

# 1 Which are the highest peaks in the US Arctic? Fodar settles the debate

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## 8 9 **Abstract**

10 Though an outstanding achievement for their time, the United States Geological Survey  
11 (USGS) topographic maps of the eastern Alaskan Arctic nonetheless contain significant  
12 errors and in this paper we address one of them. Specifically, USGS maps of different  
13 scale made in the late 1950s alternate between Mt Chamberlin and Mt Isto as being the  
14 tallest peak in the US Arctic. Given that many of the peaks here are close in height and  
15 covered with glaciers, recent climate change may also have changed their height and their  
16 order. We resolved these questions using fodar, a new airborne photogrammetric  
17 technique that utilizes Structure-from-Motion (SfM) software and requires no ground  
18 control, and validated it using GPS measurements on the peaks as well as airborne lidar.  
19 Here we show that Mt Chamberlin is currently the 3<sup>rd</sup> tallest peak and that the order and  
20 elevations of the five tallest mountains in the US Arctic are Mt Isto (2736.0 m), Mt.  
21 Hubley (2718.0 m), Mt. Chamberlin (2712.7 m), Mt. Michelson (2698.5 m), and an  
22 unnamed peak (2695.3 m); these heights are relative to the NAVD88 GEOID12A vertical  
23 datum. We find that it is indeed plausible that this ranking has changed over time and  
24 may continue to change as summit glaciers continue to shrink, though Mt Isto will remain  
25 the highest under current climate trends. Mt Isto is also over 100 m than the highest peak  
26 in Arctic Canada, making it the highest peak in the North American Arctic. Fodar  
27 elevations compared to within a few centimeters of our ground-based GPS measurements  
28 of the peaks made a few days later and our complete validation assessment indicates a  
29 measurement uncertainty of better than +/- 20 cm (95% RMSE). By analyzing time-  
30 series of fodar maps, we were able to detect topographic change on the centimeter-level  
31 on these steep slopes, indicating that fodar can be used to measure mountain snow packs  
32 for water resource availability or avalanche danger, to measure glacier volume change  
33 and slope subsidence, and many other applications of benefit to society. Compared to  
34 lidar, the current state-of-the-art in airborne topographic mapping, we found this SfM  
35 technique as accurate, more useful scientifically, and significantly less expensive,  
36 suggesting that fodar is a disruptive innovation that will enjoy widespread usage in the  
37 future.

## 38 39 **1. Introduction**

40  
41 Here we seek to answer the overarching question: “How well does modern airborne  
42 photogrammetry measure the topography of steep terrain?” We chose to settle the  
43 question of the height and order of the tallest mountains in the US Arctic both for its  
44 intrinsic value and because these rugged peaks are located in a highly glacierized region  
45 in north-eastern Alaska (Figure 1) where we have ongoing glacier research with suitable  
46 validation data (Nolan et al., 2011;Weller et al., 2007). The topographic discrepancies in

47 question are shown in Table 1. Here United States Geological Survey (USGS) maps  
48 indicate Mt Isto as either being 8975' or 9050', depending on map scale, while Mt  
49 Chamberlin is listed as 9020' on both (USGS map elevations are reported in feet).  
50 Further, the elevations of Mt Michelson and an unnamed peak in the Okpilak River  
51 valley (which we herein refer to unofficially as Mt Okpilak) are within a few meters  
52 difference, well within the half-contour accuracy specification (50') of the maps.  
53 Accurate peak elevations are intrinsically interesting to many segments of the public and  
54 academia, but also serve a practical function in aviation planning. Our interest in  
55 measuring these peaks stems primarily from our studies of the glaciers that descend from  
56 them. Located in the pristine Arctic National Wildlife Refuge along with all of these  
57 peaks, McCall Glacier has served as the sole benchmark glacier for the entire US Arctic  
58 since 1957, such that we extrapolate our local measurements from there to inform us on  
59 the impacts of climate change on the broader landscape and its ecology (Nolan et al.,  
60 2011). Ideally we wish to avoid such extrapolation by directly measuring volume change  
61 for all of the 800+ Arctic glaciers annually, which is not feasible to do from the ground in  
62 this remote, roadless terrain. We have in the past used airborne InSAR and airborne lidar  
63 and found them useful but prohibitively expensive for sustainable, academic research  
64 budgets (Geck et al., 2013). This financial obstacle led us to the development of a new  
65 photogrammetric technique. Our study of the tallest peaks in the US Arctic thus serves a  
66 dual purpose – both to resolve the discrepancies in existing maps and to use those same  
67 data to validate this technique as a means to affordably measure changes to snow and ice  
68 on the centimeter scale within steep mountain environments.

69  
70 We have given this photogrammetric technique its own name, fodar, because we believe  
71 it is substantially different from existing techniques and represents a new standard in  
72 performance and cost. Note that fodar is a portmanteau of foto and lidar  
73 (<https://en.wikipedia.org/wiki/Lidar>); it is not an acronym nor is it capitalized. Our  
74 design goal was to affordably map the topography of large, remote areas at high accuracy  
75 using manned aircraft and requiring no ground control. In previous work, we  
76 demonstrated our success by creating maps with 10 – 20 cm ground sample distances  
77 (GSD) over tens of square kilometers and validating that they had a geolocation-accuracy  
78 and map-precision (repeatability) better than +/- 30 cm and +/- 8 cm respectively, at 95%  
79 RMSE (Nolan et al., 2015). The method is distinguished from traditional methods of  
80 photogrammetry by its use of the Structure-from-Motion (SfM) algorithm (Koenderink et  
81 al., 1991; Westoby et al., 2012; Nolan et al., 2015), and it is distinguished from other  
82 forms of SfM photogrammetry by the fact that that no ground control is required to  
83 achieve such accuracy and precision. Ground control is not required because the precise  
84 timing between the shutter of the camera and survey-grade GPS yields absolute photo  
85 locations with less than 10 cm error, and this constrains the SfM bundle adjustment  
86 sufficiently to meet these specs. Thus if any ground control is utilized, it is only *after the*  
87 *map is created*, to shift the entire map uniformly by less than 30 cm some direction.  
88 Though SfM photogrammetry is currently exploding in scientific popularity with cameras  
89 mounted on inexpensive drones (d'Oleire-Oltmanns et al., 2012; Hugenholtz et al.,  
90 2013; Lucieer et al., 2013; Rinaudo et al., 2012; Ryan et al., 2014), directly georeferenced  
91 results from these systems generally have accuracies and precisions 10-100x worse than  
92 fodar because they lack survey-grade GPS on-board to constrain photo locations as well

