Sherbrooke, Québec, January 21, 2016

To:
Prof. Claude Duguay, Handling Editor

Object: Revision of Manuscript tc-2015-173

Manuscript Title: Microwave snow emission modeling uncertainties in boreal and subarctic environments.

Dear Editor,

Please find attached to this letter the revisions to the manuscript entitled: "Microwave snow emission modeling uncertainties in boreal and subarctic environments".

We would like to thank the reviewer for comments which were useful in producing an improved manuscript. We answered to all reviewer comments.

Please, do not hesitate to contact me if you have any further questions or comments, or if anything is missing from the submission of the revised manuscript.

Regards,

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In blue: Reviewer's comments. To better identify the questions, we added reference symbols: R= Reviewer ; C = Comments;
In black: Answers to reviewer
(Page): the pages where modification to text were added
In black and italic: Modification added to text.

Reviewer #1 (Comments):

This paper concerns the modeling of microwave radiation from snow with DMRT-ML, to quantify the simulation sensitivity to parameter uncertainty. This is the most complete study to date due to the consideration of the forest contribution as well as density, grain size, ice lens and soil roughness variability or uncertainty, with the latter effects providing no surprises based on other similar studies. In addition, to my knowledge, this is the first study to look at the effects of the bridging assumption between low and high density snow in the context of real data. The nominal simulations are considered to include a given grain scale factor, the density bridging assumption and appropriate treatment of ice lenses, before looking at other effects, which is a logical approach to take.

R1-C1 : This study looks at 3 different sites within the Canadian sub-Arctic, which gives a range of snowpack properties, but makes the paper somewhat hard to read. Due to the wide range of measurement locations, a figure with the sites indicated on a vegetation map would be useful.

We inserted a map of the 3 locations with the Land Cover of Canada 2005 (Latifovic et al., 2004) in background.

R1-C2 : In the James Bay measurements, the mean snow density from January to February decreased, and with minimal increase in grain size. Is this expected for this site? Is this due to the influence of recent precipitation, or spatial variability in the measurement locations? Also, how is the mean grain radius calculated?

The lower density in February is related to an error in density calculation. The snow density calculation was done considering the ice lenses. All the corrections were made (See also R2-C6)

The mean grain radius is the mean R_{opt} per layer weighted by the snow layer thickness. It is now mentioned in the text:

"During the JB_{Jan} campaign, 16 open area sites were measured where the mean ρ_{snow} *(weighted by snow layers thickness excluding ice lenses)* of all snowpits was 295.5 kg m^{-3} and the mean R_{opt} *(weighted by snow layers thickness excluding ice lenses)* was 0.17 mm (Table 1)."

R1-C3 : Constant soil parameters from a different study were used here (section 2.2.3). The authors must comment on the applicability of these parameters to the sites chosen for this study. The experiment presented in section 3.2.1 considers the effect of the roughness of the soil, but not the permittivity, which governs the Fresnel reflectivity and

is a more fundamental parameter. The authors note this limitation later in the section, but I do not agree with their statement (pg 5732, line 15) that this does not affect their main goal. It may do, as the variability in the permittivity may cause greater snow TB variability than is possible to simulate with adjustment of the roughness alone. The authors should justify why a particular constant value of permittivity derived elsewhere is an appropriate assumption here or base the sensitivity on permittivity rather than roughness variability.

The parameters were inverted from independent angular measurement taken during the same campaign at James Bay. We thus clarify that point in Section 2.2.3:

"The values of ε, σ and β at 11, 19 and 37 GHz inverted by Montpetit et al. (2015) for frozen soil (Table 6) were used in this study. *Montpetit et al. (2013) used independent snow free ground-based radiometer angular measurements taken at James Bay site in 2013 (same campaign). The parameters were also validated over Umiujaq (same campaign) snow removal experiment."*

Because we use minimal and maximal values of optimized σ the range of T_B variability of frozen ground is well represented. Also, the permittivity used were retrieved at the same site:

"However, one should be careful in interpreting these results as the optimization could also compensate for uncertainties in the permittivity of frozen ground. Nevertheless, *because the minimal and maximal values of optimized σ are taken*, this does not affect our main goal, which is to estimate the variability in snow-covered T_B introduced by the soil in the model. *Furthermore, as mentioned in Sect. 2.2.3, the permittivity used in this study were retrieved at the same site as this study."*

R1-C4 : Pg 5730 line 9-11. This is really hard to see in the figure. There are multiple outliers that easily cover this range in the simulations, so this sentence should be more precise.

We add a dotted line in the Fig. 6 to clarify the point.

R1-C5 : Figure 6, right doesn't add much to the message of the paper and diverts attention as there are many figures in this paper. As it has already been summarised in a single sentence I would recommend removing the figure.

We removed the figure and change the paragraph:

"To test the bridging parameterization (see Sect 2.2.2), we used 13 tundra sites from the Churchill tundra database (Roy et al., 2013), 4 from Umiujaq and 2 from the James Bay snowpits. In each case, at least one snow layer with a snow density higher than 367 kg m^{-3} (ice fraction of 0.4: Dierking et al., 2012) is used. For each of the 19 sites studied, simulations at 37 GHz (the most sensitive frequency to snow) with and without the bridging implementation were conducted (all input parameters kept the same). The bridging has a relatively modest impact on simulations with an improvement in the RMSE of between 2 and 4 K at tundra sites (Umijuaq and James Bay). The greatest improvements are found for deep drifted tundra snowpits where there is a very thick wind slab with high ρ_{snow} and small rounded grains are present at the top of the snowpack."

R1-C6 : Section 3.2.4. How was the density of ice lenses measured in the field and what was

the result (alternatively this comment may belong in the next section if 'was attempted' should be replaced with 'was not attempted').

We replaced for "*was not attempted*".

Technical comments (R1):

pg 5724 line 6. Make clear that the SSA is per unit mass rather than per unit volume.

We clarified the units

pg 5724 line 15 and onwards. JB may be a better, easier to read acronym than BJ.

We changed all the acronyms.

pg 5726 line 22. As a scaling factor of 3.3 has been applied following previous work, presumably non-sticky grains are assumed in the DMRT-ML simulations. This should be stated.

We changes the sentence :

"As such, a scaling factor of $\phi = 3.3$ *assuming non-sticky snow grains* from Roy et al. (2013) for the seasonal snowpack is thus applied to get an effective radius in the microwave range (R_{eff})"

pg 5727 line 21. In setting ice lens thickness to 1cm, how are the thicknesses of the adjoining layers adjusted, or is the overall depth of the profile in the simulations allowed to differ from the measured depth?

We mentioned that in the text :

"To keep the same total snow depth, the adjoining layers were adjusted by removing 0.5 cm of the layer above and below the ice layer."

pg 5728 line 11. This should be > 350, not < 350.

It was corrected

pg 5729 line 20. The bridging implementation was tested for simulations based on snowpit data rather than tested on snowpits themselves.

Done

pg 5734 line 12. gains -> grains

Done

lg 5736 line 11. weaker -> less

Done

Reviewer #2 (Comments):

General comments The authors present a study assessing uncertainties in microwave emission modeling from snow covered ground, arising from uncertainties in assigning model inputs from in situ information. One model, the DMRT-ML by Picard et al. is applied for the purpose. A set of surface-based radiometer measurements is used as a reference to model predictions. While not very original, the paper contributes regardless to an important topic in snow remote sensing. The results of the paper should be useful especially in guiding data collections in future, large scale campaigns of snow cover using passive microwave radiometry. The paper is well written and clear. However, I have some questions regarding the methodology applied, and would suggest the authors revise some of their conclusions before publication. See detailed comments in the following.

R2-C1 : Abstract, lines 42-43 and several places later on. Based on what is in the end a rather limited dataset, you draw conclusions that variations in the emission of frozen soil has only a small effect on brightness temperature of snow covered terrain. You alleviate this conclusion somewhat in the discussion (723-732), but it comes out very strongly in the abstract, which I feel is misleading. It is, for instance, unclear if the sites you had contained multiple soil types or not; the 'frozen' permittivity of clay rich soils, for example, will be quite different from that of mineral soil types, due to the ability to store free water even in sub-zero conditions. Organic soils represent yet another different scenario, as well as soils with a high saline content. You only have to look at e.g. SMOS data during winter to see that there are variabilities during the winter which clearly arise from soils with a different permittivity. It would be good to better bring out the limitations already in the abstract (i.e. your experimental findings apply only to a certain soil type), if you wish to raise this point at all

We clarify the results in the abstract. :

"A snow excavation experiment -- where snow was removed from the ground to measure the microwave emission of bare frozen ground -- shows that small-scale spatial variability *(less than 1 km)* in the emission of frozen soil is small. Hence, *in our case of boreal organic soil,* variability in the emission of frozen soil has a small effect on snow-covered brightness temperature (T_B)."

We also clarify in the results section (the soil types were mentioned in Sect. 2.1.1) that the $BJ_{Jan\text{-}transect}$ were made in an old gravel with mineral soil and, the other were made in organic boreal soil:

"The analysis of small-scale soil variability in modeling the T_B of snow-covered surfaces is conducted using the SEex from the transect during the JB_{Jan} *(mineral soil)* and JB_{Feb} campaigns *(organic soil)*."

"T_B variations of 0.5 K and 1.3 K were observed at the $JB_{Jan\text{-}transect}$ site where the soil properties were more homogeneous *(mineral soil)*, while a variation of 0.7 K to 3.8 K was measured at the JB_{Feb} site with *organic soil* (Table 8)."

R2-C2 : Abstract, lines 51-52, also later on: it is bit of a no-brainer that downwelling emission from trees affects the measured Tb. This is well known and it would simply be a mistake

not to include the downwelling canopy contribution – thus is a bit awkward to bring this out here. The absolute value of the Tb contribution, will be highly dependent on tree type and canopy conditions (frozen/thawed, snow covered/bare), as well as snow and soil reflectivity, thus I would refrain from giving a value here. If you insist, you should at least make it clear that this finding applies only to your study, test sites and the local conditions that prevailed.

From our knowledge, it is the first time that the contribution of forest emission reflected by the surface are quantified from ground-based radiometers. We think it is important to include in the abstract. We however mentioned in the abstract that the results are specific for our dataset:

"The results also show that, *in our study with the given boreal forest trees characteristics*, forest emission reflected by the surface can increase the T_B up to 40 K. *The forest contribution also varies with vegetation characteristic and a relationship between* T_{Bdown} *and the proportion of pixels occupied by vegetation (trees) in fisheye pictures was found.*"

R2-C3 : Introduction, lines 105-107 and elsewhere: Here, you claim to "quantify the sources of uncertainty in the DMRT-ML model". However, in the previous paragraph, you point out the two basic contributions to simulation (not model!) uncertainty: 1) model physics going wrong 2) insufficient or inaccurate input information. To me, the whole paper is about assessing point 2), as is in fact also pointed out in the discussion (line 740-741). This is an important distinction and you should be careful with the wording throughout the paper. In my view a better wording here would be something along the lines of: "we aim to quantify the relative importance of uncertainties of in situ information, when simulating microwave TB with the DMRT-ML model".

We clarify the main objective of the paper:

"Hence, this paper aims *to better quantify the relative importance of different geophysical parameters and small-scale spatial variability when simulating microwave* T_B *with the* Dense Media Radiative Theory-Multilayer model (DMRT-ML; Picard et al. 2013)."

We also clarify that point in the first sentence of Sect. 4 :

"This study presents a comprehensive analysis of the *geophysical parameters* contributing to uncertainty in DMRT-ML for snow-covered surfaces in boreal forest, subarctic and arctic environments."

R2-C4 : Lines 111-112: sentence a little bit incomplete. Add something like ": : : snow emission modeling: inaccuracies in quantifying snow grains, snow density"

The proposed change was done

R2-C5 : Section 2.1, lines 163-165. Measuring SSA may be robust, but being a definition for optical wavelengths, how well is SSA related to the propagation of microwaves in snow? I'm sure the authors are aware of this ongoing discussion. You do not have to delve deep into the problem here, but at least the question and the related discussion should be acknowledged by citing some recent work by e.g. Mätzler, also justifying why you use SSA regardless of the acknowledged limitations.

To our knowledge, SSA is the only robust and objective metric that can be measured in situ. We are now working on a paper showing that SSA is a better metric than D_{max}. We developed in the discussion on the justification of the use of SSA with some limitation.

"The error related to the physical simplifications in DMRT-ML was not investigated in this work, but our results suggest that the level of confidence of measurements is too low to test or significantly improve the DMRT-ML physics. *In this study, SSA was used because it is a robust and objective metric that can be measured effectively on the field. However, the derived* R_{opt} *metric used in DMRT-ML is related to an optical definition (Grenfell and Warren, 1999) and might not represent the grain for microwave wavelength (see Mätzler, 2002).* Further experiments on isolated snow layers as done by Wiesmann et al. (1998) but using new tools for snow microstructure parameterization could be applied to improve the physics of emission models. For example, more precise measurements of snow microstructure like X-ray tomography (Heggli et al., 2011) and the snow micro-penetrometer (SMP) (Schneebeli et al., 1999; Proksch et al., 2015) could be the next step to improve the understanding of the physics in DMRT-ML (e.g., Lowe and Picard, 2015)."

