Referee #3

Suggestions for revision or reasons for rejection (will be published if the paper is accepted for final publication) Second Review

Authors: Patilea et al.

Title: Combined SMAP/SMOS Thin Sea Ice Thickness Retrieval

M.S. number: tc-2017-168

I thank authors for providing responses to the queries and accordingly editing the manuscript. The revised version is much improved now.

I am glad to see a new section 5 describing uncertainties and SIC impact on SIT. However, on the validation of the proposed combined retrieval, I could not find it in the manuscript. I agree with authors that not much in situ SIT data are available for validation, but there were experiments such as SMOSIce where such data can be available for validation. It is difficult to assess the performance of the retrieval method without validation!

Section 6 (P14) has been introduced. Here we compare ship observations with SIT from the mixed product.

The mere assumption of 100% SIC is insufficient for the analysis. The SIT data must correspond to actual 100% SIC. In Figure 9, the assumed SIT on x-axis should be replaced by the available in situ SIT. Authors can also discuss, based on in situ observations (not the assumed SIT) what % of SIC corresponds to only thin sea ice.

Through Figure 9 and its associated explanations we tried to show that SIC has a big impact on the SIT retrieved, all in a theoretical framework. This was included so that it should be taken in account if the SIT data is used. Also, we provided references to papers (Ivanova et al., 2015, Tian-Kunze et al., 2014) that uncertainties in the SIC retrievals if used for a correction of the current algorithm could induce higher error than just keeping the assumption of 100% sea ice. Although a correction for SIC is not implemented, the uncertainty for SIC in the generating the retrieval curve is considered and this will be added to the SIT uncertainty already presented (paragraph starting P13L22 and Fig. 9).

P1.L26. Retrieval of what? Please use: 'To date, ice thickness retrieval algorithms…'

Done P2L1-3

P5.L8. What do you mean by 'spillover'? What is it? Provide references, if possible. Explain in details or delete.

We added extra explanation and three references to the problem of land-sea contamination (spillover) problem of SMOS. P5L12-16

P6.L28. Retrieval curve in Fig. 2 green, I cannot find it.

P7.L4. Fig. 2 black. I cannot find it.

Done. It was an typing error, it is Fig. 1

Throughout the paper: 'data' is a plural word, use verb accordingly.

Authors must provide a clear rationale for the need of merging SMAP and SMOS. Why is it needed to combine two data sets when one can have SIT products from each separately? The current algorithm allows for both. The data that will be released include SMOS, SMAP and mixed SIT and uncertainties provided separately. This is already mentioned in the conclusions: The algorithm was transferred to the 40 deg incidence angle not just so that both satellites are used together, but also so that the retrieval can be applied just to SMAP.

At the same time SMAP was calibrated to the SMOS TBs so that we can have two sources of TBs for the same algorithm, providing a continuous time series of SIT data starting in 2010 in case SMOS stops functioning after eight years in orbit.

Please be specific with the methodology, how you propose to achieve the objective of the paper in view of the above rationale.
Please write down the objectives of the paper under bullets.
We introduced an algorithm summary in Sect. 4.2.1 that should cover this comment. It describes the complete process of transforming the SMOS and SMAP data into mixed SIT and their uncertainty.

Referee #2

The revised manuscript by Patilea et al. has improved regarding clarity and writing and also the differences to the paper by Huntemann et al. (2016), which covers a very similar topic, are now made clearer. However, I still have major concerns regarding the paper:

1) Compared to the study by Huntemann et al. (2016), the authors here
a) use a newer version of SMOS data, which leads to a mean deviation in sea ice thickness (SIT) of 0.22cm & RMSD=1.35cm for TBs in the Arctic for 1 Oct - 31 Dec 2015 (this time period is also used for the following comparisons).
b) use a slightly different RFI filter and choose the SMOS TBs somewhat differently than before:
They fit the SMOS TBs to 45deg incidence angle instead of using the 40-50deg TB mean. This results in a mean deviation of -0.3cm & RMSD=2.0cm compared to a).
c) fit SMOS TBs to 40 deg incidence angle (which is the incidence angle provided by SMAP) and perform a linear regression between SMOS and SMAP TBs to apply the SIT retrieval to SMAP , which does appear to be a more "straightforward" approach for combining SMOS and SMAP for the SIT retrieval as compared to the approach in Huntemann et al. (2016). The SMOS and SMAP SITs differ on average by 0.2cm with RMSD=2.4cm. The mean deviation between the combined SIT product and the SMOS SIT derived from 40deg incidence angle is <0.1cm & RMSD=1.4cm.

>Conclusion: The modifications made to the already existing retrieval seem to be relatively small, and as none of these data sets is compared to independent data, the presented

modifications to the joint retrieval from SMOS and SMAP may be more of "technical importance" showing small changes (theoretical improvements?) to a previous suggestion to combine SMOS and SMAP data.

From the presented study it is also not clear whether there is any advantage in using a combined SMOS and SMAP SIT retrieval as compared to the existing SMOS-based retrieval. By using TBs at 40deg incidence angle instead of 45deg, the usable polarisation difference range for the retrieval reduces from Delta_TB=32K (22...54K) to Delta_TB=26K (17...43K), which can be a disadvantage. On the other hand, as one of the advantages the authors claim that the data coverage by the joint product is 6% larger (for the area north of 55.7deg N). However, from Fig. 6, I would infer that the gain in data coverage is mainly achieved at the edge of the selected area, i.e. in areas that are covered by ocean and not sea ice, which would make them somewhat irrelevant for the SIT maps

We aimed towards a more robust retrieval where the coverage is just a minor point. The major improvement of a dual sensor product we attribute to the more representative estimation of a daily average ice thickness, both regarding the radiometric stability of the signal and the variability of the surface conditions regarding day/night cycles (even though sunlight is basically absent in the polar night) as well as spatial variability of sea ice, i.e., drift within the 24h timespan of a day.

"advantage in using a combined SMOS and SMAP SIT retrieval as compared to the existing SMOS-based retrieval" - although the final objective of the manuscript is to obtain a mixed product, the changes to the initial algorithm allow also for: SMAP only retrieval and SMOS 45 deg retrieval which won't be affected by the decreased dynamic range.

Regarding the decreased dynamic range of the polarization in the 40 deg new retrieval: Although the decrease of the dynamic range could increase the sensitivity of the retrieval to small changes in Q, the non-linear change in the curve, with a big decrease at small thicknesses (approx. 11 K at 0 cm) and a smaller decrease in dynamic range at the higher thicknesses (approx. 5 K) means that the highest impact of the diminished dynamic range is at small thicknesses, an area of the retrieval which is more dependent on the change in intensity and not in polarization difference. Changes at P8L23-27.

2) In the revised manuscript version, the authors have added a section and new figures on the uncertainty assessment. For the uncertainty computation, the authors assume that TB uncertainty of SMOS is equal to the RMSD resulting from fitting the SMOS TBs to 40deg incidence angle. Firstly, as the authors also recognize, this is an underestimation because the RMSD in the fitting iteration is limited to 5K. And secondly and more importantly, this is NOT the only source of TB uncertainty!

The relationship between SIT and TB depends on the ice conditions: For example, the salinity of the ice (or more precisely: brine volume fraction), the snow cover, the ice type (these are not mentioned at all), and the ice concentration (mentioned later by the authors but not used to estimate the uncertainty). This variability (and thus uncertainty) is (partly) reflected in the scatter of the training data for the retrieval curve (only partly because the training was done only for Oct-Dec 2010 and in two specific areas of the Arctic). The

variability of TBs at the same place and time at different incidence angles should only reflect a small part of the uncertainty…

Fig. 7 shows SIT as function of TBH and TBV, although in the retrieval, SIT is a function of polarisation difference and intensity. This makes the figure and its implications hard to interpret. It is also not clear which of the shown combinations of TBH and TBV (or better: polarisation difference and intensity) are actually seen in the satellite observations. This raises also the question how the retrieval is actually performed using the retrieval curve. In Huntemann et al. (2016), I found: "The minimum euclidean distance of the fit to the data in the I-Q-space defines the retrieved ice thickness." Is the retrieval performed no matter how large this "minimum euclidean distance" is?If so, how representative are retrieved SIT with large distance from the retrieval curve? What is the distribution of distance values encountered during the retrieval? In Fig. 7, I think, we can see how not restricting the "minimum euclidean distance" to a maximum value leads to an odd behaviour, as seen for TB combinations below the TBH-TBV 1:1 line (where a small change leads to completely different SIT to be retrieved).
Also, from the text (Sect. 3.2) I understand that the retrieval is performed when at least two TB values are found (at least one below 40 deg and one above 45 deg). This issue is, for example, discussed in the paper by Schmitt et al. (2018), which also deals with combining SMOS and SMAP data for sea ice applications. They perform the incidence angle fit only if at least 15 measurements are found, which seems more appropriate considering the relatively high scatter of SMOS data…

> Conclusion: I do not agree with how the uncertainty is estimated and I would suggest to show sensitivity of polarisation difference and intensity instead of TBH and TBV for the values actually encountered during the retrieval, which have to be analysed/shown first.

The (TBh, TBv) sensitivity plot (Fig. 7 - currently Fig. 8) has been changed to a (Q,I) one. The errors are now computed relative to the (Q,I) space making a more clear connection between the retrieval curve and the sensitivity of SIT to the change in TBs.

"is the retrieval performed no matter how large this "minimum euclidean distance" is?" - Yes, the retrieval is performed no matter the actual distance from the curve.

"Also, from the text (Sect. 3.2) I understand that the retrieval is performed when at least two TB values are found (at least one below 40 deg and one above 45 deg). This issue is, for example, discussed in the paper by Schmitt et al. (2018), which also deals with combining SMOS and SMAP data for sea ice applications. They perform the incidence angle fit only if at least 15 measurements are found, which seems more appropriate considering the relatively high scatter of SMOS data…" - Due to the restrictions we have for the 40 deg retrieval, at least one value under 40 deg and at least one over 40 deg, and due to the acquisition geometry of SMOS, i.e. the shape of the snapshots, many more observations are taken at different incidence angles. Short statistics for a single day show that more than 97% of the grid cells fulfilling aboves conditions covered have at least 15 data points.
 (Fig. 6 from J. Font *et al*., "SMOS: The Challenging Sea Surface Salinity Measurement From Space," in *Proceedings of the IEEE*, vol. 98, no. 5, pp. 649-665, May 2010.)

3) Another issue is that the authors have added some more statistics based on a three month period (Oct-Dec 2015) as compared to presenting mainly statistics based on one day of data as was done in the first manuscript version. However, in the revised version, there is still conclusions based on the analysis of one single day of data (Sect. 3.3 & 5.1). I think, example maps for one day can be ok/useful, but, as far as I can see, statistics based on one day of data are not necessarily useful (unless their representativity is shown or at least discussed).

In addition, the authors use the expression "bias" for comparisons of data sets (e.g. SMOS v5.05 vs. v6.20 SIT retrieval in Sect. 3.1, fitted to 45 deg vs. 40-50deg average SMOS SIT in Sect. 3.3 and SMOS vs. SMAP in Sect. 4.1). As far as I know, "bias" is not used (and is indeed very confusing) for comparisons of two data sets, of which it is not clear which one is more realistic/better etc.). I think "mean difference" would be more appropriate here.

Section 3 contains Figure 3 so that we can show visually and discuss some of the changes that can appear for one day (as also mentioned by the referee). But in Figure 4 (and the discussion of the figure in the paper) the statistics are computed for a 3 months period that covers the freeze up period of 2010 (discussed in the last paragraph of Sect. 3.3). The term "bias" is indeed misleading and it is replaced by "mean difference" as suggested. For Sect. 5.1 (now 5.2) we included the plots to give an example how the uncertainties will look, not for long term statistics. The current day that was chosen, contains a good distribution of intermediate SIT values.

Further comments:

-p. 1, l. 4: "SMAP observes ... which makes thin sea ice thickness retrieval more consistent" -> This sounds like SIT retrieval from SMAP is more consistent than from SMOS, while you probably aim to say (as we have already discussed and agreed on in the first review round) that the retrieval is "easier" (or more consistent if you like) if a fixed incidence angle is used instead of an incidence angle range, which is, in principle, also possible with SMOS data (by choosing TBs at this incidence angle only). This should be expressed unambiguously.

