



# 1    **The significance of vertical moisture diffusion on** 2    **drifting Snow sublimation near snow surface**

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7    **Abstract.** Drifting snow sublimation is a physical process containing phase change and heat change of  
8    the drifting snow, which is not only an important parameter for the studying of polar ice sheets and  
9    glaciers, but a significant one for the ecology of arid and semi-arid lands, where snow cover is the main  
10    fresh water resource. However, in the previous studies drifting snow sublimation near surface was  
11    ignored. Herein, we built a drifting snow sublimation model containing vertical moisture diffusion  
12    equation and heat balance equation, to study drifting snow sublimation near surface. The results  
13    showed that though drifting snow sublimation near surface was strongly reduced by negative feedback  
14    effect, relative humidity near surface didn't reach the saturation state caused by vertical moisture  
15    diffusion. Therefore, the sublimation near surface will not stop in drifting snow near surface. The  
16    sublimation rate near surface is 3-4 orders of magnitude higher than that at 10 m. And the mass of snow  
17    sublimation near surface accounts for even more than half of the total if the wind velocity is small.  
18    Therefore, drifting snow sublimation near surface can't be neglected.

## 19    **1 Introduction**

20        The polar ice sheets, mountain glaciers, snowy area in high latitude of Northern Hemisphere  
21    (such as North of Canada, Greenland, etc), whose main source is snow, have profound influence on  
22    the global hydrologic cycle, climate change and ecological system. Extensive researches showed that  
23    drifting snow sublimation was an important method to change the snow distribution, especially in the  
24    polar ice sheets, highland mountains and high latitude of Northern Hemisphere. For example,  
25    Pomeroy and Jone (1995) found that the mass of drifting snow sublimation was equal to 18.3% of  
26    annual precipitation in coastal Antarctica; while Liston and Sturm (2004) found that it was equal to 22%  
27    of winter precipitation in Arctic Alaska. Pomeroy and Essery (1999) found that blowing snow  
28    sublimation fluxes during blowing snow return  $10\pm 50\%$  of seasonal snowfall to the atmosphere in  
29    North American prairie and arctic environments. MacDonald et al. (2010) found that the mass of  
30    drifting snow sublimation was equal to 17%-19% of annual precipitation in Rocky Mountains,  
31    Canada. Zhou et al. (2014) pointed out that the mass of drifting snow sublimation was equal to 24%



32 of annual precipitation in western Chinese mountains. These results indicate that drifting snow  
33 sublimation is very important to the study of global and polar hydrological systems.

34 Some scientists directly measured drifting snow sublimation using eddy covariance, but this  
35 method can only obtain a few points of information, and it is difficult to predict the whole sublimation  
36 in snowy areas (Pomeroy and Essery, 1999; Cullen et al., 2007; Marks et al., 2008; Reba et al., 2012).  
37 Therefore, there is a high demand of studying the sublimation of snow using numerical model.

38 The sublimation of snow particles in the drifting snow is normally accompanied with heat  
39 absorption and water vapor production, which will cause a decrease in the ambient air temperature  
40 and an increase in humidity. The increased humidity will in turn inhibit the sublimation of snow  
41 particles; while the lower temperature will lead to a decrease in the air saturated vapor pressure,  
42 which will also inhibit the snow sublimation. Many researchers believed that the sublimation of snow  
43 particles near surface would occur violently at the early stage of drifting snow process, since the high  
44 concentration of snow particles near surface would result in a rapid air temperature decrease and  
45 humidity increase. Then the humidity would reach saturation quickly near surface, and the  
46 sublimation would stop at the saturated layer of humidity. Therefore, the snow sublimation near  
47 surface was negligible in the fully developed drifting snow (Déry et al., 1998; Bintanja, 2001a; Mann  
48 et al., 2000). However, some researchers found that humidity near surface didn't reach saturation in  
49 the drifting snow in the field or wind tunnel experiments, which they thought was caused by water  
50 transport (convection and diffusion) (Schmidt, 1982; Groot Zwaadtink et al., 2011). Déry and Yau  
51 (1999) fix the relative humidity at 95% instead of 100% at the surface when they simulated the  
52 blowing snow sublimation. They found that the time-integrated values of sublimation increased 14%  
53 than the results which fix the relative humidity at 100%, so humidity near surface is very important  
54 for the simulations of blowing sublimation. Huang et al. (2016) calculated the snow sublimation in  
55 the saltation layer, taking into consideration of the effect of horizontal moisture convection on the  
56 non-homogeneous snow cover. Their results showed that drifting snow sublimation in the saltation  
57 layer could not be neglected in the presence of horizontal moisture convection. But they did not  
58 discuss the sublimation near surface of areas such as polar ice sheets, grassland covered by snow, etc.,  
59 where the snow cover was very large and the water convection was very weak. Therefore, studies on  
60 the snow-sublimation in these regions are of great significance for the understanding of global  
61 hydrological systems and ecosystems.



62           However, in the previous blowing snow sublimation model, the diffusion equation was often  
63 used to describe the movement of snow particles, which can describe the movement of small particles  
64 well. But the diffusion equation is difficult to describe the movement of large snow particles which  
65 are mainly distributed in the near surface area (Déry et al., 1998; Xiao et al., 2000; Vionnet et al.  
66 2014). Huang et al. (2016) used the Lagrangian particle tracing method to describe the movement of  
67 near-surface snow particles, and for the first time calculated the sublimation of saltation particles in  
68 near surface region on non-uniform snow cover. But this model can not describe snow particles  
69 suspending in upper air. Furthermore, all above exiting models did not take into consideration of the  
70 effects of vertical moisture diffusion on the sublimation.

71           Therefore, a drifting snow model has firstly been built to describe the movement of snow  
72 particles of both saltating near surface and suspending in the higher region. Then, a drifting snow  
73 sublimation model has been built the combination of the drifting snow model, a vertical moisture  
74 diffusion equation and a heat balance equation. Then drifting snow sublimation with three wind  
75 speeds was calculated. The temporal evolution and vertical profiles of temperature, relative humidity,  
76 mass concentration of snow particles, snow sublimation rate were analyzed in details. Meanwhile, the  
77 proportions of the sublimation mass of saltation snow grains and saltation layer to the total  
78 sublimation mass were also given.

