# Reflective properties of melt ponds on sea ice

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**Abstract.** Melt ponds occupy a large part of the Arctic sea ice in summer and strongly effect the radiative budget of the atmosphere-ice-ocean system. In this study, the melt pond reflectance is considered in the framework of radiative transfer theory. The melt pond is modeled as a plane-parallel layer of pure water upon a layer of sea ice (the pond bottom). We consider pond reflection as comprising of Fresnel reflection by the water surface and multiple reflections between the pond surface and its bottom, which is assumed to be Lambertian. In order to give a description of how to find the pond bottom albedo, we investigate the inherent optical properties of sea ice. Using the WKB (Wentzel-Kramers-Brillouin) approximation approach to light scattering by non-spherical particles (brine inclusions) and Mie solution for spherical particles (air bubbles), we conclude that the transport scattering coefficient in sea ice is a spectrally independent value. Then, within the two-stream approximation of the radiative transfer theory, we show that the under-pond ice spectral albedo is determined by two independent scalar values: the transport scattering coefficient and ice layer thickness. Given the pond depth and bottom albedo values, the bidirectional reflectance factor (BRF) of a pond can be calculated with analytical formulas. The effects of the incident conditions and the atmosphere state are examined. It is clearly shown that atmospheric correction is necessary even for *in situ* measurements. The atmospheric correction procedure has been used in the model verification shown. The optical model developed is verified with data from *in situ* measurements made during three field campaigns performed on landfast and pack ice in the Arctic. The comparison to field spectra demonstrates good performance of the model developed herein for the variety of melt pond types observed in the Arctic.

## 1 Introduction

Melt ponds occupy a large fraction of the Arctic sea ice surface in summer: up to 60% on multiyear ice according to Maykut et al. (1992) and up to 80% on landfast ice according to Langleben (1971) with more typical values between 20% and 40% (Polashenski et al., 2012; Rösel et al., 2012; Istomina 2015b). They reduce the ice albedo significantly and, therefore, increase the flux of absorbed sunlight energy and speed up the process of melting, thus amplifying the positive ice-albedo feedback effect (Curry et al., 1995; Eicken et al., 2004; Pirazzini, 2008; Schröder et al., 2014). Including light reflection by melt ponds into climate models is an important task (Flocco et al., 2010; Flocco et al., 2012; Hunke et al., 2013; Lüpkes et

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al., 2013), particularly in light of the environmental changes observed recently. These include observations that the melt onset is shifting earlier, and the whole melt season is getting longer (Serreze et al., 2000; Dethloff et al., 2006; Perovich et al., 2008; Markus et al., 2009; Pistone et al., 2014). As the prevailing sea ice type changes from MYI to FYI in the recent decades (Comiso, 2012; Maslanik et al., 2011; Maslanik et al., 2007), the topography of the sea ice evolves from rough

5 (MYI) to uniform, flatter surface (FYI). As the relief of the sea ice is closely connected to the MPF (Polashenski et al., 2012), the average maximum MPF is expected to increase as well. A physical model of the reflective properties of melt ponds is needed for understanding the physics of sea ice, as well as for the correct interpretation of the results of remote sensing and field measurements (Herzfeld et al., 2006; Tschudi et al., 2008; Rösel et al., 2012; Warren, 2013; Zege et al., 2015).

10 Melt ponds on summer sea ice have a wide variety of observed albedo. They can change from light blue ponds, when just formed, to dark mature ones late in melt, meaning that the character of the ponds is important in addition to their coverage (Perovich, 1996; Barry, 1996; Nicolaus et al., 2010; Sankelo et al., 2010; Polashenski et al., 2012). Although there are quite a lot of measurements of melt pond spectral albedo (e.g., Perovich, 1994; Morassutti and Ledrew, 1996; Perovich et al., 2002, 2009), an adequate physical and optical model of melt pond reflection is still absent. Makshtas and Podgorny (1996)

15 gave the analytical formula expressing the pond albedo in terms of the albedo of its bottom. However, despite asserting that bottom albedo is the main factor that determines the albedo of a pond as a whole, they did not address how to calculate it. This essential gap exists up to now. In this work we propose a simple solution for determining the pond bottom spectral albedo. This solution has required the detailed consideration of the inherent optical properties of sea ice, which forms the pond bottom. In addition, the question of the angular distribution of light reflected by a melt pond is still open. The angular

20 distribution is highly important for understanding Arctic energy balance because only the bi-directional reflectance is measured by satellite optical sensors and it is necessary to model the bi-directional reflectance distribution function (BRDF) to determine surface albedo from satellite data. Additionally, the processing of the reflectance measurement data, both satellite and ground-based, requires atmospheric correction, especially for polar regions. All these points are discussed in this work.

25 The paper is arranged as follows. First, our model of melt pond reflectance is described in Section 2. Subsection 2.1 presents the derivation of the formulas for pond reflectance, given by Makshtas and Podgorny (1996), expanded to various incident conditions. Inherent optical properties (IOPs) of sea ice are considered in subsection 2.2. A simple analytical solution for bottom albedo in terms of the ice IOPs and its thickness is given in subsection 2.3. Subsection 2.4 gives a final summary of the model developed. Section 3 discusses how illumination conditions are accounted for in processing and how the

30 experimental results are interpreted. The atmospheric correction of experimental data is considered in subsection 3.1. A possibility to use the near IR reflectance as an evidence of the ice grains presence is discussed in subsection 3.2. Notes about processing experimental data when the incident angle is unknown are given in subsection 3.3. Then, Section 4 presents the verification of the developed model with the three datasets of *in-situ* measurements (Polarstern-2012, Barrow-2008, and SHEBA-1998). The conclusion sums up the paper.

In this work we propose a simple optical model that enables the parameterization of the pond bottom albedo with a few physical characteristics and thus determines the spectral reflective properties of the melt pond as a whole, including its bidirectional reflectance.

## 2 Model description

### 2.1 Radiance reflected by a melt pond

The model of reflection by melt ponds given in Makshtas and Podgorny (1996) uses the following assumptions:

1.  the water layer is an infinite plane-parallel layer;
2.  the melt water is pure, with neither absorbing contaminants nor scatterers;
3.  the Rayleigh scattering in water is negligible compared to the water absorption; a ray inside the pond is attenuated according to the exponential law;
4.  the pond bottom reflects light by the Lambert law (the reflected radiance is independent of the direction).

The model described is illustrated in Fig. 1. In this subsection we repeat the derivation of Makshtas and Podgorny (1996), expanding it to various illumination and observation conditions.

Let $E$ be the incident spectral irradiance. Then the light intensity (radiance) at the upper pond boundary is:

$$I_0 = \delta(\mu - \mu_0)\delta(\varphi)E ,\tag{1}$$

where $\delta(x)$ is the Dirac $\delta$-function, $\mu = \cos\theta$ ($\mu_0 = \cos\theta_0$), $\theta$ is the observation zenith angle ($\theta_0$ is the solar zenith angle), $\varphi$ is the observation azimuth (counted from the solar principal plane).

The intensity of light reflected from the surface is:

$$I_0^R = R^F(\mu_0)\delta(\mu - \mu_0)\delta(\varphi)E ,\tag{2}$$

where $R^F(\mu_0)$ is the Fresnel reflectance for incidence angle $\theta_0$.

When the ray of intensity $I_0$ at incident angle $\theta_0$ is refracted by the pond boundary, the angle of refraction $\theta_0^w$ is given by Snell's law:

$$\theta_0^w = \arcsin\left(\frac{1}{n}\sin\theta_0\right),$$
$$\mu_0^w = \frac{1}{n}\sqrt{n^2 - 1 + \mu_0^2},\tag{3}$$

and the intensity of light just under the boundary is given by the law of conservation of basic radiance:

$$I_0^{w\downarrow} = T^F(\mu_0)I_0 n^2 ,\tag{4}$$

where $T^F(\mu_0)$ is the Fresnel transmittance for incidence angle $\theta_0$.

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The light field inside the pond can be divided into the up- and down-welling fluxes. The up-welling flux is the light reflected by the pond bottom. The intensity of the down-welling light inside the pond $I^{w\downarrow}$ consists of the direct light intensity $I_0^{w\downarrow}$ (direct solar light, refracted by the pond surface) and the diffuse light intensity $I_1^{w\downarrow}$ (the light that was subjected to reflections between the water-ice (WI) and air-water (AW) interfaces):

$$I^{w\downarrow} = I_0^{w\downarrow} + I_1^{w\downarrow}. \tag{5}$$

The direct light flux, incident to the pond bottom, is:

$$F_0^w = T^F(\mu_0)E\mu_0 \exp\left(-\frac{\varepsilon_w z}{\mu_0^w}\right), \tag{6}$$

where $\varepsilon_w$ is the extinction coefficient of water, equal to the sum of the water absorption ($\alpha_w$) and scattering ($\sigma_w$) coefficients:

$$\varepsilon = \alpha_w + \sigma_w. \tag{7}$$

We use the data of Segelstein (1981) for the water absorption and the power law for the spectral scattering coefficient:

$$\sigma_w(\lambda) = \sigma_0\left(\frac{\lambda_0}{\lambda}\right)^{4.3}, \tag{8}$$

where $\lambda$ is the wavelength and $\sigma_0 = 1.7 \times 10^{-3} m^{-1}$, $\lambda_0 = 550 nm$ (Kopelevich, 1983).

The intensity of up-welling light just below the AW interface is:

$$I_1^{w\uparrow}(\mu^w, 0) = I_1^{w\uparrow}(\mu^w, z)\exp\left(-\frac{\varepsilon_w z}{\mu^w}\right). \tag{9}$$

After the internal reflection, the intensity of the down-welling light just below the AW interface is:

$$I_1^{w\downarrow}(\mu^w, 0) = R_{in}(\mu^w)I_1^{w\uparrow}(\mu^w, 0) = R_{in}(\mu^w)I_1^{w\uparrow}(\mu^w, z)\exp\left(-\frac{\varepsilon_w z}{\mu_0^w}\right), \tag{10}$$

where $R_{in}$ is the internal reflection coefficient.

