

1 Simultaneous solution for mass trends on the West Antarctic Ice Sheet

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3 N.Schoen¹, A. Zammit-Mangion^{1,2}, J. C. Rougier², T. Flament³, F. Rémy⁴, S. Luthcke⁵, J. L.
4 Bamber¹

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6 [1] {Bristol Glaciology Centre, School of Geographical Sciences, University of Bristol, UK}

7 [2] {Department of Mathematics, University of Bristol, UK}

8 [3] {School of Earth and Environment, University of Leeds, UK}

9 [4] {LEGOS, Toulouse, France}

10 [5] {NASA, Greenbelt, MD, USA}

11 Correspondence to: Jonathan Bamber (j.bamber@bristol.ac.uk)

12 13 Abstract

14 The Antarctic Ice Sheet is the largest potential source of future sea-level rise. Mass loss has been
15 increasing over the last two decades for the West Antarctic Ice Sheet (WAIS), but with significant
16 discrepancies between estimates, especially for the Antarctic Peninsula. Most of these estimates
17 utilise geophysical models to explicitly correct the observations for (unobserved) processes.
18 Systematic errors in these models introduce biases in the results which are difficult to quantify. In
19 this study, we provide a statistically rigorous, error-bounded trend estimate of ice mass loss over
20 the WAIS from 2003–2009 which is almost entirely data-driven. Using altimetry, gravimetry, and
21 GPS data in a hierarchical Bayesian framework, we derive spatial fields for ice mass change,
22 surface mass balance, and glacial isostatic adjustment (GIA) without relying explicitly on forward
23 models. The approach we use separates mass and height change contributions from different
24 processes, reproducing spatial features found in, for example, regional climate and GIA forward
25 models, and provides an independent estimate, which can be used to validate and test the models.
26 In addition, spatial error estimates are derived for each field. The mass loss estimates we obtain
27 are smaller than some recent results, with a time-averaged mean rate of -76 ± 15 Gt/yr for the
28 WAIS and Antarctic Peninsula (AP), including the major Antarctic Islands. The GIA estimate
29 compares well with results obtained from recent forward models (IJ05-R2) and inverse methods
30 (AGE-1). The Bayesian framework is sufficiently flexible that it can, eventually, be used for the
31 whole of Antarctica, can be adapted for other ice sheets and can utilise data from other sources
32 such as ice cores, accumulation radar data and other measurements that contain information about
33 any of the processes that are solved for.

34 1 Introduction

35 Changes in mass balance of the Antarctic ice sheet have profound implications on sea level. While
36 there is a general consensus that West Antarctica has experienced ice loss over the past two
37 decades, the range of mass-balance estimates still differ significantly (compare, for example,
38 estimates in Shepherd et al. (2012), Tables S8 and S11 which range from -84 ± 18 for GRACE to -

39 13 ± 39 Gt yr⁻¹ for ICESat for the WAIS and from -24 ± 35 to 123 ± 60 for the East Antarctic Ice
40 Sheet). Reconciling these disparate estimates is an important problem. Previous studies have made
41 use of satellite altimetry (Zwally et al., 2005), satellite gravimetry (Chen et al., 2006; King et al.,
42 2012; Sasgen et al. 2013; Luthcke et al., 2013), or a combination of satellite and airborne data and
43 climate model simulations (Rignot et al., 2011b) to provide estimates. In the latter case, the
44 balance is found by deducting output ice flux from input snowfall in a technique sometimes
45 referred to as the Input-Output Method (IOM) or mass budget method.

46 Different approaches have different sources of error. A key error in the gravimetry-based
47 estimates is a result of incomplete knowledge on glacial isostatic adjustment (GIA), which
48 constitutes a significant proportion of the mass-change signal but leakage and GRACE errors are
49 also important (Horwath and Dietrich, 2009). For satellite altimetry, uncertainties arise from
50 incomplete knowledge of the temporal variability in precipitation (Lenaerts et al., 2012; Frezzotti
51 et al., 2012), and the compaction rates of firn (Arthern et al., 2010, Ligtenberg et al., 2011):
52 quantities which play a central rôle in determining the density of the observed volume change. For
53 the IOM, the main sources of error stem from the surface mass balance (SMB) estimates used
54 (usually obtained from a regional climate model), and uncertainties in ice discharge across the
55 grounding line. Recent improvements in regional climate modelling have reduced the uncertainty
56 in the SMB component but differences between estimates for the Antarctic ice sheet as a whole
57 still exceed recent estimates of its mass imbalance. For example, a recent update of the
58 commonly used regional climate model, RACMO, has resulted in a change in the integrated ice
59 sheet-wide SMB of about 105 Gt yr⁻¹ (Van Wessem et al, 2014), which is larger than most recent
60 estimates of the ice sheet imbalance. This change in SMB, directly impacts the IOM estimate by
61 the same amount. It is these hard-to-constrain biases in the forward models, such as the one just
62 described, that has, in part, motivated our approach.

63 In an attempt to reduce the dependency on forward models, recent studies have combined
64 altimetry and GRACE to obtain a data-driven estimate of GIA and ice loss simultaneously (Riva
65 et al., 2009; Gunter et al., 2013). Here, we extend these earlier approaches in a number of ways.
66 We provide a model-independent estimate not only of GIA, but also of the SMB variations, firn
67 compaction rates and of the mass loss/gain due to ice dynamics (henceforward simply referred to
68 as ice dynamics). In doing so, we eliminate the dependency of the solution on solid-Earth and
69 climate models. The trends for ice dynamics, SMB, GIA, and firn compaction are obtained
70 independently through simultaneous inference in a hierarchical statistical framework (Zammit-
71 Mangion et al., 2014). The climate and firn compaction forward models are used solely to provide
72 prior information about the spatial smoothness of the SMB-related processes. Systematic biases in
73 the models have, therefore, minimal impact on the solutions. In addition, we employ GPS bedrock
74 uplift rates to further constrain the GIA signal. In future work the GPS data will also be used to
75 constrain localised ice mass trends that cause an instantaneous elastic response of the lithosphere
76 (Thomas and King (2011)). The statistical framework uses expert knowledge about smoothness
77 properties of the different processes observed (i.e. their spatial and temporal variability) and
78 provides statistically sound regional error estimates that take into account the uncertainties in the
79 different observation techniques (Zammit-Mangion et al. 2014). The study reported here was
80 performed as a proof-of-concept for a time-evolving version of the framework for the whole

81 Antarctic ice sheet, which is currently under development. The time-evolving solution will use
 82 updated data sets and, as explained above, will also solve for the elastic signal in the GPS data. In
 83 addition, it will provide improved separation of the processes because of the additional
 84 information related to temporal smoothness that can be incorporated into the framework
 85 (discussed further in section 5).

86

87 **2 Data**

88 In this section we describe the data employed, which is divided into two groups. The first group
 89 contains observational data which play a direct rôle in constraining the mass trend. These include
 90 satellite altimetry, satellite gravimetry and GPS data (Sections 2.1–2.3). The second group
 91 comprises auxiliary data (both observational and information extracted from geophysical models),
 92 which we use to help with the signal separation (differentiating between the different processes
 93 we solve for accounting for their spatial smoothness) (Zammit-Mangion et al. 2014). These are
 94 discussed in Section 2.4.

95 **2.1 Altimetry**

96 We make use of two altimetry data sets in this study, obtained from the Ice, Cloud and land
 97 Elevation Satellite (ICESat) and the Environment Satellite (Envisat). In this study, we used
 98 ICESat elevation rates (dh/dt) based on release 33 data from February 2003 until October 2009
 99 (Zwally et al., 2011). The data includes the “86S” inter-campaign bias correction presented in
 100 Hofton et al., 2013) and the centroid Gaussian correction (Borsa et al., 2013) made available by
 101 the National Snow and Ice Data Centre. Pre-processing was carried out as described in Sørensen
 102 et al., (2011). Since ICESat tracks do not precisely overlap, a regression approach was used for
 103 trend extraction, in which both spatial slope (both across-track and along-track) and temporal
 104 slope (dh/dt) were simultaneously estimated (Howat et al., 2008; Moholdt et al., 2010). A
 105 regression was only performed if the area under consideration, typically 700m long and a few
 106 hundred metres wide, had at least 10 points from four different tracks that span at least a year.
 107 Regression was carried out twice, first to detect outliers (data points which lay outside the 2σ
 108 confidence interval), and second to provide a trend estimate following outlier omission. The
 109 standard error on the regression coefficient (in this case dh/dt), SE_{coef} , was calculated through:

$$110 \quad SE_{coef} = \frac{1}{\sqrt{n-2}} \sqrt{\frac{\sum_i e_i^2}{\sum_i (x_i - \bar{x})^2}} \quad (1)$$

111 where $e = [e_i]$ is the vector of residuals, n is the sample size, and $x = [x_i]$ is the input with mean \bar{x}
 112 (Yan (2009)). It should be noted that this standard error is not equivalent to the measurement error,
 113 but takes into account sample size, as well as the variance of both input data and residuals of the
 114 regression. Only elevation changes with an associated standard error on dh/dt of less than 0.40 m
 115 yr^{-1} were considered. This threshold was selected by trial and error to avoid a noisy spatial pattern
 116 of points that are close together and opposite in sign, usually because the regression is based on a
 117 small subset of overpasses. Data above the latitude limit of 86°S were omitted. The remaining
 118 data were gridded on a polar-stereographic projection (central latitude 71°S ; central longitude

119 0°W, and origin at the South Pole), at a 1 km resolution and then averaged over a 20km grid. The
120 a-priori error used in the modelling framework was then the standard deviation of the trends
121 within each 20km grid box. The Envisat mission data began in September 2002 and ended in
122 April 2012. Compared to laser altimetry, radar altimetry is, in general, less suited for
123 measurements over ice for several well-known reasons: the large spatial footprint, the relatively
124 poor performance in steeper-sloping marginal areas (Thomas et al., 2008), and the variable snow-
125 pack radar penetration (Davis, 1996). On the other hand Envisat data exhibit better temporal and
126 spatial coverage over much of the WAIS, primarily because of the instrument issues associated
127 with ICESat that resulted in a shorter repeat cycle and less frequent operation than originally
128 planned. We use along-track dh/dt trends, which were obtained by binning all points within a
129 500m radius and then fitting a 10-parameter least-squares model in order to simultaneously
130 correct for across-track topography, changes in snowpack properties and dh/dt (Flament et al.,
131 2012). The re-trended residuals were then used to obtain linear trends over the 2003–2009 ICESat
132 period for our study. As with ICESat, the data were averaged over a 20km grid and the standard
133 deviation of the trends were used as the error at this scale.