Sentence rephrase to make it less ambiguous. P1L4-6

- p. 2, l. 28: "Its resolution is..." -> better: The grid spacing is…

Done P2L32

- p. 4, l. 2: And which RFI filter are you using? Either write it here or refer to where you describe this in the paper.b

Added a reference here to Section 3.2 containing the description of the RFI filtering method. P4L5

- p. 5, l. 11-13: First, you write about "bias" and "RMSD", then about "bias" and "standard deviation". Are RMSD and standard deviation the same here?

They are all RMSD. We modified the text for consistency.

- p. 6, l. 3 : Reference to "Eq. 3" is misleading here. Eq. 3 has not been given yet and could mean that you refer to Eq. 3 in Zhao et al. (2015). Also at p. 6, l. 8: First give Eq. 3, then refer to it.

Modified the section to solve the issues raised. Removed the reference (P6L10) at the start of the paragraph which might indicate it's part of of the Zhao paper, and we moved the equation before any reference to it. P6L15-25

- p. 6, l. 8-18: It sounds like C is determined first and then only the other parameters (ah, bh,...) are determined? Is this / how is this done? Are ah, bh, ... determined differently than C?
For each iteration both C and the ah, bh,... group are determined. C is computed first (at each iteration) because is used in Eq. 3 to determine the other parameters. Since C/2 is considered to be the intensity at nadir, and the other parameters basically describe the two curves (Tbh, Tbv) as a function of incidence angle, C/2 will represent both Tbh and Tbv at 0 deg incidence angle.

"Are ah, bh, ... determined differently than C?" - it is explained in the paragraph previous to Eq. 3, that "C (Eq. 3) is determined for a given grid cell by first summing up the brightness temperatures of horizontal and vertical polarization for each individual observation and then taking the median of the result." and "The other five fit parameters ah , bh , av , bv and dv in the fit functions (Eq. 3) are determined by a least squares procedure." In short: at each iteration the C is obtained by summing up the TBs below 40 deg incidence angle and taking the median, while the rest of the parameters are determined by using a least square procedure. Both steps are done at each iteration. P6L15-26

- p. 6, l. 19-20: To make this clearer, I suggest to add something like: In this case, the least squares method to fit the parameters is repeated.
We added another sentence to make it more clear that after data removal the all the fit parameters (including C) are recomputed. P6L27-30

- p. 6, l. 8-24: It would be helpful to clearly state that you do not take into account the measurements that do not meet the defined criteria after a maximum of five iteration steps (if this is how these cases are handled...).
The measurements that still don't meet the criteria after five iterations are kept. The higher RMSD that these fits will have will result in higher uncertainty for the SIT computation. The fit measurements that are discarded are the ones that do not achieve convergence during the least square procedure. A new paragraph was added to make these things clear. P6L31-P7L2

- p. 6, l. 28 & p. 7, l. 4: You probably refer to Fig. 1 here instead of Fig. 2.
Yes. Issue solved. P7L8, P7L16

- p. 7, l. 20: "This is ..." -> What is "this" here? (bias and/or RMSD?)
Both of them. We changed the sentence to make it more clear. P7L30-P8L2

- p. 7, l. 20- 23: Complicated/unclear description of what you do here... E.g. "selecting all grid cells with that thickness..." -> what is "that" thickness?

For the daily average algorithm, we select all grid cells that contain SIT from each thickness bin (1 cm, 2 cm, 3 cm, ...) and then we compare them with the thicknesses from the same grid cells computed using the TB fitting procedure. This way we can compute the bias (relative to the daily average algorithm) and RMSD for each 1 cm bin, also we can look at the distribution of averaged differences along the thickness axis instead of a averaged difference that includes all thicknesses, since we expect higher differences at the higher thicknesses. This way we can also see if there is any change in sign of the averaged difference between the low and high thicknesses. We modified this part to make the procedure more clear. P7L30-P8L2

-p. 7, l. 22-23: " Only grid cells that contain at most 50 cm and non-zero in at least one of the two algorithms are used." -> Make it clearer whether the condition "in at least one of the two algorithms" applies also to the selection of grid cells with at most 50 cm SIT.
It doesn't apply to the 50 cm threshold. Both retrieval need to have a maximum of 50 cm since this is the upper limit that we consider for the algorithm. While the lower limit where we require that at least one algorithm contains sea ice higher or equal to 1 cm, so that we eliminate the areas where the algorithms detect just open water, making the bias and RMSD really small due to the large amount of open water pixels. We split the phrase in two sentences to reflect this. P7L33-P8L1

- p. 7, l. 27 & l. 28: "always generating" & "will generate" -> For clarity, maybe add "falsely"/'spuriously".
Sentences modified. P8L5-6

- p. 7, l.35: What is the "absolute bias" (as compared to just "bias"?)
The sentence has been removed since the RMSD conveys better the deviation from the mean. The "absolute bias" is computed as the normal bias where the differences between the data point and the expected values are computed as a modulus.

- p. 9, l. 6: Does the reference to "(Sect. 4.1) refer to Sect. 4.1 in Huntemann et al. (2016) or what is meant here?
All the Section references in the manuscript are just in-paper pointers, thus it refers to Section 4.1 of the current manuscript.

- p. 11, l. 1-2: "a weighted standard deviation... is used" -> weighted for what?
Distance. When we grid the SMAP TBs to a grid we use a nearest Gaussian weighting where the weight for each individual data point that goes into computing the value has a weight equal with exp(-dist**2/sigma**2) where sigma is FWHM/2(log2), with FWHM of SMAP taken as 40000 meters. We added Eq. 5 and its description to make this more clear. P13L13-18

- p. 11, l. 3: "The correlation was calculated for a period of seven days." -> Why only seven days?
Since we changed to Q,I space instead of TBh and TBv, the correlations have been recalculated (for Q and I) for a period of 3 months (1 Oct. - 31 Dec. 2015) P13L18-19

- p. 11, l. 22-24: Not very clear description.

For each pair of TBh and TBv that were used in the first step to compute SIT, we use Eq. 5 to change the TBs relative to a desired SIC. The TBs computed using the mix between sea ice (the TBs used in the first step) and open ocean TBs (the tie points) are decreased. The higher the SIC the higher the decrease, as expected. Then we compute the SIT containing the SIC influence.
At this point we group the initial SIT in bins of 1 cm (from 0 to 50 cm), and then for each bin, and each set of SIC(15, 30, 50…), we take the corresponding retrieved SIT from the second step and average them, thus to obtain one value of SIT, influenced by SIC, for each cm of SIT computed with the 100% SIC assumption.
Sentences modified. P12L1-4

- p. 11, l. 30-31: "As we have observations at two polarizations at each grid cell available, it should in principle be possible to retrieve SIT and ice concentration simultaneously." -> "In principle", this is only possible if TB varies independently with ice concentration and ice thickness, which would have to be shown before stating phrases like this.
We changed the phrasing so it can't be interpreted as a statement. P12L110-11

- Sect. 5.2: Why are these considerations not used to estimate SIT uncertainty?
The error of SIC in the training data is now considered for additional uncertainty in the retrieval see (new) Sect. 5.2.
- throughout the paper:
a) Use "an" instead of "a" before abbreviations RFI, RMSD, L-band.
Solved.

b) The text still contains some typos / language issues (e.g. mixed usage of singular and plural).
c) TB is introduced as abbreviation for brightness temperature, SIT for sea ice thickness, but sometimes the authors use these abbreviations, sometimes not (can even vary within one sentence).
After introduction of TB abbreviation we modified all the following words to be consistent.

-Is the area used for training and inter-calibration of SMOS and SMAP data defined somewhere in the paper?
The three training areas are the same as in Huntemann et al., (2014). The first paragraph of Sect. 3.1 was modified to also give the location of the three areas used for training.
For inter-calibration we use all the grid cells in the Arctic above 55 deg N. The paragraph starting at P8L31 is modified to make this clear.

-no (clear) references for statements on p. 1, l.15; p. 2, l. 4-8; p. 3, l. 5-8 & l. 13 & l. 14 & 16-19.
p. 1, l.15 Reference added. P1L16
 p. 2, l. 4-8 Reference added. P2L9-10
 p. 3, l. 5-8 Reference added. P3L9

& l. 13 & l. 14 & 16-19 - all of them are presented in SMOS Calibration Team and Expert Support Laboratory - SMOS L1OPv620. Sentence added so that it refers to the whole section. P3L21

Reference:

Schmitt, A. U. and Kaleschke, L. (2018): A Consistent Combination of Brightness Temperatures
from SMOS and SMAP over Polar Oceans for Sea Ice Applications, Remote Sensing, Vol. 10 (4),
553.

Combined SMAP/SMOS Thin Sea Ice Thickness Retrieval

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Abstract. The spaceborne passive microwave sensors Soil Moisture Ocean Salinity (SMOS) and Soil Moisture Active Passive (SMAP) provide brightness temperature data at L-band (1.4 GHz). At this low frequency the atmosphere is close to transparent and in polar regions the thickness of thin sea ice can be derived. SMOS ~~data~~ measurements covers a large incidence angle range whereas SMAP observes at a fixed 40° incidence angle ~~which makes~~. By using brightness temperatures at a fixed incidence

5 angle obtained directly (SMAP), or through interpolation (SMOS), thin sea ice thickness retrieval is more consistent as the incidence angle effects do not have to be taken into account. Here we transfer a retrieval algorithm for thickness of thin sea ice (up to 50 cm) from SMOS data at 40° to 50° incidence angle to the fixed incidence angle of SMAP. Now the SMOS brightness temperatures (TBs) at a given incidence angle are estimated using empirical fit functions. SMAP TBs are calibrated to SMOS for providing a merged SMOS/SMAP Sea Ice Thickness product.

10 **1 Introduction**

Sea ice is an important climate parameter (Moritz et al., 2002; Stroeve et al., 2007; Holland et al., 2010) and accurate knowledge of sea ice properties is needed for weather and climate modeling and prediction and for ship routing. The thickness of the ice is one of the parameters that determines the resistance against the deforming forces of wind and ocean currents (Häkkinen, 1987; Yu et al., 2001). Even a thin layer of sea ice inhibits evaporation, reduces heat and gas exchange between ocean and

15 atmosphere and increases the albedo (Maykut, 1978; Perovich et al., 2012). ~~It~~ Sea ice also provides a solid surface for snow to deposit, which further reduces heat exchange and increases albedo (Shokr and Sinha, 2015).

The Soil Moisture Ocean Salinity (SMOS) satellite was launched by ESA in November 2009. It is a synthetic aperture passive microwave radiometer working at L-band (1.4 GHz). The aperture synthesis requires an array of small antennas reducing the total weight and size of the satellite. The instrument works in a full polarimetric mode, recording all four Stokes parameters.

20 Its large field of view allows for multi angular observations organized in an approximately 1200 km × 1200 km snapshots.

SMOS has been developed for retrieving soil moisture (Kerr et al., 2012), by inferring the surface emissivity which is correlated with the moisture content, and sea surface salinity (Zine et al., 2008; Font et al., 2010) where the measured brightness temperatures (TB) are linked with the sea salinity through the dielectric constant of the water in the first few centimeters. Modeling and observations showed that at this frequency the radiation is sensitive to ice thickness up to ~~0.5 meters~~ 50 cm

25 (Kaleschke et al., 2010, 2012). The atmosphere has little influence on the radiation at L-band as both absorption and scattering are small (Skou and Hoffman-Bang, 2005). The correlation of ice thickness with emitted radiation together with a small

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atmospheric contribution make SMOS a candidate for thickness retrieval of thin sea ice. To date, two sea ice thickness retrieval algorithms have been developed for SMOS, one using the TB intensity averaged over incidence angles between 0° and 40° (Tian-Kunze et al., 2014) and one using intensity and polarization difference averaged over incidence angles between 40° and 50° (Huntemann et al., 2014).

5   In 2015 the Soil Moisture Active Passive (SMAP) satellite was launched by NASA ~~(Entekhabi et al., 2010, 2014)~~(Entekhabi et al., 2010, . It carries two sensors onboard, ~~a~~ an L-band radiometer, and a radar which share a rotating 6 m real aperture antenna reflector. The radar was recording high resolution (1 to 3 km) data used for soil moisture sensing, until it failed after three months. In contrast to the synthetic aperture observations of SMOS, the real aperture antenna observations of SMAP cover an area of 36 km × 47 km at a fixed incidence angle of 40° and results in a swath with an approximate width of 1000 km. ~~SMAP~~ The
10 preceding technical details of SMAP were presented in Entekhabi et al. (2014). SMAP also includes on board detection and filtering of Radio Frequency Interference (RFI) while SMOS does not (Mohammed et al., 2016).

