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Surface undulations of Antarctic ice streams tightly controlled by bedrock topography

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Full Stokes models predict that fast-flowing ice streams transmit information about their bedrock topography most efficiently to the surface for basal undulations with length scales between 1 and 20 times the mean ice thickness. This typical behaviour is independent on the precise values of the flow law and sliding law exponents, and should be universally observable. However, no experimental evidence for this important theoretical prediction has been obtained so far, hence ignoring an important test for the physical validity of current-day ice flow models. In our work we use recently acquired airborne radar data for the Rutford Ice Stream and Evans Ice Stream, and we show that the surface response of fast-flowing ice is highly sensitive to bedrock irregularities with wavelengths of several ice thicknesses. The sensitivity depends on the slip ratio, i.e. the ratio between mean basal sliding velocity and mean deformational velocity. We find that higher values of the slip ratio generally lead to a more efficient transfer, whereas the transfer is significantly dampened for ice that attains most of its surface velocity by creep. Our findings underline the importance of bedrock topography for ice stream dynamics on spatial scales up to 20 times the mean ice thickness. Our results also suggest that local variations in the flow regime and surface topography at this spatial scale cannot be explained by variations in basal slipperiness.

1 Introduction

The flow regime of the Antarctic Ice Sheet is dominated by an extensive network of fast-flowing ice streams and outlet glaciers which account for 90% of the ice sheet's discharge (Bamber et al., 2000). Recent observations have shown that along large sections of the Antarctic coastline, the flow dynamics of these features is changing fast, with increased flow speeds (Rignot et al., 2008) and dynamic thinning (Pritchard et al., 2009). A prime example are the glaciers draining into the Amundsen Sea Embayment, in particular Pine Island Glacier which is now flowing at a speed that is almost double

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that needed to balance snowfall in its catchment basin (Joughin et al., 2010; Thomas et al., 2011). Along the Siple Coast, the Kamb Ice Stream switched from fast to slow flow about 170 yr ago (Retzlaff and Bentley, 1993) and Whillans Ice Stream is currently slowing down by about 5 myr⁻¹ (Joughin et al., 2005). These changes caused the region to switch from a negative to a positive mass balance regime (Joughin and Tulaczyk, 2002), and the local ice sheet thickened by 0.25–0.65 myr⁻¹ between 2003 and 2007 (Pritchard et al., 2009).

It is clear that accurate predictions about the mass balance of the Antarctic Ice Sheet rely on a good understanding of the dynamical mechanisms that control the flow of its ice streams and glaciers. An important role in the regulation of ice stream flow is played by their basal conditions, i.e. bedrock topography and variations in basal slipperiness. In general, the slipperiness is a complicated (and often unknown) function of many physical parameters such as temperature, basal water pressure and the shear strength of subglacial sediments. For example, active ice streams of the Siple Coast exhibit high flow velocities (~ 500 myr⁻¹) despite low gravitational driving stresses (~ 10-20 kPa) due to a weak subglacial till layer (shear stresses ~ 1-5 kPa) providing basal lubrication (Tulaczyk et al., 2001). The main constraints on ice motion come from ice shelf buttressing at the front, shear resistance at the margins, and from basal drag. Basal drag can be broadly subdivided into "form drag" that arises through ice flow over and around small-scale undulations in basal topography, and "skin drag" caused by other processes that limit basal motion (Alley, 1993; Joughin et al., 2004, 2006). Since basal drag has the potential to change more dynamically than other resistive stresses such as marginal shear, the effect of small basal perturbations on flow characteristics is of particular importance.

A possible way to obtain information about the conditions at the base of ice streams is by direct access via boreholes (Kamb, 2001). Such investigations have shown that till beneath the Siple Coast ice streams is highly porous and mechanically weak, but the physical properties of tills elsewhere in Antarctica are unknown due to the challenging aspects of drilling to the bed of an ice sheet. Moreover, this method cannot be used to

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address the role of the bedrock topography on ice flow dynamics. Alternatively, remote sensing techniques such as seismic (Blankenship et al., 1986, 1987; Anandakrishnan et al., 1998; Smith et al., 2007; Smith and Murray, 2009) and radar (Bentley et al., 1998; Gades et al., 2000; Rippin et al., 2006; King et al., 2009) measurements can provide detailed maps of till conditions and basal topography over a larger area of the bed. In addition, information about the form of the basal sliding law or information about the subglacial till rheology can be obtained from the dynamic response of ice streams to tidal forcing (Tulaczyk, 2006; Gudmundsson, 2011). A different approach to the study of basal conditions involves the inversion of irregularities at the surface arising from bedrock bumps or variations in slipperiness. Control method inversion uses accurate remote sensing data about the surface velocity field in combination with theoretical ice flow models to obtain information about the basal shear stress distribution of ice streams (MacAyeal et al., 1995; Vieli and Payne, 2003; Joughin et al., 2004, 2006; Arthern and Gudmundsson, 2010). Statistical inversion methods have been developed to study the simultaneous retrieval (or update) of bed topography and basal slipperiness from surface topography and velocity measurements (Gudmundsson, 2004a; Raymond and Gudmundsson, 2009; Raymond-Pralong and Gudmundsson, 2011).

All inversion methods obtain information about the bed in an indirect way, and rely on a good theoretical understanding of how surface properties connect to conditions at the bed. Most advances in our understanding of this relation have come from the theoretical analysis of ice dynamics equations subjected to varying boundary conditions (see e.g. Nye, 1959; Budd, 1970; Landon and Raymond, 1978, for earlier studies). A substantial part of the subsequent work has concentrated on the transfer of basal disturbances in topography and slipperiness to the surface, and how they influence quantities that are directly observable such as the surface velocity and surface topography. A systematic theoretical analysis of transfer amplitudes using perturbation methods was initiated by Hutter (1983), and his results were later corrected and extended by Johannesson (1992). An analytical solution for the 3-dimensional full Stokes problem with a linear ice rheology and linear sliding law was obtained by Gudmundsson (2003).

and subsequently studied in the shallow-ice-stream approximation by Gudmundsson (2008). Numerical solutions for a nonlinear flow and nonlinear sliding law were obtained by Raymond and Gudmundsson (2005).

