

Velocity fluctuations
on the Beardmore
Glacier

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Tidally-induced velocity variations of the Beardmore Glacier, Antarctica, and their representation in satellite measurements of ice velocity

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Abstract

Ocean tides close to the grounding line of outlet glaciers around Antarctica have been shown to directly influence ice velocity, in both linear and non-linear patterns. These fluctuations can be significant and have the potential to affect satellite measurements of ice discharge which assume displacement between satellite passes to be consistent and representative of annual means. Satellite observations of horizontal velocity variation in the grounding zone are also contaminated by vertical tidal effects, shown here to be present in speckle tracking measurements. Eight TerraSAR-X scenes from the grounding zone of the Beardmore Glacier are analysed in conjunction with GPS measurements to determine short-term and decadal trends in ice velocity. Diurnal tides produce horizontal velocity fluctuations of > 50 % on the ice shelf, recorded in the GPS data 4 km downstream of the grounding line. This decreases rapidly to < 5 % only 15 km upstream of the grounding line. Daily fluctuations are smoothed to < 1 % in the 11 day repeat pass TerraSAR-X imagery but fortnightly variations over this period are still visible and show that satellite-velocity measurements can be affected by tides over longer periods. The measured tidal displacement observed in radar look direction over floating ice also allows a new method of grounding line identification to be demonstrated, using differential speckle tracking where phase coherence is too poor for SAR interferometry.

1 Introduction

The Antarctic Ice Sheet contains approximately 27 million km³ of ice (Fretwell et al., 2013). Recent estimates suggest around 2000 Gt (10¹² kg) or 0.01 % of this ice moves through the system every year (Rignot et al., 2008), which is a volume equivalent to around 5 mm per year of global sea level rise. It is clear that even a small imbalance between inputs and outputs could cause a rapid change in global sea level. Accurate methods of identifying ice discharge around the perimeter of Antarctica are necessary to quantify the mass-balance of individual glaciers and allow modelling of current and

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future contribution of the ice sheets to sea-level rise. The discharge is calculated at the grounding line, where grounded ice which is generally in a positive mass-balance state due to surface accumulation becomes floating and moves into a regime of negative balance influenced by significantly enhanced basal melting (Rignot and Jacobs, 2002).

Frequent measurement of surface displacement allows calculation of dynamic changes in glacier velocity. The velocity of ice streams and outlet glaciers terminating in ice shelves has been shown to fluctuate in response to ocean tides (e.g. Anandakrishnan et al., 2003; Bindschadler et al., 2003; Gudmundsson, 2006) and when analysing long-term trends it is important not to include bias from these short-term, unrepresentative velocity variations, or misuse a velocity “snapshot” taken over a few days to calculate an annual average ice discharge (Doake et al., 2002; Gudmundsson, 2006). The frequency and amplitude of the tidally-induced response varies with location, with velocity increases between 100 and 300 % of the mean recorded near the calving margins of large ice shelves (Brunt et al., 2010; Makinson et al., 2012) and smaller variations recorded tens of kilometres upstream of the grounding line on fast flowing ice streams (Gudmundsson, 2006). Variations close to the grounding line have been linked to perturbation in basal shear stress (Anandakrishnan et al., 2003) but it is not yet clear how longitudinal stresses are transmitted within the ice shelf (Brunt et al., 2010). Velocity also varies differently depending on the strength of tidal components, with a non-linear response of velocity associated with the semi-diurnal tides (King et al., 2010) and more regular response to diurnal tides (Bindschadler et al., 2003).

A full understanding of the drivers of this velocity fluctuation is of particular importance when annual velocity patterns are calculated using Interferometric Synthetic Aperture Radar (InSAR) or other satellite measurements of surface displacement calculated over short intervals Gudmundsson (2006). In the last two decades InSAR has become a standard way of measuring ice sheet surface velocities remotely (Goldstein et al., 1993; Rignot, 1996; Rignot et al., 2008). This technique relies on the satellite acquisitions being separated by a short time interval in order that snowfall events or other changes in the surface do not reduce the interferometric coherence. For spaceborne

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InSAR, repeat pass acquisitions are typically separated by several days depending on the repeat cycle of the satellite. Here we aim to use velocity data from GPSs at points upstream and downstream of the grounding line to quantify the temporal variability in velocity in the grounding zone, both on daily timescales and over the last 50 yr. Using these data in combination with a tide model (Padman et al., 2008) and glacier response model (Gudmundsson, 2007), we extend the measured GPS time series and predict how these variations will be visible from satellite speckle tracking. Synthesized velocities are compared with real satellite acquisitions and used to make inferences about the spatial extent of short-term velocity changes observed at GPS points and their propagation upstream of the grounding line.

TerraSAR-X and ground-based velocity measurements are presented for Beardmore Glacier, an outlet glacier in the Transantarctic Mountains, Antarctica. The high accuracy of TerraSAR-X speckle tracking also allows a new method of grounding line identification using techniques similar to differential interferometry (Goldstein et al., 1993; Rignot et al., 2011) but possible where phase coherence is not necessarily continuous.