R2-C6 : Tables 1-5: the STD values for snow density seem very high to me, especially for Tables 1&2. Can you check these? If the values are correct, do you have a reason for the high degree of variability?

The average density and standard deviation of snow density calculation included the ice lenses. The values were recalculated without the ice lenses to give a better view of the snowpack characteristics. The values were corrected in the text as well (See also R1-C2).

R2-C7 : Section 2.2.3, line 340: epsilon' is the conventional symbol for the real part of the dielectric permittivity. The Fresnel reflectivity depends on < epsilon_r> = < epsilon'+ j* epsilon">. Is your epsilon' the real part of the soil permittivity (thus neglecting the imaginary part, a reasonable approximation for frozen soil), or the magnitude of the complex permittivity?

We clarify in the text that it is the real part of the soil permittivity:

"where $\Gamma_{f,p}$ is the rough soil reflectivity at a frequency f and polarization p (H-pol or V-pol) by its smooth Fresnel reflectivity in H-Pol ($\Gamma_{f,H}$), which depends on the incidence angle (θ) and the *real part of the soil permittivity* (ε'), weighted by an attenuation factor that depends on the standard deviation in height of the surface (soil roughness, σ), the measured wavenumber (k) and a polarization ratio dependency factor (β)."

R2-C8 : Section 3.1.1., line 374-376: what is the fundamental reason for the simulation to go wrong, when the effect of ice lenses is not included? Is it not very informative to just state that "improved simulations" are achieved with ice lenses. In other words, what is the physical effect that the ice lenses manage to simulate, which was lacking in the original simulation? This should be explained.

We clarify that the ice lenses inclusion allows taking into account its strong reflectivity:

These results show that a simple ice lens implementation in DMRT-ML helps *to simulate the*

strong reflection component of ice lenses (decrease of snowpack emissivity), leading to improved simulations of T_B.

R2-C9 : Still on ice lenses: can you elaborate your statement on line 380: what, in your view, are the reasons for the limited range of simulated values versus observations, if this is related to ice lenses. Coherence effects not accounted for by DMRT? Or, can this be something different (the soil perhaps?). coherence is mentioned in the discussion, but something could be pointed out here.

We chose not to elaborate on the reason for the limited range because it is well discussed in Sect. 3.2.4 and Sect. 4. But after review we add some sentences to start the discussion on that point:

"This feature suggests some limitations of ice lens and/or snow layering modeling in DMRT-ML *that can be related to the fact that coherence effect is not taken into account. Note that this underestimation of T_B spatial variability is not related to the soil as demonstrated in Sect. 3.2.1.* The modeling uncertainties related to ice lenses will be discussed more specifically in Sect. 3.2.4."

R2-C10 : Lines 417-418: rather than '5-10 K' and '10-20 K', give precise numbers. Note e.g. that RMSE at 11H exceeds 20 K, and RMSE for 19V lower than 5 K.

The numbers were updated:

"The RMSE values oscillate between *7.8 and 21.5 K* at H-pol (Table 7). Since V-pol is less affected by layering in the snowpack at 11 GHz and 19 GHz, the RMSE are generally lower (*between 3.5 and 14.4 K*), while the RMSE at 37 GHz are similar at V-pol and H-pol."

R2-C11 : Figure8: error bars in scatterplot not very informative, they only make the symbols hard to read. I suggest to remove these

We think that the error bars allow showing that the effect of soil emission small-scale spatial variability has a very low impact on T_B. For this reason we think it worth to keep the error bars.

R2-C12 : Section 3.2.2: summing of errors; is the 12% error in SSA considered random, or systematic? I think random? Then, you should rather perform a sum-of-squares addition of the errors, depending on how many measurements were used for a given snowpit [e.g. for three SSA measurements used in a sim: err_tot = sqrt(err_1^2+ err_2^2+ err_3^2) = 0.21]. I suggest to redo the analysis (Fig9, Table 9) in this fashion.

In our case, the error of 12% is added to the SSA of each layer of snowpack. Hence, the T_B error account for the sum of the error of each layer. The error in T_B resulting from the uncertainties in SSA measurements for each layer correspond to an integrated errors which are not independent from each other, since there are multiple scattering between the layers. In the Table 9, we show the extreme variations in T_Bs for the extreme cases where all the errors in SSA are in the same way (all positive + 12%, and all negative -12%). This gives the limit cases. In reality, one can assume a random error in SSA measurements between + and - 12% to calculate T_B with a random error applied on SSA ($T_{Bsimrand}$). We assessed the average variation in T_Bs (T_{Bsim} - $T_{Bsimrand}$) resulting from 100 runs with random error (± 12) in SSA for each layers of every snowpits. The

Table R.1 below shows the results. As expected, the variation is significantly lower than those shown in Table 9 of the paper. This Table gives the lower limits , while the Table 9 gives the highest limit.

Table R.1: T_B variation (T_{Bsim} - $T_{Bsimrand}$) associated with random error (±12%) applied to each SSA measurements (average of 100 runs)

	JB_{Jan}	JB_{Feb}	JB_{Mar}	UMI
11H	0.0	0.1	0.1	0.0
11V	0.0	0.1	0.1	0.0
19H	0.3	0.6	0.8	0.3
19V	0.3	0.6	0.9	0.3
37H	2.1	2.0	1.7	1.2
37V	2.7	2.4	2.1	1.4

We added the following sentence in the text:

"*We assessed average variation in T_B resulting from 100 runs with random error between ± 12% applied to SSA for each layer and snowpit. As expected, the results show that the variations between initial simulation and simulation with random error on SSA are significantly lower than those shown in Table 9. With random error applied on SSA measurements, the variations are lower than 1 K at 11 and 19 GHz, and between 2 and 3 K at 37 GHz. These values give the lower limits of T_B error related to SSA uncertainties, while values in Table 9 give the highest limit of the variation in T_B."*

R2-C13 : Line 595: I think you mean "was NOT attempted".

It was changed.

R2-C14 : Conclusions, p26, lines 760-765. You could cite Derksen (2008) in the discussion here, who suggested the use of 11-19 GHz in place of 19-37 GHz for deep snow to alleviate saturation effects at 37 GHz.

We added a sentence on the possibility to use 11-19 instead of 19-37:

"This could be of interest for the SWE retrieval approach, knowing that 19 GHz T_B becomes sensitive to snow when snow grains become larger. *As proposed in Derksen (2008) 11 and 19 GHz frequencies could be usefull for SWE retrievals for deep snow to overcome the problem of saturation at 37 GHz (see Rosenfeld and Grody, 2000).* At 11 GHz, snow is almost transparent throughout the winter demonstrating the utility of this band for monitoring soil conditions (phase, temperature) under the snow (Kohn and Royer, 2010). "

Editorial P11, line 333 delete "therefore"

Done

Microwave snow emission modeling uncertainties in boreal and subarctic environments

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Abstract.

This study aims to better understand and quantify the uncertainties in microwave snow emission models using the Dense Media Radiative Theory-Multilayer model (DMRT-ML) with in-situ measurements of snow properties. We use surface-based radiometric measurements at 10.67, 19 and 37 GHz in boreal forest and subarctic environments and a new in situ dataset of measurements of snow properties (profiles of density, snow grain size and temperature, soil characterization and ice lens detection) acquired in the James Bay and Umiujaq regions of Northern Québec, Canada. A snow excavation experiment -- where snow was removed from the ground to measure the microwave emission of bare frozen ground -- shows that small-scale spatial variability (less than 1 km) in the emission of frozen soil is small. Hence, in our case of boreal organic soil, variability in the emission of frozen soil has a small effect on snow-covered brightness temperature (T_B). Grain size and density measurement errors can explain the errors at 37 GHz, while the sensitivity of T_B at 19 GHz to snow increases during the winter because of the snow grain growth that leads to scattering. Furthermore, the inclusion of observed ice lenses in DMRT-ML leads to significant improvements in the simulations at horizontal polarization (H-pol) for the three frequencies (up to 20 K of root mean square error). However, the representation of the spatial variability of T_B remains poor at 10.67 and 19 GHz at H-pol given the spatial variability of ice lens characteristics and the difficulty in simulating snowpack stratigraphy related to the snow crust. The results also show that, in our study with the given forest characteristics, forest emission reflected by the surface can increase the T_B up to 40 K. The forest contribution varies with vegetation characteristic and a relationship between the downwelling contribution of the vegetation and the proportion of pixels occupied by vegetation (trees) in fisheye pictures was found. We perform a comprehensive analysis of the components that contribute to the snow-covered microwave signal, which will help to develop DMRT-ML and to improve the required field measurements. The analysis shows that a better consideration of ice lenses and snow crusts is essential to improve T_B simulations in boreal forest and subarctic environments.

Keywords: DMRT-ML, snow, vegetation, ice lenses, soil emissivity, microwave

1. Introduction

Seasonal snow cover plays an important role in the surface energy balance (Armstrong and Brun, 2008). Snow, with its low thermal conductivity, has an insulating effect on soils, which can greatly influence vegetation (Liston et al., 2002) and the development of active layers in permafrost (Gouttevin et al., 2012; Shurr et al., 2013). Snow water equivalent (SWE) is also a key variable in the high latitude water cycle (Déry et al., 2009) and is important for dam management and hydroelectricity production (Roy et al., 2010). Conventional in situ observations, such as from meteorological stations, are often inadequate to monitor seasonal snow evolution given the sparse distribution of stations in northern regions. Furthermore, point measurements are subject to local scale variability and may not represent the prevailing regional conditions. For these reasons, monitoring SWE from satellite passive microwave (PMW) observations has been the subject of

numerous studies for nearly three decades (e.g., Chang et al. 1987; Goodison et al., 1986; Derksen, 2008). The PMW are sensitive to SWE, but also have the advantage of providing observations at a synoptic scale in any weather conditions: images are available at least twice a day for the northern regions. However, estimation of SWE is not straightforward and existing empirical algorithms based on linear relationships between SWE and spectral T_B are often inaccurate due to seasonal snow grain metamorphism (Rosenfeld and Grody, 2000). Vegetation contributions are also an important factor with large interannual variability (Roy et al., 2015), which is not captured by these algorithms. Hence, radiative transfer models (RTM) including microwave snow emission models (MSEM) can be used to take into account the different contributions to the microwave signal and the interannual variability of critical geophysical parameters. The GlobSnow2 SWE retrieval algorithm (Takala et al., 2011) uses an assimilation scheme combining PMW observations constrained with kriged measurements of snow depth from meteorological stations. This method, however, has some limitations in remote areas where snow measurements are sparse, thus highlighting the need to improve MSEM performance in such a way that SWE retrievals can be achieved without in situ observations (Larue et al., 2015).

At the satellite scale, PMW observations generally have a coarse spatial resolution (more than 10 km x 10 km). Nevertheless, spatial heterogeneity within PMW pixels becomes a limitation for the development and validation of MSEM because contributions from snow, vegetation and lakes are difficult to decouple. Therefore, surface-based radiometers (SBR) are used to better understand and isolate the contribution of snow-covered surfaces. However, independently of MSEM used and seasonal snow type, the comparison between simulated T_B and SBR observations leads to errors in the order of 10 K (Roy et al., 2013; Montpetit et al., 2013; Derksen et al., 2012; Kontu and Pulliainen, 2010; Lemmetyinen et al., 2010; Lemmetyinen et al., 2015; Durand et al., 2008). From SBR measurements, these errors can be explained by 1) MSEM physical simplification (Tedesco and Kim, 2006) and 2) small scale variability and uncertainty in measurements of geophysical parameters.

Hence, this paper aims to better quantify the relative importance of different geophysical parameters and small-scale spatial variability when simulating microwave T_B with the Dense Media Radiative Theory-Multilayer model (DMRT-ML; Picard et al. 2013). The study is based on a new and unique database including SBR measurements at three microwave frequencies (37, 19 and 10.67 GHz) in boreal and subarctic environments. The study assesses a wide range of contributions that could lead to uncertainties in ground-based microwave snow emission modeling: snow grains, snow density, soil roughness, ice lenses (IL) and vegetation. More specifically, the objectives of the study are:

1. Validate the snow emission modeling, including recent improvements accounting for ice lenses (Montpetit et al., 2013) and snow density in the 367-550 kg m^{-3} range (Dierking et al., 2012).

2. Evaluate the different contributions to modeling uncertainty (snow grains, snow density, ice lenses, soil and vegetation measurements).

3. Quantify the sensitivity of simulated T_B to the measurement accuracy.

2. Method

2.1 Sites and Data

Surface-based radiometer observations were acquired during the 2010 field campaign at the Churchill Northern Studies Center (Northern Manitoba) (see Roy et al., 2013 for a detailed description of the field campaign) and during four subsequent field campaigns in Northern Québec, Canada: three in James Bay (53°26'N; 76°46'W, 186 m a.s.l) in winter 2013 and one campaign in Umiujaq (56°33'N, 76°30'W, 74 m a.s.l) in winter 2014 (Fig. 1). All these campaign allow covering a wide range of environmental conditions from dense boreal forest to open tundra for a total of 51 snowpits (excluding the Churchill snowpits).