## 79    **2 Method**

### 80    **2.1 Basic Equations of the Flows**

81           The horizontal wind field satisfies the Navier–Stokes equation at the atmospheric boundary layer.  
82 Considering a fully developed steady flow field on an infinite polar ice sheet where the changes of  
83 wind field in the lateral and flow direction are negligible, the fully developed horizontal direction  
84 flow field equation can be obtained according to the theory of mixing length by Prandtl.

$$85 \quad \frac{\partial}{\partial z} (\rho_a \kappa^2 z^2 \left| \frac{du}{dz} \right| \frac{du}{dz}) + F = 0 \quad (1)$$

86           where  $\kappa$  is the von Karman constant,  $\rho_a$  is air density,  $u$  is the horizontal wind speed and  $F$  is the  
87 reaction force of the snow particle on the flow field.



88 **2.2 Snow particle motion equation**

89 The snow particles jumping from the bed are divided into saltation and suspended particles when  
 90 calculating snow particle movement. These two types of particles are distinguished based on the  
 91 particle size and flow field conditions. Then the saltation particles are calculated by Lagrange particle  
 92 tracing method, and the suspension particles are calculated by diffusion equation.

93 **2.2.1 Judging criteria of saltation and suspended particles**

94 The judging criterion of saltation and suspended particles is as follows (Scott, 1995):

$$95 \quad \begin{cases} w_s/(ku_* ) > 1, & \text{saltation particle} \\ w_s/(ku_* ) \leq 1, & \text{suspension particle} \end{cases} \quad (2)$$

96 where  $u_*$  is the friction velocity and  $w_s$  is the final sedimentation velocity of the particles (Carrier,  
 97 1953):

$$98 \quad \begin{aligned} w_s &= -\frac{A}{D} + \sqrt{\left(\frac{A}{D}\right)^2 + BD} \\ A &= 6.203\nu_a \\ B &= \frac{5.516\rho_p}{8\rho_a}g \end{aligned} \quad (3)$$

99 where  $D$  is diameter of snow particle,  $\nu_a$  is air viscosity coefficient,  $\rho_p$  is the densities of snow  
 100 particle,  $g$  is the acceleration of gravity.

101 **2.2.2 Basic equations of saltation particles**

102 Saltation particle motion equation is as follows (Huang et al., 2011):

$$103 \quad m \frac{dU_p}{dt} = F_D \left( \frac{U_a - U_p}{V_r} \right) \quad (4)$$

$$104 \quad m \frac{dV_p}{dt} = -G + F_B + F_D \left( \frac{V_a - V_p}{V_r} \right) \quad (5)$$

$$105 \quad \frac{dx_p}{dt} = U_p \quad (6)$$



106 
$$\frac{dy_p}{dt} = V_p \quad (7)$$

107 where  $m$  is the mass of snow particle,  $G$  is the gravity of snow particle,  $U_a$  and  $V_a$  are the  
 108 horizontal and vertical velocity of air,  $U_p$  and  $V_p$  are the horizontal and vertical velocities of snow  
 109 particle,  $V_r = \sqrt{(U_p - U_a)^2 + (V_p - V_a)^2}$  is the relative velocity of movement of the snow particles  
 110 and the flow field,  $F_b$  and  $F_D$  are the buoyancy and traction forces of snow particles,  $x_p$  and  $y_p$   
 111 are the horizontal and vertical positions of snow particles.

112 The splash function fitted by Sugiura and Maeno (2000) according to the observations of the low  
 113 temperature wind tunnel experiment was chosen,

114 
$$S_v(e_v) = \frac{1}{b'G(a)} e_v^{a-1} \exp\left(-\frac{e_v}{b}\right) \quad (8)$$

115 
$$S_h(e_h) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left[-\frac{(e_h - \mu)^2}{2\sigma^2}\right] \quad (9)$$

116 
$$S_e(n_e) = {}_m C_{n_e} p^{n_e} (1-p)^{m-n_e} \quad (10)$$

117 where  $S_v(e_v)$ ,  $S_h(e_h)$  and  $S_e(n_e)$  are the probability distribution functions of the vertical  
 118 restitution coefficient  $e_v$ , horizontal restitution coefficient  $e_h$ , and the number of grains ejected  $n_e$ .

### 119 2.2.3 Basic Equations of Suspended particles

120 The movement of suspension particles is described by the following vertical diffusion equation  
 121 according to horizontal uniformity condition,

122 
$$\frac{\partial q}{\partial t} = \frac{\partial}{\partial y} \left( K_s \frac{\partial q}{\partial y} + w_s q \right) + S \quad (11)$$

123 where  $q$  is the snow particle mass concentration,  $K_s$  is the vertical diffusion coefficient,  $S$  is the  
 124 volume sublimation rate of snow grain.  $K_s = \delta \kappa u_* z$ ,  $\delta$  is as follows (Csanady, 1963),

125 
$$\delta = \frac{1}{\sqrt{1 + \frac{\beta^2 f^2}{w_a^2}}} \quad (12)$$

126 where  $\beta$  is the proportionality constant,  $w'$  is the turbulent fluid velocity in the vertical, and we set



127  $\beta = 1, \overline{w'^2} = u_*'^2 \dots$

128 **2.2.4 Aerodynamic Entrainment**

129 The aerodynamic entrainment equation of Shao and Li (1999) is chosen,

130 
$$N_a = Vu_* \left( 1 - \frac{u_*'^2}{u_*^2} \right) D^3 \quad (13)$$

131 where  $N_a$  is the number of snow particles taking off causing by aerodynamic entrainment,  $\zeta$  is a  
 132 non-dimensional coefficient, approximately equal to  $1 \times 10^{-3}$ ,  $u_*$  is the friction velocity,  $u_*'$  is  
 133 the threshold friction velocity.

