

# 1 Pre-calibration of a simple Greenland Ice Sheet model for 2 use in integrated assessment studies

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## 14 15 **Abstract**

16 The Greenland Ice Sheet is vulnerable to climate warming, possibly resulting in substantial  
17 future sea level rise. Integrated assessment models combine treatments of the global economy  
18 with simplified treatments of Earth system processes. Such models are used to assess  
19 economic impacts of climate change and to identify optimal strategies for responding to  
20 climate change (for example). However, many integrated assessment models lack interactive  
21 treatments of Greenland Ice Sheet behavior. Here, we adapt a previously-published, simple  
22 model of the Greenland Ice Sheet for use in integrated assessment models. The expanded  
23 model includes improved treatments of the surface mass balance, heat transport through the  
24 ice body, and climate-enhanced basal sliding. We calibrate the model against 1) an ice  
25 volume curve from a more-complex model, and 2) data on the ice sheet's past behavior (sea  
26 level contributions in the geologic past and historical mass balance estimates). The tuned  
27 model successfully matches these data sets. Our results suggest that the expanded model can  
28 be a valuable tool for integrated assessment models and sea level studies in general. We also  
29 report implications of our study for the tuning of more-complex ice sheet models.

1

## 2 **1 Introduction**

3 The Greenland Ice Sheet (GIS) is a major feature of the Arctic and may make an important  
4 contribution to future sea level rise. The ice sheet covers an area of  $1.7 \times 10^6 \text{ km}^2$  (Bamber et  
5 al., 2001), and has a maximum elevation of 3.3 km above sea level (Ekholm, 1996). Its  
6 reflective surface and height exert an important control over middle to high northern latitude  
7 climates (Roe and Lindzen, 2001; Toniazzi et al., 2004; Lunt et al., 2004). If the GIS were to  
8 melt completely, global sea level would rise by an average of approximately seven meters  
9 (Bamber et al., 2001; Lemke et al., 2007). Although Antarctica holds more ice (~60 m sea  
10 level equivalent; Lythe et al., 2001), Greenland is often considered a more immediate concern  
11 because large parts of its surface experience melt conditions during the summer (Mote et al.,  
12 2007). In contrast, surface melting in Antarctica is largely restricted to the Antarctic  
13 Peninsula (Torinesi et al., 2003). Satellite measurements suggest that the GIS mass balance is  
14 already negative, and this negative trend may be accelerating (Velicogna, 2009; Alley et al.,  
15 2010, and references therein).

16 Many computer models describe the Greenland ice sheet's behavior (e.g., SICOPOLIS, Greve,  
17 1997; PISM, Bueller and Brown, 2009; Glimmer-CISM, Rutt et al., 2010), and the state of the  
18 art has become much more sophisticated since the Intergovernmental Panel on Climate  
19 Change's Fourth Assessment Report (Solomon et al., 2007). Much post-2007 model  
20 development effort has gone into implementing higher-order treatments of ice flow. Prior to  
21 2007, standard ice sheet models represented ice flow using the shallow-ice approximation  
22 (Hutter, 1983). This simplification applies over the bulk of the Greenland ice sheet, where the  
23 ice is grounded and flow is relatively slow (see Joughin et al., 2010, for surface velocity  
24 maps). However, it fails in ice streams and ice shelves (Kirchner et al., 2011), which are  
25 likely the most sensitive parts of the ice sheet. Improved models (e.g., Price et al., 2011;  
26 ISSM, Larour et al., 2012; Elmer/Ice, Seddik et al., 2012) provide better representations of ice  
27 flow. Other studies improve their models' surface mass balance treatments relative to  
28 standard methods (e.g., Otto-Bliesner et al., 2006; Robinson et al., 2010; Fyke et al., 2011).

29 Integrated assessment models (IAMs) represent the coupled economic-climate system, which  
30 could be strongly affected by sea level rise from enhanced Greenland Ice Sheet mass loss.  
31 Such models often include a relatively sophisticated economic model attached to simplified  
32 treatments of Earth system components (Sarofim and Reilly, 2010). These simplified

1 treatments are tuned to match results from global climate models. Some studies use IAMs to  
2 identify optimal (utility-maximizing) balances between economic growth due to fossil fuel  
3 consumption and avoidance of negative impacts through emissions mitigation or adaptation to  
4 climate change (e.g., Nordhaus, 2008). Other uses include estimation of the social cost of  
5 carbon (the cost that should be imposed on carbon dioxide emissions in order to promote  
6 economically efficient decision-making; cf. Johnson and Hope, 2012), and construction of  
7 future greenhouse gas atmospheric concentration scenarios (e.g., the Representative  
8 Concentration Pathways; Moss et al., 2010).

9 Despite the likely importance of the Greenland Ice Sheet to future sea level change, many  
10 integrated assessment models either lack any representation of the GIS, or use treatments that  
11 are perhaps oversimplified. For example, the US Interagency Working Group on the Social  
12 Cost of Carbon (2010) considered three popular IAMs (DICE, PAGE, and FUND; Nordhaus,  
13 2008; Hope, 2011; Anthoff et al., 2010; Johnson and Hope, 2012). Of these models, only the  
14 regionalized version of DICE calculates enhanced mass loss from the Greenland Ice Sheet  
15 internally. In that model, yearly sea level rise due to GIS melting is a linear function of the  
16 global mean surface air temperature anomaly, and this mass loss decreases exponentially with  
17 the stock of ice remaining in the ice sheet (Nordhaus, 2010).

18 The lack of Greenland Ice Sheet representations in many integrated assessment models  
19 suggests a need for a low-order model that captures relevant feedbacks but is quick to run  
20 (Fig. 1). Experience suggests that many model evaluations are required to satisfactorily  
21 explore parameter space in IAMs (Urban and Keller, 2010; McInerney et al., 2011), given the  
22 large number of unknowns associated with projecting future climate and economic  
23 development. For example, the Interagency Working Group on Social Cost of Carbon (2010)  
24 used  $10^4$  runs per emissions scenario, and Moles et al. (2004) give a figure of  $3.5 \cdot 10^5$  runs.  
25 Assuming a reasonable computing time of six months, these figures suggest a maximum ice  
26 sheet model execution time between 0.75 and 26 minutes, multiplied by the number of  
27 available computer processors. These times assume that the Greenland component dominates  
28 the overall computational cost of the model, but integrated assessment models include many  
29 other components that must be evaluated each time the model is run.

30 Carrying out  $10^4$ - $10^5$  model runs with a three-dimensional ice sheet model would be  
31 prohibitively expensive (Fig. 1). For example, spinning up the three-dimensional, shallow-  
32 ice-approximation model SICOPOLIS (Greve, 1997; sicopolis.greveweb.net) requires  $\sim 1.5$

1 days on one computer processor, with each spinup run covering 125,000 years (q.v.  
2 Applegate et al., 2012). This long spinup allows the modeled ice sheet to achieve a thermal  
3 state that is consistent with climate history (Rogozhina et al., 2011; Bindshadler et al., in  
4 review 2011), and the spinup must be repeated for each new parameter combination that is  
5 investigated. Thus, SICOPOLIS is ~80-3,000 times more expensive to run than the  
6 permissible upper limit for integrated assessment modeling. SICOPOLIS is a shallow-ice  
7 model, meaning that it achieves speed through the neglect of important stresses within the ice  
8 body (Kirchner et al., 2011). More-complex models that represent these stresses (e.g., Price  
9 et al., 2011) would presumably require even more computing time.

10 The problem is simplified somewhat because integrated assessment models only require  
11 estimates of ice volume change over time; accurate simulation of the geographic distribution  
12 of ice is not needed. As they are represented in IAMs, most of the impacts associated with  
13 enhanced mass loss from ice sheets are caused by sea level rise (e.g., Nicholls et al., 2008).  
14 Direct effects from global sea level rise in Greenland itself would be limited; large-scale mass  
15 loss from an ice sheet causes local sea level fall, due to gravitational effects (e.g., Mitrovica et  
16 al., 2009; Gomez et al., 2010).

17 Here, we show that the GLISTEN (GreenLand Ice Sheet ENhanced) model meets the speed  
18 criterion outlined above (Fig. 1), and reproduces ice volume trajectories from the three-  
19 dimensional ice sheet model SICOPOLIS. We also calibrate the model using geological data  
20 and modern observations, including 1) estimates of the ice sheet's contribution to sea level  
21 change at different times in the past (Alley et al., 2010), 2) historical mass balance estimates  
22 (Rignot et al., 2008), and 3) the modern ice sheet profile (Letreguilly et al., 1991).

23 GLISTEN is a Fortran port of an Excel spreadsheet model intended for classroom use  
24 (GRANTISM, the GReenland and ANTArctic Ice Sheet Model; Pattyn, 2006). We change the  
25 name of the port because GLISTEN does not treat the behavior of the East Antarctic ice sheet,  
26 which the predecessor model GRANTISM does. Beyond porting the model, we add  
27 improved treatments of the ice sheet's surface mass balance, heat transport, and climate-  
28 induced enhanced flow.

29 The paper proceeds as follows. Section 2 provides a brief description of the predecessor  
30 model GRANTISM (Pattyn, 2006) and indicates how the GLISTEN port treats various  
31 processes that are important to the real ice sheet. Section 3 describes a precalibration exercise  
32 in which we match GLISTEN to an ice volume curve from a three-dimensional model

1 (SICOPOLIS; Greve, 1997) and to various observational data sets. Finally, Section 4 places  
2 these results in a wider context and concludes the paper.

3

## 4 **2 Model description**

### 5 **2.1 The predecessor model GRANTISM**

6 GRANTISM, the GRGreenland and ANTArctic Ice Sheet Model, describes the response of the  
7 Greenland and Antarctic ice sheets to climate change (Pattyn, 2006). The model treats cross-  
8 sections through both ice sheets; for the Greenland domain, this transect follows the 72nd  
9 parallel. The model is easy to use and is implemented in Microsoft's widely-available Excel  
10 (tm) spreadsheet software.

11 To start GRANTISM (Pattyn, 2006), the user specifies the ice sheet's initial state (either the  
12 present-day ice geometry or an ice-free, relaxed-bedrock state), and the surface air  
13 temperature anomaly relative to the present-day. The user can also disable many processes  
14 that are normally active in the model, such as basal sliding, isostatic adjustment to ice loading  
15 changes, and changes in background sea level. The user then advances the model in time,  
16 with one time step elapsing for each keystroke. As model time advances, four panels on the  
17 model's graphical user interface show changes in ice thickness, bedrock elevation, velocity  
18 (total and basal sliding-only), surface mass balance (total mass balance, accumulation, and  
19 ablation), and surface air temperatures (mean annual and mean summer). The model responds  
20 in a reasonable way to user choices; for example, setting the surface temperature anomaly  
21 greater than zero causes the ice sheet to shrink.

22 GRANTISM (Pattyn, 2006) contains many features of research-grade ice sheet models. In  
23 particular, the model solves the equations describing ice flow using finite-difference methods  
24 (Pattyn, 2006; see also Hindmarsh, 2001; Greve and Calov, 2002; Greve and Blatter, 2009)  
25 much like those employed in more-complex ice sheet models (e.g., SICOPOLIS; Greve,  
26 1997). Besides ice flow, GRANTISM captures the key insight that ice sheet changes depend  
27 primarily on surface air temperatures, snowfall, and the instantaneous state of the ice sheet.  
28 The model's treatment of a profile through the ice sheet is not necessarily a fatal  
29 oversimplification; see Parizek and Alley (2004) and Parizek et al. (2005) for an example of a  
30 research-grade profile model.

