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Interaction between ice sheet dynamics and subglacial lake circulation: a coupled modelling approach

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Abstract

Subglacial lakes in Antarctica influence to a large extent the flow of the ice sheet. In this study we use an idealised lake geometry to study this impact. We employ a) an improved three-dimensional full Stokes ice flow model with a nonlinear rheology, b) a three-dimensional fluid dynamics model with eddy diffusion to simulate basal mass balance, and c) a newly developed coupler to exchange boundary conditions between individual models. Different boundary conditions are applied over grounded ice and floating ice. This results in significantly increased temperatures within the ice on top of the lake, compared to ice at the same depth outside the lake area. Basal melting of the ice sheet increases this lateral temperature gradient. Upstream the ice flow converges towards the lake and accelerates by about 10% whenever basal melting at the ice–lake boundary is present. Above and downstream of the lake, where the ice flow diverges, a velocity decrease of about 10% is simulated.

1 Introduction

During the last decades our knowledge on subglacial lake systems has greatly increased. Since the discovery of the largest subglacial lake, Lake Vostok (Oswald and Robin, 1973; Robin et al., 1977), more than 160 other lakes have been identified so far (Siegert et al., 2005; Carter et al., 2007; Bell, 2008; Smith et al., 2009). Plenty of efforts have been undertaken to reveal partial secrets subglacial lakes may hold, mostly referring to Lake Vostok. For instance the speculation that extremophiles in subglacial lakes may be encountered (e.g., Duxbury et al., 2001; Siegert et al., 2003) has been nurtured by microorganisms discovered in ice core samples (Karl et al., 1999; Lavire et al., 2006). These samples originate from the at least 200 m thick accreted ice, drilled at the Russian research station Vostok (Jouzel et al., 1999). Discussions about the origin and history of the lake (Duxbury et al., 2001; Siegert, 2004; Pattyn, 2004; Siegert, 2005) are still ongoing. It is still unknown whether Subglacial Lake Vostok existed prior

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the Antarctic glaciation or whether it could have survived during glaciation. The impact of subglacial lakes on the flow of the overlying ice sheet has been analysed (e.g., Kwok et al., 2000; Tikku et al., 2004) and modelled (Mayer and Siegert, 2000; Pattyn, 2003; Pattyn et al., 2004; Pattyn, 2008), but self-consistent numerical models are lacking at present. Numerical estimates and models (Wüest and Carmack, 2000; Williams, 2001; Walsh, 2002; Mayer et al., 2003; Thoma et al., 2007, 2008b; Filina et al., 2008) as well as laboratory analogues (Wells and Wettlaufer, 2008) of water flow within the lake have been carried out. Finally, observations (Bell et al., 2002; Tikku et al., 2004) and numerical modelling (Thoma et al., 2008a) of accreted ice at the ice–lake interface 10 gave insights about its thickness and distribution across of subglacial lakes.

Early research assumed that subglacial lakes were self contained, while only recently Gray et al. (2005), Wingham et al. (2006) and Fricker et al. (2007) found evidence that Antarctic subglacial lakes are connected, hence forming an extensive subglacial hydrological network. Several plans to unlock subglacial lakes exist (Siegert et al., 2004; Inman, 2005; Siegert et al., 2007; Schiermeier, 2008; Woodward et al., 2009) 15 and valuable knowledge will be available as soon as direct samples of subglacial water and sediments are taken.

However, current knowledge about the *interaction* between subglacial lakes and the overlying ice sheet is lacking. The most important parameter exchanged between ice 20 and water is heat. The exchange of *latent heat* associated with melting and freezing dominates *heat conduction*, but the latter process cannot be ignored in subglacial lakes (Thoma et al., 2008b). Melting and freezing is closely related to the ice draft which varies spatially over subglacial lakes (Siegert et al., 2000; Studinger et al., 2004; Tikku et al., 2005; Thoma et al., 2007, 2008a, 2009). The ice draft, and hence the water circulation 25 within the lake, is maintained by the ice flow across the lake. Without this flow, lake surfaces would even out (Lewis and Perkin, 1986). On the other hand, a spatially varying melting/freezing pattern will have an impact on the overlying ice sheet as well. In order to get an insight in the complex interaction processes between the Antarctic ice sheet and subglacial lakes, this study for the first time couples a numerical ice-flow

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and a lake-flow model.

In the first two sections we introduce the applied ice-flow model RIMBAY and lake-flow model ROMBAX, respectively. Each section starts with a general description of the particular model, describes the applied boundary conditions, and the results. Section 4 introduces the newly developed RIMBAY–ROMBAX–coupler RIROCO and discusses the impact of a coupled ice–lake system on the ice flow.

