

# Monitoring Ice Break-Up on the Mackenzie River Using MODIS Data

**P. Muhammad<sup>1</sup>, C. Duguay<sup>1</sup>, and K.-K. Kang<sup>1</sup>**

Department of Geography & Environmental Management and the Interdisciplinary

Centre on Climate Change (IC<sup>3</sup>), University of Waterloo, Waterloo, ON, Canada

Correspondence to: [pmuhamma@uwaterloo.ca](mailto:pmuhamma@uwaterloo.ca) (P. Muhammad);

[crduuguay@uwaterloo.ca](mailto:crduuguay@uwaterloo.ca) (C. Duguay)

# Abstract

The aim of this study was to develop an approach for estimating ice break-up dates on the Mackenzie River (MR) using more than a decade of MODIS Level 3 500-m snow products (MOD/MYD10A1), complemented with 250-m Level 1B radiance products (MOD/MYD02QKM) from the Terra and Aqua satellite platforms.

The analysis showed break-up began on average between DOY 115-125 and ended DOY 145-155 over 13 ice seasons (2001-2013), resulting in an average melt duration of ca. 30-40 days. Thermal processes were more important in driving ice break-up south of the MR confluence with the Liard River, while dynamically driven break-up was more important north of the Liard.

Comparison of the timing of ice disappearance with snow disappearance from surrounding land areas of the MR with MODIS Level 3 snow products showed varying relationships along the river. Ice-off and snow-off timing were in sync north of the MR-Liard River confluence and over sections of the MR before it enters the Mackenzie Delta, but ice disappeared much later than snow on land in regions where thermal ice break-up processes dominated.

MODIS observations revealed that channel morphology is a more important control of ice break-up patterns than previously believed with ice runs on the MR

strongly influenced by channel morphology (islands and bars, confluences and channel constriction).

- 25 Ice velocity estimates from feature tracking were able to be made in 2008 and 2010 and yielded 3-4 day average ice velocities of 1.21 ms<sup>-1</sup> and 1.84 ms<sup>-1</sup> respectively in agreement with estimates from previous studies.

- These preliminary results confirm the utility of daily MODIS data for monitoring  
30 ice break-up processes along the Mackenzie River. The addition of optical and synthetic aperture radar (SAR) data from recent and upcoming satellite missions (e.g., Sentinel-1/2/3 and RADARSAT Constellation) would improve the monitoring of break-up in narrower sections of the MR.

## 35 1 Introduction

- The Mackenzie River Basin (MRB) is the largest in Canada and is subject to one of the most important hydrologic events annually. River ice break-up on the Mackenzie River is a process by which upstream (lower latitude) ice is pushed downstream while intact ice resists movement downstream (higher latitude)  
40 (Beltaos and Prowse, 2009). Ice break-up is defined as a process with specific dates identifying key events in space and time between the onset of melt and the complete disappearance of ice in the river. This is the definition used in previously

published literature and which will be applied in this paper. Break-up is often associated with flooding in north flowing systems and is thus an important hydrologic event with many environmental benefits (e.g. geochemical land deposition and lake and groundwater recharge) and detriments (e.g. infrastructure damage and lost economic activity) (Prowse, 2001; Kääb et al., 2013). Investigations of river regimes in high latitude countries including Canada, the United States, Russia and Sweden and Finland have a long history related to their ice monitoring (Lenormand et al., 2002). This is important as ice freeze-up and break-up records serve as climate proxies responding to changing air temperature patterns (Magnuson et al., 2000). The ice break-up process is nonetheless under-monitored. There is therefore a gap in knowledge when attempting to understand all associated hydrologic parameters due to their highly dynamic nature (Beltaos et al., 2011).

The shortage of ice observations on the Mackenzie River and other rivers and lakes in Canada is partly the result of budget cuts, which have led to the closing of many operational hydrometric stations (Lenormand et al., 2002). Specifically, ice freeze-up and break-up observations peaked during the 1960-1990s and declined dramatically thereafter following budget cuts from the federal government (Lenormand et al., 2002). In the last decade only, the observational network of discharge and ice measurements on the MRB has declined from 65 to 15 stations. Satellite remote sensing is a viable tool for filling this observational gap. For example, Pavelsky and Smith (2004) were able to monitor ice jam floods and



break-up events discontinuously over a 10-year period (1992–1993, 1995–1998, and 2000–2003) on major high-latitude north-flowing rivers at 500-m and 1-km spatial resolutions (the Lena, Ob', Yenisey and Mackenzie rivers) using MODIS and Advanced Very High Resolution Radiometer (AVHRR) imagery. Similarly, Chaouch *et al.* (2012) showed the potential of MODIS (0.25 and 1 km spatial resolutions) for monitoring ice cover on the Susquehanna River (40°-42° N), USA, from 2002-2010. Kääb and Prowse (2011) and Kääb *et al.* (2013) have also shown the effectiveness of remote sensing data acquired at 15-m, 2.5-m and 1-m spatial resolutions using Advanced Spaceborne Thermal Emission and Reflection Radiometer (ASTER), Panchromatic Remote-sensing Instrument for Stereo Mapping (PRISM) and IKONOS, respectively, for estimating river ice velocities. However, these previous studies have been limited to spaceborne stereographic datasets capturing a few ideal (cloud-free) images a year and including revisit times ranging from 2-16 days, making detailed temporal studies difficult. Despite these recent advances, studies have yet to be conducted monitoring ice freeze-up and break-up processes by satellite remote sensing over longer periods (i.e. continuously over several years).

The aim of the present study was therefore to develop an approach to estimate key ice break-up dates (or events) on the Mackenzie River (MR) over more than a decade using Moderate Resolution Imaging Spectroradiometer (MODIS) data. The paper first provides a description of the procedure developed to monitor ice break-up on the MR. This is followed by a quantification of ice-off dates (spatially and

temporally) provided by MODIS data. Next, average ice-off dates are compared for  
**90** a 13-year period (2001-2013). Lastly, displacement of ice runs calculated with  
MODIS is used to estimate average ice velocity along sections of the MR.

## 2 Methodology

### 2.1 Study Area

The geographical area of this study focuses on the Mackenzie River extending from the western end of Great Slave Lake (61.36° N, 118.4° W) to the Mackenzie Delta (67.62° W, 134.15° W) (Figure 1). The study area encompasses the main channel and confluences of the river, including any smaller rivers that feed the Mackenzie. Currently, only 4 hydrometric stations measure water level and ice on the main channel (1100 km long) of the Mackenzie River north of Great Slave Lake. A fifth station located at Fort Providence was shutdown in 2010 (Government of Canada, 2010). The MRB forms the second largest basin in North America extending beyond the Northwest Territories at  $1.8 \times 10^6 \text{ km}^2$  (Government of Canada, 2007). Approximately 75% of the MRB lies in the zones of continuous and discontinuous permafrost with many smaller sub-basins adding to flow at different time periods during the break-up season (Abdul Aziz and Burn, 2006). The MRB experiences monthly climatological (1990-2010) averages of -20 to -23 °C air temperature between the months of December to February, respectively (Dee et al., 2011). Air temperature increases to an average of - 5 °C in April with the initiation of ice break-up near 61° N.

Air temperature plays an important role on the timing of spring freshet (Beltaos and Prowse, 2009; Goulding et al., 2009b; Prowse and Beltaos, 2002) in

the MRB. It has therefore been associated with increased flow and the initiation of ice break-up in the basin as a result of snowmelt onset (Abdul Aziz and Burn, 2006). In thermal (over-mature) ice break-up, there is an absence of flow from the drainage basin earlier in the melt season, and the ice remains in place or is entrained in flow until incoming solar radiation disintegrates the river ice increasing water temperatures (Beltaos, 1997). This slow melting process causes a gentle rise in discharge on a hydrograph, with flooding found to be less frequent during that period (Goulding et al., 2009a). In dynamic (premature) ice break-up, the accumulation of snow on the drainage basin is higher and the stream pulse (or spring freshet) from snowmelt is characterized by a high slope on the rising limb of the hydrograph (Goulding et al., 2009b; Woo and Thorne, 2003). In the presence of thick ice downstream, flow can be impeded causing a rise in backwater level and flooding upstream. However, when ice resistance is weak downstream, stress applied on the ice cover can rise with increasing water levels fracturing and dislodging ice from shorelines continuing downstream, eventually disintegrating downstream (Hicks, 2009). This process can continue until certain geometric constraints such as channel bends, narrow sections and islands can stop the ice run causing ice jams (Hicks, 2009). Here, the wide-channel jam is the most common of dynamic events which develops from the flow shear stress and the ice jams' own weight, which is formed by the collapse and shoving of ice floe accumulation and is resisted by the internal strength of the accumulation of ice flows (Beltaos, 2008). As the jam builds with ice rubble, the upstream runoff forces can increase above the downstream resistance releasing the jam and creating a wave downstream that

45 raises water levels and amplifies flow velocities (Beltaos et al., 2012).  
Observations have shown an initial increase and final decrease in water levels as  
wave celerity and amplitude attenuates downstream (Beltaos and Carter, 2009). In  
general, thermal decay and ice break-up process continue downstream after the ice  
jam release (Hicks, 2009). MODIS imagery has also shown the timing of spring  
50 flood and location of open water tributaries to have the most impact on ice break-  
up processes (Pavelsky and Smith, 2004).

## 2.2 MODIS Data and Processing

A processing chain was developed in order to determine ice presence or absence  
55 (open water) on the Mackenzie River. As seen in Figure 2, MOD/MYD10A1 Level  
3 (primary data set, 500-m) was processed in the MODIS Reprojection Toolkit in  
order to extract specific subsets of scientific data sets (snow, river ice, cloud, open  
water as seen in Table 2), perform geographic projections and write output files.  
Here, the primary data set was resampled using the nearest neighbour method and  
60 reprojected to the UTM projection. In the presence of cloud free images and  
images where cloud was not covering the MR, open water observations were  
recorded on the Mackenzie River. Observations were manually performed along  
the MR by visual interpretation wherever a cross-section of the river was partially  
or entirely ice-free. When cloud cover was found to be present in the primary  
65 dataset, which limited ice observations, MOD/MYD02QKM Level 1B (secondary  
data set, consisting of Band 1 and Band 2 at 250 m resolution) was used. This  
MODIS product was processed using the MODIS Conversion Toolkit in the

ENVI/IDL package (nearest neighbour method/UTM projection). Finally, in the presence of high cloud cover in the secondary data set no observations were recorded.

Through visual interpretation varying land attributes DN values (snow, river ice, cloud, open water) in the MOD/MYD02QKM were defined from MOD/MYD10A1 SDS values of the same land attributes. Observing and comparing the same areas of interest and dates from MOD/MYD10A1 and MOD/MYD02QKM images as seen in Table 2 completed this process. For example, MOD/MYD10A1 images ice cover at a SDS reading of 100 (river ice) was matched to a DN value ranging from 40-110 from the MOD/MYD02QKM images.