2 The Beardmore Glacier

The Beardmore Glacier (83.5° S, 172° E) drains a catchment of around 90 000 km² from East Antarctica into the Ross Ice Shelf (Fig. 1). The glacier flows steeply through the Transantarctic Mountains with a well-defined break of slope where it meets the ice shelf, between Mount Hope and Mount Kyffin. The glacier is around 25 km wide at this point. A velocity of $364.7 \pm 1.5 \text{ m a}^{-1}$ ($0.998 \pm 0.004 \text{ m d}^{-1}$) was calculated in 1960–1961 by measuring stakes over a period of close to 1 yr on the central flowline of the glacier close to the grounding line (Swithinbank, 1963). A measurement over 14 days from this study agreed with these results to within 2 % (the limit of detection), suggesting limited seasonal variability at this time.

The grounding line of the Beardmore is defined here using two methods; photogrammetrically to identify a surface impression of change in stress regime, and

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interferometrically identifying the landward limit of tidal flexure (Fig. 1). A photoclino-
metric grounding line is available from the ASAD full Antarctic grounding line map
(Bindschadler et al., 2011) but no published landward limit of tidal flexure is available
for this area. This was instead derived manually from a combination of TerraSAR-X
5 differential interferograms (2012) and ICESat data (2003–2009) for the area. The two
grounding lines differ by less than 2 km and where ICESat tracks cross the grounding
line, data from Brunt et al. (2010) using flexure information and Marsh et al. (2012)
using break of slope and surface deformation distribution also agrees well with these
grounding lines.

10 The Ross Ice Shelf has a relatively strong diurnal tide, particularly in the K1 (23.93 h)
and O1 (25.82 h) components with modelled amplitudes of 0.5 m and 0.4 m respectively
at the Beardmore Glacier grounding line; conversely the semi-diurnal tidal components
are weak and close to zero and the vertical movement of the ice shelf is consistently
diurnal (Padman et al., 2008). A baseline for expected tidal range on the ice shelf was
15 obtained from the CATS2008a_opt tide model (Padman et al., 2008) using eight major
tidal components (K1, O1, P1, Q1, M2, S2, N2, K2). The response of ice shelves to
changes in atmospheric pressure, known as the inverse barometer effect adds a fur-
ther centimetre of change per hecto-Pascal (Padman et al., 2003). These air pressure
effects are accounted for using Antarctic Weather Station Observations made at the
20 “Elaine” weather station at 83.1° S, 174° E and at “Lettau” at 82.4° S, 174° W, (Table 1).
Temporal variation in load tide and solid earth tide is negligible and therefore neglected.

Four GPS stations (1 to 4) were positioned on the centreline of the glacier at 20 km
and 10 km upstream and 4 km and 15 km downstream of the grounding line. GPS-3 was
25 positioned on the coordinates of the 1960–1961 measurement in the grounding zone
by Swithinbank (1963). Data were recorded at 15 s intervals over a 35 day period, al-
though data are not continuous at some of the sites. These data have been processed
using kinematic Precise Point Positioning algorithms in JPL’s GIPSY software (Zum-
berge et al., 1997; King, 2004). Artifacts are avoided by kinematic processing under
loose random-walk constraints although some precision is lost in comparison to static

occupation methods (e.g. King et al., 2000). Locational accuracy from this method is nominally between 1.5 and 2.5 cm. Care was taken in resolving ambiguities in horizontal and vertical velocities to avoid errors in horizontal measurements due to unmodelled vertical signals (King, 2004). Point velocities are calculated based on differencing the positions over time intervals of 6 h. This smoothes out high frequency noise associated with the coordinate location errors and any unmodelled higher harmonic tides. A comparison between horizontal velocity and vertical movement at GPS-3 is given in Fig. 2a. Local maxima in velocity in the grounding zone coincide with maximum rate of falling tide, which is in agreement with elastic flexure theory which predicts a longitudinal extension at the surface during low tide (Holdsworth, 1969). At GPS-3, 6 h mean velocities vary between 0.5 m d^{-1} and 1.5 m d^{-1} during spring tides.