2 Ice model RIMBAY

2.1 General description

The ice sheet model RIMBAY (Revised Ice sheet Model Based on frAnk pattYn) is based on the work of Pattyn (2003), Pattyn et al. (2004) and Pattyn (2008). Within this three-dimensional, full Stokes ice model, a subglacial lake is represented numerically by a vanishing bottom-friction coefficient of $\beta^2=0$, while high friction is represented by a large coefficient; in this study we use $\beta^2=10^6$. The choice of the latter parameter has only little influence on the model behaviour.

The constitutive equation, governing the creep of polycrystalline ice and relating the deviatoric stresses τ to the strain rates $\dot{\varepsilon}$, is given by Glen's flow law: $\dot{\varepsilon}=A\tau^n$ (e.g., Pattyn, 2003), with a temperature dependent rate factor $A=A(T)$. Here we apply the so-called Hooke's rate factor (Hooke, 1981). Experimental values of the exponent n in Glen's flow law vary from 1.5 to 4.2 with a mean of about 3 (Weertman, 1973; Patterson, 1994); ice models traditionally assume $n=3$. However, a simplified viscous sliding law with $n=1$ stabilises and accelerates the convergence behaviour of the implemented numerical solvers. Therefore, previous subglacial lake simulations were limited to a viscous sliding law (Pattyn, 2008).

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2.2 Model setup and boundary conditions

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The model domain used in this study is a slightly enlarged version of the one presented in Pattyn (2003): It consists of a $168\,100\text{ km}^2$ domain with a model resolution of 5 km (a resolution of 10 km is also used for comparison) and 41 terrain-following vertical layers. The surface of the initially 4000 m thick ice sheet has an initial slope of 2% (similar to Lake Vostok, Tikku et al., 2004) from left (upstream) to right (downstream). An idealized circular lake with a radius of about 48 km and an area of about 7200 km^2 is located in the center of the domain, where a 1000 m deep cavity modulates the otherwise smoothly sloped bedrock (similar to Pattyn, 2008). The lake's maximum water depth of about 600 m, resulting in a volume of about 1840 km^3 (The lake's geometry is also indicated in Fig. 3).

We apply a constant surface temperature of -50°C at the ice's surface, a typical value for central Antarctica (Comiso, 2000). The bottom layer boundary temperature depends on the basal condition: above bedrock a Neumann boundary condition is applied, based on a geothermal heat flux of 54 mW/m^2 (a value applied in former subglacial lake flow studies by Thoma et al., 2007), above the subglacial lake the bottom layer temperature is at the pressure-depended freezing point. This temperature, prescribing a Dirichlet boundary condition, depends on the local ice sheet thickness: $T_b=H\cdot8.7\times10^{-4}\text{ }^\circ\text{C/m}$ (e.g., Paterson, 1994). Accumulation and basal melting/freezing is ignored during the initial experiments, but in subsequent experiments, basal melting and freezing at the lake's interface is accounted for (Sect. 4). Lateral boundary conditions are periodic, hence values of ice thicknesses, velocities, and stresses are copied from the upstream (left) side to the downstream (right) side of the model domain and vice versa. The same applies to the lateral borders along the flow. The initial integration starts with an isothermal ice sheet geometry. The basal melt rate is set to zero over bedrock as well as over the lake.

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2.3 Model improvements

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Compared to Pattyn (2008) we improved the model RIMBAY in two significant ways to allow a numerically stable and fast representation of the more realistic non-linear flow law with an exponent of $n=3$: first, a gradual increase of the friction coefficient β^2 at the 5 lake's boundaries is considered (Fig. 1a). Physically, this smoothing can be interpreted as a lubrication of the ice sheet base on the grounded side and as stiffening due to debris on the lake side of the lake's edge. Our experiments have shown, that a slight β^2 -smoothing coefficient of (1/0) is suited to decrease the integration time significantly and stabilises the numerical results. In this notation, (1) indicates *one* lubricated node 10 on the bedrock side of the boundary and (0) indicates *no* stiffed (debris) node on the lake side is prescribed. If the number of lubricated nodes is reduced to zero, the model's integration time is increased, without a significant impact on the velocity field. If the number of stiffed nodes over the lake is increased, lower velocities over the lake 15 are achieved. However, for higher model resolutions than used in this study, higher β -values should be considered to make the transition more realistic.