93 as fodar. Without precise positioning in the air, -to improve accuracy and precision  
94 substantial photo-identifiable survey-grade ground-control needs to be incorporated into  
95 the bundle adjustment *before the map is created*, a time-consuming process similar to  
96 traditional photogrammetric methods. Practically speaking it is unclear as yet whether  
97 sufficient ground control can ever be acquired to match fodar specs over the spatial scales  
98 we are operating at. Thus fodar could be regarded as survey-grade SfM photogrammetry,  
99 and considered in much the same way that consumer GPS are distinguished from survey-  
100 grade GPS – both are useful, but which tool to use depends on the questions trying to be  
101 answered.

102  
103 In prior work, we have shown that fodar is as accurate as alternative methods but  
104 substantially less expensive. By subtracting snow-free digital elevation models (DEMs)  
105 from snow-covered ones, we found fodar was suitable for measuring thin (< 30 cm)  
106 Arctic snow depths on the watershed scale with accuracies as good as hand-probing  
107 (Nolan et al., 2015). Studies of coastlines in Alaska further validated fodar  
108 specifications, demonstrating that coastal erosion could be measured by such DEM  
109 differencing as accurately as ground measurements but over much larger areas (Gibbs et  
110 al., 2015) and that coastal mean high water vectors could be extracted from fodar DEMs  
111 with about the same accuracy as manual digitization but much more efficiently (Kinsman  
112 et al., 2015). Independent validation using about 100 GCPs by the State of the Alaska of  
113 DEMs we made of 26 coastal villages revealed that directly-georeferenced horizontal  
114 accuracy was <10 cm in all cases, that the mean directly-georeferenced vertical offset  
115 was 21 cm, and that vertical vertical precision was 10 cm at two standard deviations  
116 (Overbeck et al, 2016)ince then we have mapped over 3000 km<sup>2</sup> of coast in Alaska for  
117 similar purposes (Nolan, unpublished data). In remote locations like these, the field  
118 effort to collect ground control can greatly exceed the cost of the airborne survey itself,  
119 thus fodar can result in a tremendous savings in both cost and time. Fodar specifications  
120 also meet or exceed the capabilities of most airborne lidars, the current state of the art in  
121 topographic mapping (Deems et al., 2013;Höfle et al., 2011), yet fodar hardware costs  
122 less than \$30,000, compared to \$500k to \$1M for airborne lidar hardware suitable for  
123 mapping mountain ranges. As described in detail in (Nolan et al., 2015), the primary  
124 underlying reason for the difference in price is due to the software – utilization of the  
125 Structure-from-Motion algorithm allows for prosumer grade cameras to be used without  
126 the need for an IMU, an on-board computer, or a separate equipment operator.

127  
128 To address the overarching question of this paper, we mapped each of the five highest  
129 peaks photogrammetrically between two and four times in 2014-2015. These repeat  
130 measurements not only let us determine the repeatability (precision) of our methods in  
131 steep terrain, but also detect change of snow and ice surfaces over time. We compared  
132 these measurements to survey-grade GPS measurements we made by climbing to the top  
133 of Mt. Isto (Figure 2) and Mt. Chamberlin, as well as to lidar measurements we made of  
134 all five peaks between 2008 and 2011. Comparing all measurements also allowed us to  
135 examine rates of change of peak elevation, caused by ice and rock loss from their  
136 summits.

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138

139 **2. Methods**

140

141 2.1 Fodar

142 We mapped each of the five mountains at least two times in 2014-2015 (Table 1) using  
143 our photogrammetric system, flown in a Cessna 170B or Piper Lance by the first author.  
144 In total we flew ten airborne missions from Fairbanks, Alaska, to the study area 500 km  
145 away (Figure 1), though not every flight resulted in data published here due to weather or  
146 acquisition issues. Our flight lines were typically flown at between 10,000' and 11,000'  
147 feet, resulting in image ground sample distances (GSD) ranging from 5 cm near the  
148 summits to about 50 cm within the valleys. We processed the images into digital  
149 elevation models (DEMs) with postings ranging from 37 to 51 cm. The photogrammetric  
150 system and its processing is fully described in (Nolan et al., 2015). In short, it utilizes a  
151 Nikon D800E, a Nikkor 24 mm lens, a Trimble 5700 with roof-mounted L1/L2 antenna,  
152 and a custom intervalometer that triggers the camera and sends an event pulse to the GPS.  
153 GPS processing was done in Novatel's Grafnav software using the PPP method (Gao et  
154 al., 2002) to create an exterior orientation file that is imported in Agisoft's Photoscan for  
155 bundle adjustment and DEM creation. We processed our GPS data from the start time  
156 forwards in time and separately from the end time backwards in time, a common  
157 technique for assessing error. Comparison of forward/reverse solutions and other internal  
158 software metrics indicates that the positional accuracy of the camera was 10 cm or better  
159 typically, except when excursions occurred due to loss of satellite numbers or lock,  
160 usually caused by banking too steeply. The subsequent bundle adjustment within  
161 Photoscan confirmed this accuracy with mean shifts in photo locations of less than 10  
162 cm. GPS solutions and the subsequent DEMs were processed relative to the WGS84  
163 ellipsoid to facilitate comparison with lidar data, with peak elevations converted to  
164 NAVD88 GEOID12A using NOAA's online tools ([http://www.ngs.noaa.gov/cgi-  
165 bin/GEOID\\_STUFF/geoid12A\\_prompt1.prl](http://www.ngs.noaa.gov/cgi-bin/GEOID_STUFF/geoid12A_prompt1.prl)). Fodar creates not only a DEM but also a  
166 perfectly co-registered ortho image; herein we use 'map' generically to refer to both  
167 products.

