

First of all we would like to thank the reviewer for such a thorough review, and for such supportive comments. We have attempted to address the reviewer's main issues below, by running additional experiments where necessary. As this response contains additional figures, we would like to state to the reviewer and the editor that, while the figures presented might be relevant to the response and certainly accessible to the editor and reviewer, we do not wish to present them in the actual publication as we believe the distinction between the experiment performed for this response, and those presented in the paper, is too subtle for most readers.

The comparison with the snapshot initialization is useful but a little bit biased in my opinion because it is based on an old (and probably bad) surface DEM (2002), with velocities that are 10 years younger. This exercise highlights the difficulty of using snapshot calibration because it is not always possible to find datasets that cover the same time period. But I would be curious to see the 30 year run with a ~2010 snapshot calibration (with both surface DEM and velocity) rather than a mix of 2002–2010 data. It would not be surprising if this snapshot calibration, with better and more consistent datasets, yields results that are in a better agreement with the transient calibration. I understand that the authors want to compare the model output with existing data but it is not 100% clear whether the difference between the transient and snapshot calibration for the 30 year run is due to an inconsistency between datasets in the snapshot calibration or if it is just due to the difference between the two types of calibrations.

We attempt to address this issue at the opening of the discussion section by stating that the snapshot calibration is likely not the best possible given data currently available. However, there is a subtle underlying issue here: the importance of a model's ability to make a hindcast in order to make a forecast. These ice streams are in a transient state and have been for at least the last decade – and it seems logical one must capture this state in a model in order to address what the ice stream will do next. The method presented attempts to find this state by matching observations over some finite period. I don't believe there is any formal theory to say how long this period should be, but modelling investigations seem to point toward the decadal time scale (e.g. Payne et al 2005, Favier et al 2014). This then requires the use of less recent observations. Perhaps we are not saying anything with which the reviewer is not already in agreement. But it then must be shown that the same cannot be done with a snapshot calibration in the same manner, and this is the purpose of our snapshot calibration. We are careful to use the 2002 DEM, which is data, and not the 2001 DEM, which is backward extrapolation of data.

At the end of this letter, please find the results of a simulation similar to what you suggest (Fig 1 of this letter). We use the 2008 surface DEM from our transient data set, as this is considered to be the time point of the MEASUREs data used by Seroussi et al 2014 for Pine Island. Note that the grounding line, initially retreated, proceeds to advance and there is a thickening signal close to the grounding line. We point out that the corresponding figure for the 2002-surface snapshot calibration (which we include in the letter to Dr Cornford) shows thinning near the grounding line, but not seaward-concentrated thinning. We also point out that in the 2002-initiated snapshot calibration, some ungrounding does begin to occur, and presumably would continue.

We would claim that dual questions of whether the difference between the 30 year runs is due to an inconsistency between datasets or if it is just due to the difference between the two types of calibration are in essence the same question, as it is very unlikely that data sets of diverse observations gathered even with the same timestamp would be perfectly consistent. The lack of strong thinning in both snapshot-calibrated runs is likely a transient pattern caused by the "shock" of initialising the model without fitting to a dynamic trend (though it is likely any nonphysical transients will not continue for more than a few decades).

This is more a comment than a suggestion, but I was somewhat disappointed that the model does not include a floating ice shelf downstream of the 1996 grounding line, because this is most likely the region where important processes (such as melting at the

ice/ocean interface) triggered the acceleration and thinning that this region is undergoing. Ignoring this region and using boundary stresses as a control felt like putting all these critical processes under the rug. I understand the author's rationale, but I would have loved to see the melt rates as a control and see if the transient calibrated model could tell us more about how the pattern of melting might have changed over the past decade (even with big error bars).

I realize it may feel unsatisfactory, but one must consider (as we have) what would be involved if ice shelves were to be included in the transient calibration. We include a more detailed consideration of this issue in the Discussion section.