1 GRANTISM (Pattyn, 2006) is a user-friendly tool for teaching about the behavior of ice  
2 sheets. However, some modifications are needed before GRANTISM can be incorporated  
3 into integrated assessment studies. The model's implementation in Excel makes it difficult to  
4 couple to other Earth system components, which are typically written in high-level  
5 programming languages such as Fortran. Because it accepts just one surface air temperature  
6 anomaly value at a time, GRANTISM is best suited for examining the steady-state,  
7 equilibrium characteristics of the ice sheet under different climate states (e.g., Pattyn, 2006,  
8 his Fig. 4). Using GRANTISM to determine time-dependent changes in the ice sheet requires  
9 the model to accept input files describing surface air temperature and sea level anomalies over  
10 time.

## 11 **2.2 The updated GLISTEN model**

12 As noted above, GLISTEN is primarily a Fortran port of the predecessor model GRANTISM  
13 (Pattyn, 2006). Many process descriptions in GLISTEN are closely similar or identical to  
14 those in GRANTISM; for example, we retain GRANTISM's semi-implicit finite-difference  
15 methods for solving the ice flow equations. However, our use of Fortran, with an R wrapper  
16 for handling input and output tasks, improves the functionality of the model and makes it  
17 possible to couple GLISTEN to other models. We also update the model's surface mass  
18 balance treatment and add a parameterization of climate-induced enhanced basal slip  
19 (described below).

20 In the remainder of Section 2, we show how GLISTEN handles various ice sheet processes,  
21 being careful to point out similarities and differences between GLISTEN and GRANTISM  
22 (Pattyn, 2006). Each subsection begins with a brief description of how the process being  
23 discussed works on the real ice sheet, for the benefit of scientists from outside the cryosphere  
24 community. Hooke (2005), Greve and Blatter (2009), and Rutt et al. (2009) give more  
25 complete descriptions of ice sheet processes and model treatments.

### 26 **2.2.1 Surface mass balance**

27 At any given point on the Greenland Ice Sheet, the surface mass balance is the difference  
28 between the rate of mass addition by snowfall and the rate of mass loss from melting,  
29 sublimation, and wind erosion. The surface mass balance is positive on the central parts of  
30 the ice sheet, where low surface air temperatures prevent melting, and negative around the

1 margins. Integrating surface mass balance and calving (see below) over the ice sheet's area  
2 gives the ice sheet's instantaneous total mass balance, or its mass change per unit time.

### 3 **2.2.1.1 Accumulation**

4 The amount of yearly snowfall on the Greenland ice sheet is known approximately from field  
5 measurements (e.g., Ohmura and Reeh, 1991; Bales et al., 2006), and likely changes with  
6 background surface air temperature (see review in van der Veen, 2002). The thicknesses of  
7 ice layers in ice cores, and the oxygen isotope values in the same ice layers, provide paired  
8 estimates of the amount of accumulation as a function of surface air temperature anomaly. In  
9 such records, there is a clear contrast between the cold, low-accumulation times of the last  
10 glacial period and the Younger Dryas, and the warmer, higher-accumulation Holocene.  
11 However, the surface air temperature-accumulation relationship breaks down during the  
12 Holocene itself (Cuffey and Clow, 1997). Climate models also give widely diverging  
13 estimates of how much accumulation on Greenland should change with surface air  
14 temperature (van der Veen, 2002; cf. Gregory et al., 2006).

15 GLISTEN treats accumulation  $a_{acc}$  ( $\text{m yr}^{-1}$ ) as a function of the modern-day annual  
16 precipitation averaged over the model profile  $\bar{a}_0$  ( $\text{m yr}^{-1}$ ) and the instantaneous surface air  
17 temperature anomaly  $T_f$  ( $^{\circ}\text{C}$ ),

$$18 \quad a_{acc} = \bar{a}_0 \cdot s^{T_f} \text{ for } T_f < 0, \quad (1)$$

$$19 \quad a_{acc} = \bar{a}_0 \text{ for } T_f \geq 0$$

20 (cf. Pattyn, 2006, his Eqn. 13). Both  $\bar{a}_0$  and  $s$  are tuneable parameters with default values of  
21  $0.41 \text{ m yr}^{-1}$  and  $1.0533$  (unitless; Clausen et al., 1988; Huybrechts and de Wolde, 1999). The  
22 modern-day precipitation values come from previously-published experiments with the  
23 regional climate model RACMO (Ettema et al., 2009) compiled by the seaRISE project  
24 (Bindschadler et al., in review 2011).

25 This approach closely imitates GRANTISM's (Pattyn, 2006), except that the predecessor  
26 model uses a second-order polynomial fit to data from Ohmura and Reeh (1991) instead of  
27 our spatially-constant prefactor.

28 Because Equation 1 use the profile-averaged modern accumulation as a prefactor, GLISTEN  
29 sets accumulation to a constant value everywhere over the model profile. On the real ice  
30 sheet, accumulation is greater around the ice sheet's margins than on the central parts of the  
31 ice sheet (Bales et al., 2006; Ettema et al., 2009). The original GRANTISM second-order

1 polynomial fit shares this problem; its second-order polynomial fit has a maximum in the  
2 center of the ice sheet and declines to zero near the ice margin (Pattyn, 2006, his Fig. 3). Our  
3 approach also presumes that all precipitation falls as snow (see Stone et al., 2010, for a  
4 parallel example). In practice, ~40% of all precipitation over the Greenland Ice Sheet falls as  
5 rain (Bales et al., 2006), which may or may not refreeze in the snow pack (Marsiat et al.,  
6 1994; Reijmer et al., 2012). This treatment also prevents accumulation from going above  
7 present-day values (Pattyn, 2006; cf. Greve et al., 2011), which may be correct; we have little  
8 basis for estimating precipitation change for warmer-than-present climate states.

9 These simplifications likely bias the model's surface mass balance toward more positive  
10 values, other factors being equal. The spatially-constant accumulation field likely increases  
11 the amount of precipitation that falls on the ice sheet, instead of on unglaciated land or the  
12 open ocean. Assuming that all precipitation falls as snow overestimates accumulation over  
13 the whole ice sheet by a factor of ~1.7 (Bales et al., 2006). However, tuning of the model  
14 should allow reasonable representation of the average contribution of these processes to the  
15 ice sheet's mass balance.

#### 16 **2.2.1.2 Ablation**

17 As noted above, local ablation on the Greenland Ice Sheet is the sum of mass losses from  
18 melting, sublimation, and wind erosion. We are unaware of any systematic estimates of wind  
19 erosion, which is sensitive to small-scale topography. Sublimation is usually associated with  
20 high-altitude, low-latitude glaciers that receive little precipitation (e.g., Rupper and Roe,  
21 2008), but also happens on the Greenland ice sheet (Box et al., 2001). However, melting  
22 dominates sublimation when the whole ice sheet is considered (Ettema et al., 2009).

23 GLISTEN calculates ablation using the positive degree-day method, which is common in  
24 modeling of ice sheets (e.g., Greve et al., 2011) and small, alpine glaciers (e.g., Anderson and  
25 Mackintosh, 2006). The positive degree-day approach involves determining the integral of  
26 surface air temperature deviation above 0 °C over a time period of interest (usually a year)  
27 and multiplying by a constant, the positive degree-day factor  $f_{\text{PDD}}$ . Specifically, we apply the  
28 method of Calov and Greve (2005), which relates mean annual and mean July surface air  
29 temperatures to the number of positive degree-days. To obtain these surface air temperature  
30 estimates, we add the background temperature anomaly to the parameterizations of Fausto et  
31 al. (2009). We treat the positive degree-day factor as a tuneable parameter in GLISTEN.



1 This method assumes that the positive degree-day factor is constant over the whole ice sheet  
2 and through time. In reality, the positive degree-day factor varies with latitude (Braithwaite,  
3 1995; Tarasov and Peltier, 2002) and surface character; snow has a lower positive degree-day  
4 factor than ice. We also assume that all meltwater runs off immediately, instead of refreezing  
5 in the snowpack (Reeh, 1991; Reijmer et al., 2012).

6 The use of a positive degree-day method for calculating surface ablation represents a small  
7 improvement over the predecessor model GRANTISM (Pattyn, 2006). In particular, the  
8 Calov and Greve (2005) method allows for variation among summer-month surface air  
9 temperatures and for daily variability, meaning that some ablation will occur on the modeled  
10 ice sheet even when surface air temperature anomalies are quite negative. In contrast, there is  
11 a definite surface air temperature anomaly threshold in the GRANTISM model below which  
12 no ablation happens at present sea level. This cutoff occurs at a surface air temperature  
13 anomaly of  $-7.29^{\circ}\text{C}$  (Pattyn, 2006, his Eqns. 10 and 15), well within the range of surface air  
14 temperature anomalies experienced by the Greenland ice sheet over the last glacial-  
15 interglacial cycle (Cuffey and Clow, 1997).

16 Despite our use of positive degree-days to calculate melting, the ablation treatment used in  
17 GLISTEN is still highly simplified compared to those used in many other ice sheet models.  
18 These simplifications probably lead to overestimates of ablation, other factors being equal.  
19 The real ice sheet begins the ablation season covered with snow, which has a higher albedo  
20 and a lower positive degree-day factor than ice. Thus, using a constant, ice-appropriate  
21 positive degree-day factor will overestimate ablation during the early part of the melt season.  
22 Moreover, the model does not track refreezing in the snowpack, meaning that water that  
23 would normally refreeze runs off instead. Again, model tuning should allow us to  
24 compensate for these simplifications.

### 25 2.2.2 Heat transport

26 Heat is transported through the real ice sheet by both diffusion and advection. Sources of heat  
27 include the atmosphere, geothermal heating, and mechanical sources such as deformation of  
28 the ice and its substrate and the passage of water through englacial tunnels and vertical  
29 moulins.

30 GLISTEN uses separate treatments to calculate temperatures within and beneath the ice sheet.  
31 Temperatures within the ice sheet  $T_i$  (K) are calculated from the surface air temperature

1 anomaly  $T_f$  ( $^{\circ}\text{C}$ ) in the same way as in GRANTISM,

$$2 \quad T_i = T_f + 263.15 \text{ for } T_f < 0, \quad (2)$$

$$3 \quad T_i = 0.5T_f + 263.15 \text{ for } T_f \geq 0$$

4 (Pattyn, 2006, his Eqn. 6). This expression implies that temperatures within the ice body vary  
5 only with time, through variations in the surface air temperature anomaly  $T_f$ . Because this  
6 treatment contains no time-dependent component, changes in the surface air temperature  
7 anomaly are immediately reflected in the ice's resistance to flow (see below).

8 GLISTEN represents temperatures at the base of the ice sheet  $T_b$  ( $^{\circ}\text{C}$ ) as

$$9 \quad T_b = T_{ma} \operatorname{erfc}\left(\frac{H}{2\sqrt{\kappa t}}\right) + q_G, \quad (3)$$

10 where  $\kappa$ , the diffusion coefficient of ice, is given by

$$11 \quad \kappa = \frac{k_i}{\rho_i C_i}. \quad (4)$$

12 Here,  $T_{ma}$  is the mean annual surface air temperature ( $^{\circ}\text{C}$ ),  $H$  is the ice thickness (m),  $t$  is time  
13 (yr),  $q_G$  is a tuneable constant term that represents geothermal heating ( $^{\circ}\text{C}$ ),  $k_i$  is the thermal  
14 conductivity of ice ( $2.2 \text{ W m}^{-1} \text{ K}^{-1}$ ),  $\rho_i$  is the density of ice ( $917 \text{ kg m}^{-3}$ ), and  $C_i$  is the heat  
15 capacity of ice ( $2000 \text{ J kg}^{-1} \text{ K}^{-1}$ ).  $T_b$ ,  $T_{ma}$ , and  $H$  are all functions of distance along the profile  
16  $x$ .

