Response to Reviewer:

We thank the reviewer again for the thoughtful review. We have addressed the final minor revisions suggested as follows:

1. Error Analysis: The range bin uncertainty has been added in. In section 4.2 this was added, “The second source of error occurs during manual adjustment of the picked layers (Section 4.3.4) and is estimated to be a maximum of ±3 range bins, or ~8 cm. Given the relative standard deviation in accumulation rate, the range bin error contributes a mean uncertainty 7% with a range of 4% to 24%. Lower accumulation rates have a higher relative error from layer picking.” Using the 7% as an uncorrelated error the overall average error is estimated at a maximum of 14% and has been adjusted in the paper accordingly. This was also added to Section 4.2, “To calculate the total uncertainty on the radar-derived accumulation rate, the largest error is assumed for density (12%) and age (10%) and the error for the mean accumulation rate is assumed for layer picking (7%). … Assuming uncorrelated and normally distributed errors between density, age and layer picking the mean accumulation-rate uncertainty is 14%, with a range of 13% for the highest accumulation rates and 27% for the lowest accumulation rates. This relative uncertainty is similar to previous studies by Medley et al. (2013) and Das et al. (2015) for radar-derived accumulation rates.” We also note that our assumed pick uncertainty is 3 times that of Medley et al., 2013 for snow radar so it is a maximum assumed error. We changed the text to say that the errors sources are approximately equal. See point 3 for more details.

2. Age of First layer: We increased the age uncertainty to 10% based on the maximum error for +/- 1 month on the first 10 month layer based on reviewer’s previous comments and held this constant for all years. We feel this is an adequate and justified uncertainty. Again Medley et al. 2013 established an error of +/- 1 month (8.3%) and our assumed error is higher than this for all layers except the surface layer. The model outputs for accumulation were processed for monthly accumulation rates and we choose as the reviewer points out the mean date of 30 April to compare to the MAR model. We clarify this point in the uncertainties description so it is clearly stated in the paper as follows in Section 4.2, “the surface is assumed to be 30 April to align with the modeled accumulation rate which was processed to monthly values.” We also add further description in the discussion as suggested and detailed in point 3 below.

3. Uncertainties: We respectfully disagree with the reviewer. Radar-derived accumulation rates are inherently valuable to compare to models and this paper presents a fair comparison. The snow radar dataset will grow with each campaign and this paper will prove the feasibility of using the dataset for deriving accumulation rates. This topic is particularly timely because it highlights the problems and uncertainties in accumulation rates over Greenland. We have identified and clarified all error sources within the paper and we have been conservative. We also note that radar derived accumulation rates are proving very useful for comparing against models and reference Medley et al., 2013, Das et al., 2015 and Overly et al., 2015.

We are committed to making sure our data is clearly documented as the reviewer suggests. As suggested we have added the following paragraph to discussion, Section 6, “
Finally, the uncertainties in the radar-derived accumulation rate are approximately equally distributed between the layer picking, age and density. However, the layer picking is likely overestimated and in most cases likely much lower, leaving age and density uncertainties nearly equal (Medley et al., 2013). Age uncertainties could be better constrained with a better understanding of the timing of density peaks across the ice sheet. Our assumption that the surface date is 30 April could be adjusted to the flight date if the modeled accumulation rates were reprocessed to daily values.

With respect to density uncertainty, we assumed a constant and uniform density in the top meter of snow/firn as modeled outputs did not match measured values (Figure 2). This assumption could lead to spatial bias in our analysis if regional density deviates significantly from the mean, though existing measurements do not show any clear evidence of such spatial bias. Spatially distributed density measurements and improved density models spanning the entire firn column are required to take full advantage of the layering detected by near-surface radars and to reduce errors in radar-derived accumulation rates. The current sampling of in situ measurements has large spatial gaps over the southwestern, north and northeastern GrIS and the majority of the measurements are located in the upper-percolation and dry-snow zones (Figure 1). To further constrain and improve the density models required for radar-derived accumulation rates, these gaps must be filled. Additionally, the Snow Radar’s signal penetration around the perimeter of the GrIS is relatively shallow, resolving 1 to 3 annual layers only, with the majority of detected layers in the top meter of snow/firn (Figures 6 and 7). Accumulation rates are calculated using measurement averages in this section of the snow/firn column, likely causing less error than the MAR-modeled density. Improvement to modeled near-surface density should be considered for improved Snow Radar analysis."

As to the reviewer’s comments on if the model evaluation falls within the measurement error. We feel with is clearly evident in Figures 4, 5 and 10 that the regions we discuss, Southeast Greenland and Northwest in one year, are clearly being over/underestimated by more than 14% of the derived accumulation rate. The figures show over/underestimates by 0.25 to 1 m w.e. in those regions that get between 0.5 to 2 m w.e. per year. We do not address this directly in the text as it evident in the figures and additionally because we have no errors assessed on the model values to compare with.

We addressed all specific edits as suggested by the reviewer that can be seen in the Track Changes version of this article. The density equations were reevaluated by coauthors Alexander
and Fettweis and are correct in this version. The Brun et al reference for compaction of layers is described in Burn et al, 1989.

We have read through the article again adjusting minor grammatical errors that can be seen in Track Changes.