134 **2.2 GRACE**

135 The Gravity Recovery and Climate Experiment (GRACE, Tapley et al., 2005) has provided
136 temporally continuous gravity field data since 2002. Different methods have been used to provide
137 mass change anomalies from the Level 1 data. Most are based on the expansion of the Earth's
138 gravity field into spherical harmonics; but to make the data usable for ice mass change estimates,
139 it is generally necessary to employ further processing methods. These include the use of averaging
140 kernels (Velicogna et al., 2006), inverse modelling (Wouters et al., 2008), Sasgen et al., 2013),
141 and mass concentration (mascon) approaches (Luthcke et al., 2008). Spherical harmonic solutions
142 usually depend on filtering to remove stripes caused by correlated errors (Kusche et al., 2009),
143 Werth et al., 2009).

144 In this paper, we used a mascon approach (Luthcke et al., 2013), although we stress that the
145 framework is not limited to this class of solutions. The mascon approach employed here uses the
146 GRACE K-band inter-satellite range-rate (KBRR) data which are then binned and regularized
147 using smoothness constraints. The release 4 (RL4) Atmosphere/ Ocean model correction, which
148 utilizes the European Centre for Medium-Range Weather Forecasts atmospheric data and the
149 Ocean Model for Circulation and Tides (OMCT), was used (Dobslaw and Thomas (2007). Some
150 concerns with this correction have been reported (Barletta et al., 2012), but a release of the
151 mascon data using the corrected version (Dobslaw et al., 2013) was not available for this study.
152 Contributions to degree-one coefficients were provided using the approach by Swenson et al.,
153 2008). Our mascon approach does not call for a replacement of C20 coefficients. We assume that
154 GRACE does not observe SMB or ice mass changes over the floating ice shelves as they are in
155 hydrostatic equilibrium. Hence, all observed gravity changes over the ice shelves are assumed to
156 be caused by GIA.

157 Although the mascons are provided at a resolution of about 110km, their fundamental resolution is
158 nearer that of the original KBRR data at about 300km (Luthcke et al., 2013). For the statistical
159 framework, it is important to quantify the correlation among the mascons so that it is taken into

160 account when inferring both the processes and associated *posterior* uncertainties. We quantify the
161 spatial correlation by determining an averaging model such that the diffused signal is able to
162 loosely reconstruct the mass loss obtained using only altimetry (and assuming that all height
163 change occurs at the density of ice). The averaging strength between mascon neighbours is also
164 estimated during the inference (Zammit-Mangion et al., 2014). The error on the mascon rates is
165 assumed to be a factor of the regression residuals on the trends, in a similar manner to the
166 altimeter data (Zammit-Mangion et al. 2014). The *a-priori* errors, after these two steps, are shown
167 in Figure 1, which also indicates the length-scale over which we estimated the GRACE mascons
168 to be uncorrelated.

169 **2.3 GPS**

170 The GPS trends used in this work were taken from Thomas and King (2011). Not all of the trends
171 were suitable for our analysis, as the length of record did not always coincide with the 2003–2009
172 ICESat period. We only used stations with contemporaneous data, as well as those where we
173 could access the original time series to confirm that the trend had remained constant, within the
174 error bounds, for our observation period. For the Northern Antarctic Peninsula, we followed the
175 approach suggested in Thomas and King (2011) and used the pre-2003 trends, ignoring the later
176 trend estimates, which are strongly influenced by elastic signals. All other stations were corrected
177 for elastic rebound as in Thomas & King (2011) and subsequently assumed to be measuring GIA
178 only (the published rates were used). A more advanced approach where the estimated ice loss is
179 fed back into a dynamic estimate of the elastic rebound, is being implemented for a
180 spatiotemporal extension of the Bayesian framework. The GPS data used in this study are
181 detailed in Table 1.

182 **2.4 Additional data sets**

183 **RACMO.** Elements of the Regional Atmospheric Climate Model version 2.1 (RACMO, Lenaerts
184 et al., 2012) were used to constrain SMB properties. Spatially-varying length scales describing the
185 spatial smoothness of precipitation patterns were obtained from the 2003–2009 SMB anomalies
186 (with respect to the 1979–2002 mean). These ranged from 80km in the Antarctic Peninsula to
187 200km east of Pine Island Glacier. The amplitude of the anomalies, which peaked at 50 mm water
188 equivalent in the Antarctic Peninsula, was used to provide an order of magnitude annual
189 amplitude for expected regional SMB variability (Zammit-Mangion et al., 2014). RACMO2.1 also
190 provides a surface density map: the mean annual density of the surface layer. This was used to
191 translate height changes corresponding to the SMB field to mass changes.

192 **Firn correction.** We used the firn correction anomalies for 2003–2009 (with respect to the 1979–
193 2002 mean) from a firn compaction model (Ligtenberg et al., 2011). These anomalies were used
194 to estimate, empirically, the correlation between firn compaction rate and SMB. This relationship
195 was then subsequently used to determine jointly the SMB and firn correction processes, subject to
196 the constraint that firn compaction is a linear function of SMB (supported by the high correlation
197 between the respective 2003–2009 trends). The methodology automatically takes into account
198 inflated uncertainties due to confounding of these two processes since they have identical length
199 scales (Zammit-Mangion et al. 2014).

200 **Ice Velocities.** We use surface ice velocities derived from Interferometric Synthetic Aperture
201 Radar data (Rignot et al., 2011a). In places where no observational data were available, estimated
202 balance velocities were used (Bamber et al., 2000). This composite velocity field was employed to
203 help in the separation of signals due ice dynamics versus those due to SMB (Section 3).

204 **3 Methodology**

205 Our framework makes use of several recent improvements in statistical modelling which can be
206 exploited for geophysical purposes. Complete details regarding the mathematical methods
207 employed are given in Zammit-Mangion et al., (2014) and here, we provide a conceptual
208 overview of the approach. A description of the software implementation can also be found in
209 Zammit et al, (2015). The statistical framework hinges on the use of a hierarchical model where
210 the hierarchy consists of three layers: the observation layer (which describes the relation of the
211 observations to the measured fields), the process layer (which contains prior beliefs of the fields
212 using auxiliary data sets) and the parameter layer (where prior beliefs over unknown parameters
213 are described).

214 The ‘observation model’ is the probabilistic relationship between the observed values and the
215 height change of the each of the processes. For point-wise observations, such as altimetry and
216 GPS, the observations were assumed to be measuring the height trend at a specific location.
217 GRACE mascons, on the other hand, were assumed to represent integrated mass change over a
218 given area. These mass changes were translated into height changes via density assumptions:
219 upper mantle density was fixed at 3800 kg m^{-3} ; ice density at 917 kg m^{-3} , and SMB at values
220 ranging from $350\text{-}600 \text{ kg m}^{-3}$. Note that we used the density map from a regional climate model to
221 specify the density of the surface layer.

222 In the ‘process model’ four fields (or latent processes) are modelled: ice dynamics, SMB, GIA,
223 and a field which combines the processes which result in height changes, but no mass changes:
224 firm compaction and elastic rebound. We model the height changes due to these as spatial
225 Gaussian processes, i.e. we assume that they can be fully characterised by a mean function and a
226 covariance function. For each field we assume that the mean function is zero (we do not use
227 numerical models to inform the overall mean) and that the covariance function, which describes
228 how points in space covary, is highly informed by numerical models and expert knowledge as
229 described next. The relationship between the observations, priors and the latent process, defined
230 by the process model is shown schematically in Figure 2. Those processes that are influenced by
231 an observation are linked by a solid arrow and it is evident that the problem is underdetermined as
232 there are less independent observations than there are latent processes. This is why the use of
233 priors is important to improve source separation (i.e. for partitioning elevation change between the
234 four latent processes shown in Figure 2). It should also be noted that SMB and firm compaction
235 have been assumed, in this implementation of the framework, to covary *a priori*, as discussed
236 later.

237 The practical spatial range of surface processes – this describes the distance beyond which the
238 correlation drops to under 10% – was estimated from RACMO2.1 as described in Section 2.4.
239 This analysis revealed, for example, that locations at 100km are virtually uncorrelated in the

240 Antarctic Peninsula, but highly correlated inland from Thwaites Glacier. Similarly GIA was found
 241 to have a large practical range (~ 3000 km), from an analysis of the IJ05-R1 model (although
 242 version R2 is used for comparison in the results and discussion) (Ivins et al., 2013). These length
 243 scales impose soft constraints on the possible class of solutions for the individual fields. They are
 244 useful for helping to partition a height change between the different processes that can cause that
 245 change. For example, a long wavelength variation in height that spans different basins is likely
 246 associated with SMB, whereas a localised change that shows some relationship to surface velocity
 247 is likely associated with ice dynamics (Hurkmans et al., 2014). Hence, mass loss due to ice
 248 dynamics was assumed to mostly take place in areas of faster flow (Hurkmans et al., 2014). A
 249 “soft” constraint was thus placed on elevation rates due to ice dynamics such that it is small (1mm
 250 yr^{-1}) in areas of low velocities and can be large (up to 15m yr^{-1}) for velocities greater than 10m yr^{-1}
 251 ¹. A sigmoid function was used to describe this soft constraint:

$$252 \quad \sigma_{vel}(s) = \frac{15}{1 + \exp(-(v(s) - 10))} \quad (2)$$

253 where $v(s)$ denotes the horizontal velocity at location s . For illustration of how $\sigma_{vel}(s)$ is used, an
 254 altimetry elevation trend of 10 m yr^{-1} in Pine Island Glacier where velocities exceed 4 km yr^{-1} is
 255 within the $1\sigma_{vel}$ interval and thus classified as “probable”. On the other hand, a 10 m yr^{-1} trend in
 256 a region east of Thwaites, where velocities are 2 m yr^{-1} , would lie within the $2000\sigma_{vel}$ level and
 257 thus assumed to be a virtually impossible occurrence *a priori*. At Kamb Ice Stream, this
 258 assumption had to be relaxed as this area shows thickening from the shutdown of the ice stream
 259 about 150 years ago (Retzlaff and Bentley, 1993). Although the velocity of the ice is low, the
 260 thickening occurs at relatively high rates. To reflect this, we fix $\sigma_{vel}(s) = 2 \text{ m yr}^{-1}$ in this
 261 drainage basin. In Table 2, we outline the key length-scale and amplitude constraints placed on the
 262 fields that are solved for in the framework. These soft constraints should be seen as ones
 263 characterising the solution in the absence of strong evidence to anything else. They can be
 264 ‘violated’ if the data is sufficiently informative. In the Discussion we examine the sensitivity of
 265 the solution to these constraints.

