

Detailed response to the editor on revised manuscript tc-2014-134

“Interaction of marine ice-sheet instabilities in two drainage basins: simple scaling of geometry and transition time”

by J. Feldmann and A. Levermann

Dear editor,

We would like to thank you for the careful handling of the review process of our manuscript and are glad to hear that the manuscript might be suitable for publication after minor revisions.

As proposed by the editor and the reviewers we give a more thorough explanation of how the basal melting at the grounding line is applied (Sec. 2) to avoid possible misunderstandings and also included a discussion of the basal-melt perturbation (Sec. 4). Please note that we changed the beginning of the abstract as we think that the new version gives a more appropriate introduction to our investigation. Inspired by reviewer#1 we also added a new Sec. 3.1 in which we discuss the different scenarios of basin interaction based on a conceptual flux-balance analysis. We are confident that we have addressed all the other reviewer comments and hope that the manuscript is now ready for publication.

Please find below the *reviewers' comments in italics* and [our response in blue](#). We have further attached a revised manuscript that highlights the changes in the submission, as well as one “clean” version with applied changes.

Best wishes,

J. Feldmann and A. Levermann

Detailed response to reviewer #1:

[We would like to thank reviewer #1 specifically for the very detailed and constructive comments.](#)

Submitted on 05 Jan 2015

Referee #1: Stephen Cornford, s.l.cornford@bristol.ac.uk

For final publication, the manuscript should be accepted subject to **minor revisions**

Suggestions for revision or reasons for rejection (will be published if the paper is accepted for final publication)

Minor revisions suggested in attachment.

1 General Comments

Overall, I am happy with the response to the earlier reviews and the revised manuscript. I originally suggested the paper be extended, and speculated on a few routes the authors might follow: they considered each of those and either incorporated new material or made a reasonable response. I have a few comments.

2 Specific Comments

2.1 Response to ice divide migration

(see pdf as there are equations included)

We are thankful for the reviewer's very inspiring comment. We added a new section (3.1) to discuss and distinguish between the three scenarios S, U and C in a conceptual way, i.e. theoretically. In order to do so we analyze the steady-state flux balance of an ice sheet for the overdeepened, symmetric bed shape we use in our simulations. The corresponding new Fig. 8 compares ice discharge across the grounding line (according to Schoof) to mass gain through surface accumulation. We show the possible scenarios of basin interaction that depend on the strength of the ice-divide shift that is assumed to take place in response to a destabilization of basin r. We refer to the flux-balance analysis in the abstract (p.1 ll.17-18) as well as in the discussion section (p.15 ll.17-19). A comparison of our modeled steady-state ice-sheet profile and ice flux to Schoof's solution is additionally provided in newly included Appendix B and corresponding Fig. 13.

2.2 Melt-rate interpolation

Both reviewers noted that the response of basin r to sub-shelf melting was unexpected, given the 1HD nature of the problem. The authors make it clear that the response is essentially down to their use of a melt-rate interpolation scheme that places some melting (in effect) on grounded ice. They refer to this scheme as a caricature (a choice of word that I enjoyed), implicitly acknowledging the fact that such schemes are bound to produce some erroneous retreat, and in some cases (such as in the r-basin here) error-dominated retreat (at least to begin with – at some point on the retrograde slope the MISI retreat might be much larger, but all of the retreat on the prograde slope must be due to the sub-grid scheme rather than ice dynamics). They are, I think, correct to note that their use of this scheme does not make their results invalid with regard to the central subject of the paper, the interaction between the r and basins (the basin has no melt applied) .

I do think the paper needs some more specific statements.

1. The revised manuscript describes the melt interpolation as a highly localized perturbation. I would say that the interpolation qualitatively resembles the response to loss of buttressing by

increasing the flux out of the last grounded cell only.

2. A clear statement noting that this sort of scheme produces an extra flux proportional to $m\Delta x$ compared to not using such a scheme, where m is the melt rate and Δx is the mesh spacing, which is not likely to be correct for any given resolution and may dominate the results by inducing sustained excess grounding line retreat, especially at low spatial resolution. Schemes like this must be used with care – and in most cases, should not be used, unless the resolution is so fine that ice dynamics clearly dominates. I think this is important because so many groups have begun to use PISM, and the sub-grid melt might seem like a plausible technique to someone less familiar with grounding line dynamics.

We highly appreciate the reviewer's advice here. We completely agree that this kind of perturbation can have a large effect on ice dynamics and has to be treated with care. We appreciate the reviewer's statement that the mechanism of basin interaction, which is a central result of our study, is not affected by the melting scheme. We address both of the reviewer's points in the discussion section (p.15 l.23 – p.16 l.5)

3 Technical Corrections in the new material

P6, line 4 'The model is set up flow line and no friction is applied at the lateral ice margins' could be 'The model is set up in a flow line configuration with no lateral drag.'

Done.

P6, line 7 'Hence there is no variation in cross-ow direction (y direction)' → 'Hence there is no variation in the cross-ow (y) direction'

Done.

P8, '...investigated with a perturbation analysis' etc: should this really be described as a perturbation analysis? You could just say 'The stability of the ice in the basin is determined by the distance that the ice divide moves towards basin in response to thinning in basin r.'

Done.

P19, line 7 'grouding line' → 'grounding line'

Done.

P14, line 11 '... depicts ...' → '... imparts ...' ?

Done.

P16, line 6 'Figures 11a and b exemplary show that a destabilization in basin l is induced independent of the applied perturbation in basin r.' → 'Figures 11a and b show that similar

destabilization take place in basin in response to either the atmospheric or oceanic perturbation in basin r'

Done.

Detailed response to Anonymous Referee #3:

Submitted on 30 Jan 2015

Anonymous Referee #3

For final publication, the manuscript should be accepted subject to **technical corrections**

Suggestions for revision or reasons for rejection (will be published if the paper is accepted for final publication)

I have read the two initial reviews, the authors reply as well as the new version of the manuscript. I think the idea beyond this study is interesting and the results obtained deserve to be published. The new version has been improved after this first step review. Nevertheless, I have still some comments and suggestions to improve the manuscript, as well as some typos.

General Comments:

- despite the fact that it is shown that the way the initial perturbation is applied doesn't play a role in the obtained results, it would be nice to explain the basal melting perturbation more deeply. I am not able to understand what is really done by just reading the sentence page 4 (lines 25-27). The accumulation perturbation is even better explained in the appendix. You should make clearer what is really done to force the GL to retreat on RHS basin.

We thank the reviewer for the advice. We now give a more detailed explanation of how melting at the grounding line is applied in our perturbation experiments in Sec. 2 (p.4 l.27 – p.5 l.6).

- The notation used (x_c , x_s , x_d , bc) should be added in Figure 3.

Done.

Also, from my understanding, only bc is varied. Are the elevation in x_s and x_d keep constant should be specified and values given somewhere.

Done.

- Because of the time involved (few ka) for the perturbation to propagate, I am wondering what would be the influence of accounting for isostasy? The bedrock topography will not stay symmetric

during the perturbation phase. This missing process might change the conclusion of the paper. At least, this should be mentioned and discussed a bit in the conclusion section.

We are grateful for the reviewer's idea to consider glacial isostasy. We added a paragraph, discussing the effect of possible bed rebound (p.16 ll.14-21).

- I don't think the comparison with the Vialov profile is pertinent. By imposing from the model the dome elevation and length of the ice-sheet, this is no surprise that the Vialov shapes are in relatively good agreement. I guess that a parabola going through these two points with horizontal asymptote at the dome would do a reasonable job too? I would suggest to suppress this section.

We understand the reviewer's view point very well. We feel however that the Vialov profile is an analytically derivable profile that represents the SIA solution and therefore represents an interesting reference point. The prescription of the vertical and horizontal scale fixes a lot of the profile, but the remaining profile shape between the dome and the grounding line is determined by the exponent of the profile and is non-trivial. To provide a reference profile for the SIA case seems to be of interests for the reader. Since our statements are not explicitly wrong, we would very much appreciate if the profile could stay in the manuscript.

Minor remarks:

(It seems that the line numbering used by the reviewer below has an offset of +6 pages.)

- page 12, line 7: it should be mentioned that it is equivalent to a plane strain formulation for a 'true' flow line model.

Done.

- page 12, line 9: isn't it $x=800\text{km}$ for the front position?

The boundary condition is indeed applied at $x_c=\pm 700\text{ km}$.

- page 12, line 11: the Δy spacial resolution is of no interest (should not have any influence on the solution).

Done.

- page 15, line 16: Isn't it Q_g instead of Q_q ?

Done.

- page 16, line 3: cannot be compensated the decrease -> cannot be compensated by the decrease (?)

Done.

- page 17, line 7: why the Vialov profiles are not shown in panel a also? (In fact i would suggest not

to show the Vialov profile, see above)

We leave out the Vialov profile as well as the scaling in panel a for the sake of a clear labeling. Both Vialov and scaling profiles for this particular central bed elevation are shown in Fig. 12a.

- page 17, line 7: from our simulation -> from our steady simulation

Done.

- Equation 7: give value for Δt_{\min} , ΔH_{\min} . What is C? A constant? Give its value?

We indeed missed to mention in the text that C is a constant which we now make clear (p.13 l.13).

We now also give the values for the fit in Fig. 9 in the figure caption.

- page 20, line 15: it should be made reference to the Appendix where the accumulation perturbation is explained in detail.

Done.

- page 22, line 7: profiles differ at the end -> profiles differ only at the end

Done.