Annual Greenland accumulation rates (2009-2012) from airborne Snow Radar


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Abstract

Contemporary climate warming over the Arctic is accelerating mass loss from the Greenland Ice Sheet through increasing surface melt, emphasizing the need to closely monitor its surface mass balance in order to improve sea-level rise predictions. Snow accumulation is
the largest component of the ice sheet’s surface mass balance, but in situ observations thereof are inherently sparse and models are difficult to evaluate at large scales. Here, we quantify recent Greenland accumulation rates using ultra-wideband (2–6.5 GHz) airborne Snow Radar data collected as part of NASA’s Operation IceBridge between 2009 and 2012. We use a semi-automated method to trace the observed radiostratigraphy and then derive annual-net accumulation rates for 2009 to 2012. The uncertainty in these radar-derived accumulation rates is up to 142%, attributed mostly to uncertainty in the snow/firn density profile. A comparison of the radar-derived accumulation rates and contemporaneous ice cores shows that Snow Radar captures both the annual and long-term mean accumulation rate accurately. A comparison with outputs from a regional climate model (MAR) shows that, this model matches radar-derived accumulation rates in the ice sheet interior but overestimates over southeastern Greenland. Our results demonstrate that Snow Radar can efficiently and accurately map patterns of snow accumulation across an ice sheet, and that it is valuable for evaluating the accuracy of surface mass balance models.

1 Introduction

Contemporary climate warming over the Greenland Ice Sheet (GrIS) has accelerated its mass loss, nearly quadrupling from ~55 Gt a⁻¹ between 1993-99 (Krabill et al. 2004) to ~210 Gt a⁻¹, equivalent to ~0.6 mm a⁻¹ of sea level rise, between 2003-08 (Shepherd et al. 2012). As GrIS mass loss has accelerated, a fundamental change in the dominate mass loss process has occurred (e.g. Tedesco et al., 2015). It switched from ice dynamics to surface mass balance (SMB) processes, which include accumulation and runoff (van den Broeke, 2009; Enderlin et al., 2014). This recent shift emphasizes the need to monitor SMB which, over most of the GrIS, is dominated by net accumulation.

Here, we use the complete set of airborne Snow Radar data collected by NASA’s Operation IceBridge (OIB) over the GrIS from 2009 to 2012 to produce net-annual accumulation rates, hereafter called accumulation rates for simplicity, along those flightlines. The radar-derived accumulation rates are compared to both in situ data and model outputs from the Modèle Atmosphérique Régional (MAR).

2 Background

In situ accumulation-rate measurements are limited in number by the time and cost of acquiring ice cores, digging snow pits or monitoring stake measurements across large sectors of the ice sheet. Only two major accumulation-rate measurement campaigns have been
undertaken across the GrIS. The first in the 1950’s when the US Army collected pit data along long traverse routes (Benson, 1962), and the second in the 1990’s when the Program on Arctic and Regional Climate Assessment (PARCA) collected an extensively distributed set of ice cores (e.g. Mosley-Thompson et al., 2001). A recent traverse and study by Hawley et al. (2014) reports a 10% increase in accumulation rate since the 1950’s and highlights the need to monitor how Greenland precipitation is evolving in the midst of ongoing climate change. Although many other accumulation-rate measurements exist, they are more limited in either space or time (e.g. Dibb and Fahnstock, 2004; Hawley et al. 2014).

To date there is no annually resolved satellite-retrieval algorithm for accumulation rate across ice sheets. Hence, the two primary methods used to generate large-scale (hundreds of km) accumulation-rate patterns are model predictions and radar-derived accumulation rates (Koenig et al., 2015). High resolution, near-surface radar data have shown good fidelity at mapping spatial patterns of accumulation over ice sheets at decadal and annual resolutions from both airborne and ground-based radars (Kanagaratnam et al., 2001; 2004; Spikes et al., 2004; Arcone et al., 2005; Anshütz et al., 2008; Müller et al., 2010; Medley et al., 2013; Hawley et al., 2006; 2014; de la Peña et al., 2010; Miège et al., 2013). Radars detect the lateral persistence of isochronal layers within the firm. When these layers are either 1) dated in conjunction with ice cores or 2) annually resolved from the surface, they can be used to determine along-track accumulation rates.

Early studies by Spikes et al. (2004) in Antarctica and Kanagaratnam et al., (2001 and 2004) in Greenland used high/very high-frequency (100 to 1000 MHz) ground-based and airborne radars, with vertical resolutions of ~30 cm, to measure decadal-scale accumulation rates between dated ice cores. These high/very high-frequency radars can penetrate hundreds of meters in the dry-snow zone and tens of meters in the ablation zone (Kanagaratnam et al., 2004). Subsequent studies utilized the larger bandwidths of ultra/super-high frequency (2 to 20 GHz), frequency-modulated, continuous wave (FMCW) radars with centimeter-scale vertical resolutions capable of mapping annual layers within ice sheets (e.g. Legarsky 1999; Marshall and Koh, 2008; Medley et al., 2013). Ultra/super-high frequency radars can penetrate tens of meters in the dry-snow zone and meters in the ablation zone. Legarsky (1999) was among the first to show that such radars could image annual layers, and Hawley et al. (2006) further demonstrated that a 13.2 GHz (Ku-band) airborne radar imaged annual layers in the dry-snow zone of the GrIS to depths of up to 12 m.
Most previous studies used radar data that overlapped spatially with ice cores or snow pits for both dating layers and density information. Medley et al., (2013) and Das et al. (2015) showed that accumulation rates could also be derived using density from a regional ice core ensemble. Density end-members are used to derive uncertainty limits, and the derived regional density profile is sufficient for radar studies of accumulation and SMB (Das et al. 2015). Additionally, Medley et al. (2013) showed that Snow Radar is capable of resolving annual layering in high accumulation regions where such layers were well preserved. Therefore, it was possible to date the layers by simply counting from the surface downwards.

