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Snow cover reconstruction methodology based on historic in situ observations and recent remote sensing data

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Abstract

Spatially distributed snow cover extent can be derived from remote sensing data with good accuracy. However, such data are available for recent decades only, after satellite missions with proper snow detection capabilities were launched. Yet, longer time
series of snow cover area (SCA) are usually required e.g. for hydrological model calibration or water availability assessment in the past. We present a methodology to reconstruct historical snow coverage using recently available remote sensing data and long-term point observations of snow depth from existing meteorological stations. The methodology is mainly based on correlations between station records and spatial snow cover patterns. Additionally, topography and temporal persistence of snow patterns are taken into account. The methodology was applied to the Zerafshan River basin in Central Asia – a very data-sparse region. Reconstructed snow cover was cross-validated

against independent remote sensing data and shows an accuracy of about 85%. The methodology can be used to overcome the data gap for earlier decades when the availability of remote sensing snow cover data was strongly limited.

1 Introduction

Water resources from remote mountain catchments play a crucial role for the development of regions in or in the vicinity of mountain ranges (Pellicciotti et al., 2011). Seasonal snow is an important water resource in many of Earth's semiarid regions (Durand

et al., 2008). Particularly, in Central Asia, seasonal snowmelt decisively contributes to the total runoff volume (Ososkova et al., 2000; Unger-Shayesteh et al., 2013).

Information on snow cover and snow depth and ideally on snow water equivalent in Central Asian catchments is crucial for seasonal forecasts of water availability and for calibration and validation of hydrological models. However, the available sparse station-

²⁵ based data are insufficient to represent the snow cover variability over the large and remote mountain areas (Erickson et al., 2005). The development of remote sensing



techniques during recent decades allows to derive snow cover (Liu et al., 2012), but reliable remote sensing data with adequate spatial and temporal resolution such as MODIS (Moderate Resolution Imaging Spectroradiometer) are available for recent decades only. The derivation of snow cover from Landsat and Advanced Very High

- Resolution Radiometer (AVHRR) data which are available for longer periods (Landsat launch 1972; AVHRR launch 1978) is strongly limited by the presence of clouds and atmospheric pollutants. Although recently the reconstruction of snow cover time series from AVHRR data for Central Asia has been reported by Zhou et al. (2013). However, they are also limited in time starting in 1986 at earliest.
- Several studies used remotely sensed snow cover either as input to hydrological models (Tekeli et al., 2005; Immerzeel et al., 2008; Li et al., 2008; Wang et al., 2010) or for calibration and validation purposes (Parajka and Blöschl, 2008a; Corbari et al., 2009; Liu et al., 2012; Duethmann et al., 2014). Particularly, for hydrological model calibration, spatially distributed snow cover data offer high information content required to constrain model parameters (Finger et al., 2011; Duethmann et al., 2011).

In Central Asia, continuous hydro-meteorological records are widely available from 1960s and earlier until the collapse of the Soviet Union in 1991. In contrast, continuous remote sensing snow cover data from MODIS are readily available after 2000, when station data are very scarce. We present a methodology which enables reconstructing

²⁰ historical snow cover pattern using long-term, point-based observations from existing meteorological stations and recent remotely sensed snow cover data. By merging highresolution spatial satellite data with long-term station data, snow cover patterns can be reconstructed for several decades into the past.

Only a limited number of studies on snow cover reconstruction have been conducted in the past that use long term station observations and recent remote sensing data (Robinson, 1991; Brown, 1999; Frei et al., 1999). These studies are however conducted at the continental scale under conditions of dense station network availability and neglecting the effect of topography. Robinson (1991) and Frei et al. (1999) conducted reconstruction of snow cover based on regression analysis between snow



characteristics and snow cover area derived from AVHRR satellite observations. As snow characteristics both studies used snow cover duration derived from interpolated station records. Another study by Brown (1999) conducted reconstruction of snow cover for "pre-satellite era" interpolating snow depth data from station network. For grid cells of nearly 200 km, the interpolation of snow cover was done using different thresholds for snow depth and compared against AVHRR snow cover during "satel-

lite era". The calibration showed 2 cm to be most appropriate snow depth for accurate snow cover reconstruction based on station data. These studies can be helpful in assessing climate related variations of snow cover but are hardly transferable to smaller catchment scale with moderate resolution and limited station data availability.

Different to those studies mentioned above, we present a methodology for snow cover reconstruction (1) with moderate spatial resolution (500 m), (2) suitable for catchment scale hydrological studies, (3) accounting topography and (4) delivering spatially distributed snow cover maps. The methodology takes advantage of the strong control

- of topography on the spatial snow cover distribution. Hence, measurements from snow observation stations at different elevations can be interpreted as representative sites to predict snow cover patterns. The methodology consists of five successive steps which make use of topographic information and correlations between station records and spatial snow cover patterns. In order to test the presented methodology, snow cover
 reconstruction was conducted for four days (Table 1) for which independent Landsat
 - data were available.