After the launch of SMAP, different approaches were taken to convert data products between the two sensors. A previous approach to convert SMOS to SMAP TBs for usage in soil moisture retrieval and assimilation systems is presented in Lannoy et al. (2015) and involves a quadratic fitting of the SMOS TBs at the SMAP incidence angle and employing auxiliary data
15 and an empirical atmospheric model to correct for the atmospheric and extraterrestrial contributions, respectively. In contrast, Huntemann et al. (2016) ~~convert~~ converts SMAP 40° surface TBs to SMOS top of the atmosphere equivalent 40 to 50° averaged TBs through two linear regressions. A more recent attempt for inter-calibrating SMOS and SMAP data, and using the resulting TBs for a separate SMAP, but also a combined SIT retrieval was presented in Schmitt and Kaleschke (2018).

In this article, we present a combined Sea Ice Thickness (SIT) dataset ~~combining data of the two~~ using input from both
20 sensors by calibrating the SMAP ~~brightness temperatures~~ TBs to those of SMOS (Sect. 4). As a first step, an inter-calibration of the ~~brightness temperatures~~ TBs of the two sensors is required due to a possible warm bias in SMOS data (Sect. 2) and due to corrections for galactic noise and sun specular reflection contained in the SMAP but not in the SMOS TB data. In addition, the SIT retrieval from Huntemann et al. (2014) is adapted to the new version 6.20 of the SMOS Level 1C data and it will be used as a reference for all other comparisons (Sect. 3.1). This new retrieval is combined with a fit function for the dependence
25 of horizontal and vertical ~~brightness temperatures~~ TBs (from now on referred as TB_h and TB_v, respectively) on the incidence angle (Sect. 3.2). The fit function is used for RFI filtering and for SIT retrieval at a fixed incidence angle. The fit is also a step required for the SMOS and SMAP merged product to combine the observations of the two sensors at a common incidence angle.

2   SMOS and SMAP data sources

30 The MIRAS radiometer onboard the SMOS satellite has 69 receivers on three arms measuring radiances at 1.4 GHz (Kerr et al., 2001). One complete set of data from the aperture synthesis process done each 1.2 seconds is called a snapshot. For this investigation the SMOS Level 1C ~~sea~~ (L1C) ocean data gridded on the icosahedron Snyder equal area (ISEA) 4H9 grid (Sahr et al., 2003) is used. ~~Its resolution~~ The grid spacing is 15 km while the SMOS footprint size varies with incidence angle

from approximately 30 km×30 km at nadir to 90 km×30 km at 65° (Castro, 2008). Over the whole field of view the average resolution is approximately 43 km. The Level 1C data is provided within 24 h of acquisition.

In full polarization mode, all four Stokes parameters are measured. Data is recorded in the reference plane of the antenna as T_X, T_Y, T_3 and T_4, and is converted to TB_h, TB_v, TB_3 and TB_4 in the Earth surface plane (Zine et al., 2008) using

$$
\begin{bmatrix} T_X \\ T_Y \\ T_3 \\ T_4 \end{bmatrix} = \begin{bmatrix} \cos^2(\alpha) & \sin^2(\alpha) & -\cos(\alpha)\sin(\alpha) & 0 \\ \sin^2(\alpha) & \cos^2(\alpha) & \cos(\alpha)\sin(\alpha) & 0 \\ \sin(2\alpha) & -\sin(2\alpha) & \cos(2\alpha) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} TB_h \\ TB_v \\ TB_3 \\ TB_4 \end{bmatrix}, \tag{1}
$$

where $\alpha = \alpha_{gr} + \omega_{F_r}$, α_{gr} is the georotation angle and ω_{F_r} is the Faraday rotation angle. Within a snapshot just one or two of the Stokes parameters are measured at the same time. When only one of the Stokes parameters is measured, all three arms of the sensor record the same polarization. In the case of recording a cross-polarized snapshot, one arm of the sensor records one polarization while the other two record the other polarization (McMullan et al., 2008). Measurements of single (XX or YY) and cross-polarization ((XX,XY) or (YY,XY)) are done alternatively. In order to obtain the values for TB_h and TB_v from the matrix, depending if the current measurement is single or cross-polarization, we ~~will~~ have to use one or two adjacent snapshots. The missing values required for the conversion are interpolated from neighboring snapshots within a 2.5 s range and with a maximum incidence angle difference between the measurements of 0.5°.

The SMOS L1C ~~data~~ version 6.20 has been operationally available since 5 May 2015 and also older acquisitions were reprocessed. This version adds better RFI flagging and ~~it~~ improves the long-term and seasonal stability of the measurements. At the same time it introduces a warm bias in the ~~brightness temperatures~~ TBs of approximately 1.4 K relative to the previous version 5.05 over ocean. The bias over the ocean can be 1 K too warm with respect to the true values~~(SMOS Calibration team and Expert Support La~~. Over Antarctica and land, the bias is above 2 K, which is closer to modeled and ground based measurements. The new ~~data~~ version also reduces the difference in ~~brightness temperature~~ TB between ascending and descending overflights over ocean at low latitudes. At high latitudes such changes were not documented. Before, the difference varied considerably with time and latitude due to thermal variations in the instrument. All of the technical details described above about the new data version are presented in SMOS Calibration team and Expert Support Laboratory Level 1 (2015)

The SMAP satellite is positioned on a quasi-polar sun-synchronous orbit with an ascending equator crossing time 6 pm, while SMOS has an equator crossing time at 6 am. SMAP carries a conically scanning radiometer with a fixed incidence angle of 40° which leads to a narrower swath and decreases the area covered at the pole compared to SMOS. The footprint of a SMAP ~~observatoin~~ observation is approximately 36 km × 47 km, resulting in an approximate resolution of 40 km. In this study, the SMAP Level 1B data is used which contains time ordered ungridded Top Of the Atmosphere (TOA) ~~brightness temperatures. The data~~ TBs. It is available from 31 March 2015 and is provided with a latency of about 12 h.

SMOS and SMAP observe in a restricted band (1.400-1.427 GHz) reserved for passive radioastronomical use. Nevertheless, there are surfaced based artificial sources causing RFI (Mecklenburg et al., 2012). The image reconstruction process required to obtain the SMOS TBs includes an inverse Fourier transform (Corbella et al., 2004). Therefore, not only the grid cells that contain the RFI source are affected ~~,~~ but the whole snapshot can be contaminated, resulting in high or even negative ~~brightness~~

temperatures TBs (Oliva et al., 2012). Since in nature brightness temperature TB will not exceed 300 K over the polar ocean (Kaleschke et al., 2010; Mills and Heygster, 2011; Tian-Kunze et al., 2014), a simple RFI filter is used to eliminate the whole snapshot which contains at least one TB exceeding this threshold. This filter is used in the sea ice thickness retrieval algorithm presented in Huntemann et al. (2014). An alternative approach for filtering RFI has been shown in Huntemann and Heygster (2015) where incidence angle binning is used, resulting in a higher preservation of data and fewer gaps on the grid. In this paper we use a new iterative method based on the removal of data with high difference relative to the a SMOS TBs fit curve, as presented in Sect. 3.2. Since SMAP contains onboard hardware for detection and filtering of RFI and neighboring pixels are unaffected by a an RFI source, no additional filtering is required for the SMAP Level 1B data.

3 Sea ice thickness retrieval using a fit function

Due to the new SMOS data version 6.20 used here compared to version 5.05 used in Huntemann et al. (2014), a retraining of the SMOS thin ice thickness retrieval is necessary. First, in Sect. 3.1 we use the method presented in Huntemann et al. (2014) just using the newer data version 6.20. This involves averaging the brightness temperatures TBs between 40 and 50° incidence angle. Secondly, we employ a fitting function using the dependence of brightness temperature TB on incidence angle (Section 3.2) as input for the retrieval (Section 3.3). The fitting function is used to obtain SMOS brightness temperatures TBs at a fixed incidence angle.

3.1 SMOS retrieval retraining

Three SMOS grid cells in the Kara and Barents Sea located at (78.71°N,57.41°E),(77.37°N,81.71°E) and (75.81°N,79.57°E) were used for training over a period of three months (1 October - 26 December 2010) with sea ice thickness data obtained using the relation with the Cumulated Freezing Degree Days (CFDD) based on NCEP temperature data (Huntemann et al., 2014)as presented in Huntemann et al. (2014). CFDD is the daily average temperature below -1.8° (freezing point of sea water) , integrated over the time with sub freezing temperatures (Bilello, 1961). The relation beween the CFDD and the thickness as presented in Bilello (1961) is $SIT[cm] = 1.33 \cdot (\text{CFDD}[°C])^{0.58}$. The ASI (Spreen et al., 2008) Sea Ice Concentration (SIC) product was used to filter low SIC data during the training period. Only during the early part of the freeze-up when ice is really thin , the SIC was allowed to have a value between 0-100% (Huntemann et al., 2014) otherwise 100% SIC was required. The brightness temperatures TBs are averaged daily over the incidence angle range between 40° to 50°. The functions

$$
\begin{aligned}
I_{abc}(x) &= a - (a-b) \cdot \exp(-x/c), \\
Q_{abcd}(x) &= (a-b) \cdot \exp(-(x/c)^d) + b,
\end{aligned}
\tag{2}
$$

are fitted to the intensity I and polarization difference Q data measured over the training areas and the SIT resulting from the CFDD method, where a, b, c and d represent the curves parameters (Table 1), x is the sea ice thickness while I and Q are the brightness temperature TB intensity and polarization difference, respectively. The sea ice thickness retrieval curve is the result of using the two fitted functions from Equation 2 in the (Q, I) space. For each pair of Q and I the minimum Euclidean distance

to the retrieval curve is used to determine the SIT. The retrieval curve parameters for data version 5.05 presented in Table 1 are updated values of the Huntemann et al. (2014) that are currently used for daily processing at the University of Bremen (www.seaice.uni-bremen.de).

Figure 1 shows the retrieval curves in the (Q, I) space. The dots on the curves represent the SIT increasing with intensity and decreasing with polarization difference in steps of 10 cm from 0 cm to 50 cm. Over 50 cm the retrieval is too sensitive to small changes in intensity and polarization difference and it will be cut off. The sea ice thickness retrieval curve for data version 5.05 and the retrained curve using the 6.20 data version are shown in black and blue, respectively. The new ~~curve has about~~ exhibits a value $\sim$1.7 K higher value at zero SIT for intensity and polarization difference. The ~~difference~~ discrepancy increases up to 3 K at 50 cm SIT.

Figure 2 shows the intensity (left) for 29 October 2010 using daily mean TBs for each grid cell. The data has been re-gridded to the NSIDC polar stereographic grid with a resolution of 12.5 km. This resolution is ~~a~~ an oversampling of the true resolution of ~~the SMOS data~~ SMOS which is 43 km on average. The original validated retrieval (Huntemann et al., 2014) was trained with the old data version and is used as a reference here. The warm bias of the new ~~data~~ version is seen in the difference plot (Fig. 2 right) both over ocean area and sea ice. In regions of high contrast like the ice edge or coast-lines, both ~~data~~ versions tend to produce spillover effects (SMOS Calibration team and Expert Support Laboratory Level 1, 2015). The spillover produces an erroneous increase ~~or decrease in brightness temperature of~~ of TB over ocean areas that are found next to coastlines or ice edge or decrease in TB over the sea ice, close to the ice edge. The erroneous values vary between 1 K to 1.5 K (SMOS Calibration team and Expert Support Laboratory Level 1, 2015) in the areas mentioned (not visible in the plot). The errors in TB appear due to calibration errors in the SMOS instrument and systematic spacial ripples (Corbella et al., 2015; Martín-Neira et al., 2016; Li et al., 2017).

The algorithm trained with SMOS data version 5.05 has been compared with the one trained with version 6.20 for the period 1 October to 26 December 2010, considering sea ice thicknesses from 1 cm to 50 cm. The ~~bias~~ mean difference of the new retrieval is -0.22 cm while the RMSD is 1.35 cm. From a total of 5.1 million cumulated data points over the 87 days period and 50 cm sea ice thickness range, 97% have at most 3 cm difference. The ~~bias and standard deviation~~ mean difference and RMSD are below ± 1 cm and 2 cm, respectively, for ice thicknesses below 25 cm. For 50 cm thickness the ~~bias~~ mean difference increases to $+4$ cm while the ~~standard deviation~~ RMSD reaches 11 cm.