Regional Climate Models, General Circulation Models (RCMs and GCMs, respectively) and reanalysis products provide the only spatially and temporally extensive estimates of accumulation-rate fields at ice-sheet scales (e.g. Burgess et al., 2010; Hanna et al., 2011; Ettema et al., 2009; Fettweis, 2007; Cullather et al., 2014). In a comprehensive model intercomparison study, Vernon et al. (2013) found that modelled accumulation rates had the least spread across the RCM’s considered, but still had a ~20% variance. Chen et al. (2011) found the range in mean accumulation rate across the GrIS between five reanalysis models to be ~15 to 30 cm a⁻¹, while Cullather and Bosilovich (2011) found the range in mean accumulation rate across the GrIS between reanalysis data and RCM’s to be ~34 to 42 cm a⁻¹. While these models continue to improve, there is clearly a continuing need for large-scale accumulation-rate measurements to evaluate their outputs.

3 Data, instruments and model description

3.1 Snow radar and data

Annual layers in the GrIS snow/firm were mapped using the University of Kansas’ Center for Remote Sensing of Ice Sheets (CReSIS) ultra-wideband Snow Radar during OIB Arctic Campaigns from 2009 through 2012 (Leuschen, 2014). The Snow Radar operates over the frequency range from ~2 to 6.5 GHz (Panzer et al., 2013; Rodriguez-Morales et al., 2014). The Snow Radar uses an FMCW design to provide a vertical-range resolution of ~4 cm in
snow/firn, capable of resolving annual layering, where preserved, to tens of meters in depth (Medley et al., 2013). OIB flights operate multiple instruments, including lidars and radars, spanning a range of frequencies (Koenig et al., 2010; Rodriguez-Morales et al., 2014). The Snow Radar was chosen for this study because its vertical resolution and penetration depth is optimized for detecting annual layers from the surface of the ice sheet. It is noted, however, that the CReSIS Accumulation Radar and Multichannel Coherent Radar Depth Sounder (MCoRDS) radar are also capable of detecting accumulation on decadal to multi-millennial time scales, respectively, using dated isochrones (e.g. Miège et al., 2013; MacGregor et al., 2016).

3.2 Modelled accumulation rates and density

Accumulation rate and snow/firn density profiles were derived from the MAR RCM (v3.5.2; X. Fettweis, pers. comm., 2015). MAR is a coupled surface-atmosphere model that simulates fluxes of mass and energy in the atmosphere and between the atmosphere and the surface in three dimensions, and is forced at the lateral boundaries with climate reanalysis outputs (Gallée, 1997; Gallée and Schayes, 1994; Lefebre et al., 2003). It incorporates the atmospheric model of Gallée and Schayes (1994), and the Soil Ice Snow Vegetation Atmosphere Transfer scheme (SISVAT) land surface model, which includes the multi-layer Crocus snow model of Brun et al. (1992). The MAR v3.5.2 simulation used here utilizes outputs from the European Center for Medium Range Weather Forecasting (ECMWF) ERA-Interim global atmospheric reanalysis (Dee et al., 2011) at the lateral boundaries, with a horizontal resolution of 25 km (Dee et al., 2011). Additional details are described by Fettweis (2007), with updates described by Fettweis et al. (2011; 2013) and Alexander et al. (2014). MAR has been validated with in situ data and remote sensing data over the GrIS, including data from weather stations (e.g. Lefebre et al., 2003; Fettweis et al., 2011), in situ and remotely sensed albedo data (Alexander et al., 2014), and ice-core accumulation-rates (Colgan et al., 2015), and it has been used to model both past and future SMB (Fettweis et al., 2005; 2013). We use accumulation rates and density profiles simulated by MAR for the period during which the radar data were collected (2009 to 2012).

In MAR, the initial falling snow density ($\rho_{s,0}$) is parameterized as a function of surface air temperature—the temperature in the first model layer ($T_m$) in °C (at roughly 3 m above the
surface) and 10-meter windspeed \( V \) in m s\(^{-1}\). The parameterization differs depending on atmospheric temperature as follows:

If \( T_{air} \) is greater than -5°C:

\[
\rho_{s,0} = \max(30,109 + 6T_{air} + 26\sqrt{V}, \rho_{s,0} = \max(200,109 + 6T_{air} + 26\sqrt{V})
\]

If \( T_{air} \) is less than -5°C and \( V > 6 \text{ m s}^{-1} \), the parameterization of Kotlyakov (1961) is used instead:

\[
\rho_{s,0} = \max(200,104\sqrt{V})
\]

If \( V < 6 \text{ m s}^{-1} \) the initial snow density is set to the fixed value of 200 kg m\(^{-3}\).

After falling to the surface, snow falls to the surface, snow densification, compaction in MAR is described according to the scheme of Brun et al. (1989) where the densification rate compaction of a layer \( \frac{dz}{dt} \) at depth \( z \) of thickness \( \delta z \) is given by

\[
\frac{dz}{dt} = \frac{-\sigma}{C\rho_d \rho_0} \cdot 0.252 \exp((-0.02221\rho - 40.1)|z|),
\]

where \( \rho \) is the dry snow density (kg cm\(^{-3}\)), \( T_s \) is the snow temperature (°C at depth \( z \)) of the layer, \( \sigma \) is the vertical stress from the snow above (kg m\(^{-1}\)s\(^{-1}\)) and \( C \) is a function of snow grain size and snowpack liquid water content.