2 Study area

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The methodology for snow cover reconstruction was developed and tested for the area containing the Upper Zerafshan River basin, Central Asia (Fig. 1).

The Upper Zerafshan River basin is located in the Gissaro-Alai Mountain Range. Elevation ranges from 658 to 5402 m a.s.l. and basin area is about $12\,000\,\text{km}^2$. The Zerafshan River basin is currently an endorheic basin in the inner Central Asia that



no longer contributes to the Amudarya River. It originates in Tadjikistan and flows towards Uzbekistan, where its water is used for agricultural production in the oases of Samarkand and Bukhara. The flow regime is strongly dominated by snow and glacier melt, as can be inferred from the temperature, precipitation and flow regimes in Fig. 2.

⁵ The highest precipitation is brought by westerly flows during winter and spring, with a clear minimum during summer and early autumn (Aizen et al., 1995). The highest runoff, however, occurs during summer months and is driven by snow and glacier melt.

3 Data

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We used (1) daily in situ snow depth data, (2) daily MODIS snow cover data, (3) a digital
 elevation model (DEM), and (4) Landsat data. The first three datasets were used for snow cover reconstruction whereas Landsat data was used as an independent dataset to validate the results.

3.1 In situ snow depth data

Daily snow depth data in the period from 1964 to 2012 were available for seven climate stations located at different elevations (Fig. 1, Table 1). The data were provided by Uzbek Hydrometeorological Service (Uzhydromet).

3.2 MODIS snow cover data

MODIS daily snow cover data from the Terra satellite with 500 m spatial resolution (MOD10A, version V005) were employed for the time period of 2000 to 2012. We used MODIS Terra snow cover data due to its longer time series compared to the Aqua satellite, which delivered snow cover data only after 2002. The MODIS snow cover product is based on the Normalized Difference Snow Index (NDSI) algorithm (Hall et al., 2002a). Its accuracy was tested in different parts of the world showing good agreement with in situ data (Klein et al., 2003; Tekeli et al., 2005; Parajka et al., 2006; Ault et al., 2006;



Wang et al., 2008; Liang et al., 2008; Huang et al., 2011; Gafurov et al., 2013; Parajka et al., 2012). The main drawback of MODIS snow cover data is the limitation due to cloud cover. There have been several studies on filtering methods for reducing cloud cover or even removing it completely (e.g., Parajka and Blöschl, 2008a, b; Gafurov and

- ⁵ Bárdossy, 2009; Tong et al., 2009; Hall et al., 2010; Lòpez-Burgos et al., 2013). We used original MODIS snow cover data to exclude any uncertainty that may be introduced by cloud filtering. The data were obtained from National Aeronatics and Space Administration (NASA)'s Earth Observing System Data and Information System (EOS-DIS) Reverb platform. MODIS data are distributed as tiles with the size of 10° by 10°,
- ¹⁰ which makes up a total of 36 horizontal (h) and 18 vertical (v) tiles covering the entire globe. In this study, the tile h23v05 was used which covers the study area completely.

3.3 Digital elevation model

The void-filled DEM with 90 m spatial resolution from NASA Shuttle Radar Topography Mission (SRTM) was used. SRTM DEM data was obtained from the CGIAR CSI (Consultative Group on International Agricultural Research, Consortium for Spatial Information) Database (www.cgiar-csi.org/data). To have the same resolution as the MODIS data (500 m), the 90 m SRTM DEM was aggregated to 500 m.

3.4 Landsat data

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Optical remote sensing data from the Landsat Thematic Mapper (TM) sensor were used to validate the reconstructed snow cover maps. The Landsat data have a spatial resolution of 30 m and a temporal resolution of 16 days. Landsat data from four nearly clear-sky days in the snow season (10 April 1998, 20 November 1998, 20 April 1999 and 15 November 1999) were used for validation purposes. Snow cover maps for the Landsat footprint (see Fig. 1) were prepared using the NDSI methodology. For a detailed description of the algorithm used for deriving snow cover maps from Landsat



refer to Gafurov et al. (2013). Figure 3 shows raw and processed Landsat snow cover maps for the study area.

Since Landsat has a spatial resolution of 30 m and snow reconstruction was performed for 500 m pixels based on MODIS resolution, the processed Landsat snow cover maps were spatially aggregated to 500 m resolution. This was done by classifying each of the 500 m pixels as snow-covered or snow-free, based on the majority of the 30 m Landsat pixels within the 500 m pixel.