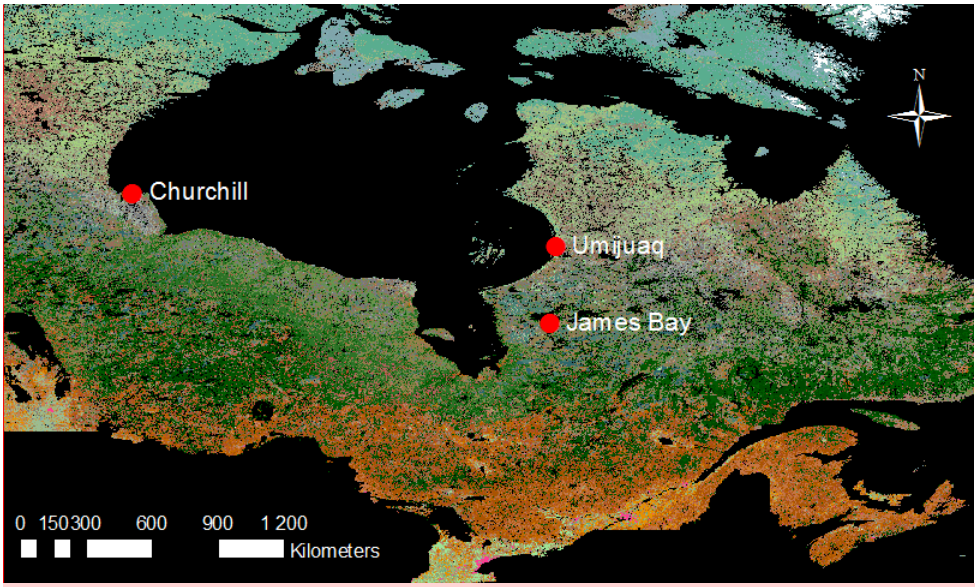

Fig. 1. Location of field campaigns. Background: Land Cover of Canada (Latifovic et al., 2004)

Comment [AR1]: New figure

T_B measurements were acquired at 37, 19 and 10.67 GHz in both vertical (V-pol) and horizontal (H-pol) polarizations at a height of approximately 1.5 m above the ground and at an angle of 55° with the PR-series Surface-Based Radiometers from Radiometrics Corporation (Langlois, 2015) (hereinafter, the 10.67 GHz SBR is noted 11 GHz for simplicity). With a beam width of 6° for 37 and 19 GHz SBR, the footprint of the measurements at the snow surface was approximately 0.6 m x 0.6 m. The 11 GHz beam width is 8° with a footprint of about 0.8 x 0.8 m. In the worst case, the measurement error

for the calibration target was estimated at 2 K. The radiometers were calibrated before and after each field campaign using ambient (black body) and cold (liquid nitrogen) targets.

Within the footprint of every SBR observation, profiles of snow temperature, snow density (ρ_{snow} in kg m^{-3}) and specific surface area (SSA in m^2 kg^{-1}) were taken at a vertical resolution between 3 and 5 cm. Visual stratigraphy assessment of the main snow layers/features, including ice lenses, was conducted. The density was measured using a 185-cm^3 density cutter, and samples were weighed with a 100-g Pesola light series scale with an accuracy of 0.5 g. The snow temperature and soil temperature were measured with a Traceable 2000 digital temperature probe (± 0.1 °C). The SSA was measured with the shortwave InfraRed Integrating Sphere (IRIS) system (Montpetit et al., 2012) at the James Bay site and using the Dual Frequency Integrating Sphere for Snow SSA measurement (DUFISSS: Gallet et al., 2009) in Umiujaq. Both instruments exploit the relationship between the SWIR snow reflectance and the SSA (Kokhanovsky and Zege, 2004) based on the principle described in Gallet et al. (2009). From SSA measurements, the optical radius of the snow grain (R_{opt}) was calculated by:

$$R_{opt} = \frac{3}{\rho_{ice} SSA} \quad (1)$$

where ρ_{ice} is the ice density = 917 kg m^{-3}. The SSA is one of the most robust and objective approaches to measure a parameter related to the size of snow grains in the field. The error for SSA measurements was estimated to be 12% (Gallet et al., 2009).

2.1.1 James Bay, Québec, Canada

Three intensive measurement periods were conducted during the 2013 winter season in the James Bay area, Québec, in January (8^{th} to 12^{th}: JB_{Jan}), February (12^{th} to 17^{th}: JB_{Feb}) and March (19^{th} to 23^{th}: JB_{Mar}) (Tables 1, 2 and 3). The sites were in a typical boreal forest environment, but most of the measurements were conducted in clearings with minimal influence of the environment (topography, vegetation) on the measured T_B. However, 15 measurements, spanning across the three campaigns, were conducted in forested areas and were treated separately to specifically investigate the contribution of vegetation on the ground-based measurements (Table 4). Several snow excavation experiments (denoted SEex) were also conducted where snow was removed to measure frozen ground emission. During SEex, large snowpits were dug (about 3 m x 3 m wide) and the snow walls removed to eliminate snow wall emission reflected on the ground. At all sites, the soil (described below) was frozen at least to a depth of 10 cm.

During the JB_{Jan} campaign, 16 open area sites were measured where the mean ρ_{snow} (weighted by snow layers thickness excluding ice lenses) of all snowpits was 218.3 kg m^{-3} and the mean R_{opt} (weighted by snow layers thickness excluding ice lenses) was 0.17 mm (Table 1). Snowpits JB_{Jan}-1 to JB_{Jan}-5 were located in forest clearings where the soil composition mainly consisted of organic matter. On January 9^{th}, a transect of 11 snowpits (JB_{Jan}-6.1 to JB_{Jan}-6.11, each separated by 3 m) was conducted in an old gravel pit

(mostly mineral soil). Five SEex were also conducted in the 30 m transect. One to two ice lenses of about 0.5 to 1 cm were observed in all snowpits, buried at depths of 10 and 30 cm.

Table 1. Average snow property values with standard deviation (in parentheses) at James Bay (JB) sites in January. Values are provided for snow depth (SD m); mean snowpack temperature (T_{snow}); bulk density (ρ_{snow}); mean optical radius (R_{opt}); soil/snow temperature (T_{soil}); number of observed ice lenses (IL); and 'bridging' (B) indicates the presence of a snow layer with a density within the bridging ice fraction limits (see Sect. 2.2.2).

SP	Type	SD (cm)	T_{snow} (K)	ρ_{snow} (kg m^{-3})	R_{opt} (mm)	T_{soil} (K)	IL	B	Date
JB_{an}-1	Forest clearing Organic soil	37	259.9 (4.8)	220.7 (37.4)	0.19 (0.09)	272.3	1		07-01-2013
JB_{an}-2		43	265.3 (3.4)	196.3 (40.4)	0.15 (0.07)	272.0	1		08-01-2013
JB_{an}-3		48	264.8 (4.2)	241.1 (37.2)	0.20 (0.10)	272.6	1		08-01-2013
JB_{an}-4		48	264.9 (3.6)	212.8 (48.5)	0.17 (0.09)	272.3	1		08-01-2013
JB_{an}-5		62	267.5 (1.8)	220.8 (45.9)	0.15 (0.08)	272.4	1		11-01-2013
JB_{an}-6.1	Old gravel pit Mineral soil $JB_{an\text{-}transect}$	51	266.8 (2.4)	223.4 (39.6)	0.17 (0.08)	271.5	1		09-01-2013
JB_{an}-6.2		52	267.4 (2.4)	240.1 (42.5)	0.18 (0.08)	271.5	1		09-01-2013
JB_{an}-6.3		43	266.5 (1.4)	212.8 (34.9)	0.17 (0.08)	271.3	1		09-01-2013
JB_{an}-6.4		45	268.0 (2.3)	204.3 (37.8)	0.18 (0.09)	272.1	1		09-01-2013
JB_{an}-6.5		53	267.2 (2.6)	244.5 (40.4)	0.16 (0.09)	272.6	1		09-01-2013
JB_{an}-6.6		51	267.0 (2.2)	224.4 (38.5)	0.18 (009)	272.0	1		09-01-2013
JB_{an}-6.7		47	267.2 (2.0)	220.1 (34.5)	0.16 (0.10)	271.6	2		09-01-2013
JB_{an}-6.8		47	267.5 (2.3)	205.4 (36.5)	0.14 (0.08)	271.8	2		09-01-2013
JB_{an}-6.9		46	267.1 (1.8)	209.4 (32.0)	0.16 (0.10)	271.1	2		09-01-2013
JB_{an}-6.10		45	266.7 (1.5)	202.6 (23.8)	0.14 (0.07)	270.3	1		09-01-2013
JB_{an}-6.11		40	266.8 (1.2)	214.7 (24.2)	0.17 (0.10)	269.6	1		09-01-2013

Nine snowpits were dug during the February campaign (Table 2), with a mean ρ_{snow} of 225.2 kg m^{-3} and a mean R_{opt} of 0.18 mm. All snowpits were conducted in clearings with frozen organic soil. On the 15th of February, for a transect of seven snowpits, a complete set of measurements was taken for each snowpit (SP). An ice lens at a depth of 30 cm was observed at each SP. In addition to SP measurements, two SEex were conducted in the transect and two others in $JB_{Feb\text{-}1}$ and $JB_{Feb\text{-}2}$.

Table 2. Same as Table 1, but for James Bay sites in February (JB_{Feb}).

SP	Type	SD (cm)	T_{snow} (K)	ρ_{snow} (kg m^{-3})	R_{opt} (mm)	T_{soil} (K)	IL	B	Date
JB_{Feb}-1	Forest clearing Organic soil	62	266.9 (2.3)	240.1 (26.2)	0.21 (0.12)	272.8	1		12-02-2013
JB_{Feb}-2		66	265.8 (5.0)	194.7 (37.8)	0.24 (0.10)	273.1	1		13-02-2013
JB_{Feb}-3.1		66	265.3 (3.2)	250.7 (90.7)	0.18 (0.09)	270.8	1	x	15-02-2013
JB_{Feb}-3.2		66	265.6 (3.3)	215.9 (57.8)	0.18 (0.09)	270.5	1		15-02-2013
JB_{Feb}-3.3		65	265.9 (3.0)	228.9 (56.5)	0.11 (0.05)	270.5	1		15-02-2013
JB_{Feb}-3.4		68	266.6 (2.6)	228.1 (54.9)	0.17 (0.09)	271.3	1		15-02-2013
JB_{Feb}-3.5		65	264.0 (4.0)	235.4 (66.0)	0.17 (0.10)	271.0	1	x	15-02-2013
JB_{Feb}-3.6		65	266.5 (4.7)	223.6 (65.8)	0.20 (0.11)	271.3	1		15-02-2013
JB_{Feb}-3.7		64	266.0 (3.2)	209.0 (61.4)	0.18 (0.11)	270.8	1		15-02-2013

During the March campaign, five snowpits with a mean ρ_{snow} of 278 kg m^{-3} and mean R_{opt} of 0.26 mm were dug (Table 3). There is a clear increase (70%) of grain size in March, linked to a strong temperature gradient metamorphism regime typical of such environments. On March 22nd, a transect of three snowpits was conducted in a clearing with frozen organic soil.

Table 3. Same as Table 1, but for James Bay sites in March (JB_{Mar}).

SP	Type	SD (cm)	T_{snow} (K)	ρ_{snow} (kg m^{-3})	R_{opt} (mm)	T_{soil} (K)	IL	B	Date
JB_{Mar}-1	Forest clearing Organic soil	83	268.2 (3.2)	261.4 (41.0)	0.25 (0.10)	272.0	1		19-03-2013
JB_{Mar}-2		67	267.5 (2.4)	265.2 (38.2)	0.25 (0.07)	270.9	1		20-03-2013
JB_{Mar}-3.1	Transect in Forest clearing Organic soil	63	269.3 (0.8)	266.1 (34.9)	0.28 (0.11)	270.5	1		22-03-2013
JB_{Mar}-3.2		69	271.0 (1.0)	303.1 (28.1)	0.26 (0.09)	272.5	1		22-03-2013
JB_{Mar}-3.3		67	270.9 (0.8)	294.2 (28.1)	0.25 (0.10)	272.1	1		22-03-2013

Measurements were also conducted in a forested area (Table 4), where the emission of the trees that is reflected on the ground contributes to the measured T_B (Roy et al., 2012). For these reasons, these snowpits were treated separately and used to better understand the influence of tree emission on ground-based radiometric measurements. On January 10th, a transect of eight snowpits was conducted in a forested area as well as transects of three snowpits on February 14th and March 21st. In addition to the usual snowpit observations, fisheye pictures (Fig. 2) were taken during the January and February campaigns to quantify vegetation density. The pictures were binarized to distinguish sky pixels from tree pixels allowing the estimation of the proportion of pixels (fraction) occupied by vegetation (χ_{veg}).

Table 4. Same as Table 1, but for James Bay sites, all in forested areas (JB_{veg}).