The intensity of the down-welling diffuse light at the pond bottom is

$$I_1^{w\downarrow}(\mu^w, z) = R_{in}(\mu^w)I_1^{w\uparrow}(\mu^w, z)\exp\left(-2\frac{\varepsilon_w z}{\mu_0^w}\right). \tag{11}$$

As the bottom is Lambertian, the intensity of the up-welling light just above the bottom is independent of direction:

$$I_1^{w\uparrow}(\mu^w, z) = I_1^{w\uparrow}(z). \tag{12}$$

The boundary conditions at the pond bottom are:

$$\pi I_1^{w\uparrow}(z) = \pi A_b f_{in}(\varepsilon_w z)I_1^{w\uparrow}(z) + A_b F_0^w, \tag{13}$$

where $A_b$ is the bottom albedo and

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$$f_{in}(x) = 2\int_0^1 R_{in}(\mu^w)\exp\left(-2\frac{x}{\mu^w}\right)\mu^w d\mu^w . \tag{14}$$

From Eq. (13) we have:

$$I_1^{w\uparrow}(z) = \frac{A_b F_0^w}{\pi\left(1 - A_b f_{in}(\varepsilon_w z)\right)} . \tag{15}$$

Putting together Eqs. (4)-(15), we get for the intensity of light $I_1^R$ that goes out from the pond:

$$I_1^R(\mu) = \frac{E\mu_0 T^F(\mu)T^F(\mu_0)A_b}{\pi n^2\left(1 - A_b f_{in}(\varepsilon_w z)\right)}\exp\left(-\frac{\varepsilon_w z}{\mu_0^w} - \frac{\varepsilon_w z}{\mu^w}\right). \tag{16}$$

The total intensity of light reflected by the melt pond is:

$$I^R = I_0^R + I_1^R = R^F(\mu_0)\delta(\mu-\mu_0)\delta(\varphi)E + \frac{E\mu_0 T^F(\mu)T^F(\mu_0)A_b}{\pi n^2\left(1 - A_b f_{in}(\varepsilon_w z)\right)}\exp\left(-\frac{\varepsilon_w z}{\mu_0^w} - \frac{\varepsilon_w z}{\mu^w}\right). \tag{17}$$

The bidirectional reflectance factor (BRF) by definition is equal to:

$$R = \frac{\pi I^R}{\mu_0 E} . \tag{18}$$

Hence the BRF of a melt pond is:

$$R = \frac{\pi}{\mu_0}R^F(\mu_0)\delta(\mu-\mu_0)\delta(\varphi) + \frac{T^F(\mu)T^F(\mu_0)A_b}{n^2\left(1 - A_b f_{in}(\varepsilon_w z)\right)}\exp\left(-\frac{\varepsilon_w z}{\mu_0^w} - \frac{\varepsilon_w z}{\mu^w}\right). \tag{19}$$

The first term describes the sun specular reflection from the AW surface; the second one describes the light, multiply reflected between the pond bottom WI and the surface AW.

The albedo at direct incidence $A(\mu_0)$ (the black-sky albedo)

$$A(\mu_0) = \frac{1}{\pi}\int_0^{2\pi}\int_0^1 R(\mu)\mu\, d\mu\, d\varphi . \tag{20}$$

is found by means of integrating Eq. (19):

$$A(\mu_0) = R^F(\mu_0) + \frac{T^F(\mu_0)f_{out}(\varepsilon_w z)A_b}{n^2\left(1 - A_b f_{in}(\varepsilon_w z)\right)}\exp\left(-\frac{\varepsilon_w z}{\mu_0^w}\right), \tag{21}$$

where

$$f_{out}(x) = 2\int_0^1 T^F(\mu)\exp\left(-\frac{x}{\mu^w}\right)\mu\, d\mu . \tag{22}$$

The albedo at diffuse incidence $A^D$ (the white-sky albedo)

$$A^D = 2\int_0^1 A(\mu_0)\mu_0 d\mu_0 . \tag{23}$$

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is found by integrating Eq. (24):

$$A^D = R^{FD} + \frac{f_{out}^2(\varepsilon_w z)A_b}{n^2(1 - A_b f_{in}(\varepsilon_w z))}, \tag{24}$$

where $R^{FD}$ is the Fresnel reflectance for the diffuse incidence.

Functions $f_{in}(x)$ and $f_{out}(x)$ are related by the equation:

$$f_{out}(2x) = n^2\left(2E_3(2x) - f_{in}(x)\right), \tag{25}$$

where $E_3(x)$ is the integral exponential function of the third power:

$$E_3(x) = \int_1^\infty \frac{e^{-xt}}{t^3} dt. \tag{26}$$

However, the relationship (25) is not very useful in numerical calculations, because these functions are evaluated at different argument values ($x$ and $2x$). The way to speed up simulations is to calculate these functions once for a given set of wavelengths and then to use a look-up-table. All the other formulas given in the manuscript are completely analytical and can be used straightforward.

## 2.2    Inherent optical properties of under-pond ice

The main factor in Eqs. (19), (21) and (24) that determines the melt pond reflection is its bottom albedo $A_b$. In order to calculate it we should first consider the inherent optical properties (IOPs) of under-pond ice that forms the pond bottom.

The IOPs of a medium used in the radiative transfer theory are the spectral scattering $\sigma(\lambda)$ and absorption $\alpha(\lambda)$ coefficients and the scattering phase function $p(\theta)$. In the following consideration, as in other radiative transfer theory applications (see, e.g., Davison, 1958; Chandrasekhar, 1960), the transport scattering coefficient $\sigma_t$ is used:

$$\sigma_t = \sigma(1 - g), \tag{27}$$

where $g$ is the average cosine of the scattering angle $\theta$:

$$g = \langle\cos\theta\rangle = \frac{1}{2}\int_0^\pi p(\theta)\cos\theta\sin\theta d\theta. \tag{28}$$

The transport coefficient is useful in calculating the reflection and transmission by a scattering layer with a very forward peaked phase function, particularly if one is interested in the layer albedo, rather than the angular structure (BRF) of the reflected light (Zege et al., 1991).

Main factors that determine optical properties of sea ice are its microphysical structure and values of complex refractive indices of its constituents; the dispersion of complex refractive indices determines the spectral properties of sea ice.

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As the volume concentration of air bubbles in sea ice is small – only up to ~5% even in the extremely bubbly ice (Gavrilo and Gaitskhoki, 1970) – and the complex refractive index of brine is very close to that of ice (see Buiteveld et al., 1994; Warren and Brandt, 2008; and Sec. 2.2b), we take the absorption coefficient of sea ice equal to that of solid ice. Impurities – sediment and organic pigments from sea water – could change absorption coefficients, particularly at shorter wavelengths.

5 At this stage we neglect their effect, keeping in mind that their absorption spectra can be added, if necessary.

The scattering takes place at inhomogeneities in sea ice and is mainly caused by air bubbles and brine inclusions (Mobley et al., 1998; Light, 2010). Another source of scattering could be salt crystals, but they precipitate at low temperatures and are not observed in summer ice, where melt ponds are formed: precipitation temperatures for mirabilite ($Na_2SO_4\ 10H_2O$) and hydrohalite ($NaCl\ 2H_2O$) crystals are $-8^0C$ and $-23^0C$, respectively (Light et al., 2003).

10 *a) Air bubbles*

The upper layer of sea ice (20-30 cm) usually contains a significant amount of air bubbles (Gavrilo and Gaitskhoki, 1970; Mobley et al., 1998), with volume concentration which can reach values of 5%, and which decreases with depth. (We do not consider here the highly scattering surface layer that is formed on top of sea ice during the water drainage process and is commonly referred to as 'white ice' or the 'surface scattering layer'). Air bubbles in sea ice are mostly spherical (Gavrilo

15 and Gaitskhoki, 1970; Mobley et al., 1998; Light, 2010). Light (2010) gives the following size distribution for bubbles in first-year sea ice:

$$N(r) \sim r^{-1.5}, \qquad 4\mu m \le r \le 70\mu m. \tag{29}$$

Gavrilo and Gaitskhoki (1970) report the presence of much larger bubbles in the bubbly ice (from 0.1 to 2 mm with the exponent $-1.24$).

20 However, since air bubbles in ice are optically hard (the refractive index of air differs strongly from that of ice) and do not absorb light, scattering by bubbles of this size range is described by the laws of geometrical optics. Thus, the scattering characteristics do not depend on the bubble size (unless considering the strictly forward and backward directions), and the shape of the size distribution is also insignificant. Particularly, the scattering efficiency $Q_{sca}$ in this case equals 2 and the phase function can be easily calculated with the Mie formulas for any type of size distribution, e.g., for the one given in

25 Eq. (29).

The refractive index of air (relative to ice) in the interval 0.35-0.95 μm changes from 0.755 to 0.768 with average value of 0.763 within this interval. The corresponding average cosine $g$ of the scattering angle, obtained with the Mie calculations, takes values from 0.851 to 0.865 with the mean value of 0.860, and therefore the spectral variability does not exceed 2%.

*b) Brine inclusions*

30 The main features of brine inclusions are the following: they are optically soft, i.e., their refractive index $n_b$ (brine relative to ice) is close to unity; their size is large (comparing to the wavelength); and their shape is strongly irregular (here we only

consider inclusions filled with brine and not drained brine pockets/channels that contain air). Under these assumptions we can apply the approximation for irregularly shaped particles developed by Malinka (2015) to describe scattering properties of brine inclusions.

