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# Numerical simulations of Gurenhekou Glacier on the Tibetan Plateau using a full-Stokes ice dynamical model

L. Zhao<sup>1</sup>, L. Tian<sup>2,3</sup>, T. Zwinger<sup>1,4</sup>, R. Ding<sup>1</sup>, J. Zong<sup>2</sup>, Q. Ye<sup>2</sup>, and J. C. Moore<sup>1,5,6</sup>

<sup>1</sup>College of Global Change and Earth System Science, Beijing Normal University, China

<sup>2</sup>Key Laboratory of Tibetan Environment Changes and Land Surface Processes, Institute of Tibetan Plateau Research, Chinese Academy of Sciences, Beijing 100085, China

<sup>3</sup>State Key Laboratory of Cryosphere Sciences, Cold and Arid Regions Environmental and Engineering Research Institute, Chinese Academy of Sciences, Lanzhou 730000, China

<sup>4</sup>CSC-IT Center for Science Ltd., Espoo, Finland

<sup>5</sup>Arctic Centre, University of Lapland, P.O. Box 122, 96101 Rovaniemi, Finland

<sup>6</sup>Department of Earth Sciences, Uppsala University, Villavägen 16, 75236 Uppsala, Sweden

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Correspondence to: J. C. Moore (john.moore.bnu@gmail.com)

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## Abstract

We investigate the impact of climate change on a small Tibetan glacier that is representative of the tens of thousands of mountain glaciers in the region. We apply a three-dimensional, thermo-mechanically coupled full-Stokes model to Gurenhekou Glacier located in the southern Tibetan Plateau. The steep and rugged geometry requires use of such a flow model to simulate the dynamical evolution of the glacier. We parameterize the temperature and mass balance using nearby automatic weather stations and an energy balance model for another glacier in the same mountain range. Summer air temperature increased at  $0.02 \text{ K a}^{-1}$  over the past 50 yr, and the glacier has retreated at an average rate of  $8.3 \text{ m a}^{-1}$ . Prognostic simulations suggest an accelerated retreating rate up to  $14 \text{ m a}^{-1}$  for the next 50 yr under continued steady warming, which is consistent with observed increased retreat in the last decade. However, regional climate models suggest a marked increase in warming rate over Tibet during the 21st century, and this rate causes about a 1 % per year loss of glaciated area and glacier volume. These changes imply that this small glacier will probably disappear in a century. Although Tibetan glaciers are not particularly sensitive to climate warming, the rather high warming rates predicted by regional climate models combined with the small sizes of most Tibetan glaciers suggest that significant numbers of glaciers will be lost in the region during the 21st century.

## 1 Introduction

The Tibetan Plateau possesses tens of thousands of mountain glaciers and these glaciers provide water for many big rivers (e.g. Brahmaputra River, Ganges, Yellow River, Yangtze, Indus, Mekong) and have important effects on millions of people's life. Observation shows that many glaciers on the Tibetan Plateau have retreated rapidly in the past 30 yr (Yao et al., 2007a; Xiao et al., 2007; Ding et al., 2006; Ye et al., 2006). Yao et al. (2007a, 2012) showed that there are important regional differences in the

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on-going response of Tibetan glaciers to climate change. The magnitude of glacier retreat increases from the continental interior to the margin of Tibetan Plateau, and reaches its maximum in the southern Tibetan Plateau and the Karakorum Mountains. Shi and Liu (2000) estimated future shrinkage of glaciers in China using an empirical relation between glacier and temperature rise since the Little Ice Age, finding that sub-continental glaciers would loose about 48 % of their volume by 2100 under a 3°C temperature rise scenario. However, little work has been done modeling the future evolution of the glaciers when driven by climate model scenarios. Here we consider a small but representative glacier in the southern Tibetan Plateau and simulate its evolution in the next 50 yr under regional climate model forcing.

Few glaciers on Tibetan Plateau and surrounding regions have detailed geophysical observations, making modeling of their further evolution problematic. Glacier No. 1 has been modeled with the widely used Shallow Ice Approximation (SIA) ice dynamics models (Li H., 2010; Zhou et al., 2009). However, the steep and rough geometry combined with significant aspect ratio makes such SIA models theoretically unsuitable (e.g. Blatter et al., 2010, 2011; Greve and Blatter, 2009; Le Meur et al., 2004). In defense of such approaches it may be argued that on shorter timescale surface mass balance plays a much greater role in glacier evolution than flow dynamics since accumulation rates are relatively high while ice velocities are relatively low. A higher order flow dynamics model, however, is useful for looking at long term (multi-decadal) change and non-steady state conditions.

The open source numerical code Elmer/Ice solves the complete three-dimensional, thermo-mechanically coupled ice dynamics equations (a so-called “full-Stokes” model, e.g. Zwinger and Moore, 2009; Zwinger et al., 2007). In addition to being suitable for mountain glacier dynamics, the model requires very few input data, essentially the bed and surface geometry and estimates of the basal heat flux, surface mass balance and temperature. In this article, the model is applied to Gurenhekou glacier (90° 28' E, 30° 11' N) which is located in the southern Tibetan Plateau, to simulate the ice dynamics in the present day and predict the dynamical evolution of this glacier in the next five

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decades. To the best of our knowledge, this is the first use of a full-Stokes model to a glacier on Tibetan Plateau.

## 1.1 Gurenhekou glacier

Gurenhekou glacier is a small cold alpine-type valley glacier in the southeast part of Nyainqentanglha Range in the central part of the southern Tibetan Plateau (Fig. 1). The region is of special interest for glacio-climatological research as it is influenced by both the continental climate of Central Asia and the Indian monsoon system, and is situated at the transition zone between temperate and sub-continental glaciers. The glacier is strikingly regular in shape, with an area of  $1.40 \text{ km}^2$  and a length of 2.9 km (Fig. 2). The elevation of Gurenhekou glacier is about 5500 ~ 6000 m a.s.l. (Pu et al., 2006; Ma et al., 2007). The glacier is smooth and flat at the surface, but steep at the tongue and the mountain ridge at the sides of the glacier. Gurenhekou glacier is a summer-accumulation type of glacier, like most of glaciers on the Tibetan Plateau (Shi, Y., 2000; Fujita et al., 2000; Ageta et al., 1992).