### 2.2.1 MODIS Data

MODIS images, for the period from one week before to one week after the ice break-up period had ended over the MRB from 2001-2013, were downloaded from the National Aeronautic and Space Administration's (NASA) Earth observing System Data and Information System (EOSDIS) (<http://reverb.echo.nasa.gov/reverb/>) for processing. This study used 500-m (primary data) and 250-m (secondary data) spatial resolution MODIS data acquired from both the Aqua and Terra satellite platforms. More specifically, MODIS L1B (MYD02QKM/MOD02QKM) and MODIS Snow Product (L3)

(MYD10A1/MOD10A1) datasets were retrieved for analysis. In this paper, the  
90 MODIS will generally be referred to as L3 and L1B.

The use of L3 data product from a single MODIS sensor (Aqua or Terra)  
limited the potential to obtain frequent ice break-up observations as a result of  
cloud cover conditions. However, using L3 product from both Aqua and Terra  
95 satellites across varying orbital tracks in combination with the L1B product greatly  
increased the number of observable events during the ice break-up period, up to  
more than 90 percent of available images. MODIS acquisitions from both the Aqua  
and Terra satellites doubled the number of images available during clear-sky  
conditions. In addition, the availability of MODIS L1B data from Aqua and Terra  
100 further increased the number of available images for analysis (i.e. cases where ice  
could be seen under thin clouds).

### 2.2.2 MODIS Data Processing

Cloud cover presence was one of the few incidences where image  
105 processing was limited. This has also been previously reported (Riggs et al., 2000)  
where cloud cover in the Arctic limited data acquisition from the study site. This,  
in combination with coarse-resolution cloud cover masks resulted in 5-10% of the  
images being omitted from analysis. Problems in snow detection arise when  
spectral characteristics important in the use of the normalized difference snow  
110 index (NDSI) make it difficult to discriminate between snow and specific cloud  
types (Hall et al., 2006). NDSI is insensitive to most clouds except when ice-

containing clouds are present, exhibiting a similar spectral signature to snow. Hence, some MOD35/MYD35\_L2 cloud mask images presented conservative over-masking of snow-cover on cloudy and foggy days (Hall et al., 2006).

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To improve temporal coverage, ice-off observations were also carried out at varying overpass times (Chaouch et al., 2012) using MODIS L1B radiance products from both Aqua and Terra satellites, which do not include the MOD35/MYD35 cloud mask. During cloud free conditions, L3 images were used  
120 to sample data along sections of the river. Furthermore, to maximize the availability of data collected, MODIS L1B was used when cloud cover was present in L3 swaths. MODIS snow product at 500-m spatial resolution presents a cloud mask at 1 km spatial resolution. Using MODIS L1B enabled a higher availability of recordable pixels at geographic locations, which were cloud covered in the L3  
125 images. It was concluded that more data pixels were available to collect from MODIS L1B when cloud cover was present in L3 images. Image sets from DOY 100 to 160 were analyzed to observe patterns over the entire ice break-up period ranging from 61° N to 68° N. Ice-off observations were recorded at latitudes where ice was present but subsequently absent from images the next Julian day. North  
130 flowing ice could generate multiple ice-on and ice-off dates at the same geographic location. Ice-off and ice-on dates are dynamic ice run events during the ice break-up period. Multiple ice-off dates observed by satellite imagery were referenced and compared to specific hydrometric stations from the Water Survey of Canada (WSC) along the Mackenzie River (Table 1).



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To avoid error in the SDS data collected, mixed pixels over the river consisting of water, ice and land were omitted. Furthermore, in sections of the river where pixel mixing was common as a result of smaller river widths, MODIS L1B was used. MODIS L1B with a spatial resolution of 250-m enabled to maximize data collection and minimize mixed pixel omission. The use of MODIS reflectance data at the 250-m spatial resolution (bands 1 and 2) has been compared to high-resolution Landsat for ice detection and produced a probability of detection at 91% (Chaouch et al., 2012). Although it would be useful to compare Landsat high-resolution images to the current MODIS sample of observations, very few Landsat images were available with the targets dates and over the specific region where ice break-up was progressing to produce a comprehensive comparison. The combination of high cloud cover, high revisit cycles and rapid ice breakup processes (~a few hours – 3 days) limited the amount usable Landsat images.

## 150 2.3 Ice Velocity

In addition to determining instances of ice break-up events with respect to location and time, this study also explored the use of MODIS as a tool for estimating velocity of ice flows. Ice velocity was observed and recorded on stretches of ice debris (> 15 km) where ice and water demarcation was distinguishable. Stretches of ice were defined by the changes in attributes on the Mackenzie River from open water to ice (37 to 100) on the leading edge of ice and

ice to open water (100 to 37) on the trailing edge of ice. Velocity was estimated by tracking the displacement of ice over time across multiple MODIS L3 and L1B swaths. Displacement estimates over time were made twice daily from Aqua and

**160** Terra satellites image captures. It should be noted that the MODIS images do not show displacement within each image capture, therefore the average velocities represent estimates between images. Average velocities were recorded until ice debris could no longer be distinguished as a result of melt or cloud cover. Ice velocities recorded also represent the lower limit of the ice flows, as the ice may

**165** not be moving at all times between image acquisitions. Therefore, the average velocities present time periods when the ice could be at rest and, therefore, the velocity measurements represent underestimation of the actual ice velocities. Ice debris movement was also referenced to WSC station provided that an operational station was on the route of the ice run.

## 3 Results

### 3.1 Thermal and Dynamic Ice Break-up

Over the 13 years of analysis, the ice break-up period ranged from as early as DOY 115 and lasted as late as DOY 155. Most ice break-up over the 13-year period (2001-2013) began between DOY 115-125 and ended between DOY 145-155. River morphology acted as an important spatial control determining the type of ice break-up process and ice run. Ice break-up processes between years showed different overall patterns with respect to location, thus temporally the beginning, end and duration of ice break-up varied. For example, the initiation of ice break-up in 2002 (Fort Simpson-330 km) began 10-days later than the average date when ice would completely clear the river section. Compared to 2007, the initiation of ice break-up began 13 days earlier than the average ice-off date at 270 km (61.57° N). As seen in Figure 3, ice break-up initiates earliest at the headwaters (headwaters at 120 km, 61.43 ° N to 345 km, 61.92° N) between the Martin River and Mill Lake, and proceeds northward towards the Mackenzie Delta (see Figure 4).

The initiation of the ice break-up period on the Mackenzie River was generally observed at the Liard River (325 km). The beginning and end of ice-off observations were observed to take place sooner near the Liard River than upstream and downstream of this location (Figure 5). The confluence where the Mackenzie River and Liard River meet (61.82 ° N, 325 km) serves as a point

where ice break-up proceeds dynamically northbound and thermodynamically southbound. South of 325 km, ice break-up was observed to be driven by a thermodynamic ice break-up regime (Figure 6). So, ice break-up advanced  
25 opposite to the direction of river flow, southbound towards Great Slave Lake. Interestingly, higher frequencies of observations were observed south of 325 km where thermodynamic ice break-up regime was prevalent. This ice break-up “reverse” to the river flow was observed to continue until it approached Mill Lake, where the ice break-up was simultaneously progressing in the direction of flow.  
30 The converging course continued until no ice remained south of Martin River (Figure 6).

As ice break-up proceeded northbound from the MR-Liard confluence, dynamic ice break-up flushed the ice downstream in a shorter period of time than  
35 the thermodynamic ice break-up south of the confluence (Figure 3 & 4). Generally, however, distances above 560 km ( $63.22^{\circ}$  N) (Wrigley, NWT) on the Mackenzie River experienced later ice break-up dates over the 13 years studied (Figure 5).

Between 350-682 km ( $61.96$ - $64^{\circ}$  N) and north of the Mackenzie River and  
40 Liard River confluence, the average ice-off date for the study period was observed at DOY 130. The river width between 350-682 km was found to be smaller than reaches upstream (feeding ice into the main river channel) and downstream (letting ice exit the channel) as seen in Figure 7. Consequently, the movement of ice into this river reach was limited causing ice entering the channel to jam while ice

45 exiting the channel present from the winter period cleared sooner. There is also the possibility that the release of ice javes (river waves generated from ice jam) at the entrance of the channel could give rise to the rapid clearance of downstream ice over 1-2 day period over this 230 km stretch of the Mackenzie River (Beltaos et al., 2011).

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Downstream of 682 km (64° N), river sections showed diagonal ice-off observations as seen in Figures 3 and 4. These patterns are most visible in 2001, 2007-2009 and 2011-2012 observed between 860-1460 km (65-67.62° N). Observations of these diagonal events were the result of a second channel

55 constriction at The Ramparts (1078 km, 66.19° N) as seen in Figure 7, preventing northerly ice run. Here, the river channel decreased from 4 km to less than 0.5 km in width. It is hypothesized that ice runs downstream of The Ramparts (as a result of an ice jam) gave rise to similar ice-off dates (estimated at the southern ice-water boundaries of these flows) to ice runs towards The Ramparts. It is estimated that

60 ice jams due to sudden decreases in river width as seen in 2001, 2007-2009 and 2011-2012 gave rise to earlier ice-off dates for river sections north of the jam resulting in impeded ice run which would normally maintain ice-on condition. This phenomenon resulted in a sequence of ice-off observations that occur simultaneously at two different latitudes, north and south of the ice jam. This

65 further outlines the important morphological controls on the Mackenzie River over ice runs.

Based on MODIS imagery, ice break-up began on average between DOY 115 and 125 and ended between DOY 145 and 155 (Figure 5). The standard deviation of estimated ice-off dates decreased with increasing latitude. MODIS derived dates showed highest deviations across river sections where thermodynamic ice break-up was prevalent. These patterns are similar to those seen from average break-up and standard deviations observed from the WSC. The 13-year average reveals similar ice conditions in the low, mid and high latitude of the Mackenzie River from MODIS and WSC data. There was an observed difference of 5 days between ice break-up observed from MODIS imagery and WSC. Also, the respective standard deviations overlap across the similar periods. Ice break-up in general continued in a north to south direction over the ice break-up periods. Near Forth Simpson (330 km, 61.85° N), it is worth mentioning that ice break-up was observed earlier than at more southern latitudes as illustrated by MODIS observations. This pattern is likewise visible from the WSC data.

### 3.2 Ice Break-Up and Snowmelt

In order to assess the relative timing of ice disappearance in relation to its surrounding sub-basin, the timing of river ice disappearance was qualitatively compared to the timing of near complete snow disappearance from the surrounding area. MODIS L3 imagery of different years was selected which clearly revealed ice-snow relation with respect to location, where cloud cover was a minimal issue.