The size of brine inclusions, which can be on the order of several millimeters, is so much larger than the wavelength of visible light that their optical properties can be considered in the limit of infinitely large particles, despite their refractive index $n_b$ is close to unity:

$$n_b - 1 \ll 1. \tag{30}$$

At this limit the size distribution is also insignificant and the scattering efficiency $Q_{sca}$ is independent of the wavelength:

$$Q_{sca} = 2. \tag{31}$$

The scattering phase function of optically soft particles can be approximated according to Malinka (2015) by:

$$p(\theta) = \frac{2x^2(1 + \mu^2)}{\left(1 + 2x^2(1 - \mu)\right)^2}, \tag{32}$$

where $\mu = \cos\theta$ and $x$ is the optical particle size (dimensionless), which for large particles equals:

$$x = \frac{n_b + 1}{n_b - 1} \sqrt{\frac{Q_{sca}}{8}}. \tag{33}$$

In view of Eqs. (30) and (31), we can write:

$$x = \frac{1}{n_b - 1}. \tag{34}$$

The average cosine $g$ of the phase function (32) is:

$$1 - g = \frac{\log 2x - 1}{x^2}. \tag{35}$$

Figure 2 demonstrates the spectral dependence of the refractive index of water relative to ice. We used the data by Warren and Brandt (2008) for ice. The refractive index of water is taken from Hale and Querry (1973), Segelstein (1981), Daimon and Masumura (2007), and Kedenburg et al. (2012) for distilled water, from the formula of Quan and Fry (1995) for brine of zero salinity , i.e., fresh water, at temperature 0°C, and from the formula of Frisvad (2009), which is based mainly on Quan and Fry (1995) and the measurements by Maykut and Light (1995), for brine with equilibrium salinity at temperatures $-2^0\text{C}$ , $-4^0\text{C}$ , and $-6^0\text{C}$ . The earlier data (Hale and Querry, 1973 and Segelstein, 1981) clearly demonstrates the spectral dependences, their dispersions being opposite. In contrast, the newer data do not demonstrate such dependence: according to the more modern data the refractive index (relative to ice) of water, including brine, is almost spectrally neutral. This question is important when describing the light scattering by brine inclusions in ice, because the transport scattering coefficient is determined mainly by the value $(n_b - 1)^2$ (see Eqs. (27) and (34) -35)). Finally, according to the newer data we

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will accept that the relative refractive index of brine, and therefore the transport scattering coefficient of brine inclusions, is spectrally neutral. E.g., $n=1.024$ for temperature $-2^0C$ and, according to Eqs.(34)- (35), $g = 0.998$. Note that the value of $g$ in this model is significantly greater than that used in many other studies, e.g., in Mobley et al., (1998) or Light et al., (1998).

5    *c)  Inherent optical properties of sea ice*

Light scattering properties of sea ice are a combination of those of brine inclusions and air bubbles. The total and transport scattering coefficients are the sum of the respective values:

$$\sigma = \sigma_b + \sigma_a,$$
$$\sigma_t = \sigma_b^t + \sigma_a^t. \tag{36}$$

We denote the values related to brine inclusions with the subscript $b$ and to air bubbles with the subscript $a$. The phase

10    function and the average cosine are the linear combination of the respective values:

$$p(\theta) = \frac{\sigma_b}{\sigma} p_b(\theta) + \frac{\sigma_a}{\sigma} p_a(\theta),$$
$$1 - g = \frac{\sigma_b}{\sigma}(1 - g_b) + \frac{\sigma_a}{\sigma}(1 - g_a) = \frac{\sigma_t}{\sigma}. \tag{37}$$

Once $g_a$ and $g_b$ are known (e.g., at $-2^0C$ $g_a = 0.86$, $g_b = 0.998$), the resulting $g$ depends only on the proportion of fractions $a$ and $b$.

Generally, the IOPs of sea ice depend on its microstructure. In view of the fact that both bubble and brine inclusion size is

15    much larger than the wavelength, the scattering coefficient equals:

$$\sigma_j = 2\psi_j \qquad (j = a,b), \tag{38}$$

where $\psi$ is the specific cross-sectional area of inclusions (air or brine):

$$\psi_j = \langle S_\perp \rangle_j N_j = \frac{3C_j^V}{4R_j}. \tag{39}$$

Here subscript $j$ shows the fraction number, $\langle S_\perp \rangle_j$ is the average cross-sectional area of $j$-inclusions, $R_j$ their effective

20    radius, $N_j$ and $C_j^V$ are their numeric and volume concentration, respectively.

The phase function (and consequently its average cosine $g$) can be characterized by the ratio of volume concentration air-to-brine $C_a^V/C_b^V$, if their effective radii are determined. E.g., for the bubble size distribution (29), the effective radius is $R_a = 42.55\mu m$. Light (2010) gives the value of 110 m$^{-1}$ for $\psi_b$, the specific cross-sectional area of brine inclusions, for a sample of typical first year ice at $-15^{\circ}C$, this value can grow up to 400 m$^{-1}$ when the ice warms. The estimate, made by Light

(2010) for the brine volume concentration in the same sample, gives the values from 1.2% to 1.9%. This allows us to estimate the effective radius of brine inclusions as $R_b \approx 100 \mu m$.

However, as the morphology of sea ice can vary drastically with place and time, the more convenient way to characterize the ratio of air and brine fractions is to use the ratio of their transport coefficients $\sigma_a^t / \sigma_b^t$. This ratio is related to the ratio of volume concentrations as:

$$\frac{\sigma_a^t}{\sigma_b^t} = \frac{1 - g_a}{1 - g_b} \frac{R_b}{R_a} \frac{C_a^V}{C_b^V}. \tag{40}$$

Figure 3 presents the phase function of mixtures with different air-to-brine fractions ratio.

We conclude that the phase function (and consequently $g$) of sea ice is spectrally neutral in the visible and near IR range. In virtue of Eq. (38), the scattering coefficient $\sigma$ is also spectrally neutral. Consequently, the transport scattering coefficient $\sigma_t$ is also spectrally neutral and can serve as a scalar parameter that characterizes scattering in sea ice.

## 2.3 Bottom albedo

If both the absorption and transport scattering coefficients are known, the albedo of a layer can be calculated within the two-stream approximation, which is widely used for practical calculations:

$$A_b = A_0 \frac{1 - \exp(-2\gamma\tau)}{1 - A_0^2 \exp(-2\gamma\tau)}, \tag{41}$$

where $A_0$ is the albedo of the semi-infinite layer with the same optical characteristics, $\gamma$ is the asymptotic attenuation coefficient, and $\tau$ is the layer optical thickness. The version of the two-stream approximation developed by Zege et al. (1991) expresses these characteristics as follows:

$$A_0 = 1 + t - \sqrt{t(t + 2)},$$
$$\gamma = \frac{3}{4} \frac{\sigma_t}{\sigma_t + \alpha_i} \sqrt{t(t + 2)}, \tag{42}$$
$$\tau = (\sigma_t + \alpha_i)H,$$

with
$$t = \frac{8\alpha_i}{3\sigma_t}, \tag{43}$$

where $\alpha_i$ is the ice absorption coefficient; $H$ is the ice layer thickness.

The two-stream approximation in the version given in Zege et al. (1991) has a wide range of applicability and can be used both for strongly and weakly absorbing media, for optically thin and thick layers. Hence, this approximation can be applied to all the variety of melt ponds: from young ponds, which are light blue and have comparatively optically thick under-pond ice, to mature dark ones, where under-pond ice is mechanically and optically thin.

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## 2.4    Model outline

Thus, in the assumption of a Lambertian bottom and plane parallel geometry, which applies in the absence of strong wind, i.e., calm pond surface, the spectral reflection of ponds is determined by two values: water layer depth $z$ and the albedo of the pond bottom $A_b$. The latter, in turn, depends on the transport scattering coefficient of under-pond ice $\sigma_t$ and its geometric thickness $H$ (or, respectively, the transport optical thickness $\sigma_t H$). Note that only value $\alpha_i$ in Eqs.(41) – (43) has a spectral behavior, while the others – $\sigma_t$ and $H$ – are scalars.

So, in the absence of pollutants just three parameters determine the pond spectral reflectance: namely, the transport scattering coefficient $\sigma_t$ and geometric thickness $H$ of the under-pond ice and water layer depth $z$. This statement is confirmed by the coincidence of measured and modeled spectra demonstrated below. The outlined model of a melt pond is shown in short in Table 1.

## 3    Illumination conditions

### 3.1    Atmospheric correction

Correct processing of the reflection measurement results requires the correct modeling of the illumination conditions. This is especially important for measurements in the Arctic, because of the low sun and the bright surface. When the sky is overcast, the incident light is close to diffuse, even if the solar disk is visually observed (Malinka et al., 2016b). In this case the measured albedo is the white-sky one. However, when the sky is clear and the sun is near the horizon, the direct solar flux is comparable to the diffuse flux from the sky, so the measured (blue-sky) albedo value is a mixture of those at direct (black-sky) and diffuse (white-sky) incidence. The black-sky albedo increases when the sun is approaching the horizon, so the difference between the white- and black-sky albedos is most essential at oblique incidence (see Fig. 4). The problem of the correct interpretation of the measured blue-sky albedo is considered in detail in Malinka et al. (2016b) for a homogeneous surface. However, the albedo of a melt pond can differ significantly from that of the surrounding background, e.g., white ice or snow. Some estimation for this case is given below.

Let $R$, $A(\mu_0)$ and $A^D$ be, as before, the BRF, black-sky, and white-sky albedo of a melt pond, respectively. Let the surrounding background be Lambertian with albedo $r_b$. Then the brightness of the incident radiance can be estimated as (Malinka et al., 2016b):

$$B_\downarrow = \left[ t_0(\mu_0)\hat{\delta} + t_d(\mu_0) + \frac{r_a r_b}{1 - r_a r_b} T(\mu_0) \right] \frac{E_0 \mu_0}{\pi}, \tag{44}$$

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where $t_0(\mu_0)$ and $t_d(\mu_0)$ are the direct and diffuse atmosphere transmittances, $\hat{\delta} = \pi\delta(\mu - \mu_0)\delta(\varphi - \varphi_0)/\mu_0$ is the identity operator ($\delta(x)$ is the Dirac delta-function), $T(\mu_0) = t_0(\mu_0) + t_d(\mu_0)$ is the atmosphere transmittance at direct incidence, and $r_a$ is the atmosphere bihemispherical reflectance at incidence from below. $E_0$ is the extra-terrestrial solar irradiance.

