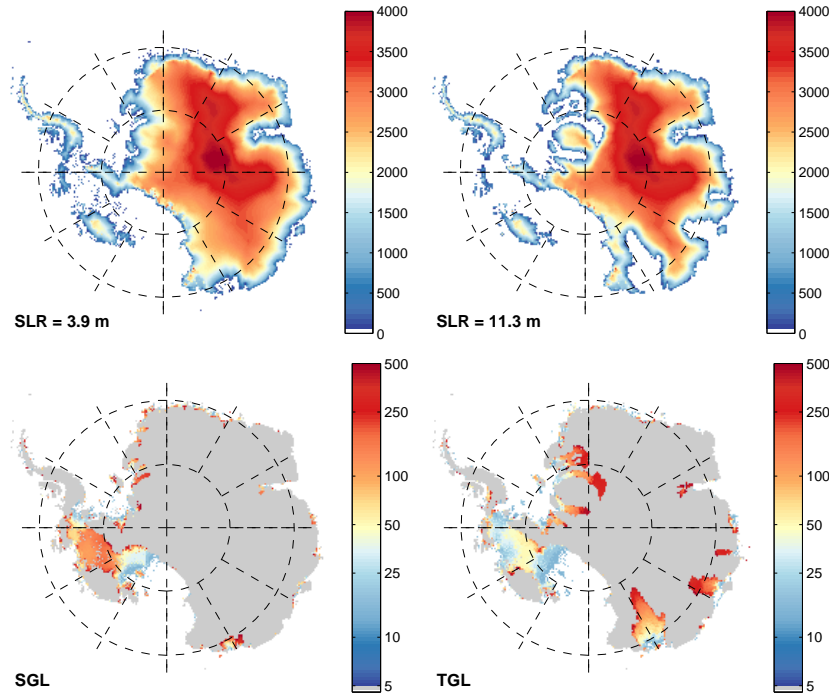


Figure 9. Top: grounded ice sheet surface elevation (m a.s.l.), 500 years after applying melt rates of Cornford et al. (2016). Bottom: grounding-line position in time according to the same experiment (colour scale is nonlinear and represents time in years) for the Weertman sliding law with SGL condition (left) and Coulomb friction law with TGL condition.

inherent physics. Differences between the model response are sought in the timing of grounding-line retreat within particular drainage basins. For instance, the grounding line in the SGL experiment starts to retreat in the Siple Coast, Ellsworth Land and PIG (as in Cornford et al., 2016), while TWG kicks in at a later time. However, for the TGL experiment, both PIG and TWG retreat at about the same time at the start of the model run. Such differences in response are to be expected, since both
 5 experiments are run on a much coarser resolution (25 km) than in Cornford et al. (2016), hence a different basal topography.

6 Discussion

In terms of model complexity, the f.ETISH model is comparable to the Pollard and DeConto (2012a) model. The major difference lies in a number of simplifications that makes the f.ETISH model two-dimensional. This is obtained by approximating the temperature coupling by relating the mean ice-column temperature to the velocity field via the commonly-used Arrhenius
 10 relationship (Cuffey and Paterson, 2010). Another major difference pertains to the marine boundary, with the implementation of the grounding-line flux condition according to Tsai et al. (2015), based on a Coulomb friction law (TGL), further extended with a Coulomb friction law for the interior ice sheet. Finally, model initialization based on Pollard and DeConto (2012b) has

been further extended with a regularization term that essentially smooths the basal friction field across marine basins and makes the results independent of spatial resolution, since regularization is made a function of horizontal distance instead of number of grid cells. Moreover, the optimization does not involve an optimization of ice-shelf basal mass balance, since observed ice-shelf velocities are used to determine the amount of buttressing at the grounding line. The resulting initialization is characterized by a small drift once the grounding line is allowed to relax, of the order of 0.2–0.3% of the ice sheet volume in 100 years. Other marine elements such as hydro-fracture and cliff failure (Pollard et al., 2015; DeConto and Pollard, 2016) are not taken into account.

Given the differences in approach with continental-scale ice-sheet models, such as AISM-VUB (Huybrechts, 1990, 2002), ANICE (de Boer et al., 2013), GRISLI (Ritz et al., 2015), ISSM (Larour et al., 2012), PISM (Bueler and Brown, 2009), PISM-PIK (Martin et al., 2011; Winkelmann et al., 2011; Gollledge et al., 2015), PSU-ISM (Pollard and DeConto, 2012a), RIMBAY (Thoma et al., 2014), or SICOPOLIS (Sato and Greve, 2012), verification of the f.ETISh model requires a detailed comparison with existing benchmarks. These are generally based on results of the models cited above. The EISMINT-I benchmark (Huybrechts et al., 1996) shows that the ice-dynamical characteristics of f.ETISh are in very close agreement with the benchmarks shown in Appendix A, despite a different numerical solution scheme. The basal temperature field is also in close agreement. The results of thermomechanical coupling of ice sheet flow is also in good agreement with the EISMINT-II benchmark (Payne et al., 2000), albeit that the range of uncertainty between the different participating models on which the benchmark is based is also much larger.

An important experiment for marine ice sheet models is a test of steady-state grounding-line positions in absence of buttressing (Pattyn et al., 2012). Boundary layer theory indeed predicts that unique grounding line positions exist on a downward sloping bed, while no stable solutions are found on reversed bed slopes (Schoof, 2007a), unless buttressing is significant (Gudmundsson et al., 2012). While the experiments are designed for flowline models, they can be extended to two dimensions to evaluate the behaviour in a qualitative way. Here, the f.ETISh model successfully passes the test independent of model resolution, as grounding-line migration is governed through a heuristic based on the above-mentioned boundary layer theory (Pollard and DeConto, 2009, 2012a) and is extended with a heuristic based on Tsai et al. (2015), that qualitatively gives the same results.

The main advantage of using a grounding-line flux parametrization based on a heuristic rule (Sect. 2.1.6) is that the model can be run at lower spatial resolutions, which is confirmed by the f.ETISh model experiments in Sect. 5.2. Solving the force balance around the grounding line requires membrane stresses at both sides of the grounding line to be resolved with sufficient detail (Schoof, 2007a), which requires the use of sub-kilometre grid sizes (Pattyn et al., 2012), unless sub-grid grounding-line parametrizations are used that may allow for larger grid sizes (Feldmann et al., 2014; Cornford et al., 2016). The main disadvantage of the heuristic rule is that its parametrization is derived from a steady-state solution based on the SSA model. It can therefore be questioned whether the formulation still holds for transients. It also overrules the hybrid model at this particular location.

A major finding in this paper is the increased sensitivity of the grounding line based on a Coulomb friction law (Tsai et al., 2015), compared to a power-law sliding condition at the grounding line. Power-law sliding mechanisms near grounding lines

have been extensively discussed, since they lead to sudden jumps in basal drag at the grounding line, especially at relatively low sliding speeds (such as in the MISMIP and MISMIP3d experiments Pattyn et al., 2012, 2013). However, sliding velocities in the Antarctic experiments are not preconditioned by a specific sliding coefficient at the grounding line, but determined from the optimization procedure. Therefore, the type of boundary is controlled by the model physics itself. The Coulomb friction condition at the grounding line is consistent with observations, as the ice-sheet profiles ‘taper off’ towards a flattening upper surface, contrary to the power-law case, and basal stresses vanish at the grounding line (Tsai et al., 2015). Moreover, the grounding-line ice flux according to Coulomb friction also depends more strongly on floatation ice thickness, implying higher sensitivity to atmospheric and ocean forcing. Furthermore, grounding is facilitated in shallower water compared to the power-law case, so that smaller perturbations may push the grounding line more easily into regions with a retrograde slope, provoking a grounding-line instability (Tsai et al., 2015). As a result of the higher sensitivity, Antarctic sea-level contribution to a given perturbation is also more than twice as high and rates of sea-level change three times as fast compared to a power-law sliding case.

