A process-based approach to estimate point snow instability

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Abstract: Snow instability data provide information about the mechanical state of the snow cover 1 2 and are essential for forecasting snow avalanches. So far, direct observations of instability (recent avalanches, shooting cracks or whumpf sounds) are complemented with field test such as the 3 4 rutschblock test, since no measurement method for instability exists. We propose a new approach 5 based on snow mechanical properties derived from the snow micro-penetrometer that takes into account the two essential processes during dry-snow avalanche release: failure initiation and crack 6 7 propagation. To estimate the propensity of failure initiation we define a stress-based failure 8 criterion, whereas the propensity of crack propagation is described by the critical cut length as 9 obtained with a propagation saw test. The input parameters include layer thickness, snow density, 10 effective elastic modulus, strength and specific fracture energy of the weak layer – all derived from 11 the penetration-force signal acquired with the snow micro-penetrometer. Both instability measures 12 were validated with independent field data and correlated well with results from field tests. 13 Comparisons with observed signs of instability clearly indicated that a snowpack is only prone to 14 avalanche if the two separate conditions for failure initiation and crack propagation are fulfilled. To 15 our knowledge, this is the first time that an objective method for estimating snow instability has 16 been proposed. The approach can either be used directly based on field measurements with the 17 snow micro-penetrometer, or be implemented in numerical snow cover models. With an objective measure of instability at hand, the problem of spatial variations of instability and its causes can now 18 19 be tackled.

20 **1** Introduction

21 Snow slope stability describes the mechanical state of the snow cover on an inclined slope and is 22 inversely related to the probability of avalanche release (McClung and Schaerer, 2006). For a given 23 time, depth within the snowpack, and location on a slope, snow stability can be described as the balance between snow strength and stress termed stability index (Roch, 1966). This index has been 24 25 widely used (e.g. Conway and Abrahamson, 1984; Perla et al., 1982) and refined by taking into account triggering by an additional load such as a skier (Föhn, 1987). Whereas, the skier stability 26 27 index has been shown to be related to the probability of skier triggering (Jamieson, 1995), this critical stress approach does not take into account that slope failure requires crack propagation. While 28 failure initiation may depend on stress only, the propagation of cracks requires deformation energy 29 30 (Bazant and Planas, 1998). Furthermore, on a slope, strength and stress are spatially variable; these 31 variations are fundamental to the fracture process (Schweizer et al., 2003). Around locally failed 32 areas stress concentrations will form and drive crack propagation, and eventually cause catastrophic 33 failure before the average material strength is reached. This observation has been termed knockdown effect (Fyffe and Zaiser, 2004) and partly explains why the stability index derived from 34 measurements at or near natural slab avalanches often indicated stable conditions (Perla, 1977). 35

36 Not surprisingly, the link between point observations of snow stability and snow slope stability is not 37 clear, yet (e.g. Bellaire and Schweizer, 2011). Scale issues due to different measurement scales, the 38 so-called support and knowledge gaps between the processes involved at both scales have 39 complicated bringing together point and slope scale snow instability results (Schweizer et al., 2008a). 40 The point stability scale is not even well defined. Failure initiation refers to the collective failing of 41 snow grains, or bonds between grains, on the scale of centimeters and the onset of a self-42 propagating crack in a weak snow layer called crack propagation. A common scale for both processes 43 is the snowpack scale which spans about one square meter (Schweizer and Kronholm, 2007) which in 44 the following we will refer to when we use the term point snow instability.

45 The stability index assumes a transition from stable to unstable when driving forces are no longer 46 balanced by resisting forces. However, this approach is questionable, primarily since dry-snow slab 47 avalanche release is the result of a series of fractures and snow properties are spatially variable. In a 48 fracture mechanical view, to describe a material's resistance to crack propagation, flaw size and 49 toughness need to be considered additionally to the stresses (Anderson, 1995). With the introduction of the propagation saw test (PST) (Gauthier and Jamieson, 2006; Sigrist and Schweizer, 50 51 2007) all these properties can be obtained from field data. PST experiments to study propagating 52 cracks have confirmed deformation of the slab to substantially contribute to the mechanical energy consumed by crack extension (van Herwijnen et al., 2010). Further, Gauthier and Jamieson (2008b) 53 have shown that the critical crack length together with the fracture result are related to slope 54 55 instability. In particular, cracks propagating to the end of the column after saw cut lengths less than 50 % of the column length were clear indicators of high crack propagation propensity. 56

There is presently no objective measurement of snow instability. Instead, recent avalanches, 57 58 whumpfs or shooting cracks are considered indicators of instability (Jamieson et al., 2009), but these 59 observations are rare. In their absence the remaining option to gather field data on snow instability is snow instability testing (Schweizer and Jamieson, 2010). The rutschblock (RB) is a traditional snow 60 stability test (Schweizer, 2002). The RB score was found indicative of the failure initiation propensity, 61 62 the RB release type of the crack propagation propensity (Schweizer et al., 2008b). Whereas the RB 63 release type only represents an ordinal rank, the propagation saw test (PST) gives a metric value, the 64 critical cut length, which eases quantitative analysis. A combination of the results of both tests 65 therefore seems appropriate for snow instability assessment.