At the very least, any trend inferred in the boundary stress parameters could indicate a change of the nature you mentioned (i.e. shift in buttressing due to ice shelf melting), though any inferences that can be drawn directly are qualitative. Inferring such a trend was an initial goal of this study; and given your comment we have elected to show it (see Fig 7), giving the caveat that we are not completely confident that J_{trans} has been lowered sufficiently to make this "real". What is sought is a measure of the nature of an "adjusted R^2 " [e.g. Glantz & Slinker (2001), Primer of Applied Regression and Analysis of Variance, McGraw-Hill, New York], which can be used to determine whether one is overfitting or not when increasing the order of a polynomial fit. To our knowledge there is no such comparable measure in this instance. We are comfortable with this shortcoming, though, as the rest of the content of the paper does not hinge on this.

The other problem with having the stress at the grounding line as a control is that there is no unique solution (as mentioned by the authors p.4470), and it is even worse for the snapshot calibration. An increase in basal friction β has the same effect on the cost function J_{snap} as an increase in normal stress σ . If, for some reason, the algorithm ends up with a σ that is too small, the model will artificially increase β in this region, generating an increase in basal friction right next to the grounding line (see Fig. 4b). With such a high increase of basal friction near the grounding line, it is not surprising that the grounding line does not retreat. Again, I agree that the transient calibration probably does a better job, because it is constrained by more datasets, but including σ in the control space will make the snapshot calibration worse than if the ice shelf was included.

We point out that were ice shelves included, this would indeed negate the need for boundary stress parameters but would then introduce melt rates, initial thickness, and B_{bar} as parameters, as mentioned above.

In a snapshot estimation, only B_{bar} would be required (as well as ice shelf thickness, which would need to be based on BEDMAP2, and the issues with this are stated above). There is undoubtedly some "compensation" of the type mentioned above between B_{bar} and β^2 , leading to some degree of equifinality which could lead to multiple solutions that lead to differing transient behaviors.

I concede it may be the case that the compensation between β^2 and boundary stresses is worse than compensation between B_{bar} and β^2 in a snapshot calibration. As the reviewer states, this may be less so in a transient calibration such as ours. But I believe that any such statements at this time are speculative; issues of equifinality cannot truly be addressed in this context without improved methods that allow Hessian characterization – a definite goal of future study as mentioned in Section 6.1.

Finally, I found the paragraph about the Rignot et al. [2014] paper not very convincing (but I might be a bit biased). First, I totally agree with the authors that Rignot et al. [2014] is based on a qualitative assessment and actual modeling is required to test this hypothesis. I also agree that when the fjords are narrow, the walls of the valley can

exert enough resistance to prevent grounding line retreat along retrograde slope. Now, I am pretty sure that if melt rates were applied at the grounding line and in its vicinity, which is not the case here, grounding line migration would have been more dramatic. This is a very conservative simulation and provides a lower bound to the contribution of this region to sea level and grounding line retreat, and we cannot rule out more dramatic scenarios.

We point out that no time scale is formally given in the Rignot et al 2014 paper, and we do make the statement that rapid retreat past the 30-year horizon cannot be discounted. But it is a very good point that we do not force newly ungrounded ice with sub-ice shelf melting, and we now include this caveat in the section under discussion. (Though I point out there is no reason to assume they will be as high as e.g. PIIS, as this would depend on not only the newly created cavity geometry but that of the existing cavity which is largely unknown.)

I am not a big fan of the title for two reasons. First the term “near-future” is a bit vague, and “inferred” generally refers to the results of inverse modeling. This is just a suggestions and I will leave it to the authors to decide if they want to change the title but I would just take out the second part of the title: “Committed retreat of Smith, Pope, and Kohler Glaciers over the next 30 years”.