168

169 2.2 GPS Ground Control

170 We conducted field campaigns to climb Mt Isto (27 April 14) and Mt Chamberlin (3 May  
171 14) to directly measure peak elevations, shortly after our primary airborne mapping  
172 mission there (22 April 14), with a climbing team led by the second author. A Trimble  
173 5700 GPS receiver with compact L1/L2 antenna was mounted on a backpack and  
174 continuously recorded during the ascents and descents (eg., Figure 2). Static occupations  
175 near the summits of both peaks ranged from 10 to 20 minutes, with the antenna either  
176 placed on a spike mount or left on the backpack which was dug into the snow for  
177 stability; because the peaks themselves were on or near cornices, the summit occupations  
178 were made ~5 m horizontally away from the actual peaks for safety concerns. Novatel's  
179 Grafnav software using the PPP method was used for all processing, given that the  
180 nearest high-quality CORS site (Snay et al., 2008) was over 160 km away and no local  
181 base station was installed due to weight and logistical requirements. The nominal  
182 antenna height on the backpack was 2.14 m; practically it varied from 0 while climbing  
183 steep ice to 1 m while wading through deep snow, and thus varied between 0 and 2.14 m.  
184 Given the extreme antenna motion during climbing, broad sections of this kinematic

185 session failed to process and much of it had errors on the 1 m level. We therefore filtered  
186 these ground control points (GCPs) to those locations where we were mostly walking  
187 upright on hard ice, as here we knew the antenna height and the improved antenna  
188 stability led to forward/reverse solution separation less than 20 cm; this occurred mostly  
189 near the summit ridges. Comparison of forward/reverse solutions indicated that static  
190 sessions had an accuracy of about +/- 10 cm. Note that our fodar validation comparisons  
191 were made to these offset measurements and that the peak measurements published here  
192 are from the highest point on the maps, not the height of these GCP locations. The same  
193 GPS system was used on McCall Glacier, directly beneath Mt Hubley, prior to our June  
194 2014 airborne measurements of it. The antenna was mounted on a snowmachine with a  
195 nominal antenna height of 1.08 m and variations likely less than +/- 0.15 m. These data  
196 were processed the same way and further filtered by distance to provide 5 m spacing  
197 between points and to ensure their solutions were accurate to < 10 cm.

198

### 199 2.3 Lidar

200 The lidar DEMs were acquired by a commercial vendor using an Optech ALTM Gemini  
201 system and delivered to us both as individual-swath point-clouds and merged DEMs,  
202 between 2008 and 2011. Using the swath data, we compared overlapping regions of  
203 adjacent swaths to assess system precision using repeatability as a metric. Two DEMs  
204 were acquired in 2008: one small DEM of just McCall Glacier had a precision of 16 cm  
205 (95% RMSE) and a second larger DEM one that covered all of the glaciers in this region  
206 (as well as the five peaks) at a precision of over 3 m, due to a variety of quality control  
207 and planning issues. ~~A~~The acquisitions ~~were of the larger area was~~ thus repeated in 2009  
208 and 2010, but these also suffered from a variety of issues. In 2011, a new map of the  
209 entire area had a measured precision of +/- 50 cm (95%) between adjacent swaths, ~~though~~  
210 ~~and~~ related swath-edge artifacts could be found within the DEM at this level. We  
211 extracted several large blocks of data (all with  $n > 10^6$ ) from both the small (better) 2008  
212 DEM and the ~~large~~ 2011 DEM over ice-free rocks to further assess repeatability, and  
213 found similar scatter of about +/- 0.50 m (95%) about the mean. This value was  
214 apparently driven by the 2011 data quality, as the point density of the 2008 data was  
215 more than 4 times higher than the 2011 data, leading to 1 and 2 m postings respectively,  
216 and thus spatial biasing of the coarser pixels in rough terrain may be the limiting factor in  
217 repeatability here. According to the metadata, the 2011 data were shifted down 0.75 m,  
218 based on co-registration with the worse of the two 2008 DEMs that covered a much  
219 larger area, which had apparently already had been shifted down 0.20 cm based on some  
220 limited ground control on tundra acquired by the vendor. We therefore used GCPs  
221 collected by us within a few weeks of the 2011 lidar acquisition using a snowmachine  
222 transect on McCall Glacier ( $n = 1703$ , 1500 - 2340 m HAE) as described above and found  
223 a mean offset of 0.61 cm (upward DEM shift) with standard deviation of 0.10 m.  
224 Unfortunately the 2011 data were delivered in two non-contiguous blocks and our GCPs  
225 come only from the eastern one; however, as described later, comparison of rock areas  
226 between the lidar and our SfM maps on both blocks showed this 0.61 m shift reduced the  
227 mean residual difference to within +/- 0.10 m and thus we applied this shift to both lidar  
228 blocks.