66 Several studies focused on snow instability in the past, thereby either concentrating on failure 67 initiation or crack propagation. Both, Bellaire et al. (2009) and Pielmeier and Marshall (2009) derived 68 stability related parameters from measured snow micro-penetrometer resistance profiles. They 69 found that weak layer strength and average slab density predicted with good accuracy stability 70 classes estimated from RB tests.

Under the assumption of a uniform slab on a rigid substratum Heierli (2008) presented estimates of critical crack lengths obtained from recalculation of PST field experiments. Yet, averaging slab properties is a strong simplification and Schweizer (1993) pointed out the importance of slab properties for failure initiation. By means of linear elastic finite element (FE) simulations of typical snow profile types Habermann et al. (2008) found the stress at the depth of the weak layer to vary by a factor of two compared to a uniform slab. McClung (2009) suggested an alternative model to estimate the critical crack length by considering a finite fracture process zone. Several numerical approaches focusing on avalanche release (for a summary see Podolskiy et al., 2013) have been made but only a few incorporate both fracture processes. Among the latest were Gaume et al. (2013) who presented a Mohr-Coulomb failure criterion based model taking into account variations of weak layer shear strength and stress redistribution by slab elasticity. Only lately, a possible refinement of the classical stability index by accounting for strength variations and their knock-down effect including a derivation of a critical crack length was presented (Gaume et al., 2014).

Predicting snow instability requires snow properties obtained either from field measurements or 85 86 from snow cover modeling. In the field, the method of choice is the snow micro-penetrometer (SMP) (Schneebeli and Johnson, 1998) that allows deriving microstructural and micromechanical properties 87 88 from the penetration force-distance signal (Johnson and Schneebeli, 1999). Marshall and Johnson (2009) showed that values of snow density, elastic modulus and strength derived from snow micro-89 90 penetrometer signals compared well with literature data. Interpreting the oscillation of the 91 penetration force as a Poisson shot-noise process Löwe and van Herwijnen (2012) suggested a more 92 robust method to extract the microstructural parameters. Their method was employed by Proksch et 93 al. (2014) who developed a reliable parameterization of snow density applicable to a wide range of 94 snow types. Reuter et al. (2013) showed that with the snow micro-penetrometer apart from snow density and effective modulus also the specific fracture energy of the weak layer can be derived. 95 96 Comparing the results for mechanical properties obtained with snow micro-tomography (Schneebeli, 97 2004) to those with particle tracking velocimetry of propagation saw tests (van Herwijnen et al., 98 2010) they substantiated the reliability of SMP-derived parameters.

Alternatively, snow cover models provide snow structural information allowing snow instability modeling (Durand et al., 1999; Lehning et al., 2004). However, snow mechanical properties are often not simulated independently, but parameterized on density only. Schweizer et al. (2006) refined the skier's stability index implemented in the snow cover model SNOWPACK and validated it with field observations. By first identifying the potential weakness in a simulated profile and then assessing its stability Monti et al. (2014) improved this approach to classify profiles into three classes of snow instability: poor, fair and good.

106 Given the fracture mechanical context of dry-snow slab avalanche release and the lack of an 107 objective measure of instability, we propose that a description of instability should take into account 108 the two essential processes in slab avalanche release, i.e. failure initiation and crack propagation, 109 and be based on snow mechanical properties measured with the snow micro-penetrometer. Our goal 110 is to provide an observer-independent methodology applicable to field measurements of snow 111 stratigraphy. To this end we introduce a two-step calculation of a stability criterion and a critical 112 crack length based on snow mechanical properties measured with the SMP. Then, we will validate 113 the performance of our approach with field experiments of snow instability. Finally, we will show 114 how classical snow instability observations may be interpreted in terms of failure initiation and crack 115 propagation.

116 **2 Methods**

First, we present the experimental data, and then we describe how the mechanical field data acquired with the snow micro-penetrometer was analyzed, before we introduce the new approach to derive snow instability.

120 **2.1 Field data**

- Two datasets of SMP measurements were exploited to test the performance of the failure initiation (A) and the crack propagation (B) part of our approach. Dataset A was originally presented by Bellaire et al. (2009). As meta data on snow instability was only available for a share of the data, 64 SMP measurements were kept for further analysis. They were all performed in close proximity (<0.5 m) to a RB test. The main results of a RB test, which is a point observation, are score and release type (Figure 1). We used the score for validating the failure initiation propensity (Schweizer and Jamieson, 2010).
- Dataset B consists of 31 SMP measurements which have been performed in a distance less than 30 cm from the lower end of the column of propagation saw tests (PST) (Figure 2). Data were collected on seven different days. We filmed the fractures in the PSTs to precisely determine the onset of propagation by measuring the critical cut length in the pictures as a criterion of crack propagation.
- Both datasets also include manually observed snow profiles including snow grain type and size and hand hardness index for each manually identified layer. In addition, 77 out of the 95 field records in
- 135 total contain information on either type or absence of signs of instability.