90        Locations where thermodynamic ice disappearance was hypothesized (south  
of 61.8° N, 325 km) corresponded with patterns where ice disappeared much later  
than snow on land (Figure 6). For example, DOY 121/2006 (Figure 8) was  
observed to be the beginning of the snowmelt period at 290-487 km (61.75 ° N –  
62.5 ° N) and this process ended when the snow had almost completely  
95        disappeared by DOY 125. However, DOY 125 corresponded to the initiation of ice  
break-up. This was not limited to 2006 so that snow generally disappeared sooner  
from surrounding sub-basins, followed by the initiation of ice-break-up.

At reaches north of the MR-Liard River confluence, ice break-up and  
100        snowmelt was observed to initiate in sync to one another. As seen in Figure 9, on  
DOY 136-137/2011, ice disappearance on the southern cross-section of the figure  
is marked by the near simultaneous disappearance of snow. In fact by DOY  
140/2011 both ice and snow had completely disappeared analogous to each other.  
On sections of the Mackenzie River before it enters the Mackenzie Delta, estimated  
105        ice break-up and snow disappearance was again observed to occur almost  
simultaneous to one another (Figure 12). Over a 6-day period (DOY137-142/2007)  
the ice break-up process continued until ice completely disappeared from the  
channel (MR). This process ensued sooner relative to complete snowmelt over the  
surrounding sub-basins. By DOY 142/2007 nearly one-third of the river was  
110        completely cleared of ice while most of the snow was still present over the MRB.

Principally, it was concluded that on the upper Mackenzie Basin snow cleared sooner than the initiation of ice break-up. In the mid-Mackenzie Basin (375-860 km, 62° N to 65° N), river ice cleared in-situ to snow clearance from the surrounding basin. In fact, ice cleared sooner in the mid basin than the upper Mackenzie Basin. Finally, in the lower Mackenzie Basin, river ice cleared sooner than the snow from the surrounding basin. This could be telling of a river continuum of the build-up of mechanical strength used to clear river ice within the Mackenzie River towards higher latitudes. The Liard River tributary accounts for one third of the total Mackenzie discharge (Woo and Thorne, 2003), and so a rise in discharge in May initiates earlier ice break-up downstream as a result of increased stress induced on ice by a rise in river stage. Mechanical stress used to shove ice is continually magnified by the addition of small and large tributaries downstream of the Mackenzie River (Great Slave River, Arctic Red River).

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### 3.3 River Ice Velocity

Figures 10 and 11 illustrate ice movement from which ice velocities could be estimated over periods of 3-4 days following secondary channel constriction at 66° N. Here, ice runs that contained over 15 km of entrained ice were chosen to estimate average ice velocities. Only periods with at least three images with partial or no cloud cover were selected for velocity estimates.

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In 2008, the open-water/ice boundary (leading edge) was recorded beginning on DOY 143 (Figure 10). The open-water/ice (northern edge of ice) and ice/open-  
**135** water (following edge) boundaries were both visible from DOY 144. Finally, the ice/open-water boundary was last observed on DOY 145. The average ice run velocity between 1063-1210 km (66-66.95° N) over the three days was estimated to be at least 1.21 ms<sup>-1</sup>. Likewise, in 2010 (Figure 11), open-water/ice (leading end) and ice/open-water (following end) was observed between DOY 138-141. The  
**140** leading edge of the ice was first observed on DOY 138 and on DOY 139 when both the leading and following edges are visible. Finally, by DOY 141 the ice run has exited into the Mackenzie Delta. Across the 4-day period average ice run velocity was estimated to be at least 1.84 ms<sup>-1</sup>.

## 4 Discussion

### 4.1 Spatial and Temporal Ice Break-up Patterns

Over the 13-year period, the average estimated ice break-up dates were found to range between DOY 115-155 between distances 60 km and 1460 km. These estimates from MODIS are in agreement with break-up dates reported by the WSC ground-based network. Previous studies on the MR, between the late 1930's to 2002, have found the initiation of ice break-up to range DOY 123-140 between 0 km and 1217 km (de Rham et al., 2008a). Furthermore, it was reported by de Rham (2008b) that the duration of average ice break-up ranged from 8-10 days over the entire basin. With respect to the findings reported in Figure 5, the observed ice-break-up patterns agree, such that the average observed break-up dates over the 13-year period ranged from  $\text{DOY } 128 \pm 8$  days at  $61.5^\circ \text{ N}$  (260 km) to  $145 \pm 4$  days at  $68^\circ \text{ N}$  (1460 km). Others have reported, using MODIS and AVHRR imagery acquired between 1992 and 2002, that ice break-up ranged between DOY 120 and 155 (Pavelsky and Smith, 2004). The earliest reports of mean ice break-up dates ranged from May 15 (DOY 135) to May 25 (145) (1946-1955 averages), from Fort Providence to Arctic Red River, respectively (MacKay, 1966). Furthermore, others have reported a range of ice break-up dates from May 22 (DOY 142) to May 31 (DOY 151) (1927-1974, Figure 3) from Fort Providence to Fort Good Hope, NWT, respectively (Allen, 1977). A summary of the approaches and results reported in

these previous investigations as well as those from this study are compared in Table 4.

In the headwaters of the Mackenzie River, ice break-up initiates the earliest  
25 between Mill Lake (120 km, 61.43° N) and Martin River (345 km, 61.92° N). As  
seen in Figures 3 - 5, ice break-up between 120-300 km initiated earlier as  
compared to other sites on the Mackenzie River, but ice cleared later than other for  
other river sections downstream. Here ice in the channel remains stagnant for  
extended periods of time as ice usually freezes to bed and is most susceptible to  
30 thermodynamic melt (MacKay and Mackay, 1973).

Furthermore, at the Liard River confluence (325 km, 61.84° N) it was found  
that the seasonal initiation of ice break-up began and cleared earliest at this central  
location where the Liard River converges into the MR. Others (Pavelsky and  
35 Smith, 2004) have noted that at the MR-Liard River confluence flooding is  
common between years, especially near channel junction. Ice break-up at the Liard  
River confluence occurs rapidly, as the flow contribution is of greater magnitude  
than the Mackenzie River (MacKay and Mackay, 1973). This causes a lifting of the  
river stage, exerting pressure on the ice cover resulting in ice jam downstream most  
40 attributed to presence of channel bending (Camsell Bend, 456 km) and channel  
constriction. Similar processes have also been reported for the Susquehanna River,  
USA, where an observed increase in discharge downstream fosters earlier ice  
break-up while sections of the upper river remain ice covered (Chaouch et al.,

2012). The severity of ice break-up stage is therefore largely controlled by  
45 upstream discharge (Goulding et al., 2009b). Pavelsky and Smith (2004) also  
observed irregularities in ice break-up timing between years, particularly at 325 km  
(MR-Liard confluence) on the MR. Here, ice break-up began earlier at distances  
north of 325 km ( $61.8^{\circ}$  N) than river sections south. Postponed ice break-up in the  
upper Mackenzie can result from the lack of discharge required to initiate ice  
50 break-up and so the ice is thermodynamically disintegrated.

Channel morphology is, therefore, a more important control on ice break-up  
patterns than previously believed. Both Pavelsky and Smith (2004) and de Rham et  
al. (2008a) alluded to the fact that channel morphology may exert influences on the  
55 patterns of ice break-up. De Munck et al (2011), through the use of geospatial  
modelling on the Chaudiere River identified that channel islands, confluences and  
channel sinuosity predisposed the Chaudiere river to ice jamming events. In this  
study, it is determined that channel constriction at 350-682 km ( $61.96-64^{\circ}$  N) and  
1078 km (The Ramparts) is responsible for the delay of ice break-up timings  
60 upstream while promoting earlier ice break-up downstream. Upstream of the Liard  
River junction, river flow is stable. However, excessive discharge supplied by the  
Liard River causes earlier ice break-up and ice jamming downstream when the  
channel constricts between 350-682 km (MacKay and Mackay, 1973).  
Furthermore, excess supply of ice cover from the Great Bear River (821 km) into  
65 the Mackenzie River, causes the development of ice jamming at The Ramparts

when the channel width decreases from over 3.5 km to less than 0.6 km (as seen in Figure 7) (MacKay and Mackay, 1973).

Ice jamming from channel width decreases gave rise to similar sequences of  
70 ice-off observations, which occurred in tandem at two different latitudes, north and south of the ice jam (as seen at The Rampart). Ice jams are therefore favorable where morphological features impede downstream ice passage (Beltaos, 1997). These ice jams are caused by channel constriction resulting from mid-channel islands and narrow reaches (Terroux et al., 1981). Channel braiding, constriction  
75 and changes in slope have also been reported to be important factors influencing ice break-up and flow regimes (de Rham et al., 2008a). In the context of our study, it was found that channel constrictions and bends represented locations where ice runs were impeded. Hicks (2009) also reported that running ice may be stalled when geometric constraints such as tight bends, narrow sections and islands are  
80 present in rivers. In fact, it has been shown that ice debris flow drop to a velocity of zero in the presence of flow depths near channels islands and bars (Kääb et al., 2013). Lastly, Kääb and Prowse (2011), using ALOS PRISM stereo imagery on the Mackenzie River determined that ice velocities decrease to zero in the presence of bars.

85

The estimated ice run events illustrated in Figures 7 and 10 may have been caused by ice jam releases (javes) initiated at The Rampart (1078 km, 66.19° N). Such processes may also be the reason why ice was estimated to be cleared at

higher latitudes before the end of the snowmelt period. Accumulated stress with the  
90 rise of water levels behind the jam can result in sufficient kinetic energy to clear  
river ice downstream before the complete snowmelt overlying the surrounding sub-  
basins.

## 4.2 Ice Velocities

95 Ice run velocities are believed to be the highest where the ice is minimally  
effected by channel morphology; unconnected from incoming tributaries; and  
channel splitting which causes the formation of islands (Kääb et al., 2013).  
Amongst the variety of ice runs observed over the 13 years, ice velocities could be  
quantified in 2008 and 2010. Over 3-4 day periods, average ice velocities were  
100 estimated to be  $1.21 \text{ ms}^{-1}$  (2008) and  $1.84 \text{ ms}^{-1}$  (2010). More importantly, it is  
believed that the evolution of such velocities is the product of javes. Our  
measurements of ice run velocity in 2008 coincidentally synchronize with other  
independent satellite- and ground-based ice measurements. Extensive  
measurements of ice runs in 2008 around MR-Arctic Red River junction is  
105 believed to be generated by waves released from released ice-jams (Beltaos, 2013).  
This aligns with ice jams, which may form at The Rampart (1078 km,  $66.19^\circ \text{ N}$ ) as  
a result of channel constriction. The evolution of ice runs north of The Rampart  
(flowing past the Arctic Red River) observed over DOY 143-146/2008 (May 22-25  
/  $1.21 \text{ ms}^{-1}$ ) matches similar ground measurements ( $1.7 \text{ ms}^{-1}$ ) made by Beltaos et al.  
110 (2012). Across the same cross-section of the MR, Kääb and Prowse (with imagery

acquired 1-2 days earlier in 2008) estimated a preceding ice run ranging from 0 - 3.2 ms<sup>-1</sup>. The highest flow velocities were outlined where ice debris flow was most concentrated on the outside turn of the river bend. Finally, in another independent study, Beltaos and Kääb (2014) found ice debris velocities to range between 1-2 ms<sup>-1</sup> using ALOS PRISM imagery in 2010. Again these high-resolution (2.5-m) image measurements compare quite well with our estimates from relatively coarse spatial resolution (250-500 m) MODIS imagery. Additionally, early investigations have reported that ice can clear at velocities of 0.27 ms<sup>-1</sup> and 0.44 ms<sup>-1</sup> at Fort Simpson and Fort Good Hope, respectively during the ice break-up season (Terroux et al., 1981).