4 Methodology

The methodology presented hereafter is based on similarity of different locations in terms of presence or absence of snow at a given time. The idea is to use the information about the presence of snow from one location in order to estimate the presence of snow at another location. The similarity between different locations was assessed using both observed snow cover at meteorological stations (i.e. records of snow depth > 0) and MODIS snow cover data. This similarity between two locations was quantified through what we call the matching ratio (MR), i.e. the fraction of daily observations for which one location shows the same coverage as the other (either snow covered or snow free) at the same time (a more detailed explanation follows). Additionally to the similarity between two locations, temporally persistent monthly snow cover patterns and elevation based classifications were used. The methodology consists of five suc-

- ²⁰ cessive steps where each step estimates a certain fraction of snow cover leading to a complete snow cover reconstruction after step 5. Once the similarities and temporally persistent snow fields are assessed using existing stations and remote sensing data, the methodology can be projected in time and is solely based on snow records at meteorological stations. The following five steps are detailed in the next sections:
- 1. station to pixel MR
 - 2. Temporally persistent monthly probability fields



- 3. Pixel to pixel MR fields
- 4. Usage of elevation information
- 5. Station to pixel MR fields for MR < 1

4.1 Station to pixel matching ratio

⁵ Let us define the "matching ratio" (MR) of a pixel at x, y and station n as:

$$MR_{(x,y),(n)}^{s} = \frac{\sum (1 - ABS(S_{x,y,t} - S_{n,t}))}{N_{x,y}} \quad \forall \quad S_{n,t} = 1$$
(1)

$$\mathsf{MR}^{\mathsf{I}}_{(x,y),(n)} = \frac{\sum (1 - \mathsf{ABS}(S_{x,y,t} - S_{n,t}))}{N_{x,y}} \quad \forall \quad S_{n,t} = 0$$
(2)

where $MR_{(x,y),(n)}^{s}$ and $MR_{(x,y),(n)}^{l}$ are matching ratios between a pixel with coordinates *x*, *y* and station *n* for snow and snow free (i.e. land) conditions, respectively. $S_{x,y,t}$ and $S_{n,t}$ are binary variables indicating the presence (S = 1) or absence (S = 0) of snow for day *t*, respectively. $N_{x,y}$ is the number of observations simultaneously available at pixel *x*, *y* (excluding cloud covered days) and station *n* over the 12 years (2000–2012), for which station *n* showed snow (S = 1) or snow free (S = 0) conditions, respectively. The value of $MR_{(x,y),(n)}^{s}$ ($MR_{(x,y),(n)}^{l}$) varies from 0 to 1, and gives the proportion of matches between the snow cover (snow free) observation. $MR_{(x,y),(n)}^{s} = 1$ ($MR_{(x,y),(n)}^{l} = 1$) indicates that a pixel at *x*, *y* was always observed as snow covered (snow free) by MODIS when station *n* measured snow depth > 0 (= 0), whilst $MR_{(x,y),(n)}^{s} = 0$ ($MR_{(x,y),(n)}^{l} = 0$) indicates an opposite relationship, i.e. that the MODIS product at *x*, *y* showed snow free (snow cover) when station *n* always had snow depth > 0 (= 0).

In meteorology and hydrology, correlations between two or more stations are commonly examined to fill data gaps. Here, MRs were computed between snow monitoring



stations and each MODIS pixel in the study area (total of 169 776 pixels) over 12 years of available MODIS observations. Hence, the daily snow cover maps from MODIS are treated as snow observation for each 500 m grid cell, giving rise to a very dense "observation network". An example for a MR map for snow and land conditions for Chimgan station is given in Fig. 4. In total, 14 maps were derived (two maps for every of the 7 stations: one for MR^s_{(x,y),(n)} and one for MR^l_{(x,y),(n)}).

The number of pixels with $MR_{(x,y),(n)}^{s} = 1$ ($MR_{(x,y),(n)}^{l} = 1$) varies from station to station. The higher the number of pixels with $MR_{(x,y),(n)}^{s} = 1$, the higher is the predictive power of the station for snow classification. Similarly, the higher the number of pixels with $MR_{(x,y),(n)}^{l} = 1$, the higher is the predictive power of the station to predict snow-free conditions. In order to quantify the predictive power of each station, we introduce two terms: Snow Predictability Index (SPI) and Land Predictability Index (LPI). These terms give the fractions of the reconstruction domain with MR = 1 for a given station for snow and land conditions, respectively:

$${}_{5} \quad \text{SPI}_{n} = \frac{\sum \left(\text{MR}_{(x,y),(n)}^{\text{s}} = 1 \right)}{N} \cdot 100 \quad [\%]$$
(3)
$$\text{LPI}_{n} = \frac{\sum \left(\text{MR}_{(x,y),(n)}^{\text{l}} = 1 \right)}{N} \cdot 100 \quad [\%]$$
(4)

where SPI_n and LPI_n are Snow Predictability Index and Land Predictability Index of station *n*. *N* is the total number of pixels (169 776) in the entire study area. Pixels ²⁰ with $MR_{(x,y),(n)}^{s} = 1$ in Fig. 4 (top) add up to 10.2% which is the SPI value of Chimgan station for the entire domain. This means that when Chimgan station shows a snow depth above zero, 10.2% of the study area can be classified as snow covered as well. Pixels with $MR_{(x,y),(n)}^{l} = 1$ in Fig. 4 (bottom) add up to 9.0%, i.e. when Chimgan station shows snow-free conditions, 9.0% of the study area can be assigned as snow free.