266 Length scales and prior soft constraints are easily defined for Gaussian processes (or Gaussian
 267 fields) which, on the other hand, are also computationally challenging to use. Gaussian fields can
 268 however be re-expressed as Gaussian Markov Random Fields (GMRF) by recognising that
 269 Gaussian fields are in fact solutions to a class of Stochastic Partial Differential Equations (SPDEs,
 270 Lindgren et al., 2011). Numerical methods for partial differential equations, namely, finite
 271 element (FE) methods, can thus be applied to the SPDEs in order to obtain a computationally
 272 efficient formulation of a complex statistical problem (Zammit-Mangion et al., 2014). Spatially
 273 varying triangulations (meshes) are used for the different processes reflecting the assumption that,
 274 for example, ice loss is more likely to occur at smaller scales near the margins of the ice sheet
 275 where fast, narrow ice streams are prevalent, than in the interior. We thus use a fine mesh at the
 276 margins (25km) and a coarse mesh in the interior for this field. GIA on the other hand is assumed
 277 to be smooth. This allows us to use a relatively coarse mesh for this process ($\sim 100\text{km}$).

278 We note that our methodology differs from others in that it is not an unweighted average of
 279 estimates with markedly different errors (Shepherd et al., 2012) or a sum of corrected data sources

280 (Riva et al., 2009), but a process-based estimate. For each of the four fields (noting that elastic
281 rebound and firn compaction covary in this implementation), we infer a probability distribution
282 and standard deviation for every point in space. By relating pre-inference and post-inference
283 variances, it is possible to assess the influence of different kinds of observation at each point on
284 the resulting fields.

285 **4 Results**

286 Inferential results are available for the four processes shown in Figure 2 in isolation. In this
287 section we report the results for each of the processes in turn, but emphasise that these are
288 presented to demonstrate the methodology rather than provide final estimates. This is because, as
289 stated in section 2, improvements are planned both to the framework and the data sets that we use
290 in it. In all the examples shown, green stippling indicates where the signal is greater than the
291 marginal standard deviation.

292 **Ice dynamics.** We obtain an ice dynamics imbalance of $-86.25 \pm 16.12 \text{ Gt yr}^{-1}$. The results for ice
293 dynamics (Fig. 3) are consistent with prior knowledge of disequilibria in ice flow in the West
294 Antarctic Ice Sheet (WAIS), for example, the ice build-up in the Kamb Ice Stream catchment
295 (Retzlaff and Bentley, 1993) and the drawdown in the Amundsen Sea Embayment (Flament et
296 al., 2012). The strength of the approach is apparent when focusing on the Antarctic Peninsula.
297 Due to the relatively narrow, steep terrain, and northern latitude (which affects the across track
298 spacing of the altimetry) satellite altimeter data are sparse, while GRACE data are influenced by
299 leakage effects, making it challenging to localise the mass sources and sinks. We find that the
300 framework places ice loss maxima at the outlets of several glaciers and ice streams, which are
301 known to have accelerated (De Angelis and Skvarca, 2003). The result is a high-resolution map of
302 ice mass loss or gain that can be linked to specific catchments. Strong ice loss can be observed on
303 the Northern Peninsula at the Weddell Sea shore, at the former tributaries of the Larsen B ice
304 shelf. The maximum ice loss rate is found in the area around Sjögren Glacier at -4.7 m yr^{-1} .
305 Neighbouring Röhss Glacier, on James Ross Island, has been thinning considerably since the
306 break-up of the Prince Gustav Ice Shelf (Glasser et al. 2011, Davies et al. 2011). This is also
307 reflected in high loss rates. Hektoria and Evans, Gregory Glacier, and glaciers the Philippi Rise
308 also show strong ice mass loss signals, most likely as a result of the collapse of the Larsen B ice
309 shelf (Scambos et al., 2004; Berthier et al., 2012). Other ice loss maxima are found in the region
310 of the Wordie Ice Shelf, Marguerite Bay, and Loubet Coast, which corroborates findings from
311 USGS/BAS and ASTER airborne stereo imagery analyses (Kunz et al., 2012). Ice loss is also
312 observed on King George Island, which is in agreement with recent analyses of satellite SAR data
313 (Osmanoğlu et al., 2013), and on Joinville Island.

314 The gap in altimeter data around the pole results in spurious estimates for that region and the
315 black shaded area, south of 86° , in Fig. 3a is not considered here. As expected, the marginal
316 standard deviation, or error estimate, (Fig. 3b) is lowest in the interior of the WAIS, where
317 sampling density by altimetry is high, and highest on the Peninsula, where data are sparse. Also,
318 steep coastal areas show larger errors, reflecting the dependency of altimeter errors on slope (see
319 Bamber et al., 2005 or Brenner et al., 2007).

320 **SMB and firn compaction.** We obtain an SMB imbalance of $10.57 \pm 4.98 \text{ Gt yr}^{-1}$. Fig. 4a shows
321 the trend of the cumulative SMB anomalies according to RACMO 2.1, calculated with respect to
322 the 1979–2010 mean. This approximately corresponds to the signal we are estimating, since we
323 are only considering trends with respect to a steady state SMB. A cursory inspection of the
324 anomalies we obtain (Fig 4b) with those from RACMO2.1 suggests relatively poor agreement. It
325 should be noted, however, that the anomalies over the seven year interval are on the order of a few
326 centimetres a year and only a limited area has a statistically significant trend in our inversion
327 (stippled regions in Fig 4b). There is a difference in sign between the model and our inversion for
328 the Northern Antarctic Peninsula but again, the rates we obtain are below a significant threshold
329 and the Peninsula possesses larger uncertainties than other areas for both our framework and the
330 regional climate model. We compare our results with ice core trends from Medley et al. (2013)
331 who conclude that, while in phase, RACMO2.1 appears to show exaggerated inter-annual
332 variability in the Amundsen Sea Sector. The ice core trend labeled ‘MEDLEY’ in Fig. 4 is the
333 mean of three cores PIG2010, THWAITES2010, and DIV2010 collected in 2010 and the location
334 is, consequently, the mean coordinates for all the cores. The trends at the single ice cores were not
335 listed, but there appears to be qualitative agreement with our negative trend in the area. Burgener
336 et al. (2013) also provide new ice core records for the Amundsen Sea sector (Satellite Era
337 Accumulation Traverse, SEAT) and Fig. 4 also shows a comparison with their data. Trends were
338 taken over the full 2003–2009 period relative to a mean for 1980–2009. The agreement is good for
339 three out of five cores published. Following Burgener et al. (2013), we exclude SEAT 10-4
340 because of the high noise level in the isotope dating and surface undulations. SEAT10-5 shows a
341 relatively strong negative trend that we do not reproduce. SEAT-01, SEAT-03, and SEAT-06
342 agree well with our results at the $\pm \text{ cm yr}^{-1}$ level. We note, however, that there is substantial short-
343 wavelength spatial variability in SMB based on the ice core data, which is below the resolution of
344 our framework. This also suggests that a single ice core measurement should be treated with
345 caution in this type of comparison.

346 Height changes from firn compaction and elastic rebound are estimated together in a single field.
347 Because they take place on similar length scales, and there is no temporal evolution in our time-
348 invariant solution presented here, they are confounded in this study. Since firn compaction occurs
349 at relatively large rates (cm a^{-1}), we cannot make any useful inferences about elastic rebound rates.
350 This issue will be less critical in the time-evolving version of the framework. The modelled
351 inverse correlation between firn compaction and SMB (Section 2.4) is visible in the results (Fig.
352 4b and Fig. 5).

353 **GIA.** We obtain a GIA rate that is equivalent to a mass trend of $12.34 \pm 4.32 \text{ Gt/yr}$. It is difficult
354 to compare this directly with other published results because the domain is not the same. We can,
355 however, examine individual basins. The GIA vertical velocities estimated by our framework are
356 lower than some older forward model solutions (e.g. Peltier (2004), Ivins and James (2005)). Our
357 results, however, agree well with a recent GRACE-derived estimate, AGE-1, which also assumes
358 that over the ice shelves, GIA is the sole process causing observed mass change (Sasgen et al.,
359 2013). Compared with AGE-I, our maxima in vertical uplift are shifted towards the open ocean
360 for both of the major ice shelves (Fig. 6a). Agreement with the trends at most GPS stations is
361 reasonable; however, the imposed smoothness constraints have a larger influence. The W06A

362 station (Table 1), which has a strong negative trend with a large error, exacerbated by a large
363 elastic signal, stands out. Thomas and King (2011) show that its rate does not fit with any of the
364 GIA models used in their comparison. The signal is effectively ignored in our framework due to
365 the large spatial scale assumed for the GIA process. Fig. 6b shows the standard deviation of our
366 GIA estimate and it is evident that, where robust GPS data exist, the errors are substantially
367 reduced locally. Comparing our results, basin by basin, with other recent GIA estimates including
368 two forward models (W12a (Whitehouse et al., 2012) and IJ05-R2 (Ivins et al., 2013)) and two
369 data-driven solutions (Gunter et al. (2013) and AGE-1 (Sasgen et al., 2013)) we find that we have,
370 in general, best agreement with AGE-1. Basin definitions are shown in Fig. 11. Both Gunter13
371 and AGE-1 rely on GRACE data. W12a, while a forward model, was adjusted to better match
372 GPS uplift rates on the Peninsula. For the Filchner Ronne Ice Shelf (basin 1), the AGE-1 estimate
373 (2.1 mm yr^{-1}) is slightly lower than ours (2.7 mm yr^{-1}), while IJ05-2 is slightly higher (3.5 mm yr^{-1}).
374 W12a (7.2 mm yr^{-1}) shows more than twice our rate in this area, while Gunter13 (4.2 mm yr^{-1})
375 lies between IJ05-R2 and W12a. At the Ross Ice Shelf (basin 18), the agreement with AGE-1 and
376 IJ05-R2 (both 1.9 mm yr^{-1} , RATES 2.0 mm yr^{-1}) is very close. Gunter13 (3.1 mm yr^{-1}) and W12a
377 (3.4 mm yr^{-1}) are slightly higher. For basin 19, again the agreement with AGE-1 and IJ05-R2 is
378 close with RATES at 2 mm yr^{-1} , AGE-1 at 1.7 mm yr^{-1} and IJ05-R2 at (1.9 mm yr^{-1}).