Second, we implement a three-dimensional Gaussian-type filter to smooth the viscosity as well as the vertical resistive stress with a variable filter width. Figure 1b shows a one-dimensional equivalent to the implemented three dimensional filter. Figure 2 compares three different smoothing parameter results on the friction coefficient β^2 as 20 well as the Gaussian-type filter impact on the viscosity for three different filter widths. Our preliminary experiments have shown, that with a slight transient β^2 smoothing at the lake edges combined with a gentle (quadratic) Gaussian filter, as shown in Fig. 2b, numerical stability is achieved.

2.4 Results

25 The standard experiment is a thermomechanically coupled full Stokes (FS) model with a horizontal resolution of 5 km. A quasi-steady state is reached after 300 000 years. Figure 3a shows the lake's position and depth in the center of the model domain. The

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frictionless boundary condition over the lake results in an increased velocity, not only above the lake, but also in its vicinity. From mass conservation it follows, that the (vertically averaged) horizontal velocity converges towards the lake from upstream and diverges downstream. The significantly flattened ice sheet surface over the lake is a consequence of the isostatic adjustment. This effect is also visible in the geometry of the profiles in Fig. 3b and c. Figure 4a shows the vertically averaged horizontal velocity and Fig. 3b a vertical cross section of the velocity along the flow at the lake's center at $y=200$ km. Over the lake, the ice sheet behaves like an ice shelf, featuring a vertically constant velocity. Towards the lake, the surface velocity increases by more than 80% from about 0.7 m/a to about 1.2 m/a. The largest velocity gradients occur at the grounding line (Fig. 4a). After reaching the lake, the accelerated ice at the surface first slows down, because of mass convergence, before it accelerates again to reach its (nearly) constant velocity maximum across the lake (Fig. 3b). The vertical temperature profile (Fig. 3c) is nearly linear, as accumulation and basal melting are neglected. Geothermal heat flux is not sufficient to melt the bottom of the ice, but over the lake the freezing point is reached. This results in submerging isotherms. At the downstream grounding line a slight overshoot of the upwelling isotherm is observed.

To investigate the impact of the horizontal resolution, a model run with a coarser 10 km grid has been performed. Although most features are reproduced well, there is a significant impact on ice velocities, in particular along the grounding line where the differences reaches about 10% (Fig. 4b). In general, the model with the higher resolution has increased velocities along the flowlines across the lake and decreased velocities outside. In addition, the local velocity maximum above the grounding line cannot be resolved with the 10 km resolution.

We also investigated, whether a higher order model (HOM), neglecting resistive stress and vertical derivatives of the vertical velocity (see Pattyn, 2003; Saito et al., 2003; Marshall, 2005, for further details), is able to reproduce the results obtained with the full Stokes model. Our experiments indicate a moderate impact on the ice flow: calculated velocities across the subglacial lake are about 5% lower compared to the

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full Stokes model (Fig. 4c). In the vicinity of the lake, the impact of the full Stokes terms decreased, but is still enhanced along the flowlines. As the HOM does not need significantly less integration time compared to the FS, all further studies are performed with the full Stokes model.

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5 3 Lake flow model ROMBAX

3.1 General description

We apply ROMBAX, a terrain-following, primitive equations, three-dimensional, fluid dynamics model (e.g., Griffies, 2004) to simulate the water flow in the prescribed subglacial lake. ROMBAX simulates the interaction between ice and subjacent water in terms of melting and freezing, according to heat and salinity conservation and the pressure dependent freezing point at the interface (Holland and Jenkins, 1999). The model uses spherical coordinates and has been applied successfully to ice-shelf cavities (e.g., Grosfeld et al., 1997; Williams et al., 2001; Thoma et al., 2006) as well as to subglacial lakes (Williams, 2001; Thoma et al., 2007, 2008a,b, 2009; Filina et al., 15 2008; Woodward et al., 2009).

3.2 Model setup and boundary conditions

The bedrock topography and the ice draft, needed for the lake-flow model ROMBAX, is obtained from the output (Sect. 2.4) of the ice-flow model RIMBAY (see Sect. 4 for further details). The horizontal resolution ($0.025^\circ \times 0.0125^\circ$, about 0.7×1.4 km), the number of vertical layers (16), as well as the horizontal and vertical eddy diffusivities ($5 \text{ m}^2/\text{s}$ and $0.025 \text{ cm}^2/\text{s}$, respectively) are adopted from a model of subglacial Lake Concordia (Thoma et al., 2009). In a model domain of about 170×88 grid cells the circulation within the lake as well as the melting and freezing rates at the lake–ice interface are calculated. At the bottom of the lake a geothermal heat flux of 54 mW/m^2 , consistent

