Dear Dr. van den Broeke,

    We have revised the manuscript according the reviewers' suggestions and responded to both reviews individually in the discussion. A copy of each of those replies is below, followed by the revised manuscript and supplement, with changes tracked. Both reviewers commented that the title needed to be improved, and in order to address these comments we request that you change the title to "*Changes in flow of Crosson and Dotson Ice Shelves, West Antarctica in response to elevated melt.*"

Thank you,
David Lilien

Response to reviewer #1

We thank the reviewer for the thoughtful comments and for useful references that have improved the quality of the manuscript. We have addressed the specific comments below (reviewer's comments in bold). We will upload the new version of the manuscript and supplement, with and without changes tracked, separately.

This paper describes observations of mass budget for the Crosson and Dotson ice shelves in the Amundsen Sea sector of the Antarctic ice Sheet and attempt to provide a narrative for the timing of imbalance and for the succession of events and interaction that led to the current state of imbalance and mass loss of both floating and grounded ice in the region. The paper integrates new and existing observations with modelling in a balanced way in the context of existing literature. The manuscript is well structured, detailed and illustrated. I support the publishing of the manuscript with only minor changes.
      We thank the reviewer for the support of publication and have incorporated the specific comments as described below.

General comments:
I find the title vague and confusing; how varied, what response, and how varied are the elevated melt in the first place. Do you imply here that the same, elevated, melt under both ice shelf induce the various response? From the findings of this paper it does not look to me that this is the case.
We have changed the title to clarify that the response is in the flow of the ice shelves, and removed "varied," which was unclear: *Changes in flow of Crosson and Dotson Ice Shelves, West Antarctica in response to elevated melt*

Thinning rates used to calculated ice shelf elevation back in time are resolved over spatial resolution of 10's of kilometres; recent work have shown that, at least for Dotson, thinning is highly localised to the grounding lines and on the western margin of the shelf. You should at least address the impact that this might have, or not, on your analysis. You allude to it in section 4.3 but can you be more specific as to where this might be the case?
We think that this most appropriately belongs in the portion of the manuscript that compares our results to previous estimates of the pattern of melt (Gourmelen et al. 2017 and Khazendar et al. 2016). In short, we expect this error affect areas of high melt. We have added the following to section 5.3: "The peak regionally-averaged melt rates found in this study (23 m/yr) occur in the same regions (K1, SW1 and SE1) as found in other studies but the values are lower than the locally computed rates (50 m/yr in Gourmelen et. al (2017) and 129 m/yr in Khazendar et al. (2016)). This difference is not surprising, since the polygon-based method we use has limited spatial resolution and thus misses variations in melt rate in small-scale features such as within the channel on Dotson. Over broad scales, flux-gate and altimetry-based methods should agree, and indeed the overall melt rate we find beneath Dotson, 7.7±1.3 m/yr, agrees with the 6.1±0.7 m/yr found by Gourmelen et al. (2017). The lower peak melt rates found here compared to prior studies may also result from our assuming a spatially constant thinning rate over shelves where thinning rates vary substantially (Gourmelen et al., 2017). The shelf-wide rates used here likely cause us to underestimate melt in small polygons where thinning is most rapid (e.g. K1, SW1,

and SE1 in Figure 3). Similarly, they may cause us to slightly overestimate melt over broad, slower-changing regions (e.g., D1 and D2), but this effect should be smaller due to the shelf-wide thinning rate being more representative of rates in these regions. On scales smaller than the polygons we use to calculate melt, thinning may reach 50 m/yr (Gourmelen et al., 2017), comparable to flux divergence in these areas, causing the polygon-averaged rates to locally underestimate melt by a factor of two and introducing an error in the polygon average that we estimate may be as high as 50% in small polygons near the grounding line. "

Specific comments

Page1
L12: Ambiguous, suggests rephrasing. Is what is meant here that the melt under Dotson is dominating the mass loss? Or that the melt under Dotson is driving the mass loss elsewhere? From fig.3 it looks as though the mass loss of Dotson and Crosson are pretty much equal, that the increase in melt rate through the study period is similar, and that one is dominated by loss through basal melt (Dotson) and the other through calving (Crosson).
The increase in melt is greater on Dotson, but indeed the overall mass loss between the shelves is similar and the change is similar. We have changed the sentence to "These ice shelves have lost mass continuously since the 1990s, and we find that this loss results from increasing melt beneath both shelves and the increasing speed of Crosson."

L17: The preceding line gives an explanation for the observation, but this one does not - what is causing the lack of response of Dotson's velocity?
Added: "likely a result of the sustained competency of the shelf."

Page 2
L36: The terminology is indeed varied - Smith West is sharing a drainage basin and an ice shelf with Kohler, shouldn't this then be Kohler East instead as in Mouginot et al., 2014?
While Smith West and Kohler share an ice shelf, Smith East and West are flowing together as they reach the grounding line. Though there are justifications for either choice, we chose this terminology because the two trunks of Smith merge while grounded, and thus naming as in Mouginot et al., 2014 necessitates drawing a division between Smith and Kohler East in the midst of fast flowing, grounded ice. Following the naming conventions here, divisions between grounded glaciers match natural boundaries in velocity.

Page 3
L15: Ambiguous, suggest: "No similar changes in extent were observed over Dotson"
Agreed, thanks.

L23: "over" -> "under"
Done.

L24: "much higher than the surrounding ice" with the exception of the grounding line regions of Smith and Kohler
Added the parenthetical "(though lower than at the grounding lines of Smith and Kohler)"

Page 5
L15: Medley has no sup. Material.
This is correct, our phrasing was poor. Changed to "details can be found in Medley et al. (2014) and the supplementary materials to Joughin et al. (2014)."

L27: What air thickness is found here and how does this compares with modelled values? There are evidence that firn-air content found using this approach differs from model output, so well worth addressing this here. A map in Supp. Mat. For example.
We have added a sentence in the main text to give the range of values we find using this approach and to compare this to the Ligtenberg et al. 2011/RACMO2.3 model output. We have also added a figure showing the spatial pattern of firn-air content in the supplement (Figure S2). The relevant portion of the main text reads: "We find the firn-air content to range between 12-18 m across most of the ice shelves (Supplementary Figure S2); a firn model forced with output from RACMO2.3 shows greater firn-air content than we observe, generally between ~20-25 m over these shelves (Ligtenberg et al., 2011)."

Page 10
Line 6: The longer dataset also agrees with recent, high-resolution, estimates.
We added "Additionally, this longer dataset matches recent, high-resolution radar-based estimates (Gourmelen et al., 2017)."

Line 10: Reference Shepherd 2010 is missing
We are unsure of what the reviewer is referring to here: the inline citation is present, and it is listed in the references as "Shepherd, A., Wingham, D., Wallis, D., Giles, K., Laxon, S. and Sundal, A. V.: Recent loss of floating ice and the consequent sea level contribution, Geophys. Res. Lett., 37(13), n/a-n/a, doi:10.1029/2010GL042496, 2010."

Page 11
L2: You might want to compare and contrast the weakening described here with the shelf weakening and impact on speedup of Smith described in goldberg et al (2016, fig 3) - I think it is relevant here as there are similitudes but also new patterns, especially along the Eastern margins.
We were unaware that these ice shelves were studied in that publication, and we thank the reviewer for the reference. We chose to address this comment in the discussion of Crosson's speedup, and added: "Prior work has addressed the effect that thinning (equivalently, weakening) over different portions of Crosson and Dotson would have on ice loss upstream (Goldberg et al., 2016), and the areas in which we find weakening encompass several regions that are important for upstream dynamics. That work suggests that while the overall dynamics are insensitive to the bulk of weakening we find here, weakening in key areas, particularly near the Haynes tongue and at the western shear margin, is important for loss of grounded ice upstream, and thus may have influenced speeds near the grounding line as well."

Page 13
L14: There is also no indication of freeze-on from EO-based basal melt extraction

We thank the reviewer for the comment clarifying this statement. We have added the following: "Previous work (Depoorter et al., 2013; Gourmelen et al., 2017; Rignot et al., 2013) found no evidence of large-scale freeze-on beneath Dotson, and we eliminated the possibility of localized freeze-on being the primary cause of the channel by comparing radar observations to floatation levels."

L35: There seems to be melting occurring at the southern end of this portion of the channel. In fact it looks to me that the effect of the advection is visible along most of the length of the channel (ice flow is transverse to the channel up to about half-way down the shelf) as the locus of melt occupies only a fraction of the entire topographic depression. Then, can other sections of the channel be used to derive timing?
We tried to use as much of the channel as possible for this analysis. There are two factors limiting where this analysis is viable: whether flow was transverse to the channel and whether there was an obvious point upstream at which to assume the channel originated. We think our analysis extends as far westward (downward in Figure 6a) as it can given these two conditions. Because of the along-flow channel coming from near the grounding line of Kohler immediately westward of where our analysis cuts off (Figure 6a), we lack an upstream edge of the channel in this region. Moreover, the westernmost (bottom) line/string-of-pearls in Figure 6a is no longer fully perpendicular to the channel, and the channel is more aligned with flow farther westward. West of the outflow channel from Kohler, the channel we analyze is nearly parallel to flow, and so cannot be used for timing.

How would ice divergence influence the time-evolution of this channel's width and depth (e.g. Drews et al., 2016)?
The difference in orientation of the portion of the channel that we analyze compared to Drews et al. makes comparison to that work difficult. Drews finds almost no expression of the channel in the along-flow velocity or strain, though he does find a gradient across flow (his figure 6). We do not expect an across-flow gradient here because the channel itself is oriented across flow, and thus the thickness gradient driving the effect on across-flow strain is absent. We also cannot find such a gradient in the across-flow surface strain (from the InSAR velocities). In the along-flow direction, there is no expression in the along-flow surface strain as calculated from the InSAR velocities. Moreover, we expect the way in which we calculate the timing to be relatively insensitive to ice divergence. Since we integrate the travel time along flow to get the timing, we are accounting for the along-flow change in ice speed/the along-flow strain. However, we acknowledge that there may be some effect of along-flow strain not detectable in the velocity, though such an effect must be small. We have added: "While ice divergence following the initiation of channel incision may have had an effect on the channel width (Drews, 2015), there is no change in the divergence of the measured surface velocities around the transverse portion of the channel (conversely, along the flow-parallel portion there is significant convergence). Thus, any change in width due to divergence is at or below the level of uncertainty in the velocity measurements, and therefore small compared to the advection of the channel."

How does this timing relate to timings deduced from grounded ice thinning and ice shelf channel formation (e.g. Konrad et al., 2017; Gourmelen et al., 2017)?
While Konrad et al. get tight bounds on the timing of imbalance on Thwaites and PIG, for these glaciers the uncertainties are extremely high, and so unsurprisingly there is significant overlap

with the timing we infer. We have added a sentence simply saying that our results are consistent with the timing found by those authors and by Gourmelen et al.: "This timing is consistent with prior work on the upstream propagation of thinning over these glaciers, which found that thinning initiated around 1970±30 at the grounding lines of Smith and Kohler (Konrad et al., 2017), as well as with an altimetry-based study of Dotson, which found that the shelf had been thinning for at least two decades but not more than a century (Gourmelen et al., 2017)."

Page 16
Line 21: Ok, how does these melt estimates fit in your comparison earlier in this paragraph between melt obtain here and melt rates obtained by Khazendar et al?
This section was changed substantially in response to comments by the other reviewer. We have made this paragraph a three-way comparison of these studies:
"The peak regionally-averaged melt rates found in this study (23 m/yr) occur in the same regions (K1, SW1 and SE1) as found in other studies but the values are lower than the locally computed rates (50 m/yr in Gourmelen et. al (2017) and 129 m/yr in Khazendar et al. (2016)). This difference is not surprising, since the polygon-based method we use has limited spatial resolution and thus misses variations in melt rate in small-scale features such as within the channel on Dotson. Over broad scales, flux-gate and altimetry-based methods should agree, and indeed the overall melt rate we find beneath Dotson, 7.7±1.3 m/yr, agrees with the 6.1±0.7 m/yr found by Gourmelen et al. (2017). The lower peak melt rates found here compared to prior studies may also result from our assuming a spatially constant thinning rate over shelves where thinning rates vary substantially (Gourmelen et al., 2017). The shelf-wide rates used here likely cause us to underestimate melt in small polygons where thinning is most rapid (e.g. K1, SW1, and SE1 in Figure 3). Similarly, they may cause us to slightly overestimate melt over broad, slower-changing regions (e.g., D1 and D2), but this effect should be smaller due to the shelf-wide thinning rate being more representative of rates in these regions. On scales smaller than the polygons we use to calculate melt, thinning may reach 50 m/yr (Gourmelen et al., 2017), comparable to flux divergence in these areas. This thinning may cause the polygon-averaged rates to locally underestimate melt by a factor of two and introduce an error in the polygon average that we estimate may be as high as 50% in small polygons near the grounding line."

Fig. 3: b and c should have the same y-axis range (e.g. [0 50])
We have matched the axes.
caption: steady state (SS) The cross-hatched light grey bar is labelled floating ice in the figure and grounded ice in the caption - should it be floating ice everywhere?
Indeed, the cross-hatched bars should be labeled floating everywhere, thanks. We have added parentheticals to define the acronyms "SS" and "GL".