It is often thought that variations in basal slipperiness are the principle cause of 5 changing flow conditions along an ice stream, and the role of the bedrock topography is rarely addressed directly in this context. However, one of the predictions that emerges from the full Stokes computations in Gudmundsson (2003), is the characteristic behaviour of the bed-to-surface transfer of small-amplitude basal undulations (small with respect to the ice thickness). It is found that for ice streams which acquire most of their speed through basal sliding, the transmission of bedrock irregularities to the surface is most efficient for length scales between 1 and 20 times the mean ice thickness, whereas variations in slipperiness only have an impact at much longer wavelengths. Theory therefore predicts that the surface topography of fast-flowing ice streams should be dominated by features of several ice thicknesses in length which reflect the presence of similar undulations at the bed. Direct observational evidence for this result has not been obtained so far, despite it's importance as a test for theoretical models. In this paper, we address the issue directly for the first time using airborne radar data along the fast-flowing Rutford and Evans ice streams, as well as the nearlystagnant Carlson Inlet, West Antarctica.

The paper is organized as follows. In Sect. 2 we introduce the theoretical framework that describes the surface response of a flowing ice mass to spatial changes at its base. The remainder of the paper focuses on the experimental validation of this framework. Section 3 contains an overview of the radar data and a discussion about the methodology which was used to estimate the transfer function for each flightline. Results of our analysis are presented in Sect. 4, followed by a discussion of the main findings in Sect. 5. Conclusions are given in Sect. 6.

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The perturbative study of transfer properties of a flowing ice mass relies on the assumption that bed topography (b), basal slipperiness distribution (c) and surface topography (s) can be expanded around a constant mean value, henceforth denoted by a superscript $^{(0)}$:

$$b(x,y) = b^{(0)} + \Delta b(x,y),$$
 $c(x,y) = c^{(0)} + \Delta c(x,y),$ $s(t,x,y) = s^{(0)} + \Delta s(t,x,y),$ (1)

where we assumed that b and c are independent on time. The deviations from the mean values are assumed to be small, i.e. $\Delta b/H \ll 1$ and $\Delta s/H \ll 1$ with H the mean thickness of the ice, and $\Delta c/c^{(0)} \ll 1$.

It is common to choose the mean values $b^{(0)}$, $c^{(0)}$ and $s^{(0)}$ as the solutions for the undisturbed flow (i.e. the zeroth order solution) of an ice mass of thickness H along an infinite-plane-slab geometry with mean surface slope α . If the x-axis is taken along the upper surface in the direction of the flow and the z-axis normal to the surface, then one finds that (for a linear ice rheology and linear sliding law)

$$s^{(0)} = 0, b^{(0)} = -H, c^{(0)} = v_{b,x}^{(0)} / \sin(\alpha) \rho g H,$$
 (2)

where $v_{b,x}^{(0)}$ is the mean forward basal sliding velocity, g is the acceleration due to gravity and ρ is the ice density.

It is often beneficial to introduce scalings that replace the dimensionfull flow variables by dimensionless quantities. In dimensionless variables, the slipperiness distribution $c^{(0)}$ is replaced by $C^{(0)} = \eta c^{(0)}/H$, with η the ice viscosity. This quantity is often referred to as the slip ratio, and can alternatively be written as the ratio of the mean basal sliding velocity and the forward deformational velocity at the surface:

$$C^{(0)} = \frac{v_{b,x}^{(0)}}{v_{d,x}^{(0)}}, \quad \text{with} \quad v_{d,x}^{(0)} = \sin(\alpha)\rho g H^2 / \eta.$$
 (3)

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The Ansatze Eq. (1) and Eq. (2) are used to solve the momentum equations and boundary conditions of the flow, up to first order in the small perturbances. The resulting relations between the perturbances define the first order transfer functions, T, which describe the transient response of a glacier's surface to small disturbances at its base:

$$\Delta s = T_{\rm sb} \Delta b + T_{\rm sc} \Delta c. \tag{4}$$

Each transfer function has two subindices, the first index relates to the effect and the second to the cause. For example, $T_{\rm sh}$ describes the effect on the surface topography caused by perturbations in the bedrock topography. The transfer functions are complex expressions; the amplitude corresponds to the amplitude ratio between the surface and basal perturbations, whereas the phase describes the shift of the surface undulations with respect to the perturbations at the bed.

An analytical solution for the full Stokes system with a linear ice rheology and linear sliding law has been presented by Gudmundsson (2003). The solutions are most easily obtained in their Fourier-transformed form, and are written in terms of transversal (λ_{v}) and longitudinal $(\lambda_{\mathbf{v}})$ wavelength components. The dependence of the transfer functions on the ice viscosity and the mean ice thickness is only indirect via the mean slip ratio, whereas the mean surface slope enters the solutions as a free parameter.

In the following, we are interested in the characteristic behavior of the transfer amplitude $T_{\rm sh}$ in the steady-state limit $(t \to \infty)$ and for long transverse wavelengths $\lambda_{\rm v}$. The latter requirement is motivated by the fact that the flow of an ice stream along a flowline will be treated as a 1-dimensional problem, and basal perturbations transverse to the flow direction will be neglected. This effectively corresponds to taking the limit $\lambda_y \to \infty$ of the three-dimensional solution $T_{\rm sb}(\lambda_x, \lambda_y, C^{(0)}, \alpha)$. The flow-line approximation is graphically represented in Fig. 1 for $\alpha = 0.003$ rad (a typical value encountered for ice streams) and various values of the slip ratio $C^{(0)}$.