3 Tidal response

An equation linking tidally-varying basal shear stress to forward surface movement was put forward by Gudmundsson (2006, 2007) and is shown to be robust in replicating observed velocity variations on the Rutford Ice Stream using vertical movement from a tide model where errors in the tide prediction are reasonable (King et al., 2010). This relationship is here used to extrapolate the observed GPS-3 coverage from 2010–2011 to the satellite data acquisition period from 2009–2012. GPS-3 is close to the grounding line and we assume the variability in ice flow at this point to be representative of the grounding zone. The forward velocity, u , is related to mean basal shear stress, $\bar{\tau}$ by the following equation:

$$u = \left(\frac{1}{r} + 1 \right) C(\bar{\tau} + K\rho_w gh(t))^m \quad (1)$$

where ρ_w is the density of ocean water, g is the gravitational constant, $h(t)$ is the tidal height, r is the ratio between mean sliding velocity and mean forward deformational velocity, K is a site-specific constant varying in proportion to the tidal influence on

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velocity, C is the sliding coefficient and m is the power law exponent, hereafter taken to be equal to 3. Although sensitive to the value m , it has been shown that $m \approx 3$ fits well to data elsewhere (King et al., 2010). Measured GPS velocities and tidal displacements over a 35 day period were used to fit parameters for this relationship between basal shear stress and velocity for the Beardmore Glacier. As model parameters are not all independent, separate estimates of shear stress and sliding are made by using:

$$\tau_d = \rho_i g h \sin \alpha \quad (2)$$

$$u_s = u - \frac{2A(\tau_b)^n}{n+1} h \quad (3)$$

where u_s is sliding velocity, τ_d is driving stress, τ_b is basal shear stress, h is ice thickness and A is the flow rate factor, here taken to be $1.6 \times 10^{-10} \text{ a}^{-1} \text{ kPa}^{-3}$ for ice at -20°C (Cuffey and Paterson, 2010).

The mean surface slope in the last 10 km before the grounding line of the Beardmore Glacier is 0.017, with an ice thickness of 1050 m at the centreline measured with ground-penetrating radar at the grounding line during 2010 and backed up by BEDMAP data (Fretwell et al., 2013). This gives an approximate driving stress of 160 kPa (Eq. 2). A very simple approximation of basal shear stress using a “shape factor” of 0.9 gives $\tau_b = 144 \text{ kPa}$. A simple depth integrated shallow ice approximation using the non-linear relation given by Glen’s flow law (Nye, 1965) produces a predicted deformation velocity about a quarter of velocities measured on the glacier surface (Eq. 3). This suggests that the contribution of basal sliding to glacier motion is approximately three-quarters of the total observed surface velocity.

We use the parameters derived from the fit and tidal information from the CATS2008_opt tidal model to extrapolate the measured velocity dataset to cover a longer time-series and predict the expected tidal component of velocity at dates of TerraSAR-X acquisitions (Table 2). With a value of 144 kPa for shear stress, 3 for r and 3 for m , the best fit to data is observed with $K = 0.8$ and $C = 0.246 \times 10^{-6} \text{ m d}^{-1} \text{ kPa}^{-3}$.

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r and C are mutually dependent (King et al., 2010) and while r is fixed from the calculation of basal sliding, C is calculated through a best-fit to observed data.

4 TerraSAR-X speckle tracking

Speckle tracking makes use of the high pixel noise inherent in coherent imaging systems such as SAR. Speckle tracking can be used to map displacement vectors over short periods but unlike optical feature tracking it does not require large scale features such as crevasses. This method can be applied where surface displacement is relatively large and phase coherence is not completely lost. Current and recent InSAR and speckle tracking calculations have used consecutive repeat pass acquisitions of the available spaceborne SAR missions with various duty cycles, e.g. 1 day repeats, for instance with ERS-1/-2 in tandem mode (e.g. Joughin et al., 1996; Burgess et al., 2005); 3 day repeats such as with ERS-1 repeat pass acquisitions during the ice phase (e.g. Kwok and Fahnestock, 1996); 11 day repeats such as with TerraSAR-X (Jezek et al., 2011); 24 day repeats as with the Radarsat-1 (Scheuchl et al., 2012); and 46 day repeats with ALOS PALSAR (Baessler et al., 2012).

For the Beardmore Glacier grounding zone, eight TerraSAR-X scenes with 11 day separation have been acquired in StripMap mode: two sets of triples in March and June 2012 and an image pair in December 2009 (Table 1). Calculating displacement between these images allows five temporally distinct measurements of velocity. At 83.5° S the data are acquired in left-looking mode on a descending orbit and processed to single-look slant-range complex (SSC) format by DLR (Breit et al., 2010). A scene centre incidence angle of 44° gives ground range pixel resolution of 2.5 m and azimuth resolution of 3.3 m for these scenes. TerraSAR-X scenes over the Beardmore are acquired with the radar look direction aligned approximately perpendicular to the main component of ice flow. Velocities are calculated from full resolution SSC data by speckle amplitude tracking simultaneously in range and azimuth direction which largely avoids coherence problems in fast flowing areas and shear zones but provides

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sub-pixel resolution (Joughin, 2002). Co-registration of image pairs is done by masking out moving areas on the glacier and ice shelf, and calculating a base offset between images for the remaining areas. The slave image is then shifted to match this offset and produce a zero velocity over non-moving areas. Patches between 64 and 512 pixels square were tested for cross-correlation and a 256^2 patch used for final matching, producing a high signal to noise ratio but minimum loss of spatial resolution. Correlations with signal-to-noise ratio below 5 are discarded. An oversampling factor is applied to increase the precision of correlation. Jezek et al. (2011) estimate an absolute error for TerraSAR-X imagery of 0.03 m d^{-1} from atmospheric path delay and solid earth tide effects. Relative velocity errors depend on patch size and shape of the correlation function but are here minimized due to large patch sizes.