Ground penetrating radar (GPR) and differential GPS measurements were taken in the years 2007, 2009 and 2011 (Ma et al., 2008, see Fig 2.). The surface elevation was measured along all the tracks in Fig. 2, and bed elevation only along the tracks “2-2009”, “3-2009”, “1-2007”, and “2-2007”. Elevations above 5860 m were not surveyed due to terrain hazards, but ice thickness appears to be rather thin in those regions. The maximum thickness observed was 140 m along a transverse line and about 550 meters away from the head of this glacier.

## 2 Surface temperature and surface mass balance on the glacier

On decadal time scales, regional climate has strong control on glacier’s surface temperature and surface mass balance (SMB), which in combination are the main driving force of the glacier dynamics and important boundary conditions to the full-Stokes

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model. Therefore, correctly prescribing these two input fields is vital for accurate simulations and predictions of the present day and the future.

2.1 Model setup

We constructed surface and bedrock digital elevation model (DEM) for the year 2007. Surface temperature was estimated by using the annual mean air temperature and lapse rates from 9 automatic weather stations (AWS) set up at a southern slope of Nyainqentanglha Range (Xie et al., 2010). A temperature inversion exists below elevations of 4950 m, so we confine our data to 4 AWS above 4950 m to estimate the surface temperature as a function of elevation ( $z$ )

$$T(z) = 273.15 + 37.17 - 0.0075z, \tag{1}$$

where the temperature  $T$  is in units of Kelvin,  $z$  denotes the elevation, and the lapse rate is  $-0.0075 \text{ Km}^{-1}$ . This regression neglects the temperature offset due to the presence of the glacier influencing local climate that may range from  $0.2^\circ\text{C}$  to  $3.5^\circ\text{C}$  (Shi, 2000). However, since the glacier is relatively small, and the ice free slopes are extensive (Figs. 1, 2), we neglect this effect. Since the glacier is below melting point throughout (see the diagnostic model, below), this offset would make little difference to the simulations in any event. Geothermal heat flux is approximated by using a measured temperature profile in an ice-core borehole of Naimonanyi Glacier on the southwestern Tibetan Plateau (Yao et al., 2007b) and taken as  $78.6 \text{ mW m}^{-2}$ .

2.2 Surface mass balance

Little information of surface mass balance is available for Gurenhekou glacier, due to the harsh climatic conditions and high altitude. By comparing the surface elevation along the central longitudinal profiles measured in 2007 and 2011 (Fig. 2), annual averaged rate of surface elevation change is obtained in the lower part of glacier (Fig. 3). In addition, mass balance during the period 2004–2010 was measured (Yao et al., 2012)

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at 12 stakes on the glacier. Since the observations are over a relatively short period, we have to also rely on modeled surface mass balance. Caidong and Sorteberg (2010) used an energy balance model to simulate the mass balance of Xibu glacier (90° 36' E, 30° 23' N), which is a large glacier (12.7 km long) in the central part of Nyainqentanglha Range and 25 km northeast of Gurenhekou glacier. Their model produces three distinct mass balance regions as a function of altitude. It is reasonable to suppose that Gurenhekou glacier exhibits a similar mass balance profile, and we prescribe a mass balance gradient and SMB for each of these three regions. We can test this hypothesis using the observed change of the glacier surface elevation and the stake mass balance measurements (Fig. 3).

The vertical mass balance gradient ( $\beta$ ) we use for Gurenhekou glacier is a function of altitude ( $z$ ) and equilibrium line altitude (ELA)

$$\beta = \begin{cases} \beta_1 = 6 \times 10^{-4}, & \text{ELA} + 170 < z < 6100 \\ \beta_2 = 0.013, & \text{ELA} - 40 < z < \text{ELA} + 170, \\ \beta_3 = 5 \times 10^{-3}, & 5400 < z < \text{ELA} - 40 \end{cases} \quad (2)$$

and similarly the annual surface mass balance is

$$\text{SMB}(z) = \begin{cases} 170\beta_2 + \beta_1(z - \text{ELA} - 170), & \text{ELA} + 170 < z < 6100 \\ \beta_2(z - \text{ELA}), & \text{ELA} - 40 \leq z \leq \text{ELA} + 170. \\ -40\beta_2 - \beta_3(\text{ELA} - 40 - z), & 5400 < z < \text{ELA} - 40 \end{cases} \quad (3)$$

The unit of SMB and  $\beta_i$  ( $i = 1, 2, 3$ ) here is  $\text{m a}^{-1}$  (ice equivalent) and  $\text{a}^{-1}$ , respectively.

The ELA of Gurenhekou glacier in the year 2008 is about 5800 m (Yao et al., 2012). Using Eq. (2) and (3) with an ELA = 5800 m is consistent with the rate of surface change observed during 2007 ~ 2011 and the stake measurements during 2004 ~ 2010 (Fig. 3).

Since the glacier is a summer accumulation type, the ELA is essentially determined only by the summer (JJA) climate. We can estimate the dependence of ELA on climate

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using the six balance years during 2004 ~ 2010 (Yao et al., 2012) and observed JJA-temperature and JJA-precipitation at Lhasa station during 2005 ~ 2010. We find that a 1 K air temperature rise results in a shift of ELA by  $79 \pm 30$  m on Gurenhekou glacier. There is no statistically significant dependence of ELA on JJA-precipitation. Hence,

5 ELA in the  $k$ th year starting from the year 2008 is estimated by

$$ELA_{(k)} = 5800 + 79\Delta T_{(k)}, \quad (4)$$

where  $\Delta T$  is the net change of JJA-temperature between 2008 and the  $k$ th year and  $79 \text{ m K}^{-1}$  is the sensitivity of ELA to temperature change.