Response to reviewer #2

We thank the reviewer for a thorough review that has helped to significantly improve the clarity of the manuscript. Comments from the reviewer (bold) and our responses follow. We will upload the new version of the manuscript and supplement, with and without changes tracked, separately.

This manuscript presents a detailed analysis of the changes in speed and grounding position of two rapidly changing ice shelves, and their respective catchment basins, in the Amundsen Sea sector: Crosson and Dotson. The work combines a diverse set of measurements: satellite remote sensing data of horizontal velocities and elevation changes, airborne radar sounding for ice thickness, satellite imagery to determine iceshelf front position, and published estimates of ice-shelf thinning rates. The authors then estimate the ice viscosity using a numerical model and perform an analysis of changes in ice-shelf flux, basal melt, and calving rates. Their results show that Dotson and Crosson ice shelves exhibit different dynamic responses to similar perturbations, and that is likely that both ice shelves were out of balance well before the beginning of the satellite record (the 1990s).

General comments:
The manuscript presents a comprehensive study on the mass balance and velocity state of Dotson and Crosson ice shelves. The work provides some important insights into the origin of the current observed mass imbalance on these ice shelves and their respective catchment basins.
I couldn't find major issues with the work. Overall, the manuscript is well written, and the science is solid. I have, however, a few comments/suggestions that I think need further clarification and will improve the presentation of the work. These edits should be straightforward to incorporate.
In particular, the Summary section needs a bit more work. I think there should be a preference for the active voice in the 'Summary' (e.g. we analyzed, we found, we concluded, we showed), briefly stating the implications of your findings, as well as summarizing the path that leads to your conclusions. I feel this is missing here.
We have changed the wording of a number of sentences in the summary to be active and to clarify what work we did and what had been done in prior work. Some examples are: "We find that thinning and speedup…", "These conditions lead us to speculate that…", "Our results indicate that…", and "We used a diagnostic ice-flow model to show that…"

On the melt rate calculation; Fig. S1 shows melt rates estimates for 1-5 year time intervals. Since these are anomalies in basal melting, it is expected (in fact it has been demonstrated, e.g., Jacobs et al., 2013; Dutrieux et al., 2014; Christianson et al., 2016; Paolo et al., 2018) that melt rates are (highly?) sensitive to changes in ocean forcing in the Amundsen Sea sector, which fluctuates substantially at interannual timescales. So, I am unsure how much "weight" one can put on these (highly variable) short-term estimates of basal melt rates in the context of past (longer-term) dynamics of the ice shelf.
I am a bit confused about the fact that you used an average thinning rate for the entire ice shelf, which it might be fine for your polygon estimates, but then compare point estimates of basal melt against Khazendar et al. (2016). How meaningful is this comparison? If I understand correctly, the spatial variation in your melt-rate estimate is determined mostly

by the flux divergence since you do not account for the spatial variability in thinning rates, is that right? If so, how significant do you expect the changes in dH/dt across the ice shelf to be compared with the spatial changes in horizontal velocity?

The spatial variation in our melt-rate estimates is almost entirely determined by the flux divergence; the only spatial variability in thinning we account for is slightly different rates for Crosson and Dotson. dH/dt (if the change is assumed to be all ice and not snow or firn) and horizontal flux divergence both map linearly into our estimate of the melt rate. Locally, horizontal flux divergence can vary between ±100 m/yr, while local thinning rates found in Gourmelen et al. (2017) reach as high as 50 m/yr. Our spatially averaged estimates do not capture these peaks, but the estimates of Khazendar et al. explicitly measure thinning and thus, when corrected for flux divergence, ought to represent the anomalous melt at that point. In short, these methods are sensitive to different sources of error, and can provide information on different spatial and temporal scales, so we think that they are complementary and the comparison is worthwhile.

In response to these comments, and suggestions from the other reviewer, we have entirely re-worked the text surrounding this comparison (section 5.3). The section now includes three paragraphs. The first discusses the limitations of Khazendar et al. study, and how our result complement theirs. The second paragraph discusses the uncertainties and limitations of the Gourmelen study, and why our results are still useful in light of this more spatially resolved estimate. The third reconciles our lower value peak melt with the prior estimates by discussing the effects of spatial averaging and spatial variation in thinning.

The title needs to be a bit more informative (Observed elevated melt? Over what period? Elevated relative to what? What kind of response?).

We have changed the title to emphasize the type of response discussed in the paper: *Changes in flow of Crosson and Dotson Ice Shelves, West Antarctica in response to elevated melt*

To facilitate the reviewing process, please use continuous line numbering throughout the entire manuscript, and number every single line.

We apologize that this numbering makes reviewing more difficult, but we have adhered to the guidelines provided by *The Cryosphere*.

Specific comments:
Page 1
Lines btw 5-10: "remotely sensed datasets". Which datasets?

Changed to "remotely sensed measurements of velocity and ice geometry"

Lines btw 10-15: "melt" => "elevated melt" or "melt in excess" (there is basal melt in the steady state)

Changed to "elevated melt"

Lines btw 20-25: "instability" => "internal instability"?

Changed to "susceptible to internal instability triggered by increased ocean melting of buttressing ice shelves." The instability generally requires some triggering (despite the potential

for internal instability, these ice streams may have maintained their position for 1000s of years with no external forcing).

Lines btw 20-25: "are the dominant source of sea level rise" => "are currently the dominant source of sea level rise" or "are the dominant source of current sea level rise"
Changed to "currently the dominant source of sea level rise"

Page 2
Lines btw 20-25: "ice flux on ice thickness" => "ice flux across the grounding line on ice thickness there"
Done

Lines btw 25-30: "deeper ocean waters are generally warmer in these systems". Careful here, this cannot be a general statement. In locations where CDW is present (not everywhere), there is more of this warm water reaching the deep grounding lines because the CDW is denser than surface waters. This is different from saying "deeper waters are warmer".
We have revised these sentences to avoid over-generalizing. They now read: "In the case of a retrograde bed, the deepening of the grounding line caused by ungrounding also increases melt because the melting point decreases with depth. For glaciers along the Amundsen Sea, this effect can be intensified because warm, dense circumpolar deep water generally intrudes at depth and results in elevated melt at deeper grounding lines (Jenkins et al., 2016; Thoma et al., 2008)."

Lines btw 30-35: "recent speed and thickness change" => "recently observed speed and thickness changes"
Done

Page 3
Lines btw 10-15: "significant changes in the extent of Crosson". How significant? Can you provide a percentage of area change?
We rephrased this to be more specific. The percentage change in area is deceptive because of extension of the middle of the calving front the absence of any large calving event during this period, so we calculated the absolute area change of the margins. The sentence now reads: "There were also significant changes in the extent of ice at the margins of Crosson (~250 km^2 of ice extent lost) and thus in the amount of contact with its sidewalls and with the tongue of Haynes Glacier (Figure 1b) through this period."

Lines btw 30-35: "not straightforward" => "challenging"
Done

Page 4
Lines btw 30-: How is the uncertainty propagated for the values predicted by the quadratic function where there is no data at all? This uncertainty should increase (substantially) as the predictions get further away from the period constrained by data.

Added "While we are unable to formally calculate the uncertainty of the surface elevations produced by this extrapolation, we estimate it as 50% of the change from the earliest measurement (in 2003)."

Lines btw 30-: Not sure I understand the following statement: "The results from this method more closely match the available ICESat-1 data than using the elevation and thinning rate from 2004 alone, as was done in Mouginot et al. (2014)". In what sense it matches better ICESat (2003-2009), which is outside of the extrapolated range (1996-2002)?
Expanded this sentence to: "To assess relative to previous methods, we calculated estimated surface elevations for 2003-2008 using this quadratic function to test its ability to match the available ICESat-1 data. Residuals are smaller than those resulting from using a quadratic fit to the elevation and thinning rate from 2004 alone, as was done in Mouginot et al. (2014)."

Page 5

Lines btw 5-10: "The thinning rates on the grounded ice are more accurate since they lack tidal effects". This is not the main reason why altimetry thinning-rate estimates may be more accurate over grounded ice. Over (rapidly-changing) grounded ice the signal-to-noise ratio is much higher than over floating ice where the altimeter only "see" about 10% of the thickness-change signal due to hydrostatic balance. Also, tide models are reasonably good (outside of the grounding zone) at the current stage.
Indeed, this effect is large. We have update the text to: "The thinning rates on the grounded ice are more accurate because the entirety of any change to thickness is manifest in the surface elevation while over floating ice ~90% of the thickness change is accommodated through raising the ice bottom due to hydrostatic balance. Thus, we smoothed the thinning over the shelves for 10 km downstream of the grounding line to preserve continuity and reasonable surface slopes."

Lines btw 15-20: "This method reduces many of the artifacts that can occur when interpolating sparse ice thickness measurements while avoiding making any assumptions about the present state of balance (e.g. assumptions for mass conservation methods (Morlighem et al., 2011))". It is still interpolation, right? Meaning that regardless of any "smart" weighting, you don't have information in between the sparse thickness samples. The mass conservation approach uses additional information (velocities) to fill in those gaps. Bottom line, one interpolation method, another interpolation method... it is still interpolation.
We were primarily concerned with pre-empting the criticism that we should have been using a mass-conserving bed. We have updated the text to clarify that this is just a different interpolation method. We added: "though like other methods used to interpolate radar data it still has high uncertainty due to the sparseness of the underlying radar profiles."

Page 7
Line 1: "m_s is the basal melt rate". m_s => m_b
Thanks, fixed.

Line 5: I think a more appropriate reference for RACMO2.3 SMB is "Van Wessem et al. (2014)".
We have updated the text and figure to use the 20% error that Van Wessem et al. estimate rather than that used in Depoorter. This sentence now reads "For the SMB, we use the annual mean for 1979-2013, which has an uncertainty of ±20% (Van Wessem et al., 2014)."

Page 8
Line 16-17: "but this choice should not have affected the overall spatial pattern". How sure can you be about this (i.e. what is the effect of many small artifacts on the overall result)?
We cannot be positive, but this would generally be more worrisome if we had found areas with strengthening and weakening intermingled, where regularization may have forced an entirely different solution. Rather, we find areas in which we infer weakening, and expect that regularization would just diffuse these areas. We have updated the text to read "The lack of regularization may have concentrated the weakening or strengthening into smaller areas than would have been found with regularization, but any solution, regularized or not, likely would have to introduce weakening into these same areas in order to reproduce velocity field. Thus, the lack of regularization likely did not affect the overall spatial pattern of weakening."

Page 9
Line 9: "and any additional amount entering the shelves in each year". Suggest adding "by precipitation over the ice shelves" or "through ice-shelf surface accumulation".
We have clarified the three categories of incoming flux that we are partitioning. This sentence is now "The incoming flux consists of ice-shelf surface accumulation and the flux across the grounding line; we partition the grounding-line flux into a steady-state amount (i.e. the accumulation in the catchment upstream) and any additional amount (in excess of steady state) entering the shelves in each year."

Page 10
Lines 12-13: "would not substantially alter our qualitative conclusions". You can remove "qualitative" here.
Done

Lines 8-9: "implying that we likely underestimate the error in our melt and flux calculations". Not necessarily. The discrepancy in the thinning rates on those studies is mostly due to some using a 5-year (laser) altimetry record while the other using an 18-year (radar) altimetry record. So, the different thinning rates are likely representing different timescales. For example, as shown more recently by Paolo et al. (2018), there are large fluctuations in ice-shelf thickness at ENSO timescales (~4-5 years), a time span comparable to the ICESat period.
Indeed, there may be real variability incorporated into these differences, but in the case of Dotson it is almost certainly error. Paolo et al. 2015 show the trend in thickness in the extended data, and it is very nearly linear in the longer timeseries. Since this longer record encompasses the time covered by the laser record, the factor of 2 difference in estimated thinning rate is not just a sampling effect on real variations, though perhaps some of it is. We have updated the text to reflect the possibility that a component of the discrepancies results from variability. The relevant text now reads: "The thinning rates measured via radar altimetry use a longer time series

of thickness data (Paolo et al., 2015), and so we expect these values to be more representative of the average thinning over our study period than previous laser-altimeter based estimates, which range from 36-63 Gt a^{-1} (Depoorter et al., 2013; Pritchard et al., 2012; Rignot et al., 2013; Shepherd et al., 2010). Some of the range in measured thinning may reflect real multi-annual variability (Paolo et al., 2018) that is sampled differently during the 5-year laser-altimetry record compared to the 18-year radar-altimetry record. However, even if this discrepancy reflects real variability, we likely underestimate the error in our melt and flux calculations by using a temporally constant thinning rate and propagating only the stated error from Paolo et al. (2015). While using different thinning rates substantially alters the estimated melt, melt rates on Dotson calculated using any of these values are larger than the grounding-line flux. Thus, using a different thinning rate within the range of published values would not substantially alter our conclusions, though it would imply greater magnitude of melt."

Page 11
Line 5: "ice that is thinner and cooler than expected" => ???
Added "This effect is likely not real, but rather is introduced by the model as compensation for poor estimates of temperature and thickness at the calving front."

Page 13
Lines 13-14: "the downstream increase in thickness is large compared to the SMB". Can you provide the typical magnitude of SMB over this region (e.g. from RACMO) to put things in context?
Done. Rates from RACMO range from 0.48 to 1.21 m/yr.