17 This treatment assumes that all heat transport takes place by diffusion from the surface of the  
18 ice sheet, neglecting advection of heat due to ice flow. Given an arbitrarily long time and  
19 constant surface air temperatures, bedrock surface elevations, and ice thicknesses, this  
20 expression yields a decrease in basal temperatures from the ice margin to the center of the ice  
21 sheet. The constant term  $q_G$  adjusts where this curve intersects the zero-degree line along the  
22 model transect, and thus the fraction of the bed over which sliding is permitted to take place  
23 (no sliding occurs where the bed is frozen).

24 This treatment of basal temperatures improves on GRANTISM (Pattyn, 2006), which handles  
25 heat transport implicitly. However, the treatment is still highly simplified relative to that used  
26 in three-dimensional ice sheet models, which treat both diffusion and advection.

### 27 2.2.3 Ice flow and basal sliding

28 Ice deforms in response to applied stresses, but ice temperature, water content (e.g., Greve,  
29 1997; Aschwanden et al., 2012), the orientation of crystal axes, and the presence or absence

1 of impurities, also affect ice flow. Ice deformation is proportional to the third power of the  
2 applied stress (Glen, 1955). This driving stress is large where the ice is thick and/or surface  
3 slopes are steep, and lower elsewhere (Alley et al., 2010). Warm ice deforms more readily  
4 than cold ice. Where ice crystals have a preferred orientation, flow occurs more readily along  
5 that direction than predicted by the "normal" equations describing ice flow. Finally,  
6 impurities generally soften the ice relative to the pure material studied in the laboratory.

7 Where grounded ice is not frozen to its bed, it can slide. The effectiveness of this process  
8 depends on the areal concentration and size of asperities (e.g., Weertman, 1957), as well as  
9 basal water pressure and sediment availability. The correct form of the basal sliding law is  
10 under discussion (for a review, see Alley, 2000).

11 Real ice sheets can be divided into three distinct flow domains, based on their velocities and  
12 whether the ice is in contact with a solid substrate (Kirchner et al., 2011; see Joughin et al.,  
13 2010, for surface velocity maps of the Greenland Ice Sheet). Normal, grounded ice moves  
14 slowly, often a few meters per year or less. Ice streams (e.g., the Northeast Greenland Ice  
15 Stream; Fahnestock et al., 2001) have higher surface velocities, up to many kilometers per  
16 year, and rest on a slippery till substrate. Finally, ice shelves consist of formerly-grounded ice  
17 that is now afloat, although they are still connected to their parent land ice bodies. Because  
18 ice streams and ice shelves lack a resistant substrate, their stress balances are closely similar  
19 to one another and different from that of grounded ice (Kirchner et al., 2011; see also Bueler  
20 and Brown, 2009).

21 GLISTEN's treatment of ice flow is nearly identical to GRANTISM's (Pattyn, 2006). The  
22 conservation of matter and the stress-strain relationship for ice yield the vertically-integrated  
23 velocity due to deformation within the ice body, accounting for temperature-based differences  
24 in ice viscosity (Eqn. 2, above). We multiply the ice deformation velocity with a tuneable,  
25 dimensionless factor  $d$  that is analogous to the ice flow enhancement factor used in three-  
26 dimensional ice sheet models (e.g., Rutt et al., 2009). We then find the change in ice  
27 thickness in each model grid cell per time step using the total horizontal velocity, including  
28 basal sliding. The translation of velocities into thickness changes is accomplished using a  
29 semi-implicit finite-difference technique (Pattyn, 2006; see also Hindmarsh, 2001; Greve and  
30 Calov, 2002; Greve and Blatter, 2009).

31 GLISTEN's method for calculating the basal sliding velocity  $u_b$  ( $\text{m yr}^{-1}$ ) comes from  
32 Hindmarsh and le Meur (2001; see also Greve, 2005),

$$1 \quad u_b = be^{(T_b/\gamma)} \left[ \frac{\tau_d^p}{(\rho_i g H)^q} \right], \quad (5)$$

2 where  $b$  is a dimensionless tuning factor,  $T_b$  is the basal temperature from eqn. 3 ( $^{\circ}\text{C}$ ),  $\gamma$  is a  
 3 sub-melt sliding parameter ( $1^{\circ}\text{C}$ ),  $g$  is the gravitational acceleration ( $9.81 \text{ m s}^{-2}$ ), and  $p$  and  $q$   
 4 are sliding law exponents (3 and 2, respectively). The driving stress  $\tau_d$  is defined as

$$5 \quad \tau_d = -\rho_i g H \nabla h \quad (6)$$

6 (Pattyn, 2006, his Eqn. 1), where  $h$  is the elevation of the ice surface.

7 Possible objections to this ice flow-basal sliding treatment are that it is calculated on a  
 8 relatively coarse, one-dimensional grid ( $\Delta x = 36 \text{ km}$ ; Pattyn, 2006), and that it depends on the  
 9 shallow-ice approximation (Hutter, 1983; Pattyn, 2006; Kirchner et al., 2011). The model  
 10 assumes that all flow follows the defined transect, thereby neglecting branches in the flow  
 11 field (see Parizek and Alley, 2004, for another example of this approach). The shallow-ice  
 12 approximation is appropriate for grounded ice, but cannot capture the larger ice velocities  
 13 associated with ice streams. Much effort is presently being devoted to developing ice sheet  
 14 models that do not have this limitation (e.g., Pollard and DeConto, 2009, 2012; Price et al.,  
 15 2011; Larour et al., 2012; Leng et al., 2012). Both branching of the flow field and enhanced  
 16 velocities due to ice streams will likely become more pronounced if the ice sheet begins to  
 17 decay. Finally, some parts of the ice sheet may be more vulnerable to mass loss than the  
 18 single transect we have chosen (e.g., Born and Nisancioglu, 2012). Thus, GLISTEN's  
 19 treatment of ice flow and basal sliding likely underestimates ice transport from the  
 20 accumulation area to the marginal ablation zones without appropriate tuning.

#### 21 2.2.4 Climate-enhanced ice transport

22 Given that our ice flow-basal sliding treatment likely underestimates future increases in ice  
 23 delivery to the margins, we incorporate a parameterization into GLISTEN that allows ice  
 24 fluxes to increase with climate warming. This parameterization is inspired by the so-called  
 25 "Zwally effect" (Zwally et al., 2002) and recent model treatments of it (Parizek and Alley,  
 26 2004; Greve and Otsu, 2007). More generally, this parameterization is a qualitative  
 27 representation of the possible "future... dynamical changes in ice flow" identified by the  
 28 Intergovernmental Panel on Climate Change's Working Group 1 (2007, their table SPM3).

29 Specifically, we multiply the basal velocity  $u_b$  (Eqn. 5) by a tuneable prefactor  $Z_f$  wherever  
 30 surface ablation exceeds accumulation (Section 2.2.1). Thus, as surface air temperatures rise

1 and the fraction of the ice sheet surface that is in the ablation zone increases, the zone of  
2 enhanced marginal flow also grows (Parizek and Alley, 2004).

3 Considered solely as a representation of the Zwally effect, this parameterization neglects  
4 much of what is known about subglacial hydrology. Conceptually, the Zwally effect involves  
5 the penetration of surface meltwater to the bed, lubricating it and resulting in larger annually-  
6 integrated ice velocities. Theoretical and modeling work show that distributed basal  
7 hydrologic networks, which enhance ice flow, collapse readily to dendritic networks that do  
8 not contribute to ice speedup (e.g., Röthlisberger et al., 1972; Bartholomew et al., 2010;  
9 Schoof, 2010; cf. Gulley et al., 2012). Thus, the Zwally effect itself likely affects ice flow  
10 only during the beginning of the melt season, and may have little effect on annually-  
11 integrated ice fluxes. However, this simple parameterization compensates, to some extent, for  
12 the lack of higher-order ice flow dynamics in GLISTEN.

### 13 2.2.5 Other processes

14 GLISTEN handles isostatic adjustment of the bedrock surface in the same way as  
15 GRANTISM (Pattyn, 2006). Given a change in the thickness of ice in a given model grid  
16 cell, the bedrock surface in that grid cell relaxes toward its new elevation with a characteristic  
17 time scale  $\theta$ . This time scale is a tuneable parameter in GLISTEN, and has a default value of  
18 3,000 years. This treatment neglects changes in ice thickness in adjacent grid cells, as  
19 considered by elastic-lithosphere methods (e.g., Greve and Blatter, 2009).

20 In GLISTEN, ice that advances into a grid cell with a nonzero water depth simply calves.  
21 This treatment clearly neglects the possibility of ice shelf formation (although ice shelves  
22 make up a small fraction of the modern Greenland Ice Sheet's area), the penetration of warm  
23 ocean water into fjords around the ice sheet margin (e.g., Straneo et al., 2010), and the  
24 complexities associated with grounding line migration (e.g., Alley et al., 2007).

### 25 2.2.6 Conversion of simulated area to Greenland ice volume

26 Sea level rise studies require the time evolution of ice volume on Greenland. However,  
27 neither GRANTISM (Pattyn, 2006) nor GLISTEN gives this information directly; instead,  
28 they yield the cross-sectional area of ice over the modeled transect at any instant in time. To  
29 convert this area to ice volume, we multiply by the ratio of the total modern ice volume (7.3  
30 m sle; Lemke et al., 2007) to the modern ice area of the transect (see Parizek and Alley, 2004,

1 for another example of this approach). This conversion is likely most accurate for small  
2 volume changes, relative to the present day.

3

### 4 **3 Precalibration of the updated GLISTEN model**

#### 5 **3.1 Motivation and methods**

6 Our goal in porting and updating GRANTISM (Pattyn, 2006) is to create a representation of  
7 the Greenland Ice Sheet for integrated assessment models. To be useful in this context,  
8 GLISTEN must

- 9 1) reproduce a curve of ice volume as a function of time from a more-complex ice sheet  
10 model, and
- 11 2) match data on the ice sheet's past behavior and present geometry.

12 Although these criteria may appear redundant, one does not imply the other. Criterion #1 is  
13 based on the needs of integrated assessment models and the standards used in the integrated  
14 assessment literature for evaluating different model components. As noted in the  
15 Introduction, integrated assessment models require estimates of ice volume change over time,  
16 not the spatial distribution of ice. Individual components of integrated assessment models are  
17 typically calibrated against more-complex models.

18 Criterion #2 acknowledges that most Greenland Ice Sheet models are tuned solely against the  
19 shape of the modern ice sheet, and occasionally its surface velocity field (Aschwanden et al.,  
20 2009; Bindschadler et al., in review 2011; for exceptions, see Tarasov and Peltier, 2003;  
21 Lhomme et al., 2005; Simpson et al., 2009). Reproducing a static "snapshot" of the modern  
22 ice sheet raises questions about whether the tuned models will behave appropriately when  
23 forced from this estimated modern state (Oreskes, 1994). Thus, we tune GLISTEN separately  
24 using time-distributed data.

25 To address the two criteria given above, we use a search algorithm to adjust GLISTEN's eight  
26 tuneable parameters (Table 1) until a good match is found between our selected tuning data  
27 sets and the model output. Based on the generally good matches that we identify (Section 3.2,  
28 below), we conclude that GLISTEN is a promising tool for incorporating insights on  
29 Greenland Ice Sheet behavior into integrated assessment models. In the remainder of Section

1 3.1, we describe the data sets that we tune the model against, our search algorithm, and our  
2 objective function for determining the quality of model fits to data.