136 **2.2** Snow micro-penetrometer

- With the snow micro-penetrometer (SMP) a penetration resistance profile is recorded to a depth well below the weak layer at sub-millimeter resolution. Based on the detailed manually observed snow profile layers were defined from the corresponding sections of the signal, namely slab layers, a weak layer and a basal layer. As every layer is later represented in a finite element (FE) model and the resolution of the SMP is higher than the one needed for FE simulations, we deal with layers for the sake of shorter computation times. Figure 3 shows an example of a SMP signal with manually assigned snow layer boundaries.
- 144 Applying the shot-noise model by Löwe and van Herwijnen (2012) snow micro-structural parameters, 145 namely the rupture force f, the deflection at rupture δ and the structural element size L were 146 calculated over a moving window w of 2.5 mm with 50% overlap and then averaged over the layer. 147 Snow density was calculated as described in Proksch et al. (2015):

148
$$\rho = a_1 + a_2 \log(\tilde{F}) + a_3 L \log(\tilde{F}) + a_4 L$$
 (1)

where a_i are coefficients, F is the penetration resistance and tilde denotes the median. The micromechanical effective modulus and strength were calculated according to Johnson and Schneebeli (1999):

152
$$E = \frac{f}{\delta L}$$
(2)

153 and

154
$$\sigma = \frac{f}{L^2}$$
 (3)

The specific fracture energy of the weak layer (WL) was calculated as the minimum of the penetration resistance integrated across the window size *w* within the weak layer (Reuter et al., 2013):

158
$$w_f = \min_{WL} \int_{-\frac{w}{2}}^{+\frac{w}{2}} F \, dz$$
. (4)

The penetration depth *PS* was calculated from Eq. 5 by integrating the penetration resistance *F* from the snow surface to *PS* until a threshold absorbed energy e_a = 0.036 J is reached. The value of e_a has been determined by comparison of SMP profiles with concurrently observed penetration depth (Schweizer and Reuter, 2015):

163
$$e_a = \int_0^{PS} F(z) \, dz.$$
 (5)

164 **2.3 Modeling**

165 In the following the modeling approach to calculate estimates of the failure initiation and the crack 166 propagation propensity of a certain slab-weak layer combination is described and validated. The 167 mechanical properties required as input are obtained from the SMP signal as described above.

168 2.3.1 Failure initiation

169 A strength-over-stress criterion *S* describes the propensity of the weak layer to fail in the case of an 170 additional load:

171
$$S = \frac{\sigma_{WL}}{\Delta \tau},$$
 (6)

172 with σ_{WL} being the strength of the weak layer and $\Delta \tau$ being the maximum additional shear stress at 173 the depth of the weak layer due to skier loading. The strength of the weak layer is approximated by 174 the micro-mechanical strength derived from the snow micro-penetrometer signal in the weak layer, 175 i.e. we cannot use the slope-parallel shear strength because the SMP is an indentation test 176 measuring an effective strength resulting from the mixed-mode breaking of bonds at the tip. The 177 maximum shear stress at the depth of the weak layer was modeled with the 2D linear elastic finite element (FE) model originally designed by Habermann et al. (2008) to calculate the shear stress at 178 179 the depth of the weak layer below a layered slab due to the weight of a skier. S may be interpreted 180 as an indicator of failure initiation with low (high) values being associated with high (low) likelihood 181 of initiating a failure. Note, the stability criterion S is not expected to yield typical values of the skier's 182 stability index (< 1 for 'unstable', > 1.5 for 'stable') (Jamieson and Johnston, 1998). One reason is that 183 SMP-derived strength values are about two orders of magnitude larger than values of shear strength 184 reported in literature (Marshall and Johnson, 2009). As the SMP is a small scale indentation test, the 185 difference between strength values measured with the SMP and the shear frame test (Jamieson and 186 Johnston, 2001) may be attributed to sample size and type of loading.

The 2D FE model by Habermann et al. (2008) has been adopted to include all relevant slab layers – usually about 5 to 10 layers. The geometry of the model (Figure 4a) was chosen such that the length of the modeled section of the snowpack (10 m) is at least one order of magnitude larger than the average depth of the weak layer to keep boundary effects small. The model consists of multiple layers including slab and basal layers as well as an embedded weak layer corresponding to the layering identified in the SMP signal. The layers are inclined by the slope angle α . Nodes at the lower end (on the right of Figure 4a) and at the snow soil interface were fixed in both coordinate directions.