So, the light flux incident to a melt pond is:

$$F_\downarrow = \frac{T(\mu_0)}{1 - r_a r_b} E_0 \mu_0 . \tag{45}$$

The radiance of light reflected by pond follows from Eq. (44):

$$
\begin{aligned}
B_\uparrow &= \left[ R(\mu, \mu_0, \varphi) t_0(\mu_0) + A(\mu)\left( t_d(\mu_0) + \frac{r_a r_b}{1 - r_a r_b} T(\mu_0) \right) \right] \frac{E_0 \mu_0}{\pi} \\
&= \left[ \left( R(\mu, \mu_0, \varphi) - A(\mu) \right) t_0(\mu_0) + A(\mu) \frac{T(\mu_0)}{1 - r_a r_b} \right] \frac{E_0 \mu_0}{\pi} .
\end{aligned} \tag{46}
$$

Therefore the reflected flux is:

$$F_\uparrow = \left[ \left( A(\mu_0) - A^D \right) t_0(\mu_0) + A^D \frac{T(\mu_0)}{1 - r_a r_b} \right] E_0 \mu_0 . \tag{47}$$

For the measured value of the blue-sky albedo $A^{blue}$ it follows:

$$A^{blue} = \frac{F_\uparrow}{F_\downarrow} = \frac{\left( A(\mu_0) - A^D \right) t_0(\mu_0)(1 - r_a r_b) + A^D}{T(\mu_0)} . \tag{48}$$

The equation for the blue-sky albedo can be written as a linear combination of the black and white-sky albedos:

$$A^{blue} = w A(\mu_0) + (1 - w) A^D , \tag{49}$$

with the proportion of direct radiance $w$:

$$w = \frac{t_0(\mu_0)}{T(\mu_0)} (1 - r_a r_b) . \tag{50}$$

Factor $(1 - r_a r_b)$ is responsible for multiple reflections between the atmosphere and surrounding background.

Modeled albedo spectra of a light melt pond (a pond with high reflectance) at different illumination conditions are shown in Fig. 5. The angle of incidence is 80° (the sun elevation is 10°). The interval of albedo changes is limited by the values of white and black-sky ones. Also shown are the blue-sky albedos for clear sky and for sky with thin cirrus layer (with optical thickness of 0.1). Both are considered with different surrounding backgrounds: perfectly black ($r_b = 0$) and white ($r_b = 1$). As seen from Fig. 5, the effect of background is negligible (only small difference between blue lines and dotted/crossed line), so the results of melt pond albedo measurements can be processed without *a priori* knowledge of the albedo of the surrounding background.

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### 3.2    IR reflectance

In contrast to the visible range, ice and water absorb a significant amount of light in the IR: a few centimeter thick layer of ice or water completely absorbs radiation in the infrared range. Thus the melt pond optical response in the IR is restricted to the Fresnel reflection by the pond surface. In contrast, ice grains in white ice are of the order of millimeters in size (and even smaller in snow). Due to this fact, the appearance of specific features in the IR portion of the reflection spectra can be used to diagnose the inclusion of unponded ice and snow. In particular, the imaginary part of the refractive index $\kappa$ has a local minimum at 1.1 µm, which provides a slight peak of reflection in the interval 1.05-1.11 µm (Wiscombe and Warren, 1980). Figure 6 shows an example of the modelled albedo's spectral dependence for white ice, snow, and a melt pond. It clearly demonstrates that for wavelengths longer than 0.9 µm the melt pond reflection is restricted by the Fresnel reflection to a constant value, while snow and white ice demonstrate a local maximum at 1.1 µm. Thus, this slight peak can serve as a criterion for determining if a spectrum is taken entirely from an open pond or partially from snow/ice surface. If this peak is observed in a measured spectrum, it clearly indicates the presence of ice grains (of white ice or snow) in the receiver field of view.

### 3.3    Measurement geometry

In the description of the field data used in this study, most sky conditions were reported as overcast. Only a few measurements were taken under clear sky conditions. Scattered clouds were not reported at all in the measurement series considered. In the cases of overcast sky, the measured albedo was interpreted as the white-sky one. In the clear sky cases, the Rayleigh atmosphere with the Arctic Background aerosol (Tomasi et al, 2007) was assumed. In this case the solar incidence angle was determined from the pond reflection in the IR: at the interval 1.25-1.3 µm (preferably) or 0.85-0.9 µm, if data at the former interval are not available. As the IR signal (both incident and reflected) is quite weak and hence some noise is always noticeable, we average the signal over one of the abovementioned intervals. The pond reflectance in these IR intervals is completely determined by the Fresnel reflection of its upper boundary. Atmosphere scattering in the IR is negligible (especially at 1.3 µm), so the incident light is unidirectional. In this situation the solar incident angle can be calculated through the Fresnel equations.

## 4    Model verification

Three different datasets with in-situ field measurements were used for the evaluation of the pond model. They are described in the next subsections.

### 4.1    Polarstern-2012

Measurements of the spectral albedo of different sea-ice  surfaces were carried out during the R/V *Polarstern* cruise ARK-XXVII/3 (August 2 – October 8, 2012). Only in the second half of the cruise did the vessel leave the marginal ice zone and

enter the ice pack. The ice thickness varied from 0.5 to 3 meters with an average of 1-1.5 meter. Melt ponds were observed in August. The ponds were both open (with no skim ice) and frozen over (with a skim of ice), sometimes snow covered. The data were collected during stations, when the vessel was parked at an ice floe for several days. This gave the possibility to obtain several-day data sequences of melting sea ice and evolving melt ponds at the same location. The stations, where ponds were observed, were located from 84°3N, 31°7E to 82°54N, 129°47E. For more information about the cruise, see Boetius et al. (2012) and Istomina et al. (2016). The ASD FieldspecPro III spectroradiometer used for these measurements has three different sensors that provide measurements from 350 nm to 2500 nm with the spectral resolution of 1.0 nm. A sensor measures the light signal supplied by a fiber optical probe, which collects light reflected by a 10x10 cm$^2$ *Spectralon* white plate. The plate was held at about 1 meter above the surface and was directed first towards the measured surface and then towards the sky. The ratio of these two measurements gives the hemispherical reflectance (albedo) of the surface. For some cases the water depth and ice thickness within the pond were measured.

For the model verification we considered the melt pond albedo in the spectral interval 0.35 – 1.3 μm. The retrieval procedure implies searching for the pond parameter values shown in Table 1. These three parameters comprise a 3D-vector, which is varied to provide the best fit (in the sense of the least squares) of the measured and modeled spectra. For the cases where the pond depth and underlying ice thickness were measured, the pond parameters retrieved were compared to the measured ones. Some ponds were frozen over, i.e., they had a layer of newly formed ice on top of their surface. It is evident that a layer of flat, transparent ice at the pond surface practically does not change pond reflection, so we consider the ponds with ice crust in the same manner as open ones. However, if the upper ice layer is bubbly or snow covered, the pond reflectance can change drastically: the pond gets brighter and may become indistinguishable from the surrounding ice in the visible range. These "bright" or snow-covered ponds would require other means for their characterization. We exclude such cases from consideration.

Figures 7-10 present photos of different ponds and their reflectance spectra, measured and simulated with the retrieved parameters (denoted as 'retrieved' in the legend).

Figure 7 shows the photos, modeled and measured spectra of light blue melt ponds which have a uniform bottom on thick first-year ice under clear and cloudy skies, measured in the Central Arctic on 10.08.2012, 10.08.2012 and 22.08.2012, respectively. The albedo values are extraordinary high. This could be related to the fact that the ponds are frozen over with a 2-3 cm layer of ice, which is likely not perfectly transparent. Figure 8 shows three cases of frozen over blue ponds with heterogeneous bottom under overcast skies measured on 11.08.12, 22.08.12 and 22.08.12, respectively. One can see darker parts in the ponds, which result from sea ice melting from the lower boundary or lower bubble content in regions of the pond bottom. Figure 9 presents dark open melt ponds on thinner first year ice under overcast skies, all measured on 26.08.2012. The albedo of these ponds is much lower than that of the previous ones: from about 0.07 to 0.14 in the visible and about 0.05 in the IR. Figure 10 presents two cases of light blue ponds, both measured on 26.08.12 and a dark pond contaminated with algae aggregates measured on 21.08.2012, all under overcast skies. Surprisingly, the spectrum of the pond with algae is reproduced quite well. This is because the contribution of the yellow algae spots to a total reflection is proportional to their

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area, which is not very large. However, their effect can be clearly seen in the spectrum: the measured values are less than the modeled ones in the blue range (0.3-0.5 μm) and greater in the yellow-green (0.5-0.6 μm).

The above ponds are quite different from one another. They range from dark to very light blue in color, open and frozen over, clear and contaminated with organic matter. In spite of this, the model is able to reproduce the measured spectra in the visible region with high accuracy in all studied cases. The root-mean-square difference (RMSD) between the measured and simulated spectra has the average value of 0.01 for the whole considered spectrum from 0.35 to 1.3 μm and 0.007 for the visible range up to 0.73 μm .

The retrieved and measured geometrical parameters of the ponds, as well as the RMSD between the measured and simulated spectra, are presented in Table 2 and shown in Fig. 14.

## 4.2    Barrow-2008

Melt pond spectra were observed near Utgiagvik, Alaska USA (formerly Barrow) in 2008 as part of the SIZONET program, observing pond formation (Polashenski et al., 2012). Observations were collected at sites approximately 1 km offshore from Niksiuraq in the Chukchi sea, near 71.366N, 156.542W on level, landfast first year ice. For this work, a total of 27 measured melt pond spectra were used (no photographs were taken). All melt ponds were quite dark and polluted with sediments and their spectra look quite similar. Three of them are presented in Fig. 11. The albedo does not exceed the value of 0.3 in its maximum and show a discrepancy in the blue range, presumably due to the presence of mineral sediments. Because of this, the RMSD between the measured and simulated spectra for the visible range (0.01) is greater than that for the whole spectrum (0.009). The ice thickness was not measured. The pond depths, measure and retrieved, as well as the RMSD, are shown in Table 2 and Fig. 14.

## 4.3    SHEBA-1998

SHEBA was a year-long drift experiment conducted in the Beaufort Sea from October 1997 to October 1998 (Perovich et al., 1999; Uttal et al., 2002). Extensive measurements of the characteristics of sea ice were made. This included observations of the spatial variability and temporal evolution of the spectral albedo of the ice cover (Perovich et al., 2002).