We agree “near-future” is vague and have modified accordingly but do not see a problem with invoking a term from inverse modelling, as many studies featuring snapshot calibrations present their studies as inverse modelling as well. Macayeal (1992) used the term “inferred” in its title, and that study used a control method just as we have. “Transient Calibration” may in fact be a term new to ice modelling though “model calibration” is very well established in the computational physics literature, see e.g., Oden, T., Moser, R., & Ghattas, O. (2010), “Computer predictions with quantified uncertainty”, Part I. *SIAM News*, 43(9), 1–3.

p.4460 l.1: keep present tense “is calibrated”.

Done, thank you.

• p.4460 l.12: I don’t really like the term “steady-state” because snapshot inversions do not assume steady state (i.e. they do not assume that time derivatives are 0).

Yes, sorry, this slipped in here by accident. As the term is immediately explained we have simply removed this sentence fragment.

• p.4461 l.6: As such, (comma missing)

Done, thank you.

• p.4461 l.15: “ice thickness” is not really a surface properties. How about surface height?

Done, thank you.

• p.4461 l.18: “stiffness” generally refers to elasticity, viscosity might be more appropriate

Done, thank you.

• p.4462 l.4: you might want to cite Seroussi et al. [2011]

Thanks for pointing this one out.

• p.4462 l.19: integrated → run

Done.

• p.4463 eq.2: It is not really standard to add a factor of 2 for the constraints.

Apologies, this was a typo.

• p.44634 l.1: **Minimizing J is not equivalent to minimizing J 0 , because otherwise you see that by taking $L_i > 0$ and $\mu_i \rightarrow -\infty$, we would achieve $J 0 \rightarrow -\infty$. We actually want to find the saddle point of J 0 .**

You are correct. The wording is changed.

p.4464 eq.3: since basal friction opposes motion, you probably want a minus sign

this depends on how basal stress is defined, and the momentum balance is not stated in this paper; however, the formulation is consistent with Goldberg 2011, which is cited elsewhere.

• **p.4464 l.16: the Lagrange multipliers are not the gradient of the cost function J generally. But they can be used together with the state variables to compute the gradient of J pretty easily.**

“are then used to calculate”

• **p.4471 eq.6: I am not sure to understand the equation, I would have defined the ice height above floatation as follows: $h_{AF} = s - R + \min(\rho_w \rho_i R, 0)$ (1)**

Unless I am mistaken this expression can be negative where ice is floating, which the b_{obs} expression is required in order to determine, by saying that if ice is floating its hydrostatic base will be above R. But you are right that the additional expression for HAF was not actually given, it is now.

• **p.4472 l.8: Thus, (missing comma)**

Done.

• **p.4472 l.10: I kind of disagree with this statement (if I understood correctly). When the grounding line retreats, the velocity increases over the entire domain instantaneously (e.g. Seroussi et al. [2014]). The only way to make sure that the inflow boundary does not affect the model is to go all the way to the divide, assuming that the position of the divide does not change. Now, given the time scale involved in this paper, I don't think the imposed flux affects the model significantly.**

This is a subtle point. Just as in Seroussi et al 2014, we are not using a SIA model, and so of course stress perturbations are felt throughout the model instantaneously. But one would also expect stress transmission to be far less effective over strong bed. The region over which speedup is seen in Fig 5 of Seroussi et al is still quite fast-flowing, whereas velocities at the rightmost part of the domain are down to 100m/a or less, and the only parts of the domain that have low basal stress are the ice streams, as seen from Fig 4(b) of this paper. Thus I would not expect significant velocity change there (were I not imposing it) in response to frontal perturbation and GL retreat. Such a simple model as the kinematic wave theory I apply for this estimate is by no means accurate, just as it is not completely accurate when applied in other studies looking at the region. It is intended only as a back-of-the-envelope estimate as to how long thickness changes should take to propagate across the domain. Payne et al 2005 applied diffusive theory to the trunk of Pine Island Glacier to estimate the timescale of upstream propagation of thinning, which we now cite.