Page 16
Lines 16-24: When estimating basal melt rates using ice-shelf surface height changes (e.g. estimates derived from altimetry), there is a substantial uncertainty associated with fluctuations in surface mass balance, which can have large amplitudes at seasonal-to-interannual timescales. Moreover, it has been shown that, often, increase basal melting and surface height change are out of phase (i.e. they can go in opposite directions) (e.g. Paolo et al., 2018).
We have reworked this section in response to the general comments of this reviewer, though this point remains relevant. We have added the following: "While Gourmelen et. al (2017) are able to compute spatially resolved melt rates beneath all of Dotson, their altimetry-based method has greater sensitivity to certain errors than the methods we employ. The amount of snow on an ice shelf significantly influences surface elevations because the lower-density snow does not hydrostatically depress the shelf as much as an equivalent thickness of ice. Thus, uncertainty in SMB leads to significant uncertainty in thickness changes, particularly because SMB may be inversely correlated with basal melt on seasonal-to-interannual timescales (Paolo et al., 2018). Moreover, mismeasurement of the surface elevation is increased tenfold in estimating the melt rate using altimetry-based methods, leading to substantial uncertainty. Our method is primarily sensitive to horizontal flux divergence, so it is less sensitive to errors in surface elevation and SMB than the method of Gourmelen et al."

Line 28: "similar" => comparable
Done

Line 28: "changes in melt" => changes in basal melt
Done

Line 30: "were associated" => by whom?
We changed this sentence to the active voice: "We find that thinning and speedup early in the study period are likely an ongoing response to earlier changes."

Line 32: "total basal melt was further increased" => by whom? Please avoid the passive voice. It is not clear whether you are stating known facts (from the literature) or stating your conclusions.
We clarified what has been established previously and made this sentence active: "Similar to previous studies, we show that basal melt rates increased on areas that were floating throughout the study period, and we find that total basal melt was further increased as ungrounding exposed more area to melt. "

Line 34: "A change in ocean forcing years or decades before 1974 likely led to in Dotson's imbalance in 1996". This is highly speculative, particularly regarding "a change in ocean forcing". It is OK to speculate but clarify (in the Summary) what led you to this conclusion.
We amended this sentence to make explicit that this is our speculation. The sentence is now: "These conditions lead us to speculate that change in melt, likely resulting from a change in ocean forcing years or decades before 1974, may have led to in Dotson's imbalance in 1996. "

Page 17: Lines 4-6: Are you suggesting this as future work? If so, please clarify you are pointing the future direction of work needed; and justify why we would need such direction (i.e. what's the relevance in the context of understanding and predicting future ice-shelf/icesheet loss).
We have added an additional sentence to state the importance and clarified that we are suggesting this as future work. The last lines now read: "Determining the initial cause of change to this system is key to understanding whether the present retreat results from ongoing oceanic or climatic changes, natural variability, or internal instability, and thus important for placing these observations in the context of other changes to submarine basins around Antarctica. In the future, prognostic modeling of this system beginning in 1996 or before (i.e. "hindcasting"), could help test how different initial perturbations to the system would have affected its flow speed and mass balance, and thus provide context to these changes relative to those observed in other glaciers."

Supp. Page 2:
Line 18: "and we are unsure of the exact method used by Khazendar et al". Why don't you ask them?
We emailed Ala Khazendar, and he indicated that he thought this point anomalous. Those authors had referred to an anomalous point in the text, though the connection between that portion of the text and this particular measurement had not been clear to us. We thus eliminated the speculation that interpolation caused this discrepancy and note only that they identify that point as anomalous. The relevant text now reads "…our values for the thinning rate agree to within error for the 27 points that they do not identify as anomalous (Table S2)." Additionally,

we have added a note to the caption of table S2 stating: "Note that Khazendar et al. identify point 24 as anomalous, though the value we calculate is similar to others in the area."

Changes in flow of Crosson and Dotson Ice Shelves, West Antarctica in response to elevated melt

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Abstract. Crosson and Dotson Ice Shelves are two of the most rapidly changing outlets in West Antarctica, displaying both significant thinning and grounding-line retreat in recent decades. We used remotely sensed measurements of velocity and ice geometry to investigate the processes controlling their changes in speed and grounding-line position over the past 20 years. We combined these observations with inverse modeling of the viscosity of the ice shelves to understand how weakening of the shelves affected this speedup. These ice shelves have lost mass continuously since the 1990s, and we find that this loss results from increasing melt beneath both shelves and the increasing speed of Crosson. High melt rates persisted over the period covered by our observations (1996-2014), with the highest rates beneath areas that ungrounded during this time. Grounding-line flux exceeded basinwide accumulation by about a factor of two throughout the study period, consistent with earlier studies, resulting in significant loss of grounded as well as floating ice. The near doubling of Crosson's speed in some areas during this time likely is the result of weakening of its margins and retreat of its grounding line. This speedup contrasts with Dotson, which has maintained its speed despite high, increasing melt rates near its grounding line, likely a result of the sustained competency of the shelf. Our results indicate that changes to melt rates began before 1996 and suggest that observed increases in melt in the 2000s compounded an ongoing retreat of this system. Advection of a channel along Dotson, as well as the grounding-line position of Kohler Glacier, suggest that Dotson experienced a change in flow around the 1970s, which may be the initial cause of its continuing retreat.

1 Introduction

Glaciers in the Amundsen Sea Embayment are susceptible to internal instability triggered by increased ocean melting of buttressing ice shelves and are currently the dominant source of sea level rise from Antarctica (Shepherd et al., 2012). Observations (Rignot et al., 2014) and modeling (Favier et al., 2014; Joughin et al., 2010, 2014) suggest that collapse is potentially underway on Pine Island and Thwaites Glaciers, the largest in the region. The neighboring Smith, Pope, and Kohler Glaciers thinned at 9 ma^{-1} just upstream of their grounding lines from 2003-2008, outpacing the mass loss of those larger catchments in relative terms (Pritchard et al., 2009). The lower reaches of these glaciers, which discharge to Crosson and Dotson Ice Shelves (for brevity, we hereafter refer to these ice shelves simply as Crosson and Dotson), doubled their speeds, as their respective grounding lines retreated by as much as 35 km in places from 1996 to 2011 (Rignot et al., 2014). During this same period, portions of Crosson sped up at a rate comparable

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to the grounded areas upstream, while Dotson remained at near-constant velocity (Mouginot et al., 2014). Thus, this pair of ice shelves with differing speedup but similar incoming fluxes and neighboring catchments provides an ideal area in which to study the processes controlling ice-shelf stability.

5   Ice shelves affect upstream dynamics by exerting stresses at the grounding line. For ice masses, the driving stress, τ_d, is resisted by basal drag, τ_b, longitudinal stress gradients, τ_L, and lateral stress gradients, τ_W. To maintain force balance, any reduction in resistance must be compensated by increases in other forces. This adjustment generally causes the glacier to speed up to increase strain-rate dependent stresses (τ_L and τ_W) within the ice. Reduction in ice-shelf resistance (also called buttressing) can be caused by thinning (e.g. from increased basal melt) or changes in
10   extent (e.g. from shelf breakup or increased calving). Weakening of ice-shelf margins, due to heating, fabric formation, or crevassing or rifting (through-propagating crevasses) also effectively reduces the lateral stress gradients and reduces buttressing (Borstad et al., 2016; Macgregor et al., 2012). Despite either mechanical or rheological "weakening", marginal ice can still exert a greater resistance to flow as a glacier speeds up due to the dependence of stress on strain rate.

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Areas of compression and tension in ice shelves have been identified as key to shelf stability (Doake et al., 1998; Sanderson, 1979). There is generally a region of tensile stress near the calving front, while upstream of this region, some components of the stress tensor are in a compressive regime; the boundary between the two is often arcuate, and thus is referred to as a "compressive arch." Changes seaward of the arch have little effect on upstream dynamics since
20   the shelf is essentially freely spreading in this region. Changes at or upstream of the arch, such as rifting, or other weakening, can cause widespread speedup because compression, and thus resistance to upstream flow, is reduced.

The dynamics and stability of ice shelf/ice stream systems are also strongly controlled by grounding-line position. Retreat of the grounding line along a landward-sloping (retrograde) bed causes imbalanced flux due to the nonlinear
25   dependence of ice flux across the grounding line on ice thickness there in what is termed the marine ice-sheet instability (Weertman, 1974). Theoretical work has shown that, once perturbed, a grounding line on a retrograde bed will retreat until it reaches a prograde slope (Schoof, 2007). Additionally, ungrounding increases the sensitivity to melt by exposing more ice to the ocean (Jenkins et al., 2016). In the case of a retrograde bed, the deepening of the grounding line caused by ungrounding also increases melt because the melting point decreases with depth. For glaciers
30   along the Amundsen Sea, this effect can be intensified because warm, dense circumpolar deep water generally intrudes at depth and results in elevated melt at deeper grounding lines (Jenkins et al., 2016; Thoma et al., 2008). Retreat of the grounding line thus causes both imbalanced flux at the grounding line and allows elevated melt rates beneath floating ice. Theoretical arguments provide some insight into the importance of rifting, ungrounding, and loss of buttressing in idealized conditions, but their role in controlling flow during complex evolution of real ice streams is
35   not fully known. Here we investigate the role of these processes in recently observed speed and thickness changes of Crosson, Dotson and their tributary glaciers.

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1.1 Study Area

Pope Glacier and the eastern branch of Smith Glacier together feed Crosson, while the western branch of Smith Glacier and Kohler Glacier feed Dotson (Figure 1). The terminology for these tributaries has varied in the literature, and we adopt the names used in Scheuchl et al. (2016) for consistency and clarity. The largest grounding line retreat (>2 km

5 a^{-1}) occurred in the area where the branches of Smith Glacier flow together before splitting into their respective shelves (Figure 2). The grounding-line position of Smith Glacier was relatively stable from 1992 to 1996, but it then retreated substantially in the 18 years following (Rignot et al., 2014; Scheuchl et al., 2016). By contrast, the grounding line of Kohler experienced limited retreat (~0.2 km a^{-1}) from 1996 to 2011 and subsequently re-advanced to near its 1996 position by 2014 (Scheuchl et al., 2016). Though data are unavailable for intermediate dates, Pope Glacier's grounding

10 line retreated by 11.5 km (0.64 km a^{-1}) from 1996 to 2014 (Scheuchl et al., 2016). The ice generally thinned most strongly over the areas that ungrounded and up to ~15km upstream (contours in Figure 2). This correspondence between thinning and retreat is spatially coincident with speedup, which was strongest over grounded portions of Smith Glacier. Ice speeds in the strongly thinned, grounded area and downstream on Crosson peaked in 2009 and 2010 then declined slightly by 2014. There were also significant changes in the extent of ice at the margins of Crosson

15 (~250 km² of ice extent lost) and thus in the amount of contact with its sidewalls and with the tongue of Haynes Glacier (Figure 1b) through this period. Digitized shelf-front positions throughout the ASE indicate extensive rifting of Crosson, resulting in detachment from both of its margins, as well as breakup of the Haynes Glacier tongue from 1984 to 2004 (Macgregor et al., 2012), which could have reduced the ability of the shelf to transmit resistive stresses. No similar changes in extent were observed over Dotson.

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The extensive and synchronous changes in the ASE have mainly been attributed to changes in basal melt (e.g. Joughin et al., 2012 and references therein) caused by warming ocean water or increased intrusion of warm, salty circumpolar deep water (Jenkins et al., 2010; Pritchard et al., 2012; Thoma et al., 2008). Recent work has used radio echo sounding (RES) data to infer thinning rates of 70 m a^{-1} (Khazendar et al., 2016), but the extent of these estimates is limited in

25 space and time, and converting to a melt rate requires assumptions about the magnitude of dynamic thinning in the area, and about the steady-state melt rates. Gourmelen et al. (2017) used thinning rates from Cryosat-2 to obtain a more spatially complete record of melt rates under Dotson, particularly focusing on melt rates in a channel beneath the shelf (Figure 1), and found that melt rates in the channel are much higher than the surrounding ice (though lower than at the grounding lines of Smith and Kohler). Observations of ocean temperature in front of Crosson are sparse

30 due to persistent sea ice and ice mélange, though there are observations elsewhere in nearby Pine Island Bay (Jacobs et al., 2012; Wåhlin et al., 2013). Recently, the front of Dotson has been better instrumented, and observations show inflow at the eastern margin of the shelf and outflow at the western margin (Ha et al., 2014; Miles et al., 2015), indicating clockwise circulation beneath the shelf. The inflow is persistently warm at depth while the outflow is cooler and fresher, indicating the presence of meltwater. Available data suggest that in 2006, water in Pine Island Bay, which

35 may access Crosson, was about 0.7°C warmer, and less variable in temperature, than the inflow to Dotson (Jacobs et al., 2012; Walker et al., 2007). However, attempting to infer melt rates beneath the shelves from these few

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measurements is challenging. Furthermore, sub-ice-shelf bathymetry has only recently become available (Millan et al., 2017), limiting model-based analyses of ocean circulation beneath these shelves.

Previous ice-flow modeling, which excluded the floating ice, suggested that these glaciers will continue to retreat even in the absence of a change in forcing (Goldberg et al., 2015). Since changes in the ASE are thought to be ocean-forced, however, understanding of processes over the floating ice and at the grounding line are key to explaining recent behavior and to any prediction of future behavior. Here we use remote-sensing observations of ice velocities, surface elevations, and ice-bottom elevations of these ice shelves through time to determine the partitioning of their mass loss and to constrain snapshot inversions of their viscosity. We use the history of melt, terminus position, and shelf viscosity to understand the causes of changes to these shelves' mass balance and speed.