SP	Type	SD (cm)	T_{snow} (K)	ρ_{snow} (kg m^{-3})	R_{opt} (mm)	T_{soil} (K)	IL	Date
JB_{veg}-1		62	267.6 (1.8)	222.5 (44.5)	0.14 (0.08)	272.4	1	11-01-2013
JB_{veg}-2.1	First transect of 30 m	64	267.4 (2.7)	202.6 (43.3)	0.18 (0.09)	273.3	1	10-01-2013
JB_{veg}-2.2		67	269.0 (2.3)	211.6 (49.9)	0.15 (0.09)	273.3	1	10-01-2013
JB_{veg}-2.3		60	268.3 (3.1)	201.4 (58.5)	0.16 (0.09)	273.4	1	10-01-2013
JB_{veg}-2.4		60	267.6 (2.1)	197.2 (40.0)	0.19 (0.10)	272.4	1	10-01-2013
JB_{veg}-2.5		65	267.1 (2.5)	200.7 (48.9)	0.15 (0.08)	272.8	1	10-01-2013
JB_{veg}-2.6		60	266.3 (2.0)	195.5 (59.8)	0.15 (0.08)	271.9	1	10-01-2013
JB_{veg}-2.7		56	268.4 (2.5)	199.4 (36.5)	0.15 (0.09)	272.9	1	10-01-2013
JB_{veg}-2.8		68	268.1 (2.9)	205.4 (45.2)	0.14 (0.08)	273.1	1	10-01-2013
JB_{veg}-3.1	Second transect of 6 m	78	267.0 (2.8)	231.6 (44.1)	0.19 (0.10)	272.4	2	14-02-2013
JB_{veg}-3.2		78	267.4 (2.4)	217.0 (55.8)	0.19 (0.10)	272.6	2	14-02-2013
JB_{veg}-3.3		75	267.5 (2.2)	222.0 (62.1)	0.19 (0.12)	272.4	1	14-02-2013
JB_{veg}-4.1	Third	88	268.1 (1.5)	281.4 (55.3)	0.20 (0.11)	271.9	3	21-03-2013

JB_{veg}-4.2	transect of 6 m	88	269.9 (1.5)	283.2 (42.8)	0.22 (0.12)	272.9	3	21-03-2013
JB_{veg}-4.3		87	271.5 (1.0)	288.8 (43.7)	0.28 (0.12)	272.9	3	21-03-2013

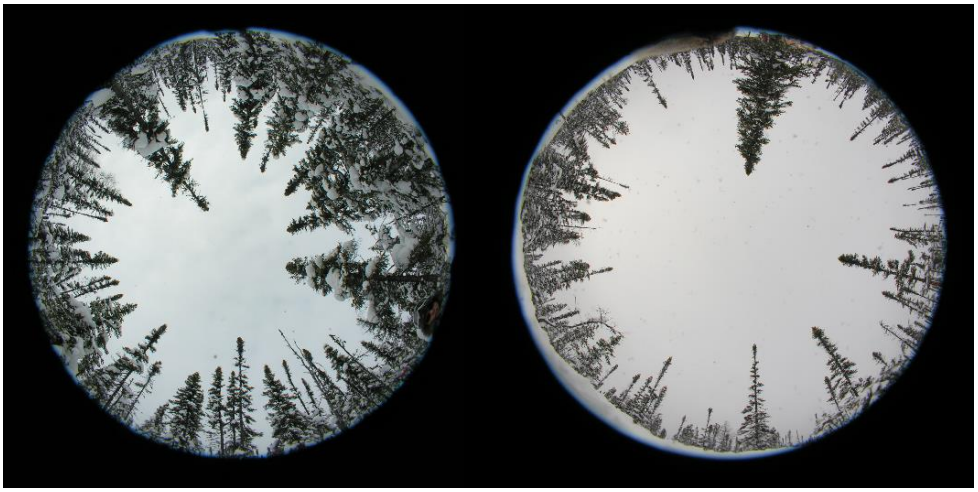

Fig. 2. Fisheye pictures for JBveg-3.3 (left) and JBveg-2.2 (right) sites, showing the sky view proportion around the SBR site measurements.

2.1.2 Umiujaq

An intensive measurement campaign was conducted in January 2014 (21^{st} to 28^{th}) in the region of Umiujaq. All the measurements were conducted in a tundra environment except for the Umi-3 site, which was located in a clearing (Table 5). The tundra sites were characterized by typical dense snow drift layers near the surface that fall into the bridging limits of 0.4 and 0.6 for the ice fraction as defined by Dierking et al. (2012) (see Sect. 2.2.2). Furthermore, one to two ice lenses were observed at the UMI-1, UMI-2 and UMI-4 sites.

Table 5. Same as Table 1, but for Umiujaq sites (UMI).

SP	Type	SD (cm)	T_{snow} (K)	ρ_{snow} (kg m^{-3})	R_{opt} (mm)	T_{soil} (K)	IC	B	Date
UMI-1	Tundra	35	253.9 (2.6)	361.8 (54.4)	0.15 (0.12)	258.4	2	x	22-01-2014
UMI-2		70	256.2 (4.6)	379.0 (40.5)	0.18 (0.09)	265.2	2	x	23-01-2014
UMI-3	Forest clearing	132	263.5 (5.8)	319.0 (51.2)	0.18 (0.08)	271.8	0	x	24-01-2014
UMI-4	Tundra	57	256.9 (4.2)	280.7 (46.5)	0.23 (0.11)	264.4	1		25-01-2014
UMI-5		93	254.0 (3.9)	350.6 (42.3)	0.19 (0.09)	261.6	0	x	26-01-2014

2.2 Models

The study uses the DMRT-ML model to simulate the microwave emission of snow-covered surfaces (Brucker et al. 2011; Picard et al., 2013). It is a multilayer

electromagnetic model based on the DMRT theory (Tsang and Kong, 2001). The theory assumes that a snow layer is composed of ice spheres where the effective permittivity is calculated using the first-order quasi-crystalline approximation and the Percus-Yevick approximation. The propagation of energy between the different layers is calculated with the Discrete Ordinate Radiative transfer (DISORT) method as described in Jin et al. (1994). In this paper, the propagation of electromagnetic radiation was calculated for 64 streams.

The snowpit measurements (ρ_{snow}, T_{snow}, T_{soil} and R_{opt}) were integrated as input to the model to simulate snow microwave emission. However it was shown in previous studies (Brucker et al. 2011; Roy et al., 2013; Picard et al. 2014) that using R_{opt} was inadequate as input to DMRT-ML. As such, a scaling factor of $\phi = 3.3$ assuming non-sticky snow grains from Roy et al. (2013) for the seasonal snowpack is thus applied to get an effective radius in the microwave range (R_{eff}):

$$R_{eff} = R_{opt} \cdot \phi \quad (2)$$

Roy et al. (2013) shows that the need for a scaling factor in DMRT-ML could be related to the grain size distribution of snow and the stickiness between grains, which leads to an increase of the R_{eff}.

The atmospheric downwelling T_B that is reflected by the snow surface to the radiometer was modeled using the millimeter-wave propagation model (Liebe et al., 1989) implemented in the Helsinki University of Technology (HUT) snow emission model (Pulliainenet al., 1999). The atmospheric model was driven with the air temperature and air moisture of the atmospheric layer above the surface from the 29 North American Regional Reanalysis (Mesinger et al., 2006) atmospheric layers.

2.2.1 Ice lenses

The microwave signal is very sensitive to ice lens formation within a snowpack at H-pol (Montpetit et al., 2013; Rees et al., 2010; Lemmetyinen et al., 2010). To simulate the ice lenses present in this study's database (see Tables 1 to 5) using DMRT-ML, snow layers with a high density of 900 kg m^{-3} close to the density of pure ice (917 kg m^{-3}) and a null snow grain size were integrated into the snowpack input file where ice lenses were observed. The value of 900 kg m^{-3} was chosen because only pure ice lenses were observed. To keep the same total snow depth, the adjoining layers were adjusted by removing 0.5 cm of the layer above and below the ice layer. However, an analysis of the effect of ice lens density on T_B simulations will be conducted in Sect. 3.2.4. Because coherence is neglected in DMRT-ML (Matzler, 1987), the ice lens thickness has a negligible effect on simulated T_B. Hence, because no precise measurements of ice lens thickness were performed in the field, ice lens thickness was set to 1 cm in DMRT-ML.

2.2.2 Bridging

It has been shown that DMRT theory is in agreement with numerical solutions of the 3-D Maxwell equations up to a density of 275 kg m^{-3} (ice fraction of 0 - 0.3) (Tsang et al., 2008), which is a relatively low density for snow. Although most of the applications of DMRT theory concern snow, DMRT can be applied to other dense media such as bubbly ice (Dupont et al., 2014). In this case, the background is pure ice, and the scatterers are air spheres to represent bubbles. To the best of our knowledge, no validity tests have been done in this configuration; but if we assume a similar range of validity in terms of volume fraction of scatterers, the DMRT theory would be valid in the range 0.7 – 1 for the ice fraction, that is 642 - 917 kg m^{-3}. Even in this case, a large range of intermediate densities remains for which the absorption and scattering coefficients might not be accurate. Following Dierking et al. (2012), an empirical extrapolation of these coefficients from a spline fitted in both validity ranges was implemented to calculate coefficients for a layer with an ice fraction between 0.4 (ρ_{snow} = 367 kg m^{-3}) and 0.6 (ρ_{snow} = 550 kg m^{-3}) (Fig. 3). As an example, the bridging leads to a decrease of T_B at 37 GHz for high snow density (> 350 kg m^{-3}) related to the increase of scattering (Fig. 4). In the following, this approach is denoted as 'bridging' and the limits will be set at 0.4 and 0.6 for the ice fraction following the study of Dierking et al. (2012).

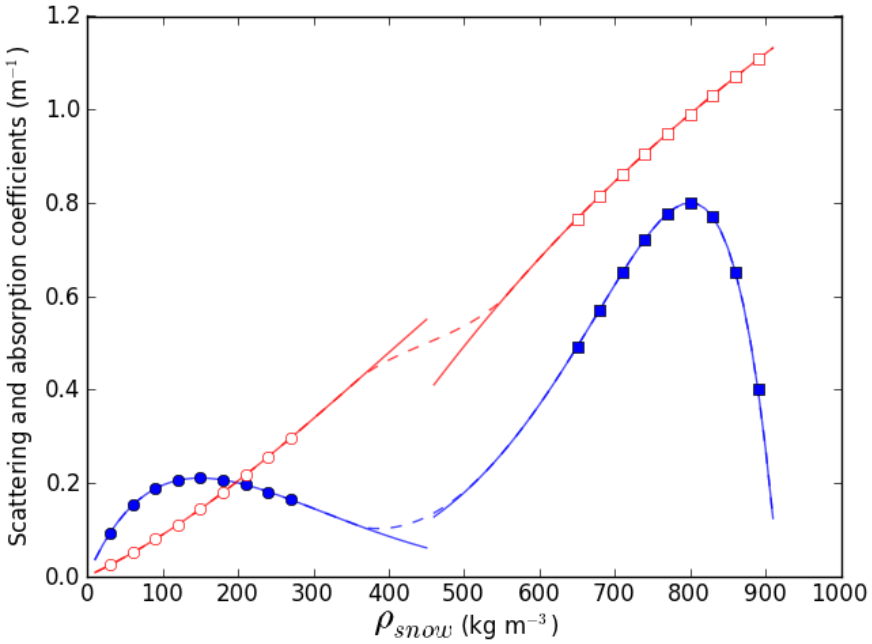

Fig. 3. Absorption (red) and scattering (blue) coefficients as a function of ρ_{snow} at 37 GHz (T_{snow} = 260 K, T_{soil} = 270 K, SD = 1.0 m and R_{eff} = 0.3 mm). The dotted lines show the bridging implementation for an ice fraction between 0.4 and 0.6.

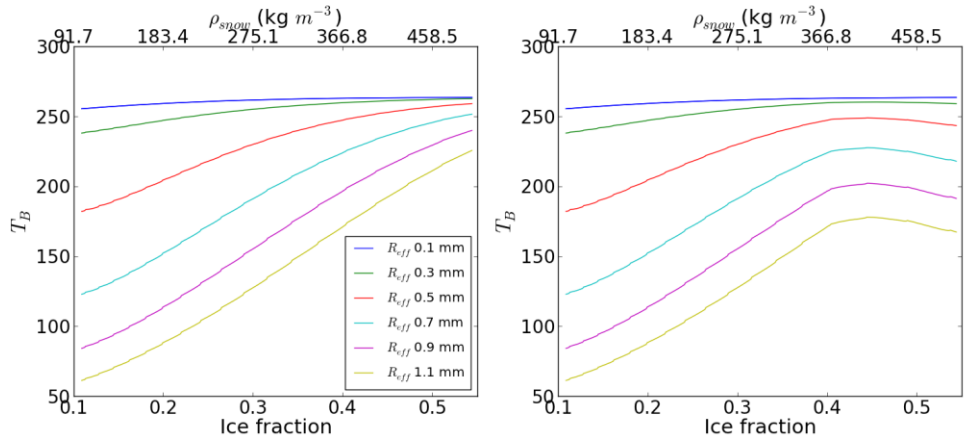

Fig. 4. T_B without (left) and with the bridging implementation (right) at 37 GHz (V-pol) for different R_{eff} (T_{snow} = 260 K, T_{soil} = 270 K and SD = 1.0 m).