134 **2.3 Sublimation formula**

135 The sublimation formula is as follows (Thorpe and Mason, 1966),

136 
$$\frac{dm}{dt} = \frac{\pi D(RH - 1)}{\frac{L_s}{K\nu T_a} \left( \frac{L_s}{R_v T_a} - 1 \right) + \frac{R_v T_a}{Sh K_i e_s}} \quad (14)$$

137 where  $RH$  is the relative humidity of air,  $T_a$  is air temperature,  $L_s$  is the latent heat of sublimation  
 138 (equal to  $2.84 \times 10^6$  J kg<sup>-1</sup>),  $K_a$  is the thermal conductivity of air,  $R_v$  is the gas constant of water  
 139 vapor (equal to  $461.5$  J kg<sup>-1</sup> K<sup>-1</sup>),  $K_i$  is the molecular diffusion of water vapor of atmosphere,  $e_s$  is  
 140 the saturated vapor pressure relative to the ice surface.  $Nu$  and  $Sh$  are the Nusselt and Sherwood  
 141 numbers (Thorpe and Mason, 1966; Lee, 1975),

142 
$$Nu = Sh = \begin{cases} 1.79 + 0.606 Re^{0.5} & 0.7 < Re \leq 10 \\ 1.88 + 0.580 Re^{0.5} & 10 < Re < 200 \end{cases} \quad (15)$$

143 where  $Re = \frac{DV_c}{\nu_a}$  is Reynolds number.

144 **2.4 Heat and humidity equation**

145 The heat and humidity equations of air are as follows (Déry and Yau, 1999; Bintanja, 2000),

146 
$$\frac{\partial \theta}{\partial t} = \frac{\partial}{\partial z} \left( K_\theta \frac{\partial \theta}{\partial z} \right) - \frac{L_s S}{\rho_f C} \quad (16)$$

147 
$$K_\theta = \kappa u_* z + K_T \quad (17)$$



148 
$$\frac{\partial h_w}{\partial t} = \frac{\partial}{\partial z} \left( K_q \frac{\partial h_w}{\partial z} \right) + \frac{S}{\rho_f} \quad (18)$$

149 
$$K_h = \kappa u_* z + K_v \quad (19)$$

150 where  $K_q$  and  $K_v$  are the molecular diffusion coefficients of heat and water vapor,  $C$  is the specific  
 151 heat of air.

152 **2.5 Initial and boundary conditions**

153 The initial potential temperature  $\theta_0 = 263.15K$ , and the initial absolute temperature is

154 
$$T_0 = \theta_0 \left( \frac{p}{p_0} \right)^{0.286} \quad (20)$$

155 Where  $p$  is atmospheric pressure, its initial value is

156 
$$p = p_0 \exp \left( - \frac{y g}{R_d \theta_0} \right) \quad (21)$$

157 where  $p_0 = 1000hpa$ ,  $R_d = 287JKg^{-1}K^{-1}$  is the gas constant for dry air.

158 The initial relative humidity profile is

159 
$$RH = 1 - R_s \ln(z / z_0) \quad (22)$$

160 where  $z_0$  is the surface roughness, and its value is  $3 \times 10^{-5}m$  at snow bed (Nemoto and Nishimura,  
 161 2001), and  $R_s = 1.9974 \times 10^{-2}$ .

162 The conversion relationship of relative humidity and specific humidity is

163 
$$q = 0.622 \cdot \frac{e_s}{p - e_s} \cdot RH \quad (23)$$

164 where  $e_s = 610.78 \exp \left[ 21.87(T - 273.16) / (T - 7.66) \right]$

165 The calculation area is set to 1 m in length, 10 m in height, and 0.01 m in width. The time step is  
 166  $10^{-5}s$  for saltation particles,  $10^{-2}s$  for suspended particles,  $10^{-3}s$  for wind, and the calculation time is  
 167 1500 s. The motion of saltation particles is only calculated for 10 s in consideration of the practical  
 168 simplicity, since saltation particles will stabilize within a few seconds. The data of saltation particles  
 169 in the air and the jumping particles from bed are then replaced by the data averaged in 10 s. The  
 170 threshold friction velocity is 0.21 m/s (Nemoto and Nishimura, 2001).

171 The snow particle size distribution fits the results of Schmidt (1982) field observations (Fig. 1).



172 3 **Results and Discussion**

173 In order to verify the judging criteria in eq.2, we divided the particles into sets varied by  $10 \mu m$   
174 ( $1-600 \mu m$ ), and used eq.16 to simulate all the jumping particles. Then we accumulated the mass of  
175 snow particles in the air from small to large particles until the mass was equal to 99.9% of the total  
176 mass of snow particles in the air, and the particle diameter  $D_{99\%}$  was recorded.  $D_{99\%}$  and threshold  
177 particle diameter  $D_{th}$  calculated by eq.2 were compared, and the results is shown in Table1.

178 As shown in Table 1, particles which are larger than the threshold particle do not enter into air  
179 according to the vertical diffusion, indicating that these particles can not be described by the diffusion  
180 equation. Thus, the judging criteria in eq.2 are reliable.

181 In order to verify the reliability of the blowing snow model in this paper, we compared our mass  
182 concentration results with that of the field observations (Fig.2). The red dot in Fig. 2 is the field  
183 observation results near Saskatoon, Canada in 26 January 1987 (Pomeroy and Male, 1992). And the  
184 black line in Fig.2 is our numerical simulation results using the same conditions with the above filed  
185 observation results. It is shown that our simulation results are basically consistent with those observed  
186 in the field, which demonstrates the reliability of our simulations.

187 We also compared our sublimation results with that of the field observations to verify their  
188 reliability (Fig.3). The red lines in Fig. 3 are the results gotten from the observed data by Schmidt  
189 (1982) in Wyoming, U.S.A, in 1982. The black line was the simulated results using the same  
190 environmental conditions as those of Schmidt's. It can be seen that the total sublimation rates  
191 calculated by the model of this paper (black line) are approximately the same as Schmidt's results,  
192 and the sublimation rate at 0.01 m was two orders of magnitude larger than that at 0.1 m. These  
193 results demonstrate that our snow sublimation results are reliable too.