The full Stokes solution shows three distinctive regimes: for short wavelengths $\lambda_x < H$ the transfer is close to zero; for long wavelengths $\lambda_x > 10^3 H$ the transfer **TCD**

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converges towards unity; and for intermediate wavelengths $H < \lambda_x < 10^3 H$ the transfer function has a local maximum. The amplitude of this maximum is strongly dependent on the value of $C^{(0)}$. For low values of the slip ratio, i.e. $C^{(0)} < 10$, the peak is almost absent, whereas it is much more prominent for $C^{(0)} > 100$. In other words, for slippery beds – such as those underneath fast-flowing ice streams – the transfer of information about bedrock undulations to the surface is expected to happen very efficiently at intermediate wavelengths. This feature distinguishes ice streams with a high slip ratio from slower moving ice that obtains a substantial part of its surface speed by internal creep, such as the surrounding ice sheet. It is exactly this important distinction that will be the subject of our study. The theoretical form of $T_{\rm sh}$ will be compared to its estimated value from observational data for fast as well as slow flowing sections of the Antarctic Ice Sheet. Results will provide important insights into the applicability of the full Stokes theory to ice stream modelling. Commonly used approximations such as the shallow ice sheet approximation and shallow ice stream approximation fail to reproduce the transfer behaviour of the full Stokes system for wavelengths below 100 and 10 ice thicknesses, respectively (see Gudmundsson, 2008, and Fig. 1), and are therefore less appropriate as a theoretical basis for our study.

It is important to note that the solutions presented in Fig. 1 are only valid for a linear ice rheology (Glen's flow law exponent n = 1) and linear sliding law (sliding law exponent m = 1). Therefore the question remains whether the predicted peak in the transfer amplitude is related to this specific choice of n and/or m, or whether it is a more general, and therefore present for more realistic values of n > 1 and m > 1. Since an analytical solution to the full Stokes transfer problem for arbitrary n and m is not known, an answer to this question relies on the numerical analysis of the momentum equations and boundary conditions. This numerical problem was addressed by Raymond and Gudmundsson (2005). The authors concluded that there is no qualitative difference between the solutions for a linear ice rheology and a non-linear medium, with only a small increase of the transfer for n > 1, and a shift of the local maximum towards longer wavelengths. Also the dependence of $T_{\rm sh}$ on m is weak, with a minor decrease **TCD**

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in the transfer amplitude for m > 1. In addition, it is expected that $T_{\rm sb}$ exhibits a fast convergence towards a limiting curve for increasing values of m. As a consequence, the transfer amplitude for a plastic bed ($m = \infty$) is roughly equal to the transfer amplitude for $m \sim 10$. In summary, a local peak in the transfer function is to be expected for high values of the slip ratio, irrespective of the physical values of n and m.

3 Data and methods

3.1 Data description

In this work we used unmigrated bed and surface returns from an extensive radio echo sounding survey (RES) over the southwestern margin of the Filchner-Ronne Ice Shelf and the adjacent West Antarctic Ice Sheet (inset of Fig. 2). In January 2007, the British Antarctic Survey flew twenty-two RES sorties from two remote field camps (Rutford Ice stream Camp at 78° 08′ S, 83° 54′ S and Ski-Blu at 74° 51′ S, 71° 35′ W), covering a total distance of about 20 000 km. The radar platform consisted of a Twin-Otter equipped with the ice-sounding radar system PASIN (Polarimetric Airborne Survey INstrument), dual-frequency carrier-wave GPS for navigation and high frequency radar altimeter. The RES system operated at a center frequency of 150 MHz and 12 MHz bandwidth. More details about the radar system and data processing methods can be found in Corr et al. (2007), Vaughan et al. (2006), and Rippin et al. (2011), respectively. Comparisons of ice thickness recorded at flight-line crossover points for a similar RES survey using the same equipment at Pine Island Glacier has indicated a root-meansquare error of ~ 23 m (Vaughan et al., 2006). The errors from crossovers in measurements of ice-surface elevation were considerably lower, ~ 1 m. The greatest source of uncertainty for the surface measurements is the false determination of the airplane's position, the errors in the ice thickness result largely from off-nadir reflections and interpretation/digitizing uncertainty. The errors in surface and bed profiles are small and they are not of any concern for our work.

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- (i) Each radar line was flown approximately parallel to the ice flow direction. This allowed us to treat the bed-to-surface transfer problem in a 2-dimensional plane (1 horizontal and 1 vertical direction), with the ice velocity vector lying in that plane. Transverse effects cannot be excluded, but in Sect. 5 we show that they do not influence the qualitative behaviour of the transfer amplitude.
- (ii) All profiles were restricted to the grounded part of the ice sheet. Some sections were cut off at their upstream end to reduce variations in flow conditions, i.e. variations in surface and basal velocity. For all profiles along the Rutford and Evans ice streams, velocities vary from $50 \, \text{myr}^{-1}$ or more at the upstream end to several hundred meters per year near the grounding line. Despite the large variability in flow speed along each profile, there is a distinctive difference with profiles along the Carlson Inlet, which have velocities of typically a few tens of meters per year. In addition, profile lengths needed to be sufficiently long, as we are interested in elevation perturbations with wavelengths up to 20 times the ice thickness. For our dataset, track lengths (/) vary from $I = 72 \, \text{km}$ (E2) to $I = 207 \, \text{km}$ (E10), and the mean ice thickness along profiles has values between $I = 1316 \, \text{m}$ (E12) and $I = 2631 \, \text{m}$ (E3).