379 Basin 23, which connects the ASE to the Southern Peninsula, also yields a small uplift rate
380 (0.4 mm yr^{-1}). AGE-1 (0.5 mm yr^{-1}) lies within the error estimate, with IJ05-R2 (1.7 mm yr^{-1}) and
381 Gunter13 (2.0 mm yr^{-1}) just outside, and W12a considerably higher at 5 mm yr^{-1} . On the Southern
382 Peninsula (basin 24), agreement with AGE-1 (1.2 mm yr^{-1} , RATES 1.3 mm yr^{-1}) is very good, but
383 W12a is close (1.8 mm yr^{-1}). Gunter13 and IJ05 both show uplift on the Southern Peninsula, but at
384 a higher rate of 2.4 mm yr^{-1} and 3.1 mm yr^{-1} , respectively. On the Northern Peninsula, again the
385 agreement is best with AGE-1 (0.8 mm yr^{-1} , RATES 0.7 mm yr^{-1}), followed by IJ05-R2 (0.5 mm
386 yr^{-1}). The W12a rate is higher at 1.7 mm yr^{-1} . Gunter13 is the only model that shows a negative
387 GIA trend (-0.70 mm yr^{-1}) in this region. This comparison is designed to be illustrative rather than
388 definitive as our final GIA solution from the time-evolving framework for the whole of Antarctica
389 will contain several improvements related to both the data and the methodology. Specifically, we
390 will have improved and extended GPS time series and coverage, a new GRACE mascon solution,
391 will solve directly for elastic deformation and will include a spatially varying length scale.

392 **5 Discussion**

393 In Fig. 8 and Table 3 we present the basin-scale combined ice and SMB mass balance in
394 comparison with two recent studies using GRACE (King et al., 2012; Sasgen et al., 2013). The
395 latter study spans the ICESat period and the rates were taken from the publication. The former
396 study, however, spans the 2002–2010 period. Basin definitions are the same as those in Sasgen et
397 al. (2013) but differ from King et al. (2012): the sum of our basins 1 and 24 match the sum of their
398 basins 1, 24 and 27. Our basin 25 matches the sum of their basins 25 and 26. Consequently,
399 comparisons for these basins are not shown in Fig. 8 but provided in Table 3.

400 Overall, we obtain good agreement with Sasgen et al. (2013). Our mean, time-averaged ice loss
401 rate of $-76 \pm 15 \text{ Gt yr}^{-1}$, deviates by less than one standard deviation from the value of $-87 \pm 10 \text{ Gt}$
402 yr^{-1} obtained by Sasgen et al. (2013). Agreement at the basin scale is also good. For Basin 18, our

403 error estimates are inflated because of the pole gap in the altimetry data. The largest differences
404 occur in basins 19, 20 and 23. For 19 and 20, agreement is very good when comparing the sums of
405 the two adjacent basins – suggesting that leakage effects might be affecting the ability of a
406 GRACE-only solution to fully isolate the signal to each basin. For basin 23, the altimetry – both
407 Envisat and ICESat – show a clear positive trend in this area (ICESat: $+4 \text{ Gt yr}^{-1}$), with only very
408 localized ice loss signals on Ferrigno ice stream. This positive trend (as opposed to a negative
409 trend from GRACE) reduces the ice loss estimate and causes the difference between the two
410 estimates. The strong GRACE mass loss signal for the Amundsen Sea sector leads to increased
411 leakage in the coastal basins. The King et al. (2012) result shows basins 23 and 21 are strongly
412 correlated at $p=0.96$. When comparing the sum over the coastal basins 21, 22, and 23, the
413 difference between the Sasgen et al. (2013) estimate (-80 Gt yr^{-1}) and ours (-74 Gt yr^{-1}) reduces to
414 6 Gt yr^{-1} .

415 We also compare our basin scale results to ice loss rates from King et al. (2012). Here, the
416 observation periods are not identical, and the GIA estimates differ. Still, there is generally good
417 agreement at the basin-scale, in particular, where their GIA estimates (Whitehouse et al., 2012) lie
418 within our error ranges (basins 18, 19) and worst where their GIA uplift rate is a multiple of ours
419 (sum of basins 1 and 24). Overall, their ice loss rate of $-118 \pm 9 \text{ Gt yr}^{-1}$ is significantly higher than
420 ours.

421 Integrated over the domain studied, our loss estimate is smaller than other recent estimates:
422 Shepherd et al. (2012) arrive at $-97 \pm 20 \text{ Gt yr}^{-1}$ for WAIS over the ICESat period; while Gunter et
423 al. (2013) obtain $-105 \pm 22 \text{ Gt yr}^{-1}$. With regards to Shepherd et al. (2012) and other altimetry-
424 based results, the discrepancy is partly explained by our estimate of a negative SMB anomaly in
425 the ASE, while RACMO2.1 gives a positive trend in this region (Fig. 4a). Methodologies
426 employing RACMO2.1 will, thus, attribute a greater loss (for a given height change) to ice
427 dynamics. Since these losses occur at a higher density than SMB, the inferred mass loss is greater.
428 With regards to Gunter et al. (2013), the discrepancy arises from the different GIA rates used in
429 the ASE. One cause for this might be the different GRACE solutions used. Our GRACE data set
430 (Luthcke et al., 2013) is equivalent to a RL04 GRACE solution and uses the same antialiasing
431 products. In Gunter et al. (2013), RL05 GRACE solutions appear to yield higher overall mass loss
432 estimates. Preliminary comparisons of new (RL05) mascon solutions with the RL04 ones appear
433 to show, however, little impact on the trends.

434 The results for SMB are more challenging to interpret because the trend, over this time period, is
435 relatively small (a few cm yr^{-1}) and below one standard deviation for most of the domain (Fig
436 4b). There is, however, some agreement with new *in-situ* data from ice cores (Medley et al., 2013;
437 Burgener et al., 2013). It should be remarked that in the ASE, where we also observe an ice loss
438 maximum, the statistical framework might have difficulty in partitioning SMB and ice dynamics.
439 The reason for this is that the density of the SMB changes tends to be higher at the coast, with
440 higher temperatures and melt rates. Some of the large, negative trends seen in the ASE could thus
441 be falsely attributed to SMB. This could be remedied in principle by including more information
442 on the spatial patterns of SMB into our framework by using, for example, a more informative
443 prior. Also, it should be noted that the uncertainties on our SMB rates, although low on a basin
444 scale, are comparatively high on a small spatial scale. These issues will become less critical in a

445 time-evolving solution because ice dynamics and SMB have very different temporal frequencies:
446 the former tends to vary smoothly in time, while the latter has relatively large high-frequency
447 variability. This important difference in temporal smoothness will elicit significant improvement
448 in source separation.

449 Methods that combine altimetry and gravimetry such as Gunter et al. (2013) and also the
450 framework presented here are sensitive to the SMB anomaly used. We illustrate this sensitivity
451 through a simple calculation: let the unobserved processes on a 1 m^2 unit area be as follows: SMB
452 amounts to 0.2 m yr^{-1} at 350 kg m^3 density; GIA is 1 mm yr^{-1} at 3500 kg m^3 ; and ice loss is at -1.0
453 m yr^{-1} at 917 kg m^3 . This amounts to an observed height change of -0.799 m yr^{-1} . The observed
454 mass change is $-897.5 \text{ kg yr}^{-1}$ over the unit area. We now try to explain these signals by taking
455 into account GRACE and altimetry, but erroneously assume a SMB rate that is 10% too high at
456 0.22 m yr^{-1} (amounting to a positive mass change of 77 kg yr^{-1}). The remaining mass signal that
457 needs to be explained by ice and GIA is now $-974.5 \text{ kg yr}^{-1}$. The unexplained height change is -
458 1.019 m . We arrive at two equations, one for height and one for mass, that can be solved by
459 finding the intersection of the two lines (see Fig. 9). Solving the equations, we arrive at an ice
460 mass loss rate of -1.025 m yr^{-1} with a high, but still plausible, GIA rate of 6 mm yr^{-1} . Thus, in this
461 example, a 10% difference in SMB can result in a GIA estimate that is markedly higher (5 mm yr^{-1})
462 than the truth. The resulting ice mass difference would be in the range of -40 Gt yr^{-1} when taken
463 over the whole of West Antarctica. Naturally, this sensitivity acts both ways, so an underestimate
464 in SMB would result in a lower GIA, and less ice loss. In this context, both GRACE filtering and
465 the treatment of the ICESat trends also play a major rôle. As the mass loss signal in West
466 Antarctica is relatively localised, with high rates of elevation change confined to only a few
467 percent of the area of a basin, the inclusion or exclusion of a single (informative) altimetry data
468 point can alter the spatial distribution of height change considerably but less, the overall mass
469 trend, as this is constrained by GRACE.

470 It is also worth examining the sensitivity of the solution to the prior distributions that were derived
471 from the forward models, auxiliary data sets, such as surface ice velocity, and expert knowledge.
472 To do this, we changed the original amplitude and length-scale constraints as detailed in Table 4.
473 The Table also lists the original mass trend (using constraints detailed in Table 2) alongside the
474 new estimates using the revised constraints. Changes in the characteristic length scale for GIA
475 and SMB have a rather small effect on the integrated mass trend. On the other hand, the velocity
476 threshold that is used to determine whether the signal is likely to be associated with ice dynamics
477 appears to have a significant effect for the three basins that comprise the Antarctic Peninsula: 23,
478 24, 25. This is because, for the Peninsula, observed and balance velocities are missing in a number
479 of places. Where this is the case, they were set to 5 m yr^{-1} . With a 50 m yr^{-1} soft threshold, this
480 means that an ice dynamics signal is extremely unlikely in all locations with a missing velocity.
481 Improving the velocity field in this area would, therefore, reduce this sensitivity.

482 The GIA estimates from our study agree well with a recent GRACE-based estimate (Sasgen et al.,
483 2013) and also compare well with a recent forward model (Ivins et al., 2013). Compared to AGE-
484 1, the spatial pattern of our uplift maximum is shifted away from the Peninsula and towards the
485 Ronne Ice Shelf. The spatial pattern is closer to that of W12a and ICE-5G models, with a bimodal
486 uplift maximum centred underneath the Ronne and Ross Ice Shelves (Fig 6a). This spatial

487 structure is likely to have resulted from the use of GPS uplift rates, which were also used in the
488 calibration of the most recent forward models (Whitehouse et al., 2012; Ivins et al., 2013). The
489 W12a model yields slightly higher estimates for most basins but shows good agreement on the
490 Southern Antarctic Peninsula. Whitehouse et al. (2012) remark that the uplift rates using the W12
491 de-glaciation history – which are already substantially lower than the ICE-5G (Peltier 2004)
492 model rates – can be viewed as an upper bound. Separating secular and present-day viscous and
493 elastic signals from the trends in this area remains a challenging task and will be treated in greater
494 detail in the spatio-temporal version of our framework.