Figure 4 shows that $MR^{s}_{(x,y),(n)} = 1$ occurs mainly at high elevations (cf. Fig. 1), whilst $MR_{(x,y),(n)}^{I} = 1$ occurs mainly at low elevations. Pixels with an elevation far higher than the elevation of Chimgan station tend to be snow covered if Chimgan station records positive snow depth, whilst pixels with an elevation far below the elevation of Chimgan s station tend to be snow free if Chimgan station records snow depth of zero. Table 1 shows the SPI and LPI values for each station. The stations Kul' and Minchukur near the Zerafshan basin (see Fig. 1) have the highest SPI values (23.2 and 22.6, respectively). Other stations, located further away from the catchment, have smaller SPI values. Noticeably, Oigaing station located farthest away from the Zerafshan basin has the highest LPI value (12.3%). This can be explained with the high elevation of the 10 station. When the station indicates snow free conditions, pixels with significantly lower elevation are likely to be snow-free as well. Assuming that the dependencies remain stable in time, the computed MRs between station and MODIS data can be used to classify individual pixels for any arbitrary day prior to the availability of MODIS data (before 2000) for which station records are available: 15

$$S_{(x,y,t)} = 1$$
 if $\left(MR_{(x,y,n)}^{s} = 1$ and $S_{(n,t)} = 1 \right)$ (5)

 $S_{(x,y,t)} = 0$ if $\left(\mathsf{MR}^{\mathsf{I}}_{(x,y,n)} = 1 \text{ and } S_{(n,t)} = 0 \right)$

This step leads to a partially reconstructed snow cover map which is further enhanced in the next steps.

4.2 Monthly probability fields

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Snow cover extent is a seasonally variable parameter. The probability of a certain pixel to be covered by snow or land varies with time. The second step for reconstructing snow cover is based on the idea that certain pixels within the basin are snow covered

or snow free with high confidence during different months. This allows detecting temporally persistent (continuous snow/snow free coverage) spatial patterns of snow or

(6)

land cover for a certain month. Such spatial patterns can be identified using the available MODIS daily snow cover data in the period 2000–2012 and computing "monthly probability" (MP) of each pixel to be covered as snow or land in a certain month:

$$MP_{(x,y),(m)}^{s} = \frac{\sum (S_{(x,y,t),(t \in m)} = 1)}{N_{(x,y),(m)}}$$

$$MP_{(x,y),(m)}^{l} = \frac{\sum (S_{(x,y,t),(t \in m)} = 0)}{N_{(x,y),(m)}}$$
(8)

5

where $MP_{(x,y),(m)}^{s}$ and $MP_{(x,y),(m)}^{l}$ are the monthly probabilities of pixel x, y in month m for snow and land, respectively. $S_{(x,y,t)}$ indicates the coverage (snow or land) of pixel x, y on day t of month m. $N_{(x,y),(m)}$ is the number of total MODIS observations of pixel x, y and month m in the period 2000–2012. The value of $MP_{(x,y),(m)}^{s}$ ($MP_{(x,y),(m)}^{l}$) can be at maximum 1, meaning that the pixel x, y was covered always by snow (land) in month m during the cloud-free days in the period 2000–2012. Computation of MPs for every pixel in the study area leads to MP maps for all 12 months as illustrated exemplarily in Fig. 5 for April with MP^s and MP^l equal 1.

¹⁵ Pixels with $MP_{(x,y),(m)}^{s} = 1$ in Fig. 5, i.e. pixels that were always snow covered in April, add up to 12.7% of the whole area. This means that 12.7% of the study area can be classified as snow covered in April. Pixels with $MR_{(x,y),(m)}^{l} = 1$ add up to 14.9%, i.e. 14.9% of the domain can be classified as snow free in April. To remain consistent with the terminology used in the first step, we call the sum of pixels with $MP_{(x,y),(m)}^{s} =$

²⁰ 1 ($MP_{(x,y),(m)}^{I} = 1$) monthly SPI (LPI) value for snow (land). Monthly SPI and LPI are defined in a similar way as in step 1 (Eqs. 3 and 4).

The main idea in this step is to transfer these temporally persistent monthly spatial snow/land patterns (SPI_m/LPI_m) to the past to reconstruct historical snow cover. However, the validity of these temporally persistent spatial snow/land patterns over longer time in the past is not accurate due to a negative spatial snow/land patterns over longer

time in the past is not assured, due to e.g. potential warmer/cooler or wetter/dryer climate conditions. In order to account for possible climatic variability, we introduce



a buffer as vertical elevation shift from month-specific minimum snow and maximum land lines. We define a month-specific minimum snow line $(H_{\min,m}^s)$ and a month-specific maximum land line $(H_{\max,m}^l)$ as:

$$H_{\min,m}^{s} = \min(H_{x,y}) \quad \forall \quad \mathsf{MP}_{(x,y,m)}^{S} = 1$$
(9)

