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Tel: +32 (0)2 650 22 15 / +32 (0)2 650 22 27**Email:** rdrews@ulb.ac.be**Response to Reviews :
Evolution of ice-shelf channels in Antarctic
ice shelves (tc-2015-44)**

Dear Editors,

thank you for handling the review process of this manuscript. The provided reviews are constructive and helpful; virtually all comments were taken into account leading to a revised version which is more accessible and easier to follow. The main changes were to expand the introduction and to explain the model setup in more detail (section 2.4). Figures 4 and 5 have been rearranged into new Figures 4—7 to show the surface topography and to better fit the layout of the journal. Additionally, a typo in the denominator of equation (3) was corrected for. The applied changes did not alter the conclusions from the initial manuscript. The annex contains the point-by-point responses to reviewers 1 and 2 together with a PDF version of the revised manuscript with changes marked in bold.

Please do not hesitate to contact me if questions arise.

With greetings from Belgium,

Reinhard Drews

Annex:

- Response to Reviewer 1 (RC C309)
- Response to Reviewer 2 (RC C356)
- Revised version with changes in bold

Response to reviewer's comment RC C309

Thank you for your constructive comments which helped to improve the current version of the manuscript, particularly in the way the model setup is explained. Virtually all of the proposed points have been implemented in the revised version. Attached is a point-by-point response. Reviewer's comments are marked italic, responses are marked in bold. In the revised manuscript changes are marked in bold.

Reinhard Drews,
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1 - The fact that the ice-shelf is not at the hydrostatic equilibrium is not only true in the channels vicinity. This is also occurring in the vicinity of the grounding line (GL), and can be shown both on observations [e.g. Anandakrishnan et al., 2007] and modelling [Lestringant, 1994; Durand et al., 2009]. The point is that specificity is not accounted for in the modelling as it seems that at the inflow BC (at the GL), the ice thickness is imposed to the floatation thickness. This is not clearly specified (it is only said that the mass flux is specified at this boundary). I would first suggest to be more precise on the landward BC. What is the horizontal velocity profile (homogeneous i guess)? Is only the horizontal velocity imposed? Not the vertical and lateral? Is the ice thickness imposed? Then, I am wondering how strong is this latter hypothesis. From Figs. 2 and 3, one can see that the melt is not imposed right at the GL, but few km downstream (how many?). Why? How are influenced the results if the melt is imposed closer to the GL, as expected from observations. My understanding is that by prescribing the ice thickness at the GL, the hydrostatic equilibrium is forced there and the melt has then to be artificially shifted downstream the GL if one wants to observe the bridging effect. I think this modelling point should be at least mentioned and the influence of a fixed geometry at the GL discussed.

Agreed with comment and implemented in revised version in section 2.4. The simulations presented here do not include the hydrostatic imbalance which naturally occurs at the grounding-line (indicated in the initial manuscript by “excluding grounding-line dynamics” (p. 1611, l. 5)). On the contrary, hydrostatic equilibrium is forced. During the ice-shelf evolution, the landward thickness can evolve freely and the inflow velocities are adjusted so that the mass flux remains constant (for example: initial conditions are 500 m landward thickness and 100 m a⁻¹ inflow velocities, lateral and vertical velocities are initially zero; after relaxation to steady state the landward boundary is 436 m with an inflow of 115 m a⁻¹ for the unconstrained cases). Because hydrostatic equilibrium is forced at the landward boundary, melting is initiated farther downstream to avoid numerical complications. This was not well enough explained and is now more detailed in section 2.4. Due to the model simplifications, no claims can be made about how channel initiate at the grounding-line and what the effects of the hydrostatic imbalance would be. The focus here is how channels evolve downstream of the grounding-line and how that compares to data which were collected comparatively close to the ice-shelf front of RBIS.

2 - My second main concern is about the use of the surface topography in the vicinity of the channels and how it compares from the observation and the modelling. From Fig. 1 it is obvious that these channels are visible from the surface. I am then wondering why the measured surface topography (especially the one transverse to the channels) is not compared to the modelled one? I agree that the real surface topography is not only the result of the

channels but also the perturbation of the accumulation distribution by the presence of a depression above the channels, which is certainly too complex to be accounted for in the modelling. But, it might be that some signatures of the surface topography are still observable and could be compared to the modelling. At least, this should be discussed.

Agreed with comment and implemented in revised version in Figures 4c and 5c. New Figures 4c and 5c now include the modeled and measured surface topography. Both figures agree qualitatively: Narrow channels with bridging are equally incised at the ice-shelf bottom as the wider channels where bridging is negligible. However, the corresponding depression at the surface are significantly shallower for the narrower channels. This is discussed in the revised version.

3 - As I said in the introduction, the strength of the work is certainly to couple both observations and modelling. In some sense this is also its weakness because the modelling should have been performed using the Roi Baudouin Ice Shelf geometry, which would have allow to get more specific conclusions (about melt rate for example) on the observed channels. I know it would have been a more challenging modelling effort, but the choice of a simplified and synthetic geometry should be better justified.

Ok and partially implemented in section 4. A real case application would give more quantitative results and that is something to be done in the future. However, a number of variables are yet uncertain, to name only two which have been discussed in the original version: (1) how does the surface mass balance change inside the channels and how does the change depend on the channel orientation relative to the main wind direction? The radar data shown here (and, for example, in Langley et al., 2014 (GRL, doi: 10.1002/2013GL058947)) indicate that this effect can be quite strong and it is not straightforward to model it quantitatively (as stated in your own comment #2); (2) does the density change inside the channels? If so, this imprints the traveltime-to-depth conversion of shallow layering and the corresponding SMB estimate, as well as the hydrostatic inversion. The advantage of using a basic synthetic geometry is that all mechanisms of the channel creation/advection/decay can be easily distinguished. Following the suggestions given here, this is more clearly motivated in the revised version in section 2.4.

page 1604, line 9: Inverting surface elevation for ice thickness -> Inverting surface elevation assuming hydrostatic equilibrium for ice thickness

Ok, inserted.

page 1604, line 22: I am not sure the Schoof (207) reference is relevant for this sentence.

Ok, removed.

page 1605, line 16: entirely Rignot and Steffen (2008). -> entirely (Rignot and Steffen, 2008).

Ok, inserted brackets.

page 1608, line 25: the choice of $i = 900 \text{ kg/m}^3$ should be discussed. Other works related to ice-shelves hydrostatic equilibrium, as the cited one by Holland et al. (2011), are using a higher value.

Ok, also in-line with the comment of Reviewer 2 it was updated to 918 kg m^{-3} which is a standard value. The initial reasoning was that pure ice density is only reached in very deep ice, but there was no strong justification for using 900 kg m^{-3} .

page 1610, line 20: from crevassetops -> from crevasse tops

Ok, implemented.

page 1611, 2.4 Model setup: missing information should be added (see main point 1). Also, I guess that as in the previous works using Elmer/Ice, you have specified a viscous spring at the base of the ice-shelf to account for the depth dependency of the sea hydrostatic pressure? This should be mentioned.

Ok, implemented in revised section 2.4. The viscous spring has been used and is explained and referenced in revised version.

page 1613, line 19: the choice of applying or not the lateral friction is not clearly discussed. It seems that it is switched on or off in an ad hoc way, but its effect is not really discussed. Would the results be similar if instead of applying lateral friction to decrease the main flow the inflow flux itself would simply be decreased (and no lateral friction applied)? In other words, are there other effects induced by lateral friction than decreasing the main ice flow of the ice-shelf?

Ok. Also in-line with comments from Reviewer 2 this is better explained at the end of section 2.4 and in the discussion. The point of applying lateral friction is to reduce longitudinal stretching rates to provide a scenario which can explain the enhanced horizontal shearing across a channel in the observations. This effect does not occur if longitudinal stretching is too dominant (as is the case for the unconstrained scenarios).

page 1615, line 22: which is too large at the channel trough, and too small at the channel flanks -> (?) which is larger at the channel trough, and smaller at the channel flanks

ok, implemented.

page 1615: I am wondering if having two channels in one model conducts to the same results/conclusions than having two simulations of one channels at a time. In other words, are the two channels interacting and influencing each other, or are they sufficiently distant not to interact? Is the purpose of having two channels with different melt distribution for the modelling MS4 only to have one plot showing two channels at a time? This point should be discussed/specified.