MODIS is shown to be a viable tool for estimating river ice velocities. This study finds that in order to monitor ice cover the river width needs to be at least 0.5 to 1 km wide. Furthermore, to quantify river ice velocities, the river width needs to be at least 1 km wide. With respect to the MR, ice velocities were only quantifiable above The Rampart. The presence of morphological controls and therefore river width shortening leading to impeded ice run prevented quantifying velocities, as leading river-ice demarcations were difficult to locate. However, it was possible to estimate the overall velocity by observing ice-open water boundaries. Lastly, it was determined that in order to measure ice run velocities without major disturbance with impeded flows with respect to river morphology, estimates with MODIS should be made north of The Rampart. North of The Rampart, river widths were generally observed to be largest with respect to other parts of the MR.

## 135 5 Conclusion

The aim of this study was to develop an approach to estimate ice break-up dates on the Mackenzie River over more than a decade using MODIS snow and radiance products. It was found that the initiation of ice break-up started on average between DOY 115-125 and ended DOY 145-155 over the 13 years analyzed. Thermal ice break-up was an important process driving ice break-up south of the Liard River. Conversely, north of the Liard, ice break-up was dynamically driven. The addition to discharge from the MR-Liard River confluence outlined a location where initial ice break-up began. Furthermore, MODIS images allowed for the identification of important factors controlling ice runs and ice break-up, including morphological controls such as channel bars, river meandering and channel constriction.

MODIS is currently the most promising tool for frequent monitoring of river ice processes as ground-based stations along the Mackenzie River are continuously being closed. Operating aboard two satellites (Aqua and Terra), the MODIS sensor allows for multiple daily acquisitions simultaneously along extensive stretches of the MR. Furthermore, MODIS is proving to be a viable sensor for the monitoring of river ice as shown in this and other recent investigations (e.g. Chaouch et al., 2012). In this study, monitoring of ice break-up on the Mackenzie River with MODIS proved to be a robust approach when compared to WSC ground-based



155 observations. MODIS observations also allowed for the analysis of basin level  
processes influencing ice break-up, including river morphology and snowmelt.

Finally, future research should focus on investigating river ice processes using  
a combination of ground-based and satellite-based sensors; particularly for  
160 examining relations between river morphology, ice strength and discharge. Data  
from these complementary technologies would be valuable in the context of an  
early warning system for municipalities where river ice break-up is an important  
spring event causing significant flood damage. Furthermore, a multi-sensor  
approach using both optical and synthetic aperture radar (SAR) data would be  
165 advantageous in order to monitor ice river processes and floods in near real-time.  
Satellite data from recent and upcoming SAR (Sentinel-1 and RADARSAT  
Constellation) and optical (Sentinel-2 and Sentinel-3) satellite missions will make  
such monitoring possible in the near future.

170

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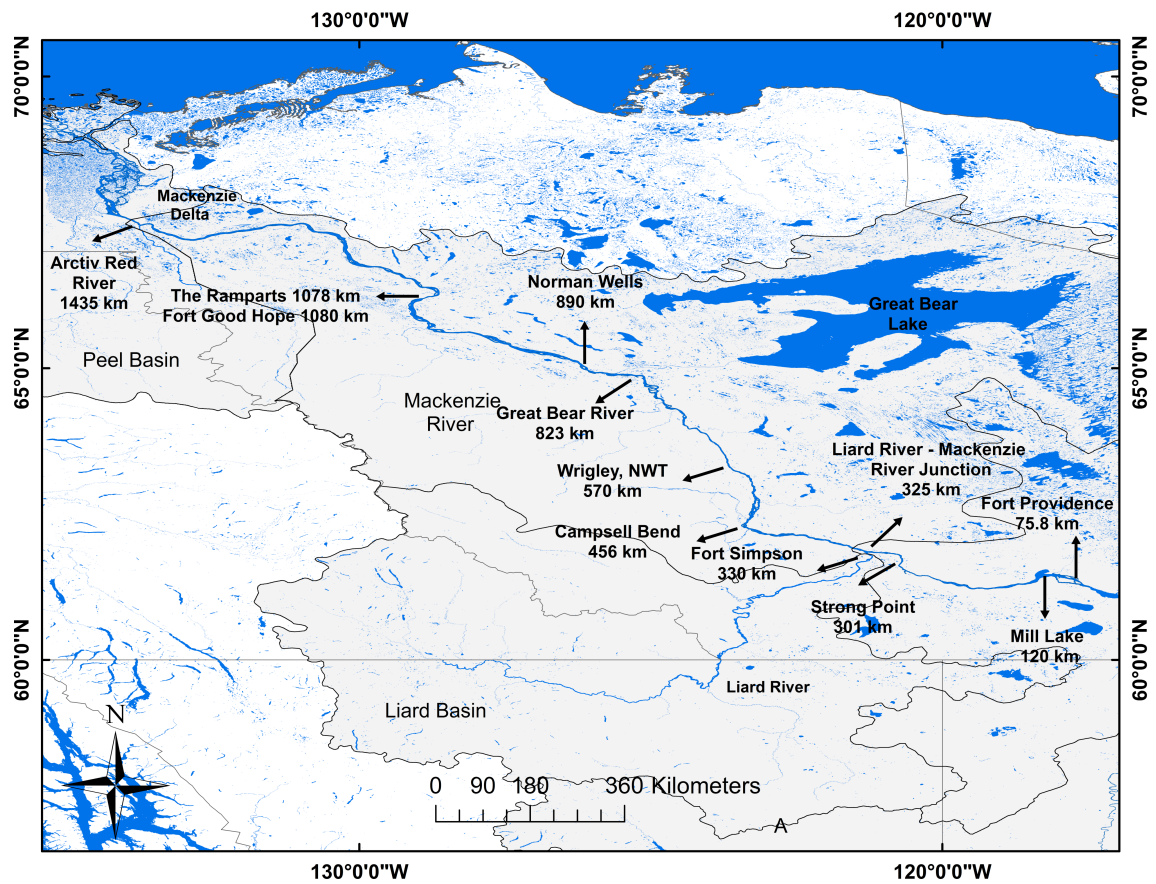


Figure 1: Northern reaches of the Mackenzie River Basin (MRB), its sub-basins and major rivers and lakes. The MRB extends from 54° N to 68° N flowing from the southeast to northwest. The names of sub-basins and tributaries feeding into the Mackenzie River as well distances downstream (marked by arrows) from the mouth of the Mackenzie River are also shown.

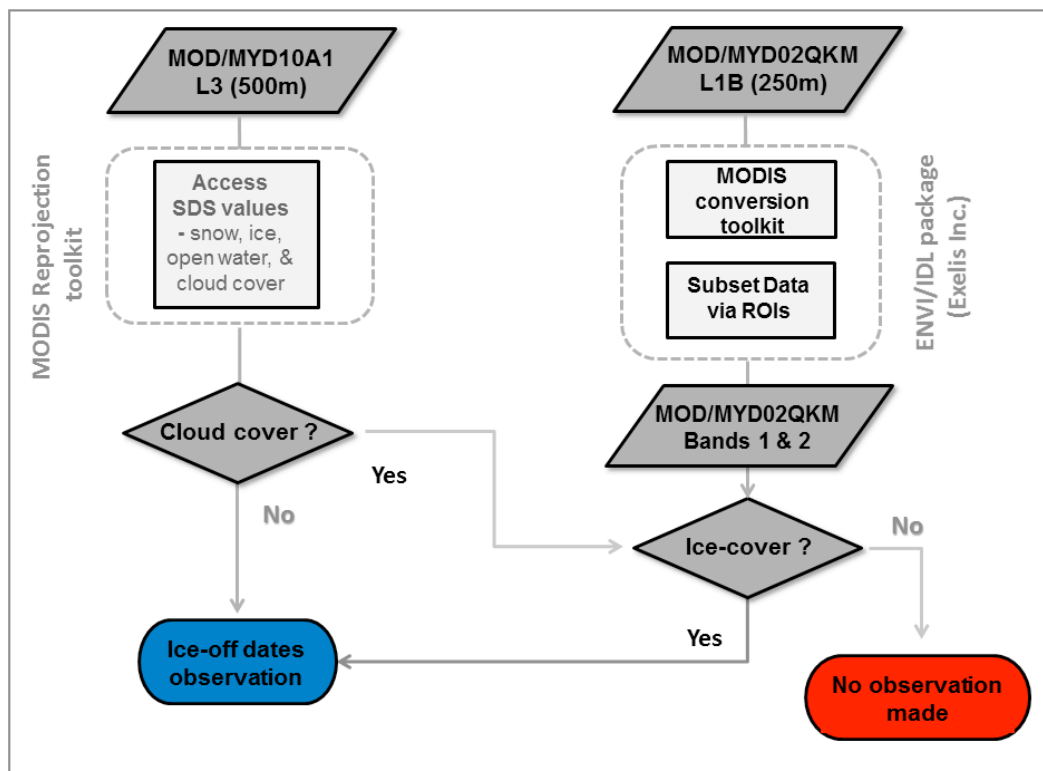


Figure 2: Illustration of the processing steps of ice of observations (manually and by visual interpretation) on the Mackenzie River.

Table 1: Description of Water Survey of Canada hydrometric stations on the Mackenzie River.

Station Name	Coordinates	Distance Downstream from Mouth of Mackenzie River
Mackenzie River at Fort Providence	61.27° N, 117.54° W	75.8 km
Mackenzie River at Strong Point	61.81° N, 120.79° W	301 km
Mackenzie River at Fort Simpson	61.86° N, 121.35° W	330 km
Mackenzie River at Norman Wells	65.27° N, 126.84° W	890 km
Mackenzie River at Arctic Red River	67.45° N, 133. 75° W	1435 km

Table 2: Scientific data set (SDS) and digital number (DN) values from MODIS L1B and L3 products used for the Mackenzie River.