### 3 3.1.1 Tuning data sets

4 To tune GLISTEN against a more-complex ice sheet model (criterion #1, above), we use the  
5 ice volume(time) curve from run #29 of a 100-member perturbed-parameter ensemble  
6 (Applegate et al., 2012) produced with the SICOPOLIS ice sheet model (Greve, 1997; Greve  
7 et al., 2011; sicopolis.greveweb.net). This ensemble member provided the best agreement  
8 with the modern ice volume (~7.2 m sea level equivalent, integrated over SICOPOLIS' 10-km  
9 grid; Bamber et al., 2001; Greve et al., 2011; cf. Lemke et al., 2007). As recommended by the  
10 seaRISE project (Bindschadler et al., in review 2011;  
11 [http://websrv.cs.umt.edu/isis/index.php/SeaRISE\\_Assessment](http://websrv.cs.umt.edu/isis/index.php/SeaRISE_Assessment)), the SICOPOLIS ensemble  
12 was forced by surface air temperature anomalies derived from oxygen isotopes in the GRIP  
13 ice core (Dansgaard et al., 1993) from 125 ka to preindustrial times (1840). The sequence of  
14 oxygen isotope measurements in this ice core is disturbed by flow before ~90 ka (e.g.,  
15 Chappellaz et al., 1997). After 1840, the ensemble was driven by observed surface air  
16 temperatures from Vinther et al. (2006). The ensemble was also forced by background sea  
17 levels estimated from oxygen isotope values measured in planktonic foraminifera from ocean  
18 sediment cores (Imbrie et al., 1984).

19 To independently match GLISTEN to data on the ice sheet's past behavior and present shape,  
20 we use 1) assessed ice volume changes, relative to the present, during key periods in the last  
21 glacial-interglacial cycle (Alley et al., 2010, their Fig. 13), and the modern ice volume  
22 (Bamber et al., 2001); 2) estimates of the ice sheet's total mass balance in five individual years  
23 during the last six decades (Rignot et al., 2008); and 3) ice thicknesses along the model  
24 transect (Letreguilly et al., 1991). The Letreguilly et al. (1991) data set has been superseded  
25 by subsequent compilations (Bamber et al., 2001) and additional data collection; we use it  
26 here because it provides the basal boundary and initial condition for GRANTISM (Pattyn,  
27 2006) and GLISTEN.

### 28 3.1.2 Search algorithm and objective function

29 We use Differential Evolution (Storn and Price, 1997; Price et al., 2007) to identify parameter  
30 combinations that produce good matches between model output and the data sets described  
31 above. Differential Evolution is a genetic algorithm that is widely used in optimization

1 problems. It generates successive generations of model parameter combinations, testing each  
2 combination for "fitness" according to a user-defined objective function. Differential  
3 Evolution requires few evaluations to identify an optimal solution, and is less likely to  
4 become "stuck" in a local minimum of the response surface than gradient descent methods.  
5 We found that 8,000-11,000 model realizations per optimization were required to achieve  
6 good results with Differential Evolution for our problem. Given that each model run covers  
7 about 125,000 model years, this number of evaluations implies at least one billion ( $10^9$ ) model  
8 years per calibration experiment.

9 Our objective function uses the product of Gaussian likelihoods, with a correction for  
10 autocorrelated residuals where appropriate (see discussion in Olson et al., 2012). Each  
11 individual "data point"  $i$  has a central estimate  $\mu_i$  and an uncertainty  $\sigma_i$ , and these two  
12 parameters define a normal distribution for that data point. A model-produced value for the  
13 same quantity  $v_i$  will fall some distance from the best-estimate value  $\mu_i$ , and the "correctness,"  
14 or likelihood, of the model realization predicated on just data point  $i$  is calculated from the  
15 offset between the central estimate and the model prediction. Larger offsets, which indicate a  
16 worse fit to the observations, receive a smaller likelihood. The product of the likelihoods for  
17 all data points  $i = 1, 2, \dots, n$  is then an estimate of the "correctness" of the model run as a  
18 whole, given the available data. In practice, we sum the logarithms of our Gaussian  
19 likelihoods, to avoid computer underflow errors.

20 We assign central estimates and uncertainties to our tuning data sets as follows.

21 *SICOPOLIS emulation:* We extract central estimates from SICOPOLIS' hindcast ice volumes  
22 (run #29 from Applegate et al., 2012) over two periods in the geologic past, plus the  
23 simulated modern ice volume. For the Eemian and the Last Glacial Maximum, we average  
24 these simulated ice volumes over the periods 118.5-115 ka and 20-19 ka. The actual Eemian  
25 warm period is somewhat older, with maximum ice loss from Greenland occurring  $\sim$ 125 ka  
26 (Kopp et al., 2009). However, our SICOPOLIS run is driven by the GRIP oxygen isotope  
27 curve, which has a quasi-Eemian warm period at  $\sim$ 118.5-115 ka. We assign an uncertainty of  
28 one meter sea level equivalent to all three "data points" from the SICOPOLIS ice volume  
29 curve.

30 *Assessed ice volume changes:* This set of constraints is similar to that described under  
31 "SICOPOLIS emulation," above, but uses ice volume changes relative to the present day from  
32 Alley et al. (2010, their Fig. 13) for the Eemian and Last Glacial Maximum.



1 *Historical mass balance:* Rignot et al. (2008) provide estimates of the Greenland Ice Sheet's  
2 total mass balance, with uncertainties, during six years covered by our model runs (1958,  
3 1964, 1996, 2000, 2004, and 2005). Our runs do not include the years 2006 and 2008, also  
4 covered by Rignot et al. (2008), because the Vinther et al. (2006) surface air temperature  
5 record that drives the model ends in 2005.

6 *Ice thicknesses:* The data set of Letreguilly et al. (1991) provides the basal boundary  
7 condition and initial ice thicknesses for both GRANTISM (Pattyn, 2006) and GLISTEN (see  
8 Bamber et al., 2001, for an updated data set). We evaluate the likelihood of model parameter  
9 combinations for this data set using the method of Olson et al. (2012), which accounts for  
10 autocorrelated residuals.

### 11 3.1.3 Initial conditions, forcing functions, and time steps

12 For the pre-calibration experiments, we ran GLISTEN over two periods, 125 ka to 1840 and  
13 1840 to 2005. The initial condition for the paleo-spinup (125 ka-1840) was the modern ice  
14 thicknesses and bedrock topography, as given by Letreguilly et al. (1991) and projected onto  
15 the model transect by Pattyn (2006). For each model run, the final state from the paleo-  
16 spinup provided the initial state for the historical part of the run (1840-2005).

17 As in Applegate et al. (2012; see above), the forcing functions for the paleo-spinup period  
18 were surface air temperature anomalies derived from the GRIP ice core (Dansgaard et al.,  
19 1993) and sea level anomalies based on ocean cores used in the SPECMAP project (Imbrie et  
20 al., 1984). After 1840, we used surface air temperature anomalies from Vinther et al. (2006)  
21 to drive the model. The sea level anomaly was held constant at 0 over the historical period,  
22 but this simplification should have little or no effect on our results (Applegate et al., 2012).

23 The time step over the paleo-spinup was 20 years, and this time step was shortened to 1 yr for  
24 the historical period.

25

## 26 3.2 Precalibration results

27 As noted above, we perform two precalibration experiments with GLISTEN. The first of  
28 these experiments matches GLISTEN to an ice volume curve from the SICOPOLIS ice sheet  
29 model (run #29 from Applegate et al., 2012). The second experiment matches GLISTEN to  
30 assessed ice volume changes, historical mass balance data, and modern ice thicknesses.

1 GLISTEN reproduces the data reasonably well, given appropriate tuning (Figs. 2-5). For  
2 example, GLISTEN matches the overall shape of the ice volume curve from SICOPOLIS  
3 when the two models are forced by the same surface air temperature and sea level anomaly  
4 curves (Fig. 2). Similarly, GLISTEN agrees well with assessed ice volume changes over  
5 geologic time (Fig. 3), mass balance estimates covering the last few decades (Fig. 4), and the  
6 observed ice profile (Fig. 5).

7 The best-fit values from the two experiments diverge widely for many parameters (Table 1).  
8 Given the general resemblance of the ice volume curves resulting from these experiments  
9 (compare Figs. 2 and 3), these differences may seem surprising. However, ice sheet models  
10 can yield similar results for key model outputs, even given very different input parameter  
11 combinations (Applegate et al., 2012, their Figs. 1, 3, and 9). Some parameters trade off  
12 against one another; for example, similar velocities can arise from either a high value of the  
13 ice deformation parameter  $d$  and a low value of the basal sliding parameter  $b$ , or vice versa.  
14 Further work is needed to characterize the likelihood surfaces near our best-fitting parameter  
15 combinations and potential tradeoffs among parameters.

16

## 17 **4 Discussion**

18 We have shown that the one-dimensional ice sheet model GLISTEN reproduces 1) an ice  
19 volume curve from a more-complex model, and 2) data on the ice sheet's past behavior and  
20 present geometry, after appropriate tuning. GLISTEN is a Fortran port of an earlier,  
21 spreadsheet-based model developed for classroom use (GRANTISM; Pattyn, 2006). We  
22 improved the ported model's treatments of surface mass balance, heat transport within the ice  
23 body, and climate-enhanced ice flux.

24 GLISTEN's success in meeting these tests suggest that it may be a useful tool for integrated  
25 assessment modeling and sea level studies in general. As noted in the Introduction, most  
26 integrated assessment models lack an intrinsic treatment of Greenland Ice Sheet melt, despite  
27 its potential importance for future sea level rise. GLISTEN runs quickly and successfully  
28 imitates other models, thereby satisfying two important criteria for new integrated assessment  
29 model components. In terms of sea level studies, GLISTEN may occupy an important niche  
30 between semi-empirical projections of future sea level rise (e.g., Rahmstorf, 2007; Grinsted et  
31 al., 2009) and three-dimensional, higher-order ice sheet models (e.g., Price et al., 2011;  
32 Bindshadler et al., in review 2011; Seddik et al., 2011; Larour et al., 2012).

1 GLISTEN's speed proved vital for calibrating the model against observations of the ice sheet's  
2 past behavior, raising implications for the calibration of other ice sheet models. Each of our  
3 two calibration experiments required 8,000-11,000 model evaluations covering the period 125  
4 ka to present. These simulations took a few hours with GLISTEN, but a three-dimensional  
5 model like SICOPOLIS would require decades to carry out the same experiment on a single  
6 processor (Fig. 1). SICOPOLIS is a shallow-ice approximation model that trades mechanistic  
7 complexity for speed; higher-order ice sheet models, with more parameters and increased  
8 computational cost, simply cannot be calibrated in this way. Instead, such models are tuned  
9 primarily against the modern state of the ice sheet (e.g., Bindshadler et al., in review 2011).  
10 Tuning a model solely against the ice sheet's present state raises questions about whether the  
11 model behavior is reasonable when forced away from the present climate (e.g., Oreskes et al.,  
12 1994). Our tuning exercises with GLISTEN demonstrate that the model reproduces the  
13 expected amplitude of ice volume change between the Eemian, Last Glacial Maximum, and  
14 the present day, and simulates recent mass balance changes.