229

230



### 3. Accuracy and Precision Assessments

We assessed horizontal geolocation accuracy of the fodar DEMs by assessing co-registration offsets between our repeat-maps, because none of our GCPs were photo-identifiable. While in principle comparing maps to themselves only assesses precision and not accuracy, our prior work with photo-identifiable GCPs demonstrated that such comparisons yield the same results as GCP comparisons (Gibbs et al., 2015; Kinsman et al., 2015; Nolan et al., 2015; [Overbeck et al, 2016](#)). Using two orthoimages each on Mt Isto, Mt Chamberlin and Mt Michelson made in 2014, we used standard image-correlation techniques in Matlab to determine there was a sub-pixel (5-10 cm) horizontal-coregistration between them. In other work, we have also mapped the McCall Glacier valley five times from 2013-2015 and again found horizontal coregistration was subpixel (Nolan, unpublished data). Given that our pixels are roughly 25 cm GSD and our camera positioning accuracy is 10 cm or better, this subpixel horizontal accuracy makes sense, but given the ambiguities caused by the amount of real change on the surface due to snow, it was not possible to determine a precise value. Thus our assessment of the horizontal geolocation accuracy of our maps is that they are accurate to the subpixel level [as we found in previous studies](#) and we therefore applied no horizontal geolocation offsets to these data. We validated this horizontal accuracy visually by creating difference maps of all peaks and found no systematic horizontal alignment issues, though this was difficult to assess visually at the decimeter level because real changes on ground revealed correlations with aspect, largely due to wind direction and solar aspect. Figure 3A shows an example of this on Mt Chamberlin. On a broad scale, the southeast face (right) shows strong avalanche dynamics, the southwest face (left) shows melt dynamics, and the northwest face (top) shows glacier motion and wind redistribution. Note that the color scale here is only +/- 50 cm, so even if these differences were caused by misalignment, that misalignment must be quite small in this steep (>45°) terrain. On the scale of a few hundred meters (eg, small rock outcrops), dozens of informal transects revealed no systematic offsets, providing further validation.

We assessed vertical geolocational accuracy by comparison with our GCPs. On Mt Chamberlin, the 24 March and 22 April fodar elevations were -0.18 m and -0.04 m different respectively from the near-summit GPS measurement on 3 May of 2716.38 m HAE (note that this measurement was taken about 10 m from the true summit and relative to the WGS84 ellipsoid). Kinematic points near the summit (n=288, 2411 – 2513 m HAE) were -0.17 m and +0.08 m from the March and April map elevations respectively, with a +/- 0.10 m standard deviation. Though the March map has a larger offset, it is not unreasonable to expect 10-20 cm of change on these snow and ice covered locations over the intervening month. Given that these residuals for the 22 April map are within the accuracy of the GPS, we did not apply any shifts to these maps to geolocate them further. On Mt Isto, we found the 24 March and 22 April maps within -0.06 m and -0.03 m respectively of the 27 April near-summit GCP measurement of 2738.88 m HAE. Kinematic points near the summit (n=1247, 2735-2736 m HAE) showed residuals of +0.26 and -0.05 m for the March and April maps respectively with a 0.27 m standard deviation. Again given that the April residuals (made 5 days apart) are within their error bounds and March measurements so close, we did not apply any geolocation offsets to

277 these maps either. For the Mt Hubley map, we compared snowmachine GCPs from  
278 McCall Glacier (n=1432, 1500 – 1900 m HAE) acquired on 28 April 2014 to the SfM  
279 map made on 16 June and found a mean offset of -0.10 m with a standard deviation of  
280 0.15 m. Given that this is within the noise level of both measurements and an unknown  
281 amount of melt occurred (probably less than 10 cm), we applied no shift to these data  
282 either. That is, we consider the fodar maps to be as accurate as our GCP validation data  
283 in all cases, with those measurements having the least temporal influence all within +/-  
284 10 cm. We have no GCPs for comparison to Mt Chamberlin or Mt Okpilak, though  
285 informal comparison of some rock areas here to the 2011 lidar showed near perfect  
286 vertical agreement.

287  
288 We assessed precision of the fodar DEMs primarily by comparing repeat-maps to each  
289 other in areas where real changes to the surface were minimized. In the context of this  
290 paper, we consider precision to be analogous with repeatability, and we use this  
291 repeatability to determine the measurement uncertainty in our peak measurements.  
292 Unfortunately 2014 was an unusually snowy spring and it was impossible to find large  
293 blocks of data that were free of change due to snow or ice (eg, Figure 3A). Figures 3B-C  
294 gives a clear example of the real changes on the ground that confound attempts to use  
295 large-scale repeatability as a measure of precision with measurements only a month apart.  
296 Here a fresh snowfall in March has largely avalanched off in the gullies by April, causing  
297 the April DEM to be up to 6 m lower within them, as seen in Figure 3C. The ridges in  
298 between the gullies show little to no change, as validated by the orthoimages, and this  
299 profile is typical of many that we extracted here. Figure 3D shows Mt Isto, similar to Mt  
300 Chamberlin in Figure 3A; note that there is somewhat less aspect-dependent difference.  
301 In the full domains of A and D, we found 95% of points were within +/- 140 cm and +/-  
302 52 cm respectively (n>10<sup>7</sup>). Within the subdomains indicated by the black rectangles,  
303 however, these values dropped to +/- 38 cm and +/- 20 cm respectively (n>10<sup>6</sup>), as shown  
304 in Figures 3E and 3F; carefully choosing yet smaller domains results in yet smaller  
305 differences. We believe these values are more representative of our actual precision,  
306 though are still erroneously high due to real changes still being captured here (more so on  
307 Mt Chamberlin). We found values of +/- 20 cm on the other mountains as well for areas  
308 of about this size. This precision is about twice as high as we found previously (~8 cm)  
309 on smooth, low-relief surfaces like runways and frozen lakes (Nolan et al., 2015), and we  
310 suspect that the bulk of the difference is due to real change and to spatial biasing caused  
311 by averaging of steep terrain into relatively large pixels. The scatter in our GCP  
312 comparisons is another measure of precision, and perhaps a better one since there was  
313 less intervening real change on the ground. As described previously, in our April  
314 comparisons (5 day interval), we found 95% of points within +/- 7 cm combining data for  
315 both peaks, similar to the values we found in our prior study. Thus we believe a  
316 conservative reasonable estimate of our precision on mountain peaks to be +/- 20 cm.