194 We further compared our results with corresponding results of other models under the same  
195 conditions. The black line in Fig. 4 is the result of the suspension particles sublimation rate calculated  
196 by our model ( $u_* = 0.89, T = 253.15K$ ). The other four lines are the results calculated by Xiao et al.  
197 (2001) using four existing blowing snow sublimation models, in which the sublimation of saltation  
198 particles near surface was neglected. It is shown from Fig. 4 that all the rates of suspension particle  
199 increase with height first, and then start to decrease, and the peak is at about 0.1 m. The results of this  
200 paper are higher than that of Xiao et al. (2001). The peaks of total sublimation rate using our model





201 and Schmidt (1982) are all at a height about 0.01 m, which is lower than that of the four blowing  
202 snow models in Fig. 4. But the values of peak in this paper and Schmidt (1982) are two orders of  
203 magnitude larger than that of the four blowing snow models. This is because the sublimation of  
204 saltation particles is neglected in the four models, which is the main movement of snow particles near  
205 surface.

206 Fig. 5 is the temporal evolution of the mass of saltation particles and suspended particles versus  
207 various friction velocities. It is shown that the mass of saltation and suspended particles increase with  
208 time, and finally reach steady. The mass of saltation particles is much larger than that of suspension  
209 particles in the steady state. The time for saltation particles to reach steady state is about 2 s, and  
210 about 300 s for suspended particles.

211 Fig. 6 shows the curves of temperature and humidity with height in the near-surface region of  
212 saltation particles and they are compared with their initial conditions. It is shown that drifting snow  
213 sublimation changes air temperature and relative humidity, and the change amplitude increases with  
214 the friction velocity. This is because the larger the friction velocity is, the more snow particles in the  
215 air are, and the more sublimation will occur, which makes a greater impact on temperature and  
216 humidity.

217 We compared the temperature and humidity with height. It is shown in Fig. 7 and 8 that the  
218 change amplitude of temperature and relative humidity increases while the height decreases.  
219 Combined with the results from Fig. 10, the mass concentration of snow particles increases while  
220 height decreases, which can make a stronger sublimation.

221 It is shown in Fig. 8 that the time for humidity to reach steady is about 2 s at 0.01 m, which is  
222 consistent with the stability time of saltation snow particles; and at 10 m is about 300 s, which is  
223 consistent with the stability time of suspension snow particles. This is because the main part of snow  
224 particles near surface is saltation particles, opposite to that in upper air which is mainly suspension  
225 particles (Fig. 10).

226 Fig. 8 shows that the relative humidity near surface with three kinds of friction velocities does  
227 not reach saturation when the blowing snow reaches steady, which indicates that the snow sublimation  
228 does not stop. It also shows that the vertical diffusion of water vapor can reduce the negative feedback  
229 effect effectively.



230 It can be seen from Fig. 9a that the sublimation rate of saltation particles increases with time first,  
231 then starts to decrease, in which the peak is at about 2 s and finally reaches stability at about 300 s.  
232 The negative feedback effect on saltation particles is very obvious and the time to reach a steady state  
233 is about 300 s. Because the mass of saltation particles increases with time during the first 2 s, and the  
234 increasing amplitude of which is larger than that of relative humidity, and the saltation sublimation  
235 rate increases with time. However, the mass of saltation particles basically stay unchanged after 2 s,  
236 while the relative humidity near surface gradually increases. Therefore, the sublimation rate decreases  
237 with time. The relative humidity near surface also reaches steady after 300 s, which results in the  
238 stability of sublimation rate. The saltation particles distribute mainly near surface, where the change  
239 amplitude of relative humidity is strong which results in a strong negative feedback effect on saltation  
240 particles.

241 It is shown in Fig. 9b that sublimation rate of suspended particles increases with time and  
242 finally reaches steady at about 300 s. The negative feedback effect on suspended particles is not  
243 obvious. The mass of suspension particles increases with time during the first 300 s, which the  
244 increase amplitude of is larger than that of relative humidity, so the suspension sublimation rate  
245 increases with time. Then the mass of suspended particles and relative humidity both reach stable,  
246 which leads to the sublimation rate of suspended particles reaching stable. Since the suspended  
247 particles mainly distribute in upper air where the change amplitude of relative humidity is weak, the  
248 negative feedback effect on suspended particles is not strong.

249 Although the effect of negative feedback on saltation particles is stronger than suspended  
250 particles, the sublimation rate of saltation particles is still greater than that of suspended particles,  
251 indicating that the sublimation of saltation particles is very strong even under the effect of negative  
252 feedback.

253 Fig. 10 shows that the mass concentration of snow particles increases with friction velocity and  
254 decreases with height, and the mass concentration of saltation particles is much higher than that of  
255 suspended particles. It can be seen from Fig. 10a that saltation particles mainly distribute below 0.1 m,  
256 which is consistent with the previous experimental results (Takeuchi, 1980).

257 Fig. 11 shows that sublimation rates increases with friction velocity. Sublimation rates of  
258 saltation and suspended particles increase with height first, then start to decrease. The peak of



259 saltation particles is at about 0.01 m, and that of suspended particles is at about 0.1 m. This is because  
260 the mass concentration and relative humidity of snow decrease with height, while temperature  
261 increases. However, mass concentration of saltation particles changes more strongly than that of  
262 suspension particles with height. Therefore, sublimation rate of saltation particles reaches peak at  
263 lower height.

264 Table 2 shows that the sublimation rate at 0.01 m is two orders of magnitude faster than that at  
265 0.1 m, which is same as the experimental results in Fig. 3, and it's 3-4 times faster than that at 10 m,  
266 although the negative feedback effect near surface is stronger than other regions. Because the mass  
267 concentration of snow particles near surface is much higher than that in other regions (Fig. 8), and  
268 water vapor near surface is not saturated, the sublimation rate near surface is much faster than that in  
269 other regions.