15 As we emphasize in the model description (Section 2), GLISTEN lacks many processes that  
16 may be important to the real ice sheet. For example, it does not have any treatment of  
17 advanced dynamics beyond a qualitative parameterization of climate-induced enhanced flow  
18 (Section 2.2.4), and the profile treatment means that any complexities in the flow field are not  
19 captured (see Sergienko et al., 2012, for a discussion of profile models and their limitations).  
20 GLISTEN best describes feedbacks associated with the ice sheet's surface mass balance,  
21 although many important details of these processes are also not treated by the model.

22 Future work with GLISTEN will involve further testing and calibration, and incorporation into  
23 integrated assessment models. At present, the model uses the outdated Letreguilly et al.  
24 (1991) bedrock topography and ice thickness data set as its basal boundary and initial  
25 condition; this data will be replaced by the Bamber et al. (2001) compilation, and the effects  
26 of different horizontal spacings on the model results will be investigated. We will investigate  
27 how using transects other than the one chosen by Pattyn (2006; 72° N) affects GLISTEN's  
28 ability to reflect the whole ice sheet's behavior. Finally, our present calibration identifies only  
29 best-guess parameter values, hindcasts, and projections. Probabilistic calibration with  
30 Markov chain Monte Carlo (e.g., Olson et al., 2012) will allow characterization of  
31 uncertainties associated with these quantities.

32

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10

11 **Author contributions**

12 BCT ported the original GRANTISM model to Fortran and wrote a preliminary R wrapper to  
13 control model input and output. JDHM modified BCT's Fortran code to include additional  
14 processes, developed R code to match the model to data, and wrote the initially-submitted  
15 version of the manuscript. PJA provided information on ice sheet processes and revised the  
16 paper text according to the reviewers' suggestions. REN produced Figure 1. KK designed the  
17 study and provided insight into integrated assessment modeling and sea level rise studies. All  
18 authors participated in discussions.

19

## 1 **References**

- 2 Alley, R. B., Anandakrishnan, S., Dupont, T. K., Parizek, B. R., and Pollard, D., Effect of  
3 sedimentation on ice-sheet grounding-line stability, *Science*, 315, 1838-1841, doi:  
4 10.1126/science.1138396, 2007.
- 5 Alley, R. B., Andrews, J. T., Brigham-Grette, J., Clarke, G. K. C., Cuffey, K. M., Fitzpatrick,  
6 J. J., Funder, S., Marshall, S. J., Miller, G. H., Mitrovica, J. X., Muhs, D. R., Otto-Bliesner, B.  
7 L., Polyak, L., and White, J. W. C.: History of the Greenland ice sheet: paleoclimate insights,  
8 *Quaternary Sci. Rev.*, 29, 1728–1756, 2010.
- 9 Alley, R. B.: Continuity comes first: recent progress in understanding subglacial deformation,  
10 in: *Deformation of Glacial Materials*, edited by: Maltman, A. J., Hubbard, B., and Hambrey,  
11 M. J., *Geol. Soc. Spec. Publ.*, 176, 171–179, 2000.
- 12 Anderson, B., and Mackintosh, A.: Temperature change is the major driver of late-glacial and  
13 Holocene glacier fluctuations in New Zealand, *Geology*, 34, 121-124, doi: 10.1130/G22151.1,  
14 2006.
- 15 Anthoff, D., Nicholls, R. J., and Tol, R. S. J.: The economic impact of substantial sea-level  
16 rise, *Mitig Adapt Strateg Glob Change*, 15, 321-335, doi: 10.1007/s11027-010-9220-7, 2010.
- 17 Applegate, P. J., Kirchner, N., Stone, E. J., Keller, K., and Greve, R.: An assessment of key  
18 model parametric uncertainties in projections of Greenland Ice Sheet behavior, *The*  
19 *Cryosphere*, 6, 589–606, doi:10.5194/tc-6-589-2012, 2012.
- 20 Aschwanden, A., Bueller, E., Khroulev, C., and Blatter, H.: An enthalpy formulation for  
21 glaciers and ice sheets, *J. Glaciol.*, 58, 441–457, doi:10.3189/2012JoG11J088, 2012.
- 22 Aschwanden, A., Khroulev, C., and Bueller, E.: SeaRISE Greenland – on “spin-up”  
23 procedures, *EOS*, 90, abstract C23B-0500, 2009.
- 24 Bales, R. C., Guo, Q., Shen, D., McConnell, J. R., Guoming, D., Burkhart, J. F., Spikes, V.  
25 B., Hanna, E., and Cappelen, J.: Annual accumulation for Greenland updated using ice core  
26 data developed during 2000–2006 and analysis of daily coastal meteorological data, *J.*  
27 *Geophys. Res.*, 114, D06116, doi:10.1029/2008JD011208, 2009.
- 28 Bamber, J. L., Layberry, R. L., and Gogineni, S. P.: A new ice thickness and bed data set for  
29 the Greenland ice sheet, 1. Measurement, data reduction, and errors, *J. Geophys. Res.*, 106,  
30 33773–33780, 2001.

- 1 Bartholomew, I., Nienow, P., Mair, D., Hubbard, A., King, M. A., and Sole, A.: Seasonal  
2 evolution of subglacial drainage and acceleration in a Greenland outlet glacier, *Nat. Geosci.*,  
3 3, 408– 411, 2010.
- 4 Bindschadler, R. A., Nowicki, S., Abe-Ouchi, A., Aschwanden, A., Choi, H., Fastook, J.,  
5 Granzow, G., Greve, R., Gutowski, G., Herzfeld, U., Jackson, C., Johnson, J., Khroulev, C.,  
6 Levermann, A., Lipscomb, W. H., Martin, M. A., Morlighem, M., Parizek, B. R., Pollard, D.,  
7 Price, S. F., Ren, D., Saito, F., Sato, T., Seddik, H., Seroussi, H., Takahashi, K., Walker, R.,  
8 Wang, W.: Ice-sheet model sensitivities to environmental forcing and their use in projecting  
9 future sea-level (the SeaRISE project), *J. Glaciol.*, in review, 2011.
- 10 Born, A. and Nisancioglu, K. H.: Melting of Northern Greenland during the last  
11 interglaciation, *The Cryosphere*, 6, 1239-1250, doi:10.5194/tc-6-1239-2012, 2012.
- 12 Box, J. E., and Steffen, K.: Sublimation estimates for the Greenland ice sheet using automated  
13 weather station observations, *J. Geophys. Res.*, 106, 33,965– 33,982, 2001.
- 14 Braithwaite, R. J.: Positive degree-day factors for ablation on the Greenland ice sheet studied  
15 by energy-balance modelling, *J. Glaciol.*, 41, 153–160, 1995.
- 16 Bueler, E. and Brown, J.: Shallow shelf approximation as a “sliding law” in a  
17 thermomechanically coupled ice sheet model, *J. Geophys. Res.*, 114, F03008,  
18 doi:10.1029/2008JF001179, 2009.
- 19 Calov, R. and Greve, R.: A semi-analytical solution for the positive degree-day model with  
20 stochastic temperature variations, *J. Glaciol.*, 51, 173–175, 2005.
- 21 Chappellaz, J., Brook, E., Blunier, T., and Malaize, B.: CH<sub>4</sub> and δ<sup>18</sup>O of O<sub>2</sub> records from  
22 Antarctic and Greenland ice: a clue for stratigraphic disturbance in the bottom part of the  
23 Greenland Ice Core Project and the Greenland Ice Sheet Project 2 ice cores, *J. Geophys. Res.*,  
24 102, 26547–26557, 1997.
- 25 Clausen, H. B., Gundestrup, N. S., Johnsen, S. J., Bindschadler, R., and Zwally, J.:  
26 Glaciological investigations in the Crete area, Central Greenland: A search for a new drilling  
27 site. *Ann. Glaciol.*, 10, 10–15, 1988.
- 28 Cuffey, K. M. and Clow, G. D.: Temperature, accumulation, and ice sheet elevation in Central  
29 Greenland through the last deglacial transition, *J. Geophys. Res.*, 102, 26383–26396, 1997.

- 1 Dansgaard, W., Johnsen, S., Clausen, H., Dahl-Jensen, D., Gundestrup, N., Hammer, C., Hvid  
2 berg, C., Steffensen, J., Sveinbjornsdottir, A., and Jouzel, J.: Evidence for general instability  
3 of past climate from a 250-kyr ice-core record, *Nature*, 364, 218–220, 1993.
- 4 Ekholm, S.: A full coverage, high-resolution, topographic model of Greenland computed from  
5 a variety of digital elevation data, *J. Geophys. Res.*, 101, 21961–21972, 1996.
- 6 Ettema, J., van den Broeke, M. R., van Meijgaard, E., van de Berg, W. J., Bamber, J. L., Box,  
7 J. E., and Bales, R. C.: Higher surface mass balance of the Greenland Ice Sheet revealed by  
8 high resolution climate modeling, *Geophys. Res. Lett.*, 36, L12501,  
9 doi:10.1029/2009GL038110, 2009.
- 10 Fahnestock, M., Abdalati, W., Joughin, I., Brozena, J., and Gogineni, P.: High geothermal  
11 heat flow, basal melt, and the origin of rapid ice flow in central Greenland, *Science*, 294,  
12 2338–2342, 2001.
- 13 Fausto, R. S., Ahlstrom, A. P., van As, D., Boggild, C. E., and Johnsen, S. J.: A new present-  
14 day temperature parameterization for Greenland, *J. Glaciol.*, 55, 95–105, 2009.
- 15 Fyke, J. G., Weaver, A. J., Pollard, D., Eby, M., Carter, L., and Mackintosh, A.: A new  
16 coupled ice sheet/climate model: description and sensitivity to model physics under Eemian,  
17 Last Glacial Maximum, late Holocene and modern climate conditions, *Geosci. Model Dev.*, 4,  
18 117–136, doi:10.5194/gmd-4-117- 2011, 2011.
- 19 Glen, J. W.: The creep of polycrystalline ice, *P. R. Soc. Lond. A*, 228, 519–538,  
20 doi:10.1098/rspa.1955.0066, 1955.
- 21 Gomez, N., Mitrovica, J. X., Huybers, P., and Clark, P. U.: Sea level as a stabilizing factor for  
22 marine-ice-sheet grounding lines, *Nat. Geosci.*, 3, 850–853, 2010.
- 23 Gregory, J. M. and Huybrechts, P.: Ice-sheet contributions to future sea level change, *Phil.*  
24 *Trans. R. Soc. A*, 364, 1709–1731, 2006.
- 25 Greve, R. and Blatter, H.: *Dynamics of Ice Sheets and Glaciers*, Monograph Series Advances  
26 in Geophysical and Environmental Mechanics and Mathematics, 2009.
- 27 Greve, R. and Calov, R.: Comparison of numerical schemes for the solution of the ice-  
28 thickness equation in a dynamic/thermodynamic ice-sheet model. *Journal of Computational*  
29 *Physics* 179, 649–664, 2002.