One pond in this expedition was especially interesting, because its bottom had a region that was much brighter than the surrounding bottom. This region had sharp borders with rectangular corners (see the photo in Fig. 12). This likely was a broken piece of bubbly multiyear ice that was incorporated into the ice cover. This piece of ice had more air bubbles than the darker adjacent ice. This dual pond was observed during the entire period of its formation and development. The most intensive pond formation process was observed from July 17 through August 14. The spectra were taken every four days during this period. The spectra processing results are shown in Figs. 12 and 13.

Figure 12 shows the spectra and the photos of the SHEBA dual pond. For the first five dates (July 17, 21, 25, 29, August 2) the retrieval is excellent (for the visible range RMSD = 0.0038 for July 17 and has a maximal value of 0.0061 for July 29, see Table 2) and for the last three (August 6, 10, 14) the retrieval is a little bit worse, but still quite good (for the visible

range RMSD = 0.0085 for August 6 and 10). The reason for this difference is not obvious and we may assume that some contaminant got into the pond those days. So, the regression analysis relies on the first five measurement dates.

Figure 13 presents the retrieved pond depth and ice thickness (for both parts independently) for these dates. The retrieved pond depth at the light part of the pond is 7 cm greater than the average reported pond depth (37 cm) ) and 13 cm greater at the dark part. Albedo of the light part (in the visible part of spectrum) is approximately twice greater than that of the dark part. In general, this agrees with the different nature of the pond's physical properties. The retrieved ice thickness in the light part is lower by 34 cm in average than that of the dark part. The slope of the linear regression for the retrieved ice thickness gives the melt rate of 1.9 cm/day and 2.6 cm/day for the light and dark parts, respectively. Taking the average surface and bottom melt for SHEBA ponded ice from 17 July to 14 August gives an estimated surface ice melt of 35 cm and bottom melt of 28 cm for a total of 63 cm, which gives a melt rate of 2.25 cm/day (Perovich et al., 2003).

Suppose that the difference between the transport scattering coefficient $\sigma_t$ for the light and dark portion is due to air bubbles only, then the scattering coefficient by air bubbles can be estimated as:

$$\sigma_a = \frac{\sigma_t^{light} - \sigma_t^{dark}}{1 - g_a} . \tag{51}$$

The retrieved values, averaged for the first five dates, are the following: the transport scattering coefficient for the light part $\sigma_t^{light}$ is 5.6 m$^{-1}$, for the dark part $\sigma_t^{dark} = 1.0$ m$^{-1}$. The slope of the regression line for these five dates is much less than the values scatter. Using the value of 0.86 for $g_a$, we found that the average retrieved scattering coefficient by air bubbles $\sigma_a$ is 33 m$^{-1}$. In the bubble saturated ice observed by Gavrilo and Gaitskhoki (1970) the air volume concentration was up to 5% and the effective bubble radius was $R_a = 1.3$ mm. If we suppose the same effective radius, the average air volume concentration in the light ice will be $C_a^V = 2/3 R_a \sigma_a = 2.8\%$, which is quite reasonable for bubbly ice.

## 4.4    Verification results

The retrieved and measured pond parameters (melt water depth and underlying ice thickness), as well as root mean square difference (RMSD) between the measured and simulated albedo spectra, are given in Table 2. The RMSD is shown both for the whole spectrum and for the visible range ($\lambda < 0.73 \mu m$). A scatter plot of the retrieved pond parameters is shown in Fig. 14. The retrieval of the underlying ice thickness is made with reasonable accuracy; the maximal error is 55%, the relative RMSD is 37% and $R^2 = 0.56$. The retrieval of the pond depth is more uncertain: its value can differ up to 2 times from the measured one and RMSD = 65%. This is to be expected, because the pond water depth has much less effect on the pond albedo than the underlying ice thickness. Nevertheless, the correlation for the entire dataset of the measured and retrieved pond depth values is quite high ($R^2 = 0.62$) and 70% of the retrieved values are inside the 50%-error range. The observed scatter in the retrieval results might partly be explained by the specifics of the field measurements of the water depth and ice

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thickness in the melt pond: ice drillings or water depth measurements are performed at one single point of the melt pond and do not necessarily represent the average ice thickness or water depth values, which can be highly variable.

Summarizing the verification, we can say that the spectra retrieval in the visible range is good for all cases considered. Some difference is observed in the blue, when colored organic matter or mineral sediments are present in the ice or melt water, and

5    in the IR, where the reflectance is too low and the signal is noisy.


## 5    Conclusion

This work presents an optical model of melt pond covered sea ice. We assume a pond to be a plane-parallel layer of melt water on an under-pond ice layer. We paid particular attention to the pond bottom albedo as the main factor that determines the pond reflectance. The albedo of the under-pond ice is calculated within the modified two-stream approximation (Zege et

10    al, 1991), which relates the layer albedo to its thickness and to the transport scattering coefficient of a medium. The analysis of the spectral behavior of the inherent optical properties of sea ice, using the WKB approximation approach to light scattering by non-spherical particles (brine inclusions) and Mie solution for spherical particles (air bubbles), has shown that the average cosine of the scattering phase function, and therefore the transport scattering coefficient of sea ice, is spectrally neutral. Hence, the pond can be characterized by only three independent parameters that determine its reflectance through the

15    visible and near IR spectral range: the pond depth, the under-pond ice thickness, and the ice transport scattering coefficient.

The model developed proposes a simple analytical formula to calculate the main reflective characteristics of a melt pond: the bidirectional reflectance factor and the black and white-sky albedo. The model is simple in its implementation, because it is entirely based on analytical formulas. The derivation of the analytical formulas becomes possible due to the assumption of the Lambert reflection by the pond bottom. Although this commonly used assumption has no reliable experimental basis, the

20    model verification with a wide set of field measurements (SHEBA-1998, Barrow-2008, and Polarstern-2012) confirms that this assumption is reasonable, at least, concerning the spectral albedo. Its validity for the pond BRF requires further investigations. Nevertheless, the coincidence of measured and modeled albedo spectra allows us to state that more pond parameters will not help improving the model and make it closer to reality. We would attribute potentially appearing differences between observed and modeled spectra  to possible sediment.

25    Additional attention is paid to correctly accounting for the illumination conditions during the field measurements. It is shown that multiple reflections of light between the atmosphere and surrounding background can be neglected, so the *a priori* knowledge of the background (surrounding ice) albedo is not necessary. However, the sky conditions (overcast or clear, presence of cirrus or aerosol load) should be specified to interpret the pond albedo as the white, black, or blue-sky ones. In the last case it is highly desirable to know the spectrally resolved atmospheric optical thickness during the measurements.

30    Unfortunately, such information is rarely available for field measurements of the sea ice reflective properties.

The model presented was successfully used in an algorithm for sea ice albedo and melt pond fraction retrieval from MERIS satellite data (Zege et al., 2015; Istomina et al., 2015a; Istomina et al., 2015b). The model provides accurate description of

the melt pond reflective properties: not only pond albedo, but also pond bi-directional reflectance, which is of great importance for processing remote sensing data, which is commonly measured under a specific, narrow incidence angle. Moreover, the approach presented can be easily extended to describe the light transmittance through sea ice, which is also important for the radiative budget of the Arctic Ocean. The model presented is able to reproduce a variety of melt pond types observed in the field. It can be applied to the problems of physics of sea ice and for monitoring the melt of specifically the Arctic melt-pond covered but also of the Arctic and Antarctic sea ice cover. Also, it makes it possible to improve the parameterization of the underlying surface in various atmospheric remote sensing retrievals over the Arctic summer sea ice (clouds, aerosols, trace gases) and potentially re-evaluate the climatic feedbacks and radiative budget of the Arctic region at a new accuracy level.

## 6    Data availability

The field data from the R/V *Polarstern* cruise ARK XXVII/3 are available at the PANGAEA data repository (Istomina et al., 2016, 2017).
The field data from the Barrow-2008 expedition are available at the Arctic Data Center:
spectral albedos – https://arcticdata.io/catalog/#view/doi:10.5065/D6NZ85TB,
line photos – https://arcticdata.io/catalog/#view/doi:10.5065/D6J1019P .
The field data from the SHEBA-1998 expedition are available in a supplement to this manuscript.

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**Table 1. Melt pond characteristics**

| Layer | Predefined characteristics | Variable characteristics |
|---|---|---|
| Air-water boundary (AW) | Spectral refractive index $n$ ; Fresnel reflectance $R^F$ and transmittance $T^F$ | No |
| Water | Water absorption coefficient $\alpha_w$ (spectral); Rayleigh scattering coefficient $\sigma_w$ (in the law of extinction only) | Pond depth $z$ |
| Under-pond ice layer (pond bottom) | Ice absorption coefficient $\alpha_i$ (spectral); scattering within the two-stream and transport approximations | Transport scattering coefficient $\sigma_t$<br><br>Thickness $H$ |