The implementation of the bridging was evaluated with James Bay and Umiujaq snowpit data that include at least one snow layer with an ice fraction of more than 0.4 (Tables 2 and 5). Because ρ_{snow} is relatively low in boreal regions due to weakening of the wind by trees, we also evaluated this approximation using a tundra dataset to increase the number of high density snow layers for the specific validation of the bridging. The database acquired at the Churchill Northern Studies Center (58°44'N, 93°49'W) (Roy et al., 2013; Derksen et al., 2012) from the winter 2010 campaign is composed of 13 sites with at least one layer in the bridging range.

2.2.3 Soil model

Soil reflectivity models are included in DMRT-ML to account for the soil contribution to the measured T_B. In this paper, the Wegmüller and Mätzler (1999) soil reflectivity model improved for frozen soil by Montpetit et al. (2015) is used. The Wegmüller and Mätzler (1999) model for incidence angles lower than 60° is described by:

$$\Gamma_{f,H-pol} = \Gamma_{f,H}^{Fresnel} \exp(-(k\sigma)^{\sqrt{-0.1\cos\theta}}) \quad (3)$$

$$\Gamma_{f,V-pol} = \Gamma_{f,H} \cos\theta^{\beta} \quad (4)$$

where $\Gamma_{f,p}$ is the rough soil reflectivity at a frequency f and polarization p (H-pol or V-pol) by its smooth Fresnel reflectivity in H-Pol ($\Gamma_{f,H}$), which depends on the incidence angle (θ) and the real part of the soil permittivity (ε'), weighted by an attenuation factor that depends on the standard deviation in height of the surface (soil roughness, σ), the measured wavenumber (k) and a polarization ratio dependency factor (β). The values of ε', σ and β at 11, 19 and 37 GHz inverted by Montpetit et al. (2015) for frozen soil (Table

6) were used in this study. Montpetit et al. (2013) used independent snow free ground-based radiometer angular measurements taken at James Bay site in 2013 (same campaign). The parameters were also validated over Umiujaq (same campaign) from snow removal experiment.

Table 6. Main parameters used in DMRT-ML

Frequency (GHz)	ε'	β	ϕ	fluxes	σ (cm)	θ (°)
11	3.197	1.077	3.3	64	0.193	55
19	3.452	0.721				
37	4.531	0.452				

3. Results

In this section, the impact of model improvements (ice lenses and bridging) is first presented. Afterward, the evaluation of the effect of the different sources (soil, snow grain size, snow density, ice lenses and vegetation) on T_B is shown.

3.1 Model validation and improvement

Initial simulations ignoring the presence of ice lenses and bridging show a clear overestimation of T_B mostly at H-pol. The observed root mean square error (RMSE) is greater than 35 K at 11 and 19 GHz and greater than 20 K at 37 GHz (Fig. 5). There is also a positive bias for T_B at 11 and 19 GHz at V-pol. In this section, the effect of ice lenses on T_B is evaluated, while the bridging implementation was tested on snowpits data.

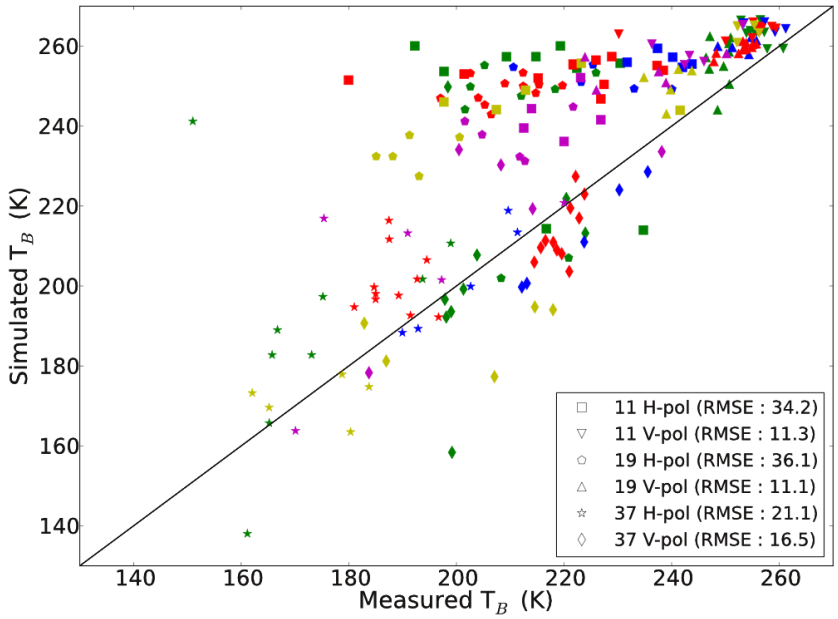

Fig. 5. T_B simulated without ice lenses in DMRT-ML and bridging. RMSE (K) between measured and simulated T_B are given in parentheses. The symbol types correspond to the frequency and colors to the sites: Red = $JB_{Jan\text{-}transect}$; Green = $JB_{Jan\text{-}others}$; Blue = JB_{Feb}; Yellow = JB_{Mar}; Magenta = UMI.

3.1.1 Ice lenses

Simulations including observed ice lenses were conducted on all snowpits (Fig. 6) leading to a strong decrease in simulated T_B H-pol (up to 40 K). At H-pol, the RMSE are thus improved by 15.4, 23.4 and 9.3 K at 11, 19 (initially > 35 K) and 37 GHz (initially > 20 K) respectively. The ice lenses also slightly decrease the bias measured at V-pol for all frequencies leading to a RMSE improvement of 3 to 4 K. These results show that a simple ice lens implementation in DMRT-ML helps to simulate the strong reflection component of ice lenses (decrease of snowpack emissivity), leading to improved simulations of T_B.

However, a large variability (190 to 245 K) in T_B observations at H-pol at 11 and 19 GHz is not reproduced by the simulations (dotted black line in Fig. 6). This feature suggests some limitations of ice lens and/or snow layering modeling in DMRT-ML that can be related to the fact that coherence effect is not taken into account. Note that this underestimation of T_B spatial variability is not related to the soil as it is demonstrated in Sect. 3.2.1. The modeling uncertainties related to ice lenses will be discussed more specifically in Sect. 3.2.4.

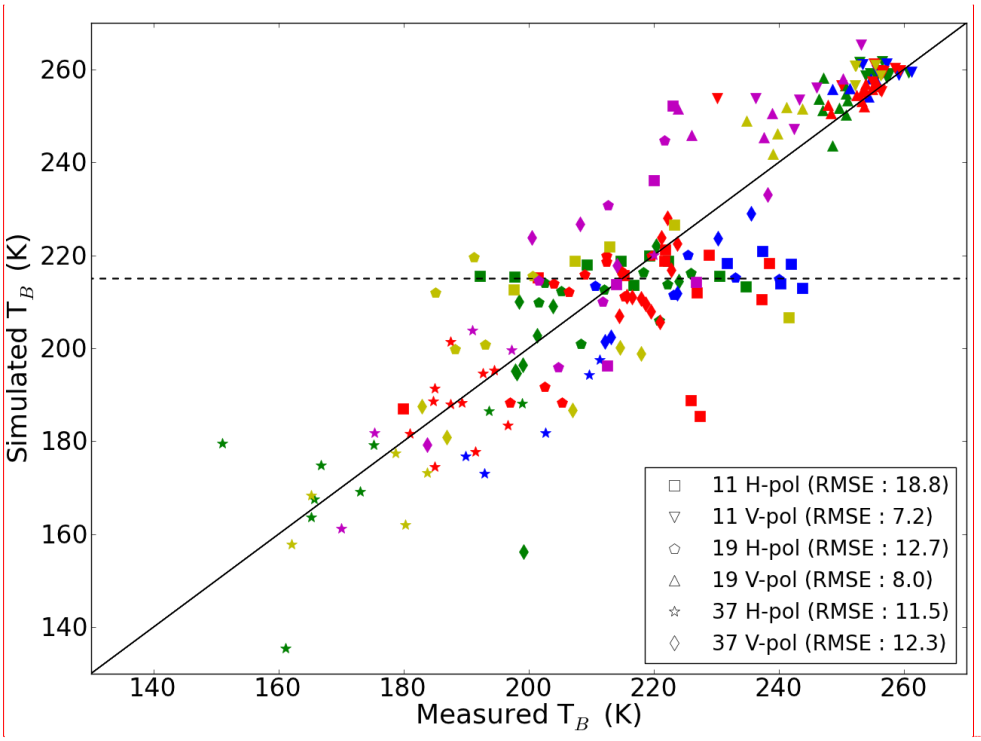

Fig. 6. T_B simulated with ice lenses included in DMRT-ML, but without bridging. The symbol types correspond to the frequency and colors to the sites: Red = $JB_{Jan\text{-}transect}$; Green = $JB_{Jan\text{-}others}$; Blue = JB_{Feb}; Yellow = JB_{Mar}; Magenta = UMI. The dotted black line represents the T_B where the simulations underestimated the spatial variability at 11 and 19 GHz H-pol.

3.1.2 Bridging

To test the bridging parameterization (see Sect 2.2.2), we used 13 tundra sites from the Churchill tundra database (Roy et al., 2013), 4 from Umiujaq and 2 from the James Bay snowpits. In each case, at least one snow layer with a snow density higher than 367 kg m^{-3} (ice fraction of 0.4: Dierking et al., 2012) is used. For each of the 19 sites studied, simulations at 37 GHz (the most sensitive frequency to snow) with and without the bridging implementation were conducted (all input parameters kept the same). The bridging has a relatively modest impact on simulations with an improvement in the RMSE of between 2 and 4 K at tundra sites (Umiujaq and James Bay). The greatest improvements are found for deep drifted tundra snowpits where there is a very thick wind slab with high ρ_{snow} and small rounded grains are present at the top of the snowpack.

3.2 Signal contributions and modeling uncertainties

Comment [AR2]: The dotted line was added

Comment [AR3]: The old Fig. 6 was removed (bridging scatterplot)

In the following, all DMRT-ML simulations consider the bridging implementation and include the observed ice lenses. Table 7 shows the overall RMSE for all campaigns that are described in Sect. 3.3.1 to 3.3.4. The RMSE values oscillate between 7.8 and 21.5 K at H-pol (Table 7). Since V-pol is less affected by layering in the snowpack at 11 GHz and 19 GHz, the RMSE are generally lower (between 3.5 and 14.4 K), while the RMSE at 37 GHz are similar at V-pol and H-pol. This is due to the higher sensitivity of higher frequencies to snow grain scattering when compared to the lower frequencies that are less affected by stratigraphy. Table 7 also suggests that the inclusion of bridging only decreases the RMSE by 0.5 K and 0.3 K at 37 GHz at H-pol and V-pol respectively (see Fig. 5). These RMSE will thus be used as a reference to quantify the effect of spatial variability and uncertainty in measurements on the T_B simulations.

Table 7: Overall RMSE (K) between measured and simulated T_B for all sites considering ice lenses and bridging in DMRT-ML.

	JB_{Jan}	JB_{Feb}	JB_{Mar}	UMI	All
11H	21.5	13.6	18.2	14.3	18.8
11V	6.4	5.5	6.3	9.8	7.2
19H	11.7	8.7	19.8	11.2	12.7
19V	3.5	5.7	9.2	13.4	8.0
37H	12.1	15.1	9.7	9.7	11.5
37V	7.8	15.3	14.4	16.8	12.3

3.2.1 Soil roughness

The analysis of small-scale soil variability in modeling the T_B of snow-covered surfaces is conducted using the SEex from the transect during the JB_{Jan} (mineral soil) and JB_{Feb} campaigns (organic soil). The JB_{Jan} SEex data represent the variability within a 30 m transect in a relatively homogeneous mineral soil area (quarry). The JB_{Feb} SEex were conducted at four different locations in clearings with organic soil and within about 1 km from each other. The strategy behind the evaluation of the small-scale spatial variability on snow-covered T_B is to first calculate the soil emission variability (optimization of σ) from SEex measurements. This variability is then introduced in the simulations with snow-covered surfaces to evaluate the sensitivity of T_B to variability in the emission of frozen soil.

For each SEex measurement, the surface roughness parameter σ was optimized using the three frequencies and both polarizations for bare soil measurements. The σ value was changed by increments of 0.01 cm, up to 1 cm (Eq. 3 and 4) and the associated $RMSE_\sigma$ was calculated as a function of the measured T_B (T_{Bmes}) and simulated T_B (T_{Bsim}) in V-pol and H-pol as follows:

$$RMSE_\sigma = \sqrt{\frac{\sum_{j=1}^{3}\sum_{i=1}^{N}(T_{B\,sim;i}^{jV} - T_{B\,mes;i}^{jV})^2 + (T_{B\,sim;i}^{jH} - T_{B\,mes;i}^{jH})^2}{6N}} \quad (5)$$

where j corresponds to the frequencies (j=1,2,3 respectively for 11, 19 and 37 GHz) and i corresponds to the sites. The optimal σ was determined by the lowest $RMSE_\sigma$ (Eq. 5) value for all sites at JB_{Jan} and JB_{Feb}.