### 3.3 In situ density and accumulation-rate data

The SUrface Mass balance and snow depth on sea ice working group (SUMup) dataset (July 2015 release) compiles publically available accumulation-rate, snow depth and density measurements over both sea ice and ice sheets (Koenig et al., 2012). We use two subsets of these data. First, to characterize density across the GrIS, we extract the snow/firn density measurements ranging in depth from the snow surface to 15 m (the depth to which MAR predicts firn density), which contains over 1500 measurements from snow pits and cores at 62 sites. At each site, the number of measurements ranges in number between 8 and 170 and maximum depths range from 1 to 15 m. (Koenig et al., 2015; Koenig et al., 2014; Miège et al., 2013; Mosley-Thompson et al., 2001; Hawley et al., 2014; Baker 2015) (Figure 1). Second, to
compare radar-derived and in situ accumulation rates, we consider only accumulation-rate
measurements within 5 km of OIB Snow Radar data, a criterion that includes 11 cores from the
SUMup dataset (Mosley-Thompson et al., 2001). To expand this comparison, an additional
dataset of 71 cores was included (J. McConnell, pers. comm., 2015) was included, providing
23 additional cores within 5 km of OIB Snow Radar data (Figure 1).

4 Methods

4.1 Determining the density profile and uncertainties

Because we seek to derive accumulation rates from near-surface radars across large
portions of the ice sheet, we require firm density profiles that cover the entire GrIS. Modelled
snow/firm density profiles from MAR were investigated for use. However, a preliminary
comparison of the SUMup-measured density profiles to MAR-estimated density profiles
showed that MAR simulated density values in the top 1 m of snow/firm were significantly lower
\( 0.280 \pm 0.040 \text{ g cm}^{-3} \) than observed \( 0.338 \pm 0.039 \text{ g cm}^{-3} \) (Figure 2). The comparison of
measured and modeled density was simultaneous in time, meaning that the MAR
density profile output on the day of the measurement was used in this comparison. We consider
it beyond the scope of this study to investigate and explain why MAR underestimates near-
surface density. Therefore, here we assume that the firm density in the top 1 m is \( 0.338 \text{ g cm}^{-3} \). Below 1 m, the model and observed densities are similar (4% mean difference with the model
generally overestimating measured density slightly), so the spatially-varying modelled density
profiles are used for April 30 of each year. Hence, a hybrid measured-modelled density profile
is used to determine accumulation rates from the snow radar data (Figure 2).

Our assigned uncertainty in the top meter is assigned by the ±1σ variation relative
standard deviation in observed density (12%) which we assume is due to the natural variability
in surface density. This natural variation, however, represents a smaller assumed uncertainty
than the mean difference between the modelled and observed values within the top meter (16%).

4.2 Deriving accumulation rates from Snow Radar and uncertainties

The radar travel time is converted to depth \( z \) using the snow/firm density profile and the
dielectric mixing model of Looyenga (1965). Errors in radar-derived depth come from two
primary sources: 1) the dielectric mixing model chosen and 2) layer picking. The choice of the
dielectric mixing model maximizes potential error at a density of ~0.300 g cm\(^{-3}\). The maximum possible difference in depth over 15 m is 3% assuming a constant density of 0.320 g cm\(^{-3}\) and <1% assuming a constant density of 0.600 g cm\(^{-3}\) (Wiesmann and Matzler, 1999; Gubler and Hiller, 1984; Schneebecher et al., 1998; Looyenga, 1965; Tiuri et al., 1984). The second source of error occurs during manual adjustment of the picked layers (Section 4.3.4) and is estimated to be a maximum of ±3 range bins, or ~8 cm. Given the relative standard deviation in accumulation rate, the range bin error contributes a mean uncertainty of 7% with a range of 4% to 24%. Lower accumulation rates have a higher relative error from layer picking.

The \textit{water-equivalent} accumulation rate \(\dot{b} \text{ m w.e. a}^{-1}\) at along-track location \(x\) is derived by:

\[
\dot{b}(x) = \frac{z(x)\rho(x)}{\rho_w \left( \frac{\epsilon'_i}{\rho_i} \right)^{1/3} + 1} \quad (1)
\]

Where \(\dot{b}\) is water equivalent accumulation rate in m w.e. a\(^{-1}\), \(z\) is the depth of layer in m, \(\rho\) is cumulative average snow/firn density to depth \(z\) in kg m\(^{-3}\). Hence, the numerator is the cumulative mass in kg m\(^{-2}\) to depth \(z\), \(a\) is age of the layer in years from the date of radar data collection and \(\rho_w\) is the density of water in kg m\(^{-3}\) (e.g. Medley et al., 2013; Das et al., 2015).

Depth \(z\) is calculated using the radar two-way travel time (TWT), the snow/firn density \(\rho\) and the Looyenga (1965) dielectric mixing relationship as follows:

\[
z = \frac{TWT(x)\rho(x)c}{z \left( \frac{\rho_w \left( \frac{\epsilon'_i}{\rho_i} \right)^{1/3} + 1} {\rho_i} \right)^{3/2}} \quad (2)
\]

Where \(TWT\) is the travel time to the dated layer in sec, \(c\) is the speed of light in m s\(^{-1}\), \(\rho_i\) is ice density in kg m\(^{-3}\) and \(\epsilon'_i\) is the dielectric permittivity of pure ice. Combining these two equations gives:

\[
\dot{b}(x) = \frac{TWT(x)\rho(x)c}{z \left( \frac{\rho_w \left( \frac{\epsilon'_i}{\rho_i} \right)^{1/3} + 1} {\rho_i} \right)^{3/2}} \quad (3)
\]

The cumulative mean snow/firn density \(\bar{\rho}\) is determined by the density profile described in Section 4.1. The layers are picked in the radar data using a semi-automated approach described in Section 4.3.