**Table 2. Measure and retrieved pond geometric parameters derived from the spectral range 0.35 to 1.3 µm (total). RMSD values between measured and retrieved pond water depth are given for the complete spectral range and the visible part ($\lambda < 0.73 \mu m$).**

| Fig | Pond codename /station number (for *Polarstern* expedition) | ice thickness (cm), retrieved | ice thickness (cm), measured | water depth (cm), retrieved | water depth (cm), measured | RMSD ×10³ (total) | RMSD ×10³ (visible) |
|---|---|---|---|---|---|---|---|
| 7 | 1008_P2 / 1 | 276 | 230 | 12 | 21 | 13. | 10. |
|  | 1008_P3 / 1 | 130 | 225 | 12 | 14 | 22. | 15. |
|  | 210812purbp1e00000 / 3 | 163 | 182 | 6 | 11 | 15. | 14. |
| 8 | 110812ROVtransect23e24p00000/ 1 | 182 | - | 29 | - | 16. | 10. |
|  | 210812purbp3e00000 (2208_P3) / 3 | 212 | 143 | 24 | 30 | 12. | 7.2 |
|  | 210812purwhitep4e00000 (2208_P4) / 3 | 89 | 132 | 0 | 20 | 15. | 13. |
| 9 | 260812Larm2pond1e00000 / 4 | 28 | - | 89 | 30 | 8.6 | 0.52 |
|  | 260812Larm2pond2e00000 / 4 | 33 | - | 59 | 30 | 8.1 | 0.71 |
|  | 260812purdpw3e00000 (2608_P3) / 4 | 63 | 49 | 38 | 30 | 6.6 | 0.40 |
| 10 | 260812purbp1e00000 (2608_P1) / 4 | 164 | 256 | 61 | 36 | 9.7 | 6.0 |
|  | 260812purbp2de00000 / 4 | 170 | - | 63 | 50 | 11. | 4.0 |
|  | 210812puralg5e00000 (2208_P5) /4 | 15 | 33 | 22 | 20 | 6.6 | 4.6 |
| 11 | Barrow, Blue MP #7 | 53 | - | 22 | 15 | 9.3 | 12. |
|  | Barrow, BubblyBlue MP #4 | 55 | - | 11 | 6 | 10. | 12. |
|  | Barrow, BlueWithBrownSpots #3 | 52 | - | 17 | 20.5 | 8.3 | 11. |
| 12 | SHEBA light Jul 17 | 72 | - | 38 | 30 | 3.2 | 3.8 |
|  | SHEBA light Jul 21 | 70 | - | 38 | 33 | 3.7 | 4.2 |
|  | SHEBA light Jul 25 | 41 | - | 45 | 38 | 4.9 | 5.8 |
|  | SHEBA light Jul 29 | 44 | - | 51 | 40 | 6.5 | 6.1 |
|  | SHEBA light Aug 2 | 48 | - | 49 | 43 | 4.7 | 5.6 |
|  | SHEBA light Aug 6 | 6 | - | 72 | 44 | 7.4 | 8.5 |
|  | SHEBA light Aug 10 | 9 | - | 68 | - | 7.6 | 8.5 |
|  | SHEBA light Aug 14 | 83 | - | 30 | - | 6.4 | 6.9 |
|  | SHEBA dark Jul 17 | 107 | - | 41 | 30 | 2.0 | 2.2 |
|  | SHEBA dark Jul 21 | 108 | - | 44 | 33 | 2.0 | 2.3 |
|  | SHEBA dark Jul 25 | 84 | - | 47 | 38 | 2.1 | 2.4 |
|  | SHEBA dark Jul 29 | 68 | - | 67 | 40 | 5.3 | 3.3 |

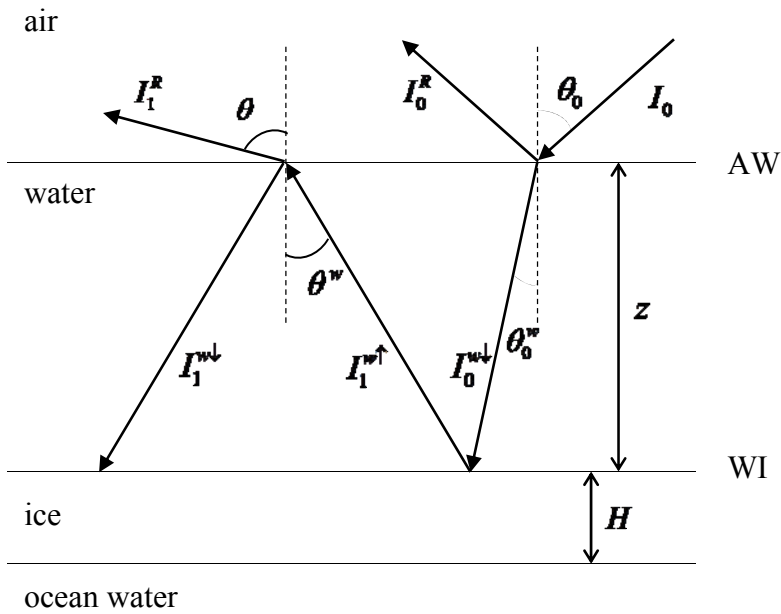| | | | | | | |
|---|---|---|---|---|---|---|
| SHEBA dark Aug 2 | 75 | - | 52 | 43 | 2.1 | 2.3 |
| SHEBA dark Aug 6 | 11 | - | 101 | 44 | 4.1 | 2.5 |
| SHEBA dark Aug 10 | 14 | - | 100 | - | 3.7 | 1.3 |
| SHEBA dark Aug 14 | 87 | - | 35 | - | 1.8 | 2.1 |

**Figures**



**Figure 1.** Schematic image of light rays in a melt pond. $I_0$ is the intensity of the incident light, $\theta_0$ is the angle of incidence; $I_0^R$ is the intensity of light, reflected from the air-water interface (AW); $I_0^{w\downarrow}$ is the intensity of light, refracted by the AW interface, $\theta_0^w$ is the angle of refraction; $I_1^{w\uparrow}$ is the intensity of the up-welling diffuse light, $\theta^w$ is the angle of internal reflection; $I_1^{w\downarrow}$ is the intensity of light after internal reflection by the AW interface, $\theta^w$ is the angle of internal reflection; $I_1^R$ is the intensity of light that comes out of the melt pond after refraction by the AW interface, $\theta$ is the observation angle equal to the angle of refraction.

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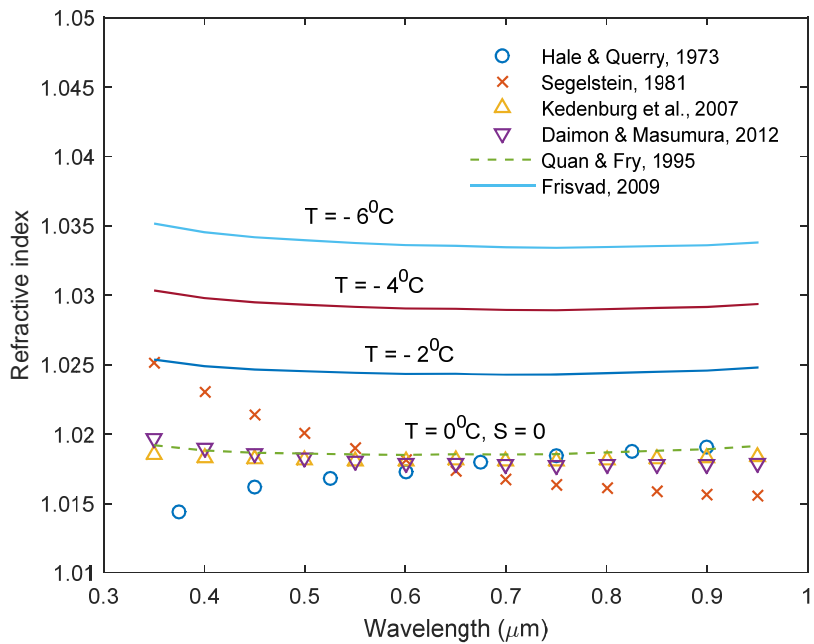
**Figure 2**. Spectra of the relative refractive index 'water-to-ice': distilled water (symbols), fresh water at $0^0$C (dashes), and brine with equilibrium salinity at different temperatures (solids).
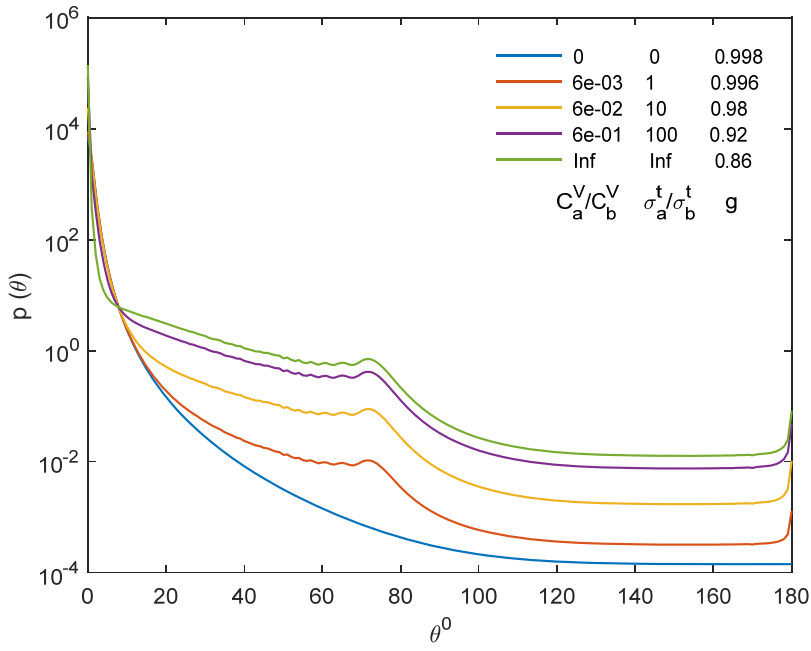
**Figure 3.** Phase functions of the mixture of air bubbles and brine inclusions at $-2^0$C with different fraction ratio $C_a^V/C_b^V$. The ratio of transport scattering coefficients $\sigma_a^t/\sigma_b^t$ and the average cosine $g$ are also shown. The effective sizes are $R_a$=42.55 μm, $R_b$=100 μm.