Ok, implemented in sections 3.2 and 4. In terms of the two channel's amplitudes and bridging there is no significant interaction between the two channels because they are sufficiently far apart. The purpose of having two channels is to more easily compare the simulations to the radar data.

Table 1: I would suggest to add a column with the number of channels (1 except for MS4 for which it is 2)

Ok, implemented.

Figure 2: I would suggest to remove the unnecessary black background

Ok, implemented.

Figure 3c: is the channel amplitude? It is not clear from the legend of the figure.

Misunderstanding: Channel amplitude was indicated by Y-Label. Legend marks melt scenarios.

Figures 4 and 5 are two small. The axe texts are difficult to read. I understand the paper was initially prepared for GRL, which has a limited number of figures. I would suggest to split these two figures in four figures to make them more readable. It should be also specified in the Legend of Fig. 4 that the two channels for the case MS4 have different melt distribution, as specified in Table 1.

Ok, implemented in new format/captions of Figures 4-7.

Manuscript: Evolution of ice-shelf channels in Antarctic ice shelves

Response to reviewer's comment RC C356

Thank you for your constructive comments which helped to improve the current version of the manuscript, particularly by making it more accessible for readers. Virtually all of the proposed points have been implemented in the revised version. Attached is a point-by-point response. Reviewer's comments are marked italic, responses are marked in bold. In the revised manuscript changes are marked in bold.

Reinhard Drews,

The paper presents results from observations and modelling of ice shelf channels, which is a topic of interest to a number of communities. I echo the sentiments of previous reviewers that the results aren't hugely original, but there is merit to the approach which utilises both field observations and modelling. The paper could be improved by making it slightly easier for the reader to compare the field and modelling results - especially by making Fig. 4 more user-friendly. A couple of extra references should be included, firstly the discussion of stabilisation of ice shelves (p1605) should include Khazander et al. (2009). The reader would also benefit from a short description of the role of plumes in forming the channels, and the suggested cause of basal accretion in filling in the channel downstream of the melting. The author assumes a large amount of contextual knowledge in some of the statements (e.g. p1615, line 7). Jenkins (2011) should be included in this description, and also on p1611, line 16: "...following the suggestions of Jenkins (2011) and Le Brocq et al. (2013)."

Ok, implemented. The figures have been revised (see new Figures 4-7) and the suggested references are included (plus some additional ones) in section 1. The basis of the plume model has been inserted in the revised version of section 1.

The purpose of the 5 experiments aren't well described – the reason for them becomes clear later, but a description at the end of page 1611 before the results section would help. Figure 4 could be greatly improved to help the comparison of the field & modelling evidence. Fig 4b and 4f are the comparison between the modelling result and the field evidence, and as such, they should be presented in as similar a way as possible. Show either lower surface OR ice thickness in both plots, at the moment it is very hard to compare. Also the effective meaning of the blue and red lines are switched in the two plots. Further, the inconsistent scaling of the x-axis makes it very hard to compare channel widths.

Ok, implemented. The different experiments are now better motivated at the end of section 2.4. Figures 4—7 have been revised, also in-line with comments of Reviewer 1.

Further, the discrepancy of hydrostatic thickness and radar thickness in "non-channel" ice shelf in Fig 4f suggests that you could improve the values/parameters which you use to derive hydrostatic thickness – this would make it easier to see when a channel isn't in hydrostatic equilibrium. At first I wasn't sure why you needed the non-channel part of the radargram, but it does help to see what the discrepancy is in non-channel areas. A section on how the model could be extended to answer more complex questions to do with the "evolution" of the channels

would also be useful. The paper has looked at fairly basic scenarios, more complex scenarios such as why the channels “meander” across the overall ice shelf flow direction would be an interesting question for example.

Ok. Using 918 kg m^{-3} instead of 900 kg m^{-3} (also see comment of Reviewer 1) removed the unphysical negative bias between hydrostatic- and radar-thickness. Section 4 has been revised, it now includes an outlook at the end on how the model and the observations can be further extended.

p1617, line 12: should this be “local maximum of the effective” rather than “off”?

Ok corrected.

P1618, line 17: should be trough rather than through?

Ok corrected.

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Evolution of ice-shelf channels in Antarctic ice shelves

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Abstract

Ice shelves buttress the continental ice flux and mediate ice–ocean interactions. They are often traversed by channels in which basal melting is enhanced, impacting ice-shelf stability. Here, channel evolution is investigated using a transient, three-dimensional full Stokes model and geophysical data collected on Roi Baudouin Ice Shelf (RBIS), Antarctica. The modeling confirms basal melting as a feasible mechanism for channel creation, although channels may also advect without melting for many tens of kilometers. Channels can be out of hydrostatic equilibrium depending on their width and the upstream melt history. Inverting surface elevation for ice thickness using hydrostatic equilibrium in those areas is erroneous and corresponding observational evidence is presented at RBIS by comparing the hydrostatically inverted ice thickness with radar measurements. The model shows that channelized melting imprints the flowfield characteristically, which can result in enhanced horizontal shearing across channels. This is exemplified for a channel at RBIS using observed surface velocities and opens up the possibility to classify channelized melting from space, an important step towards incorporating these effects in ice–ocean models.

1 Introduction

Almost three-quarters of the Antarctic ice-sheet boundary are in contact with the ocean (Bindschadler et al., 2011) where the majority of ice-mass loss occurs (Rignot et al., 2013; Depoorter et al., 2013). Floating ice shelves extend from the continental ice seawards, providing an interface for melting and refreezing processes at the ice-shelf base. Confined ice shelves transmit stresses landwards, controlling the grounding-line position and the continental mass flux (Gudmundsson, 2013; Pattyn et al., 2013). In the extreme case of an ice-shelf collapse (as observed on the Antarctic Peninsula), the regulating effect is entirely lost and leads to an acceleration of the grounded ice flow, hence sea level rise (Scambos et al., 2004). In some cases in West Antarctica, reduced ice-shelf buttressing has already led to irreversible mass loss (Joughin et al., 2014; Mouginit et al., 2014).

The ice-shelf integrity is influenced by fractures and rifts (e.g Borstad et al., 2013), as well as by the formation of ice mélange and marine ice with different rheological properties than meteoric ice (Khazendar et al., 2009; Pattyn et al., 2012; Dierckx and Tison, 2013; Kulesa et al., 2014). Melting and refreezing processes at the ice-shelf base are governed by the presence of ice-shelf water. The latter is formed inside the ice-shelf cavity by mixing of fresh water with other water sources such as high salinity shelf water or circumpolar deep water. The fresh water originates from melting at the ice–ocean interface and/or from basal water of the ice-sheet’s interior exiting at the grounding-line (Jenkins, 2011). Regardless of the specific origin, ice-shelf water is part of a buoyancy-driven circulation described as the ‘ice pump’ (Lewis and Perkin, 1986) which typically leads to high basal melt rates near the grounding-line and also to accretion of marine ice elsewhere. These ice–ocean interactions trigger a complex response of the continental ice sheet; knowledge of the basal mass exchange, and its spatial variability in particular, are important for predicting the ice-sheet evolution (Gagliardini et al., 2010).

A distinct feature of many ice shelves are longitudinal channels. They often start near the grounding-line, extend many tens of kilometers towards the ice-shelf front (Fig. 1a), and vary between a few hundred meters to a few kilometers in width. Channels may form spontaneously from transverse variability in ice thickness (Sergienko, 2013), and/or originate from subglacial water outlets of in-flowing glaciers (Le Brocq et al., 2013). In both cases current understanding suggests that the initial thickness perturbations near the grounding-line are amplified farther downstream through a buoyancy driven plume with enhanced basal melting within the channels. Channelized melting, with significantly higher melt rates inside than outside the channels, has been reported for Petermann Glacier Ice Shelf in Greenland (Rignot and Steffen, 2008; Dutrieux et al., 2014), and for Pine Island Ice Shelf (Vaughan et al., 2012; Mankoff et al., 2012; Stanton et al., 2013; Dutrieux et al., 2013, 2014) and for Fimbul Ice Shelf (Langley et al., 2014) in Antarctica. Channels may weaken ice shelves structurally through crevasse formation (Vaughan et al., 2012), or by breaking-up entirely (Rignot and Steffen, 2008). Channels can also stabilize ice shelves, by preventing

area-wide basal melting (Gladish et al., 2012; Millgate et al., 2013). In both cases the basal mass balance inside the channels is key.