Direct comparison is not possible with recent studies of Antarctic ice mass loss that are forced by atmosphere-ocean models following so-called RCPs (Representative Concentration Pathways). Direct comparison with the SeaRISE experiments (Bindschadler et al., 2013; Nowicki et al., 2013) is also hampered due to the lower melt rates applied to the Ross and Ronne-Filchner ice shelves. This differentiation was deliberately chosen, as the de-buttressing experiments show that the highest buttressing stems from those large ice shelves. However, their grounding lines are also farthest from the continental shelf break, hampering the intrusion of warmer waters compared to the smaller ice shelves that are closer to the edge. However, considering the f.ETISH model with the SGL condition comparable to the PSU-ISM model (Pollard and DeConto, 2009, 2012a), some comparison on sensitivity can be made. For the SeaRISE experiments, the PSU-ISM model predicts a sea-level contribution after 500 years according to a $2 \times$ A1B scenario (without sub-shelf melting) of ~ 0.45 m, while the f.ETISH SGL model results in ~ 0.4 m for similar forcing conditions. One has to note, however, that the initialization of both models is different (spinup versus optimization).

However, the TGL model is less sensitive than the PSU-ISM model including cliff failure and hydrofracturing (DeConto and Pollard, 2016). These processes potentially lead to a sea level contribution of 12-13 m after 500 years under a RCP8.5 scenario forced by atmosphere/ocean models. This result corresponds well with the results of the f.ETISH TGL model under complete de-buttressing (without ice-shelf growth), with complete collapse of the West Antarctic ice sheet and major ice loss in the Wilkes and Aurora basins (Fig. 6).

Finally, computational time of f.ETISH largely depends on the spatial resolution, which also governs time steps needed under the CFL condition. A hybrid-model 5000 year run with a grid size of 40 km and a time step of 0.2 year takes approximately 10,000 CPU seconds on a single AMD Opteron 2378 2.4 GHz core of the Hydra cluster (VUB-ULB) and 20,000 CPU seconds for a 500 year run with a grid size of 16 km and time step of 0.02 years on a multicore. Future developments will focus on improving the numerical solution schemes in order to reduce the calculation time (larger time steps), especially at higher spatial resolutions.

7 Conclusions

I developed a new marine ice sheet model, based on common descriptions of ice physics (combined shallow-ice and shallow-shelf approximation) and novel implementation of parametrizations of thermodynamics and grounding line migration. The model has been extensively tested against existing benchmarks and has been shown to be scale-independent, with the exception
5 of grounding zones with small-scale bedrock variability, where grounding-line response to atmospheric and oceanic forcing is sensitive to spatial resolution. This makes the model extremely attractive to couple within Earth System models.

The model has been initialized to the present-day Antarctic ice sheet conditions in order to obtain initial steady-state conditions as close as possible to the observed ice sheet. Independent validation has been obtained through comparison with observed surface velocities that are not utilised during the optimization phase.

10 Two forcing experiments over a period of 500 years are carried out, one during which all floating ice shelves are removed, and one during which sudden atmospheric and oceanic forcing is applied. Both experiments show a very high sensitivity to grounding-line conditions, as Coulomb friction in the grounding-line transition zone leads to significantly higher mass loss in both West and East Antarctica, compared to commonly-used power-law sliding laws (such as Weertman-type). For the ice-shelf removal experiment this leads to 5 m and 16 m SLR for the power-law basal sliding and Coulomb friction conditions at the
15 grounding line, respectively. This high-end response is of the same order of magnitude as obtained by DeConto and Pollard (2016) using ice-shelf debuttressing caused by hydro-fracture and cliff failure.

The atmospheric/oceanic forcing experiments clearly show the dominance of ocean forcing in sea-level response, where significant MISIs (Marine Ice Sheet Instabilities) occur under relatively mild sub-shelf melt scenarios over centennial time scales (500 years).

20 8 Data availability

All datasets used in this paper are publicly available, such as Bedmap2 (Fretwell et al., 2013) and geothermal heat flow data (Purucker, 2013). Results of the RACMO2 model were kindly provided by Melchior Van Wessem.

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Exp	Variable	Benchmark	f.ETISH
FM	h_{summit}	3419.90 ± 1.70	3421.82
	q_{midpoint}	789.95 ± 1.83	790.43
	T_{summit}^b	-8.84 ± 1.04	-7.54
MM	h_{summit}	2997.5 ± 7.4	2986.41
	q_{midpoint}	999.24 ± 17.91	994.49
	T_{summit}^b	-13.43 ± 0.75	-11.81

Table A1. Comparison of f.ETISH with the EISMINT-I fixed (FM) and moving margin (MM) experiment benchmark based on an ensemble of 2–3 models (Huybrechts et al., 1996) for the steady-state experiment.

Appendix A: EISMINT-I benchmark

A1 Fixed-margin experiment

The EISMINT-I benchmark is the first series of ice-sheet model intercomparisons aiming at benchmarking large-scale ice sheet models under idealized and controlled conditions (Huybrechts et al., 1996). The first (fixed margin) experiment considers a square grid of 1500×1500 km with a flat bed at zero elevation. Grid spacing is taken as $\Delta = 50$ km leading to 31×31 regularly-spaced grid points. Starting from zero ice thickness, the model is forced with a constant surface mass balance of 0.3 m a^{-1} and surface temperature according to $T_s = 239 \text{ K} + (8 \times 10^{-8})d_{\text{summit}}^3$, where d_{summit} is defined as $\max(|x - x_{\text{summit}}|, |y - y_{\text{summit}}|)$, expressed in km. Further boundary conditions for the model are zero ice thickness at the edges of the domain and a constant geothermal heat flux of $G = 0.042 \text{ W m}^{-2}$. The ice temperature is not coupled to the ice flow field and a constant value for the flow parameter of $10^{16} \text{ Pa}^{-n} \text{ a}^{-1}$ is considered.

The f.ETISH model is a 3d Type I model according to the classification scheme in EISMINT-I, i.e., diffusion coefficients for the grounded ice sheet are calculated on a staggered Arakawa-B grid. Table A1 lists the comparison with data from other 3d Type I models. Both ice thickness and flux compare very well within error bounds of the sample range (limited to only 2–3 models in the EISMINT-I benchmark, unfortunately). Also the basal temperature at the divide and along the profile is within the limits given by the EISMINT-I benchmark. Differences can be attributed to the use of the shape functions for the velocity field as well as to the use of a staggered grid for the temperature field, whereby the temperature at the divide and along the profile are interpolated values along the central line.

A2 Moving margin experiment

The moving-margin experiment includes ice ablation, hence the presence of an equilibrium line on the ice sheet. This is obtained by defining the climatic conditions by $\dot{a} = \min\{0.5, h_s(R_{\text{el}} - d_{\text{summit}})\}$ and $T_s = 270 - 0.01h$, where d_{summit} is here defined as the radial distance from the centre (in km), and s and R_{el} are $10^{-2} \text{ m a}^{-1} \text{ km}^{-1}$ and 450 km, respectively (Huybrechts et al., 1996). The steady-state ice sheet according to this experiment does not reach the edge of the domain, but is

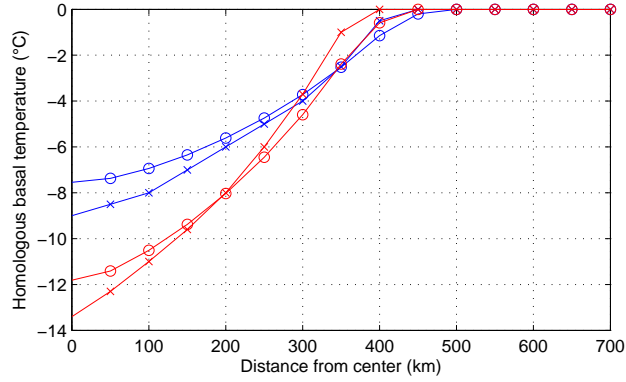


Figure A1. Homologous basal temperatures along the central line according to the EISMINT-I experiment calculated with f.ETISh (circles) and according to the EISMINT-I benchmark (crosses) for the fixed margin (blue) and moving margin (red) experiment.

circular in shape. Note that, contrary to the fixed margin experiment, surface temperature is a function of surface elevation and not of the geometrical characteristics of the domain. Surface mass balance, however, remains a function of the distance to the centre of the domain.

Basic characteristics of the experiment are listed in Table A1, and simulated values of ice thickness (h_{summit}) and basal temperature at the divide (T_{summit}^b), as well as ice flux between divide and margin are in good agreement with the benchmark. Also the basal temperature profile agrees well with the benchmark and differences can be attributed to the factors listed in Appendix A1.