### 3 Numerical model

#### 10 3.1 Geometry set-up and meshing

We constructed a digital elevation model (DEM) of the surface and bedrock by interpolation of the GPS and radar profiles (Fig. 2). Both the bedrock and surface profiles were smoothed and extended to the boundary defined from satellite images. Using the surface and bedrock DEM and the boundary shape, the three-dimensional geometry of Gurenhekou glacier was built by extruding the two-dimensional footprint from the bedrock to the surface containing 15 terrain-following layers of varying thickness (Fig. 4). We applied a refinement of layer thickness towards the bedrock to capture the highest deformation rates better. Additionally, a vertically section along the center line of the glacier was included for post processing reasons. The three-dimensional mesh

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20 consists of 62 271 nodes and 78 197 elements (including boundary elements). The domain is decomposed into 6 parts for parallel computation. A diagnostic (steady state with fixed geometry) run only required 20 min, and the 50 yr prognostic run completed within 17 h on a workstation.

### 3.2 Governing equations and boundary conditions

A three-dimensional, thermo-mechanically coupled full-Stokes model was employed to model the glacier dynamics. Elmer/Ice uses the Finite Element Method (FEM) to solve the partial differential equations. The full-Stokes model consists of a momentum conservation equation, a mass conservation equation for an incompressible fluid and a heat transfer equation for the temperature:

$$\nabla \cdot \boldsymbol{\tau} - \nabla p = \rho \mathbf{g}, \quad (5)$$

$$\text{div} \mathbf{u} = 0 \quad (6)$$

$$\rho c \left( \frac{\partial T}{\partial t} + (\mathbf{u} \cdot \nabla) T \right) = \text{div}(\kappa \nabla T) + \sigma, \quad (7)$$

where  $\mathbf{u} = (u_x, u_y, u_z)$  denotes the ice flow velocity,  $T$  is the temperature,  $p$  is the pressure, and  $\mathbf{g}$  is the gravity acceleration. Ice density  $\rho$  is assumed to be constant  $910 \text{ kg m}^{-3}$  due to the incompressibility condition. The deviatoric stress tensor,  $\boldsymbol{\tau}$ , is related to strain rate tensor,  $\boldsymbol{\varepsilon} = (\nabla \mathbf{u} + \nabla \mathbf{u}^T)/2$ , by the inverse form of Glen's Law (Cuffey and Paterson, 2010):

$$\boldsymbol{\tau} = A(T)^{-1/3} \varepsilon_E^{-2/3} \boldsymbol{\varepsilon}, \quad (8)$$

where  $\varepsilon_E = \sqrt{\frac{1}{2} \text{tr}(\boldsymbol{\varepsilon}^2)}$  is the effective strain tensor. The rate factor  $A(T)$  is described by the Arrhenius law and the enhancement factor  $E$  is taken as 1. The heat capacity  $c$  and the heat conductivity  $\kappa$  are functions of temperature

$$c(T) = 146.3 + 7.253T, \quad \kappa(T) = 9.828 \exp(-5.7 \times 10^{-3}T) \quad (9)$$

where the temperature is in Kelvin. Due to the relatively low strain-rates and stresses, we neglect the internal heat source  $\sigma$  caused by strain heating.

Given the geothermal heat flux and surface temperatures of the glacier, we expect that the glacier is below melting point throughout the whole domain (this is supported

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by the simulations below). Hence, we prescribe a no-slip boundary condition for velocity at the bedrock. At the surface of the glacier, the atmospheric pressure and wind stress exerted against the upper interface is neglected, which implies the deviatoric stress vector on the tangential plane of the surface vanishes, i.e.

$$\tau \cdot \mathbf{n}|_{\text{surface}} = 0 \quad (10)$$

where  $\mathbf{n}$  is the unit normal vector of the surface.

The temperature at the glacier surface is taken as a function of elevation, see Eq. (1). At the bedrock, a Neumann boundary condition for the temperature is set:

$$\kappa(T) \frac{\partial T}{\partial \mathbf{n}} = q_{\text{geo}}, \quad (11)$$

where the geothermal heat flux  $q_{\text{geo}}$  is taken as  $78.6 \text{ mW m}^{-2}$ , as described earlier.

For the prognostic run, the kinematic boundary condition is applied at the surface since the surface elevation change with time,

$$\frac{\partial h}{\partial t} + u_x \frac{\partial h}{\partial x} + u_y \frac{\partial h}{\partial y} - u_z = \text{SMB}, \quad (12)$$

where  $h$  is the surface elevation, and the surface mass balance SMB is estimated by using Eqs. (2–3). The full-Stokes model is solved by using an open source FEM package Elmer/Ice (<http://elmerice.elmerfem.org>).

### 3.3 Model experiments

We perform 3 separate simulations. The first is diagnostic simulation, i.e. assuming steady state with constant surface elevation which then defines a mass balance pattern over the glacier that is constant over time. We also perform 2 prognostic simulations with differing 21st century temperature increases to produce mass balance on the glacier as a function of elevation and time. To produce estimates of warming rate

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representative of the later half of the 20th century and the first half of this century, we use results from the Regional Climate Model Version 3.0 (RegCM3). The horizontal grid spacing of RegCM3 is 25 km, and the model domain covers all of China and surrounding East Asia areas (Gao et al., 2012). RegCM3 reproduces the observed spatial structure of surface air temperature and precipitation well.

Since the glacier is a summer accumulation type, conditions in June, July and August are far more important than the rest of the year. Figure 5 shows summer annual surface temperature evolution from 1951 to 2100 for the nine 25 × 25 km grid boxes centered on the cell containing Gurenhekou glacier. Since we are interested in climatic impacts rather than inter-annual variability in ELA caused by factors such as monsoon intensity etc. we focus on the smoothed response to temperature rises. Figure 5 shows that two simple linear rates ( $\dot{T}$ ) of temperature rise fit both, the past simulated temperature history, and the simulated future temperature rise well. The historical simulation rate for the period 1955 to 2005 is 2 °C per century. This is also the observed temperature rise rate at Lhasa station (the station was established in 1955), hence we have confidence that the regional model reproduces observed temperature trends well in this area, and that this rate represents the on-going situation on the glacier. The second prognostic simulation uses a rate of 5 °C per century for warming which is the slope of the RegCM3 result for the period 2005–2100.