The optimization was also done for each site individually to estimate the spatial variability in σ. The results presented in Fig. 7 show that a clear minimum in the $RMSE_\sigma$ can be found at every site. Fig 7 (right) shows that the optimal σ at $JB_{Jan\text{-}transect}$ values are located between 0.22 and 0.54 cm, while 0.31 is found for all 5 sites. The variability can be explained by the variation of the gravel size that affects the surface roughness. For JB_{Feb}, the observed spatial variability is more significant with variations ranging between 0.195 cm and 1.987 cm with an optimized σ = 0.411 cm for all 4 sites (Fig. 7 left). However, one should be careful in interpreting these results as the optimization could also compensate for uncertainties in the permittivity of frozen ground. Nevertheless, because the minimal and maximal values of optimized σ are taken, this does not affect our main goal, which is to estimate the variability in snow-covered T_B introduced by the soil in the model. Furthermore, as mentioned in Sect. 2.2.3, the permittivity used in this study were retrieved at the same site as this study.

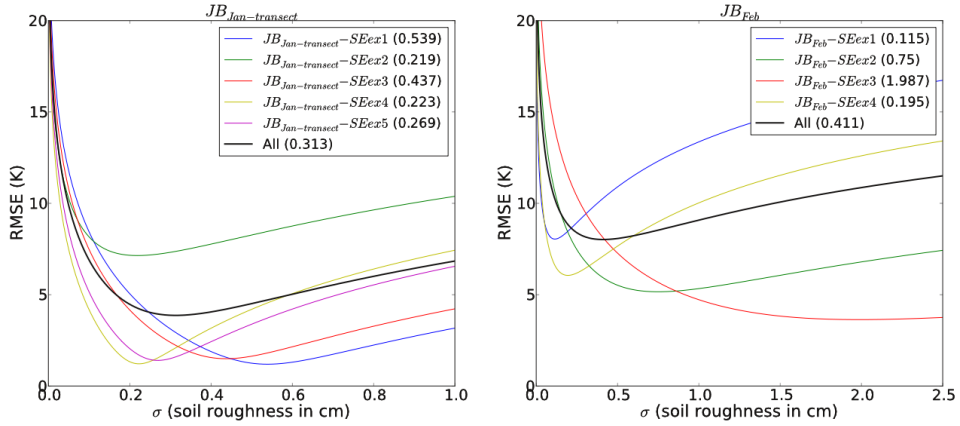

Fig. 7. $RMSE_\sigma$ for bare frozen soil sites (snow excavation experiment, SEex) as a function of soil roughness (σ) for (left) $JB_{Jan\text{-}transect}$ and (right) JB_{Feb}. The optimized σ for each site is given in parentheses.

We evaluated the small-scale spatial variability of soil emissivity resulting from the observed roughness variability. For the sites with observations taken with snow on the ground (Tables 1, 2, 3 and 5, for both campaigns), we simulated the T_B with DMRT-ML considering the lowest and highest optimized σ (see Fig. 7). Note that we have not used the standard deviation of σ that would have led to negative values. Fig. 8 (left) shows that the T_B sensitivity to the variation of soil roughness is very weak. T_B variations of 0.5 K and 1.3 K were observed at the $JB_{Jan\text{-}transect}$ site where the soil properties were more homogeneous (mineral soil), while a variation of 0.7 K to 3.8 K was measured at the JB_{Feb} site with organic soil (Table 8). The sensitivity is higher at 11 and 19 GHz because the soil emission is less attenuated by snow grain scattering. We also performed the same

calculation without the ice lens implementation where results are similar (less than 1 K change) suggesting that despite a potential low transmissivity, ice lenses are not responsible for the attenuation of the soil upwelling emission.

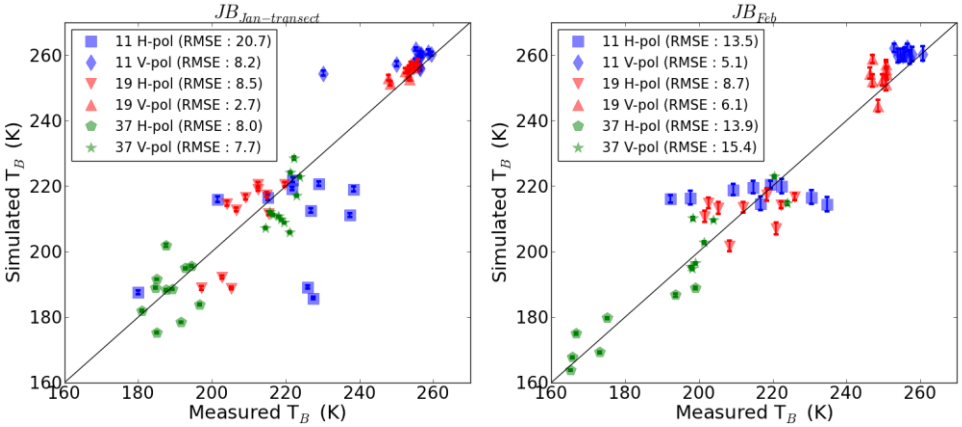

Fig. 8. Sensitivity of snow-covered surface T_B to the variation of soil roughness (σ) for (left) $JB_{Jan\text{-}transect}$ and (right) JB_{Feb}. The error bars show the variation of T_B for maximum and minimum optimized σ derived from SEex during both campaign (Fig. 7). The RMSE (K) values correspond to the retrievals using the initial (Table 6) σ value.

Table 8: T_B sensitivity (ΔT_B) (K) associated with the small-scale variability of soil roughness (σ).

	$JB_{Jan\text{-}transect}$	JB_{Feb}
11H	1.3	3.8
11V	1.3	3.8
19H	1.2	3.2
19V	1.4	3.5
37H	0.5	0.7
37V	0.6	0.7

The results show that the soil small-scale spatial variability is much lower than the RMSE for most of the frequencies and polarizations (Tables 7 and 8). However, for 11 and 19 GHz at V-pol, the soil-induced variability calculated during JB_{Feb} campaign leads to ΔT_B values (Table 8) similar to the measured RMSE (Table 7). Hence, the modeling error cannot be solely explained by small-scale variability in the emissivity of frozen soil, except possibly for 11 and 19 GHz at V-pol. However, these conclusions are only valid for frozen soils, but the higher dielectric contrast of thawed soil would have a greater impact on the emissivity of snow-covered surfaces.

3.2.2 Snow grain size

To test the sensitivity of the simulations to the grain size (SSA) measurement errors, the simulations considered an error of 12% in SSA when using the shortwave infrared reflection measurement approach as reported in Gallet et al. (2009). Hence two simulations were conducted: one with all SSA data along the profile increased by 12%

($T_{BSSA+12\%}$), and one with all SSA data decreased by 12% ($T_{BSSA-12\%}$). From these two simulations, the variation of T_B related to SSA errors (ΔT_{BSSA}: $T_{BSSA+12\%}$ - $T_{BSSA-12\%}$) was calculated, keeping in mind that this should be the maximum ΔT_B error, since the variations in SSA are all in the same direction for the whole profile. The soil parameterization is kept the same for all sites (see Table 6).

Figure 9 shows the error bars related to a variation of + 12% in SSA (upper bars: higher SSA leads to smaller grains and less scattering) and - 12 % (lower bars: lower SSA leads to larger grains and more scattering). The results show that 37 GHz is the most sensitive to the grain size with variations between 16.2 K and 27.4 K (Table 9). The variations are generally higher at V-pol, which has a higher penetration depth with less sensitivity to stratification and ice lenses. As such, 37 GHz is more influenced by large depth hoar grains at the bottom of the snowpack. Hence, because the relationship between the scattering and the particle size reaches a maximum sensitivity within the particle range (Picard et al. 2013), the variation of 12% for depth hoar SSA will cause a higher increase of ΔT_{BSSA}. In all cases, ΔT_{BSSA} are higher than the RMSE (Table 7) suggesting that grain size can explain the uncertainty in the T_B simulations.

At 19 GHz, there is an increase in ΔT_{BSSA} of about 7 K at V-pol and H-pol during the three James Bay campaigns. This increase of ΔT_{BSSA} is linked to snow grain metamorphism (Colbeck, 1983) that tends to increase the particle size through the winter (see Table 1, 2 and 3). With a higher sensitivity on the particle range and the dependence of scattering to the particle size, the variation of large grains will increase ΔT_{BSSA}. This phenomenon shows that at 19 GHz, the effect of SSA measurement uncertainty on T_B depends on the type of grains. For small snow grains in January, the error in SSA is small compared to the RMSE, which is not the case in March where the error is closest to the RMSE in the presence of larger grains. A very small increase of ΔT_{BSSA} is also seen at 11 GHz, but with much lower ΔT_{BSSA} (less than 1 K). These results show that scattering is negligible at 11 GHz for seasonal snow, even with large grains such as depth hoar.

We assessed average variation in T_B resulting from 100 runs with random error between ± 12% applied to SSA for each layer and snowpit. As expected, the results show that the variations between initial simulation and simulation with random error on SSA are significantly lower than those shown in Table 9. With random error applied on SSA measurements, the variations are lower than 1 K at 11 and 19 GHz, and between 2 and 3 K at 37 GHz. These values give the lower limits of T_B error related to SSA uncertainties, while values in Table 9 give the highest limit of the variation in T_B.

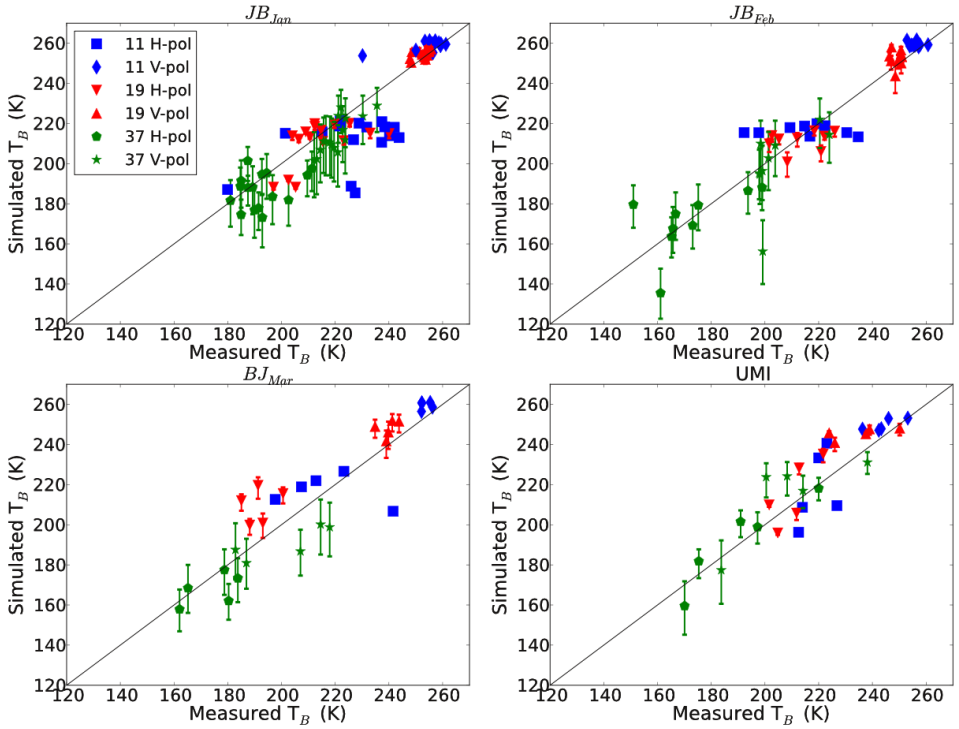

Fig. 9. T_B sensitivity associated to the error of SSA measurements (12%) for the James Bay (three dates) and Umiujaq sites.

Table 9: T_B sensitivity (ΔT_{BSSA}: $T_{BSSA+12\%}$ - $T_{BSSA-12\%}$) (K) associated with the error of SSA measurements

	JB_{Jan}	JB_{Feb}	JB_{Mar}	UMI
11H	0.3	0.7	1	0.5
11V	0.3	0.7	1.1	0.5
19H	2.8	6.5	10	4.5
19V	3.3	6.9	11.1	4.5
37H	21.2	21.6	22.5	16.2
37V	27.4	26.7	25.9	18.6

3.2.3 Snow density

A similar analysis was conducted to evaluate the T_B sensitivity to an error in ρ_{snow} of +/- 10% ($T_B\rho_{snow+10\%}$ and $T_B\rho_{snow-10\%}$). The ice lens density was left at 900 kg m^{-3} and the variations in T_B related to the ρ_{snow} error ($\Delta T_B\rho_{snow}$: $T_B\rho_{snow+10\%}$ - $T_B\rho_{snow-10\%}$) were calculated.

The highest sensitivity to ρ_{snow} is seen at 37 GHz (Fig. 10). The $\Delta T_B\rho_{snow}$ are about 13 K during the JB_{Jan} campaign and increase to 20 K for JB_{Mar} (Table 10). Again, this increase is explained by the growth in snow grain size due to snow metamorphism that leads to lower density values. In the given range of sphere sizes and ρ_{snow} at 37 GHz, the impact

of ρ_{snow} on T_B increases with a larger grain size (Fig. 3). These results show that the effect of ρ_{snow} at 37 GHz on DMRT-ML simulations depends on grain size and evolves throughout the winter due to snow metamorphism. It should, however, be noted that if the ice fraction limits of the bridging (Sect. 3.1.2) were extended to a lower ice fraction density, the impact for high ρ_{snow} would be lower or even the opposite, because of the increase in scattering due to bridging. Table 10 shows that $\Delta T_B \rho_{snow}$ are of the same magnitude as RMSE. Hence, depending on the grain size, ρ_{snow} can explain part of the error in the simulations.