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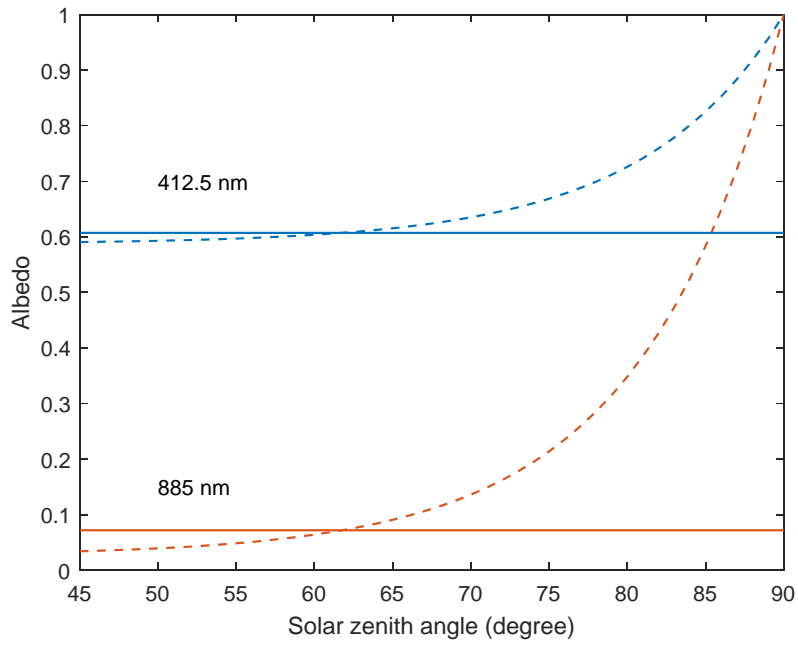
**Figure 4.** Black-sky albedo of a light melt pond ( $z = 17\text{cm}$ , $\sigma_t = 3.2\text{m}^{-1}$ , $H = 1.25\text{m}$ ) vs. the angle of incidence (dashed). The white-sky albedo values are shown in solid.
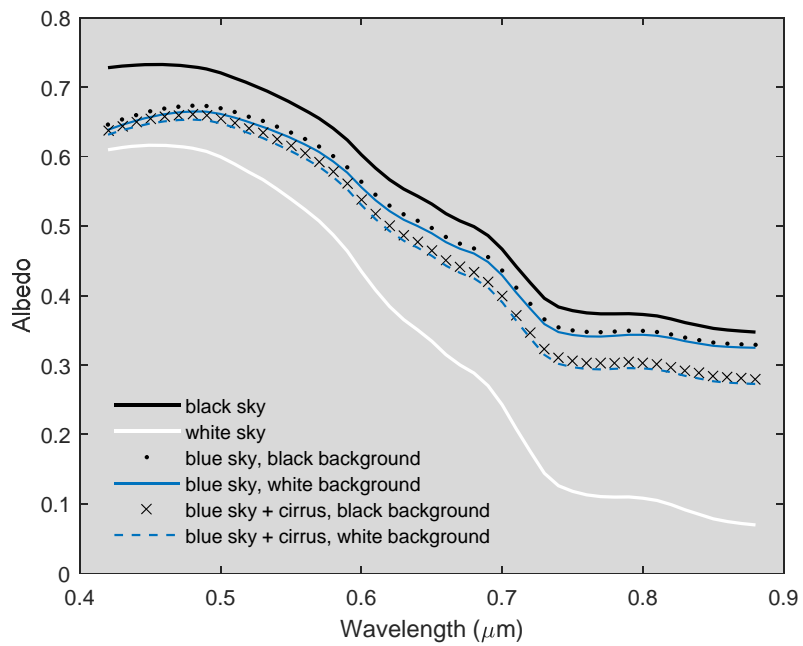
**Figure 5.** Modeled spectra of melt pond albedos at various sky conditions and background albedo at sun elevation $10°$.
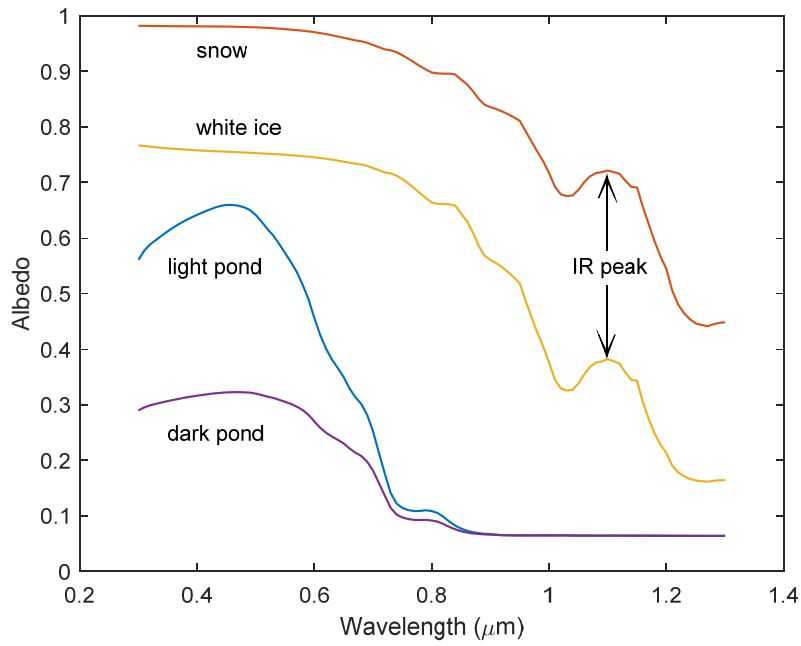
**Figure 6.** Typical spectral albedo of melt ponds, snow, and white ice, calculated for the following parameters: light pond – depth $z$ is 20 cm, $\sigma_t = 4\text{m}^{-1}$, $H = 1.25\text{m}$ (transport optical depth is 5); dark pond – depth $z$ is 20 cm, $\sigma_t = 2\text{m}^{-1}$, $H = 0.5\text{m}$ (transport optical depth is 1); white ice – the effective grain size is 2mm, optical depth is 12; snow – the effective grain size is 0.2mm, optical depth is 200 (see Malinka et al., 2016 for details).