Despite the importance of ice-shelf channels for ice–ocean interaction and for ice-shelf stability, little is known about their evolution from a glaciological perspective. This is because ice shelves are typically simulated in a computationally efficient manner by applying a number of simplifications to the Stokes equations. Most common is the hydrostatic approximation (e.g. Greve and Blatter, 2009, p. 117) which assumes in the vertical momentum balance:

$$\frac{\partial \sigma_{xz}}{\partial x} + \frac{\partial \sigma_{yz}}{\partial y} + \frac{\partial \sigma_{zz}}{\partial z} = \rho_i g \quad (1)$$

that the shear-stress gradients $\frac{\partial \sigma_{xz}}{\partial x}$ and $\frac{\partial \sigma_{yz}}{\partial y}$ play no role in balancing the gravitational force (given by the ice density ρ_i and the gravitational acceleration g acting in the vertical direction z). In that case, the vertical normal stress σ_{zz} is purely determined by the weight of the overburden ice column. Further approximations neglect vertical gradients of the horizontal velocities, leading to a vertically integrated set of equations with a linear profile of the vertical velocity (the shallow-shelf approximation, Morland, 1987; MacAyeal, 1989). While those approximations are well-suited to describe the large-scale flow of ice shelves, they fail to capture the full dynamics in ice-shelf channels where ice thickness and stresses change substantially over horizontal distances which are comparable to the mean ice thickness. For example, the negligence of the shear-stress gradients entails that ice is locally balanced by the water pressure (i.e. it is in hydrostatic equilibrium). However, observations indicate (Vaughan et al., 2012; Dutrieux et al., 2013) that some channels are out of hydrostatic equilibrium due to lateral stress transfer along the channel walls, an effect referred to as bridging (van der Veen, 2013, p. 57).

In this study we use a three-dimensional, transient, full Stokes model (Elmer/Ice, Gagliardini et al., 2013) pursuing three main questions: (1) how do channel amplitudes evolve as a function of basal melting and horizontal advection?, (2) under which conditions are channels out of hydrostatic equilibrium and how does the imbalance develop downstream?, and

(3) what is the imprint of the channel formation on the flow pattern of the surrounding ice shelf? Once a channel is formed, ice starts to converge into the channels (Dutrieux et al., 2013), presumably causing a reduction of the channel's amplitude while it is being advected downstream. Simulating those effects, helps to pinpoint the channel-state (active channelized melting or simple advection) as a function of its longitudinal position in the ice shelf. The second question is needed for deriving the basal mass balance in the channels using the continuity equation either in an Eulerian (e.g. Rignot and Steffen, 2008), or a Lagrangian (e.g. Dutrieux et al., 2013) framework. Both approaches require the ice thickness in the channels which is typically inferred from surface elevation using hydrostatic equilibrium. This assumption fails if bridging stresses prevent a full adjustment of the ice surface to hydrostatic equilibrium. Thirdly, observations (Dutrieux et al., 2013) show that melting channels imprint the surrounding flow field in a characteristic fashion. Simulating these patterns in an idealized geometry helps to better understand the mechanisms involved, and opens up the possibility to exploit the observed velocity anomalies for the classification of channels from high-resolution surface velocities.

We approach questions (1)–(3) using the full Stokes model and by comparing the results with radar and GPS data collected in 2012 and 2013 on the Roi Baudouin Ice Shelf (RBIS), Dronning Maud Land, Antarctica (Fig. 1). Section 2 details the methodology regarding surface elevation and ice flow (Sect. 2.1), the hydrostatic-thickness (Sect. 2.2), the radar-thickness (Sect. 2.3), and the model setup (Sect. 2.4). We then investigate the evolution of channel amplitudes (Sect. 3.1), hydrostacy (Sect. 3.2), and the imprint of channels on the surrounding ice flow (Sect. 3.3). We discuss the results in Sect. 4 and close by drawing conclusions regarding the role and characteristics of channels in ice shelves in Sect. 5.

2 Methods

2.1 Measuring of surface elevation and ice flow

Geodetic GPS data were collected to position radar profiles (kinematic mode) and for measuring ice flow (static-mode). All data were processed differentially relative to a base station on a grounded pinning-point with velocities of less than 3 cm per day (Fig. 1b). Daily base-station coordinates stem from precise point positioning of the Canadian Geodetic Survey. The solutions agree within centimeters with results from the Atomium software (Defraigne et al., 2008).

The kinematic elevations were corrected for the tidal displacement using the CATS02.01 model from Padman et al. (2002). The model was verified by comparing the simulated vertical displacements with the observed vertical displacements of GPS markers which measured continuously over an 8 day period. Differences between the model and the observations are 0.01 ± 14 cm (mean and standard deviation). The de-tided kinematic profiles differ in height at cross-over points with 0.08 ± 0.7 m.

For measuring ice flow, seven 3 m-long stakes were installed in 2013 along a 4 km long cross section traversing a channel (profile O-O' in Fig. 1). The GPS antennas were mounted on top of the stakes, and measured for at least 30 min. About 3–4 stakes were occupied simultaneously, in order to position the stakes in a network approach using closed loops of relative baselines. The processing was done using the GAMIT, GLOBK/TRACK v.10.5 (Herring et al., 2013) software package, and followed the procedure described in Bergeot et al. (2009) including GPS dual frequency observables, precise GPS orbits, and absolute phase center corrections for the ground and satellites antennas. Positioning errors reported from the software are within a few centimeters. The measurements were repeated after 7 days to measure the marker's displacement. Because this time interval is comparatively short to infer velocity differences between the markers, the same stake array was revisited in 2014. In order to cross-check the results with a different processing technique, we used precise point positioning of the Canadian Geodetic Survey to infer the yearly averaged marker velocities. Both sets of measurements show spatially the same pattern, and differ

in magnitude by less than 3%. Regardless whether this constant offset reflects processing-uncertainties and/or a real change in flow behaviour between the weekly and the yearly averages, the uncertainties are small enough to use the GPS-derived velocities as ground-truth for satellited-based velocities.

5 2.2 Determination of the hydrostatic-thickness

The hydrostatic-thickness H of a freely floating ice shelf can be derived from the freeboard height h_{asl} (i.e. the ice shelf's height relative to the ocean surface) using the buoyancy formula with the densities of sea water ($\rho_w = 1027 \text{ kg m}^{-3}$), ice ($\rho_i = 918 \text{ kg m}^{-3}$), and air ($\rho_a = 2 \text{ kg m}^{-3}$):

$$10 \quad H = \frac{\rho_w h_{\text{asl}}}{\rho_w - \rho_i} - \frac{\rho_a - \rho_i}{\rho_i - \rho_w} H_a. \quad (2)$$

To account for lower-density firn, the ice shelf is decomposed into layers of ice (H_i) and air (H_a), so that $\overline{\rho(z)}H \equiv \rho_i H_i + \rho_a H_a$ holds for the depth-averaged density $\overline{\rho(z)}$. In areas where the ice shelf is not freely floating (i.e. where the ice column is not only balanced by the water pressure, but also by stresses within the ice as is the case near the grounding-line and potentially in ice-shelf channels) this equation is not valid. This will be investigated in
15 more detail in Sects. 3 and 4.

The freeboard height follows from the GPS height (z , referenced to the WGS84 ellipsoid) by correcting for the geoid (G) and the mean dynamic topography (MDT): $h_{\text{asl}} = z - (G + \text{MDT})$. Here, the EIGEN-GL04C geoid (Förste et al., 2008) is used which, at RBIS, varies
20 between 18 and 19 m and deviates less than 0.3 m from the EGM2008 ellipsoid (Pavlis et al., 2012). However, geodetic measurements in nearby Breid Bay (Shibuya et al., 1999) result in a geoid height of approximately 22 m, a value which is close to the presumably outdated EGM96 geoid (developed by NASA, NIMA and Ohio State University). The MDT corrects for long-term differences between geoid and ocean surface. At RBIS it is estimated
25 with -1.2 m (Andersen and Knudsen, 2009), but uncertainties of the MDT are large for the Antarctic perimeter (O. Andersen, personal communication, 2014).