At 11 and 19 GHz, the highest $\Delta T_B \rho_{snow}$ are found at H-pol with values around 7 K (Table 10). These highest values are related to the change in the permittivity discontinuity between layers, mostly at interfaces around the ice lenses leading to a change in the reflectivity at the different interfaces (Montpetit et al., 2013). Because V-pol is less affected by horizontal layering, the effect is smaller. Hence, the effect of ρ_{snow} uncertainty on T_B is lower than the measured RMSE at 11 and 19 GHz, but has a significant impact on T_B at H-pol. These results are in agreement with studies that show that the microwave polarization ratio (H-pol/V-pol) can potentially be used for snow density retrievals (Champollion et al., 2013; Lemmetyinen et al., submitted).

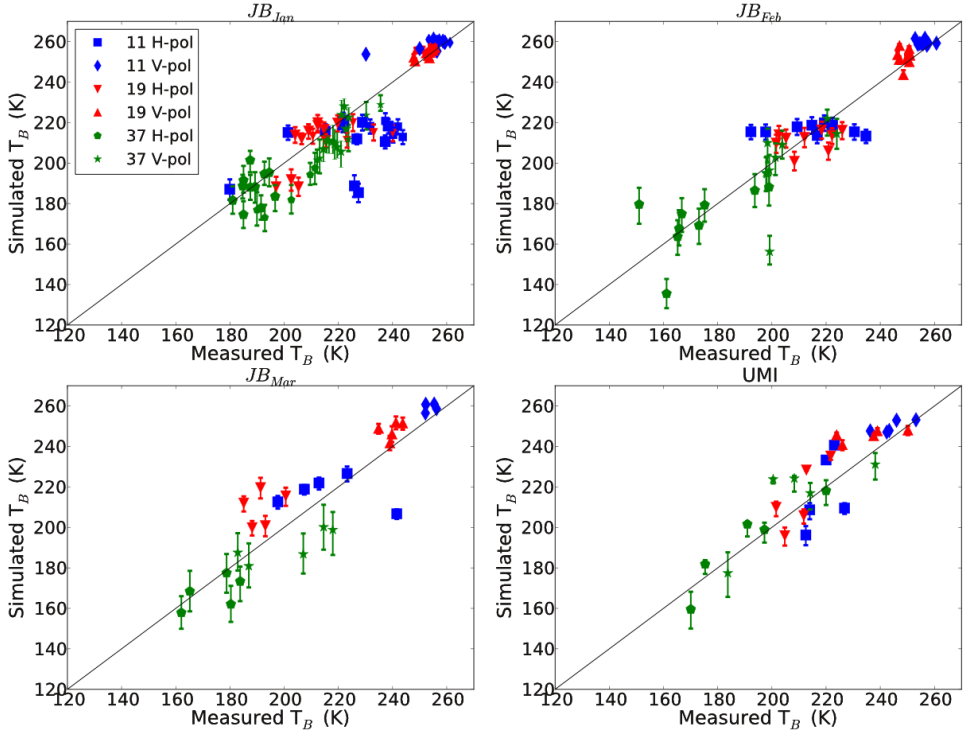

Fig. 10. T_B sensitivity associated with the error in snow density measurements (±10%). The ice lens density remains at 900 kg m^{-3}.

Table 10. T_B sensitivity ($\Delta T_B\rho_{snow}$: $T_B\rho_{snow+10\%}$ - $T_B\rho_{snow-10\%}$) (K) associated with the error in snow density measurements

	JB_{Jan}	JB_{Feb}	JB_{Mar}	UMI
11H	7.6	7.5	5.6	6.1
11V	1.4	1.4	2.1	1.9
19H	8	8.8	8.3	6.2
19V	2.4	3.2	6.7	3.6
37H	13.5	16.5	18.4	11.6
37V	12.6	15.3	21.4	13.4

3.2.4 Ice lenses

While including ice lenses in DMRT-ML significantly reduces the RMSE (section 3.1.1), the underestimation of T_B variability remains strong at 11 and 19 GHz. Given that the remaining bias cannot be explained by the soil, grain size or ρ_{snow} (Sect. 3.3.1, 3.3.2 and 3.3.3), we further explore here the role of ice lenses. The ice lens density (ρ_{IL}) variations can explain part of the variability as the density of ice influences the internal reflection (Durand et al., 2008; Rutter et al., 2013). In fact, ice lenses can be snow crusts with a density as low as 630 kg m^{-3} (Marsh and Woo, 1984). However, measuring the density of such layers is challenging and it was not attempted during our campaigns. The sensitivity was evaluated for a range of ice density between 700 kg m^{-3} ($T_B\rho_{IL700}$) and 917 kg m^{-3} ($T_B\rho_{IL917}$) for all snowpits with ice lenses. The variation of T_B related to ρ_{IL} uncertainties ($\Delta T_B\rho_{IL}$: $T_B\rho_{IL917} - T_B\rho_{il700}$) was then calculated (all other parameters being constant).

Figure 11 shows that ρ_{IL} variations have a significant impact on H-pol T_B mostly at 11 and 19 GHz. The low $\Delta T_B\rho_{IL}$ at 37 GHz (Table 11) is not related to the insensitivity of 37 GHz to ice lenses, but rather to the attenuation owing to snow grains dominating the effect of ice lenses. In fact, Table 11 shows that the effect of the variation of ice lens density decreases throughout the winter at James Bay because of increasing attenuation related to grain size metamorphism. It should be noted that no scattering occurs in these layers in the model because the R_{eff} was kept null. Hence, ρ_{IL} can only explain the underestimation of T_B, not the overestimation. Part of the error could be explained by the coherence that is not taken into account in DMRT-ML. The coherence is caused by multiple reflections within a thin layer and associated interference when the thickness of the ice lenses is less than a quarter of the wavelength ($\lambda/4$) (Mätzler et al., 1987; Montpetit et al., 2013). Since DMRT-ML does not take into account the coherence, the thickness of the ice layer has a negligible impact on T_B and was kept at 1 cm. However, simulations with MEMLS accounting for coherence have shown that variation in the ice lens thickness can change T_B by up to 100 K at H-pol at 19 and 37 GHz (Montpetit et al., 2013). Also, in this study, only the main ice lenses were noted and inserted in DMRT-ML. Many other melt/refreeze thin snow crusts were present but not recorded, and they can have a large impact on T_B observations (see Rutter et al., 2013). These thin crusts (less than 2 mm) with a high density (over 600 kg m^{-3}) can also have significant coherence effects (less than $\lambda/4$).

During the JB_{Jan} campaign, at the transect, two ice lenses were observed at three consecutive snowpits (JB_{Jan}-6.7, JB_{Jan}-6.8 and JB_{Jan}-6.9). The simulations at these sites show the three lowest simulated T_B at 11 GHz and 19 GHz at H-pol (Fig. 11). The second observed ice lens inserted in DMRT-ML significantly decreases the simulated T_B. Including the second observed ice lens allows an improvement in the T_B simulation at JB_{Jan}-6.8 (Table 1), while the accuracy decreases for the two other snowpits, especially at 11 GHz. These results show the importance of small-scale spatial variability in the distribution of ice lenses. In this case, since the SBR footprint is not exactly where the snowpit was dug, the 11 GHz measured the two ice lenses at JB_{Jan}-6.8, but not at JB_{Jan}-6.7 and JB_{Jan}-6.9. Rutter et al. (2013) showed that such small-scale discontinuities in ice lenses have a strong impact on T_B.

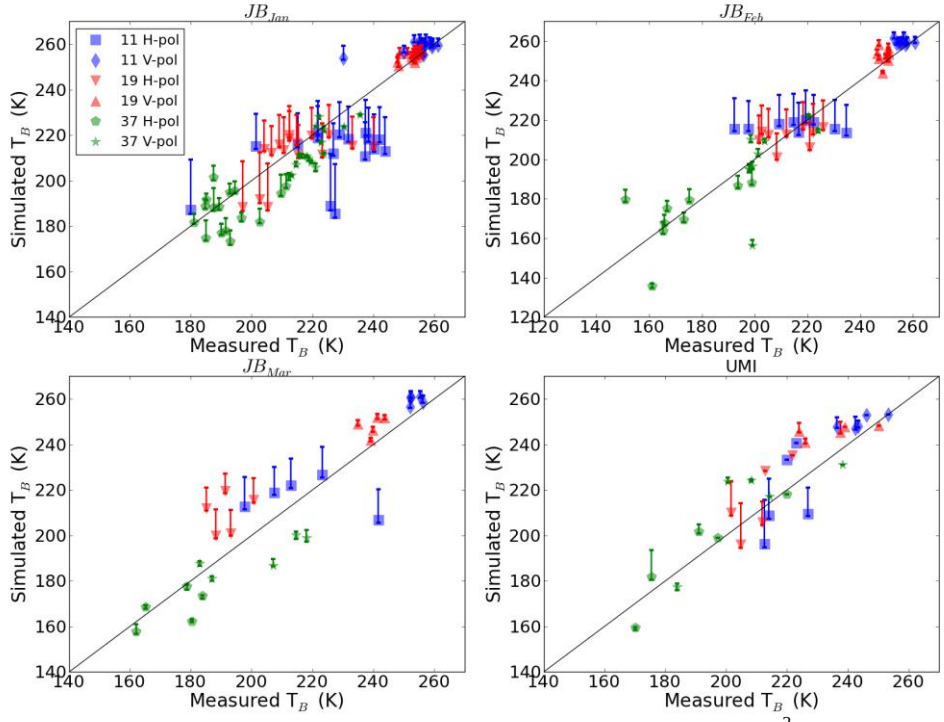

Fig. 11. T_B sensitivity associated with the ρ_{IL} variation (700 to 917 kg m^{-3}).

Table 11. T_B sensitivity ($\Delta T_B \rho_{IL}$: $T_B\rho_{IL917} - T_B\rho_{il700}$) (K) associated with the ρ_{IL} variation (700 to 917 kg m^{-3})

	JB_{Jan}	JB_{Feb}	JB_{Mar}	UMI
11H	17	15.9	11.9	13.4
11V	3.7	3.1	2.6	3.5
19H	15.4	14.3	9.2	12.1
19V	3.2	2.4	1.8	3.1
37H	6.4	5.7	1.2	6.1
37V	0.8	1.5	1.7	1.1

3.2.5 Surrounding vegetation effects

In a forested area, tree emission reflected by the snowpack can significantly contribute to the measured T_B on the ground (Roy et al., 2012). An analysis was conducted on 18 site measurements taken in a forest during the three James Bay campaigns (Table 4) to quantify the forest contributions to measured T_B using DMRT-ML. A first simulation, neglecting the emission coming from the trees in the downwelling T_B (T_{Bdown}) reflected by the surface was conducted. Figure 12 shows a clear underestimation (biases ≈ 40 K at H-pol) of simulated T_B at all frequencies, except for 11 and 19 GHz at V-pol. Table 12 shows that these biases are much greater than the uncertainties induced by the snow cover in open areas, showing that the tree emission reflected by the surface significantly increased the measured T_B. The low influence of vegetation (low $bias_{forest}$: Table 12) at 11 and 19 GHz V-pol is explained by the fact that the reflectivity of the surface at these frequencies is very low because the volume scattering is weak and the reflectivity at the interfaces is close to zero near the Brewster angle.

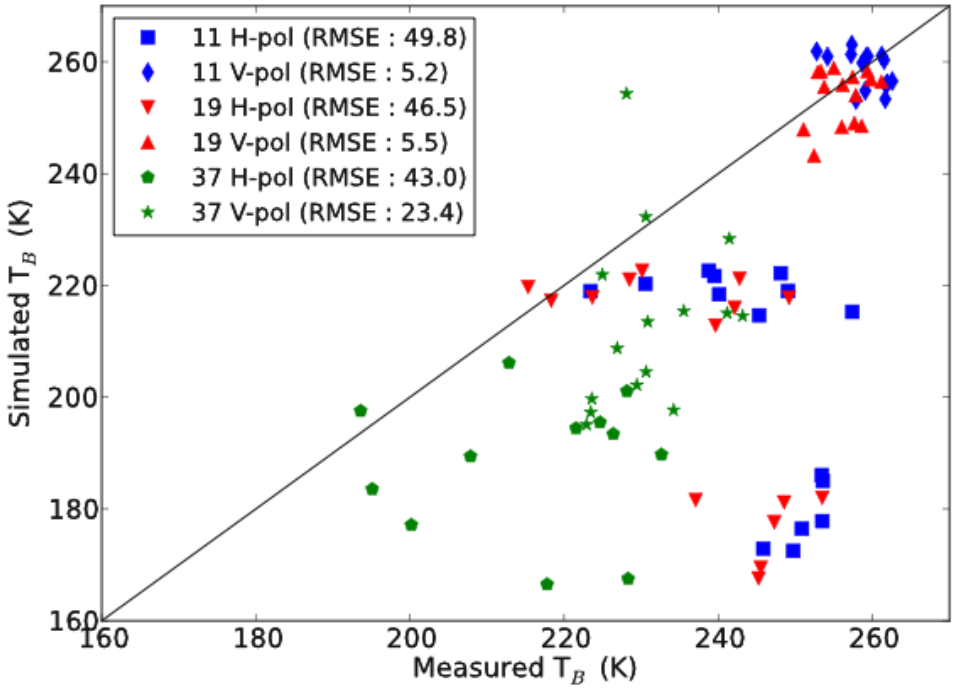

Fig. 12. Simulated T_B in forested sites neglecting the vegetation contribution (T_{Bdown}).