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with the ice-flow model's boundary condition, is applied. Previous subglacial lake simulations of Lake Vostok (Thoma et al., 2007, 2008a; Filina et al., 2008), Lake Concordia (Thoma et al., 2009), or Lake Ellsworth (Woodward et al., 2009) used a prescribed heat conduction into the ice ($Q_{\text{ice}} = dT/dz \cdot 2.1 \text{ W/(K m)}$), based on borehole temperature measurements or simple thickness temperature-gradient estimates. The coupling to an thermomechanical ice-sheet model permits a spatially varying Q_{ice} (Fig. 5a). Across the lake's center, a general draft-following gradient from about 27 mW/m^2 on the upstream side of ice flow to about 24 mW/m^2 on the downstream side results from the modelled temperature gradient in the ice (Fig. 3c) and is used as input for the lake-flow model.

3.3 Results

The initial model run starts with a lake at rest. After about 200 years a quasi-steady state is reached. The circulation within the lake is shown in Fig. 5b and c. The vertically integrated mass transport stream function (with a strength of about 1.3 mSv , $1 \text{ mSv} = 1000 \text{ m}^3/\text{s}$) as well as the zonal overturning (about 0.3 mSv) show a two-gyre structure, while the meridional overturning (about 1.3 mSv) indicates just one anticyclonic gyre. The strength of the mass transport is between those modelled for Lake Vostok and those for Lake Concordia (Thoma et al., 2009). There is only a slight ice draft slope from about 4006 to 3927 m across the 90 km of the lake (Fig. 3b and c). This results in a decrease of melting from about 12 mm/a in the West to a negligible freezing along the eastern coastline (Fig. 5d). A significant amount of freezing would only be modelled if the ice draft would have a steeper slope.

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4.1 General description

The bedrock topography and the ice draft, necessary to set up the geometry for the lake-flow model ROMBAX (Sect. 3.2), was obtained from the modelled output geometry of the ice-flow model RIMBAY (Sect. 2.4). In addition, the thermodynamic boundary condition of the heat conduction into the ice was calculated from the temperature gradient at the ice sheet's bottom. The left part of Fig. 6 (gray lines) shows schematically the performed operations. A coordinate conversion is necessary as RIMBAY uses Cartesian coordinates while ROMBAX is based on spherical coordinates.

The modelled melting and freezing rates (Fig. 5d) are considered to replace the former neglected lower boundary condition in the ice-flow model RIMBAY (indicated by the central triangle within the yellow area in Fig. 6). Again a coordinate transformation is necessary. To speed up the integration time, ice geometry, ice flow, and ice temperature from the initial model run are reused (indicated by the black-lined triangle within the blue area within Fig. 6). An additional process has to be considered since the lake's area may change during an ice-model run. As the basal mass balance (melting/freezing) depends on the former lake-model results and cannot be calculated during a specific model run, extrapolation of neighbouring values may be necessary (indicated by the embedded yellow oval in the blue area of Fig. 6).

Successive initialisations of the lake-flow model ROMBAX are performed with the slightly changed ice draft and water column thickness (indicated by the right triangle in the yellow area of Fig. 6), as well as the temperature field of the previous model-run (indicated by the central triangle in the orange area of Fig. 6). Because the lake flow model does not permit dynamically changing geometry, temperatures of re-emerging nodes have to be extrapolated from neighbouring nodes (indicated by the embedded yellow oval in the orange area of Fig. 6). It is not necessary to reuse (and possibly extrapolate) the water circulation, as this value is based on the tracer distribution and converges quickly.

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The coupling mechanism, including initial starts of the individual models, parameter exchanges, coordinate transformations, and restart-initialisations are embedded into and controlled by the RIMBAY–ROMBAX–Coupler RIRoCo.

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4.2 Results

- 5 From ROMBAX the basal mass balance at the ice sheet–lake interface is considered for subsequent initialisations of RIMBAY. Melting dominates freezing (which is negligible) and hence the ice sheet is loosing mass. Note that the melted ice does not affect the lake's volume, neither in the ice-sheet model nor in the lake-flow model, as this is constant per definition. Ice sheet volume in the model domain is decreasing by about
- 10 600 km³ per 100 000 years, equivalent to about 3.5 m thickness. Ice draft reduction in the lake-flow model within 100 000 years is shown in Fig. 7a. Most ice is lost in the center of the lake (up to 8 m), and the area of maximum mass loss is slightly shifted to the upstream side of the lake. Consequently, the impact on the water column (Fig. 7b) is increased where most ice is melted and decreased where less ice is melted. However,
- 15 this ice-thickness reduction and slope adjustment is too small to change the surface pressure on the lake water, and hence the water flow, significantly. Just a few iteration cycles are needed to bring this coupled lake-water system into a quasi-steady state.