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(iii) There are no substantial gaps in the data, although some smaller gaps (< 5km) are present for R2, C1, E2, E3 and E7. Two profiles, E1 and E5, with larger gaps of 18 km and 8 km, respectively were retained, and results for these two profiles should thus be treated with greater caution.</p>

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Plane-slab approximation

For each flow-line the surface and bed profiles (s and b) were separated into a mean value and a deviatoric part, following Eq. (1). The mean values were obtained from a linear regression of the elevation data, and were used to determine the parameters of a plane-slab plug flow: the mean slope α was set equal to the slope of the surface trend $s^{(0)}$, and the mean ice thickness H was chosen as the difference between $s^{(0)}$ and $b^{(0)}$ averaged along the profile. The deviations Δs and Δb have typical values on the order of $10^{-3}H$ and $10^{-2}H$, respectively, so a comparison of our results to perturbation theory is justified.

The mean slipperiness or slip ratio along each profile was determined from estimates of the mean forward deformational velocity and mean basal sliding velocity, according to Eq. (3). The mean basal sliding velocity is given by the difference between the mean surface velocity and the forward deformation, where the former was estimated from InSAR data (Rignot et al., 2011). The forward deformational velocity was computed from $v_{\alpha \nu}^{(0)} = \frac{1}{2}A[\rho g \sin(\alpha)]^3 H^4$, where we chose n = 3 and a spatially constant rate factor for ice at -10 °C, i.e. $A = 3.5 \times 10^{-25} \, \mathrm{s}^{-1} \, \mathrm{Pa}^{-3}$ (Cuffey and Paterson, 2010). Although the ice viscosity is generally a function of depth and position along the flow, exact knowledge about A is not required as it only enters our analysis via the mean slip ratio. The latter is inversely proportional to A, which is a weak dependency in the context of this work, as can be illustrated for a typical active ice stream with a mean surface velocity of 250 myr⁻¹, a mean surface slope of 0.003 rad and a mean ice thickness of 1500 m. Assuming an upper and a lower limit for A corresponding to temperate ice and polar ice at -20°C, respectively, values for the slip ratio vary from $C^{(0)} \approx 60$ to $C^{(0)} \approx 1200$. Even for these extreme (and unrealistic) ice properties, the slip ratio is significantly larger than unity, and a peak in the transfer function is expected.

In summary, values for both $v_{b,x}^{(0)}$ and $v_{d,x}^{(0)}$ were obtained for each profile, resulting in estimates for the mean slip ratio ranging from $C^{(0)} < 1$ for flightlines along the slow

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flowing Carlson Inlet, to $C^{(0)} > 1000$ for the fast-flowing central sections of the Evans Ice Stream (see Fig. 3). As emphasized above, the conclusions of our analysis are insensitive to the exact value of $C^{(0)}$, since theory predicts a local peak in the bed-to-surface transfer amplitude as long as $C^{(0)} \gg 1$. For completeness, the extreme values of $C^{(0)}$ corresponding to temperate ice (lower limit) and polar ice at $-20\,^{\circ}$ C (upper limit) are added as errorbars in Fig. 4.

3.3 Estimated transfer amplitudes

For each flightline we estimated the along-flow transfer amplitude between the detrended bed profile and the detrended surface profile as a function of wavelength. The estimated amplitudes will be denoted by $\mathcal{T}_{\mathrm{sb}}^{(\mathrm{obs})}(\lambda_x)$ and are defined as the quotient of the Cross Power Spectral Density of Δb and Δs (i.e. the Fourier transform of the cross-correlation between the bed and surface signal), and the Power Spectral Density of Δb (i.e. the Fourier transform of the autocorrelation of the bed signal).

The evaluation of $T_{\rm sb}^{({\rm obs})}$ requires a Fourier-based analysis of the data. Therefore, each radar section was re-sampled onto an equally spaced grid of 2^N data points. The value of N was chosen independently for each profile, such that the new sampling interval is close to the mean original sampling interval (between 19.9 m and 23.8 m). The new data points were obtained using a cubic spline interpolation method, which also fills the data gaps. It should be noted that our results do not crucially depend on this interpolation method, and a piecewise linear interpolation could be used instead.

The calculation of transfer amplitudes (or equivalently, power spectra) from observational data can be surprisingly difficult, and results are often sensitive to various assumptions made in the analysis method. A common issue is the leakage of power between adjacent frequency bands, which results in a large variance for the spectral coefficients. In order to minimize this systematic error, we used Thompson's multitaper spectrum estimation method (Thomson, 1982; Prieto et al., 2009) whith 2 Slepian tapers and a time bandwith product of 4. Results were cross-checked using Welch's

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averaged periodogram method (Welch, 1967) with a Hamming window applied to a minimum of two overlapping segments with a fixed length of 45 km. Although the quantitative results were found to be sensitive to specific parameters in the applied processing (such as the number of tapers or the length of the Hamming window), qualitative results were robust and independent of the chosen method. In this text we only present results from the multitaper analysis.

4 Results

The estimated transfer amplitudes for all profiles are shown in Fig. 3, ranked from low values of the mean slip ratio in the top left to high values in the bottom right. Additionally, the dashed blue line in each figure represents the theoretical flow-line approximation, $T_{\rm sh}(\lambda_x, C^{(0)}, \alpha, H)$, with $C^{(0)}$ and α the estimated slip ratio and mean surface slope, respectively. As will be detailed in Sect. 5.1, the flow-line approximation generally overestimates the transfer amplitude as it neglects three-dimensional effects that cannot be accounted for from available observational data. In order to incorporate possible threedimensional effects, all flow-line curves in Fig. 3 have been rescaled by a constant factor f = 0.25 which was obtained from an optimal least square fit with observations. Although the physical origin of the scaling factor f < 1 is clear, the accuracy of the fit is rather poor in some cases (e.g. R3 and E10) and much better in other cases (e.g. R5 and E12). This variability can be related to uncertainties in our estimate of the mean slip ratio $C^{(0)}$, but it also suggests that the value of f is not unique across different profiles or across the entire range of wavelengths. Hence, three-dimensional effects cannot be captured by a simple parametrization. In addition, it should be noted that the obtained scale factor depends on particular details of the multitaper analysis method, which therefore reduces the physical relevance of its value.