194 The model domain was divided into two-dimensional, quadrilateral plane strain elements having eight nodes each. The mesh consisted of 75 nodes in the horizontal and 100 nodes in the vertical per 195 196 meter. The model has been implemented in ANSYS workbench to calculate the maximum shear 197 stress within the weak layer. We assumed plane strain as stresses in the direction normal to the x-y 198 plane are smaller than within and linear elastic behavior as the loading rate is high considering skier 199 loading. The skier load was modeled as a static strip load P of 780 N spread over a width a of 0.2 m. To account for skier penetration we assumed the layers within the penetration depth to be 200 compacted to a density of 300 kg m⁻³ with a corresponding elastic modulus of 16 MPa according to 201 202 Scapozza (2004); the thickness of those slab layers was adjusted so that the mass remained the 203 same. All snow layers in the FE model were assigned thickness, density and effective modulus values 204 as derived from the SMP signal. A fixed value of the Poisson's ratio was chosen (v = 0.25), as its 205 influence is small compared to our measurement uncertainties for density or elastic modulus. From the modeled linear elastic behavior the maximum shear stress within the weak layer was computed 206 207 yielding $\Delta \tau$ of Eq. 6, i.e. not considering the stress due to the weight of the slab.

208 The FE model was tested to reproduce the analytical solution of McClung and Schweizer (1999) for 209 the shear stress for a strip load on a finite area $\tau(\theta, H)$ where θ and H are two-dimensional polar 210 coordinates. To do so, the maximum shear stress at a certain depth H was determined by varying θ . 211 The FE model was run with a Poisson's ratio of v = 0.49, as the analytical solution assumes an 212 incompressible half space. The slab was not stratified, but uniform having a density of 200 kg m⁻³. 213 Hence, the solution is independent of the elastic modulus. The simulation results for different slab 214 thickness H are presented in Figure 4b together with the analytical solution. The FE model reproduced the maximum shear stress as obtained with the analytical solution very well ($R^2 = 0.94$, 215 regression slope m = 1.2) especially for slab depth larger than the width of skier load (0.2 m). 216

217 2.3.2 Crack propagation

In order to estimate the crack propagation propensity the critical crack length as measured in a PST
 experiment was calculated for a weak layer embedded by a layered slab and a basal layer.

A theoretical expression (Eq. 7) linking the fracture energy of the weak layer, the elastic modulus of the slab and the critical crack length for a self-propagating crack is obtained by replacing the mechanical energy in Griffith's criterion with the total energy of the slab weak layer system found by Heierli (2008) and was presented in detail by Schweizer et al. (2011). The formulation of the total mechanical energy of the slab-weak layer system has been proven to describe the released mechanical energy of the slab in a PST reasonably well (van Herwijnen et al., 2010).

226
$$w_f(E, r_c) = \frac{H}{2E} \left[w_0 + w_1 \frac{r_c}{H} + w_2 \left(\frac{r_c}{H} \right)^2 + w_3 \left(\frac{r_c}{H} \right)^3 + w_4 \left(\frac{r_c}{H} \right)^4 \right],$$
227 with
(7)

$$w_0 = \frac{3\eta^2}{4}\tau^2,$$

$$w_1 = \left(\pi\gamma + \frac{3\eta}{2}\right)\tau^2 + 3\eta^2\tau\sigma + \pi\gamma\sigma^2,$$

$$w_2 = \tau^2 + \frac{9\eta}{2}\tau\sigma + 3\eta^2\sigma^2,$$

$$w_3 = 3\eta\sigma^2,$$

$$w_4 = 3\sigma^2,$$

228 and $\tau = -\rho g H \sin(\alpha)$ the shear stress, $\sigma = -\rho g H \cos(\alpha)$ the normal stress, γ the elastic mismatch parameter, which is about one according to Heierli (2008), $\eta = \sqrt{4(1 + \nu)/5}$ and $\nu = 0.25$. Provided 229 the elastic modulus E, the density ρ and the thickness of the slab H, the fracture energy of the weak 230 layer $w_{\rm f}$, and the slope angle α are known, the calculation of the critical crack length $r_{\rm c}$ reduces to 231 finding the roots of Eq. 7. This fourth degree polynomial of r_c has real, ever positive coefficients. 232 233 Figure 5 illustrates the dependence of the polynomial's discriminant on slab thickness and density, which is the case if a dependence of the elastic modulus on density is assumed. As the polynomial's 234 235 discriminant does not change sign for typical values of density (and the elastic modulus), solutions consist of a pair of complex conjugated and two real roots. A physically meaningful solution of $r_{\rm c}$ is 236 obtained, if the complex roots and the one with an unexpected sign are discarded. 237

To relax the assumption of a uniform, i.e. not stratified, slab a FE model was designed to determine the equivalent bulk modulus E' of a stratified slab (Figure 6a). The model performed a stepwise calculation of the mechanical strain energy M of a stratified slab due to bending over an increasing crack of length r. In order to recover an equivalent bulk modulus E', in a next step the pairs of mechanical energy and crack length (M, r) were fitted with a theoretical expression of the total mechanical energy of the slab M (Heierli, 2008):