Although speckle tracking has previously been used to infer a horizontal velocity independent of tidal interference (e.g. Baessler et al., 2012), here we demonstrate that with high resolution sensors such as TerraSAR-X, the quality of speckle tracking velocity measurements is high enough that vertical tidal effects can also be observed in radar range. At an incidence angle of 44° , a 1 m change in tide between satellite passes produces a 1.036 m error in the horizontal displacement which translates to approximately 0.094 m d^{-1} error in velocity in look direction over the 11 day repeat pass interval of TerraSAR-X (Fig. 3). This is significant for many outlet glaciers and ice streams surrounding Antarctica, particularly where the main component of flow is in look direction, and must be removed in the velocity calculations. Where the main component of flow direction is in azimuth direction there will instead be a net effect on estimated flow direction. Where incidence angle is smaller than 44° , as is the case with many side-looking radar systems, these biases will be further amplified.

A stacked velocity map using data from three pairs gives a smoothed spatial velocity over three 11 day periods (Fig. 4). Comparison between TerraSAR-X derived velocities and GPS velocities highlights the absolute error in the TerraSAR-X data. TerraSAR-X and GPS velocities respectively in m d^{-1} at GPS-1 are 0.756 and 0.770; at GPS-2 are 0.748 and 0.782; at GPS-3 are 0.972 and 0.990; and at GPS-4 are 0.934 and 0.940.

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This shows agreement within 5% at all sites and $< 2\%$ at all but one site, supporting estimates of TerraSAR-X error of around 0.03 m d^{-1} . A 10% error as predicted by the vertical tidal movement between scenes should therefore be observable well above random noise in the TerraSAR-X data.

5 Grounding line identification

The unmodified velocity difference map shown in Fig. 5a shows an apparent significant increase in velocity in radar look direction over the ice shelf between December 2009 and June 2012 with little change on the grounded ice. This increase averages around 0.09 m d^{-1} , a difference which can be explained by error in calculated horizontal velocity induced by the vertical tidal movement of the ice shelf (Fig. 3). The Dec-1 to Dec-2 tidal and atmospheric difference is -0.589 m and Jun-1 to Jun-2 is $+0.615 \text{ m}$, giving a double difference of $+1.204 \text{ m}$ and expected velocity error of 0.113 m d^{-1} based on the radar incidence angle. This differential vertical movement allows identification of the areas of floating ice affected by the tides, similar to established techniques using interferometry (Goldstein et al., 1993; Rignot et al., 2011) but without the need for the very high coherence required by InSAR in the often crevassed shear zones around the grounding line.

6 Tidally-induced velocity change

Gudmundsson (2011) showed how long-period velocity fluctuations could occur in response to semi-diurnal tides but were weak in response to diurnal tides when the ice was modelled using viscoelastic rheology. Testing such models requires more detailed knowledge of how glacier velocities vary, both temporally and spatially. The temporal variation in velocity for a single point in the grounding zone is shown in Fig. 2a, while a spatial pattern averaged over time is shown in Fig. 4. Velocity smoothed over 3 days by looking at total horizontal displacement over this period reduces the influence of

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diurnal tides and highlights a spring-neap fortnightly velocity variation (Fig. 2b). This shows that despite the small variation in this region, velocities from 3 day repeat pass satellite imagery would be sensitive to the acquisition period and not suitable for measuring long-term trends in surface velocity on this glacier. The daily fluctuations are further damped when velocities are calculated over an 11 day repeat orbit, such as with TerraSAR-X, and the changes in horizontal velocity predicted by Eq. (1) are largely due to the non-linear interaction between the tidal components over longer periods. As this signal is small for the Beardmore Glacier, it is not clear from the short GPS dataset whether the resulting frequency is at the lunisolar fortnightly period (M_f) or at the lunisolar synodic fortnightly period (M_{sf}) due to the small semi-diurnal tides as has been observed elsewhere (Gudmundsson, 2007).

On the Beardmore Glacier the predicted variability in real horizontal velocity due to the diurnal tides over 11 days is $< 3\%$ (Table 2), approximately equivalent to the confidence in the TerraSAR-X velocities of around 0.03 m d^{-1} . The velocity difference map shown in Fig. 5b shows a velocity increase across the lower glacier from mid-late March 2012 to early April 2012 (a period of only 11 days) where the vertical tide differences are approximately the same. Unlike the vertical signal observed in Fig. 5a, there is no well-defined break at the grounding line and the signal slowly reduces within a few tens of kilometres upstream of the grounding line. Assuming that all observed velocity change is real, the glacier experiences an increase of approximately 0.035 m d^{-1} or 4% . This is around 5 to 6 times larger than the 0.006 m d^{-1} predicted by the tide response model (Table 2) but falls within the error margin of the TerraSAR-X data.