The results depicted in Fig. 3 can be divided into three broad categories, depending on the value of the slip ratio. Profiles C1–C5 run along a steeper and slow-flowing section of the ice sheet, which results in larger internal deformation and low values of the

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slip ratio: $0.4 \le C^{(0)} \le 2.6$. For all these profiles, the theoretical estimate for the transfer amplitude is close to zero with a slight increase in transfer towards longer wavelengths. The observed amplitudes roughly follow this pattern, although the results lie systematically above the theoretical prediction and an increase towards longer wavelengths is not generally observed. Only in the case of C2 and C3, the transfer amplitude reaches a maximum at wavelengths above 10 ice thicknesses, whereas other profiles are relatively constant.

The second set of profiles, E1-E5, have mean slip ratios which are an order of magnitude larger. These sections follow relatively steep surface slopes with mean ice thickness values that vary from 2100 m to 2600 m. For these profiles the internal deformation velocity contributes to up to 15% of the surface speed, which leads to estimates of the mean slip ratio with values between 6.4 and 13.9. The theoretical curves in Fig. 3 predict a slight increase in transfer for wavelengths between 1 and 10 ice thicknesses. whereas the observed transfer amplitudes show a more varied behaviour: E2 and E4 follow the theoretical result, whereas E1 and E5 overestimate the transfer at wavelengths above 10 times the mean ice thickness, and E3 shows a distinctive maximum for wavelengths between 2 and 3 ice thicknesses. Except for the latter case, none of the other profiles shows a noticeable increase of transfer at intermediate wavelengths.

The remaining profiles, E6–E12 and R1–R5, have mean slip ratios ranging from 52 to 2111 which is reflected in higher surface speeds and/or less internal deformation. As expected from theory, all observed transfer amplitudes have a distinctive maximum at wavelengths between 1 and 20 ice thicknesses, providing strong evidence for the efficient transfer of medium-scale bedrock undulations to the surface of fast-flowing sections of the Rutford and Evans ice streams.

The results in Fig. 3 express a clear dependence of the peak amplitude on the mean slip ratio. This relationship is further exhibited in Fig. 4, which shows a scatter plot of slip ratios versus peak amplitudes for all profiles (blue squares). The estimated peak amplitudes are defined as the maximum of each transfer function between 1 and 20 ice thicknesses. The error bars in Fig. 4 correspond to extreme values of the slip ratio for

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each profile; the lower limit corresponds to its value for temperate ice whereas the upper limit is computed for a uniform ice column at -20°C. Despite a substantial amount of scatter, the plot indicates an increasing trend of about 350% over the considered range of slip ratios. This increasing trend is supported by theory (dashed line in Fig. 4), 5 although the flow-line model predicts a more rapid increase and a peak amplitude which converges quickly towards unity for mean slip ratios between 10 and 1000.

In all of the analysis so far we have assumed a constant value for the slip ratio along each profile, with the error bars in Fig. 4 indicating a maximum range of uncertainty due to unknown variations in the ice viscosity. In addition, it is feasible to assume that along-flow values of $C^{(0)}$ can change considerably due to variations in surface slope and surface speed. As a result, the transfer characteristics of an ice stream are spatially variable, with a gradual increase of the transfer from the upstream catchment towards the fast-flowing region near the grounding line. For longer flightlines this variability can be investigated by splitting the radar profiles into different sections and by analysing these sections separately. Results of such an analysis for the three longest profiles, E10 (207 km), E11 (183 km) and E12 (160 km), are represented by the red datapoints in Fig. 4. It is clear that for the upper sections (denoted by E10u, E11u and E12u), the mean slip ratio is suppressed due to lower ice velocities, and the transfer has decreased simultaneously. On the other hand, for the fast-flowing downstream sections (denoted by E10d, E11d and E12d) the mean slip ratio is significantly higher and the observed transfer is enhanced accordingly. These findings underline the large variability in the slip ratio and transfer along long profiles, but E10d, E11d and E12d also provide strong additional evidence for the efficient transfer of small bedrock perturbations to the surface of fast flowing sections of an ice stream.

In summary, the data confirms the existence of a maximum transfer amplitude for $C^{(0)} \gg 1$, and validates theoretical predictions about the relation between $C^{(0)}$ and the maximum transfer amplitude. Despite this good qualitative agreement between theory and observations, a more detailed comparison also marks several discrepancies. First, it should be noted that, unlike for theoretical estimates, most observed amplitudes do

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not have one continuous peak, but consist of several local maxima. A separation into two or more peaks, not necessarily of equal height, is apparent for most profiles, with R3 and E7-E8 being exceptions. Another notable difference is related to the absolute value of the peak height. Recall that the theoretical curves in Fig. 3 are rescaled by 5 a factor 0.25, and hence observed peak amplitudes are generally lower than expected from theoretical flow-line estimates. In general, the transfer is dampened by at least 60% and up to 70%, except for C1-C5 for which all estimates systematically exceed theoretical values. This dampening is also clear from Fig. 4, which shows observed peak heights as a function of the slip ratio and where the solid line represents the theoretical prediction. For $C^{(0)} > 20$, observed peak amplitudes lie consistently below the theoretical curve. In addition, for most profiles the peak position is shifted towards higher (e.g. for R2, R3) or lower (e.g. for E8-E11) wavelengths as compared to the analytical solution, and the observed shape of the transfer curve is markedly narrower than the shape of the corresponding theoretical curve. The potential physical and/or methodical origins of these discrepancies are numerous, and it is arguable that a complicated combination of several effects influences the observations. We will restrict our discussion to an overview of the principle mechanisms that might affect the results, and we provide a list of theoretical assumptions that need to be considered in order to aim for a better fit with observations.