244
$$M(E',r) = -\frac{\pi\gamma r^2}{4E'}(\tau^2 + \sigma^2) - \frac{r^3}{6E'H}[\lambda_{\tau\tau}\tau^2 + \lambda_{\sigma\tau}\tau\sigma + \lambda_{\sigma\sigma}\sigma^2],$$
245 with
(8)

246
$$\lambda_{\tau\tau} = 1 + \frac{9}{4}\eta \left(\frac{r}{H}\right)^{-1} + \frac{9}{4}\eta^2 \left(\frac{r}{H}\right)^{-2},$$

247
$$\lambda_{\tau\sigma} = \frac{9}{2}\eta + \frac{9}{2}\eta^2 \left(\frac{r}{H}\right) ,$$

248
$$\lambda_{\sigma\sigma} = 3\eta^2 + \frac{9}{4}\eta\frac{r}{H} + \frac{9}{5}\left(\frac{r}{H}\right)^2.$$

249 The FE model consists of stratified layers, which were assigned SMP-derived values of density, effective modulus and thickness (Figure 6a). The Poisson's ratio was kept constant (v = 0.25). Due to 250 251 its geometry (only considering slab layers) and boundary conditions (rigid support along the ligament 252 length (L-r)) the FE model only considers the behavior of the slab layers as described with the formulation of the total mechanical energy of the slab-weak layer system, neglecting deformation in 253 the weak or basal layers. In our model, the deflecting beam never got in touch with the basal layer, 254 255 which, however, may be the case in field experiments, in particular with soft slabs. The FE model reproduced the theoretical formulation very well ($R^2 = 0.85$), especially for crack lengths r greater or 256 257 equal the thickness of the overlying slab H (Figure 6b). With the bulk equivalent modulus E', we find the exact solution of Eq. 7 and obtain the critical crack length $r_{\rm c}$ for the specific slab-weak layer 258 259 combination.

260 **3 Results**

In the following both model parts predicting the propensity of the snowpack to failure initiation and
 crack propagation are evaluated with the two independent data sets (A and B).

263 **3.1 Failure initiation**

264 For each of the 66 SMP profiles with corresponding RB test (dataset A) the failure initiation criterion 265 S was calculated. SMP-derived density, effective modulus, strength and layer thickness were used to drive the FE model. For the comparison with the RB score we grouped scores 1 and 2 as well as 6 and 266 7 because scores 1 and 7 were observed infrequently. The criterion S increased with increasing RB 267 score (Figure 7a). If for a given S there was no overlap of the boxes, the predictive power of S would 268 269 obviously be very good. Although this is not the case, the medians of the failure initiation criterion 270 (indicated by gray lines) per RB score increased monotonically with increasing RB scores. This 271 monotonic increase is reflected in a high Spearman rank correlation coefficient ($r_s > 0.9$). If results are grouped by scores in two stability classes of RB < 4 and RB \geq 4, a threshold previously found to 272 273 separate lower and higher stability (e.g. Schweizer and Jamieson, 2003), the criterion S discriminated 274 well between the two classes (Wilcoxon rank sum test, level of significance p = 0.01) with a 275 classification tree splitting value of S = 133.

276 **3.2 Crack propagation**

277 All 31 SMP signals from dataset B were analyzed and the critical cut length r_c was calculated from Eq. 7 with SMP-derived mechanical properties being density, effective modulus, specific fracture 278 279 energy and layer thickness. In Figure 8 the results are contrasted with the critical crack lengths 280 measured in the field in the PST experiments adjacent to the SMP measurements. On the left (Figure 8a) model results are shown for the case of a uniform slab, i.e. density and effective modulus 281 were averaged to show the effect of neglecting the stratigraphy of the slab. Modeled values 282 overestimated the critical cut length yielding a rather fair Pearson correlation coefficient of $r_P=0.58$ 283 and a coefficient of determination of $R^2 = 0.29$. Only for a few experiments modeled and observed 284 crack lengths were similar indicating that assuming a uniform slab is not a good approximation. In 285 286 fact, Figure 8b shows that the agreement between model results and observations improved if the 287 stratification of the slab was taken into account. All identified slab layers were assigned the 288 corresponding density and effective modulus obtained from SMP signal processing and input in the 289 FE model to determine the bulk effective modulus of the slab. The modeled values of critical crack length were clearly related to the measured values ($r_{\rm P}$ = 0.83) as indicated by the collapse of the 290 linear regression on the 1:1 line (Figure 8b). The regression slope was well-defined (p < 0.01) with 291 some scatter ($R^2 = 0.50$) indicating the uncertainty involved with the presented approach. The critical 292 crack length was predicted with a root mean squared error of 2 cm, a mean absolute error of 7 cm 293 294 and a mean absolute percentage error of 9%.