A3 Transient experiment

Temporal changes in ice thickness/volume and basal temperature are analysed with a forcing experiment, where the surface temperature and mass balance perturbations are defined as follows (Huybrechts et al., 1996):

$$\Delta T = 10 \sin\left(\frac{2\pi t}{T}\right), \quad (\text{A1})$$

$$\Delta \dot{a} = 0.2 \sin\left(\frac{2\pi t}{T}\right) \quad \text{for fixed margin,} \quad (\text{A2})$$

$$\Delta R_{\text{el}} = 100 \sin\left(\frac{2\pi t}{T}\right) \quad \text{for moving margin.} \quad (\text{A3})$$

The model run starts from the steady-state ice sheet obtained in the previous section and the forcing is applied for a period of 200 ka, with a periodicity of $T = 20$ and 40 ka, respectively. Results are depicted in Fig. A2 for the fixed margin and in Fig. A3 for the moving margin experiment. Table A2 lists the main characteristics of ice thickness and basal temperature amplitude variations, as well as ice thickness at the divide at the end of the experiment (200 ka).

Exp	Variable	Benchmark	f.ETISH
FM 20ka	h_{summit} (200 ka)	3264.8 ± 5.6	3266.02
	Δh_{summit}	563.0 ± 3.7	566.20
	$\Delta T_{\text{summit}}^b$	2.11 ± 0.09	2.67
FM 40ka	h_{summit} (200 ka)	3341.7 ± 3.9	3344.51
	Δh_{summit}	619.0 ± 3.2	621.53
	$\Delta T_{\text{summit}}^b$	4.12 ± 0.06	2.79
MM 20ka	h_{summit} (200 ka)	2813.5 ± 2.0	2805.19
	Δh_{summit}	528.6 ± 11.3	533.66
	$\Delta T_{\text{summit}}^b$	2.54 ± 0.00	0.95
MM 40ka	h_{summit} (200 ka)	2872.5 ± 6.8	2871.85
	Δh_{summit}	591.4 ± 4.6	595.38
	$\Delta T_{\text{summit}}^b$	7.61 ± 0.05	6.51

Table A2. Comparison of f.ETISH with the EISMINT-I fixed (FM) and moving margin (MM) experiment benchmark based on an ensemble of 2–3 models (Huybrechts et al., 1996) for the forcing experiments with a sinusoidal signal of 20 and 40 ka, respectively. Bold values are those outside the range given by the benchmark results.

All ice thickness changes (amplitude and phase) as well as the phase in temperature according to the two forcing scenarios are in close agreement with the benchmark. However, amplitude differences for the basal temperatures deviate, but the EISMINT I data sample is rather limited for comparison. The phase of the basal temperature response is in agreement with the benchmark. All other parameters are within the bounds of the benchmark (Table A2).

5 Appendix B: EISMINT-II benchmark

The EISMINT-II benchmark (Payne et al., 2000) is based on the moving margin experiment of Huybrechts et al. (1996), but includes thermomechanical coupling of the ice flow to the temperature field. Contrary to the EISMINT-I benchmark, inter-model differences are considerably larger, especially with respect to the area of the ice sheet that reaches pressure melting point at the base. The standard experiment consists of a flat bed of the same size as the EISMINT-I benchmark, but with a spatial resolution of 25 km, leading to 61×61 grid points. The basic experiment (A in Payne et al., 2000) runs the ice sheet in equilibrium starting from zero ice thickness on the domain and with $u_b = 0$. The climatic conditions are defined as:

$$\dot{a} = \min \{ \dot{a}_{\text{max}}, s(R_{\text{el}} - d_{\text{summit}}) \} \quad (\text{B1})$$

$$T_s = T_{\text{min}} + s_T d_{\text{summit}}, \quad (\text{B2})$$

where d_{summit} is defined as in the moving margin experiment as the radial distance from the centre (in km), s and R_{el} are taken as in the moving margin experiment ($10^{-2} \text{ m a}^{-1} \text{ km}^{-1}$ and 450 km, respectively), and \dot{a}_{max} , T_{min} and s_T are defined as

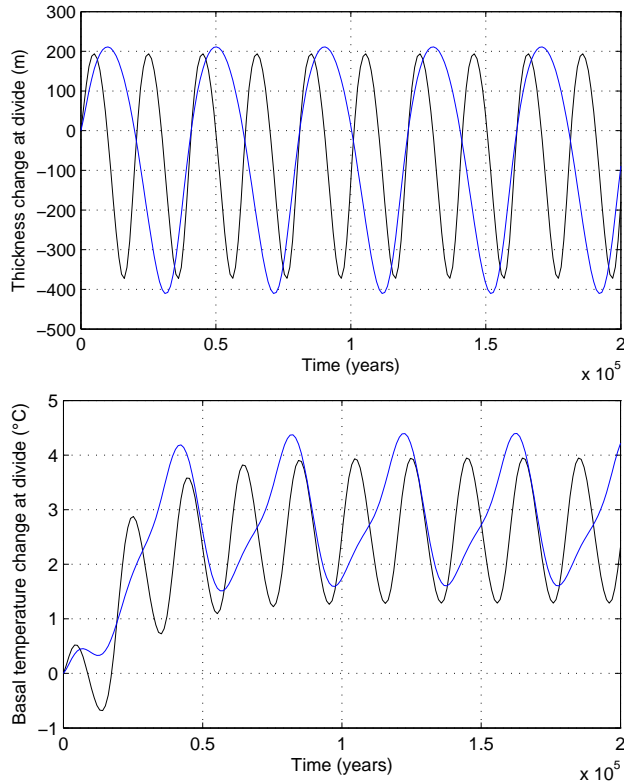


Figure A2. Ice thickness and basal temperature variations for the EISMINT-I fixed margin experiment with a 20 ka (black) and a 40 ka (blue) forcing.

0.5 m a^{-1} , 238.15K , and $1.67 \times 10^{-2} \text{ K km}^{-1}$, respectively. Contrary to the moving margin experiment, climatic conditions are independent of ice sheet surface elevation, hence the mass-balance elevation feedback is excluded.

- Six further experiments were carried out, i.e., experiment B, C, D, F, G and H (in Payne et al., 2000). They consist of a stepwise change in surface temperature, $T_{\min} = 243.15\text{K}$ (B), a stepwise change in surface mass balance $\dot{a}_{\max} = 0.25$, $R_{\text{el}} = 425 \text{ km}$ (C) and a stepwise shift in equilibrium-line altitude $R_{\text{el}} = 425 \text{ km}$. Experiments B, C and D start from the steady-state solution of A. Experiment F is similar to A, but starting with a value of $T_{\min} = 223.15\text{K}$ (model run starting without ice). Experiment G incorporates basal slip according to a linear sliding law ($m = 1$ and $A_b = 10^{-3} \text{ m a}^{-1} \text{ Pa}^{-1}$) with a similar setup as A. Finally, experiment H is similar to G, but where sliding is limited to areas that are at pressure melting at the base.
- 10 Results for experiments A–H are summarized in Table A3. The majority of parameters are within the bounds of the benchmark, but major differences are related to the basal temperature at the divide. All experiments exhibit a radial pattern in basal temperatures that are at pressure melting point for the outer part of the ice sheet, with a cold spike in the center of the ice sheet. In all experiments, our temperature spike is slightly less cold than the one given by the benchmark. However, despite

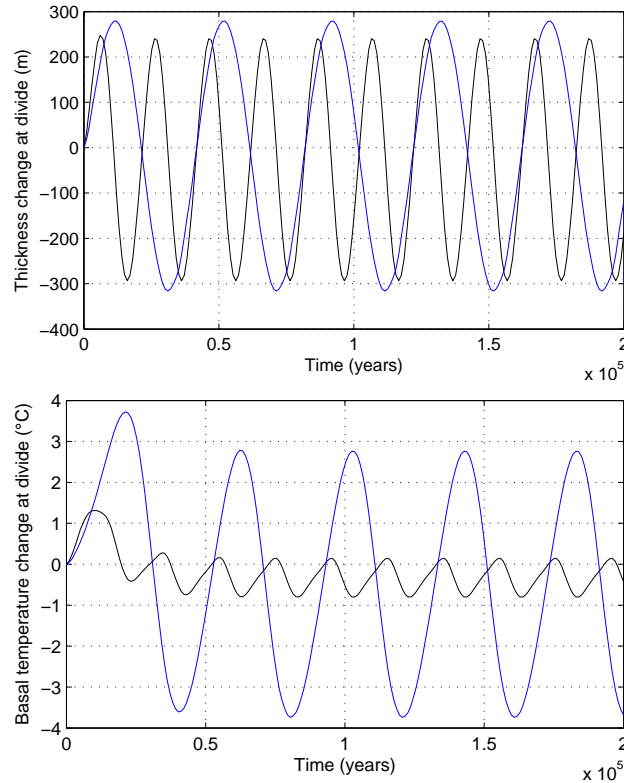


Figure A3. Ice thickness and basal temperature variations for the EISMINT-I moving margin experiment with a 20 ka (black) and a 40 ka (blue) forcing.

this difference, the size of the basal area at pressure melting point is in accord with the benchmark. Again, the main reason for this difference is that temperatures in f.ETISh are calculated on a staggered Arakawa-B grid and not exactly at the ice divide. Despite these differences in temperature, ice volume and area coverage are totally in agreement with the benchmark mean.