Layer ages are determined by assuming spatially continuous layers are annually resolved and dated accordingly from the year the radar data were collected. The radar data were collected during springtime (April-May) and the surface is assumed to be 30 April to align with the
modeled accumulation rate which was processed to monthly values. The Subsurface picked layers at depth are assumed to be 1 July ± 1 month as follows, therefore, so the first layer represents 10 months and each subsequent layer is 12 months. Peaks in radar reflectivity are, assuming ice with no impurities, caused by the largest change in snow density. In the ablation and percolation zone, the peak in density difference occurs in the summer between the snow layer and ice or the snow/firn layer and the high-density melt/crust layer, respectively (e.g. Nghiem et al., 2005). In the dry snow zone, the peak density contrast also occurs in the summer between the summer hoar layer and the denser snow/firn layer (e.g. Alley et al., 1990). While melt/crust and hoar layers can form at other times, it is assumed they will be smaller, density contrasts and, therefore, cause a smaller radar reflection than the dominate layers which occur near 1 July.

To calculate the total uncertainty on the radar-derived accumulation rate, the the maximum error is largest error is assumed for both density (12%) and age (10%) and the error for the mean accumulation rate is assumed for layer picking (7%), in the first layer and 8% in subsequent layers. Equation 3 shows that the density profile is used for calculating both depth and water equivalent. The derivative of Equation 3 determines the correlated error between depth and density. Assuming uncorrelated and normally distributed errors between density and age and layer picking, the maximum mean accumulation-rate uncertainty is 142%, with a range of 13% for the highest accumulation rates and 27% for the lowest accumulation rates, with uncertainty in the density profile in the top meter of firm being the largest contributor. This relative uncertainty is similar to previous studies by Medley et al. (2013) and Das et al. (2015) for radar-derived accumulation rates.

4.3 Semi-Automated Radar Layer Picker

A semi-automated layer detection algorithm is developed to process the large amounts of OIB Snow Radar data (>10^4 km year^-1), analogous to the challenges faced by MacGregor et al. (2015) for analysis of very high frequency radar sounder data. While a fully automated method is ultimately desirable, we have found that it is necessary to manually check every automated pick, making adjustments as needed by an experienced analyst, to distinguish between spatially discontinuous radar reflections, caused by the natural heterogeneity of firm microstructure, and spatially consistent annual layers. Our algorithm processes the OIB Snow Radar data in four steps outlined below.
4.3.1 Surface Alignment
The snow surface is detected by a threshold, set to four times the mean radar return from air, which is assumed to be the radar background noise level. A median filter is applied vertically to each radar trace to minimize noise. Any surface detection that is displaced by greater than 10 range bins (~25 cm) from its adjacent traces is not used and that entire vertical trace is ignored in subsequent analysis. Data arrays are then aligned to the surface and truncated above and below the surface (200 and 800 range bins, respectively), equivalent to ~25 m into the snow/firm, to reduce data volumes. Layer depths are measured relative to the snow surface. The radar data are then horizontally averaged (stacked) 10 times to an along-track spacing of ~10 m (2009 and 2010) and ~50 m (2011 and 2012), and split into equally sized sections of 2000 traces per radargram for easier processing. The change in along-track spacing between 2009–2010 and 2011–2012 is due to additional incoherent averaging introduced in 2011.

4.3.2 Layer Detection
The algorithm takes advantage of the difference between high-frequency and low-frequency spatial variability in the traveltime/depth domain to identify peaks in returned power in the radar data. Such peaks are formed by the stratified accumulation layers of interest in this study, and they form over small spatial scales, equivalent to high frequency, in the traveltime/depth domain. Our peak detection process is thus a type of high-pass filter, resulting in the set of disjointed points detected at radar reflection peaks in the time domain and in adjacent traces along the flight path. These points are connected into continuous layer segments using the half-maximum width of each peak’s waveform (Figure 3, locations of radargrams shown in Figure 1).

4.3.3 Layer indexing
Each along-track detected layer is indexed, with both a number and the corresponding year, counting down from the surface detection (Figure 3). This indexing begins with the segmentation of the layers, so that each layer is uniquely identified with a layer number. The peak points within each segment are connected by spline fitting, resulting in a set of sharply defined along-track layers at different depths (Figure 3). These layers represent 1 July in the appropriate year counting from the surface and the year collected.
4.3.4 Manual adjustment with the Layer Editor

A graphical user interface (GUI) was developed to verify automated layer detections by displaying the Snow-Radar radargram and the resulting automated-layer detections. An analyst uses the GUI to quickly visually compare the picked layers and the radargram. The GUI application allows for layer editing as needed including tools for layers, or parts of layers to be added, deleted, gap-filled, and re-indexed. The GUI accelerates layer picking by providing the ability to scroll through all the radargrams and picked layers, including the previous and subsequent along-track data, to detect errors. Scrolling allows for spatially continuous layers, which may not be datable at all locations, to be propagated and dated from a location where annually resolved layers are evident from the surface. Error statistics for the automatic algorithm were not kept, but depend generally on the quality of the radar data, influenced by both radar and aircraft operations, and the regional characteristics of the snow/firm microstructure, which can either preserve or erode layering.

5 Results

5.1 Radar-derived accumulation rates

Annual radar-derived accumulation rates and their uncertainties were calculated for all 2009–2012 OIB radar data that contained detected layers (Figure 4). The increase in coverage from 2009 to 2012 is related to an increasing number of OIB flights over the GrIS and adjustments to the Snow Radar antenna and operations that improved overall data quality. These accumulation-rate patterns are consistent with observed and modelled large-scale spatial patterns for the GrIS: high accumulation rates in the southeast-coastal sector and lower accumulation rates in the northeast (Figure 5). Year-to-year variability in the accumulation rate is also evident, even at the ice-sheet scale, e.g., in the southeast accumulation rates were lower in 2010 than in 2011.