- 1 Greve, R. and Otsu, S.: The effect of the north-east ice stream on the Greenland ice sheet in  
2 changing climates, *The Cryosphere Discuss.*, 1, 41–76, doi:10.5194/tcd-1-41-2007, 2007.
- 3 Greve, R., Saito, F., and Abe-Ouchi, A.: Initial results of the SeaRISE numerical experiments  
4 with the models SICOPOLIS and IcIES for the Greenland ice sheet, *Ann. Glaciol.*, 52, 23–30,  
5 2011.
- 6 Greve, R.: Application of a polythermal three-dimensional ice sheet model to the Greenland  
7 ice sheet: response to steady-state and transient climate scenarios, *J. Climate*, 10, 901–918,  
8 1997.
- 9 Greve, R.: Relation of basal measured temperatures and the spatial distribution of the  
10 geothermal heat flux for the Greenland Ice Sheet, *Ann. Glaciol.*, 42, 424–432, 2005. Greve,  
11 2005
- 12 Grinsted, A., Moore, J. C., and Jevrejeva, S.: Reconstructing sea level from paleo and  
13 projected temperatures 200 to 2100 AD, *Clim. Dyn.* doi: 10.1007/s00382-008-0507-2, 2009.
- 14 Gulley, J. D., Grabiec, M., Martin, J. B., Jania, J., Catania, G., and Glowacki, P.: The effect of  
15 discrete recharge by moulins and heterogeneity in flow-path efficiency at glacier beds on  
16 subglacial hydrology, *J. Glaciol.*, 58, 926-940, doi: 10.3189/2012JoG11J189, 2012.
- 17 Hindmarsh, R. C. A. and Le Meur, E.: Dynamical processes involved in the retreat of marine  
18 ice sheets, *J. Glaciol.*, 47, 271–279, 2001.
- 19 Hindmarsh, R.: Notes on basic glaciological computational methods and algorithms. In  
20 Straughan, B., Greve, R., Ehrentraut, H., Wang, Y. (Eds.), *Continuum Mechanics and*  
21 *Applications in Geophysics and the Environment*, Springer, Berlin, 222–249, 2001.
- 22 Hooke, R. LeB.: *Principles of Glacier Mechanics*, 2nd Edn., Cambridge, 429, 2005.
- 23 Hope, C.: The PAGE09 integrated assessment model: A technical description, Cambridge  
24 Judge Business School Working Paper, 2011. Available online at available online at  
25 [http://www.jbs.cam.ac.uk/research/working\\_papers/2011/wp1104.pdf](http://www.jbs.cam.ac.uk/research/working_papers/2011/wp1104.pdf), accessed 14 Nov 2012.
- 26 Hutter, K.: *Theoretical Glaciology: Material Science of Ice and the Mechanics of Glaciers and*  
27 *Ice Sheets*, D. Reidel, Dordrecht, 1983.
- 28 Huybrechts, P. and de Wolde, J.: The dynamic response of the Greenland and Antarctic ice  
29 sheets to multiple-century climatic warming, *J. Climate*, 12, 2169–2188, 1999.



1 Imbrie, J., Hays, J. D., Martinson, D. G., McIntyre, A., Mix, A. C., Morley, J. J., Pisias, N. G.,  
2 Prell, W. L., and Shackleton, N. J.: The orbital theory of Pleistocene climate: support from a  
3 revised chronology of the marine  $\delta^{18}O$  record, in: *Milankovitch and climate: understanding*  
4 *the response to astronomical forcing, Part 1*, edited by: Berger, A. J., Imbrie, J., Hays, J.,  
5 Kukla, G., and Saltzman, B., D. Reidel Publishing Co., Dordrecht, 269–305, 1984.

6 Johnson, L. T., and Hope, C.: The social cost of carbon in U.S. regulatory impact analyses: an  
7 introduction and critique, *J. Environ. Stud. Sci.*, 2, 205-221, doi: 10.1007/s13412-012-0087-7.

8 Joughin, I., Smith, B. E., Howat, I. M., Scambos, T., and Moon, T.: Greenland flow  
9 variability from ice-sheet-wide velocity mapping, *J. Glaciol.*, 56, 415–430, 2010.

10 Kirchner, N., Hutter, K., Jakobsson, M., and Gyllencreutz, R.: Capabilities and limitations of  
11 numerical ice sheet models: a discussion for Earth-scientists and modelers, *Quaternary Sci.*  
12 *Rev.*, 30, 3691–3704, 2011.

13 Kopp, R. E., Simons, F. J., Mitrovica, J. X., Maloof, A. C., and Oppenheimer, M.:  
14 Probabilistic assessment of sea level during the last interglacial stage, *Nature*, 462, 863-868,  
15 doi: 10.1038/nature08686, 2009.

16 Larour, E., Seroussi, H., Morlighem, M., and Rignot, E.: Continental scale, high order, high  
17 spatial resolution ice sheet modeling using the Ice Sheet System Model (ISSM), *J. Geophys.*  
18 *Res.*, 17, F01022, doi:10.1029/2011JF002140, 2012.

19 Lemke, P., Ren, J., Alley, R. B., Allison, I., Carrasco, J., Flato, G., Fujii, Y, Kaser, G., Mote,  
20 P., Thomas, R. H., and Zhang, T.: *Observations: changes in snow, ice, and frozen ground*,  
21 edited by: Solomon, S., Qin, D., Manning, M., Chen, Z., Marquis, M., Averyt, K. B., Tignor,  
22 M. and Miller, H. L., Cambridge University Press, Cambridge, 2007.

23 Leng, W., Ju, L., Gunzburger, M., Price, S., and Ringler, T.: A parallel high-order accurate  
24 finite element nonlinear 5 Stokes ice sheet model and benchmark experiments, *J. Geophys.*  
25 *Res.*, 117, F01001, doi:10.1029/2011JF001962, 2012.

26 Letreguilly, A., Huybrechts, P., and Reeh, N.: Steady-state characteristics of the Greenland  
27 ice sheet under different climates, *J. Glaciol.*, 37, 149–157, 1991.

28 Lhomme, N., Clarke, G. K. C., and Marshall, S. J.: Tracer transport in the Greenland ice  
29 sheet: constraints on ice cores and glacial history, *Quaternary Sci. Rev.*, 24, 173–194, 2005.

- 1 Lythe, M. B., Vaughan, D. G., and the Bedmap Consortium: Bedmap: a new ice thickness and  
2 subglacial topography model of Antarctica, *J. Geophys. Res.*, 106, 11335–11351, 2001.
- 3 Marsiat, I.: Simulation of the Northern Hemisphere continental ice sheets over the last  
4 glacial–interglacial cycle: experiments with a latitude–longitude vertically integrated ice sheet  
5 model coupled to a zonally averaged climate model. *Palaeoclimates: Data and Modelling*,  
6 1(1), 59–98, 1994.
- 7 McInerney, D., Lempert, R., and Keller, K.: What are robust strategies in the face of uncertain  
8 climate threshold responses?, *Climatic Change*, 112, 547–568, doi:10.1007/s10584-011-0377-  
9 1, 2011.
- 10 Mitrovica, J. X., Gomez, N., Clark, P. U.: The sea-level fingerprint of West Antarctic  
11 collapse, *Science*, 323, 753, doi: 10.1126/science.1166510, 2009.
- 12 Moles, C. G., Banga, J. R., and Keller, K.: Solving nonconvex climate control problems:  
13 pitfalls and algorithm performances, *Appl. Soft Comput.*, 5, 35–44,  
14 doi:10.1016/j.asoc.2004.03.011, 2004.
- 15 Moss, R. H., Edmonds, J. A., Hibbard, K. A., Manning, M. R., Rose, S. K., van Vuuren, D.  
16 P., Carter, T. R., Emori, S., Kainuma, M., Kram, T., Meehl, G. A., Mitchell, J. F. B.,  
17 Nakicenovic, N., Riahi, K., Smith, S. J., Stouffer, R. J., Thomson, A. M., Weyant, J. P., and  
18 Wilbanks, T. J.: The next generation of scenarios for climate change research and assessment,  
19 *Nature*, 463, 747–756, doi: 10.1038/nature08823, 2010.
- 20 Mote, T. L.: Greenland surface melt trends 1973–2007: evidence of a large increase in 2007,  
21 *Geophys. Res. Lett.*, 34, L22507, doi: 10.1029/2007GL031976, 2007.
- 22 Nicholls, R. J., Tol, R. S. J., and Vafeidis, A. T.: Global estimates of the impact of a collapse  
23 of the West Antarctic ice sheet: an application of FUND, *Climatic Change*, 91, 171–191, doi:  
24 10.1007/s10584-008-9424-y, 2008.
- 25 Nordhaus, W. D.: A question of balance: weighing the options on global warming policies,  
26 Yale University Press, 256, 2008.
- 27 Nordhaus, W. D.: Projections of sea level rise (SLR), 2010. Available online at  
28 <http://nordhaus.econ.yale.edu/RICEmodels.htm>, accessed 14 Nov 2012.
- 29 Ohmura, A., and Reeh, N.: New precipitation and accumulation maps for Greenland, *J.*  
30 *Glaciol.*, 37, 140–148, 1991.

1 Olson, R., Sriver, R., Goes, M., Urban, N. M., Matthews, H. D., Haran, M., and Keller, K.: A  
2 climate sensitivity estimate using Bayesian fusion of instrumental observations and an Earth  
3 System model, *J. Geophys. Res.*, 117, D04103, doi:10.1029/2011JD016620, 2012.

4 Oreskes, N., Shrader-Frechette, K., and Belitz, K.: Verification, validation, and confirmation  
5 of numerical models in the Earth sciences, *Science*, 264, 641–646, 1994.

6 Otto-Bliesner, B. L., Marshall, S. J., Overpeck, J. T., Miller, G. H., Hu, A., and CAPE Last  
7 Interglacial Project members: Simulating Arctic climate warmth and icefield retreat in the last  
8 interglaciation, *Science*, 311, 1751-1754, doi: 10.1126/science.1120808, 2006.

9 Parizek, B. R. and Alley, R. B.: Implications of increased Greenland surface melt under  
10 global-warming scenarios: ice sheet simulations, *Quaternary Sci. Rev.*, 23, 1013–1027, 2004.

11 Parizek, B.R., Alley, R.B., and MacAyeal, D.R: The PSU/UofC finite-element  
12 thermomechanical flowline model of ice-sheet evolution, *Cold Reg. Sci. Technol.*, 42, 145-  
13 168, 2005.

14 Pattyn, F.: GRANTISM: an Excel(TM) model for Greenland and Antarctic ice-sheet response  
15 to climate changes, *Comput. Geosci.*, 32, 316–325, 2006.

16 Pollard, D. and DeConto, R. M.: Description of a hybrid ice sheet-shelf model, and  
17 application to Antarctica, *Geosci. Model Dev.*, 5, 1273-1295, doi:10.5194/gmd-5-1273-2012,  
18 2012.

19 Pollard, D. and DeConto, R.: Modelling West Antarctic ice sheet growth and collapse through  
20 the past five million years, *Nature*, 458, 329–333, 2009.

21 Price, K. V., Storn, R. M., and Lampinen, J. A.: Differential evolution: a practical approach to  
22 global optimization, Springer-Verlag, New York, 2005.

23 Price, S. F., Payne, A. J., Howat, I. M., and Smith, B. E.: Committed sea-level rise for the  
24 next century from Greenland ice sheet dynamics during the past decade, *P. Natl. Acad. Sci.*  
25 *USA*, 108, 8978–8983, 2011.

26 Rahmstorf, S.: A semi-empirical approach to projecting future sea-level rise, *Science*, 315,  
27 368-370, doi: 10.1126/science.1135456, 2007.

28 Reeh, N.: Parameterization of melt rate and surface temperature on the Greenland ice sheet,  
29 *Polarforschung*, 59, 113–128, 1898.

1 regulatory impact analysis under Executive Order 12866, 2010. Available online at  
2 <http://www.epa.gov/oms/climate/regulations/scc-tsd.pdf>, accessed 14 Nov 2012.