The emblematic experiments F and H in Payne et al. (2000) displayed an irregular pattern in the basal temperatures of the benchmark for all participating models, leading to cold spikes reaching to the edge of the ice sheet. The pattern was shown to be model-dependent and further investigations traced its origin to an interaction between vertical advection (cooling down the base) and strain heating (Hulton and Mineter, 2000). The pattern was found to be highly dependent on spatial grid resolution due to the lack of membrane stresses in the shallow-ice approximation (Hindmarsh, 2006, 2009). Also f.ETISh produces a similar patterning for this particular experiment, despite the approximations in the thermomechanical coupling (using a vertically-integrated temperature) and the use of shape functions (Figure A4).

Exp	Variable	Benchmark	f.ETISH
A	Volume (10^6 km^3)	2.128 ± 0.145	2.133
	Area (10^6 km^2)	1.034 ± 0.086	1.092
	Melt fraction	0.718 ± 0.290	0.703
	H_{summit} (m)	3688.342 ± 96.740	3605.157
	T_{summit}^b (K)	-17.545 ± 2.929	-11.033
B	Δ Volume (%)	-2.589 ± 1.002	-3.628
	Δ Melt fraction (%)	11.836 ± 18.669	17.589
	ΔH_{summit} (%)	-4.927 ± 1.316	-5.259
	$\Delta T_{\text{summit}}^b$ (K)	4.623 ± 0.518	4.115
C	Δ Volume (%)	-28.505 ± 1.204	-27.739
	Δ Area (%)	-19.515 ± 3.554	-21.002
	Δ Melt fraction (%)	-27.806 ± 31.371	-45.160
	ΔH_{summit} (%)	-12.928 ± 1.501	-12.764
	$\Delta T_{\text{summit}}^b$ (K)	3.707 ± 0.615	3.045
D	Δ Volume (%)	-12.085 ± 1.236	-12.377
	Δ Area (%)	-9.489 ± 3.260	-10.139
	Δ Melt fraction (%)	-1.613 ± 5.745	-4.848
	ΔH_{summit} (%)	-2.181 ± 0.532	-2.168
	$\Delta T_{\text{summit}}^b$ (K)	-0.188 ± 0.060	-0.341
G	Volume (10^6 km^3)	1.589 ± 0.702	1.529
	Area (10^6 km^2)	1.032 ± 0.071	1.088
	Melt fraction	0.352 ± 0.530	0.319
	H_{summit} (m)	2365.206 ± 1468.880	2220.538
	T_{summit}^b (K)	-24.016 ± 7.681	-17.864
H	Volume (10^6 km^3)	1.900 ± 0.461	1.807
	Area (10^6 km^2)	1.032 ± 0.067	1.807
	Melt fraction	0.529 ± 0.429	0.496
	H_{summit} (m)	3507.984 ± 394.380	3225.787
	T_{summit}^b (K)	-17.925 ± 2.977	-12.664

Table A3. Comparison of f.ETISH with the EISMINT-II experiments (Payne et al., 2000).

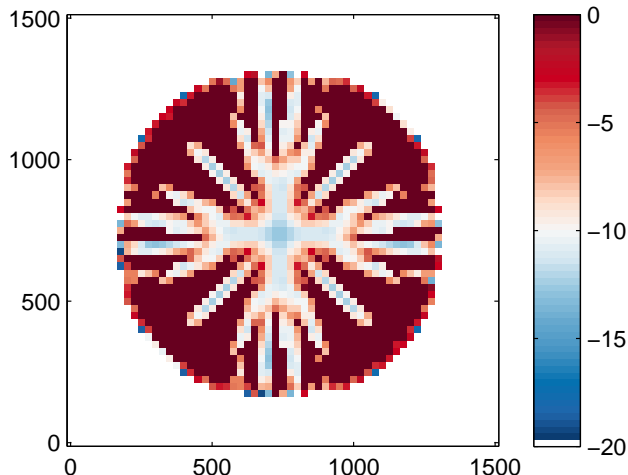


Figure A4. Predicted basal temperatures (corrected for pressure-dependence) according to EISMINT-II experiment H.

Appendix C: Modified MISMP experiments

The capacity of an ice sheet model to cope with the marine boundary, and more specifically migration of the grounding line, is essential in Antarctic ice-sheet modelling. Since grounding-line dynamics were elucidated mathematically based on boundary layer theory (Schoof, 2007a, b, 2011), two intercomparison exercises were established. The first one tested grounding-line migration and stability on downward sloping beds and instability on retrograde slopes for flow-line models (Pattyn et al., 2012), and the second tested the effect of buttressing for two- and three-dimensional ice-sheet models (Pattyn et al., 2013). Given that marine ice sheet instability is a crucial feedback process in marine ice sheet behaviour, we performed the flow-line experiments for a plan-view model setup. Experiments were carried out for both grounding-line flux conditions SGL and TGL. Ice shelves are included, but without exerting any buttressing strength, i.e. $\tau_{xx} = \tau_f$. The first experiment is an ice sheet on a seaward-sloping bedrock, which in plan view results in a conic bed, defined by (Pattyn et al., 2012):

$$B = 720 - \frac{778.5}{750} d_{\text{summit}}, \quad (\text{C1})$$

where d_{summit} (km) is the radial distance from the centre of the domain. The second experiment consists of an overdeepened section in the bedrock profile, hence the presence of a retrograde slope, defined by (Pattyn et al., 2012):

$$B = 729 - \frac{2184.8}{750^2} d_{\text{summit}}^2 + \frac{1031.72}{750^4} d_{\text{summit}}^4 - \frac{151.72}{750^6} d_{\text{summit}}^6. \quad (\text{C2})$$

The initial ice sheet is obtained for a constant value of the flow parameter A of $10^{-16} \text{ Pa}^{-n} \text{ a}^{-1}$ and a constant surface mass balance of $\dot{a} = 0.3 \text{ m a}^{-1}$. A grid-size spacing of $\Delta = 50 \text{ km}$ is employed. All other parameters are listed in Tables 1–3. Subsequently, the flow-rate parameter A is altered to a new value to obtain a new steady state, where lower/higher values of A leads to grounding-line advance/retreat, respectively. According to theory, a given set of boundary conditions leads to unique steady state grounding-line positions on a downward sloping bedrock, while the grounding line never reaches a steady-state position on an upward-sloping bedrock, which is depicted in Fig. A5. For the overdeepened bed, this leads to hysteresis, i.e., multi-valued grounding-line positions and ice sheet profiles for the same set of boundary conditions (Figs. A5 and A6). The numerical error was estimated by determining the position of each grounding-line grid cell compared to its radial distance from the centre of the ice sheet (both experiments results in radial ice caps). The mean position of the grounding line and the standard deviation corresponding to each steady-state are shown in Fig. A6. Interpolation of the exact position within a grid cell was not considered. All errors are smaller than the nominal grid size of 50 km. The lowest numerical error corresponds to the grounding-line treatment according to the power-law sliding law without the presence of ice shelves ($\sigma \sim 20 \text{ km}$). Including ice shelves makes the ice sheet more rapidly advance across the unstable section, since ice shelf thickness increases for lower values of A . Associated errors are also larger. Finally, the flux condition for Coulomb friction (Tsai et al., 2015) results in a generally smaller ice sheet, as the ice flux across the grounding line is higher than in the previous case. The ice sheet is also more sensitive to changes in A , i.e., small changes make the grounding line advance and retreat more rapidly. Associated errors are smaller for the no-shelf experiment, but significantly larger for the ice-shelf experiment. Given the larger sensitivity, the numerical solution is also less stable compared to the power-law flux condition SGL of Schoof (2007a) and the use of smaller time steps could probably improve the results.