### 3.3.1 Diagnostic simulation

The initial surface DEM was built for the year 2007. The surface was kept constant at the 2007 geometry. The thermo-mechanically coupled model then produces a so-called “diagnostic” simulation for this geometry by using a fixed point iteration scheme. Figure 6 shows the simulated surface velocity. The maximum speed found is 1.92 m a<sup>-1</sup> around the middle part of the glacier. The surface velocity in the southern terminus is about 0.4 m a<sup>-1</sup> due to the steep surface slope there. The temperature distribution at the bedrock and along the center line in Fig. 7 shows that the whole glacier is below pressure melting point. The highest temperature is about –1.6 °C, hence justifying the

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no basal sliding condition we imposed in the model setup. We also performed a “surface relaxation” experiment (Zwinger and Moore, 2009) to determine if parts of the glacier exhibit unrealistic surface velocities that are likely caused by errors in the surface or bedrock DEMs. We find that this procedure did not detect systematic errors in the DEMs we used.

### 3.3.2 Prognostic simulations with $\dot{T} = 0.02$ & $\dot{T} = 0.05$

The dynamical evolution of the glacier is simulated by so-called “prognostic” simulations. The steady state solution from the diagnostic run was taken as the starting point (initial condition) for the prognostic simulation from the year 2008 to 2057. The surface mass balance was calculated by using (2) and (3) for the five decades. The thermo-mechanically coupled full-Stokes model and the kinematic boundary condition (12) were solved at each time step. Consequently, the surface DEM evolved every year due to ice movement and surface mass balance, and the resulting change of surface elevation and ELA then changed the surface mass balance. The surface elevation change from 2008 to 2057 is shown in Fig. 8. The termini in the year 2007, 2032 and 2057 are compared in Fig. 9.

In the first 25-yr period 2008–2032, the terminus of glacier in the northeast retreats more intensively than that in the southwest due to thinner ice there. The maximal retreat rate is about  $13 \text{ m a}^{-1}$  in the northeast of the tongue and  $4.6 \text{ m a}^{-1}$  in the southwest for the period 2008–2032. There is no noticeable difference in both retreat rate and percentage of area loss for the period 2008–2032 between prognostic simulations using temperature rise rate of  $\dot{T} = 0.02 \text{ K a}^{-1}$  and using  $\dot{T} = 0.05 \text{ K a}^{-1}$  (see Table 1).

Using topographic maps and aerial photos, the annual average retreat rate of this glacier was about  $7.0 \text{ m a}^{-1}$  from the last of Little Ice Age to the 1970s and  $8.3 \text{ m a}^{-1}$  during 1974–2004. In-situ observations showed that the glacier retreated at  $9.5 \text{ m a}^{-1}$  from 2004 to 2005 and  $17.0 \text{ m a}^{-1}$  from 2005 to 2006 (Pu et al., 2006). Hence the modeled retreat rate is consistent with the trend over the last decade. The similarity of retreat rate under the  $2^\circ\text{C}$  and  $5^\circ\text{C}$  per century scenarios shows that the observed rapid

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acceleration between 2004 and 2006 is likely due to inter annual climate variability and stochastic variability in local ice thickness rather than to a change in summer warming rate. The modeled retreat rate is also consistent with the retreat rates of about  $10 \text{ m a}^{-1}$  for five glaciers in Nyainqentanglha range from 1976 to 2009 (Bolch et al., 2010).

5 The annual average area reduction rate during 2008–2032 is about  $-0.96\%$  with  $\dot{T} = 0.02 \text{ K a}^{-1}$  and  $-1.08\%$  with  $\dot{T} = 0.05 \text{ K a}^{-1}$ . These estimates are much greater than annual area change observed in southeast Nyainqentanglha Range during the period 1980–2001 of  $-0.17\%$  per year (Yao et. al, 2012) and during 1976–2001 of  $-0.22\%$  per year (Bolch et al, 2010) based on remote sensing images and maps, but similar  
10 to the estimated  $-0.7\%$  per year from Frauenfelder and Kääb (2009) over a similar period. We discuss these differences further in Sect. 4.

In the second 25 yr period 2033–2057, the retreat rates of glacier terminus using  $\dot{T} = 0.02 \text{ K a}^{-1}$  and  $\dot{T} = 0.05 \text{ K a}^{-1}$  are also similar, with the maximum of about  $14.6 \text{ m a}^{-1}$ . However, there is obviously more area reduction (see Table 1) from prognostic simulations using  $\dot{T} = 0.05 \text{ K a}^{-1}$  than that using  $\dot{T} = 0.02 \text{ K a}^{-1}$ . The largest differences are in the upper glacier, since there the glacier is very thin and surface lowering exposes bedrock (see Fig. 8). The annual average area decreasing rate during  
15 2033–2057 is  $-0.44\%$  with  $\dot{T} = 0.02 \text{ K a}^{-1}$  and  $-0.74\%$  with  $\dot{T} = 0.05 \text{ K a}^{-1}$ .

In either case using  $\dot{T} = 0.02 \text{ K a}^{-1}$  or  $\dot{T} = 0.05 \text{ K a}^{-1}$ , the area loss rate is slower  
20 in the second 25 yr than the first 25 yr, however, the volume shrinkage rate is almost the same during the five decades. Faster increasing temperature rate causes greater surface thinning (Fig. 8) and more intensive volume loss (see Table 1).

The surface velocity pattern of the ice flow looks similar in each year, but the magnitude of surface velocity shows a decreasing trend. The maximum value of surface velocity decreases from  $1.92 \text{ m a}^{-1}$  in the year 2007 (Fig. 6) to  $0.96 \text{ m a}^{-1}$  with  $\dot{T} = 0.02 \text{ K a}^{-1}$  and  $0.32 \text{ m a}^{-1}$  with  $\dot{T} = 0.05 \text{ K a}^{-1}$  in the year 2057 (Fig. 9). The decreasing trend is because the glacier thinning dominates ice flow speed despite the  
25 increasing steepness as the accumulation area builds up and the ablation area thins.

