

1 **Diffusive equilibration of N₂, O₂ and CO₂ mixing**

2 **ratios in a 1.5 million years old ice core**

3 **Authors**

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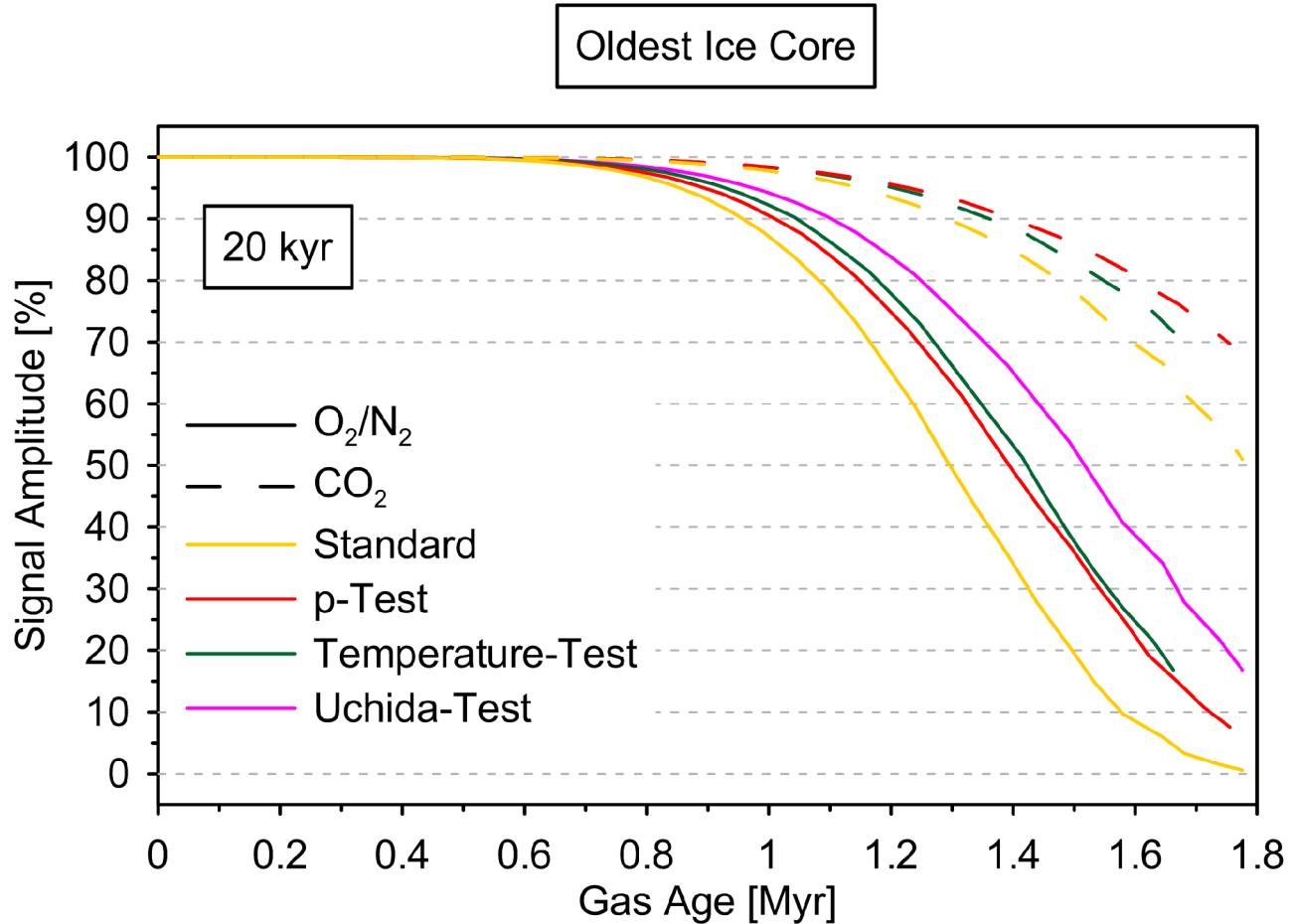
10 **Supplement: Model Sensitivity Tests**

11 Here we show three different model sensitivity tests for the Oldest Ice Core simulations. The first
12 two tests regard uncertainties in two ice parameter, since these values (Table 1) are not well
13 constrained: the tuning parameter p and the bedrock temperature/geothermal heat flux (Qg). The
14 third test regards the very low total air permeation coefficients of Uchida et al. (2011).