3.3 Validation with signs of instability

296 Model results were further compared with independent field observations of signs of instability such 297 as whumpfs, shooting cracks and recent avalanches. Both datasets (A and B) included records of such 298 field observations which we grouped in three categories: whumpfs, shooting cracks with or without 299 whumpfs ('cracks') or 'all signs' (whumpfs, cracks and recent avalanches), i.e. fresh avalanches were only observed simultaneously with whumpfs and cracks (Figure 9). To jointly relate our modeled 300 estimates of instability to the observations of instability we contrasted the propensity to crack 301 302 propagation, i.e. modeled critical crack length, and failure initiation, i.e. initiation criterion S, in 303 Figure 9. Signs of instability were primarily present in the lower left of Figure 9, i.e. for low values of 304 the failure initiation criterion and the critical crack length. Vice versa no signs of instability were

305 reported if both criteria yielded high values (upper right). This finding suggests that both criteria, the 306 one for failure initiation and the one for crack propagation, are linked to snow instability. A 307 classification tree with the two independent variables S and r_c yielded splits of S = 234 and r_c = 0.41 m which separate between the cases with and without concurrently observed signs of instability (Figure 308 309 9). These thresholds divide the plot into four quadrants. In the lower left quadrant all 35 cases with 310 signs of instability as well as ten cases without signs of instability were found. Our split value (S=234) 311 for the initiation criterion S is very similar to the one found by Schweizer and Reuter (2015) who 312 reported a value of 212. In regard to the modeled critical crack length, Gauthier and Jamieson (2008a) suggested a value of <50% of the column length which in their study corresponded to 50 cm. 313 314 Assuming crack propagation to be likely (two lower quadrants) or failure initiation to be easy (two left quadrants) does not distinguish sharply between signs of instability present or absent. However, 315 316 if both criteria had low values unstable snow conditions were observed (lower left quadrant).

317 **4 Discussion**

In our present understanding avalanche release is seen as a sequence of fractures. To capture the two most important steps preceding the detachment of a snow slab we addressed the stress at the depth of a potential weakness with the failure initiation criterion *S* and the critical crack size for selfpropagation with the critical crack length r_c . We presented a model approach to derive both quantities from snow micro-penetrometer signals which is a fast method to acquire information on mechanical properties in the field.

324 Assessing the performance of the model approach with two different field tests (RB and PST) yielded 325 plausible results. However, the main source of uncertainty is related to the mechanical properties 326 needed as input for the model. Snow density, effective modulus and specific fracture energy were all 327 determined from SMP measurements. Uncertainties related to the determination of these 328 mechanical properties have recently been addressed by Proksch et al. (2015) and Reuter et al. (2013) 329 and lie within 10-20% for density and fracture energy. Other SMP error sources are known and so 330 erroneous signals were identified and discarded. Some errors were user-related such as mechanical disturbances. Other unavoidable errors such as signal drift due to strong temperature changes in the 331 332 snowpack or stick slip of the rod at high snow densities were rare.

The SMP-derived failure initiation criterion S performed well based on the evaluation with 333 rutschblock tests, yielding a better correlation than the one lately observed by Schweizer and Reuter 334 335 (2014) using the compression test. They concluded that the dimensions of the compression test and 336 the type of loading are not ideal for modeling purposes. While the RB test includes six different 337 loading steps, the load is only increased twice in a compression test, but numerous taps are 338 performed within the same loading range. The loading of the RB and consequently the stress exerted on the weak layer increases monotonically with the score (score four and five have the same load). 339 This is reflected in the fair discrimination of RB scores four and five with the failure initiation 340 criterion S. Furthermore, RB loading steps are ordinal numbers, i.e. they can be ranked, but they do 341 342 not follow a known relation with stability. Hence, the stress in the weak layer increases stepwise in the experiment, whereas the modeled stability is continuous. The boxplots in Figure 7 group 343 344 modeled values of failure initiation (S) with rutschblock classes. The monotonic increase of the 345 medians suggests that the criterion S reflects the propensity of failure initiation in a weak layer below

a layered slab. Correlations of the rutschblock release type were neither significant with the initiation criterion S ($r_s = 0.11$, p = 0.39), nor with the modeled critical cut length ($r_s = 0.04$, p = 0.76).

348 The critical cut length was modeled with an accuracy of a few centimeters (RMSE of 2 cm). It was 349 shown that the slab layering played an important role in the process of crack propagation. Only with 350 the introduction of the bulk effective modulus imitating the bending behavior of a layered slab 351 measured critical cut lengths were reproduced with good accuracy (Figure 8). Until now research on 352 snow instability had mainly focused on weak layer or average slab properties (Bellaire et al., 2009; Pielmeier and Marshall, 2009). Alternatively, the critical value of the crack length could have been 353 354 determined by stepwise increasing the crack length in an FE model until the critical energy release 355 rate reaches the specific fracture energy of the weak layer. This approach, comparable to that of 356 Mahajan and Joshi (2008), however, was not followed due to its high computational expenses, as 357 repeated meshing for every single iteration step would be costly.