TerraSAR-X velocities in azimuth direction only from December, March and June are shown along a central flowline for comparison with the predicted velocities from the tide response model (Fig. 6). By ignoring the range component any bias due to tidal displacement is avoided, and as velocity is largely in azimuth direction results remain representative of trends. There is no discernible change in velocity between these periods well upstream of the grounding line and although the observed differences approach the predicted absolute error for TerraSAR-X, slightly lower velocities

are observed around the grounding line in March and June, agreeing with the tide response model.

7 Conclusions

Building on existing knowledge of how glaciers react to tides, it is shown that velocity fluctuations in the grounding zone can be observed using high-resolution satellite data with short repeat pass intervals. On a timescale of 11 days these fluctuations are heavily smoothed and become close to the limit of detection ($< 3\%$) for the diurnally-dominated flow variation on the Beardmore Glacier. The relatively higher basal shear stress in comparison to fast-flowing ice streams is thought to contribute to the limited upstream propagation of these fluctuations (Gudmundsson, 2003) with 1 to 2% variation in 6 h averaged velocities during spring tide periods at the GPS 15 km upstream of the grounding line.

Averaged GPS data from December 2010 shows a 1% decrease in velocity at the grounding line of the Beardmore Glacier over the 50 yr period since 1960–1961 from $0.998 \pm 0.004 \text{ m d}^{-1}$ to $0.990 \pm 0.001 \text{ m d}^{-1}$. This difference is greater than the combined error estimates given for the 1960–1961 and 2010–2011 data but suggests that discharge from this glacier has remained stable over the last fifty years (Swithinbank, 1963) in contrast to glaciers elsewhere in Antarctica.

Velocity fluctuations have previously been observed only on ice streams with significant basal sliding. Here we observe $> 50\%$ diurnal fluctuations in GPS records from the grounding zone of the Beardmore Glacier which are not observed 15 km upstream from the grounding line. Detrending of daily signals in the grounding zone highlights fortnightly velocity fluctuation, here with a best fit around M_f period (13.7 days). This is in contrast to observations of the Rutford Ice Stream where interaction of the semi-diurnal tides causes much larger fortnightly fluctuations at the M_{sf} period. The 5-week data period is not long enough to make a firm statement that this is indeed an M_f signal, which could be a residual effect of the small semi-diurnal tides still present at this site

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and longer periods of observation would be necessary to draw further conclusions on the applicability of the Gudmundsson (2007) flow model at this location.

The viability of using SAR speckle tracking to map spatial variability in these short-term velocity fluctuations is also examined. In addition to horizontal displacements, speckle tracking offsets in radar look direction contain a component of the tidal vertical displacement over the ice shelf, proportional to radar incidence angle. This effect distorts calculations of horizontal velocity and flow direction in this area and should be removed using a separate tide model or reference measurements in stagnant areas over the ice shelf nearby. It can also be used to map the grounding zone where tidal range between image acquisitions exceeds the limit of detection for the radar, as is demonstrated for the Beardmore Glacier. Fortnightly horizontal velocity changes upstream of the grounding line are too small to be accurately detected here as the non-linear interaction between diurnal tides is thought to be small, however it is quite likely that spatial patterns of velocity fluctuation could be detected by this method on ice streams which exhibit stronger fortnightly velocity variations.

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Table 1. Modelled tidal height above mean sea level and inverse barometer effect derived from atmospheric pressure at “Elaine” weather station for individual TerraSAR-X acquisition dates.

TSX ID	Date	Tide (m) (CATS_2008opt)	Atmospheric Pressure (hPa)	Inverse Barometer Effect (m)
Dec-1	16 Dec 2009	0.606	982.5*	−0.175
Dec-2	27 Dec 2009	0.024	981.7*	−0.183
Mar-1	20 Mar 2012	0.271	982.0	−0.180
Mar-2	31 Mar 2012	−0.198	990.3	−0.097
Mar-3	11 Apr 2012	−0.684	981.2	−0.188
Jun-1	05 Jun 2012	−0.596	972.3	−0.277
Jun-2	16 Jun 2012	−0.116	985.2	−0.142
Jun-3	27 Jun 2012	−0.019	998.2	−0.018

* Data from “Lettau” station (83.1° S, 174° E).

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Table 2. Predicted absolute mean glacier velocity at GPS-3 (V) for TerraSAR-X acquisition periods from tidal response modelling and expected tidal (V_t) and atmospheric (V_{IBE}) induced-error in observed radar look-direction velocity due to vertical displacement.