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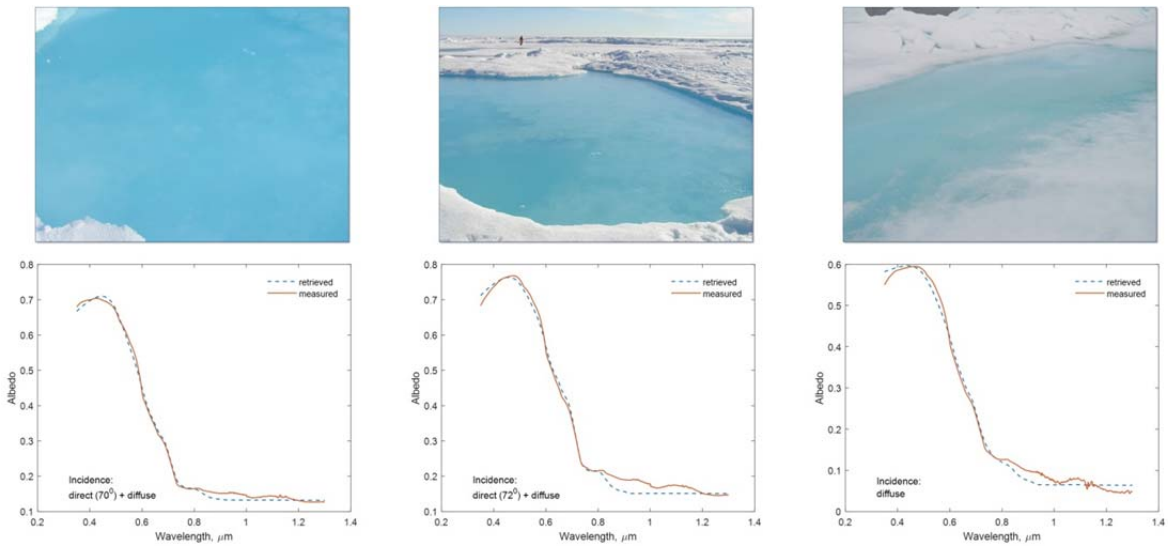
**Figure 7.** Light frozen (2-3 cm layer of ice) blue ponds.
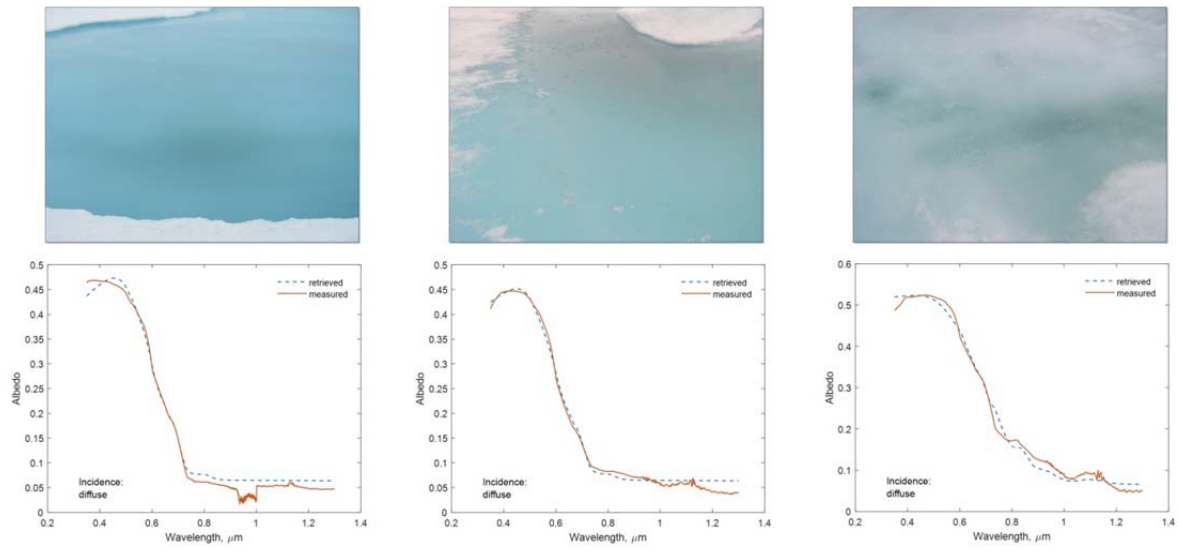
**Figure 8.** Frozen blue ponds.
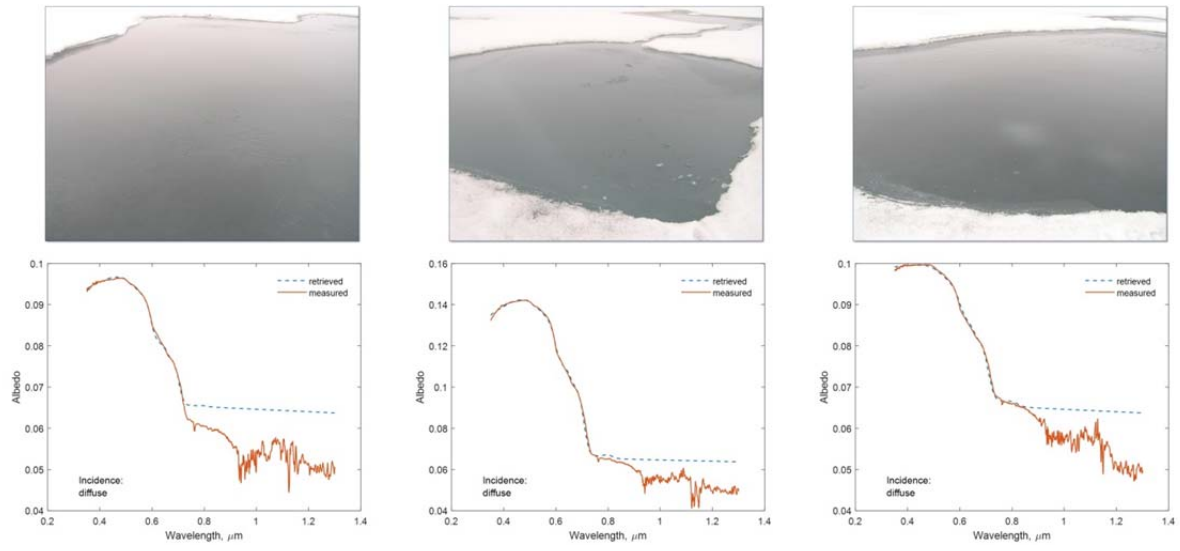
**Figure 9.** Dark open ponds.
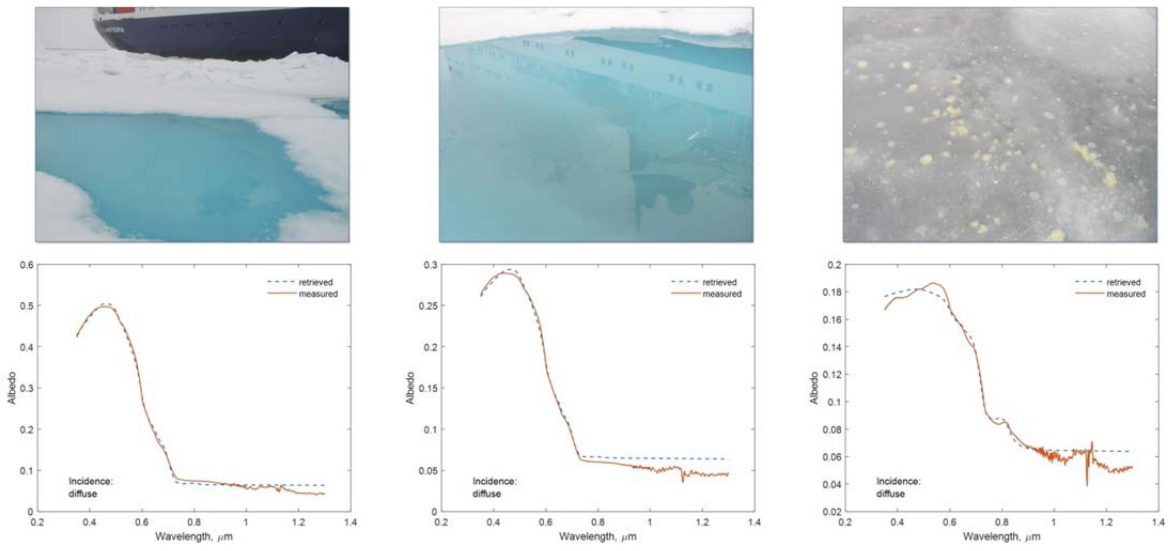
**Figure 10.** From left to right: the light blue pond, a darker part of the blue pond, and the dark pond with yellow algae.
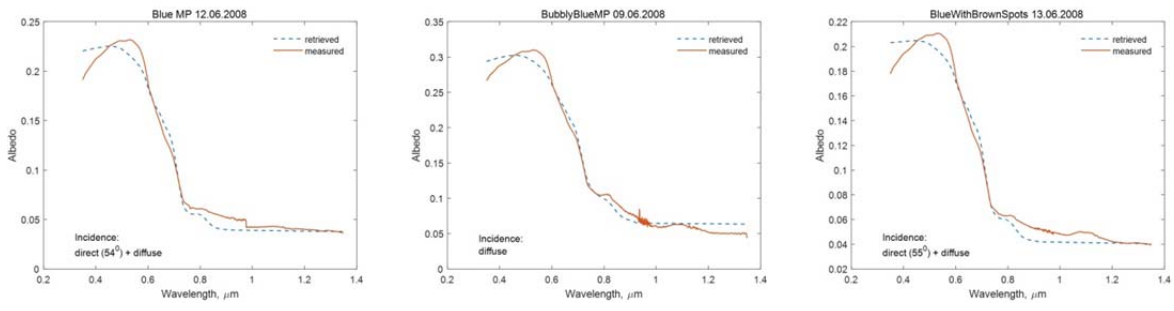
**Figure 11.** Spectra of some melt ponds from *Barrow-2008*: (left to right) a blue melt pond, a bubbly blue melt pond, and a blue melt pond with brown spots.
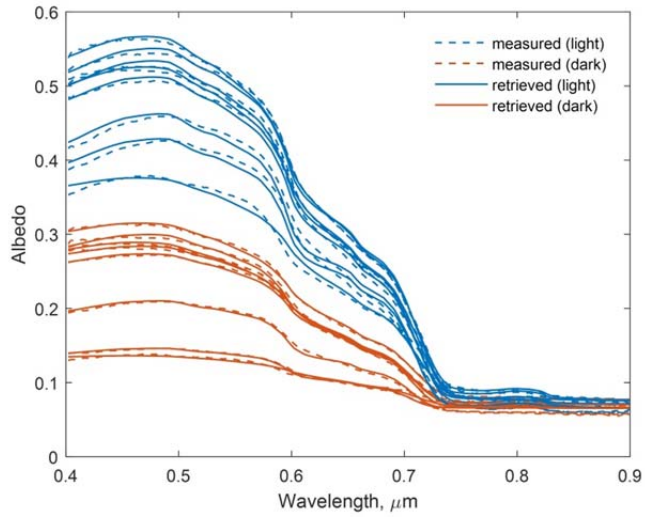
**Figure** 12. SHEBA dual pond: photos and spectra, measured (dashed) at the light (blue) and dark (red) parts and simulated (solid). The photographs are taken at the early and late melt season (on July 3 and August 8, respectively).
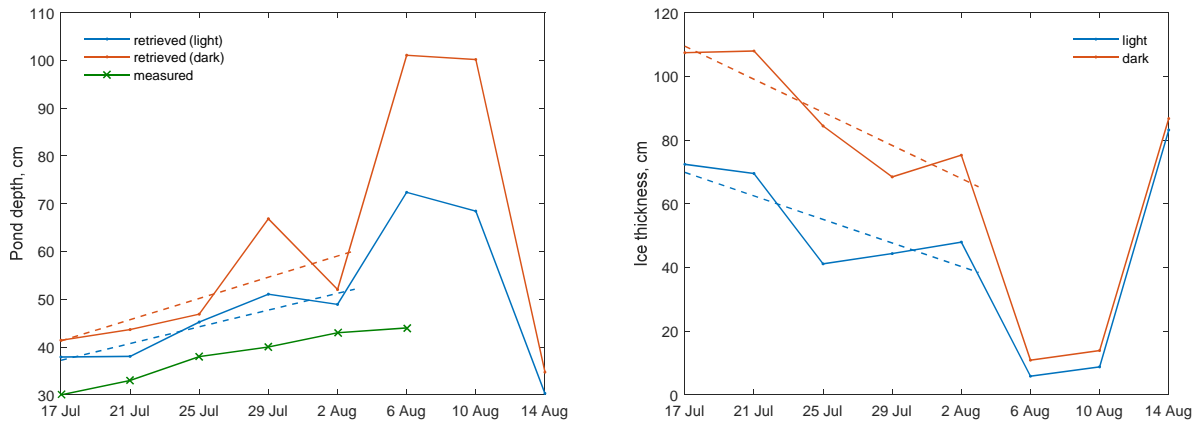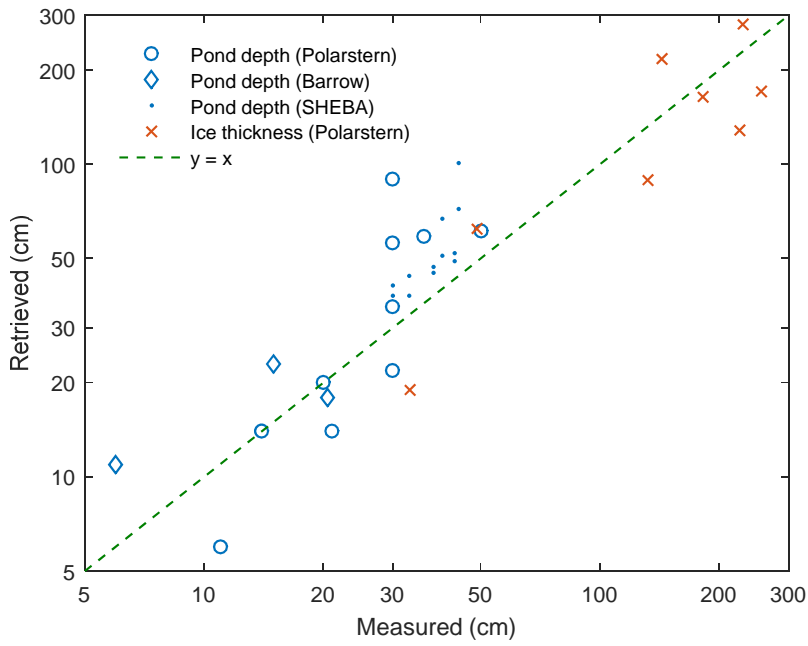
**Figure 13.** Retrieved pond depth (left) and ice thickness (right) for the two parts of the dual pond shown in Fig. 12. The measured pond depth is shown with crosses. The dashed lines show the linear regression for the first 5 dates.

**Figure 14.** Ice thickness and pond depth, measured at different stations and retrieved. For ice thickness $R^2 = 0.56$ (N=8) and for pond depth $R^2 = 0.62$ (N=26).