The equivalent air content (H_a) is 15 m, based on ice-core measurements (Hubbard et al., 2013), and approximately 12 m based on atmospheric modeling (Ligtenberg et al., 2014). Differences may partially reflect spatial variability, given that the ice-core's location, close to both the ice-shelf front and a rift system, is not fully representative for the research grid (Fig. 1b).

The dominating uncertainties for obtaining the hydrostatic-thickness are hence rooted in the determination of h_{asl} (mainly due to uncertainties in G , MDT, and cross-over errors of the kinematic GPS profiles) and H_a (reflecting uncertainties of the depth-averaged density). Uncertainties of the geoid and the MDT have little spatial variation within the research grid and biases carry over to the hydrostatic thickness as constant offsets without spatial dependence. To represent the combined uncertainty, we calculate a lower and an upper estimate (the lower estimate assuming $h_{\text{asl}} - 2.0$ m and $H_a = 15$ m, the upper estimate assuming $h_{\text{asl}} + 2.0$ m and $H_a = 12$ m). The mean difference between those two cases is 50 m.

2.3 Determination of the radar-thickness and internal layering

The thickness of ice can be determined with radar by measuring the two-way traveltime of a radar pulse which is emitted at the surface and reflected at the base. For ice shelves, the radar-thickness is ambiguous because basal reflections may either originate from a meteoric ice–ocean interface or from a meteoric ice–marine ice interface (e.g. Blindow, 1994; Kulesa et al., 2014). For the latter case, the radar-thickness is smaller than the hydrostatic-thickness, and the difference corresponds to the thickness of the marine ice layer. For a reliable detection, the marine ice layer should have a thickness larger than 50 m (measured in the ice equivalent density of meteoric ice), given the uncertainties derived in the previous section.

The radar-thickness was measured using a 10 MHz radar with resistively loaded dipole antennas (e.g. Matsuoka et al., 2012). Kirchhoff depth migration was applied to account for off-nadir reflections from slanted channel walls. For the examples presented here, the non-migrated data show reflection hyperbolas from crevasse tops. The travel-time to depth conversion uses the pure ice velocity ($v_i = 168 \text{ m } \mu\text{s}^{-1}$) and corrects for faster wave prop-

agation in firn by adding 6.5 m. The correction is based on the ice-core density and an empirical density-permittivity model (Kovacs et al., 1995). The previously discussed uncertainty of the depth–density profile (corresponding to the uncertainty in H_a) changes the radar thickness by less than 2 m. Post-processing for visualizing the deeper internal layers (> 50 m depth) included low-cut filtering, bandpass filtering, and a depth-variable gain function. The shallow layering (< 50 m depth) was measured with a 400 MHz radar (GSSI:SIR 3000) which occupied the same profile lines as the 10 MHz radar. The post-processing is that used for the 10 MHz data.

2.4 Model setup

The ice-shelf model is based on the ones used in previous studies (e.g. Durand et al., 2009; Favier et al., 2012, 2014), but simplified by excluding grounding-line dynamics and thermal effects. It is three-dimensional, transient, and full Stokes (based on Elmer/Ice, Gagliardini et al., 2013) with a Glen rheology (Cuffey and Paterson, 2010, p. 51), and has a constant surface mass balance (0.3 m a^{-1}) and uniform temperature (-10°C). **Ocean pressure is applied at the front and at the bottom. The buoyancy pressure at time t is determined by the unknown ice-shelf geometry of this time step. Because small hydrostatic imbalances cause large vertical velocities, the geometry cannot easily be approximated with the previous time step. The system is therefore stabilized by introducing a time-dependent scheme for the bottom interface evolution (a.k.a. viscous spring), which is explained in more detail in Durand et al. (2009, section 3.4).**

At the lateral boundaries the normal velocities are zero, and for the unconstrained case, horizontal shearing parallel to the boundary is equally zero. The constrained case includes horizontal shearing by using a constant slip coefficient with a linear sliding law. The surface and the bottom can move freely. **The landward boundary is in hydrostatic equilibrium; initial inflow velocities and ice thickness are 100 m a^{-1} and 500 m , respectively. Lateral and vertical velocities are initialized with 0 m a^{-1} and not further imposed. The thickness at the landward boundary changes during the evolution, and the inflow velocities are adapted so that the mass flux remains constant. The ice shelf is evolved**

without basal melting until it reaches a steady-state geometry (for the unconstrained cases the steady-state landward thickness and inflow velocities are 436 m and 115 m a⁻¹, respectively). Channels are then initiated through localized melting near the upstream-boundary, following the suggestions of Jenkins (2011) and Le Brocq et al. (2013). The prescribed melt rates have the form:

$$M(x, y) = A \frac{e^{-(y-y_0)^2 / (2\sigma_y^2)}}{(e^{b((x-x_0)-a)} + 1) \cdot (e^{b(-(x-x_0)-a)} + 1)} \quad (3)$$

using a coordinate system where x is along-flow, y across-flow, and z vertically upwards. Across-flow, M is a Gaussian curve with RMS width σ_y and peak A . The curve is extended along-flow with a determining the extension length, and b the steepness of M along x to reach A ; x_0 and y_0 describe the center of melting in x and y direction, respectively. Table 1 and Fig. 2 summarize the characteristics and parameters of the individual simulations discussed below.

The forced hydrostatic equilibrium at the landward-boundary saves computation time, but is unphysical because grounding-lines are typically not in hydrostatic equilibrium (e.g. Lestringant, 1994; Durand et al., 2009; Bindshadler et al., 2011). The applied simplifications cause small hydrostatic imbalances at the lateral boundaries which, however, do not imprint the ice-shelf center where the channel evolution is investigated. Because the landward boundary is freely floating, channels are carved into the steady-state ice shelf with an approximately 4 km seaward offset. This hampers the investigation of how channels behave directly at the grounding-line, but does not impact the channel evolution farther downstream. The latter is the focus of this study, as field data has been collected relatively close to the ice-shelf front (Figure 1).

The synthetic ice-shelf geometry applied here hampers a one-to-one comparison with the field data and excludes quantification of basal melt rates. In turn, the simplified geometry allows to distinguish more easily between the different mechanisms acting during the channel creation, advection, and decay. Laterally unconstrained

cases are used to study the channel-amplitudes and bridging effects. A laterally constrained case, with reduced longitudinal stretching, is used for investigating the channel's imprint on the surrounding flowfield. This is done to provide a scenario for an effect seen in the observed surface velocities (i.e. increased horizontal shearing across channels) which is not apparent in the simulations when longitudinal stretching is too dominant.

3 Results

3.1 Development of channel amplitudes

Figure 3 displays the along-flow development of channel amplitudes in an unconfined ice shelf for three melt scenarios differing in the peak magnitude and longitudinal extent ($A = 14, 2.3, \text{ and } 1.6 \text{ m a}^{-1}$ over $a = 1, 6.5, \text{ and } 8.5 \text{ km}$, respectively; MS 1–3, Table 1 and Fig. 2a–c). The channel amplitudes A_{ch} are defined as:

$$A_{\text{ch}} \equiv 1 - H_{\text{in}}/H_{\text{out}} \quad (4)$$

with H_{in} , and H_{out} for the ice thickness at the channel trough and the channel keel, respectively. The melt functions $M(x, y)$ are chosen so that at the downstream end of the longest prescribed melting (here at distance $L = 20 \text{ km}$ from the grounding line), the cumulative melt rate is equal for all cases. Along the central flowline ($y = 0$), this means: $\int_0^L M_1(x, 0)dx = \int_0^L M_2(x, 0)dx = \int_0^L M_3(x, 0)dx$ (Fig. 3a). The cumulative effective melt ($M_{\text{eff.}}$, Fig. 3b) for each scenario is different, because the residence time in which ice is subject to melt also depends on the modelled along-flow velocities v_x :

$$M_{\text{eff.}}(x) = \int_0^x \frac{M(x', 0)}{v_x(x')} dx'. \quad (5)$$

Figure 3c shows that channel amplitudes increase in areas where channelized melting is sustained and that they decay when melting ceases. The amplitudes at the downstream-end differ less than 10% for all scenarios.