317  
318 Based on these comparisons, our assessment is that the horizontal and vertical  
319 geolocation accuracy of +/-10 cm in steep terrain is *better* than we found previously in flat  
320 to moderate terrain at +/- 30 cm (Nolan et al., 2015), and we thus made no corrections to  
321 our maps based on ground control. That is, the DEMs we created using only airborne  
322 data cannot be improved further using all of the ground control available to us. Given

323 that we found our precision was +/- 20 cm and that we found no consistent systematic  
324 bias in our accuracy, we conservatively consider this our accuracy level too, noting that  
325 our precision values are likely artificially-high due to undocumented real changes to the  
326 surface and due to spatial biasing. In any case, based on this analysis, we conservatively  
327 consider the measurement uncertainty in our peak elevations to be +/- 20 cm at 95%  
328 confidence.

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330

#### 331 **4. Summit Elevations**

332

333 We determined peak elevations simply by locating the highest pixel for each mountain  
334 within its DEM, which all had postings of 51 cm or smaller. For our final results (Table  
335 1, in bold), we selected the values from those maps that were made closest in time to our  
336 GCPs for the tallest three, and because we had no GCPs for the other two we used the 6  
337 July 2015 measurements for both to provide the best comparison by eliminating  
338 uncertainties due to any temporal changes. As seen in Table 1, the measured differences  
339 in peak elevations (3 – 18 m) are all greater than the uncertainty of those measurements  
340 (20 cm), lending strong confidence that they are currently ranked correctly by elevation.  
341 Our fodar and GPS measurements confirm that none of the peaks are over 9000' and that  
342 Mt Chamberlin is not the tallest peak in the US Arctic, as indicated by the 1:63,360 scale  
343 maps, but rather is currently the 3<sup>rd</sup> tallest peak, as originally indicated by our lidar.  
344 Figure 4 presents 3D synthetic visualizations of several of these peaks using fodar DEMs  
345 and orthoimages.

346

347

#### 348 **5. Discussion**

349

350 Based on our results, there is no longer doubt regarding which is the tallest peak in the  
351 US Arctic today: Mt Isto at 2736 m. Given the consistency between our results and the  
352 1:63,360 maps, it seems clear that the 9050' measurement indicated on the 1:250,000  
353 scale map was in error. Note that none of the peaks today are over 9000', as indicated on  
354 the USGS maps (made over 60 years ago) and still re-published today in the FAA's  
355 aviation sectional charts. Given that the highest peak in the Canadian Arctic is Barbeau  
356 Peak on Ellesmere Island at 2616 m and that it is unlikely that any potential mapping  
357 errors there exceed the 120 m difference, Mt Isto is also the highest peak in the North  
358 American Arctic and, to our knowledge, the highest Arctic peak outside of Greenland.

359

360 Given the survey control available in Arctic Alaska in the late 1950s, it is remarkable  
361 how well the USGS elevations compared to our own. As there is no official  
362 transformation between the USGS map datum of NGVD29 and the current NAVD88  
363 datum in Alaska, we cannot directly compare these elevations, but likely these  
364 transformations would be less than 2 m, based on several benchmark surveys. Note too  
365 that the latest official geoid model available from NOAA, GEOID12A, model will soon  
366 be replaced by GEOID15B, and our use of the 15B model indicates the elevations will  
367 uniformly decrease by about 1.4 m. Ignoring these uncertainties, four out of five peaks  
368 on the 1:63,360 maps are within 1-2 meters of our measurements, well within the



369 published uncertainty of those maps of 15 m, and truly a testament to the quality of the  
370 survey teams and photogrammetrists that produced those maps in such challenging  
371 circumstances. Unfortunately, given the published uncertainty of 15 m, we cannot rule  
372 out that this amazing correspondence in actual peak values was not spurious. However,  
373 given that the 33 m difference at Mt Chamberlin is more than double the published  
374 uncertainty and that the other peaks showed a much closer correspondence with our  
375 measurements, it is conceivable that some portion of this difference could be due to a real  
376 change here over the past 50 years.

377  
378 Our own results show that elevation change occurs here essentially continually; that is,  
379 the scatter in our own measurements is not due solely to measurement error either. For  
380 example, on Mt Okpilak we found that the location of the peak moved more than 15 m  
381 laterally between April and July 2015 even though the elevation changed by only 15 cm,  
382 as the peak is located on a broad, flat corniced ridge. Similarly, the 1 m difference on Mt  
383 Chamberlin between April 2014 and April 2015 was largely real, since nearby rock did  
384 not show any such difference with analyses similar to Figure 3. Thus the short-term  
385 temporal variations in actual peak height are likely as high or higher than the uncertainty  
386 in our measurements, and any future measurements should anticipate at least a +/-1 m  
387 uncertainty due to recent storms. While such dynamics are noise for this study, our  
388 results indicate that our methods are a valuable new tool in the study of snow thickness  
389 (eg., Figure 3C), wind redistribution (eg., Figure 5), and avalanche redistribution (eg.,  
390 Figure 3A) in steep mountain environments. However such dynamics are not large  
391 enough to explain the 33 m difference in Mt Chamberlin.