$$H^{l}_{\max,m} = \max \left(H_{x,y} \right) \quad \forall \quad \mathsf{MP}^{l}_{(x,y,m)} = 1$$

where $H_{(x,y)}$ is the elevation of the pixel x, y. $H_{\max,m}^{l}$ is thus the maximum elevation of all pixels with $MP_{(x,y,m)}^{l} = 1$ in month m. Note that below the altitude $H_{\max,m}^{l}$ not all pixels necessarily have $MP_{(x,y,m)}^{l} = 1$. Similarly, $H_{\min,m}^{s}$ is the minimum elevation of all pixels with $MP_{(x,y,n)}^{s} = 1$ in month m. Again, $H_{\min,m}^{s}$ does not necessarily represent the elevation above which all pixels have $MR_{(x,y,n)}^{s} = 1$. Table 2 lists monthly SPI and LPI values, as well as $H_{\min,m}^{s}$ and $H_{\max,m}^{l}$ values for the selected area.

These $H_{\min,m}^{s}$, $H_{\max,m}^{l}$, and monthly SPI/LPI maps were used to further reconstruct the snow cover resulting from step 1:

¹⁵
$$S_{(x,y)} = 1$$
 if $(H_{(y,x)} > H_{\min,m}^{s} + \text{buffer and } MR_{(x,y,m)}^{s} = 1)$ (11)

$$S_{(x,y)} = 0 \quad \text{if} \quad \left(H_{(y,x)} < H_{\max,m}^{l} - \text{buffer and } MR_{(x,y,m)}^{l} = 1\right)$$
(12)

where buffer is a parameter accounting for the possible vertical shift in snow line. In order to account for climate variability not represented by the period for which satellite
observations are available, "buffer" was set to 500 m. Due to absence of historical data on snow line variations in the region, the buffer was estimated corresponding to the maximum observed variation in the Equilibrium Line Altitude (ELA) of Abramov Glacier (Table 3, see Fig. 1 for location) for the period 1972–1998 (WGMS 2001; Pertziger 1996), and is, thus, a conservative estimate for the variations in snow line for the study area.



(10)

4.3 Pixel to pixel matching-ratio fields

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In step 1, MRs between each pixel and station were computed, and any pixel that had MR = 1 was classified according to the station record. The idea behind the third step is similar, but MRs between different pixels are computed this time. In such a way, the state of different pixels is used as a predictor for snow cover elsewhere. We define the MR between two pixels with coordinates *x*, *y* and *i*, *j* as:

$$MR_{(i,j),(x,y)}^{s} = \frac{\sum \left(1 - ABS(S_{i,j,t} - S_{x,y,t})\right)}{N_{(i,j)}} \quad \forall \quad S_{x,y,t} = 1$$
$$MR_{(i,j),(x,y)}^{l} = \frac{\sum \left(1 - ABS(S_{i,j,t} - S_{x,y,t})\right)}{N_{(i,j)}} \quad \forall \quad S_{x,y,t} = 0$$

where $S_{i,j,t}$ indicates whether the pixel with coordinates *i*, *j* is snow covered (S = 1) or snow free (S = 0) for a given day *t*, and $N_{(i,j)}$ is the total number of valid observations (clear sky, no cloud) at pixel *i*, *j* simultaneously available for a given condition ($S_{x,y,t} = 1$ or $S_{x,y,t} = 0$) in the period 2000–2012.

The computation of $MR_{(i,j),(x,y)}^{s}$ and $MR_{(i,j),(x,y)}^{l}$ according to Eqs. (13) and (14) is repeated in an "all-vs.-all" procedure, which means that all possible combinations of (x, y)and (i, j) are considered. For the region of interest, this yields at maximum 339552 (2 × total number of pixels) MR maps (i.e. two maps for every pixel: for snow and land condition). However, not all of those maps were used for snow reconstruction since some pixels may have no dependence (no pixels with MR = 1) to any other pixel in the study area and were thus discarded. An example of the MR maps for snow and snow free conditions for the pixel located at x = 100 and y = 100 is given in Fig. 6.

The pixel with coordinates x = 100, y = 100 has $MR_{(i,j),(100,100)}^{s} = 1$ with 30 684 (18%) other pixels in the study area, which means that when the particular pixel was snow covered during 2000–2012, 30 684 other pixels were always snow covered as well. Thus, 18% is the SPI value of that pixel and can be interpreted as predictive



(13)

(14)

power for snow of the pixel for the entire study area. Analogously, 23 770 pixels (14%) have $MR_{(i,j),(100,100)}^{l} = 1$ with this pixel and is LPI value of this pixel. The SPI and LPI values of each pixel are derived through Eqs. (3) and (4) and illustrated in Fig. 7 for all pixels in the study area.