5 Discrepancies between flow-line theory and observations

5.1 Transfer dampening

For all profiles with a slip ratio $C^{(0)} > 20$, the observed transfer amplitudes are consistently lower than the full Stokes flow-line predictions. Such a suppression of the surface response can have several (indistinguishable) causes.

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5.1.1 Three-dimensional effects

The most significant source of transfer dampening is related to the inherent three-dimensional character of the problem at hand. In the foregoing analysis, we have assumed that all analysed radar profiles were, to good approximation, parallel to the surface velocity field, and that transverse ice dynamical effects could be neglected. These assumptions were implemented in the theoretical transfer amplitude by taking the flow-line limit $\lambda_y \to \infty$ of the full three-dimensional solution $T_{\rm sb}(\lambda_x,\lambda_y,\mathcal{C}^{(0)},\alpha)$. In reality, corrections to the flow-line model come from a combination of two different sources: (i) flightlines are likely to have a small and variable across-flow component, and (ii) the limit $\lambda_y \to \infty$ is not exact as bedrock features have a finite size in the transverse direction. Due to the lack of observational knowledge about transverse bedrock and surface properties, an assessment of three-dimensional effects relies on synthetic modelling.

Previous modelling efforts by Reeh (1987) and Sergienko (2012) have shown that a non-zero ratio between longitudinal and transverse wavelengths can have a substantial effect on the flow as the wavelength ratio increases, and surface amplitudes can be reduced by more than one order of magnitude as compared to the two-dimensional plane approximation. In order to study the effect of finite transverse wavelengths on the estimated transfer amplitude, we analyse a full Stokes flow with linear ice rheology over a Gaussian-shaped bedrock undulation with mean bedrock inclination $\alpha = 0.003$ rad and mean slipperniness $C^{(0)} = 100$. Figure 5a, b shows the bedrock profile and surface response along four different transects (denoted by FL1–FL4) which are oriented at different angles with respect to the flow direction. The bed-to-surface transfer for each profile is presented in Fig. 5c (black curves), together with the two-dimensional flow-line prediction (red curve). The results show two clear tendencies: (i) The three-dimensional transfer in the direction of the flow (FL1) is suppressed by about 15 % as compared to two-dimensional result, and (ii) the suppression of the transfer increases as the angle between the flightline and the flow direction increases. This systematic

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5.1.2 Non-isothermal ice

All theoretical results discussed so far were derived for a spatially constant viscosity, whereas more realistic treatments use a depth-dependent relation for η . For example, if one assumes an exponential decrease of the viscosity with depth,

$$\eta(z) = \eta_{\rm s} {\rm e}^{\mu z},\tag{5}$$

with $\eta_{\rm s}$ the viscosity at the surface, and μ a factor that scales the vertical variation of η , then the full Stokes system can be solved analytically, and one finds that a gradual increase of the viscosity towards the surface leads to a systematic reduction of the transfer (Gudmundsson, 2004b). The amount of reduction depends on μ , a parameter that can vary along an ice stream and between different ice streams. The reason for the reduced transfer is the presence of stiffer, more viscous ice near the surface, which has a dampening effect. We have partially taken this effect into account by setting η equal to its recommended base value at $-10\,^{\circ}$ C. As such, the ice stream is not treated as a temperate feature ($\sim 0\,^{\circ}$ C) with a value for η that is generally too low, nor is it treated as a cold feature ($\sim -20\,^{\circ}$ C) with a value for η that is too high and only valid in the uppermost layers.

5.1.3 Ice rheology

Analytical solutions for the transfer in the full Stokes system are only known for a linear flow law and linear sliding law. It has been pointed out by Raymond and Gudmundsson (2005) that higher values of Glen's exponent generally lead to an *increase* of the maximum transfer by about 20 % for n = 3. On the other hand, the effect of a non-linear sliding law on the maximum transfer amplitude is negligible. As it is generally assumed

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that the physical value of *n* is larger than unity, this result at least partially offsets the dampening effects discussed above. Also anisotropic properties of the ice affect the flow and hence the transfer characteristics. For ice streams, anisotropic effects are conveniently parametrized by a constant enhancement factor in Glen's flow law, which effectively describes a softening of the ice and therefore an increase in the transfer. The uncertainties related to this effect are included in the error bars in Fig. 4, which correspond to extreme limits for the ice viscosity.

5.2 Multiple peaks

It is not immediately obvious how the presence of multiple peaks in the observed transfer amplitudes can be explained within the current theoretical framework. Certainly, there is no combination of parameter values α and $C^{(0)}$ that reproduces such behavior. However, one should recall that $T_{\rm sb}(\lambda_x)$ describes the amplitude ratio between surface undulations (Δs) and bedrock undulations (Δb) for all wavelengths, whereas it is likely that certain wavelengths (or intervals of wavelengths) are dampened or totally absent from physical bedrock profiles. Therefore, the overlying ice and the surface topography in particular, contain little or no information about these wavelengths. Only a uniform basal power spectrum and its corresponding surface expression allow the exact retrieval of $T_{\rm sb}(\lambda_x)$ for all wavelengths $0 < \lambda_x < \infty$. For basal profiles that deviate from a uniform distribution, including all physical profiles, an accurate retrieval of the transfer is restricted to wavelengths that carry sufficient weight in the powerspectrum. In addition, the finite length and finite sampling interval of each profile prevent an accurate retrieval of $T_{\rm sb}(\lambda_x)$ at short and long wavelengths, independent on the power spectral density.

To elaborate on these points we study a synthetic model with a representative 20 m grid resolution and 2^{13} grid points, slip ratio $C^{(0)} = 100$, uniform inclination $\alpha = 0.003$ rad and three different bedrock profiles.

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(i) The first bedrock topography has a uniform frequency distribution, as shown in Fig. 6a. The difference between the "observed" transfer amplitude $T_{ch}^{(obs)}$ and the theoretical curve $T_{\rm sb}$ is depicted in Fig. 6b, and is close to zero for all wavelengths between 1 and 20 ice thicknesses. For wavelengths $\lambda_x > 20H$ the finite length of the profile (164 km) introduces additional errors.