- Figure 1: add the other notation x_c , ..., b_c

Done (Figure 3).

- Figure 4, legend: The bottom panel is the c panel

Done.

- Last figure is 11 not 1.

Done.

Interaction of marine ice-sheet instabilities in two drainage basins: simple scaling of geometry and transition time

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Abstract

Recent regional simulations and observations suggest a destabilization of The initiation of a marine ice-sheet instability (MISI) is generally discussed from the ocean side of the Amundsen-Sea sector of West Antarctica. Whether the initiated ice drainage will be limited to Pine Island and Thwaites basin or extend to the Filchner-Ronne basin depends on the possibility of an interaction of the different drainage basins ice sheet. It has been shown that the reduction in ice-shelf buttressing and softening of the coastal ice can destabilize a marine ice sheet if the bedrock is sloping upward towards the ocean. Using a conceptual flow-line geometry, we investigate the possibility of whether a ~~marine ice-sheet instability (MISI)~~ MISI can be triggered from the direction of the ice divide as opposed to coastal forcing and investigate explore the interaction between connected basins. We find that the initiation of a MISI in one basin can induce a destabilization in the other. The underlying mechanism of basin interaction is based on dynamic thinning and a consecutive motion of the ice divide which induces a thinning in the adjacent basin and a successive initiation of the instability. Our simplified and symmetric topographic set-up allows to scale both the geometry and the transition time between both instabilities. We find that the ice profile follows a universal shape that is scaled with the horizontal extent of the ice sheet and that the same exponent of $1/2$ applies for the scaling relation between central surface elevation and horizontal extent as in the pure Shallow Ice Approximation (Vialov profile). Altering the central bed elevation we find that the extent of ~~grounding-line~~ grounding-line retreat in one basin determines the degree of interaction with the other. Different scenarios of basin interaction are discussed based on our modeling results as well as on a conceptual flux-balance analysis. We conclude that for the three-dimensional case the possibility of drainage basin interaction on time scales in the order of 1 kyr or larger cannot be excluded and hence needs further investigation.

1 Introduction

Recent studies that investigate the future evolution of the West Antarctic Ice Sheet (WAIS) by basin-scale numerical modeling suggest that a destabilization of parts of it is under way (Katz and Worster, 2010; Favier et al., 2014; Joughin et al., 2014). The bed geometry of the WAIS (Figs. 1 and 2) makes it susceptible to a marine ice-sheet instability (MISI), proposed several decades ago (~~Mercer, 1978; ?, Joughin and Alley, 2011~~) (Mercer, 1978; Schoof, 2007a; Joughin and Alley, 20 Pine Island Glacier (PIG) and Thwaites Glacier (TG) are two major tributaries of the WAIS, are most likely out-of-balance and exhibit the highest single-glacier mass loss in Antarctica (Rignot et al., 2008; Medley et al., 2014). Among other smaller glaciers in the Amundsen Sea sector they show a ~~grounding line~~ grounding line retreat on retrograde (inland down-sloping) bed sections (Fig. 2) that reach deep into the interior of their basins (Vaughan et al., 2006; Tinto and Bell, 2011). The lack of substantial bed obstacles along these sections indicates that observed rapid changes, including ~~grounding line~~ grounding line retreat, ice acceleration and thinning (Shepherd et al., 2002; Pritchard et al., 2012; Park et al., 2013; Mouginot et al., 2014), and thus destabilization are likely to continue (Rignot and Mouginot, 2014). The changes are attributed to increased sub-ice-shelf melting that is driven by relatively warm circumpolar deep water reaching towards the glaciers' grounding lines (Walker et al., 2007; Jacobs et al., 2011; Rignot et al., 2013). PIG and TG basins contain enough ice to raise global sea level by ~ 24 cm and ~ 59 cm, respectively (Holt et al., 2006; Vaughan et al., 2006).

It can be presumed that a full drainage of one of these basins or of both basins would imply an even larger sea-level contribution due to additional ice supply from other connected basins (Stuiver et al., 1981; Holt et al., 2006). Multiple studies show that due to ice stream thinning, marginal (grounding line) retreat or changing accumulation patterns ice divides can indeed shift (Anandakrishnan et al., 1994; Cuffey and Clow, 1997; Nereson et al., 1998). Prominent examples are Siple Dome and two other inter-ice-stream ridges in West Antarctica whose ice divides have migrated in response to changed dynamics in their

lateral ice streams (Nereson and Raymond, 2001). Numerical modeling of the response of the Antarctic Ice Sheet to extensive sub-ice-shelf melting (SeaRISE project, Bindshadler et al., 2013) showed the possibility of a collapse of the WAIS that implies the migration of ice divides and the eventual merging of several drainage basins in West Antarctica. However, in the SeaRISE experiments the coastal forcing was applied to the whole Antarctic Ice Sheet and hence all drainage basins were perturbed simultaneously. With this approach no statements can be made on the influence of a perturbed basin on a connected unperturbed basin.

Here we investigate how the ice dynamics in a drainage basin can be affected by changes originating from the direction of the ice divide as opposed to coastal forcing and analyze the interaction between connected basins. Using a flow-line setup, we show that the initiation of a MISI in one basin leads to ~~grounding-line~~ grounding-line retreat in a connected basin and can trigger its destabilization. First of all we describe our symmetric model setup and the set of experiments, designed to perturb a steady-state ice sheet. We then analyze the evolution of the relaxing ice sheet in response to the perturbation. Different scenarios of basin interaction are examined based on our results from modeling as well as conceptually. A simple scaling of the steady-state ice surface elevation as well as the transition time between the instabilities in both basins is proposed. Finally, we discuss the results and conclude.

2 Model and experiments

The model we use in our experiments is the Parallel Ice Sheet Model (PISM). It is an open-source, thermo-mechanically coupled, three-dimensional model (Bueler and Brown, 2009, <http://www.pism-docs.org>). PISM uses a superposition of the shallow ice and the shallow shelf approximations (SIA and SSA) of the stress balance to calculate ice velocities (Winkelmann et al., 2011). Since the SSA velocities are used as basal velocities for the grounded parts of the ice, a smooth transition of the velocity field between the grounded and floating regimes is ensured (Martin et al., 2011). The model used in this study is based

on PISM version stable0.5. The combination of (1) a linear interpolation of the grounding line with locally interpolated basal friction and (2) a modified driving-stress computation across the grounding line led to a significantly improved performance of PISM in MISMP3d (shown in Feldmann et al., 2014, compare to Pattyn et al., 2013).

For the perturbation experiments in the present study sub-ice-shelf melt rates are parameterized following ~~Beckmann and Goosse (2003)~~ (Beckmann and Goosse, 2003; Martin et al., 2006). According to the parameterization the melt rates are proportional to the temperature difference between a prescribed value for the water in the sub-shelf cavity and the local pressure melting point of the ice. ~~Ocean melting is also applied at~~ The basal melt rates are not only calculated for the floating ice shelf but also for grounded grid cells with bed below sea level adjacent to ~~the ocean or a floating grid cell through a buoyancy-dependent basal-melt interpolation (coastal grid cells)~~. Using a linear interpolation of the grounding-line position on a sub-grid (Gladstone et al., 2010) that yields an effective floating fraction for each grid cell (between 0 and 1, illustrated in Feldmann et al., 2014, Fig. 1) we scale the melt rate for each grid cell in the vicinity of the grounding line. Hence (reduced) ocean melting is also applied to coastal grid cells that are partially floating according to the sub-grid scheme. This caricature of a grounding zone allows us to force a ~~grounding-line~~ grounding-line retreat in our flow-line setup, i.e. in the absence of buttressing, which would not be possible by melting solely under the ice shelf (Pattyn et al., 2006; Gagliardini et al., 2010; Gudmundsson, 2013). This kind of perturbation depicts a minimally invasive and very localized forcing. Other forcings, such as the modification of ice softness or basal friction, can also trigger grounding-line migration (~~?Pattyn et al., 2013~~) (Schoof, 2007a; Pattyn et al., 2013) but affect the ice sheet on a larger scale. Since the specific way in which the ~~grounding-line~~ grounding-line retreat is triggered is not central to the mechanism described here, we chose the trigger that is changing least of the ice sheet and especially does not interfere with the rheology of the ice or the bedrock. The results obtained here are independent of the selected trigger mechanism (see Appendix A).

The computational domain of our setup stretches from -800 to 800 km in x direction (flow direction). The bed geometry (Fig. 3, black line) is symmetric around $x_c = 0$ and is similar

to a bed geometry introduced by [Schoof \(2007a\)](#), which was later used in MISIP (Pattyn et al., 2012, hysteresis experiment EXP 3) and also used (modified) in other studies that conceptually investigate the stability of marine ice sheets (Goldberg et al., 2009; Gudmundsson et al., 2012). We use a piecewise cubic spline interpolation between the nodes x_c (location of the maximum of a central ridge), $\pm x_d$ (location of the minimum of a bed depression) and $\pm x_s$ (location of a coastal sill). At each of these nodes a value for the bed elevation as well as the first derivative (equal to zero, since the nodes are locations of local extrema) are prescribed. On the ocean-ward side of the sill another node with a non-zero first derivative ensures the steep sloping of the bed. The bed section between $\pm x_d$ and $\pm x_s$ is down-sloping inland and hence referred to as retrograde section in the following. Given the symmetry, the domain can be divided into two drainage basins, mirroring each other (“basin l” for the LHS of the domain, i.e. for $x < x_c$, and “basin r” for the RHS of the domain, i.e. for $x > x_c$). Retrograde bed sections can be found in several connected drainage basins of the WAIS. To illustrate this, Fig. 2 shows cross-sections through the WAIS and its underlying bed topography along three transects, each of which connects two major drainage basins. The transects do not represent flow lines of the ice but exemplify the overdeepened geometry of parts of the basins. The average slope of PIG’s retrograde bed section along transect [a-a](#) (that indeed goes through the main trough of the ice stream, Figs. 1 and 2a) is comparable to the maximum slope of the retrograde section in our setup (both are in the order of -10^{-3}).