- The maximum value of Fig. 7 (top) is 46%, meaning that, according to the observations of the period 2000–2012, 46% (78 189 pixels) of the study area was always snow covered when that particular pixel was snow covered. The maximum LPI value (Fig. 7 bottom) is 88%, meaning that this particular pixel is able to predict snow free conditions for 88% (149 685 pixels) of the basin. These two pixels with maximum SPI and LPI values are located within an area which has the highest predictive power for snow and land, respectively. When interpreting Fig. 7, three further features are worth notice: (1) pixels with SPI = 0 or LPI = 0 exist as well; these pixels have no predictive power and are therefore not used in the snow cover reconstruction; (2) SPI and LPI maps generally reflect the topography of the catchment: lower elevation pixels have
- higher SPI values and pixels at higher elevations have higher LPI values; (3) snow free pixels are easier to predict than snow covered ones.

The SPI and LPI maps were used for classifying pixels that are still undefined after the previous steps:

$$S_{(i,j,t)} = 1$$
 if $\left(MR_{(i,j),(x,y)}^{s} = 1 \text{ and } S_{(x,y,t)} = 1 \right)$ (15)

²⁰
$$S_{(i,j,t)} = 0$$
 if $\left(\mathsf{MR}^{\mathsf{I}}_{(i,j),(x,y)} = 1 \text{ and } S_{(x,y,t)} = 0 \right)$ (16)

Since in this step SPI and LPI maps were generated for every pixel in the basin, this step tends to classify a significantly larger area than the first step where only 7 stations were used for constructing MRs.



4.4 Snow cover estimation using elevation information from neighbouring pixels

This step is adapted from Gafurov et al. (2009) and is based on the information of neighbouring pixels. Let us consider a pixel that has not been classified as snow cov-

⁵ ered or snow free in any of the previous steps. If any of the adjacent eight pixels is covered by snow and the elevation of that snow-covered pixel is lower than the pixel that is still undefined, then the undefined pixel is classified as snow covered. The same idea is applied for snow-free pixels. Hence, this step can be formalized as follows:

$$S_{(x,y,t)} = 1$$
 if $S_{(x+k,y+k,t)} = 1$ and $H_{(x+k,y+k)} < H_{(x,y)}$ $k \in (-1,1)$ (17)

¹⁰
$$S_{(x,y,t)} = 0$$
 if $S_{(x+k,y+k,t)} = 0$ and $H_{(x+k,y+k)} > H_{(x,y)}$ $k \in (-1,1)$ (18)

4.5 Snow cover estimation with MR < 1

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In the last step, the $MR_{(x,y),(n)}^{s}$ and $MR_{(x,y),(n)}^{l}$ values calculated in step 1 were used again. Whereas in step 1 only relations with MR = 1 were considered, this step considers MR < 1 relations to classify still undefined pixels. As illustrated in Fig. 4, MR values vary from 0 to 1. Such cases were considered in this step: still undefined pixels were classified according to the maximum MR value at this pixel (which however is < 1) among 14 MR values (7 MRs for snow and 7 MRs for land) through Eqs. (19) and (20).

$$S_{(x,y,t)} = 1 \quad \text{if} \quad \max\left(\mathsf{MR}^{\mathsf{s}}_{(x,y,n)} \forall S_{n,t} = 1\right) > \max\left(\mathsf{MR}^{\mathsf{l}}_{(x,y,n)} \forall S_{n,t} = 0\right) \tag{19}$$

²⁰
$$S_{(x,y,t)} = 0$$
 if $\max\left(\mathsf{MR}^{\mathsf{I}}_{(x,y,n)} \forall S_{n,t} = 0\right) > \max\left(\mathsf{MR}^{\mathsf{s}}_{(x,y,n)} \forall S_{n,t} = 1\right)$ (20)

Taking maximum MR values for still undefined pixels in the last step allows to complete the classification for all pixels. However, since in this step MR < 1 was considered, the reconstruction is subject to uncertainty that stems from non-perfect agreement between station records and a pixel in the period 2000–2012.



5 Results and discussion

Applying the five steps described above, snow cover maps for the area containing Zerafshan basin were reconstructed for four days in 1998 and 1999. The maps contain binary information showing whether a given pixel was covered by snow or not. The

accuracy of the reconstructed snow cover maps was assessed by comparing against independent snow maps derived from four Landsat images from the same days. The validation could be done only for recent years (1998 and 1999) due to availability of cloud free Landsat images during the snow period only for those days. The comparison was performed on a pixel-to-pixel basis, and the accuracy was assessed in a contin gency table (Table 4). In Table 4, the sum of percentages of "SS" and "LL" columns represent the degree of accuracy after each reconstruction step, related to the total share of reconstructed pixels. Accordingly, the sum of "SL" and "LS" indicate the error in relation to the total percentage.

As an example, Fig. 8 shows the reconstructed and Landsat-derived snow cover

maps for 10 April 1998. The comparison of these maps results in 86.4% of correct reconstruction (cases SS + LL in Table 4) and 13.6% of erroneous reconstruction (SL + LS). Steps 1–4 show high accuracy with only little erroneous reconstruction (ER) whereas step 5 has the lowest accuracy in all validation days. However, the reconstruction fraction (RF) is very high in step 5 compared to previous steps. Note that ER may
 also be enhanced by erroneous snow cover estimation from raw Landsat data and due to the spatial aggregation of Landsat 30 m original resolution to 500 m.