TSX Pairs	Δ Tide (m)	V_t (m d^{-1})	Δ IBE (m)	V_{IBE} (m d^{-1})	V (m d^{-1})
Dec-1/2	-0.581	+0.052	-0.008	+0.001	1.003
Mar-1/2	-0.469	+0.042	+0.083	-0.008	0.973
Mar-2/3	-0.486	+0.044	-0.091	+0.008	0.979
Jun-1/2	0.480	-0.043	+0.135	-0.012	0.992
Jun-2/3	0.0970	-0.009	+0.124	-0.011	0.997

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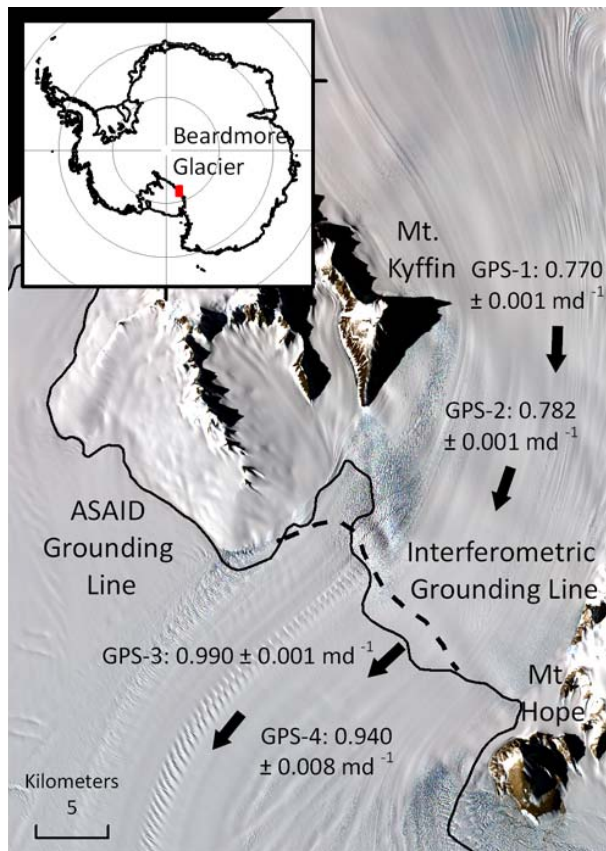


Fig. 1. Beardmore Glacier GPS positions and velocities in December 2010 superimposed on an ASTER image from 2008. GPS positions correspond to the centres of arrows. The ASAID (solid line) and Interferometric (dashed line) grounding lines are also shown.

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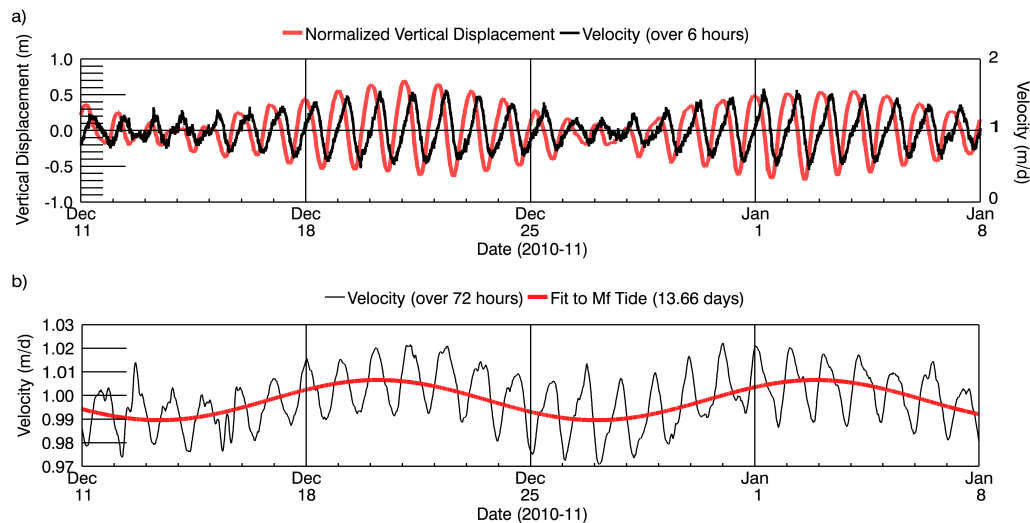


Fig. 2. (a) Recorded vertical displacement and 6 h averaged surface velocity at GPS-3. Peaks in velocity match closely to peak rate of falling tide both in phase and amplitude. **(b)** 3 day running average velocity at the Beardmore Glacier grounding line from GPS data. Velocities show the outcome of 3 day repeat feature tracking. Short-term velocities throughout the paper are given in m d^{-1} instead of m a^{-1} .