495 For this proof-of-concept study, our focus lies mainly on ice dynamics, SMB and GIA estimates,
496 neglecting to a certain extent the influence of mass-invariant height changes (due to firn
497 compaction and elastic deformation of the bedrock). At this stage, the framework solves for a
498 single process that combines both these processes. In this time-invariant framework, the two are
499 confounded and cannot be separated, as they are not distinguishable by different densities or
500 length scales. A better approach to solve for the elastic rebound of the crust would be to integrate
501 a dynamic estimate that depends on the ice load changes. This approach is being implemented in
502 the spatiotemporal version of the framework. Firn compaction is currently linked with SMB
503 through a simple correlation model (Zammit-Mangion et al., 2014). This approach could be
504 further improved by adding a temperature dependence, along the lines of a simple firn compaction
505 model (Helsen et al., 2008). Finally, another open question concerns the extent of present-day
506 viscoelastic rebound in the ASE.

507 **6 Conclusion**

508 Our proof-of-concept study shows that hierarchical modelling is a powerful tool in separating ice
509 mass balance, SMB and GIA processes when combining satellite altimetry, GPS and gravimetry.
510 We demonstrate that, using only smoothness criteria derived from forward models, it can provide
511 an accurate estimate of the different processes. A time-varying version of the framework is
512 currently being developed, which includes a number of improvements, mentioned earlier. In
513 particular, estimation of elastic rebound in the GPS time series, and more robust partitioning of ice
514 dynamics and SMB will provide substantial improvements in source separation, error reduction
515 and GIA estimation. A central advantage of the framework is that new data – which need be
516 neither regular, or gridded – can be added at any point. For example, it is possible to extend the
517 observation period forward or back in time using data from ERS2, or Cryosat2, or any other data
518 set that contains information about one of the processes being solved for. This could include, for
519 example, accumulation radar data or shallow ice cores for SMB variability or additional GPS sites
520 as they become available. Preliminary tests have shown that the inference can also be performed
521 without GRACE data. .

522 **Author contributions**

523 JLB conceived the study, co-wrote the m/s and made all revisions during review. NS and AZM
524 prepared the data and implemented the framework and co-wrote the paper. JCR advised on the
525 statistical inference framework and methodology. TF and FR provided the Envisat data, SL
526 provided the GRACE data. All authors commented on the m/s.

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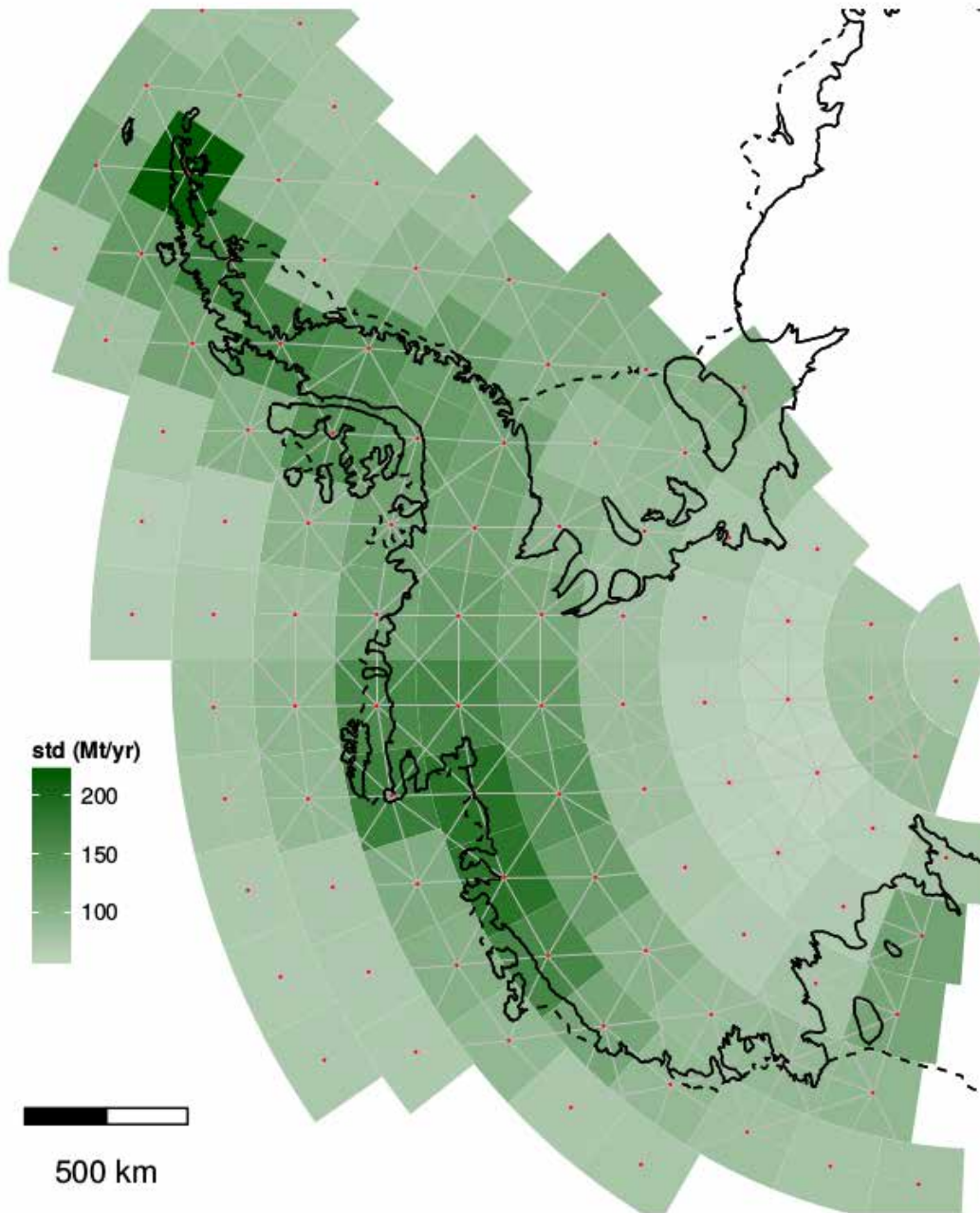
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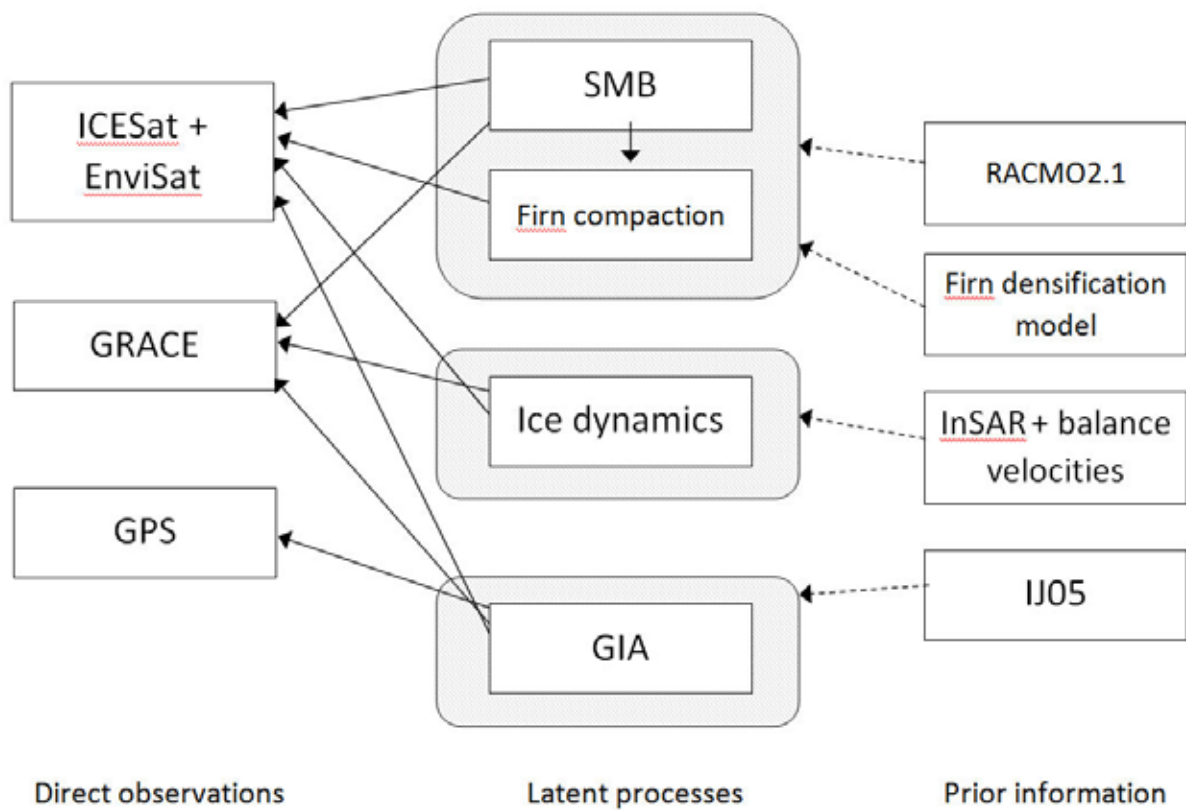
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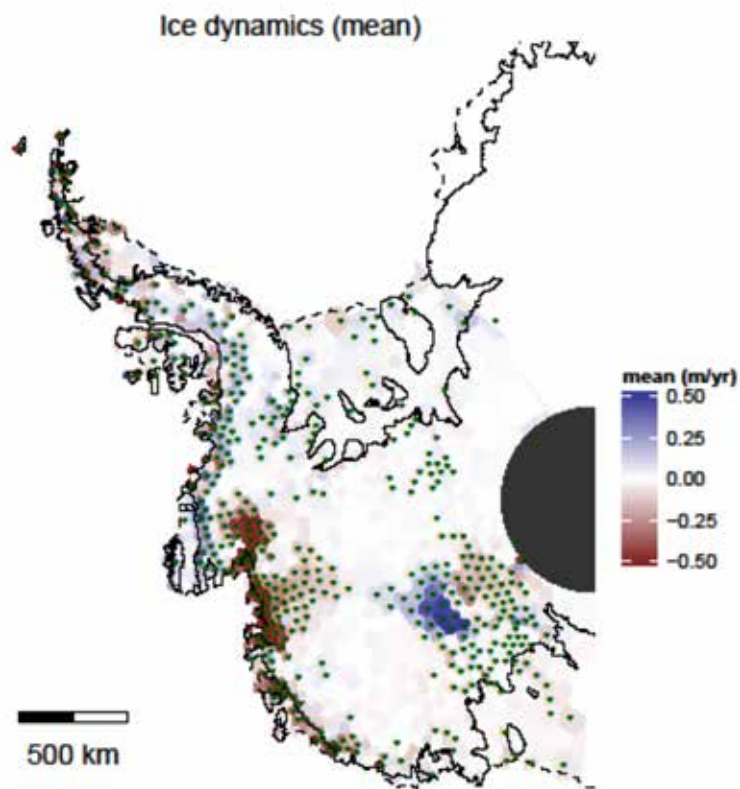
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690 Figure 1. Error estimates for the GRACE mascon solutions, derived from a regression of the data
691 (Zammit-Mangion, et al, 2014).
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695 Figure 2. Schematic diagram showing the relationship between the observations, process model
 696 defining the latent processes and the priors employed.