In order to better illustrate snow reconstruction in step 5, Fig. 9 shows the areal fraction for which the reconstruction was performed in steps 1–4 and maximum MRs obtained in step 5 under MR < 1 condition for the validation day of April, 10. Most of the

still unclassified pixels after steps 1–4 have MR values close to 1 and only few pixels have a lower MR value (reddish and light blue colours in Fig. 9). Figure 10 illustrates the trade-off between RF and ER as a function of MR in step 5. For example, for the validation day of 10 April, ER from steps 1–4 adds up to 1.5% (Table 4) and RF to



51.4 % (snow and land classes in Fig. 9). With decreasing MR, RF increases, but at the cost of an increased ER. However, Fig. 10 also shows that RF is relatively high until about MR = 0.9 with increasing ER. In all four days used for validation, an almost complete reconstruction is achieved with MR > 0.9.

- Figures 8–10 also demonstrate that the methodology provides two types of results for snow cover reconstruction: deterministic and probabilistic snow cover maps. Deterministic maps result from the complete classification of pixels (Fig. 8) with binary information (snow/snow free) taking MR < 1 in step 5 into account at the expense of the overall accuracy. However, the accuracy is still quite high with a range of 83.6–
- 86.4% for the four validation days and is only slightly less than the accuracy of MODIS snow cover product in Central Asia (ca. 92%) when compared to Landsat snow information (Gafurov et al., 2013). Alternatively, probabilistic snow cover maps (Fig. 9) deliver a partial snow cover reconstruction with high accuracy resulting from steps 1–4, and, as result from step 5, a probability statement for snow cover for the remaining pixels.

6 Limitations of the methodology

The predictive power of the observations at meteorological stations for snow cover reconstruction is limited by the elevation range of the stations. If all meteorological stations are located at high elevations, they will be good predictors during summer for snow-free conditions, but will perform poorly when predicting snow-covered areas during winter due to their elevation and correspondingly lower SPI values. Conversely, low-elevation stations are better indicators for snow-covered pixels at higher altitudes than they are for snow-free ones. Hence, a wide spread in station elevation is optimal for accurate snow cover reconstruction. In our case study, the application of the pre-

A higher number of stations would lead to a higher number of SPI and LPI maps and



would allow to reconstruct a larger areal fraction of snow cover in the first four steps. Noticeably, the stations do not need to be located inside the area of interest.

Reconstruction of the snow cover for the past is based on the assumptions that (1) the calibration period, i.e. the MODIS data period, is representative for the past period,

- and (2) the relationship between station records and spatial snow patterns derived from MODIS data is stationary, i.e does not significantly change in time. A calibration period which lacks extreme conditions, e.g. snow-rich or snow-scarce years, might lead to larger errors in the reconstruction. A longer calibration period is expected to lead to more robust relationships for reconstructing snow cover.
- ¹⁰ The problem of representativity of the MODIS period in the reconstruction step 2 is tackled by the introduction of the elevation buffer to capture the effect of interannual temporal variability of snow line elevation. For this the temporal variability of the recorded ELA from the neighbouring Abramov glacier was used as a proxy. Through changes in climatic conditions of the calibration period going beyond temporal variabil-
- ity of the snow line elevation in the reconstruction period, the relationships between station records and some pixels (step 1) and between pixels (step 3) may become non-representative. This occurs if snow line in the future/calibration period more often separates the station of the pixels compared to the reconstruction period. Hence, an analysis of temperature and precipitation trends and comparison of climatology be-
- ²⁰ tween calibration and reconstruction periods may provide some confidence on representativeness of the relationships used.

7 Conclusions

In this study, a methodology for reconstructing past snow cover using historical in situ snow depth data, recent remote sensing snow cover data and topographic data was presented. The methodology is based on (1) constructing relationships between station observations and remote sensing data, (2) estimating the monthly variation of snow cover from remote sensing data, (3) deriving pixel-to-pixel relationships using remote



sensing data, and (4) using neighbourhood relations. Once the dependence between individual pixels and station records is derived, this dependence is used to reconstruct past snow cover based solely on station records.

- The methodology was applied to a study area containing the Zerafshan River basin ⁵ a basin with high topographic gradients – in Central Asia and showed correct classification in the range of 83.6 to 86.4 % when compared to four Landsat snow cover scenes. This high agreement is noteworthy, given that only 7 stations and 12 years of remote sensing data were available. The agreement is only slightly less than of original MODIS snow cover product with accuracy of about 92% for Central Asia when compared to
- Landsat (Gafurov et al., 2013). Just 12 years of MODIS data were sufficient to extract stable patterns of snow cover and relate them to station records. Hence, we conclude that the developed methodology is suitable to derive past snow cover in remote mountainous regions with very limited data availability. Reconstructed snow cover patterns can be used for hydrological model calibration/validation and for understanding snow

cover dynamics over large areas prior the age of satellite observations. 15

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Interactive Discussion

Table 1. Uzhydromet snow observation stations with indication of elevation (Elev), and SPI
(Snow Predictability Index) and LPI (Land Predictability Index) values for the study area (see
Sect. methodology for definitions). The entries "records on snow reconstucted days" indicate
whether a station was snow covered (0) or snow free (1) during a day for which snow cover
reconstruction was conducted and Landsat scenes were available for validation.