The model is set up in [flow line and no friction is applied at the lateral ice margins](#) [a flow line configuration with no lateral drag](#). However, to maintain the function of the model (i.e. the finite difference scheme), which is designed for two horizontal dimensions, we use three grid cells in y direction and the lateral boundaries are periodic. Hence there is no variation in [the cross-flow direction \(\$y\$ -direction\)-\) direction and the configuration is equivalent to the plane strain formulation of a flow line model](#). A boundary condition in x direction is prescribed such that the calving front may not exceed $x = \pm 700$ km. Relevant parameter values as well as the non-linear friction law are the same as in the MISIP3d experiments (Pattyn et al., 2013). The experiments are carried out on a fixed regular grid with a spatial resolution

of $\Delta x = 1$ km and $\Delta y = 1.5$. Our modeled ice-sheet profile in steady-state is compared to Schoof's semi-analytic solution (Schoof, 2007a) in Appendix B.

Each of the simulations presented in this study is a set of three subsequent experiments, namely spinup, perturbation and relaxation. The spinup starts from an initial block of ice with a uniform upper surface elevation of 2000 m. A symmetric ice-sheet-shelf system evolves with grounding lines located on the ocean-ward sides of the sill (Fig. 3). The system is run into equilibrium (the grounding-line grounding-line positions are constant and the rate of relative volume change is smaller than 10^{-7} after 30 kyr). The steady-state ice sheet is then perturbed locally by applying melting beneath the ice shelf only in the RHS basin r ($x > 0$). The parameters of the melt-rate equation are chosen such that the grounding line in basin r is forced to retreat beyond the tip of the sill, being located on the retrograde section of the bed at the end of this 1.3 kyr perturbation phase. In the third and last experiment, the sub-shelf melt rates are set to 0 again (i.e. the same boundary conditions as in the spinup experiment apply) and the model is run for several 10 kyr, allowing the previously perturbed system to relax into a new steady-state. This relaxation phase is analyzed in the results section.

This sequence of experiments is carried out for a range of different elevations of the central bed ridge, i.e. the bed section between the minima of the depressions, $-x_d < x < x_d$ $x_d \leq x \leq x_d$ (compare Fig. 3a to c). To this end, the piece-wise cubic spline interpolation that defines the bed geometry between x_c and $\pm x_d$ is modified by prescribing a different value of b_c at node x_c for each individual setup. The interpolation remains unchanged otherwise, thus the bed sections for $x \leq -x_d$ and $x \geq x_d$ $x \leq x_d$ and $x \geq x_d$, respectively, are smoothly connected to the modified central bed section and are identical throughout all simulations. In the following text, individual simulations are abbreviated with "BC" followed by the value of the prescribed central bed elevation, e.g. BC+200 names the simulation using a value of $b_c = +200$ m.

3 Results

Depending on the bed geometry, we investigate three qualitatively different scenarios of the time evolution of the ice sheet after cessation of the perturbation by basal ice-shelf melting in the RHS basin r. In all three scenarios the grounding line in basin r continues to retreat after cessation of the forcing. It then migrates beyond the local minimum of the bed depression and stabilizes on the RHS flank of the central ridge.

The further evolution of the ice sheet depends on the bed topography. In the simulations with central bed elevation values ranging from $b_c = -460$ to $+330$ m the grounding line in the LHS basin l starts to retreat after a time of some kyr to several 10 kyr. The grounding line passes the tip of the local sill followed by an unstable retreat on the retrograde section of the bed. Similar to the previous retreat in basin r the grounding line then stabilizes on the LHS flank of the central ridge. The resulting steady-state ice sheet is symmetric again and has shrunk significantly compared to its initial steady-state. This scenario is referred to as “unstable” scenario U afterwards (Figs. 3 and 4a). For the simulations with $b_c \geq +340$ m the grounding line in basin l remains located on the ocean-ward side of the sill. The resulting steady-state ice sheet hence has an asymmetric shape (“stable” scenario S, Fig. 4b). Simulations using a central bed elevation of $b_c \leq -470$ m initially show the same process of unstable ~~grounding-line~~ grounding-line retreat in basin l as in scenario U. However, in contrast to scenario U, the grounding line in basin l does not stabilize and at some point a ~~grounding-line~~ grounding-line retreat in basin r sets in again. This results in a total collapse of the ice sheet (“collapsing” scenario C). We visualize the time evolution of the ice-sheet profile also in a short movie for the scenarios U and S, respectively (see Supplement).

Characteristic features that go along with the triggered unstable ~~grounding-line~~ grounding-line retreat in the RHS basin r are a shift of the ~~ice divide~~ ice divide position (defined as the location through which there is zero ice flux) towards the LHS basin l (Figs. 5–7, panel b), a non-zero and increasing ice flux through x_c (from basin l into basin r) and a decrease in grounded ice sheet volume. The simulations of the unstable scenario U imply a triggered MISI also in basin l, causing the ice divide to shift back to its original position,

including a further decrease in ice sheet volume. Before stabilization, a slight ~~grounding line~~grounding-line retreat in basin r sets in again (Fig. 5a). In the stable scenario S the position of the ice divide, the ice flux through x_c and the ice volume adjust only slightly after the grounding line in basin r has stabilized, reflecting the asymmetric shape of the resulting ice sheet (Figs. 4b and 6). The collapsing scenario C is very similar to scenario U with the difference that in the former the reoccurrence of ~~grounding line~~grounding-line retreat in basin r is significantly larger with grounded ice volume dropping to zero eventually as both grounding lines synchronously reach $x = 0$ (Fig. 7).

3.1 ~~Basin perturbation by ice-divide migration~~Conceptual analysis of interaction of instabilities

The stability of the ice in the left basin l of our setup can be investigated with a perturbation analysis. ~~It is determined by the magnitude of ocean-ward motion~~ We here discuss possible scenarios of basin interaction for a given bed topography $b(x)$ and surface accumulation a conceptually. According to Schoof (2007a) the flux across the grounding line for the present unbuttressed SSA problem in flow line is a function of local bed topography and for our used parameters has the form of

$$Q_g(x) \sim -b(x)^{19/4}. \quad (1)$$

We thus can calculate a theoretical grounding-line flux for each x given a fixed bed geometry like the symmetric, overdeepened bed shape we prescribe in this study (Fig. 8a, black curve). Possible steady-state grounding-line positions exist where inflow equals outflow, i.e., where the integrated mass gain between ice divide and grounding line equals ice discharge across the grounding line, and hence are given by the intersections of the line ax with $Q_g(x)$ in Fig. 8a. In the case of a symmetric ice sheet the same number of stable solutions exists on both sides of the ice sheet (number depending on magnitude of surface accumulation). Grounding-line positions on the retrograde bed section are unstable (Schoof, 2007a).

We now consider the case examined in our experiments: A symmetric steady-state ice sheet with grounding lines located on the ocean side of the coastal sill (Fig 8b, grey line) is perturbed in basin r such that the RHS grounding line enters the retrograde bed section. A new stable solution is found on the central landward up-sloping bed section. The corresponding leftward ice-divide shift then alters the set of possible stable grounding-line positions in basin l. The strength of the shift determines the extent to which the basin's area of mass gain is reduced (Fig. 8b, colored lines). For a small displacement of the ice divide that is induced by the destabilization (blue line) a stable grounding-line position in basin l still exists oceanward of the coastal sill. Basin l thus remains stable and the final steady-state ice sheet is of asymmetric shape, corresponding to Scenario S (Fig. 4b). For a moderate shift of the ice divide (red line) only one stable grounding-line solution in basin l remains, i.e. on the central bed section. The ice in basin l hence has destabilized (Scenario U). The ice divide will move back to the center ($x = 0$) such that the stable solutions in basins l and r will be symmetric again (Fig. 4a). If the ice-divide shift is large (purple line) no grounding-line solution exists in basin l (basin collapse, Scenario C).

3.2 Basin perturbation by ice-divide migration

The stability of the ice in the right basin l is determined by the distance that the ice divide moves towards basin l in response to thinning in basin r. The shift of the ice divide depicts a perturbation to basin l in a way that the basin's area of mass gain through surface accumulation is reduced. The strength of this perturbation, to which ice dynamics in the basin have to adjust, decides about whether the system remains stable (scenario S) or undergoes an instability (scenarios U and C).