392  
393 Perhaps not coincidentally, of all of five peaks Mt Chamberlin is covered by the largest  
394 glacier and also shows signs of the largest changes to its peak. In recent years, many  
395 glaciated peaks in Alaska have experienced massive rock/ice avalanching (Molnia et al.,  
396 2014), and the destabilizing effect of climate warming on mountain peaks has been noted  
397 world-wide (Gruber et al., 2007;Huggel, 2009;Huggel et al., 2012;Enkelmann et al.,  
398 2015). For example, Mt Cook in New Zealand lost more than 10 m of its peak due to a  
399 rock avalanche, and the subsequent destabilization has caused another 20 m rock and ice  
400 loss (Vivero et al., 2012;Petley, 2014). Thus if Mt Chamberlin was indeed over 30 m  
401 higher when the USGS maps were made, likely the change occurred abruptly rather than  
402 through gradual melting. The northwest face of Mt Chamberlin was once covered by a  
403 glacier tens of meters thick that likely avalanched catastrophically, as can be deduced by  
404 the ice that still remains there through various visualizations (Figure 6A). The steep  
405 southeast face is now completely free of ice, and at its base there are also large  
406 accumulations of rock debris that appears to originate from Mt Chamberlin rather than  
407 the valley glacier at its base (Figure 6B). The rock near and under these corniced peaks is  
408 also prime for frost shattering and rock avalanches, with liquid water from the surface  
409 now able to percolate into the bed where temperatures are still below freezing and likely  
410 near the optimum -5C to -15C to cause failures (Walder et al., 1985), and our images  
411 show that minor rockfalls are common here. Overall, the evidence of massive  
412 avalanching on the northwest face combined with the notched shape of the peak with ~75  
413 degree slopes heading into debris fields at the base of the southeast face (Figure 6C) lend  
414 strong credibility that either rock or ice or both have been lost here. Whether a 33 m loss

415 could have occurred here is beyond the scope of this paper to determine, but a 5 m loss  
416 seems probable at some point in the recent past, which is enough for Mt Chamberlin to  
417 have once claimed the #2 spot above Mt Hubley. We were unable to locate the original  
418 photos used to create the USGS maps, and unfortunately other photos we found from that  
419 time period are inconclusive due to resolution or snow cover, so for the time being this  
420 debate is not fully settled.

421

422 Will the ranking of these peaks change in the future? As long as current climate trends  
423 continue and no massive rock avalanches occur, the order of the top three are not likely to  
424 change due to loss of ice or snow on the summits. Mt Isto would have to lose over 18 m  
425 of ice to lose its crown, but there is no evidence that such a thickness exists there: the ice  
426 is only a few meters thick as gaged from the lee side and exposed rock is encroaching  
427 from nearly all sides. Mt Hubley is the only peak that is not covered by a glacier or  
428 permanent cornice as it is on an arête (Figure 7A), though it does accumulate snow in  
429 winter. Mt Chamberlin will continue to lose elevation, perhaps in catastrophic events,  
430 and single storm events are unlikely to even temporarily increase it by the 5 m needed.  
431 Our measurements showed that Mt Michelson and Mt Okpilak were only ~1.5 m apart  
432 relative to the WGS84 ellipsoid; a relative geoid anomaly between them of 1.5 m  
433 increased that spread to about 3 m. Both mountains are covered by glaciers that are at  
434 least 3 m thick at their peaks, though where the eventual rock peaks will be is uncertain  
435 (Figure 7B-C). Adding to the uncertainty are future improvements to the geoid model  
436 here. We tested the experimental 15B model and found it gave all peaks ~1.4 m  
437 downward shift compared to the 12B model we used, but given that the 12B model  
438 indicates a spatial gradient of 1.5 m between these peaks, future higher resolution data  
439 could yield gradients of that size but with opposite sign, suggesting that this debate is not  
440 fully settled. Given that the ranking of these peaks is determined by height differences of  
441 3 to 19 m, a rock avalanche smaller than the size of Mt Cook's in 1991 could change the  
442 order of any of these at any time, though determining whether the local geology is likely  
443 to support such large changes will take further research.

444

445 We found other sources of error in our data which did not affect our peak measurements,  
446 so we did not include them in our uncertainty estimates. Deep shadows on fresh snow on  
447 steep headwalls occasionally caused a reduced point density in the fodar point clouds.  
448 Here there was essentially no contrast available to find match points. These areas were  
449 small and isolated, amounting to less than 5% of the total areas mapped, as even the track  
450 left by a rock rolling downhill can provide enough contrast to constrain elevations there  
451 (Figure 8). Where this point density was simply reduced, a coarser mesh could be  
452 applied and the results interpolated into the DEM; further research is required to  
453 determine how well our accuracy and precision specs apply to such areas, but spatial  
454 biasing errors will certainly be larger. Where there were no points, gaps could only be  
455 filled by pure interpolation or by re-acquiring with a different sun angle. Because our  
456 areas could take an hour or more to acquire, moving shadows also caused some noise  
457 artifacts at the edges of the shadows moving over low-contrast snow. Occasionally these  
458 artifacts were quite large, on the order of 10 m, but in all cases it was clearly apparent  
459 that they were actually artifacts and were easily distinguishable from valid data (eg  
460 Figure 8d).