3.2 Channels and hydrostatic equilibrium

5 In order to check if the simulated channels are in hydrostatic equilibrium, we invert the simulated surface topography for ice thickness using Eq. (2) (with $H_a = 0$ because firn is excluded in the simulations) and compare this hydrostatic-thickness with the modelled-thickness. Channels are in hydrostatic equilibrium if both thicknesses are equal. The channels investigated in the previous section have a keel-to-keel width of approximately
10 2 kilometers ($\sigma_{y1} = 500$ m) and are essentially in hydrostatic equilibrium everywhere. Some channels at RBIS are narrower, and we investigate bridging by considering two channels with $\sigma_{y1} = 100$ m and $\sigma_{y2} = 75$ m, using otherwise the same boundary conditions as above (MS4, Table 1). **This setup is comparable to channels observed at RBIS. In the simulations, we observe no significant interaction between the two channels, and the varying channel-width is the main difference regarding the channel evolution.** Figure 4a shows that, unlike the wider channel, the narrower channel is out of hydrostatic equilibrium for tens of kilometers along-flow. The imbalance increases along-flow in areas of channelized melting and decreases farther downstream. Bridging stresses are larger in the narrower channel than in the wider one (Fig. 4b), **the surface is less depressed in the narrower channels (Fig. 4c)**, and the hydrostatic-thickness deviates from the modelled thickness inside the narrower channel (Fig. 4d). .
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Figure 5a–d compares this situation with two radar/GPS cross sections (A-A', B-B' Fig. 1) across two channels (Ch.-1, Ch.-2) with variable widths. Hydrostatic- and radar-thickness agree in most areas within their error bounds, except for the narrower Ch.-2 on profile B-B', where the hydrostatic-thickness is anomalously larger. This anomaly is consistently
25 observed in profiles across Ch.-2 farther upstream.

3.3 Imprint of channels on the surrounding flow field

The imprint of channel formation on the surrounding flowfield is depicted for a laterally constrained ice shelf (MS5, Table 1) in Fig. 6a–f. The large-scale pattern of the along-flow velocities, and the along-flow strain rates ($\dot{\epsilon}_{xx}$) is inconspicuous (Fig. 6a and d). Across-flow velocities (which are zero without a channel), however, point towards the channel with magnitudes of a few meters per year (Fig. 6b). This convergence is prominent in the across-flow and vertical-strain rates ($\dot{\epsilon}_{yy}$ and $\dot{\epsilon}_{zz}$, Fig. 6d, e), both showing an increasing anomaly up to the point where channelized melting stops. Without channelized melting, the characteristic patterns decay at greater distances. The otherwise smoothly varying along-flow velocities increase step-wise in across-flow profiles (Fig. 7a) near areas of channelized melting. The velocity-step is evident in lateral shearing ($\dot{\epsilon}_{xy}$), and accompanied by a peak in the effective strain rate ($\dot{\epsilon}_E = \sqrt{\frac{1}{2}(\dot{\epsilon}_{xx}^2 + \dot{\epsilon}_{yy}^2 + \dot{\epsilon}_{zz}^2) + \dot{\epsilon}_{xz}^2 + \dot{\epsilon}_{xy}^2 + \dot{\epsilon}_{yz}^2}$).

A comparable feature is found in the field data: Fig. 7b displays the measured speed for a line of markers, densely placed across a channel (O-O', Fig. 1). **The marker's displacements were measured after one week and after one year. Both type of measurements show the same tendency:** Speed increases from East to West, following the general ice-flow pattern in this area. Near the channel's trough, however, the velocity increase is anomalously larger than the underlying East–West tendency. The signal is equally apparent in four different sets of satellite-based velocities derived from different techniques, time intervals, and sensors (1: speckle and phase offset tracking in RADARSAT data from 2000 (Callens et al., 2014); 2: mosaicked velocities by Rignot et al. (2011); 3: interferometric SAR from European Remote Sensing (ERS) satellites in 1996 (S. Berger, personal communication, 2014); 4: speckle tracking using data from the Advanced Land Observing Satellite in 2010 (S. Berger, personal communication, 2014)). Strain rates derived from the ERS data surrounding the stake array are depicted in Fig. 8a–c.

4 Discussion

The simulations presented here confirm that channelized basal melting is a feasible mechanism to transform initially small thickness perturbations near the grounding-line into mature channels farther downstream. In that sense, the full Stokes model supports, from a glaciological perspective, the studies of Gladish et al. (2012) and Sergienko (2013), both using simplified ice dynamics to allow for an efficient coupling with ocean models. The along-flow amplification rate of the channel amplitudes is primarily determined by the upstream ratio of basal melting and along-flow advection (determining the effective melt M_{eff}). The maximum amplitude of MS1 is largest, because all basal melt occurs where ice is slow; the ratios between the maximum effective melt of the different scenarios are equal to the ratios between the corresponding maximum channel amplitudes (Fig. 3b and c).

Without basal melting, channels decay. In the unconstrained case considered here, horizontal advection is fast and the channels still have a considerable amplitude when reaching the ice-shelf front. In the constrained case (not shown here), horizontal advection is reduced resulting in smaller final amplitudes for the same melt scenarios. Because channels can be sustained without basal melting for many tens of kilometers, their mere existence in satellite imagery or radar data is not a sufficient condition to infer channelized melting at this location. Conversely, the disappearance of a channel does not necessarily imply basal accretion, and more data are required to characterize the channel's state. A typical approach to obtain the channel geometry is the hydrostatic inversion of highly-resolved elevation models, a method which fails if bridging stresses prevent a full adjustment of the channel surface to hydrostatic equilibrium.

In order to compare the geometries of the simulated channels with the observations at RBIS, we use the ratio (α) between the keel-to-keel width and the ice thickness at the channel keel. Figure 4 illustrates that for steady-state conditions, and for the range of melt parameters considered here, channels with $\alpha > 5$ are essentially in hydrostatic equilibrium. Narrower channels ($\alpha < 5$) can deviate from hydrostatic equilibrium. In Fig. 4a, the imbalance is largest at the downstream end of channelized melting, and contains a memory of

the upstream melt history: melt scenarios with higher peak values over a shorter longitudinal extent (e.g. MS1-type vs. MS4-type, Fig. 2) produce channels with comparable α , but with a smaller imbalance. Regardless of the upstream melt history, a typical feature for simulated channels that are out of hydrostatic equilibrium **is that the surface depression is wider and shallower (Figure 4c) than what would be suggested from hydrostatic equilibrium. Consequently,** the hydrostatic-thickness is larger at the channel trough, and smaller at the channel flanks. The spatial pattern of the imbalance may be different when melting is concentrated on the channel's walls only (Dutrieux et al., 2013, 2014).

To validate if bridging does play an important role for channels observed at RBIS, we investigate the anomalously large hydrostatic-thickness in Ch.-2 on profile line B-B' (Fig. 5d): **While Ch.-1 and Ch.-2 are almost equally incised at the ice-shelf bottom, the surface of Ch.-2 is less depressed than that of Ch.-1 (Fig. 5c). This causes a mismatch between radar- and hydrostatic-thickness, which is significant because, with the exception of Ch.-2 on B-B', the radar thickness is within the error bounds of the hydrostatic-thickness (including Ch.-1 and Ch.-2 on profile line A-A').**

For the large hydrostatic-thickness in Ch.-2 on profile line B-B' three explanations can be put forward: (1) the depth-averaged density varies laterally across channels, (2) bridging stresses prevent a full relaxation of Ch.-2, and/or (3) Ch.-2 contains a 20–60 m thick layer of marine ice which is not detected by radar. Variations of the depth-averaged densities across channels can be caused by changes in the surface mass balance (SMB), which is a function of surface slope (e.g. Lenaerts et al., 2014). Increased SMB inside the channels can explain the observed synclines in the shallow radar layers (Fig. 5a), and accords with observations from Langley et al. (2014) for channels perpendicular to the wind direction (as is the case here). Rearranging Eq. (2) allows us to calculate how the equivalent air content H_a must change spatially in order to obtain hydrostatic equilibrium in the absence of marine ice (c.f. Holland et al., 2011). This scenario necessitates $H_a \sim 22$ m inside Ch.-2, compared to a baseline of $H_a = 13$ –16 m outside the channel (Fig. 5d). Such a large change is only required for Ch.-2 along B-B', not for any other channel. **Given that the surface depression of Ch.-2 is smaller than that of Ch.-1 (Fig. 5c), this seems unlikely.**

Regarding the channel width, Ch.-1 is always wider than Ch.-2, and Ch.-2 along B-B' is narrower ($2.5 < \alpha < 3.5$) than Ch.-2 along A-A' ($4 < \alpha < 5$). The observations cannot directly be compared with the simulations from above (due to the unknown melt history, and because of ambiguities in locating the channel keels), however, the narrowing of Ch.-2 and the subsequent mismatch between hydrostatic- and radar-thickness accord with what would be expected from the simulations. While other mechanisms (i.e. spatially variable density or marine ice) may still be at work, the combined evidence from modelling and observations presented here shows that bridging effects are non-negligible for narrow ice-shelf channels. Studies inverting elevation models to obtain ice thickness inside channels must take this effect into account.