A test is done to estimate the error introduced by the ~~usage of~~ use of of the original retrieval (Huntemann et al., 2014) with the 6.20 data version. The two algorithms trained with the different data versions ~~have taken~~ take as input the 6.20 data only. The ~~data~~ dataset covers the freeze-up period from 1 October to 26 December 2010. The ~~bias~~ mean difference between the retrained retrieval and the original one is 0.33 cm with 99% of the data having a difference of 3 cm or less, while the RMSD is 0.91 cm. This means ~~,~~ that although it is recommended to use the algorithm adapted for the new data version, the error is below 1 cm thickness on average for SIT below 51 cm if processed with the old algorithm.

3.2 SMOS TBs fit characteristics

In the previous section, we have shown that the SIT output with the new data version and new retrieval is consistent with the old data version and retrieval. In all of the next sections the SMOS Level 1C 6.20 version will be used, and when making reference to the original daily mean sea ice thickness retrieval, the retrained 6.20 version algorithm from Sect. 3.1 will be used. In each grid cell, the number of data points and the covered incidence angle range are highly variable due to the orbit characteristics, the large incidence angle range of $0°$ to $65°$, and the complex distribution of incidence angle within a SMOS snapshot. Grid cells located closer to the center of the swath will cover a large incidence angle range. Near the swath edges, the range is reduced and low incidence angles are not covered (Font et al., 2010). The snapshots removed using the over 300 K RFI filter can create a local bias in the average incidence angle. The existence of an RFI source before an observed grid cell, relative to the trackline, will result in the elimination of snapshots with high incidence angle data points for that cell. As opposite, an RFI source located after the grid cell of interest will result in elimination of the low incidence angle data points. The varying angle distribution depending on the position in the swath and the data removal due to the RFI filtering for one grid cell may shift the average incidence angle of the ensemble of observations between $40°$ and $50°$ away from the assumed average of $45°$. The average TBs and SIT values retrieved from the affected grid cells will be shifted accordingly. This error can be avoided by fitting a curve to the angular dependent TBs, allowing for a retrieval which uses TBs estimated for a fixed incidence angle.

Here we propose as a solution a modified version of the fit functions described in Zhao et al. (2015). The fit is applied separately to each polarization, horizontal and vertical, for each grid cell using daily observations. An initial filtering of RFI is done by removing observations which are flagged in Level 1C data for either being affected by tails of point source RFI or for indicating RFI by the system temperature standard deviation exceeding the expected trend (Indra Sistemas S.A., 2014). The flagged data is removed before the TBs are transformed from the antenna to the earth reference frame.

The fit functions that describe the dependence of TB_h and TB_v on the incidence angle are

$$TB_h(\theta) = a_h \cdot \theta^2 + \frac{C}{2} \cdot [b_h \cdot \sin^2(\theta) + \cos^2(\theta)]$$

$$TB_v(\theta) = a_v \cdot \theta^2 + \frac{C}{2} \cdot [b_v \cdot \sin^2(d_v \cdot \theta) + \cos^2(d_v \cdot \theta)].$$

(3)

where θ represents the incidence angle, $C/2$ is the intensity at nadir, a_h, b_h, a_v, b_v and d_v are five additional parameters used to fit the curves. The Brewster angle effect on the vertically polarized TBs is represented by the additional parameter d_v. The fit is done iteratively with a maximum of five steps. For each step the parameter C (Eq. 3) is determined for a given grid cell by first summing up the TBs of horizontal and vertical polarization for each individual observation and then taking the median of the result. The median is used so that any RFI influenced outliers will not influence C. Due to asymmetric change in TB between horizontal and vertical polarization at higher incidence angles, only grid cells with at least one observation under $40°$ are considered. This increases the stability of the fit since $C/2$ represents the intensity at nadir. The $40°$ threshold is selected due to increased asymmetry between vertical and horizontal TBs at higher

6

incidence angles which will generate a bias in the computation of the parameter C. The other five fit parameters a_h, b_h, a_v, b_v and d_v in the fit functions

$$TB_h(\theta) = a_h \cdot \theta^2 + \frac{C}{2} \cdot [b_h \cdot \sin^2(\theta) + \cos^2(\theta)]$$

$$TB_v(\theta) = a_v \cdot \theta^2 + \frac{C}{2} \cdot [b_v \cdot \sin^2(d_v \cdot \theta) + \cos^2(d_v \cdot \theta)].$$

are determined by a least squares procedure. ~~The Brewster angle effect on the vertically polarized TBs is represented by the~~
5 ~~additional parameter d_v.~~

At each iteration of the fitting procedure ~~20% of the observations with the highest absolute difference from the fit are~~ ~~removed~~ if the RMSD of the fit is higher than 5 K or if the RMSD fit difference between successive iterations exceeds 1 K~~.~~, 20% of the observations with the highest absolute difference from the fit are removed. After the removal of data, in the next iteration the computation of C and the least squares method to fit the parameters is repeated. The data removal in the iterative
10 process is the second step used to discard possible RFI influences.

At the last iteration, if the RMSD of the fit is higher than 5 K or the RMSD fit difference relative to the fourth iteration is higher than 1 K, the fit parameters will still be used for computation of TBs, at the desired incidence angle, but with a higher RMSD. In the case of non convergence of the least squares procedure for the fit parameters, the grid cell will be discarded from TB computation.
15 The fit function is not optimized for extrapolation of the covered incidence angle range. Incidence angles not covered by the observations will have high uncertainty. To avoid extrapolation, only grid cells which contain observations with incidence angle both below and above the desired angle, e.g. 45°, are used for the retrieval.

3.3 Sea ice thickness retrieval training using fitted data

The retrieval algorithm ~~has been~~ is retrained as described in Sect. 3.1 but instead of using TBs averaged over 40-50° incidence
20 angle, ~~now we use brightness temperatures~~ we use TBs from the fit process (Sect. 3.2) at a nominal incidence angle of 45°. The resulting retrieval curve (Fig. ~~2~~ 1 green) has 1.3 K higher polarization difference at 0 cm ice thickness than the algorithm trained with the daily mean data (Fig. 1 blue). The difference decreases to 0.1 K at 20 cm thickness and increases to approximately 0.5 K at 50 cm. This can come from variability in the mean incidence angle. The daily averaged observations have an incidence angle bias of -0.5° (with single differences as high as -2.5°) relative to the assumed 45° one. The smaller incidence angle will
25 result in a smaller ~~polarization difference~~ Q since this decreases when approaching nadir. The ocean and thin sea ice have low ~~intensities and high polarization difference~~ I and a high Q. As the sea ice gets thicker, the intensity increases and the polarization difference decreases. For the same incidence angle bias at higher ~~thicknesses the polarization difference~~ thickness values Q error will be smaller. The ~~intensity~~ I values for the two curves at the same sea ice thickness are nearly the same. The difference between these two curves is small compared to the difference to the ~~retrieval curve for the~~ SMOS 5.05 data version retrieval
30 curve (Fig. ~~2~~ 1 black).

Figure 3 shows the retrieved sea ice thickness using the daily mean method (left) presented in Sect. 3.1 and the retrained retrieval curve at nominal 45° incidence angle (center) based on the fitted ~~brightness temperatures for 29~~ TBs for the 29th of October 2010. Due to ~~the requirement for the fit computation to have observation~~ fit computation requirement to have observations below 40° (Sect. 3.2), some grid cells in the central Arctic are not covered anymore. The decrease is around 1°

5 in latitude, corresponding to approximately 1000 grid cells. This area is mostly covered by ice with thickness higher than 50 cm thus not being the focus of the retrieval. On the other hand for many ocean areas which formerly were excluded by the RFI filtering (grey in Fig. 3 left) now data is available, e.g. around Iceland, Eastern Greenland and Vladivostok. At the same time in the ~~area of the Hudson Bay~~ Hudson Bay area there is a 30% decrease in the ~~area covered due to not fulfilling~~ covered surface due to failing the incidence angle criteria ~~required for SIT retrieval~~ (Sect. 3.2) or the failure of the least square procedure to

10 converge to a solution. For 90% of the grid points the difference is less than 3 cm which is below the estimated retrieval error of 30% of SIT computed in Huntemann et al. (2014). The daily mean retrieval has a positive ~~bias~~ mean difference of 0.41 cm. The highest differences appear north of Alaska with values up to 10 cm (Fig. 4 right). This is a result of a biased distribution of the incidence angles, resulting in a large number of grid points having under 45° mean incidence angle. This decreases the polarization difference dragging the resulting SIT to higher values. Overall the RMSD for this day is 1.9 cm which is within

15 the expected 30% error margin of the retrieval.

Figure 4 (top) represents the ~~bias~~ mean difference (blue) and RMSD (red) of the SIT based on the 45° incidence angle fitted TBs relative to the 40-50° daily mean SIT calculated for the period ~~1 October to 26~~ of 1st of October to 26th of December 2010. ~~This is computed by dividing the~~ To compute the the mean difference and the RMSD we first divide the daily mean SIT into bins of 1 cm thickness, from 0 to 50 cm~~, selecting~~ . To compute the mean difference for each 1 cm bin, we select all grid cells

20 with that thickness from the daily averaged SIT and subtracting ~~them~~ the thicknesses of the same grid cells obtained from the fitted TBs~~SIT.~~ . The RMSD is also calculated between the two datasets for each 1 cm bin. Only grid cells that contain at most 50 cm ~~and~~ are used. Also there must be a non-zero thickness in at least one of the two algorithms ~~are used~~ so that the high number of open water grid cells in both algorithms won't influence the statistics. Overall the SIT from the fitted TB is smaller than the SIT from the 40-50° incidence angle mean TB. Until 40 cm of thickness the ~~bias~~ mean difference varies between 0

25 and −1 cm and then increases gradually up to -5 cm at 50 cm SIT. The green curve shows the cumulative histogram for daily mean TB at each sea ice thickness. Approximately 52% of the ~~data~~ values is below or equal to 3 cm in the daily averaged TB SIT. This can be explained by the coarse resolution of about 43 km of SMOS ~~, always~~ falsely generating thin sea ice at the ice edge due to ~~brightness temperature~~ TB contamination from either the ocean or the ice pack. In addition also coastal areas will spuriously generate thin sea ice due to spillover effects. Overall we can see that 95% of all data is below 40 cm while thickness

30 ~~corresponding to just~~ values corresponding to 40 and 50 cm are contained in the remaining 5% of the data so that the region of high ~~bias~~ mean difference is small. Figure 4 bottom shows the daily ~~bias~~ mean difference (blue) and RMSD (red) of the 45° fitted ~~brightness temperatures~~ TBs SIT relative to the daily average TB SIT. Over the whole period the ~~bias~~ mean difference stays between 0 and −0.6 cm while the RMSD increases from 1.3 K to 2.5 K. The increase in RMSD can be explained by the freeze-up period which contains larger areas with intermediate thicknesses compared to the start and peak freeze-up periods

35 which contain either ocean or over 50 cm SIT grid cells. The ~~overall bias of the~~ 45° fitted ~~brightness temperatures SIT~~ TBs SIT

overall mean difference for the whole period for all thicknesses is −0.3 cm with ~~a~~ an RMSD of 2.02 cm. ~~The absolute bias for over 3 cm thicknesses is 1.6 cm.~~

4 Sea ice thickness retrieval using SMAP data

This section ~~adapts the SMOS SIT algorithm to observations of SMAP~~ describes the adaptation of SMOS based SIT to SMAP TBs. Because SMOS observations have a variable incidence angle, they have to be computed at the fixed incidence angle of SMAP using the fitting function method described in Section 3.2. In order to apply ~~the SIT retrieval calibrated with SMOS data also to those of~~ SMOS calibrated SIT retrieval to SMAP, first the ~~brightness temperatures~~ TBs of both sensors have to be inter-calibrated (Sec. 4.1). In Section 4.2 the resulting inter-calibrated ~~brightness temperatures~~ TBs are mixed and used for generating a combined SMOS/SMAP sea ice thickness dataset.

4.1 SMAP/SMOS inter-calibration

The first step is to retrain the SMOS retrieval as in Sect. 3.3 using the nominal incidence angle of 40°, which is the fixed incidence angle of SMAP. The resulting SIT retrieval curve is shown in red in Fig. 1. As expected, the lower incidence angle results in a lower ~~polarization difference~~ Q, especially for thin ice and reduces the usable ~~polarization difference~~ Q range for the retrieval from 22-54 K to 17-43 K. Although the decrease of the dynamic range can increase the sensitivity of the retrieval to small changes in Q, the change is non-linear. At small thicknesses the decrease in dynamic range is large, 11 K at 0 cm, while the reduction of the dynamic range at 50 cm is approximately 5 K. The result is that the large change in dynamic range is affecting the low thicknesses which have low sensitivity to the change of Q.