Image Cover	MOD/MYD L3 (SDS)	MOD/MYD L1B (DN)
Spatial resolution	<b>(500-m)</b>	<b>(250-m)</b>
Cloud Cover	50	150 <
Snow	200	111-150
Ice (Snow Covered)	100	40-110
Open Water	37	30
Land	25	< 28
Bands	Wavelength (nm)	Wavelength (nm)
1		620-670
2		841-876
3	459-479	
4	545-565	
5	1230-1250	
7	2105-2155	



Table 3: Time periods of observations and number of MODIS L3 and L1B images analyzed during break-up on the Mackenzie River (2001-2013).

Year	Time period of observations (Julian Day)	MODIS L3 images		MODIS L1B images	
		Aqua	Terra	Aqua	Terra
2001	119-153		20	1	1
2002	136-150		13	2	1
2003	115-153	16	13	1	1
2004	122-151	9	6	3	2
2005	116-144	14	15	2	2
2006	123-144	12	15	1	1
2007	115-153	23	21	2	4
2008	124-154	18	23	2	4
2009	125-147	15	16	2	1
2010	115-141	17	18	1	1
2011	128-148	16	14	2	2
2012	123-149	20	16	1	2
2013	131-149	14	14	1	1
Total		174	204	21	23

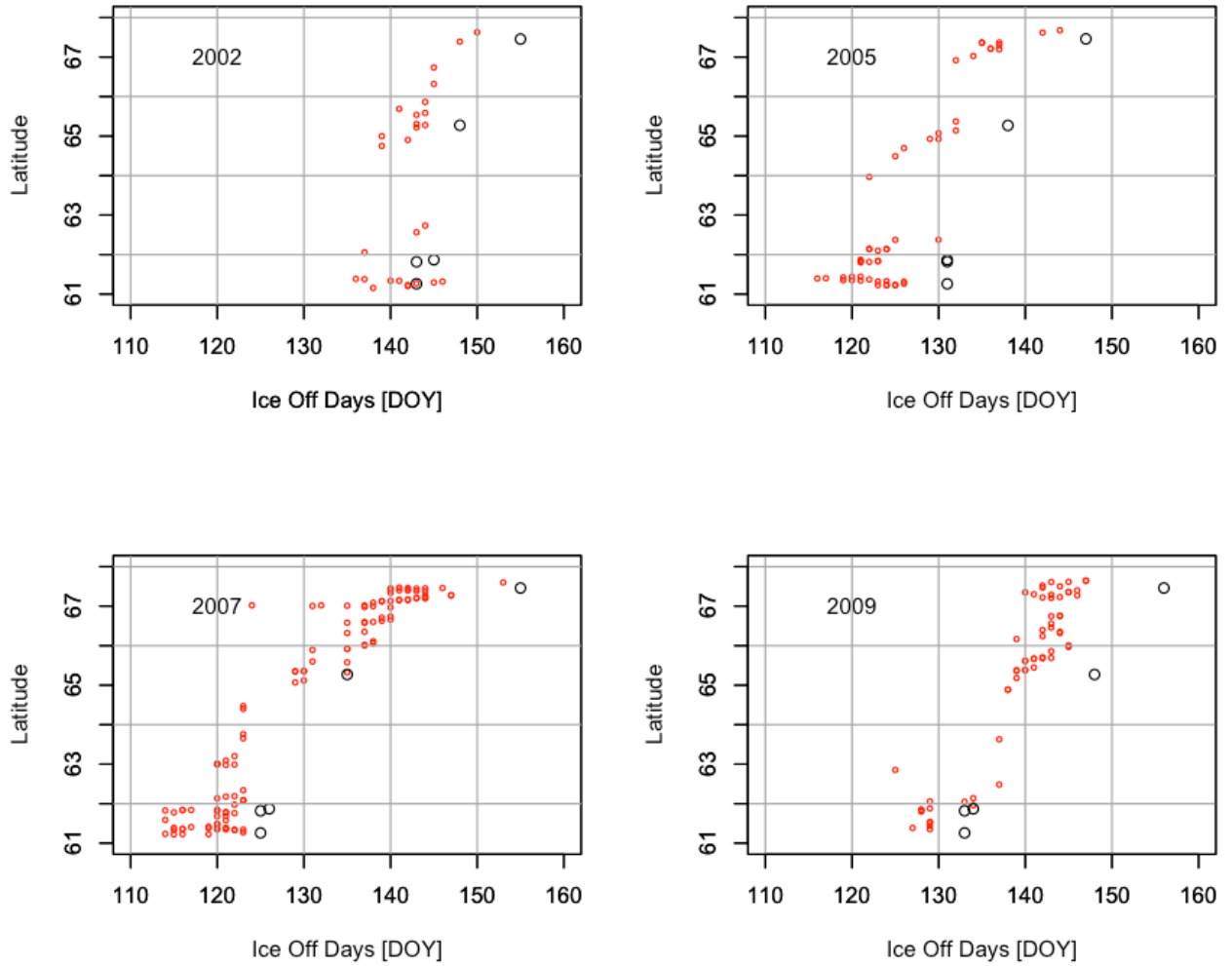


Figure 3: Estimated ice-off dates as illustrated by the red circles for selected years (2002, 2005, 2007 and 2009) on the Mackenzie River. Terra observations were made throughout the study period, while Aqua observations were available from 2003-onward. Black circles are indicative of WSC ice observation dates.

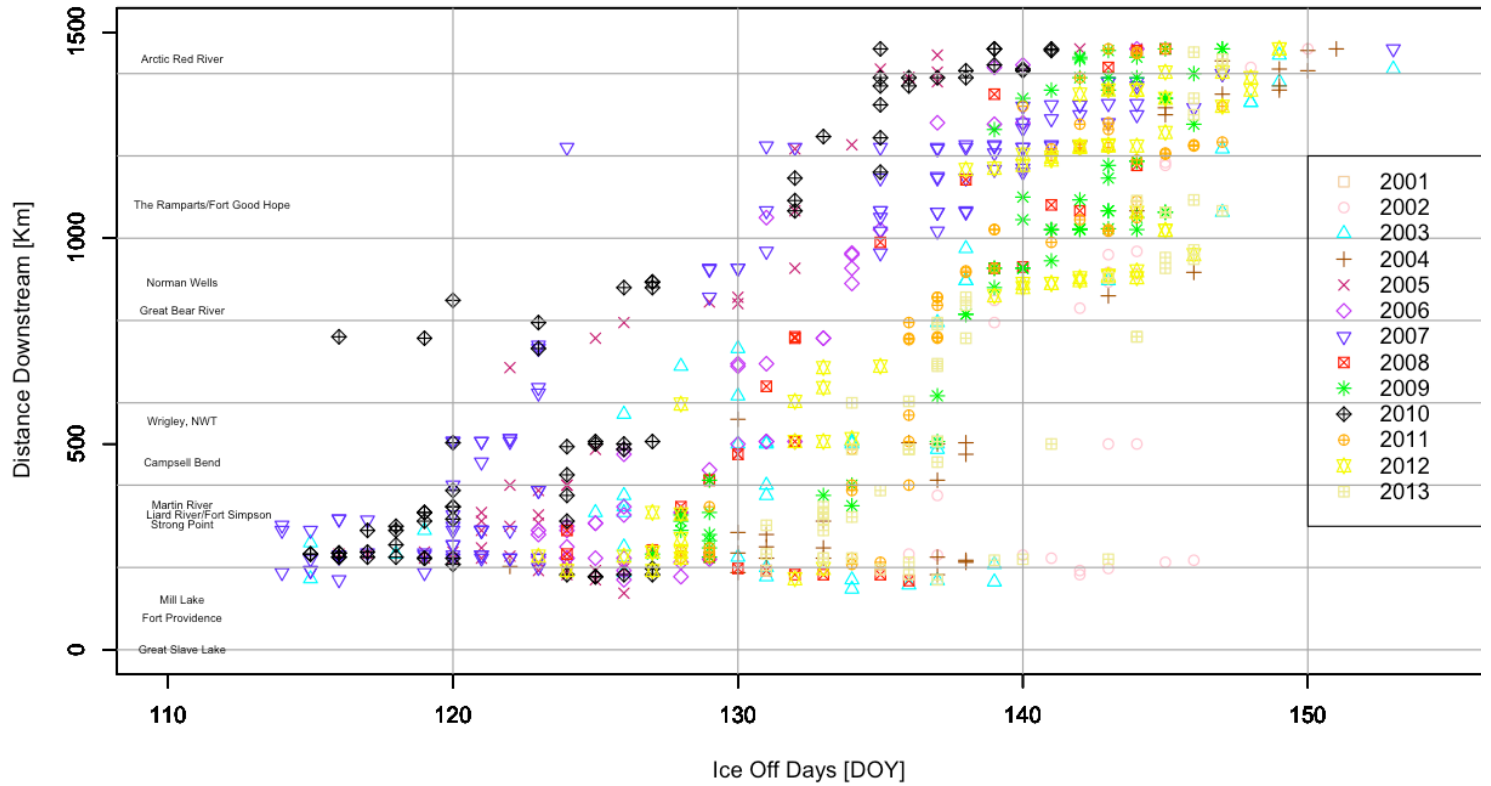


Figure 4: Compilation of all ice-off dates from 2001 to 2013 DOY [Day of Year] on the Mackenzie River. First ice break-up dates generally began near 325 km. Ice break-up processes are more protracted just south of 325 km as seen with the higher density of measurements. Near 1078 km, a second channel constriction is present giving rise to two distinct ice-run patterns.