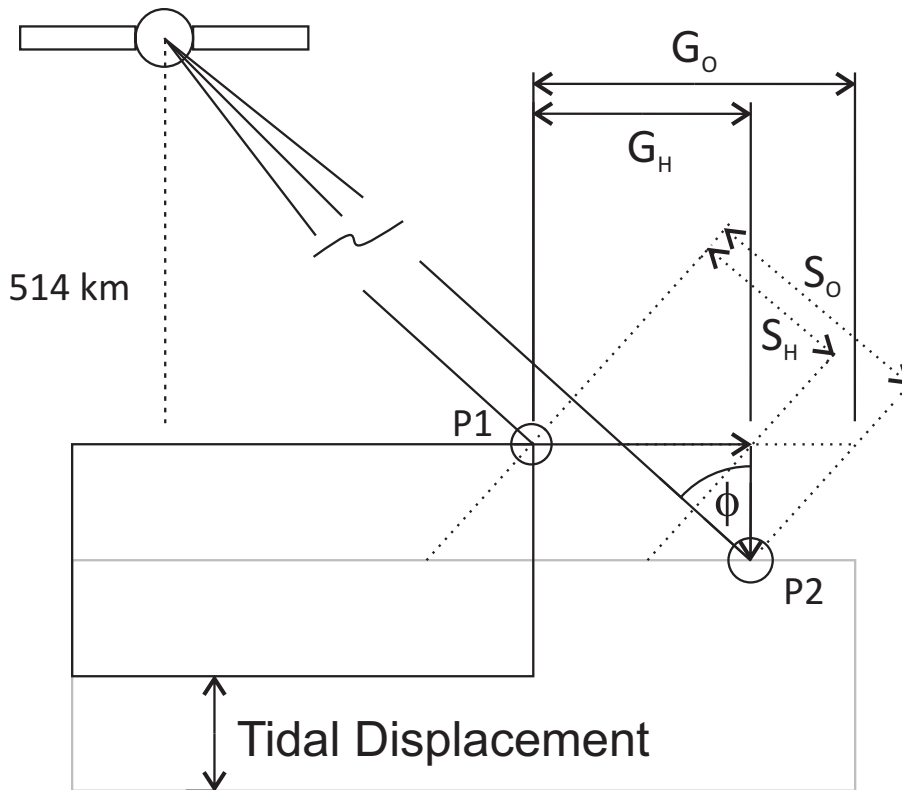


Fig. 3. Schematic showing the effect of tidal displacement on observed displacement in slant range (S_O) and ground range (G_O) compared to actual horizontal displacement (G_H). When slant range is converted into ground range the additional displacement equals the tidal change divided by the tangent of the incidence angle ($S = T / \tan(\phi)$).

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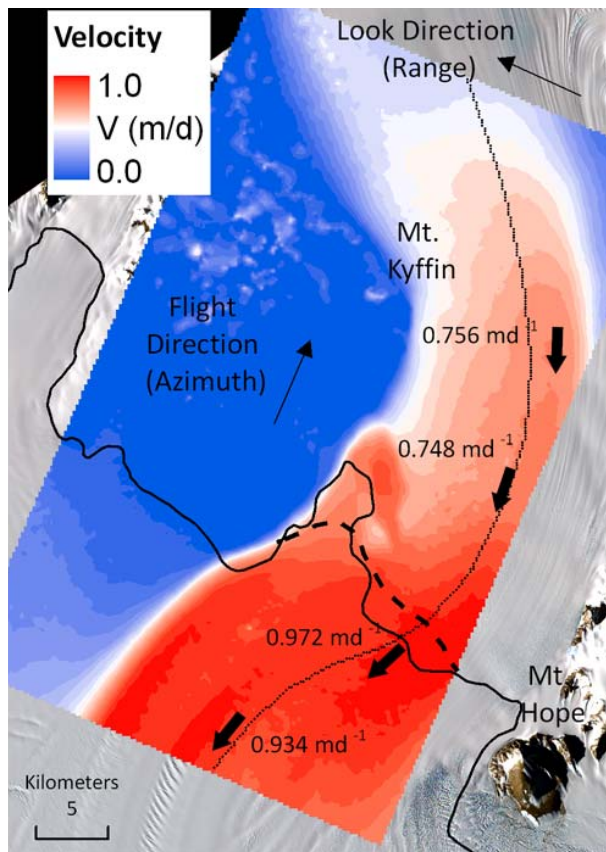


Fig. 4. Absolute velocity across the Beardmore Glacier grounding line created by stacking velocity data from Dec-1/2, Jun-1/2 and Jun-2/3. Velocity arrows show TerraSAR-X velocities at GPS points for comparison with Fig. 1.