The stability of the ice in basin l can be analyzed by considering the temporal evolution of its grounded volume, which can be written as

$$\frac{\partial V_l}{\partial t} = \frac{\partial}{\partial t} \int_{x_g(t)}^{x_i(t)} H(x, t) dx, \quad (2)$$

where H is the ice thickness and x_g and x_i denote the location of the grounding line and ice divide, respectively. Carrying out the Leibniz integration rule and using the ice-thickness equation, $\frac{\partial H}{\partial t} = -\frac{\partial Q}{\partial x} + a$, yields

$$\frac{\partial V_l}{\partial t} = H_i \frac{\partial x_i}{\partial t} - H_g \frac{\partial x_g}{\partial t} + Q_g + a \cdot (x_i - x_g), \quad (3)$$

where H_i and H_g give the ice thickness at the ice divide and the grounding line, respectively. Q_g is the ice flux across the grounding line, which is negative in basin I, and a is the constant surface accumulation. A sufficient condition for the left basin to remain stable is that the basin does not loose ice volume ($\frac{\partial V_l}{\partial t} \geq 0$). This condition is equivalent to

$$H_i \frac{\partial x_i}{\partial t} + a \cdot (x_i - x_g) \geq H_g \frac{\partial x_g}{\partial t} - Q_g. \quad (4)$$

An ocean-ward motion of the ice divide hence would have to be compensated by an equally-directed motion of the grounding line and/or a decrease of the ice-flux magnitude across the grounding line. This is not the case for any of our investigated scenarios. Regarding scenarios U and C, on the short term, the grounding-line-grounding-line position remains constant and $Q_g - Q_g$ increases only very slightly, approximately balancing the reduction of the basin's mass gain through surface accumulation (Fig. 5c). The decrease in basin length hence translates directly into a volume decrease of the system (Fig. 5d). The time scale of adjustment of the ice flow is much larger than the perturbation time scale and thus the grounding-line-grounding-line retreat sets in not before the ice divide has almost reached its maximum displacement (Fig. 5a and b). The slow retreat of the grounding line is nearly balanced by a back shift of the ice divide such that the total ice volume is close to stabilization. At the time when the grounding line starts to undergo unstable retreat on the reverse bed slope, the magnitude of flux across the grounding line increases significantly, resulting in abrupt mass loss which cannot be compensated by the accelerated back shift of the ice divide. The volume starts to stabilize once the grounding-line-grounding-line retreat slows down and the grounding-line-flux-grounding-line-flux magnitude decreases. Regarding

scenario U, the system reaches a new equilibrium as the motion of its boundaries attenuates and grounding-line grounding-line flux is again in balance with surface accumulation. In scenario C (Fig. 7) the grounding-line grounding-line retreat continues and the associated reduction in basin length cannot be compensated by the decrease in flux magnitude across the grounding line, resulting in continued net grounded ice loss of basin I.

Regarding scenario S, the short-term evolution of basin I is similar to the other two scenarios (compare Fig. 6 to Figs. 5 and 7). However, during the time of ice-flow adjustment the system equilibrates with mass gain and grounding-line ice grounding-line flux remaining in balance. The grounding line hence stays approximately located at its original position and also the ice divide reaches a stable position. The ice-divide ice-divide perturbation is not large enough to induce self-sustained grounding-line grounding-line retreat and associated basin destabilization.

3.3 Scaling of symmetric steady-state ice sheets

For several simplified ice-sheet problems analytic solutions of steady-state ice-sheet profiles have been derived (Greve and Blatter, 2009; Bueler, 2014). Vialov (1958) derived an analytic solution for the profile of a symmetric, isothermal steady-state flow-line ice sheet for the SIA of the momentum balance, where vertical shearing is dominant. The surface elevation h of the ice sheet that is grounded on a flat bed is then basically determined by its length L :

$$h(x) = h_c \cdot \left[1 - \left(\frac{x}{L} \right)^{(n+1)/n} \right]^{n/(2n+2)} \quad \text{with } x \in [-L, L], \quad (5)$$

where

$$h_c = 2^{n/(2n+2)} \cdot \left(\frac{a}{A} \right)^{1/(2n+2)} \cdot L^{1/2} \quad (6)$$

is the surface elevation at the center of the ice sheet (at the ice divide) with uniform accumulation a and ice softness A . The equation in brackets in Eq. (45) represents the non-dimensionalized universal shape of an SIA-ice sheet under the above conditions.

Vialov's and our idealized cases share several assumptions but also differ substantially in some respects. In contrast to Vialov, we use a non-flat bed, allow for basal sliding and longitudinal stresses in the ice sheet are predominant over vertical shearing (the SSA-velocities are large compared to the SIA-velocities for the major part of the grounded ice sheet; [SIA influence discussed in Appendix C](#)), features which are typical for ice streams found in the WAIS. However, using Eq. (45) with $n = 3$ and prescribing h_c and L from model output, the Vialov profile (dotted lines in Fig. 3b and c) resembles the profile that we obtain from our [steady](#) simulation (solid gray lines in Fig. 3b and c).

For a given bed topography in our simulations of scenario U the initial and final symmetric steady-state profiles of the ice sheet substantially differ in size but have a similar shape. Equation (45) can be used to scale between two such ice sheets of lengths L_0 and L_1 , respectively,

$$h_1(x_1) = h_0(x) \cdot \left(\frac{L_1}{L_0} \right)^{1/2}, \quad \text{where } x_1 = x \cdot \frac{L_1}{L_0} \quad \text{with } x \in [-L_0, L_0], \quad (7)$$

using the same scaling exponent of $1/2$ as derived for the central ice-thickness of the Vialov profile. We apply the above scaling using the initial surface elevation h_0 as well as the initial and final [grounding-line](#) [grounding-line](#) positions from model output to arrive at the final surface elevation h_1 (shown exemplary for two different central ridge elevations as dashed lines in Fig. 4b and c). That is to say, the simulated ice sheet exhibits more or less the same relation between its central ice thickness and its horizontal extent.

3.4 Scaling of transition time between instabilities

In the unstable scenario U two MISIs succeed each other. The first MISI in the RHS basin r (which was previously triggered by a local perturbation) causes the initiation of a second MISI in the connected LHS basin l, a process going on only due to internal ice sheet dynamics. The transition time Δt between the occurrence of both events of unstable [grounding-line](#) [grounding-line](#) retreat (Fig. 5a) ranges from several kyr to 10 kyr and is practically independent of the initial trigger. Assuming that the difference between the ice thickness of the

two states is the internal force for the transition, we scale Δt with $\Delta H_c = (h_1 - h_0)(x = 0)$, i.e. the central ice thickness difference between the final and initial steady-states of the ice sheet (Fig. 3a). The relation

$$\Delta t = \Delta t_{\min} + C \cdot (\Delta H_c - \Delta H_{c,\min})^{-1} \quad (8)$$

provides a good approximation of the transition time with constants C , Δt_{\min} and $\Delta H_{c,\min}$ (Fig. 89). Here ~~the constants~~ Δt_{\min} and $\Delta H_{c,\min}$ have clear physical interpretations and represent a minimum transition time and a minimum ice thickness difference, respectively (Fig. 8). These asymptotes constrain the regime for which the MISI in basin I is triggered and the final steady-state ice sheet is of symmetric shape (scenario U): for $\Delta H_c < \Delta H_{c,\min}$ the ice sheet remains asymmetric (scenario S) whereas in the regime $\Delta t < \Delta t_{\min}$ it collapses completely (scenario C).

Replacing ΔH_c with the above definition and using Eq. (67), the transition time (Eq. 78) can be rewritten as

$$\Delta t = \Delta t_{\min} + C \cdot \left(h_{0,c} \cdot \left[\left(\frac{L_1}{L_0} \right)^{1/2} - 1 \right] - \Delta H_{c,\min} \right)^{-1}, \quad (9)$$

which allows a scaling of the transition time based on the initial central surface elevation of the ice sheet, $h_{0,c}$, and Vialov's $L^{1/2}$ -dependency.

The transition time can also be expressed in terms of the grounding-line grounding-line shift between the ice sheet's two steady-states $\Delta L = L_0 - L_1$. Since ΔL is approximately a linear function of the central ice thickness difference ΔH_c , Eq. (78) can also be written as

$$\Delta t = \Delta t_{\min} + D \cdot (\Delta L - \Delta L_{\min})^{-1} \quad (10)$$

by using a different coefficient D instead of C . The threshold $\Delta H_{c,\min}$ is replaced by a threshold of a minimum grounding-line grounding-line retreat, ΔL_{\min} , which has to be exceeded to enable the MISI initiation in basin I.

3.5 Transient dynamic thinning and ~~basin-stability~~basin stability

Here we describe the temporal evolution of the ice sheet after cessation of its perturbation in detail. We reveal the origin of the qualitative difference between the unstable/collapsing scenarios U/C, which imply a MISI transition between basin l and r, and the stable scenario S, which does not imply such a transition. The ~~grounding-line~~grounding-line retreat in the RHS basin r, which continues after the perturbation, is associated with a dynamic thinning of the upstream ice (Figs. ~~9-and-10~~10 and 11). The thinning declines with increasing distance from the grounding line towards the interior of the domain but is still non-zero in the center of the ice sheet and reaches further into the LHS basin l with time. While the grounding line stabilizes in basin r and the local thinning rate goes to zero, the inland thinning propagates far enough into basin l to reach the local grounding line. Here the increasing thinning rate eventually results in a ~~grounding-line~~grounding-line retreat. Depending on the scenario, the thinning in basin l then continues to propagate back into the interior of the basin (scenarios U and C, instability in basin l triggered) or ceases (scenario S, instability not triggered).