Table 12. Comparison between the calculated biases in an open area and in a forested area

	$Bias_{open}$	$Bias_{forest}$
11H	4.7	-41.7
11V	-4.0	-1.1

19H	-4.0	-35.9
19V	-5.7	-3.4
37H	2.2	-37.4
37V	3.3	-21.4

To quantify the forest contribution, the T_{Bdown} was inverted with DMRT-ML. From the simulated T_B neglecting the forest contribution (Fig. 12), an iteration process was performed to find the T_{Bdown} value that minimized the $RMSE_{veg}$ between simulated and measured T_B at V-pol and H-pol for each frequency independently:

$$RMSE_{veg} = \sqrt{\frac{\sum_{i=1}^{N}(T_{B\,sim;i}^{fV} - T_{B\,mes;i}^{fV})^2 + (T_{B\,sim;i}^{fH} - T_{B\,mes;i}^{fH})^2}{2N}} \quad (6)$$

where *f* is the frequency.

Table 13 shows that the averaged optimized T_{Bdown} are 147 K, 120 K and 110 K respectively at 11, 19 and 37 GHz. The optimized T_{Bdown}, however, decrease with frequency, which is opposite to what was shown in other studies (Kruopis et al., 1999; Roy et al., 2012; Roy et al., 2014). This is probably related to the inherent error in the snow surface T_B simulation in DMRT-ML (Table 7), which induces error in the calculation of the reflectivity of the snow-covered surface.

Table 13. Average optimized T_{Bdown} and standard deviation (in parentheses) (K)

	11 GHz	19 GHz	37 GHz
T_{Bdown} (K)	147 (±64)	120 (±74)	110 (±43)

Table 13 also shows that there are large variations between the different snowpits with a standard deviation between 43 K and 74 K. The average T_{Bdown} of the three frequencies was calculated for each site and compared with χ_{veg} obtained from fisheye pictures taken at the twelve JB_{veg} sites in January and February (fisheye pictures were not taken in March). Figure 13 shows that there is a good correlation (R^2 = 0.75) between averaged T_{Bdown} (mean for the three frequencies) and χ_{veg}. These results confirm that the optimized T_{Bdown} are related to the tree emission reflected by the surface (see an example of variations in Fig. 1). For comparison, the calculated atmospheric downwelling contributions were around 6 K at 11 GHz and 25 K at 37 GHz. It also shows the potential of using fisheye pictures to quantify tree microwave emission in boreal forests. However, further considerations are necessary to improve the method. Because of the non-Lambertian component of the snow reflection and the non-homogeneity of the trees surrounding the site measurements, the direction (azimuth) in which the SBR is pointing has an important influence on the signal (Courtemanche et al., 2015). DMRT-ML assumed that the T_{Bdown} is isotropic, and does not take into account these specular components. For example, the T_B will be higher if the SBR is pointing in the direction of a large trunk close to the snowpit instead of pointing in the direction of a forest opening.

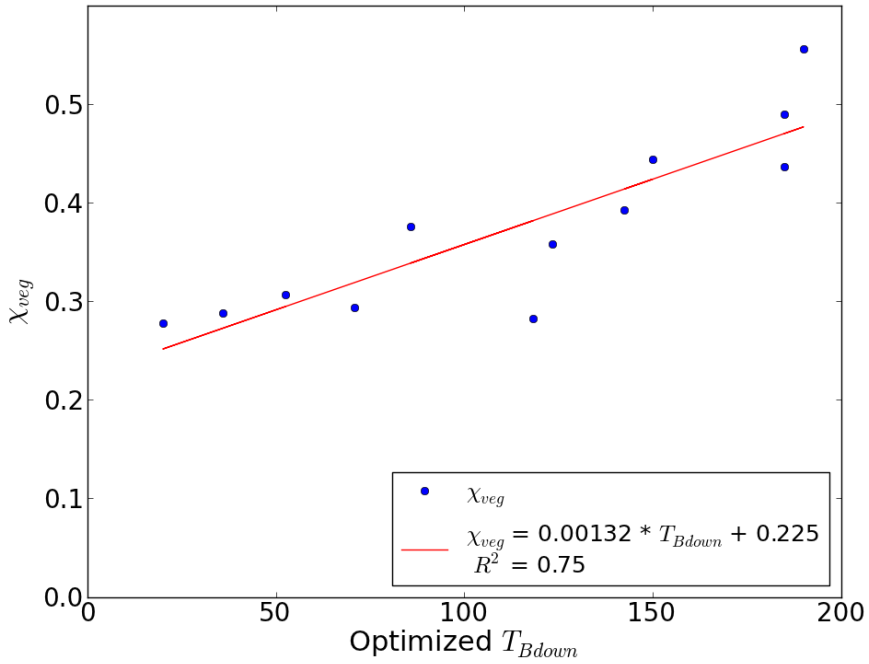

Fig. 13. Relationship between the average T_{Bdown} of the three frequencies and the proportion of pixels occupied by vegetation (trees) in the fisheye pictures (χ_{veg}) for the 12 JB_{veg} sites in January and February.

4. Discussion / conclusion

This study presents a comprehensive analysis of the geophysical parameters contributing to uncertainty in DMRT-ML for snow-covered surfaces in boreal forest, subarctic and arctic environments. A unique in situ database, including key information on the snowpack temporal winter evolution, allowed the assessment of the impact of spatial variability of 1) soil emission, 2) errors in snow grains and 3) density measurements, 4) ice lenses and 5) vegetation emission reflected from the surface on DMRT-ML simulations.

The implementation in DMRT-ML of the bridging aiming at filling the gap between low and high snow density ranges where the theory is invalid has been tested. Bridging leads to a small improvement for tundra snow where wind slabs are present. These improvements are modest and could compensate for the measurement uncertainties or other limitations related to the use of the model such as stickiness and grain size distribution (Roy et al., 2013). Based on the work of Dierking et al. (2012), the range of the ice fraction where bridging was applied was limited to 0.4 - 0.6, but could be extended and lead to a stronger impact of bridging on the results (Tsang et al., 2008). But as shown in this study, the uncertainties in measurements make it difficult to make sure

740 that any optimization of the bridging range does not compensate for other uncertainties.
741 In practice, this new version of DMRT-ML with bridging facilitates simulation of snow
742 and/or ice without identification of the snow layer state.
743
744 Based on several snow removal experiments, the study shows that small-scale variability
745 in soil emissivity in a boreal forest has a second order effect on the snow-covered surface
746 T_B when the soil is frozen, even for lower frequencies that are more transparent to the
747 snowpack (11 and 19 GHz). In practice, this implies that the use of constant soil
748 parameters for frozen soil emission modeling for a given environment is adequate for
749 snow emission studies. This result is surprising since soil roughness, soil wetness,
750 freeze/thaw state and stratigraphy are usually difficult to measure in boreal conditions.
751 However, further experiments should be done to validate this aspect for other types of
752 environments. Exploring larger scales could help to determine at what scale soil
753 emissivity has an influence on snow-covered T_B.
754
755 This study shows the strong sensitivity of DMRT-ML to snow grain size and density at
756 37 GHz, and that the error related to the measurements can explain most of the RMSE at
757 this frequency and probably at higher frequencies. These results are in agreement with
758 studies using MEMLS (Durand et al., 2008) and HUT (Rutter et al., 2013; Lemmetyinen
759 et al., 2015). It remains difficult to distinguish the sources of error related to DMRT-ML
760 simulations at 37 GHz. The study, however, underlines that measurement error limits the
761 accuracy of the simulations. The error related to the physical simplifications in DMRT-
762 ML was not investigated in this work, but our results suggest that the level of confidence
763 of measurements is too low to test or significantly improve the DMRT-ML physics. In
764 this study, SSA was used because it is a robust and objective metric that can be measured
765 effectively on the field. However, the derived R_{opt} metric used in DMRT-ML is related to
766 an optical definition (Grenfell and Warren, 1999) and might not represent the grain for
767 microwave wavelength (Mätzler, 2002). Further experiments on isolated snow layers as
768 done by Wiesmann et al. (1998) but using new tools for snow microstructure
769 parameterization could be applied to improve the physics of emission models. For
770 example, more precise measurements of snow microstructure like X-ray tomography
771 (Heggli et al., 2011) and the snow micro-penetrometer (SMP) (Schneebeli et al., 1999;
772 Proksch et al., 2015) could be the next step to improve the understanding of the physics
773 in DMRT-ML (e.g., Lowe and Picard, 2015). However, each snow microstructure
774 measurement method has its own limitations. Combining the different information could
775 be an avenue to better quantify the snow scattering mechanism in DMRT-ML.

776 This analysis confirms that the scaling factor ($\phi = 3.3$) proposed by Roy et al. (2013) is a
777 general value as it yields accurate results with the new data set presented in this paper.
778 We do not pretend that this value exactly applies to other environments as Picard et al.
779 (2014) found a lower value (2.3) for Antarctica with a SSA measurement technique that
780 was inter-calibrated with ours. The temporal analysis during the three campaigns in
781 James Bay, however, shows that the sensitivity to snow measurement uncertainties
782 evolve during winter due to snow metamorphism. This sensitivity change is also
783 important at 19 GHz. Although snow is almost transparent at this frequency at the
784 beginning of winter when the grains are small, T_B at 19 GHz becomes sensitive to snow
785 in March because of snow grain growth. This could be of interest for the SWE retrieval

786 approach, knowing that 19 GHz T_B becomes sensitive to snow when snow grains become
787 larger. As proposed in Derksen (2008) 11 and 19 GHz frequencies could be usefull for
788 SWE retrievals for deep snow to overcome the problem of saturation at 37 GHz (see
789 Rosenfeld and Grody, 2000). At 11 GHz, snow is almost transparent throughout the
790 winter demonstrating the utility of this band for monitoring soil conditions (phase,
791 temperature) under the snow (Kohn and Royer, 2010).
792
793 The inclusion of ice lenses in DMRT-ML significantly improves the simulations at H-
794 pol. However, the model is not able to reproduce the observed spatial variability at 11
795 and 19 GHz at H-pol, which was shown to be related to snowpack stratigraphy
796 inaccuracies, mostly related to ice lenses and strong variations in snow density (for
797 example, thin snow crust). The large spatial variability of ice lenses and snow crusts at
798 the meter scale (Rutter et al., 2013) can lead to the strong spatial variability of observed
799 T_B. This ice lenses and snow crust spatial variability raise the need to develop efficient
800 and practical methods to effectively characterize ice lenses and thin snow crusts,
801 especially their density (Marsh and Woo, 1984). Using short-wave infrared photography
802 (Montpetit et al., 2012) or SMP profiles (Proksch et al., 2015) are possible options. The
803 coherence, which is not taken into account in DMRT-ML, is responsible for a large
804 sensitivity of T_B to ice lens thickness and can explain the observed T_B variability at 19
805 and 11 GHz at H-pol. The implementation of the coherence in DMRT-ML is not difficult,
806 but collecting the input variables in the field remains the major challenge.
807
808 In boreal forest areas, our analysis shows that the vegetation emission reflected by the
809 snow-covered surface can contribute more than 200 K and that neglecting the reflection
810 of the signal on the snow surface can lead to a bias of up to 40 K, mostly at H-pol where
811 the surface reflectivity is the highest. This bias is coupled to the snow state, depending on
812 the snow reflectivity. These results clearly show the importance of the vegetation
813 contribution and avoiding this contribution in measurements imply to operate in clearings
814 with minimal forest cover mostly on the opposite side of the measurements (specular
815 contributions). However, some promising results on the use of fisheye photographs to
816 quantify that vegetation contribution were shown. The use of a Lambertian microwave
817 surface for retrieving the downwelling contribution in ground-based radiometric
818 measurements (Courtemanche et al., 2015) may also be a promising avenue.
819
820 To the best of our knowledge, this is the first time that an analysis has been carried out of
821 all the elements (soil, grain size, snow density, ice lenses, and vegetation) that contribute
822 to the microwave signal at three frequencies (36.5, 18.7 and 10.65 GHz) in a boreal
823 forest. The study sheds light on DMRT-ML uncertainties related to small-scale variability
824 and measurement errors in different environments and for different periods in the winter.
825 Some limitations were raised on the accuracy of DMRT-ML to simulate the T_B of snow-
826 covered surfaces, and this analysis will help to design future studies to improve the
827 ability of DMRT-ML and other MESM to model the radiative transfer processes of snow-
828 covered surfaces.
829
830
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