A procedure to convert between SMOS and SMAP TBs over land was previously suggested in Lannoy et al. (2015). It uses a radiative transfer model and auxiliary data ~~for taking in account~~ to account for atmospheric and galactic contributions for SMOS. For the interpolation of SMOS TBs to 40° incidence angle it fits a quadratic function to the angular dependent SMOS TBs.

In this study the procedure to convert from SMAP ~~brightness temperatures~~ TBs to SMOS equivalent TBs is done through simple linear regression. For the procedure we use SMOS 40° measurements data and SMAP L1B TOA observations for the period between 1 October to 31 December 2015, which covers the first freeze-up in the Arctic observed by both sensors. All the data over 55°N is considered for intercalibration. In the first step, the SMAP data is gridded daily on the SMOS ISEA 4H9 grid (the native SMOS Level 1C data grid) using a Gaussian resampling with a cutoff distance from the grid cell center of 20 km and Full Width Half Maximum (FWHM) range of 40 km. Only grid cells located more than 100 km away from the coast are considered to minimize the land contamination. In the second step we determine the fit function parameters for the SMOS data on a daily basis and compute the 40° SMOS TBs for each grid cell~~for each day~~. Figure 5 shows the scatter plots between the TBs of SMAP and SMOS 40° for horizontal (left) and vertical (right) polarization. For each polarization the magenta line shows the linear regression. We can distinguish two areas of high data point density at the two ends of the ~~clouds~~ open water and ~~for~~ thick sea ice clouds, respectively. Over open water at a ~~brightness temperature~~ TB of 80 K and 120 K for

TB_h and TB_v, respectively, SMOS has a ~~warm bias~~ positive mean difference of approximately 3.3 K and 5.2 K. At the high ~~brightness temperatures~~ TBs representing the solid ice cover, the ~~bias~~ mean difference for SMOS decreases to 2.7 K and 3.3 K for TB_h and TB_v, respectively. The bias of SMOS TBs in the 6.20 data version that is presented in Section 2 can be one of the sources for the difference between SMOS and SMAP TBs. The asymmetry between low TBs and high TBs can come

5   from the high and low reflectivities of ocean and sea ice, respectively at L-band. Unlike SMAP, SMOS data does not include correction for galactic noise which can have a higher influence over water due to its high reflectivity. The reflectivity decreases over sea ice, resulting in galactic noise having a smaller impact on recorded values thus lower differences between corrected and uncorrected TBs. The overall RMSD of the two linear regressions is 2.7 K and 2.81 K for TB_h and TB_v, respectively. The resulting linear regression parameters are presented in Table 2.

10   For this study, in order to use SMAP data for SIT retrieval, we adjust the SMAP TBs by a linear regression to 40° SMOS incidence angle ~~data~~TBs. A similar calibration of SMAP to SMOS TBs was presented previously in Huntemann et al. (2016)~~.~~ ~~For that calibration, however,~~, where the SMAP Level 1C TB product was used which contains surface ~~brightness temperatures~~ TBs on a 36 km EASE grid. They ~~contain~~ include an atmospheric correction unlike the TOA Level 1B data that is used in the current paper. ~~Also, the~~ The calibration is done through two separate linear regressions. The SMAP and SMOS 38-42°

15   incidence angle data is daily averaged and compared to each other for the period ~~1 October to 31 December~~ October 1st to December 31st 2015 (Sect. 4.1). In the second step, since the SMOS SIT retrieval algorithm used in Huntemann et al. (2016) was developed for 40-50° daily averaged data another calibration is required. Using SMOS L1C data for the same period ~~,~~ a linear regression is done between SMOS 40-50° and SMOS 38-42° daily averaged data. The main differences between the Huntemann et al. (2016) and the current paper is that here the SIT retrieval has been retrained to the fixed incidence angle of

20   40° and is not necessary anymore to correlate SMAP TBs with the 40-50° SMOS averaged TBs. Instead we retrain the retrieval to work directly with 40° TBs. Since the incidence angle difference between the SMAP data and the SMOS 40-50° does not need to be corrected anymore, the calibration that is done in the current paper is necessary to compensate for extraterrestrial contributions that are corrected in SMAP ~~data~~ TBs and for the warm bias of the SMOS data. The RMSD for the linear relation between SMAP and SMOS ~~data~~ observations in Huntemann et al. (2016) is over 4 K for both polarizations, with at least 1.3 K

25   higher than the one presented in this paper.

For a daily sea ice thickness retrieval, based on ~~SMAP brightness temperatures only, both~~ horizontal and vertical ~~, are first~~ SMAP TBs, the TBs first are adjusted to the SMOS ~~brightness temperature~~ TB using the linear regression parameters. Then they are gridded into a 12.5 km resolution NSIDC polar stereographic grid using a Gaussian weighting for the distance with a cutoff from the grid cell center of 15 km and FWHM range of 40 km. For the period from ~~1 October to 31~~ 1st of October to

30   31st of December 2015, the difference in sea ice thickness between SMOS 40° incidence angle fitted TBs retrieval and SMAP retrieval are small, 2.39 cm RMSD and -0.2 cm average difference for the SMOS SIT relative to the SMAP retrieval taking into account only grid cells containing at most 50 cm SIT and at least one of the two retrievals having over 0 cm.

4.2 SMOS/SMAP combined sea ice thickness retrieval

Because of the small differences between the retrievals from the two sensors, combined maps are produced using both of them. The daily mean horizontal and vertical TBs are computed separately for both sensors. For each grid point of the SMOS ISEA 4H9 grid we compute the daily SMOS TBs using the 40° fit (as in Sect. 3.3). Then the TBs are regridded to the NSIDC 12.5 km grid commonly used for sea ice maps. SMAP TB data is gridded directly to the NSIDC grid using a Gaussian resampling as was done in Sect. 4.1. The two resulting TB datasets are averaged. Finally the sea ice thickness retrieval for 40° incidence angle is applied. The result is a SIT map that has the benefit of using data from both sensors (e.g. Fig. 6 (left)) which has a larger coverage, and is less affected by RFI. For the area north of 55.7°N the coverage in the mixed dataset increases by over 6% compared to the 40-50° daily mean TB retrieval. Also the combined TBs are more representative for a daily mean due to the 12 hours difference in the equator crossing time between the two sensors. The RMSD between the original 40° to 50° incidence angle daily mean retrieval from Sect. 3.1 and the new mixed sensor one is 2.05 cm for the 1st of October to the 31st of December 2015 period investigated, while the mean difference is -0.58 cm. The result means that the mixed sensor SIT is on averaged smaller than the SMOS daily averaged TB SIT. Figure 6 center shows the difference between SMOS 40-50° incidence angle averaged TBs sea ice thickness and the mixed data for the 24th of October 2015. The highest differences appear mostly in the transition area of 40 cm to over 50. Taking into account just data points with maximum value of 50 cm and for at least one of the two datasets a value over 0 cm, 93% of the data has an absolute difference of at most 2 cm for the three months compared. Figure 6 right compares the retrieval done just with the SMOS 40° fitted TBs to the mixed data one. For this comparison, the averaged difference is below -0.1 cm and the RMSD is 1.37 cm for the complete three months period.

4.2.1 SMOS/SMAP combined sea ice thickness retrieval algorithm summary

To reach the final objective of the paper, combining TB data from both SMOS and SMAP sensors for a one day SIT retrieval several steps are required:

- SMOS L1C data is read and converted to the (H,V) reference frame and limit the data to the region covered by the NSIDC polar stereographic grid

- for each SMOS grid cell the fit parameters for both H and V and corresponding uncertainties are derived and observations not covering 40° incidence angle are excluded.

- landmask is applied

- TBs at 40° are derived from the fit parameters

- the resulting TBs and uncertainties are gridded to the NSIDC polar stereographic 12.5 km grid

- SMAP L1B data is read and cropped to a minimum latitude of 55°N

- TOA TBs of SMAP are gridded to the NSIDC polar stereographic 12.5 km resolution grid. TB uncertainties are an output of this step

- the gridded SMAP TBs are converted to SMOS equivalent TBs

- for each NSIDC grid cell the SMOS and the converted SMAP TBs are averaged to obtain the combined TBs

- the uncertainties for the combined TB (for each polarization) are computed error propagation from the uncertainties of TB_h and TB_v from SMOS and SMAP

  - Q and I are computed from the combined TBs ; the associated uncertainties are calculated by from the combined TB_h and TB_v uncertainties

  - SIT is computed from each (Q,I) pair ; the uncertainties associated are computed at the same step using the results of the sensitivity study procedure discussed in Sect. 5

- the SIC and CFDD error are being included to the SIT uncertainty resulting from the previous step

- the SIT and the uncertainty is saved in an hdf file

- additionally, after the gridding procedure for each sensor, SIT computation is done separately also for them, using the same procedure presented above but by using the TBs and uncertainties of the specific sensor instead of the combined ones

5 Assessment of uncertainties

5.1 Sea Ice Concentration impact

The SIT retrieval used in this paper assumes 100% ice concentration. As a result, the retrieved sea ice thickness decreases if this condition is not fulfilled. We assume that TB over sea ice varies linearly with the change in sea ice concentration:

$$TBp(SIT, IC) = TBp_i(SIT) \cdot IC + TBp_w \cdot (1 - IC) \tag{4}$$

where p represents the polarization, TBp_i and TBp_w are the TBs of ice and water, respectively and IC is the sea ice concentration.

For this study, as a first step, we first use 40° SMOS TBs from 11 October 2015 for retrieval. The resulting SIT will be considered the Ice Thickness (IT) for the assumption that we have a 100% ice concentration. In the second step we take the same TBs as input for the sea ice TBp_i, use fixed tie points for TBp_w with 85 K and 125 K as values for the horizontal and vertical TBs, respectively. For each pair of SMOS TBs used in the first step we consider a range of sea ice concentrations (15, 30, 50, 70, 80 and 90%) for which we compute SIT using Eq. 4. The result is an IT value with its corresponding set of six SIC influenced SIT. As a last step, the IT data points are grouped in bins of 1 cm thickness. For each 1 cm bin of IT, we select

its corresponding thicknesses from the second step and we averaged them for each SIC separately. Figure 7 shows how the retrieved SIT varies relative to the IT depending on the SIC. For a SIC of 90% at 10 cm the retrieved SIT is 8.5 cm, while at 50 cm is just 28 cm.

Current retrievals for SIC are influenced by thin sea ice. In Heygster et al. (2014), SIC algorithms have been tested for 100%
5   sea ice concentration with thicknesses below 50 cm. All algorithms show less than 100% SIC for thicknesses below 30 cm. In Ivanova et al. (2015) all SIC algorithms registered a decrease in SIC, up to 60% at 5 cm, and an overall bias of 5% for over 30 cm. An attempt to retrieve both SIC and SIT at the same time done in Kaleschke et al. (2013) showed a strong increase in noise for the SIT retrieval.

During the winter most of the Arctic is covered by SIC of 90% and higher (Andersen et al., 2007). For an assumed uncertainty
10   of the sea ice concentration data of 4% (Ivanova et al., 2015) the error that could be introduced by a correction of sea ice thickness for high SIC is higher than that of the error introduced by the assumption of 100% sea ice concentration (Tian-Kunze et al., 2014) . The uncertainty of SIC algorithms at high concentration and their covariation at thin thicknesses will cause high errors if a correction to SIT is applied using current SIC datasets. As a result full ice cover is assumed for the SIT retrieval.

5.2   Sea ice thickness uncertainties

15   In the SIT retrieval using 40° incidence angle TBs of the two sensors several factors contribute to the uncertainty: the radiometric accuracy of the observations, RFI contamination in the TB data, the uncertainty in the auxiliary data used for the training of the retrieval, the influence of the SIC on the TBs and the sub-daily variability of the TBs themselves.