2 Data

Before describing the calculations of mass loss and modeling, we first summarize the data used in this study.

2.1 Velocity

Surface velocities were obtained from both synthetic aperture radar (SAR) and optical satellites. The SAR velocities come from the European Remote-sensing Satellites (ERS-1 and -2) for 1996 and the Advanced Land Observation Satellite for 2006-2010. These SAR data were processed using a combination of interferometry and speckle tracking (Joughin, 2002). We used feature tracking of Landsat-8 imagery to obtain velocities for the 2014-2015 austral summer. Velocity data for 2006 and 2011 are part of the NASA Making Earth System Data Records for Use in Research Environments (MEaSUREs) data set (Mouginot et al., 2014). Errors range from a few meters per year over slower grounded ice to >100 m a^{-1} over Dotson in 1996 due to the short satellite repeat period and errors introduced by tidal displacement.

2.2 Surface elevations

To estimate past surface elevations, we began with elevations from a high-quality digital elevation model (DEM) with elevations relative to the EGM2008 geoid. This reference surface is a mosaic DEMs created through processing of stereo imagery from the DigitalGlobe WorldView/GeoEye satellites (Shean et al., 2016), using imagery spanning 2010-2015. Most of the stereo pairs used to create this mosaic come from the 2010-11, 2012-13, and 2013-14 austral summers, so we assign the mosaic an approximate timestamp of January 1, 2013. This surface elevation product is posted at 32m, and we estimate the error to be ±1.0 m. To find surface elevations in different years, we added the observed thinning rates, as discussed below, to this reference surface. Because there are published estimates of thinning rates over the ice shelves (Paolo et al., 2015; Shepherd et al., 2004), we used these rates for floating ice and addressed grounded ice separately.

Over grounded ice, we used thinning rates derived from a combination of points from ICESat-1 and the Airborne Topographic Mapper (ATM) as well as DEMs produced from stereo pairs of Worldview imagery; details of how this

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time series was produced can be found in Appendix A of Goldberg et al. (2015). These observations of surface elevation span 2003-2015, necessitating extrapolation to determine elevations at the beginning of our study period. To extend to 1996, we fit a quadratic function to each pixel of the 2003-2014 elevation change record; the use of a quadratic description of the thinning follows previous work (Wingham et al., 2009). We then used these thinning functions to calculate surface elevations over these glaciers during 1996-2002. To assess relative to previous methods, we calculated estimated surface elevations for 2003-2008 using this quadratic function to test its ability to match the available ICESat-1 data. Residuals are smaller than those resulting from using a quadratic fit to the elevation and thinning rate from 2004 alone, as was done in Mouginot et al. (2014). While we are unable to formally calculate the uncertainty of the surface elevations produced by this extrapolation, we estimate it as ~50% of the change from the earliest measurement (in 2003).

Over floating ice, we used 1994-2012 thinning rates derived from satellite radar altimetry data by Paolo et al. (2015). The results from Paolo et al. (2015) show little spatial variability over these particular shelves, and so we used the thinning rates for the middle of each shelf where low surface slopes should lead to the smallest errors. These values were 3.1 m a^{-1} for Crosson and 2.6 m a^{-1} for Dotson. Because of relatively high surface slopes and the 30-km resolution of these estimates, the thinning rates are not accurate fully to the margins of the shelves, and there are ~5 m a^{-1} differences in our thinning function upstream and downstream of the grounding line. The thinning rates on the grounded ice are more accurate because the entirety of any change to thickness is manifest in the surface elevation while over floating ice ~90% of the thickness change is accommodated through raising the ice bottom due to hydrostatic balance. Thus, we smoothed the thinning over the shelves for 10 km downstream of the grounding line to preserve continuity and reasonable surface slopes.

2.3 Ice-bottom Elevations

We use a 1-km bed elevation dataset generated from all available airborne RES data with an anisotropic interpolation routine that weights measurements along flow more heavily than those across flow; details can be found in Medley et al. (2014) and the supplementary materials to Joughin et al. (2014). This method reduces many of the artifacts that can occur when interpolating sparse ice thickness measurements, while avoiding making any assumptions about the present state of balance (e.g. assumptions for mass conservation methods (Morlighem et al., 2011)), though like other methods used to interpolate radar data it still has high uncertainty due to the sparseness of the underlying radar profiles. We assume bed elevation errors of ~50 m for the study area.

Over floating ice, we used the surface elevation for a given year and an assumption of hydrostatic equilibrium to calculate the elevation of the lower ice surface. In doing so, we first determined the firn-air content by choosing the value that minimizes the misfit in ice thickness between coincident surface elevation (converted to ice thickness by subtracting the air content and assuming floatation) and ice thickness measurements; elevation and thickness measurements were taken from the ATM and Multichannel Coherent Radar Depth Sounder (MCoRDS) flown on NASA's Operation IceBridge. The ice thickness measurements from the MCoRDS radar are calculated from the two-

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way travel time of the radar using a wave speed for pure ice, but the air content in the firn changes the radar wavespeed. In our minimization, we convert the thickness to a travel time, reversing the MCoRDS processing methods, then convert the travel time back to thickness using a wavespeed that accounts for the air content of the firn. This approach provides point measurements of firn-air content along tracks separated by several kilometers, which we then gridded and subtracted from the surface elevation, resampled to 400-m posting, before applying the assumption of hydrostatic equilibrium to compute the ice bottom elevation. We find the firn-air content to range between 12-18 m across most of the ice shelves (Supplementary Figure S2); a firn model forced with output from RACMO2.3 shows greater firn-air content than we observe, generally between ~20-25 m over these shelves (Ligtenberg et al., 2011). Residuals between the ice thickness obtained using firn-air content estimates and direct measurements of ice thickness from MCoRDS have an RMS of 22 m. This error is larger than the ~10-m crossover precision in the MCoRDS data in this area, but comparable to the absolute accuracy of those measurements, which include error from uncertainty from the dielectric constant, limited sampling rate, and uncertainty in picking the reflector.

2.4 Ice-front positions

We digitized the shelf-front positions of Crosson and Dotson from 2012 to 2016, extending the earlier 1972-2012 record (Macgregor et al., 2012). The shelf-front positions were traced on Landsat-8 imagery, using the panchromatic data (band 8). Shadowing and brightening of steep areas causes an approximately four-pixel (±60m) nominal uncertainty in the front position, though actual error is ~500m on Crosson due to ambiguity in discriminating between ice front and persistent mélange.

3 Methods

We derived annual flux, melt, and calving rates through time using the observed velocity and ice thickness. We compared these values to flux at the grounding line and accumulation on the shelves to determine changes in the ice-shelf mass balance. Since stresses in the ice cannot be measured remotely, we performed snapshot inversions for viscosity using a numerical model to quantify how changes in velocity and geometry affected the stress balance and strength of Crosson and Dotson.

3.1 Flux and melt calculation

Following earlier work (Mouginot et al., 2014), we used the average of five closely spaced gates to calculate inflow and outflow fluxes along the shelf boundaries. For grounding-line flux, gates were drawn at 2-km intervals beginning just upstream of the 2014 grounding line. Onto each gate profile, we interpolated surface and bed elevations and the component of velocity orthogonal to the gate. We filled gaps < 3km wide via 2-D linear interpolation of surrounding velocities and filled larger gaps by 1-D linear interpolation between the velocities at that point the two closest years with sufficient coverage. Where we have velocity data, we take the error to be the formal value, and where we have interpolated we estimate it to be the difference between the interpolated value and the values at neighboring years.

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We calculated melt rates over different portions of the shelves to understand the spatial distribution of melt. Basal melt is effectively a downward flux of ice out of the shelf bottom, so to calculate melt we divided the shelves into polygons (Figure 3a), calculated the incoming and outgoing flux for each polygon, then used mass conservation to determine the melt rate. We used the average flux through five parallel gates on each side of the polygons to reduce

5 errors in the horizontal fluxes. Where possible, we located the upstream sides of the polygons over ice that was grounded in 1996 to reduce errors in the velocity caused by tidal variation over the short repeat cycle employed by ERS during this period. We estimate the error in the margins of floating ice, which propagates to error in the area, to be 5%; this error does not affect our calculation of melt for individual polygons, but does affect our estimate of total melt on each shelf. To relate the flux into and out of a polygon to the melt rate, we integrated the mass change of the

10 polygon and applied divergence theorem:

$$\int_{\Omega} \dot{m}_b \, dA = \int_{\Omega} \left(-\nabla \cdot \boldsymbol{Q} + \dot{m}_s + \frac{\partial H}{\partial t} \right) dA = -\oint_{d\Omega} \boldsymbol{Q} \cdot \hat{\boldsymbol{n}} ds + \int_{\Omega} \left(\dot{m}_s + \frac{\partial H}{\partial t} \right) dA \qquad (1)$$

where $\dot{m}_b$ is the basal melt rate, $\boldsymbol{Q}$ the depth-integrated flux, $\dot{m}_s$ the surface mass balance (SMB, water equivalent), $\frac{\partial H}{\partial t}$ the thickness change, Ω a polygon with boundary dΩ, $\hat{\boldsymbol{n}}$ the unit normal to the boundary, $\boldsymbol{A}$ the area of the polygon, and $\boldsymbol{s}$ the distance along the boundary. To determine melt rates from the flux balance of each polygon, we used the

15 rate of thickness change from Paolo et al. (2015) and SMB from RACMO2.3 (Van Wessem et al., 2014). For the SMB, we use the annual mean for 1979-2013, which has an uncertainty of ±20% (Van Wessem et al., 2014). The assumption of a spatially uniform thinning rate for each shelf introduces additional error that is difficult to quantify, but without more measurements of surface change this difficulty is unavoidable. We computed mass loss rates for both ice shelves and catchments. The former is useful because the ablation on the shelves is greater than the grounding

20 line flux, causing them to lose significant mass annually, while the latter gives an indication of the system's contribution to global sea level rise and is useful for comparison to other studies.

3.2 Modeling

We used a diagnostic model implemented in Elmer/Ice (Gagliardini et al., 2013; Zwinger et al., 2007) to infer ice-shelf viscosity. Elmer/Ice is an open-source, finite element software package capable of solving the full Stokes

25 equations in three dimensions, or lower-order approximations to ice flow such as the shallow-shelf equations (Gagliardini et al., 2013; MacAyeal, 1989). We used a three-dimensional, full-Stokes model with separate domains for grounded and floating ice. While the assumptions of the shallow-shelf equations are likely applicable at least to the floating portion of our domain, we implemented the Full-Stokes model to accurately capture the effects of ~10 pinning points beneath these shelves and avoid approximations to the stress state.

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We performed multiple diagnostic runs in which we varied the model geometry to reflect different years, which allowed us to infer properties through time as a series of snapshot inversions. The upstream margins of the model domain were located at the divides in ice flow, determined from InSAR velocity measurements. We found the downstream margin using the digitized shelf-front positions described above. The grounding-line positions from

35 (Rignot et al., 2014; Scheuchl et al., 2016) were used to determine the boundary between the grounded and floating

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domains for each year. We used these horizontal extents, in conjunction with the different surface and bed DEMs described above, to create a suite of three-dimensional model meshes using the software GMSH (Geuzaine and Remacle, 2009). These horizontally unstructured meshes have a resolution of ~300-m over floating ice. The meshes have eleven vertical layers, with six of these in the bottom third to capture the zone of maximum internal deformation; there is little internal deformation over most of the floating domain, but this concentration of layers is useful for capturing temperature gradients in the ice column and dynamics around pinning points.

To obtain an initial estimate of viscosity for the enhancement factor inversions, we first determined a temperature profile in the ice. This initial estimate was made using a steady-state thermo-mechanical model in Elmer/Ice. The model solves the Stokes equations to determine advection, with ice viscosity as a function of temperature, and solves an advection-diffusion equation for heat using limiters to prevent ice from going above the pressure-melting point (Zwinger et al., 2007). Strain heating and frictional heating at the bed were both included in this temperature model. For boundary conditions, we used surface temperatures from RACMO2.3 (Van Wessem et al., 2014) and geothermal heat flux estimates from geomagnetics (Maule et al., 2005). We first ran the temperature model over grounded ice; the downstream temperatures from the grounded ice were then used as the upstream boundary condition for a similar model of the floating ice.

After obtaining an initial viscosity from the temperature model, we used inverse methods to infer the enhancement factor that produced modeled velocities that best match observations. The enhancement factor alters the viscosity of the ice relative to that predicted solely by modeled temperature. It would be possible to use the model to find a depth-variable enhancement factor, but, to have the number of degrees of freedom in the inversion match the number of observables, we instead determined a single depth-independent value. We began with a profile of viscosity with depth from the temperature model, and used adjoint methods (MacAyeal, 1993; Morlighem et al., 2010) to infer an enhancement factor that results in the best fit to observations for each column of ice. Because we were inferring variations along shear margins with sharp transitions in velocity, temperature, and rheology, we did not apply regularization to the inversion for the enhancement factor, and simply minimized the areally integrated misfit between observed and modeled velocity. The lack of regularization may have concentrated the weakening or strengthening into smaller areas than would have been found with regularization, but any solution, regularized or not, likely would have to introduce weakening into these same areas in order to reproduce the velocity field. Thus, the lack of regularization likely did not affect the general spatial pattern of weakening.