The radar-derived accumulation rate in Figure 4 represents only the first layer detected by the Snow Radar, or approximately the annual accumulation rate from the year prior to data collection. For simplicity, we refer to this quantity as the annual accumulation rate, but we caution that it does not strictly represent the calendar year. The values shown in Figure 4 represent only 10 months of accumulation, based on our assumption that the radar layers date to 1 July (Section 4.2) and that the data collection date is 30 April for all OIB data, which may differ from the actual flight date by up to a month. When comparing the first layer of radar-
derived accumulation to modelled estimates from MAR (Figure 5) or other accumulation measurements, these timing differences must be considered. Although the first layer represents only a partial year, all deeper layers represent a full year, from 1 July to 30 June. We simultaneously compare the time represented by the layer to MAR estimates of accumulation.

Figure 6 shows the number of detected layers, or previous years, discernable in the OIB radar data. For the majority of the GrIS, 1 to 3 annual layers are discernable. OIB flightlines are clustered in the ablation/percolation zones of the GrIS, where radar penetration depths are reduced by the increased density, englacial water and layering structure of the firn column (Figure 3). In the GrIS interior, where dry snow conditions allow deeper radar penetration, annual layering going back over two decades is detectable (Figure 3). Figure 7 shows a histogram of depths for the first layer detected for years 2009 through 2012; 63% are within the top 1 meter of snow.

Crossover points were assessed to determine the internal consistency of the radar-derived accumulation rates (Figure 8 and 9). While no consistent spatial pattern is found in the crossover errors, the largest discrepancies were found in 2011 and 2012 in the northwest and southeast (Figure 8). Other inconsistencies are likely due to snow storms deposition occurring between flights in the southeast and incorrectly picked layers that were either sub- or multi-annual in the northwest. Figure 9 shows a scatterplot of crossover points. There are relatively few outliers, and those that are outliers are generally offset by a factor of two, suggesting an error in layer detection/dating rather than a radar-system error. Crossover differences per year, including the mean, standard deviation and maximum, are given in Table 1. These differences are comparable (mean of 0.04 m w.e. a⁻¹ or 4 range bins) to our inferred relative uncertainty of 142%, which emphasizes the overall validity of our chosen methodology.

5.2 Comparison with modelled accumulation

The along-track radar-derived accumulation rates were gridded to the MAR grid for comparison. The mean-local, radar-derived accumulation rate was used when gridding. Because OIB flightlines are not spatially homogeneous, each MAR grid cell represents a different number of radar-derived values, so grid cells are not sampled equally. With this discrepancy noted, this gridding method is still the most straightforward approach for this comparison. Figure 10 shows the difference between the radar-derived and MAR
accumulation rates. The mean difference for all years is low (0.02 m w.e. a\(^{-1}\)). Table 1 shows
the annual variability of the mean difference, which is low for every year except 2010, when
large differences are seen over the southeast coastal region of the GrIS (Figure 10).

Figure 10 shows that MAR generally predicts accumulation rates well in the GrIS interior
(consistent with the comparison with ice core estimates presented by Colgan et al., 2015), but
has larger errors around the periphery, especially in the southeast and northwest. In the
southeast, MAR generally overestimates accumulation rates, except in 2011 when there is a
mixed pattern of agreement and overestimation. Overestimated values in the southeast are not
surprising and are likely due to both the lack of previous measurements in the region to
constrain accumulation rates and the large changes in surface topography that are not resolved
by the relatively coarse model grid. This pattern of overestimation in the southeast is not
surprising and is likely due to the lack of previous measurements in the region to constrain
accumulation rates and the large changes in surface topography that are not resolved by the
relatively large grid size used in modelled estimates (Burgess et al., 2010). In 2011, the
northwest coastal region of the GrIS was well sampled by OIB and MAR underestimates
accumulation rates there. The origin of this anomaly is less clear, but may be related to forcing
at the lateral boundaries of MAR that does not capture a relatively small storm track into this
region.

Figure 10 shows a scatterplot of the radar-derived and MAR-estimated accumulation
rates. These values are not well correlated (Pearson correlation coefficient \(r^2 = 0.2\)) and have
large RMSE (0.24 m. w.e. a\(^{-1}\)), emphasizing that further improvements in accumulation-rate
modeling and measurements are needed, particularly over the southeast and northwest GrIS.

5.3 Comparison with annually resolved in situ data

Between 2009 and 2012, OIB flew within 5 km of 34 core locations but only two
locations, NEEM and Camp Century (Figure 1) were coincident in time with the layers we
detected. Each of these locations has two cores, providing annual accumulation rates and a
measure of spatial variability. Figure 12 compares the radar-derived to core measured
accumulation rates. At NEEM, the two ice cores and radar data are nearly co-located, within
0.6 km of each other. The radar-derived accumulation rates are self-consistent between 2011
and 2012 and agree well with the ice cores (root mean square error (RMSE) of 0.06 m w.e. a\(^{-1}\)). For comparison, the two NEEM cores have a RMSE of 0.05 m w.e. a\(^{-1}\) for the period of
overlap. A timing discrepancy arises with this comparison because the ice cores, with higher
dating resolution from isotopic and chemical analysis, are dated and reported as the for calendar
years, whereas the radar-derived accumulation is assumed 30 June—1 July — 30 June (Section
4.2). This mismatch in the measurement is likely evident in Figure 12 by the differences in the
annual peaks between the cores and radar-derived accumulation having similar means yet
differing magnitudes from year to year.