• **p.4472 l.15: Finally**

Copernicus's fault, not mine

• **p.4473 l.20: Thus, (missing comma)**

Done.

• **p.4474 eq.8: you probably forgot a factor 1/5**

I did.

• **p.4475 l.22: “rigour” → rigor (most of the paper is in American English)**

done

• p.4482 I.3: Eq. B2 (no parentheses)

done

• p.4482 I.14: Thus, (missing comma)

done

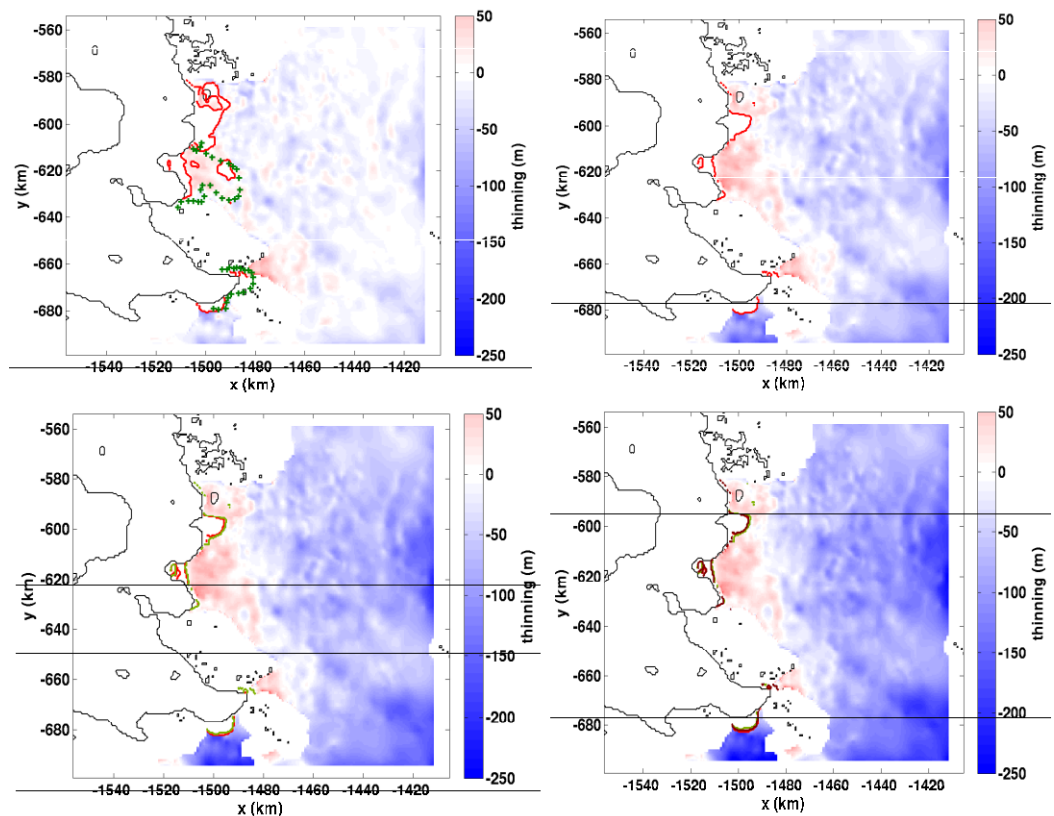
• p.4483 I.14: Thus, (missing comma)

done

• p.4483 I.26: parentheses missing for references

Done

FIGURE 1: the equivalent of Fig 6 of the manuscript for an experiment initialized in 2008 with a snapshot calibration. The snapshot calibration uses MEaSURES velocities, as in the main text, but with a surface elevation closest to 2008. Shading is thinning relative to 2001 as in Fig 6. Years of results are 2011, 2021, 2031, and 2041



corresponding to top left, top right, bottom left, bottom right. Ungrounding is widespread in 2011 but this is because it is imposed in the initial condition; the solution tends to ground downstream over time even as there is thinning upstream.