461

462 The results of our analyses indicate that our photogrammetric measurements are  
463 essentially as accurate as either our GPS or lidar measurements in determining peak  
464 elevations, as well as many measuring other features of interest. Table 1 shows that the  
465 fodar measurements on all peaks were within 40 cm of the 2011 lidar. Our repeated  
466 fodar measurements at Mt Isto and Mt Chamberlin in spring 2014 had differences of only  
467 8 cm and 19 cm respectively (Table 1), noting that the cornices on these peaks could have  
468 changed on this level or higher due to wind redistribution and melt between  
469 measurements. Comparisons of our April 22nd maps of Mt Isto and Mt Chamberlin to  
470 our GPS measurements made 5 - 11 days later were within only 4 cm, which is better  
471 than the accuracy level of the GPS measurements themselves. Note that these fodar  
472 measurements involved no corrections for ground control—these are directly  
473 georeferenced results utilizing only airborne data. Comparison of two Mt Isto fodar maps  
474 to each other over small areas indicate a repeatability on the order of +/-20 cm (95%  
475 RMSE), including real changes due to snow and ice. This repeatability is superior to the  
476 precision we measured using our two best lidar maps over large ice-free areas by more  
477 than double. Given that all techniques experience worse precision in steep mountain  
478 environments due to spatial biasing caused by GSDs being large compared to terrain  
479 variations, fodar outperforms lidar in the sense that fodar GSDs are much smaller than  
480 lidar GSDs for the same amount of flight time. That is, fodar's data acquisition rate is  
481 over 100x higher than lidar (eg, 20-30 megapixels per second compared to 200-300 kHz)  
482 and this results in lower GSDs for the same flying heights and swath widths. In addition  
483 to having better precision than lidar, we find photogrammetry much more useful  
484 scientifically due to the creation of a perfectly co-registered orthoimage. Using this  
485 image, we can, for example, easily distinguish snow from rock (important for snow-free  
486 assessments of vertical accuracy, or distinguishing landslides from avalanches),  
487 determine snow lines on the glacier (important for estimating the density component of  
488 volume change), or distinguish vegetation types (important for estimating the  
489 compressibility of vegetation due to snow compaction).

490

491 The potential value of fodar to earth sciences is difficult to overestimate. The impacts of  
492 modern climate change on the Arctic landscape are profound, yet nearly impossible to  
493 grasp without a means for affordable time-series of landscape-scale measurements of  
494 topography with centimeter resolution. Though our main usage relates to climate change,  
495 there are many other changes occurring globally that can now be measured with  
496 improved accuracy and interpretative ability for the benefit of society, such as  
497 measurement of snow packs in mountain environment for water resource planning,  
498 measurement of avalanche danger, or measurement of coastal erosion. Given that we can  
499 now not only measure topographic change as accurately from the air than we can from  
500 the ground but do so economically over much larger spatial scales, the design, accuracy,  
501 and sustainability of our field research programs and operational monitoring efforts can  
502 be improved tremendously. In one way or another, landscape change is a driver or  
503 response in nearly every physical and ecological study of our planet, and thus we believe  
504 that this technology will have a major impact on our understanding of these dynamics.

505

506

507 **6. Conclusions**

508

509 Here we have demonstrated a new airborne photogrammetric method that is capable of  
510 measuring mountain peaks with an accuracy and precision of better than +/- 20 cm at  
511 95% RMSE. We used this method to measure the heights of the five tallest mountains in  
512 the US Arctic, which in order are: Mt Isto, Mt Hubley, Mt Chamberlin, Mt Michelson,  
513 and an unnamed peak we refer to as Mt Okpilak. From these results and our substantial  
514 prior work in flat and moderate terrain (Gibbs et al., 2015;Kinsman et al., 2015;Nolan et  
515 al., 2015; [Overbeck et al., 2016](#)), we conclude that this photogrammetric method, fodar,  
516 works without reservation to measure ground surface elevation in all terrain types at  
517 roughly the same accuracies and precision. The implications of this are manifold – we  
518 now have the capability to measure topographic change on the centimeter to decimeter  
519 level in flat or mountainous regions using an airborne tool that requires no ground control  
520 and is more than 10x less expensive than the current state-of-the-art.

521

522

523

524 **Author Contributions**

525

526 Nolan led all aspects of technique development, fodar acquisitions, data processing, and  
527 data analysis. DesLauriers led all aspects of the climbing expeditions and their GPS  
528 measurements.

529

530

531

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544

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649

650

651 **Table 1.** Elevations of the 5 tallest peaks in the US Arctic. USGS peak elevations in feet  
652 are taken directly from labels on the printed map sheets, except for Mt Okpilak at  
653 1:63,360 which was interpolated from the contours surroundin the peak; Mt Okpilak is  
654 our unofficial name for that unnamed peak. Fodar data were processed in WGS84 for  
655 comparison with ground control; as described in the text, we selected one of these  
656 measurements (bold) for the final value, which was converted to NAD83 using  
657 GEOID12A and presented in column 6, with its geographic coordinate shown in column  
658 7.  
659  
660

	<b>USGS 1:63,360 (NGVD29)</b>	<b>USGS 1:250,000 (NGVD29)</b>	<b>2011 Lidar (WGS84)</b>	<b>Fodar (WGS84)</b>	<b>Fodar (NAVD88 Geoid 12A)</b>	<b>Latitude Longitude</b>
<b>Mt Isto</b>	2735.6 m (8975')	2758.4 m (9050')	2739.63 m	2739.59 m (24 March 14) <b>2739.40 m (22 April 14)</b> 2738.75 m (6 July 15)	<b>2736.0 m</b> (8976.4')	69.202506N 143.800941W
<b>Mt Hubley</b>	2717.3 m (8915')	2717.3 m (8915')	2720.64 m	<b>2720.97 m (13 June 14)</b> 2720.55 (6 July 14)	<b>2718.0 m</b> (8917.3')	69.276101N 143.799277W
<b>Mt Chamberlin</b>	2749.3 m (9020')	2749.3 m (9020')	2717.29 m	2716.51 m (24 March 14) <b>2716.59 m (22 April 14)</b> 2717.56 (23 April 15)	<b>2712.7 m</b> (8900.0')	69.277673N 144.911625W
<b>Mt Michelson</b>	2699.0 m (8855')	2699.0 m (8855')	2702.29 m	2701.30 m (30 June 14) <b>2701.69 m (6 July 15)</b>	<b>2698.5 m</b> (8853.3')	69.307756N 144.268992W
<b>Mt Okpilak</b>	2697.5 m (8850')	2670.0 m (8760')	2699.84 m	2699.95 m (23 April 15) <b>2699.80 m (6 July 15)</b>	<b>2695.3 m</b> (8842.8')	69.14572N 144.041046W

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664

665 **Figure Captions**

666

667 Figure 1. The five tallest peaks in the US Arctic are located within about 40 km of each  
668 other in north-eastern Alaska, within the Arctic National Wildlife Refuge.