Several impacts of bottom melting on ice on top of the lake are are observed: First, the temperature gradient at the ice sheet's bottom is increased. This results in an

- 20 increase of heat conduction into the ice by about 22% (Fig. 7d), compared to a model run without basal melting (Fig. 5a). Consequently, more heat is extracted from the lake and the modelled average melting decreases by about 7% (Fig. 7c). Second, ice sheet thickness above the lake is reduced. This increases the surface gradient towards the upstream part and decreases the surface gradient towards the downstream part.
- 25 Hence, the ice flow upstream accelerates and decelerates downstream (Fig. 8a). The magnitude of the ice velocity change is about 10%. Third, bottom melting removes mass and a vertical downward velocity follows from mass conservation. This advects colder ice from the surface towards the bottom, resulting in a relative cooling of up

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to -2.1°C (Fig. 8b) above the lake. This negative temperature anomaly (compared to the model run without melting, Fig. 3c) is advected downstream by the horizontal velocity. The artificial cooling, visible at the lateral boundaries in Fig. 8b, results from the periodic boundary conditions and is not discussed here.

5 Summary

Observations from space show that subglacial lakes have a significant impact on the shape and dynamics of the Antarctic Ice Sheet. These regions depict a change in surface slope due to the isostatic adjustment of the ice sheet. This, combined with the lacking bottom friction, results in an observable redirection of ice flow. In this study,

10 we apply a newly coupled ice sheet–lake flow model on an idealized ice sheet–lake configuration to investigate the feedbacks between the individual systems. The full Stokes ice sheet model (Pattyn, 2008) is improved to handle a more realistic non-linear rheology. The lake-flow model is based on a three dimensional fluid dynamics model with eddy diffusivity and simulates the lake flow as well as the mass balance at the 15 lake–ice interface. This model is based on previous lake-exclusive studies, but now receives its geometry directly from the ice flow model. In addition, heat flux from the lake into the ice sheet is an exchange parameter. Besides other external forcing fields, the ice-flow model receives the basal mass balance at the interface from the dynamic lake-flow model.

20 In order to stabilise the ice-flow model numerically with a nonlinear rheology, a slight Gaussian filtering of the ice viscosity is necessary.

The ice flow converges and accelerates towards the lake, where an ice-shelf type flow structure establishes. Mass conservation requires a downstream divergence of flow, because of the deceleration when the flow reaches the bedrock again. Melting 25 at the lake–ice interface increases the ice flow acceleration upstream and decreases the ice flow on top of the lake as well as downstream, because of the reduced surface slope. The temperature at the ice sheet bottom is at the pressure melting point, and

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hence warmer than the bedrock-based ice in the vicinity. According to our simulation, melting at the lake–ice interface reduces the temperature on top of the lake. Advection transports the relatively colder ice downstream, and hence the temperature dependent rheology will have impacts on the ice flow beyond the lake.

5 Our idealised configuration of an ice–lake system indicates an important impact of the interaction between both systems. Future applications to more realistic configurations, such as Lake Vostok and its glacial drainage system, will show the impact for a more realistic scenario.

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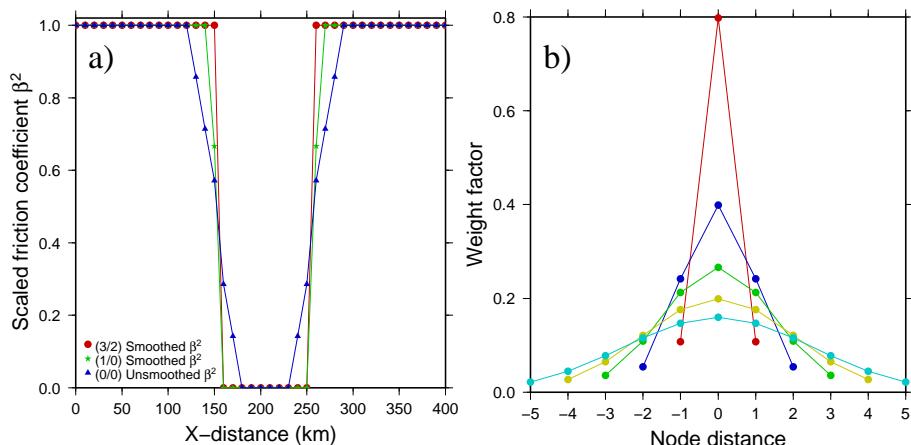


Fig. 1. (a) Friction coefficient β^2 (scaled to the maximum of 10^6) along the central x -axis for an unsmoothed and two test-smoothed cases. The smoothing coefficient (x/y) represents the number of nodes smoothed outside and inside of the lake's border, respectively. (b) Weight factors for a Gaussian-type filter with different width from one (red) to five (cyan) depending on the distance to the central node located at zero.