The introduced FE models assumed linear elastic behavior and were confined to two dimensions. These assumptions are in contrast with our knowledge that snow is a porous medium consisting of a non-isotropic ice/air matrix, exhibiting plastic, elastic and viscous behavior at the macro scale. However, as loading rates in RB tests and PSTs are high, linear elastic assumptions are justified – for the rutschblock test at least at a certain depth below the snow surface. Two dimensional modeling seems sufficient, as three dimensional modeling is not advantageous due to the lack of experimental orthotropic material properties at this point of time.

365 **5 Conclusions**

We have developed a novel approach to determine quantitative estimates of both, the failure initiation and crack propagation propensity of the snowpack based on mechanical properties derived from objective snow micro-penetrometer measurements. Based on the current understanding of dry-snow slab avalanche release it includes the mechanical properties of all relevant layers embedding the weak layer to make predictions on the propensity of initiating a failure and spreading the crack in a weak layer within the snowpack. The presented approach is process-based, observerindependent and relies on measurements of mechanical properties.

373 The performance of the two novel measures of instability has been assessed in comparisons with two 374 different datasets of field tests (rutschblock and propagation saw test). Both measures of instability, the stress criterion S as well as the critical crack length r_c were well correlated with the results of field 375 376 tests. In addition, the importance of slab layering especially with respect to crack propagation has 377 been shown. The comparison of our modeled estimates of snow instability with field observations of 378 signs of instability clearly indicated that a snowpack is unstable only in case of high failure initiation 379 as well as high crack propagation propensity. Whereas we anticipated this finding, i.e. that both 380 conditions have to be fulfilled, we are not aware, to the best of our knowledge, that it has been demonstrated before. 381

Recent field studies have frequently focused on identifying spatial variations of snow instability and its drivers which requires an objective measure of instability – which was so far lacking. With the observer-independent method we presented, taking into account both failure initiation and crack propagation processes, it will become possible to resolve causes of spatial snow instability variations. With respect to operational application in the context of avalanche forecasting, our approach based on field measurements could be employed, provided a robust and reliable snow micro-penetrometer is at hand which in addition allows remote data transfer and automatic processing, or be implemented in numerical snow cover models.

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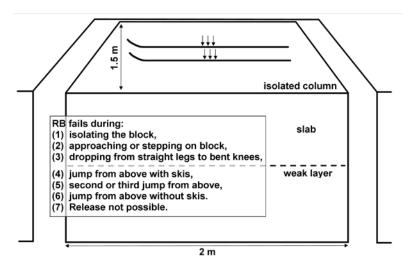
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Figure Captions and Figures



508 Figure 1: Sketch presenting the rutschblock (RB) test as it is seen looking upslope: After isolating a 509 block of snow 2 m wide and 1.5 m upslope it is loaded progressively by a skier. The loading steps and 510 scores are described in the inset. The release type was not considered here.

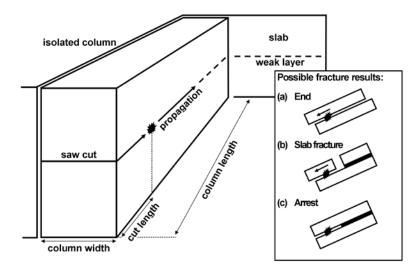
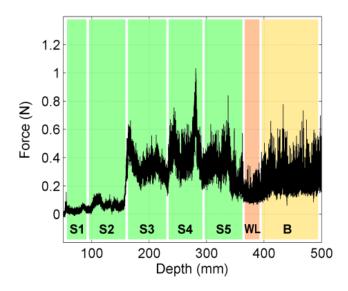




Figure 2: Sketch presenting the propagation saw test (PST) as it is seen looking upslope: After isolating a column 30 cm wide and at least 1.2 m upslope, the weak layer is cut with a snow saw from its lower end continuing upslope. Possible fracture results are described in the inset. Here, we only

515 consider tests where the fracture went to the end of the column (End).



516Figure 3: Penetration resistance (black) as measured with the SMP vs. snow depth. Slab layers (S1 to517S5) shaded in light green, weak layer (W) shaded in light red, basal layer (B) shaded in light orange.

518 50 mm of air signal cut off.

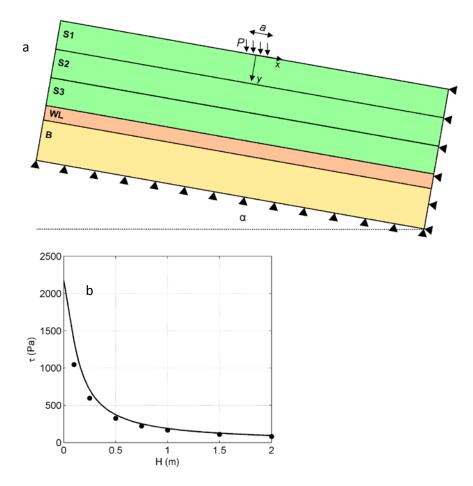
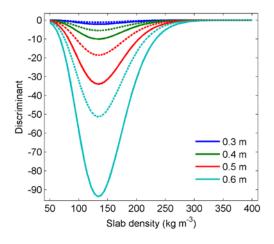