For boundary conditions, we used observed surface velocity for all depths over lateral margins (including shear margins, calving front, and grounding line). For the basal boundary, we used zero basal shear stress over floating ice and basal shear stress equal to half the driving stress over the pinning points observed from SAR grounding lines.

3.3 Stress Changes

The location of changes in rheology relative to the compressive arch is an important factor in determining whether those rheological changes affect the broader flow patterns of the shelf. To determine the location of the compressive arch on Crosson and Dotson, we used the modeled stress field to calculate the stress associated with shelf spreading, $\tau_L = 2\bar{\tau}_{xx} + \bar{\tau}_{yy}$ where $\bar{\tau}_{xx}$ and $\bar{\tau}_{yy}$ are the depth averaged deviatoric stresses along and across flow. We chose this criterion because where it is compressive it shows resistance to spreading upstream and where it is tensile it indicates a spreading shelf not resisting flow. This approach differs from previous literature, which used the second principal stress to identify compressive arches; other studies choose that criterion in part because the first principal stress is consistently tensile (Doake et al., 1998), which is not the case on Crosson and Dotson, and so ignoring the first principal stress misses an important aspect of the stress balance here.

4 Results

4.1 Flux and melt

Figure 3 shows the components of the flux balance of Crosson and Dotson throughout the study period. The three columns for each year show the outgoing flux, incoming flux, and loss, respectively. The outgoing flux is partitioned into the melt on different portions of the shelves and the calving flux. The outgoing flux from some polygons is equal to the incoming flux of others; when adding all the melt together the flux across these internal boundaries cancels, leaving the total melt on the shelf. The incoming flux consists of ice-shelf surface accumulation and the flux across the grounding line; we partition the grounding-line flux into a steady-state amount (i.e. the accumulation in the catchment upstream) and any additional amount (in excess of steady state) entering the shelves in each year. The difference between the incoming and outgoing fluxes for the shelves provides an estimate of net mass loss from the shelves, while the difference between upstream accumulation and grounding-line flux yields net loss from grounded ice.

The grounding-line fluxes into Crosson and Dotson both exceeded their upstream accumulation in 1996. By 2014, the fluxes across the grounding lines increased by 30% and 60%, respectively. Increases in outgoing flux (calving and melt) outpaced increases in grounding-line flux for both Crosson and Dotson, leading to loss of shelf volume. Due to Crosson's speedup, its calving-front fluxes increased from 1996 to 2010 then declined slightly to 2014, while the calving-front flux from Dotson declined due to both thinning and slight slowdown. Total melt beneath each shelf also increased from 1996 to 2010 and declined slightly to 2014. The melt beneath Dotson (27.7 Gt a^{-1}) in 1996 was higher than beneath Crosson (10.9 Gt a^{-1}). This difference is due in part to the much greater area of the shelf (~5200 km^2 vs ~2400 km^2), but also due to high melt rates near the grounding lines of Kohler and western Smith Glaciers, which feed Dotson. Notably, sub-shelf melt rates on Dotson are greater than the grounding-line flux for each of the years surveyed, resulting in loss of shelf volume irrespective of its calving rate

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Figure 3 also shows melt for different regions of each shelf. The greatest increase in melt occurred on western Smith Glacier (SW1 in Figure 3), but the most intense melt (~23 m a^{-1}) in 1996 was within 10 km of Kohler's grounding line (K1 in Figure 3) and rates there remained high through our study period. Melt rates ~10km farther downstream from Kohler (K2) were lower (~7 m a^{-1}) but doubled during the study period. The areas of western Smith Glacier with the highest melt (SW1 in Figure 3), found both here and elsewhere (Khazendar et al., 2016), had ungrounded since 1996 (Figure 1). Melt rates increased through the study period beneath all portions of Crosson except that nearest the calving front (C2 in Figure 3). Melt over areas that were floating throughout the study period is unaffected by ungrounding, so the increasing melt in these areas is indicative of a change in ocean forcing through this time. By contrast, the decrease in melt rates from 2010-2014 may have been caused either by the ice draft shallowing into cooler water or by a change in ocean forcing.

Table 1 compares our estimates of flux and melt to those from previous studies. Our estimates of grounding-line flux agree with previous estimates (Depoorter et al., 2013; Mouginot et al., 2014; Rignot, 2008; Rignot et al., 2013). Our estimate of the partitioning of the mass loss, however, differs substantially from Rignot et al. (2013) and Depoorter et al. (2013); this discrepancy stems from different values of the calving-front flux, as well as different data used to determine the thinning. Published estimates of thinning rates range from 2.6 m a^{-1} to 5.6 m a^{-1} over Dotson and do not agree to within their stated errors, leading to a difference of 16 Gt a^{-1} when applied to the whole shelf (Paolo et al., 2015; Pritchard et al., 2012; Shepherd et al., 2004). The thinning rates measured via radar altimetry use a longer time series of thickness data (Paolo et al., 2015), and so we expect these values to be more representative of the average thinning over our study period than previous laser-altimeter based estimates, which range from 36-63 Gt a^{-1} (Depoorter et al., 2013; Pritchard et al., 2012; Rignot et al., 2013; Shepherd et al., 2010). Additionally, this longer dataset matches recent, high-resolution radar-based estimates (Gourmelen et al., 2017). Some of the range in measured thinning may reflect real multi-annual variability (Paolo et al., 2018) that is sampled differently during the 5-year laser-altimetry record compared to the 18-year radar-altimetry record. However, even if this discrepancy reflects real variability, we likely underestimate the error in our melt and flux calculations by using a temporally constant thinning rate and propagating only the stated error from Paolo et al. (2015). While using different thinning rates substantially alters the estimated melt, melt rates on Dotson calculated using any of these values are larger than the grounding-line flux. Thus, using a different thinning rate within the range of published values would not substantially alter our conclusions, though it would imply greater magnitude of melt.

4.2 Buttressing

Previous work has shown rifts along the margins causing gradual separation of Crosson from the seaward portion of its embayment between 1984 and 2012 (Macgregor et al., 2012). Our tracing of more recent ice-front positions shows that this separation has continued to the present (Figure 4a). We find that in 2014 the rifts on the eastern margin of Crosson connected to the ice front, effectively detaching the last ~35 km of the shelf from the right side of the embayment (see labels in Figure 4). Since the ice shelf was already separated from its western margin, this detachment left the outer ~35 km essentially as a floating ice tongue within its embayment. Since there have been no large calving

Deleted: estimates (Depoorter et al., 2013; Pritchard et al., 2012; Rignot et al., 2013). We note, however, that the range of published

Deleted: rates leads to much larger errors than those we report propagating only the stated error from Paolo et al. (2015), implying that

Deleted: . Using different thinning rates, prior studies have rates of loss for ca. 2009 ranging from 36 Gt a^{-1} (Depoorter et al., 2013; Rignot et al., 2013) up to 63 Gt a^{-1} (Shepherd et al., 2010).

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events, the central portion of the ice front advanced back to near its 1972 position but provided no buttressing and did not change the force balance.

There was also a progressive loss of contact between the front of Crosson and the Haynes Glacier tongue from 1984-
5   2004 (Macgregor et al., 2012). These changes continued through 2012, and rifting also increased through this period (Figure 4b and c). We found the linear extent of ice along three transects near the front of Crosson through time to determine the portion of the ice front that may have experienced back force from neighboring ice. This ice extent is similar to the calving-front position for Haynes Glacier found in MacGregor et al. (2012), but we used two additional transects to determine the locality of effects on the front of Crosson, the Haynes tongue, and the Thwaites tongue. We
10 find a generally decreasing trend starting at least as early as 1984, with reduction to almost no area in contact by 2004 (Figure 4d). The approximately steady decline of this tongue suggests there was no sudden drop in resistance at the margin of Crosson, and any speedup caused by the breakup of this tongue would most likely have been gradual, beginning at least as early as the 1980s and continuing into the 2000s.

15 **4.3 Modeled Weakening**

Figure 5 shows the inferred enhancement through time from the diagnostic model, which indicates a reduction in the strength of Crosson's margins from 1996 to 2014. By contrast, there is no notable change in the inferred rheology of Dotson. Stiff ice at the calving front of Crosson is similar to results from Thomas and MacAyeal (1982), which they attribute to ice that is thinner and cooler than expected. This effect is likely not real, but rather is introduced by the
20 model as compensation for poor estimates of temperature and thickness at the calving front. The general pattern of weakening is consistent with areas of high shear, where increases in strain heating, crystal fabric, or rifting could have caused a positive feedback with speedup; faster ice motion could have caused weakening through strain heating or rifting, allowing further speedup. Because we do not account for spatial variability of thinning within each shelf, what we interpret as weakening could in fact be a result of thinning; i.e. we may infer weaker ice in regions where ice is in
25 fact simply thinner. Similarly, areas where the model identifies strengthening may result from local thickening on those portions of the shelves. While this ambiguity prevents us from interpreting changes in enhancement as a particular physical process, it does not adversely affect our determination of which areas afforded more or less resistance to flow.

5   Discussion

30 Here we examine how variations in ice thickness, melt, and ice strength appear to have affected the flow pattern, grounding line position, and mass balance of these ice shelves. Because of the differing behavior of the shelves, we address different processes over each shelf. On Dotson, melt alone exceeded flux onto the shelf for every year surveyed, implying elevated melt rates at least as early as 1996. Crosson's speedup, which caused more ice to reach the calving front, may have caused its imbalance, and we are unable to determine if Crosson's melt rates would be
35 sustainable in the absence of this speedup. Thus, we first focus on the causes and implications of Dotson's elevated

melt and then discuss Crosson's speedup in the following section. Finally, we compare the estimates of melt from this study to previous work and discuss the implications for the dynamics of the system.

5.1 Causes of Dotson's imbalance

Changes in the Amundsen Sea Embayment have generally been attributed to oceanic forcing (Joughin et al., 2010; e.g. Shepherd et al., 2004). It is possible that an increase in ocean heat content prior to our study period may have contributed to Dotson's observed imbalance. In this case, elevated melt rates on Dotson may have directly led to a retreat of its grounding line, resulting in further exposure to melt and continued retreat. Alternatively, some of the change may have resulted from ongoing thinning. For example, model results indicate a glacier catchment may thin for decades, leading to an abrupt retreat of the grounding line (Jamieson et al., 2012; Joughin et al., 2014). Thus, even modest but sustained thinning could perturb the grounding line from a stable position. In either case, once perturbed, the grounding line may undergo a rapid retreat to another stable position, thus leading to greater exposure of sub-shelf area and elevated melt (e.g. Jenkins et al., 2016). We now present evidence that suggests a large retreat of Kohler's grounding line took place prior to our study period, then evaluate whether ongoing thinning or ocean forcing caused this grounding-line retreat and Dotson's mass imbalance.

5.1.1 Prior retreat of Dotson's grounding line

The bathymetry near Dotson's present-day grounding line suggests that any recent unstable retreat would likely have taken place at Kohler Glacier. While the Smith Glacier grounding line was positioned on a bedrock high in 1996, Kohler Glacier's grounding line was ~1200m deep, just upstream of a ~20 km long retrograde slope (Figure 6b) (Millan et al., 2017). If the grounding line formerly was positioned downstream of this retrograde slope (e.g. dashed line in Figure 6b), it likely would have retreated rapidly if perturbed. The unsustainably high melt rates in this area (K1 and K2 in Figure 3) indicate that such a retreat of Kohler's grounding line had likely taken place recently prior to 1992. The overall mass balance for Dotson implies that exposure of K1 and K2 to ocean forcing would have been the difference between sustainable and non-sustainable melt. Comparing the calving flux and the melt from D1 and D2 alone to the steady-state grounding-line flux (Figure 3) shows that Dotson would have been approximately in balance with 1996 melt rates if only this area had been exposed. Adding in the melt found beneath K1 and K2, even at 1996 rates (the lowest in our study period), however, would have resulted in melt exceeding grounding-line flux. Extrapolating back using current thinning rates of ~2.5 m a^{-1}, most of the shelf would have been entirely grounded 150 years prior, implying that the melt rates within this overdeepening could not have been sustained over centennial timescales. Thus, it is possible that some time in the several decades prior to 1990s, the grounding line retreated several 10s of kilometers from our hypothesized position (Figure 6 dashed line), increasing exposure to melting in the K1 and K2 region (Figure 3).

Velocity data provide an additional constraint on the possible timing of a retreat of Kohler's grounding line. Feature tracking of Landsat imagery gives sparse velocity measurements on Dotson for the period 1974-1982, and comparison of these data with recent velocities suggests that there was no substantial speedup of Dotson from 1974 to the present

(Lucchitta et al., 1994; Rignot, 2008). Speedup near the grounding line usually accompanies ungrounding due to the associated loss of basal resistance, so the lack of speedup suggests any substantial grounding line retreat on Dotson likely took place prior to 1974. Combining this lower limit on retreat initiation with the upper limit placed by the unsustainably high melt rates, we infer that the imbalance began years to decades before 1974. Previous work has

5   found that grounding-line flux over Crosson and Dotson combined approximately balanced accumulation in 1974 (Rignot, 2008). That balance is inferred primarily from speedup of the outer portion of Crosson during that time; however, speedup on the outer portion of the shelf can take place independently of speedup near the grounding line (see section 5.2 below). On the other hand, the near-constant velocities on Dotson from 1974-1996, combined with the imbalance in 1996, suggest that Dotson may have been out of balance in the 1970s. Moreover, even if Dotson's

10 grounding-line flux were in balance with upstream accumulation, the melt rates on the shelf may have been elevated. We therefore consider the available data to be ambiguous about the state of balance from the mid 1970s to early 1990s, and thus reconcilable with this proposed timing of retreat initiation.