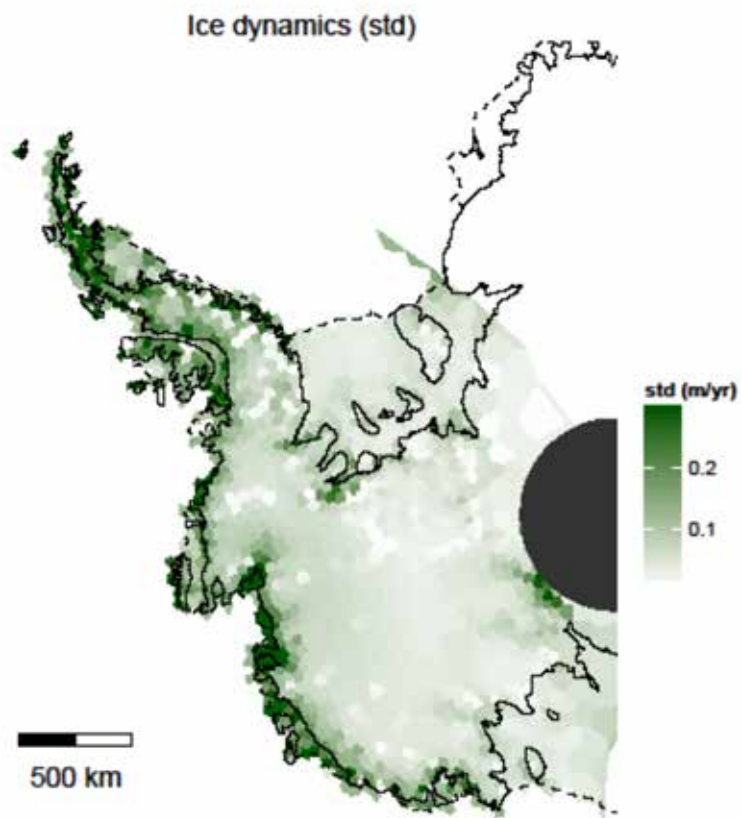
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699 Figure 3a. Ice dynamics for 2003–2009 in m yr⁻¹. Stippled points denote areas in which the mean
700 signal is larger than the marginal standard deviation.

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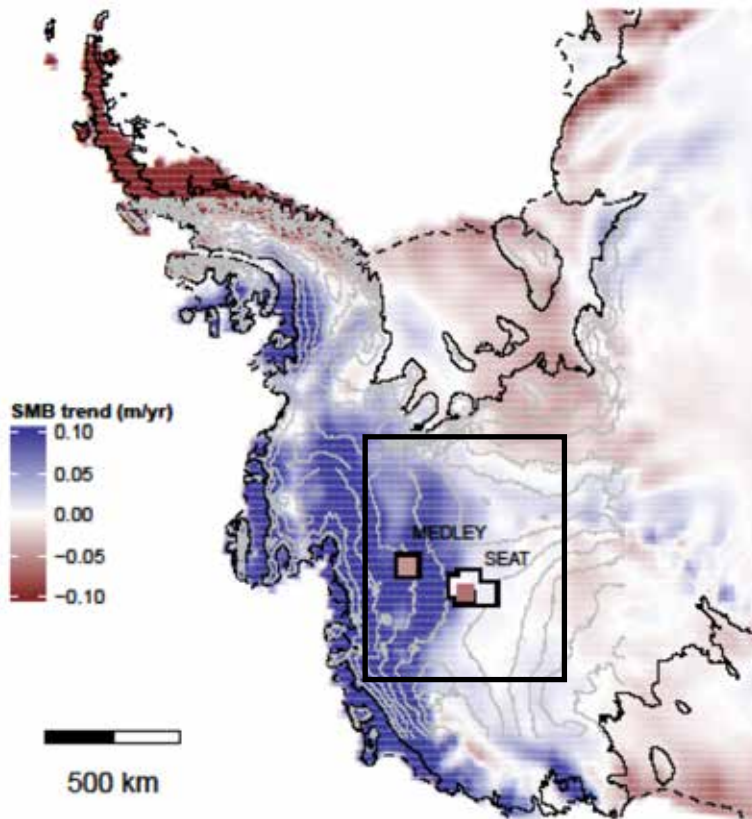
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704 Figure 3b. Marginal standard deviation of ice dynamics for 2003–2009 in m yr^{-1} .

RACMO trend of cumulative SMB anomalies 2003–2009



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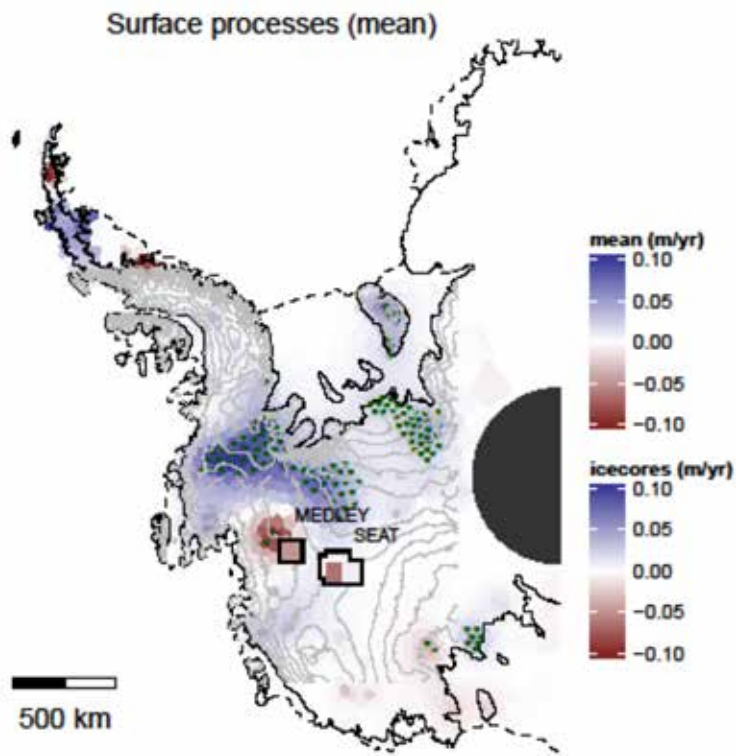
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Figure 4a. The SMB trend for 2003–2009 as obtained from RACMO. Contour lines (shown from -1000 to 1000km Northing) are elevations from BEDMAP surface (Fretwell et al., 2013). Mean ice core accumulation rates from Medley et al. (2013) (denoted MEDLEY) and ice core accumulation rates from Burgener et al. (2013) (denoted SEAT). Rectangle shows area in close-up (Fig. 5).



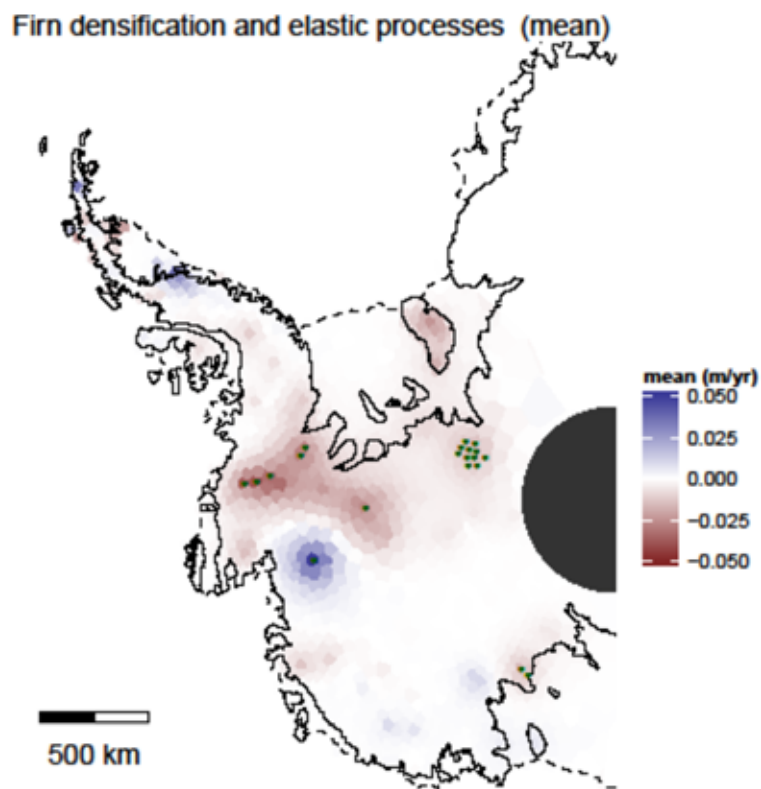
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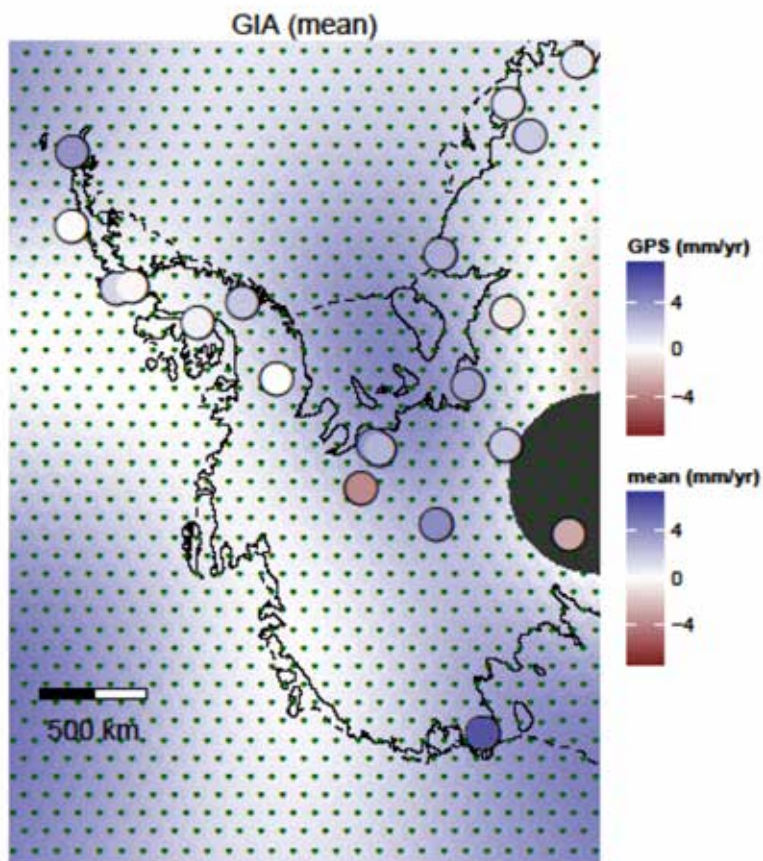
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715 Figure 4b. SMB rates for 2003–2009 in m yr^{-1} and locations of the ice cores from Burgener et al.
 716 (2013) and Medley et al. (2013). Contour lines are elevations from the BEDMAP surface
 717 (Fretwell et al., 2013). Stippled points denote areas in which the mean signal is larger than the
 718 marginal standard deviation.