- (ii) The second bedrock profile has a Gaussian shape with height 0.025H and variance 1.5H. The power spectral density is monotonically increasing whith a zero asymptote for wavelengths < 2H and a limiting value of 7.3×10^5 for wavelengths > 20H. The observed transfer amplitude shows the largest deviations from the theoretical result for $\lambda_{x} < H$, i.e. for wavelengths that are suppressed or absent in the basal spectrum.
- (iii) The third topography is similar to the previous one, but the spectral density has additionally been suppressed by a factor 0.2 for wavelengths between 4H and 6.5H. The difference between the estimated and theoretical transfer amplitudes is now largest for $3.5 < \lambda_v < 10H$, and the estimated transfer amplitude has been separated into two maxima with wavelengths 3.5H and 7H (not shown).

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In summary, all three idealized cases illustrate the possible effects of a finite profile length on the estimated transfer. In this study we have minimized this sampling error through the use of sufficiently long profiles, arguably at the cost of introducing larger variability in the basal slipperiness (recall Sect. 4). Synthetic results also suggest that the presence of multiple peaks and a reduction of transfer at certain wavelengths can be related to properties of the basal power spectral density. If such a relation is significant, it should be readily inferable from the observed basal power spectrum and the observed transfer amplitudes. However, no general support for such a relation was found in our dataset, despite synthetic evidence that attributes the existence of multiple peaks to limitations of the dataset, and discards deficiencies in the theoretical model or our analysis method.

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We find that for large values of the slip ratio, i.e. for fast-flowing ice streams, the surface topography carries important information about bedrock undulations with wavelengths between 1 and 20 times the mean ice thickness. The efficiency of the bed-to-surface transfer at these wavelengths increases at a rate of $\sim 350\,\%$ with increasing values of the slip ratio. These observations are in good qualitative agreement with the theoretical results obtained for a full Stokes system by Gudmundsson (2003) and Raymond and Gudmundsson (2005). Results from the slow-flowing Carlson Inlet confirm the important difference between the flow characteristics of ice streams for which most (95 % and often more) of the velocity is due to basal sliding, and Alpine-type glaciers which attain a considerable fraction of their surface speed by internal creep. The latter do not exhibit any significant transfer of small-scale topographic features to the surface.

Several differences between observations and theoretical flow-line predictions have been observed and clarified. (i) The separation of the transfer peak into several local maxima and the suppression of the transfer for certain wavelength intervals has its possible origin in a non-uniform power spectral density of the bedrock profile. (ii) The measured transfer for fast-flowing ice is systematically reduced by a factor of 60 % or more as compared to the flow-line theory, which is arguably due to the inherent three-dimensional character of an ice stream. I.e., the presence of finite transverse bedrock undulations leads to a reduction in the surface expression of longitudinal wavelengths.

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Additionally, non-isothermal ice properties generate a layer of stiffer ice near the surface which dampens the transfer.

Our analysis provides an important verification for the use of current theoretical models in ongoing efforts to study ice stream dynamics, and for their use in inverse methods to obtain information about basal perturbations (topography and slipperiness) from surface measurements. Results show a good qualitative agreement with the full Stokes theory, which suggests that other predictions of this theory can also be trusted and are of importance for our understanding of ice stream dynamics. For example, Gudmundsson (2003) shows that the length scale which characterizes the transmission of horizontal deviatoric stresses increases with increasing values of the slip ratio. This length scale becomes particularly large (100 or 1000 times the mean ice thickness) for fast-flowing ice streams, which means that its value is controlled by ice-stream width rather than ice thickness. On the other hand, results of our analysis disagree with models that are based on the shallow ice sheet and shallow ice stream approximations. These approximations, which are commonly used for the inversion of basal properties, either grossly overestimate the transfer at wavelengths < 10H (shallow ice stream) or do not reproduce an increase in the transfer at intermediate wavelengths at all (shallow ice sheet), as can be seen from Fig. 1. As such, forward (inversion) results about the surface (basal) topography at these wavelengths are bound to be erroneous when obtained from shallow ice flow models.

Finally, we stress that the correspondence between observed and theoretical transfer amplitudes implies that local surface undulations of the Rutford and Evans ice streams are largely controlled by local variation in the bedrock topography. In our analysis, which is restricted to wavelengths less than 20 times the mean ice thickness, we find no direct evidence for the impact of variations in basal slipperiness on surface topography. Theoretical results indeed suggest that the effect of small-scale perturbations in slipperiness only become relevant at wavelengths much larger than 20 times the mean ice thickness (Gudmundsson, 2003). It also confirms previous results for the Rutford Ice Stream (Raymond-Pralong and Gudmundsson, 2011), and suggests that variations in

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basal topography should be treated carefully when inverting surface data for spatial variation in basal shear stress at length scales less than 20 ice thicknesses.

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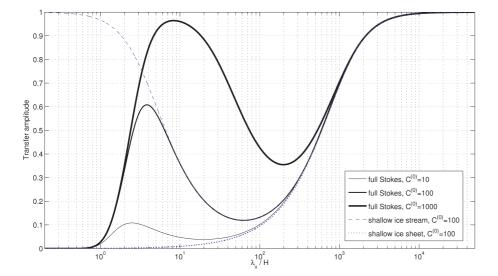


Fig. 1. Two-dimensional steady-state transfer amplitude $T_{\rm sb}(\lambda_x)$ for $\alpha=0.003\,{\rm rad}$ and 3 values of the mean slip ratio; $C^{(0)}=10,\ C^{(0)}=100\,{\rm and}\ C^{(0)}=1000$. Black curves represent the full Stokes solution, whereas dashed and dotted blue lines correspond to the shallow ice stream and shallow ice sheet approximation, respectively. All solutions are given for a linear ice rheology and linear sliding law.