The simulations presented in Fig. 6a–f exemplify characteristic points of channel formation: basal melting reduces the ice thickness inside channels and causes vertical velocities at the ice-shelf bottom to be negative. This increases the vertical strain rates ($\dot{\epsilon}_{zz}$) inside the channels, causing subsequent lateral convergence ($\dot{\epsilon}_{yy}$) while longitudinal stretching ($\dot{\epsilon}_{xx}$) is only slightly affected. The spatial patterns of $\dot{\epsilon}_{yy}$ and $\dot{\epsilon}_{zz}$ mirror the prescribed channelized melting: they increase downstream as long as bottom melting is sustained, and they decrease where bottom melting is absent. Dutrieux et al. (2013) have noted lateral convergence of ice into melting channels, and this idealized simulation provides the theoretical underpinning for these observations. It becomes evident that lateral convergence increases as long as bottom melting is sustained, after bottom melting ceases, the convergence decreases. For the specific setting investigated here (**i.e. for a laterally constrained ice shelf vs. a laterally unconstrained ice shelf**), changes of $|\dot{\epsilon}_{xx}|$ and $|\dot{\epsilon}_{yy}|$ result in a local maximum of the effective strain rate inside the channel. Because ice deforms more readily when the effective strain rate is elevated (according to Glen's flow law, Cuffey and Paterson, 2010, p. 51), the simulated velocity changes step-wise inside the channel (Fig. 7a). This feature is not universal for channelized melting. It can be essentially absent when longitudinal stretching is too dominant (e.g. in the unconstrained case in which changes in $|\dot{\epsilon}_{xx}|$ offset changes in $|\dot{\epsilon}_{yy}|$ in the effective strain rate).

The simulations propose that channelized melting imprints the channel's flow field in a characteristic way which can be detected in the surface velocities. The flow of ice shelves, however, is often dominated by other mechanisms (e.g. divergence/convergence through tributary glaciers) which may mask the comparatively small effects of channelized melting. Nevertheless, along profile O-O' (Fig. 7b) a similar velocity step occurs in the observational data. This step is significant, given the coherence of the yearly- and weekly-averaged GPS velocities, confirming the available satellite data. The latter may partially be biased, because interferometric surface velocities require elevation models (e.g. Neckel et al., 2012), which typically do not fully resolve the channel topography. This effect, however, appears to be negligible here. Figure 8a–c shows that the cross section displayed in Fig. 7b is spatially coherent, and that the channel in this area exhibits a similar behaviour as suggested by the simulations above: lateral convergence is clearly evident and accompanied by enhanced horizontal shearing. Longitudinal extension changes little. Although no direct evidence for the melt history of Ch.-1 exists, this is a likely show-case for both, i.e., how channels imprint the surrounding flow field, and how this can be measured with GPS and satellite-based data. This foreshadows a large potential of analysing high-resolution surface velocities to determine channelized melting from space.

The basic model scenarios studied here can be extended by including merging, diverging, and meandering channels to investigate to what extent ice shelves archive temporal changes in basal hydrology at the grounding-line. Because vertical velocities vary across channels, enhanced advection of cold ice from the surface should be accounted for by including thermo-mechanical coupling. From the observational side, it will be important to better understand the surface mass balance anomaly inside channels and to establish a link between the channel orientation and main wind direction. This directly impacts on the quantification of basal melt rates either using mass conservation principles or using dipping internal radar layers in an inversion procedure. The observed and simulated velocity anomaly presented here is restricted to comparatively simple strain regimes. The application of the model on a real-case geometry will guide the detection of velocity anomalies in more complex

flow settings, facilitating a larger-scale mapping of melting channels using surface velocities only.

5 Conclusions

The full Stokes modelling confirms enhanced channelized melting as a feasible mechanism for the formation of ice-shelf channels. If melting is not sustained, channels gradually decay but may still persist in ice shelves for many tens of kilometers. Therefore, the mere existence of channels in satellite or radar data does not directly imply channelized melting at the location where the channel is observed. In turn, the disappearance of channels does not necessitate basal ice accretion.

The simulations show that channels can be out of hydrostatic equilibrium, and a corresponding example has been discussed for an ice-shelf channel at RBIS. Assuming that melting peaks at the channel's trough, bridging results in a hydrostatic-thickness which is larger at the channel troughs, and smaller at the channel flanks. The imbalance is a function of both the channel width and the upstream melt history. This effect must be taken into account when inverting the surface elevation for ice thickness in order to obtain the basal mass balance using mass conservation.

The channel formation imprints the surrounding flow field characteristically. In areas where longitudinal stretching is not too dominant (e.g. for ice shelves which are sufficiently constrained by embayments or pinning-points), this increases the effective strain rate, locally softens the ice, and produces a characteristic velocity-anomaly across the channels which has been observed at RBIS in ground- and satellite-based velocities. Independent of the specific flow setting, melting channels produce generic velocity patterns on kilometer scales which are likely suited for identifying channelized melting from space, allowing to pinpoint the important role of channels on ice–ocean interactions and ice-shelf stability on large spatial scales.

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Table 1. Parameters (number of channels (#Ch.), along-flow distance (x), across-flow distance (y), mean thickness (\overline{H}), mean along-flow velocity ($\overline{v_x}$), number of elements (#elem.), lateral boundary condition (BC)) for the different scenarios MS1–5.

Name	#Ch.	dim. ($x, y; \overline{H}$)	$\overline{v_x}$	#elem. (x, y, z)	BC ¹	parameters $M(x, y)$
MS1	1	30 × 10 km; 260 m	210 m a ⁻¹	90 × 60 × 10	uc	$y_0 = 0$ km; $x_0 = 4.5$ km; $a = 1.0$ km; $b = 0.2$; $\sigma_y = 0.5$ km; $A = 14$ m a ⁻¹
MS2	1	30 × 10 km; 260 m	210 m a ⁻¹	90 × 60 × 10	uc	$y_0 = 0$ km; $x_0 = 9$ km; $a = 6.5$ km; $b = 0.2$; $\sigma_y = 0.5$ km; $A = 2.3$ m a ⁻¹
MS3	1	30 × 10 km; 260 m	210 m a ⁻¹	90 × 60 × 10	uc	$y_0 = 0$ km; $x_0 = 12$ km; $a = 8.5$ km; $b = 0.2$; $\sigma_y = 0.5$ km; $A = 1.6$ m a ⁻¹
MS4	2	30 × 6 km; 260 m	210 m a ⁻¹	90 × 90 × 10	uc	$y1_0 = -0.7$ km; $x1_0 = 4.5$ km; $y2_0 = 0.7$ km; $x2_0 = 4.5$ km; $a1 = 1.0$ km; $b1 = 0.2$; $\sigma_{y1} = 0.2$ km; $A1 = 2.3$ m a ⁻¹ ; $a2 = 1.0$ km; $b2 = 0.2$; $\sigma_{y2} = 0.075$ km; $A2 = 2.3$ m a ⁻¹
MS5	1	30 × 15 km; 260 m	122 m a ⁻¹	90 × 60 × 10	c	$y_0 = -1.5$ km; $x_0 = 4.5$ km; $a = 1.0$ km; $b = 0.2$; $\sigma_y = 0.5$ km; $A = 3.5$ m a ⁻¹

¹ For the lateral boundaries: unconstrained (uc) or constrained (c).