We compare the time evolution of the ice in basin l for two simulations which show this qualitative difference in stability while having almost the same bed topography (simulations BC+330 and BC+340). In simulation BC+330 the grounding line in basin l retreats beyond the point of maximum sill elevation. The thinning continues to propagate into the interior and the thinning rate increases during the grounding line's unstable retreat on the retrograde section of the bed. Temporarily, basin r is now affected by an inland thinning, which results in a slight retreat of the previously stabilized grounding line in basin r (Fig. ~~9~~10). The rate of the thinning in both basins goes to zero as the grounding lines find their steady-state position synchronously. In simulation BC+340, the thinning rate in basin l goes to zero as the grounding line migrates upstream towards the point of local maximum bed elevation (Fig. ~~10e~~11c). The cumulative thinning there (at the tip of the sill) is insufficient to cause the ice to become afloat (indicated by dotted cross in Fig. ~~10b~~11b). Due to the almost identical setups of both simulations we identify the location of maximum elevation of the sill in basin

l as the instability threshold, i.e. a grounding-line grounding-line retreat beyond this point implies the initiation of a MISI in basin l.

4 Discussion and conclusions

We investigate the possibility of whether a MISI can be triggered from the direction of the ice divide as opposed to coastal forcing and to this end study the interaction between connected basins. In our experiments we perturb one basin to analyze its interaction with a connected basin. The extent of grounding-line grounding-line retreat in the aftermath of the triggered MISI in the perturbed basin significantly determines the degree of interaction with the other basin, including a scenario of an induced MISI (scenarios U and C). Our results can also be interpreted such that the motion of the ice divide that is induced by the destabilization of one basin depicts imparts a perturbation to the connected basin. The magnitude of the ice-divide shift decides about the stability of the connected basin. This not only comes out of our results from simulation but can also be explained by means of a conceptual flux-balance analysis in steady state (Fig. 8).

The transition of the MISI between the two basins takes place without external forcing and hence only due to internal ice sheet dynamics. This feature is robust against a reduction in surface accumulation (simulations using an accumulation rate one order of magnitude lower demonstrate the same quality like the runs shown here). Our results are also independent of the selected perturbation (Fig. 11). -see Appendix A and Fig. 12). In most of our experiments grounding-line retreat is forced by ocean melting that is also applied (in a reduced way) to grounded grid cells below sea level adjacent to a floating grid cell. This way an extra flux out of these coastal grid cells is produced that qualitatively resembles the response of an ice sheet to a reduction in ice-shelf buttressing. Such imposed resolution-dependent flux increase has to be handled with care due to the possibility of overriding actual ice dynamics. However, since we use such melting only to force grounding-line retreat until a certain point, stopping it afterwards, the MISI process and the mechanism of basin interaction revealed in this study are left unaffected by the perturbation method.

While the unstable ~~grounding-line~~ ~~grounding-line~~ retreat in our experiments is in accordance with findings by Schoof (2007a), the possibility of a MISI in three dimensions highly depends on the geometry of the ice sheet and the underlying bed (Joughin et al., 2010; Katz and Worster, 2010; Gudmundsson, 2013; Parizek et al., 2013; Mengel and Levermann, 2014; Joughin et al., 2014). The time scales of ice sheet response in our experiments are in the order of magnitude of 1 kyr (unstable ~~grounding-line~~ ~~grounding-line~~ retreat) to 10 kyr (transition time between MISIs in basin l and r). The stabilizing effect of buttressing in three dimensions would most probably slow down basin interaction.

On the time scales discussed here the influence of glacial isostatic adjustment (Peltier, 2004; Bueler et al., 2007), which for simplicity is not included in our study, might become relevant. In response to ice thinning and grounding-line retreat an asymmetrical bed deformation with feedback on grounding-line motion has to be expected, including the possibility of an earlier grounding-line stabilization in basin r than in the static-bed case. However, the three scenarios investigated in our study are expected to remain valid in the dynamic-bed case since each scenario exists for a broad range of central bed elevations, though the thresholds between the scenarios presumably would shift.

The underlying mechanism of basin interaction in our simulations is based on a dynamic thinning of the ice (Fig. 4). Originating in one basin and reaching as far as to the grounding line of the other basin, it enables far field communication between the grounding lines of both basins (Figs. ~~9 and 10~~ 10 and 11). Dynamic thinning is of course not limited to two dimensions. However, in three dimensions it might propagate less straight away from the grounding line but also spread laterally. Nevertheless, a possible influence of future thinning in the basins of the Amundsen Sea Sector onto other basins in the WAIS, e.g. extensive thinning of PIG affecting FRIS basin, cannot be excluded.

Based on the Vialov profile (Eq. 45) we do a simple scaling of the initial and final symmetric steady-state surface elevations of the grounded ice sheet for the unstable scenario U. The Vialov profile was derived using several assumptions which don't apply to our setup. In particular it is an SIA-solution for a flat, non-sliding bed, while our simulations are SSA-dominated, our bed topography is non-trivial and we allow for basal sliding. Given these

substantial differences, the ice sheet profiles from Vialov's equation and from our model results are in good agreement and also the scaling of steady-state surface elevations via Eq. (67) works reasonably well.

The elevation of the central bed ridge in our setup has a strong influence on the steady-state ~~grounding-line~~grounding-line position in the RHS basin r (Fig. 3). With increasing elevation of the central ridge the grounding line stabilizes farther from the center with the result that far field thinning in the LHS basin l becomes weaker and thus takes longer to affect the grounding line in basin l (Fig. 89). This also becomes apparent from Eq. (910), which states that the transition time scales inversely with the extent of ~~grounding-line~~grounding-line retreat and includes a threshold of a minimum ~~grounding-line~~grounding-line retreat below which basin l remains stable. The central ridge may hence be considered as a barrier which can dampen/facilitate basin interaction when being elevated/lowered. In other words, ~~grounding-line~~grounding-line retreat in the perturbed basin strongly determines the degree and the quality of the interaction with the connected basin.

Appendix A: Applying an alternative perturbation in basin r

We apply a different type of perturbation to show that the mechanism of MISI interaction revealed in our study does not depend on the particular way the destabilization of basin r is triggered. The set of experiments is carried out as described in Sec. 2 with the exception that during the perturbation phase the ocean forcing is replaced by an atmospheric one. Ocean melting hence remains zero throughout the whole sequence of experiments. Instead, the surface accumulation a is set zero for $x > 0$ (basin r in steady state) and for the rest of the domain a remains at its original value. The perturbation length is the same as for the ocean-forced simulations (1.3 kyr).

Figures ~~11a and b exemplary show that a destabilization~~12a and b show that similar destabilization takes place in basin l ~~is induced independent of the applied~~in response to either the atmospheric or oceanic perturbation in basin r. The ice sheet profiles differ only at the end of the perturbation phase (red profiles). The atmospheric perturbation causes

large-scale ice thinning in basin r associated with an ice-divide shift that is much larger compared to the more localized oceanic perturbation. However, the steady-state profiles that result after the destabilization of basin l are quasi-identical. It is hence not decisive by which kind of forcing but *that* the MISI in basin r is triggered.

5 **Appendix B: Comparison to Schoof's solution from boundary layer theory**

We here compare our modeled steady-state ice-sheet profile to Schoof's solution derived from boundary layer theory (Schoof, 2007a, b). Schoof's grounding-line position and the corresponding ice-sheet profile are obtained by finding the roots of Eq. (22) with Newton's method and subsequent integration of Eq. (25), both in Schoof (2007a), using the parameters of our setup. The solution is complemented by Van der Veen's profile for an ice shelf in equilibrium (Van der Veen, 2013).

The modeled ice-sheet profile is similar to the semi-analytical profile but has a downstream offset of the grounding-line position (Fig. 13a). The difference in grounding-line position might be explained by the dip in ice flux at the grounding line in our simulations (Fig. 13b). A larger grounding-line flux would cause upstream ice thinning and hence result in a grounding-line location that is closer to the theoretical solution. Part of the difference in grounding-line position might also be explained by the finite horizontal grid resolution of 1 km used in our simulations.

Appendix C: Influence of SIA in our simulations

To test the influence of the SIA in our hybrid SSA+SIA simulations (see Sec. 2) we additionally carry out simulations which only account for the SSA. We find that the mechanism of MISI interaction still exists in the SSA-only case, i.e. in the absence of vertical shearing.

During spinup under SSA-only conditions the symmetric grounding lines migrate further upstream than in the SSA+SIA case which can be explained by the lack of horizontal ice diffusion. The grounding lines enter the retrograde bed section and equilibrate at the flank

of the central ridge. To achieve an equilibrium ice sheet with stable grounding lines that are located on the ocean-ward sides of the coastal sills (as in the SSA+SIA case), we apply an increased rate of surface accumulation. Carrying out the whole sequence of experiments in this modified setup reveals that the mechanism of MISI interaction is also present in the SSA-only case (exemplary shown in Fig. 11e12c). In comparison to the SSA+SIA simulations the ice sheet is thicker, which is a direct effect of the applied increased surface accumulation. However, the ice-sheet profiles are very similar (compare Figs. 11a12a and c), which confirms that the SSA plays the dominant role in our simulations.

**The Supplement related to this article is available online at
doi:10.5194/tcd-0-1-2015-supplement.**

Acknowledgements. We would like to thank Stephen Cornford for extremely helpful comments during the review process and also two anonymous reviewers for their detailed comments which helped to improve the paper. The research leading to these results has received funding from the European Union Seventh Framework Programme FP7/2007-2013 under grant agreement n° 603864. J. Feldmann is funded by Deutsche Bundesstiftung Umwelt.