270 In the previous studies the snow sublimation near surface was ignored. That is, to define a wind  
271 velocity related height, below which saltation particles move. Then assumed that moisture in the  
272 region was saturated and therefore the snow sublimation would not be counted (Déry et al., 1998;  
273 Xiao et al. 2000; Vionnet et al. 2014). Three heights at several wind velocities proposed by Déry et al.  
274 (1998), Pomeroy and Male (1992), and Xiao et al. (2000) were respectively given in Table 3 (The  
275 height by Vionnet et al. was the same as that of Pomeroy and Male). Fig. 12 shows the actual ratio of  
276 our simulated sublimation mass below the three heights to the total. It is shown that all the  
277 sublimation masses below three heights account for more than half of the total sublimation mass. This  
278 is because the main part of snow particles is saltation particles (Mellor, 1965), which mainly  
279 distribute in near surface region. And although sublimation near surface leads to significant changes  
280 of temperature and humidity, which have a strong inhibition effect on sublimation, moisture near  
281 surface does not reach saturation due to the vertical diffusion of water vapor, which results in  
282 continuous snow sublimation. Therefore, the main part of the mass of sublimation is sublimation of  
283 saltation particles, and the previous methods neglecting blowing snow sublimation near surface is not  
284 appropriate. Fig. 12 also shows that the proportion of the sublimation mass near surface decreases  
285 with friction velocity. Because more snow particles can enter into upper air with increased wind  
286 velocity, which will lead to decreasing proportion of snow particles near surface, the proportion of the  
287 mass of sublimation near surface will decrease as well.



288 Fig.13 shows the vertical profiles of vapor flux. It is shown that vapor flux increases rapidly in  
289 near surface region, where most of saltation particles move, then slows down greatly after reaching a  
290 certain height. For there is no horizontal flux of water vapor, the water vapor flux at any height must  
291 be equal to the total amount of water vapor generated per second below the height. So most of the  
292 water vapor is coming from near surface regions. From Fig. 13 it can also be seen that vapor flux  
293 increases with friction velocity, for humidity (Fig.5) and moisture diffusion coefficient (eq.17)  
294 increase with friction velocity.

#### 295 **4 Conclusions**

296 We have established a blowing snow sublimation model, which includes vertical moisture  
297 diffusion and heat balance, to study the snow sublimation near surface in large snow cover area in this  
298 paper. The simulation results showed that the blowing snow sublimation decreased air temperature  
299 and increased humidity of air. Meanwhile, the snow sublimation was reduced by the negative  
300 feedback effect of temperature and humidity, especially for near surface, which is in agreement of  
301 previous researches. However, moisture near surface was not saturated due to the vertical moisture  
302 diffusion, so snow sublimation near surface continued. The sublimation rate near surface was even  
303 larger than that in the upper air, because mass concentration of snow particles near surface was much  
304 higher than that in other regions. The sublimation rate at 0.01 m is two orders of magnitude greater  
305 than that at 0.1 m, and is 3-4 orders of magnitude greater than that at 10 m. Furthermore, when the  
306 wind speed was low, the mass of sublimation near surface accounted for more than half of total mass  
307 of sublimation, and could not be neglected. Most of the air vapor in blowing snow is from near  
308 surface region. Therefore, blowing snow sublimation near surface should be taken seriously in the  
309 study of snow sublimation and water vapor transport in the future.

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**Table 1: Comparison of  $D_{th}$  and  $D_{99\%}$**

	$u_* = 0.35ms^{-1}$	$u_* = 0.41ms^{-1}$	$u_* = 0.54ms^{-1}$
$D_{th}$	80.55 $\mu m$	87.84 $\mu m$	102.61 $\mu m$
$D_{99\%}$	$\leq 80\mu m$	$\leq 90\mu m$	$\leq 110\mu m$

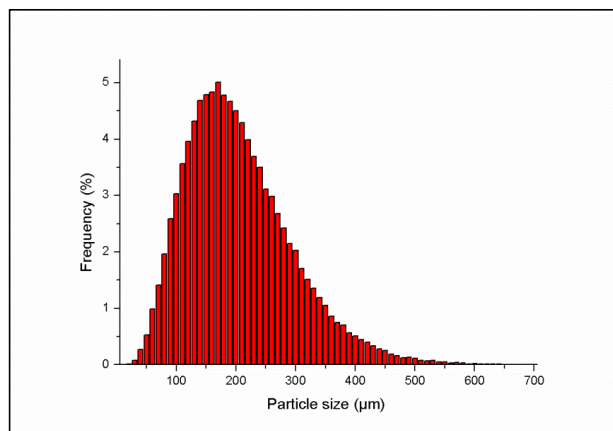
**Table 2: Sublimation rate at 1500s for various heights (\*: friction velocity (m/s); \*\*: height (m); \*\*\*:**

**sublimation rate ( $kgm^{-3}s^{-1}$ ))**

	$u_* = 0.35ms^{-1}$	$u_* = 0.45ms^{-1}$	$u_* = 0.55ms^{-1}$
<b>h=0.01**</b>	3.71E-04***	4.05E-04	4.21E-04
<b>h=0.05</b>	1.22E-05	2.31E-05	3.18E-05
<b>h=0.1</b>	6.11E-07	3.08E-06	5.37E-06
<b>h=1</b>	1.68E-07	1.12E-06	2.29E-06
<b>h=5</b>	2.93E-08	2.88E-07	7.52E-07
<b>h=10</b>	8.44E-09	1.09E-07	3.31E-07

**Table 3: Height which most of saltation particles distributed below for various friction velocities**

	$u_* = 0.35ms^{-1}$	$u_* = 0.45ms^{-1}$	$u_* = 0.55ms^{-1}$
<b>Déry et al. (1998)</b>	0.0196m	0.0253m	0.0316m
<b>Pomeroy and Male(1992)</b>	0.0222m	0.0306m	0.0395m
<b>Xiao et al.(2000)</b>	0.05m	0.05m	0.05m