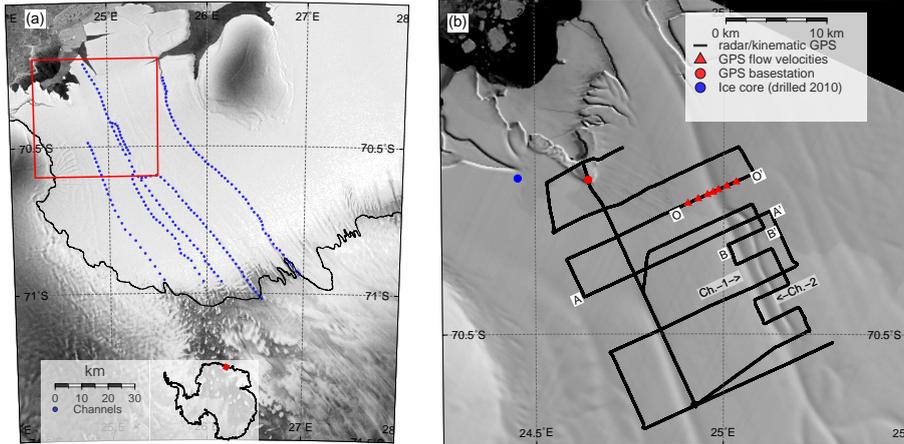


Figure 1. Overview of Roi Baudouin Ice Shelf, Dronning Maud Land, Antarctica: **(a)** Ice-shelf channels start near the grounding-line and extend into the ice shelf (marked with blue dots in the Radarsat Mosaic, Jezek and RAMP-Product-Team, 2002). The red box marks the close-up in **(b)** locating radar/GPS profiles of the surveys. Channels (e.g. Ch.1, Ch.2) appear in the background image (Landsat 8 in December 2013) as elongated lineations.

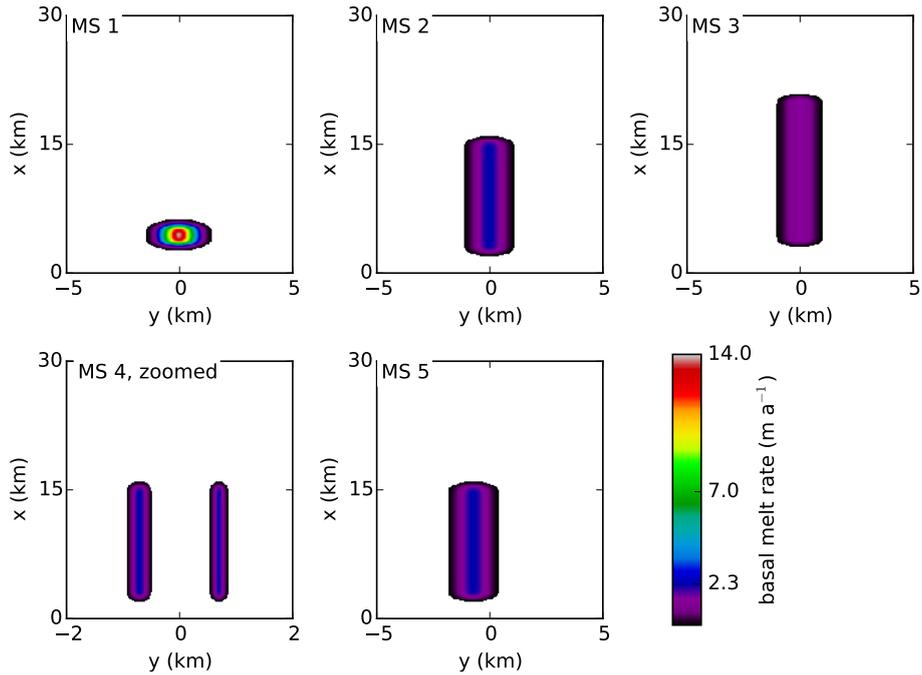


Figure 2. Visualization of melt scenarios MS1–5 detailed in Table 1.

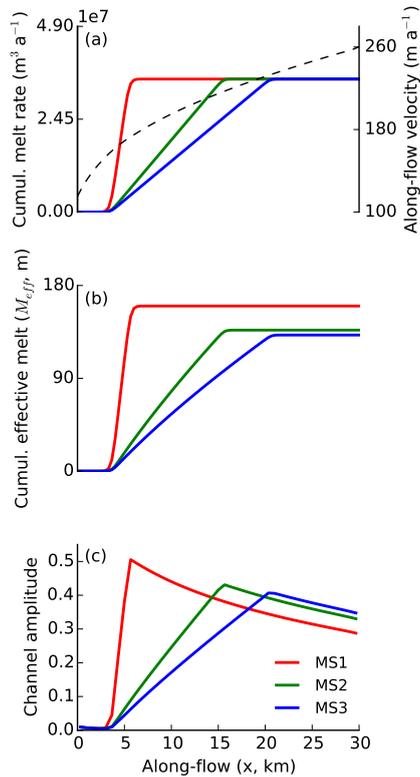


Figure 3. Colored curves display the along-flow cumulative melt rates for the different melt scenarios (MS1–3, Table 1) in (a), the effective melt in (b) and the corresponding channel amplitudes in (c) for a laterally unconstrained ice shelf in steady state.

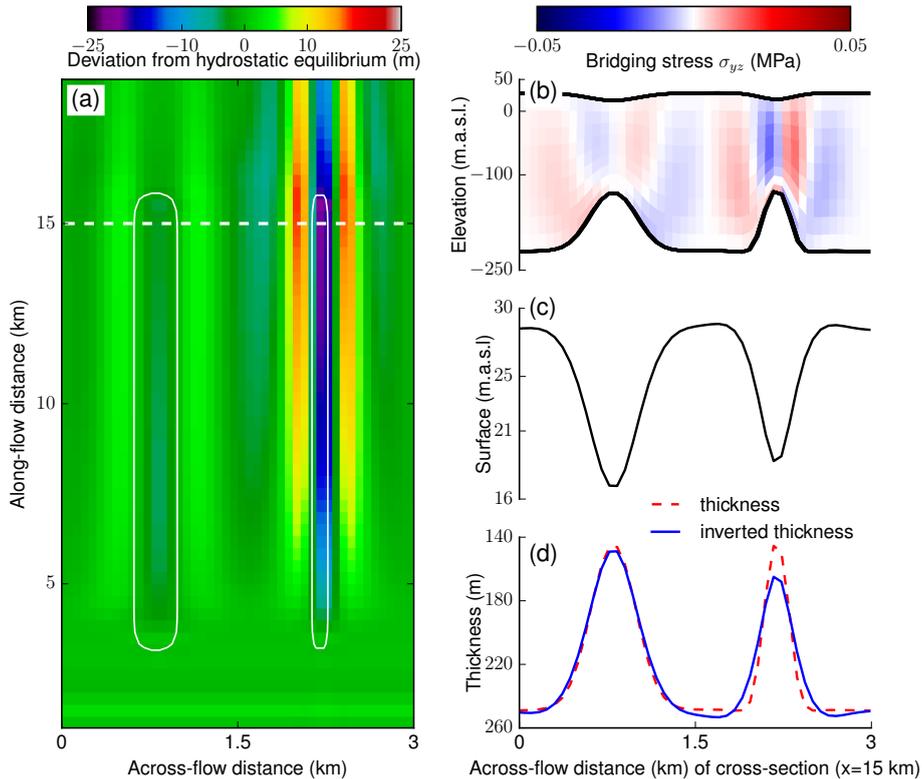


Figure 4. Steady-state results for a laterally unconstrained ice shelf with two channels. The prescribed melt function has the same peak amplitude for both channels but varies in the across-flow width (MS4, Table 1). The deviation from hydrostatic equilibrium is shown in (a). The white curves mark zones of melting, the dashed line depicts the cross-section showing bridging stresses in (b), the surface in (c), and ice thickness in (d).