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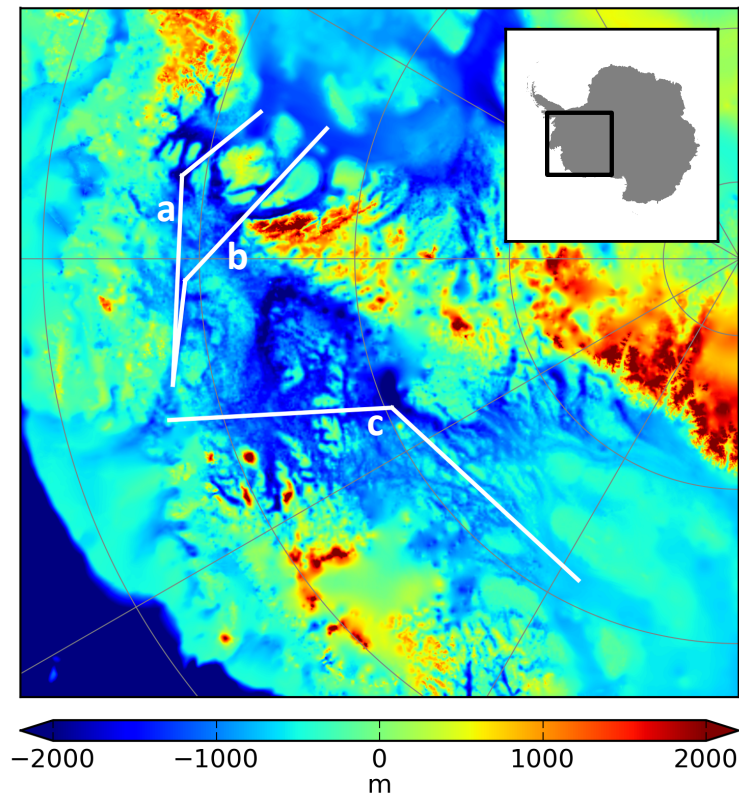
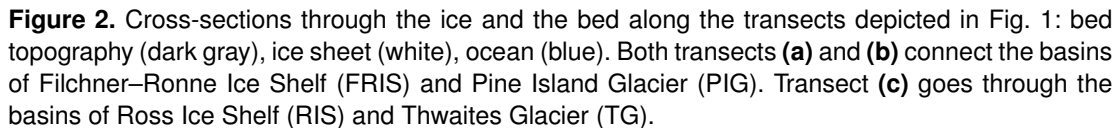


Figure 1. Topographic map of the bedrock underlying the Antarctic Ice Sheet. Each of the transects (white lines) connects two major drainage basins of the WAIS. The bed topography and the ice profile along transects a, b and c are shown in the corresponding panels of Fig. 2.



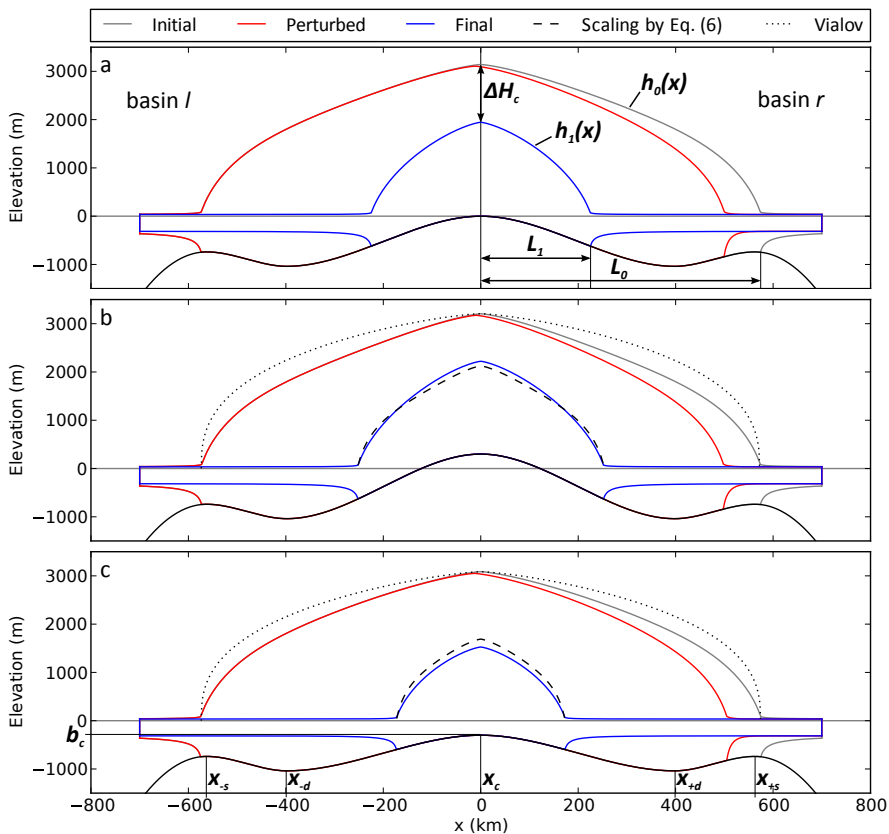


Figure 3. Ice sheet profiles at three stages of simulation for three different values of central bed elevation **(a)** $b_c = 0$ m, **(b)** $b_c = +300$ m and **(c)** $b_c = -300$ m. **Panel-(b)** depicts **Panel (a)** and **(c)** depict the notation used in the text.

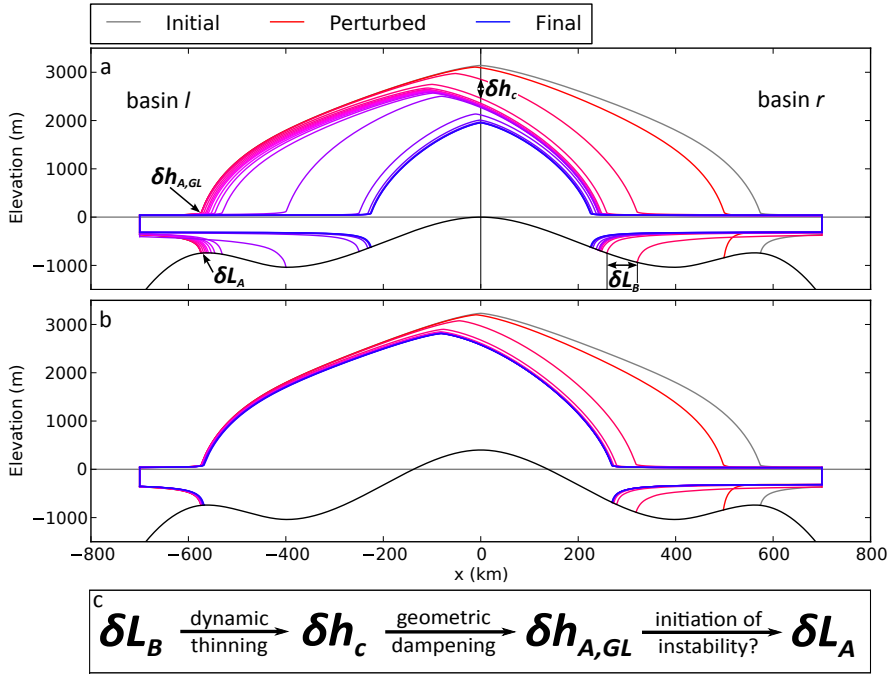


Figure 4. Profiles of the transient ice sheet between the end of perturbation (red) and the final steady-state (blue) for two different values of central bed elevation **(a)** $b_c = 0$ m (example of unstable scenario U, same as in Fig. 3a) and **(b)** $b_c = +400$ m (example of stable scenario S). The time interval between two consecutive profiles is 1 kyr. **The bottom panel Panel (c)** explains the mechanism of basin interaction conceptually with the notation depicted in panel **(a)**.

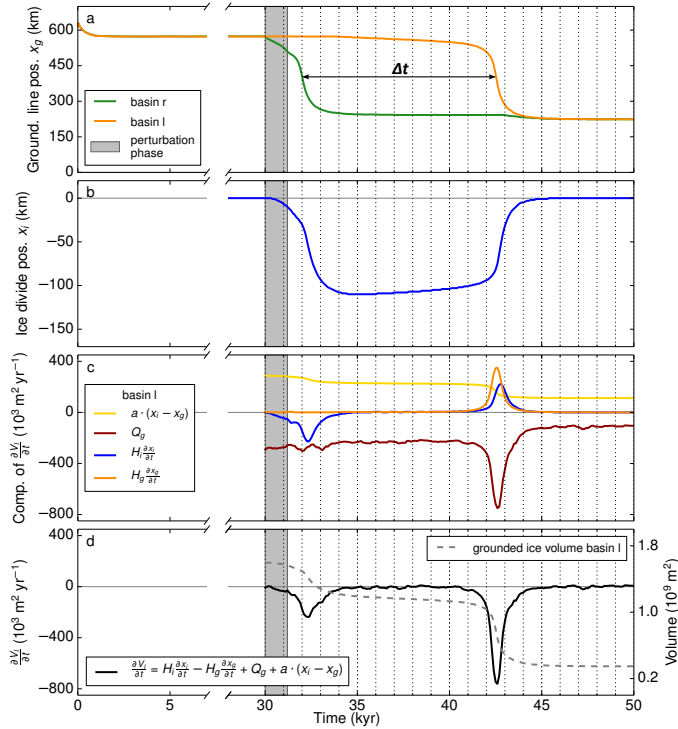


Figure 5. Timeseries for the unstable scenario U (simulation BC0, see Figs. 2a–3a and 3a4a) of (a) the absolute value of the grounding line positions (b) the position of the ice divide (as defined in the text), (c) the individual components of $\frac{\partial V_i}{\partial t}$ (as derived in Sec. 3.1, smoothed with a 500-year moving window), (d) the sum of these components and the grounded ice volume of basin I. The transition time Δt , used in Eqs. (78)–(910), is depicted by a double-headed arrow in panel (a).