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Basal temperatures remain below pressure melting point throughout the period 2008–2057.

In these simulations we limited the maximal surface increase at any point on the glacier to 15 m. We chose to do this because the valley glacier is unlikely to grow above the level of the surrounding mountain ridge and side walls. If the glacier did grow the flow geometry would change dramatically as overflow out of the valley would occur (with no geomorphological evidence of it having done so), and also the new geometry would affect the snow accumulation pattern and effectively destroy the basic assumptions of the mass balance model. However we tested the impact of such a constraint on ice elevation increase in the accumulation area on the net glacier area and volume change. We performed two prognostic simulations for 20 yr using  $\dot{T} = 0.02 \text{ Ka}^{-1}$ : one as previously with maximal surface increase restricted by 15 m, and the other with unrestricted elevation rise. The surface changes in two cases are shown in Fig. 10. Only a small fraction of glacier surface increases by more than 15 m in the unrestricted case. The area loss is the same in both cases, at the rate of  $-0.91\%$  per year. The annual volume change rate is  $-0.85\%$  in the unrestricted case and  $-0.89\%$  in the restricted case. Therefore, we are confident that the maximal surface increase of 15 m will keep this glacier geometry realistic and will not introduce large differences in estimates of glacier change.

## 4 Discussion and conclusion

Prognostic simulations have been made for the period 2008–2057 using different temperature change rates,  $\dot{T} = 0.02 \text{ Ka}^{-1}$  and  $\dot{T} = 0.05 \text{ Ka}^{-1}$ , to produce mass balance on the glacier as a function of elevation and time. For the first 25 yr period 2008–2032, the computed maximal retreat rate for Gurenhekou glacier is about  $13 \text{ ma}^{-1}$ , and the annual average area reduction rate is about  $-0.96\%$  with  $\dot{T} = 0.02 \text{ Ka}^{-1}$ . There is no noticeable difference in terminus retreat rate and area change rate between prognostic simulations using  $\dot{T} = 0.02 \text{ Ka}^{-1}$  and  $\dot{T} = 0.05 \text{ Ka}^{-1}$ . For the second 25 yr

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period 2033–2057, the computed maximal retreat rate for Gurenhekou glacier is about  $14.6 \text{ m a}^{-1}$ , and the annual average area loss rate is about  $-0.44 \%$  with  $\dot{T} = 0.02 \text{ K a}^{-1}$  and  $-0.74 \%$  with  $\dot{T} = 0.05 \text{ K a}^{-1}$ . The modeled retreat rate is consistent with the trend observed over the last decade.

In either scenario,  $\dot{T} = 0.02 \text{ K a}^{-1}$  or  $\dot{T} = 0.05 \text{ K a}^{-1}$ , the area loss rate is much slower in the second 25 yr than the first 25 yr, however, the rate of volume loss remains almost unchanged over the whole five decades. This is because for this uniform width glacier, the volume loss depends mostly on the surface mass balance. The function we specify for mass balance depends linearly on temperature which we increase at constant rate over time in our scenarios. In contrast, the rate of area loss depends on the relative surface and bedrock slopes close to the terminus. The higher temperature rise rate  $\dot{T} = 0.05 \text{ K a}^{-1}$  results in more surface thinning, and hence greater volume loss than the lower temperature rise rate.

The annual average volume change for the period 2008–2057 is about  $-1.03 \%$  using  $\dot{T} = 0.02 \text{ K a}^{-1}$  and  $-1.46 \%$  using  $\dot{T} = 0.05 \text{ K a}^{-1}$ , respectively. These changes suggest that this glacier will probably disappear within a century. This glacier is typical in many respects of many small glaciers in the Nyainqentanglha region: in its size, elevation range, recent retreat rate and aspect. Bolch et al. (2010) report that only about 40 out of 960 glaciers in the Nyainqentanglha range are larger than  $1 \text{ km}^2$  in area, and they make up about 28 % of the total glacier area. Hence if our results are representative then they suggest that 95 % of glaciers in the range would disappear by 2100. Bolch et al. (2010) estimated that areal loss rates were about  $-0.25 \%$  per year over across the whole the Nyainqentanglha range for the period 1976–2001. This rate is significantly lower than some other studies in the region that report area loss rates of  $-0.7 \%$  per year for southeast Nyainqentanglha range (Frauenfelder and Kääb, 2009). It is clear that some differences in remote sensing and mapping glacier areas result from inconsistencies in defining termini on debris-covered or seasonal snow obscured glaciers. Detailed analysis of five glaciers by Bolch et al. (2010) showed an increased rate between 2001

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and 2009 of  $-0.5\%$  per year, but with large variations from  $-0.16$  to  $-0.84\%$  per year. Hence it is not clear if Gurenhekou glacier is really representative in its area loss rate.

Reasons for differences in mass wastage estimates include varying climate across the mountain range (Shangguan et al., 2008), debris cover which provides insulating cover on small scales but can cause accelerated mass loss on larger scales (e.g. Benn et al., 2012), and general stochastic variability between glacier responses to climate forcing. There is a difference in climate between the northeast and southwest sides of the Nyainqentanglha range (Shangguan et al., 2008), with the southeast side receiving more snow fall than the northwest side and also more direct radiation, at present the two sides have similar average areal loss rates (Bolch et al., 2010; Shangguan et al., 2008). In future, since regional climate models suggest only modest increases in precipitation, but large temperature rises, it is likely that southerly facing glaciers will accelerate their mass loss. Furthermore using the past changes as guide to future change may not be reliable as decreases in surface albedo from deposition of anthropogenic pollutants is becoming more significant (Xu et al., 2009; Ramanathan and Carmichael, 2008). In the Nyainqentanglha range only about 29 glaciers have significant debris cover (Bolch et al., 2010), and recent observations of glacier thinning rates on the Tibet Plateau indicate similar rates for both clean and debris covered glaciers (Kääb et al., 2012; Gardelle et al., 2012). This can be explained by the spatially inhomogeneous ablation processes on debris covered glaciers (Gardelle et al., 2012; Benn et al., 2012) whereby the peak ablation occurs up-glacier of the tongue and is driven by rapid down-wasting associated with supraglacial melt ponds and thermokarst processes that effectively cut off the terminus from the dynamical ice flow. Over Tibet as a whole, total volume is likely dominated by ice in large glaciers. These glaciers, being thicker, will suffer proportionally less ice wastage per year and remain well past the end of this century.