Here we propose a method to quantify the uncertainty of the retrieval. We first compute the SIT in the (TB_h, TB_v Q, I) space using the 40° TBs trained retrieval (Fig. 7 8 (left)). The TBs that that will be used in a retrieval will more likely be found
20   above the one-to-one line (black line)where the vertical brightness temperature is higher than the horizontal one. The color in the diagram indicates the retrieved SIT according to the retrieval curve for 40° incidence angle (red curve in Fig. 1). The TB space covered by the 40 close to retrieval curve (Fig. 1 (red)) but there is variability, with data points, with values going above and below the curve. To cover also the less likely (Q, I) pairs we chose to cover a large range of values for Q and I, from 0 K to 80 K and from 80 K to 300 K, respectively. The resulting figure follows the training curve pattern, with an I dominating the
25   change in SIT at below 20 cm thicknesses, while Q becomes more important at higher thicknesses. The SIT over 51 cm is removed from the figure since we restrict maximum retrieved thicknesses to 50 cmthickness is small compared with the rest of the thickness range. The one cm thickness over 50 cm is kept so that we can compute the derivative for 50 cm.

As a second step we compute the derivative of as SIT as a function of TB_h and TB_v Q and I seen in Fig. 7 8 center and right, respectively. Almost all of the data points will be found above the one-to-one line where the polarization difference is
30   positive. For most of TB_hs below 200 K For Q values below the 20 cm line the rate of change of the SIT is below change rate is below 0.25 cm per K due the thickness isolines being parallel with the Q axis thus for the same value of the intensity, a large change in Q will result in a similar thickness value. For thicknesses between 20 and 40 cm the change increases to 0.5 cm per K and is increasing sharply with increased TB_h at over 230 KTB_v. In contrast, the derivative for TB_v (Fig. 7 right) at values above 230 K is positive for TB_h below 213 K, and becomes negative above itk for Q below 60 K. While for thicknesses over

13

40 cm the change rate of thickness with Q quickly goes over one cm, especially in the area with Q between 20 and 30 K where most of the data points will fall in. A similar patter appears also for I with the difference that at thicknesses below 20 cm the change rate of SIT is higher than the one from Q due to I axis being perpendicular to the SIT isolines. The sensitivity of SIT relative to ~~TB_h and TB_v~~ Q and I will be used to compute the uncertainty of the retrieval. For a given pair (~~TB_h, TB_v~~ Q, I)

5   and their associated uncertainties we compute the SIT and corresponding SIT uncertainties:

$$
\underline{sigma}\sigma_{SIT} = \sqrt{\left(\frac{\partial SIT}{\partial TB_h}\right)^2 \cdot \sigma_{TB_h}^2 + \left(\frac{\partial SIT}{\partial TB_v}\right)^2 \cdot \sigma_{TB_v}^2 + 2 \cdot \left(\frac{\partial SIT}{\partial TB_h}\right) \cdot \left(\frac{\partial SIT}{\partial TB_v}\right) \cdot \sigma_{TB_h} \cdot \sigma_{TB_v} \cdot \rho_{TB_h TB_v}} \sqrt{\left(\frac{\partial SIT}{\partial Q}\right)^2 \cdot \sigma_Q^2 + \left(\frac{\partial SIT}{\partial I}\right)}
$$

(5)

where ~~σ_{TB_v} and σ_{TB_v} represent the TB uncertainties , $\rho_{TB_h TB_v}$~~ σ_Q and σ_I represent the Q and I uncertainties derived through an error propagation method from the errors of TB_h and TB_v, and ρ_{QI} is the correlation between the ~~two polarizations~~ Q and I. The values of the SIT derivatives are taken from the second step of the method for each pair of (~~TB_h, TB_v~~ Q, I).

10   For this study we do not take into account the radiometric accuracy of either sensor because they are small compared to the other errors, especially the ~~brightness temperature~~ TB variation during one day. For each SMOS observation at 40°incidence angle, the TB uncertainty is assumed to be the RMSD resulting from the fitting process presented in Sect. 3.2. During the fitting routine the RMSD is computed for each iteration and a 5 K threshold is used for eliminating outliers. Although this process is used to eliminate potential RFI influences in the data, it will also reduce the variability that comes from observations of the

15   same grid cell at different times of the day. For SMAP ~~brightness temperatures~~ TBs a weighted standard deviation for each grid cell using all observations from one day is used as uncertainty. The weights are applied for each data point that is considered into calculating the TB for that grid cell and are computed using

$$
w_i = \exp\left(-\frac{4 \cdot \log 2 \cdot d^2}{\text{FWHM}^2}\right)
$$

(6)

where, w_i is the weight, d is the distance of the SMAP data point location to the center of the grid cell and FWHM is the Full

20   Width Half Maximum beamwidth of SMAP with a value of 40 km. The correlation between the ~~TB_h and TB_v is 0.81 and 0.97~~ Q and I is -0.68 and -0.66 for SMOS and SMAP, respectively. The correlation was calculated for ~~a period of seven days.~~ the period 1 October to 31 December 2015. It was computed ~~per day~~ for the whole three months over the whole Arctic using daily ~~averaged TB for~~ fitted TBs for SMOS and daily gaussian resampled TBs for SMAP for each grid cell~~and is consistent during the whole period~~.

25   ~~Figure 8~~ Another source of error for the current retrieval is the uncertainty in the training data. For this study we included two parameters that could generate uncertainty in the creation of the retrieval curve and thus in the retrieval itself. The first parameter is the SIC. In the training data as presented in Huntemann et al. (2014) the SIC is assumed to be 100% although this cannot be ensured for the whole period covered. The initial freeze-up period, where thin sea ice can covary with SIC (as discussed here in Sect. 5.1), is allowed SIC between 0 and 100%, while later drops in SIC are removed. To take in account

30   the uncertainty in the SIC data used for the training, we take a one day of TBs and corresponding SIT data and order it in

1 cm bins from 0 to 50 cm. Then we vary the SIC taken in account with ±5% standard deviation and compute the range of ice thickness that will derive from this, i.e., assuming 105% SIC and 95% using the linear mixing of open water contribution to TBs as discussed in Sect. 5.1. The result is shown in Fig. 8 (left). A 5% variation in the SIC for an assumed 100% SIC cover we obtain a polynomial increase in SIT error with increasing SIT, starting from nothing at 0 cm and reaching approximately 31 cm at 50 cm.

The second additional parameter used for estimating error in the retrieval curve comes from the CFDD daily variability in the estimation of training ice thickness using the model. While SMOS passes over a training area in the Arctic region, the recorded TBs are representative for that specific time of the over pass. Close to the poles a specific location can be covered multiple time by consecutive overpasses. For the generation of the retrieval curve, connecting the daily average temperature from NCEP with a localized in time daily averaged TB will create a bias between the retrieved thickness and actual SIT. The variation in temperature, with lower temperatures increasing the ice generation rate, and it's non-linearity, with thinner ice growing faster for the same temperature than thicker sea ice, generates an uncertainty in the SIT computed for the retrieval curve. For quantifying this uncertainty we will select a fixed daily temperature of -25°C for which we compute the amount of thickness increase for 1 cm thickness as a starting point. This thickness will be considered the uncertainty of the SIT retrieval due non correct representation of the total sea ice increase in a day relative to the recorded TBs in the training areas. The result is shown in Fig. 7 (right). At small thicknesses the error added by the CFDD daily variability is over 5 cm due to the easier exchange of heat between the ocean and the atmosphere, while it decreases exponentially towards 1 cm at the higher thickness. Also it can be seen that lower temperatures will increase the error due to higher exchange of heat between the ocean and the atmosphere.

To derive the final uncertainty for SIT, we use a simple error propagation method for the three uncertainty values that we want to include: uncertainty derived from the TBs and the associated retrieval, the uncertainty in the SIC training data and the uncertainty due to CFDD daily variability. Figure 10 shows as an example the scatter plot and moving average (red lines) of the SIT uncertainty (Eq. 5) for 11 the 24th of October 2015 for SMOS (top) and SMAP (bottom). The restrictions imposed on the RMSD of the SMOS data have a clear impact on results. The TB uncertainties for SMOS in majority over 2 K lead at higher thicknesses to high uncertainty. Because the SMAP data is still containing the full daily variability of observations of one day, there will be grid cells with over 5 K uncertainty, but overall the median is around 1.2 K, in comparison with SMOS where the uncertainties are clustered around 4 K. Again, the smaller uncertainty of the SMOS data is only due to the TB fitting procedure, which removes outliers. Without that, for the raw data, the SMOS uncertainty would be similar or even larger than for SMAP. The CFDD daily variability uncertainty offers an offset of the SIT uncertainty relative to the zero line until approximately 20 cm. For both sensors we can observe a rapid increase of the uncertainties beyond 35 20 cm SIT (Fig. 8) 10) which can be explained by the high impact of SIC and the high sensitivity of the retrieval at values over 30 cm.

5.3 Sea Ice Concentration impact

6 Comparison to ship based observations

~~The SIT retrieval used in this paper assumes 100% ice concentration. As a result, the retrieved sea icethickness decrease if this condition is not fulfilled. We assume that brightness temperature over sea ice varies linearly with the change in sea ice concentration:~~

$$TBp(SIT, IC) = TBp_i(SIT) \cdot IC + TBp_w \cdot (1 - IC)$$

5 ~~where *p* represents the polarization, TBp_i and TBp_w are the brightness temperatures of ice and water, respectively and *IC* is~~ Due to the nature of thin sea ice, in situ observations are extremely rare. Thin sea ice appears usually during the initial stages of the freeze-up period. Depending on the surface radiative energy fluxes and precipitation the sea ice ~~concentration.~~

~~For this study we first use 40° SMOS brightness temperatures from 11 October~~ growth may vary. From the initial formation sea ice to 50 cm thickness it may take less than one month. This can leave a short amount of time for in situ observations. In this

10 section we will compare the SIT recorded from the R/V Sikuliaq during the period 5th of October to 4th of November 2015 ~~for retrieval. The resulting SIT will be considered the assumed sea ice thickness. In the second step we take the same TBs as input for TBp_i, use fixed tie points for TBp_w with 85 K and 125 K as values for the horizontal and vertical TBs, respectively. For each pair of SMOS and water brightness temperatures we consider a range of sea ice concentrations for which we compute SIT using Eq. 4. The assumed SIT is grouped in bins~~ in the Beaufort and Chukchi Seas with SIT data obtained from our combined

15 SMOS/SMAP product. With more than 75 % of the ship observations being of thin ice below 50 cm ice thickness, the dataset is well suited for comparison to the SMOS/SMAP product presented in this paper. The SIT and SIC data recorded by the ship was done mainly by hourly visual ice observations using the ASPeCT protocol. During the day this allowed for an approximate radius of 1 ~~cm thickness. Its corresponding thicknesses from~~ km, while during the night just in the ship vicinity covered by the floodlights.

20 We divide the ship data into separate days, and average the ice thicknesses within a 20 km radius from the center of each 12.5 km sized NSIDC grid cell. Figure 11 shows the ~~second step are averaged for each SIC separately. Figure7 shows how the retrieved SIT varies relative to the assumed SIT depending on the SIC. For a SIC of~~ comparison between the SMOS/SMAP product and the ship based observations with the color indicating the ice concentration. The estimation of the ice area fraction was done using the ASI ice concentration product from the university of Bremen resampled to the 12.5km grid. The points

25 are well aligned around the one-to-one line even though with a high scatter. We eliminate grid cells which contain in the ship data thicknesses between 60 and 120 cm. With the remaining data we compute a linear regression of the two datasets which results with a slope of 0.71, an RMSD of 6.58 cm and a correlation coefficient of 0.58. In this comparison, no SMOS/SMAP observations show higher ice thicknesses than 30 cm which may be caused by the reduced ice concentrations, e.g., for 90~~% at 10 cm the retrieved SIT is 8.5 cm, while at 50 cm is just 28 cm.~~

30 ~~Current retrievals for SIC are influenced by thin sea ice. In Heygster et al. (2014), SIC algorithms have been tested for 100% sea ice concentration with thicknesses below 50 cm . All algorithms show less than 100% SIC for thicknesses below~~ % SIC the retrieved SIT cannot be higher than 30 cm (see Fig. **??**). We can see that there is high covariance between the SIC and the SIT with most low thicknesses appearing in areas with low SIC. ~~In another study done by Ivanova et al. (2015) all SIC algorithms registered a decrease in SIC, up to 60% at 5 cm, and an overall bias of 5% for over 30 cm. As we~~

~~have observations at two polarizations at each grid cell available, it should in principle be possible to retrieve SIT and ice concentration simultaneously.However, an attempt has shown a strong noise increase in SIT (Kaleschke et al., 2013).~~

~~During the winter~~ The outliers at high SIT are probably caused by the local effects, e.g., small pieces of very thick ice close to the ship while in a larger area in order of 20 km radius SMOS/SMAP footprints thin ice is dominant. The fact that most of the ~~Arctic is covered by SIC of 90% and higher (Andersen et al., 2007). For an assumed uncertainty of~~ area was covered by thin ice makes it quite likely that larger area averages yield thinner ice compared to the local observations.