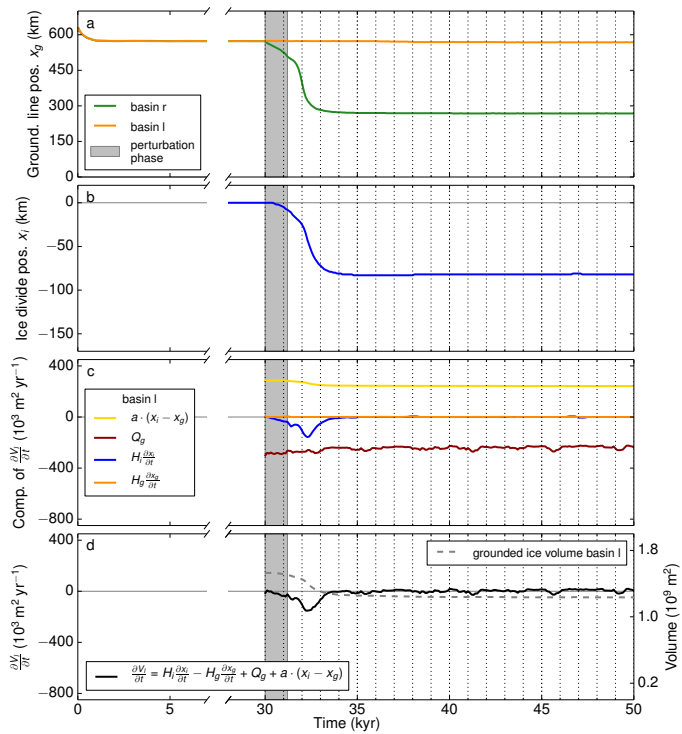


Figure 6. Same as Fig. 5 but here for the stable scenario S (simulation BC+400, see Fig. 4b).

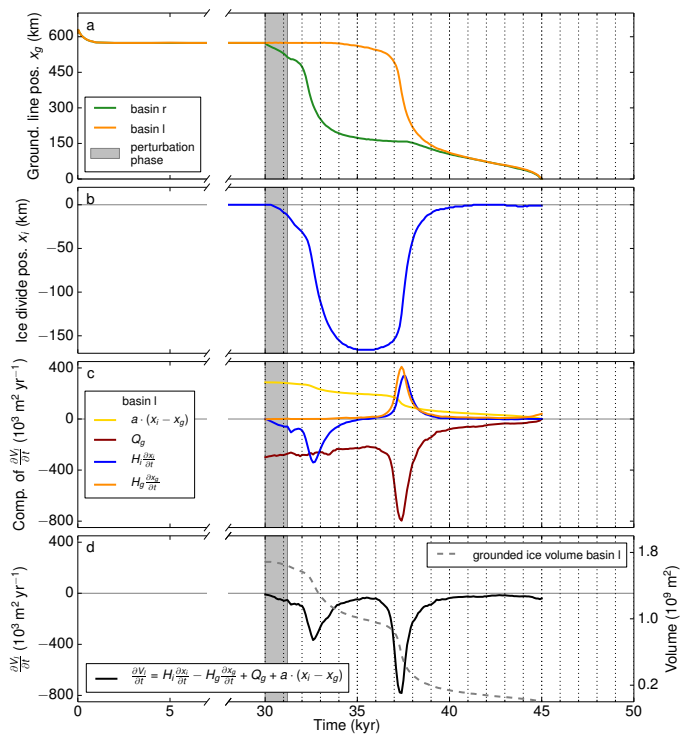


Figure 7. Same as Fig. 5 but here for the collapsing scenario C (simulation BC-500).

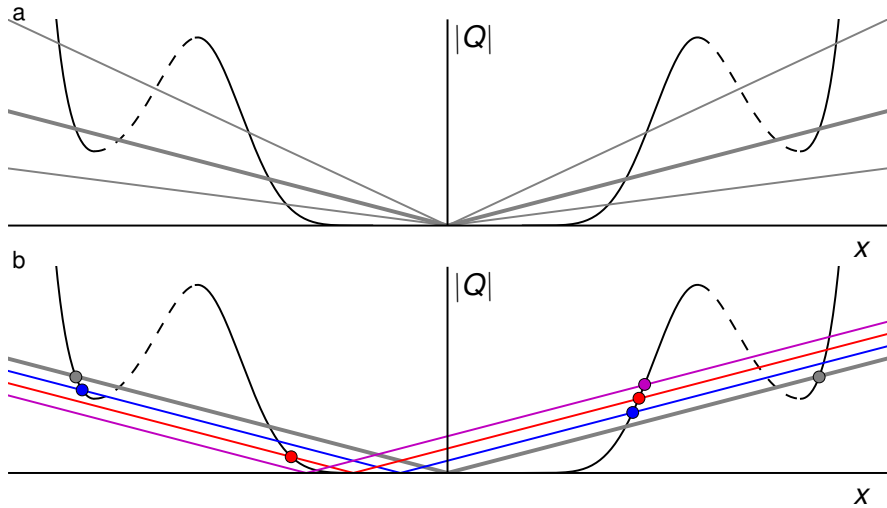


Figure 8. Conceptual picture to identify steady-state grounding line positions and analyse basin stability. The grounding-line flux Q_g (black curve) according to Eq. (1) is shown for a symmetric, overdeepened bed shape used in our experiments. The dashed lines mark the sections of retrograde bed. (a) Different grey lines show the mass gain through snowfall, ax , for a symmetric ice sheet for three different magnitudes of surface accumulation a . Intersections of Q_g and ax yield possible steady-state grounding line positions. (b) Colored lines give $a(x - x_i)$ for one accumulation magnitude (thick line in panel (a)) but different positions of the ice divide, x_i , that is shifted leftward in response to an assumed destabilization of basin r . Grounding line positions (circles) are shown for the three scenarios S (blue), U (red) and C (purple) discussed in this study as well as an initial symmetric steady state (grey).

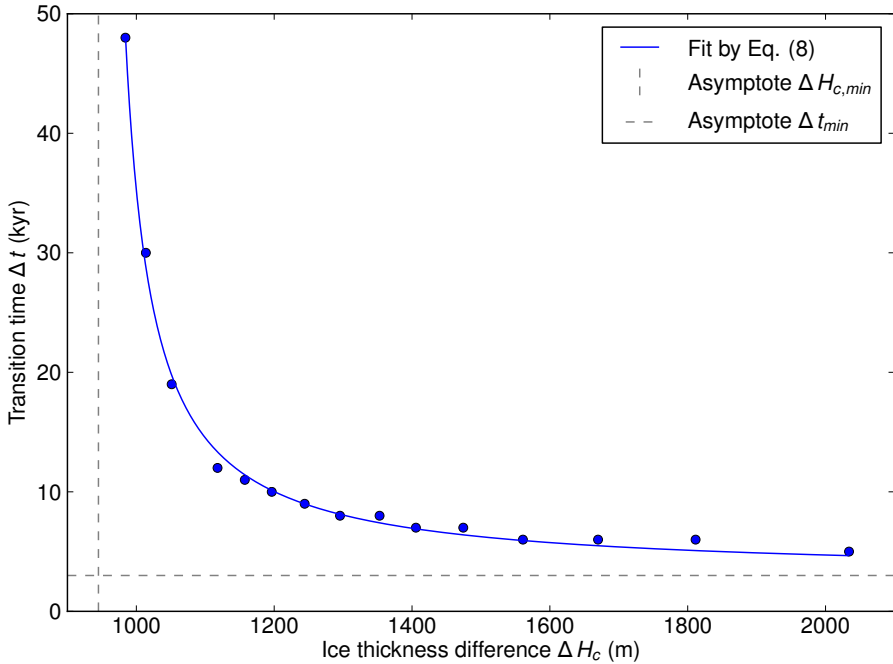


Figure 9. Transition time of MISI Δt plotted against central ice thickness difference between initial and final steady states of the ice sheet ΔH_c . Each dot represents a simulation of scenario U with a different central bed elevation b_c . The constants for the fit by Eq. (8) are $\Delta t_{min} = 3000$ yr, $\Delta H_{c,min} = 945$ m and $C = 1727$ yr m.