In summary, observations of grounding line position and velocity are consistent with past retreat of Kohler Glacier

15 due to marine ice-sheet instability (e.g. retreat from the example position shown in Figure 6b), and this retreat likely occurred in the years to decades before 1974. This consistency does not, however, identify the initial cause of that retreat, which could have been triggered either by an unstable response to ongoing thinning or by an increase in basal melt. To further investigate these two scenarios, we discuss how the present-day geometry of Dotson, particularly a large basal channel (Figure 1c and 6a), informs our understanding of its history of melt and flow.

20 **5.1.2 History of melt**

Surface features on an ice shelf can preserve information about the flow and melt history as ice advects seaward (Fahnestock et al., 2000). To help differentiate whether ongoing thinning or ocean forcing triggered Kohler's grounding line retreat and Dotson's imbalance, we use the large surface trough visible in the surface topography (Figures 1c and 6a) to estimate the onset and spatial extent of changes on Dotson. Present day melt rates in this

25 channel, particularly after it turns towards the ice front, have been previously studied (Gourmelen et al., 2017), but here we focus on the portion of the channel that is transverse to flow. The surface expression of this portion of the channel is 5-10 km wide in a region where ice speeds are 150-200 m a^{-1}. Downstream of this channel, the shelf thickens by ~200 m. In steady state, an ice shelf should only thicken along flow if there is basal freeze-on, high SMB, or a narrowing of the embayment. Dotson has nearly parallel sidewalls and the magnitude of the downstream increase

30 in thickness is large compared to the SMB (~0.5-1.2 m a^{-1}; Van Wessem et al., 2014), so these causes can be eliminated. Previous work (Depoorter et al., 2013; Gourmelen et al., 2017; Rignot et al., 2013) found no evidence of large-scale freeze-on beneath Dotson, and we eliminated the possibility of localized freeze-on being the primary cause of the channel by comparing radar observations to floatation levels. Where marine ice is present, ice penetrating radar generally does not propagate into the saline marine ice layer, hence the radar only records the thickness of the meteoric

35 ice. As result, significant differences between the radar (meteoric-only) and hydrostatic-equilibrium (full column) derived thicknesses indicate the presence of marine ice (Crabtree and Doake, 1986; Robin et al., 1983; Thyssen, 1988).

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No such differences are found for Dotson, indicating little or no marine ice (Further details can be found in the supplementary materials). Thus, having ruled out other causes, we conclude the channel was produced by a transient change in ice flux or melt.

5   The channel originates near the grounding line on the eastern (shelf-right) margin of Dotson and continues along the grounding line to the western (shelf-left) margin and extends to the shelf front. This pattern is similar to the pattern of ocean circulation inferred from oceanographic measurements. Available data show warm inflow at the eastern margin and meltwater-laden outflow at the western margin, indicating clockwise circulation beneath the shelf (Ha et al., 2014; Miles et al., 2015). This circulation pattern suggests that the channel originates where the warm CDW inflow first

10   comes into contact with the ice shelf draft. Generally, melt that begins at depth is sustained by entrainment of additional warm water as the buoyant meltwater plume rises along the underside of the ice (Jenkins, 2011). Basal melt channels have been observed in many locations around Antarctica (e.g. Alley et al., 2016), and are thought to form in the location where the meltwater plume rises along the bottom of the shelf (Marsh et al., 2016; Stanton et al., 2013). The shallowing of this channel as it curves along the grounding line to the western margin of Dotson is

15   consistent with this model of channel formation. The abrupt beginning of the channel on the eastern margin and the continuation of the channel to the shelf front on the left are thus consistent with the available oceanographic constraints. However, high resolution measurements of melt from 2010-2016 do not show high melt rates throughout this channel, but rather localized melt near the grounding line along the western portion of the channel before it turns toward the shelf front (Gourmelen et al., 2017). While ice divergence following the initiation of channel incision may

20   have had an effect on the channel width (Drews, 2015), there is no change in the divergence of the measured surface velocities around the transverse portion of the channel (conversely, along the flow-parallel portion there is significant convergence). Thus, any change in width due to divergence is at or below the level of uncertainty in the velocity measurements, and therefore small compared to the advection of the channel. Thus, the present pattern of melt suggests that transverse portion of the channel is at least partially a mark of past thinning rather than a signal of

25   currently elevated melt.

To constrain the timing of the formation of the channel, we assumed that it resulted from a perturbation at the grounding line and used the 1996 velocity to determine how long the perturbation would take to advect to the current channel location (Figure 6a). For this calculation, we assume the perturbation happens at or close to the grounding

30   line; since grounding line positions and surface elevations before 1992 are unknown, this is the simplest assumption. Additionally, the present-day concentration of melt immediately near the grounding line in the western portion of this channel suggests such an assumption is reasonable (Gourmelen et al., 2017). Estimates for the timing of the perturbation are 30-45 years before 2013 (i.e. 1968-1983) for various points along the channel. This timing is consistent with our inference of when a retreat of Kohler's grounding line may have occurred, suggesting that there

35   were widespread changes in melt near Dotson's grounding line in the decades prior to 1974, and that the channel and the retreat of Kohler's grounding line were both consequences of these changes. This timing is consistent with prior work on the upstream propagation of thinning over these glaciers, which found that thinning initiated around 1970±30

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at the grounding lines of Smith and Kohler (Konrad et al., 2017), as well as with an altimetry-based study of Dotson, which found that the shelf had been thinning for at least two decades but not more than a century (Gourmelen et al., 2017). Grounding-retreat is thought to have begun on other glaciers in the region at a similar time (e.g. Jenkins et al., 2010), but the complex nature of ice streams' response to perturbations prevents interpreting a synchronous change

5   as evidence of synchronous forcing.

While ocean forcing is likely responsible for these changes, we cannot fully eliminate other possibilities. The most likely alternative is that retreat of Kohler Glacier's grounding line, perhaps due to ongoing thinning, resulted in changes to the circulation patterns beneath the shelf, causing increased melt and channel incision. Exposure of deeper

10   ice at Kohler's retreated grounding line could have led to increased melt not only at the grounding line, but also downstream as meltwater from the grounding line entrained warm water. This increased outflow, which would have risen along the bottom of the shelf as it flowed northward along the left margin of Dotson, may have enhanced overall circulation beneath the shelf, incising the channel as additional warm water cycled through the cavity. Such grounding line retreat may have also resulted in speedup and thus dynamic thinning in the area of the channel as the portion of

15   shelf downstream of Kohler thinned and resistance to flow was reduced. Incision of the transverse portion of the channel through dynamic thinning would also be consistent with the low melt rates in that area found by Gourmelen et al. (2017).

5.2 Causes of Crosson's speedup

Understanding the changes in flow in this area, particularly the observed changes in Crosson's velocity, is important

20   for predicting the future stability of this system as well as understanding the causes of increased calving and grounding-line flux through the study period. Crosson's speedup was strongest in two distinct regions: near eastern Smith Glacier's grounding line and near the eastern (shelf-right) margin of the calving front (Figure 2). These two regions suggest that multiple processes may have influenced the speedup, and so we discuss these regions separately.

5.2.1 Speedup of the outer shelf

25   The most notable changes near Crosson's calving front are the loss of the Haynes Glacier tongue and the increased rifting near the eastern margin. The rifts in this area coincide with inferred enhancement from our diagnostic model (Figure 5), suggesting that the strength of this area is important to the flow of the shelf. To understand how this rifting may have affected the shelf, we compared the enhancement to Crosson's compressive arch (contour in Figure 5).

30   The spreading side walls of Crosson's embayment result in a transition from compression to extension that is nearly perpendicular to flow, with most changes to enhancement downstream of this transition (Figure 5). The overall dynamics of Crosson would have been relatively insensitive to weakening seaward of this transition, but changes landward of this transition would have resulted in broad speedup. Because the weakening on Crosson was primarily just in the tensile area, the effects of the weakening would have been isolated to the freely spreading area downstream

35   of the arch, which is consistent with the observed speedup (Figure 2b&c). This weakening is unlikely to have had a

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widespread effect on the shelf dynamics, but breakup of the outer shelf exposes the inner shelf to further weakening. This weakening would involve dynamic effects beyond the immediate vicinity of the rifting/damage, possibly causing speedup upstream on the portions of Crosson that remained at nearly constant velocity through the 1990s and 2000s. By contrast, there has been little weakening of Dotson.

The local nature of the speedup on the outer portion of Crosson suggests a local cause (e.g. the breakup of neighboring ice). Loss of resistance at the shelf front can increase calving rates, reducing lateral contact area and initiating speedup (Cassotto et al., 2015). The Haynes Glacier tongue may have provided a small but critical shear resistance on the corner of the shelf, and the gradual loss of this tongue may have allowed a cycle of increasing speedup and weakening of Crosson's eastern corner. The speedup of this area of the shelf began before the 1990s (Lucchitta et al., 1994; Rignot, 2008) and continued through 2009, and the Haynes tongue broke up throughout this same period. However, due to feedbacks between strain heating or rifting and speedup, the observed Crosson weakening may either have caused or been caused by its speedup, and the simultaneous breakup of the Haynes tongue may have been unrelated or a response to the same forcing that weakened Crosson. Utilizing a parameterization of damage (e.g. Borstad et al., 2016) in a prognostic model, which would let weakening of the shelf evolve with speedup, could help to identify whether these changes initiated with the breakup of the Haynes tongue or some other forcing.

5.2.2 Speedup near the grounding line

Speedup near eastern Smith Glacier's grounding line is most likely associated with loss of basal resistance caused by grounding-line retreat. The grounding line could have been perturbed directly through increased basal melt, either synchronously or asynchronously with the increased melt on Dotson. However, the changes in Crosson's grounding-line position also could be a result of the ungrounding on Dotson. Thinning of western Smith Glacier would have led to thinning of the eastern branch as well. Such thinning could have led to ungrounding of the trunk of eastern Smith Glacier and thus loss of basal resistance, dynamic thinning, and speedup. Finally, we cannot eliminate the possibility that weakening of the outer shelf resulted in this speedup. Prior work has addressed the effect that thinning (equivalently, weakening) over different portions of Crosson and Dotson would have on ice loss upstream (Goldberg et al., 2016), and the areas in which we find weakening encompass several regions that are important for upstream dynamics. That work suggests that while the overall dynamics are insensitive to the bulk of weakening we find here, weakening in key areas, particularly near the Haynes tongue and at the western shear margin, is important for loss of grounded ice upstream, and thus may have influenced speeds near the grounding line as well. The velocity and thinning signatures of these different causes of retreat could be addressed with a prognostic ice-flow model.

5.3 Comparison to previous melt estimates

Despite the limited resolution, the broad spatial and temporal coverage afforded by the methods used here have advantages compared to previous estimates of melt. First, the radar-based methods used by Khazendar et al. (2016) do not directly represent melt but rather anomalous melt under the assumption of no dynamic thinning. Adding the flux divergence recovers the melt rate (Supplementary Table 1 and Supplementary Figure 1) and yields a different

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spatial pattern with higher peak melt (187 m/yr). Irrespective of correction for this dynamic component, these estimates are 1-5 year snapshots of melt at single points, and the interannual variability in melt rates in the region (e.g. Dutrieux et al., 2014; Jacobs et al., 2012) prevents extrapolation through time. Average melt rates beneath the shelves cannot be easily obtained from these point measurements, but the polygon-based methods we use, though limited in spatial resolution, yield average rates beneath large portions of the shelves.

While Gourmelen et. al (2017) are able to compute spatially resolved melt rates beneath all of Dotson, their altimetry-based method has greater sensitivity to certain errors than the methods we employ. The amount of snow on an ice shelf significantly influences surface elevations because the lower-density snow does not hydrostatically depress the shelf as much as an equivalent thickness of ice. Thus, uncertainty in SMB leads to significant uncertainty in thickness changes, particularly because SMB may be inversely correlated with basal melt on seasonal-to-interannual timescales (Paolo et al., 2018). Moreover, mismeasurement of the surface elevation is increased tenfold in estimating the melt rate using altimetry-based methods, leading to substantial uncertainty. Our method is primarily sensitive to horizontal flux divergence, so it is less sensitive to errors in surface elevation and SMB than the method of Gourmelen et al.