The comparison of ship based with satellite based observations is problematic as the scale of the ~~sea ice concentration data of 4% (Ivanova et al., 2015) the error that could be introduced by a correction of sea ice thickness for high SIC is higher than that of the error introduced by~~ observations differ by a large amount. Satellite footprint sizes from SMOS and SMAP are in an order of 20 km radius while the observations based on the ASPeCT protocol are very local with 1 km radius. With a straight route of the ship based ice observations through a SMOS/SMAP satellite footprint, only about 6 % of the area is covered. Therefore this comparison heavily relies on the assumption of ~~100% sea ice concentration (Tian-Kunze et al., 2014).The uncertainty of SIC algorithms at high concentration and their covariation at thin thicknesses will cause high errors if a correction to SIT is applied using current SIC datasets.As a result full ice cover is assumed for the SIT retrieval~~ consistency of ice conditions, i.e., high spatial autocorrelation of ice thickness.

7   Conclusions

The existing retrieval for thickness of thin sea ice (Huntemann et al., 2014) from the L-band sensor SMOS (launched 2009) has been adapted to SMAP (launched 2015) by (i) modifying the SMOS retrieval to use 40° incidence angle instead of the average in the range 40° to 50°, and (ii) establishing a linear regression between the SMOS and SMAP ~~brightness temperatures~~ TBs at 40° incidence angle.

To derive the SMOS ~~brightness temperature~~ TB at 40° incidence angle required for the first step, an analytical function is fitted to the incidence angle dependent ~~brightness temperatures~~TBs. SMAP top of the atmosphere data and the SMOS data fitted to the same incidence angle yield a small TB RMSD between the two datasets for both polarizations of 2.7 K and 2.81 K for TB_h and TB_v, respectively. This is an improvement compared to previous attempts (Huntemann et al., 2016) where the RMSD for both polarizations was over 4 K. Moreover the SMOS based ice thickness retrieval has been adjusted to the new SMOS data version 6.20. The new algorithm contains a new RFI filtering routine exploiting the dependence of the ~~brightness temperatures~~ TBs on the incidence angle. This method improved coverage of previously RFI affected areas. Although the TB datasets of the two sensors are processed differently, the overall resulting thicknesses are similar, with SMOS TBs having smaller variability at lower thicknesses due to the iterative observations removal operation~~,.~~. The comparison with in situ data shows a good agreement between the combined product and the ship observations.

Concluding, the benefit of SMAP for retrieval of thickness of thin sea ice is twofold: first, the combined product has a better spatial and temporal coverage that in future studies can allow insights even on a sub-daily scale. The overall increase in spatial coverage is 6%, although most of this is found in the lower latitudes where the existence of sea ice is minimal. Second, SIT

can be retrieved from any of the two sensors alone with similar accuracy, making the production chain more stable in the case of malfunction of one of the two sensors. The small differences in retrieved SIT between the presented method and the method from Huntemann et al. (2014) allows us to refer to their comparisons for the assessment of the quality of this product. ~~A full validation of the current retrieval requires a comparison with independent in-situ sea ice thickness data currently not available~~

5   ~~at the scales of thickness (below 50 cm) and horizontal extent of the sensor footprint (~43 km diameter).~~

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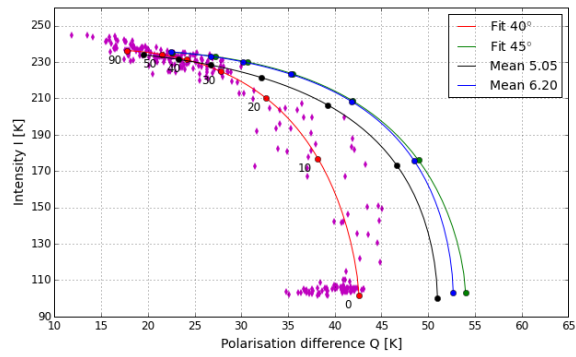
Figure 1. Sea Ice Thickness retrieval curves derived from SMOS data representing original algorithm (black), new data version (blue), 45°
(green) and 40° (red) incidence angle fitted ~~brightness temperatures~~TBs. Dots represent data from the three training areas used for obtaining
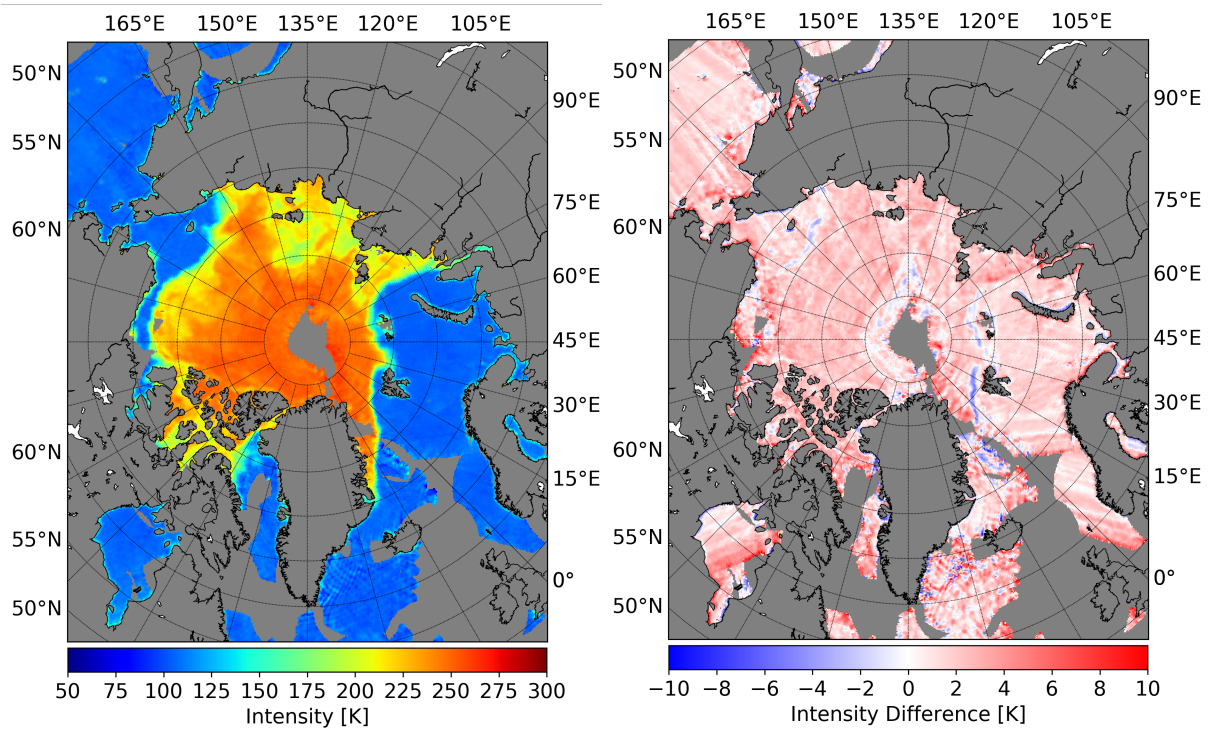the 40° fit curve. Numbers under the curve represent the SIT in centimeters.