**Figure 1: Particle size distribution**



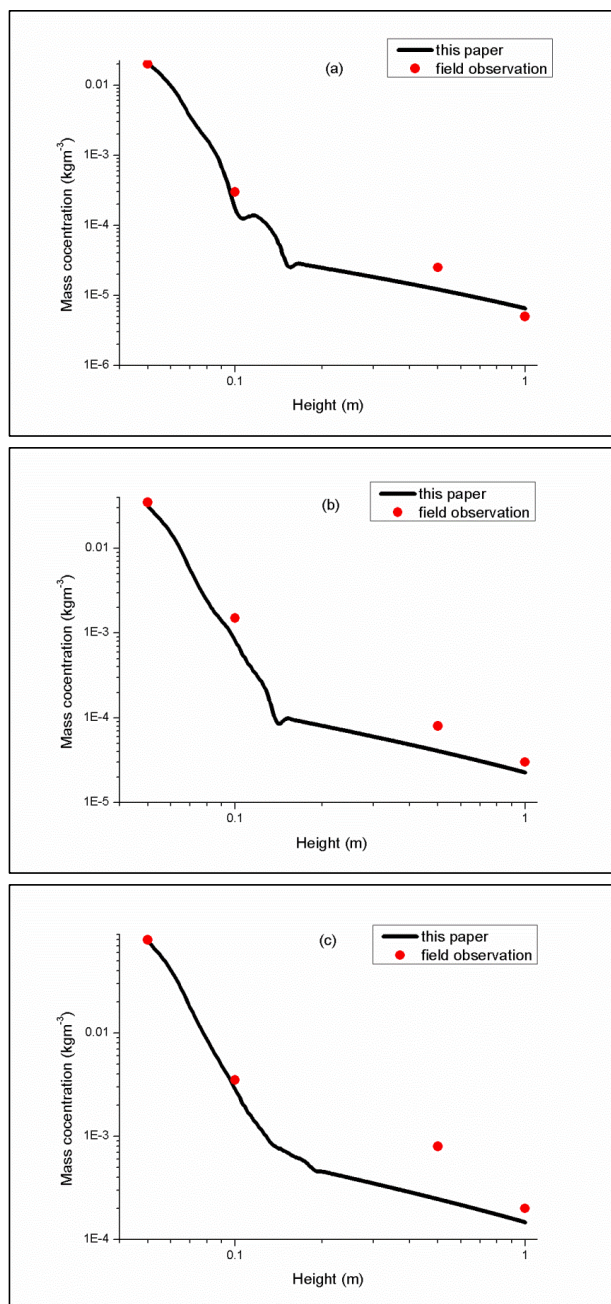
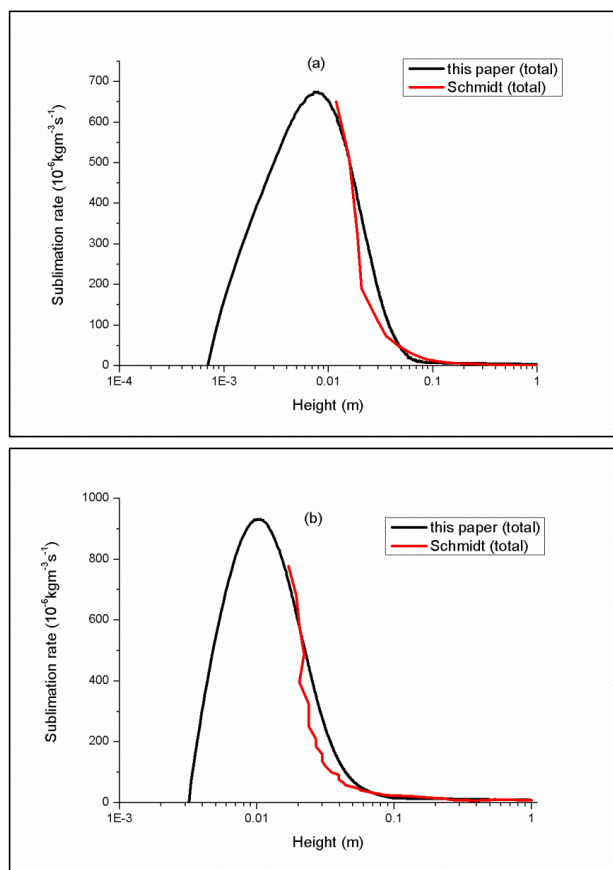


Figure 2: Comparison of mass concentration for this paper and field observation (a:  $u_s = 0.35 \text{ ms}^{-1}$ ; b:  $u_s = 0.41 \text{ ms}^{-1}$ ; c:  $u_s = 0.54 \text{ ms}^{-1}$ )



**Figure 3: Comparison of sublimation rate for this paper and Schmidt (1982) (a):  $u_e = 0.632 \text{ms}^{-1}, T = 267.45 \text{K}$  ;**

**b):  $u_e = 1.072 \text{ms}^{-1}, T = 265.65 \text{K}$**

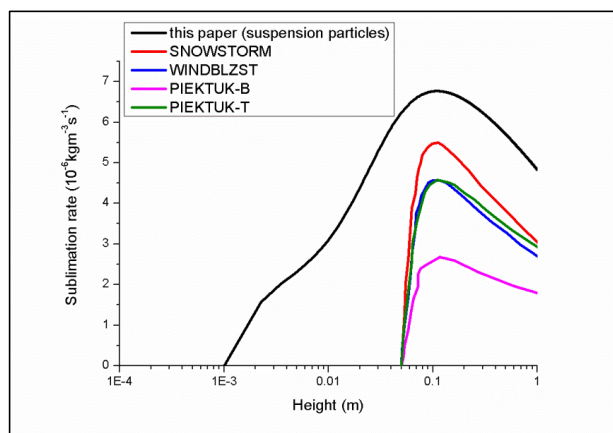
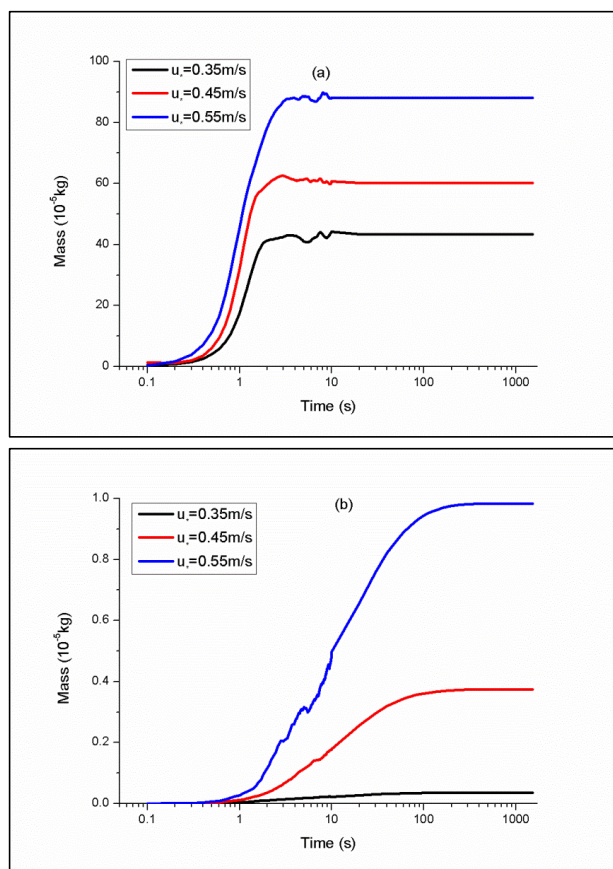