669

670 Figure 2. Mt Isto, currently the tallest peak in the US Arctic, shown as a 3D visualization  
671 of our fodar data. Yellow dots indicate position of some of the ground control collected  
672 (yellow) used for validation, spanning ~1000 m. Closely spaced points are on the climb  
673 up, widely spaced points are on the ski down.

674

675 Figure 3. Precision assessments. A) Difference in elevation between March and April  
676 2014 acquisitions at Mt Chamberlin, shown as a top view with slight sun shading to  
677 highlight underlying topography. Color represents change (-50 cm to + 50 cm). The  
678 consistency of color shift between mountain faces is not due to a spatial misalignment of  
679 the data but rather to substantial, real changes that are dependent on aspect, as described  
680 in the text. Such real changes confound our repeatability estimates which assume no  
681 change on the ground. B) 3D oblique view of domain in A, draped with orthoimage from  
682 April, indicating the locations of snow-filled gullies on the southeast face. Profile line is  
683 shown as both straight line and terrain hugging and is about 1000 m long, crossing five  
684 gullies. C) Profile of difference (that is, data in A), revealing patterns of snow  
685 redistribution. Much of the snow that had recently fallen in March avalanched out of the  
686 gullies, leaving them up to 6 m deeper in April. Note that the ridges in between show  
687 little to no change, qualitatively indicating the high quality of the data and the technique's  
688 suitability for measurement of snow depth in steep terrain. D) Difference in elevation  
689 between March and April 2014 acquisitions at Mt Isto, with same coloration as A.  
690 Again, there is substantial real change between acquisitions, but less than in A.  
691 Histogram of differences of elevations calculated from boxes in A (E) and D (F) over  
692 smoother glacier surfaces. Both are roughly gaussian with 95% of points within +/- 38  
693 cm and +/- 20 cm. Inspection of orthoimages here reveals that real changes are still  
694 occurring on the glaciers in these smaller domains, but there are no large locations that  
695 have less change, so these estimates of precision are conservative as they are confounded  
696 by real change.

697

698 Figure 4. Oblique 3D visualizations using our fodar data of A) the south face of Mt  
699 Hubley with Schwanda Glacier in foreground, B) the south face of Mt Michelson  
700 descending to Esetuk Glacier, and C) the south and east faces of Mt Okpilak. Red  
701 markers indicate peak location. Note the slight noise seen at the shadow on the right of  
702 B; this was common at the edge of dark, fast-moving shadows. Despite the range of  
703 exposure value and contrast, this technique is able to map nearly all terrain, and the  
704 orthoimage eliminates guesswork when it comes to distinguishing rock and ice, and even  
705 ice and snow.

706

707 Figure 5. Temporal dynamics of cornices near the peak of Mt Isto (red pushpin). Shown  
708 here are 3D oblique visualizations of fodar from A) 6 July 15 and B) a difference image  
709 between 6 July 2015 and 22 April 14. The consistency of the greens and yellows on  
710 either side of the ridge in B indicates that there are no spatial misalignments of the two

711 data sets, and clearly reveals the differences in cornice size between acquisition dates.  
712 The profile comparison (C ) confirms visual inspection of the ridge line – a cornice about  
713 5 m wide and 10 m high formed, perhaps during a single storm. With these tools we can  
714 clearly measure subtle topographic changes in steep mountain environments that would  
715 otherwise be impossible to detect or measure, and comparisons like these show change  
716 down to the centimeter scale. Dynamics can also be addressed, as the crevassing behind  
717 these new cornices (A) indicates the existing ones are ready to spall and the blue colors  
718 (B) indicate that many already have.

719

720 Figure 6. Evidence for recent ice and rock loss from Mt Chamberlin. A) The northwest  
721 face shows massive, catastrophic loss of ice. B) The southeast face is now completely  
722 free of ice, and rock debris piles have accumulated at its base. C) Looking down from  
723 the peak to towards the southeast face reveals a curious notch in its shape, suggesting  
724 rock and ice avalanches may have occurred here in the past. The large map discrepancy  
725 along with these clues suggests that Mt Chamberlin may have been the 1<sup>st</sup> or 2<sup>nd</sup> tallest  
726 mountain in the US Arctic at one time.

727

728 Figure 7. The peak of My Hubley (A) is on a rock arête along a ridge that is too steep  
729 and narrow to support large glaciers. Mt Michelson (B) and Mt Okpilak (C) are only a  
730 few meters apart in height and both are covered by cornices several meters thick. As  
731 climate continues to warm, the ranking of these two may yet change. The location of Mt  
732 Okpilak’s “peak” moved more than 15 m between 2014 and 2015, as it lies on a nearly  
733 flat ridge, but its elevation changed by less than 20 cm.

734

735 Figure 8. Spatially coherent grooves seen in a 22 April 2014 – 6 July 15 difference image  
736 on Mt Isto (A, arrows) are clearly revealed in the July orthoimage (B) to be caused from a  
737 small avalanche. As seen in C, left arrow points to a ~20 cm chute and right arrow points  
738 to a ~20 cm ridge between chutes on this ~40 degree slope. Resolving 20 cm features  
739 like this requires centimeter-scale signal detection, despite that the noise is on the 5-20  
740 cm level. This snow fell recently and is over a meter thicker than in 2014, located just  
741 downhill from the 5-10 m cornices found in Figure 5. D) In the deepest shadows of this  
742 fresh snow, the noise level increased ~ +/- 1 m (up to 10 m, not shown), but these regions  
743 were quite small compared to the whole. Note that the 2014 data (red line) shows no  
744 such noise.

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