Errors on the advance and retreat grounding-line positions are displayed in the bottom panel of Fig. A6. In all cases, the difference in grounding-line position between advance and retreat is less than 10 km (one-fifth of the spatial resolution of the model). In some cases the error is exactly zero, meaning that the steady state ice sheets (the one obtained during advance compared to the one obtained after retreat) are exactly the same.

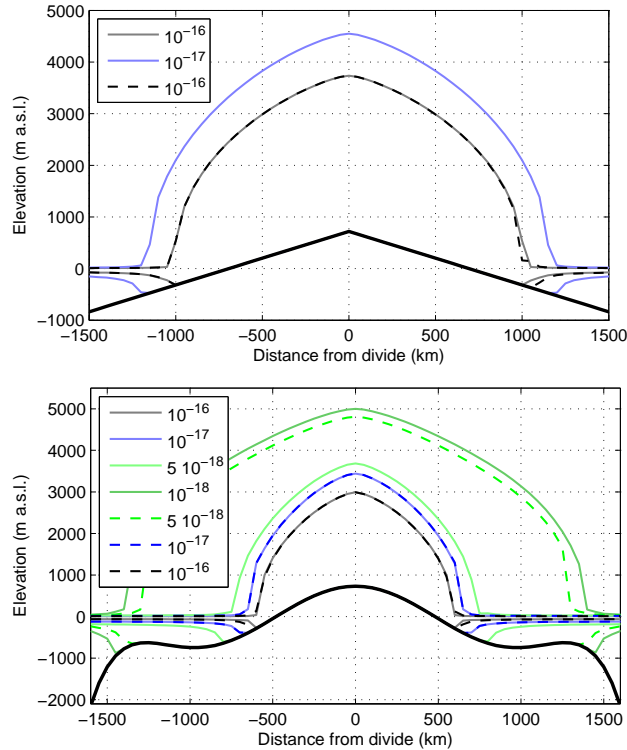


Figure A5. Steady-state ice-sheet/ice-shelf profiles for the MISIMIP experiments corresponding to different values of the flow parameter A ($\text{Pa}^{-n} \text{a}^{-1}$) along the center-line for the downward-sloping bedrock (upper panel) and the overdeepened bedrock case (lower panel) according to the advance (solid line) and retreat (dashed line) experiments and a grounding-line flux-condition according to Eq. (18).

References

- Asay-Davis, X. S., Cornford, S. L., Durand, G., Galton-Fenzi, B. K., Gladstone, R. M., Gudmundsson, G. H., Hattermann, T., Holland, D. M., Holland, D., Holland, P. R., Martin, D. F., Mathiot, P., Pattyn, F., and Seroussi, H.: Experimental design for three inter-related Marine Ice-Sheet and Ocean Model Intercomparison Projects, *Geoscientific Model Development Discussions*, 8, 9859–9924, doi:10.5194/gmdd-8-9859-2015, 2015.
- 5 Aschwanden, A., Adalgeirsdóttir, G., and Khroulev, C.: Hindcasting to measure ice sheet model sensitivity to initial states, *The Cryosphere*, 7, 1083–1093, doi:10.5194/tc-7-1083-2013, 2013.
- Beckmann, A. and Goosse, H.: A parameterization of ice shelf–ocean interaction for climate models, *Ocean Modelling*, 5, 157 – 170, doi:http://dx.doi.org/10.1016/S1463-5003(02)00019-7, 2003.
- 10 Berger, S., Favier, L., Drews, R., Derwael, J.-J., and Pattyn, F.: The control of an uncharted pinning point on the flow of an Antarctic ice shelf, *Journal of Glaciology*, 62, 37–45, doi:10.1017/jog.2016.7, 2016.
- Bernales, J., Rogozhina, I., Greve, R., and Thomas, M.: Comparison of hybrid schemes for the combination of Shallow Approximations in numerical simulations of the Antarctic Ice Sheet, *The Cryosphere Discussions*, 2016, 1–32, doi:10.5194/tc-2016-117, 2016.

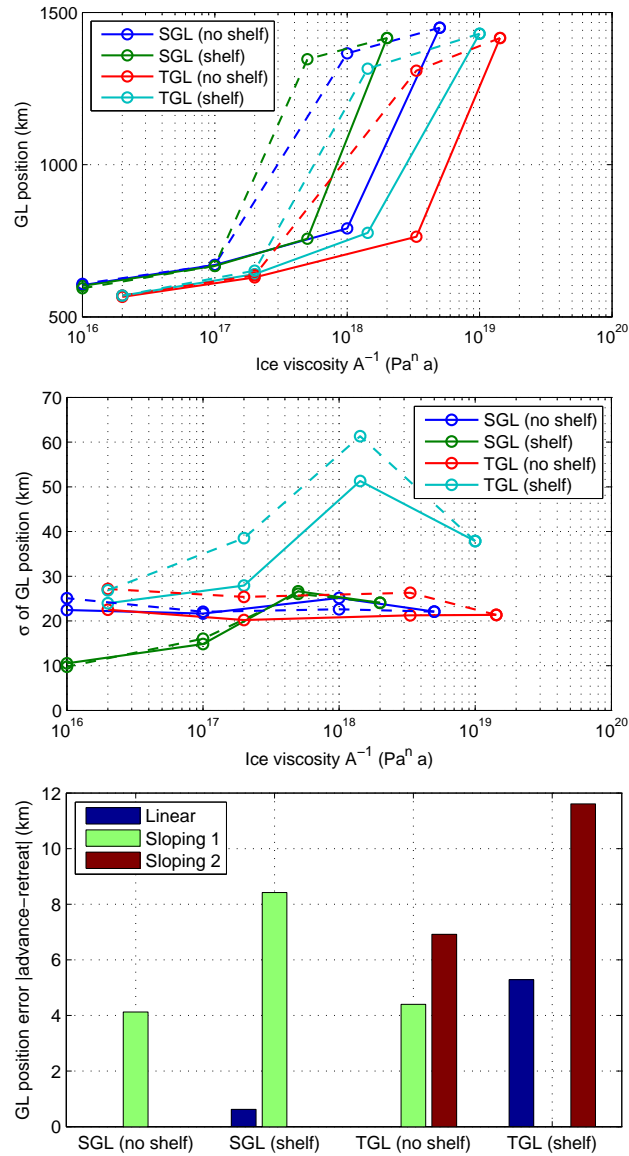


Figure A6. Median (upper panel) and standard deviation (centre panel) of steady-state grounding-line positions according to the MISIMIP experiments for a circular ice sheet as a function of the flow parameter A ($\text{Pa}^{-n} \text{a}^{-1}$) for the overdeepened bedrock experiment according to different flux conditions at the grounding line and inclusion/exclusion of ice shelves. Solid lines represent advance and dashed lines represent retreat experiments. The lower panel displays the difference in grounding-line position for the steady-state ice sheets obtained during advance with those obtained during retreat (same parameter values) for the linear-sloping bed (Linear) and the overdeepened bed. The latter has two sections with stable steady-state solutions, i.e., a small ice sheet (Sloping 1) and a large one (Sloping 2).