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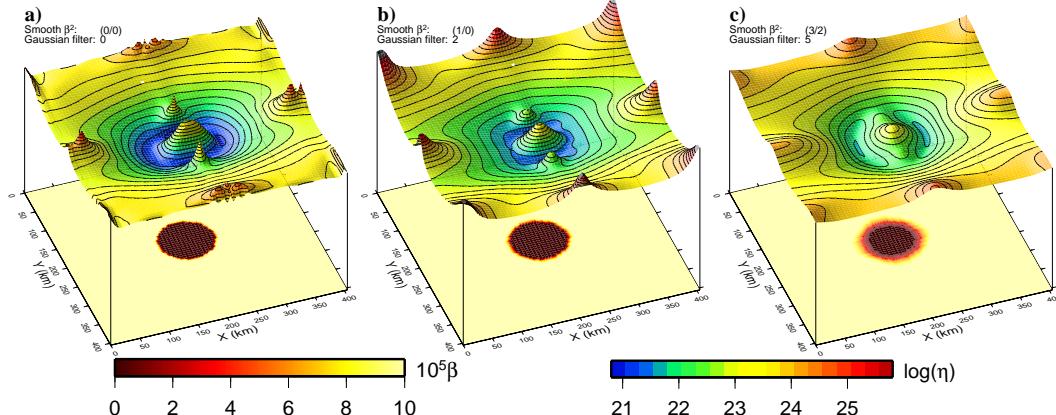


Fig. 2. Logarithm of viscosity η of the surface layer and bedrock-friction parameter β^2 for an idealized model. **(a)** No β^2 -smoothing or Gaussian filtering. **(b)** Slight β^2 -smoothing (1/0) and Gaussian filtering with a filter width of two. **(c)** Strong β^2 -smoothing (3/2) and Gaussian filtering with a filter width of five.

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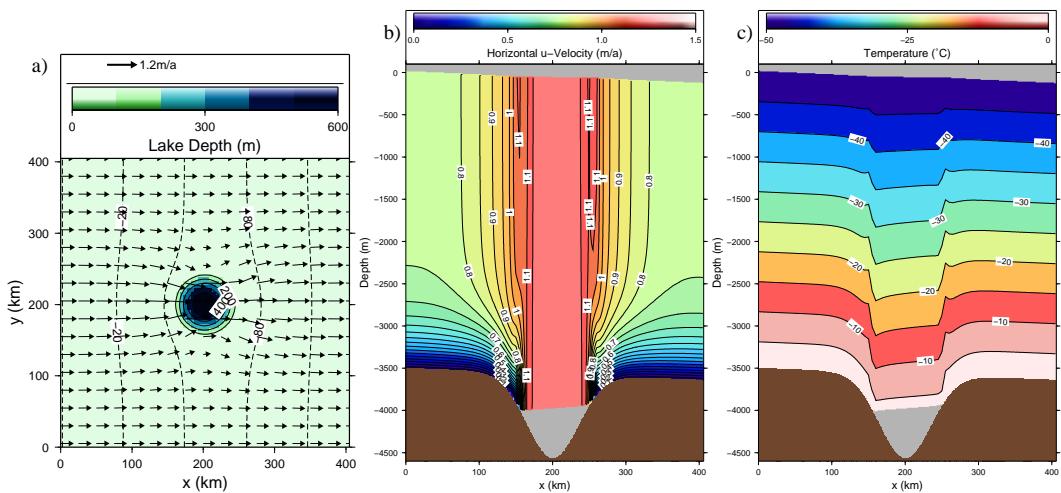


Fig. 3. Results for a full Stokes ice dynamic model with a horizontal resolution of 5 km. **(a)** Lake depth (color), ice sheet surface elevation (dashed contours), and ice-flow velocity (black arrows). **(b)** Horizontal downstream velocity (in x -direction). **(c)** Temperature profile.