Figure 4: Comparison of sublimation rate for this paper and four blowing snow's models (Xiao et al., 2000)



**Figure 5 : Temporal evolution of mass of saltation particles and suspension particles (a: saltation particles; b: suspended particles)**

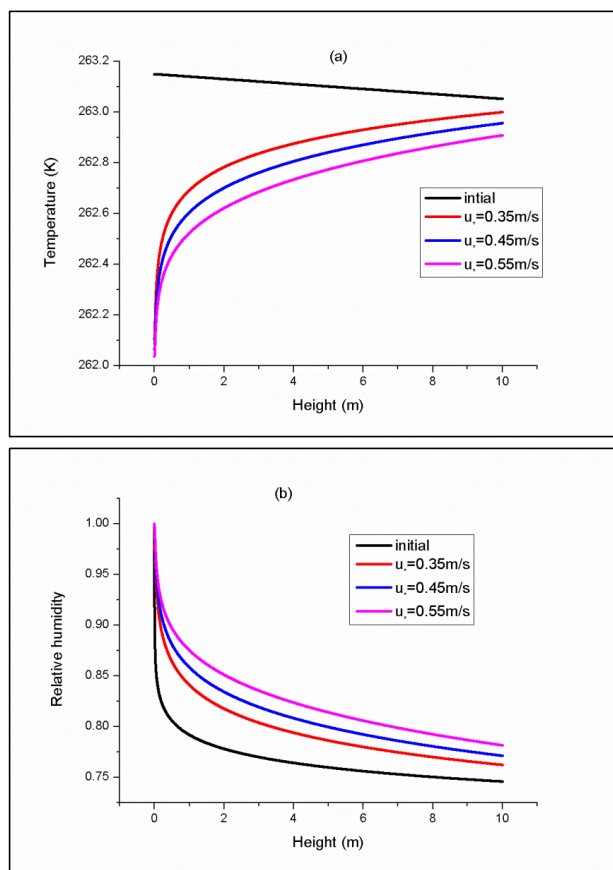


Figure 6: Vertical profiles of temperature and relative humidity

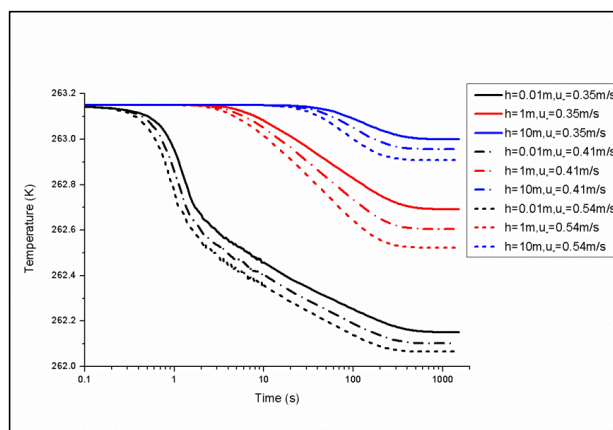


Figure 7: Temporal evolution of temperature for various heights

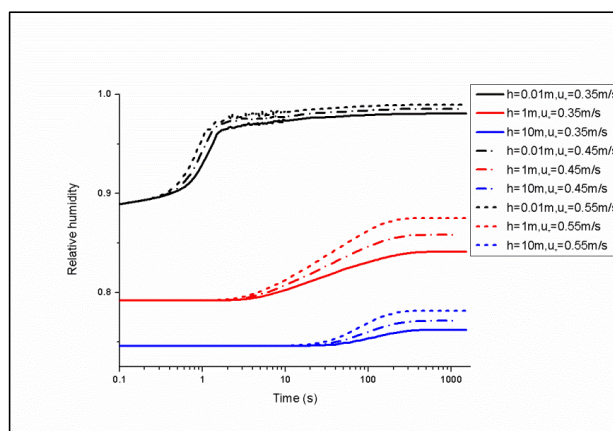
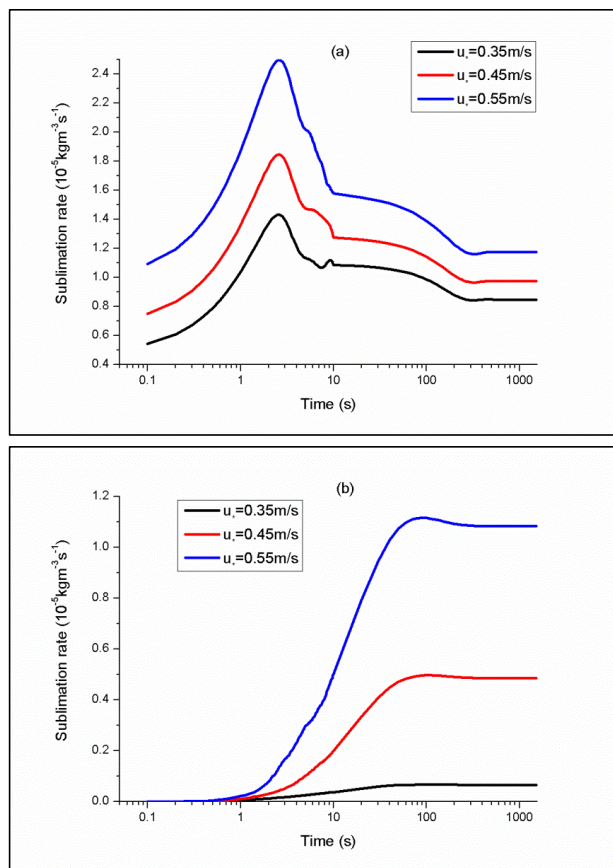