- Bindschadler, R. A., Nowicki, S., Abe-Ouchi, A., Aschwanden, A., Choi, H., Fastook, J., Granzow, G., Greve, R., Gutowski, G., Herzfeld, U., Jackson, C., Johnson, J., Khroulev, C., Levermann, A., Lipscomb, W. H., Martin, M. A., Morlighem, M., Parizek, B. R., Pollard, D., Price, S. F., Ren, D., Saito, F., Sato, T., Seddik, H., Seroussi, H., Takahashi, K., Walker, R., and Wang, W. L.: Ice-sheet model sensitivities to environmental forcing and their use in projecting future sea level (the SeaRISE project), *Journal of Glaciology*, 59, 195–224, doi:10.3189/2013JG12J125, 2013.
- 5 Bueler, E. and Brown, J.: Shallow shelf approximation as a “sliding law” in a thermomechanically coupled ice sheet model, *Journal of Geophysical Research: Earth Surface*, 114, doi:10.1029/2008JF001179, f03008, 2009.
- Bueller, E. and van Pelt, W.: Mass-conserving subglacial hydrology in the Parallel Ice Sheet Model version 0.6, *Geoscientific Model Development*, 8, 1613–1635, doi:10.5194/gmd-8-1613-2015, 2015.
- 10 Cornford, S. L., Martin, D. F., Payne, A. J., Ng, E. G., Le Brocq, A. M., Gladstone, R. M., Edwards, T. L., Shannon, S. R., Agosta, C., van den Broeke, M. R., Hellmer, H. H., Krinner, G., Ligtenberg, S. R. M., Timmermann, R., and Vaughan, D. G.: Century-scale simulations of the response of the West Antarctic Ice Sheet to a warming climate, *The Cryosphere*, 9, 1579–1600, doi:10.5194/tc-9-1579-2015, 2015.
- Cornford, S. L., Martin, D. F., Lee, V., Payne, A. J., and Ng, E. G.: Adaptive mesh refinement versus subgrid friction interpolation in simulations of Antarctic ice dynamics, *Annals of Glaciology*, 57, 1–9, doi:10.1017/aog.2016.13, 2016.
- 15 Cuffey, K. and Paterson, W. S. B.: *The Physics of Glaciers*. 4th ed, Elsevier, New York, 2010.
- de Boer, B., van de Wal, R. S. W., Lourens, L. J., Bintanja, R., and Reerink, T. J.: A continuous simulation of global ice volume over the past 1 million years with 3-D ice-sheet models, *Climate Dynamics*, 41, 1365–1384, doi:10.1007/s00382-012-1562-2, 2013.
- de Boer, B., Dolan, A. M., Bernales, J., Gasson, E., Goelzer, H., Gолledge, N. R., Sutter, J., Huybrechts, P., Lohmann, G., Rogozhina, I., Abe-Ouchi, A., Saito, F., and van de Wal, R. S. W.: Simulating the Antarctic ice sheet in the late-Pliocene warm period: PLISMIP-ANT, an ice-sheet model intercomparison project, *The Cryosphere*, 9, 881–903, doi:10.5194/tc-9-881-2015, 2015.
- 20 DeConto, R. M. and Pollard, D.: Contribution of Antarctica to past and future sea-level rise, *Nature*, 531, 591–597, doi:10.1038/nature17145, 2016.
- Durand, G. and Pattyn, F.: Reducing uncertainties in projections of Antarctic ice mass loss, *The Cryosphere*, 9, 2043–2055, doi:10.5194/tc-9-2043-2015, 2015.
- 25 Durand, G., Gagliardini, O., Zwinger, T., Le Meur, E., and Hindmarsh, R. C.: Full Stokes modeling of marine ice sheets: influence of the grid size, *Annals of Glaciology*, 50, 109–114, doi:10.3189/172756409789624283, 2009.
- Favier, L., Durand, G., Cornford, S. L., Gudmundsson, G. H., Gagliardini, O., Gillet-Chaulet, F., Zwinger, T., Payne, A. J., and Le Brocq, A. M.: “Retreat of Pine Island Glacier controlled by marine ice-sheet instability”, *Nature Climate Change*, 4, 117–121, 2014.
- Favier, L., Pattyn, F., Berger, S., and Drews, R.: Dynamic influence of pinning points on marine ice-sheet stability: a numerical study in Dronning Maud Land, East Antarctica, *The Cryosphere*, 10, 2623–2635, doi:10.5194/tc-10-2623-2016, 2016.
- 30 Feldmann, J. and Levermann, A.: Collapse of the West Antarctic Ice Sheet after local destabilization of the Amundsen Basin, *Proceedings of the National Academy of Sciences*, 112, 14 191–14 196, doi:10.1073/pnas.1512482112, 2015.
- Feldmann, J., Albrecht, T., Khroulev, C., Pattyn, F., and Levermann, A.: Resolution-dependent performance of grounding line motion in a shallow model compared with a full-Stokes model according to the MISMIP3d intercomparison, *Journal of Glaciology*, 60, 353–360, doi:10.3189/2014JG13J093, 2014.
- 35 Fox-Maule, C., Purucker, M. E., Olsen, N., and Mosegaard, K.: Heat Flux Anomalies in Antarctica Revealed by Satellite Magnetic Data, *Science*, 309, 464–467, 2005.

- Fretwell, P., Pritchard, H. D., Vaughan, D. G., Bamber, J. L., Barrand, N. E., Bell, R., Bianchi, C., Bingham, R. G., Blankenship, D. D., Casassa, G., Catania, G., Callens, D., Conway, H., Cook, A. J., Corr, H. F. J., Damaske, D., Damm, V., Ferraccioli, F., Forsberg, R., Fujita, S., Gim, Y., Gogineni, P., Griggs, J. A., Hindmarsh, R. C. A., Holmlund, P., Holt, J. W., Jacobel, R. W., Jenkins, A., Jokat, W., Jordan, T., King, E. C., Kohler, J., Krabill, W., Riger-Kusk, M., Langley, K. A., Leitchenkov, G., Leuschen, C., Luyendyk, B. P., Matsuoka, K., Mouginit, J., Nitsche, F. O., Nogi, Y., Nost, O. A., Popov, S. V., Rignot, E., Rippin, D. M., Rivera, A., Roberts, J., Ross, N., Siegert, M. J., Smith, A. M., Steinhage, D., Studinger, M., Sun, B., Tinto, B. K., Welch, B. C., Wilson, D., Young, D. A., Xiangbin, C., and Zirizzotti, A.: Bedmap2: improved ice bed, surface and thickness datasets for Antarctica, *The Cryosphere*, 7, 375–393, 2013.
- Gagliardini, O., Cohen, D., Raback, P., and Zwinger, T.: Finite-element modeling of subglacial cavities and related friction law, *J. Geophys. Res.*, 112, doi:10.1029/2006JF000576, 2007.
- 10 Gladstone, R. M., Payne, A. J., and Cornford, S. L.: Parameterising the Grounding Line in Ice Sheet Models, *The Cryosphere*, 4, 605–619, doi:10.5194/tc-4-605-2010, 2010.
- Gladstone, R. M., Payne, A. J., and Cornford, S. L.: Resolution requirements for grounding-line modelling: sensitivity to basal drag and ice-shelf buttressing, *Annals of Glaciology*, 53, 97–105, doi:10.3189/2012AoG60A148, 2012.
- Golledge, N. R., Kowalewski, D. E., Naish, T. R., Levy, R. H., Fogwill, C. J., and Gasson, E. G. W.: The multi-millennial Antarctic commitment to future sea-level rise, *Nature*, 526, 421–425, 2015.
- 15 Gudmundsson, G. H., Krug, J., Durand, G., Favier, L., and Gagliardini, O.: The Stability of Grounding Lines on Retrograde Slopes, *The Cryosphere Discuss.*, 6, 2597–2619, doi:10.5194/tcd-6-2597-2012, 2012.
- Hindmarsh, R. C. A.: Qualitative Dynamics of Marine Ice Sheets, in: *Ice in the Climate System*, edited by Peltier, W., NATO ASI Series I (12), pp. 67–99, Berlin, Springer-Verlag, 1993.
- 20 Hindmarsh, R. C. A.: On the Numerical Computation of Temperature in an Ice Sheet, *J. Glaciol.*, 45, 568–574, 1999.
- Hindmarsh, R. C. A.: Stress gradient damping of thermoviscous ice flow instabilities, *Journal of Geophysical Research: Solid Earth*, 111, doi:10.1029/2005JB004019, b12409, 2006.
- Hindmarsh, R. C. A.: Consistent generation of ice-streams via thermo-viscous instabilities modulated by membrane stresses, *Geophysical Research Letters*, 36, doi:10.1029/2008GL036877, l06502, 2009.
- 25 Hindmarsh, R. C. A., Leysinger Vieli, G. J. M. C., and Parrenin, F.: A Large-Scale Numerical Model for Computing Isochrone Geometry, *Ann. Glaciol.*, 50, 130–140, 2009.
- Holland, D. M. and Jenkins, A.: Modeling Thermodynamic Ice-Ocean Interactions at the Base of an Ice Shelf, *J. Phys. Oceanogr.*, 29, 1787–1800, 1999.
- Holland, P. R., Jenkins, A., and Holland, D. M.: The response of ice shelf basal melting to variations in ocean temperature., *Journal of*
- 30 *Climate*, 21, 2008.
- Hulton, N. R. J. and Mineter, M. J.: Modelling self-organization in ice streams, *Annals of Glaciology*, 30, 127–136, doi:doi:10.3189/172756400781820561, 2000.
- Hutter, K.: *Theoretical Glaciology*, Dordrecht, Kluwer Academic Publishers, 1983.
- Huybrechts, P.: A 3-D Model for the Antarctic Ice Sheet: a Sensitivity Study on the Glacial-Interglacial Contrast, *Climate Dyn.*, 5, 79–92,
- 35 1990.
- Huybrechts, P.: The Antarctic Ice Sheet and Environmental Change: a Three-Dimensional Modelling Study, *Berichte für Polarforschung*, 99, 1–241, 1992.