Near Camp Century, the cores and radar data are farther apart from each other. The radar-
data are located within 4.4 km of the Camp Century core and the GITS core is located ~8.2 km
from the Camp Century core. These separations are likely responsible for the poorer agreement
at this site of radar-derived accumulation rate to the Camp Century core (RMSE 0.10 m w.e. a-
1) and the larger difference (RMSE 0.07 m w.e. a- 1) in accumulation rate between the two cores
for the period of overlap. At Camp Century, and throughout much of northern Greenland, two
older, continuous layers were dated from the interior of the ice sheet and spatially traced. These
layers, dated 2000.5 and 2001.5, could not be dated with the Camp Century data alone—and,
hence, the temporal gaps in annual accumulation rate at this location. While it is more difficult
to analyze the results at Camp Century, with only three overlapping points of overlap and no
continuous annual time series of radar-derived accumulation rates, our estimates are within the
expected variability and capture the long-term mean value.

6 Discussion

This study is the first to derive annual accumulation rates from near-surface airborne radar
data collected across large portions of the GrIS. The pattern of radar-derived accumulation
rates compares well with known large-scale patterns and clearly shows that these accumulation-
rate measurements are useful for evaluating model estimates. At the two locations with
contemporaneous cores, radar-derived rates agree well with the long-term mean. Additional
cores, with direct overflights, are clearly needed to continue assessing the accuracy of the radar-
derived accumulation rates.

The work shown here only incorporates layering detected in the radar data that is annual
and continuously dated from the surface to depth at some location. We did not exhaustively
trace all layering detected by the Snow Radar, i.e., there are still contiguous layers, not
connected to a dated layer, in the dataset that were not utilized. For example, in the central-
northern GrIS, there is a strongly reflecting layer varying between 15 and 18 m that cannot be
dated with the radar data alone. If ice cores were drilled to identify the age of this layer,
techniques similar to those developed by MacGregor et al. (2015) or Das et al. (2015) could be used to determine multi-annual accumulation rates in additional regions of the GrIS and extend the Snow Radar record. Further deconvolution processing of the Snow Radar data, currently ongoing, will likely also resolve additional deeper layers in the Snow Radar data.

Annual-radar-derived accumulation rates are not extrapolated spatially here, due to their relative sparseness relative to the scale of the entire ice sheet. Such extrapolation between flightlines, which vary from year to year, must be left for future work, as additional data are collected and fill in gaps.

In 2010 the largest overall discrepancy is evident between radar-derived and MAR estimates of accumulation is in 2010. It does appear that MAR is overestimating accumulation rate over the southeastern GrIS in this year 2010 (Figure 10) and a previous study (Burgess et al., 2010) showed that modeling accumulation rate is difficult in this region. However, the discrepancy is also due, at least in part, to the fact that in 2010 there is a higher percentage of radar data collected over the lower portions of the southeastern GrIS compared to other regions. This spatial sampling bias is amplifying the discrepancy in 2010. Because OIB data is not spatially consistent from year to year caution must be used when extrapolating to ice sheet scales.

In 2011 MAR appears to underestimate accumulation rates over the northwestern GrIS in a region just to the south of Camp Century. This small region is known to receive higher accumulation snowfall locally than the surrounding areas, because storms on Greenland’s west coast are diverted as the land mass to the north protrudes farther west into Baffin Bay (K. Steffen, personal communication). MAR does show increased accumulation in this region (Figure 5), but not of however, not to the same magnitude as the radar-derived measurements. It is possible that MAR is not reproducing this local pattern because it is close to MAR’s lateral boundaries, where the coarser GCM may not adequately represent this phenomena. This discrepancy emphasizes the importance of understanding the possible effects of lateral forcing of RCMs on accumulation-rate fields and warrants further study. It is possible that MAR not estimating the magnitude of this relatively local high in precipitation due to it close proximity to the lateral boundaries where the larger resolution GCM may not
completely capture the phenomena. This emphasizes the importance of understanding the possible effects of lateral forcing of RCM on accumulation fields and warrants further study.

Finally, the largest uncertainties in the radar-derived accumulation rate come from the hybrid measured-modeled density profiles used, are approximately equally distributed between the layer picking, age and density. However, the layer picking is likely overestimated and in most cases likely much lower, leaving age and density uncertainties nearly equal (Medley et al., 2013). Age uncertainties could be better constrained with a better understanding of the timing of density peaks across the ice sheet. Our assumption that the surface date is 30 April could be adjusted to the flight date if the modeled accumulation rates were reprocessed to daily values.

With respect to density uncertainty, we assumed a constant and uniform density in the top meter of snow/firn as modeled outputs did not match measured values (Figure 2). This assumption could lead to spatial bias in our analysis if regional density deviates significantly from the mean, though existing measurements do not show any clear evidence of such spatial bias. Spatially distributed density measurements and improved density models spanning the entire firn column are required to take full advantage of the layering detected by near-surface radars and to reduce the errors in radar-derived accumulation rates. The current sampling of in situ measurements has large spatial gaps over the southwestern, north and northeastern GrIS and the majority of the measurements are located in the upper-percolation and dry-snow zones (Figure 1). To further constrain and improve the density models required for radar-derived accumulation rates, these gaps must be filled with additional measurements. Additionally, the Snow Radar’s signal penetration around the perimeter of the GrIS is relatively shallow, resolving 1 to 3 annual layers only, with the majority of detected layers in the top meter of snow/firn (Figures 6 and 7). Accumulation rates are calculated using measurement averages in this section of the snow/firn column, likely causing less error than the MAR-modeled density. Improvement to modeled near-surface density should be considered for improved Snow Radar analysis.