3 Reijmer, C. H., van den Broeke, M. R., Fettweis, X., Ettema, J., and Stap, L. B.: Refreezing  
4 on the Greenland ice sheet: a comparison of parameterizations, *The Cryosphere*, 6, 743-762,  
5 doi:10.5194/tc-6-743-2012, 2012.

6 Rignot, E., Box, J., Burgess, E., and Hanna, E.: Mass balance of the Greenland ice sheet from  
7 1958 to 2007, *Geophys. Res. Lett.*, 35, L20502, doi:10.1029/2008GL035417, 2008.

8 Robinson, A., Calov, R., and Ganopolski, A.: An efficient regional energy-moisture bal30  
9 ance model for simulation of the Greenland Ice Sheet response to climate change, *The*  
10 *Cryosphere*, 4, 129–144, doi:10.5194/tc-4-129-2010, 2010.

11 Roe, G. H., and Lindzen, R. S.: A one-dimensional model for the interaction between  
12 continental-scale ice sheets and atmospheric stationary waves, *Clim. Dyn.*, 17, 479-487, 2001.

13 Rogozhina, I., Martinec, Z., Hagedoorn, J. M., Thomas, M., and Fleming, K.: On the long-  
14 term memory of the Greenland Ice Sheet, *J. Geophys. Res.*, 116, F01011,  
15 doi:10.1029/2010JF001787, 2011.

16 Rupper, S. and Roe, G.: Glacier changes and regional climate: a mass and energy balance  
17 approach, *J. Climate*, 21, 5384–5401, 2008.

18 Rutt, I. C., Hagedorn, M., Hulton, N. R. J., and Payne, A. J.: The Glimmer community ice-  
19 sheet model, *J. Geophys. Res.-Earth*, 114, F02004, doi:10.1029/2008JF001015, 2009.

20 Röthlisberger, H.: Water pressure in intra- and subglacial channels, *J. Glaciol.*, 11, 177– 203,  
21 1972.

22 Sarofim, M. C., and Reilly, J. M.: Applications of integrated assessment modeling to climate  
23 change, *WIREs Climate Change*, 2, 27-44, doi: 10.1002/wcc.93, 2011.

24 Schoof, C.: Ice-sheet acceleration driven by melt supply variability: *Nature*, 468, 803–806,  
25 2010.

26 Seddik, H., Greve, R., Zwinger, T., Gillet-Chaulet, F., and Gagliardini, O.: Simulations of the  
27 Greenland ice sheet 100 yr into the future with the full Stokes model Elmer/Ice, *J. Glaciol.*,  
28 58, 209, 427–440, 2012.

1 Sergienko, O. V., The effects of transverse bed topography variations in ice-flow models, *J.*  
2 *Geophys. Res.*, 117, F03011, 1–16, doi:10.1029/2011JF002203, 2012.

3 Simpson, M. J. R., Milne, G. A., Huybrechts, P., and Long, A. J.: Calibrating a glaciological  
4 model of the Greenland Ice Sheet from the Last Glacial Maximum to present-day using field  
5 observations of relative sea level and ice extent, *Quat. Sci. Rev.*, 28, 1631–1657, 2009.

6 Solomon, S., Qin, D., Manning, M., Chen, Z., Marquis, M., Averyt, K. B., Tignor, M., and  
7 Miller, H. L., eds.: *Climate change 2007: the scientific basis: contribution of Working Group*  
8 *1 to the Fourth Assessment Report of the Intergovernmental Panel on Climate Change*,  
9 Oxford University Press, 1008, 2007.

10 Stone, E. J., Lunt, D. J., Rutt, I. C., and Hanna, E.: Investigating the sensitivity of numerical  
11 model simulations of the modern state of the Greenland ice-sheet and its future response to  
12 climate change, *The Cryosphere*, 4, 397–417, doi:10.5194/tc-4-397-2010, 2010.

13 Storn, R. and Price, K.: Differentia evolution: a simple and efficient heuristic for global  
14 optimization over continuous spaces, *J. Global Optim.*, 11, 341–359, 1997.

15 Straneo, F., Hamilton, G. S., Sutherland, D. A., Stearns, L. A., Davidson, F., Hammill, M. O.,  
16 Stenson, G. B., and Rosing-Asvid, A.: Rapid circulation of warm subtropical waters in a  
17 major glacial fjord in East Greenland, *Nat. Geosci.*, 3, 182–186, 2010.

18 Tarasov, L. and Peltier, W. R.: Greenland glacial history and local geodynamic consequences,  
19 *Geophys. J. Int.*, 150, 198–229, 2002.

20 Tarasov, L. and Peltier, W. R.: Greenland glacial history, borehole constraints, and Eemian  
21 extent, *J. Geophys. Res.*, 108, 2143, doi:10.1029/2001JB001731, 2003.

22 Toniazzo, T., Gregory, J. M., and Huybrechts, P.: Climatic impact of a Greenland  
23 deglaciation 30 and its possible irreversibility, *J. Climate*, 17, 21–33, 2004.

24 Torinesi, O., Fily, M., and Genthon, C.: Variability and trends of the summer melt period of  
25 Antarctic ice margins since 1980 from microwave sensors, *J. Climate*, 16, 1047–1060, 2003.

26 Urban, N. M. and Keller, K.: Probabilistic hindcasts and projections of the coupled climate,  
27 carbon cycle and Atlantic meridional overturning circulation system: a Bayesian fusion of  
28 century scale observations with a simple model, *Tellus A*, 62, 737–750, 2010.

29 US Interagency Working Group on the Social Cost of Carbon: Technical support document:  
30 social cost of carbon for

1 van der Veen, C. J.: Polar ice sheets and global sea level: how well can we predict the future?,  
2 Global Planet. Change, 32, 165–194, 2002.

3 Velicogna, I.: Increasing rates of ice mass loss from the Greenland and Antarctic ice sheets  
4 revealed by GRACE, Geophys. Res. Lett., 36, L119503, doi:10.1029/2009GL040222, 2009.

5 Vinther, B., Andersen, K., Jones, P., Briffa, K., and Cappelen, J.: Extending Greenland  
6 temperature records into the late eighteenth century, J. Geophys. Res., 111, D11105,  
7 doi:10.1029/2005JD006810, 2006.

8 Weertman, J.: On the sliding of glaciers, J. Glaciol., 3, 33–38, 1957.

9 Zwally, H. J., Abdalati, W., Herring, T., Larson, K., Saba, J., and Steffen, K.: Surface  
10 meltinduced acceleration of Greenland Ice-Sheet flow, Science, 297, 218–222, 2002.

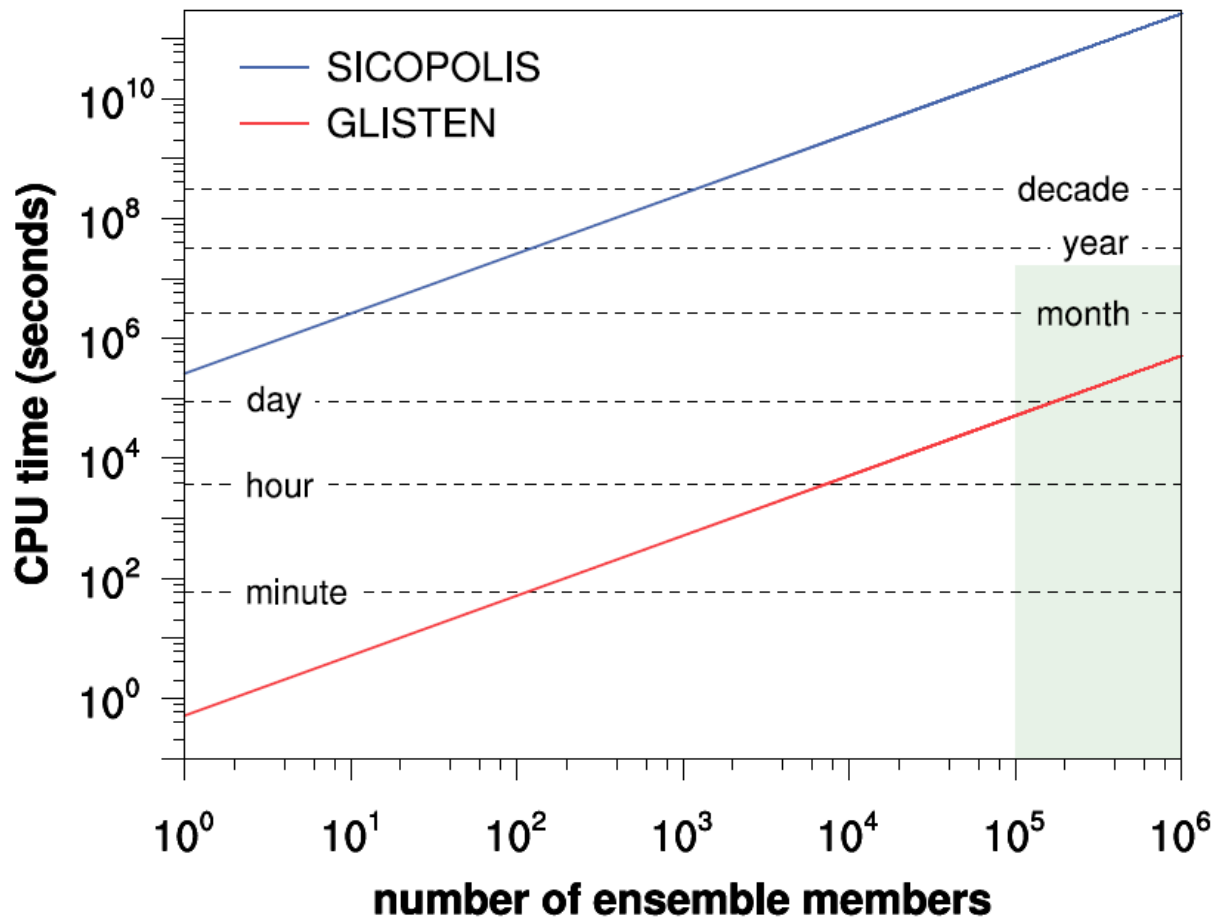
11

1 **Table 1.** Tuneable parameters in the updated GLISTEN model and their best-estimate values  
 2 in our two Differential Evolution tuning experiments (Section 3).