- Huybrechts, P.: Sea-level Changes at the LGM from Ice-Dynamic Reconstructions of the Greenland and Antarctic Ice Sheets during the Glacial Cycles, *Quaternary Science Reviews*, 21, 203–231, 2002.
- Huybrechts, P. and de Wolde, J.: The dynamic response of the Greenland and Antarctic ice sheets to multiple-century climatic warming, *Journal of Climate*, 12, 2169–2188, 1999.
- 5 Huybrechts, P., Payne, A., and The EISMINT Intercomparison Group: The EISMINT Benchmarks for Testing Ice-Sheet Models, *Ann. Glaciol.*, 23, 1–12, 1996.
- Huybrechts, P., Abe-Ouchi, A., Marsiat, I., Pattyn, F., Payne, A., Ritz, C., and Rommelaere, V.: Report of the Third EISMINT Workshop on Model Intercomparison, European Science Foundation (Strasbourg), 1998.
- Joughin, I., Smith, B. E., and Medley, B.: Marine Ice Sheet Collapse Potentially Under Way for the Thwaites Glacier Basin, West Antarctica, *Science*, 344, 735–738, doi:10.1126/science.1249055, 2014.
- 10 Katz, R. F. and Worster, M. G.: Stability of ice-sheet grounding lines, *Proc. R. Soc. A*, p. 10.1098/rspa.2009.0434, 2010.
- Larour, E., Seroussi, H., Morlighem, M., and Rignot, E.: Continental Scale, High Order, High Spatial Resolution, Ice Sheet Modeling using the Ice Sheet System Model, *J. Geophys. Res.*, 117, 10.1029/2011JF002140, 2012.
- Levermann, A. and Winkelmann, R.: A simple equation for the melt elevation feedback of ice sheets, *The Cryosphere*, 10, 1799–1807, doi:10.5194/tc-10-1799-2016, 2016.
- 15 Levermann, A., Albrecht, T., Winkelmann, R., Martin, M. A., Haseloff, M., and Joughin, I.: Kinematic first-order calving law implies potential for abrupt ice-shelf retreat, *The Cryosphere*, 6, 273–286, doi:10.5194/tc-6-273-2012, 2012.
- Ma, Y., Gagliardini, O., Ritz, C., Gillet-Chaulet, F., Durand, G., and Montagnat, M.: Enhancement factors for grounded ice and ice shelves inferred from an anisotropic ice-flow model, *Journal of Glaciology*, 56, 805–812, doi:10.3189/002214310794457209, 2010.
- 20 MacAyeal, D. R.: Large-scale Ice Flow over a Viscous Basal Sediment: Theory and Application to Ice Stream B, Antarctica, *J. Geophys. Res.*, 94, 4071–4087, 1989.
- Machguth, H., MacFerrin, M., van As, D., Box, J. E., Charalampidis, C., Colgan, W., Fausto, R. S., Meijer, H. A. J., Mosley-Thompson, E., and van de Wal, R. S. W.: Greenland meltwater storage in firn limited by near-surface ice formation, *Nature Climate Change*, doi:10.1038/nclimate2899, 2016.
- 25 Maris, M. N. A., de Boer, B., Ligtenberg, S. R. M., Crucifix, M., van de Berg, W. J., and Oerlemans, J.: Modelling the evolution of the Antarctic ice sheet since the last interglacial, *The Cryosphere*, 8, 1347–1360, doi:10.5194/tc-8-1347-2014, 2014.
- Martin, M. A., Winkelmann, R., Haseloff, M., Albrecht, T., Bueller, E., Khroulev, C., and Levermann, A.: The Potsdam Parallel Ice Sheet Model (PISM-PIK) Part 2: Dynamic equilibrium simulation of the Antarctic ice sheet, *The Cryosphere*, 5, 727–740, doi:10.5194/tc-5-727-2011, 2011.
- 30 Mengel, M. and Levermann, A.: Ice plug prevents irreversible discharge from East Antarctica, *Nature Climate Change*, 4, 451–455, doi:10.1038/nclimate2226, 2014.
- Mercer, J.: West Antarctic Ice Sheet and CO₂ Greenhouse Effect: a Threat of Disaster, *Nature*, 271, 321–325, 1978.
- Morland, L.: Unconfined Ice-Shelf Flow, in: *Dynamics of the West Antarctica Ice Sheet*, edited by van der Veen, C. J. and Oerlemans, J., pp. 99–116, Kluwer Acad., Dordrecht, Netherlands, 1987.
- 35 Nowicki, S., Bindschadler, R. A., Abe-Ouchi, A., Aschwanden, A., Bueller, E., Choi, H., Fastook, J., Granzow, G., Greve, R., Gutowski, G., Herzfeld, U., Jackson, C., Johnson, J., Khroulev, C., Larour, E., Levermann, A., Lipscomb, W. H., Martin, M. A., Morlighem, M., Parizek, B. R., Pollard, D., Price, S. F., Ren, D., Rignot, E., Saito, F., Sato, T., Seddik, H., Seroussi, H., Takahashi, K., Walker, R., and Wang, W. L.:

- Insights into spatial sensitivities of ice mass response to environmental change from the SeaRISE ice sheet modeling project I: Antarctica, *Journal of Geophysical Research: Earth Surface*, 118, 1002–1024, doi:10.1002/jgrf.20081, 2013.
- Pattyn, F.: Numerical Modelling of a Fast-Flowing Outlet Glacier: Experiments with Different Basal Conditions, *Ann. Glaciol.*, 23, 237–246, 1996.
- 5 Pattyn, F.: Antarctic Subglacial Conditions inferred from a Hybrid Ice Sheet/Ice Stream Model, *Earth Planet. Sci. Lett.*, 295, 451–461, 2010.
- Pattyn, F. and Durand, G.: Why marine ice sheet model predictions may diverge in estimating future sea level rise, *Geophysical Research Letters*, 40, 4316–4320, doi:10.1002/grl.50824, 2013.
- Pattyn, F., Huyghe, A., De Brabander, S., and De Smedt, B.: Role of Transition Zones in Marine Ice Sheet Dynamics, *J. Geophys. Res.*, 111, 10.1029/2005JF000394, 2006.
- 10 Pattyn, F., Schoof, C., Perichon, L., Hindmarsh, R. C. A., Bueler, E., de Fleurian, B., Durand, G., Gagliardini, O., Gladstone, R., Goldberg, D., Gudmundsson, G. H., Huybrechts, P., Lee, V., Nick, F. M., Payne, A. J., Pollard, D., Rybak, O., Saito, F., and Vieli, A.: Results of the Marine Ice Sheet Model Intercomparison Project, MISMP, *The Cryosphere*, 6, 573–588, doi:10.5194/tc-6-573-2012, 2012.
- Pattyn, F., Perichon, L., Durand, G., Favier, L., Gagliardini, O., Hindmarsh, R. C., Zwinger, T., Albrecht, T., Cornford, S., Docquier, D., Fürst, J. J., Goldberg, D., Gudmundsson, G. H., Humbert, A., Hütten, M., Huybrechts, P., Jouvét, G., Kleiner, T., Larour, E., Martin,
- 15 D., Morlighem, M., Payne, A. J., Pollard, D., Rückamp, M., Rybak, O., Seroussi, H., Thoma, M., and Wilkens, N.: Grounding-line migration in plan-view marine ice-sheet models: results of the ice2sea MISMP3d intercomparison, *Journal of Glaciology*, 59, 410–422, doi:10.3189/2013JG12J129, 2013.
- Payne, A. J.: Limit Cycles in the Basal Thermal Regime of Ice Sheets, *J. Geophys. Res.*, 100, 4249–4263, 1995.
- Payne, A. J. and Dongelmans, P. W.: Self-organisation in the Thermomechanical Flow of Ice Sheets, *J. Geophys. Res.*, 102, 12219–12234,
- 20 1997.
- Payne, A. J., Huybrechts, P., Abe-Ouchi, A., Calov, R., Fastook, J. L., Greve, R., Marshall, S. J., Marsiat, I., Ritz, C., Tarasov, L., and Thomassen, M.: Results from the EISMINT Model Intercomparison: the Effects of Thermomechanical Coupling, *J. Glaciol.*, 46, 227–238, 2000.
- Pollard, D. and DeConto, R. M.: Modelling West Antarctic Ice Sheet Growth and Collapse Through the Past Five Million Years, *Nature*,
- 25 458, 10.1038/nature07809, 2009.
- Pollard, D. and DeConto, R. M.: Description of a Hybrid Ice Sheet-Shelf Model, and Application to Antarctica, *Geosci. Model Dev.*, 5, 1273–1295, doi:10.5194/gmd-5-1273-2012, 2012a.
- Pollard, D. and DeConto, R. M.: A simple inverse method for the distribution of basal sliding coefficients under ice sheets, applied to Antarctica, *The Cryosphere*, 6, 953–971, doi:10.5194/tc-6-953-2012, 2012b.
- 30 Pollard, D., DeConto, R. M., and Alley, R. B.: Potential Antarctic Ice Sheet retreat driven by hydrofracturing and ice cliff failure, *Earth and Planetary Science Letters*, 412, 112 – 121, 2015.
- Purucker, M.: Geothermal heat flux data set based on low resolution observations collected by the CHAMP satellite between 2000 and 2010, and produced from the MF-6 model following the technique described in Fox Maule et al. (2005), <http://websrv.cs.umt.edu/isis/index.php>, 2013.
- 35 Reeh, N.: Parameterization of melt rate and surface temperature on the Greenland ice sheet, *Polarforschung*, 59, 113–128, 1989.
- Ridley, J., Gregory, J. M., Huybrechts, P., and Lowe, J.: Thresholds for irreversible decline of the Greenland ice sheet, *Clim. Dyn.*, 35, 1049–1057, 2010.
- Rignot, E., Mouginot, J., and Scheuchl, B.: Ice Flow of the Antarctic Ice Sheet, *Science*, 333, 1427–1430, 2011.