Name	Elev	SPI	LPI	Records on snow reconstructed days					
	(m a.s.l)	(%)	(%)	10 Apr 1998	20 Nov 1998	29 Apr 1999	15 Nov 1999		
Dukant	1984	12.4	3.7	1	0	0	1		
Kamchik	2145	10.0	9.1	1	0	0	1		
Kul'	2161	23.2	6.5	0	0	0	1		
Minchukur	2136	22.6	4.2	0	0	0	0		
Oigaing	2187	2.2	12.3	1	1	1	1		
Pskem	1256	2.9	0.8	1	0	0	1		
Chimgan	1677	10.2	9.0	1	0	0	1		



Table 2. Monthly SPI, LPI, $H_{\min,m}^{s}$, and $H_{\max,m}^{l}$ values for the study region.

Month	SPI		LPI			
	Fraction (%)	H_{\min}^{s}	Fraction (%)	$H_{\rm max}^{\rm I}$		
1	10.1	1544	0.0	658		
2	11.4	1164	0.0	2233		
3	24.0	1658	0.4	2923		
4	12.7	2354	14.9	3323		
5	1.1	2900	32.7	3707		
6	0.0	3568	49.5	4387		
7	0.0	5402	66.3	4434		
8	0.0	5402	78.3	4520		
9	0.0	4285	51.2	4330		
10	0.2	3405	25.3	4089		
11	0.9	2750	0.4	2581		
12	8.5	2373	0.0	1707		

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Table 3. ELA records of Abramov Glacier (WGMS, 2001; Pertziger, 1996).

Year	1972	1977	1987	1988	1989	1990	1991	1992	1993	1994	1995	1996	1997	1998
ELA (ma.s.l)	4020	4393	4130	4170	4200	4220	4242	4110	4120	4250	4240	4163	4440	4130

Table 4. Contingency table (in %) for the reconstructed snow cover maps validated against four aggregated Landsat snow cover images. Four cases are distinguished: SS, LL, SL, and LS. The first (second) letter indicates the classification according to the presented algorithm (Landsat). "S" stands for "snow", "L" for "land". "Total" indicates the percentage of pixels classified after each step. Results refer to the Landsat domain (dashed line) shown in Fig. 1b.

Day	Step	SS	LL	SL	LS	Total
10 Apr 1998	1	8.5	7.2	0.0	0.0	15.7
	2	13.0	14.9	0.1	0.1	28.1
	3	17.5	27.1	0.8	0.1	45.5
	4	20.6	29.3	1.3	0.2	51.4
	5	44.3	42.1	11.6	2.0	100.0
20 Nov 1998	1	0.1	11.2	0.0	0.0	11.3
	2	0.2	11.3	0.0	0.0	11.5
	3	0.5	30.5	0.0	0.0	31.0
	4	1.4	33.4	0.0	0.1	34.9
	5	18.2	66.6	2.1	13.1	100.0
29 Apr 1999	1	0.1	13.9	0.0	0.0	14.0
	2	7.6	21.5	0.0	0.5	29.6
	3	9.0	35.2	0.1	0.7	45.0
	4	11.0	38.1	0.3	0.9	50.3
	5	24.9	58.7	13.9	2.5	100.0
15 Nov 1999	1	18.4	4.1	0.0	0.4	22.9
	2	18.4	4.2	0.0	0.4	23.0
	3	24.8	15.7	0.4	0.8	41.7
	4	28.5	18.3	0.7	1.3	48.9
	5	42.3	41.7	10.6	5.4	100.0

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Figure 1. Location of the Upper Zerafshan River basin in the Gissaro-Alai Mountain Range, Central Asia. Snow cover reconstruction was conducted for the entire area of **(b)** and validated for the area with Landsat footprint.











Figure 3. Original Landsat scenes (top row) and derived snow cover maps used for validation (bottom row). See Fig. 1a for areal coverage of Landsat footprint.









Figure 5. Temporally persistent spatial snow ($MP^s = 1$) and land ($MP^l = 1$) patterns for April in the study area shown in Fig. 1b. Pixels with "undef" indicate $MP^s < 1$ or $MP^l < 1$, for which classification is not possible in this step.









Figure 7. SPI (top) and LPI (bottom) values of each pixel (in %) in the study area defined in Fig. 1b.



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Figure 8. Reconstructed (top) and Landsat (bottom) snow cover maps for 10 April 1998.



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Figure 10. Trade-off between erroneous reconstruction (ER, dashed lines) and reconstruction fraction (RF, solid lines) after step 4 as a function of MR.