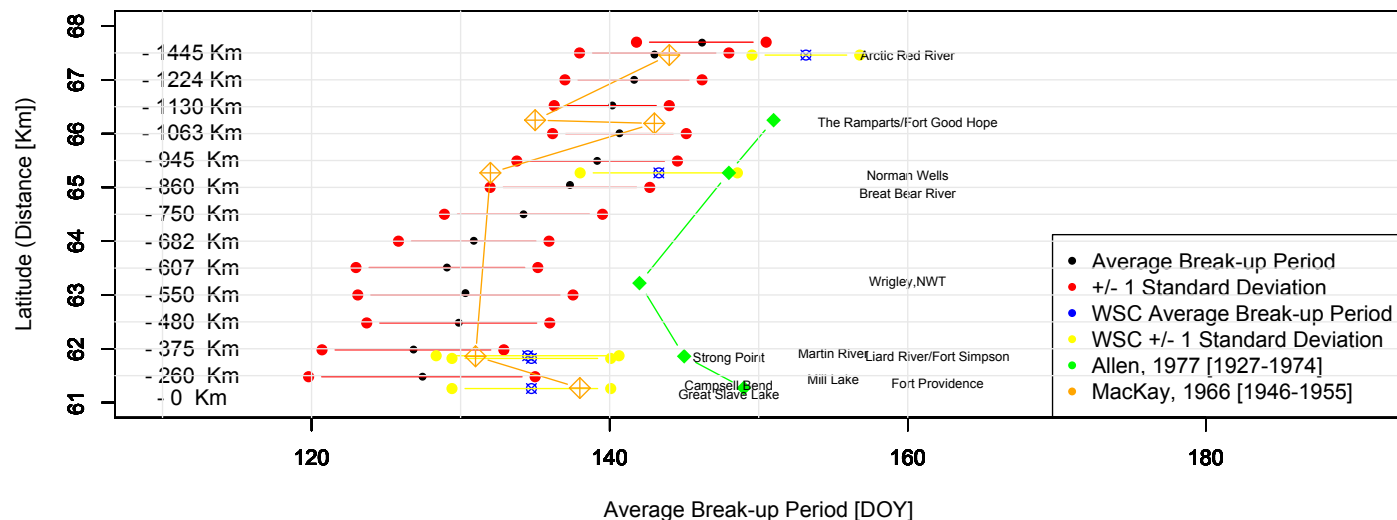
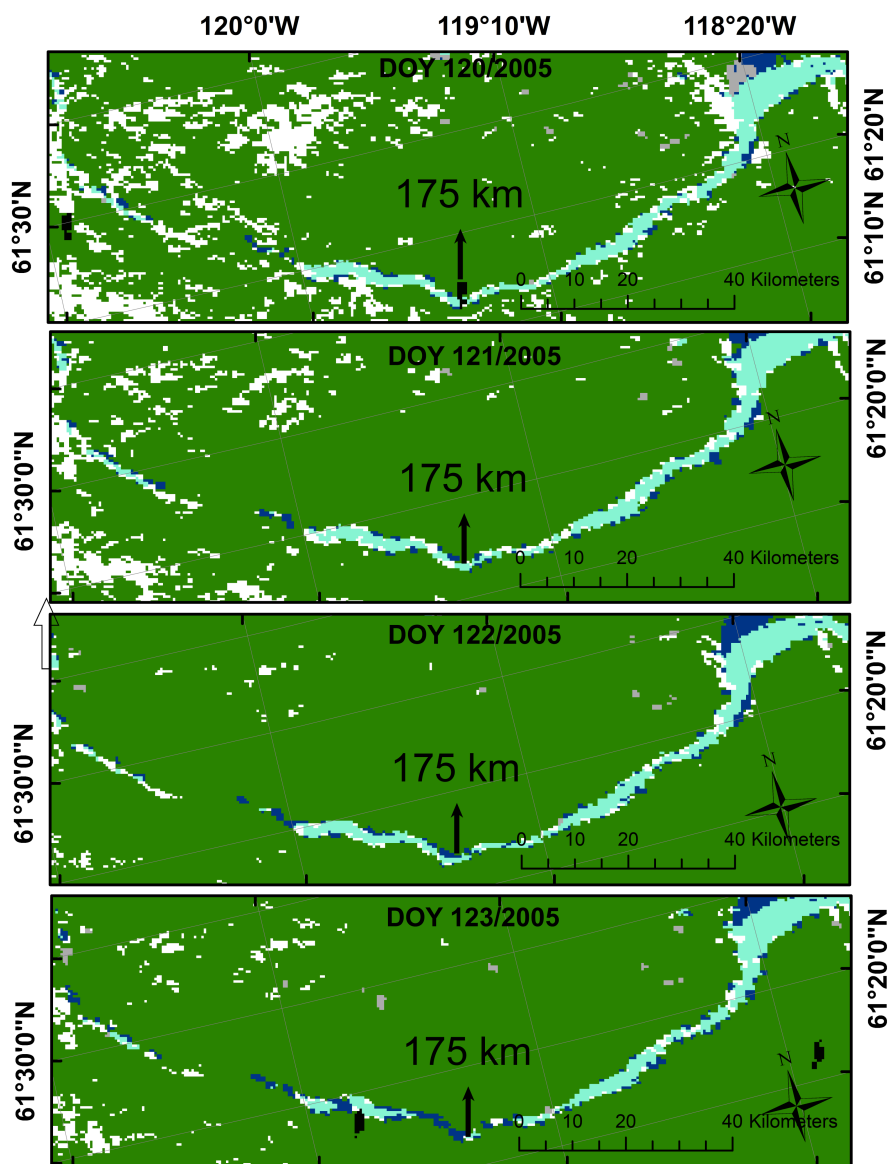


Figure 5: Average ice break-up dates estimated from MODIS (2001-2013) are given by the black dots, with  $\pm$  one standard deviation showed with the red dots. The blue dots illustrate the WSC average ice break-up dates and the yellow dots  $\pm$  one standard deviation. The green and orange dots represent average ice break-up dates from Allen (1977) from the time period of 1927 to 1974 and MacKay (1966) from the time period of 1946 to 1955, respectively.



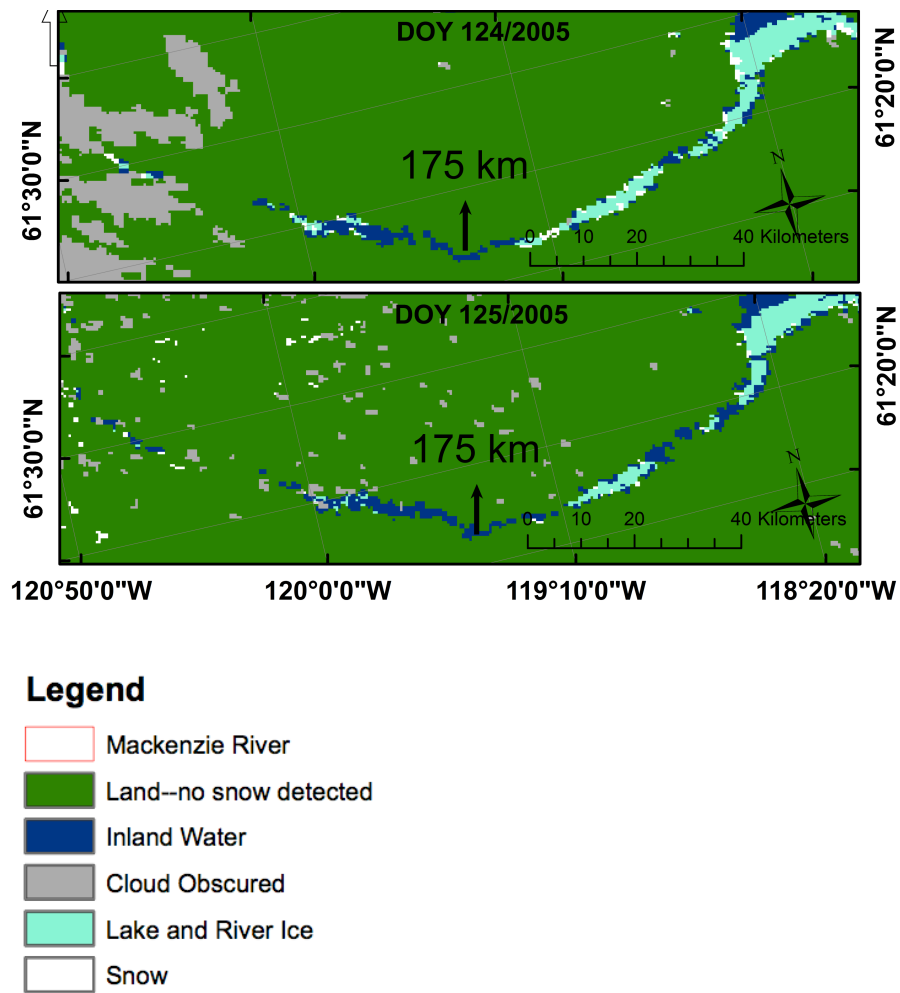


Figure 6: This example illustrates ice break-up at the headwaters of the Mackenzie River system in 2005 from DOY 120 - 125.