Figure 4: (a) FE model to simulate the maximum shear stress at the depth of the weak layer consisting of three slab layers (green), the weak layer (red) and a basal layer below (orange) inclined by the slope angle α . Triangles indicate fixed nodes. The applied strip load *P* is illustrated by black arrows pointing towards the snow surface. The axes of the coordinate system are indicated by arrows. (b) Maximum shear stress from FE simulations (dots) and from the analytical solution (line)

524 for a uniform slab with density 200 kg m⁻³ and a slope angle of 38° versus slab thickness *H*.



525 Figure 5: The polynomial's (Eq. 5) discriminant versus slab density for typical values of slab thickness 526 (colors); different line styles indicate flat terrain (dashed) and a slope inclined by $\alpha = 38^{\circ}$ (solid lines).

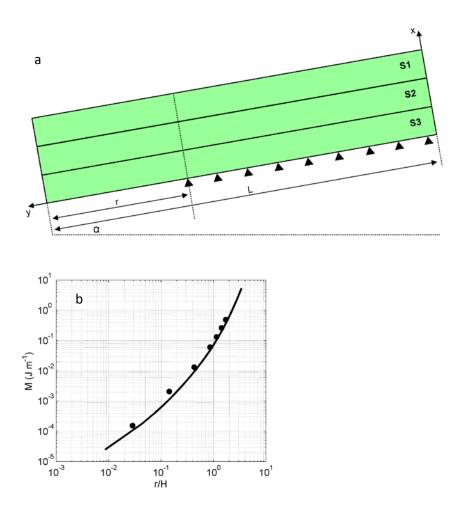


Figure 6: (a) The FE model to calculate the equivalent effective modulus contains as many slab layers as necessary to reflect the stratigraphy found in the SMP signal. Triangles indicate fixed nodes. The beam of length *L* is overhanging a crack of length *r* and is inclined by the slope angle α . (b) Mechanical energy *M* over the ratio of crack length and slab thickness (*r/H*) modeled with FE (dots) and calculated from the analytical solution (line) for a homogeneous slab with density 200 kg m⁻³ and a slope angle of 30°.

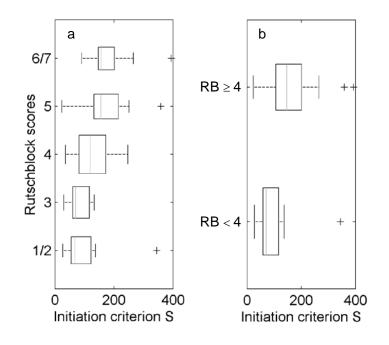


Figure 7: Modeled failure initiation criterion *S* (a) vs. RB score and (b) vs. RB stability classes: RB < 4 (N = 38) and RB \ge 4 (N = 26). Boxes span the interquartile range from 1st to 3rd quartile with a horizontal line showing the median (grey line). Widths of the boxes correspond to the number of cases. Whiskers extend to the most extreme data points not considered outliers (crosses) within 1.5 times the interquartile range above the 3rd and below the 1st quartile.

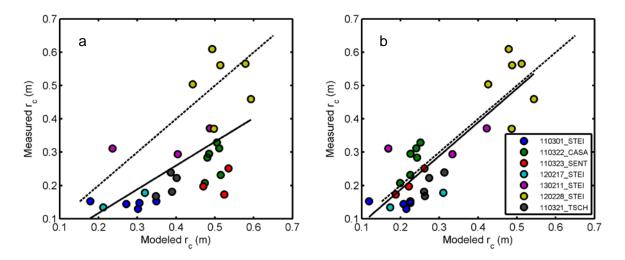


Figure 8: Critical crack lengths r_c predicted from Eq. 7 are contrasted with critical crack lengths measured in the field (N = 31). Experiments grouped by date and location with colors. Solid line shows linear regression, dashed line indicates the 1:1 line. (a) Slab stratigraphy neglected (average density, average effective modulus). (b) Density and effective modulus of each snow layer taken into account by FE simulation.

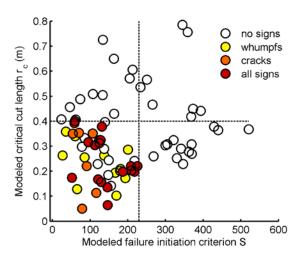


Figure 9: Type and presence of signs of instability against failure initiation criterion *S* and critical crack length r_c , both modeled, for datasets A and B, if reported (N = 77). Colors indicate type of observed signs of instability: whumpfs, shooting cracks with or without whumpfs (cracks) or all signs (whumpfs, cracks and recent avalanches observed). Open circles indicate that no signs of instability were reported explicitly (no signs). Dashed lines represent split values dividing the plot into four quadrants as found with a classification tree.