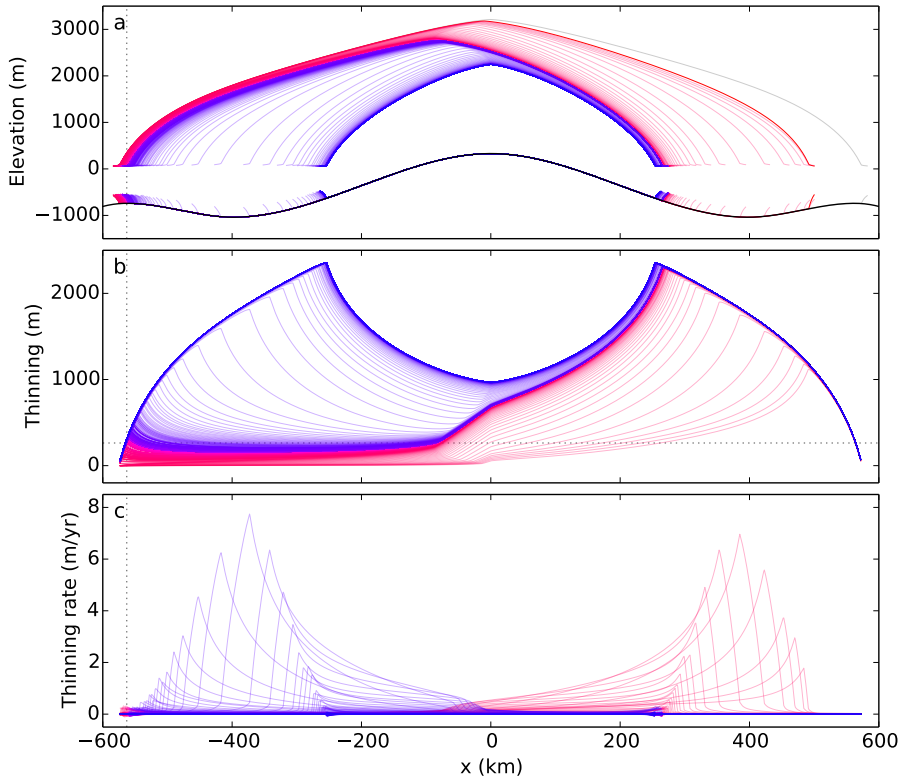


Figure 10. Ice sheet (a) profile, (b) thinning with respect to the ice thickness at the end of perturbation and (c) thinning rate at multiple stages (time interval 100 yr) of the unstable scenario U (simulation BC+330). The ice shelf is truncated for better visibility. The vertical dotted line indicates the location of maximum sill elevation x_{ss} . The horizontal dotted line in panel (b) gives the amount of cumulative thinning necessary to cause the ice situated on the local bed maximum to become afloat. The same color-coding as in Fig. 4 applies.

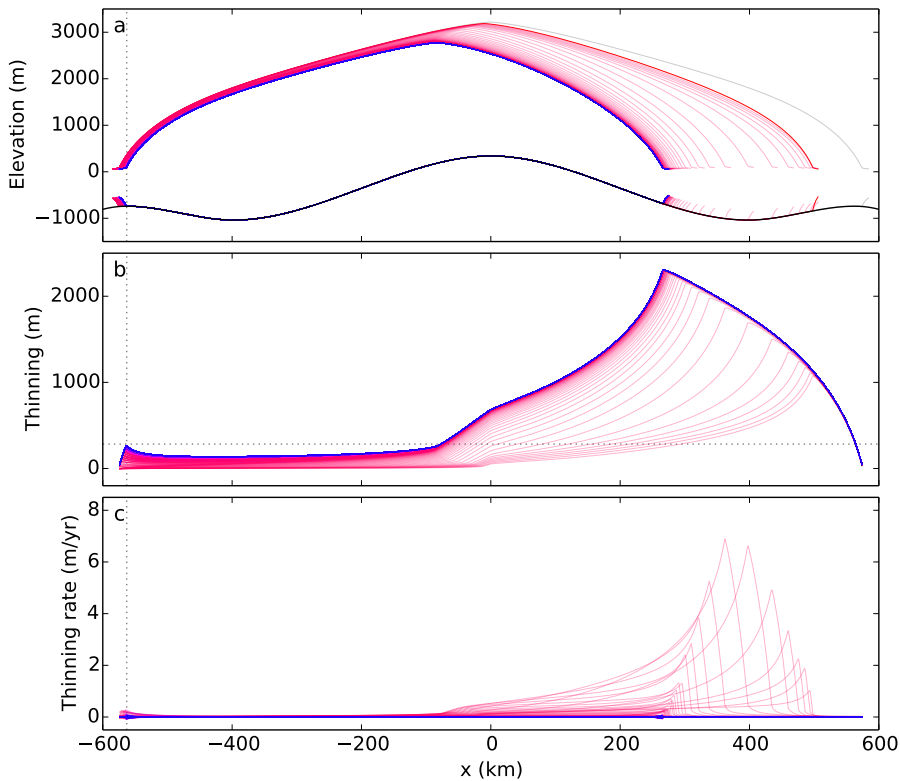


Figure 11. Same as Fig. 9–10 but here for the stable scenario S (simulation BC+340).

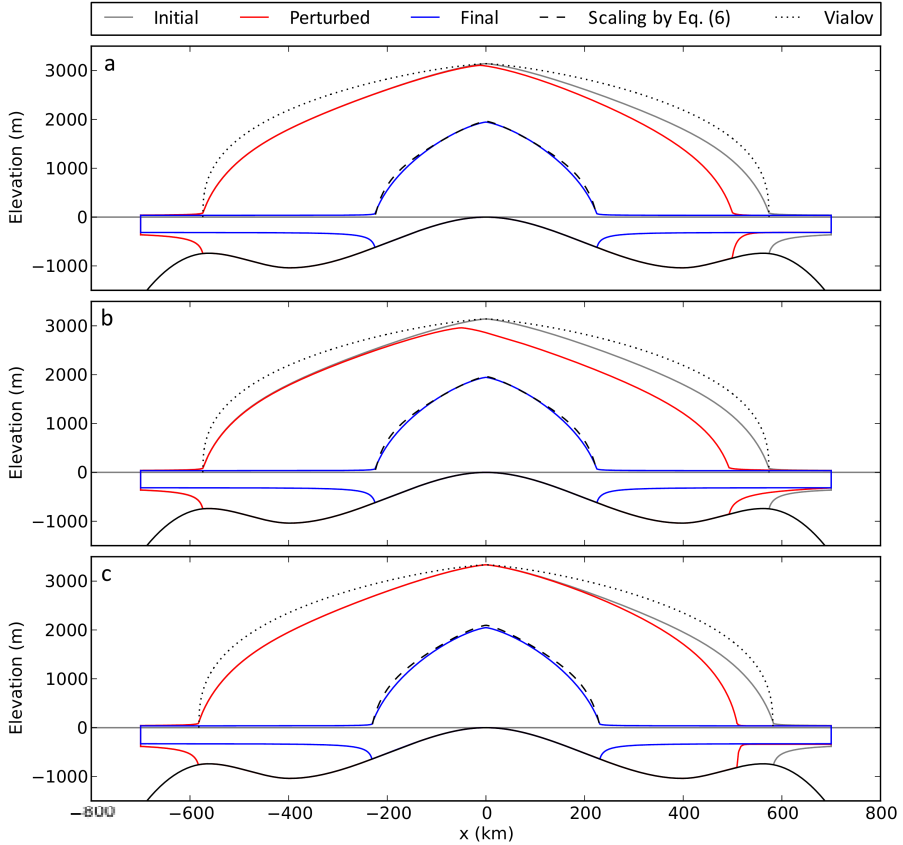


Figure 12. Ice sheet profiles at three stages of simulation for a central bed elevation of $b_c = 0$ m with applied (a) oceanic (same as Fig. 3a) and (b) atmospheric perturbation. Panel (c) shows a set of SSA-only simulations using an oceanic perturbation.

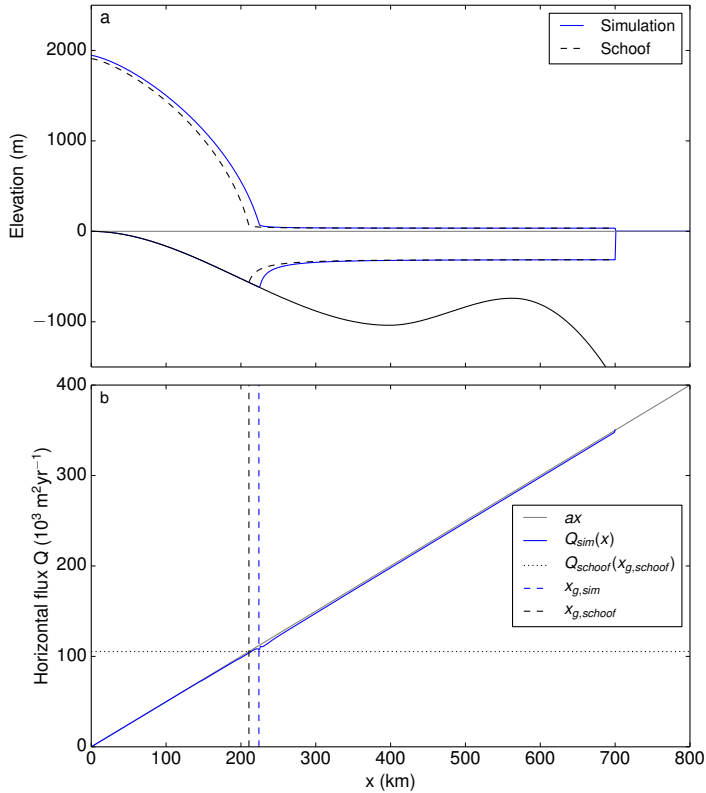


Figure 13. (a) Comparison between the semi-analytical ice sheet profile from Schoof and our modeling result for the final steady-state ice sheet of simulation BC0 (only the RHS of the symmetric ice sheet is shown here). Panel (b) shows Schoof's and the modeled grounding line position, $x_{g,schoof} = 211$ km and $x_{g,sim} = 224$ km, respectively, as well as the steady-state ice flux from simulation, $Q_{sim}(x)$, along the model domain to compare with ax and the analytically-derived Schoof flux, Q_g , at $x_{g,schoof}$.