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**Table 1.** Annual area and volume percentage change during 2008–2057 from the prognostic simulations with  $\dot{T} = 0.02 \text{ K a}^{-1}$  and  $\dot{T} = 0.05 \text{ K a}^{-1}$ .

Periods	$\dot{T} = 0.02 \text{ K a}^{-1}$		$\dot{T} = 0.05 \text{ K a}^{-1}$	
	$\Delta A$	$\Delta V$	$\Delta A$	$\Delta V$
2008–2032	–0.96 %	–0.99 %	–1.08 %	–1.33 %
2033–2057	–0.44 %	–1.07 %	–0.74 %	–1.59 %
2008–2057	–0.70 %	–1.03 %	–0.91 %	–1.46 %

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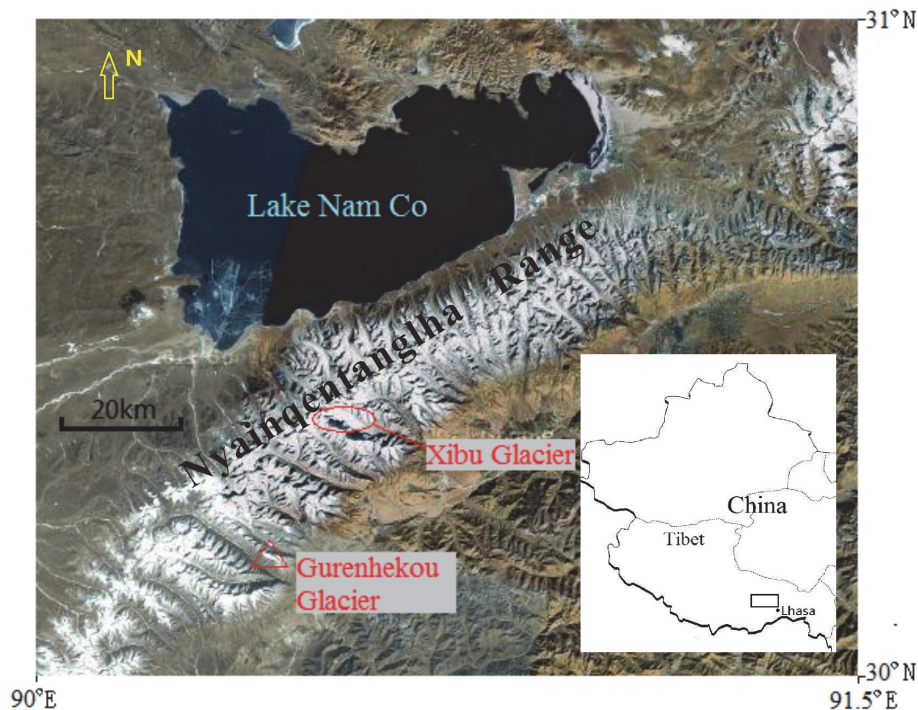
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**Fig. 1.** The location of Nyainqentanglha Range, Lake Nam Co, Gurenhekou glacier and Xibu glacier. The box in the map of China indicates the location of study area in China.

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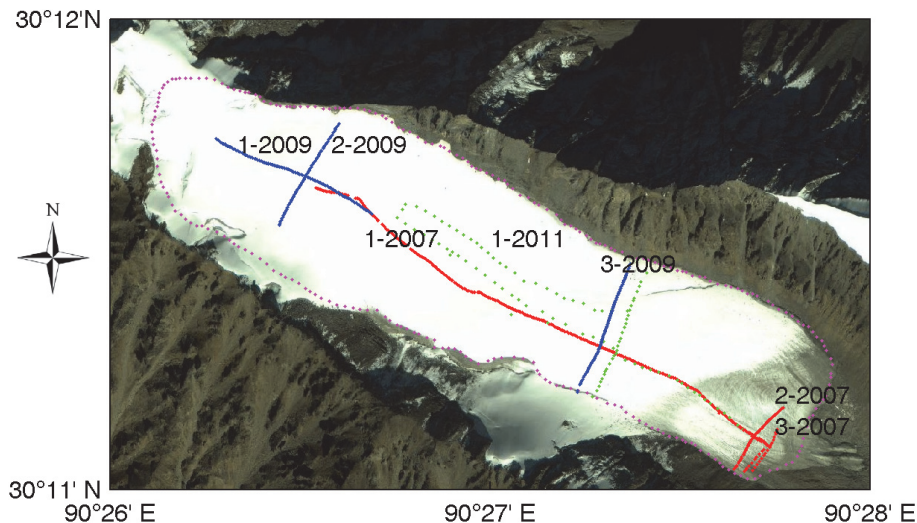
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**Fig. 2.** The magenta curve is the boundary profile of Gurenhekou glacier. The boundary profile of the glacier is taken from satellite remote sensing image, and fits well with the real image of the glacier from Google maps. Seven tracks were measured in the years 2007, 2009 and 2011. Tracks in different years are denoted in different colors: red for 2007, blue for 2009, green for 2011. For instance, “1-2009” means the first track measured in the year 2009.