- Rignot, E., Mouginot, J., Morlighem, M., Seroussi, H., and Scheuchl, B.: Widespread, rapid grounding line retreat of Pine Island, Thwaites, Smith, and Kohler glaciers, West Antarctica, from 1992 to 2011, *Geophysical Research Letters*, 41, 3502–3509, doi:10.1002/2014GL060140, 2014.
- Ritz, C., T. L. Edwards a, d. G. D., Payne, A. J., Peyaud, V., and Hindmarsh, R. C. A.: Potential sea-level rise from Antarctic ice-sheet instability constrained by observations, *Nature*, doi:10.1038/nature16147, 2015.
- Rommelaere, V. and Ritz, C.: A thermomechanical model of ice-shelf flow, *Annals of Glaciology*, 23, 13–20, 1996.
- Sato, T. and Greve, R.: Sensitivity experiments for the Antarctic ice sheet with varied sub-ice-shelf melting rates, *Annals of Glaciology*, 53, 221–228, doi:10.3189/2012AoG60A042, 2012.
- Scambos, T. A., Hulbe, C., Fahnestock, M., and Bohlander, J.: The link between climate warming and break-up of ice shelves in the Antarctic Peninsula, *Journal of Glaciology*, 46, 516–530, doi:doi:10.3189/172756500781833043, 2000.
- Scambos, T. A., Bohlander, J. A., Shuman, C. A., and Skvarca, P.: Glacier Acceleration and Thinning after Ice Shelf Collapse in the Larsen B Embayment, *Geophys. Res. Lett.*, 31, L18 402, 2004.
- Schoof, C.: Variational methods for glacier flow over plastic till, *Journal of Fluid Mechanics*, 555, 299–320, doi:10.1017/S0022112006009104, 2006.
- 15 Schoof, C.: Ice Sheet Grounding Line Dynamics: Steady States, Stability and Hysteresis, *J. Geophys. Res.*, 112, doi:doi:10.1029/2006JF000664, 2007a.
- Schoof, C.: Marine ice sheet dynamics. Part I. The case of rapid sliding, *J. Fluid Mech.*, 573, 27–55, 2007b.
- Schoof, C.: Ice-sheet acceleration driven by melt supply variability, *Nature*, 468, 803–806, 2010.
- Schoof, C.: Marine ice sheet dynamics. Part 2. A Stokes flow contact problem, *J. Fluid Mech.*, 679, 122–155, 2011.
- 20 Seroussi, H., Morlighem, M., Rignot, E., Mouginot, J., Larour, E., Schodlok, M., and Khazendar, A.: Sensitivity of the dynamics of Pine Island Glacier, West Antarctica, to climate forcing for the next 50 years, *The Cryosphere*, 8, 1699–1710, doi:10.5194/tc-8-1699-2014, 2014.
- Stokes, G.: On the theories of internal friction of fluids in motion, *Trans. Cambridge Philos. Soc.*, 8, 287–305, 1845.
- Thoma, M., Grosfeld, K., Barbi, D., Determann, J., Goeller, S., Mayer, C., and Pattyn, F.: RIMBAY – a multi-approximation 3D ice-dynamics model for comprehensive applications: model description and examples, *Geoscientific Model Development*, 7, 1–21, doi:10.5194/gmd-7-1-2014, 2014.
- Thomas, R. H.: The Dynamics of Marine Ice Sheets, *J. Glaciol.*, 24, 167–177, 1979.
- Truffer, M., Harrison, W. D., and Echelmeyer, K. A.: Glacier motion dominated by processes deep in underlying till, *Journal of Glaciology*, 46, 213–221, doi:10.3189/172756500781832909, 2000.
- 30 Tsai, V. C., Stewart, A. L., and Thompson, A. F.: Marine ice-sheet profiles and stability under Coulomb basal conditions, *Journal of Glaciology*, 61, 205–215, doi:doi:10.3189/2015JogG14J221, 2015.
- Tulaczyk, S. M., Kamb, B., and Engelhardt, H. F.: Basal Mechanics of Ice Stream B, West Antarctica. II. Undrained-Plastic-Bed Model, *J. Geophys. Res.*, 105, 483–494, 2000a.
- Tulaczyk, S. M., Kamb, B., and Engelhardt, H. F.: Basal Mechanics of Ice Stream B, West Antarctica. I. Till Mechanics, *J. Geophys. Res.*, 105, 463–481, 2000b.
- 35 Van Wessem, J., Reijmer, C., Morlighem, M., Mouginot, J., Rignot, E., Medley, B., Joughin, I., Wouters, B., Depoorter, M., Bamber, J., Lenaerts, J., De Van Berg, W., Van Den Broeke, M., and Van Meijgaard, E.: Improved representation of East Antarctic surface mass balance in a regional atmospheric climate model, *Journal of Glaciology*, 60, 761–770, doi:doi:10.3189/2014JogG14J051, 2014.

Vieli, A. and Payne, A.: Assessing the Ability of Numerical Ice Sheet Models to Simulate Grounding Line Migration, *J. Geophys. Res.*, 110, doi:doi:10.1029/2004JF000202, 2005.

Weertman, J.: Stability of the Junction of an Ice Sheet and an Ice Shelf, *J. Glaciol.*, 13, 3–11, 1974.

Weertman, J.: Milankovitch solar radiation variations and ice age ice sheet sizes, *Nature*, 261, 17–20, 1976.

- 5 Winkelmann, R., Martin, M. A., Haseloff, M., Albrecht, T., Bueler, E., Khroulev, C., and Levermann, A.: The Potsdam Parallel Ice Sheet Model (PISM-PIK) Part 1: Model description, *The Cryosphere*, 5, 715–726, 2011.

Winkelmann, R., Levermann, A., Ridgwell, A., and Caldeira, K.: Combustion of available fossil fuel resources sufficient to eliminate the Antarctic Ice Sheet, *Science Advances*, 1, doi:10.1126/sciadv.1500589, 2015.