The peak regionally-averaged melt rates found in this study (23 m/yr) occur in the same regions (K1, SW1 and SE1) as found in other studies but the values are lower than the locally computed rates (50 m/yr in Gourmelen et. al (2017) and 129 m/yr in Khazendar et al. (2016)). This difference is not surprising, since the polygon-based method we use has limited spatial resolution and thus misses variations in melt rate in small-scale features such as within the channel on Dotson. Over broad scales, flux-gate and altimetry-based methods should agree, and indeed the overall melt rate we find beneath Dotson, 7.7±1.3 m/yr, agrees with the 6.1±0.7 m/yr found by Gourmelen et al. (2017). The lower peak melt rates found here compared to prior studies may also result from our assuming a spatially constant thinning rate over shelves where thinning rates vary substantially (Gourmelen et al., 2017). The shelf-wide rates used here likely cause us to underestimate melt in small polygons where thinning is most rapid (e.g. K1, SW1, and SE1 in Figure 3). Similarly, they may cause us to slightly overestimate melt over broad, slower-changing regions (e.g., D1 and D2), but this effect should be smaller due to the shelf-wide thinning rate being more representative of rates in these regions. On scales smaller than the polygons we use to calculate melt, thinning may reach 50 m/yr (Gourmelen et al., 2017), comparable to flux divergence in these areas. This thinning may cause the polygon-averaged rates to locally underestimate melt by a factor of two and introduce an error in the polygon average that we estimate may be as high as 50% in small polygons near the grounding line.

6 Summary

We used observations of elevation and velocity along with an inverse model to investigate the causes of grounding-line retreat and speedup on Crosson and Dotson ice shelves. These two ice shelves exhibited contrasting responses to changes in forcing, despite comparable grounding-line flux and similar changes in basal melt. Confirming earlier results (Mouginot et al., 2014; Rignot, 2008), we find that both ice shelves were out of balance at the beginning of our observational period in 1996. We find that thinning and speedup early in the study period are likely an ongoing

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Deleted: Our melt estimates for Crosson and Dosson are lower than the peak values reported by Khazendar et al. (2016), which is expected because our methods measure a fundamentally different quantity. While we measure total melt rates over large regions, Khazendar et al. (2016) used RES to estimate ice-bottom elevation change at particular points, and assumed that these thickness changes directly represent basal melt. The total melt rate at each point is higher than the thinning rate they calculate, since some amount of melt would still occur if the shelf were in steady state. The estimation of anomalous melt also requires an assumption that dynamic thinning is negligible; Khazendar et al.

Deleted: justify this assumption based on observed thinning rates for grounded ice, which are low compared to their peak melt estimates. However, the rates of flux divergence on the shelves are comparable to the thinning rates in many areas. We calculated flux divergence using 1000-m velocity grids for the period 2009-2014 and applied this correction to the radar observations, resulting in our estimate of anomalous melt rate differing by over 100 m a^{-1} in some places (further detail can be found in Supplementary Materials). Our recalculated values for RES-derived melt rates range up to 200 m a^{-1} (which is up to 70 m a^{-1} higher than peak rates in Khazendar et al.), and show a different pattern of melt from that found in Khazendar et al. (Supplementary Table 1 and Supplementary Figure 1). However, the use of repeat thickness measurements to find anomalous melt may still be biased by crevasses or keels advecting through the radar-track intersections, causing incorrect interpretation of structural anomalies as melt. While the polygon-based method we employed is more limited in spatial resolution, it is much less sensitive to these small-scale variations and thus more representative of melt rates for large sections of the shelves, though we may smooth out areas of peak melt. The method used by Gourmelen et al. (2017) resolves these small scale variations by accounting for advection, but it requires spatially dense satellite coverage and so is temporally limited compared to the

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response to earlier changes. Similar to previous studies, we show that basal melt rates increased on areas that were floating throughout the study period, and we find that total basal melt was further increased as ungrounding exposed more area to melt. We find that the melt rates, grounding line position, and incised channel geometry on Dotson suggest that it began to retreat in the early 1970s or before. These conditions lead us to speculate that a change in melt, likely resulting from a change in ocean forcing years or decades before 1974, may have led to Dotson's imbalance in 1996. Our results indicate that Dotson's grounding-line retreat and thinning exposed more sub-shelf area, increasing its sensitivity to ocean forcing and likely contributing to the high melt rates that we and others find during the 2000s. Prior work has shown that Crosson sped up through our study period, primarily near eastern Smith Glacier's grounding line and near the former tongue of Haynes glacier. We used a diagnostic ice-flow model to show that this speedup was likely the result of multiple factors, including weakening at its eastern margin and a retreat of eastern Smith Glacier's grounding line. Determining the initial cause of change to this system is key to understanding whether the present retreat results from ongoing oceanic or climatic changes, natural variability, or internal instability, and thus important for placing these observations in the context of other changes to submarine basins around Antarctica. In the future, prognostic modeling of this system beginning in 1996 or before (i.e. "hindcasting") could help test how different initial perturbations to the system would have affected its flow speed and mass balance, and thus provide context to these changes relative to those observed in other glaciers.

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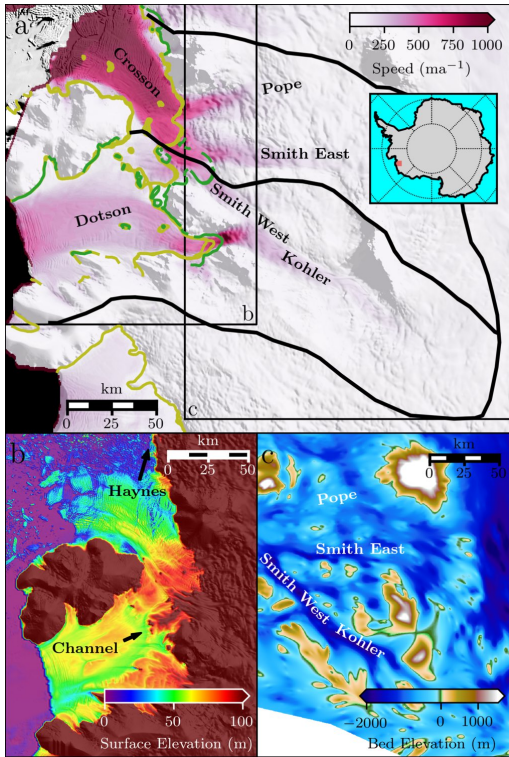
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Figure 1: Overview of study area a) 1996 surface speed overlaid on the mosaic of Antarctica (MOA) (Haran et al., 2013). Yellow and green lines show grounding line positions in 1996 and 2011 respectively (Rignot et al., 2014). Black lines indicate catchment boundaries of Crosson and Dotson used for flux calculations. b) Surface elevation relative to the EGM2008 geoid from WorldView/GeoEye stereo DEM mosaic (Shean et al., 2016). c) Ice bottom elevation relative to the EGM2008 geoid, which represents bed elevation over grounded ice.
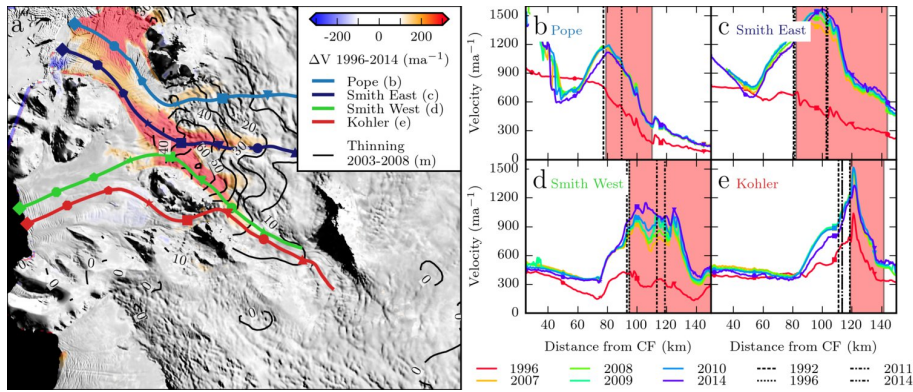
Figure 2: Recent changes in velocity and surface elevation. a) Color shows change in speed from 1996 to 2014. Contours indicate thinning of grounded ice from 2003-2008 at 10-m intervals, derived from OIB altimetry, ICESat-1 and WorldView/GeoEye DEMs. Colored lines indicate flowlines plotted in panels (b - e). Background is MOA. **b – e)** Velocity profiles as distance from the 2014 calving front (CF). Dashed lines indicate grounding line positions in different years. Red shading indicates areas that thinned by more than 5 m a⁻¹ from 2003-2008.
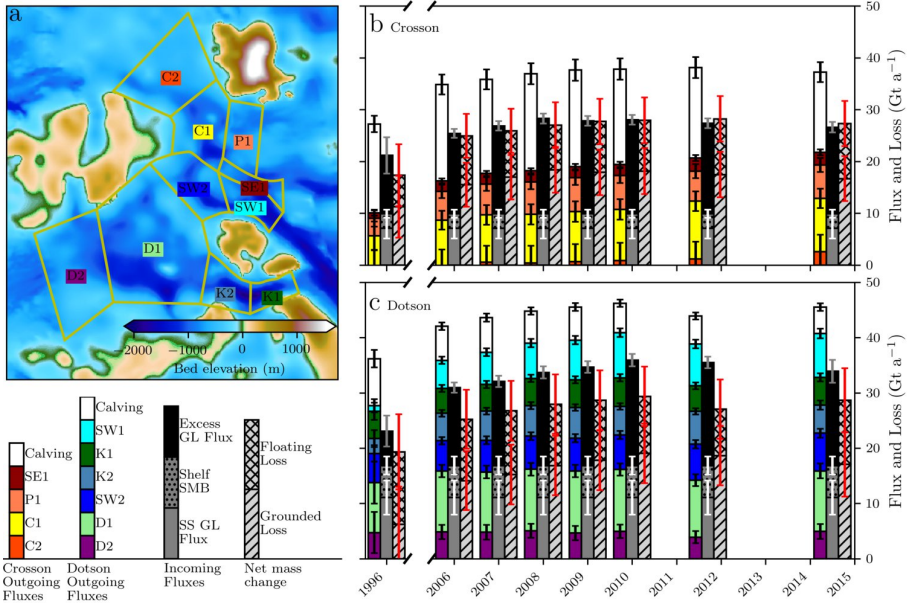
Figure 3: Flux and melt changes over Crosson and Dotson. a) Areas used for flux divergence calculations, outlined in yellow, plotted over bathymetry from Millan et al., (2017). b) and c) Flux and melt over Crosson and Dotson respectively. Stacked, colored bars show melt over each of the polygons from (a) while white bars on top show calving flux; these bars sum to the total outgoing flux. Solid gray bars show the steady-state (SS) grounding line (GL) flux (calculated from catchment-wide SMB), the dotted gray bars show the SMB over the shelves, and the solid black bar indicates the additional flux crossing the grounding line each year due to dynamic imbalance; these bars total to all incoming flux to the shelves. Light gray slashed bars indicate the loss of grounded ice (equal to the black bars in the previous column) and the cross-hatched light grey region shows the additional loss of floating ice (equal to the difference between the first two columns); these total to the annual mass loss rates.