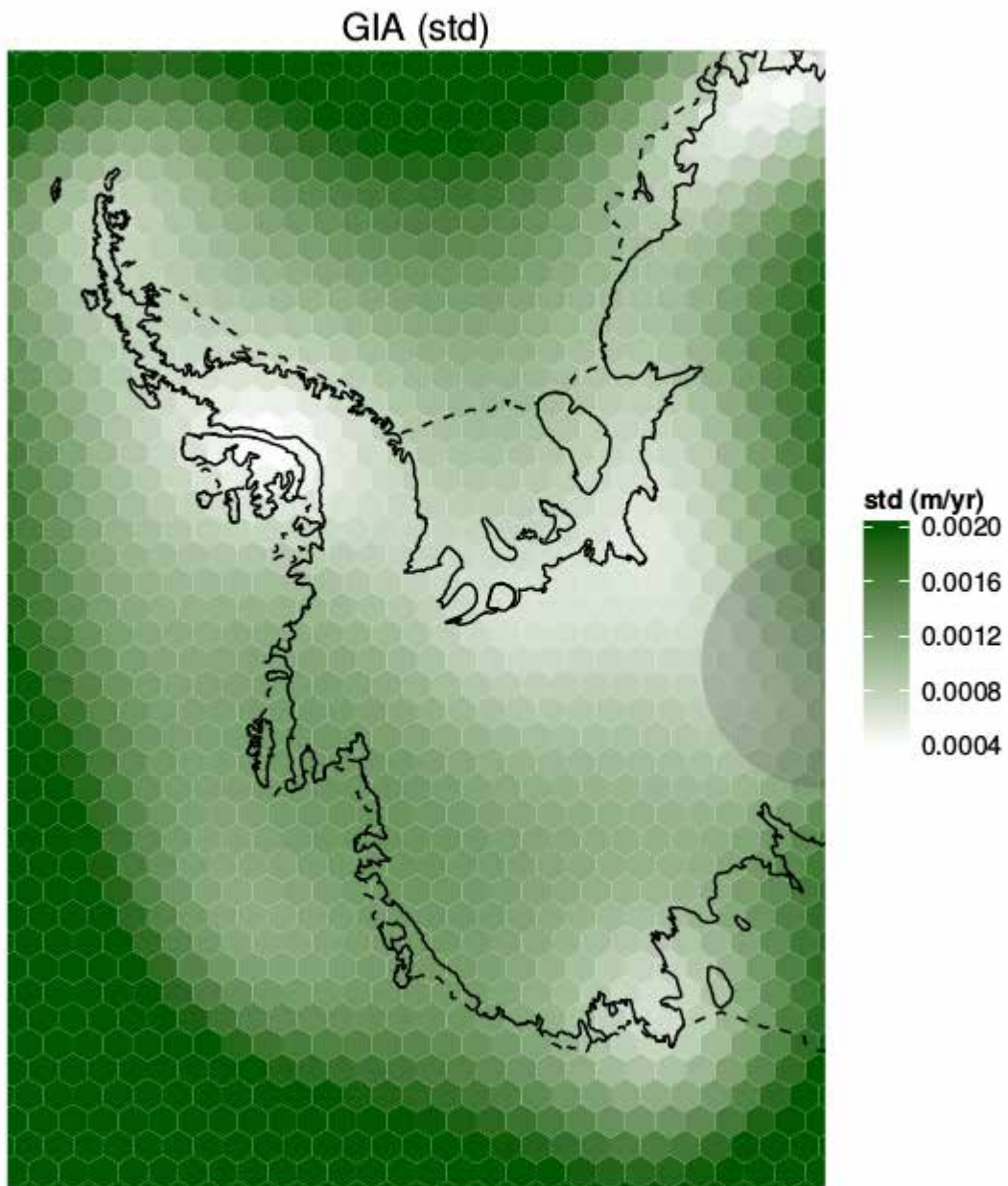
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720
 721 Figure 5. Height changes from firn compaction and elastic uplift of the crust for 2003–2009 in m
 722 yr^{-1} . Stippled points denote areas in which the mean signal is larger than the marginal standard
 723 deviation.
 724



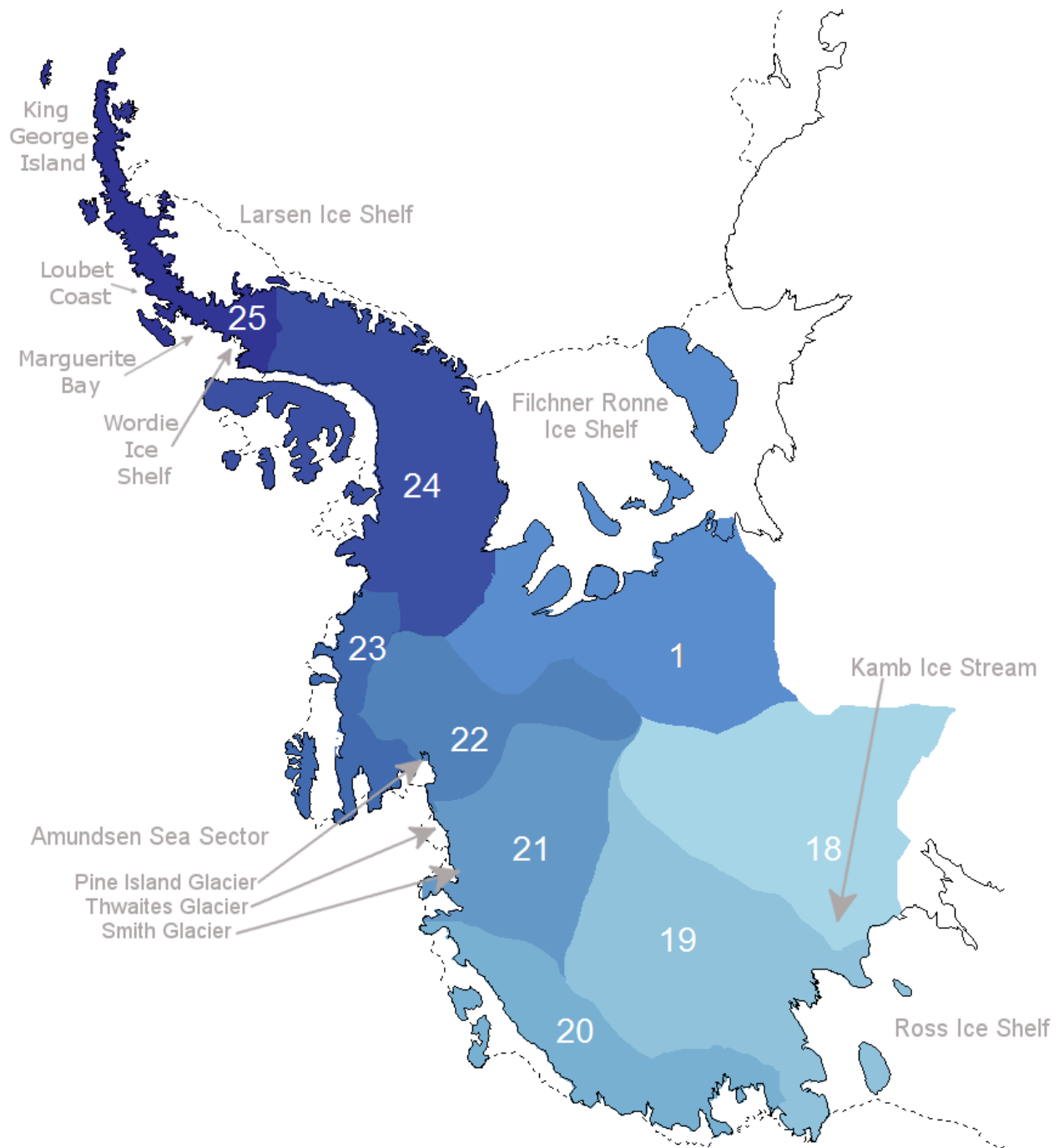
725
 726 Figure 6a. GIA estimate with GPS stations and their rates. Stippled points denote areas in which
 727 the mean signal is larger than the marginal standard deviation.
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730 Figure 6b. GIA error estimate (one standard deviation).