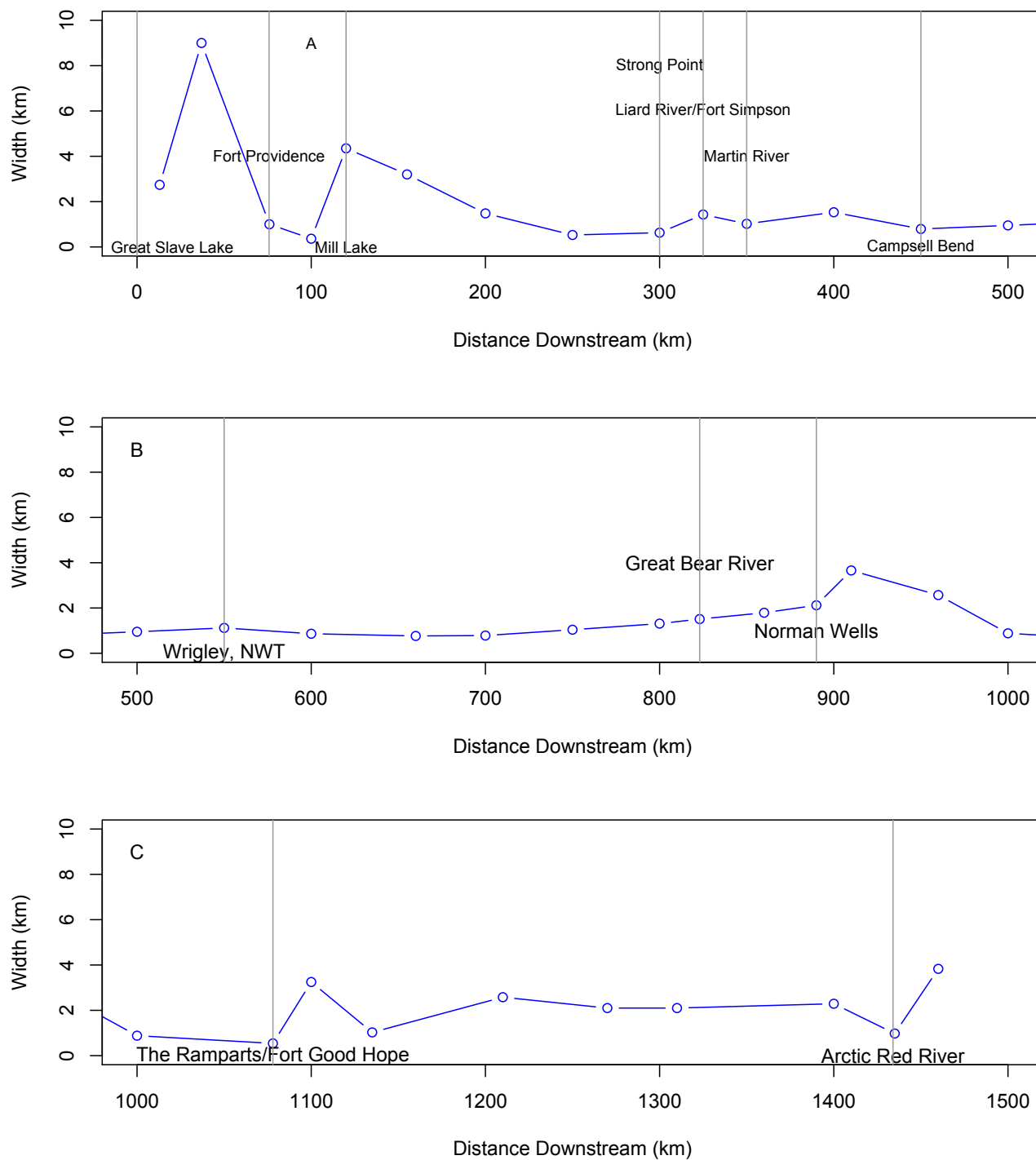
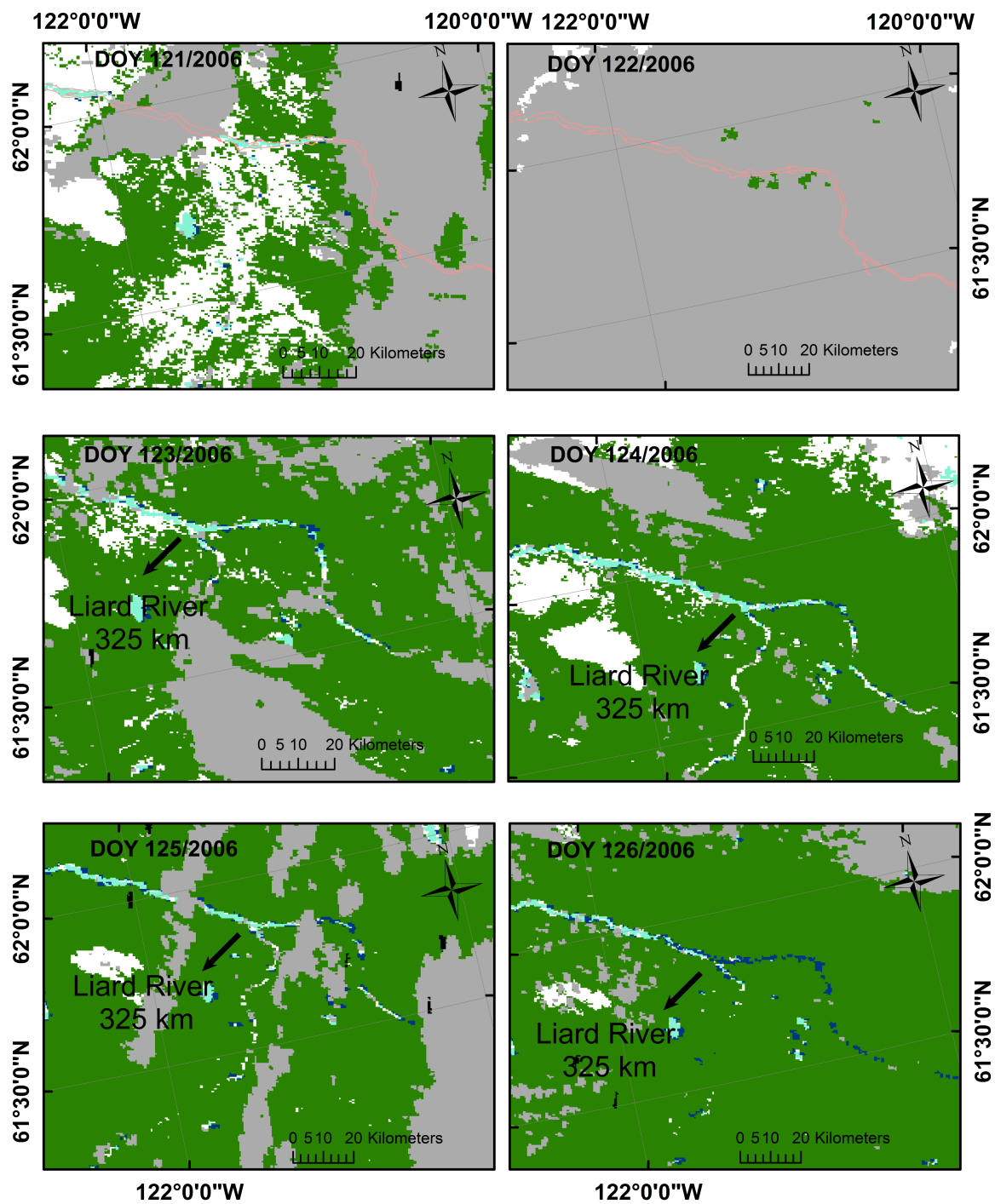


Figure 7: Change in channel width along the Mackenzie River as observed in A (ca. 0-500 km), B (ca. 500-1000 km) and C (ca. 1000-1500 km).







### Legend

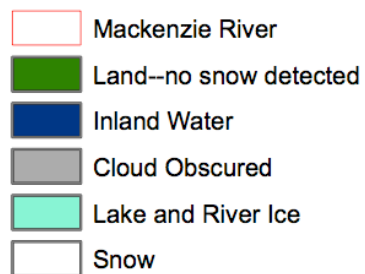
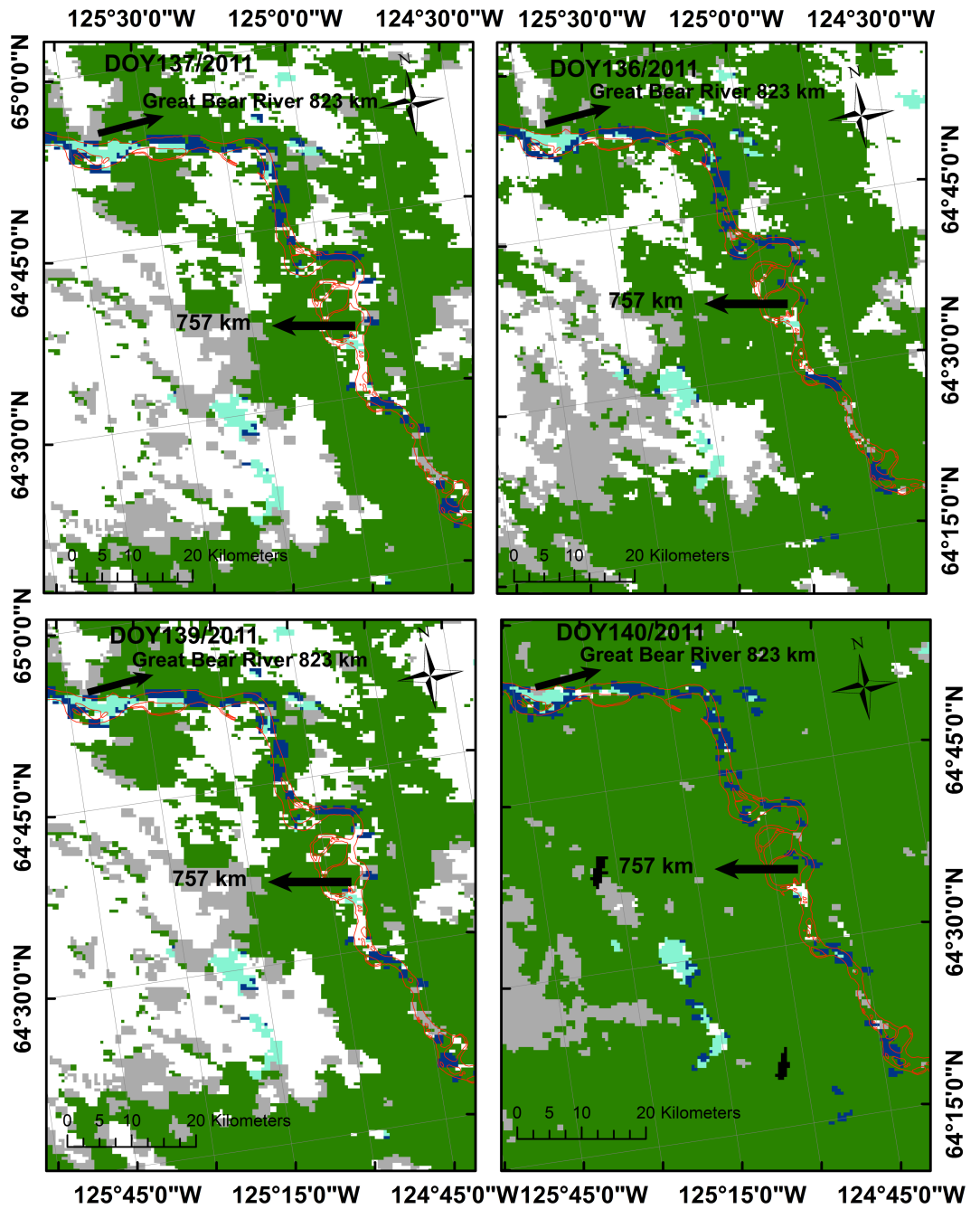


Figure 8: Example of thermodynamic break-up, where ice within the river requires an extra 2-3 days to be cleared after snow has melted over the immediate drainage basin. This process was observed in 2006 between DOY 121-126.



## Legend

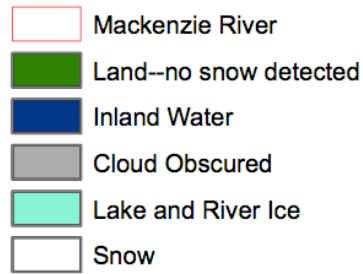
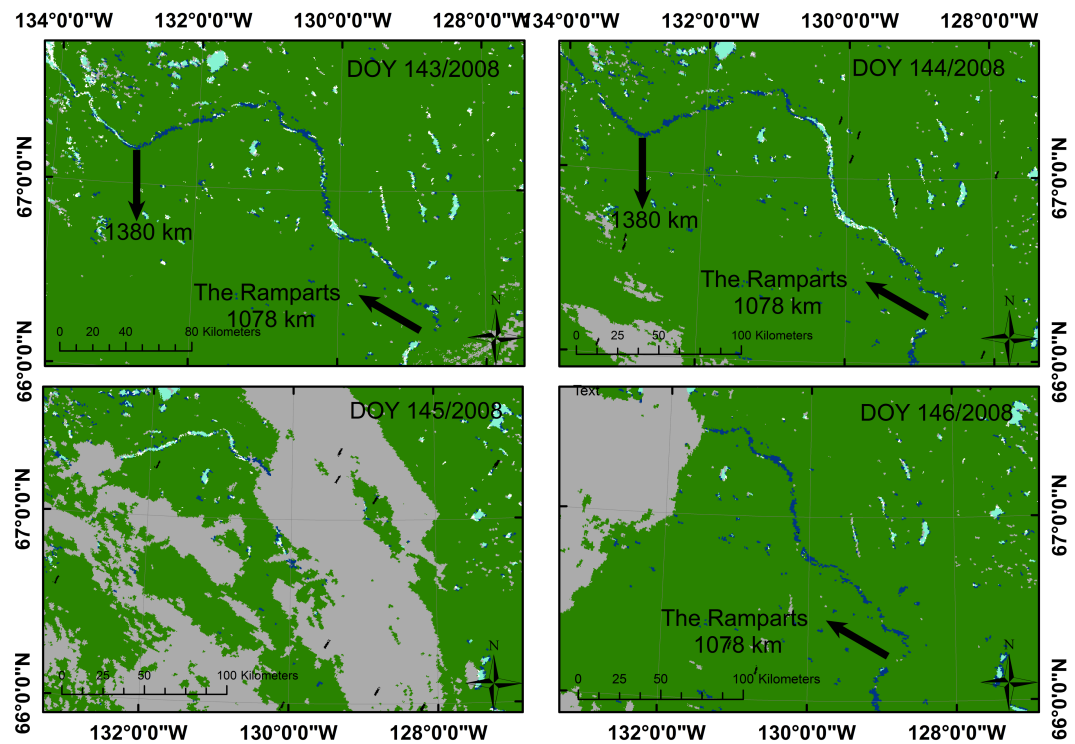