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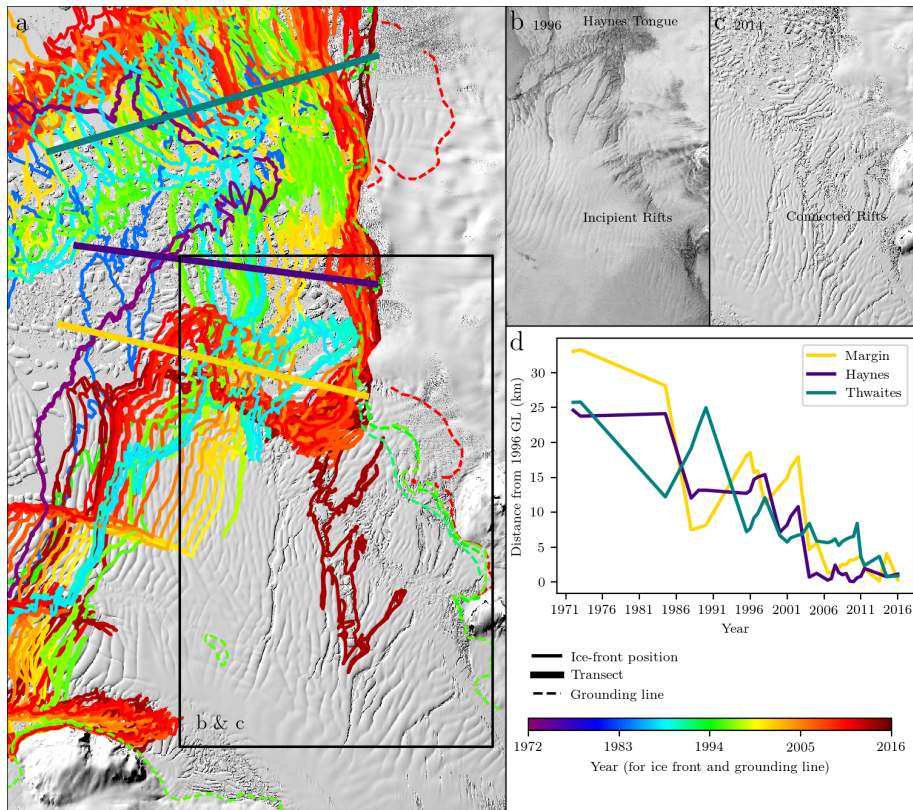
Figure 4: Crosson Ice Shelf front position. a) Selection of digitized shelf-front positions from MacGregor et al. (2012) and from our work, with grounding lines from Rignot et al. (2014). Teal, purple, and gold overlays correspond to transects used for (d). Box shows the outline of zoomed in area for (b) and (c). b-c) Zoomed in Landsat imagery from 1996 and 2014 respectively. Isolated rifts in 1996 appear connected by 2014, effectively detaching Crosson from its eastern margin. The disintegration of the Haynes Glacier Tongue also occurred during this period. d) Time series of ice-shelf-front distance relative to the 1996 grounding line.
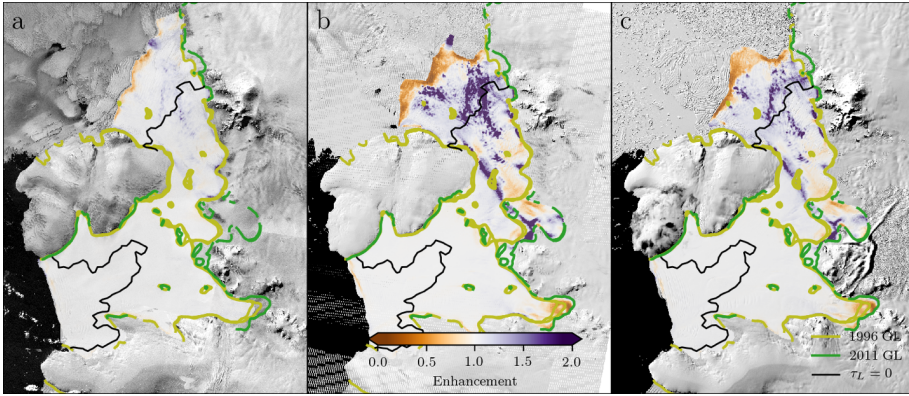
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Figure 5: Inferred enhancement to ice flow in a) 1996, b) 2010, and c) 2014. The enhancement factor gives the depth-averaged weakening of the ice relative to that predicted by a temperature model, with values larger than 1.0 indicating weakening. Black line indicates the zero contour of τ_L in 1996, i.e. the boundary between the compressive (upstream) and extensional (seaward) regimes. Backgrounds are Landsat images from the same year as the inversion.
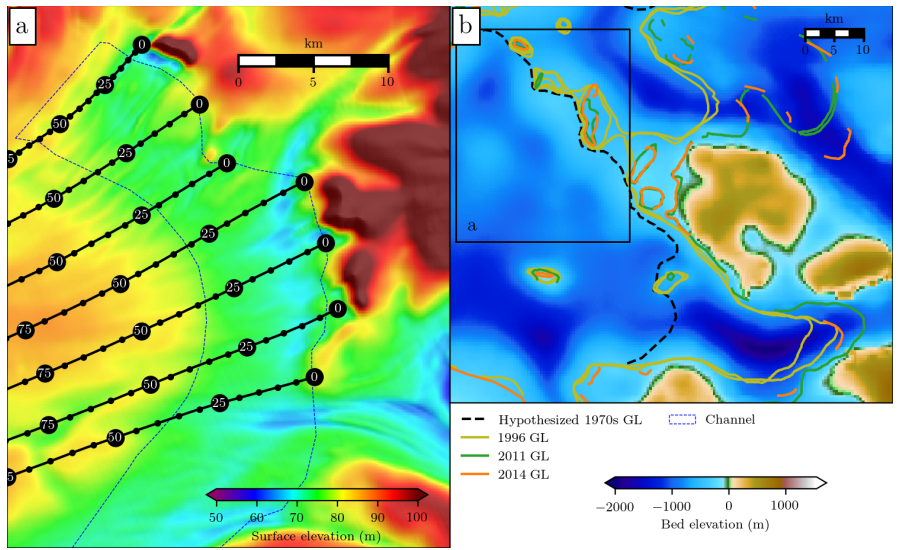
Figure 6: a) Detail of Dotson surface trough (region outlined in blue). Solid black lines show flowlines calculated from the 1996 velocity, with dots placed every 5 years. Large black circles are spaced every 25 years and labeled with age in years. Background is 2012 surface elevation. b) A possible location of the grounding line before recent retreat (black dashed line). This position is illustrative only, but shows a location that would have been susceptible to a retreat that would have increased melt rates and grounding line flux. Other lines show grounding line positions as above. Black box shows location of panel (a). Background is bathymetry (Millan et al., 2017).

	Grounding-Line Flux			Calving Flux			Basal Melt Rate			Volume Change		
		(R13)	(D13)		(R13)	(D13)		(R13)	(D13)		(R13)	(D13)
Crosson	25±1	27.4±2	--	18±2	12±2	--	19±3	38.5±3	--	-9±2	-19±1	--
Dotson	30±1	28.4±3	--	5±1	6±1	--	41±2	45.2±3	--	-11±3	-17±2	--
Total	55±2	55±5	51±5	25±3	17±3	18±2	60±5	83.7±6	78±7	-20±4	-36±3	-36±3

Table 1: Comparison of fluxes and melt between this study (white columns) and those from *Rignot et al.* (2013) (R13) and *Depoorter et al.* (2013) (D13). Values from this study are for 2010, while the *Depoorter et. al.* values are for 2009, and the *Rignot et al.* values are for 2007-2008. Columns show grounding-line flux, calving flux, basal melt rate, and volume change. All values are given in gigatons per year (Gt a^{-1}).

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Supplementary material: <u>Changes in flow of Crosson and Dotson Ice Shelves, West Antarctica in response to elevated melt</u>

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1   Evidence against marine ice accretion on Dotson

Significant marine ice accretion downstream of the transverse portion of the channel on Dotson should cause a discrepancy between measurements of freeboard and ice thickness. Ice penetrating radar generally does not penetrate into saline marine ice (Crabtree and Doake, 1986; Robin et al., 1983; Thyssen, 1988), so the bottom reflector from the MCoRDS radar comes from the fresh/saline transition in areas with accreted ice. The radar measurement thus indicates the thickness of fresh ice only, while the freeboard is determined by the total ice thickness, including marine ice. In areas of marine ice, the difference between the full thickness and the fresh ice thickness should cause the actual freeboard to be greater than that which would be calculated from the thickness of the fresh ice alone.

To determine whether there is marine ice accretion on Dotson, we calculate an expected freeboard from ice-thickness measurements made by the MCorDS radar and compare this expected freeboard to surface elevations measured simultaneously by the ATM. To calculate freeboard from the MCorDS radar product, two firn corrections must be made: (1) radar waves propagate at different speeds in ice and firn, which is not accounted for in the estimates of thickness from the MCorDS radar and (2) the total thickness of the shelf includes the air in the firn, so the freeboard is greater would be expected if the full column were the density of ice. To correct for the propagation speed difference, we calculate the 2-way travel from the MCorDS thickness, then convert that value back to depth using a propagation speed that accounts for firn-air content. We calculate a floatation height from this thickness by assuming the column is pure ice, then add to that the thickness of the air column to obtain the final estimate for expected freeboard. For both of these calculations, we assume a constant firn-air content of 13 m. This value is near the median of the spatially variable values we calculate in the main text, and using a spatially constant value prevents aliasing marine ice as variations in firn-air content. We compare surface elevations calculated using hydrostatic equilibrium to the surface elevations from the ATM, which we reference to the EGM2008 geoid and interpolate onto the MCoRDS data using the 5 nearest points, slope correcting and weighting by inverse square distance.

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Along flight lines approximately parallel to flow, we find that the freeboard height calculated from ice thickness corresponds to measured surface elevation with standard deviations ranging from 2.9-4.3 m. The channel has a surface expression of 10 m over large portions of these flightlines and up to 15 m in places, so the channel is deep compared to the errors in our method. We the calculated freeboard to have 3-4 m bias towards a higher surface than the direct freeboard measurements, opposite of what is expected if marine ice is present. Further, we find no correlation between distance along flow and misfit between observed and measured ice thickness. If marine ice accreted downstream of this channel, we would expect a trend towards the hydrostatic calculation of freeboard being smaller than the freeboard measured with the ATM farther downstream. Thus, we conclude that the thickening downstream of the channel on Dotson is not caused by marine ice accretion, but rather by dynamic thinning or a temporal change in melt.

2   Calculation of melt rates following Khazendar et al. (2016)

We converted the thinning rates in Khazendar et al. (2016), which represent anomalous thinning under the assumption of no dynamic thinning, to melt rates using the flux divergence. As in Khazendar et al., we first calculated the thinning rate at each crossover of the MCorDS radar over Crosson and Dotson, and our values for the thinning rate agree to within error for the 27 points that they do not identify as anomalous (Table S2). To obtain the flux divergence correction, we resampled velocity and ice thickness to a 1000-m grid and calculated the flux divergence at each grid point. We then linearly interpolated the flux divergence from the grid to each radar crossover and subtracted this value from the thinning rate to obtain the melt rate. We plot the melt rate in Figure S1 and present the values in Table S1. The peak value we find (187 m a^{-1}) is greater than the peak thinning rate found in Khazendar et al. (2016), though the magnitude of melt that we find is generally comparable to the thinning rates in the area. The distribution of melt is different than the distribution of thinning found in Khazendar et al. (2016), but as expected melt is highest near the grounding line and decreases downstream. These recalculated values are still sensitive to advection of heterogeneous properties of the shelf (e.g. crevasses or parcels of thick ice) that are not accounted for in the flux divergence, and thus may not be representative of melt.

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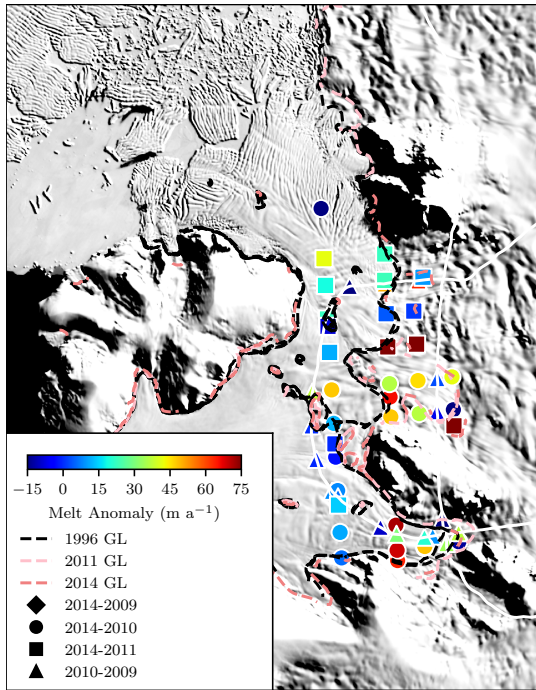
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Figure S1. Melt rate anomalies, calculated using the thinning rate and flux divergence, at crossover points of Operation Icebridge flightlines 2009-2014. Color indicates melt rate, and shape of the symbol indicates the years of crossover. Dashed lines show grounding lines, and the solid white line indicates the flightpath repeated in 2002 and 2009. See Khazendar et al. (2016).
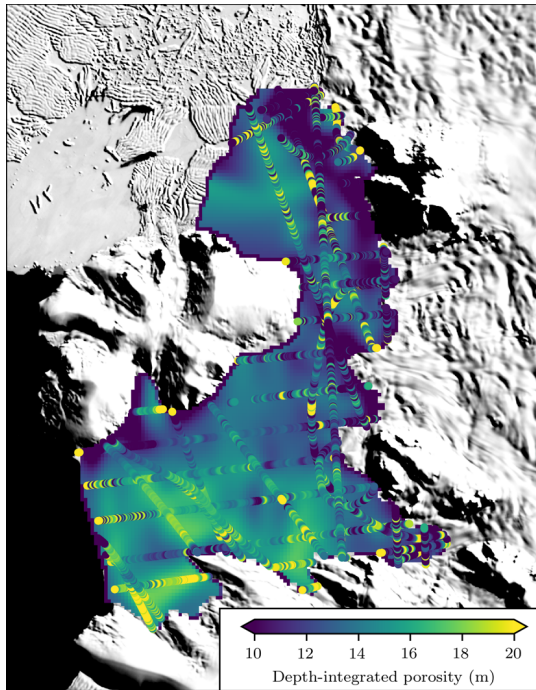
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Figure S2. Depth-integrated porosity (firn-air content) over Crosson and Dotson ice shelves. Colors in the background show gridded product, colored circles show individual radar traces from the MCoRDS radar.

Point Number	$\partial H/\partial t$ (m a^{-1})	$\partial H/\partial t$ (m a^{-1}) from (Khazendar et al., 2016)	Anomalous melt rate (m a^{-1})
1	-2	-3	23
2	-10	-10	10
3	49	38	63
4	27	30	50
5	2	5	1
6	51	44	106
7	139	129	127
8	24	16	42
9	20	14	46
10	0	-2	36
11	43	37	66
12	59	51	48
13	36	18	37
14	66	57	-30
15	41	44	3
16	59	65	-7
17	88	83	187
18	37	32	72
19	22	13	69
20	35	33	64
21	21	19	48
22	15	15	37
23	-13	-20	-13
24	-15	109	34
25	-18	-9	10
26	22	19	37
27	10	13	21
28	18	19	30

Table S1. Comparison of values for thinning and melt rate here and in Khazendar et al. (2016). We retain the numbering of points used in that paper's supplementary material. Columns 2 and 3 show the thickness changes estimated here and that paper respectively. Column 4 shows the melt rate, calculated by subtracting the flux divergence from the thinning rate. Note that Khazendar et al. identify point 24 as anomalous, though the value we calculate is similar to others in the area.

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