Parameter	Description	Search range and units	First occurs	Tuning to SICOPOLIS	Tuning to observations
$s$	Factor controlling accumulation change with temperature	0.1 to 10 (unitless)	2.2.1.1	1.1693	1.0841
$a_0$	Profile-averaged yearly precipitation	0.205 to 0.82 m yr <sup>-1</sup>	2.2.1.1	0.6161	0.4119
$f_{\text{PDD}}$	Positive degree-day factor	-2.5* 10 <sup>-3</sup> to -1.0* 10 <sup>-2</sup> m day <sup>-1</sup> °C <sup>-1</sup>	2.2.1.2	-2.9* 10 <sup>-3</sup>	-2.6* 10 <sup>-3</sup>
$q_G$	Geothermal heating term	-10 to 10 °C	2.2.2	-7.5545	2.0214
$d$	Ice flow factor	0.1 to 10 (unitless)	2.2.3	6.9947	1.5355
$b$	Basal sliding factor	0.1 to 10 (unitless)	2.2.3	5.6669	1.0718
$Z_f$	Scaling factor for climate-enhanced ice flow	0.55 to 2.2 (unitless)	2.2.4	1.9624	0.8849
$\theta$	Time scale of bedrock elevation adjustment	1500 to 6000 yr	2.2.5	5126	3928

3

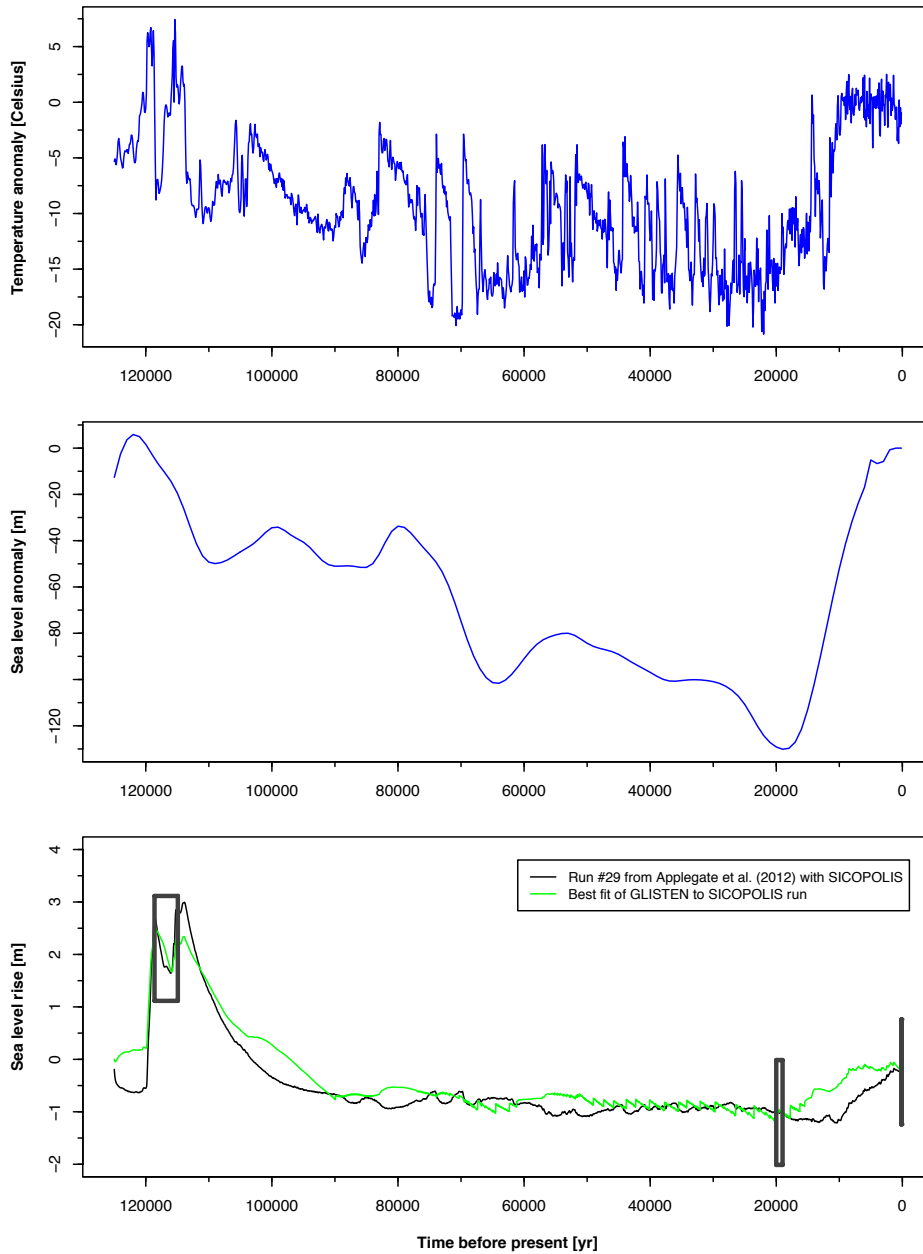
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1  
 2 **Figure 1.** Computing time required for 125,000-yr ice sheet calculations using GLISTEN  
 3 (red line) and the three-dimensional ice sheet model SICOPOLIS (blue line; Greve et al.,  
 4 2011), as a function of the desired number of model runs, assuming that only one processor is  
 5 available to perform the calculations. The green rectangle indicates an "acceptable zone" for  
 6 integrated assessment studies, which require  $\sim 10^5$  model evaluations (Moles et al., 2004) in  
 7 six months or less. GLISTEN can complete this number of model evaluations in weeks to  
 8 months, whereas SICOPOLIS would require decades.

9



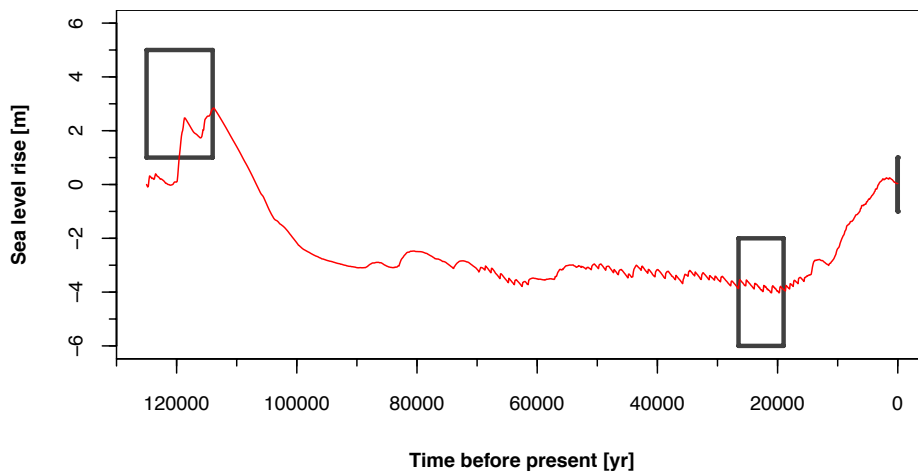


1

2 **Figure 2.** Forcings used to model ice sheet evolution over the last 125,000 yr, and  
 3 demonstration that GLISTEN is able to match results from a three-dimensional ice sheet  
 4 model (SICOPOLIS; Greve, 1997; Greve et al., 2011). Top: Greenland annual mean surface  
 5 air temperature anomaly reconstructed from oxygen isotopes in the GRIP ice core (Dansgaard

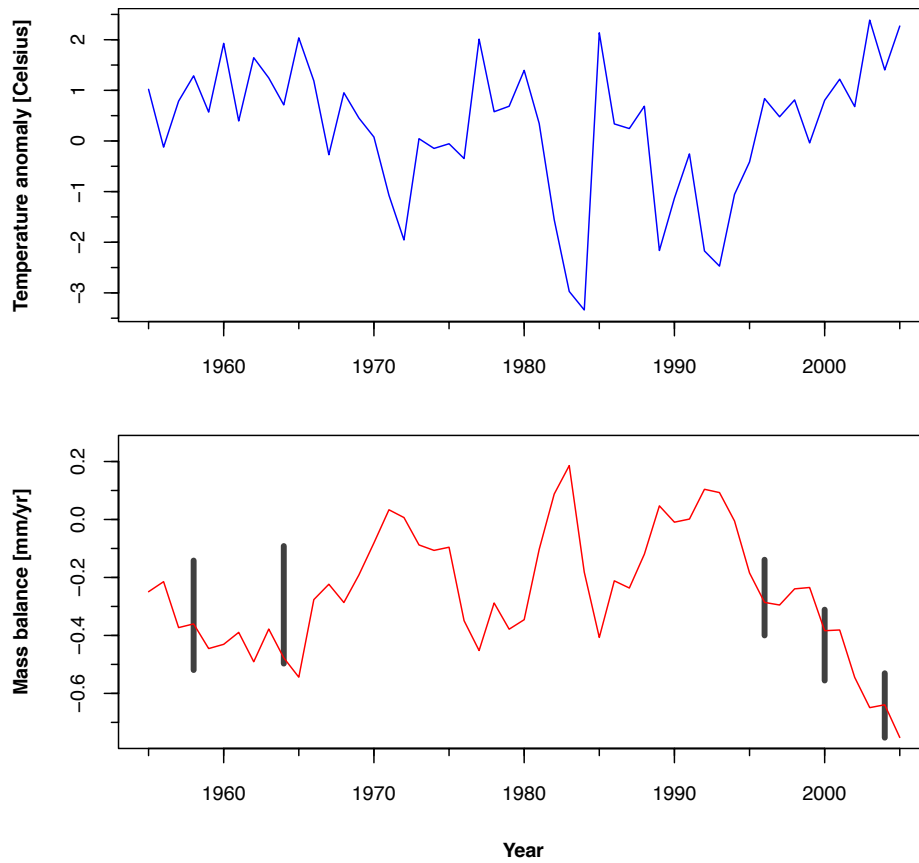
1 et al., 1993; Johnsen et al., 1997). Middle: Sea level anomaly reconstructed from ocean  
2 sediment core oxygen isotopes (Imbrie et al., 1984). Bottom: Best fit of GLISTEN (green  
3 line) to run #29 from Applegate et al. (2012) using the SICOPOLIS ice sheet model (black  
4 line). The agreement between the model curves was tested for each calibration run during the  
5 periods indicated by the gray boxes. Both SICOPOLIS and GLISTEN were driven using the  
6 forcing curves in the top two panels.

7

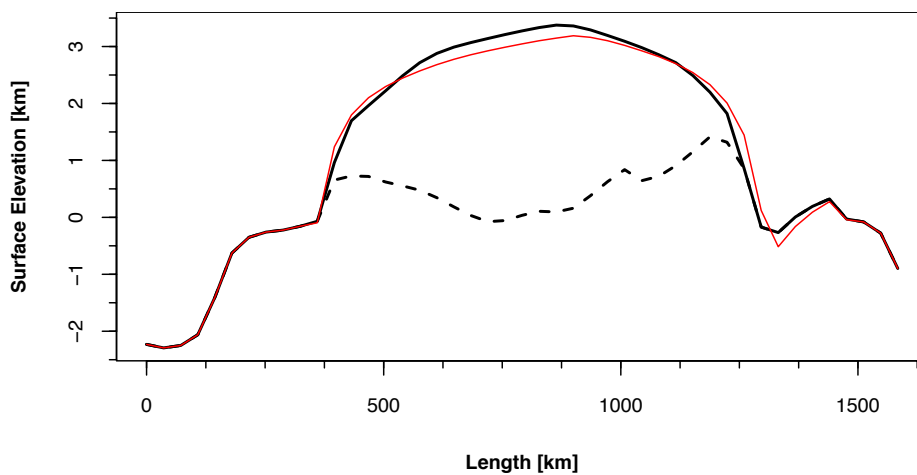


1

2 **Figure 3.** Sea level rise hindcast from the GLISTEN model over the last 125,000 years (red  
 3 curve), after tuning to assessed past ice volume changes (gray boxes; Alley et al., 2010, their  
 4 Fig. 13), the modern ice volume (Bamber et al., 2001), historical mass balance values (Fig. 4),  
 5 and modern ice thicknesses (Fig. 5).



1  
 2 **Figure 4.** Surface air temperature anomalies used to force GLISTEN over the period 1955-  
 3 2005 (top panel; Vinther et al., 2006), and GLISTEN's mass balance hindcast (red line) after  
 4 tuning to historical mass balance values (gray bars; Rignot et al., 2008), assessed past ice  
 5 volume changes and the modern ice volume (Fig. 3), and modern ice thicknesses (Fig. 5).



1  
 2 **Figure 5.** Modern Greenland Ice Sheet profile as estimated by GLISTEN (red line), after  
 3 tuning to modern ice thicknesses, assessed past ice volume changes and the modern ice  
 4 volume (Fig. 3) and historical mass balance values (Fig. 4). The observed modern ice surface  
 5 and bedrock surface are shown for comparison (black lines; Letreguilly et al., 1991).