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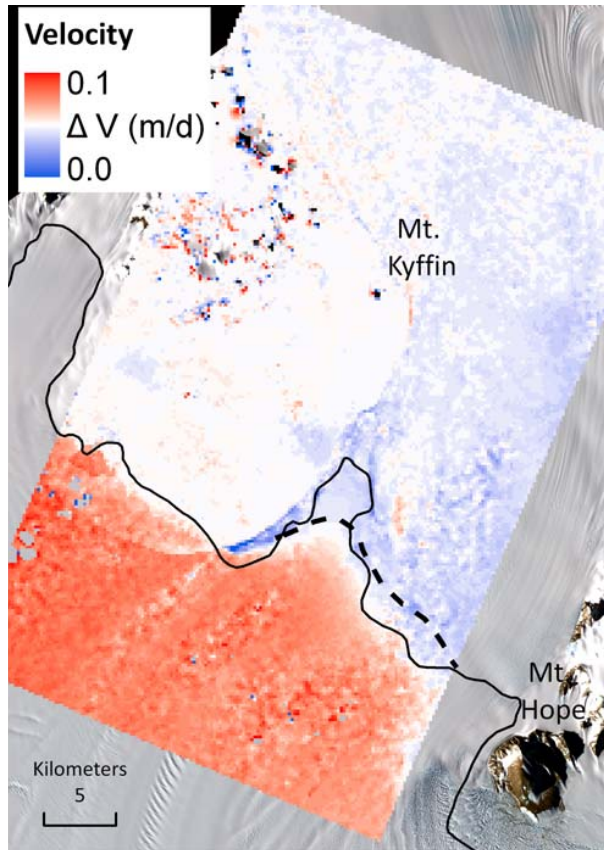


Fig. 5a. Difference in velocity in look direction between Dec-1/2 and Jun-1/2 highlighting the influence of the tides downstream of the grounding line.

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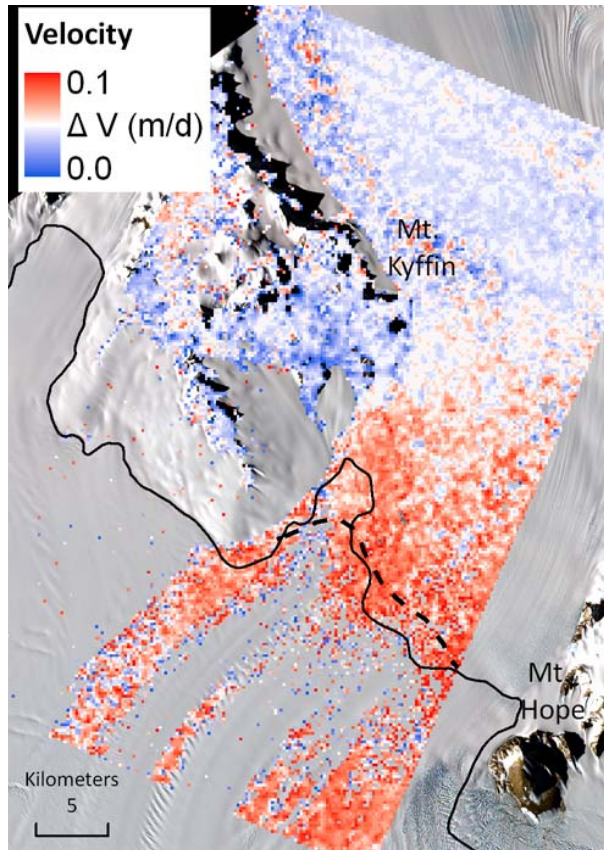


Fig. 5b. Difference in absolute velocity between Mar-1/2 and Mar-2/3. Poor image coherence reduces data quality over the ice shelf.

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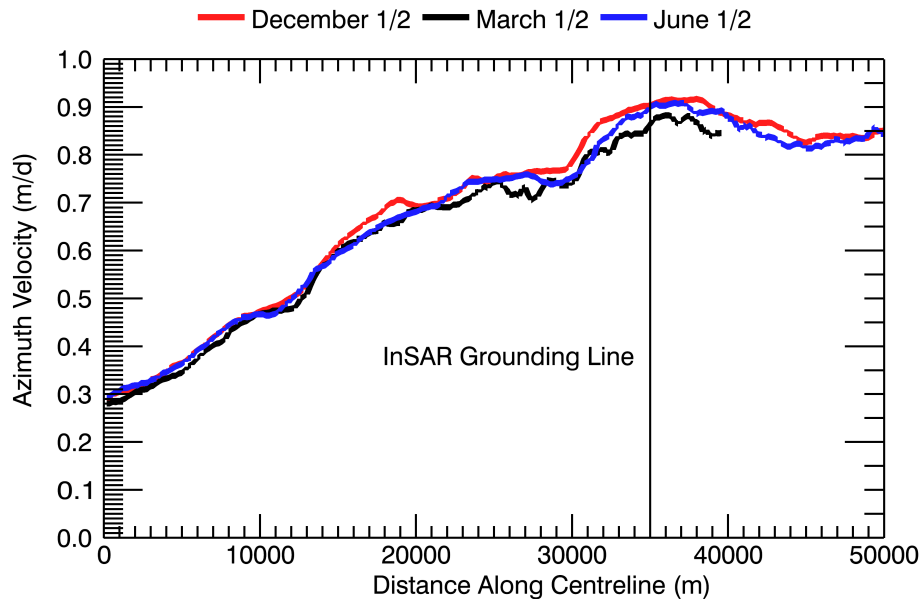


Fig. 6. TerraSAR-X velocities in radar azimuth direction for December 2010, March 2012 and June 2012. The location of the centreline is shown in Fig. 4 with the origin at the upstream edge of the image.