Figure 2. SMOS intensity for data version 6.20 data (left) for 29 October 2010 ; intensity difference (right) between the 6.20 and the 5.05 data versions.
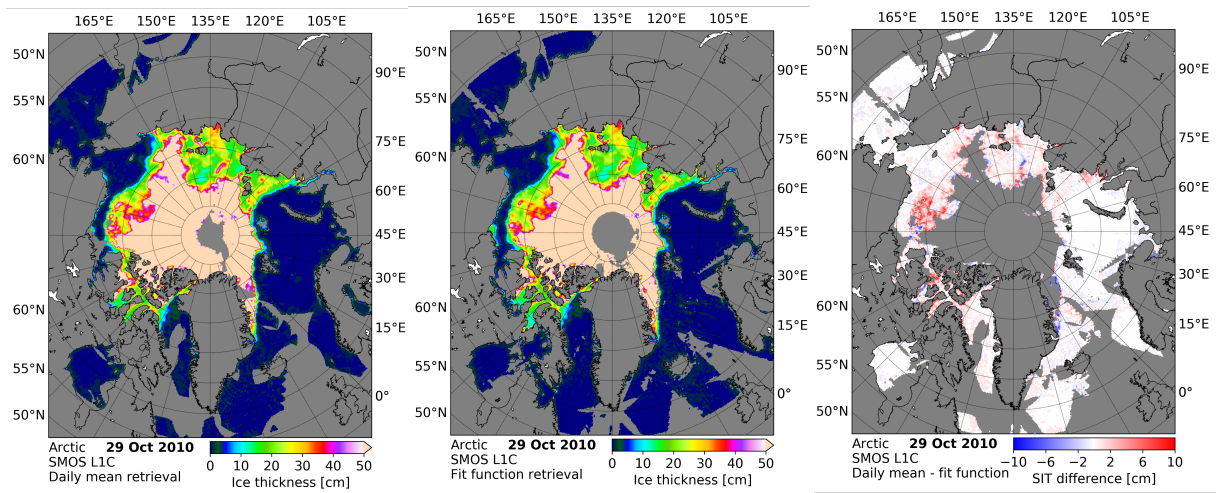
Figure 3. SMOS sea ice thickness retrieved on 29 October 2010 using 6.20 retrieval (left), retrieval using 45° incidence angle fitted ~~brightness temperatures~~ TBs (central), and the difference between the two (right) with areas over 50 cm SIT not shown.
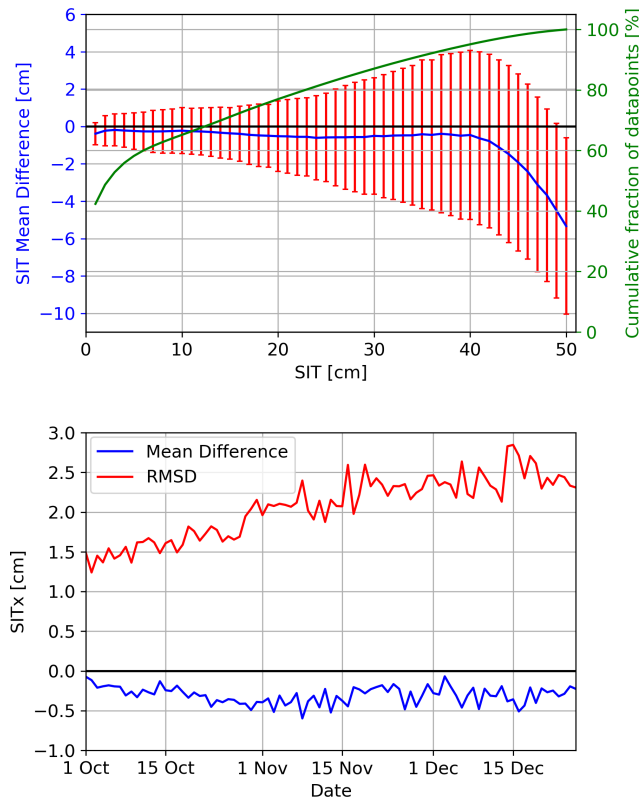
Figure 4. (Top) SIT ~~bias~~ mean difference (blue) calculated by substracting the SIT computed using 40-50° daily average from SIT using TBs fitted at 45° for the 1 Oct. to 26 Dec. 2010 period. ~~Bias~~ Mean difference is computed relative to the daily average SIT in bins of 1 cm and its coresponding RMSD (red). Green curve represents the fraction from the total amount of data points for each thickness bin. Bottom figure shows the ~~bias~~ mean difference (blue) and RMSD (red) for each day separately.
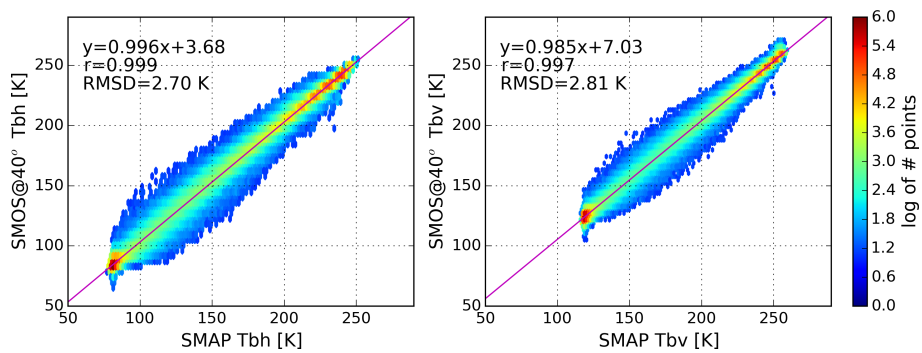
Figure 5. Logarithmic density plot of TB_h (left) and TB_v (right) data from SMAP and SMOS for the period 1 October to 31 December 2015. Magenta lines represent the linear regression between the two datasets.
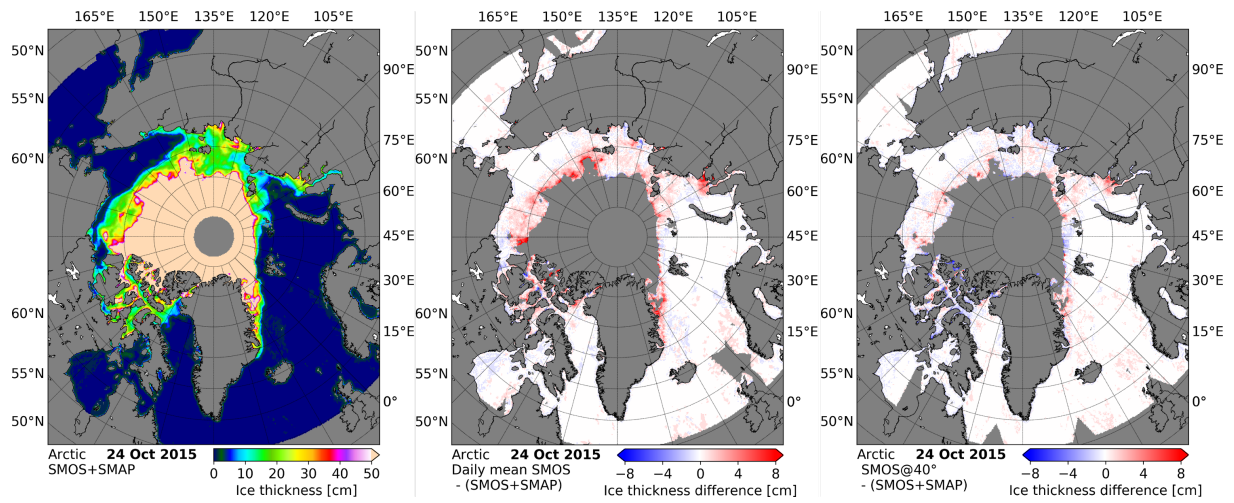
Figure 6. Sea Ice Thickness retrieved on 24 October 2015 for the joint SMOS+SMAP product (left), the SIT difference between the SMOS daily mean retrieval and the joint retrieval (center), and the SIT difference between SMOS fitted TBs at 40° incidence angle and the joint retrieval (right).
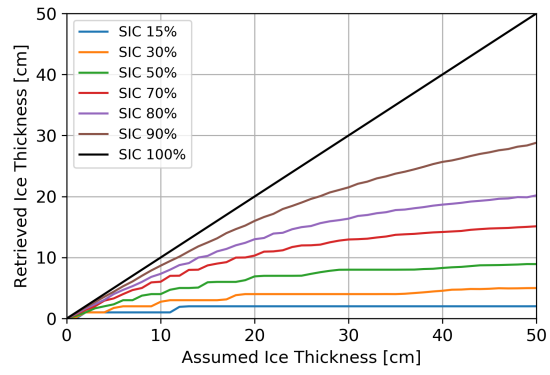
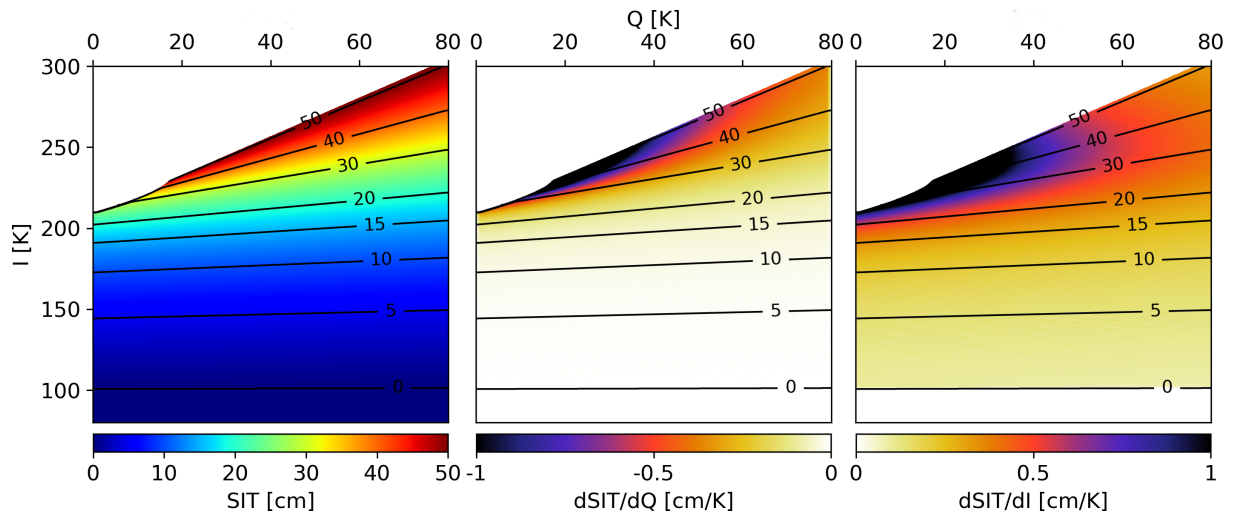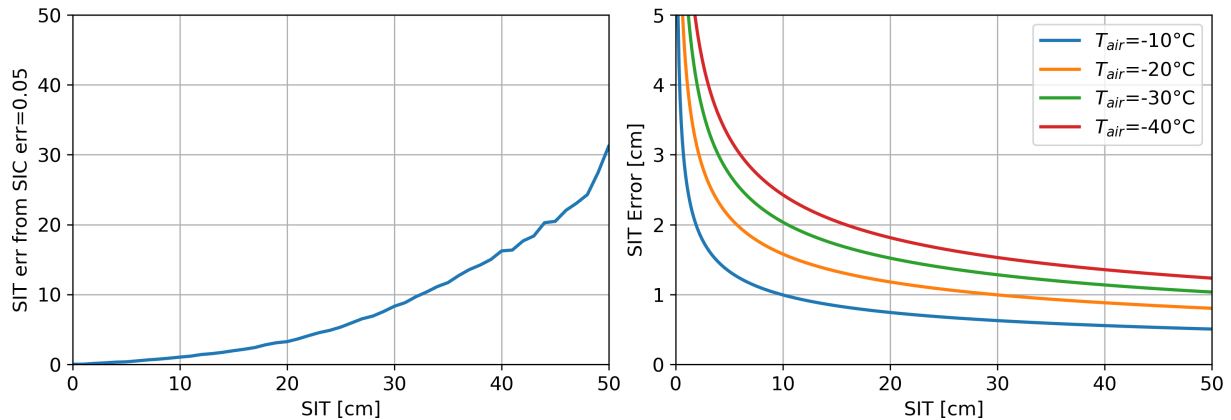**Figure 7.** SIT retrieved as function of the assumed SIT under different SIC values.

Figure 8. SIT (left) computed with the 40° TB algorithm (Fig. 1 red curve) represented in the space of TB_h Q and TB_v I. Derivative of SIT as a function of TB_h Q (center) and TB_v I (right). ~~Black line represents~~ The black lines in all three figures represent the ~~location~~ isolines of ~~equal TB_h and TB_v, with~~ the ~~area above~~ SIT derived from the ~~line (TB_v higher than TB_h) representing values found in observations~~ left figure.

(Right) SIT ~~retrieved~~ error as function of ~~the assumed~~ SIT ~~under different SIC values~~due to CFDD daily variability calculated for various fixed 2 meters air temperatures.

(Right) SIT ~~retrieved~~ error as function of ~~the assumed~~ SIT ~~under different SIC values~~due to CFDD daily variability calculated for various fixed 2 meters air temperatures.

Figure 9. ~~Scatter of SMOS (top~~Left~~) and SMAP (bottom) retrievals at 40incidence angle for 11 Oct. 2015 in the Arctic and their respective uncertainties. Red line represent the rolling average~~ SIT error with change of ~~the~~ SIT for a SIC uncertainty of 5%.

(Right) SIT ~~retrieved~~ error as function of ~~the assumed~~ SIT ~~under different SIC values~~due to CFDD daily variability calculated for various fixed 2 meters air temperatures.
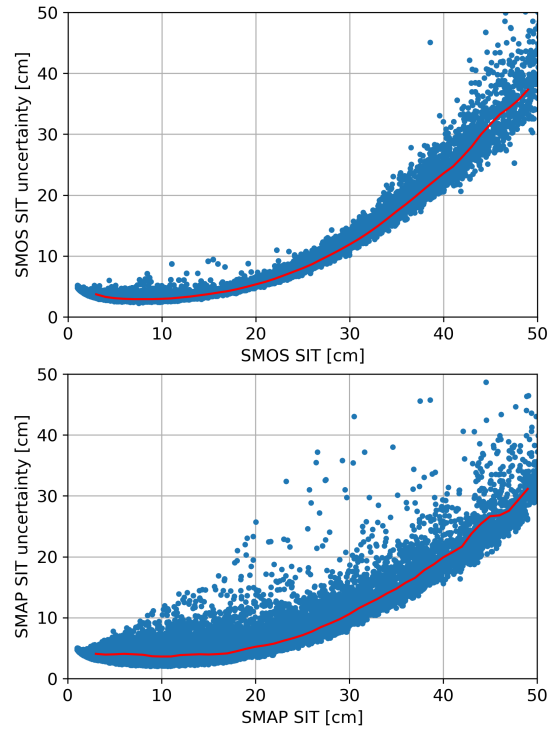
Figure 10. Scatter of SMOS (top) and SMAP (bottom) retrievals at 40°incidence angle for 24 Oct. 2015 in the Arctic and their respective uncertainties. Red line represent the rolling average of the uncertainty.
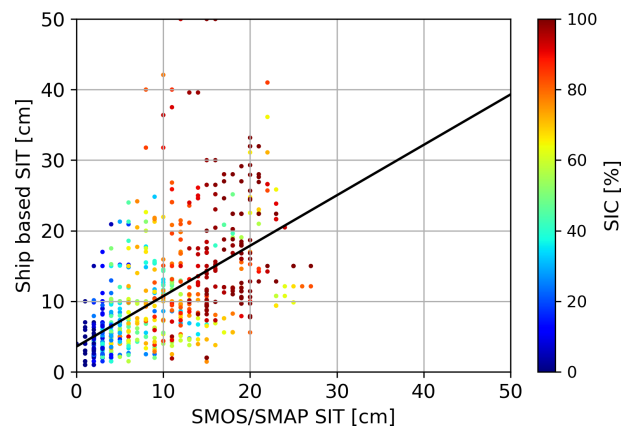
Figure 11. Comparision of ASPeCT based ice thicknesses observations by R/V Sikuliaq and the SMOS/SMAP retrieval. Ice concentration from the ASI product for the corresponding ice thickness observation is colorcoded. Black line represents the linear regression of the two datasets.

Table 1. Sea ice thickness retrieval curve parameters for the original 5.05 data version training, 6.20 training, and the two fit curve parameters for 40° and 45° incidence angle

Retrieval	Parameter	a [K]	b [K]	c [cm]	d
5.05	I_{abc}	234.1	100.2	12.7	-
	Q_{abcd}	51.0	19.4	31.8	1.65
6.20	I_{abc}	235.7	103.0	12.7	-
	Q_{abcd}	52.7	22.3	33.2	1.60
fit 40°	I_{abc}	236.4	101.5	12.2	-
	Q_{abcd}	42.6	17.3	32.9	1.39
fit 45°	I_{abc}	235.4	103.3	12.5	-
	Q_{abcd}	54.0	22.2	33.0	1.47

Table 2. Parameters for linear regression between SMOS and SMAP ~~brightness temperatures~~TBs

Polarization	Slope	Intercept [K]	RMSD [K]	r
H	0.996	3.68	2.70	0.999
V	0.985	7.03	2.81	0.997