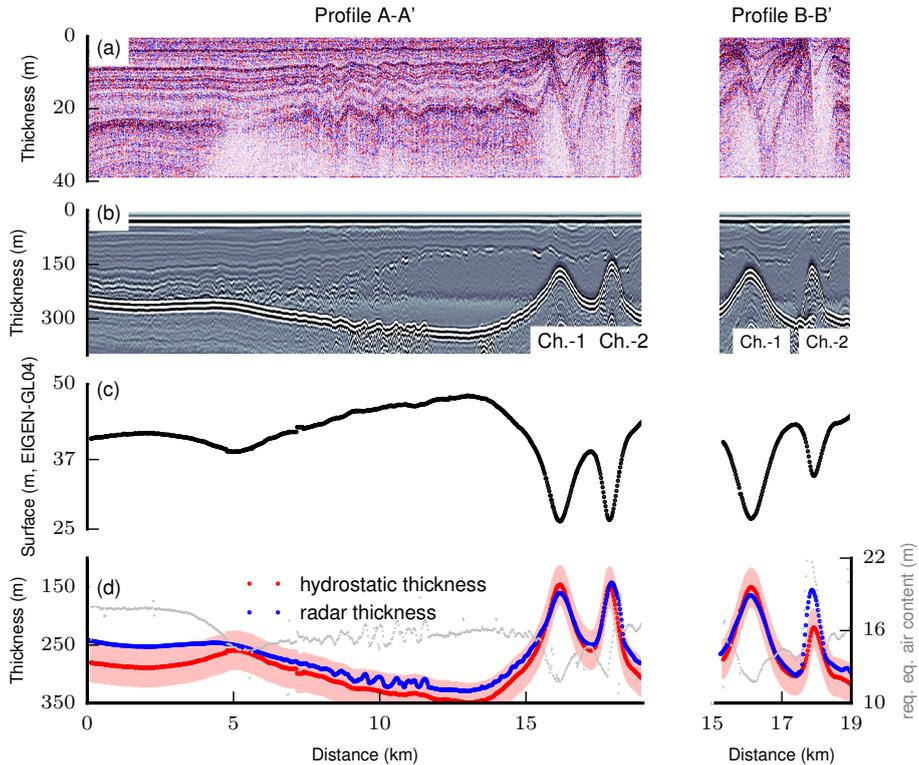


Figure 5. Observations for two channels (Ch.-1, Ch.-2) along profiles A-A' and B-B' (Fig. 1) are shown for the 400 MHz data in (a) and for the 10 MHz data in (b). Based on the surface profile (c), radar- and hydrostatic-thickness in (d) agree within the error bounds except for Ch.-2 along B-B' where the hydrostatic-thickness is anomalously larger. The grey curve shows the required changes in the equivalent air content to obtain hydrostatic equilibrium.

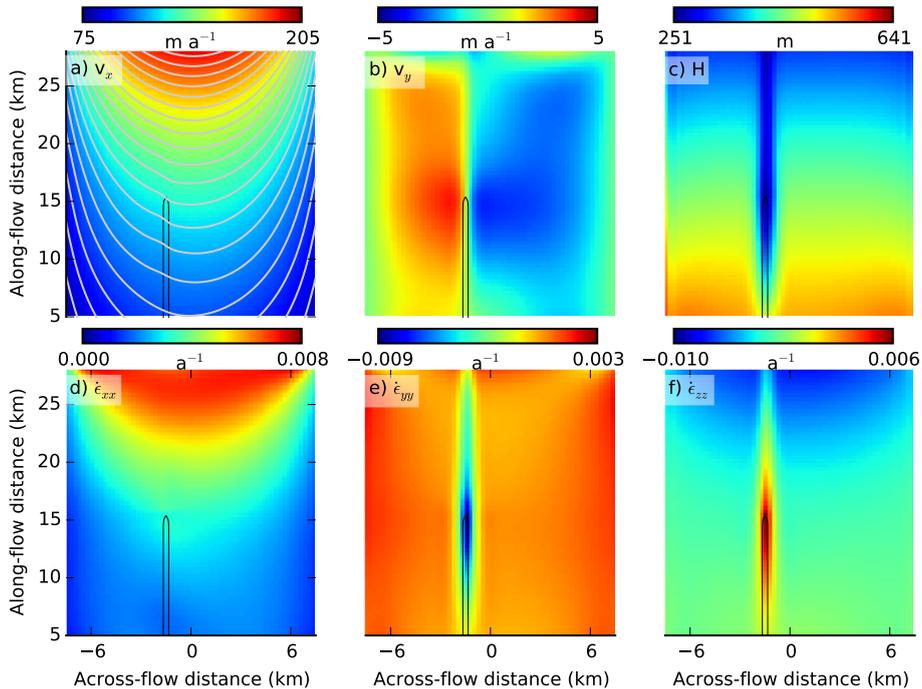


Figure 6. Steady-state results for a laterally constrained ice shelf (MS5, Table 1) showing the horizontal velocities (**a**, **b**), ice thickness (**c**), and principal strain rates (**d–f**). Gray contours mark surface speed in (**a**), black curves in (**a–f**) delineate zones of channelized basal melting. For a cross section see Fig. 7a

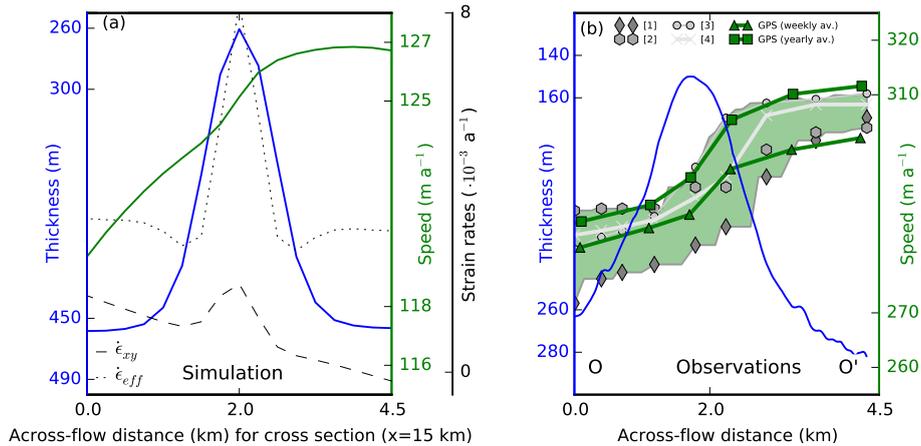


Figure 7. (a) Effective strain rate, horizontal shearing and the along-flow velocity profile for a cross section ($x = 15$ km) off the simulations shown in Figure 6 (MS5, Table 1). Prominent features are the velocity-step and the enhanced horizontal shearing inside the channel. For comparison, **(b)** displays GPS inferred ice-flow speed across a channel at RBIS (O-O', Fig. 1) confirming a step in velocity seen in satellite-derived velocities (1): Callens et al. (2014); (2): Rignot et al. (2011); (3) interferometric SAR from European Remote Sensing satellites (S. Berger, personal communication, 2014), and (4) speckle tracking using the Advanced Land Observing Satellite (S. Berger, personal communication, 2014).

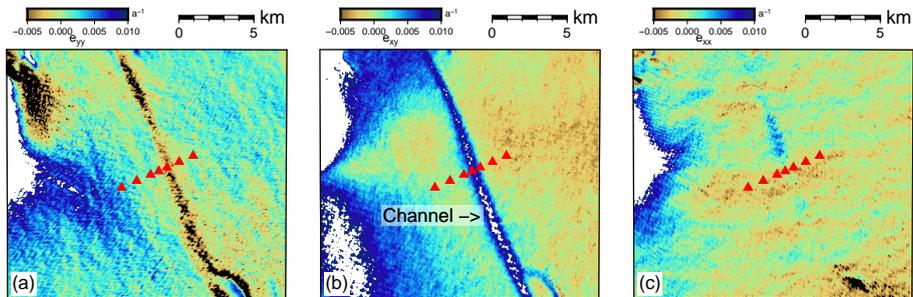


Figure 8. Strain rates inferred from ERS1/2 surface velocities on a 50 m grid dating from 1996 (S. Berger, personal communication, 2014). All values are calculated in a local coordinate systems (x along-flow, y across-flow). The ice-shelf channel is evident due to across-flow convergence in (a) and enhanced horizontal shearing in (b) whereas along-flow extension remains inconspicuous (c). The red triangles mark positions of GPS-derived flow velocities (Fig. 7b).