15 For the Oldest Ice Core simulations shown in section 4 we used a theoretical value for the tuning
16 parameter p (vertical ice flow tuning parameter) calculated according to Parrenin et al. (2007b).
17 This theoretical value, however, is not applicable for the EDC and the Dome Fuji ice cores
18 (Parrenin et al., 2007b). Realistic p values for these ice cores are in the range of 1-4, which is
19 significantly lower than the theoretical ones (see section 2.2 for more details). In order to test the
20 sensitivity of our results in this regard, we have performed an Oldest Ice Core simulation
21 comparable to the one shown in Fig. 6, but using our p value for the EDC ice core simulations (red
22 lines in Fig. A1). Since the change of the p value results also in different age-depth and
23 temperature-depth distributions, we also adjusted the geothermal heat flux Qg in addition to the p
24 value in order to keep the ice temperature of the 1.5 Myr old ice (130 m above bedrock) equal to the
25 standard simulation. In this way the difference between the results for the 1.5 Myr old ice of the
26 standard and the p-test simulation is a measure for the influence of the ice flow tuning parameter p.
27 Due to the weaker thinning of the deep ice in the p-test simulation, the result for O₂/N₂ in 1.5 Myr
28 old ice shows a 15% weaker dampening compared to the standard run, with a total amplitude
29 dampening of 65%. With respect to the large uncertainties in the gas parameters, the uncertainty in
30 the p value is not critical.

31 For the bedrock temperature sensitivity test, we have used the standard Oldest Ice Core parameters
32 of Table 1 with the only difference of a geothermal heat flux Q_g of 50 mW/m² (green lines in Fig.
33 A1). This results in a bedrock ice temperature of about 260 K, roughly 5 K lower than in the
34 standard simulations. The influence of the lower temperature is comparable to the influence of the
35 lower p value and is therefore also not critical for the findings in this work. A lower bedrock
36 temperature is also likely to be found at a location where the ice sheet is significantly thinner than
37 assumed in our Oldest Ice Core simulations. But for a given accumulation rate a thinner ice sheet
38 also implies thinner annual layers on average, with consequently higher diffusion rates. Hence, the
39 gain of lower bedrock temperatures at a place with a thinner ice sheet would to some extent be
40 compensated by thinner annual layers.

41 For temperatures near the bedrock, where the majority of diffusive dampening takes place, the
42 estimate of total air permeation in ice of Uchida et al. (2011) suggests lower permeabilities than the
43 SS parameters (see Fig. 2). For temperatures below the BCTZ the same estimate suggests higher
44 permeabilities similar to the SS parameters, which is not supported by the results in section 3.
45 Nonetheless, we tested the influence of such low permeabilities. Since the estimate of Uchida et al.
46 (2011) does only give total air permeabilities and not for the single components, we mimicked such
47 low permeabilities by scaling down the SS and FS parameters, respectively, with a constant factor
48 such that they reached the total air permeability of Uchida et al. (2011) at 265 K (bedrock
49 temperature). This approach results also in lower total air permeability compared to Uchida et al.
50 (2011) throughout the ice core with the exception of the very bottom since we kept the temperature
51 sensitivities of the original sets equal. Therefore the results of the corresponding two simulations
52 are actually representing even lower total air permeabilities than suggested by Uchida et al. (2011).
53 The two simulations (one for downscaled SS and one for downscale FS parameters) show very
54 similar results for which reason only the FS result is shown in Fig. A1. The original O₂/N₂
55 amplitude is damped by about 50% after 1.5 Myr (30% less as for the standard run) suggesting that
56 also with lower air permeabilities in the range of Uchida et al. (2011) the precessional O₂/N₂ signal
57 is significantly damped in this case. However, the precessional signal would not be lost and,
58 hence, orbital tuning of the ice age scale using O₂/N₂ would still be possible.



59 Figure A1: Simulated amplitude dampening of CO₂ concentration (dashed lines) and O₂/N₂ ratio
 60 (solid lines) signals with a 20 kyr period. The yellow lines represent the results of the standard
 61 Oldest Ice Core parameters set of Table 1 and the SS parameters (also shown in Fig. 8). The
 62 magenta line (Uchida-Test) shows the results using the same ice parameters, but downscaled FS
 63 parameters (see text). The other coloured lines represent results using the SS parameters as in the
 64 standard run but with different sets of Oldest Ice Core parameters: red: $p = 3.8$, $Q_g = 56 \text{ mW/m}^2$;
 65 green: $Q_g = 50 \text{ mW/m}^2$.

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