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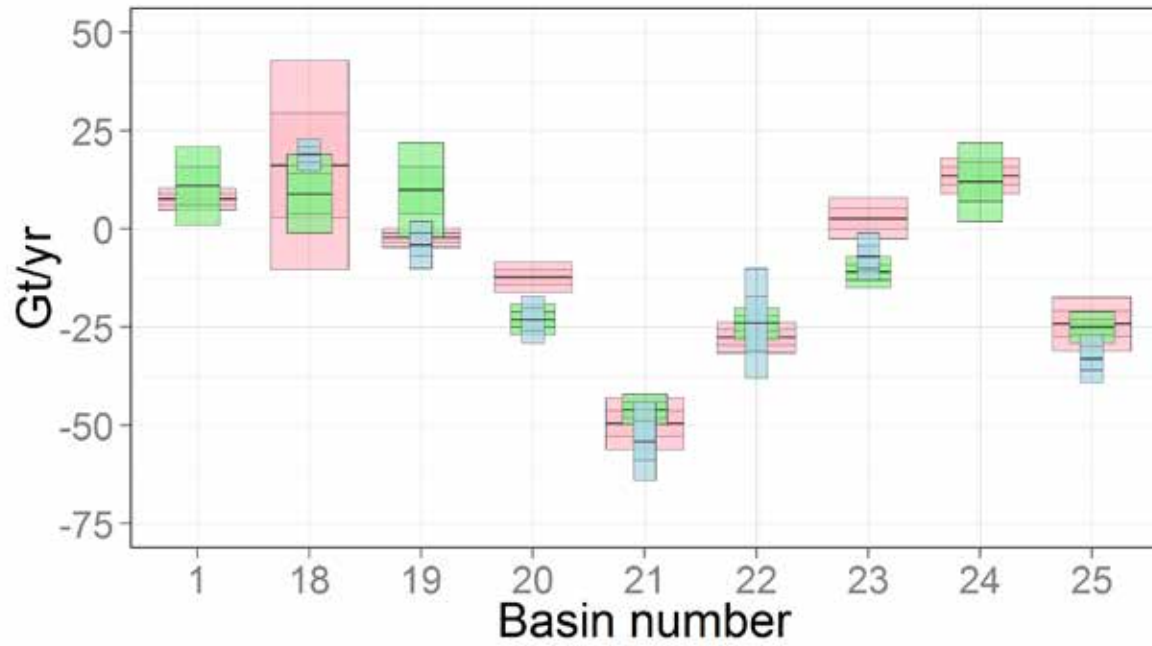


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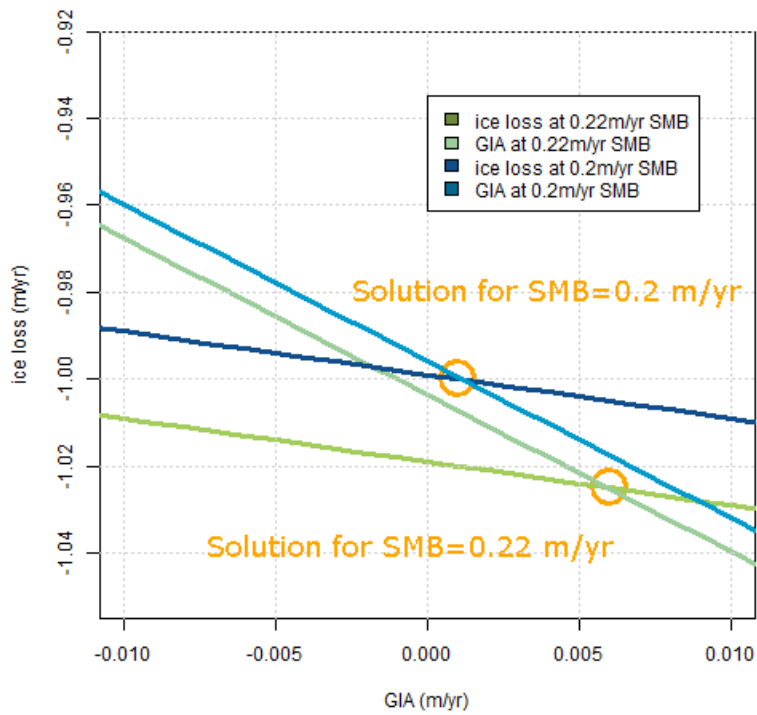
733 Figure 7. Basin definitions used for West Antarctica (adapted from Sasgen et al., 2013).

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736
 737 Figure 8. Combined Ice and SMB loss trends for West Antarctica using RATES (pink), results
 738 from King et al. (2013)(blue), and from Sasgen et al. (2013) (green). Basin definitions for King et
 739 al. (2012) differ for basins 1 and 24, so they are given in Table 3 instead. Our basin 25 is equal
 740 to the sum of basins 25 and 26 in King et al. (2012), this is given here as basin 25 for the King
 741 estimate.
 742
 743



744

745 Figure 9. Toy example illustrating the sensitivity of combination methods to differing SMB
 746 estimates. The blue lines represent the set of equations that solve for ice loss and GIA when
 747 SMB=0.2 m yr⁻¹. The green lines represent the equations for SMB=0.22 m yr⁻¹.

748

749 Table 1. GPS stations with vertical rate and errors, modelled elastic correction and adjusted rates.
 750 The latter are used for inference.

Site Name	Lat	Lon	Start Year	Start Day of year	End Year	End Day of year	data days	GPS rate (mm yr ⁻¹)	Sigma	modelled elastic	adjusted GPS
ABOA	-73.04	346.59	2003	31	2010	11	1959	1.4	0.84	0.27	1.13
BELG	-77.86	325.38	1998	33	2005	45	1517	2.97	1.47	0.02	2.95
BREN	-72.67	296.97	2006	362	2010	194	463	3.85	1.6	1.85	2
FOS1	-71.31	291.68	1995	35	2010	364	317	2.14	0.4	1.64	0.5
MBL1_AV	-78.03	204.98						3.28	1.09	0.28	3
OHIG	-63.32	302.1	1995	69	2002	48	1667	3.8	1	NULL	3.8
PALM	-64.78	295.95	1998	188	2002	59	1181	0.08	1.87	NULL	0.08
ROTB	-67.57	291.87	1999	54	2002	59	239	1.5	1.9	NULL	1.5
SMRT	-68.12	292.9	1999	112	2002	59	751	-0.22	1.93	NULL	-0.22
SVEA	-74.58	348.78	2004	317	2008	20	1030	2.07	1.95	0.24	1.83
VESL	-71.67	357.16	1998	212	2010	328	3081	1.06	0.45	0.25	0.81
W01_AV	-87.42	210.57						-2.8	1.17	-0.09	-2.71
W02_AV	-85.61	291.45						2.17	1	0.28	1.89
W03_AV	-81.58	331.6						-2.47	1.28	-1.73	-0.74
W04_AV	-82.86	306.8						3.42	0.84	0.16	3.26
W04B/CRDI	-82.86	306.8	2002	358	2008	24	16	4.06	1.32	0.16	3.9
W06A	-79.63	268.72	2002	356	2005	358	12	-2.2	2.42	1.53	-3.73
W07_AV	-80.32	278.57						3.61	1.58	0.97	2.64
W09	-82.68	255.61	2003	9	2006	8	34	4.54	2.59	0.49	4.05
W12A/PATN	-78.03	204.98	2003	331	2007	363	17	6.41	1.61	0.28	6.13
W08A/B/SUGG	-75.28	287.82	2003	3	2006	4	13	1.31	1.28	1.3	0.01

751

752 Table 2. Prior information and soft constraints applied to length-scales and amplitudes based on
 753 expert judgement and analysis of the forward models discussed in section 2.4

Process	Length scale	Softly constrained amplitude (1sigma)	Dependency
GIA	3000 km	5mm yr ⁻¹	Independent
Ice dynamics	50 km	1 mm yr ⁻¹ in interior – 15m yr ⁻¹ in areas flowing faster than ~15 m yr ⁻¹	Independent
Firn compaction	80 km at coast – 200 km at interior	1 mm yr ⁻¹ in interior – 140 mm yr ⁻¹ at coast	Anti-correlated with SMB (rho = -0.4)
SMB	80 km at coast – 200 km at interior	1 mm yr ⁻¹ in interior – 240 mm yr ⁻¹ at coast	Anti-correlated with firn compaction (rho = -0.4)

754

755

756 Table 4. Mass trend values for each basin shown in Figure 8 for different values of the GIA length
 757 scale, SMB length scale and ice surface velocity threshold. All values in columns 2-4 are in Gt/yr.

Basin Number	Original mass trend	GIA length scale 1000 km	SMB length scale from RACMO: 150 km everywhere	Ice horizontal velocity threshold 50 m yr ⁻¹
01	7.57 ± 1.41	7.49 ± 1.40	8.11 ± 1.36	5.40 ± 1.0
18	16.16 ± 13.26	13.48 ± 12.92	15.12 ± 13.05	24.80 ± 3.18
19	-2.24 ± 1.19	-2.23 ± 1.26	-2.18 ± 1.29	-0.71 ± 0.91
20	-12.22 ± 1.94	-11.47 ± 1.98	-12.28 ± 1.93	-13.21 ± 1.67
21	-49.48 ± 3.32	-45.31 ± 3.56	-49.53 ± 3.41	-47.01 ± 3.38
22	-27.62 ± 1.95	-26.34 ± 2.02	-27.34 ± 1.90	-24.12 ± 1.75
23	2.68 ± 2.65	3.28 ± 2.67	2.62 ± 2.65	-0.18 ± 2.59
24	13.57 ± 2.28	13.65 ± 2.30	13.39 ± 2.30	7.92 ± 1.67
25	-24.09 ± 3.39	-24.75 ± 3.20	-24.43 ± 3.42	-8.09 ± 1.90

758

759

760 Table 3. Ice and SMB mass trends from RATES, Sasgen et al. (2013), and King et al. (2012), in Gt yr. *Our basin 25 is equal to the sum of
 761 basins 25 and 26 in King et al. (2012). The sum of our basins 1 and 24 is equal to their sum of basins 1, 24, and 27.

Basin	RATES 03/2009- 10/2009	Sasgen (2013) 03/2009-10/2009	King (2012) 2002–2010	Diff RATES-Sasgen	Diff RATES-King
1	7.6	11	-	-3.4	-
18	16.2	9.5	19.2	6.7	-3
19	-2.2	10	-4	-12.2	1.8
20	-12.2	-23	-23	10.8	10.8
21	-49.5	-46	-54	-3.5	4.5
22	-27.6	-24	-24	-3.6	-3.6
23	2.7	-11	-7	13.7	9.7
24	13.6	12	-	1.6	-
25 (25+26)*	-24.1	-25	-33	0.9	8.9
(1+24+27)*	21.2	23	8.5	-1.8	12.7
WAIS	-75.5	-86.5	-117.3	9.2	41.8