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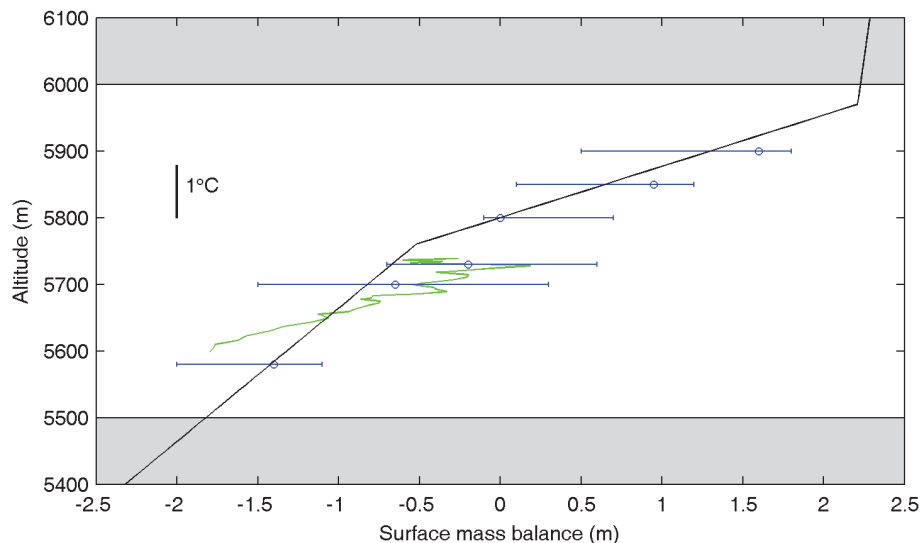
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**Fig. 3.** Annual surface mass balance modeled by Eqs. (2) and (3) with ELA = 5800 m (black curve). The grey region corresponds to the altitude outside the altitude range of Gurenhekou glacier, which is 5500 ~ 6000 m a.s.l. The green curve is the rate of annual average surface change observed during the year 2007 ~ 2011. The blue circles represent the median value of SMB from stake measurements (Yao et al., 2012), and the blue bar widths shows their variability. The vertical bar represents the change in ELA for a 1 °C change in summer temperature.

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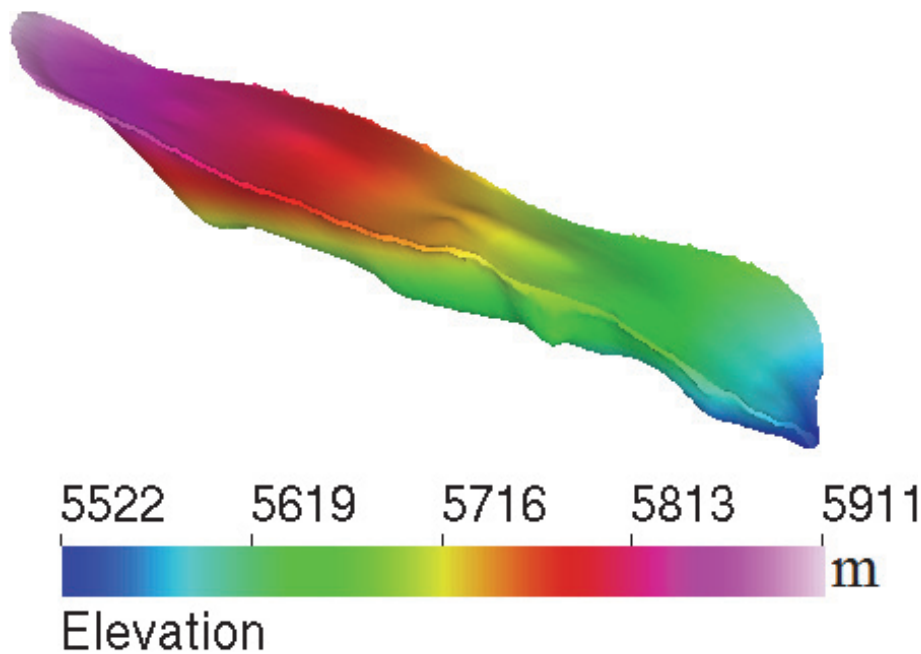
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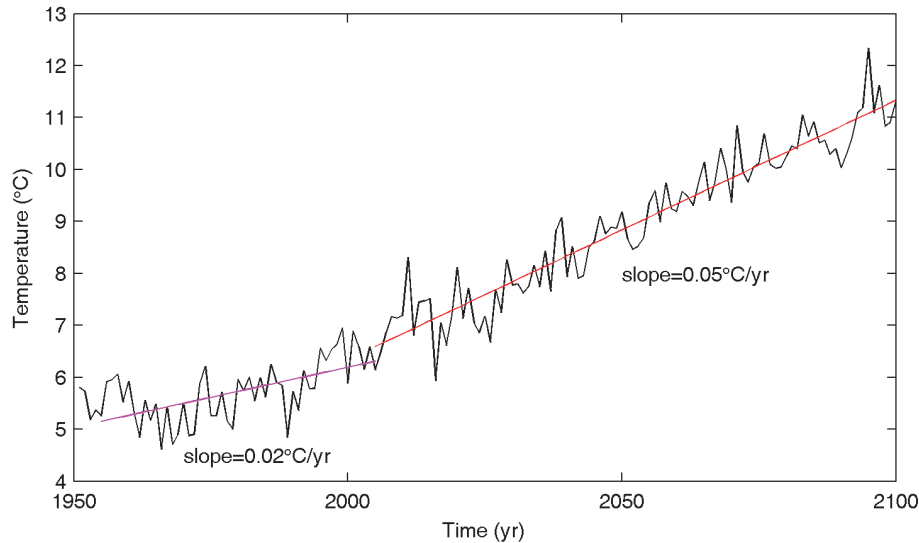
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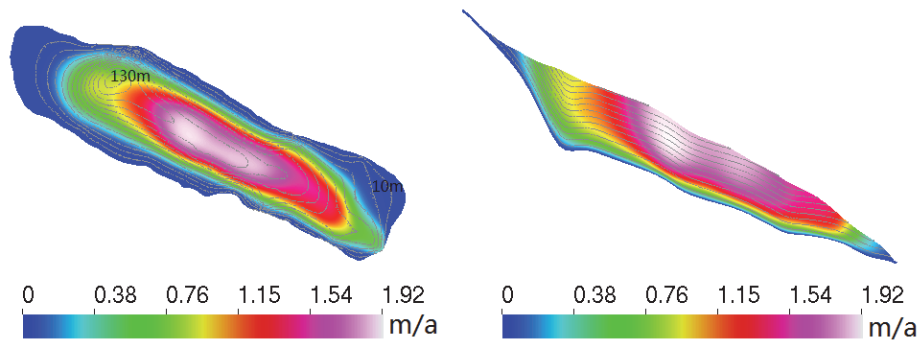


**Fig. 4.** Three-dimensional representation of the glacier geometry created by DEM (the vertical coordinate is stretched by a factor of 3).