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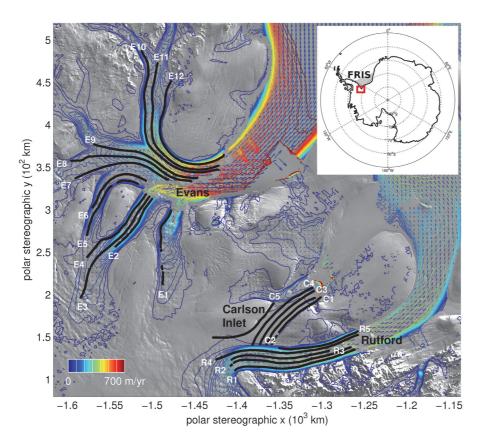


Fig. 2. Map showing the Rutford Ice Stream, Evans Ice Stream and Carlson Inlet which flow into the Filchner-Ronne Ice Shelf (FRIS), West Antarctica (see inset). The color scale and arrows indicate the InSAR-derived surface velocity field (Rignot et al., 2011) overlaid on a subset of the MODIS mosaic for Antarctica. Only velocities higher than 20 myr⁻¹ are shown. Black lines represent the 22 sections of radar profiles that were analyzed in this work.

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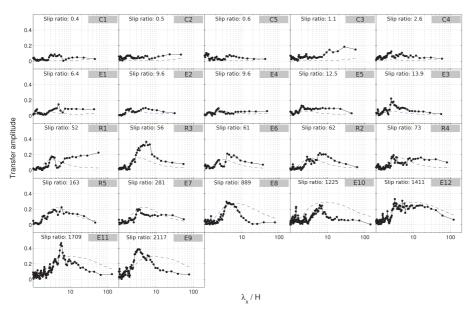


Fig. 3. Estimated transfer amplitudes for radar profiles along the Carlson Inlet (C1–C5), Rutford Ice Stream (R1-R5) and Evans Ice Stream (E1-E12), ranked from low to high values of the slip ratio. The dashed blue lines show the corresponding flow-line prediction, scaled by a factor f = 0.25 in order to account for three-dimensional effects. The value of f was obtained from an optimal least-square fit with the observations.

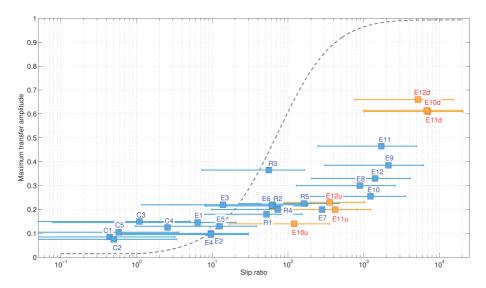


Fig. 4. Blue squares represent a scatter plot of the maximum transfer amplitude as a function of the mean slip ratio for all 22 profiles in this study. The plot shows a clear increasing trend for increasing values of the slip ratio. Error bars depict the maximum uncertainty in the slip ratio due to a lack of knowledge about the ice viscosity. Lower limits correspond to the assumption of a temperate ice column, whereas upper limits are obtained for a uniform ice temperature of $-20\,^{\circ}$ C. The dashed line corresponds to the flow-line prediction of the full Stokes system for $\alpha = 0.003\,\text{rad}$. Orange data points show the maximum transfer amplitude and mean slip ratio for the upper sections (denoted by an index u) and lower sections (denoted by an index d) along flightlines E10, E11 and E12.

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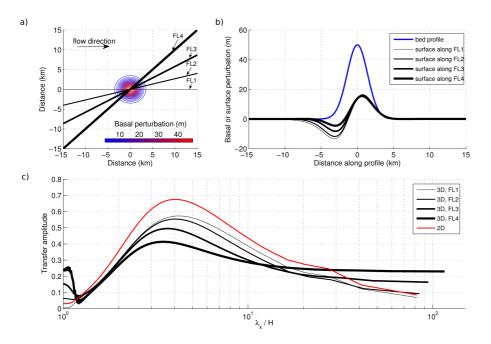


Fig. 5. (a) Gaussian-shaped bedrock undulation which was used to simulate the three-dimensional flow. Sections were taken at an angle of 0, 15, 30 and 45 degrees with respect to the flow direction and are denoted by FL1, FL2, FL3 and FL4, respectively. (b) The blue curve represents the basal perturbation which is identical along each section. Black curves represent the three-dimensional surface response along each section, showing a clear angle-dendence with increased dampening of the transfer for larger angles. (c) Transfer amplitudes estimated from Δs and Δb along each section (black lines), as well as the two-dimensional result (red curve) for the same bedrock profile, uniform inclination and slip ratio. The two-dimensional flow-line limit neglects three-dimensional effects, which leads to a systematic overestimation of the transfer at wavelengths less than 20 times the mean ice thickness.

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Observed bed-to-surface transfer

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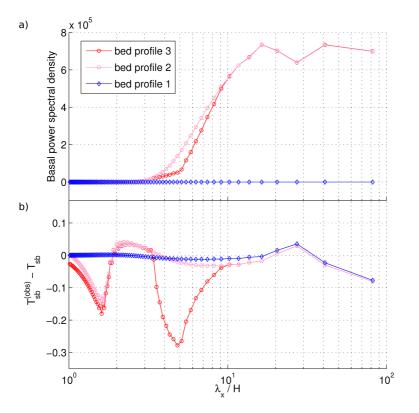


Fig. 6. (a) Power spectral densities for three different bedrock profiles. The blue profile has a uniform spectral distribution and corresponds to a delta peak, the pink profile corresponds to a Gaussian basal undulation, and the red profile represents the same Gaussian undulation but with part of the wavelength spectrum suppressed (see text for more details). (b) Difference between the estimated transfer amplitude for each synsthetic profile in (a), and theoretical transfer amplitude.

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