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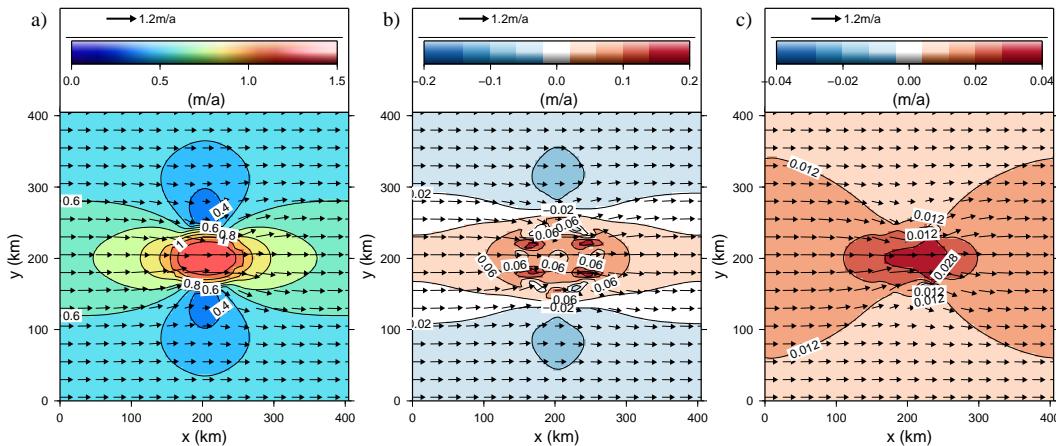


Fig. 4. (a) Vertically averaged horizontal velocity of the standard full Stokes experiment with a horizontal resolution of 5 km. (b) Difference between (a) and the corresponding velocities calculated with a coarser model resolution of 10 km. (c) Difference between (a) and the corresponding velocities calculated with a higher order model.

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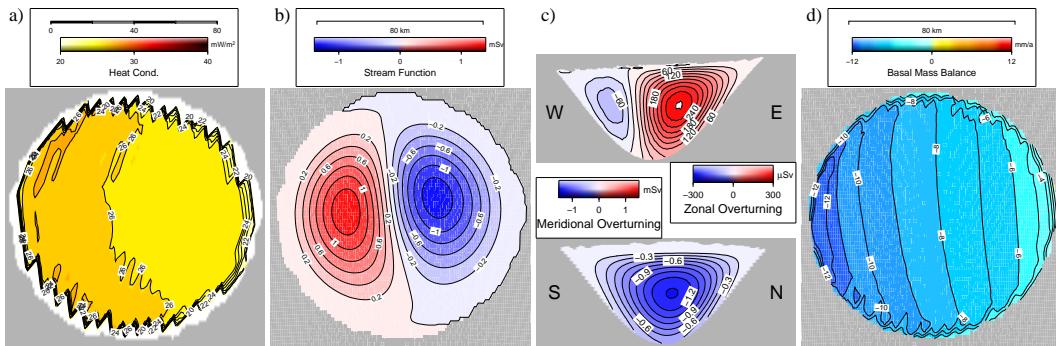


Fig. 5. (a) Heat conduction into the ice. (b) Vertically integrated mass transport stream function. (c) Zonal (from west to east) and meridional (from south to north) overturning. (d) Basal mass balance.

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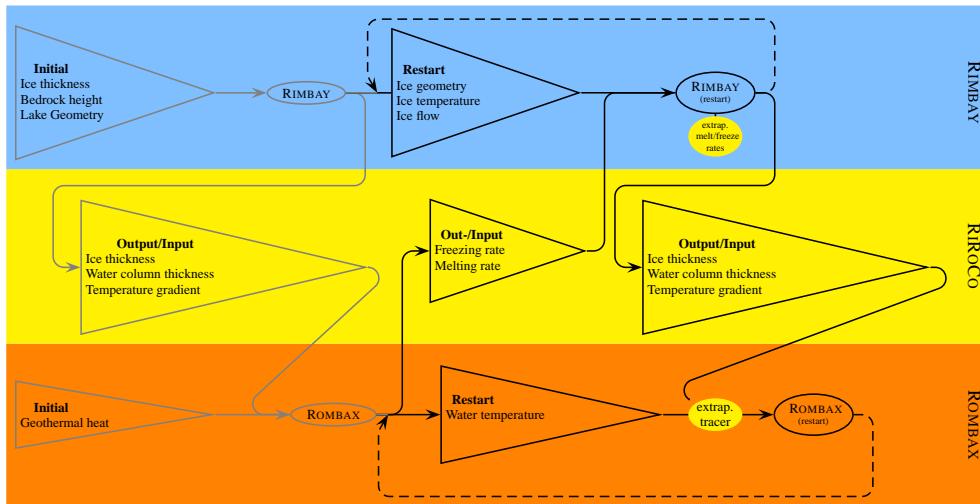
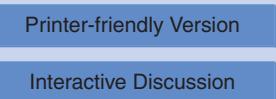
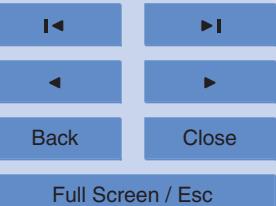
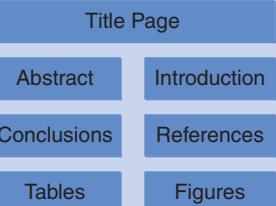