**Fig. 5.** JJA-mean air temperature from RegCM 3.0 simulations for mean temperatures of the 9 grid cells surrounding Gurenhekou glacier. The linear warming trends for the periods 1955 ~ 2005 and 2005 ~ 2100 are drawn in magenta and red, respectively.





**Fig. 6.** The absolute value of ice flow velocity on the surface (left) and on the transect along the central line (right) of the diagnostic run (the vertical coordinate is stretched by 3). The contours indicate the ice thickness in 10 m interval from 10 m to 130 m.

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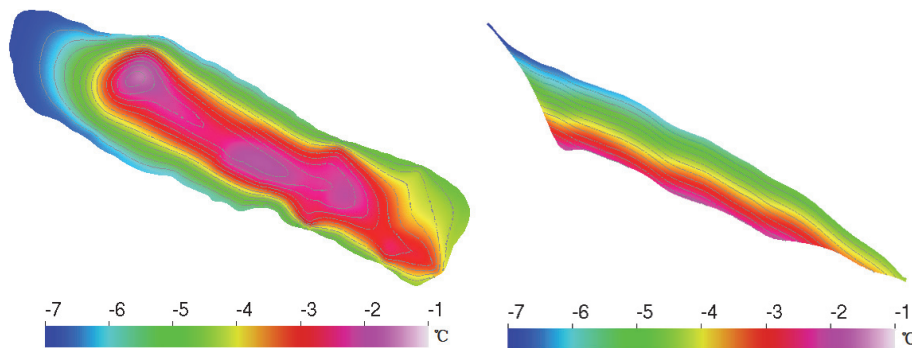
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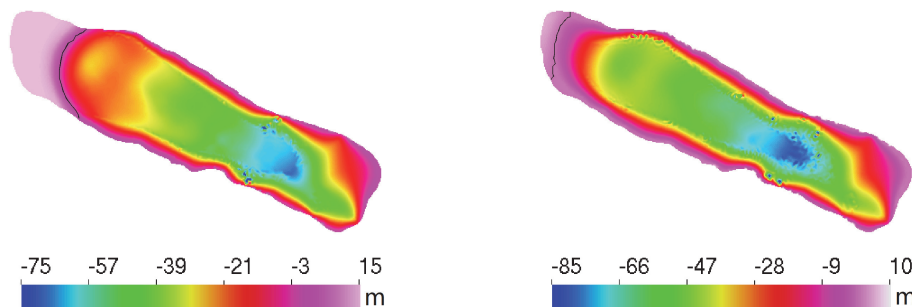
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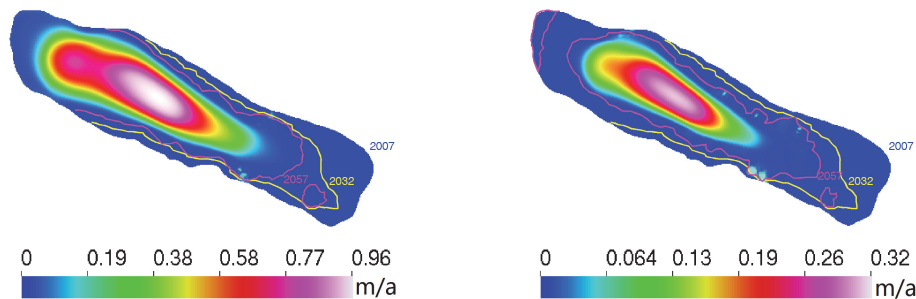




**Fig. 7.** Distribution of temperature relative to pressure melting point at the bedrock (left) and along the center line (right) of the diagnostic run (the vertical coordinate is stretched by 3). The contours indicate the ice thickness in 10 m interval from 10 m to 130 m.



**Fig. 8.** Surface elevation change from 2008 to 2057 of prognostic simulations with  $\dot{T} = 0.02 \text{ K a}^{-1}$  (left) and  $\dot{T} = 0.05 \text{ K a}^{-1}$  (right). The black solid lines indicate zero net elevation change.



**Fig. 9.** Result for surface flow velocity in the year 2057 of prognostic simulations with  $\dot{T} = 0.02 \text{ Ka}^{-1}$  (left) and  $\dot{T} = 0.05 \text{ Ka}^{-1}$  (right). The color bar shows the magnitude of velocity. The computed position of outlines in 2032 and 2057 are marked with solid lines in yellow and magenta, respectively.

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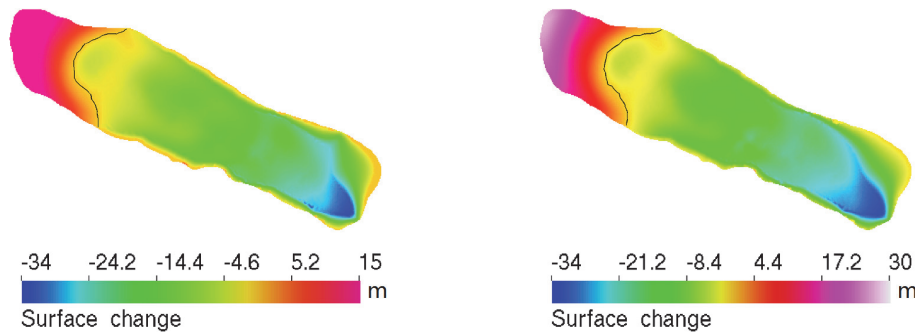
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**Fig. 10.** Surface elevation change from 2008 to 2027 with surface increase restricted by 15 m (left) and unrestricted (right) from prognostic simulations using  $\dot{T} = 0.02 \text{ K a}^{-1}$ . The black solid lines indicate zero net elevation change.