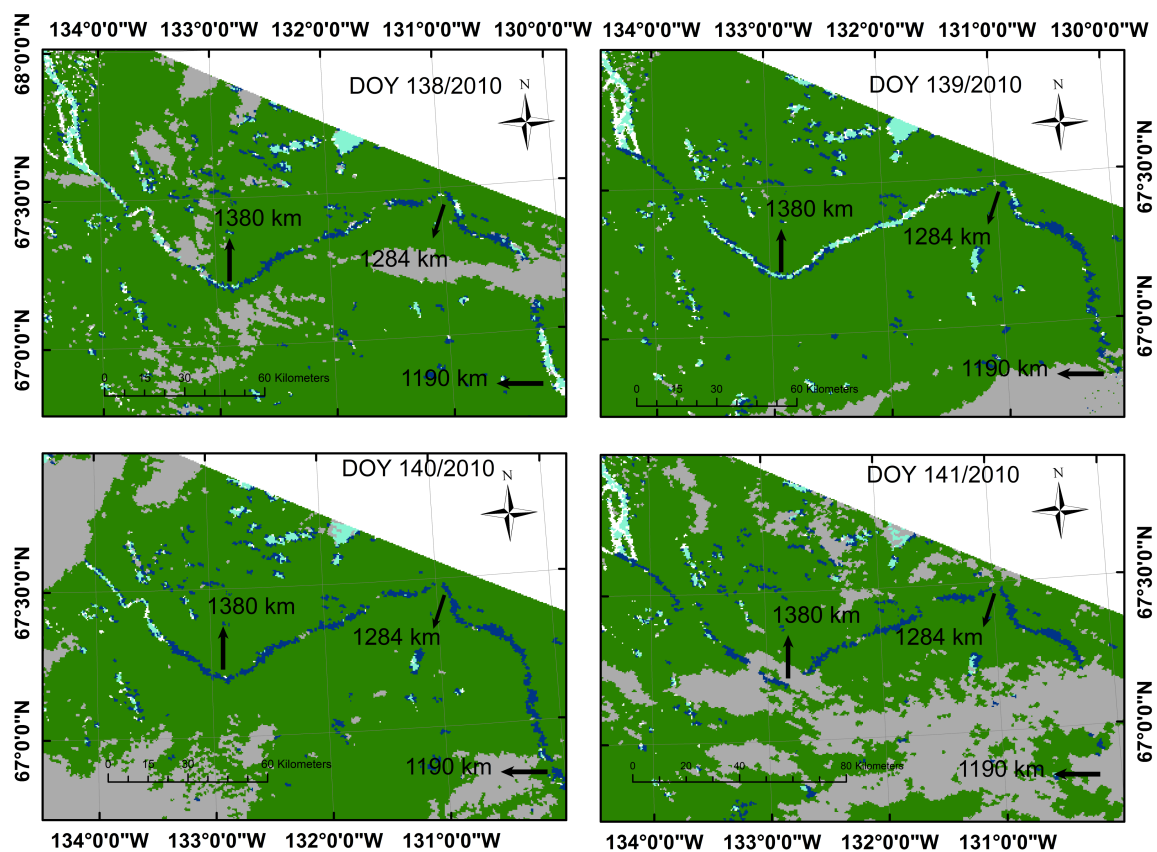
Figure 9: Snowmelt and ice run over the Mackenzie River Basin in 2011 between the DOY 137-140. There is a 2-day lag between the complete clearance of snow on land and the clearance of ice on the Mackenzie River.



## Legend

- Mackenzie River
- Land--no snow detected
- Inland Water
- Cloud Obscured
- Lake and River Ice
- Snow

Figure 10: Ice flushing event recorded in 2008 between DOY 143-146.



### Legend

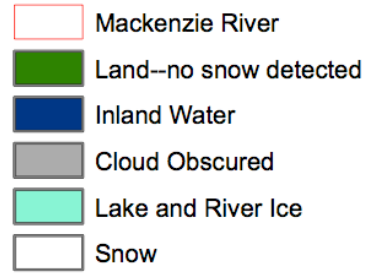
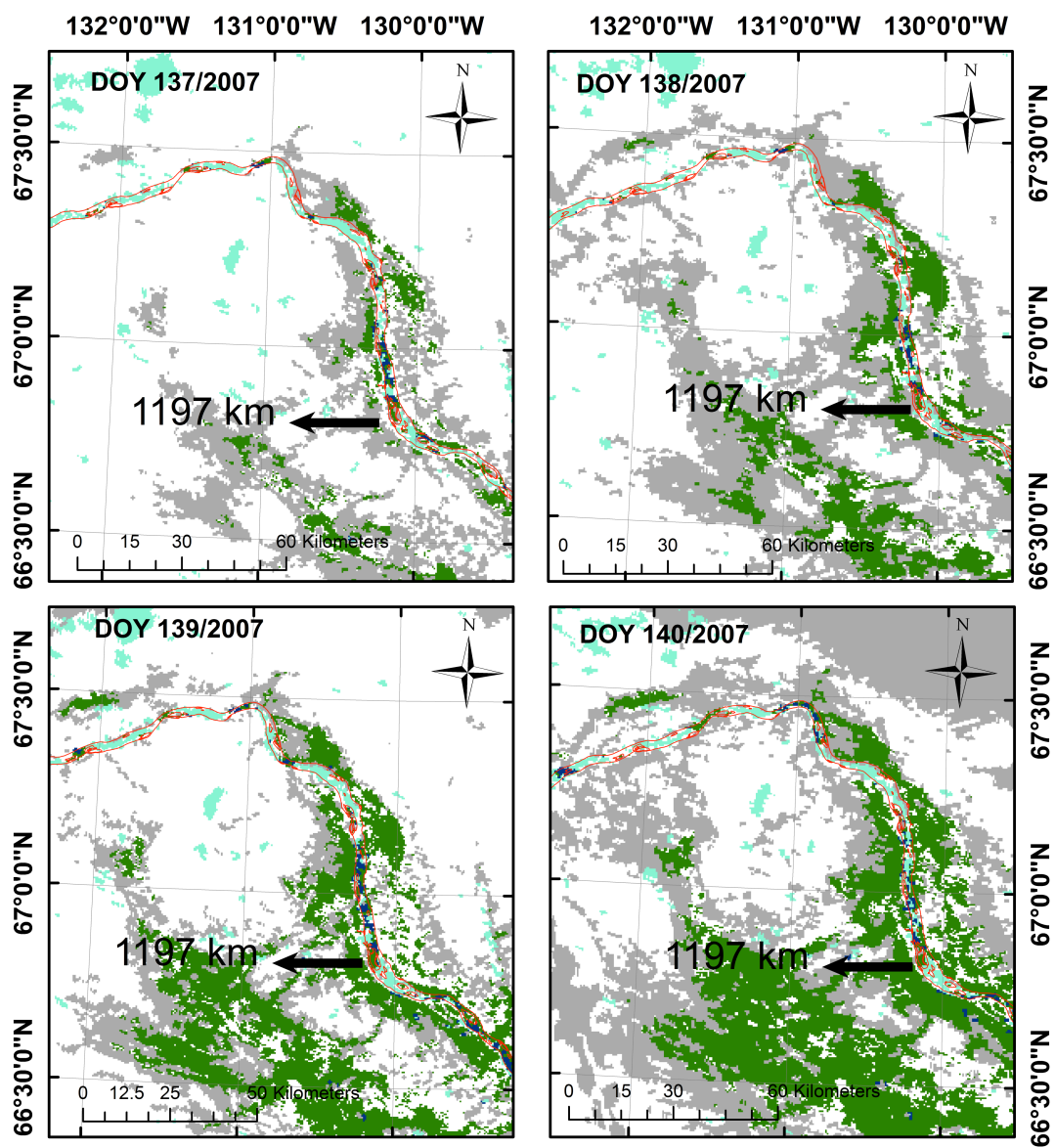


Figure 11: Ice flushing event recorded in 2010 between DOY 138-141. Here, on DOY141, the ice movement is last recorded after existing into the Mackenzie Delta.



### Legend

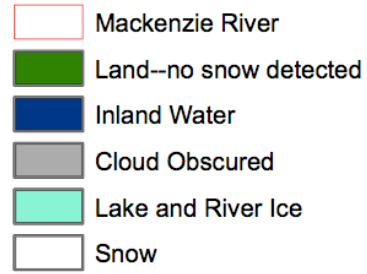


Figure 12: Observation of dynamic break-up over a section of the Mackenzie River Basin, showing concurrent ice break-up and snowmelt over 6 days. This was observed in 2007 between DOY 137-142.



Table 4: Summary of results from previous investigations and this study showing the beginning and end of the ice break-up period with respect to location and range and duration of period. Also shown are the sources of data used and years covered for analyses, and corresponding references.

Locations	Distances (km)	This Study	Beginning and End of Ice Breakup Dates Relative to Distance on the Mackenzie River as Reported by Previous Investigations			
Great Slave Lake	0			Beginning-120		
Fort Providence	75.8	Beginning-128 $\pm$ 8 days	Beginning-123		Beginning-135	Beginning-142
Campsell Bend	456					
Fort Good Hope	1080		End-140			End-151
Arctic Red River	1437				End-145	
Mackenzie River End	1460	End-145 $\pm$ 4 days		End-155		

Range of Break-up Dates		Beginning- $\pm$ 8 End- $\pm$ 4 days	8-10 days	N/A	N/A	N/A
Data Source		MODIS	WSC Hydrometric stations	MODIS/AVHRR	Ice Surveys	WSC Hydrometric Stations
Years Covered		2001-2013	1930's-2002	1992-2002	1946-1955	1927-1974
Reference			De Rham, 2008b	Pavelsky and Smith, 2004	MacKay, 1966	Allen, 1977