Fig. 6. Couple scheme schematics. The upper part represents the ice-flow model RIMBAY, the lower part the lake-flow model ROMBAX. In the middle the parameters exchanged by the coupler RiRoCo are shown. The gray lines in the left part of the figure represent the initial start-up sequence, dotted loops indicate cycles that may repeat an a priori unspecified number of times. Two additional yellow ovals indicate the individual model needs regarding successive restarts/coupling: the ice flow calculated by RIMBAY may result in new lake nodes. For these nodes the basal mass balance is calculated by averaging adjacent nodes. For ROMBAX a modified geometry desires the extrapolation of temperatures (and other tracers) from a previous model run to skip the time-consuming spin-up process.



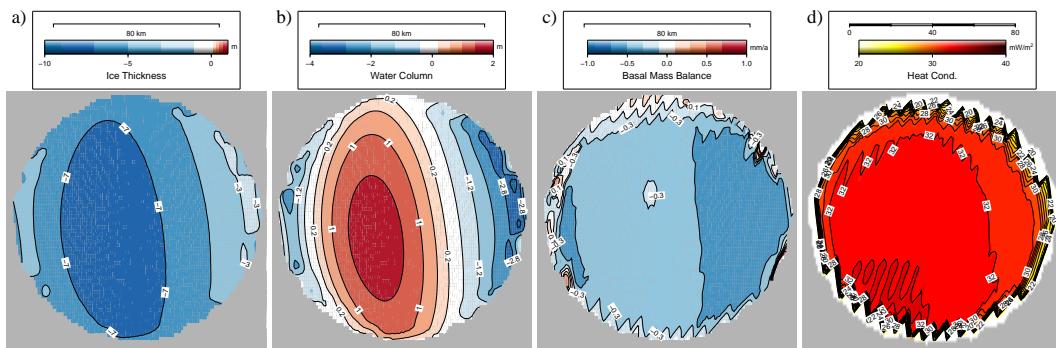


Fig. 7. Impact of melting after 100 000 years on (a) the ice draft, (b) the water column thickness, and (c) the basal mass balance. Shown is the geometry difference between the lake-flow model restart and the initial geometry. (d) Indicates the heat conduction into the ice.

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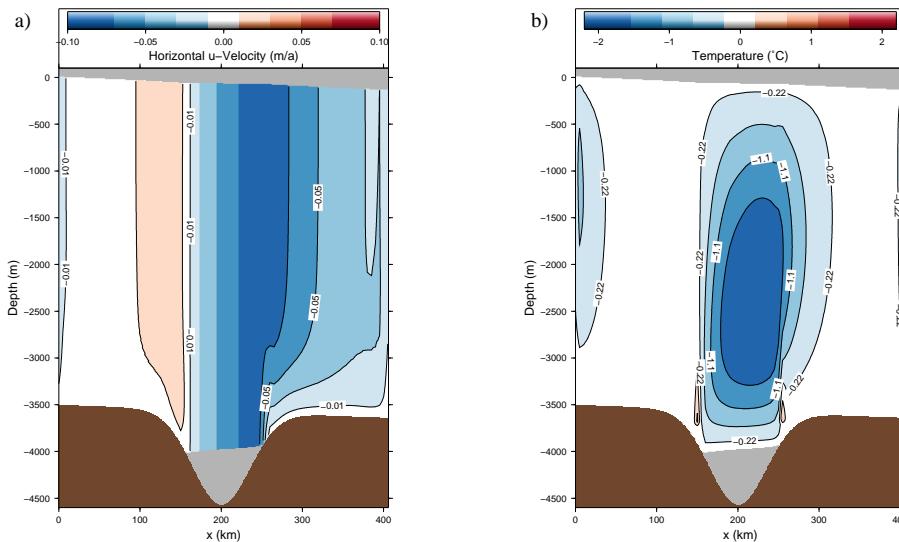


Fig. 8. Differences between coupled-model result and initial model (Fig. 3b and c) for (a) horizontal downstream velocity and (b) temperature.

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