Figure 8: Temporal evolution of relative humidity for various heights



**Figure 9: Temporal evolution of saltation sublimation rate and suspension sublimation rate(a: saltation particles; b: suspended particles)**



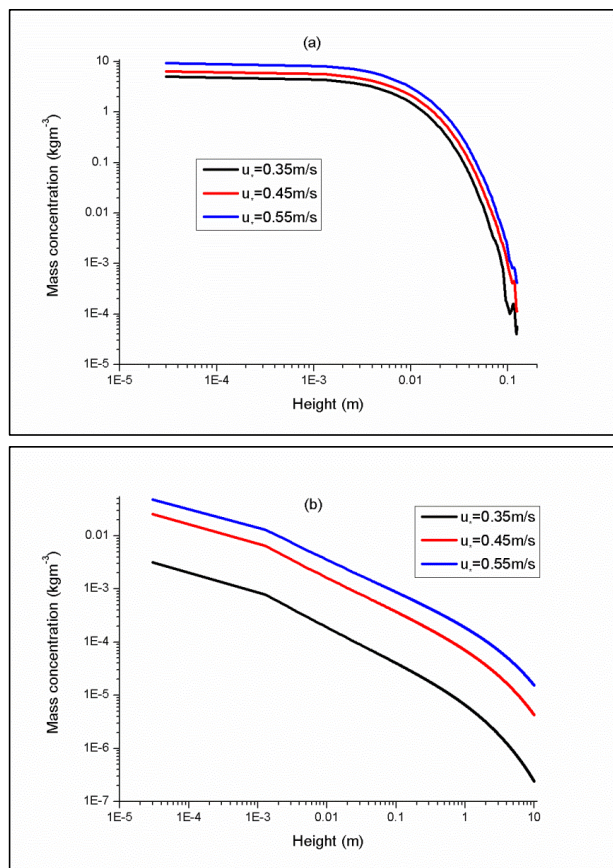
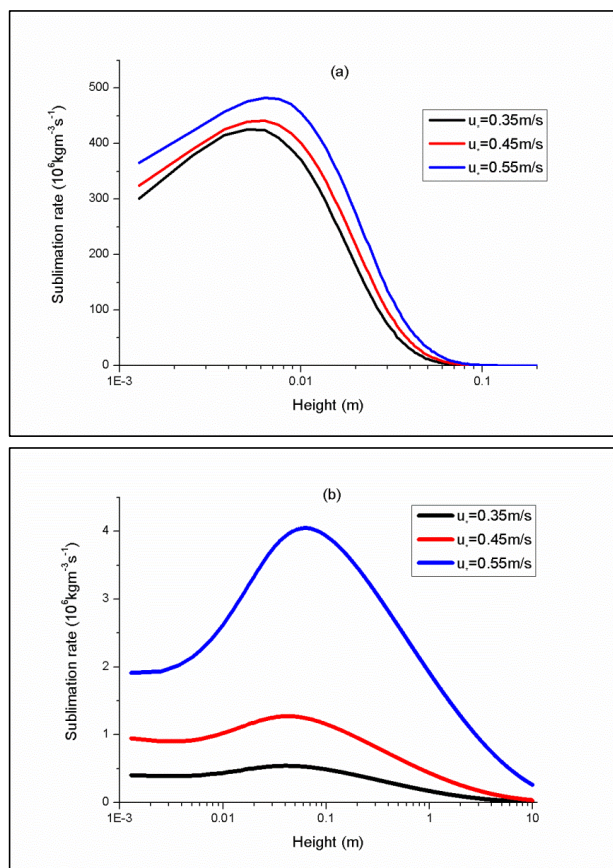
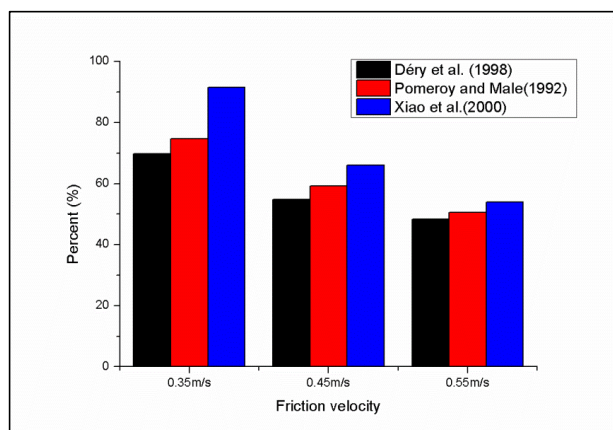


Figure 10: Vertical profiles of mass concentration for saltation and suspension (a: saltation particles, b: suspended particles)



**Figure 11: Vertical profiles of sublimation rate for saltation and suspension (a: saltation particles; b: suspended particles)**



**Figure 12: The ratio of sublimation mass below three heights to the total (the sublimation mass below a height is the sublimation mass that was ignored by other's model, such as Déry et al. (1998), Pomeroy and Male (1992), and Xiao et al. (2000).)**

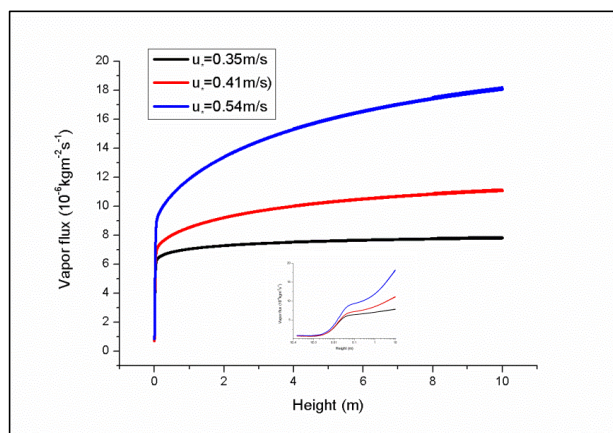


Figure 13: Vertical profiles of vapor flux