7 Conclusions

A semi-automated method was developed to process tens of thousands of kilometers of airborne Snow Radar data collected by OIB across the GrIS between 2009 and 2012. The resulting radar-derived accumulation-rate dataset represents the largest validation dataset for recent annual accumulation rates across the GrIS to date. This dataset captures the large-scale
accumulation-rate patterns of the GrIS well. Over two decades of annual radiostratigraphy is observed in the dry snow zone, near Summit Station, and 1 to 3 years are generally detectable in the ablation/percolation zones. Our estimated uncertainty in the radar-derived accumulation is 1\%2\%, with the largest error contribution coming from the hybrid measured-modeled density profiles. This study emphasizes the need for ice cores coincident in time with airborne overflights and, more importantly, for improved density profiles, particularly in the top 1 m of snow/firn. These radar-derived accumulation-rate datasets should be used to evaluate RCM/GCM and reanalysis products, as demonstrated here using the MAR model. MAR matches the radar-derived accumulation rates well for most of the interior of the GrIS, but tends to overestimate accumulation rates in the southeastern coastal region of the GrIS and, in at least one year, underestimates accumulation rates in the northwestern coastal region of the GrIS. While determining the precise nature of these differences is left for future work, we have clearly demonstrated the usefulness of the ice-sheet-wide, radar-derived accumulation-rate datasets for improving SMB estimates. As the GrIS continues to lose mass through SMB processes, monitoring accumulation rates directly is vital.

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Table 1: Radar-derived accumulation-rate crossover analysis. Columns include the year the radar data were collected, the number of, the mean, the standard deviation and the maximum difference of radar-derived accumulation at crossover points. Minimum crossover values were zero for all years. The final column shows the mean difference between the gridded-radar-derived accumulation and the MAR estimates of accumulation from July 1 to April 30.

<table>
<thead>
<tr>
<th>Year</th>
<th># of Crossovers</th>
<th>Mean Crossover in m w.e. a⁻¹ and (range bin)</th>
<th>Std. Crossover in m w.e. a⁻¹ and (range bin)</th>
<th>Max Crossover in m w.e. a⁻¹ and (range bin)</th>
<th>Mean Difference Radar-MAR in m w.e. a⁻¹</th>
</tr>
</thead>
<tbody>
<tr>
<td>2009</td>
<td>21</td>
<td>0.03(5)</td>
<td>0.04(7)</td>
<td>0.12(23)</td>
<td>-0.05</td>
</tr>
<tr>
<td>2010</td>
<td>270</td>
<td>0.02(3)</td>
<td>0.02(5)</td>
<td>0.16(40)</td>
<td>-0.18</td>
</tr>
<tr>
<td>2011</td>
<td>992</td>
<td>0.04(3)</td>
<td>0.06(4)</td>
<td>0.60(59)</td>
<td>0.01</td>
</tr>
<tr>
<td>2012</td>
<td>579</td>
<td>0.04(5)</td>
<td>0.04(6)</td>
<td>0.31(39)</td>
<td>0.03</td>
</tr>
</tbody>
</table>
Figure 1: Locations of snow/firn density measurements (red circles) and ice core accumulation measurements (blue circles) used in this study with OIB flightline coverage from 2009 through 2012 (gray lines). Camp Century (CC) and NEEM core locations are labeled and the red lines indicate the locations of the radargrams in Figure 3.
Figure 2: Mean observed (blue) and MAR modelled (red) densities profiles with one standard deviation (shaded regions) showing an underestimation of modelled densities in the top 1 m of snow/firn. The mean observed density in the top 1 m (green) was used with the modelled densities below to create a hybrid measured-modelled density profile. The locations of the density measurements are shown in Figure 1 and the measurements and modeled profiles are contemporaneous.
Figure 3: Example Snow Radar radargrams from 2011 in the percolation zone (top), inland from Jakobshavn Isbrae, and dry snow zone (bottom), near the ice divide ~220 km south of Summit Station, showing automatically picked layers (black) resulting from the layer picking algorithm before any manual adjustments. Indexing by year is shown at the left end of each picked layer. Snow Radar data frames represented are 20110422_01_218 to 20110422_01_244 (top) and 20110426_03_155 to 20110426_03_180 (bottom) (Leuschen, 2014). Locations of the radargrams are shown by the red lines in Figure 1.
Figure 4: Radar-derived-annual accumulation rate (m w.e. a$^{-1}$) for 2009 through 2012 from Operation IceBridge Snow Radar data representing the top layer in each year (July 1 to April 30).
Figure 5: Modelled estimates of annual accumulation (m w.e. a\(^{-1}\)) over the GrIS for 2009 through 2012 from the Modèle Atmosphérique Régional (MAR) regional climate model (v3.5.2) (representing July 1 to April 30 to match the radar-derived estimates).
Figure 6: Number of detected annual layers from 2009 through 2012 showing that, for the majority of the GrIS, fewer than three layers, or previous years of accumulation, were detected.
Figure 7: Histogram of first layer depth from 2009 through 2012 showing that the majority 63% of the first layer depths are within the top 1 m of snow.
Figure 8: Maps of annual-crossover error (m w.e. a⁻¹) from the radar-derived accumulation for 2009 through 2012.
Figure 9: Crossover errors from the radar from 2009 through 2012 in range bins. Figure 8 shows the spatial distribution of these crossover errors in (m w.e. a$^{-1}$).
Figure 10: Difference between annual radar-derived and MAR-estimated accumulation rate (m w.e. a⁻¹) showing MAR overestimation in red and underestimation in blue.
Figure 1: Comparison between radar-derived and MAR-estimated accumulation rate (m w.e. a\(^{-1}\)).

Radar-derived accumulations (Figure 4) were averaged within each MAR grid cell. Figure 9 shows the spatial distribution of the differences.
Figure 12: Annual accumulation rate measured from two cores at both the NEEM and Camp Century locations compared to temporally overlapping radar-derived values.